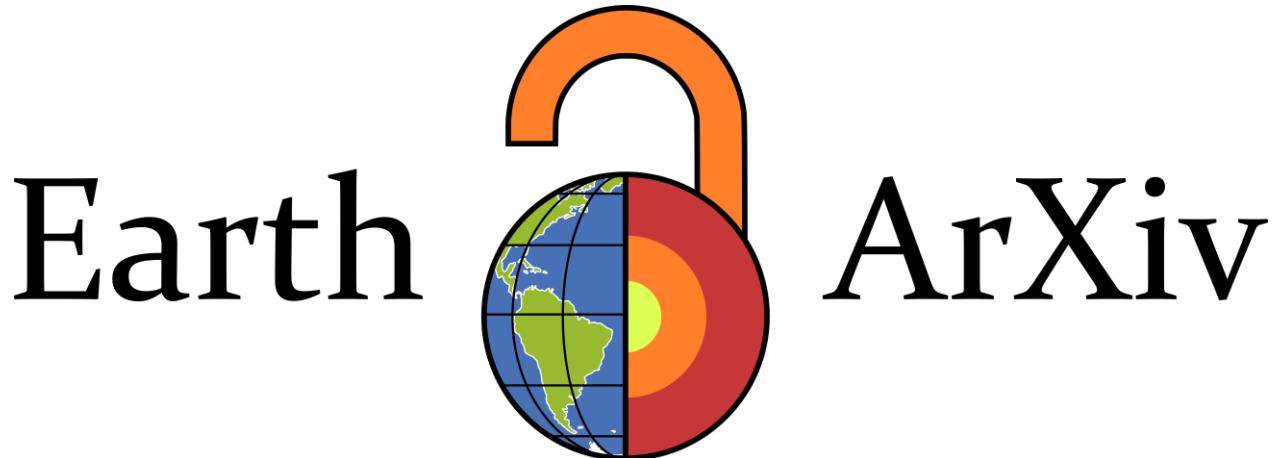


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14 this manuscript will be available via the 'Peer-reviewed Publication
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16 contact any of the authors; we welcome feedback.

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20 **Title**

21 **Calcium promotes carbon rich grassland soils**

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40 **Abstract**

41 Dark colored grassland soils, known as Mollisols, are intensively farmed and exceptionally
42 rich in organic matter, and hence have an important role in the carbon cycle. Elevated carbon
43 storage in Mollisols may be facilitated by calcium (Ca) released by carbonate and silicate
44 weathering. This synergy between carbon and Ca cycling has not been definitively
45 quantified. To close this knowledge gap, we developed a novel geochemical model and
46 leveraged continental-scale datasets to simulate Ca release in soils across the USA. We
47 found that Ca released by mineral weathering helps to predict the distribution of Mollisols
48 and soil organic carbon storage. Our model also indicates that agriculture has increased Ca
49 inputs to cultivated USA Mollisols 2 to 5 fold, demonstrating that humans have
50 fundamentally changed the geochemical conditions that sustain carbon storage in these
51 soils. By implication, moderating the quantity of and timing of Ca release may be essential
52 for sustaining soil carbon storage in the world's most intensively farmed landscapes.

53 **Teaser**

54 Calcium released by dissolving carbonate and silicate minerals helps to store organic
55 carbon in Earth's most intensively farmed soils.

63 **Introduction**

64 Temperate grasslands feature exceptionally fertile, dark-colored soils known as Mollisols.
65 Mollisols are the world's most intensively farmed soil type (1). Based on recent data (2, 3), we
66 estimate that Mollisols comprise only 7% of the Earth's land area yet support 24% of agricultural
67 land and 32% of all calories from production of corn, soy, and wheat. Mollisols also contribute
68 disproportionately to soil organic carbon storage, storing 32% of the organic carbon held in Earth's
69 agricultural soils (see Materials and Methods). This makes Mollisols critical to land-based climate
70 mitigation efforts. At the same time, Mollisols are exposed to environmental threats, including soil
71 erosion (4), and have lost a significant fraction of their carbon to cultivation (5). Effective
72 stewardship of Mollisols in the face of these threats requires a comprehensive understanding of the
73 environmental factors that make them fertile and carbon rich.

74 There are several ecological processes that contribute to the carbon richness of Mollisols, and these
75 have implications for protecting and restoring soil organic carbon. As early as the 1860's, grassland
76 vegetation was identified as the main driver of Mollisol formation (6). Perennial grasses grow
77 extensive fibrous root systems, and root turnover is an important pathway of soil organic carbon
78 accrual (7, 8). Grasslands and savannas are characterized by frequent fires, and fires can generate
79 persistent pyrogenic carbon that might explain the origin of Mollisols (9). Grasslands also support
80 robust populations of burrowing animals that contribute to the thick, carbon-rich topsoil layers
81 characteristic of Mollisols (10). Contemporary proposals for restoring carbon storage in cropland
82 soils mimic ecological processes that are thought to be important in Mollisols; for instance, carbon
83 sequestration might be achieved by returning deep rooted cultivars to croplands (11), increasing
84 plant diversity (12), or amending soils with pyrogenic carbon (13),

85 Geologic factors can also help to explain the origins of Mollisols. Mollisols are commonly formed
86 from calcareous rocks or from aeolian deposits rich in calcium carbonate (6). A growing body of
87 evidence shows that Ca stabilizes soil organic matter. Ca facilitates sorption of organic molecules
88 on clays and promotes the growth of bacterial biofilms that are retained on mineral surfaces (14–
89 16). These processes manifest at continental scales, where soil organic carbon is spatially correlated
90 with exchangeable Ca^{2+} , i.e., Ca^{2+} that is reversibly bound to surfaces (17, 18). The relative
91 abundance of exchangeable Ca^{2+} and other base cations (Mg^{2+} , K^+ , and Na^+) is important in
92 classifying Mollisols, reflecting their role in Mollisol genesis (19). These facts suggest that
93 judicious management of soil Ca might also be a tool to promote organic carbon storage, although
94 this possibility has received relatively scant attention. This is in part because the availability of Ca^{2+}
95 in soil is a function of complex interactions among vegetation, geology, and climate. This makes it
96 challenging to disentangle the role of Ca from other drivers of carbon storage in Mollisols.

97 We addressed the role of Ca in Mollisol organic carbon storage by developing and applying a novel
98 geochemical model across the conterminous USA. Our modeling approach leveraged soil
99 mineralogy data available across the USA (20), which enabled us to represent soil chemical
100 processes at an unprecedented spatial extent. We designed our model to track the inputs and outputs
101 of major cations and anions to the soil solution, allowing us to simulate soil pH, mineral weathering
102 rates, and associated Ca release and retention. We used the model to quantify specific Ca sources:
103 carbonate weathering, silicate weathering, and atmospheric deposition. We then statistically
104 estimated the effect of each source on Mollisol extent and carbon storage while accounting for
105 vegetation and climate. Using this approach, we isolated the effect of specific geologic Ca sources
106 on Mollisols and quantified the role of Ca in sustaining Mollisol organic carbon stocks.

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112 **Results and Discussion**

113 Geochemical model performance

114 We used our geochemical model to estimate the input of available Ca to soil across the
115 conterminous USA and then related Ca inputs to: [1] Mollisol extent, derived from ground based
116 soil classification and mapping (21) (Fig. 1a); and [2] observations of topsoil (A-horizon) organic
117 carbon stocks (22, 23) (Fig. 1b). We first parametrized the model with input data including climate,
118 atmospheric deposition of major solutes, net primary productivity, agricultural element budgets,
119 and soil mineralogy (see Methods). The model integrated these variables by linking inputs and
120 outputs of solutes, the release of CO₂ and organic acids by biota, and mineral weathering via a set
121 of pH-dependent equilibrium reactions. We calibrated two unconstrained parameters related to
122 mineral surface reactivity, training the model to match modern observations of soil pH. The model
123 performed relatively well, explaining 69% of the spatial variation in depth-averaged soil pH (0-100
124 cm), 39% of the variation in soil exchangeable Ca²⁺, and 64% of the variation across all
125 exchangeable ions when applied to a separate validation set of ground observations (Fig. S1, Fig.
126 S2, Table S1). We re-parametrized the model to reflect preindustrial (1850) rates of atmospheric
127 deposition (24) and eliminated agricultural processes following calibration and validation steps. We
128 then simulated Ca release from carbonate and silicate weathering and exchangeable Ca²⁺ under pre-
129 industrial conditions.

130

131 Environmental controls on Mollisols

132 Our geochemical model shows that Mollisol extent correlates with the inputs of available Ca (Fig.
133 1c) and also with the presence of grassland vegetation (Fig. 1d). To disentangle these correlations,
134 we applied a multivariate logistic regression, quantifying the present-day influence of Ca on the
135 geographic distribution of Mollisols while accounting for vegetation and other climate and soil
136 factors. We used the base saturation percentage to represent the influence of Ca in the regression
137 because this index is one of several factors used to classify and map Mollisols in the USA (19)
138 [base saturation = 100*(total base cation charge / cation exchange capacity)]. We also included six
139 additional factors: [1] the pre-agricultural grassland and savanna distribution, which we
140 approximated with a potential vegetation map derived from remotely sensed patches of relict
141 vegetation (25); [2] mean annual temperature; [3] mean annual precipitation; [4] soil silt and clay
142 content [5] soil drainage class; [6] net primary productivity. We compared the independent
143 explanatory power of these factors by computing scaled regression coefficients (Table S2). The
144 regression model matched the observations relatively well, classifying 79% of locations correctly.
145 We found that base saturation was the strongest predictor of the distribution of Mollisols, followed
146 by grassland and savanna presence, mean annual air temperature, precipitation, and other soil
147 properties (Fig. 2a). Together, these results indicate that Mollisols are associated with grassland
148 environments rich in Ca²⁺ and other base cations, particularly in drier and cooler climates.

149 Our results indicate that base cations, including Ca²⁺, are an important control on the distribution
150 of Mollisols. However, these results are not direct evidence that Ca enhances Mollisol organic
151 carbon storage; rather, they show that the relative abundance of exchangeable Ca²⁺ and other base
152 cations strongly influences where Mollisols are mapped. To address the role of Ca in organic carbon
153 storage directly, we related modeled exchangeable Ca²⁺ to soil carbon stock data retrieved from
154 two databases, the US Department of Agriculture Rapid Carbon Assessment and the National
155 Cooperative Soil Survey archives (22, 23). We used these data to quantify A-horizon organic carbon
156 stocks across the USA (Fig. 1b). Mollisols are characterized by thick, carbon-rich A-horizons (19);
157 hence we used total A-horizon carbon—incorporating both topsoil thickness and carbon content—
158 to quantify the primary mode of carbon storage in Mollisols.

159 We related A-horizon organic carbon stocks to total exchangeable Ca²⁺ using multiple linear
160 regression. We also included the same set of variables used for interpreting Mollisol extent, plus

161 the sum of non-Ca exchangeable cations (Mg^{2+} , K^+ , Na^+ , Al^{3+} , and H^+). The regression model
162 explained 30% of the variation in A-horizon organic carbon stocks. Comparison of the scaled
163 regression coefficients revealed that net primary productivity and temperature were the most
164 important predictors of A-horizon carbon storage, followed by exchangeable Ca^{2+} , the presence of
165 grasslands or savannas, and then other factors (Fig. 2b; Table S3). The controls on A-horizon carbon
166 storage across the conterminous USA are distinct from the controls on Mollisol extent because
167 Mollisols are not the only soil types that feature carbon-rich topsoil. For instance, cool, productive
168 forests in the northwestern USA accumulate soil organic carbon due to high organic matter inputs,
169 inhibition of decomposition by low temperatures, and abundant reactive Al and Fe minerals (26).
170 It is nonetheless clear that exchangeable Ca^{2+} is an important secondary control on A-horizon
171 carbon storage. Furthermore, the combined effect of other exchangeable ions was weak, suggesting
172 that it is specifically Ca, rather than total cation exchange capacity, that contributes to A-horizon
173 carbon storage.

174 Our regression analysis identifies a major role for Ca in Mollisol function, but also suggests that
175 grassland and savanna vegetation influence the distribution of Mollisols independent of other
176 factors. Grasslands and savannas can be maintained by fire, helping grasses to persist in climates
177 that would otherwise support forest (27, 28). In this case, fire regimes that maintain grass
178 dominance might directly determine where Mollisols form. On the other hand, Mollisols are notably
179 uncommon in tropical grasslands and savannas (29), which suggests that ecological factors
180 common to grasslands and savannas are not sufficient to generate Mollisols. Tropical soils are
181 typically highly weathered, host less reactive minerals, and are generally more acidic than
182 temperate soils that received Ca-rich minerals following Pleistocene glaciation (30, 31). These
183 geologic limits to Ca supply, in addition to climate, may curtail Mollisol development in the tropics.
184 By contrast, multiple overlapping environmental factors—including Ca weathering in post-glacial
185 soils, cooler temperatures, mesic climate, and the presence of grasses—converge in certain
186 temperate regions, and Mollisols are an emergent result of these overlapping factors.

187 Geologic drivers of Mollisol carbon storage

188 Our geochemical model enabled us to consider the specific geologic mechanisms that explain the
189 distribution of Mollisols. We evaluated the effect of Ca sources on Mollisol extent by constructing
190 counterfactual scenarios in which Ca sources were suppressed under simulated preindustrial
191 conditions. Specifically, we [1] set carbonate weathering, all silicate weathering, or atmospheric Ca
192 deposition to zero in the geochemical model, [2] used updated outputs from the geochemical model
193 to generate predictions using the previously fitted logistic regression, and [3] quantified changes in
194 the predicted area of Mollisols. For reference, we also created a counterfactual scenario in which
195 all vegetation was assumed to be non-grassland. This analysis revealed that both carbonate and
196 silicate weathering help to explain the presence of Mollisols. In the absence of carbonate
197 weathering, predicted preindustrial Mollisol extent was 4% lower (4 Mha), and without silicate
198 weathering Mollisol extent was 27% lower (52 Mha). When both weathering sources were
199 eliminated, the effect was non-additive: Mollisol extent dropped by 90% (174 Mha), which was
200 comparable to the effect of eliminating grassland vegetation (85%, 166 Mha). By contrast,
201 eliminating atmospheric Ca deposition reduced Mollisol extent by only 2% (4 Mha) (Fig. 3a).

202 We also evaluated the effects of specific geologic Ca sources on A-horizon organic carbon by
203 eliminating Ca sources in the geochemical model as above. This analysis indicated that carbonate
204 and silicate weathering jointly promote A-horizon soil organic carbon storage. Across the
205 conterminous USA, predicted preindustrial A-horizon carbon storage was 5% (1.2 Pg C) lower
206 when carbonate weathering was eliminated, 2% (0.6 Pg C) lower when silicate weathering was
207 eliminated, and 11% (2.9 Pg C) lower when both were eliminated together (Fig. 3b). This combined
208 effect was similar to eliminating grassland vegetation, which reduced A-horizon organic carbon

210 storage by 10% (2.7 Pg C) (Fig. 3b). When we focused our analysis on Mollisol regions, we found
211 A-horizon organic carbon stocks were even more sensitive to eliminating carbonate and silicate
212 weathering (16% reduction, 1.2 Pg C) and grassland vegetation (19%, 1.5 Pg C).

213 Taken together, our results show that carbonate weathering and silicate weathering have modest
214 effects on Mollisol extent and A-horizon carbon storage when considered alone, but a more
215 substantial effect when combined at a continental scale. This result emerges because carbonate
216 weathering and silicate weathering suppress each other via their alkalizing effect on soil pH; hence
217 eliminating one Ca source yields a compensatory increase in Ca release from the other.
218 Consequently, when either silicates or carbonates are sufficiently abundant, soil Ca^{2+} availability is
219 high and Ca^{2+} generally predominates over other exchangeable ions. These conditions favor
220 Mollisol formation and organic carbon accrual across a range of geologic settings.

221 Our model suggests that the elevated Ca inputs that generate Mollisols in the midcontinental USA
222 are derived from specific geologic sources, particularly carbonate minerals (Fig. 3b). Glacial
223 deposition explains elevated carbonate weathering in the north-central USA, where lobes of the
224 Laurentide ice sheet ground up and distributed underlying limestone and dolomite rocks during the
225 last ice age (32). Farther south, soil carbonates are abundant in the aeolian Bignell Loess deposits
226 (33), and in the predominately limestone rocks of the Edwards Plateau (34), both of which support
227 Mollisols. Carbonate minerals are also abundant in the arid Western USA; however, our
228 geochemical model predicts that carbonates are either a minor source or a Ca sink in this region
229 (Fig. S3). While some of the carbonates in these soils may be derived from sedimentary rocks,
230 desert carbonates are often primarily derived from in-situ precipitation of CaCO_3 from aeolian Ca
231 (35). Our model suggests that some of these carbonates may be slowly weathering under late-
232 Holocene conditions, supplying Ca to overlying Mollisols.

233 Our model also predicts that inputs of Ca from deposition are significant in much of the USA (Fig.
234 3c); however, we found that atmospheric deposition of Ca is a minor control on Mollisol extent
235 (Fig. 3a). We assumed that preindustrial Ca deposition was five-fold lower in North America than
236 at present based on paleo dust records (36). Dust fluxes in the midcontinental USA were
237 substantially higher in the late Pleistocene than in recent preindustrial times due to glaciation (37).
238 Ca in modern soil carbonates is often inherited from Pleistocene dust (38), and carbonates continue
239 to weather in Pleistocene loess deposits. Thus, over geologic timescales, atmospheric Ca deposition
240 during glacial periods may set the stage for future carbonate weathering, helping to build Mollisol
241 organic carbon stocks.

242 Implications for Mollisol conservation and climate mitigation

243 Our results imply that changes in soil Ca inputs due to cultivation might affect organic carbon
244 cycling in Mollisols. To address this possibility, we used our model to evaluate the magnitude of
245 changes to the Ca balance of Mollisol croplands relative to preindustrial conditions. We
246 parametrized the model with modern day atmospheric deposition chemistry, enabled agricultural
247 fertilizer addition and nutrient removal, and estimated agricultural liming rates. This analysis shows
248 that soil Ca cycling has changed dramatically in two ways (Fig. 4). First, the model predicts that
249 acid inputs from fertilizer and atmospheric deposition have accelerated Ca release from carbonate
250 weathering by 23% ($\pm 20\%$) in Mollisols. Second, agricultural liming has massively increased Ca
251 inputs to cropland soils (Fig. 4). Taking modeled liming rates as a reference point, agriculture has
252 more than doubled Ca inputs to Mollisol cropland soils and increased Ca input to non-Mollisol
253 cropland soils by 9-fold relative to preindustrial levels. Alternatively, we can take the most recent
254 available agricultural census liming data (39), which are from 1987, as a reference point. We
255 estimate that agriculture has increased Ca inputs to Mollisol cropland soils by 5-fold and non-
256 Mollisol cropland soils by 16-fold based on 1987 liming rates assuming that lime is 20% dolomite
257 and 80% calcite (40).

259 Clearly humans have dramatically altered the Ca cycle, and this has the potential to alter carbon
260 storage in Mollisols. Our finding that agriculture has accelerated dissolution of native carbonates is
261 consistent with other studies that have linked agricultural soil acidification to soil inorganic carbon
262 loss, although the acceleration of carbonate weathering predicted by our model is modest compared
263 to estimates in highly acidified systems (e.g., in China) (41–43). Our simulations indicate that the
264 more significant perturbation to the soil Ca cycle is agricultural lime addition. Adoption of
265 enhanced silicate (44) or carbonate (45) weathering for carbon dioxide removal will further perturb
266 the Ca cycle. These practices increase soil Ca inputs, which we have shown contribute to Mollisol
267 organic carbon storage over geologic timescales. However, increased Ca inputs have occurred in
268 response to unprecedented acid addition to cropland soils, and the effects of these competing
269 processes are hard to predict. For instance, experimental studies have found that the effect of
270 agricultural liming on soil organic carbon is not necessarily positive in the short term (46).
271 Similarly, enhanced silicate weathering does not necessarily benefit soil organic carbon storage in
272 the short term (47). Liming may affect soil carbon differently than natural weathering because it is
273 intermittent: in the USA only 5–20% of cropland is limed in any given year (48). Variable Ca
274 availability caused by intermittent liming may alternately stimulate and suppress decomposition,
275 with net effects that are challenging to predict.

276 In the broader context of conservation agriculture, our results suggest that farming practices that
277 mimic pre-agricultural vegetation in grasslands by increasing root inputs, increasing plant diversity,
278 or reducing tillage may not be sufficient to preserve Mollisol carbon. Instead, vegetation-focused
279 strategies may need to be complimented with geochemical strategies that mimic the natural Ca
280 cycle of these soils. For instance, reducing excess N can protect soil carbonates, which reduces
281 emissions from dissolution of soil inorganic carbon by strong acids (43), while also preserving a
282 critical Ca reservoir that helps to protect soil organic carbon. In addition, changing the cadence and
283 quantity of lime applied to croplands could better simulate the natural weathering regime. These
284 efforts must be supported by collection of baseline statistics on the agricultural Ca budget, which
285 remains poorly quantified (48). Closing these knowledge gaps is critical to managing Earth's most
286 fertile soils sustainably.

287

288

289 **Materials and Methods**

290 Quantifying global role of Mollisols

291 We calculated the total land area of Mollisols, the fraction of global agricultural production
292 occurring on Mollisols, and the fraction of agricultural soil organic carbon stored by Mollisols
293 using the Harmonized World Soil Database, Version 2.0 (HWSD) (2). For this analysis we
294 assumed that the distribution of Mollisols can be approximated by aggregating three World
295 Reference Base soil groups: Chernozems, Phaeozems, and Kastanozems (49). HWSD soil
296 mapping units were assigned values based on the dominant soil type in each unit. Organic carbon
297 storage in croplands and Mollisols was calculated from the HWSD and summed to 1 m depth. We
298 then combined the HWSD with the 1 km resolution GFSAD 2010 croplands mask (3) to estimate
299 the area of croplands and cropland organic carbon storage. Production of wheat, corn, and soy
300 occurring on Mollisols was obtained by combining the HWSD with SPAM global production
301 maps for 2010 (50). Production values were rescaled to calories based on UN Food and
302 Agriculture Organization Annex I food composition tables (51).

303 Geochemical model overview

305 We developed a simplified geochemical model to simulate the release of Ca from silicate and
306 carbonate weathering in the top 1 m of soil across the USA. We parametrized the model with
307 existing data when possible and then calibrated remaining parameters related to mineral surface
308 reactivity so that modeled soil pH matched observed modern soil pH across the study region. We
309 based our model on existing geochemical models that were designed to simulate soil acid-base
310 chemistry in response to acid rain (52). Our model also incidentally resembles approaches used to
311 simulate enhanced silicate weathering (53), although it was not designed for this purpose and is
312 less complex. The model treated the entire upper 100 cm of soil as a single chemically
313 homogeneous reservoir, tracking the inputs and outputs of seven ions that control soil pH and
314 weathering rates: Ca^{2+} , Mg^{2+} , Na^+ , K^+ , SO_4^{2-} , NO_3^- , Cl^- . These ions were sourced from dissolution
315 of silicate and carbonate minerals, atmospheric deposition, agricultural inputs, and biological
316 fixation in the case of N. Ions were lost via leaching, carbonate mineral precipitation, export in
317 crop biomass, and volatilization in the case of N. Additional ions were assumed to equilibrate
318 instantaneously with the soil solution and hence were modeled implicitly as a function of other
319 factors: H^+ , Al^{3+} , $\text{Al}(\text{OH})^{2+}$, $\text{Al}(\text{OH})_2^+$, $\text{AlH}_2\text{Org}^{2+}$, AlHOrg^+ , OH^- , CO_3^{2-} , HCO_3^- , H_2Org^- , HOrg^{2-} ,
320 Org^{3-} , $\text{Al}(\text{OH})_4^-$. We approximated ion activities with concentrations because under most
321 conditions modeled ionic strengths were too low to affect our results. Mineral concentrations
322 were treated as constant at the timescales being modeled. While the model was able to simulate
323 year-to-year weathering dynamics, for the purposes of this analysis, we applied a steady-state
324 solution because this simplified computations substantially. The model had nine governing
325 equations: one for each of the seven conserved ions and two algebraic constraints stipulating
326 charge balance and conservation of ions adsorbed on the soil exchange complex (Table S4). A
327 full description of the model is provided in the Supplementary Materials file.

328 Input data

330 Whenever possible, we used spatially explicit environmental data to assign model parameters.
331 When applicable, we used time-averaged environmental parameters to drive the model, setting the
332 years 2001-2010 as our reference period for recent environmental conditions. To capture pre-
333 industrial conditions, we reset deposition rates for N and S, reset atmospheric pCO_2 , and turned
334 off the model's agricultural nutrient budget.

335 To parametrize climate and soil hydrologic properties, we used several sources. We derived mean
336 annual air temperature from PRISM 30-year normals (1991-2020) at an 800 m resolution (54) and
337 treated air temperature as a proxy for soil temperature when running the model. We calculated

338 recharge (RC) using the Global Streamflow Characteristics Database (GSCD), which provides
339 0.125 degree resolution estimates of streamflow and base flow index (55). We calculated recharge
340 by multiplying streamflow by the baseflow index. We constrained soil moisture with the satellite-
341 informed Global Land Evaporation Amsterdam Model (GLEAM) V3.8 root zone soil moisture
342 dataset (0.25 degree resolution) (56). We also obtained pedotransfer-based maps of wilting point
343 and field capacity from GLEAM. Finally, we parameterized net primary productivity (NPP) using
344 MOD17 (500 m resolution) (57).

345 We parameterized soil mineralogy using two sources. For silicate minerals, we spatially
346 interpolated data from the North American Soil Geochemical Landscapes Project (NASGLP)
347 (20), which includes estimates of major element abundance and quantitative X-ray diffraction
348 data for a selection of silicate and carbonate minerals. We used these data to directly constrain
349 some minerals and approximate concentrations of others that are not directly reported by
350 NASGLP. First, we averaged A-horizon and C-horizon data at the NASGLP sampling locations.
351 We then interpolated the NASGLP data for each mineral to locations where we ran the
352 geochemical model, using inverse distance weighting with an exponent of 2 and an averaging
353 neighborhood of 75 km. Plagioclase feldspar and the plagioclase anorthite fraction (fAn) were
354 estimated by first multiplying the molar concentration of Na from the NASGLP by the formula
355 weight of albite. Where albite exceeded 80% of the total plagioclase feldspar content obtained
356 from the NASGLP, albite was reset to 80% of the plagioclase content. Anorthite was then
357 assumed to make up the remainder of the plagioclase pool (26). K-feldspar, hornblende, and
358 pyroxene were taken directly from the NASGLP X-ray diffraction estimates. To represent clay
359 minerals, we limited our analysis to chlorite (clinochlore) and illite (approximated as muscovite),
360 which we treated as generalized categories that stand in for the full diversity of Mg- and K-
361 bearing 2:1 phyllosilicates (e.g. vermiculite and smectite group clays). Illite was calculated by
362 subtracting the K in K-feldspar from total K and assigning all residual K to illite. Similarly,
363 chlorite was calculated by first calculating the amount of Mg in hornblende, pyroxene, and
364 dolomite (Table S6). This value was subtracted from total Mg, and any residual Mg was assigned
365 to chlorite.

366 To estimate carbonate mineral stocks, we did not use NASGLP data directly. Given the high
367 weatherability of carbonates, small quantities of carbonate mineral had a large effect on modeled
368 soil pH values; hence we used high-resolution digital soil maps from NATSGO (21) to ensure
369 accurate assignment of soil carbonate content. We first calculated the stock of carbonate in
370 CaCO_3 equivalents to 1 meter depth from NATSGO. Next, we subdivided this stock into calcite
371 and dolomite components by using the data from the NASGLP to calculate the ratio of calcite to
372 dolomite. In addition to CaCO_3 content, we derived soil texture (silt, sand, and clay percentages),
373 cation exchange capacity, and soil bulk density parameters from NATSGO, averaging these
374 properties over the top 1 meter of soil or to bedrock if shallower than 1 meter. All NATSGO soil
375 properties were summarized by calculating the share-weighted average within soil mapping units.
376 Data were then extracted using the 30-meter resolution gridded version of NATSGO.

377 We parameterized the cropland N inputs and outputs using a county-level nutrient budget for the
378 period 1987-2012 (58). We ran the geochemical model in one of two modes, either with cropland
379 nutrient imports and exports enabled or with only natural N fixation rates enabled. We determine
380 which mode to use by assigned modeled locations to cropland or non-cropland land cover using
381 the GFSAD 1 km cropland mask (3).

382 We parameterized deposition of N, S, Cl, Ca, Mg, Na, and K, using gridded data from the US
383 Environmental Protection Agency's National Trend Network (59), which we averaged for 2001-
384 2010. To represent preindustrial deposition of N and S, we used the multi-model average from the
385 ACCMIP project for the year 1850 (24). For Cl, Ca, Mg, Na, and K no data from before the year
386 2000 were available. Human activity has increased deposition of base cations, including Ca, in the

387 Western USA (36). To account for this trend, we applied a factor of 5 difference between recent
388 and preindustrial times, which approximates dynamics recorded in lake sediment cores in
389 Colorado (36). We applied this multiplier to Ca, Mg, and K, but left Na unchanged since this
390 solute is primarily derived from marine aerosols outside of deserts.

391

392 Model calibration and uncertainty

393 We implemented the model at point locations, extracting data from the aforementioned
394 environmental datasets at each point. For the calibration and validation steps, we selected points
395 by acquiring soil pH data from the USDA NRCS National Cooperative Soil Survey (NCSS)
396 Kellogg Soil Survey Laboratory database. We computed depth weighted average pH values in a
397 1:1 water matrix for all soil profiles with available data to a depth of 1 m, or to the depth of the
398 lowermost C horizon in cases where the profile terminated below 1 m. Similarly, we computed
399 depth-weighted average values for exchangeable cations using the NCSS database. We
400 represented Ca^{2+} , Mg^{2+} , Na^+ , and K^+ using NH_4 -acetate (pH 7) extraction data and Al^{3+} from KCl
401 extraction. Exchangeable H^+ was estimated by subtracting the sum of exchangeable Ca^{2+} , Mg^{2+} ,
402 Na^+ , K^+ , and Al^{3+} from the cation exchange capacity (CEC) obtained by the NH_4 -acetate method.
403 When the sum of these ions exceeded the CEC, exchangeable H^+ was set to zero and the values of
404 all ions were rescaled by the value (CEC / sum cations) so that the sum equaled the CEC.

405 We spatially resampled the pH and exchangeable cation data by binning them into 1 degree by 1
406 degree cells based on their latitude and longitude and then resampling 6,000 locations with
407 replacement, with sampling weights inversely proportional to the number of profiles in each cell.
408 We extracted environmental data at these points and discarded those with missing data, yielding
409 4,149 unique pH observations that were evenly distributed across the conterminous USA (Fig.
410 S1). Exchangeable ions were only reported at 2,484 locations with pH measurements. Because we
411 resampled with replacement, some soil profiles occurred more than once by design; the total
412 number of pH observations was 5,389 (including pseudo-replicates) and the total number of
413 exchangeable cation observations was 3,280.

414 We calibrated the model by randomly sampling 2,000 training points from the NCSS profiles and
415 using them for model inversion based on soil pH. We optimized two parameters, r_2 and r_3 , which
416 controlled the reactivity for secondary phyllosilicate minerals and carbonate minerals respectively
417 (see Supplementary Materials). We calibrated the model using a Markov Chain Monte Carlo
418 (MCMC) approach, applying the adaptive Metropolis Hastings algorithm with delayed rejection
419 (60) implemented via the R package FME (61). The cost function was defined to minimize errors
420 in soil pH. We initiated the MCMC algorithm with manually calibrated initial parameter values
421 and uninformative priors. The initial model variance was set equal to the mean squared residuals
422 based on the initial parameter estimates, and the initial jump values were set to 10% of the initial
423 parameters. The adaptive stage of the algorithm was run for a burn-in period of 1,000 iterations
424 updating the covariance matrix every 50 iterations with the number of delayed rejections steps set
425 to 2. After burn-in sampling continued for an additional 1,000 iterations. We checked for
426 convergence by running the algorithm using perturbed values of the starting parameters and
427 different training samples and found that results were comparable. The final calibration yielded
428 values of $10^{-6.8}$ for r_2 and $10^{-6.3}$ for r_3 .

429 We estimated uncertainty in modeled Ca fluxes using a Monte Carlo approach. We expanded this
430 analysis beyond the calibrated parameters to address uncertainty in all parameters, excepting
431 chemical formulae and well-known physical constants. Variables and parameters included in the
432 uncertainty analysis included: soil moisture, field capacity, wilting point, recharge, net primary
433 productivity, temperature, all deposition fluxes, all components of the agricultural N budget,
434 cation exchange capacity, sand, silt and clay fractions, bulk density, the reaction order for silicate
435 weathering, all mineral surface areas, all constants related to organic acid equilibria, Q_{10} , decay

436 rate, and input rate for DOC, the coefficient for gaseous loss of N, weathering rate parameters r_1 ,
437 r_2 , and r_3 , and all cation exchange constants. Uncertainties for most of these parameters could not
438 be constrained. Instead, we applied a uniform relative uncertainty distribution of +/- 20% to each
439 variable or parameter. Specifically, we ran the model at the 2,000 calibration points 1,000 times,
440 randomly rescaling each parameter or environmental input by a value between 80% and 120% of
441 the observed value. We treated the standard deviation of the Ca flux distributions derived from
442 this process as a first-order estimate of uncertainty given an assumed 20% range in all inputs.
443

444 Statistical analysis

445 After calibrating the geochemical model, we used it to create maps of preindustrial Ca pools and
446 fluxes across the conterminous USA. We used these maps to quantify the strength of the
447 relationships between occurrence of Mollisols, A-horizon organic carbon, and soil Ca availability
448 using logistic regression. To create the maps, we established a 10-kilometer resolution grid across
449 the study region and extracted environmental data at each point in the grid. Presence or absence of
450 Mollisols was obtained from NATSGO. For each NATSGO map unit, we identified the soil order
451 with the largest share (areal contribution), excluding non-soil land classes. When modelling
452 Mollisol extent, we represented soil Ca availability with the modern base saturation percentage.
453 Predicted Mollisol extents were obtained by applying a probability threshold to the logistic
454 regression output, with the threshold optimized so that predicted Mollisols land area equaled the
455 actual mapped area (probability = 0.4).

456 Following a similar protocol, we quantified the strength of the relationship between A-horizon
457 soil organic carbon (SOC) stocks from RaCA (22) and the NCSS (23) databases and Ca using
458 ordinary least squares regression. When working with data from RaCA and NCSS, we calculated
459 the SOC stock in all horizons with the master designation “A”. The SOC stock (kg C m^{-2}) was
460 calculated from the organic carbon percentage (OC%), the inorganic carbon percentage (IC%), A-
461 horizon thickness (TH, cm), rock fraction (RF, unitless) and bulk density (BD, g cm^{-3}) as:

$$462 \text{SOCstock} = ((\text{OC\%} - \text{IC\%})/100) * \text{BD} * \text{TH} * (1 - \text{RF}) * 10 \quad (\text{Equation 23})$$

463 Inorganic carbon was calculated from CaCO_3 equivalents reported in RaCA. In the few cases
464 where IC% exceeded OC%, OC% was set to zero. In the case of NCSS, we used the “estimated
465 organic C” field, which is already corrected for IC where applicable, or organic carbon content
466 estimated via the Walkley Black method when this field was not available. After calculating SOC
467 in each A horizon, we summed all A horizon stocks for each pedon to obtain total A-horizon
468 SOC. We log transformed A-horizon SOC stocks before fitting the model. When modelling A-
469 horizon SOC, we used modern total exchangeable calcium (ceq kg^{-1}), and also included the sum
470 of all other exchange ions as an additional predictor in the regression model.

471 In specifying both regression models, we included the presence of grassland vegetation as a
472 predictor using potential natural vegetation maps developed by ISCLP. We treated grassland
473 presence as a binary predictor, combining grasslands and savannas into a single category (present
474 = 1, absent = 0). In addition to vegetation, we controlled for mean annual temperature and mean
475 annual precipitation based on 30-year normals from Prism (54). We also included three additional
476 potential confounding variables: the logarithm of average NPP, derived from MOD17 for the
477 period 2001-2010, average silt plus clay content of the top meter of soil, and soil drainage class.
478 The latter two variables were derived from NATSGO (21). Drainage class categories were
479 assigned numerical values from 1-7, with 1 being excessively drained and 7 being very poorly
480 drained. When fitting the regression model for SOC, we also included the sum of non-Ca
481 exchangeable ions (ceq kg^{-1}) as an additional predictor. We compared the relative importance of
482 different predictors in the regression models by standardizing all predictors upstream of fitting the

483 models. We standardized by dividing predictors by two times the standard deviation, which is
484 recommended in cases when some predictors are binary (62).

485 In addition to computing scaled coefficients, we evaluated the effect of specific Ca sources on
486 Mollisol extent and A-horizon SOC under preindustrial conditions. We evaluated the effect of
487 cation inputs from carbonate weathering and silicate weathering by running the model with each
488 mineral cation source eliminated, which meant that Ca, but also Mg, K, and Na fluxes were
489 affected by removing each source. We achieved this by re-setting the surface areas of all silicates,
490 all carbonates, or both mineral types to zero. In the case of deposition, we set base cation
491 deposition to zero. Each of these modified model runs generated predictions of exchangeable Ca
492 in the absence of each cation source; these values were then used as inputs to the fitted regression
493 models and used to predict either Mollisol extent or A-horizon SOC. We also quantified the effect
494 of eliminating grasslands by setting the ISCLP-derived grassland and savanna predictor to zero
495 everywhere and then obtaining predictions from the fitted regression models.

496 We ran regressions on the full population of model evaluation points ($n = 77,115$ points sampled
497 from NATSGO; 11,332 A-horizon SOC estimates from RaCA and NCSS). We addressed the
498 spatial dependence of these observations by performing nonparametric spatially blocked
499 bootstrapping (26). This involved dividing the data (NATSGO grid or RaCA/NCSS based) into
500 blocks defined by 2-by-2 degree grid cells and then resampling the cells with replacement 1,000
501 times. We fit a logistic or ordinary least squares regression to each of the 1,000 resampled
502 datasets and stored the regression coefficients. We then calculated bias corrected and accelerated
503 95% confidence intervals from the bootstrap replicates (63). We followed the same protocol for
504 estimating uncertainty associated with predicted Mollisol areas and A-horizon SOC stocks after
505 resetting the model inputs as described above.

506 Soil organic matter can contribute to cation exchange capacity, which may explain a relationship
507 between total exchangeable calcium and SOC even in the absence of an effect of Ca on SOC
508 persistence. To account for this possibility, we conducted an additional regression analysis after
509 correcting total cation exchange capacity for the contribution of soil organic matter. Corrected
510 cation exchange capacity (CEC-c, ceq kg^{-1}) was obtained from the uncorrected CEC and the soil
511 organic matter percentage (SOM%) from NATSGO:

512
$$\text{CEC-c} = \text{CEC} - \text{CEC-OM} * (\text{SOM\%}/100) \quad (\text{Equation 24})$$

513 Where CEC-OM is the cation exchange capacity of organic matter, assumed equal to 200 ceq kg^{-1}
514 (64). This formula could generate negative or zero values, and so in cases where CEC-c was less
515 than a minimum value of 0.01 we re-set it to this value. The results of the regressions computed
516 with CEC-c were similar to the primary results (Fig. S5).

517

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673

674

675 **Acknowledgments**

676 **Funding:**

677 LLNL Laboratory Directed Research and Development grant 22-ERD-19 (EWS, KG)

678 LLNL Laboratory Directed Research and Development program 24-SI-002 (JP)

679 DOE Carbon Negative Energy Earthshot Research Center SCW1841 (JP)

680 Work at LLNL was performed under the auspices of the DOE, Contract DE-AC52-
681 07NA27344.

682 **Author contributions:**

684 Conceptualization: EWS, HRG, RL, KJM, JP, NS, DZ, KG

685 Methodology: EWS, KG

686 Investigation: EWS

687 Visualization: EWS

688 Supervision: EWS, KG

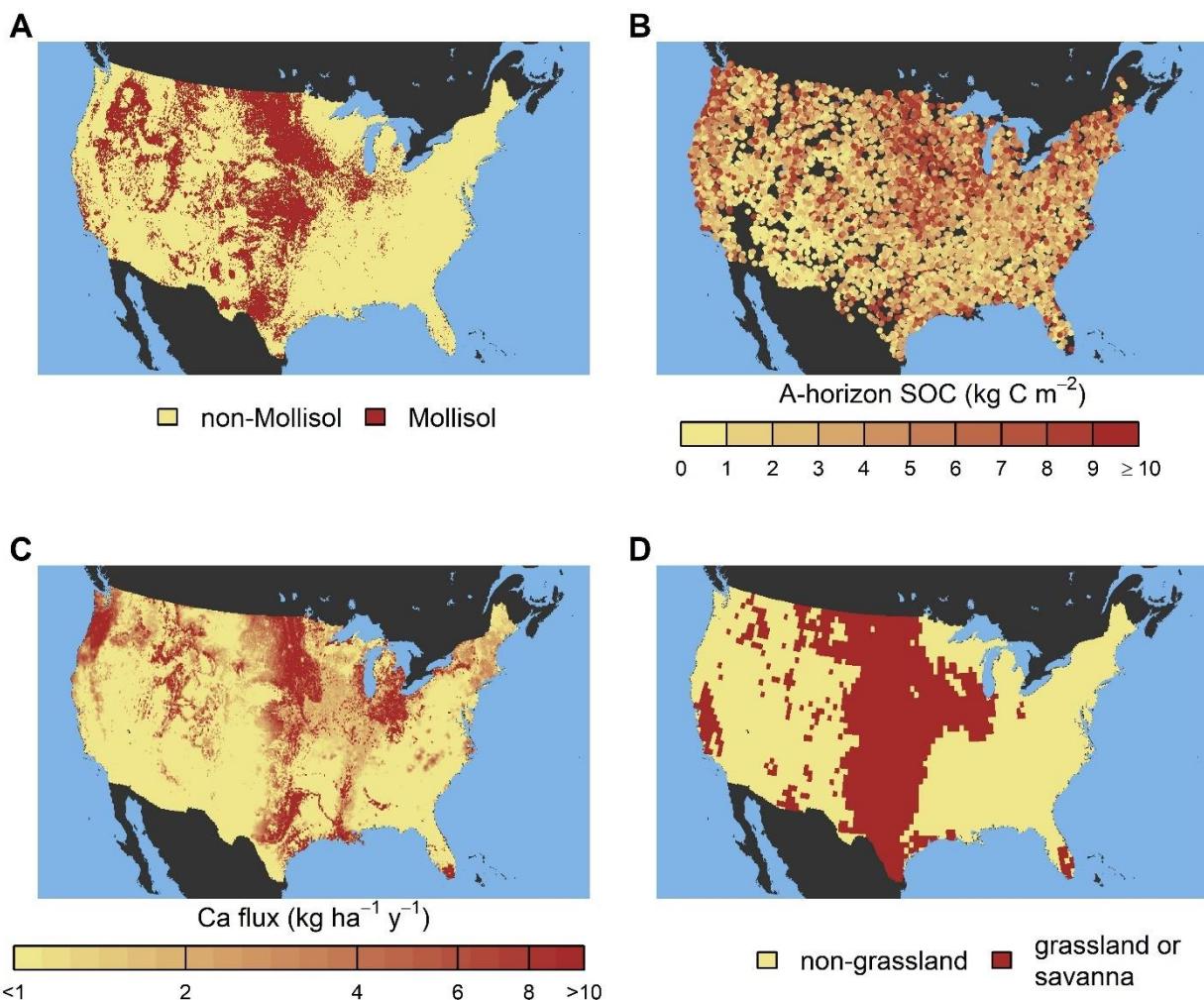
689 Writing—original draft: EWS

690 Writing—review & editing: EWS, HRG, RL, KJM, JP, NS, DZ, KG

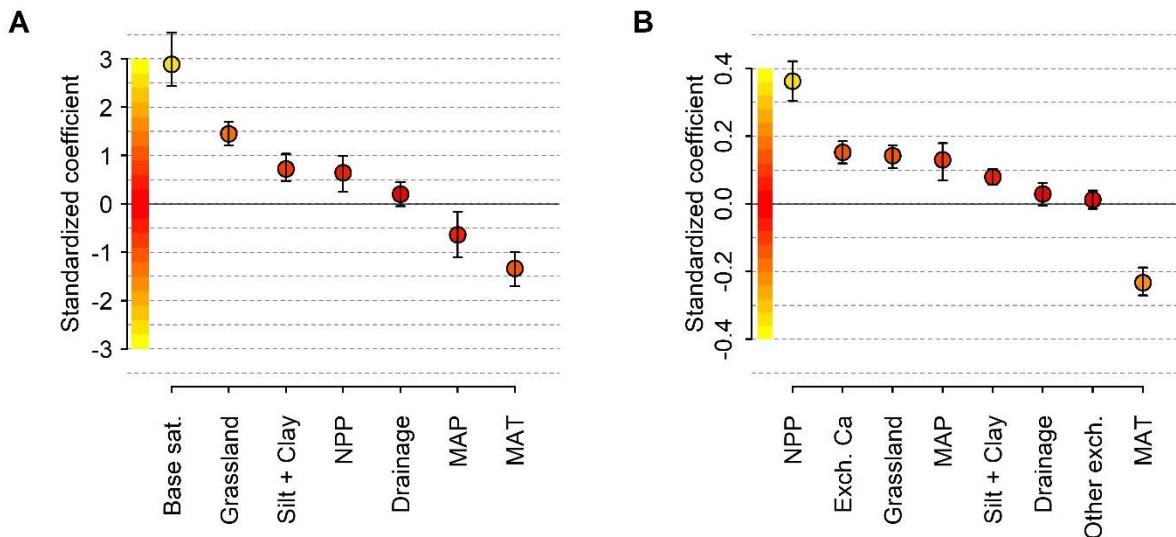
691 **Competing interests:** Authors declare that they have no competing interests.

692 **Data and materials availability:** The R code used to perform these analyses is available at
693 <https://github.com/eslessarev/Calcium-promotes-carbon-rich-grassland-soil-R-Code>.

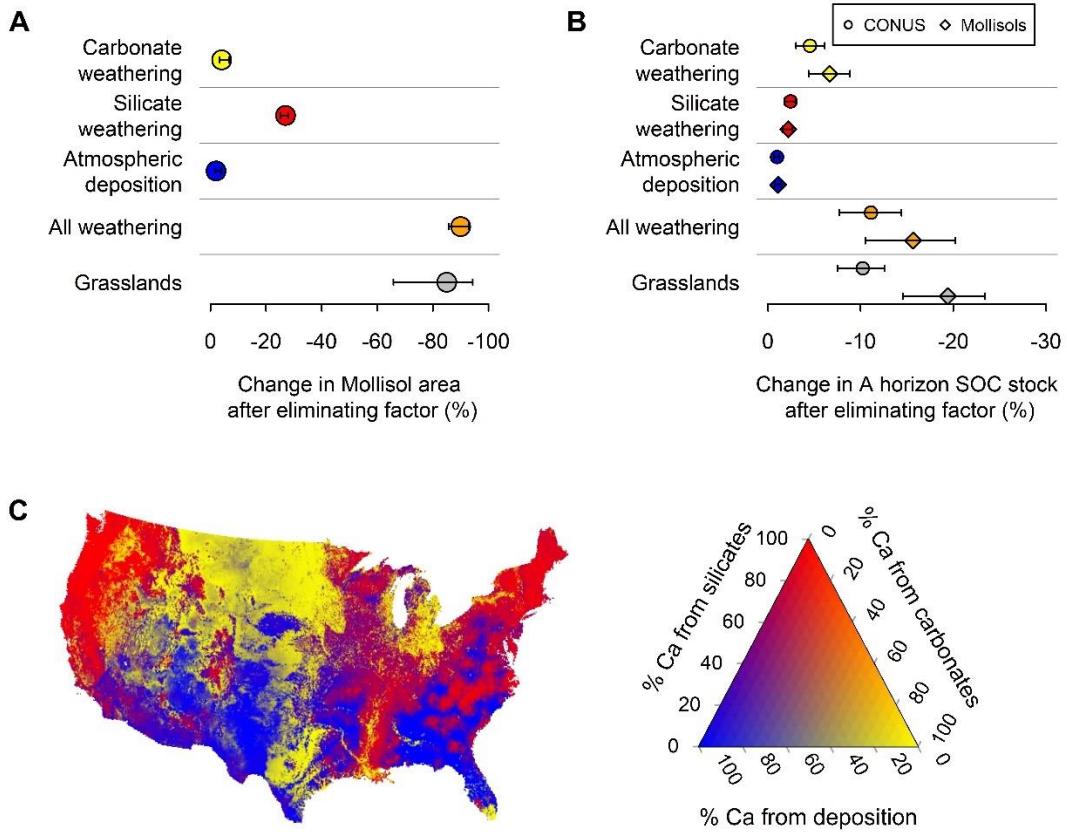
Figures and Tables



700
701 **Fig. 1. Potential environmental controls on Mollisols across the USA. (A)** The
702 distribution of the Mollisol soil order across the conterminous USA based on
703 digital soil mapping (21). **(B)** Point observations of A-horizon soil organic carbon
704 (SOC) derived from two databases (22, 23). **(C)** Modeled preindustrial available
705 calcium flux from silicate weathering, carbonate weathering, and atmospheric
706 deposition. **(D)** The potential distribution of grasslands and savannas (25).



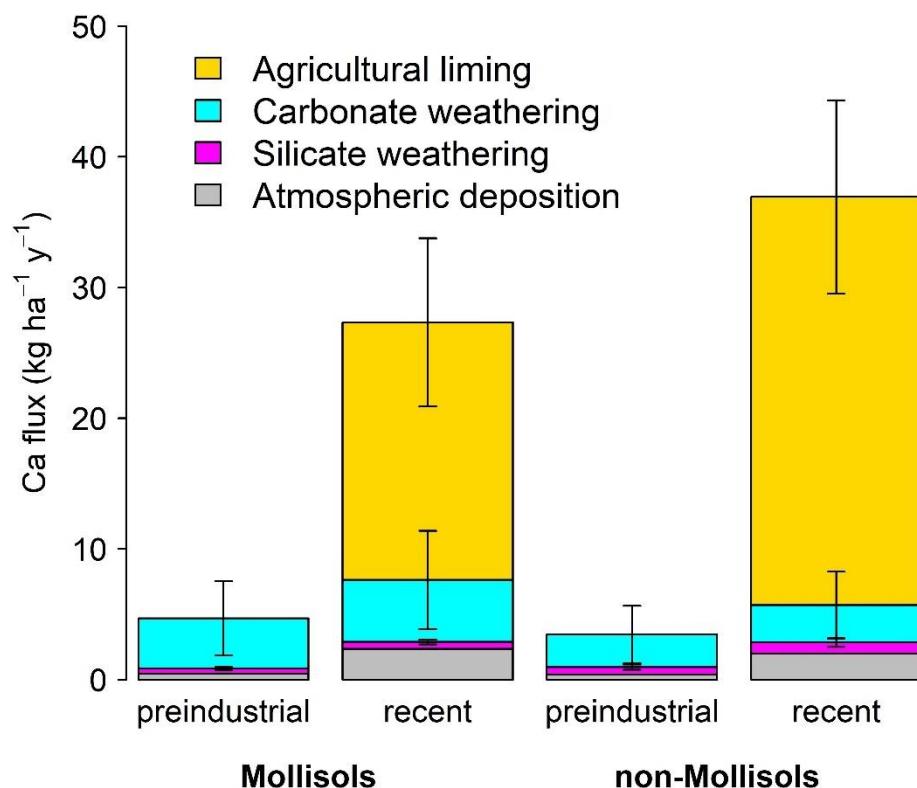
707
708 **Fig. 2. Controls on Mollisol distribution and A-horizon soil organic carbon stocks in**
709 **the USA. (A)** Standardized regression coefficients derived from a multivariate
710 logistic regression model, where the presence or absence of Mollisols was
711 predicted as a function of the seven variables listed on the horizontal axis. **(B)**
712 Standardized regression coefficients derived from a multivariate linear regression
713 model, where A-horizon organic carbon stocks were predicted as a function of the
714 eight variables listed on the horizontal axis. In both panels, whiskers show 95%
715 confidence intervals derived from a spatial blocked bootstrapping procedure (see
716 Materials and Methods). Standardization was performed by dividing each non-
717 binary variable by two times the standard deviation.⁴⁹ The absolute value of each
718 regression coefficient is an index of how strongly related each variable is to the
719 response variable, and is shown with a relative color scale: yellow = maximum, red
720 = zero. Abbreviations: Base sat. = base saturation, NPP = net primary productivity,
721 MAT = mean annual temperature, MAP = mean annual precipitation, Exch. Ca =
722 total exchangeable Ca, Other exch. = sum of non-Ca exchangeable ions.



723
 724 **Fig. 3. Sources of available Ca and their effect on Mollisol extent across the USA. (A)**

725 The relative effect of removing Ca sources on predicted Mollisol area and the
 726 effect of eliminating grasslands. **(B)** The relative effect of removing the same set
 727 of environmental factors on total A-horizon soil organic carbon across the
 728 conterminous USA (CONUS; circles) and Mollisol areas only (diamonds).
 729 Whiskers show 95% confidence intervals derived from spatial blocked
 730 bootstrapping (see Methods). **(C)** The relative contributions of carbonate
 731 weathering, silicate weathering, and atmospheric deposition to available Ca across
 732 the USA. Across all panels red = silicate weathering, yellow = carbonate
 733 weathering, and blue = deposition.

734



736
737 **Fig. 4. Modeled available Ca fluxes to croplands, preindustrial (1850) versus recent**
738 **(2000-2010).** Stacked bars show the Ca sources: atmospheric deposition, carbonate
739 weathering, silicate weathering, and agricultural liming. Data for Mollisol regions
740 are shown on the left and non-Mollisol regions on the right. Whiskers show
741 standard error estimates for each quantity derived from a Monte Carlo uncertainty
742 analysis assuming +/- 20% variability in the model inputs and parameters. Liming
743 estimates are based on the conservative assumption that farmers lime sufficiently
744 to maintain soil pH (see Supplementary Materials).
745

Supplementary Materials for

Calcium promotes carbon-rich grassland soils

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This supplement includes:

Supplementary Text
Figs. S1 to S5
Tables S1 to S7
References (1 to 34)

769 **Supplementary Text: Geochemical model description**

770 Governing equations

771 Our model was specified to track inputs and outputs of seven ions that control soil pH and
772 weathering rates: Ca^{2+} , Mg^{2+} , Na^+ , K^+ , SO_4^{2-} , NO_3^- , Cl^- (Table S3). These ions were sourced from
773 dissolution of silicate and carbonate minerals, atmospheric deposition, agricultural inputs, and
774 biological fixation in the case of N. Ions were lost via leaching, carbonate mineral precipitation,
775 export in crop biomass, and volatilization in the case of N. Additional ions were assumed to
776 equilibrate instantaneously with the soil solution and hence were modeled implicitly as a function
777 of other factors: H^+ , Al^{3+} , $\text{Al}(\text{OH})^{2+}$, $\text{Al}(\text{OH})_2^+$, $\text{AlH}_2\text{Org}^{2+}$, AlHOrg^+ , OH^- , CO_3^{2-} , HCO_3^- , H_2Org^- ,
778 HOrg^{2-} , Org^{3-} , $\text{Al}(\text{OH})_4^-$.

779

780 Hydrology

781 We parametrized leaching rates for major ions as a function of recharge or hydrologic baseflow
782 (RC , mm y^{-1}), which we assume represents the flux of water that infiltrates the soil without being
783 lost to evapotranspiration or overland flow. We partitioned the total amount of soil water (V , l)
784 into mobile and immobile components, under the assumption that only a fraction of the soil pores
785 are leached during leaching events. The immobile component of the soil water was equal to the
786 water content at wilting point (V_{wp} , l), which governed the fraction of soil water mobilized during
787 recharge:

788

789
$$F_{\text{mob}} = (\text{V} - \text{V}_{\text{wp}})/\text{V} \quad (\text{Equation 1})$$

790

791 We assumed that only the solutes in the mobile fraction are vulnerable to leaching loss and that
792 solutes are partitioned into mobile and immobile fractions by F_{mob} . We also assumed that solutes
793 in the mobile fraction are conservatively diluted at the timescale of recharge events. The
794 concentration of solute i leached during recharge events (C_i) was therefore a function of the soil
795 moisture at field capacity, V_{fc} :

796

797
$$C_i = M_i * F_{\text{mob}} / (\text{V}_{\text{fc}} - \text{V}_{\text{wp}}) \quad (\text{Equation 2})$$

798

799 Where M_i was the total moles of the solute in the soil. The leaching rate for a given ion, L_i (mol y^{-1})
800 was a function of concentration in recharge water (mol l^{-1}) times recharge (l y^{-1}):

801

802
$$L_i = \text{RC} * C_i \quad (\text{Equation 3})$$

803

804 Weathering kinetics

805 Weathering kinetic expressions vary widely in complexity. We adopted a simple power law
806 description for silicate weathering kinetics. More complex approaches, such as transition state
807 theory, incorporate multiple reaction mechanisms. These approaches are sensitive to assumptions
808 regarding the type and reactivity of secondary minerals and the extent of mineral surface
809 passivation, which we could not parametrize at the scale of the USA. To further reduce
810 complexity, dissolution kinetics of tectosilicates and inosilicates were referenced to the reactivity
811 of plagioclase feldspar based on a compilation of field-based weathering rate measurements (1).
812 This was not possible for pyroxene given a lack of field based weathering rate estimates, so we
813 assigned this mineral a reaction rate of 1.0 relative to plagioclase. For tecto- or inosilicate mineral
814 i , weathering rates in the top 100 cm of soil (mol y^{-1}) were a function of total geometric surface
815 area (A_i , m^2), a reaction rate coefficient (r_i , $\text{mol m}^{-2} \text{y}^{-1}$), the ratio giving reaction rate relative to
816 plagioclase (RR_i , unitless), an Arrhenius-type term governing temperature dependence (T_f ,
817 unitless), volumetric water content ($\theta \text{ m}^3 \text{ m}^{-3}$), the hydrogen ion concentration ($[\text{H}^+]$), a reference
818 hydrogen ion concentration ($[\text{H}^+]_r$, set equal to 10^{-5}), and the reaction order with respect to H^+ (n).

819
820 $W_i = A_i * r_1 * R R_i * T_f * \theta * (H^+ / H^+_{ref})^n$ (Equation 4)

821
822 For phyllosilicate minerals, the rate expression was identical except that the term $R R_i$ was omitted
823 and an affinity term was added to make the reactions reversible, allowing clay synthesis.

824
825 $W_{i, phyllo} = A_i * r_2 * T_f * \theta * (H^+ / H^+_{ref})^n * (1 - \Omega_i)$ (Equation 5)

826
827 The term r_2 gives a reaction rate coefficient for phyllosilicates. The parameter Ω_i was the
828 saturation index for phyllosilicate mineral i , where $\Omega_i = IAP_i / K_{sp}$. The IAP was the ion activity
829 product or reaction quotient. K_{sp} was the solubility constant for each mineral.

830
831 We assumed that the temperature and pH dependence of silicate weathering was the same for all
832 minerals. The activation energy for silicate weathering was set to equal $74 \text{ kJ mol}^{-1} \text{ K}^{-1}$ (2). The
833 temperature modifier for silicate weathering was given by the following equation:

834
835 $T_f = \exp(-E_{asil}/R * (1/(T) - 1/(T_{ref})))$ (Equation 6)

836
837 Where E_{asil} was the activation energy for silicates, R was the universal gas constant, T was the
838 soil temperature approximated as the mean annual air temperature (K) and T_{ref} was a reference
839 temperature (298 K).

840
841 We assigned several silicate weathering parameters manually in order to match published
842 compilations of field weathering rates (3, 4). The parameter r_1 represented the bulk plagioclase
843 feldspar weathering rate coefficient (y^{-1}) at a reference pH of 5.0 ($H_{ref} = 10^{-5}$). We assumed that
844 under the wettest climate conditions, mean soil pH approaches a value of 5.0 (5), and so bulk
845 feldspar weathering rates ought to approach r_1 under these conditions. Across our calibration
846 dataset, the 95th percentile value for recharge (RC) equaled 474 mm, which implies that r_1 equals
847 $10^{-4.3}$ based on the power law relationship between recharge and bulk weathering rates reported by
848 Yu and Hunt (2018) (4). Based on similar reasoning, we set the reaction order for H^+ , n , equal to
849 0.66. We chose this value because field estimates of silicate weathering rates increase by roughly
850 two orders of magnitude in the transition from dry conditions (infiltration rates $\sim 0.1 \text{ m y}^{-1}$) to
851 humid conditions (infiltration rates $\sim 1 \text{ m y}^{-1}$) (3), and soil pH spans roughly 3 units in the
852 transition from wet to dry climates (5). This implies that weathering rates should increase by two
853 orders of magnitude over a three order of magnitude range in pH (reaction order = 0.66). This
854 value is reasonable for many silicates (6), and allowed us to recover the observed relationship
855 between feldspar weathering rates in the field and infiltration reasonably well with the calibrated
856 model (Figure S4).

857
858 We modeled carbonate weathering kinetics using a more complex expression based on transition
859 state theory because carbonate minerals dissolve and precipitate congruently in soil, reducing
860 uncertainty regarding secondary minerals and surface passivation. Dissolution and precipitation
861 for carbonate minerals was governed by the following equation:

862
863 $W_{i, carb} = A_i * r_3 * \theta * (R_{acid} * [H^+]^{nH} + R_{neutral} + R_{CO2} * pCO_2^{nCO2}) * (1 - \Omega_i)$ (Equation 7)

864
865 Where A_i was the total surface area for mineral i , r_3 was ratio of reactive surface area to geometric
866 surface area for carbonates, R_{acid} , $R_{neutral}$, and R_{CO2} were separate reaction mechanisms for acid,
867 neutral, and CO_2 driven dissolution reactions, nH was the reaction order for H^+ , and nCO_2 was the
868 reaction order for CO_2 . The parameter Ω_i was the saturation index for carbonate mineral i , where

869 $\Omega_i = IAP_i/K_{sp}$. The IAP was the ion activity product or reaction quotient. K_{sp} was the solubility
870 constant for each mineral. Reaction mechanisms (R_m) were governed by equations with the form:
871

872 $R_m = A_m * \exp(-E_{am}/R * (1/(T) - 1/(T_{ref})))$ (Equation 8)
873

874 Where A_m and E_{am} were the preexponential factor ($\text{mol m}^{-2} \text{y}$) and activation energy ($\text{kJ mol}^{-1} \text{K}^{-1}$)
875 for mechanism m .
876

877 All spatially invariant parameters related to weathering reactions are given in Table S5. Our
878 treatment of weathering kinetics left two unknown parameters: r_2 , the reaction rate coefficient for
879 phyllosilicates, and r_3 , the ratio of reactive to total surface area for carbonates. These parameters
880 were obtained by model inversion (see Methods in main article).
881

882 Mineral surface areas

883 We estimated geometric surface areas for each mineral. For tectosilicates, inosilicates, and
884 carbonates, we assumed that particles were silt- and sand-sized and spherical. We calculated
885 surface area to volume ratios (SVR, $\text{m}^2 \text{m}^{-3}$) for silt and sand:
886

887 $SVR = (4 * \pi * (D/2)^2) / (4/3 * \pi * (D/2)^3)$ (Equation 9)
888

889 Where D was the particle diameter, which we set to the geometric mean of each size class (7).
890 The average surface area to volume ratio for minerals in the silt and sand fraction was then
891 calculated as a weighted average based on silt and sand percentages derived from the NATSGO
892 database (see below). Clays (illite and chlorite) were modeled as cylindrical plates with a
893 diameter of 1 um and a diameter to height ratio of 10:1 (7):
894

895 $SVR_{clay} = ((D/10 * 2 * \pi * D/2) + (2 * \pi * (D/2)^2)) / ((D/10) * (\pi * (D/2)^2))$ (Equation 10)
896

897 Total geometric surface area for each mineral was obtained by multiplying the surface area to
898 volume ratio by the total volume of each mineral in the soil.
899

900 $A_i = SVR_i * P_i * (\rho_s / \rho_i) * h * 10^{-5}$ (Equation 11)
901

902 Where P_i was the percentage of mineral i in the soil, ρ_s was the bulk density of the soil, ρ_i was the
903 density of mineral i , and h was the soil thickness in mm. Chemical formulas and densities for the
904 minerals that we included in the model are shown in Table S6. For clay minerals, we limited our
905 analysis to chlorite (clinochlore) and illite (approximated as muscovite), which we treated as
906 generalized categories that stand in for the full diversity of Mg- and K-bearing 2:1 phyllosilicates
907 (e.g. vermiculite and smectite group clays).
908

909 Equilibrium chemistry

910 We parametrized a set of major equilibrium reactions that governed carbonate ion speciation,
911 aluminum hydrolysis, organic acid speciation, Al-organo ion pair formation, and cation exchange
912 reactions (Table S7). When possible, we obtained equilibrium constants by calculating them from
913 standard enthalpies and entropies, which we obtained from the SUPCRT92 thermodynamic
914 database (8) loaded with the R package CHNOSZ (9).
915

916 Carbonate equilibria depended on the average soil $p\text{CO}_2$, which we parametrized as a function of
917 soil respiration (10):
918

919 $pCO_2 = pCO_{2atm} + 1.03 * R_s / T^2$ (Equation 12)

920
921 Where pCO_{2atm} was atmospheric pCO_2 , set to 380 ppm for 2001-2010 (11) and 280 ppm for
922 preindustrial times (12), and R_s was soil respiration in $g m^{-2} y^{-1}$. We obtained R_s from net primary
923 productivity (NPP, $g m^{-2} y^{-1}$) (13):

924
925 $R_s = 1.24 * NPP + 24.5$ (Equation 13)

926
927 We modeled dissolution and precipitation of carbonates and phyllosilicates as reversible
928 processes governed by chemical equilibria (Table S7), which defined the saturation index (Ω)
929 used in weathering rate calculations. In the case of phyllosilicates, the saturation state depended
930 on dissolved H_4SiO_2 , which we did not model explicitly as a state variable. Instead, the
931 concentration of H_4SiO_2 was assumed to be determined by instantaneous dissolution and
932 precipitation of secondary amorphous SiO_2 (Table S7).

933
934 We represented organic acid speciation using the triprotic model and allowed for formation of ion
935 pairs between Al^{3+} and organic acids. Equilibrium constants for these reactions were obtained by
936 averaging published values from New England lakes, streams, and soils (14). To parametrize
937 equilibrium reactions involving organic acids, we estimated the amount of dissolved organic
938 carbon and then calculated total organic acid charge (Org_{tot} , moles charge) from total DOC
939 (moles). We converted DOC to Org_{tot} based on a charge density ($m = 0.049 \text{ mol mol}^{-1}$) averaged
940 from the New England water survey (14). We approximated soil DOC concentrations by
941 assuming that DOC inputs are equal to NPP, reasoning that over the long run all plant inputs to
942 soil must be converted to DOC before they are respiration or sequestered. We then assumed that
943 DOC decays as a first order process and is lost due to leaching:

944
945 $dDOC/dt = NPP - k_{DOC} * Q_{10}^{((T - 293)/10)} * DOC - DOC * RC * F_{mob} / (V_{fc} - V_{wp})$ (Equation 14)

946
947 Where k_{DOC} was a decay constant and Q_{10} defined the temperature dependence of DOC decay. We
948 obtained k_{DOC} by taking the geometric mean of previously reported “fast” and “slow” DOC decay
949 constants (15). Assuming that DOC is maintained at steady state for our purposes, the organic
950 acid concentration ($mol \text{ l}^{-1}$) was obtained from the following equation:

951 $Org_{tot} = m * (NPP / 12.01) / (1 + k_{DOC} * Q_{10}^{((T - 293)/10)}) * (1/V)$ (Equation 15)

952
953 Exchange reactions were specified using the Gaines-Thomas approach. We parameterized cation
954 exchange reactions using an existing compilation (16), which summarized Gaines-Thomas
955 exchange constants for sand, loess (silt enriched), and clay dominated soils in the Netherlands. As
956 a first order approximation, we assigned exchange constants by calculating the weighted mean of
957 the profile-averaged constants listed in the compilation, with weights given by the sand, silt, and
958 clay fractions obtained from NATSGO.

959
960 When calibrating the model, we simulated re-equilibration of soil pH with laboratory conditions
961 because in-situ pH and laboratory-measured pH can vary substantially (17). To do this, we fixed
962 soil water content so that the soil mass to water ratio equaled 1:1, set the temperature to 20°C, and
963 adjusted pCO_2 to reflect the ambient atmospheric concentration. Concentrations of conserved ions
964 were adjusted to reflect the change in soil water content during measurement. Charge balance and
965 exchange reactions were solved based on laboratory parameters to yield laboratory pH. In cases
966 where the soil contained calcite, we assumed that calcite could partially buffer pH at the timescale
967 of laboratory measurement. This assumption is supported by a global pH compilation, which
968 shows that pH approximates a calcite-buffered value when carbonates are present in even small

969 amounts (5). To represent carbonate buffering in the lab, we fixed the saturation index for calcite
970 so that it would equal its value in the field and then solved for the equilibrium Ca concentration at
971 the laboratory pCO₂ and temperature.

972

973 Nutrient budgets

974 While our main goal was to model pre-agricultural Ca weathering across the USA, we considered
975 nutrient inputs and outputs in modern croplands to assist with model calibration and to help us
976 understand how Ca fluxes have changed over time. Nitrogen had the most complex nutrient
977 budget. To simplify N accounting, we assumed that all reduced N is completely nitrified
978 following DON export; hence all N is treated as NO₃⁻ (18). In natural systems, the only N inputs
979 in the model were atmospheric deposition and nitrogen fixation (F_N, mol m⁻² y⁻¹), which we
980 modeled as a function of NPP (19):

981

$$982 F_N = 1.8 * (1 - \exp(-0.003 * NPP)) / 14.01 \quad (\text{Equation 16})$$

983 In addition to leaching of NO₃⁻, we considered leaching of organic N, which we assume happens
984 before nitrification. We assigned a molar CN ratio of 20, which is typical for dissolved organic
985 matter (20), and modeled DON export as a function of DOC leaching:

986

$$987 L_N = N * R_C * F_{mob} / (V_{fc} - V_{wp}) + DOC / CN_{DOM} * R_C * F_{mob} / (V_{fc} - V_{wp}) \quad (\text{Equation 17})$$

988 Because we fixed the CN ratio for DOM, DON export could exceed inputs, leading to negative
989 NO₃⁻ concentrations. In these cases, we forced DON export to equal inputs and NO₃⁻
990 concentrations equaled zero.

991 In croplands, we considered N inputs from fertilizer, manure, crop N fixation, free living N
992 fixation, and N removal in crop biomass:

993

$$994 C_N = N_{fert} + N_{man} + N_{fix,crop} + N_{fix,free} - N_{rem} \quad (\text{Equation 18})$$

995 The first three of these parameters as well as the N removal rate varied spatially and were taken
996 from a published county-level compilation (21) whereas free-living N fixation rates were
997 approximated at 0.036 mol m⁻² y⁻¹ (22) and did not vary spatially. The parameter N_{man} was set
998 equal to 20% of total manure N to account for inefficiency in manure recovery (23).

999 Nitrogen can be lost from soil via ammonia volatilization, NO_x emission, and denitrification to
1000 N₂O or N₂. The processes governing these fluxes are complex and representing them in detail was
1001 beyond the scope of our effort. Instead, we manually calibrated a single parameter, r_v, that
1002 controlled the N volatilization rate:

1003

$$1004 V_N = N / N_{inputs} * r_v \quad (\text{Equation 19})$$

1005 The expression was based on the assumption that N volatilization is proportional to the total
1006 available N pool but inversely proportional to N inputs. We reasoned that as N inputs increase,
1007 the opportunity for denitrification and ammonia volatilization would be lower because more N
1008 would escape the soil before volatilization. This is consistent with the observation that low-input
1009 ecosystems volatilize a greater fraction of N than high-input agricultural systems (24). We
1010 selected a value of 0.3 y⁻¹ for r_v, which ensured plausible nitrate stocks for the top 1 meter of soil:
1011 in the range of 100-200 kg NO₃⁻-N ha⁻¹ in croplands (25, 26) and less than 10 kg NO₃⁻-N ha⁻¹ in
1012 forests (27).

1019
1020 Nitrogen removal in harvest could sometimes exceed N inputs, leading to implausibly low NO_3^-
1021 concentrations. At locations where N surplus in croplands was less than $0.1 \text{ mol m}^{-2} \text{ y}^{-1}$, we
1022 assumed that imbalances in the N budget were being met by an unknown source (e.g.,
1023 decomposition of soil organic matter or higher than 20% manure recoverability). In these cases,
1024 we assigned a minimum value of $0.1 \text{ mol m}^{-2} \text{ y}^{-1}$ for the net nitrogen balance before applying
1025 losses from NO_3^- leaching and volatilization. This minimum value maintained cropland NO_3^-
1026 levels within reported ranges (25, 26).

1027 Cropland C budgets were also adjusted to account for import and export of C in agriculture. We
1028 adjusted NPP in croplands to account for removal of crop biomass, which accounts for 43% of
1029 cropland NPP (28). We also accounted for C introduced with manure. We assumed a molar C:N
1030 ratio of 10 for manure, and used this number to scale manure C based on county-level estimates
1031 for manure N.

1032 We also considered cropland nutrient budgets for some additional nutrients. For simplicity, we
1033 assumed that S and K inputs in fertilizer equaled outputs; hence C_S and C_K were set equal to zero.
1034 For Ca and Mg, we accounted for inputs in manure and ag-lime and outputs in crop harvest.
1035 Manure inputs were constrained by assigning Ca:N and Mg:N values for manure and scaling Ca
1036 and Mg inputs to the manure N application rate. Ca:N and Mg:N for manure were averaged across
1037 dairy solids, swine solids, and poultry manure types (29). Similarly, average Ca:N and Mg:N
1038 values were assigned for crop biomass using published values for corn and soy (30), allowing us
1039 to approximate Ca and Mg removal in harvest.

1040 We modeled liming rates endogenously as a function of pH. We first aligned county level liming
1041 data from 1987 (31) (the most recent available date) with maps of soil pH derived from NATSGO
1042 (32). We assigned a pH value to croplands in each county by extracting NATSGO pH values in a
1043 10 km grid across the USA and masking out non-cropland areas using the GFSAD cropland mask
1044 (33). We then calculated the median cropland pH value in each county. This revealed that liming
1045 rates vary widely below pH 7, but are low above pH 7. We modeled the maximum rate of lime
1046 addition as a function of pH using a sigmoid function:

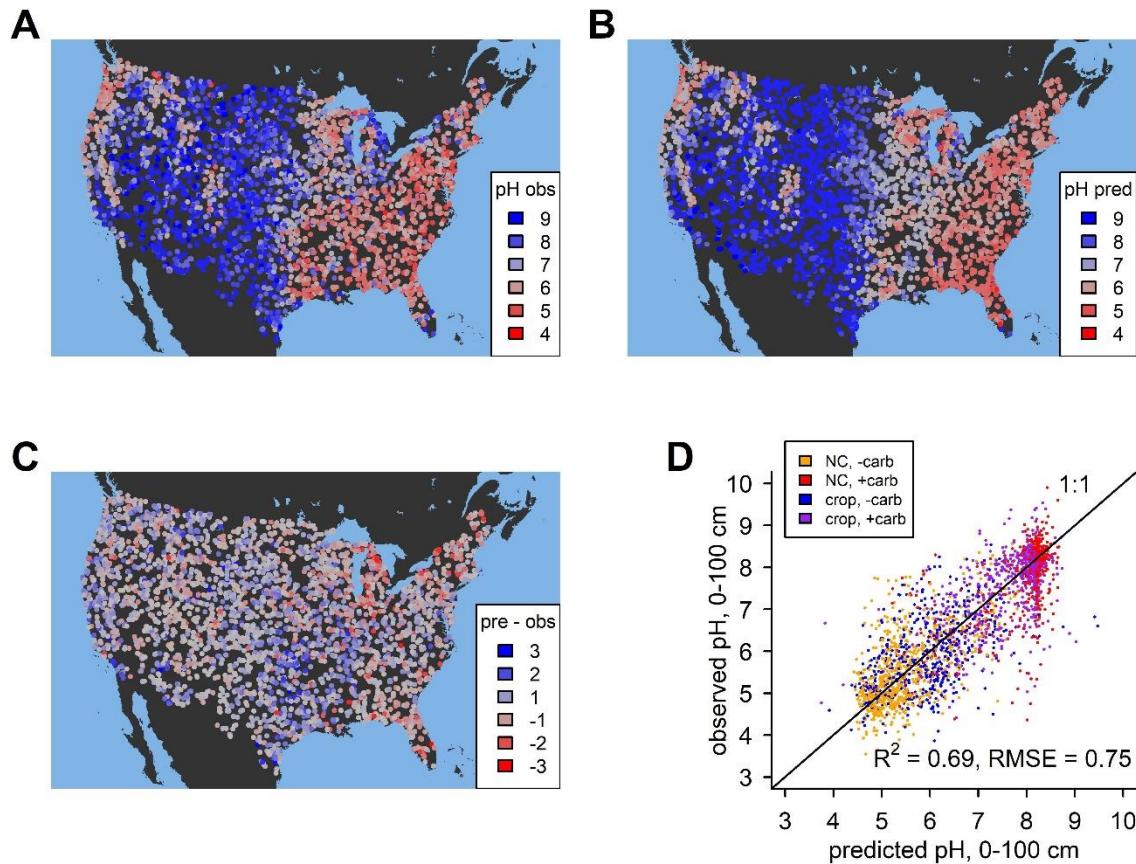
1047
1048
1049
1050
1051 $\text{Lime}_{\text{max}} = p_1 * (1 - \exp(-10^{-pH_{\text{lab}}}/p_2))^{p_3}$ (Equation 20)

1052 Where Lime_{max} was the maximum observed liming rate ($\text{t ha}^{-1} \text{ y}^{-1}$) p_1 , p_2 , and p_3 were empirical
1053 constants and pH_{lab} was the laboratory-measured soil pH assumed equal to the median pH from
1054 NATSGO. We fit this function to the condition 90th percentiles of the data obtained in 0.5 pH-unit
1055 bins using the R function “nls”. The parameters received estimated values of $p_1 = 0.424$, $p_2 =$
1056 $1.42 * 10^{-7}$, and $p_3 = 1.13$.

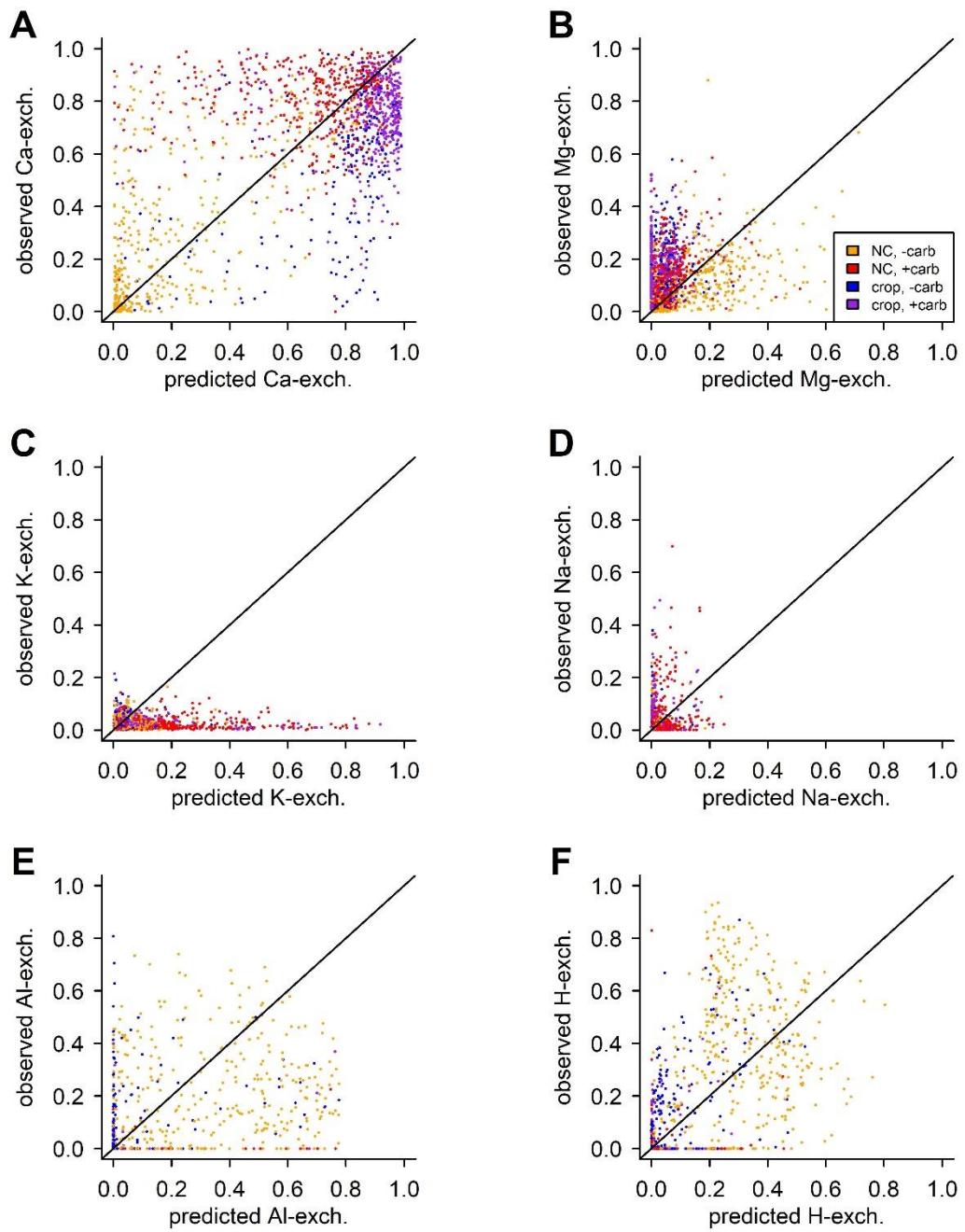
1057 Below the maximum liming rate, we assumed that farmers add enough lime to neutralize acidity
1058 from fertilizer and replace Ca and Mg lost in crop biomass. Consequently, the main effect of
1059 liming in the model was to maintain soil pH at the same level it would have attained under
1060 unfarmed conditions. We made this assumption because it was a reasonable compromise between
1061 two extreme alternatives: [1] assuming that farmers generally add lime aggressively to raise their
1062 soil pH to agronomically optimal levels; or [2] farmers generally do not add enough lime to
1063 maintain soil pH, and croplands are broadly acidified compared to unfarmed baseline conditions.
1064 To estimate the liming rate, we first ran the model without agricultural influence, which yielded
1065 the target pH value, pH_{target} . We then modeled lime addition as a function of pH_{lab} that increases
1066 steeply towards Lime_{max} at pH_{target} .

1069
1070 $Lime_{tot} = Lime_{max} * (1 - \exp(-10^{-pH_{lab}}/10^{-pH_{target}})^{20})$ (Equation 21)
1071

1072 Applying this equation required approximating pH_{lab} because the model was designed to calculate
1073 the in-situ field pH, while laboratory pH was estimated as a post-processing step at some
1074 computational cost. To address this, we derived empirical linear relationships between the in-situ
1075 pH and the laboratory pH prior to running cropland simulations, with a separate relationship fitted
1076 for carbonate-buffered and carbonate free soils. These regressions explained >90% of the
1077 variation in pH_{lab} and could be used to solve Equation 21 without explicitly estimating this
1078 quantity at every model iteration, speeding up computations substantially. After applying
1079 Equation 21, we partitioned lime added into calcitic and dolomitic components. In general, crop
1080 Mg removal exceeded inputs, and so we satisfied Mg demand first. Mg demand ($\text{mol m}^{-2} \text{ y}^{-1}$) was
1081 set equal to the cropland partial Mg budget (crop removal – manure inputs) where removal
1082 exceeded inputs and set to zero elsewhere. Dolomitic lime addition ($\text{mol m}^{-2} \text{ y}^{-1}$) was then set to
1083 equal to Mg demand. Where Mg demand could not be met because the mass of dolomite added
1084 exceeded $Lime_{max}$, the cropland Mg budget was set equal to zero and it was assumed the Mg came
1085 from other unknown sources. Calcitic lime addition was calculated as the difference between the
1086 mass of dolomite added and $Lime_{tot}$. Ca and Mg added in lime were obtained from dolomitic and
1087 calcitic lime based on the chemical formulae for calcite and dolomite (Table S6).
1088

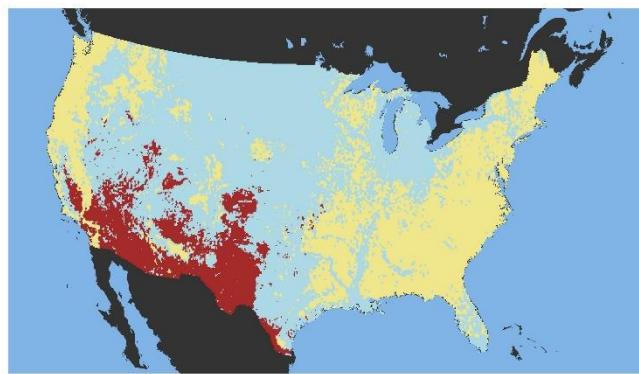


1091 **Fig. S1. Model performance matching soil pH.** (A) shows observed depth-weighted average
1092 soil pH of the top 100 cm at 4,247 unique locations used for model training and validation. (B)
1093 shows pH simulated by the calibrated model at the same locations, and (C) shows the model
1094 residuals (predicted – observed pH). (D) shows a plot of predicted versus observed pH, with
1095 colors representing different combinations of land use and soil carbonate status (NC, -carb = non-
1096 cropland, carbonate free; NC, +carb = non-cropland, carbonates present; crop, -carb = cropland,
1097 carbonates free; crop, +carb = cropland, carbonates present). RMSE is the root mean squared error.



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1099 **Fig. S2. Model performance for exchangeable ions.** (A) – (F) show predicted versus observed
1100 exchange fractions for Ca, Mg, K, Na, Al, and H⁺. Observed values represent depth-weighted
1101 averages to 100 cm taken from the NCSS database(34) (n = 2,563 unique profiles). Values are
1102 normalized by total cation exchange capacity (moles cation charge / CEC). Colors represent
1103 different combinations of land use and soil carbonate status (NC, -carb = non-cropland, carbonate
1104 free; NC, +carb = non-cropland, carbonates present; crop, -carb = cropland, carbonate free; crop,
1105 +carb = cropland, carbonates present). Diagonal lines show the 1:1 relationship.
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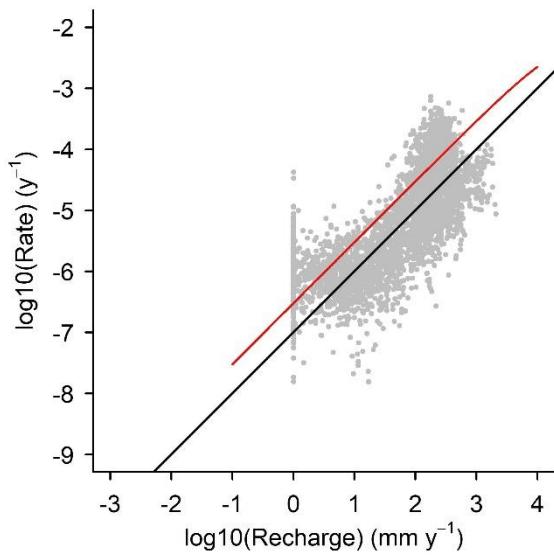
Carbonate Ca source/sink status

■ source ■ absent ■ sink

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1108 **Fig. S3. Modeled carbonate source / sink status.** Data show model simulations under
1109 preindustrial late Holocene conditions. Areas mapped in yellow are carbonate free, areas mapped
1110 in blue are releasing Ca via carbonate weathering, and areas mapped in red are a sink for Ca via
1111 carbonate formation.

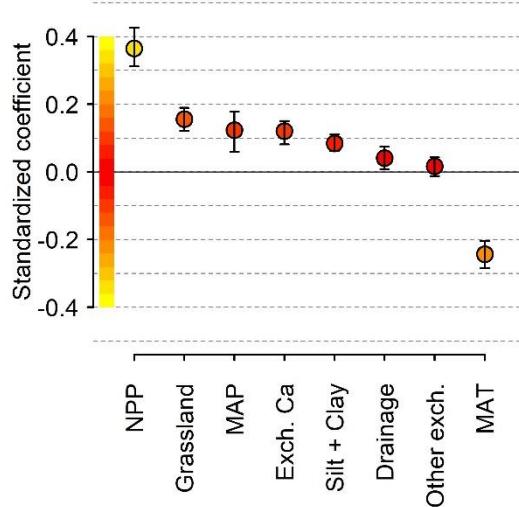
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1115 **Fig. S4. Modeled plagioclase feldspar weathering rate versus recharge.** Gray points show
1116 modeled feldspar weathering rates normalized by the feldspar stock versus the recharge
1117 parameter. The red line shows the non-linear fit to a compilation of field and lab weathering rates
1118 from Maher 2010 (3), and the black line shows a fit to the same complication from Yu and Hunt
1119 2018 (4).
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1122 **Fig. S5. Controls on A-horizon soil organic carbon stocks in the USA, with corrected CEC.**
 1123 Standardized regression coefficients were derived from a multivariate linear regression model,
 1124 where A-horizon organic carbon stocks were predicted as a function of the eight variables listed
 1125 on the horizontal axis. In this case, cation exchange capacity (CEC) was corrected for the
 1126 contribution from soil organic matter prior to calculating exchangeable ion pools. In both panels,
 1127 whiskers show 95% confidence intervals derived from a spatial blocked bootstrapping procedure
 1128 (see Methods). The absolute value of each regression coefficient is an index of how strongly
 1129 related each variable is to the response variable, and is shown with a relative color scale: yellow =
 1130 maximum, red = zero. Abbreviations: NPP = net primary productivity, MAT = mean annual
 1131 temperature, MAP = mean annual precipitation, Exch. Ca = total exchangeable Ca, Other exch. =
 1132 sum of non-Ca exchangeable ions.

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| | R ² | RMSE |
|------------------|----------------|------|
| Ca ²⁺ | 0.39 | 0.27 |
| Mg ²⁺ | 0.03 | 0.15 |
| Na ⁺ | 0.06 | 0.06 |
| K ⁺ | 0 | 0.16 |
| Al ³⁺ | 0.27 | 0.17 |
| H ⁺ | 0.45 | 0.16 |
| All | 0.64 | 0.17 |

1136 **Table S1. Validation statistics for exchangeable ions.** R² values are derived by regressing
 1137 observations on predictions; root mean squared error (RMSE) was calculated as the square root of
 1138 the mean of the squared residuals (geochemical model predictions – observations). Statistics for
 1139 all cations were obtained by treating all observed and predicted cation fractions as independent
 1140 values and pooling them. Observed values represent depth-weighted averages to 100 cm taken
 1141 from the NCSS database (34) (n = 2,563 unique profiles; 3,423 total including repeats from
 1142 spatially weighted resampling). Values are normalized by total cation exchange capacity (moles
 1143 cation charge / CEC).

| | value | CI |
|-------------|--------|------------------|
| intercept | -2.342 | [-2.644, -2.082] |
| grassland | 1.45 | [1.205, 1.695] |
| base sat. | 2.887 | [2.433, 3.544] |
| silt + clay | -1.333 | [-1.706, -1.004] |
| NPP | 0.202 | [-0.048, 0.451] |
| Drainage | 0.724 | [0.470, 1.039] |
| MAT | 0.644 | [0.253, 0.994] |
| MAP | -0.638 | [-1.102, -0.162] |

1147 **Table S2. Results of logistic regression analysis for Mollisol extent.** Statistics are derived from
 1148 a multivariate logistic regression, where the presence or absence of Mollisols was modeled as a
 1149 function of potential grassland and savanna vegetation (grassland), base saturation (base sat.), soil
 1150 silt + clay content, net primary productivity (NPP), USDA drainage class (drainage), Mean annual
 1151 temperature (MAT), and mean annual precipitation (MAP). Continuous predictors were scaled by
 1152 their standard deviations prior to fitting, whereas the binary predictor (grassland) was scaled by
 1153 two times its standard deviation. Model null deviance = 136,055; Residual deviance = 97075. At
 1154 a probability threshold of 0.4 the accuracy rate was 0.79; sensitivity was 0.61; and specificity was
 1155 0.86. Confidence intervals were derived from a spatially blocked bootstrapping procedure (see
 1156 Methods).

| | value | CI |
|-------------|--------|------------------|
| intercept | -0.051 | [-0.067, -0.036] |
| NPP | 0.143 | [0.106, 0.172] |
| MAP | 0.152 | [0.120, 0.185] |
| exch. Ca | 0.013 | [-0.014, 0.039] |
| grassland | -0.233 | [-0.270, -0.188] |
| silt + clay | 0.029 | [-0.005, 0.062] |
| Drainage | 0.079 | [0.057, 0.103] |
| other exch. | 0.362 | [0.304, 0.421] |
| MAT | 0.13 | [0.069, 0.179] |

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1159 **Table S3. Results of multiple regression analysis for A-horizon SOC.** Statistics are derived
 1160 from a multivariate logistic regression, where log-transformed A-horizon organic carbon stocks
 1161 were modeled as a function of potential grassland and savanna vegetation (grassland),
 1162 exchangeable Ca (Ca exch.), non-Ca exchangeable ions (other exch.), soil silt + clay content, net
 1163 primary productivity (NPP), USDA drainage class (drainage), Mean annual temperature (MAT),
 1164 and mean annual precipitation (MAP). Continuous predictors were scaled by their standard
 1165 deviations prior to fitting, whereas the binary predictor (grassland) was scaled by two times its
 1166 standard deviation. Model $R^2 = 0.30$ and residual standard error was 0.4189. Confidence intervals
 1167 were derived from a spatially blocked bootstrapping procedure (see Methods).

| Ion or algebraic constraint | Equation |
|-----------------------------|--|
| Ca^{2+} | $d\text{Ca}/dt = D_{\text{Ca}} + A_{\text{Ca}} + C_{\text{Ca}} + R_{\text{Cc,Ca}} + R_{\text{Do,Ca}} + R_{\text{Pl,Ca}} + R_{\text{Hb,Ca}} + R_{\text{Py,Ca}} - L_{\text{Ca}}$ |
| Mg^{2+} | $d\text{Mg}/dt = D_{\text{Mg}} + A_{\text{Mg}} + C_{\text{Mg}} + R_{\text{Do,Mg}} + R_{\text{Hb,Mg}} + R_{\text{Py,Mg}} + R_{\text{Cl,Mg}} - L_{\text{Mg}}$ |
| Na^+ | $d\text{Na}/dt = D_{\text{Na}} + R_{\text{Pl,Na}} - L_{\text{Na}}$ |
| K^+ | $d\text{K}/dt = D_{\text{K}} + C_{\text{K}} + M_{\text{K}} + R_{\text{Ks,K}} + R_{\text{Il,K}} - U_{\text{K}} - L_{\text{K}}$ |
| NO_3^- | $d\text{N}/dt = D_{\text{N}} + C_{\text{N}} + F_{\text{N}} - V_{\text{N}} - L_{\text{N}}$ |
| SO_4^{2-} | $d\text{S}/dt = D_{\text{S}} + C_{\text{S}} - L_{\text{S}}$ |
| Cl^- | $d\text{Cl}/dt = D_{\text{Cl}} - L_{\text{Cl}}$ |
| Charge Balance | $0 = (2[\text{Ca}^{2+}] + 2[\text{Mg}^{2+}] + [\text{K}^+] + [\text{Na}^+] + 3[\text{Al}^{3+}] + 2[\text{Al}(\text{OH})^{2+}] + [\text{Al}(\text{OH})_2^+] + 2[\text{AlH}^{2+}] + [\text{AlH}_2^{+}] + [\text{H}^+]) - ([\text{OH}^-] + [\text{HCO}_3^-] + 2[\text{CO}_3^{2-}] + [\text{H}_2\text{Org}^-] + 2[\text{H}^{+}] + 2[\text{Org}^{3-}] + 3[\text{Org}^{2-}] + [\text{Al}(\text{OH})_4^-] + 2[\text{SO}_4^{2-}] + [\text{NO}_3^-] + [\text{Cl}^-])$ |
| Exchange | $1 = f\text{Ca} + f\text{Mg} + f\text{Na} + f\text{K} + f\text{Al} + f\text{H}$ |

Table S4 Governing equations. Capital letters indicate rates: D = deposition (wet + dry); A = agricultural liming, C = cropland nutrient budget (inputs – uptake); R = weathering; L = leaching; F = fixation; V = volatilization. Weathering rates ($\text{mol mineral y}^{-1}$) were multiplied by the molar concentration of each element the mineral to yield the flux of each element from the mineral; this is indicated in the subscripts, with the mineral listed first and then the corresponding element. Minerals: Cc = calcite; Do = dolomite; Pl = plagioclase; Hb = hornblende; Py = pyroxene; Cl = chlorite; Ks = K-feldspar; Il = illite.

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| Parameter | Description | Value | Units | Source |
|-----------------------------------|---|-----------|------------------------------------|------------|
| Ea_{sil} | Silicate weathering activation energy | 74 | $\text{kJ mol}^{-1} \text{K}^{-1}$ | (2) |
| H_r | Reference $[\text{H}^+]$ value | 10^{-5} | mol l^{-1} | This study |
| nH | Silicate weathering reaction order for H^+ | 0.6667 | - | This study |
| RRP_{Pl} | Relative reaction rate, plagioclase | 1 | - | (1) |
| RRK_{K} | Relative reaction rate, K-feldspar | 0.63 | - | (1) |
| RRH_{Hb} | Relative reaction rate, hornblende | 0.25 | - | (1) |
| RRP_{Py} | Relative reaction rate, pyroxene | 1 | - | This study |
| $\log(A_{\text{acid,cc}})$ | Acid mechanism preexponential factor, calcite | -0.3 | $\text{mol m}^{-2} \text{s}^{-1}$ | (6) |
| $\log(A_{\text{neut,cc}})$ | Neutral mechanism preexponential factor, calcite | -5.81 | $\text{mol m}^{-2} \text{s}^{-1}$ | (6) |
| $\log(A_{\text{CO}_2,\text{cc}})$ | CO_2 mechanism preexponential factor, calcite | -3.48 | $\text{mol m}^{-2} \text{s}^{-1}$ | (6) |
| $\log(A_{\text{acid,do}})$ | Acid mechanism preexponential factor, dolomite | -3.19 | $\text{mol m}^{-2} \text{s}^{-1}$ | (6) |
| $\log(A_{\text{neut,do}})$ | Neutral mechanism preexponential factor, dolomite | -7.53 | $\text{mol m}^{-2} \text{s}^{-1}$ | (6) |
| $\log(A_{\text{CO}_2,\text{do}})$ | CO_2 mechanism preexponential factor, dolomite | -5.11 | $\text{mol m}^{-2} \text{s}^{-1}$ | (6) |
| $Ea_{\text{acid,cc}}$ | Acid mechanism activation energy, calcite | 14.4 | $\text{kJ mol}^{-1} \text{K}^{-1}$ | (6) |
| $Ea_{\text{neut,cc}}$ | Neutral mechanism activation energy, calcite | 23.5 | $\text{kJ mol}^{-1} \text{K}^{-1}$ | (6) |
| $Ea_{\text{CO}_2,\text{cc}}$ | CO_2 mechanism activation energy, calcite | 35.4 | $\text{kJ mol}^{-1} \text{K}^{-1}$ | (6) |
| $Ea_{\text{acid,do}}$ | Acid mechanism activation energy, dolomite | 36.1 | $\text{kJ mol}^{-1} \text{K}^{-1}$ | (6) |
| $Ea_{\text{neut,do}}$ | Neutral mechanism activation energy, dolomite | 52.2 | $\text{kJ mol}^{-1} \text{K}^{-1}$ | (6) |
| $Ea_{\text{CO}_2,\text{do}}$ | CO_2 mechanism activation energy, dolomite | 34.8 | $\text{kJ mol}^{-1} \text{K}^{-1}$ | (6) |
| nH_{cc} | Reaction order for H^+ , calcite | 1 | - | (6) |
| $nCO_{2,\text{cc}}$ | Reaction order for CO_2 , calcite | 1 | - | (6) |
| nH_{do} | Reaction order for H^+ , dolomite | 0.5 | - | (6) |
| $nCO_{2,\text{do}}$ | Reaction order for CO_2 , dolomite | 0.5 | - | (6) |

1176 **Table S5 Weathering rate parameters**

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| Mineral | Abbr. | Type | Formula | Density |
|-------------|-------|----------------|--|--|
| Plagioclase | Pl | tectosilicate | $\text{Na}_{(1-f_{\text{An}})}\text{Ca}_{f_{\text{An}}}\text{Al}_{(1+f_{\text{An}})}\text{Si}_{(3-f_{\text{An}})}\text{O}_8$ | $2.75f_{\text{An}} + 2.625(1-f_{\text{An}})$ |
| K-feldspar | Ks | tectosilicate | KAlSi_3O_8 | 2.59 |
| Pyroxene | Py | inosilicate | $\text{MgCa}(\text{SiO}_3)_2$ | 3.3 |
| Hornblende | Hb | inosilicate | $\text{Ca}_2(\text{Mg}_2\text{Fe}_2\text{Al})\text{Si}_7\text{AlO}_{22}(\text{OH})_2$ | 3.1735 |
| Chlorite | Cl | phyllosilicate | $\text{Mg}_5\text{Al}_2\text{Si}_3\text{O}_{18}\text{H}_8$ | 2.915 |
| Illite | Il | phyllosilicate | $\text{K}(\text{Al}_2)(\text{Si}_3\text{Al})\text{O}_{10}(\text{OH})_2$ | 2.795 |
| Calcite | Cc | carbonate | CaCO_3 | 2.7102 |
| Dolomite | Do | carbonate | $\text{CaMg}(\text{CO}_3)_2$ | 2.85 |

Table S6 Mineral properties. f_{An} = anorthite molar fraction. Densities are midpoints of reported ranges from Mindat.org.

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| Reaction | $\Delta S \text{ (kJ K}^{-1} \text{ mol}^{-1}\text{)}$ | $\Delta H \text{ (kJ mol}^{-1}\text{)}$ | logK | source |
|---|--|---|--|--------|
| $\text{CO}_2 \text{ (g)} \leftrightarrow \text{CO}_2 \text{ (aq)}$ | -0.09616924 | -20.28821600 | | (8, 9) |
| $\text{CO}_2 \text{ (aq)} + \text{H}_2\text{O} \leftrightarrow \text{HCO}_3^- + \text{H}^+$ | -0.08904506 | 9.70167230 | | (8, 9) |
| $\text{HCO}_3^- \leftrightarrow \text{CO}_3^{2-} + \text{H}^+$ | -0.14844832 | 14.69839200 | | (8, 9) |
| $\text{H}_2\text{O} \leftrightarrow \text{OH}^- + \text{H}^+$ | -0.08063522 | 55.81353630 | | (8, 9) |
| $\text{Al(OH)}_3 \text{ (s)} \leftrightarrow \text{Al(OH)}_3 \text{ (aq)}$ | -0.00908996 | 50.45803923 | | (8, 9) |
| $\text{Al(OH)}_3 \text{ (aq)} + 3\text{H}^+ \leftrightarrow \text{Al}^{3+} + 3\text{H}_2\text{O}$ | -0.18933085 | -153.61153602 | | (8, 9) |
| $\text{Al(OH)}_3 \text{ (aq)} + 2\text{H}^+ \leftrightarrow \text{Al(OH)}_2^+ + 2\text{H}_2\text{O}$ | -0.10062704 | -98.86893231 | | (8, 9) |
| $\text{Al(OH)}_3 \text{ (aq)} + 1\text{H}^+ \leftrightarrow \text{Al(OH)}^{2+} + \text{H}_2\text{O}$ | -0.01697332 | -39.97106033 | | (8, 9) |
| $\text{Al(OH)}_3 \text{ (aq)} + \text{H}_2\text{O} \leftrightarrow \text{Al(OH)}_4^- + \text{H}^+$ | -0.02572859 | 25.43199965 | | (8, 9) |
| $\text{CaCO}_3 \text{ (s)} \leftrightarrow \text{Ca}^{2+} + \text{CO}_3^{2-}$ | -0.19820780 | -11.49904000 | | (8, 9) |
| $\text{CaMgC}_2\text{O}_6 \text{ (s)} \leftrightarrow \text{Ca}^{2+} + \text{Mg}^{2+} + 2\text{CO}_3^{2-}$ | -0.44944386 | -34.26448628 | | (8, 9) |
| $\text{Mg}_5\text{Al}_2\text{Si}_3\text{O}_{18}\text{H}_8 \text{ (s)} + 10\text{H}^+ \leftrightarrow 2\text{Al(OH)}_3 \text{ (aq)} + 5\text{Mg}^{2+} + 3\text{H}_4\text{SiO}_4 \text{ (aq)}$ | -0.08814278 | -56.42611 | | (8, 9) |
| $\text{KAl}_3\text{Si}_3\text{O}_{12}\text{H}_2 \text{ (s)} + \text{H}^+ + 9\text{H}_2\text{O} \leftrightarrow 3\text{Al(OH)}_3 \text{ (aq)} + \text{K}^+ + 3\text{H}_4\text{SiO}_4 \text{ (aq)}$ | -0.0772809 | 199.2072 | | (8, 9) |
| $\text{SiO}_2 \text{ (amorph)} + 2\text{H}_2\text{O} \leftrightarrow \text{H}_4\text{SiO}_4$ | -0.01114692 | 10.56612 | | (8, 9) |
| $\text{H}_3\text{Org} \leftrightarrow \text{H}_2\text{Org}^- + \text{H}^+$ | | | -2.653 | (14) |
| $\text{H}_2\text{Org}^- \leftrightarrow \text{H}\text{Org}^{2-} + \text{H}^+$ | | | -6.233 | (14) |
| $\text{H}\text{Org}^{2-} \leftrightarrow \text{Org}^{3-} + \text{H}^+$ | | | -7.467 | (14) |
| $\text{AlH}_2\text{Org}^{2+} \leftrightarrow \text{H}^+ + \text{AlH}\text{Org}^+$ | | | -4.963 | (14) |
| $\text{AlH}\text{Org}^+ \leftrightarrow \text{H}^+ + \text{AlOrg}$ | | | -4.040 | (14) |
| $\text{AlOrg} \leftrightarrow \text{Al}^{3+} + \text{Org}^{3-}$ | | | -10.020 | (14) |
| $3\text{Ca-X} + 2\text{Al}^{3+} \leftrightarrow 2\text{Al-X} + 3\text{Ca}^{2+}$ | | | 2.026 (s); 1.195 (lo); 0.106 (cl) | (16) |
| $3\text{Mg-X} + 2\text{Al}^{3+} \leftrightarrow 2\text{Al-X} + 3\text{Mg}^{2+}$ | | | 2.811 (s); 1.244 (lo); 0.599 (cl) | (16) |
| $3\text{Na-X} + \text{Al}^{3+} \leftrightarrow \text{Al-X} + 3\text{Na}^+$ | | | 1.811 (s); 0.646 (lo); 1.045 (cl) | (16) |
| $3\text{K-X} + \text{Al}^{3+} \leftrightarrow \text{Al-X} + 3\text{K}^+$ | | | -0.917 (s); -2.413 (lo); -3.561 (cl) | (16) |
| $3\text{H-X} + \text{Al}^{3+} \leftrightarrow \text{Al-X} + 3\text{H}^+$ | | | -6.924 (s); -7.532 (lo); -9.923 (cl) | (16) |

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Table S7 Equilibrium reactions and thermodynamic parameters. For exchange reactions logK values are for sand, loess, and clay respectively based on (16).

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