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Land subsidence in Jakarta in Three Dimensions (2014–2025) using InSAR–GNSS Datum Connection and the Strapdown Decomposition †

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Abstract

Several coastal megacities face compounding hazards from rising sea levels and land subsidence. Jakarta, one of the fastest-sinking megacities, already experiences recurrent flooding amplified by rapid land subsidence. However, Jakarta's three-dimensional (3D) ground-surface motion has remained poorly resolved due to sparse ground-based geodetic observations and the line-of-sight (LoS) limitation of conventional InSAR observations. Assessing and mitigating this hazard requires reliable estimates of three-dimensional ground motion over wide spatial and temporal scales in a well-defined geodetic reference frame and datum. Here we combine spaceborne InSAR and GNSS measurements to align multi-track InSAR LoS datasets between 2014 and 2025 to a common datum for unbiased three-dimensional velocity decomposition, and connect the resulting velocity field to the Sunda plate-fixed frame using GNSS. This yields a spatially extensive 3D characterization of Jakarta's ground-surface motion on a 450 × 450 m grid in a globally consistent reference frame. Our results show that Jakarta's land motion is dominated by several distinct subsidence bowls, with subsidence and directional horizontal rates of up to −7.9 cm/yr and 1.7 cm/yr, respectively, superimposed on slow regional subsidence of −0.9 cm/yr across the metropolitan area. The resulting 3D velocity field, including its variance–covariance information, is publicly available as a reference dataset for ground-deformation studies in

† Abbreviations: DePSI, Delft Persistent Scatterer Interferometry; IGRS, Integrated Geodetic Reference Station; PoV, projection onto the vertical; RUM, region of uniform motion; TLN, transversal–longitudinal–normal.

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Jakarta. Given that only one continuous GNSS station provides sufficient temporal overlap with the InSAR observations for the datum connection, we recommend installing dedicated geodetic ground-based infrastructure to ensure robust and sustainable monitoring in the future.

Keywords: InSAR, GNSS, datum, geodesy, land subsidence, Jakarta

1. Introduction

Jakarta, the world's most populous city with close to 42 million residents [1], is among the fastest-sinking megacities on Earth. Historically, using observations since 1925 [2, 3], subsidence occurred at two distinct scales: a citywide north-dipping tilt spanning ∼30 km[1], with rates declining from −4.5 cm/yr in the north to near-zero in the south, and localized subsidence bowls superimposed on this trend, whose extent and intensity vary spatiotemporally, with maximum rates ranging from −7 to −15 cm/yr [4, 5, 6]. Currently, ∼15% of Jakarta's land area—mainly in the northern districts—already lies below mean sea level, leaving these areas prone to inundation during ordinary high tides [7]. While citywide catastrophic floods in the past decade have been mostly driven by extreme rainfall and river runoff, in North Jakarta it is the subsidence that is causing recurrent tidal flooding, a risk further intensified by ongoing regional sea-level rise [8]. Jakarta's subsidence is attributed to three interacting mechanisms: (i) natural compaction of young Quaternary coastal alluvium, (ii) increased effective stress from the load of dense urban development and infrastructure, and (iii) groundwater extraction, which reduces pore pressure in the aquifer system and induces localized, bowl-shaped subsidence [9, 4, 10, 11]. While natural compaction and loading act gradually, groundwater withdrawal produces rapid and spatially concentrated deformation. The combined effects are structural damage to buildings, cracking and tilting [12, 13], and recurrent flooding [14, 15, 16, 17], making land subsidence one of the most critical hazards for Jakarta's long-term sustainability. The combined processes [6, 18, 17, 10, 14, 15, 16] of land subsidence, sea-level rise, extreme precipitation, and runoff put Jakarta at risk, with subsidence amplifying hazards by lowering ground elevation, increasing coastal flood exposure, and accelerating runoff. These impacts make pre-

[1] from Ancol to Pasar Rebo

cise estimation and continuous monitoring of land subsidence essential for effective risk assessment and flood mitigation [12].

Over the past four decades, a range of geodetic techniques [19] have been applied, each with distinct strengths and limitations. Spirit leveling in the 1980s [4, 20, 2, 3] provided millimeter-level precision but was costly, slow, and spatially sparse. Of the 45 benchmarks established in 1982 [4], many have since disappeared due to Jakarta's rapid urban development. GNSS campaigns from the 1990s onward [4, 21, 22, 23] expanded from 13 benchmarks to 65 by 2010, improving spatial coverage and revealing broader subsidence patterns, but in the meantime several benchmarks became unobservable due to monument destruction [5]. Thus, for both leveling and GNSS, the loss or inaccessibility of benchmarks limits the temporal continuity and spatial completeness of the subsidence record. The introduction of spaceborne Interferometric Synthetic Aperture Radar (InSAR) [24] in the 1990s revolutionized monitoring, offering dense spatial coverage and frequent temporal sampling across Jakarta's metropolitan area [25, 5]. Early InSAR studies [25, 26, 27, 28, 29] from Jakarta relied on short, single-track SAR datasets and suffered from temporal decorrelation [30]. Advances in processing methods (e.g., Persistent Scatterer Interferometry (PSI) [31, 32] and Small Baseline Subset (SBAS) [33, 34]) combined with greater computational capacity, have enabled longer time series and multi-track coverage [35, 36, 37].

As InSAR observes the projection of the 3D displacement vector onto the radar LoS, these estimates are often projected onto the vertical (PoV), an error-free operation only if horizontal displacements are negligible [38, 39]. Consequently, vertical PoV displacements are biased in localized subsidence bowls. Although Ohenhen et al. [40] and Harintaka et al. [41] combined ascending and descending tracks to estimate the projection of the displacement onto the east–up plane, the result remains biased due to omission of the north component [39]. Therefore, no InSAR product currently provides a complete three-dimensional and unbiased view of ground motion in Jakarta.

Nearly all InSAR-based velocity maps of Jakarta are relative, given in an arbitrary local InSAR datum. The physical 'null-location', where the displacement rate is 0 mm/yr, is unknown. This rank defect can result in misleading geophysical interpretations, such as apparent uplift in central Jakarta [29, 36], which is physically unrealistic. Consequently, studies focusing on fast-subsiding bowls driven by groundwater extraction may overlook slower, widespread regional subsidence, which can be obscured if the InSAR datum is not linked to a plate-fixed reference frame, such as the Sunda plate-

fixed frame [42]. Previous GNSS-based InSAR datum connection approaches have relied on spatially distributed GNSS networks, using spatial interpolation or assumed co-location with InSAR measurements [43, 44, 45, 46], whereas dedicated instrumentation has also been used to establish physical co-location of GNSS antennas and radar targets [47]. However, Jakarta's limited availability of long-term GNSS observations motivates a robust 3D datum connection procedure that exploits the redundancy of multi-track InSAR observations to establish a common datum [48] and then uses the available GNSS observations to connect this datum to a terrestrial reference frame.

Using a modified strapdown decomposition [49] that jointly estimates 3D velocities and aligns multi-track InSAR data to a common datum, followed by a final GNSS-based connection to a terrestrial reference frame, we present the first estimation of three-dimensional velocity vectors across Jakarta in the Sunda plate-fixed frame. In Sec. 2 we present the input datasets and the methodology for multi-track InSAR alignment and GNSS-based datum connection of the InSAR velocity map to the Sunda plate-fixed frame. In Sec. 3, we apply the method to two InSAR track velocity datasets to obtain 3D velocities aligned to a common InSAR datum. We then estimate the velocity offset between this local InSAR datum and the Sunda plate-fixed frame at the location of a continuously operating GNSS reference station (CORS) and apply it uniformly to all provisory 3D velocities, producing the final 3D velocity field for Jakarta in the Sunda plate-fixed frame. This final 3D velocity field is validated using an independent co-located GNSS site. Sec. 4 presents the resulting subsidence patterns, and the final section summarizes the key findings and their implications for Jakarta.

2. Methodology

We subsequently discuss the input datasets and the decomposition assumptions, followed by the inter-track datum alignment establishing a common InSAR datum, and a procedure for estimating the motion of this common InSAR datum within the Sunda plate-fixed frame.

2.1. Dataset Preparation

We use two datasets of InSAR Point Scatterer[2] (PS) LoS displacement time series spanning 2014–2025, see Fig. 1. The datasets were generated from 281

[2]We use the Delft taxonomy for scatterer classification, see [50].

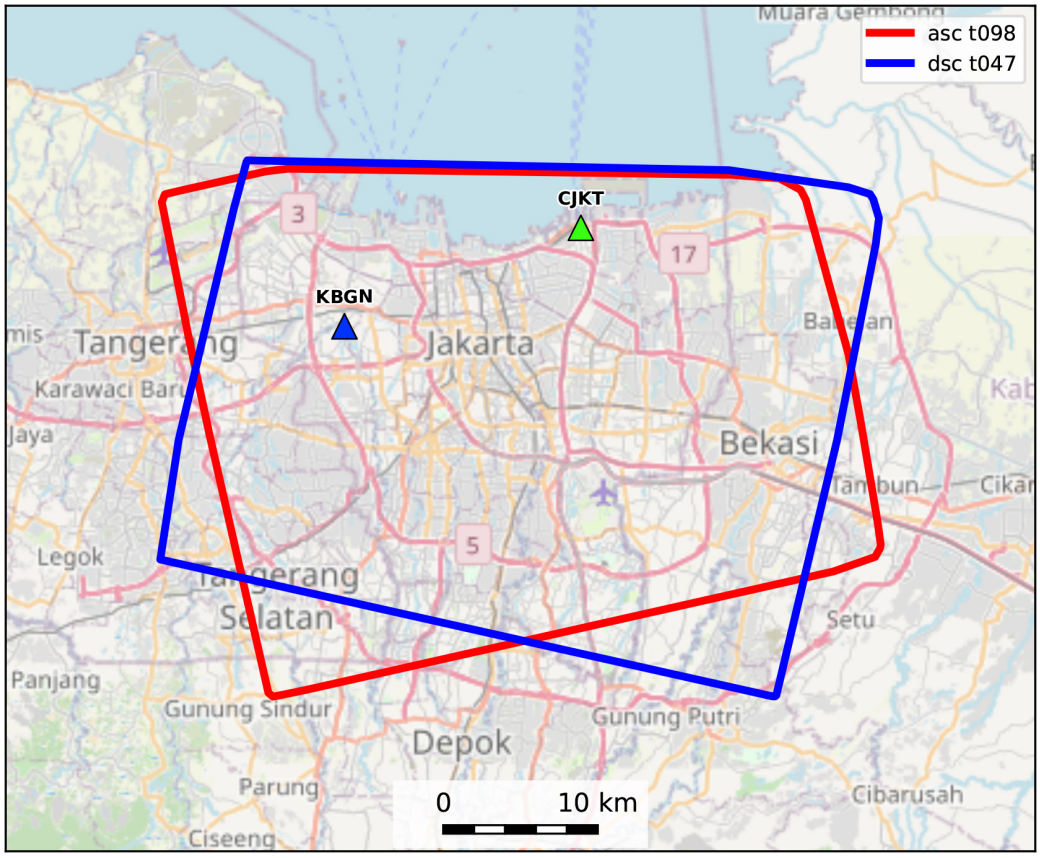


Figure 1: Area of Interest (AOI) covering the Jakarta metropolitan area, showing the Sentinel-1 ascending (track 98, red) and descending (track 47, blue) footprints. The location of the CORS GNSS station CJKT (2014–2022) used for datum alignment is indicated as a green triangle, and the GNSS station KBGN (2023–2025), used to validate the final 3D velocity field, is indicated by a blue triangle

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Sentinel-1 acquisitions from ascending track 98 and 183 acquisitions from descending track 47, using the Delft implementation of Persistent Scatterer Interferometry, DePSI [51, 52]. We adopt a linear velocity parametrization for all subsequent estimates, supported by post-fit residual analysis and hypothesis testing, see Sup. S2. Each track uses a unique local datum defined by its mean linear velocity. Consequently, all velocities are relative and must be interpreted in terms of the spatial variability.

Additionally, we use GNSS observations from two stations with distinct roles, see Fig. 1. Station CJKT is the only long-term CORS in Jakarta with substantial temporal overlap with the InSAR observations, and is used to align the common InSAR datum with the Sunda plate-fixed frame. Station KBGN provides a representative site for independent validation of the final 3D velocity field. CJKT is a CORS located at Tanjung Priok and operated by Badan Informasi Geospasial (BIG). Its antenna is mounted on a 2 m tall concrete pillar on the roof of a two-story concrete building, see Fig. 2D. This station is the only existing long-term CORS in Jakarta that was operational during the InSAR observation period. Its daily station coordinates were derived from continuous GPS phase observations collected between October 2010 and January 2022.[3]

Station KBGN is located in Kembangan, north-west Jakarta, and was installed by the Jakarta Survey Division for continuous land-subsidence monitoring. The station is monumented on a metal pole founded to 1 m depth. Its daily station coordinates were estimated from available GPS code and phase observations within 2023–2025.[4]

To express the GNSS time series in the Sunda plate-fixed frame, we re-

[3]The CJKT GNSS data were processed by Susilo et al. [23] in differential mode using the GAMIT/GLOBK software package version 10.71 [53]. Daily station positions were estimated using double-differenced, ionosphere-free phase observations with respect to 12 IGS reference stations, applying precise IGS orbits, atmospheric delay modeling, and standard tidal and loading corrections. The daily solutions were subsequently combined and aligned in GLOBK to IGb14—the International GNSS Service (IGS) reference frame aligned with ITRF2014—using eight stable global reference stations.

[4]The KBGN GNSS data were processed via ambiguity-resolved precise point positioning in PRIDE-PPP A.R software package version 3.2.8 [54]. The processing used Wuhan University WUM rapid products, including satellite orbits, clocks, code/phase biases, Earth-rotation parameters, and satellite attitude information. Antenna phase-center corrections were applied using the IGS ANTEX model in the IGS20/ITRF2020 reference frame, yielding daily station coordinates in ITRF2020.

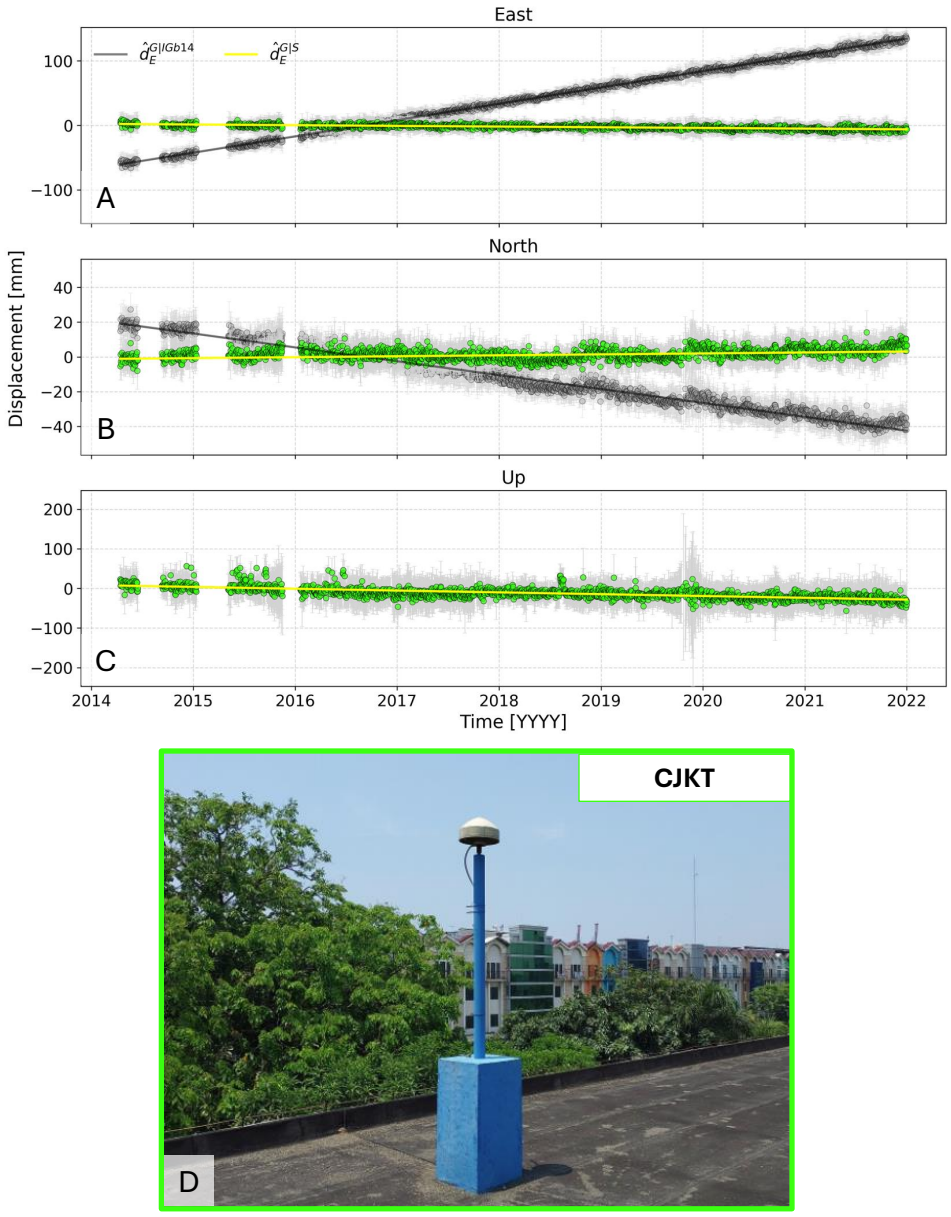


Figure 2: (A–C) East, North, and Up displacement time series of the CJKT GNSS station (2014–2022) with 2σ uncertainties. Gray markers show IGb14 displacements, while green markers show the time series expressed in the Sunda plate-fixed frame after removing Sunda Plate motion using the GSRM v2.1 model. This removal eliminates the southeast horizontal plate motion of 26.52 ± 0.05 mm/yr, yielding near-zero horizontal velocity. The corresponding 3D linear velocities in both reference frames are reported in Tab. 1. (D) CJKT GNSS configuration, located on the roof of a two-story concrete building, supported on deep piles.

Table 1: Linear velocities of GNSS station CJKT in the IGb14 ($\hat{d}^{\mathrm{G|IGb14}}$) and Sunda Plate-fixed ($\hat{d}^{\mathrm{G|S}}$) reference frames, corresponding to the linear models fitted to the displacement time series in Fig. 2, with 2σ uncertainties. The Sunda plate-fixed frame values show small residual horizontal motion after plate-motion removal, likely reflecting limitations of the plate-motion model or local monument motion.

	$\hat{d}^{\mathrm{G|IGb14}}$ [mm/yr]	$\hat{d}^{\mathrm{G|S}}$ [mm/yr]
East	25.28 ± 0.05	-1.06 ± 0.05
North	7.99 ± 0.04	0.54 ± 0.04
Up	-4.6 ± 0.2	-4.6 ± 0.2

moved the rigid motion of the Sunda Plate using the GSRM v2.1 plate-motion model [55][5]. The GNSS time series of CJKT and KBGN—originally expressed in IGb14 and ITRF2020, respectively—were first transformed to IGS08/ITRF2008. For each station, the horizontal Sunda Plate velocity was then computed from the plate-motion model, propagated linearly over the corresponding observation period, and subtracted from the time series. This yields GNSS displacement time series in the Sunda plate-fixed frame, as shown for CJKT in Figs. 2A–C.

To ensure consistency with the InSAR velocity estimates, the CJKT 3D displacement time series and associated 2σ-uncertainties were restricted to the overlapping 2014–2022 InSAR period and fitted with a linear-rate model in the Sunda plate-fixed frame. The resulting CJKT velocities before and after removal of Sunda Plate motion are summarized in Tab. 1. For station KBGN, a linear 3D velocity was estimated over its available observation period and used solely for validation, see Sec. 3.2.

2.2. LoS decomposition to 3D velocity

To convert the InSAR LoS velocities[6] into physically meaningful 3D components, we apply the strapdown decomposition method [49, 56], which transforms ascending and descending LoS observations into a local transversal-longitudinal-normal (TLN) coordinate system [57], and subsequently to an east-north-up (ENU) coordinate system [49].

[5]Euler pole and angular velocity in the IGS08/ITRF2008 realization.

[6]see Sup. Fig. S1

First, the method assumes that deformation within each region of uniform motion (RUM), defined here as a 450×450 m area, is spatially constant, i.e., all PS within the RUM share the same displacement behavior and average linear velocity. In this study, the RUM size of 450×450 m is chosen to preserve deformation homogeneity while retaining sufficient PS sampling for reliable spatial statistics, with at least 50 PS per track per RUM. For the strapdown decomposition, the input observations consist of track-specific RUM-averaged velocities, see Sup. S1, computed as the robust median[7] of all PS LoS velocities within each RUM. This yields two representative velocities per RUM, one per viewing geometry, which serve as the observations for the decomposition. In principle, the velocity variability and contributing PS within each RUM should be evaluated individually, discarding anomalous PS where justified, as done for the RUM used to connect to the Sunda plate-fixed frame. Second, as the local TLN frame is right-handed, with the longitudinal direction tangential to the iso-displacement contours and the transversal direction defined positive downslope, i.e., toward increasing subsidence, centripetal motion in a subsidence bowl is represented by positive transversal velocity estimates.

The initial TLN coordinate system orientation [49] is approximated using three angles: Λ, the azimuth of the longitudinal direction relative to geographic north, initialized by computing the 2D gradient of LoS velocities projected onto the vertical; Φ, the elevation angle of the longitudinal direction relative to the horizontal; and Ω, the elevation angle of the transversal direction. Based on Jakarta's relatively flat terrain, with topographic slopes less than 2° [25], we assume and set $\Phi = \Omega = 0$. Conservative uncertainties of $\sigma_\Lambda = 10°$, and $\sigma_\Phi = \sigma_\Omega = 3°$ are assigned to account for potential imperfections in the TLN orientation, yielding quality metrics for the ENU displacement velocity estimates.

A full mathematical description of the strapdown decomposition, including the observation equations, TLN to ENU transformation, and uncertainty propagation is given in Sup. S1.

[7]The median is inherently robust, meaning it is unaffected by point scatterers that deviate strongly from the RUM median velocity, beyond ±2 times the median absolute deviation (MAD).

2.3. Inter-track InSAR datum alignment

The strapdown method requires the contributing InSAR viewing geometries to be expressed in a common datum. In the absence of dedicated control points for inter-track datum connection, we exploit a physical constraint characteristic of subsiding regions: *transversal velocities must be centripetal, i.e., directed toward increasing subsidence* [58]. A mismatch between track datums alters both the magnitude and sign of the decomposed (transversal, $\hat{d}_T$, and normal, $\hat{d}_N$) velocities, producing physically implausible results, such as transversal velocities pointing upslope and normal velocities indicating uplift, see Sup. S3.

We use this constraint to jointly estimate the inter-track datum offset and the unbiased 3D velocities. The north component is therefore estimated within the physically constrained strapdown decomposition, rather than being resolved by the SAR viewing geometry alone. In practice, the inter-track datum alignment is performed by taking the descending track as reference.[8] A trial offset, $\Delta d^{\text{asc}}_{\text{LoS}}$, is applied to the ascending-track LoS velocities, the strapdown decomposition is recomputed for each trial, and the optimal offset is found by sampling the solution space of possible datum offsets and selecting the one that minimizes the number of negative transversal velocities

$$\min_{\Delta d^{\text{asc}}_{\text{LoS}}} \sum_{i=1}^{n} \mathbb{1}\Big(\hat{d}_{T_i}(d^{\text{asc}}_{\text{LoS},i} + \Delta d^{\text{asc}}_{\text{LoS}}, d^{\text{dsc}}_{\text{LoS},i}) < 0\Big), \tag{1}$$

where $i = 1, \ldots, n$ indexes the RUM observations, $d^{\text{asc}}_{\text{LoS},i}$ and $d^{\text{dsc}}_{\text{LoS},i}$ are the ascending- and descending-track LoS velocities for observation i, $\hat{d}_{T_i}(\cdot)$ is the resulting transversal velocity from the strapdown decomposition given the input LoS velocities, $\Delta d^{\text{asc}}_{\text{LoS}}$ is the trial offset applied to the ascending-track velocities, and $\mathbb{1}(\cdot)$ is an indicator function equal to 1 if the argument is true (i.e., if the transversal velocity is negative) and 0 otherwise.

The optimal offset, $\Delta\hat{d}^{\text{asc}}_{\text{LoS}}$, is determined by sampling the solution space of trial offsets within a pre-defined range, using increments of 0.1 mm yr^{-1} to match InSAR precision (2σ), and then identifying the global minimum analytically. The decomposition solution corresponding to this optimal offset produces physically consistent transversal and normal velocities, $\hat{d}_{T_i}$ and $\hat{d}_{N_i}$,

[8] The inter-track datum alignment procedure is independent of the choice of reference track; here, the descending track is used as the reference datum.

together with ENU velocity estimates and variance–covariance matrices in the local datum of the descending InSAR viewing direction.

2.4. InSAR and GNSS datum alignment

Since the decomposed ENU displacement velocities from the strapdown decomposition are expressed in the datum of the descending InSAR track, they must be transformed into a terrestrial reference frame for geophysical interpretation. This transformation assumes a spatially constant 3D velocity offset, estimated using co-located RUMs, defined as RUM cells whose footprint contains at least one GNSS antenna. Within a co-located RUM, the point-like GNSS velocity in the chosen terrestrial reference frame—here the Sunda plate-fixed frame [59]—is assumed to represent the same deformation signal as the spatially averaged InSAR velocity obtained from the strapdown decomposition.

For each co-located RUM i, a 3D datum-connection vector is computed as the difference between the GNSS velocity in the Sunda Plate–Fixed Frame, $\hat{\boldsymbol{d}}_i^{\mathrm{G|S}}$, and the RUM-averaged InSAR velocity in the local InSAR datum, $\hat{\boldsymbol{d}}_i^{\mathrm{I}}$

$$\Delta \boldsymbol{d}_i^{\mathrm{I}\to\mathrm{S}} = \hat{\boldsymbol{d}}_i^{\mathrm{G|S}} - \hat{\boldsymbol{d}}_i^{\mathrm{I}}, \tag{2}$$

where $\Delta \boldsymbol{d}_i^{\mathrm{I}\to\mathrm{S}}$ is the 3D offset needed to align the InSAR-derived velocity of RUM i in the local InSAR datum (superscript I) with the corresponding GNSS velocity in the Sunda Plate–Fixed Frame (superscript G|S).

In the general case of multiple co-located RUMs, the final datum-connection vector, $\Delta \boldsymbol{d}^{\mathrm{I}\to\mathrm{S}}$, and its uncertainty are estimated by a least-squares adjustment of all individual datum-connection vectors $\Delta \boldsymbol{d}_i^{\mathrm{I}\to\mathrm{S}}$ derived from the RUM–GNSS pairs. The resulting best-fitting 3D offset is then applied uniformly to the entire InSAR velocity field, thereby connecting it to the chosen terrestrial reference frame. In the present study, the alignment is performed to the Sunda plate-fixed frame (S) using the only existing GNSS station in Jakarta with substantial temporal overlap with the InSAR observations (2014-2025), as described in Sec. 2.1 and detailed in Sec. 3. Consequently, the datum-connection vector is the 3D offset computed from a single co-located RUM, and added uniformly to all RUM velocities to express the InSAR-derived field in the Sunda plate-fixed frame

$$\hat{\boldsymbol{d}}_i^{\mathrm{I|S}} = \hat{\boldsymbol{d}}_i^{\mathrm{I}} + \Delta \boldsymbol{d}^{\mathrm{I}\to\mathrm{S}}. \tag{3}$$

Here, $\hat{\boldsymbol{d}}_i^{\mathrm{I}}$ is the RUM-averaged ENU velocity obtained from the strapdown decomposition and expressed in the descending InSAR datum, and $\hat{\boldsymbol{d}}_i^{\mathrm{G|S}}$ is the ENU GNSS velocity in the Sunda plate-fixed frame. The uncertainties of $\Delta\boldsymbol{d}^{\mathrm{I}\to\mathrm{S}}$ are derived through standard variance propagation, assuming independent uncertainties of the co-located GNSS and RUM-averaged InSAR velocities.

The complete processing workflow, together with the subsequent independent validation step, is illustrated in Sup. Fig. S2.

3. Results

3.1. Jakarta's 3D velocity field in the Sunda plate-fixed frame

To estimate three-dimensional land motion in Jakarta with associated uncertainties, the ascending-track datum is first aligned to the descending-track datum, establishing a common InSAR datum for both tracks. Following Sec. 2.3, a relative datum offset of $\Delta\hat{d}_{\mathrm{LoS}}^{\mathrm{asc}} = 1.2$ mm/yr is estimated by evaluating the objective function in Eq. (1) over all 4779 RUMs, with trial offsets sampled within the range $[-2.4, 2.4]$ mm/yr at 0.1 mm/yr increments. The optimal offset corresponds to the global minimum of this function, i.e., the minimum number of RUMs with negative transversal velocities[9]. The strapdown decomposition using this offset yields an intermediate 3D velocity field for Jakarta expressed in the common InSAR datum.

We connect this intermediate 3D velocity field to the Sunda plate-fixed frame following Sec. 2.4. The 3D datum connection vector is computed at the co-located RUM containing the CJKT GNSS station. Because CJKT is the only GNSS station operational during the study period, this vector is obtained directly from the ENU velocity difference between the GNSS velocity in the Sunda plate-fixed frame and the decomposed co-located RUM velocity in the common InSAR datum, following Eq. (2).

The final datum connection is based on the assumption that the GNSS point velocity and the InSAR velocity of representative PS within the co-located RUM describe the same local deformation signal. In general, this assumption should be treated with caution because PS within the same RUM may correspond to ground-level objects, low-rise buildings, or taller structures whose motion can differ depending on foundation depth and structural

[9] see Sup. animation Supplementary_Animation_S1_rum_bias_animation.gif

coupling to the ground. Inspection of the original PS LoS velocities within the CJKT RUM, see Fig. 3, shows moderate velocity heterogeneity when all PS are considered (range $\sim$2.0 mm/yr, $\sigma = 0.5$ mm/yr, MAD = 0.4 mm/yr), and no strong correlation between PS velocities and their elevations. Using all PS would therefore result in an empirical co-location uncertainty of approximately 2 mm/yr. Because the CJKT antenna is installed on a two-story concrete building and its antenna height is known, we use this information to preferentially select PS that are structurally comparable to the GNSS monument. Specifically, as the antenna is located at 32.205 m above the WGS84 ellipsoid, and Sentinel-1 PS heights have a formal 2σ-uncertainty of approximately 8–10 m [60], we select PS with $H_{\mathrm{WGS84}} \geq 22.205$ m to compute the RUM-averaged LoS velocity for each track prior to the decomposition. This selection is based on structural representativeness and reduces the empirical co-location uncertainty from $\sim$2 to 1 mm/yr.

The estimated 3D datum offset is applied component-wise to all RUM velocities in the ENU frame, transforming the strapdown-derived velocity field into the Sunda plate-fixed frame. The final 3D velocity map is shown in Fig. 4, with vertical velocities shown in color and directional horizontal, i.e., transversal, velocities shown as vectors. Only vectors with magnitudes greater than (2σ) are plotted, so that they represent statistically significant motion. Horizontal velocity uncertainties are represented by the 2σ confidence ellipses in Fig. 4, while the spatial distributions of the east, north, and vertical velocity uncertainties are provided separately in Sup. Fig. S4. The map clearly shows several subsidence bowls. Along the rims of the major bowls, outlined and numbered in magenta in Fig. 4, horizontal velocities exceed 10 mm/yr and include distinct north components. These horizontal velocity vectors point toward the centers of the subsidence bowls [58], indicating centripetal motion driven by sediment compaction. Such lateral motion may generate shear along bowl slopes and extension near bowl edges, potentially affecting building stability and increasing the vulnerability of underground pipelines.

3.2. Validation

As a full validation of the final 3D velocity field shown in Fig. 4 is not possible due to the lack of ground truth, we assess its agreement with co-located GNSS velocity estimates at station KBGN over 2023–2025, see Fig. 5. At KBGN, we compute the 3D ENU residual vector in the Sunda plate-fixed

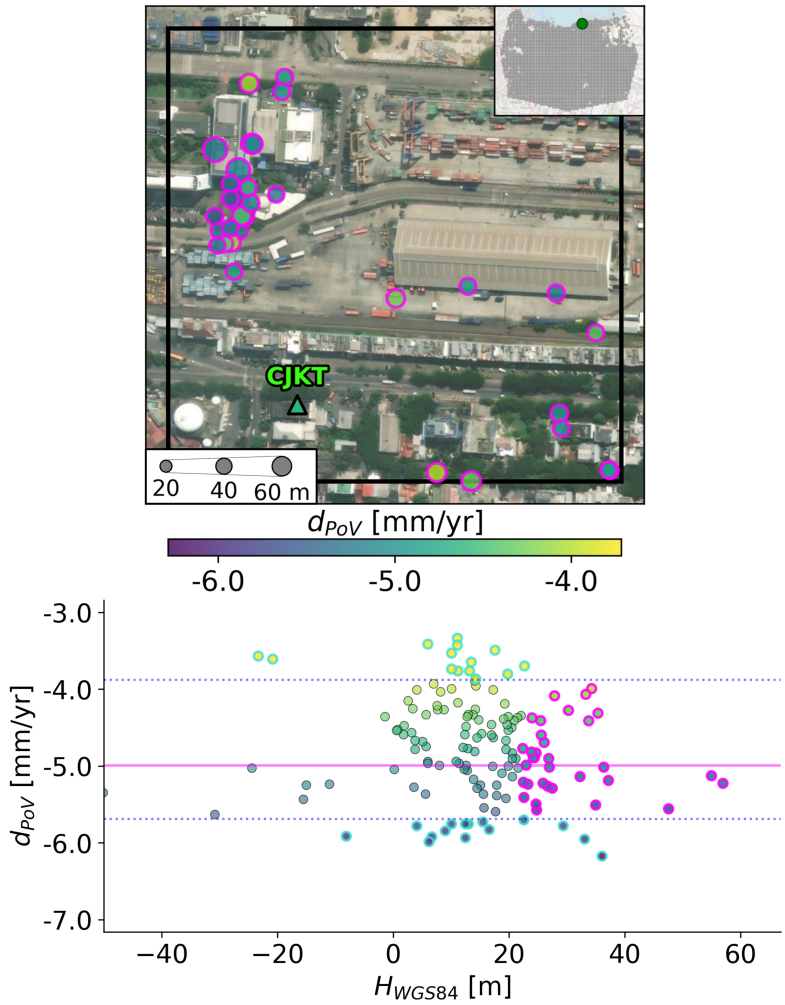


Figure 3: Height-based PS selection within the CJKT co-location RUM for establishing a precise datum connection to the Sunda plate-fixed frame. For visualization, LoS velocities from both tracks are first aligned to the common InSAR datum and projected onto the vertical direction. Although no strong correlation is observed between PS velocity and elevation, the known CJKT antenna height is used to select scatterers that are more structurally comparable to the GNSS monument. Selected PS satisfy $H_{\mathrm{WGS84}} \geq 22.205$ m, corresponding to the antenna height minus the 2σ Sentinel-1 PS height uncertainty. Relative to using all PS, this selection changes the estimated datum offset by $\sim$0.3 mm/yr and reduces the empirical co-location uncertainty from approximately 2 to 1 mm/yr. **Top:** The 450×450 m co-location RUM, CJKT GNSS station, and selected PS are shown by the black outline, green triangle, and magenta-outlined points, respectively. Marker size scales with H_{WGS84}, and marker color shows d_{PoV}. **Bottom:** d_{PoV} versus H_{WGS84} for all PS. Magenta-outlined points are selected for datum connection, while light-blue outlined points are excluded. Dashed blue lines show the ± 2 MAD interval for all PS, and the magenta line shows the median LoS velocity of the selected PS.

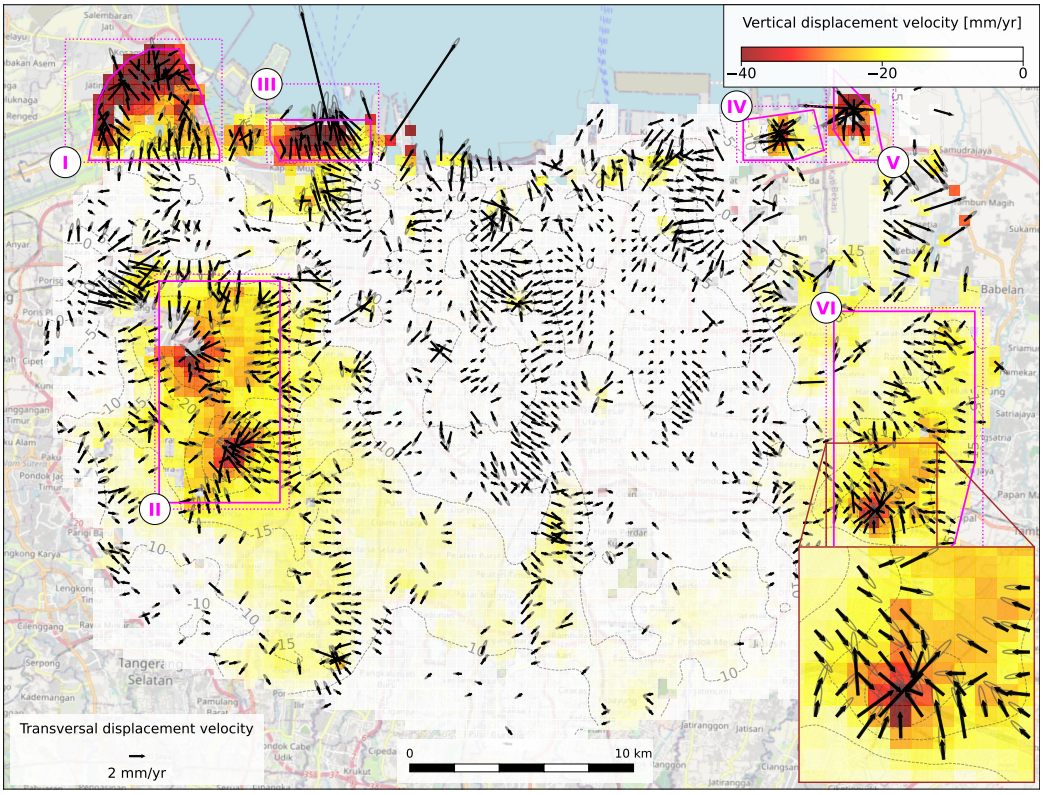


Figure 4: Sunda plate-fixed InSAR velocity map of the Jakarta metropolitan area (2014–2025) obtained via the single-station GNSS (green triangle) based datum connection. Vertical velocities are shown in color, and directional horizontal velocities are shown as vectors with 2σ confidence ellipses (see the enlarged inset in the lower-right corner); only a subset of the vectors exceeding 2σ are displayed. Main subsidence bowls, (> 1 mm/yr) are indicated by magenta roman numbers I–VI. Directional horizontal velocities near the bowl rims reach up to 10 mm/yr, including distinct north components. Central Jakarta shows little vertical subsidence compared to the bowls. The mean background subsidence rate outside the major bowls is -9.1 mm/yr. The inset in the bottom right corner zooms into Bowl VI, highlighting the centripetal horizontal velocity vectors; for a zoomed-in overview of each bowl see Sup. Fig. S3. The corresponding decomposed 3D ENU velocity components and associated uncertainties are provided in Sup. Fig. S4.

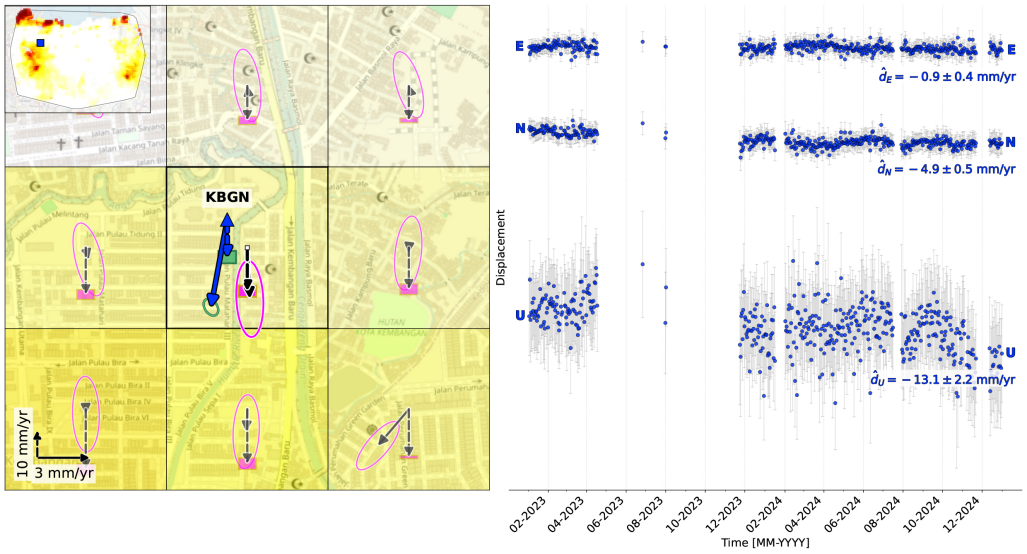


Figure 5: GNSS–InSAR validation of the final 3D velocity field in the Sunda plate-fixed frame at KBGN. The left panel shows the validation RUM containing the GNSS station and its neighboring RUMs, colored by RUM-averaged InSAR vertical velocity; the inset locates the validation RUM within the Jakarta-wide vertical velocity field. The blue arrow shows the GNSS velocity, and black arrows show the Sunda plate-fixed frame RUM-averaged InSAR velocities at each RUM center; the central arrow is used for comparison. Filled and dashed arrows represent horizontal and vertical velocities, respectively, with green and magenta ellipses/intervals showing GNSS and InSAR (2σ) uncertainties. The right panel shows the 2023–2025 GNSS ENU displacement time series used to estimate the KBGN velocity. The comparison shows millimeter-per-year agreement between GNSS and InSAR, with a 3D misfit of 3.1 ± 2.4 mm/yr, providing site-specific validation of the final 3D velocity field at KBGN.

Table 2: Summary of mean and maximum vertical and directional horizontal (i.e., transversal) subsidence rates and cumulative displacements in Jakarta for each subsidence bowl, based on the CORS-based datum alignment. Velocities are in mm/yr, and cumulative displacements cover a 10.7-year period (October 2014 to June 2025) in mm.

Bowl #	**# RUMs**	$\hat{d}_{U_i}$ [mm/yr]			$\hat{d}_{T_i}$ [mm/yr]		
		mean	**max**	**max cum. [mm]**	**mean**	**max**	**max cum. [mm]**
I	112	−31.1	−55.9	−594.9	1.5	6.6	69.6
II	275	−21.9	−39.8	−423.4	1.0	3.8	40.4
III	44	−29.7	−78.5	−835.3	2.4	16.9	179.5
IV	32	−15.6	−35.1	−373.9	1.1	4.8	51.1
V	22	−26.0	−51.0	−542.6	2.1	9.8	104.0
VI	358	−17.1	−47.0	−500.2	0.7	5.8	61.7

frame as

$$\hat{\boldsymbol{e}}_i = \hat{\boldsymbol{d}}_i^{\mathrm{G|S}} - \hat{\boldsymbol{d}}_i^{\mathrm{I|S}}, \tag{4}$$

where i denotes the co-located RUM. Uncertainties are propagated from the GNSS and InSAR ENU covariance matrices, assuming independent errors, and are reported as 2σ. The comparison shows millimeter-per-year agreement between GNSS and InSAR, with a vertical residual of 2.1 ± 2.9 mm/yr, a horizontal residual magnitude of 2.3 ± 1.9 mm/yr, and a 3D misfit of 3.1 ± 2.4 mm/yr. The horizontal velocity directions differ by $13.4° \pm 15.9°$, which is within the 2σ uncertainty. This millimeter-level 3D agreement is consistent with the linear subsidence behavior of the KBGN RUM over 2014–2025, which supports comparison of the final InSAR RUM-averaged velocity with the shorter 2023–2025 GNSS velocity, see Sup. S2

4. Discussion

4.1. Geophysical discussion

The 3D velocity map in the Sunda plate-fixed frame reveals several spatially localized subsidence bowls, labeled I to VI in Fig. 4 and outlined in magenta. These bowls exhibit maximum vertical velocities of up to −78.5 mm/yr, and their subsidence characteristics are summarized in Tab. 2. Bowl III in the Muara Angke region shows the strongest deformation, with vertical velocities up to −78.5 mm/yr, a cumulative vertical displacement of −84 cm over the October 2014–June 2025 period, and transversal (i.e., directional horizontal) velocities up to 16.9 mm/yr that may pose risks to utility infrastructure. Bowl I, near Soekarno–Hatta International Airport, also exhibits

severe vertical subsidence (maximum −55.9 mm/yr; cumulative −59 cm). The remaining four bowls show substantial but less extreme vertical motion. Across these bowls, the vertical and horizontal velocity components exhibit coupled deformation patterns. Vertical subsidence is generally greatest toward the bowl centers, while the strongest horizontal velocities occur along their flanks and converge toward the centers, see Sup. S4. The bowls span a variety of urban functions, including industrial areas, residential neighborhoods, commercial districts, and mixed-use zones. In the absence of a clear correlation, subsidence cannot be attributed to specific urban functions.

The reported maximum vertical velocities and cumulative displacements are comparable with those of Harintaka et al. [41]. Other studies, such as Sidiq et al. [37], report higher vertical velocities for the 2017–2023 period using descending-track LoS velocities projected onto the vertical. This vertical projection neglects horizontal motion and can increase the apparent vertical velocity by 12–14 mm/yr in Bowl III.

Several regions along the northern and northeastern coast of Jakarta, represented by the yellow RUMs in Sup. Fig. S8B , exhibit higher intra-RUM velocity variability than the rest of the study area. This is evidenced by larger residual LoS velocities after removal of a planar trend within each RUM, as detailed in Sup. S4.These areas correspond to densely built neighborhoods dominated by low-rise structures, likely supported by shallow or absent foundations, which experience slow subsidence with moderate spatial variability and lack the bowl-like velocity patterns characteristic of the major subsidence bowls, see Fig. 4. The observed velocity variability therefore points to a different subsidence mechanism, likely related to shallow subsurface processes. Two explanations are plausible: i) localized subsidence due to shallow groundwater extraction, or ii) slow consolidation of young coastal alluvium. Given that these regions are located in districts such as Tanjung Priok, Tambora, Pademangan, and Pluit—where municipal piped-water coverage is high and the phreatic aquifer is polluted [61]—shallow groundwater pumping is unlikely. Slow consolidation of young coastal alluvium is therefore the more probable mechanism.

Beyond the distinct subsidence bowls, the entire metropolitan area experiences slow regional subsidence, with a mean vertical velocity of −9.1 mm/yr across Jakarta.

The validity of the geophysical interpretation of Jakarta's subsidence depends on the quality of the final datum connection to the Sunda plate-fixed frame, anchored to the single CORS station at CJKT. As detailed in Sec. 3

and discussed further below, this connection is robust for the study period (2014–2025), with a co-location precision of ∼1 mm/yr. However, relying on a single GNSS station in a dynamic urban environment has inherent limitations: changes in local building subsidence, or the relocation or destruction of the GNSS monument, could reduce the precision of future datum connections—or even prevent InSAR connection to the Sunda plate-fixed frame entirely. To support reliable long-term monitoring and rigorous InSAR–GNSS alignment, new infrastructure is urgently needed in Jakarta. Establishing multiple Integrated Geodetic Reference Stations (IGRS) [62], combining GNSS and corner reflectors visible in multiple InSAR geometries, would ensure precise ties and consistent alignment of the InSAR datum to the Sunda plate-fixed frame.

4.2. Geodetic discussion

Millimeter-scale misalignments between InSAR LoS datasets from different tracks can propagate through the strapdown decomposition and distort the estimated 3D velocity components. A sensitivity analysis for Jakarta, see Sup. S3, shows that neglected inter-track datum offsets may produce biases in both magnitude and direction (including sign flips) of the transversal velocities, whereas normal velocities are affected only about one quarter as much in magnitude and roughly one tenth as much in direction. As the CJKT GNSS station exhibits millimeter-level residual horizontal motion after plate motion removal, see Fig. 2, using this station to align the ascending and descending LoS datums prior to the strapdown decomposition would propagate these residuals into the decomposed 3D velocities, particularly affecting the transversal velocities. To avoid introducing such errors from the earliest stage of the decomposition, the methodology in Sec. 2.3 instead exploits the high redundancy[10] of InSAR observations to simultaneously estimate 3D RUM-averaged velocities and perform inter-track datum alignment with sub-millimeter precision. This alignment is fully independent of GNSS data, providing a physically constrained and internally consistent means to tie multi-track InSAR observations to a common datum. GNSS observations at CJKT are used only for the final connection to the Sunda plate-fixed frame, as described later in this section.

The inter-track datum alignment assumes positive centripetal horizontal

[10] > 50 PS per RUM per track across all 4779 RUMs

motion toward areas of increasing subsidence, a deformation-driven assumption in which gravity-driven compaction induces coupled vertical settlement and inward horizontal motion. For Jakarta, this is justified: the study area lies on coastal alluvial soils [12, 10, 13] with no known active faults crossing it, and the southward-dipping Baribis Fault [63], 50 km to the north, is too distant and oriented away to produce significant tectonic uplift or centrifugal horizontal motion. Consequently, the observed inward horizontal motion toward the centers of subsidence bowls is consistent with compaction-driven subsidence, likely linked to groundwater extraction [58].

The strapdown decomposition in Jakarta relies on a spatially coherent deformation regime, where velocity change along iso-displacement lines is zero and radial velocity gradients within subsidence bowls define the local TLN orientation, enabling accurate 3D velocity reconstruction. To assess this coherence, a planar trend is fitted to the LoS velocities within each RUM, see Sup. S4. Most RUMs (88%) show low residuals and semivariance after planar removal, with the strongest reduction inside the six main subsidence bowls, indicating that deep-seated, long-wavelength compaction dominates Jakarta's primary subsidence signal. By contrast, a small subset of RUMs, shown in yellow in Sup. Fig. S8B , retains higher residual variability. In these RUMs, PS elevations vary by only $\sim$20 m (2σ), and the LoS velocity variability remains within $\pm$3.5 mm/yr (2σ), indicating that the variability is not primarily elevation-dependent. These regions show slow subsidence, weak velocity gradients, and less well-resolved horizontal motion. This pattern suggests a different subsidence mechanism from that of the main bowls, most likely related to shallow subsurface processes such as consolidation of young coastal alluvium, as discussed earlier.

In the final step, the strapdown-derived 3D velocity field is aligned to the Sunda plate-fixed frame using the CORS station at CJKT, the only long-term GNSS infrastructure available for datum connection in Jakarta, as confirmed by national geospatial authorities.[11] This step assumes that the GNSS point velocity and the InSAR velocity of selected PS within the co-located RUM capture the same deformation signal. To satisfy this assumption, the co-location RUM velocity is computed before decomposition using only PS at or above the CJKT antenna height. These roof-level or taller scatterers are expected to behave similarly to the GNSS building, yielding a co-location

[11] Badan Informasi Geospasial (BIG) and Jakarta Survey Division

uncertainty of ∼1 mm/yr for 2014–2025, see Fig. 3. This supports a reliable datum connection for the study period. However, future differential settlement or modifications to the structures hosting the selected PS or the GNSS monument could degrade or prevent this connection. Ensuring consistent, long-term alignment of InSAR-derived 3D velocity products to the Sunda plate-fixed frame will therefore require establishing multiple co-located GNSS–InSAR benchmarks across Jakarta.

5. Conclusion

The first unbiased 3D displacement velocity field for Jakarta is estimated on a 450×450 m grid covering 2014–2025 and referenced to the Sunda plate-fixed frame, achieving millimeter precision that resolves detailed subsidence patterns beyond the capability of traditional GNSS or leveling surveys. All estimates are accompanied by a full variance–covariance matrix, allowing displacement significance to be assessed for groundwater management, flood-risk assessment, city planning and asset management.

The velocity field shows that Jakarta's land motion is dominated by distinct subsidence bowls with extreme localized displacement, reaching a maximum vertical velocity of −78.5 mm/yr. These bowls are superimposed on slower regional subsidence, characterized by a mean background vertical velocity of −9.1 mm/yr outside the bowl regions. Smaller coastal areas along the northern and northeastern shores show slower, spatially heterogeneous subsidence with no coherent bowl-shaped pattern. This suggests shallow subsidence processes, in addition to the deep-seated, long-wavelength compaction observed in the major bowls, with natural consolidation of young coastal alluvium as one possible mechanism. Localized directional horizontal displacements of up to 16.9 mm/yr are observed, providing statistically significant information for assessing deformation pathways and infrastructure risk.

The InSAR 3D velocity field is tied to the Sunda plate-fixed frame through the single long-term CORS GNSS station at CJKT—the only one currently available in Jakarta. The selected high-elevation point scatterers co-located with CJKT provide a reliable datum connection for 2014–2025 with ∼1 mm/yr precision. However, future settlement or structural changes at the selected point scatterers or the GNSS monument could affect long-term alignment. The deployment and maintenance of multiple co-located GNSS–InSAR bench-

marks across Jakarta is therefore imperative for continued, accurate connection of InSAR-derived 3D velocities to the Sunda plate-fixed frame.

The findings demonstrate a novel procedure that combines strapdown decomposition of ascending and descending InSAR displacement velocities, a deformation-driven internal datum connection, and a GNSS-based InSAR datum alignment to a global terrestrial reference frame. This approach provides a comprehensive 3D subsidence monitoring method for Jakarta and establishes a transferable framework for other rapidly subsiding megacities, provided that spatially coherent deformation, suitable multi-track InSAR geometry, a physically justified internal datum constraint, and at least one reliable GNSS–InSAR co-location are available. Effectively, careful InSAR datum alignment is as critical as the subsidence measurements themselves.

Supplementary material

Supplementary material is available for this article as a PDF and accompanying standalone files. It includes methodological details, parameterization choices and sensitivity analyses, velocity-homogeneity assessment, additional LoS and 3D velocity figures, zoomed views of the main subsidence bowls, and an animation of the inter-track datum-alignment procedure described in Sec. 2.3. All supplementary items should be considered supporting information to the main article.

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Declaration of competing interests

Declarations of interest: none.

Data availability

The final 3D ground displacement velocity estimates (east, north, up) for the Jakarta city and metropolitan area, including variance-covariance values are available at `https://doi.org/10.4121/39e7a39c-d305-425f-b238-1f3a4271dda9`.

The North–East–Up GNSS time series of the CJKT CORS station are available from the Zenodo repository at `https://doi.org/10.5281/zenodo.7775016` [23].

All other data and materials required to evaluate the conclusions of this study are included in the article and the supplementary material.

Author Contributions

A.M.L. contributed to Conceptualization, Methodology, Formal analysis, Investigation, Data Curation, Visualization, and Writing – Original Draft; designed the research, performed the analysis, created the figures, and wrote the first draft. H.A. contributed to Investigation, Resources, Data Curation, and Writing – Review & Editing; conducted, processed, and provided the GNSS data and additional metadata on the GNSS benchmarks. D.P. contributed to Investigation, Resources, and Data Curation; conducted, processed, and provided the GNSS data and additional metadata on the GNSS benchmarks. W.B. contributed to Methodology and Software; developed the strapdown method and provided feedback on its application. S.v.D. contributed to Investigation and Data Curation; processed the InSAR data. R.H. contributed to Supervision and Writing – Review & Editing; analyzed, reviewed, and edited the manuscript.

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Supplementary Material: Land Subsidence in Jakarta in Three Dimensions (2014–2025) using InSAR–GNSS Datum Connection and the Strapdown Decomposition†

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S1. Mathematical Formulation of Strapdown Decomposition

The strapdown decomposition is used to estimate 3D displacement velocities from InSAR LoS velocity observations, following the approach of Brouwer and Hanssen [1].

Let the vector of unknown parameters for each RUM be

$$\boldsymbol{x} = \begin{bmatrix} d_T & d_L & d_N & \Lambda & \Omega & \Phi \end{bmatrix}^{\mathrm{T}}, \tag{S1}$$

where d_T, d_L, d_N are the displacement velocities in the transversal, longitudinal (along the iso-displacement contour lines), and normal directions of the local TLN coordinate system, and Λ, Ω, Φ are the orientation angles of the TLN coordinate system, treated as pseudo-observation representing prior approximations for the TLN frame orientation.

The observations used to estimate these RUM-specific parameters are organized into $s = 1, \ldots, m$ sets, each corresponding to a distinct SAR viewing geometry (ascending or descending). These observations consist of RUM-averaged LoS velocities for each SAR viewing geometry and the pre-set TLN

†Abbreviations: OMT, Overall Model Test; RUM, region of uniform motion; TLN, transversal–longitudinal–normal; WMAB, weighted mean absolute bias.

orientation angles, related to the unknowns through

$$\mathrm{E}\{\begin{bmatrix} \underline{d}_{\mathrm{LoS}}^{(1)} \\ \vdots \\ \underline{d}_{\mathrm{LoS}}^{(m)} \\ \underline{\Lambda} \\ \underline{\Omega} \\ \underline{\Phi} \end{bmatrix}\} = \begin{bmatrix} a_1(\boldsymbol{x}) \\ \vdots \\ a_m(\boldsymbol{x}) \\ \Lambda \\ \Omega \\ \Phi \end{bmatrix}, \text{ with } a_s(\boldsymbol{x}) = \left[P_T^{(s)}, P_L^{(s)}, P_N^{(s)}\right]_{\Lambda,\Omega,\Phi} \begin{bmatrix} d_T \\ d_L \\ d_N \end{bmatrix}, \quad \text{(S2)}$$

where $P_T^{(s)}, P_L^{(s)}, P_N^{(s)}$ project the TLN velocities onto the LoS for all observations in set s.

For Jakarta, each RUM has two sets, corresponding to Sentinel-1 ascending track 98 and descending track 47. In the equations of the main text, the set index is indicated as a superscript: $s = \mathrm{asc}$ for the ascending track and $s = \mathrm{dsc}$ for the descending track. The RUM-averaged LoS velocity observations are computed as the robust median of all PS within each RUM (see Sec. 2.2) and, together with the pre-set TLN angles Φ and Ω (set to 0) and the longitudinal azimuth Λ initialized from the 2D gradient of PoV velocities, are used to estimate the RUM-specific 3D displacement velocity parameters.

The dispersion of the observations is described by the covariance matrix

$$\mathrm{D}\{\begin{bmatrix} \underline{d}_{\mathrm{LoS}}^{(1)} \\ \vdots \\ \underline{d}_{\mathrm{LoS}}^{(m)} \\ \underline{\Lambda} \\ \underline{\Omega} \\ \underline{\Phi} \end{bmatrix}\} = \begin{bmatrix} \boldsymbol{Q}_{\mathrm{LoS},1} & 0 & \cdots & 0 & 0 & 0 & 0 \\ 0 & \boldsymbol{Q}_{\mathrm{LoS},2} & \cdots & 0 & 0 & 0 & 0 \\ \vdots & \vdots & \ddots & \vdots & \vdots & \vdots & \vdots \\ 0 & 0 & \cdots & \boldsymbol{Q}_{\mathrm{LoS},m} & 0 & 0 & 0 \\ 0 & 0 & \cdots & 0 & \sigma_\Lambda^2 & 0 & 0 \\ 0 & 0 & \cdots & 0 & 0 & \sigma_\Omega^2 & 0 \\ 0 & 0 & \cdots & 0 & 0 & 0 & \sigma_\Phi^2 \end{bmatrix}, \quad \text{(S3)}$$

where $\boldsymbol{Q}_{\mathrm{LoS},s}$ is the variance–covariance matrix of the RUM-averaged LoS observation in set s, derived via standard error propagation for the median averaging, and σ_Λ^2, σ_Ω^2, and σ_Φ^2 are the variances of the TLN pseudo-observation angles. For Jakarta, these are pre-set to $\sigma_\Lambda = 10^\circ$ and $\sigma_\Omega = \sigma_\Phi = 3^\circ$ (see Sec. 2.2).

The displacement velocity vector from $\boldsymbol{x}$, $\boldsymbol{d}_{\mathrm{TLN}} = [d_T, d_L, d_N]^{\mathrm{T}}$, is projected onto the LoS direction via a projection onto the plane orthogonal to the LoS, using the projector

$$\boldsymbol{P}_{\mathrm{LoS}^\perp}^R = [P_T, P_L, P_N], \quad \text{(S4)}$$

with components

$$
\begin{aligned}
P_T &= (\sin\theta \sin\alpha_d \cos\Lambda - \sin\theta \cos\alpha_d \sin\Lambda)\cos\Omega \\
&\quad - \Big((-\sin\theta \sin\alpha_d \sin\Lambda + \sin\theta \cos\alpha_d \cos\Lambda)\sin\Phi \\
&\quad + \cos\theta \cos\Phi\Big)\sin\Omega, \qquad \text{(S5)} \\
P_L &= (\sin\theta \sin\alpha_d \sin\Lambda + \sin\theta \cos\alpha_d \cos\Lambda)\cos\Phi \\
&\quad + \cos\theta \sin\Phi, \qquad \text{(S6)} \\
P_N &= (\sin\theta \sin\alpha_d \cos\Lambda - \sin\theta \cos\alpha_d \sin\Lambda)\sin\Omega \\
&\quad + \Big((-\sin\theta \sin\alpha_d \sin\Lambda + \sin\theta \cos\alpha_d \cos\Lambda)\sin\Phi \\
&\quad + \cos\theta \cos\Phi\Big)\cos\Omega. \qquad \text{(S7)}
\end{aligned}
$$

Here, θ denotes the incidence angle toward the radar, and α_d is the azimuth of the zero-Doppler plane at the target location, measured in the direction toward the satellite [2].

The unknown parameter vector $\boldsymbol{x}$ in Eq. (S1) is estimated using an iterative Gauss–Newton approach applied to the observation model in Eq. (S2). At each iteration, the nonlinear equations are linearized around the current estimate and solved in a weighted least-squares sense until convergence is reached, yielding the final parameter estimates $\hat{\boldsymbol{x}}$ and their associated covariance matrix $\boldsymbol{Q}_{\hat{\boldsymbol{x}}}$. The latter can be written in block-diagonal form as $\boldsymbol{Q}_{\hat{\boldsymbol{x}}} = \mathrm{blockdiag}\big(\boldsymbol{Q}_{\underline{\hat{\boldsymbol{d}}}_{\mathrm{TLN}}}, \boldsymbol{Q}_{\underline{\hat{\Lambda}}}, \boldsymbol{Q}_{\underline{\hat{\Omega}}}, \boldsymbol{Q}_{\underline{\hat{\Phi}}}\big)$.

The estimated TLN displacement velocities $\underline{\hat{\boldsymbol{d}}}_{\mathrm{TLN}} = [\underline{\hat{d}}_T, \underline{\hat{d}}_L, \underline{\hat{d}}_N]^{\mathrm{T}}$ and their covariance matrix $\boldsymbol{Q}_{\underline{\hat{\boldsymbol{d}}}_{\mathrm{TLN}}}$ are subsequently rotated into the local East–North–Up (ENU) coordinate system using the estimated orientation angles $\underline{\hat{\Lambda}}$, $\underline{\hat{\Omega}}$, and $\underline{\hat{\Phi}}$

$$
\boldsymbol{R}_{\mathrm{TLN}\to\mathrm{ENU}} = \boldsymbol{R}_{\underline{\hat{\Lambda}}}\, \boldsymbol{R}_{\underline{\hat{\Omega}}}\, \boldsymbol{R}_{\underline{\hat{\Phi}}}, \qquad \text{(S8)}
$$

$$
\boldsymbol{R}_{\underline{\hat{\Lambda}}} = \begin{bmatrix} \cos\underline{\hat{\Lambda}} & \sin\underline{\hat{\Lambda}} & 0 \\ -\sin\underline{\hat{\Lambda}} & \cos\underline{\hat{\Lambda}} & 0 \\ 0 & 0 & 1 \end{bmatrix}, \quad \boldsymbol{R}_{\underline{\hat{\Omega}}} = \begin{bmatrix} \cos\underline{\hat{\Omega}} & 0 & \sin\underline{\hat{\Omega}} \\ 0 & 1 & 0 \\ -\sin\underline{\hat{\Omega}} & 0 & \cos\underline{\hat{\Omega}} \end{bmatrix}, \quad \boldsymbol{R}_{\underline{\hat{\Phi}}} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos\underline{\hat{\Phi}} & \sin\underline{\hat{\Phi}} \\ 0 & -\sin\underline{\hat{\Phi}} & \cos\underline{\hat{\Phi}} \end{bmatrix}. \qquad \text{(S9)}
$$

The ENU displacement velocities are obtained by rotating the estimated TLN velocities using $\boldsymbol{R}_{\mathrm{TLN}\to\mathrm{ENU}}$, i.e., $\underline{\hat{\boldsymbol{d}}}_{\mathrm{ENU}} = \boldsymbol{R}_{\mathrm{TLN}\to\mathrm{ENU}}\, \underline{\hat{\boldsymbol{d}}}_{\mathrm{TLN}}$, while the associated covariance matrix is propagated as $\boldsymbol{Q}_{\underline{\hat{\boldsymbol{d}}}_{\mathrm{ENU}}} = \boldsymbol{R}_{\mathrm{TLN}\to\mathrm{ENU}}\, \boldsymbol{Q}_{\underline{\hat{\boldsymbol{d}}}_{\mathrm{TLN}}}\, \boldsymbol{R}^{\mathrm{T}}_{\mathrm{TLN}\to\mathrm{ENU}}$,

yielding the final 3D displacement components in the ENU coordinate system together with their full variance–covariance information.

For a full description of the equations and the estimation procedure, see Brouwer and Hanssen [1].

S2. Statistical hypothesis testing of linear LoS displacement behavior

We assessed whether an average linear velocity parameterization is representative of the 2014–2025 PS LoS displacement time series. The assessment was performed at the level of regions of uniform motion (RUMs), defined in Sec. 2.2 as 450×450 m spatial units within which deformation is assumed to be spatially constant. For each RUM, the PS LoS displacement time series were aggregated at each epoch by taking the median. This yields a RUM-averaged LoS displacement time series that describes the average displacement behavior of the RUM.

To assess linearity, a linear displacement model was fitted to the RUM-averaged LoS displacement time series for each RUM i and track $s \in \{\text{asc}, \text{dsc}\}$. The post-fit residuals were then tested against a prescribed track-specific LoS displacement uncertainty using an Overall Model Test (OMT) [3]. The test statistic is

$$T_i^{(s)} = \frac{\sum_{t=1}^{n^{(s)}} \left(r_i^{(s)}(t) \right)^2}{\left(\sigma_{\text{LoS}}^{(s)} \right)^2}, \tag{S10}$$

where $r_i^{(s)}(t)$ is the residual of the linear model at epoch $t = 1, \ldots, n^{(s)}$, $n^{(s)}$ is the number of valid epochs for track s, and $\sigma_{\text{LoS}}^{(s)}$ is the prescribed LoS displacement uncertainty for that track. The test was applied with a false-alarm probability of $\alpha = 0.05$, using $\sigma_{\text{LoS}}^{(s)} = 5.0$ mm for both ascending and descending tracks. The null hypothesis H_0 of linear displacement was rejected when

$$T_i^{(s)} > k_{\alpha=0.05, n^{(s)}-2}, \tag{S11}$$

where $k_{\alpha=0.05, n^{(s)}-2}$ is the critical value for $n^{(s)} - 2$ degrees of freedom, corresponding to the fitted intercept and linear velocity. If H_0 was not rejected, the RUM was classified as linear for that track; otherwise, it was classified as nonlinear.

Across the combined ascending and descending OMT results, 92% of the evaluated RUMs are linear and 8% are nonlinear, see Tab. S1. Nonlinear

Table S1: Hypothesis testing classification of RUMs over 2014–2025 using the OMT. The OMT is applied separately to each RUM and track to test whether the linear displacement model is rejected. The table reports the combined ascending and descending results; therefore, one RUM can contribute up to two classifications. Percentages are computed relative to the number of classifications in each row.

Subset	**# classifications**	**Linear**	**Nonlinear**
Full RUM field	9558	8752 (92%)	806 (8%)
Inside subsidence regions	1686	1216 (72%)	470 (28%)
Region I	224	139 (62%)	85 (38%)
Region II	550	430 (78%)	120 (22%)
Region III	88	43 (49%)	45 (51%)
Region IV	64	35 (55%)	29 (45%)
Region V	44	10 (23%)	34 (77%)
Region VI	716	559 (78%)	157 (22%)
Outside subsidence regions	7872	7536 (96%)	336 (4%)

RUMs are mainly located within the outlined subsidence regions in Fig. S5, which contain 58% of all nonlinear classifications. Among these regions, Region V has the highest nonlinear fraction, followed by Regions III and IV; Regions I, II, and VI are predominantly linear. At the GNSS sites, both the CJKT datum-connection site and the KBGN validation site are located in RUMs showing linear subsidence behavior.

Overall, the predominance of linear RUMs supports the average linear velocity parameterization used to derive RUM-averaged LoS velocity observations for the strapdown decomposition.

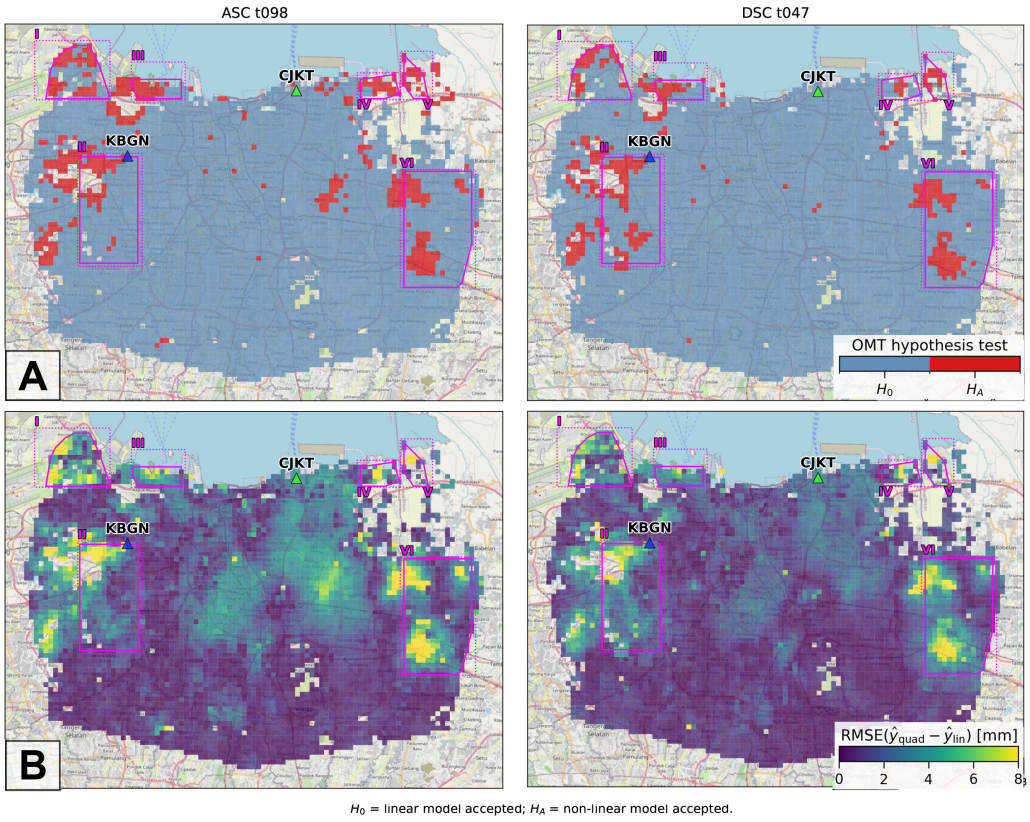


Figure S5: Hypothesis testing of whether RUM-averaged LoS displacement time series can be represented by a linear displacement model over 2014–2025 for ascending track 98 and descending track 47. **A:** OMT classification for each RUM and track, using $\alpha = 0.05$ and a prescribed LoS displacement uncertainty of $\sigma_{\mathrm{LoS}}^{(s)} = 5.0$ mm for both tracks; H_0 (light blue) denotes RUMs for which the linear displacement model is not rejected, whereas H_A (red) denotes nonlinear RUMs. **B:** Magnitude of deviation from linear behavior, computed as RMSE($\hat{y}_{\mathrm{quad}} - \hat{y}_{\mathrm{lin}}$) between fitted quadratic and linear displacement models. Magenta outlines mark the main subsidence regions, corresponding to the turquoise outlines in Fig. 4. The CJKT datum-connection GNSS station is shown in green, and the KBGN validation GNSS station is shown in blue. Both CJKT and KBGN are located in RUMs showing linear subsidence behavior. Nonlinear behavior is mainly concentrated in and around the outlined subsidence regions.

S3. Effect of inter-track datum misalignment on the relative velocity map of Jakarta

To quantify the impact of datum misalignment on the decomposed 3D velocity field, we compute both magnitude and directional (sign flip) residuals between the unaligned ($\Delta d^{\text{asc}}_{\text{LoS}} = 0$ mm/yr) and aligned ($\Delta \hat{d}^{\text{asc}}_{\text{LoS}} = 1.2$ mm/yr) decomposed velocity fields of each RUM, after the inter-track datum alignment, see Sec. 2.3. Magnitude residuals are defined as

$$\begin{aligned} \Delta \hat{d}_{T_i} &= \hat{d}_{T_i}\big(d^{\text{asc}}_{\text{LoS}_i}, d^{\text{dsc}}_{\text{LoS}_i}\big) - \hat{d}_{T_i}\big(d^{\text{asc}}_{\text{LoS}_i} + \Delta d^{\text{asc}}_{\text{LoS}_i}, d^{\text{dsc}}_{\text{LoS}_i}\big), \\ \Delta \hat{d}_{N_i} &= \hat{d}_{N_i}\big(d^{\text{asc}}_{\text{LoS}_i}, d^{\text{dsc}}_{\text{LoS}_i}\big) - \hat{d}_{N_i}\big(d^{\text{asc}}_{\text{LoS}_i} + \Delta d^{\text{asc}}_{\text{LoS}_i}, d^{\text{dsc}}_{\text{LoS}_i}\big). \end{aligned} \tag{S12}$$

The magnitude bias is expressed as the Weighted Mean Absolute Bias (WMAB):

$$\begin{aligned} \text{WMAB}_T &= \frac{1}{n}\sum_{i=1}^{n} \big|\Delta \hat{d}_{T_i}\big|, \\ \text{WMAB}_N &= \frac{1}{n}\sum_{i=1}^{n} \big|\Delta \hat{d}_{N_i}\big|. \end{aligned} \tag{S13}$$

Directional bias is quantified as the percentage of RUMs exhibiting a sign flip

$$\begin{aligned} \Delta\theta_T &= \frac{100}{n}\sum_{i=1}^{n} \mathbb{1}\Big(\hat{d}_{T_i}\big(d^{\text{asc}}_{\text{LoS}_i}, d^{\text{dsc}}_{\text{LoS}_i}\big) \cdot \hat{d}_{T_i}\big(d^{\text{asc}}_{\text{LoS}_i} + \Delta d^{\text{asc}}_{\text{LoS}_i}, d^{\text{dsc}}_{\text{LoS}_i}\big) < 0\Big), \\ \Delta\theta_N &= \frac{100}{n}\sum_{i=1}^{n} \mathbb{1}\Big(\hat{d}_{N_i}\big(d^{\text{asc}}_{\text{LoS}_i}, d^{\text{dsc}}_{\text{LoS}_i}\big) \cdot \hat{d}_{N_i}\big(d^{\text{asc}}_{\text{LoS}_i} + \Delta d^{\text{asc}}_{\text{LoS}_i}, d^{\text{dsc}}_{\text{LoS}_i}\big) < 0\Big), \end{aligned} \tag{S14}$$

where $\mathbb{1}(\cdot)$ is the indicator function, which equals 1 if the argument is true (i.e., if the unaligned decomposed velocity has the opposite sign to the aligned decomposed velocity for the same RUM, their product will be negative) and 0 otherwise. For transversal velocities, the positive direction is defined as downslope (centripetal), while normal velocities are expected to be negative in sinking regions.

Fig. S6 compares the unaligned and aligned decomposed velocities over the entire RUM field. Transversal velocities show a magnitude bias of $\text{WMAB}_T = 6.86$ mm/yr and directional flips $\Delta\theta_T = 33\%$, whereas normal velocities show smaller biases: $\text{WMAB}_N = 1.51$ mm/yr and $\Delta\theta_N = 2\%$.

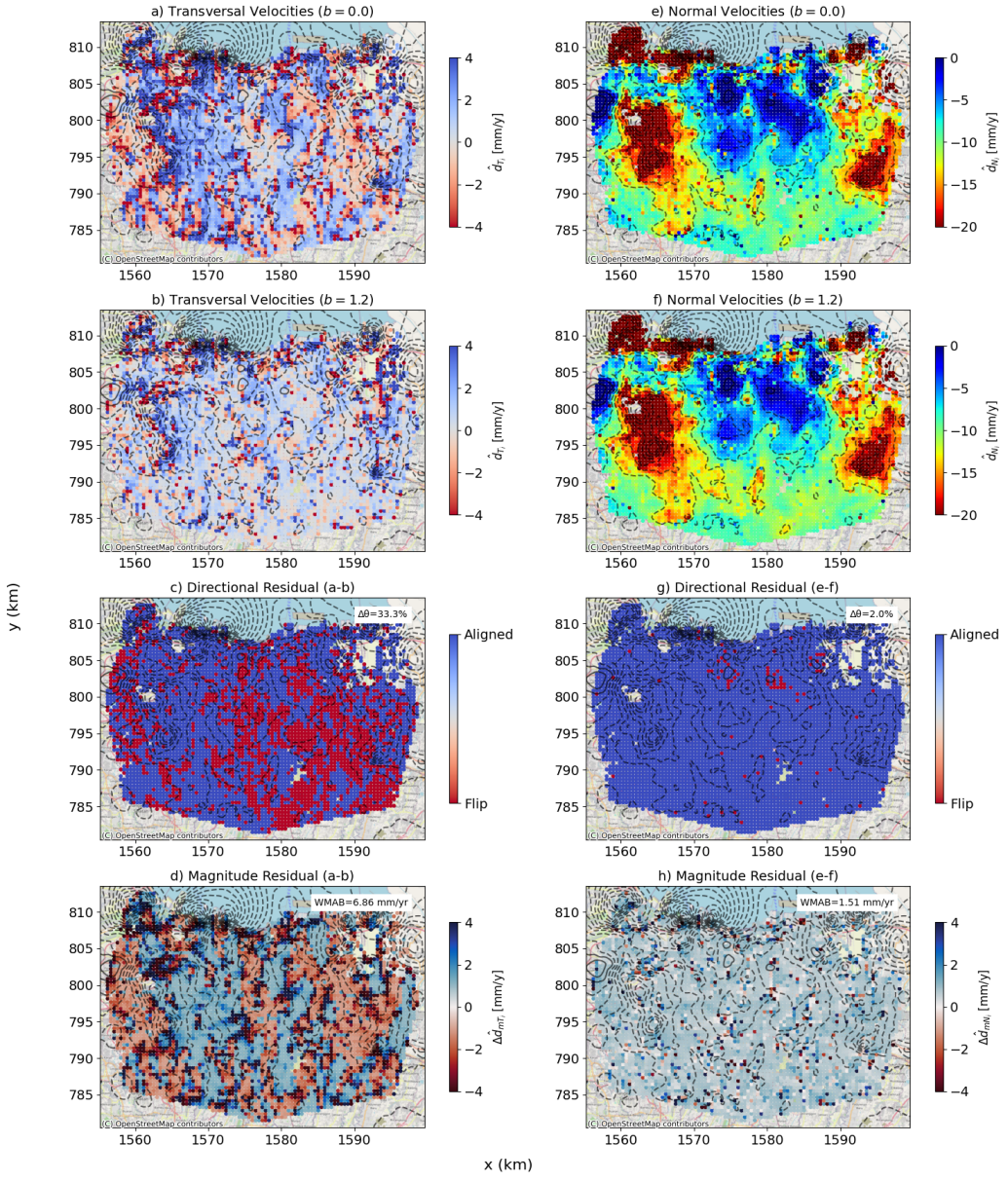


Figure S6: Directional and magnitude biases due to inter-track datum misalignment in Jakarta. Columns show transversal (first) and normal (second) velocity components. Panels (a)–(b) compare unaligned ($\Delta d^{\text{asc}}_{\text{LoS}} = 0.0$ mm/yr) and aligned ($\Delta d^{\text{asc}}_{\text{LoS}} = 1.2$ mm/yr) transversal velocities; panels (e)–(f) show the same for normal velocities. Panels (c)–(d) and (g)–(h) display spatial variability of directional and magnitude biases.

Fig. S7 shows the effect of varying the ascending track datum offset, $\Delta d_{\mathrm{LoS}}^{\mathrm{asc}}$, from -2.4 to $+2.4$ mm/yr in steps of 0.1 mm/yr. Transversal velocities reach up to 20 mm/yr (WMAB) and 45% directional flips, while normal velocities reach up to 4.8 mm/yr and 5% flips. Both magnitude and directional biases show a clear minimum at $\Delta d_{\mathrm{LoS}}^{\mathrm{asc}} = 1.2$ mm/yr, highlighting the necessity of proper datum alignment.

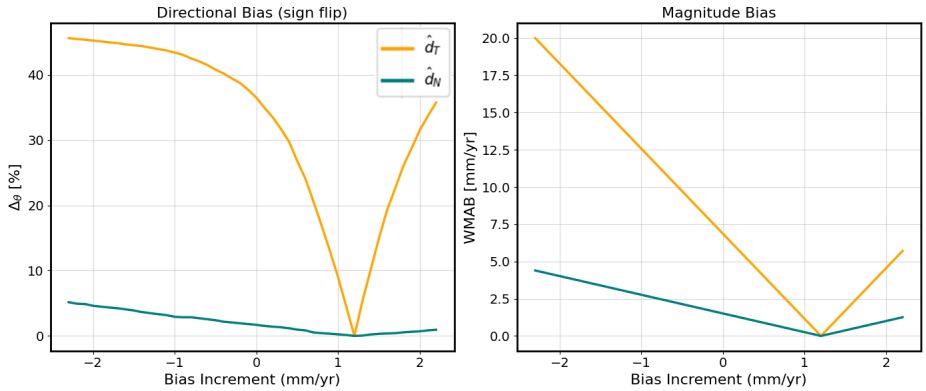


Figure S7: Directional bias ($\Delta\theta$, left) and magnitude bias (WMAB, right) for transversal (T, orange) and normal (N, blue) velocity components across inter-track datum offsets. Transversal velocities are more sensitive, reaching 20 mm/yr (WMAB) and 45% ($\Delta\theta$). Both curves show a minimum at $\Delta d_{\mathrm{LoS}}^{\mathrm{asc}} = 1.2$ mm/yr.

S4. Intra-RUM LoS velocity homogeneity assessment

Fig. S8 evaluates intra-RUM LoS velocity homogeneity for the ascending and descending tracks to determine whether the estimated 3D velocity field of Jakarta (Fig. 4) reflects a spatially coherent subsidence regime. Within each RUM, homogeneity was assessed using the standard deviation of LoS velocities, the standard deviation and the semivariance $\gamma(h)$ of residual velocities after planar detrending. The semivariance lag was set to $h \approx 60$ m, determined by first computing the mean nearest-neighbor distance d_{nn} between PS points ($\sim$ 11 m ascending, $\sim$ 9.5 m descending) and then incrementally evaluating the scale-dependent heterogeneity $H(n) = \gamma(n\, d_{\mathrm{nn}})/\sigma^2$ for increasing multiples n until the critical lag n_{crit} is reached. The critical lag n_{crit} is defined as the smallest n for which $H > 1$, indicating that local residual velocity variability exceeds the total RUM variance.

RUM velocities are considered spatially uniform—and therefore dominated by homogeneous, long-wavelength subsidence—if the LoS velocities are well described by a planar fit, with small residuals ($\sigma < 1$ mm/yr) and low semivariance ($\gamma < 0.8$ mm^2/yr^2). Approximately 88% of RUMs meet these criteria, especially within the major subsidence bowls, highlighting areas dominated by deep-seated, long-wavelength compaction. In contrast, a small subset of RUMs along the northern and northeastern coasts (yellow regions in Fig. S8B), including Tanjung Priok, Tambora, Pademangan, Pluit, and a north-south feature from Muara Baru to Central Jakarta, exhibits higher residual variability and semivariance. These areas are less spatially coherent and likely reflect different, shallower or more localized subsidence mechanisms, making the 3D velocity estimates there less well constrained.

Captions for separately supplied supplementary files

Supplementary Figure S1.
Input ascending- and descending-track LoS velocity fields used for the three-dimensional velocity decomposition.

Supplementary Figure S2.
Technical workflow for estimating the 3D ground-surface velocity field in the Sunda Plate-Fixed Frame (Sunda plate-fixed frame). Multi-track PSI-derived LoS velocities are aggregated within 450×450 m RUMs and used as observations in the joint inter-track datum alignment and 3D strapdown decomposition. The resulting 3D ENU velocity field in the common InSAR datum is connected to the Sunda plate-fixed frame using the co-located CJKT GNSS observations, while KBGN is reserved for independent validation of the final 3D velocity field.

Supplementary Figure S3.
Zoomed views of the major subsidence bowls outlined in turquoise in the Jakarta-wide three-dimensional velocity field shown in Fig. 4. Vertical velocities are shown in color, and directional horizontal velocities are shown as vectors with 2σ confidence ellipses; only a subset of vectors exceeding 2σ is displayed.

Supplementary Figure S4.
Decomposed east, north, and up velocity components and associated uncertainties across the Jakarta metropolitan area.

Supplementary Animation S1.

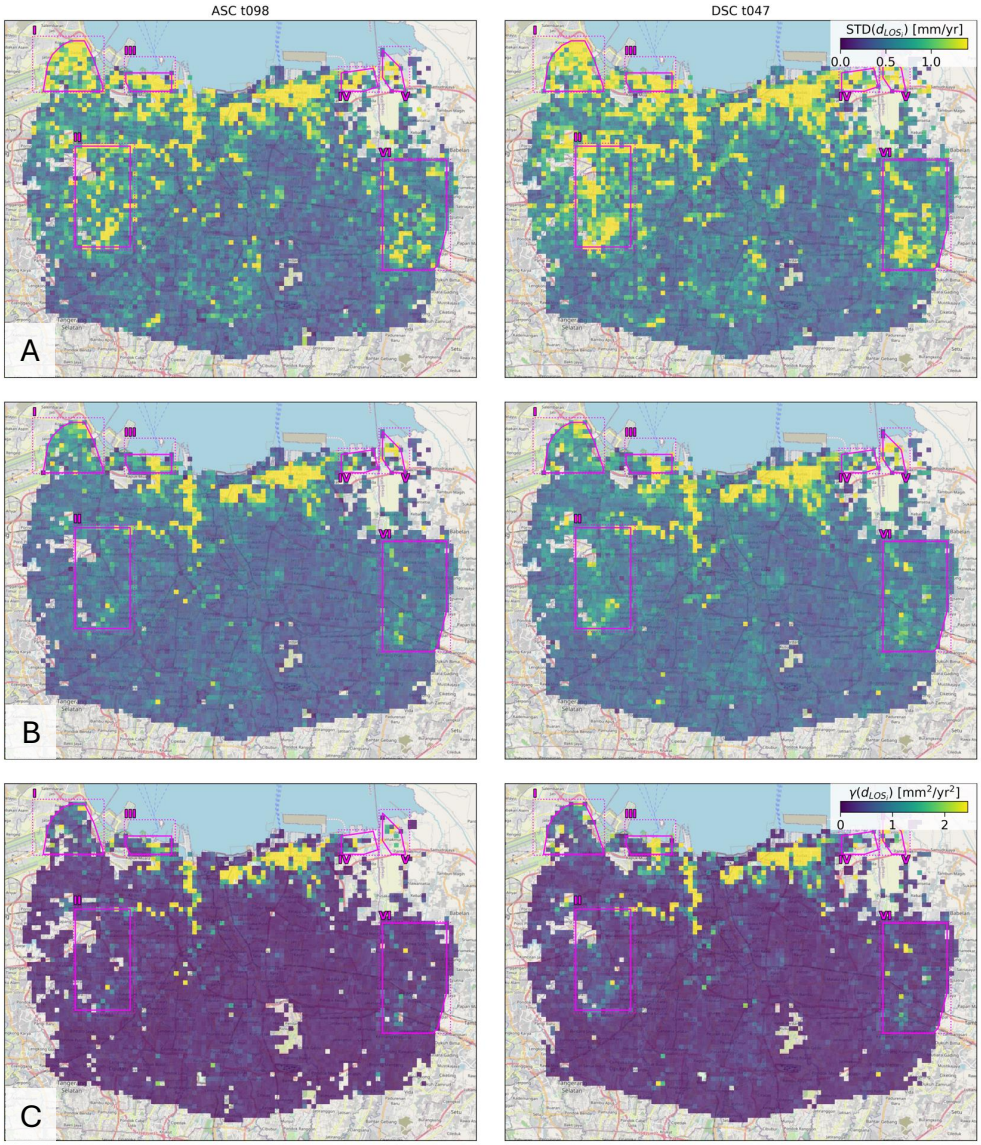


Figure S8: Intra-RUM LoS velocity variability assessment. The major subsidence bowls (outlined in turquoise in Fig. 4) are highlighted in magenta. **Row A:** Standard deviation of original ascending (left) and descending (right) LoS velocities at the RUM level. **Row B:** Standard deviation of residual velocities after removing a planar trend within each RUM. After plane removal, 88% of RUMs have $\sigma < 1$ mm/yr, with the largest reductions in the subsidence bowls, indicating long-wavelength, spatially coherent motion. **Row C:** Semivariance of residual velocities computed at a distance lag of $h \approx 60$ m, showing spatial correlation at short distances. Again, 88% of the AOI exhibits low semivariance ($\gamma < 0.8$ mm^2/yr^2), while northeastern and northern coastal regions (yellow) retain higher residuals, suggesting subsidence there is not dominated by a uniform, deep-seated mechanism.

Iterative estimation of the ascending-track datum offset used for inter-track datum alignment. The animation shows the transversal (top left) and normal (top right) velocities obtained from the strapdown decomposition, together with their standard deviations (bottom panels), as the ascending-track velocity is incrementally shifted by 0.1 mm/yr. The optimal inter-track datum alignment is obtained at an offset of 1.2 mm/yr, corresponding to the minimum number of negative transversal velocities.

References

[1] W. S. Brouwer, R. F. Hanssen, Estimating Three-Dimensional Displacements with InSAR: The Strapdown Approach, J. Geod. 98 (2024) 110. https://doi.org/10.1007/s00190-024-01918-2.

[2] W. S. Brouwer, R. F. Hanssen, A Treatise on InSAR Geometry and 3-D Displacement Estimation, IEEE Trans. Geosci. Remote Sens. 61 (2023) 1–11. https://doi.org/10.1109/TGRS.2023.3322595.

[3] P. J. G. Teunissen, Testing Theory: An Introduction, TU Delft Open, 2024.