# The magnitude of equilibrium isotope fractionation of Mg between forsterite, diopside and melt at liquidus temperatures.

Bram de Winter[a,*], Andrew M. Walker[a], Elena Melekhova[a], Xiao-Ning Liu[b], Tim Elliott[b],

[a] Department of Earth Sciences, University of Oxford, South Parks Road, Oxford, OX1 3AN, UK

[b] School of Earth Sciences, University of Bristol, Wills Memorial Building, Queen's Road, Bristol, BS8 1RJ, UK

[*]Corresponding Author, bram.dewinter@earth.ox.ac.uk

# The magnitude of equilibrium isotope fractionation of Mg between forsterite, diopside and melt at liquidus temperatures.

Bram de Winter[a,*], Andrew M. Walker[a], Elena Melekhova[a], Xiao-Ning Liu[b], Tim Elliott[b],

[a] *Department of Earth Sciences, University of Oxford, South Parks Road, Oxford, OX1 3AN, UK*

[b] *School of Earth Sciences, University of Bristol, Wills Memorial Building, Queen's Road, Bristol, BS8 1RJ, UK*

[*]*Corresponding Author, bram.dewinter@earth.ox.ac.uk*

## Abstract

We examine the equilibrium fractionation of Mg isotopes between forsterite, diopside, and a coexisting melt at liquidus temperatures using a combination of analyses of petrological-experiment products and atomic-scale simulations. Our experiment yields $\Delta^{26}Mg_{ol/melt}$ = -0.058 ± 0.032 ‰ (2s.e.) and $\Delta^{26}Mg_{cpx/melt}$ = 0.060 ± 0.034 ‰ (2s.e.) for crystals grown from a near-cotectic basaltic melt in the CMAS system, which combine to give $\Delta^{26}Mg_{cpx/ol}$ = 0.131 ± 0.045 ‰ at 1300 °C. The value of $\Delta^{26}Mg_{ol/melt}$ is within the uncertainty of the mean olivine-melt fractionation determined for unzoned phenocrysts and naturally quenched glass from ocean island and mid-ocean ridge basalts. We compare the experimentally determined Mg isotope fractionation between olivine and clinopyroxene with *ab initio* calculations using different DFT functionals. We demonstrate that when using the revised Perdew–Burke–Ernzerhof (PBESOL) exchange-correlation functional, accounting for thermal expansion, and site-averaging for forsterite, our ab initio results are in good agreement with our experiments, yielding $\Delta^{26}Mg_{cpx/ol}$ = 0.134‰ at 1300°C. Using the Local Density Approximation (LDA) or other Generalised Gradient Approximation (GGA) functionals, or neglecting thermal expansion, lowers $\Delta^{26}Mg_{cpx/ol}$ values to approximately 0.03–0.06 ‰ below the experimentally measured values. Neglecting site-averaging in forsterite results in positive (using only M1) or negative (using only M2) deviations in fractionation of 0.08‰ from averaged isotope ratios. Comparison of

27  our experimentally and theoretically derived $\Delta^{26}Mg_{cpx/ol}$ values with empirical estimates from

28  natural samples reveals a systematic offset, underscoring the need to distinguish equilibrium

29  mineral–mineral fractionation from empirically derived relationships that may incorporate

30  kinetic or compositional effects.

31  Keywords: Mg isotopes, equilibrium isotope fractionation, density functional theory, high-

32  temperature experiments.

## 1. Introduction

34  Atomic-scale simulations are increasingly used to provide information on isotopic fractionation

35  driven by deep-Earth and planetary processes (e.g Young et al., 2015). Validating these

36  simulations has been challenging due to the small, predicted effects (Blanchard et al., 2017;

37  Schauble, 2011) relative to the limits of traditional analytical reproducibility and the difficulty

38  of acquiring suitable natural samples or experiments that demonstrate pure equilibrium isotope

39  fractionation. Here, we focus on the relatively simple case of equilibrium fractionation of

40  magnesium isotopes between high-temperature silicate phases at ambient pressure. Magnesium

41  is a major rock-forming element, representing a fundamental building block of geological

42  reservoirs. The stable isotopes of magnesium (approx. 79% $^{24}Mg$, 10% $^{25}Mg$, 11% $^{26}Mg$)

43  exhibit a notable relative mass difference of up to 8%, which promotes significant isotopic

44  fractionation, as has been documented in igneous systems that can operate on planetary scales

45  (Hin et al., 2017; Sedaghatpour & Teng, 2016; Teng et al., 2010).

46  Atomic-scale simulations based on density functional theory (DFT) suggest significant

47  equilibrium fractionation of Mg isotopes among major mantle minerals (e.g. Huang et al., 2013;

48  Schauble, 2011; Wang et al., 2023), broadly consistent with observations of Mg isotopic

49  differences in apparently equilibrated natural samples (Young et al., 2009). While such

50  simulations are ideally *ab initio* (i.e., based on first principles without adjustable parameters),

51  important choices must be made that may affect their reliability. For example, it is necessary

52  to choose the exchange-correlation functional and to decide how to incorporate thermal

53  expansion or the presence of different crystallographic sites in the minerals being studied.

54  Previous studies have made use of the local density approximation (LDA; Perdew & Zunger,

55  1981) or the PBE (PBE; Perdew et al., 1996), semi-local generalised gradient approximation

56  (GGA) for exchange-correlation functional, but newer functionals are now routinely available

57  (e.g. PBESOL; Perdew et al., 2008). PBESOL was created to model the equilibrium properties

58  of solids better and has proven to more accurately reproduce the lattice parameters and elastic

59  properties of silicate minerals than previous GGA functionals. Moreover, many studies have

60  overlooked the effect of thermal expansion. Wang et al. (2023) demonstrate that thermal

61  expansion alters the equilibrium fractionation of Mg isotopes between different minerals.

62  Given the sensitivity of equilibrium isotope fractionation to both exchange-correlation

63  functional and thermal expansion, thorough validation against well-constrained measurements

64  is needed.

65  Analysis of natural samples, including inter-mineral Mg isotope fractionations preserved in

66  mantle peridotites, as well as mineral-melt isotope fractionations recorded in mid-ocean ridge

67  basalts (MORB), ocean island basalts (OIB), and chondritic meteorites, has provided an

68  empirical foundation for understanding high-temperature isotope fractionation in planetary

69  materials (e.g. Pogge von Strandmann et al., 2011; Stracke et al., 2018; Teng et al., 2010; Yang

70  et al., 2009). Early studies provided valuable information but were limited in their ability to

71  resolve these effects because equilibrium fractionations at magmatic temperatures are small

72  and approach the precision limits of sample-standard bracketing techniques (Teng et al., 2015).

73  Recent development of the critical mixture double-spiking technique (Coath et al., 2017) has

74  substantially improved analytical reproducibility, enabling more robust detection of subtle Mg

75   isotope fractionations (Liu et al., 2023) and small but significant Mg isotope differences

76   between chondrites and Earth (Hin et al., 2017).

77   Interpreting isotopic variations requires well-constrained equilibrium fractionation factors,

78   especially the key equilibrium melt-solid fractionation factors. Particularly, the recent

79   argument of the widely occurring diffusion-driven Mg isotope fractionations in the MORB

80   samples was based mainly on the empirically determined non-zero melt-olivine fractionation

81   factor (Liu et al., 2024, EPSL), while others, adopting a zero value of melt-olivine fractionation

82   factor, concluded equilibrium isotope fractionations (Soderman et al., 2024). Despite this, a

83   non-zero melt-olivine fractionation factor was carefully determined previously (Liu et al.,

84   2022) given the difficulties in obtaining fully equilibrated glass-mineral pairs from natural

85   samples and the fact that diffusion processes can easily influence Mg isotopes (Lai et al., 2015;

86   Richter et al., 2009; Teng et al., 2011), further constrains from theoretical prediction, and

87   petrological experimental work are necessary. Direct comparison between measured Mg

88   isotope fractionation in natural samples and ab initio calculations of equilibrium fractionation

89   remains nontrivial.

90   Petrological experiments offer an alternative method for studying equilibrium isotope

91   fractionation, as they theoretically enable control over key variables like temperature, pressure,

92   and composition. However, in practice, this potential is not always achieved because

93   experimental samples, like natural ones, can experience kinetic fractionation, especially in the

94   form of Soret diffusion, caused by temperature gradients within the experiments, as reported

95   by Liu et al. (2022). The Soret effect is a thermodiffusion process in which isotopes migrate

96   along a temperature gradient, with heavier isotopes tending to concentrate on the cooler side

97   and can impose very significant isotopic fractionations (Richter et al., 2008). To address this,

98   experiments should explicitly aim to minimise kinetic effects by ensuring minimal thermal

99   gradients across the experimental charge and by homogenising initial compositions. The

100 current lack of controlled studies that can truly isolate equilibrium isotope fractionation

101 between major silicate minerals and co-existing melt highlights the necessity for such research.

102 This study assesses the influence of various DFT parameters on calculated equilibrium isotope

103 fractionation factors for Mg between forsterite-melt, diopside-melt, and forsterite-diopside, by

104 comparing modelling results with experimental results. Forsterite and diopside were

105 synthesised at near-liquidus conditions at 1 atm in the CMAS system (Ca-Mg-Al-Si).

106 Additionally, DFT calculations are performed from 0 to 4000 K at 1 atm, using different

107 exchange-correlation functionals, site-averaging methods, and thermal expansion factors

108 (following the approach of Walker et al. (2025)) to calculate isotopic differences between

109 forsterite and diopside. These paired experimental and theoretical results provide a basis for

110 evaluating Mg isotope fractionation at high temperatures.

## 2. Methods

112 We use two complementary methods to assess equilibrium Mg isotope fractionation between

113 forsterite and diopside. We do this because atomic-scale simulations are most reliable for

114 fractionation between crystalline solids; in this case, the fractionation is driven by mass-

115 dependent changes in crystal vibrations, which lattice dynamics can describe. This approach is

116 not directly applicable to liquids. In our first approach, we used samples from a pair of

117 experiments in which we grew forsterite or diopside crystals from a melt composition at a

118 temperature designed to leave a residual melt near the CMAS cotectic. We measured

119 $\Delta^{26}Mg_{ol/melt}$ and $\Delta^{26}Mg_{cpx/melt}$. Because the residual melt compositions are similar, we can use

120 these experiments to determine $\Delta^{26}Mg_{cpx/ol}$. Since diopside and forsterite are endmembers of

121 clinopyroxene (cpx) and olivine (ol), we label this fractionation as $\Delta^{26}Mg_{cpx/ol}$ (eq. 1)

122 throughout the text for consistency with literature conventions:

$$\Delta^{26}\mathrm{Mg}_{\underset{ol}{cpx}} = \Delta^{26}\mathrm{Mg}_{\underset{melt}{cpx}} - \Delta^{26}\mathrm{Mg}_{\underset{melt}{ol}} =$$

$$\left( \frac{\frac{^{26}Mg}{^{24}\mathrm{Mg}}_{cpx}}{\frac{^{26}Mg}{^{24}\mathrm{Mg}}_{melt}} \right) - \left( \frac{\frac{^{26}Mg}{^{24}\mathrm{Mg}}_{ol}}{\frac{^{26}Mg}{^{24}\mathrm{Mg}}_{melt}} \right) \qquad (1)$$

123    Our experiments are designed to minimise the influence of non-equilibrium isotope

124    fractionation processes. We aimed to eliminate the effects of Soret diffusion and Fe-Mg

125    interdiffusion by working in an iron-free system with minimal temperature gradients to

126    minimize soret diffusion, and by using long durations to ensure phase homogeneity. With this

127    approach, we create a situation designed to achieve near-equilibrium isotope fractionation.

128    In our second approach, we utilise atomic-scale simulations to constrain the equilibrium

129    fractionation of $^{24}$Mg relative to $^{26}$Mg in cpx and ol as a function of temperature. By design,

130    these simulations yield only equilibrium fractionation and are not sensitive to other processes

131    that cause isotopic fractionation. In this approach, $\Delta^{26}\mathrm{Mg}_{cpx/ol}$ is derived from the reduced

132    partition function, ß (X, $^{24}$Mg, $^{26}$Mg), which is the equilibrium constant for the isotopic

133    exchange reaction between the phase of interest, X, and an ideal gas (Urey, 1947). The

134    equilibrium isotope fractionation factor, between two solid mineral phases (cpx and ol) and

135    two isotopes of an element ($^{24}$Mg, $^{26}$Mg) can be determined as the ratio of ß (X, $^{24}$Mg, $^{26}$Mg),

136    or as reduced partition functions or as the difference in expected measured isotopic content:

$$\Delta^{26}Mg_{\underset{ol}{cpx}}(DFT) \approx (\ln\left(\beta(\mathrm{Di}, {}^{24}Mg, {}^{26}Mg) - \ln(\beta(\mathrm{Fo}, {}^{24}Mg, {}^{26}Mg))\right)$$

$$(2)$$

137    where $\Delta^{26}\mathrm{Mg}_{cpx/ol}$ is the isotopic difference between cpx and ol. In our calculations, $\beta$ is

138    obtained from the phonon density of states via atomic-scale simulations. However, important

139    choices must be made when undertaking these calculations, and these have not been directly

140    compared with isotopic measurements. Our combined approach offers an opportunity to

141    explore the impact of these choices and to validate the overall computational approach in

142    situations where experiments are more challenging.
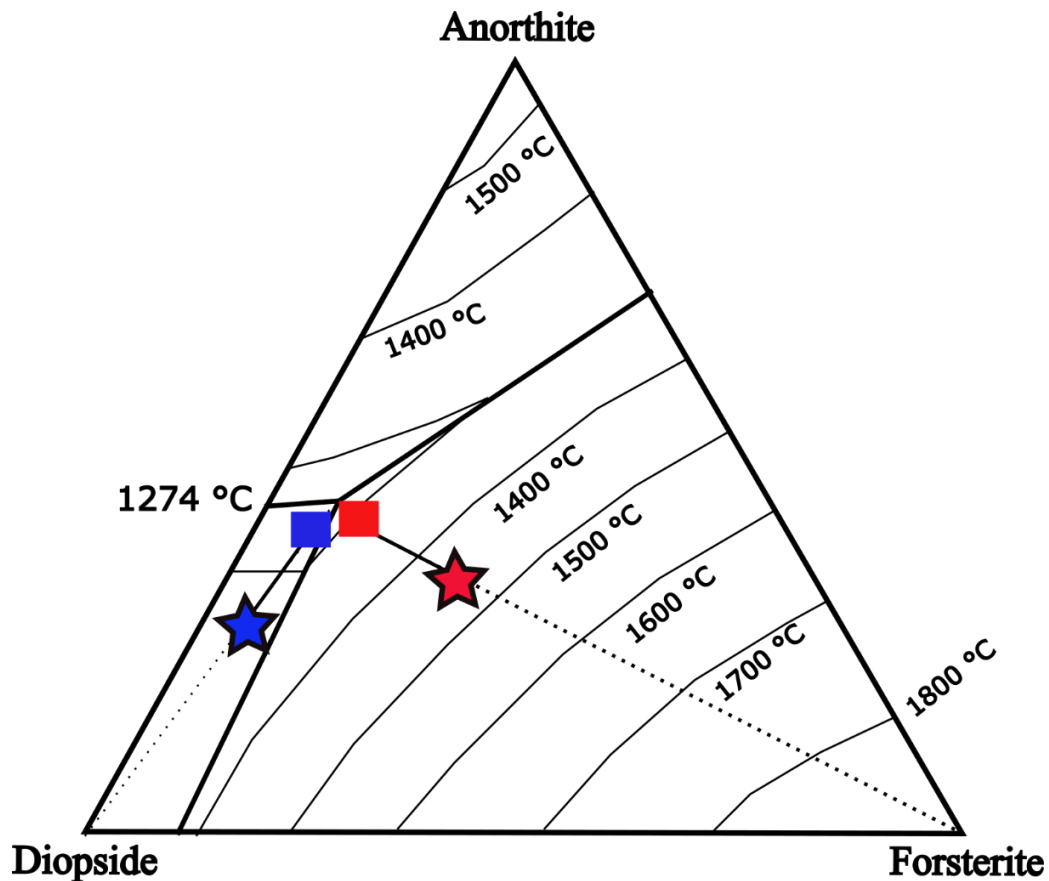
143    *2.1 Experiments*



**Figure 1**, Ternary diagram of Diopside-Anorthite-Forsterite after Morse (1980).

Starting composition (stars) and the measured residual melt (squares) are joined by

tie lines for experiments that crystallise diopside (blue) and forsterite (red).

144    We synthesised forsterite and diopside crystals from starting compositions within the CaO-

145    MgO-Al2O3-SiO$_2$ (CMAS) system. We selected starting compositions and equilibration

146    temperatures near the liquidus to achieve melt fractions of 65 vol.% and 80 vol.% for diopside

147    and forsterite experiments, respectively, to keep the residual melt composition close to the

148    eutectic (Figure 1).

149 Starting compositions were synthesised using high-purity oxide and carbonate reagents:

150 calcium oxide (CaO), magnesium oxide (MgO), aluminium oxide ($Al_2O_3$), silicon dioxide

151 ($SiO_2$), and calcium carbonate ($CaCO_3$). All oxides were subjected to a drying process at

152 1000°C for 12 hours to eliminate any absorbed moisture ($H_2O$). The dried oxides and

153 carbonates were then accurately weighed, mixed and ground for 30 minutes to ensure a uniform

154 distribution of components. Following this grinding, $CaCO_3$ was added, and the starting

155 mixture was then decarbonated at 1000°C overnight. After decarbonation, the mixture was

156 subjected to a second grinding to enhance homogeneity. Starting composition mixtures were

157 glassed at 1375°C for glass BDW-S2 (used to grow Di) and 1500°C for glass BDW-S1 (used

158 to grow Fo) for 2 hours in a Gera vertical box furnace (HTRV 70-250/18) at the Earth Science

159 Department of the University of Oxford. Subsequently, the glassed starting composition were

160 quenched in water. To ensure a consistent and homogeneous starting composition, two cycles

161 of melting and grinding were performed (Table 1).

**Table 1.** Experimental starting composition measured by EPMA at the University of Oxford. Elemental concentrations are given as wt% oxide.

| Experiment | $n^a$ | MgO | s.d | $SiO_2$ | s.d | $Al_2O_3$ | s.d | CaO | s.d | Total |
|---|---|---|---|---|---|---|---|---|---|---|
| BDW-S2 (Di) | 12 | 15.43 | 0.17 | 50.86 | 0.22 | 10.36 | 0.13 | 22.96 | 0.13 | 99.62 |
| BDW-S1 (Fo) | 25 | 21.36 | 0.13 | 47.15 | 0.18 | 12.37 | 0.1 | 17.59 | 0.09 | 99.47 |

$^a$Compositions are given as the average of n analyses.

162

163 The crystal growth experiments were conducted in a vertical furnace under atmospheric

164 pressure in air. A "chandelier" assembly was designed to accommodate four platinum loops,

165 each containing a mixture of starting material and a small amount of PVA glue to ensure

166 attachment of the starting material to the loop. In prior experiments, the hot spot and

167 temperature gradient in the furnace were carefully calibrated. We observed a 2 °C temperature

168 gradient over a 10 cm vertical distance within the hotspot using an external Type B

169 thermocouple. The beads in our setup are spaced 1 cm apart. Assuming similar thermal

170     gradients along the horizontal axis, we expect temperatures to vary by <0.2 °C between beads

171     within a single experiment.

172     A "chandelier" was positioned at the vertical hotspot at $1500 \pm 2.5$ °C for 2 hours to ensure

173     thermal equilibration. Subsequently, the temperature was gradually decreased to the target

174     endpoint at a controlled rate of 1 °C/min, as outlined by Mallmann & O'Neill (2009). The

175     furnace was then held at the final temperature (Table 2) for seven days to allow the growth of

176     crystals exceeding 100 μm. The experiments were quenched in water. Subsequently, the

177     quench beads were extracted, mounted in Araldite epoxy resin, and first polished with abrasive

178     paper and then with a series of diamond pastes. In Figure 2, we present backscattered SEM

179     images of two run products, BDW-S2-1 (Di) and BDW-S1-4 (Fo).

180     The experimental numbering scheme sequentially indicates: the starting composition (BDW-

181     S1 or BDW-S2), the experimental run (e.g., BDW-S2-1), the bead from each experimental run

182     (e.g., BDW-S2-1-1), and a letter for the individual drill site (e.g., BDW-S2-1-1A).

183     *2.2 Analytical techniques*

184     The morphology and size of recovered forsterite and diopside crystals were determined using

185     a FEI Quanta 650 scanning electron microscope (SEM) at the Department of Earth Sciences,

186     University of Oxford. Backscatter images of all recovered beads are given in Supplementary

187     Figure S1-1.

188     The major element compositions of starting compositions and experimental run products were

189     analysed by Electron Microprobe Analysis (EMPA) using a CAMECA SX-5 FE system at the

190     University of Oxford's Department of Earth Sciences, operating at 10 nA and 20 kV with a spot

191     size of 1 μm. For calibration, we used natural albite (Si, Al, Mg) and andradite (Ca) standards.

192     To ensure that experimental run products are homogeneous, transect lines were set up across

193     minerals and melt pools (see Supplementary Figure S1-2).

194    For magnesium isotope analysis, beads BDW-S1-4 (Fo) and BDW-S2-1 (Di) were chosen

195    because they contained the largest mineral phases (Supplementary Figure S1-1). The material

196    drilling and isotope analysis follow the procedures detailed by Liu et al. (2022, 2023). In brief,

197    a New Wave Research microdrill was used to obtain two samples each of forsterite and

198    diopside, as well as four samples of silicate melt from BDW-S2-1 (Di) and two from BDW-

199    S1-4 (Fo). The sample material was drilled in a droplet of approximately 5 μL of Milli-Q water

200    placed on the surface mount. The water containing the drilled powder was then recovered using

201    a pipettor and transferred to a cleaned Teflon beaker. The drilled samples were subsequently

202    digested in a mixture of ultra-pure concentrated $HNO_3$, HCl, and HF in a 3:1:1 volume ratio

203    on a hotplate at 150 °C. Following complete digestion, the samples were dissolved in 1 M

204    $HNO_3$ for magnesium column chemistry. Magnesium was purified using two-column cation-

205    exchange chromatography with BioRad AG50W-X12 resin. Aliquots of 1 mL of eluent were

206    taken before and after the Mg collection window to check the yield, which exceeded 99.8% for

207    all samples. Magnesium isotope measurements were performed on a Thermo-Finnigan

208    Neptune MC-ICPMS. Jet sample cone and H skimmer cone were used. The sample solution

209    was aspirated into the mass spectrometer in a 0.3 M HNO3 solution containing 1 μg/ml Mg,

210    using the combination of a Savillex PFA nebuliser and Apex HF (Element Inc.). The

211    Instrumental mass bias is corrected through the $^{25}Mg$-$^{26}Mg$ critical mixture double spike

212    method (Coath et al., 2017; Hin et al., 2017; Liu et al., 2023). Mg isotope data are reported as

213    $\delta^{26}Mg$ DSM-3 (the relative difference of $^{26}Mg/^{24}Mg$ between the sample and the reference

214    standard DSM-3), and are subsequently abbreviated as $\delta^{26}Mg$. Analyses of the rock standard

215    BHVO-2 and BIR-1 yielded a $\delta^{26}Mg$ value of -0.206±0.035‰ and -0.206±0.023‰,

216    respectively, consistent with the previous reports (He et al., 2022; Liu et al., 2023)

217        *2.3 First-principles calculations*

218   The *ab initio* approach for isotope fractionation is similar to previous studies of Mg isotope

219   fractionation (Huang et al., 2013; Schauble, 2011; Wang et al., 2023; Wu et al., 2015; Young

220   et al., 2009) as well as other isotope systems (Blanchard et al., 2009; Javoy et al., 2012; Li et

221   al., 2009; Li & Liu, 2011; Rustad & Dixon, 2009). To calculate $\Delta^{26}Mg_{cpx/ol}$, we use plane waves

222   and pseudopotential (Payne et al., 1992) approach to density functional theory (DFT:

223   Hohenberg & Kohn, 1964; Kohn & Sham, 1965) and lattice dynamics in CASTEP (Clark et

224   al., 2005). Our reference calculations are undertaken in two steps. First, we determine the

225   equilibrium structure of forsterite and diopside. These calculations were performed using a

226   generalised gradient approximation functional designed to give improved equilibrium

227   properties of solids (PBESOL; Perdew et al., 2008), and initial crystal structures of forsterite

228   and diopside were obtained from the American Mineralogist Crystal Structure Database

229   (Downs & Hall-Wallace, 2003). These structures were refined by minimising the static energy

230   with respect to atomic positions and cell parameters, with convergence assumed when the

231   maximum force on each atom was below $1.0 \times 10^{-4}$ eV/ang, maximum stress 0.05 GPa and total

232   energy changes less than $1.0 \times 10^{-5}$ eV. All our calculations were performed with norm-

233   conserving pseudopotentials for core electrons and the 2p electrons for O, the 3s and 3p

234   electrons for Si, and the 3s electrons for Ca and Mg included in the valence. The electron

235   density was expanded on a plane-wave basis with a cutoff energy of 1000 eV and sampled in

236   reciprocal space with 4×2×4 and 4×4×2 Monkhorst-Pack grids (Monkhorst & Pack, 1976) for

237   forsterite and diopside, respectively (these parameters were chosen by convergence testing of

238   the phonon frequencies).

239   In the second step, we calculate the phonon frequencies of both minerals with one magnesium

240   atom substituted for either the heavy ($^{26}$Mg) or light ($^{24}$Mg) isotope and the masses of all other

241   atoms set according to their natural isotopic abundances. We used variational Density

242   Functional Perturbation Theory (DFPT: Gonze, 1997; Gonze & Lee, 1997; Refson et al., 2006)

243 to calculate phonon frequencies on a shifted grid (to include the gamma point) in reciprocal

244 space, as used for the expansion of the electronic wavefunctions. These were supplemented

245 using Fourier interpolation (Giannozzi et al., 1991) to interpolate frequencies at wave vectors

246 between those included in the DFPT calculation. We calculated the ß (X, Y, Y*) for diopside

247 and forsterite:

$$\beta(X, Y, Y^*) = \prod_{i=1}^{n^q} \left[ \prod_{j=1}^{3N^{at}} \left( \frac{\omega_{i,j}^*}{\omega_{i,j}} \frac{e^{-h\omega_{i,j}^*/(2kT)}}{1 - e^{-h\omega_{i,j}^*/(2kT)}} \frac{1 - e^{-h\omega_{i,j}/(2kT)}}{e^{-h\omega_{i,j}/(2kT)}} \right) \right]^{w_i} \qquad (3)$$

248

249 (Kieffer, 1982; Schauble, 2004), where $\omega_{i,j}$ and $\omega^*_{i,j}$ are the vibrational frequencies calculated

250 for the two different isotopes in phase X at the $i^{th}$ reciprocal lattice sampling point for $j^{th}$ branch

251 within the simulation cell that contains $N_{at}$ atoms in the crystal unit cell. T is the temperature

252 in Kelvin, and $k$ is Boltzmann's constant. At a large grid of $N^q$ points sampled in the first

253 Brillouin Zone, we run the second product of Eq. (3) over all modes. We utilised the symmetry

254 of the reciprocal lattice to reduce computational costs. This symmetry is applied to equivalent

255 points with weighting factors $w_i$, ensuring proper accounting for points on the edges of the

256 sampled irreducible volume. The aim is, therefore, to compute $\omega_{i,j}$ and $\omega^*_{i,j}$ with enough

257 accuracy within the available computational limitations.

258 The reference calculations are supplemented by others where different choices are made for

259 the calculation of equilibrium isotope fractionation. We alter the exchange correlation

260 functional using the LDA (Perdew & Zunger, 1981), or a common generalised gradient

261 approximation due to PBE (Perdew et al., 1996). We also explore altering the site in forsterite

262 where the Mg isotope substitution is made. Duan et al. (2023) show that accounting for the

263 presence of two different Mg sites in forsterite is important when calculating isotope

264     fractionation factors. These sites have different polyhedron volumes, affecting isotope

265     fractionation up to 0.5‰ at 900 K (Duan et al., 2023).

266     Finally, we account for the thermal expansion of the forsterite and diopside crystals. In this

267     study, we employ the approach described by Walker et al. (2025) to investigate the differential

268     thermal expansion of forsterite and also apply it to diopside. For each cell volume, V

269     (calculated by performing geometry optimisation with various pressures while neglecting

270     temperature effects), we calculate phonon frequencies to evaluate the Helmholtz free energy.

271     The volume-energy data obtained are used to fit isothermal third-order Birch-Murnaghan

272     equations of state (EOS), incorporating temperature dependence for parameters such as the

273     zero-pressure volume ($V_0$), the zero-pressure bulk modulus ($K_0$), and its pressure derivative

274     ($K'_0$).

275     Before comparing with experimental data, it is essential to define the theoretical setup most

276     likely to produce accurate predictions of equilibrium isotope fractionation. In cases where

277     direct experimental data is unavailable, we consider the combination of the PBESOL

278     exchange–correlation functional, explicit thermal expansion treatment, and averaging across

279     the two distinct Mg sites in forsterite as the most physically sound and consistent

280     methodological approach. This setup offers the best overall representation of the structural and

281     vibrational properties in silicate minerals and is thus used as the reference model for further

282     analysis.

283     **3. Results**

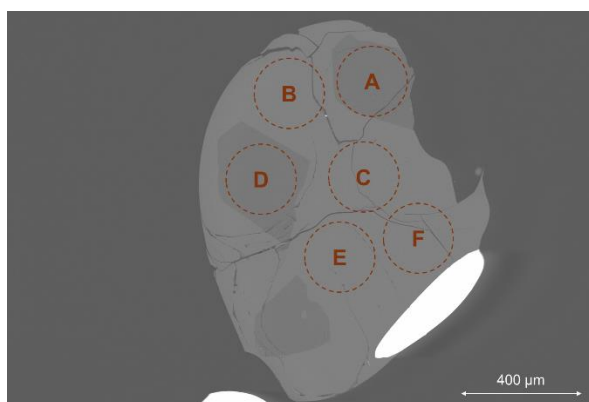284     *3.1 Experimental run products*

**Table 2,** Experimental run conditions, phase proportions and compositions of runs analysed for their isotopic compositions.

| Experiment | Phase | T (K) | Duration (days) | Phase proportions (wt%) | $n^a$ | MgO | $SiO_2$ | $Al_2O_3$ | CaO | Total | $n^a$ | $\delta^{26}Mg$ | 2 s.e. |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|

| | | | | n | | | | | Total | | n | | |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| *S2-1(Di)* | 1573 | 7 | Glass (64), Di (36) | | | | | | | | | | |
| | melt | | | 10 | 11.61 (5) | 49.11 (3.7) | 17.47 (9) | 22.21 (2.6) | 100.41 | | 12 | -1.372 | 0.023 |
| | diopside | | | 14 | 17.62 (2.7) | 52.93 (3.6) | 5.27 (8.1) | 25.01 (2.1) | 100.83 | | 12 | -1.312 | 0.023 |
| *S1-4 (Fo)* | 1560 | 7 | Glass (80), Di (20) | | | | | | | | | | |
| | melt | | | 10 | 13.86 (0.9) | 48.72 (2.3) | 15.7 (0.7) | 21.62 (0.6) | 99.9 | | 36 | -1.362 | 0.018 |
| | forsterite | | | 20 | 56.95 (2.4) | 42.7 (1.3) | 0.08 (0.1) | 0.68 (0.1) | 100.42 | | 18 | -1.42 | 0.025 |

[a] Compositions are given as the averages of *n* analyses. [b] Mass fraction phase proportions obtained by mass-balance calculations. Major element compositions reported as weight percentages with uncertainties given in parentheses as $10^{-1}$ (s.e.).

285    We selected the two beads with the biggest crystals for isotope analysis: BDW-S2-1 (Di),

286    comprising diopside crystals with diameters ≥ 400 μm, and BDW-S1-4 (Fo), containing

287    forsterite crystals with diameters ≥ 250 μm (Figure 2). Several additional experimental charges

288    were created during this study; however, most produced crystals too small for reliable

289    microdrilling or isotope analysis, leaving only two charges suitable for determining equilibrium

290    fractionation factors. A representative backscattered electron image (BSE) of a polished cross-

291    section is shown in Figure 2. Neither the melt nor the mineral phases show any heterogeneity,

292    despite the skeletal textures of the diopside crystals (Table 2 and Supplementary Figures S1-1,

293    S1-2). Mass balance calculations reveal that the mineral phases comprise 19.57 wt% for S1

294    (Fo) and 36.56 wt% for S2 (Di), within 1 wt% of the proportions expected by applying the

295    lever rule to the phase diagram shown in Figure 1.
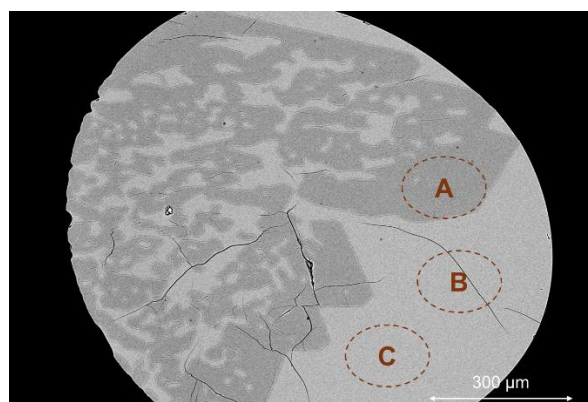


BDW-S1-4 (Fo)                                        BDW-S2-1 (Di)

**Figure 2,** BSE images of experimental run products: a) bead BDW-S1-4 containing three Fo crystals and b) bead BDW-S2-1 containing a large Di crystal. These beads were used for micro drilling and isotope analysis. Orange dotted circles show the drill sites with letters corresponding to isotope samples reported in Supplementary Table S1-1.

### 3.2 Experimental isotope analysis

Liu et al. (2022) observed that, in the experimental materials, the isotope ratio varied systematically with position within experimental charges that experience significant temperature differences, suggesting the occurrence of the Soret diffusion, making the experimental runs less reliable for providing convincing isotope fractionation factors. In contrast, our measurements (Supplementary Table S1-1) show nice homogeneity (2 s.e. = ± 0.025‰, comparable to the analytical precision limit of ± 0.027‰, Liu et al., 2023) across multiple sites within a single sample, in contrast to the up to 0.6 ‰ $\delta^{26}Mg$ variance seen in Liu et al. (2022). Therefore, we believe our samples do not exhibit thermal gradients or the Soret effect under the current analytical precision.

We drilled out a total of six melt samples across the beads (Figure 2, orange dotted circles). Individual measurements of drill sites are given in Supplementary Table S1-1. The average Mg isotope composition for each phase in each bead is reported in Table 2. Average $\Delta^{26}Mg$ for ol-melt and cpx-melt are $\Delta^{26}Mg_{ol/melt} = -0.058 \pm 0.032$ at $1573 \pm 2.5$ K and $\Delta^{26}Mg_{cpx/melt} = 0.060 \pm 0.034$ at $1560 \pm 2.5$ K. Assuming this fractionation varies as $1/T^2$ (where T is temperature in K) and tends to zero as the temperature tends to infinity (expected for equilibrium fractionation: Urey, 1947)) results in $\Delta^{26}Mg_{cpx/melt} = (1.49 \pm 0.84) \times 10^5/T^2$ and $\Delta^{26}Mg_{ol/melt} = (-1.44 \pm 0.79) \times 10^5/T^2$ (Fig. 3a&b). Our $\Delta^{26}Mg_{ol/melt}$ value is in good consistence with previous reported $\Delta^{26}Mg_{ol/melt}$ value obtained from naturally quenched olivine-glass pairs (Liu et al., 2022) (Fig. 3a). Furthermore, based on these obtained $\Delta^{26}Mg_{ol/melt}$ and $\Delta^{26}Mg_{cpx/melt}$ values, we can then

315    have a $\Delta^{26}Mg_{cpx/ol} = 0.118 \pm 0.045$ at an average temperature of $1566.5 \pm 6$ K, and yielding

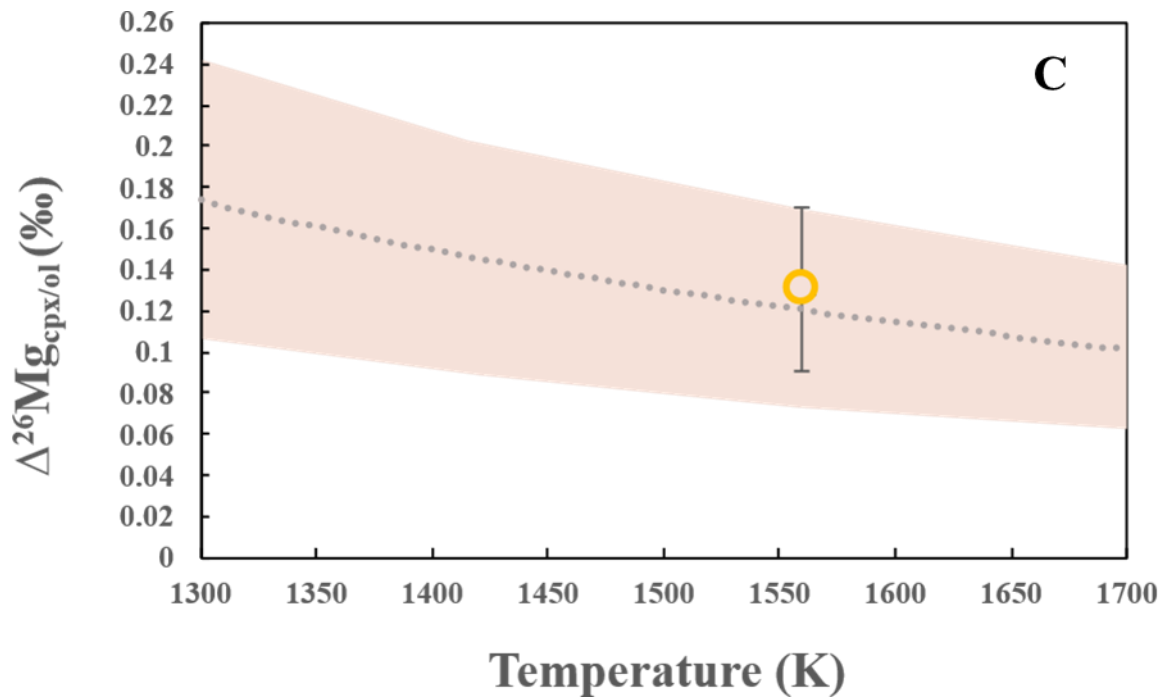316    $\Delta^{26}Mg_{cpx/ol} = (2.93 \pm 1.15) \times 10^5/T^2$ (Fig. 3c).
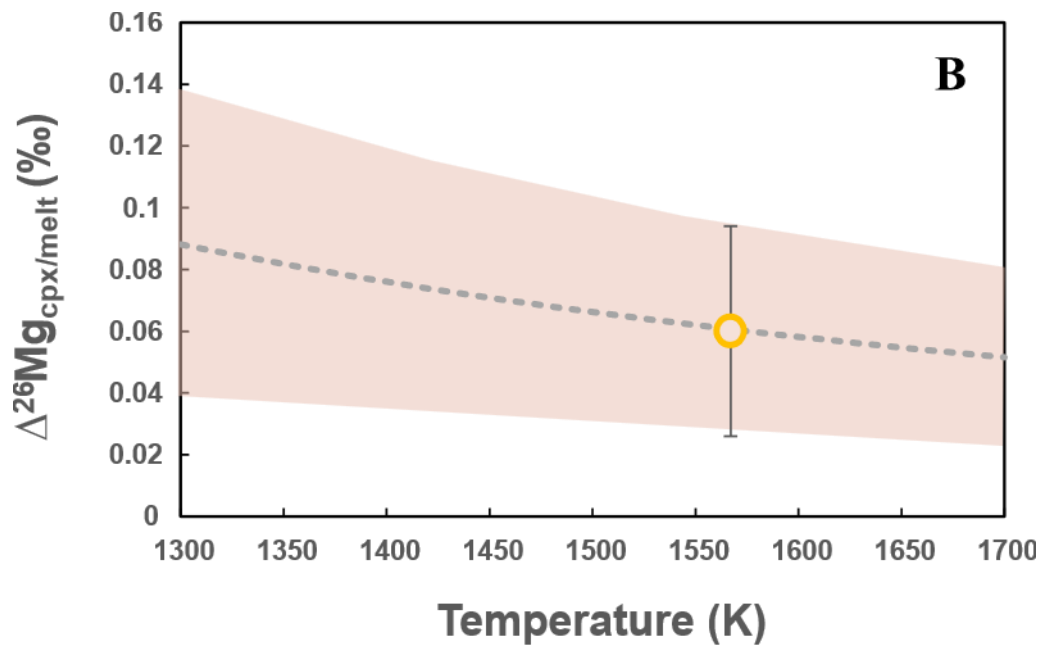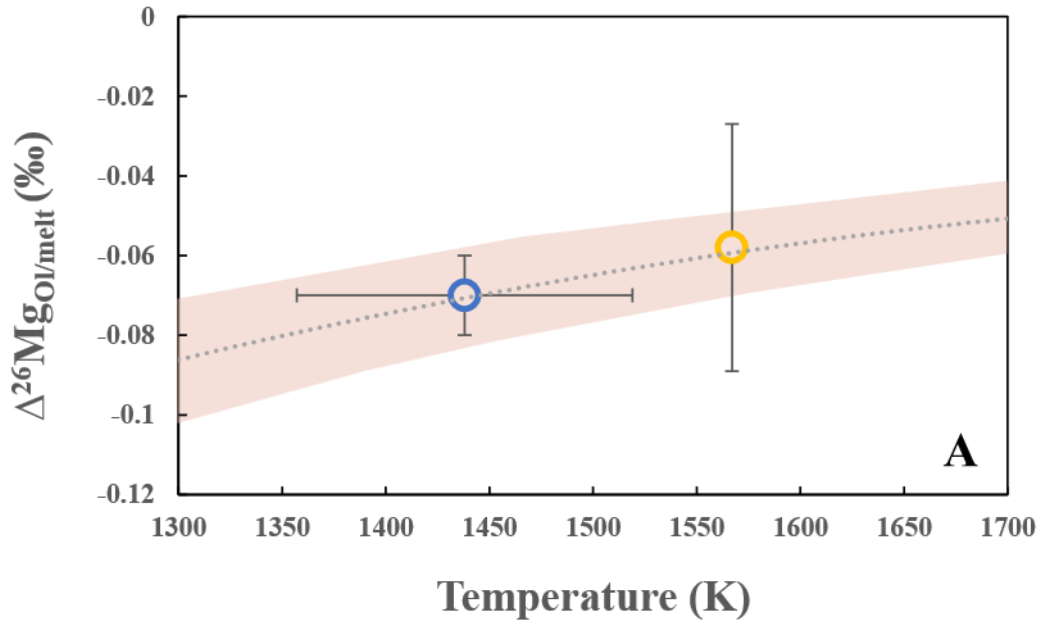
**Figure 3,** Mg isotopic difference between: (a) olivine-melt plotted against temperature for this study (yellow symbol) and compared with data from Liu et al. 2022 (blue symbol). Temperature uncertainties in experiments are expected to be < 2.5 K (°C) and therefore not plotted as error bars. Dashed line represents the estimated $\Delta^{26}Mg_{ol/melt}$ as a function of temperature from Liu et al. (2022). (b) clinopyroxene-melt plotted against temperature with $\Delta^{26}Mg_{cpx/melt}$ calculated in this study. (c) clinopyroxene-olivine plotted against temperature.

317     *3.3 Ab initio calculations*

318     First, we evaluate the influence of the chosen exchange-correlation functionals on the mineral

319     structures of diopside and forsterite. Our calculations were conducted using the LDA, GGA,

320     and PBESOL exchange-correlation functionals. Results following geometry optimisation show

321     that the calculated cell parameters (Table S2-2) and the Mg-O bond lengths (Table S2-1) for

322     the PBESOL functional are much closer to experimental values than those obtained with LDA

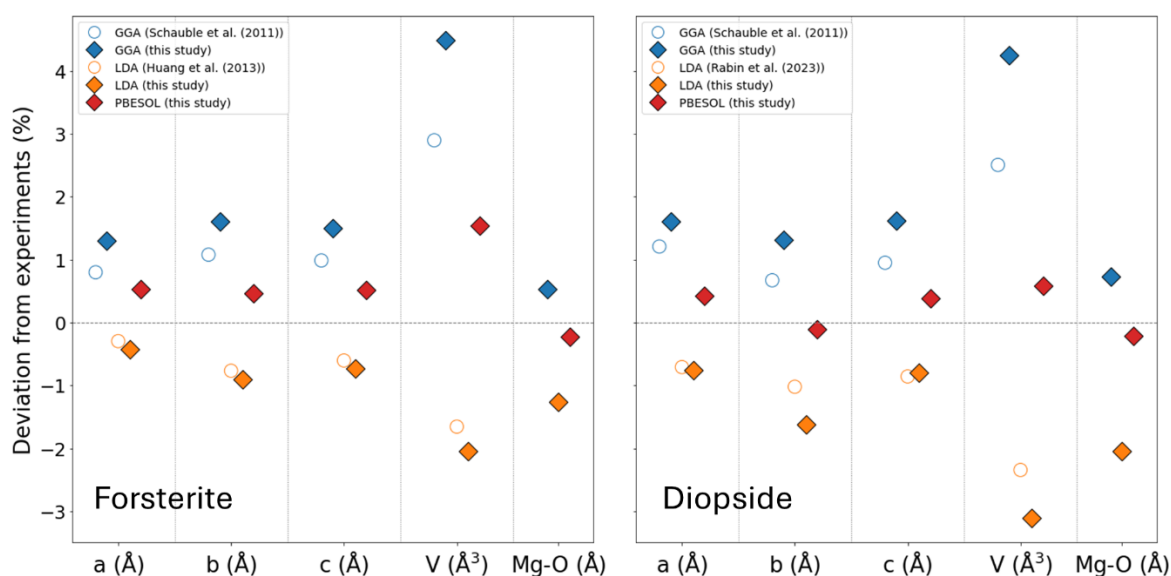323     or PBE functionals (Figure 4).

**Figure 4,** Deviation of calculated cell parameters and Mg–O bond lengths (Supplementary Table S2-2) from experimentally determined crystal structures, with static (0 K) DFT results compared to experimental studies at the lowest temperature found. Diopside at 10 K (Prencipe et al., 2000), forsterite at 77 K (Hazen, 1976). PBESOL shows the smallest deviation across all metrics, indicating better agreement with the experimental crystal structure.

324 Supplementary Figure S2-1 illustrates the temperature dependence of the averaged reduced

325 partition function (ß) of forsterite and diopside using $E_{xc}$ PBESOL, LDA and PBE compared

326 to previous studies. (Huang et al., 2013; Schauble, 2011; Wang et al., 2023). An overview of

327 the methodologies used in the literature is given in Supplementary Table 2-3. The polynomial

328 fit parameters of the ß-values calculated in this study are detailed in Table 3.

329 It is important to understand how the choice of exchange–correlation functional affects the

330 relative reduced partition functions that enter isotope fractionation factors, and to distinguish

331 this effect from differences that arise solely from changes in the calculated crystal structure.

332 To explore this, we conducted additional calculations using the PBESOL, PBE, and LDA

333 exchange-correlation functionals for forsterite while fixing the unit cell volume to its

334 experimental value. First, we used fixed-volume calculations for forsterite and observed

335    differences in ß($^{26}$Mg/$^{24}$Mg) of 0.04 ‰ (LDA) and -0.02 ‰ (PBE) relative to PBESOL. To

336    assess how structural differences influence isotope fractionation independently of the

337    exchange–correlation functional, we conducted PBESOL calculations to examine the effect of

338    variations in Mg–O bond lengths on the reduced partition function. Small bond length changes

339    were induced by applying different external pressures, which systematically altered the unit-

340    cell volume while maintaining a fixed functional. These calculations revealed a Mg isotope

341    fractionation sensitivity of 0.00375‰ for every 0.001 Å change in Mg–O bond length. Using

342    the sensitivity of Mg isotope fractionation to Mg–O bond length derived from the PBESOL

343    pressure-dependent calculations, and the differences in average Mg–O bond length between

344    the fixed-volume PBESOL, LDA, and PBE structures (Supplementary Table S2-1), we

345    estimate that only ~0.003‰ (LDA) and ~0.0006‰ (PBE) of the total offset can be attributed

346    to bond length differences. The remaining offsets, therefore, arise from the direct effect of the

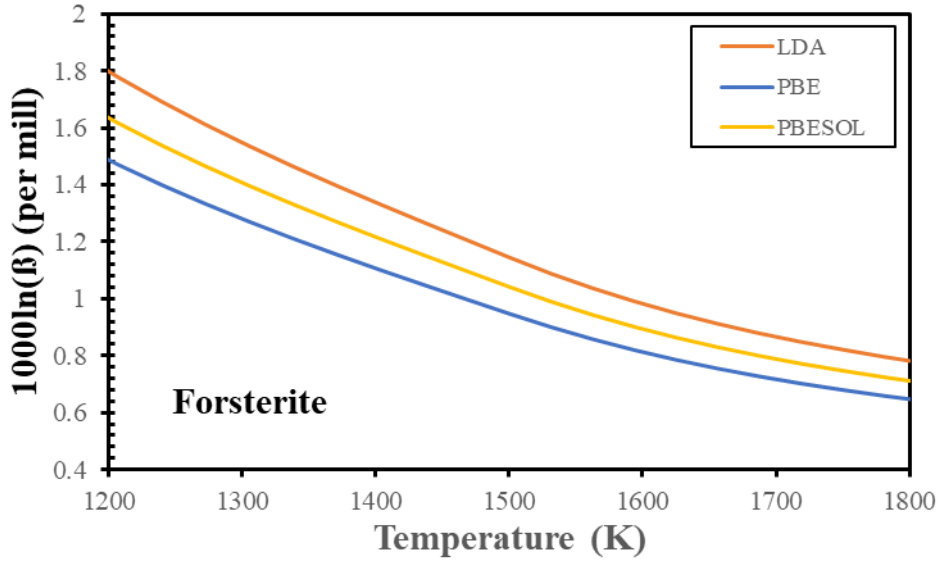347    exchange–correlation functional force constants.
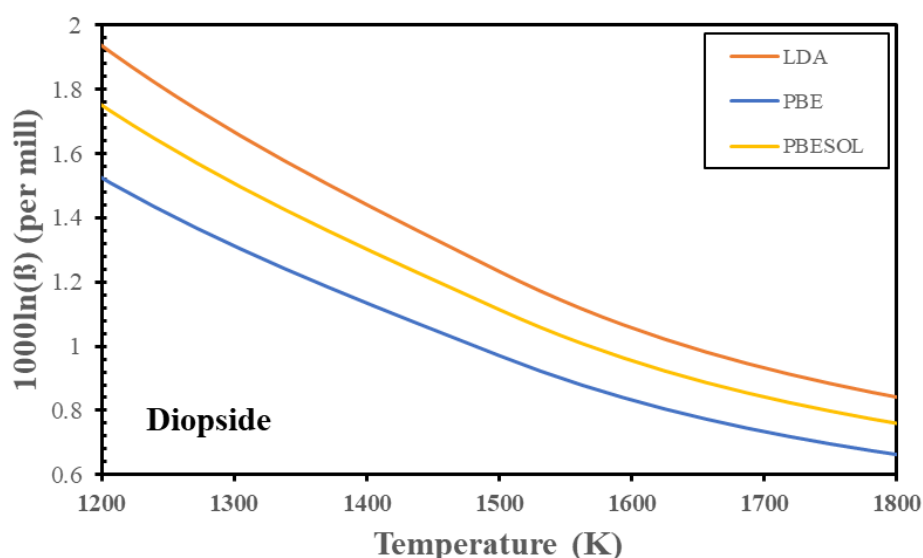
**Figure 5**, Reduced partitioning function for magnesium isotopes in a) diopside and b) Forsterite.

| | A | B | C |
|---|---|---|---|
| Forsterite PBESOL M1 | $2.809 \times 10^{14}$ | $-1.766 \times 10^{10}$ | $2.523 \times 10^{6}$ |
| *Forsterite PBESOL Average* | *$2.613 \times 10^{14}$* | *$-1.642 \times 10^{10}$* | *$2.346 \times 10^{6}$* |
| Forsterite PBESOL M2 | $2.416 \times 10^{14}$ | $-1.519 \times 10^{10}$ | $2.170 \times 10^{6}$ |
| Forsterite PBE | $2.325 \times 10^{14}$ | $-1.464 \times 10^{10}$ | $2.134 \times 10^{6}$ |
| Forsterite LDA | $2.447 \times 10^{14}$ | $-1.541 \times 10^{10}$ | $2.247 \times 10^{6}$ |
| Diopside PBESOL | $2.163 \times 10^{14}$ | $-1.565 \times 10^{10}$ | $2.518 \times 10^{6}$ |
| Diopside PBE | $1.535 \times 10^{14}$ | $-1.218 \times 10^{10}$ | $2.188 \times 10^{6}$ |
| Diopside LDA | $2.720 \times 10^{14}$ | $-1.880 \times 10^{10}$ | $2.783 \times 10^{6}$ |

**Table 3.** Polynomial fitted constants for $1000 \ln (\text{ß} (X, {}^{24}Mg, {}^{26}Mg) = AT^{-6}+BT^{-4}+CT^{-2}$ as a function of T in Kelvin from 1000-4000 K.

348   Here, we approach the different cation sites in forsterite, similar to Duan et al. (2023), where

349   we calculate the M1 and M2 sites and average them to produce a single $10^3 \ln\beta$ for $\delta^{26}Mg$ in

350   forsterite (Figure 6). We observe a 14% difference in $10^3 \ln\beta$ for $\delta^{26}Mg$ between the M1 and

351   M2 sites. Diopside has only one cation site for Mg, so it does not require averaging.

352   Lastly, recent studies have shown the impact of thermal expansion on phonon frequencies and,

353   consequently, on isotope fractionation. (Walker et al., 2025; Wang et al., 2023). Our calculated

354  temperature dependent third-order Birch-Murnaghan parameters were fitted to fifth-order

355  polynomials (Supplementary S2-4). These were then used to evaluate cell volume as a function

356  of temperature and pressure. In addition, we calculated ß as a function of temperature. We fitted

357  this to a polynomial in volume and temperature (Supplementary table S2-5). Figure 6 illustrates

358  the $10^3$ lnβ for $\delta^{26}$Mg for Fo and Di, accounting for thermal expansion. The correction for

359  thermal expansion is significant, as this slight change in unit-cell parameters leads to larger

360  differences in $\Delta^{26}$Mg$_{cpx/ol}$ values. Our thermal expansion corrections yield average the thermal

361  expansivity coefficients calculated for forsterite, $\alpha = 4.92 \times 10^{-5}$ K$^{-1}$; for diopside, $\alpha = 2.50 \times$

362  $10^{-5}$ K$^{-1}$. These values are consistent with those found in previous experimental studies

363  (Bouhifd et al., 1996; Finger & Ohashi, 1976). In contrast, the *ab initio* study of Wang et al.

364  (2023) reported that diopside ($\alpha = 7.22 \times 10^{-5}$ K$^{-1}$) expands more than forsterite ($\alpha = 6.44 \times 10^{-}$

365  $^5$ K$^{-1}$), which leads to opposite effects in their $\Delta^{26}$Mg$_{cpx/ol}$ calculations using different exchange-

366  correlation functionals (LDA). This discrepancy highlights how the choice of exchange

367  functional and the thermal expansion correction significantly influence the accuracy of isotope
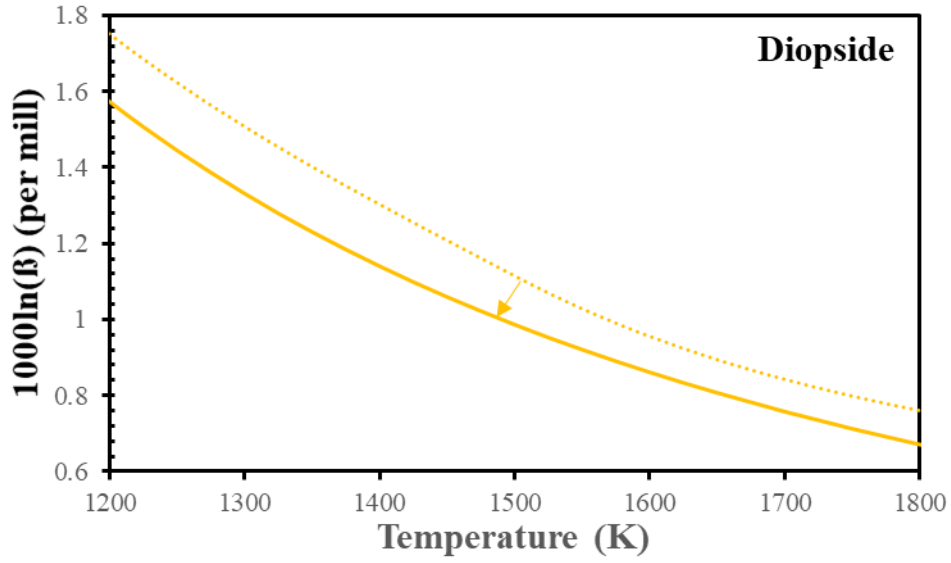
368  fractionation predictions.
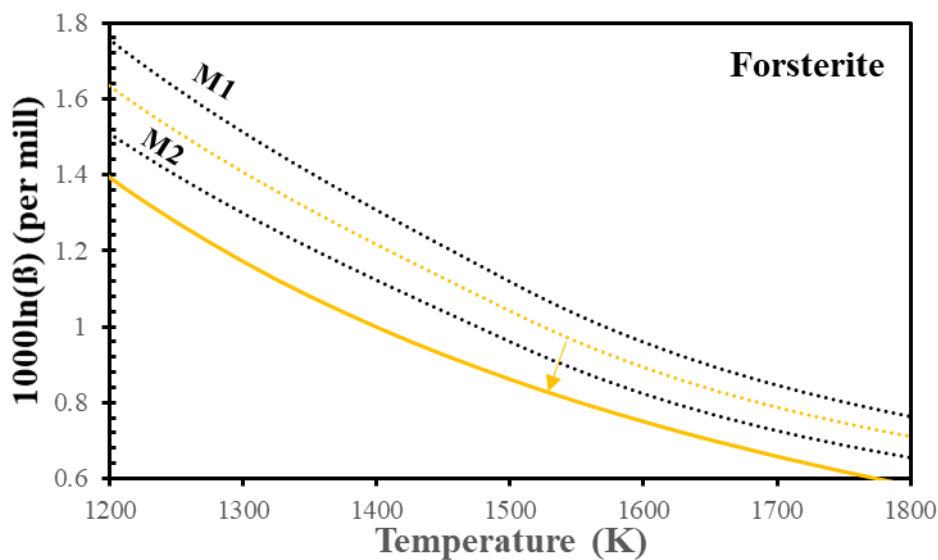
**Figure 6,** Reduced partitioning function with thermal expansion correction (yellow solid line) and without thermal expansion (yellow dotted line). The M1 and M2 sites (black dotted line) are averaged and then corrected for thermal expansion.

| | Fo | Di |
|---|---|---|
| $A_1$ (K$^6$) | -1.5252 × 10$^{15}$ | -9.4405 × 10$^{14}$ |
| $A_2$ (K$^6$Å$^3$) | 5.2452 × 10$^{17}$ | 5.1513 × 10$^{17}$ |
| $B_1$ (K$^4$) | -1.2555 × 10$^{11}$ | -2.8136 × 10$^{11}$ |
| $B_2$ (K$^4$Å$^3$) | 9.1326 × 10$^{13}$ | 2.7616 × 10$^{14}$ |
| $B_3$ (K$^4$Å$^6$) | -1.7484 × 10$^{16}$ | -7.0174 × 10$^{16}$ |
| $C_1$ (K$^2$) | 1.1904 × 10$^6$ | 9.5665 × 10$^6$ |
| $C_2$ (K$^2$Å$^3$) | -1.3578 × 10$^9$ | -9.7941 × 10$^9$ |
| $C_3$ (K$^2$Å$^6$) | 5.0313 × 10$^{11}$ | 2.9521 × 10$^{12}$ |

369

370 **Table 4,** Coefficients of the polynomial $1000 \ln (\beta(V, T)) = (A_1 + A_2 V^{-1}) T^{-6} + (B_1 + B_2 V^{-1} +$

371 $B_3 V^{-2}) T^{-4} + (C_1 + C_2 V^{-1} + C_3 V^{-2}) T^{-2}$ to calculate the reduced partition functions with thermal

372 expansion correction between 300-1900 K with respective cell volumes.

373 *3.4 Comparison between experimental and theoretical results.*

374 We demonstrate a good agreement between the $\Delta^{26}Mg_{cpx/ol}$ ratios obtained from our

375 experiments and those predicted by our PBESOL *ab initio* calculations performed with thermal

376  expansion correction (Figure 7). The experimentally determined $\Delta^{26}Mg_{cpx/ol}$ ratios offer a

377  reference point to evaluate the impacts of various exchange-correlation functionals, site

378  averaging, and thermal expansion treatments on calculated equilibrium isotope fractionation.

379  Notably, the calculated isotope fractionation ratios utilising the PBESOL functional with

380  thermal expansion correction fall within the uncertainty range of the measured $\Delta^{26}Mg_{cpx/ol}$

381  values (Fig 7). In contrast, calculations based on other exchange–correlation functionals,

382  including LDA (Huang et al., 2013), LDA + QHA (Wang et al., 2023), and GGA (Schauble,

383  2011), yield $\Delta^{26}Mg_{cpx/ol}$ values that are lower than our experimentally constrained value by

384  ~0.02‰ at 1573 K. These studies do not explicitly account for thermal expansion in the

385  calculation of inter-mineral fractionation factors. Our results show that thermal expansion

386  introduces a correction due to the reduced partition functions of olivine being relatively larger

387  compared to diopside, suggesting that neglecting this effect is likely to contribute substantially

388  to the apparent offset between these calculations and experimental constraints.

389  Interestingly, the calculations performed by Schauble et al. (2011) using GGA as $E_{xc}$ do not

390  agree with our GGA (PBE) calculations. The variations between our calculations and Schauble

391  et al. (2011) reflect instead a difference in approach to translating phonon frequencies to

392  reduced partition function ratios (ß). Previously, it was a common approach to use a scale factor

393  to correct vibrational frequencies for softening in the functional group when comparing results

394  with those from vibrational spectroscopy (Schauble, 2011). More recent work (Huang et al.,

395  2013; Walker et al., 2025; Young et al., 2015) shows that computational methods have

396  improved, and uniform scaling is physically simplistic; first-principles predictive accuracy can

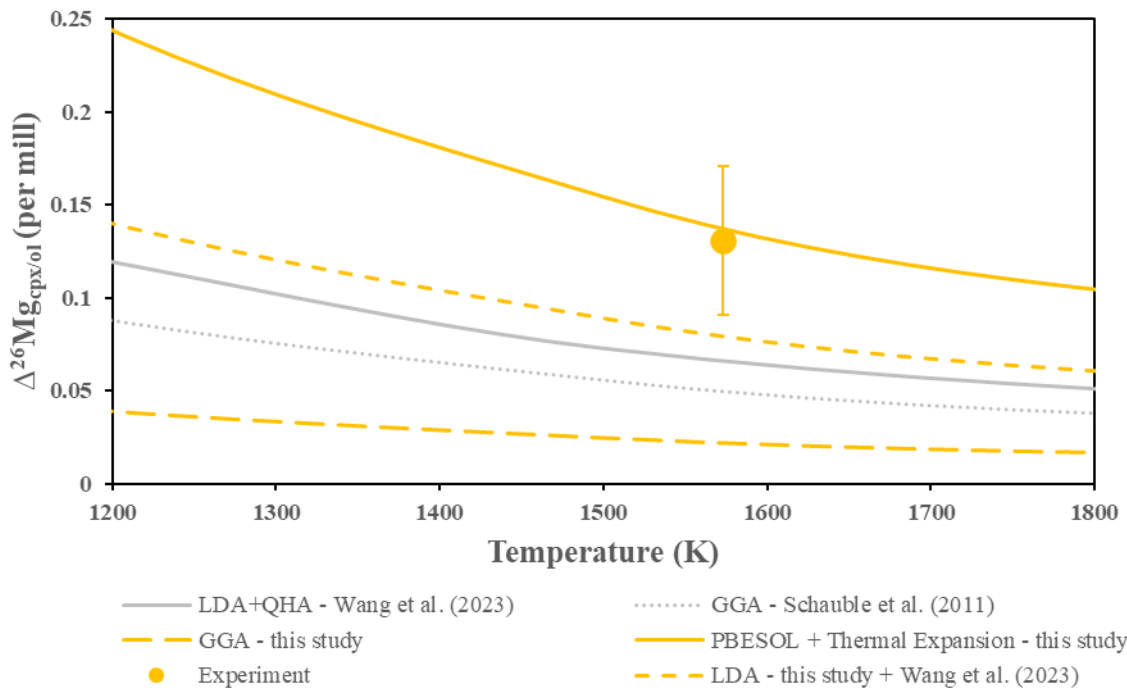397  be reached (e.g., PBESOL) without empirical tuning.

**Figure 7,** Inter-mineral Mg isotope fractionation between diopside and forsterite plotted as a function of temperature and compared with density functional theory calculations at 0 GPa from this study and from the literature. Static-volume calculations using GGA/PBE (yellow striped) and LDA (yellow dotted) are shown. LDA results from this study and from Wang et al. (2023) overlap within the resolution of the figure and are therefore represented by the same symbol.

## 4. Discussion

Our results show good agreement between experimental determination of a value of $\Delta^{26}Mg_{cpx/ol}$ and its DFT Mg calculation (Fig.7). The PBESOL functional, when combined with thermal expansion and site averaging in forsterite, reproduces the measured $\Delta^{26}Mg_{cpx/ol}$ values most accurately, suggesting that this approach provides the most reliable basis for modelling equilibrium isotope behaviour in silicate minerals. In comparison, LDA and PBE underestimate Mg isotope fractionation in diopside and forsterite.

*4.1 Comparison with literature data for Mg isotopic fractionation between olivine and clinopyroxene in naturally occurring samples*

407  Previous studies (e.g Chen et al., 2018; Hu et al., 2020; X. Liu et al., 2022; X.-N. Liu et al.,

408  2023; Pogge von Strandmann et al., 2011; Stracke et al., 2018; Yang et al., 2009) have

409  investigated magnesium isotopic fractionation across various mineral phases in natural

410  samples. $\Delta^{26}Mg_{cpx/ol}$ from most studies relying on sample–standard bracketing exhibit

411  significant analytical uncertainties (> ±0.1‰, 2sd; Supplementary Table S1-3) and are

412  therefore not well suited for quantitative testing of ab initio predictions. Nevertheless, despite

413  their limited precision, such measurements have consistently shown fractionation factors of the

414  same sign and order of magnitude as those predicted by atomic-scale simulations (e.g. Stracke

415  et al., 2018; Young et al., 2009). The recent dataset from Liu et al. (2022 & 2023), which

416  employs a critical mixture double-spiking method, provides a higher precision benchmark

417  against which our experimental findings can be compared (Figure 8). While our measurements

418  show a $\Delta^{26}Mg_{cpx/ol}$ value that closely matches Liu et al. (2023), who reported 0.131 ± 0.045‰,

419  our experimental temperature is roughly 300 K higher than the temperatures estimated for their

420  natural samples. Our theoretical calculations of equilibrium fractionation predict that at

421  temperatures around 1300 K, we would expect the $\Delta^{26}Mg_{cpx/ol}$ values to be approximately 0.2‰

422  higher between the diopside-olivine phases. This suggests that other processes influence

423  isotope ratios beyond equilibrium isotope fractionation.

424  This conclusion is further supported when the data are evaluated using relative olvine-

425  clinopyroxene Mg#. We calculated the relative Mg# differences between coexisting olvine and

426  clinopyroxene in the samples used by Liu et al. (2023), following Sen (1988). Most samples

427  exhibit small Mg# differences, usually within ±0.5 Mg#, suggesting near-equilibrium Fe-Mg

428  partitioning between olivine and cpx. A smaller group of samples shows slight positive offsets,

429  with olivine containing more Mg than cpx, up to +2 Mg#. Importantly, however, even samples

430  that show near-equilibrium Fe-Mg partitioning yield $\Delta^{26}Mg_{cpx/ol}$ values that are systematically

431  lower than our experimentally determined equilibrium fractionation. This indicates that

432    agreement in Fe-Mg exchange does not guarantee equilibrium Mg-isotope fractionation and

433    suggests that kinetic effects or incomplete isotopic equilibrium may persist in natural systems

434    even where major-element partitioning appears equilibrated.

435    Minor but systematic deviations from equilibrium Mg isotope fractionation may arise during

436    xenolith ascent, when decreasing temperature shifts the equilibrium Fe-Mg partitioning

437    between olivine and clinopyroxene. Experimental and thermodynamic studies show that

438    cooling favors an increase in Mg# of clinopyroxene relative to olivine, driving Mg diffusion

439    from olivine into clinopyroxene as the system attempts to re-equilibrate (Putirka, 2008; Sen,

440    1988). Because Mg diffusion is faster than complete Fe-Mg re-equilibration, this process may

441    halt before equilibrium is fully achieved. Diffusion-driven isotope fractionation then results in

442    isotopically light Mg being concentrated in clinopyroxene rims, while olivine rims become

443    relatively heavy, leading to a net reduction in $\Delta^{26}Mg_{cpx/ol}$ compared to the high-temperature

444    equilibrium value. Such kinetic isotope effects during mineral diffusion are well documented

445    in a range of mineral systems (Oeser et al., 2015; Richter et al., 2009; Sio et al., 2013).

446    However, the effect in Hawaiian xenoliths studied by Liu et al. (2023) is likely limited, since

447    these samples erupted explosively and cooled quickly, reducing the time for post-entrapment

448    diffusion. The small $\Delta^{26}Mg_{cpx/ol}$ values and lack of major-element disequilibrium in mineral

449    cores indicate that Fe–Mg re-equilibration was minimal, and that diffusive changes mostly

450    dampened, rather than overprinted, the original Mg isotope signatures.

451    Alternatively, differences in $\Delta^{26}Mg_{cpx/ol}$ between natural and experimental mineral pairs could

452    reflect the simplified, iron-free nature of the experimental system. However, our results show

453    that both $\Delta^{26}Mg_{ol/melt}$ and $\Delta^{26}Mg_{cpx/melt}$ determined in this iron-free system are consistent, within

454    uncertainty, with values from natural, Fe-bearing samples (Liu et al., 2022; Liu et al., 2023).

455    This suggests that iron content does not exert a first-order control on equilibrium Mg isotope

456    fractionation between mineral phases and melt and therefore is unlikely to dominate olvine-

457 clinopyroxene fractionation either. While theoretical frameworks have proposed that cation

458 electronegativity and bonding environment may influence isotope fractionation (Méheut &

459 Schauble, 2014), direct experimental constraints on the effect of iron on Mg isotope

460 fractionation remain limited. Further experiments incorporating iron would nonetheless be

461 valuable for testing for any subtle or second-order effects beyond the scope of this study.
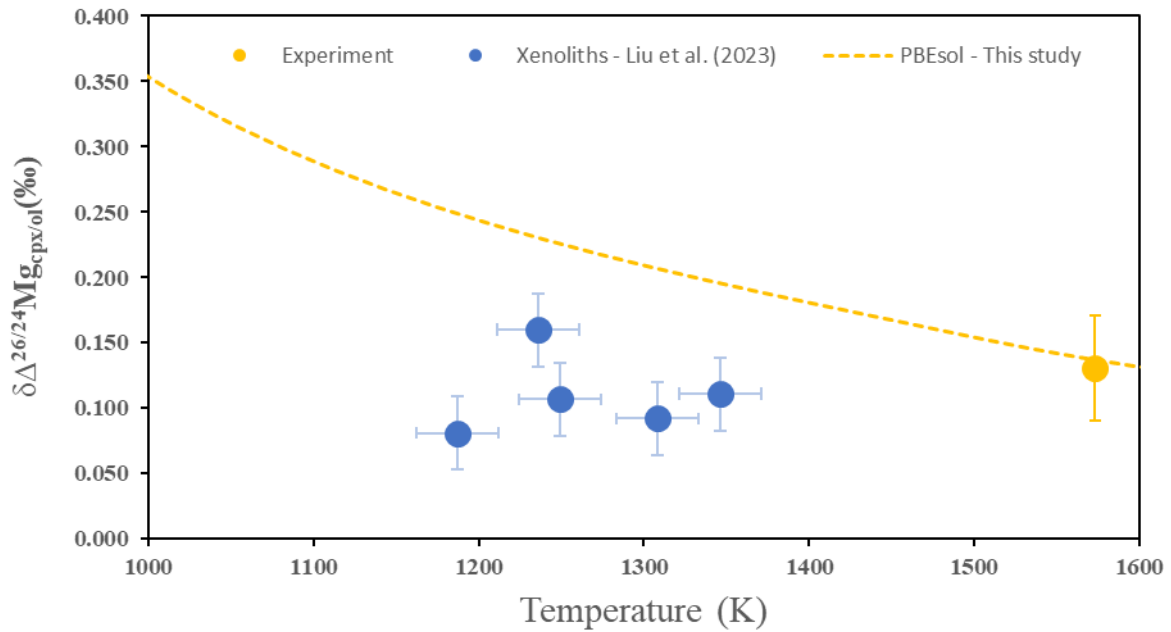


**Figure 8,** Inter-mineral Mg isotopic differences for clinopyroxene-olivine with PBESOL + site averaging + thermal expansion (tallow line) plotted against temperature in Kelvin and compared to xenoliths from Liu et al. (2023)

462 *4.2 Constraints on $\Delta^{26}Mg_{ol/melt}$ from experiments.*

463 Unlike the $\Delta^{26}Mg_{cpx/ol}$, our $\Delta^{26}Mg_{ol/melt}$ matches the ratio reported by Liu et al. (2022) (Figure

464 3a). Although the compositions of residual melts and mineral phases in our experiments differ

465 from those in the natural samples analysed by Liu et al., our results are complementary and

466 consistent with the observed $\Delta^{26}Mg_{ol/melt} = (-1.46 \pm 0.26) \times 10^5/T^2$. This contrasts with the

467 assumption of $\Delta^{26}Mg_{ol/melt} = 0$ (e.g. Soderman et al., 2024; Stracke et al., 2018) based on the

468 work of Teng et al. (2007). The difficulty of accounting for the $\delta^{26}Mg$ of many mantle-derived

469 basalts using equilibrium melting processes with the olivine-melt fractionation factor of Liu et

470     al. (2022) led Soderman et al. (2024) to argue for the continued use of $\Delta^{26}Mg_{ol/melt} = 0$. That

471     our new experimental results strongly support the $\Delta^{26}Mg_{ol/melt}$ reported by Liu et al (2022), this

472     emphasises the need to consider diffusive fractionation during magma migration to the surface

473     in shaping erupted $\delta^{26}Mg$ (and $\delta^{57}Fe$) of mantle-derived melts (Liu et al., 2024).

474     Future research should focus on refining mineral–melt Mg isotope fractionation factors by

475     expanding high-temperature experimental datasets to include a wider range of melt

476     compositions, pressures, and redox conditions. Additionally, better constraints on the isotopic

477     equilibrium between crystals and coexisting melts are needed. Specifically, systematic

478     experiments that isolate compositional effects- such as melt polymerisation and Mg

479     coordination, and exclude kinetic overprints are important for enhancing the accuracy of

480     mineral–melt fractionation factors and precise modelling of Mg isotope fractionation during

481     large-scale differentiation in larger planetary bodies, where the pressure–temperature

482     conditions and crystallisation timescales substantially differ from those studied in this research.

## 5. Conclusions

484     In this study, we assess the magnitude of Mg equilibrium isotope fractionation between

485     forsterite and diopside at liquidus temperatures, using both data from petrological experiments

486     and theoretical calculations. Our measurements of $\Delta^{26}Mg_{ol/melt}$ = -0.058 ± 0.032 and

487     $\Delta^{26}Mg_{cpx}/_{melt} = 0.060 \pm 0.034$ at 1300 °C / 1573 K allow us to calculate the first experimentally

488     derived isotope fractionation factor for this mineral pair, with $\Delta^{26}Mg_{cpx/ol}$ = 0.131 ± 0.04 at

489     1576 K.

490     Our findings align well with ab initio calculations based on density functional theory (DFT),

491     particularly emphasising the effectiveness of the PBESOL exchange-correlation functional and

492     the thermal expansion correction in accurately modelling the $\Delta^{26}Mg_{cpx/ol}$ ratio. These consistent

493    constraints emphasise the value of precise computational methods and experimentally obtained

494    fractionation factors by producing a single, experimentally anchored $\Delta^{26}Mg_{cpx/ol}$ ratio.

505    **Data availability**

506    Density functional theory calculations were performed using the CASTEP code, available via

507    https://www.castep.org/. Input and output files for these calculations are available through

508    Zenodo via https://doi.org/10.5281/zenodo.18195898.

509    **Appendix A. Supplementary Material**

510    The supplementary material provides further details on the experiments and ab initio

511    calculations employed in this study.

512    **References**

513    Blanchard, M., Balan, E., & Schauble, E. A. (2017). Equilibrium Fractionation of Non-

514        traditional Isotopes: A Molecular Modeling Perspective. *Reviews in Mineralogy and*

515        *Geochemistry*, *82*(1), 27–63. https://doi.org/10.2138/rmg.2017.82.2

516    Blanchard, M., Poitrasson, F., Méheut, M., Lazzeri, M., Mauri, F., & Balan, E. (2009). Iron

517        isotope fractionation between pyrite (FeS2), hematite (Fe2O3) and siderite (FeCO3): A

518        first-principles density functional theory study. *Geochimica et Cosmochimica Acta*,

519        *73*(21), 6565–6578. https://doi.org/10.1016/j.gca.2009.07.034

520    Bouhifd, M. A., Andrault, D., Fiquet, G., & Richet, P. (1996). Thermal expansion of forsterite

521        up to the melting point. *Geophysical Research Letters*, *23*(10), 1143–1146.

522        https://doi.org/10.1029/96GL01118

523    Chen, H.-W., Claydon, J. L., Elliott, T., Coath, C. D., Lai, Y.-J., & Russell, S. S. (2018).

524        Chronology of formation of early solar system solids from bulk Mg isotope analyses of

525        CV3 chondrules. *Geochimica et Cosmochimica Acta*, *227*, 19–37.

526        https://doi.org/10.1016/j.gca.2018.02.011

527    Clark, S. J., Segall, M. D., Pickard, C. J., Hasnip, P. J., Probert, M. I. J., Refson, K., & Payne,

528        M. C. (2005). First principles methods using CASTEP. *Zeitschrift Für Kristallographie*

529        -   *Crystalline Materials*, *220*(5–6), 567–570.

530        https://doi.org/10.1524/zkri.220.5.567.65075

531    Coath, C. D., Elliott, T., & Hin, R. C. (2017). Double-spike inversion for three-isotope systems.

532        *Chemical Geology*, *451*, 78–89. https://doi.org/10.1016/j.chemgeo.2016.12.025

533    Downs, R. T., & Hall-Wallace, M. (2003). The American Mineralogist crystal structure

534        database. *American Mineralogist*, *88*(1), 247–250.

535    Duan, H., Yang, B., & Huang, F. (2023). Site-specific isotope effect: Insights from equilibrium

536        magnesium isotope fractionation in mantle minerals. *Geochimica et Cosmochimica*

537        *Acta*. https://doi.org/10.1016/j.gca.2023.05.014

538    Finger, L. W., & Ohashi, Y. (1976). The thermal expansion of diopside to 800 degrees C and

539         a refinement of the crystal structure at 700 degrees C. *American Mineralogist*, *61*(3–4),

540         303–310.

541    Giannozzi, P., de Gironcoli, S., Pavone, P., & Baroni, S. (1991). Ab initio calculation of phonon

542         dispersions in semiconductors. *Physical Review B*, *43*(9), 7231–7242.

543         https://doi.org/10.1103/PhysRevB.43.7231

544    Gonze, X. (1997). First-principles responses of solids to atomic displacements and

545         homogeneous electric fields: Implementation of a conjugate-gradient algorithm.

546         *Physical Review B*, *55*(16), 10337–10354. https://doi.org/10.1103/PhysRevB.55.10337

547    Gonze, X., & Lee, C. (1997). Dynamical matrices, Born effective charges, dielectric

548         permittivity tensors, and interatomic force constants from density-functional

549         perturbation theory. *Physical Review B*, *55*(16), 10355–10368.

550         https://doi.org/10.1103/PhysRevB.55.10355

551    Hazen, R. M. (1976). Effects of temperature and pressure on the crystal structure of forsterite.

552         *American Mineralogist*, *61*(11–12), 1280–1293.

553    He, Y., Sun, A.-Y., Zhang, Y.-C., Yang, R.-Y., Ke, S., Wang, Y., & Teng, F.-Z. (2022). High-

554         precision and high-accuracy magnesium isotope analysis on multiple-collector

555         inductively coupled plasma mass spectrometry using a critical mixture double spike

556         technique. *Solid Earth Sciences*, *7*(3), 188–199.

557         https://doi.org/10.1016/j.sesci.2022.05.001

558    Hin, R. C., Coath, C. D., Carter, P. J., Nimmo, F., Lai, Y. J., Pogge von Strandmann, P. A. E.,

559         Willbold, M., Leinhardt, Z. M., Walter, M. J., & Elliott, T. (2017). Magnesium isotope

560         evidence that accretional vapour loss shapes planetary compositions. *Nature*,

561         *549*(7673), 511–527. https://doi.org/10.1038/nature23899

562  Hohenberg, P., & Kohn, W. (1964). Inhomogeneous electron gas. *Physical Review*, *136*(3B),

563      B864. https://doi.org/10.1103/PHYSREV.136.B864/FIGURE/1/THUMB

564  Hu, Y., Teng, F.-Z., & Ionov, D. A. (2020). Magnesium isotopic composition of metasomatized

565      upper sub-arc mantle and its implications to Mg cycling in subduction zones.

566      *Geochimica      et      Cosmochimica      Acta*,      *278*,      219–234.

567      https://doi.org/10.1016/j.gca.2019.09.030

568  Huang, F., Chen, L., Wu, Z., & Wang, W. (2013). First-principles calculations of equilibrium

569      Mg isotope fractionations between garnet, clinopyroxene, orthopyroxene, and olivine:

570      Implications for Mg isotope thermometry. *Earth and Planetary Science Letters*, *367*,

571      61–70. https://doi.org/10.1016/j.epsl.2013.02.025

572  Javoy, M., Balan, E., Méheut, M., Blanchard, M., & Lazzeri, M. (2012). First-principles

573      investigation of equilibrium isotopic fractionation of O- and Si-isotopes between

574      refractory solids and gases in the solar nebula. *Earth and Planetary Science Letters*,

575      *319–320*, 118–127. https://doi.org/10.1016/j.epsl.2011.12.029

576  Kieffer, S. W. (1982). Thermodynamics and lattice vibrations of minerals: 5. Applications to

577      phase equilibria, isotopic fractionation, and high-pressure thermodynamic properties.

578      *Reviews of Geophysics*, *20*(4), 827–849. https://doi.org/10.1029/RG020i004p00827

579  Kohn, W., & Sham, L. J. (1965). Self-Consistent Equations Including Exchange and

580      Correlation      Effects.      *Physical      Review*,      *140*(4A),      A1133–A1138.

581      https://doi.org/10.1103/PhysRev.140.A1133

582  Lai, Y.-J., Pogge von Strandmann, P. A. E., Dohmen, R., Takazawa, E., & Elliott, T. (2015).

583      The influence of melt infiltration on the Li and Mg isotopic composition of the

584      Horoman Peridotite Massif. *Geochimica et Cosmochimica Acta*, *164*, 318–332.

585      https://doi.org/10.1016/j.gca.2015.05.006

586 Li, X., & Liu, Y. (2011). Equilibrium Se isotope fractionation parameters: A first-principles study. *Earth and Planetary Science Letters*, *304*(1), 113–120. https://doi.org/10.1016/j.epsl.2011.01.022

589 Li, X., Zhao, H., Tang, M., & Liu, Y. (2009). Theoretical prediction for several important equilibrium Ge isotope fractionation factors and geological implications. *Earth and Planetary Science Letters*, *287*(1), 1–11. https://doi.org/10.1016/j.epsl.2009.07.027

592 Liu, X., Hin, R. C., Coath, C. D., van Soest, M., Melekhova, E., & Elliott, T. (2022). Equilibrium olivine-melt Mg isotopic fractionation explains high δ26Mg values in arc lavas. *Geochemical Perspectives Letters*, *22*, 42–47. https://doi.org/10.7185/geochemlet.2226

596 Liu, X.-N., Hin, R. C., Coath, C. D., Bizimis, M., Su, L., Ionov, D. A., Takazawa, E., Brooker, R., & Elliott, T. (2023). The magnesium isotopic composition of the mantle. *Geochimica et Cosmochimica Acta*, *358*, 12–26. https://doi.org/10.1016/j.gca.2023.08.011

600 Liu (刘效宁), X.-N., Hin, R. C., Coath, C. D., & Elliott, T. (2024). Mg and Fe isotope compositions of mid-ocean ridge basalts modified by Mg-Fe inter-diffusion during melt transport. *Earth and Planetary Science Letters*, *642*, 118868. https://doi.org/10.1016/j.epsl.2024.118868

604 Mallmann, G., & O'Neill, H. St. C. (2009). The Crystal/Melt Partitioning of V during Mantle Melting as a Function of Oxygen Fugacity Compared with some other Elements (Al, P, Ca, Sc, Ti, Cr, Fe, Ga, Y, Zr and Nb). *Journal of Petrology*, *50*(9), 1765–1794. https://doi.org/10.1093/petrology/egp053

608 Méheut, M., & Schauble, E. A. (2014). Silicon isotope fractionation in silicate minerals: Insights from first-principles models of phyllosilicates, albite and pyrope. *Geochimica et Cosmochimica Acta*, *134*, 137–154. https://doi.org/10.1016/j.gca.2014.02.014

Monkhorst, H. J., & Pack, J. D. (1976). Special points for Brillouin-zone integrations. *Physical Review B*, *13*(12), 5188–5192. https://doi.org/10.1103/PhysRevB.13.5188

Morse, S. A. (1980). *Basalts and phase diagrams*. Springer.

Oeser, M., Dohmen, R., Horn, I., Schuth, S., & Weyer, S. (2015). Processes and time scales of magmatic evolution as revealed by Fe–Mg chemical and isotopic zoning in natural olivines. *Geochimica et Cosmochimica Acta*, *154*, 130–150. https://doi.org/10.1016/j.gca.2015.01.025

Pamato, M. G., Nestola, F., Novella, D., Smyth, J. R., Pasqual, D., Gatta, G. D., Alvaro, M., & Secco, L. (2019). The High-Pressure Structural Evolution of Olivine along the Forsterite–Fayalite Join. *Minerals*, *9*(12), Article 12. https://doi.org/10.3390/min9120790

Payne, M. C., Teter, M. P., Allan, D. C., Arias, T. A., & Joannopoulos, J. D. (1992). Iterative minimization techniques for ab initio total-energy calculations: Molecular dynamics and conjugate gradients. *Reviews of Modern Physics*, *64*(4), 1045–1097. https://doi.org/10.1103/RevModPhys.64.1045

Perdew, J. P., Burke, K., & Ernzerhof, M. (1996). Generalized gradient approximation made simple. *Physical Review Letters*, *77*(18), 3865.

Perdew, J. P., Ruzsinszky, A., Csonka, G. I., Vydrov, O. A., Scuseria, G. E., Constantin, L. A., Zhou, X., & Burke, K. (2008). Restoring the Density-Gradient Expansion for Exchange in Solids and Surfaces. *Physical Review Letters*, *100*(13), 136406. https://doi.org/10.1103/PhysRevLett.100.136406

Perdew, J. P., & Zunger, A. (1981). Self-interaction correction to density-functional approximations for many-electron systems. *Physical Review B*, *23*(10), 5048–5079. https://doi.org/10.1103/PhysRevB.23.5048

635 Pogge von Strandmann, P. A. E., Elliott, T., Marschall, H. R., Coath, C., Lai, Y.-J., Jeffcoate,

636      A. B., & Ionov, D. A. (2011). Variations of Li and Mg isotope ratios in bulk chondrites

637      and mantle xenoliths. *Geochimica et Cosmochimica Acta*, *75*(18), 5247–5268.

638      https://doi.org/10.1016/j.gca.2011.06.026

639 Prencipe, M., Tribaudino, M., Pavese, A., Hoser, A., & Reehuis, M. (2000). A SINGLE-

640      CRYSTAL NEUTRON-DIFFRACTION INVESTIGATION OF DIOPSIDE AT 10 K.

641      *The Canadian Mineralogist*, *38*(1), 183–189.

642      https://doi.org/10.2113/gscanmin.38.1.183

643 Putirka, K. D. (2008). Thermometers and barometers for volcanic systems. *Reviews in*

644      *Mineralogy and Geochemistry*, *69*(1), 61–120.

645 Refson, K., Tulip, P. R., & Clark, S. J. (2006). Variational density-functional perturbation

646      theory for dielectrics and lattice dynamics. *Physical Review B*, *73*(15), 155114.

647      https://doi.org/10.1103/PhysRevB.73.155114

648 Richter, F. M., Dauphas, N., & Teng, F.-Z. (2009). Non-traditional fractionation of non-

649      traditional isotopes: Evaporation, chemical diffusion and Soret diffusion. *Chemical*

650      *Geology*, *258*(1), 92–103. https://doi.org/10.1016/j.chemgeo.2008.06.011

651 Richter, F. M., Watson, E. B., Mendybaev, R. A., Teng, F.-Z., & Janney, P. E. (2008).

652      Magnesium isotope fractionation in silicate melts by chemical and thermal diffusion.

653      *Geochimica et Cosmochimica Acta*, *72*(1), 206–220.

654      https://doi.org/10.1016/j.gca.2007.10.016

655 Rustad, J. R., & Dixon, D. A. (2009). Prediction of Iron-Isotope Fractionation Between

656      Hematite ($\alpha$-Fe2O3) and Ferric and Ferrous Iron in Aqueous Solution from Density

657      Functional Theory. *The Journal of Physical Chemistry A*, *113*(44), 12249–12255.

658      https://doi.org/10.1021/jp9065373

659     Schauble, E. A. (2004). Applying Stable Isotope Fractionation Theory to New Systems.

660         *Reviews in Mineralogy and Geochemistry*, *55*(1), 65–111.

661         https://doi.org/10.2138/gsrmg.55.1.65

662     Schauble, E. A. (2011). First-principles estimates of equilibrium magnesium isotope

663         fractionation in silicate, oxide, carbonate and hexaaquamagnesium(2+) crystals.

664         *Geochimica et Cosmochimica Acta*, *75*(3), 844–869.

665         https://doi.org/10.1016/j.gca.2010.09.044

666     Sedaghatpour, F., & Teng, F.-Z. (2016). Magnesium isotopic composition of achondrites.

667         *Geochimica et Cosmochimica Acta*, *174*, 167–179.

668         https://doi.org/10.1016/j.gca.2015.11.016

669     Sen, G. (1988). Petrogenesis of spinel lherzolite and pyroxenite suite xenoliths from the Koolau

670         shield, Oahu, Hawaii: Implications for petrology of the post-eruptive lithosphere

671         beneath Oahu. *Contributions to Mineralogy and Petrology*, *100*(1), 61–91.

672         https://doi.org/10.1007/BF00399440

673     Sio, C. K. I., Dauphas, N., Teng, F.-Z., Chaussidon, M., Helz, R. T., & Roskosz, M. (2013).

674         Discerning crystal growth from diffusion profiles in zoned olivine by *in situ* Mg–Fe

675         isotopic analyses. *Geochimica et Cosmochimica Acta*, *123*, 302–321.

676         https://doi.org/10.1016/j.gca.2013.06.008

677     Soderman, C. R., Matthews, S., Shorttle, O., Jackson, M. G., Day, J. M. D., Kamenetsky, V.,

678         & Williams, H. M. (2024). Global oceanic basalt sources and processes viewed through

679         combined Fe and Mg stable isotopes. *Earth and Planetary Science Letters*, *638*,

680         118749. https://doi.org/10.1016/j.epsl.2024.118749

681     Stracke, A., Tipper, E. T., Klemme, S., & Bizimis, M. (2018). Mg isotope systematics during

682         magmatic processes: Inter-mineral fractionation in mafic to ultramafic Hawaiian

683　　　xenoliths. *Geochimica et Cosmochimica Acta*, *226*, 192–205.

684　　　https://doi.org/10.1016/j.gca.2018.02.002

685　Teng, F.-Z., Dauphas, N., Helz, R. T., Gao, S., & Huang, S. (2011). Diffusion-driven

686　　　magnesium and iron isotope fractionation in Hawaiian olivine. *Earth and Planetary*

687　　　*Science Letters*, *308*(3), 317–324. https://doi.org/10.1016/j.epsl.2011.06.003

688　Teng, F.-Z., Li, W.-Y., Ke, S., Marty, B., Dauphas, N., Huang, S., Wu, F.-Y., & Pourmand, A.

689　　　(2010). Magnesium isotopic composition of the Earth and chondrites. *Geochimica et*

690　　　*Cosmochimica Acta*, *74*(14), 4150–4166. https://doi.org/10.1016/j.gca.2010.04.019

691　Teng, F.-Z., Wadhwa, M., & Helz, R. T. (2007). Investigation of magnesium isotope

692　　　fractionation during basalt differentiation: Implications for a chondritic composition of

693　　　the terrestrial mantle. *Earth and Planetary Science Letters*, *261*(1), 84–92.

694　　　https://doi.org/10.1016/j.epsl.2007.06.004

695　Teng, F.-Z., Yin, Q.-Z., Ullmann, C. V., Chakrabarti, R., Pogge von Strandmann, P. A. E.,

696　　　Yang, W., Li, W.-Y., Ke, S., Sedaghatpour, F., Wimpenny, J., Meixner, A., Romer, R.

697　　　L., Wiechert, U., & Jacobsen, S. B. (2015). Interlaboratory comparison of magnesium

698　　　isotopic compositions of 12 felsic to ultramafic igneous rock standards analyzed by

699　　　MC-ICPMS. *Geochemistry, Geophysics, Geosystems*, *16*(9), 3197–3209.

700　　　https://doi.org/10.1002/2015GC005939

701　Tribaudino, M., Prencipe, M., Bruno, M., & Levy, D. (2000). High-pressure behaviour of Ca-

702　　　rich C2/c clinopyroxenes along the join diopside-enstatite (CaMgSi2O6-Mg2Si2O6).

703　　　*Physics and Chemistry of Minerals*, *27*(9), 656–664.

704　　　https://doi.org/10.1007/s002690000106

705　Urey, H. C. (1947). The thermodynamic properties of isotopic substances. *Journal of the*

706　　　*Chemical Society (Resumed)*, *0*, 562–581. https://doi.org/10.1039/JR9470000562

707    Walker, A., Hin, R., & Elliott, T. (2025). *Controls on Mg isotopic fractionation between deep*

708          *mantle phases and relict signatures of a terrestrial magma ocean.*

709          https://eartharxiv.org/repository/view/9866/

710    Wang, W., Wu, Z., Huang, S., & Huang, F. (2023). First-principles investigation of equilibrium

711          magnesium isotope fractionation among mantle minerals: Review and new data. *Earth-*

712          *Science Reviews*, *237*, 104315. https://doi.org/10.1016/j.earscirev.2023.104315

713    Wu, Z., Huang, F., & Huang, S. (2015). Isotope fractionation induced by phase transformation:

714          First-principles investigation for Mg2SiO4. *Earth and Planetary Science Letters*, *409*,

715          339–347. https://doi.org/10.1016/j.epsl.2014.11.004

716    Yang, W., Teng, F.-Z., & Zhang, H.-F. (2009). Chondritic magnesium isotopic composition of

717          the terrestrial mantle: A case study of peridotite xenoliths from the North China craton.

718          *Earth and Planetary Science Letters*, *288*(3), 475–482.

719          https://doi.org/10.1016/j.epsl.2009.10.009

720    Young, E. D., Manning, C. E., Schauble, E. A., Shahar, A., Macris, C. A., Lazar, C., & Jordan,

721          M. (2015). High-temperature equilibrium isotope fractionation of non-traditional stable

722          isotopes: Experiments, theory, and applications. *Chemical Geology*, *395*, 176–195.

723          https://doi.org/10.1016/j.chemgeo.2014.12.013

724    Young, E. D., Tonui, E., Manning, C. E., Schauble, E., & Macris, C. A. (2009). Spinel-olivine

725          magnesium isotope thermometry in the mantle and implications for the Mg isotopic

726          composition of Earth. *Earth and Planetary Science Letters*, *288*(3–4), 524–533.

727          https://doi.org/10.1016/j.epsl.2009.10.014

728

# Supplementary Material

**The magnitude of equilibrium isotope fractionation of Mg between forsterite, diopside and melt at liquidus temperatures.**

Bram de Winter, Department of Earth Sciences, Department of Earth Sciences, University of Oxford, South Parks Road, Oxford, OX1 3AN, UK

# 1. Experiments

**Fig. S1-1.** SEM pictures of samples with composition BDW-S1 and BDW-S2

| BDW-S1 composition |
|:---:|



BDW-S1-1



BDW-S1-2



BDW-S1-3



BDW-S1-4

| BDW-S2 Composition |
|:---:|



BDW-S2-1



BDW-S2-3
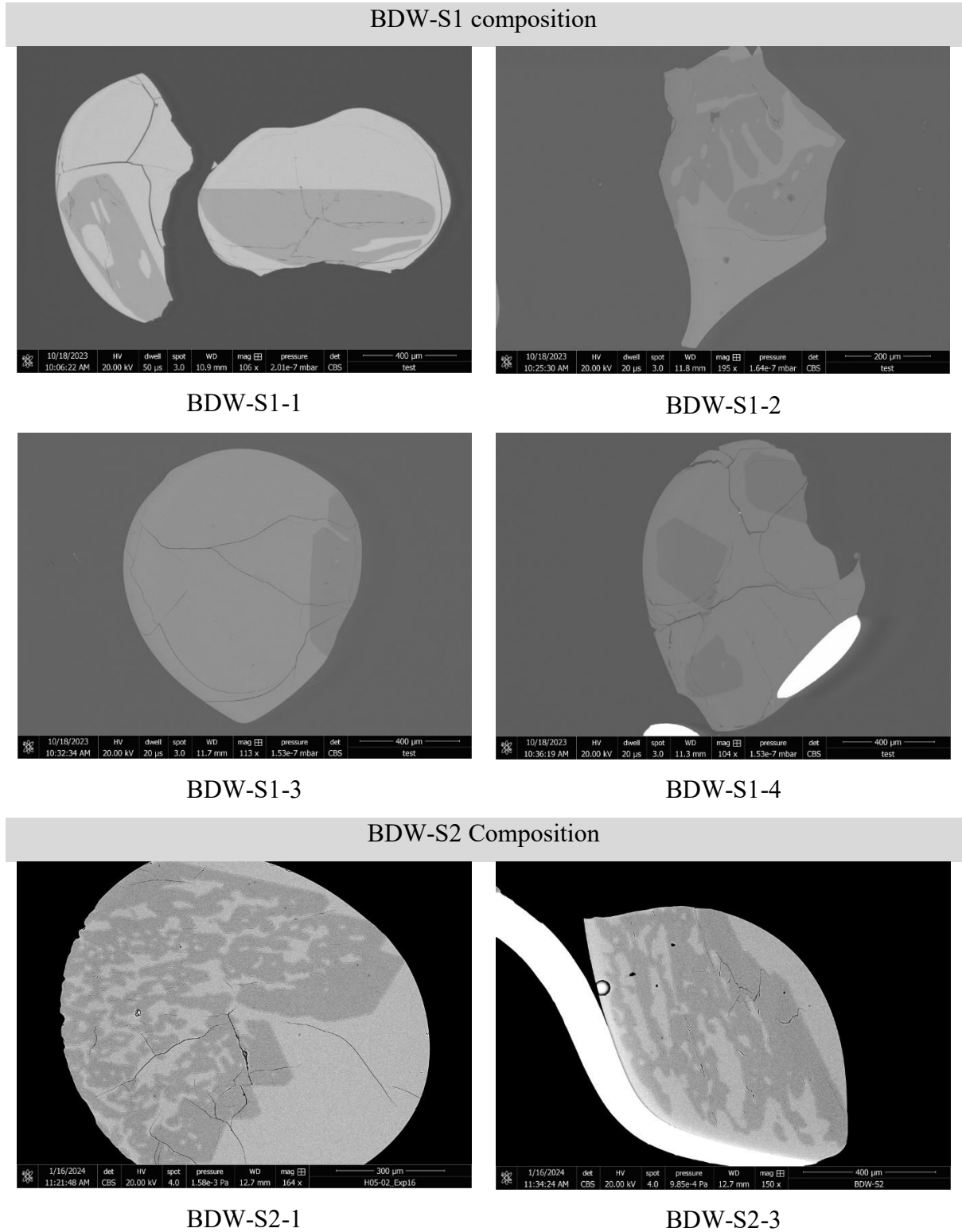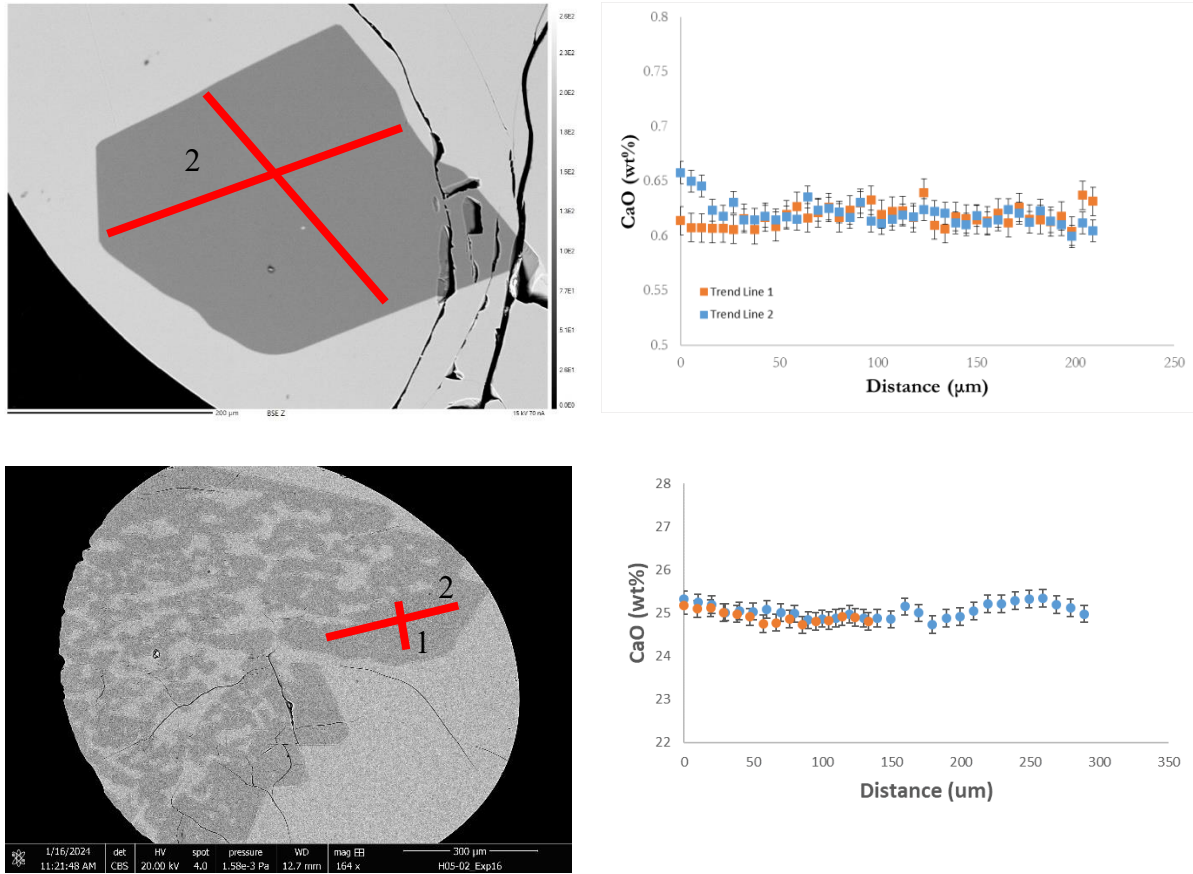
**Fig. S1-2** a) EMPA picture with highlighted lines that represent measurement analysis line stages through the forsterite crystal. Analyses were performed every 10 ųm with a spot size of 5 ųm. B) Concentration of CaO versus distance on the cross-section line stages. C) EMPA picture diopside crystal. D) Concentration of CaO versus distance on the cross-section line stages in diopside.

### 1.1 Experimental isotope analysis

**Table S1-1,** Individual $\delta^{26}Mg$ measurements (‰) for olivine (Ol), diopside (Di), and coexisting melt from experiments BDW-S1-4 (Fo) and BDW-S2-1 (Di). Error bars represent two standard errors (2 s.e.).

| Experiment | Drill site | Phase | $\delta^{26}Mg$ | 2 s.e. | n[a] |
|---|---|---|---|---|---|
| *BDW-S1-4 (Fo)* | | | | | |
| | A | Ol | -1.427 | 0.035 | 9 |
| | B | Melt | -1.347 | 0.035 | 9 |
| | C | Melt | -1.366 | 0.035 | 9 |
| | D | Ol | -1.413 | 0.035 | 9 |

| | | | | | |
|---|---|---|---|---|---|
| E | Melt | -1.381 | 0.035 | 9 |
| F | Melt | -1.354 | 0.035 | 9 |
| *BDW-S2-1 (Di)* | | | | |
| A | Di | -1.312 | 0.023 | 12 |
| B | Melt | -1.361 | 0.023 | 6 |
| C | Melt | -1.338 | 0.023 | 6 |
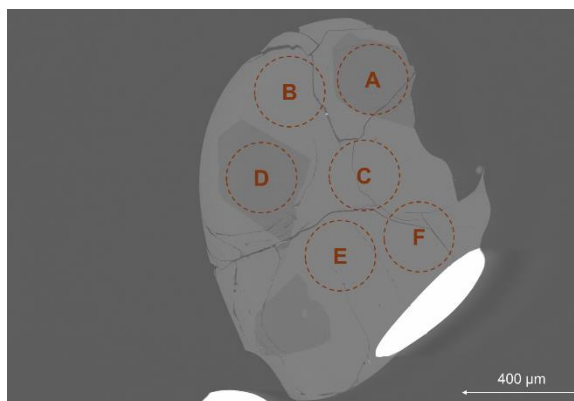


BDW-S1-4 (Fo)
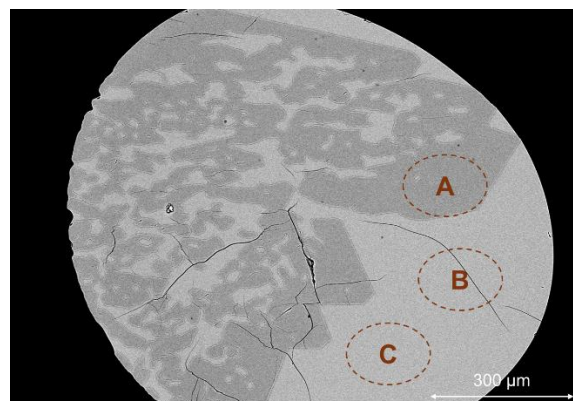


BDW-S2-1 (Di)

### *1.2 Literature data (simple bracketing)*
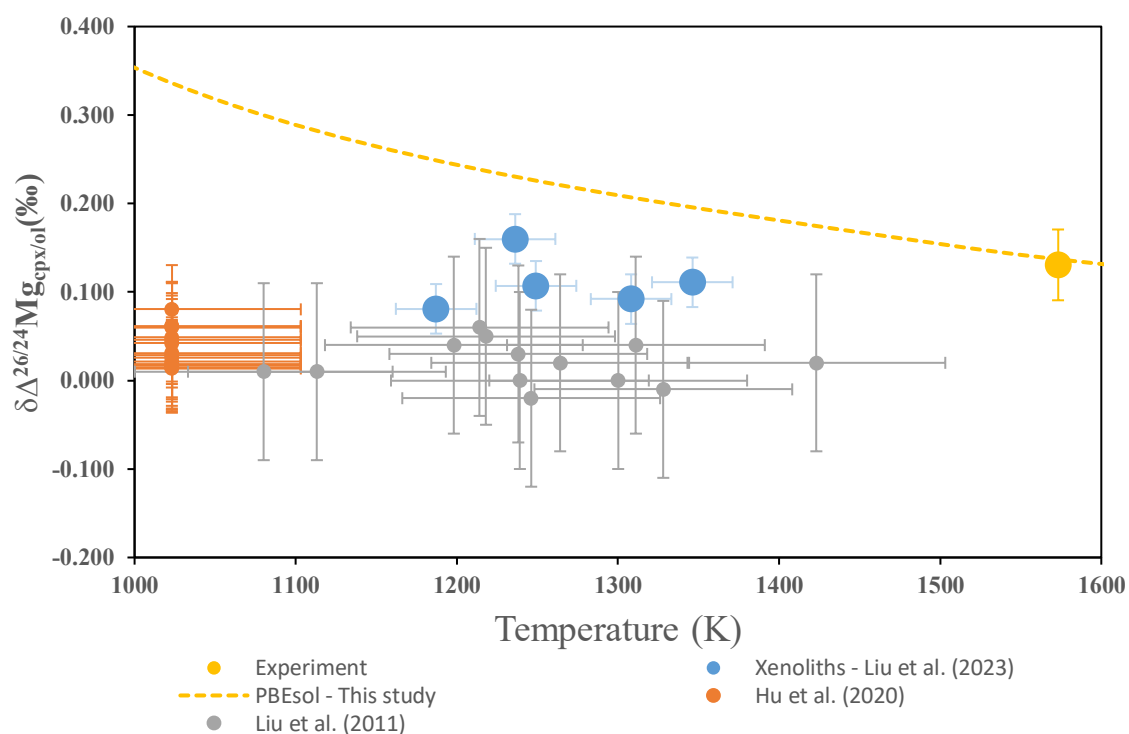
# 2. Ab initio calculations

| Minerals | | Mg-O |
|---|---|---|
| **Forsterite** | LDA | 2.0587 |
| | GGA | 2.0962 |
| | PBESOL | 2.0802 |
| **Diopside** | LDA | 2.0189 |
| | GGA | 2.0761 |
| | PBESOL | 2.0565 |

**Table S2-1** Average Mg-O and Si-O bonds in Å, for 0 GPa calculations performed for diopside and forsterite mineral cells using LDA, GGA and PBESOL exchange-correlation functionals.

**Table S2-2**, unit cell parameters and static volume at 0 K for different $E_{xc}$ used in this study and literature studies. *Ab initio* studies are compared with experimentally determined unit cell volume parameters. Experiments are extrapolated towards 0 K unit cell parameters.

| | $E_{xc}$ | a | b | c | static volume (Å³) | |
|---|---|---|---|---|---|---|
| Forsterite | LDA | 4.732 | 10.101 | 5.933 | 283.584 | this study |
| | LDA | 4.738 | 10.115 | 5.941 | 284.714 | Huang et al. (2013) |
| | GGA | 4.814 | 10.357 | 6.067 | 302.491 | this study |
| | GGA | 4.790 | 10.303 | 6.036 | 297.885 | Schauble (2011) |
| | PBESOL | 4.777 | 10.241 | 6.008 | 293.948 | this study |
| | Experiments | 4.758 | 10.190 | 5.982 | 290.000 | Pamato et al. (2019) |
| Diopside | LDA | 9.687 | 8.781 | 5.015 | 427.101 | this study |
| | LDA | 9.692 | 8.835 | 5.213 | 430.477 | Wang et al. (2023) |
| | GGA | 9.918 | 9.043 | 5.128 | 459.524 | this study |
| | GGA | 9.879 | 8.986 | 5.308 | 451.844 | Schauble (2011) |
| | PBESOL | 9.802 | 8.917 | 5.070 | 443.353 | this study |
| | Experiments | 9.749 | 8.925 | 5.252 | 439.465 | Tribaudino et al. (2000) |

**Table S2-3,** Polynomial fitted constants for 1000 ln (ß (X, $^{24}$Mg, $^{26}$Mg) = $AT^{-6}+BT^{-4}+CT^{-2}$ as a function of T in Kelvin for different studies with 1000lnß at 1000 K.

| Mineral | $E_{xc}$ | Study | T-exp | Site averaging | Polynomial fits (static) 1000ln(ß) = $Ax+Bx^2+Cx^3$ | 1000ln(ß) (1000K) | | |
|---|---|---|---|---|---|---|---|---|
| | | | | | **A** | **B** | **C** | |
| Diopside | LDA | Wang et al. (2023) | Yes | N/A | 2.767 | -0.01812 | 0.0001877 | 2.7487 |
| Diopside | LDA | Huang et al. (2013) | No | N/A | 2.2442 | 0.1052 | -0.0117 | 2.3353[*] |
| Diopside | B3LYP | Gao et al. (2018) | No | N/A | 2.5287 | -0.014671 | 0.00012343 | 2.5142 |
| Diopside | PBE | Duan et al. (2023) | No | No | 2.3365 | −0.01415 | 0.0001 | 2.3235 |
| Forsterite | LDA | Wang et al. (2023) | Yes | No | 2.565 | -0.01735 | 0.0001947 | 2.5478 |
| Forsterite | LDA | Huang et al. (2013) | No | No | 2.0748 | 0.1052 | -0.0119 | 2.1681[*] |
| Forsterite | LDA | Wu et al. (2015) | No | No | -0.108 | 2.29 | 0.0094 | 2.1914 |
| Forsterite | B3LYP | Gao et al. (2018) | No | No | 2.387 | -0.015128 | 0.00014897 | 2.3720 |
| Forsterite | PBE | Duan et al. (2023) | No | Yes | 2.4265 | −0.01555 | 0.00015 | 2.4111 |
| | | | | | **1000ln(ß) = $AT^{-6}+BT^{-4}+CT^{-2}$** | | | |
| | | | | | **A** | **B** | **C** | |
| Forsterite | PBESOL | This Study | Yes | Yes | $2.61 \times 10^{14}$ | $-1.64 \times 10^{10}$ | $2.35 \times 10^6$ | 2.3964 |
| Forsterite | PBE | This Study | Yes | Yes | $1.43 \times 10^{14}$ | $-1.43 \times 10^{10}$ | $2.32 \times 10^6$ | 2.2315 |
| Forsterite | LDA | This Study | Yes | Yes | $2.45 \times 10^{14}$ | $-1.54 \times 10^{10}$ | $2.25 \times 10^6$ | 2.5642 |
| Diopside | PBESOL | This Study | Yes | N/A | $2.16 \times 10^{14}$ | $-1.57 \times 10^{10}$ | $2.52 \times 10^6$ | 2.5024 |
| Diopside | PBE | This Study | Yes | N/A | $1.54 \times 10^{14}$ | $-1.22 \times 10^{10}$ | $2.19 \times 10^6$ | 2.1763 |
| Diopside | LDA | This Study | Yes | N/A | $2.72 \times 10^{14}$ | $-1.88 \times 10^{10}$ | $2.78 \times 10^6$ | 2.7647 |
| Diopside | PBE | Schauble et al. (2011) | No | N/A | $1.4032 \times 10^{14}$ | $-1.4915 \times 10^{10}$ | $2.4806 \times 10^6$ | 2.4658 |
| Forsterite | PBE | Schauble et al. (2011) | No | Yes | $1.5614 \times 10^{14}$ | $-1.5115 \times 10^{10}$ | $2.3547 \times 10^6$ | 2.3397 |
| Forsterite | PBE | Walker et al. (2025) | Yes | No | $1.8414 \times 10^{14}$ | $-1.6279 \times 10^{10}$ | $2.4312 \times 10^6$ | 2.4151 |

[*]Huang et al. (2013) polynomials provide different 1000 K 1000lnß compared to their provided supplementary data
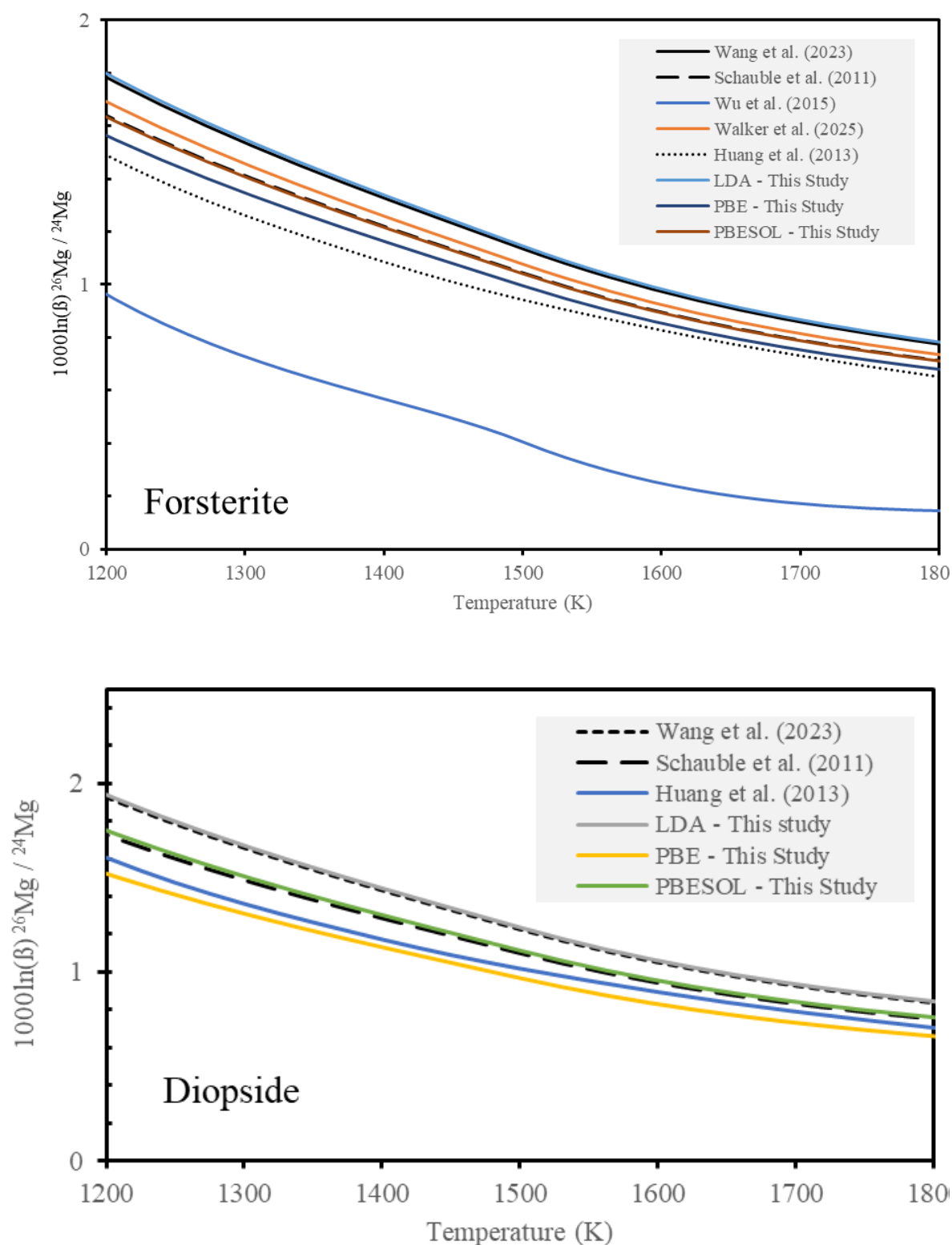
**Figure S2-1** , Reduced partitioning function for magnesium isotopes in a) forsterite and b) Diopside. An overview of the literature is given in the Supplementary table S2-3

| | | Forsterite | Diopside |
|---|---|---|---|
| **F0** | x0 | $-8.96 \times 10^3$ | $-1.68 \times 10^4$ |

|  |  | | |
|---|---|---|---|
|  | x1 | $1.06 \times 10^{-3}$ | $9.80 \times 10^{-4}$ |
|  | x2 | $-9.68 \times 10^{-6}$ | $-1.33 \times 10^{-5}$ |
|  | x3 | $2.85 \times 10^{-9}$ | $3.95 \times 10^{-9}$ |
|  | x4 | $-5.15 \times 10^{-13}$ | $-7.16 \times 10^{-13}$ |
|  | x5 | $3.61 \times 10^{-17}$ | $5.40 \times 10^{-17}$ |
| **V0** | x0 | $2.96 \times 10^{2}$ | $4.47 \times 10^{2}$ |
|  | x1 | $1.18 \times 10^{-2}$ | $7.31 \times 10^{-3}$ |
|  | x2 | $1.48 \times 10^{-5}$ | $-1.06 \times 10^{-5}$ |
|  | x3 | $1.83 \times 10^{-8}$ | $1.65 \times 10^{-8}$ |
|  | x4 | $-7.20 \times 10^{-12}$ | $-5.98 \times 10^{-12}$ |
|  | x5 | $9.99 \times 10^{-16}$ | $6.56 \times 10^{-16}$ |
| **K0** | x0 | $1.22 \times 10^{2}$ | $9.70 \times 10^{1}$ |
|  | x1 | $-8.41 \times 10^{-3}$ | $-1.65 \times 10^{-3}$ |
|  | x2 | $-1.85 \times 10^{-5}$ | $-4.72 \times 10^{-5}$ |
|  | x3 | $1.03 \times 10^{-8}$ | $-2.72 \times 10^{-10}$ |
|  | x4 | $-2.89 \times 10^{-12}$ | $6.84 \times 10^{-12}$ |
|  | x5 | $2.86 \times 10^{-15}$ | $-1.11 \times 10^{-15}$ |
| **K'0** | x0 | 4.35 | 7.06 |
|  | x1 | $1.88 \times 10^{-3}$ | $2.92 \times 10^{-1}$ |
|  | x2 | $-4.60 \times 10^{-6}$ | $-9.88 \times 10^{-4}$ |
|  | x3 | $4.17 \times 10^{-9}$ | $9.48 \times 10^{-7}$ |
|  | x4 | $-1.48 \times 10^{-12}$ | $-3.08 \times 10^{-10}$ |
|  | x5 | $1.85 \times 10^{-16}$ | $3.24 \times 10^{-14}$ |

**Table S2-4,** Birch-Murnaghan equation of state (EOS) for forsterite and diopside using PBESOL exchange-correlation functional. Parameters can be fitted to V using equation 1:

$$F(V) = F_0 + \frac{9V_0K_0}{16}\left\{ \left[ \left(\frac{V_0}{V}\right)^{\frac{2}{3}} - 1 \right]^3 K_0' + \left[ \left(\frac{V_0}{V}\right)^{\frac{2}{3}} - 1 \right]^2 \left[ 6 - 4\left(\frac{V_0}{V}\right)^{\frac{2}{3}} \right] \right\} \qquad (1)$$

|  | Forsterite M1 | Forsterite M2 | Forsterite average | Diopside |
|---|---|---|---|---|
| **A1** | $-1.64 \times 10^{15}$ | $-1.41 \times 10^{15}$ | $-1.53 \times 10^{15}$ | $-9.44 \times 10^{14}$ |
| **A2** | $5.64 \times 10^{17}$ | $4.85 \times 10^{17}$ | $5.25 \times 10^{17}$ | $5.15 \times 10^{17}$ |
| **B1** | $-1.35 \times 10^{11}$ | $-1.16 \times 10^{11}$ | $-1.26 \times 10^{11}$ | $-2.81 \times 10^{11}$ |

| | | | | |
|---|---|---|---|---|
| **B2** | $9.82 \times 10^{13}$ | $8.45 \times 10^{13}$ | $9.13 \times 10^{13}$ | $2.76 \times 10^{13}$ |
| **B3** | $-1.88 \times 10^{16}$ | $-1.62 \times 10^{16}$ | $-1.75 \times 10^{16}$ | $-7.02 \times 10^{16}$ |
| **C1** | $1.28 \times 10^{6}$ | $1.10 \times 10^{6}$ | $1.19 \times 10^{6}$ | $9.57 \times 10^{6}$ |
| **C2** | $-1.46 \times 10^{9}$ | $-1.26 \times 10^{9}$ | $-1.36 \times 10^{9}$ | $-9.79 \times 10^{9}$ |
| **C3** | $5.41 \times 10^{11}$ | $4.65 \times 10^{11}$ | $5.03 \times 10^{11}$ | $2.95 \times 10^{12}$ |

**Table S2-5,** Fitted parameters with thermal expansion correction. 1000 ln (beta) can be found using equation 2:

$$1000 \ln \beta(V,T) = (A_1 + A_2 V^{-1})T^{-6} + (B_1 + B_2 V^{-1} + B_3 V^{-2})T^{-4} \\ + (C_1 + C_2 V^{-1} + C_3 V^{-2})T^{-2} \qquad (2)$$

# References

Gao, C., Cao, X., Liu, Q., Yang, Y., Zhang, S., He, Y., Tang, M., & Liu, Y. (2018). Theoretical calculation of equilibrium Mg isotope fractionations between minerals and aqueous solutions. *Chemical Geology*, *488*, 62–75. https://doi.org/10.1016/j.chemgeo.2018.04.005

Hu, Y., Teng, F.-Z., & Ionov, D. A. (2020). Magnesium isotopic composition of metasomatized upper sub-arc mantle and its implications to Mg cycling in subduction zones. *Geochimica et Cosmochimica Acta*, *278*, 219–234. https://doi.org/10.1016/j.gca.2019.09.030

Huang, F., Wu, Z., Huang, S., & Wu, F. (2014). First-principles calculations of equilibrium silicon isotope fractionation among mantle minerals. *Geochimica et Cosmochimica Acta*, *140*, 509–520. https://doi.org/10.1016/j.gca.2014.05.035

Liu, S.-A., Teng, F.-Z., Yang, W., & Wu, F.-Y. (2011). High-temperature inter-mineral magnesium isotope fractionation in mantle xenoliths from the North China craton. *Earth and Planetary Science Letters*, *308*(1), 131–140. https://doi.org/10.1016/j.epsl.2011.05.047

Liu, X.-N., Hin, R. C., Coath, C. D., Bizimis, M., Su, L., Ionov, D. A., Takazawa, E., Brooker, R., & Elliott, T. (2023). The magnesium isotopic composition of the mantle. *Geochimica et Cosmochimica Acta*, *358*, 12–26. https://doi.org/10.1016/j.gca.2023.08.011

Schauble, E. A. (2011). First-principles estimates of equilibrium magnesium isotope fractionation in silicate, oxide, carbonate and hexaaquamagnesium(2+) crystals. *Geochimica et Cosmochimica Acta*, *75*(3), 844–869. https://doi.org/10.1016/j.gca.2010.09.044

Walker, A., Hin, R., & Elliott, T. (2025). *Controls on Mg isotopic fractionation between deep mantle phases and relict signatures of a terrestrial magma ocean*. https://eartharxiv.org/repository/view/9866/

Wang, W., Wu, Z., Huang, S., & Huang, F. (2023). First-principles investigation of equilibrium magnesium isotope fractionation among mantle minerals: Review and new data. *Earth-Science Reviews*, *237*, 104315. https://doi.org/10.1016/j.earscirev.2023.104315

Wu, Z., Huang, F., & Huang, S. (2015). Isotope fractionation induced by phase transformation: First-principles investigation for Mg2SiO4. *Earth and Planetary Science Letters*, *409*, 339–347. https://doi.org/10.1016/j.epsl.2014.11.004