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Calcium promotes carbon rich grassland soils

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35 **Abstract**

36 **Dark colored grassland soils, known as Mollisols, are intensively farmed and exceptionally**
37 **rich in organic matter, and hence have an important role in the carbon cycle. Storage of soil**
38 **organic carbon (SOC) in Mollisols may result from interactions between organic matter and**
39 **calcium (Ca) released by carbonate and silicate weathering. This synergy between SOC and**
40 **Ca cycling has yet to be tested at scale. To close this knowledge gap, we developed a novel**
41 **geochemical model and leveraged continental-scale datasets to simulate Ca release in soils**
42 **across the USA. We found that Ca released by mineral weathering is associated with SOC**
43 **storage and that this effect is stronger in Mollisols than in non-Mollisols. Our model also**
44 **shows that agriculture has increased Ca inputs to cultivated USA Mollisols 5-6 fold,**
45 **indicating that humans have fundamentally changed the geochemical conditions that sustain**
46 **SOC in these soils. By implication, moderating the quantity of and timing of Ca release may**
47 **help to preserve and restore SOC in the world’s most intensively farmed landscapes.**

48 **Main**

49 Temperate grasslands feature exceptionally fertile, dark-colored soils known as Mollisols.
50 Mollisols are the world’s most intensively farmed soil type.¹ Based on recent data,^{2,3} we estimate
51 that Mollisols comprise only 7% of the Earth’s land area yet support 24% of agricultural land and
52 32% of all calories from production of corn, soy, and wheat. Mollisols also contribute
53 disproportionately to soil organic carbon (SOC) storage, containing 32% of the organic C held in
54 Earth’s agricultural soils (see Methods). This makes Mollisols critical to land-based climate
55 mitigation efforts. At the same time, Mollisols are disproportionately exposed to environmental
56 threats, including soil erosion,⁴ and have lost a significant fraction of their SOC to cultivation.⁵
57 Effective stewardship of Mollisols in the face of these threats requires a comprehensive
58 understanding of the environmental factors that make them fertile and C rich.

59 There are several ecological processes that contribute to the C richness of Mollisols, and
60 these have implications for protecting and restoring SOC. As early as the 1860's, grassland
61 vegetation was identified as the main driver of Mollisol formation.⁶ Perennial grasses grow
62 extensive fibrous root systems, and root turnover is an important pathway of SOC accrual.^{7,8}
63 Grasslands and savannas are characterized by frequent fires, and fires can generate persistent
64 pyrogenic C that might explain the origin of Mollisols.⁹ Grasslands also support robust populations
65 of burrowing animals that help to engineer to the thick, C-rich topsoil layers characteristic of
66 Mollisols.¹⁰ Contemporary proposals for restoring SOC storage in cropland soils mimic ecological
67 processes that are thought to be important in Mollisols. For instance, C sequestration might be
68 achieved by returning deep rooted cultivars to croplands,¹¹ increasing plant diversity,¹² or
69 amending soils with pyrogenic C.¹³

70 Geologic factors can also help to explain the C richness of Mollisols. Mollisols are
71 commonly formed from calcareous rocks or from aeolian deposits rich in calcium carbonate.⁶
72 Mollisols are, by definition, enriched in exchangeable Ca^{2+} and other base cations (Mg^{2+} , K^+ , and
73 Na^+).¹⁴ A growing body of evidence shows that Ca stabilizes SOC. Ca facilitates sorption of
74 organic molecules on clays and promotes the growth of bacterial biofilms that are retained on
75 mineral surfaces.¹⁵⁻¹⁷ These processes manifest at continental scales, where SOC is spatially
76 correlated with exchangeable Ca^{2+} , i.e., Ca that is reversibly bound to surfaces as an exchangeable
77 cation.^{18,19} Exchangeable Ca^{2+} may directly link organic matter to minerals via cation bridging,
78 and may also be a proxy for more complex mechanisms that protect organic matter, such as
79 stabilization of soil aggregates by Ca^{2+} .¹⁶ Regardless of the mechanism(s), these facts suggest that
80 release of Ca from carbonate and silicate dissolution may link SOC storage to mineral weathering
81 in Mollisols. This effect would be analogous to the link between silicate weathering and SOC

82 mediated by reactive iron and aluminum in other soil types.²⁰ The hypothesis that Ca inputs from
83 weathering enhance SOC in Mollisols is challenging to test because soil Ca availability depends
84 on complex interactions between vegetation, geology, and climate.

85 We addressed the role of Ca in Mollisol SOC storage by developing and applying a novel
86 geochemical model across the conterminous USA. Our modeling approach leveraged soil
87 mineralogy data²¹ that enabled us to represent soil chemical processes at an unprecedented spatial
88 extent. We designed our model to track the inputs and outputs of major cations and anions to the
89 soil solution, simulating soil pH, mineral weathering rates, and associated Ca release and retention.
90 We estimated the effect of Ca availability on SOC statistically while accounting for vegetation,
91 climate and other confounding factors. Next, we used the model to constrain specific Ca sources:
92 carbonate weathering, silicate weathering, and atmospheric deposition. We then quantified the
93 sensitivity of SOC storage to Ca inputs from weathering in Mollisols (Figure 1a) versus non-
94 Mollisol soils. Using this approach, we were able to test the hypothesis that Ca released from
95 carbonate and silicate weathering helps to explain the C richness of Mollisols.

96 **Geochemical model performance**

97 We used our geochemical model to estimate Ca availability in soil across the conterminous USA.
98 We first parametrized the model with input data including climate, atmospheric deposition of major
99 solutes, net primary productivity, agricultural element budgets, and soil mineralogy (see Methods).
100 The model integrated these variables by linking inputs and outputs of solutes, the release of CO₂
101 and organic acids by biota, and mineral weathering via a set of pH-dependent equilibrium
102 reactions. We calibrated two unconstrained parameters related to mineral surface reactivity,
103 training the model to match modern observations of soil pH. The model was able to explain 69%
104 of the spatial variation in depth-averaged soil pH (0-100 cm) across the USA. Performance was

105 more modest when predicting soil exchangeable cations: the model explained 40% of the variation
106 in the soil exchangeable Ca^{2+} fraction and 66% of the variation across all exchangeable cations
107 when applied to validation data (Figure S1, Figure S2, Table S1). Notably, these validation results
108 were depth-averaged to 100 cm because our model treated the uppermost 100 cm of soil as
109 chemically and mineralogically homogenous. A vertically resolved, multi-phase reactive transport
110 model would better capture gradients in soil pH, weathering rates, and exchangeable ions, but at
111 the cost of added complexity and uncertain parameters (e.g., rates of biological nutrient uplift). We
112 expect that the geographic patterns captured by our simplified geochemical model would likely be
113 qualitatively similar if vertical resolution was added because these patterns are driven by
114 continental-scale gradients in soil soil pH, which are stronger than vertical gradients.²²

115 **Relating Ca to SOC stocks**

116 After calibrating the geochemical model, we developed a statistical approach to link soil Ca with
117 SOC stocks. Mollisols are characterized by thick, C-rich A-horizons;¹⁴ hence we used total A-
118 horizon SOC—incorporating both topsoil thickness and C content—as an index that captures the
119 primary mode of C storage in Mollisols. We obtained SOC stock data from two databases: the US
120 Department of Agriculture Rapid Carbon Assessment and the National Cooperative Soil Survey
121 archives^{23,24} (Figure 1b). We then quantified the relationship between A-horizon SOC stocks and
122 modeled soil exchangeable Ca^{2+} across the conterminous USA using multiple linear regression.
123 We included eight potentially confounding factors in the regression: (1) the pre-agricultural
124 grassland and savanna distribution, which we approximated with a potential vegetation map
125 derived from remotely sensed patches of relict vegetation;²⁵ (2) mean annual soil temperature; (3)
126 mean annual precipitation; (4) soil silt and clay content (5) soil drainage class; (6) soil pH derived
127 from the geochemical model; (7) net primary productivity, and (8) the sum of non- Ca^{2+}

128 exchangeable cations derived from the geochemical model (Mg^{2+} , K^+ , Na^+ , Al^{3+} , and H^+). We also
129 experimented with including interaction terms between vegetation and geochemical parameters,
130 but these were not statistically significant at a threshold of $p=0.05$, and so we did not include them.
131 The regression model explained 30% of the variation in A-horizon SOC stocks. Comparison of the
132 scaled regression coefficients revealed that net primary productivity and soil temperature were the
133 most important predictors of A-horizon SOC storage, followed by exchangeable Ca^{2+} , the presence
134 of grasslands or savannas, and then other factors (Figure 2; Table S3). These results indicate that
135 modeled exchangeable Ca^{2+} is positively correlated with A-horizon SOC storage. The combined
136 effect of other exchangeable ions on SOC across the USA—including the effect of Al^{3+} and H^+ in
137 acid soils—was weak. This implies that Ca, rather than total cation exchange capacity, drives this
138 correlation.

139 Notably, the association between modeled soil Ca availability and SOC is subject to several
140 sources of uncertainty. The geochemical model was relatively skilled at matching spatial patterns
141 in soil pH, yet the majority of the variation in the soil exchangeable Ca^{2+} fraction remained
142 unexplained and the relative abundances of individual non- Ca^{2+} base cations Mg^{2+} , K^+ , and Na^+
143 could not be predicted with confidence (Figure S2, Table S1). These uncertainties likely reduced
144 effect sizes for both Ca^{2+} and non- Ca^{2+} base cations in the regression analysis due to statistical
145 attenuation bias. In addition to this limitation, the majority (70%) of the variation in A-horizon
146 SOC stocks remained unexplained by our regression, meaning that unobserved confounding
147 factors could affect our results. Keeping these caveats in mind, our modeled results successfully
148 recover the positive relationship between measured exchangeable Ca^{2+} and SOC that emerges in
149 purely observational studies.^{18,19} This suggests that simulated exchangeable Ca^{2+} , while highly

150 approximate, was an effective index for soil available Ca and its potential to facilitate organo-
151 mineral association.

152 While our model-driven estimates of Ca^{2+} are uncertain, they enable us to test specific
153 causal hypotheses that are not accessible using direct observations. For instance, statistical
154 correlations between metal ions and SOC concentrations may emerge simply because organic
155 matter provides more sorption sites for metals.²⁶ We were able to control for this effect by
156 correcting for the contribution of soil organic matter to cation exchange capacity, and found that
157 the positive association between simulated exchangeable Ca^{2+} and SOC is robust (Figure S3).
158 More importantly, our modeling approach allowed us to consider how the ultimate drivers of Ca
159 availability might affect SOC storage. Specifically, we were able to estimate indirect effects of
160 carbonate and silicate weathering on SOC storage mediated by soil Ca availability.

161 **Linking Ca sources to SOC storage**

162 We evaluated the long-term effect of silicate and carbonate weathering on A-horizon SOC stocks
163 by constructing counterfactual scenarios in which natural Ca sources were suppressed under
164 preindustrial conditions. We focused on pre-industrial conditions to isolate the effects of geologic
165 sources of Ca over the centennial timescales that govern SOC accrual. To represent preindustrial
166 conditions, we re-parametrized the model to reflect atmospheric deposition in 1850²⁷ (see
167 Methods), eliminated agricultural processes, and ran simulations under preindustrial carbon
168 dioxide levels. We then performed the following steps: (1) we set carbonate weathering, all silicate
169 weathering, or atmospheric Ca deposition to zero in the geochemical model, (2) we used updated
170 outputs from the geochemical model to generate predictions using the previously fitted regression,
171 and (3) we quantified changes in the predicted A-horizon SOC stocks. For reference, we also
172 created a counterfactual scenario in which all vegetation was assumed to be non-grassland.

173 Our model experiment revealed that both carbonate and silicate weathering help to explain
174 A-horizon SOC stocks across the USA. Across the Mollisol regions of the conterminous USA,
175 predicted preindustrial A-horizon SOC storage was 6.5% (0.5 Pg C) lower when carbonate
176 weathering was eliminated, 2.4% (0.2 Pg C) lower when silicate weathering was eliminated, and
177 16% (1.2 Pg C) lower when both were eliminated together. The effect of eliminating all weathering
178 was similar to the effect of eliminating grassland vegetation, which reduced A-horizon SOC
179 storage by 19% (1.5 Pg C) (Figure 3b). We obtained the same statistics for non-Mollisol soils and
180 computed the difference in the sensitivity of Mollisol and non-Mollisols regions, i.e., the effect of
181 eliminating each factor on Mollisols minus the effect on non-Mollisols. He found that A-horizon
182 SOC stocks in Mollisols were particularly sensitive to Ca inputs from carbonate weathering and
183 the combined action of carbonates and silicates (Figure 3b). Eliminating grassland vegetation also
184 had a substantially larger effect on SOC in Mollisols (Figure 3b, gray square). These results suggest
185 that the C richness of Mollisols is related to vegetation and are also consistent with our hypothesis
186 that Ca inputs from mineral weathering augment SOC in Mollisols.

187 Interestingly, eliminating carbonate weathering had a modest effect on A-horizon SOC
188 storage when considered alone, but a more substantial effect when silicate weathering was also
189 eliminated. Similarly, eliminating Ca inputs from silicate weathering had no clear effect on A-
190 horizon SOC storage on its own, but a substantial effect when both mineral sources were
191 eliminated. This result emerged from the geochemical model because carbonate weathering and
192 silicate weathering suppressed each other via their alkalizing effect on soil pH; hence eliminating
193 one Ca source in the model yielded a compensatory increase in Ca release from the other.
194 Suppression of silicate weathering by carbonate weathering has been observed in the field across
195 soil chronosequences²⁸⁻³⁰ and in weathering mesocosms,³¹ which suggests that this model behavior

196 captures a real geochemical dynamic. When either silicates or carbonates are sufficiently abundant,
197 soil Ca availability is high and Ca^{2+} generally predominates over other exchangeable ions. These
198 conditions appear to favor Mollisol formation and SOC accrual across a range of geologic settings.

199 Our model suggests that the elevated Ca inputs associated with Mollisols in the
200 midcontinental USA are derived from specific geologic sources, particularly carbonate minerals
201 (Figure 3b). Glacial deposition explains elevated carbonate weathering in the north-central USA,
202 where lobes of the Laurentide ice sheet ground up and distributed underlying limestone and
203 dolomite rocks during the last ice age.³² Farther south, soil carbonates are abundant in the aeolian
204 Bignell Loess deposits³³ and in the predominately limestone rocks of the Edwards Plateau,³⁴ both
205 of which support Mollisols. Carbonate minerals are also abundant in the arid Western USA;
206 however, our geochemical model predicts that carbonates are either a minor source or a Ca sink in
207 this region (Figure S3). While some of the carbonates in these soils may be derived from
208 sedimentary rocks, desert carbonates are often primarily derived from in-situ precipitation of
209 CaCO_3 from aeolian Ca.³⁵ Our model suggests that some of these carbonates may be slowly
210 weathering under late-Holocene conditions, supplying Ca to overlying Mollisols.

211 Our model also predicts that inputs of Ca from deposition are significant in much of the
212 USA (Figure 3c); however, we found that atmospheric deposition of Ca is a minor control on A-
213 horizon SOC storage (Figure 3a). We assumed that preindustrial Ca deposition was five-fold lower
214 in North America than at present based on paleo dust records.³⁶ Dust fluxes in the midcontinental
215 USA were substantially higher in the late Pleistocene than in recent preindustrial times due to
216 glaciation.³⁷ Ca in modern soil carbonates is often inherited from Pleistocene dust,³⁸ and
217 carbonates continue to weather in Pleistocene loess deposits. Thus, over geologic timescales,

218 atmospheric Ca deposition during glacial periods may set the stage for future carbonate
219 weathering, potentially helping to build Mollisol SOC stocks.

220 Our analysis finds a role for Ca in Mollisol SOC storage but also suggests that grassland
221 and savanna vegetation promote SOC in Mollisols independent of other factors. Grasslands and
222 savannas can be maintained by fire, helping grasses to persist in climates that would otherwise
223 support forest.^{39,40} In this case, fire regimes that maintain grass dominance might directly
224 determine where Mollisols form.⁹ On the other hand, Mollisols are notably uncommon in tropical
225 grasslands and savannas,⁴¹ which suggests that ecological factors common to grasslands and
226 savannas—including high belowground productivity and fire—are not sufficient to generate the
227 C-rich A horizons characteristic of Mollisols. Tropical soils are typically highly weathered, host
228 less reactive minerals, and are generally more acidic than temperate soils that received Ca-rich
229 minerals following Pleistocene glaciation.^{22,42} These geologic limits to Ca supply, in addition to
230 climate, may curtail Mollisol development in the tropics. By contrast, multiple overlapping
231 environmental factors—including Ca weathering in post-glacial soils, cooler temperatures, mesic
232 climate, and the presence of grasses—converge in certain temperate regions, and Mollisols are an
233 emergent result of these overlapping factors.

234 **Implications for Mollisol conservation and climate mitigation**

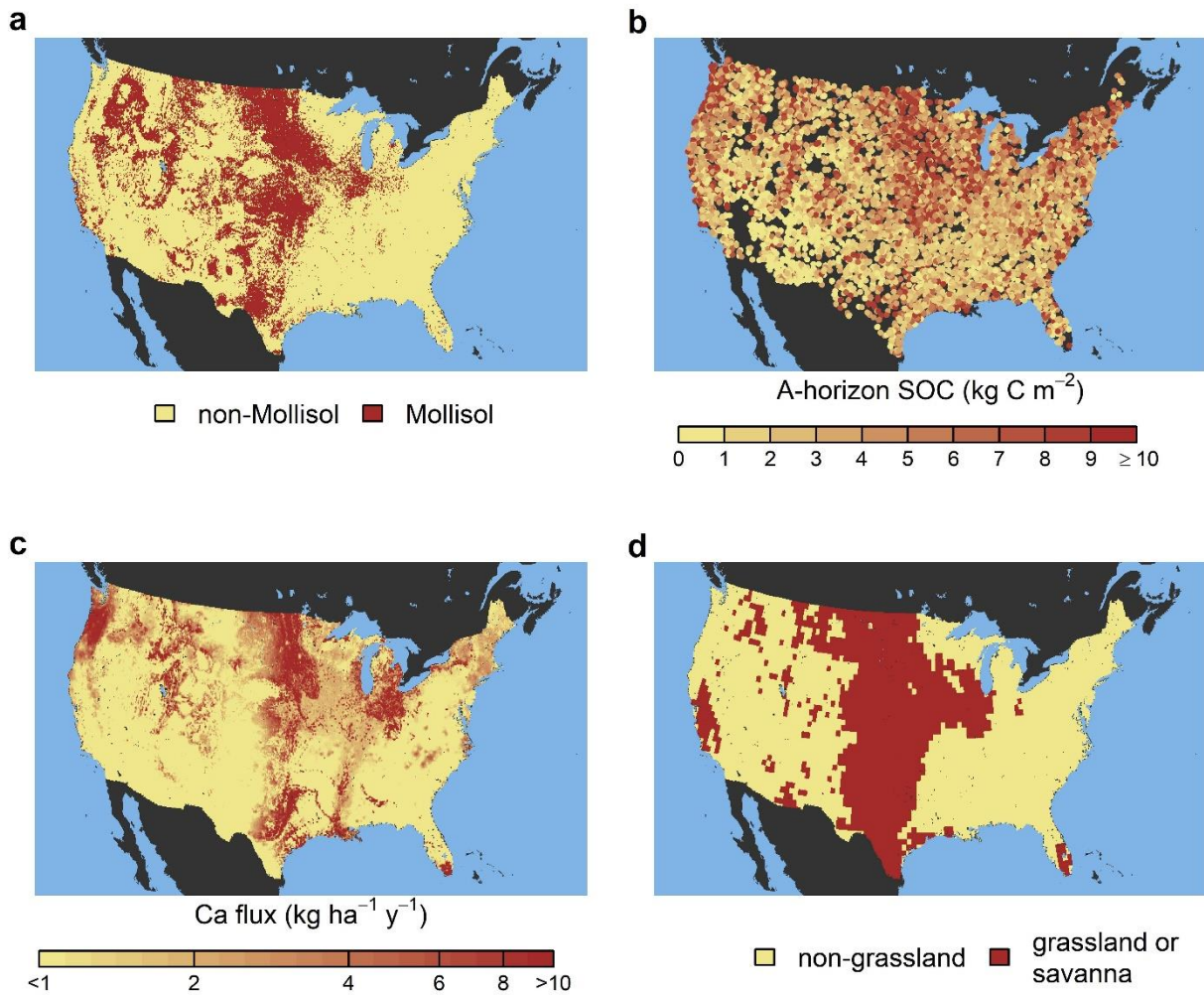
235 Our results imply that changes in soil Ca inputs due to cultivation might affect SOC cycling in
236 Mollisols. To address this possibility, we used our model to evaluate the magnitude of changes to
237 the Ca balance of Mollisol croplands relative to preindustrial conditions. We parametrized the
238 model with modern day atmospheric deposition chemistry, enabled agricultural fertilizer addition
239 and nutrient removal, and estimated agricultural liming rates. This analysis shows that soil Ca
240 cycling has changed dramatically in two ways (Figure 4). First, the model predicts that acid inputs

241 from fertilizer and atmospheric deposition have accelerated Ca release from carbonate weathering
242 by 20% in Mollisols. Second, agricultural liming has massively increased Ca inputs to cropland
243 soils (Figure 4). Taking modeled liming rates as a reference point, agriculture has increased Ca
244 inputs to Mollisol cropland soils by approximately 5-fold and increased Ca input to non-Mollisol
245 cropland soils by 10-fold relative to preindustrial levels. Alternatively, we can take the most recent
246 available agricultural census liming data,⁴³ which are from 1987, as a reference point. We estimate
247 that agriculture has increased Ca inputs to Mollisol cropland soils by 6-fold and non-Mollisol
248 cropland soils by 19-fold based on 1987 liming rates assuming that lime is 20% dolomite and 80%
249 calcite.⁴⁴

250 Clearly humans have dramatically altered the Ca cycle, and this has the potential to affect
251 SOC storage in Mollisols. The finding that agriculture has accelerated dissolution of native
252 carbonates is consistent with other studies that have linked agricultural soil acidification to soil
253 inorganic C loss, although the acceleration of carbonate weathering predicted by our model is
254 modest compared to estimates in highly acidified systems (e.g., in China).⁴⁵⁻⁴⁷ Our simulations
255 indicate that the more significant perturbation to the soil Ca cycle is agricultural lime addition.
256 Adoption of enhanced silicate⁴⁸ or carbonate⁴⁹ weathering for carbon dioxide removal will further
257 perturb the Ca cycle. These practices increase soil Ca inputs, which our analysis suggests
258 contribute to SOC storage over geologic timescales. However, increased Ca inputs have occurred
259 in response to unprecedented acid addition to cropland soils, and the effects of these competing
260 processes are hard to predict. For instance, field experiments indicate that the effect of agricultural
261 liming on SOC is highly variable over the short term.⁵⁰ Similarly, enhanced silicate weathering
262 does not necessarily benefit SOC storage in the short term,^{51,52} although a compilation of
263 experiments suggests a positive effect on average.⁵³ Liming may affect SOC differently than

264 natural weathering because it is intermittent: in the USA only 5-20% of cropland is limed in any
265 given year.⁵⁴ Variable Ca availability caused by intermittent liming may alternately stimulate and
266 suppress decomposition, with net effects that are challenging to predict.

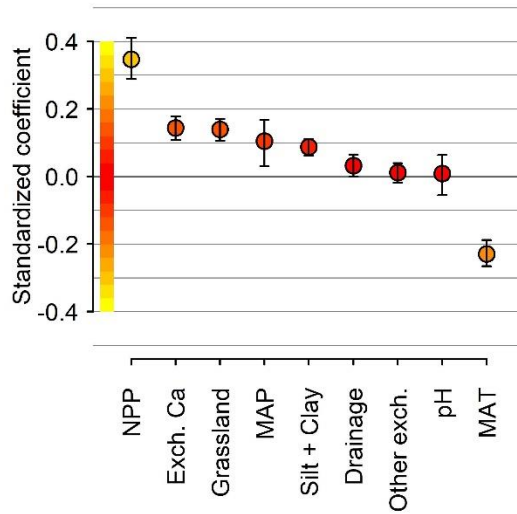
267 In the broader context of conservation agriculture, our results suggest that farming practices
268 that mimic pre-agricultural vegetation in grasslands by increasing root inputs, increasing plant
269 diversity, or reducing tillage may not be sufficient to preserve Mollisol SOC. Instead, vegetation-
270 focused strategies may need to be complemented with geochemical strategies that mimic the
271 natural Ca cycle of these soils. For instance, reducing excess N can protect soil carbonates, which
272 reduces emissions from dissolution of soil inorganic C by strong acids,⁴⁷ while also preserving a
273 critical Ca reservoir that likely helps to protect SOC. In addition, changing the cadence and
274 quantity of lime applied to croplands could better simulate the natural weathering regime. These
275 efforts must be supported by collection of baseline statistics on the agricultural Ca budget, which
276 remains poorly quantified.⁵⁴ Closing these knowledge gaps is critical to managing Earth's most
277 fertile soils sustainably.



278

279 **Figure 1. Potential environmental controls on Mollisols across the USA.** (a) The distribution
 280 of the Mollisol soil order across the conterminous USA based on digital soil mapping.⁵⁵ (b) Point
 281 observations of A-horizon soil organic carbon (SOC) derived from two databases.^{23,24} (c)
 282 Modeled preindustrial available calcium flux from silicate weathering, carbonate weathering, and
 283 atmospheric deposition. (d) The potential distribution of grasslands and savannas.²⁵

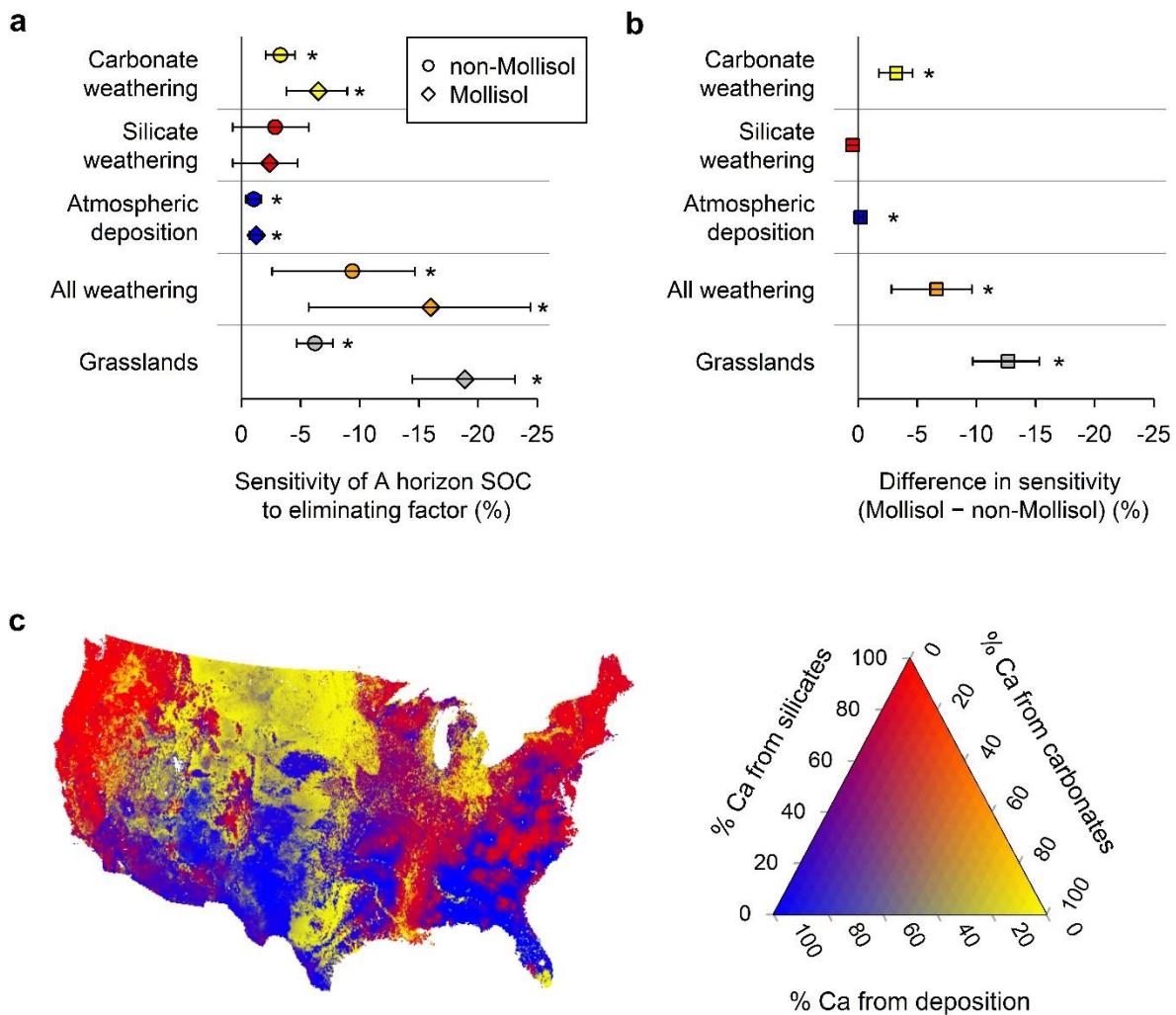
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286 **Figure 2. Predictors of A-horizon SOC stocks across the USA.** Standardized regression
 287 coefficients are derived from a multivariate linear regression model. Whiskers show 95%
 288 confidence intervals derived from a spatial blocked bootstrapping procedure (see Methods).
 289 Standardization was performed by dividing each non-binary variable by two times the standard
 290 deviation.⁵⁶ The absolute value of each regression coefficient is an index of how strongly related
 291 each variable is to A-horizon SOC stocks. Abbreviations: NPP = net primary productivity, Exch.
 292 Ca = total exchangeable Ca²⁺, MAP = mean annual precipitation, Other exch. = sum of non-Ca
 293 exchangeable ions, MAT = mean annual soil temperature.

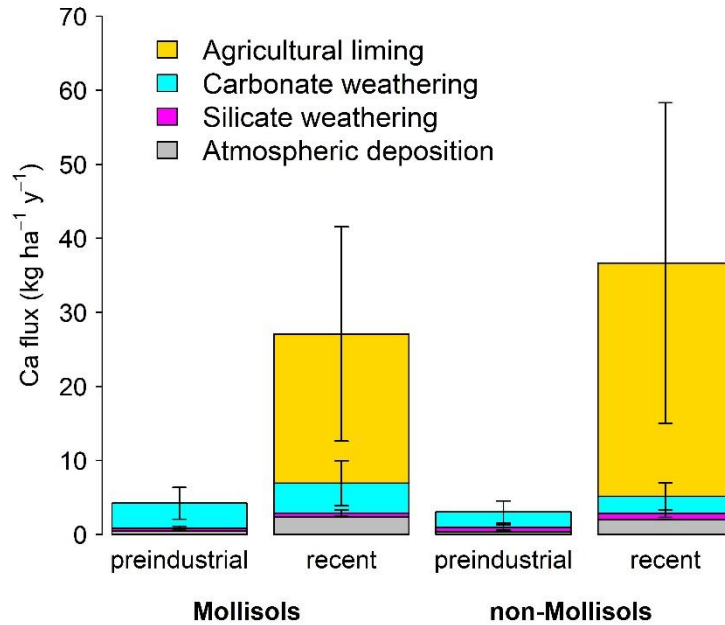
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296 **Figure 3. Sensitivity of Mollisol extent and A-horizon organic carbon to Ca sources.** (a) The
 297 relative effect of removing Ca sources on predicted A-horizon soil organic carbon (SOC) stocks
 298 across non-Mollisol soils (circles) versus Mollisols (diamonds). Sources include carbonate
 299 weathering (yellow), silicate weathering (red), atmospheric deposition (blue), and carbonate and
 300 silicate weathering combined (orange). The effect of setting all grassland vegetation to non-
 301 grassland is shown in gray. (b) The difference in sensitivities: effect of removing factor in
 302 Mollisols minus effect in non-Mollisols. Whiskers show 95% confidence intervals derived from
 303 spatial blocked bootstrapping (see Methods) and are marked with an asterisk when they do not
 304 overlap zero. (c) The relative contributions of carbonate weathering, silicate weathering, and
 305 atmospheric deposition to available Ca across the USA.

306



307

308 **Figure 4. Modeled Ca fluxes to croplands, preindustrial (1850) versus recent (2000-2010).**
 309 Stacked bars show the Ca sources: atmospheric deposition, carbonate weathering, silicate
 310 weathering, and agricultural liming. Data for Mollisol regions are shown on the left and non-
 311 Mollisol regions on the right. Whiskers show Monte Carlo standard errors derived from
 312 approximated parameter uncertainties. Liming estimates are based on the conservative
 313 assumption that farmers lime sufficiently to maintain soil pH (see Supplementary Information).

314

315 **Methods**

316 **Quantifying global role of Mollisols**

317 We calculated the total land area of Mollisols, the fraction of global agricultural production
318 occurring on Mollisols, and the fraction of agricultural SOC stored by Mollisols using the
319 Harmonized World Soil Database, Version 2.0 (HWSD).² For this analysis we assumed that the
320 distribution of Mollisols can be approximated by aggregating three World Reference Base soil
321 groups: Chernozems, Phaeozems, and Kastanozems.⁵⁷ HWSD soil mapping units were assigned
322 as Mollisol or non-Mollisol based on the dominant soil type in each unit. SOC was calculated
323 from the HWSD and summed to 1 m depth. We then combined the HWSD with the 1 km
324 resolution GFSAD 2010 croplands mask³ to estimate the area of croplands and cropland SOC
325 storage. Production of wheat, corn, and soy occurring on Mollisols was obtained by combining
326 the HWSD with SPAM global production maps for 2010.⁵⁸ Production values were rescaled to
327 calories based on UN Food and Agriculture Organization Annex I food composition tables.⁵⁹

328 **Geochemical model overview**

329 We developed a simplified geochemical model to simulate the release of Ca from silicate and
330 carbonate weathering in the top 1 m of soil across the USA. We parametrized the model with
331 existing data when possible and then calibrated unknown parameters related to mineral surface
332 reactivity so that modeled soil pH matched observed modern soil pH across the study region. We
333 based our model on existing geochemical models that were designed to simulate soil acid-base
334 chemistry in response to acid rain.⁶⁰ Our model also incidentally resembles approaches used to
335 simulate enhanced silicate weathering,⁶¹ although it was not designed for this purpose and is less
336 complex. The model treated the entire upper 100 cm of soil as a single chemically homogeneous
337 reservoir, tracking the inputs and outputs of seven ions that control soil pH and weathering rates:
338 Ca^{2+} , Mg^{2+} , Na^+ , K^+ , SO_4^{2-} , NO_3^- , Cl^- . These ions were sourced from dissolution of silicate and

339 carbonate minerals, atmospheric deposition, agricultural inputs, and biological fixation in the
340 case of N. Ions were lost via leaching, carbonate mineral precipitation, export in crop biomass,
341 and volatilization in the case of N. Additional ions were assumed to equilibrate instantaneously
342 with the soil solution and hence were modeled implicitly as a function of other factors: H^+ , Al^{3+} ,
343 $Al(OH)^{2+}$, $Al(OH)_2^+$, AlH_2Org^{2+} , $AlHOrg^+$, OH^- , CO_3^- , HCO_3^- , H_2Org^- , $HOrg^{2-}$, Org^{3-} , and
344 $Al(OH)_4^-$. We approximated ion activities with concentrations because, under most conditions,
345 modeled ionic strengths were too low to affect our results. Mineral concentrations were treated as
346 constant at the timescales being modeled. While the model was able to simulate year-to-year
347 weathering dynamics, for the purposes of this analysis, we applied a steady-state solution
348 because this simplified computations substantially. The model had nine governing equations: one
349 for each of the seven conserved ions and two algebraic constraints stipulating charge balance and
350 conservation of ions adsorbed on the soil exchange complex (Table S4). A full description of the
351 model is provided in the Supplementary Information file.

352 **Input data**

353 Whenever possible, we used spatially explicit environmental data to assign model parameters.
354 When time series were available, we used time-averaged environmental parameters to drive the
355 model, setting the years 2001-2010 as our reference period for recent environmental conditions.
356 To capture pre-industrial conditions, we reset deposition rates for N and S, reset atmospheric
357 pCO_2 , and turned off the model's agricultural nutrient budget.

358 To parametrize climate and soil hydrologic properties, we used several sources. We
359 derived soil temperature from statistical estimates of the mean annual soil temperature at 50-15
360 cm depth,⁶² which we assume approximates the mean temperature of the upper 100 cm of soil on
361 an annually averaged basis. We calculated recharge (RC) using the Global Streamflow

362 Characteristics Database (GSCD), which provides 0.125 degree resolution estimates of
363 streamflow and base flow index.⁶³ We calculated recharge by multiplying streamflow by the
364 baseflow index. We constrained soil moisture with the satellite-informed Global Land
365 Evaporation Amsterdam Model (GLEAM) V3.8 root zone soil moisture dataset (0.25 degree
366 resolution).⁶⁴ We also obtained pedotransfer-based maps of wilting point and field capacity
367 associated with GLEAM. Finally, we parametrized net primary productivity (NPP) using
368 MOD17 (500 m resolution).⁶⁵

369 We parametrized soil mineralogy using two sources. For silicate minerals, we spatially
370 interpolated data from the North American Soil Geochemical Landscapes Project (NASGLP),²¹
371 which includes estimates of major element abundance and quantitative X-ray diffraction data for
372 a selection of silicate and carbonate minerals. We used these data to directly constrain some
373 minerals and approximate concentrations of others that are not directly reported by NASGLP.
374 First, we averaged A-horizon and C-horizon data at the NASGLP sampling locations. We then
375 interpolated the NASGLP data for each mineral to locations where we ran the geochemical
376 model, using inverse distance weighting with an exponent of 2 and an averaging neighborhood
377 of 75 km. Plagioclase feldspar and the plagioclase anorthite fraction (fAn) were estimated by
378 first multiplying the molar concentration of Na from the NASGLP by the formula weight of
379 albite. Where albite exceeded 80% of the total plagioclase feldspar content obtained from the
380 NASGLP, albite was reset to 80% of the plagioclase content. Anorthite was then assumed to
381 make up the remainder of the plagioclase pool.²⁰ K-feldspar, hornblende, and pyroxene were
382 taken directly from the NASGLP X-ray diffraction estimates. To represent clay minerals, we
383 limited our analysis to chlorite (clinochlore) and illite (approximated as muscovite), which we
384 treated as generalized categories that stand in for the full diversity of Mg- and K-bearing 2:1

385 phyllosilicates (e.g. vermiculite and smectite group clays). Illite was calculated by subtracting
386 the K in K-feldspar from total K and assigning all residual K to illite. Similarly, chlorite was
387 calculated by first calculating the amount of Mg in hornblende, pyroxene, and dolomite (Table
388 S5). This value was subtracted from total Mg, and any residual Mg was assigned to chlorite.

389 To estimate carbonate mineral stocks, we did not use NASGLP data directly. Given the
390 high weatherability of carbonates, small quantities of carbonate mineral had a large effect on
391 modeled soil pH values; hence we used high-resolution digital soil maps from NATSGO⁵⁵ to
392 ensure accurate assignment of soil carbonate content. We first calculated the stock of carbonate
393 in CaCO₃ equivalents to 1 meter depth from NATSGO. Next, we subdivided this stock into
394 calcite and dolomite components by using the data from the NASGLP to calculate the ratio of
395 calcite to dolomite. In addition to CaCO₃ content, we derived soil texture (silt, sand, and clay
396 percentages), cation exchange capacity, and soil bulk density parameters from NATSGO,
397 averaging these properties over the top 1 meter of soil or to bedrock if shallower than 1 meter.
398 All NATSGO soil properties were summarized by calculating the share-weighted average within
399 soil mapping units. Data were then extracted using the 30-meter resolution gridded version of
400 NATSGO.

401 We parametrized the cropland N inputs and outputs using a county-level nutrient budget
402 for the period 1987-2012.⁶⁶ We ran the geochemical model in one of two modes, either with
403 cropland nutrient imports and exports enabled or with only natural N fixation rates enabled. We
404 determine which mode to use by assigned modeled locations to cropland or non-cropland land
405 cover using the GFSAD 1 km cropland mask.³

406 We parameterized deposition of N, S, Cl, Ca, Mg, Na, and K, using gridded data from the
407 US Environmental Protection Agency's National Trend Network,⁶⁷ which we averaged for 2001-

408 2010. To represent preindustrial deposition of N and S, we used the multi-model average from
409 the ACCMIP project for the year 1850.²⁷ For Cl, Ca, Mg, Na, and K no data from before the year
410 2000 were available. Human activity has increased deposition of base cations, including Ca, in
411 the Western USA.³⁶ To account for this trend, we applied a factor of 5 difference between recent
412 and preindustrial times, which approximates dynamics recorded in lake sediment cores in
413 Colorado.³⁶ We applied this multiplier to Ca, Mg, and K, but left Na unchanged since this solute
414 is primarily derived from marine aerosols outside of deserts.

415 **Model calibration and uncertainty**

416 We implemented the model at point locations, extracting data from the aforementioned
417 environmental datasets at each point. For the calibration and validation steps, we selected points
418 by acquiring soil pH data from the USDA NRCS National Cooperative Soil Survey (NCSS)
419 Kellogg Soil Survey Laboratory database. We computed depth weighted average pH values in a
420 1:1 water matrix for all soil profiles with available data to a depth of 1 m, or to the depth of the
421 lowermost C horizon in cases where the profile terminated below 1 m. Similarly, we computed
422 depth-weighted average values for exchangeable cations using the NCSS database. We
423 represented Ca^{2+} , Mg^{2+} , Na^+ , and K^+ using NH_4 -acetate (pH 7) extraction data and Al^{3+} from KCl
424 extraction. Exchangeable H^+ was estimated by subtracting the sum of exchangeable Ca^{2+} , Mg^{2+} ,
425 Na^+ , K^+ , and Al^{3+} from the cation exchange capacity (CEC) obtained by the NH_4 -acetate method.
426 When the sum of these ions exceeded the CEC, exchangeable H^+ was set to zero and the values
427 of all ions were rescaled by the value $(\text{CEC} / \text{sum cations})$ so that the sum equaled the CEC.

428 We spatially resampled the pH and exchangeable cation data by binning them into 1
429 degree by 1 degree cells based on their latitude and longitude and then resampling 6,000
430 locations with replacement, with sampling weights inversely proportional to the number of

431 profiles in each cell. We extracted environmental data at these points and discarded those with
432 missing data, yielding 4,149 unique pH observations that were evenly distributed across the
433 conterminous USA (Figure S1). Exchangeable ions were only reported at 2,484 locations with
434 pH measurements. Because we resampled with replacement, some soil profiles occurred more
435 than once by design; the total number of pH observations was 5,389 (including pseudo-
436 replicates) and the total number of exchangeable cation observations was 3,280.

437 We calibrated the model by randomly sampling 2,000 pH training points from the NCSS
438 profiles and using them for model inversion based on soil pH. We optimized two parameters, r_2
439 and r_3 , which controlled the reactivity for secondary phyllosilicate minerals and carbonate
440 minerals respectively (see Supplementary Information). We calibrated the model using a Markov
441 Chain Monte Carlo (MCMC) approach, applying the adaptive Metropolis Hastings algorithm
442 with delayed rejection⁶⁸ implemented via the R package FME.⁶⁹ The cost function was defined to
443 minimize the sum of squared errors in soil pH. We initiated the MCMC algorithm with manually
444 calibrated initial parameter values and uninformative priors. The initial model variance was set
445 equal to the mean squared residuals based on the initial parameter estimates, and the initial jump
446 values were set to 10% of the initial parameters. The adaptive stage of the algorithm was run for
447 a burn-in period of 1,000 iterations updating the covariance matrix every 50 iterations with the
448 number of delayed rejections steps set to 2. After burn-in sampling continued for an additional
449 1,000 iterations. We checked for convergence by running the algorithm using perturbed values of
450 the starting parameters and different training samples and found that results were comparable.
451 The final calibration yielded values of $10^{-6.7}$ for r_2 and $10^{-6.4}$ for r_3 .

452 We estimated uncertainty in modeled Ca fluxes using a Monte Carlo approach. Parameter
453 uncertainties were largely unconstrained and could only be approximated. Given this, our goal

454 was to quantify the robustness of our results given arbitrary but substantial parameter
455 uncertainty. Based on our best judgement, we divided the model parameters into “low”,
456 “moderate” and “high” uncertainty categories. Low uncertainty parameters were treated as fixed.
457 Moderate uncertainty parameters were randomly perturbed within a uniform range spanning 50%
458 - 150% of the default value. High uncertainty parameters were varied uniformly within an order
459 or magnitude range: each was transformed with a base-10 logarithm, randomly perturbed within
460 a range spanning 50% - 150%, and then transformed back to the original scale. This procedure
461 was repeated 1,500 times at the model calibration locations. We treated the coefficient of
462 variation of the average Ca fluxes derived from this process as an approximate estimate of
463 uncertainty. Parameters assigned moderate uncertainty included: all mineral surface areas,
464 combined N inputs, N removal in croplands, dissolved organic carbon inputs, the charge density,
465 C:N ratio, and temperature dependence (Q_{10}) of dissolved organic matter, the leaching rate, and
466 both the temperature dependence and H^+ reaction order for silicate weathering. Parameters
467 assigned high uncertainty included, the decomposition rate coefficient for dissolved organic
468 matter, the N volatilization rate, weathering rate coefficients for silicates and carbonates (r_1 , r_2 ,
469 and r_3), all equilibrium constants relating to dissolved organic matter, and all ion exchange
470 selectivity coefficients.

471 **Statistical analysis**

472 After calibrating the geochemical model, quantified the strength of the relationship between soil
473 Ca availability and A-horizon SOC using multiple linear regression. We obtained A-horizon SOC
474 stocks from the RaCA²³ and the NCSS²⁴ databases. We ran regressions on the full population of
475 11,332 A-horizon SOC estimates from RaCA and NCSS. When working with data from RaCA
476 and NCSS, we calculated the SOC stock in all horizons with the master designation “A”. The

477 SOC stock (kg C m^{-2}) was calculated from the total carbon percentage (C%), the inorganic
478 carbon percentage (IC%), A-horizon thickness (TH, cm), rock fraction (RF, unitless) and bulk
479 density (BD, g cm^{-3}) as:

$$480 \text{ SOCstock} = ((\text{C\%} - \text{IC\%})/100) * \text{BD} * \text{TH} * (1 - \text{RF}) * 10 \quad (\text{Equation 23})$$

481 Inorganic carbon was calculated from CaCO_3 equivalents reported in RaCA. In the cases where
482 IC% exceeded C%, OC% was set to zero. In the case of NCSS, we used the “estimated organic
483 C” field, which is corrected for IC where applicable, or organic carbon content estimated via the
484 Walkley Black method when this field was not available. After calculating SOC in each A
485 horizon, we summed all A horizon stocks for each pedon to obtain total A-horizon SOC. We log
486 transformed A-horizon SOC stocks before fitting the model.

487 We used linear regression to model log-transformed A-horizon SOC as a function of total
488 exchangeable Ca^{2+} (ceq kg^{-1}) and other ecologically important or potentially confounding
489 factors. In addition to exchangeable Ca^{2+} , we included two additional outputs of the geochemical
490 model: the sum of non- Ca^{2+} exchangeable cations and the simulated soil pH. We used potential
491 natural vegetation maps²⁵ to capture the effect of grasses, treating grass presence as a binary
492 predictor with grasslands and savannas combined into a single category (present = 1, absent = 0).
493 We accounted for the effect of plant inputs on SOC by including the logarithm of average NPP,
494 derived from MOD17 for the period 2001-2010. We used gridded climate maps to control for
495 mean annual soil temperature⁶² and mean annual precipitation (1991-2020).⁷⁰ We also controlled
496 for the average silt plus clay content of the top meter of soil and soil drainage class, which we
497 derived from NATSGO.⁵⁵ Drainage class categories were assigned numerical values from 1-7,
498 with 1 being excessively drained and 7 being very poorly drained. We compared the relative
499 importance of different predictors in the regression models by standardizing all predictors

500 upstream of fitting the models. We standardized by dividing continuous predictors by two times
501 the standard deviation, which is recommended in cases when some predictors are binary.⁵⁶ We
502 estimated uncertainty associated with the coefficients by performing nonparametric spatially
503 blocked bootstrapping to account for spatial dependence.²⁰ This involved dividing the data into
504 blocks defined by 2-by-2 degree grid cells and then resampling the cells with replacement 1,000
505 times. We fit a regression to each of the 1,000 resampled datasets and stored the regression
506 coefficients. We then calculated bias corrected and accelerated 95% confidence intervals from
507 the bootstrap replicates.⁷¹

508 After fitting the regression, we estimated the sensitivity of A-horizon SOC to eliminating
509 specific Ca sources under preindustrial conditions. This first involved using the geochemical
510 model to estimate soil exchangeable Ca^{2+} under a preindustrial baseline scenario. In the baseline
511 scenario, we eliminated all agricultural components of the geochemical model and used our best
512 estimate of preindustrial deposition rates for major cations and anions (see Supplemental Text).
513 Next, we evaluated the sensitivity to cation inputs from carbonate weathering and silicate
514 weathering by running the model with each mineral cation source eliminated, setting either
515 carbonate or silicate surface areas to zero. This meant that Ca, but also Mg, K, and Na
516 weathering fluxes were affected by removing each source. To evaluate sensitivity to deposition,
517 we set all base cation deposition fluxes to zero. Each of these modified model runs generated
518 predictions of exchangeable Ca^{2+} in the absence of each cation source. We also quantified the
519 effect of eliminating grasslands by setting the grassland predictor to zero everywhere.

520 To calculate sensitivity values, we followed the following protocol. First, we fit a linear
521 regression to the SOC data using present day model outputs as described above, but with
522 response and predictors left unscaled. Next, we used the fitted regression to obtain predictions in

523 a 10-km grid across the USA with inputs derived from each of the preindustrial scenarios
524 described above. We then calculated the total stock of A-horizon SOC in Mollisols and non-
525 Mollisol soils across the grid under the baseline scenario. The distribution of Mollisols was
526 obtained from NATSGO, and 10-km grid cells were assigned to the Mollisol category when
527 Mollisols comprised the dominant soil order at the coordinates of the grid cell center. Within
528 each soil taxonomic domain, we estimated the sensitivity to eliminating Ca sources and
529 grasslands as the percent change in SOC from the preindustrial baseline after each factor was
530 eliminated: $100 * [(SOC \text{ under elimination scenario} - SOC \text{ under baseline scenario}) / SOC \text{ under}$
531 $\text{baseline scenario}]$. We estimated uncertainty in the sensitivity values by repeating this protocol
532 1,000 times during the spatially-blocked bootstrap resampling and calculating bias-corrected
533 95% confidence intervals as above. We also calculated the difference in sensitivity in Mollisol
534 versus non-Mollisol soils, estimating uncertainty using the same bootstrapping procedure.

535 Soil organic matter can contribute to cation exchange capacity, which may explain a
536 relationship between total exchangeable Ca^{2+} and SOC even in the absence of an effect of Ca on
537 SOC persistence. To account for this possibility, we conducted an additional regression analysis
538 after correcting total cation exchange capacity for the contribution of soil organic matter.
539 Corrected cation exchange capacity (CEC-c, $ceq \text{ kg}^{-1}$) was obtained from the uncorrected CEC
540 and the soil organic matter percentage (SOM%) from NATSGO:

$$541 \text{ CEC-c} = \text{CEC} - \text{CEC-OM} * (\text{SOM\%/100}) \quad (\text{Equation 24})$$

542 Where CEC-OM is the cation exchange capacity of organic matter, assumed equal to 200 ceq kg^{-1}
543 ^{1.72} This formula could generate negative or zero values, and so in cases where CEC-c was less
544 than a minimum value of 0.01 we re-set it to this value. The results of the regressions computed
545 with CEC-c were similar to the primary results (Figure S3).

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- 730

731 **Supplemental Information: Calcium promotes carbon-rich grassland soils**

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748 **Contents:**

749 1) Supplemental Text: Geochemical model description

750 2) Figures S1 – S5

751 3) Tables S1 – S6

752 4) References

Supplemental Text: Geochemical model description

754 **Governing equations**

755 Our model was specified to track inputs and outputs of seven ions that control soil pH and
756 weathering rates: Ca^{2+} , Mg^{2+} , Na^+ , K^+ , SO_4^{2-} , NO_3^- , Cl^- (Table S3). These ions were sourced from
757 dissolution of silicate and carbonate minerals, atmospheric deposition, agricultural inputs, and
758 biological fixation in the case of N. Inputs of ions from deposition and ag-lime were treated as
759 instantaneous (i.e., kinetics of lime dissolution were not explicitly modeled). Ions were lost via
760 leaching, secondary mineral precipitation, export in crop biomass, and volatilization in the case
761 of N. Additional ions were assumed to equilibrate instantaneously with the soil solution and
762 hence were modeled implicitly as a function of other factors: H^+ , Al^{3+} , $\text{Al}(\text{OH})^{2+}$, $\text{Al}(\text{OH})_2^+$,
763 $\text{AlH}_2\text{Org}^{2+}$, AlHOrg^+ , OH^- , CO_3^- , HCO_3^- , H_2Org^- , HOrg^{2-} , Org^{3-} , $\text{Al}(\text{OH})_4^-$. Apart from export in
764 crop biomass, nutrient uptake and return via litterfall were assumed to be in equilibrium; hence
765 chemical dynamics caused by net growth or mortality of non-agricultural ecosystems were not
766 considered in this study.

767 **Hydrology**

768 We parametrized leaching rates for major ions as a function of recharge or hydrologic baseflow
769 (RC, mm y^{-1}), which we assume represents the flux of water that infiltrates the soil without being
770 lost to evapotranspiration or overland flow. We set a minimum recharge value of 1 mm y^{-1}
771 because zero-recharge values yielded undefined values in the model. After constraining recharge,
772 we partitioned the total amount of soil water (V, l) into mobile and immobile components, under
773 the assumption that only a fraction of the soil pores are leached during leaching events. The
774 immobile component of the soil water was equal to the water content at wilting point (V_{wp}, l),
775 which governed the fraction of soil water mobilized during recharge:

776 $F_{\text{mob}} = (V - V_{\text{wp}})/V$ (Equation 1)

777 We assumed that only the solutes in the mobile fraction are vulnerable to leaching loss and that
778 solutes are partitioned into mobile and immobile fractions by F_{mob} . We also assumed that solutes
779 in the mobile fraction are conservatively diluted at the timescale of recharge events. The
780 concentration of solute i leached during recharge events (C_i) was therefore a function of the soil
781 moisture at field capacity, V_{fc} :

782 $C_i = M_i * F_{\text{mob}} / (V_{\text{fc}} - V_{\text{wp}})$ (Equation 2)

783 Where M_i was the total moles of the solute in the soil. The leaching rate for a given ion, L_i (mol
784 y^{-1}) was a function of concentration in recharge water (mol l^{-1}) times recharge (l y^{-1}):

785 $L_i = RC * C_i$ (Equation 3)

786 **Weathering kinetics**

787 Weathering kinetic expressions vary widely in complexity. We adopted a simple power law
788 description for silicate weathering kinetics. More complex approaches, such as transition state
789 theory, incorporate multiple reaction mechanisms. These approaches are sensitive to assumptions
790 regarding the type and reactivity of secondary minerals and the extent of mineral surface
791 passivation, which we could not parametrize at the scale of the USA. To further reduce
792 complexity, dissolution kinetics of tectosilicates and inosilicates were referenced to the reactivity
793 of plagioclase feldspar based on a compilation of field-based weathering rate measurements.¹
794 This was not possible for pyroxene given a lack of field based weathering rate estimates, so we
795 assigned this mineral a reaction rate of 1.0 relative to plagioclase. For tecto- or inosilicate
796 mineral i , weathering rates in the top 100 cm of soil (mol y^{-1}) were a function of total geometric
797 surface area (A_i , m^2), a reaction rate coefficient (r_1 , mol $\text{m}^{-2} \text{y}^{-1}$), the ratio giving reaction rate

798 relative to plagioclase (RR_i , unitless), an Arrhenius-type term governing temperature dependence
799 (T_f , unitless), volumetric water content (θ m³ m⁻³), the hydrogen ion concentration ($[H^+]$), a
800 reference hydrogen ion concentration ($[H^+]_r$, set equal to 10^{-5}), and the reaction order with
801 respect to H^+ (n).

$$802 \quad W_i = r_1 * A_i * RR_i * T_f * \theta * (H^+ / H^+_r)^n \quad (\text{Equation 4})$$

803 For phyllosilicate minerals, the rate expression was identical except that the term RR_i was
804 omitted and an affinity term was added to make the reactions reversible, allowing clay synthesis.

$$805 \quad W_{i, \text{phyllo}} = r_2 * A_i * T_f * \theta * (H^+ / H^+_r)^n * (1 - \Omega_i) \quad (\text{Equation 5})$$

806 The term r_2 gives a reaction rate coefficient for phyllosilicates. The parameter Ω_i was the
807 saturation index for phyllosilicate mineral i , where $\Omega_i = IAP_i / K_{sp}$. The IAP was the ion activity
808 product or reaction quotient. K_{sp} was the solubility constant for each mineral.

809 We assumed that the temperature and pH dependence of silicate weathering was the same
810 for all minerals. The activation energy for silicate weathering was set to equal $74 \text{ kJ mol}^{-1} \text{ K}^{-1}$.^[2]
811 The temperature modifier for silicate weathering was given by the following equation:

$$812 \quad T_f = \exp(-E_{a_{\text{sil}}} / R * (1/(T) - 1/(T_{\text{ref}}))) \quad (\text{Equation 6})$$

813 Where $E_{a_{\text{sil}}}$ was the activation energy for silicates, R was the universal gas constant, T was the
814 soil temperature (K) and T_{ref} was a reference temperature (298 K).

815 We assigned several silicate weathering parameters manually in order to match published
816 compilations of field weathering rates.^{3,4} The parameter r_1 represented the bulk plagioclase
817 feldspar weathering rate coefficient (y^{-1}) at a reference pH of 5.0 ($H_{\text{ref}} = 10^{-5}$). We assumed that
818 under the wettest climate conditions, mean soil pH approaches a value of 5.0,⁵ and so bulk

819 feldspar weathering rates ought to approach r_1 under these conditions. Across our calibration
820 dataset, the 95th percentile value for recharge (RC) equaled 474 mm, which implies that r_1 equals
821 $10^{-4.3}$ based on the power law relationship between recharge and bulk weathering rates reported
822 by Yu and Hunt (2018).⁴ Based on similar reasoning, we set the reaction order for H^+ , n , equal to
823 0.66. We chose this value because field estimates of silicate weathering rates increase by roughly
824 two orders of magnitude in the transition from dry conditions (infiltration rates $\sim 0.1 \text{ m y}^{-1}$) to
825 humid conditions (infiltration rates $\sim 1 \text{ m y}^{-1}$),³ and soil pH spans roughly 3 units in the transition
826 from wet to dry climates.⁵ This implies that weathering rates should increase by two orders of
827 magnitude over a three order of magnitude range in pH (reaction order = 0.66). This value is
828 reasonable for many silicates,⁶ and allowed us to recover the observed relationship between
829 feldspar weathering rates in the field and infiltration reasonably well with the calibrated model
830 (Figure S5).

831 We modeled carbonate weathering kinetics using a more complex expression based on
832 transition state theory because carbonate minerals dissolve and precipitate congruently in soil,
833 reducing uncertainty regarding secondary minerals and surface passivation. Dissolution and
834 precipitation for carbonate minerals was governed by the following equation:

$$835 \quad W_{i, \text{carb}} = r_3 * A_i * \theta * (R_{\text{acid}} * [H^+]^{nH} + R_{\text{neutral}} + R_{\text{CO}_2} * p\text{CO}_2^{n\text{CO}_2}) * (1 - \Omega_i) \quad (\text{Equation 7})$$

836 Where A_i was the total surface area for mineral i , r_3 was ratio of reactive surface area to
837 geometric surface area for carbonates, R_{acid} , R_{neutral} , and R_{CO_2} were separate reaction mechanisms
838 for acid, neutral, and CO_2 driven dissolution reactions, nH was the reaction order for H^+ , and
839 $n\text{CO}_2$ was the reaction order for CO_2 . The parameter Ω_i was the saturation index for carbonate
840 mineral i , where $\Omega_i = \text{IAP}_i / K_{\text{sp}}$. The IAP was the ion activity product or reaction quotient. K_{sp}

841 was the solubility constant for each mineral. Reaction mechanisms (R_m) were governed by
842 equations with the form:

$$843 R_m = A_m \cdot \exp(-E_{a_m}/R \cdot (1/T - 1/T_{ref})) \quad (\text{Equation 8})$$

844 Where A_m and E_{a_m} were the preexponential factor ($\text{mol m}^{-2} \text{ y}$) and activation energy ($\text{kJ mol}^{-1} \text{ K}^{-1}$)
845 ¹⁾ for mechanism m .

846 All spatially invariant parameters related to weathering reactions are given in Table S5.

847 Our treatment of weathering kinetics left two unknown parameters: r_2 , the reaction rate
848 coefficient for phyllosilicates, and r_3 , the ratio of reactive to total surface area for carbonates.
849 These parameters were obtained by model inversion (see Methods in main article).

850 **Mineral surface areas**

851 We estimated geometric surface areas for each mineral. For tectosilicates, inosilicates, and
852 carbonates, we assumed that particles were silt- and sand-sized and spherical. We calculated
853 surface area to volume ratios (SVR, $\text{m}^2 \text{ m}^{-3}$) for silt and sand:

$$854 \text{SVR} = (4 \cdot \pi \cdot (D/2)^2) / (4/3 \cdot \pi \cdot (D/2)^3) \quad (\text{Equation 9})$$

855 Where D was the particle diameter, which we set to the geometric mean of each size class.⁷ The
856 average surface area to volume ratio for minerals in the silt and sand fraction was then calculated
857 as a weighted average based on silt and sand percentages derived from the NATSGO database
858 (see below). Clays (illite and chlorite) were modeled as cylindrical plates with a diameter of 1
859 μm and a diameter to height ratio of 10:1 [7]

$$860 \text{SVR}_{\text{clay}} = ((D/10 \cdot 2 \cdot \pi \cdot D/2) + (2 \cdot \pi \cdot (D/2)^2)) / ((D/10) \cdot (\pi \cdot (D/2)^2)) \quad (\text{Equation 10})$$

861 Total geometric surface area for each mineral was obtained by multiplying the surface area to
862 volume ratio by the total volume of each mineral in the soil.

$$863 A_i = SVR_i * P_i * (\rho_s / \rho_i) * h * 10^{-5} \quad (\text{Equation 11})$$

864 Where P_i was the percentage of mineral i in the soil, ρ_s was the bulk density of the soil, ρ_i was
865 the density of mineral i , and h was the soil thickness in mm. Chemical formulas and densities for
866 the minerals that we included in the model are shown in Table S6. For clay minerals, we limited
867 our analysis to chlorite (clinochlore) and illite (approximated as muscovite), which we treated as
868 generalized categories that stand in for the full diversity of Mg- and K-bearing 2:1 phyllosilicates
869 (e.g. vermiculite and smectite group clays).

870 **Equilibrium chemistry**

871 We parametrized a set of major equilibrium reactions that governed carbonate ion speciation,
872 aluminum hydrolysis, organic acid speciation, Al-organo ion pair formation, and cation exchange
873 reactions (Table S7). When possible, we obtained equilibrium constants by calculating them
874 from standard enthalpies and entropies, which we obtained from the SUPCRT92 thermodynamic
875 database⁸ loaded with the R package CHNOSZ.⁹

876 Carbonate equilibria depended on the average soil $p\text{CO}_2$, which we parametrized as a
877 function of soil respiration:¹⁰

$$878 p\text{CO}_2 = p\text{CO}_{2\text{atm}} + 1.03 * R_s / T^2 \quad (\text{Equation 12})$$

879 Where $p\text{CO}_{2\text{atm}}$ was atmospheric $p\text{CO}_2$, set to 380 ppm for 2001-2010^[11] and 280 ppm for
880 preindustrial times,¹² and R_s was soil respiration in $\text{g m}^{-2} \text{y}^{-1}$. We obtained R_s from net primary
881 productivity (NPP, $\text{g m}^{-2} \text{y}^{-1}$):¹³

$$882 R_s = 1.24 * \text{NPP} + 24.5 \quad (\text{Equation 13})$$

883 We modeled dissolution and precipitation of carbonates and phyllosilicates as reversible
884 processes governed by chemical equilibria (Table S7), which defined the saturation index (Ω)
885 used in weathering rate calculations. In the case of phyllosilicates, the saturation state depended
886 on dissolved SiO_2 , which we did not model explicitly as a state variable. Instead, the
887 concentration of $\text{SiO}_{2(\text{aq})}$ was assumed to be determined by instantaneous dissolution and
888 precipitation of amorphous SiO_2 (Table S7).

889 We represented organic acid speciation using the triprotic model and allowed for
890 formation of ion pairs between Al^{3+} and organic acids. Equilibrium constants for these reactions
891 were obtained by averaging published values from New England lakes, streams, and soils.¹⁴ To
892 parametrize equilibrium reactions involving organic acids, we estimated the amount of dissolved
893 organic carbon and then calculated total organic acid charge (Org_{tot} , moles charge) from total
894 DOC (moles). We converted DOC to Org_{tot} based on a charge density ($m = 0.049 \text{ mol mol}^{-1}$)
895 averaged from the New England water survey.¹⁴ We approximated soil DOC concentrations by
896 assuming that DOC inputs (I_{DOC} , moles $\text{m}^{-2} \text{ y}^{-1}$) are equal to NPP, reasoning that over the long
897 run all plant inputs to soil must be converted to DOC before they are respired or sequestered. We
898 then assumed that DOC decays as a first order process and is lost due to leaching:

$$899 \quad \frac{d\text{DOC}}{dt} = I_{\text{DOC}} - k_{\text{DOC}} * Q_{10}^{((T-293)/10)} * \text{DOC} - \text{DOC} * \text{RC} * F_{\text{mob}} / (V_{\text{fc}} - V_{\text{wp}}) \quad (\text{Equation 14})$$

900 Where k_{DOC} was a decay constant and Q_{10} defined the temperature dependence of DOC decay.
901 We obtained k_{DOC} by taking the geometric mean of previously reported “fast” and “slow” DOC
902 decay constants.¹⁵ Assuming that DOC is maintained at steady state for our purposes, the organic
903 acid concentration (molc l^{-1}) was obtained from the following equation:

$$904 \quad \text{Org}_{\text{tot}} = m * (I_{\text{DOC}}) / (1 + k_{\text{DOC}} * Q_{10}^{((T-293)/10)}) * (1/V) \quad (\text{Equation 15})$$

905 Exchange reactions were specified using the Gaines-Thomas approach. We parameterized
906 cation exchange reactions using an existing compilation,¹⁶ which summarized Gaines-Thomas
907 exchange constants for sand, loess (silt enriched), and clay dominated soils in the Netherlands.
908 As a first order approximation, we assigned exchange constants by calculating the weighted
909 mean of the profile-averaged constants listed in the compilation, with weights given by the sand,
910 silt, and clay fractions obtained from NATSGO.

911 When calibrating the model, we simulated re-equilibration of soil pH with laboratory
912 conditions because in-situ pH and laboratory-measured pH can vary substantially.¹⁷ To do this,
913 we fixed soil water content so that the soil mass to water ratio equaled 1:1, set the temperature to
914 20°C, and adjusted pCO₂ to reflect the ambient atmospheric concentration. Concentrations of
915 conserved ions were adjusted to reflect the change in soil water content during measurement.
916 Charge balance and exchange reactions were solved based on laboratory parameters to yield
917 laboratory pH. In cases where the soil contained calcite, we assumed that calcite could partially
918 buffer pH at the timescale of laboratory measurement. This assumption is supported by a global
919 pH compilation, which shows that pH approximates a calcite-buffered value when carbonates are
920 present in even small amounts.⁵ To represent carbonate buffering in the lab, we fixed the
921 saturation index for calcite so that it would equal its value in the field and then solved for the
922 equilibrium Ca concentration at the laboratory pCO₂ and temperature.

923 **Nutrient budgets**

924 While our main goal was to model pre-agricultural Ca weathering across the USA, we
925 considered nutrient inputs and outputs in modern croplands to assist with model calibration and
926 to help us understand how Ca fluxes have changed over time. Nitrogen had the most complex
927 nutrient budget. To simplify N accounting, we assumed that all reduced N is completely nitrified

928 following DON export; hence all N is treated as NO_3^- .¹⁸ In natural systems, the only N inputs in
929 the model were atmospheric deposition and nitrogen fixation (F_N , $\text{mol m}^{-2} \text{y}^{-1}$), which we
930 modeled as a function of NPP:¹⁹

$$931 \quad F_N = 1.8 * (1 - \exp(-0.003 * \text{NPP})) / 14.01 \quad (\text{Equation 16})$$

932 In addition to leaching of NO_3^- , we considered leaching of organic N, which we assume happens
933 before nitrification. We assigned a molar CN ratio of 20, which is typical for dissolved organic
934 matter,²⁰ and modeled DON export as a function of DOC leaching:

$$935 \quad L_N = N * RC * F_{\text{mob}} / (V_{\text{fc}} - V_{\text{wp}}) + \text{DOC} / \text{CN}_{\text{DOM}} * RC * F_{\text{mob}} / (V_{\text{fc}} - V_{\text{wp}}) \quad (\text{Equation 17})$$

936 Because we fixed the CN ratio for DOM, DON export could exceed inputs, leading to negative
937 NO_3^- concentrations. In these cases, we forced DON export to equal inputs and NO_3^-
938 concentrations equaled zero.

939 In croplands, natural N fixation was set to zero and we considered N inputs from
940 fertilizer, manure, crop N fixation, free living N fixation, and N removal in crop biomass:

$$941 \quad C_N = N_{\text{fert}} + N_{\text{man}} + N_{\text{fix,crop}} + N_{\text{fix,free}} - N_{\text{rem}} \quad (\text{Equation 18})$$

942 The first three of these parameters as well as the N removal rate varied spatially and were taken
943 from a published county-level compilation²¹ whereas free-living N fixation rates were
944 approximated at $0.036 \text{ mol m}^{-2} \text{y}^{-1}$ ^[22] and did not vary spatially. The parameter N_{man} was set
945 equal to 20% of total manure N to account for inefficiency in manure recovery.²³

946 Nitrogen can be lost from soil via ammonia volatilization, NO_x emission, and
947 denitrification to N_2O or N_2 . The processes governing these fluxes are complex and representing

948 them in detail was beyond the scope of our effort. Instead, we manually calibrated a single
949 parameter, r_v , that controlled the N volatilization rate:

$$950 \quad V_N = N/N_{\text{inputs}} * r_v \quad (\text{Equation 19})$$

951 The expression was based on the assumption that N volatilization is proportional to the total
952 available N pool but inversely proportional to N inputs. We reasoned that as N inputs increase,
953 the opportunity for denitrification and ammonia volatilization would be lower because more N
954 would escape the soil before volatilization. This is consistent with the observation that low-input
955 ecosystems volatilize a greater fraction of N than high-input agricultural systems.²⁴ We selected a
956 value of 0.3 y^{-1} for r_v , which ensured plausible nitrate stocks for the top 1 meter of soil: in the
957 range of $100\text{-}200 \text{ kg NO}_3^- \text{-N ha}^{-1}$ in croplands^{25,26} and less than $10 \text{ kg NO}_3^- \text{-N ha}^{-1}$ in forests.²⁷

958 Nitrogen removal in harvest could sometimes exceed N inputs, leading to implausibly
959 low NO_3^- concentrations. At locations where N surplus in croplands was less than $0.1 \text{ mol m}^{-2} \text{ y}^{-1}$
960 ¹, we assumed that imbalances in the N budget were being met by an unknown source (e.g.,
961 decomposition of soil organic matter or higher than 20% manure recoverability). In these cases,
962 we assigned a minimum value of $0.1 \text{ mol m}^{-2} \text{ y}^{-1}$ for the net nitrogen balance before applying
963 losses from NO_3^- leaching and volatilization. This minimum value maintained cropland NO_3^-
964 levels within reported ranges.^{25,26}

965 Cropland C budgets were also adjusted to account for import and export of C in
966 agriculture. We adjusted NPP in croplands to account for removal of crop biomass, which
967 accounts for 43% of cropland NPP.²⁸ We also accounted for C introduced with manure. We
968 assumed a molar C:N ratio of 10 for manure, and used this number to scale manure C based on
969 county-level estimates for manure N.

970 We also considered cropland nutrient budgets for some additional nutrients. For
971 simplicity, we assumed that S and K inputs in fertilizer equaled outputs; hence C_S and C_K were
972 set equal to zero. For Ca and Mg, we accounted for inputs in manure and ag-lime and outputs in
973 crop harvest. Manure inputs were constrained by assigning Ca:N and Mg:N values for manure
974 and scaling Ca and Mg inputs to the manure N application rate. Ca:N and Mg:N for manure were
975 averaged across dairy solids, swine solids, and poultry manure types.²⁹ Similarly, average Ca:N
976 and Mg:N values were assigned for crop biomass using published values for corn and soy,³⁰
977 allowing us to approximate Ca and Mg removal in harvest.

978 We modeled liming rates endogenously as a function of pH. We first aligned county level
979 liming data from 1987^[31] (the most recent available date) with maps of soil pH derived from
980 NATSGO.³² We assigned a pH value to croplands in each county by extracting NATSGO pH
981 values in a 10 km grid across the USA and masking out non-cropland areas using the GFSAD
982 cropland mask.³³ We then calculated the median cropland pH value in each county. This revealed
983 that liming rates vary widely below pH 7, but are low above pH 7. We modeled the maximum
984 rate of lime addition as a function of pH using a sigmoid function:

$$985 \text{Lime}_{\max} = p_1 * (1 - \exp(-10^{-\text{pH}_{\text{lab}}/p_2})^{p_3}) \quad (\text{Equation 20})$$

986 Where Lime_{\max} was the maximum observed liming rate ($\text{t ha}^{-1} \text{y}^{-1}$) p_1 , p_2 , and p_3 were
987 empirical constants and pH_{lab} was the laboratory-measured soil pH assumed equal to the median
988 pH from NATSGO. We fit this function to the condition 90th percentiles of the data obtained in
989 0.5 pH-unit bins using the R function “nls”. The parameters received estimated values of $p_1 =$
990 0.424 , $p_2 = 1.42 * 10^{-7}$, and $p_3 = 1.13$.

991 Below the maximum liming rate, we assumed that farmers add enough lime to neutralize
992 acidity from fertilizer and replace Ca and Mg lost in crop biomass. Consequently, the main effect
993 of liming in the model was to maintain soil pH at the same level it would have attained under
994 unfarmed conditions. We made this assumption because it was a reasonable compromise between
995 two extreme alternatives: (1) assuming that farmers generally add lime aggressively to raise their
996 soil pH to agronomically optimal levels; or (2) farmers generally do not add enough lime to
997 maintain soil pH, and croplands are broadly acidified compared to unfarmed baseline conditions.
998 To estimate the liming rate, we first ran the model without agricultural influence, which yielded
999 the target pH value, pH_{target} . We then modeled lime addition as a function of pH_{lab} that increases
1000 steeply towards $Lime_{max}$ at pH_{target} :

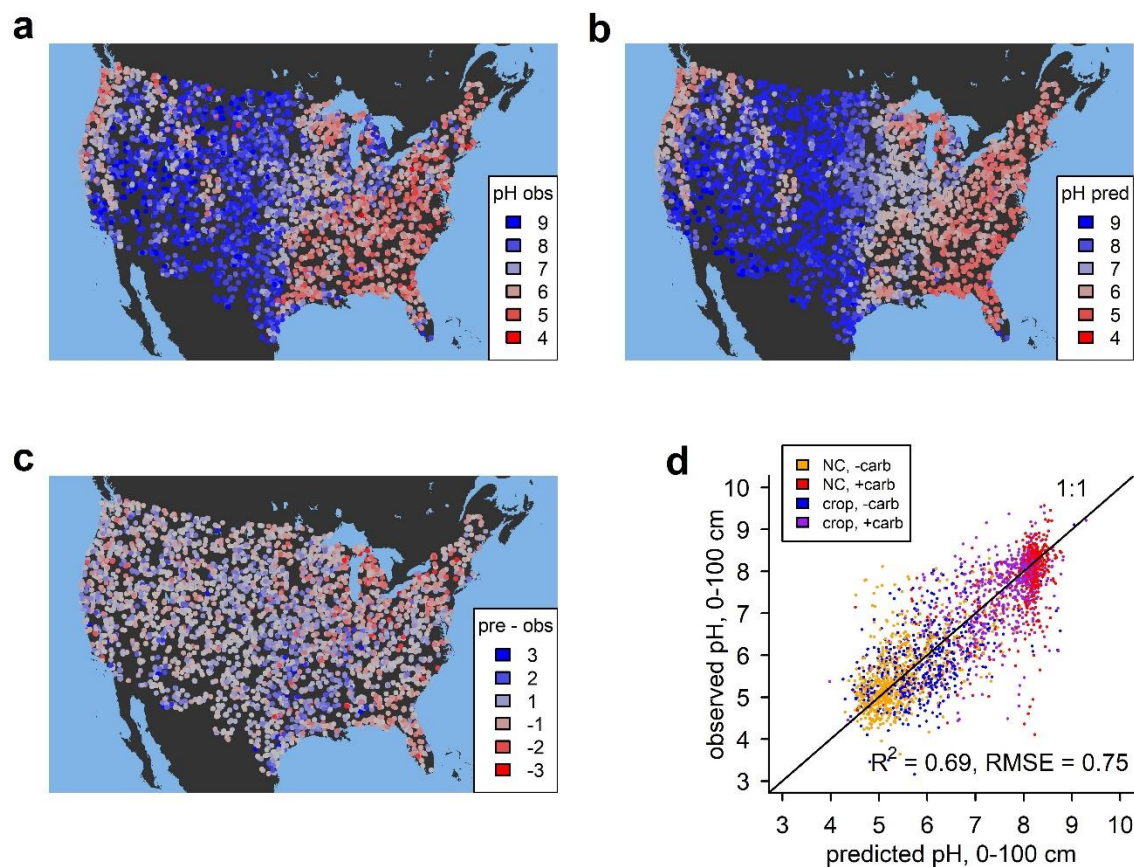
$$1001 \quad Lime_{tot} = Lime_{max} * (1 - \exp(-10^{-pH_{lab}} / 10^{-pH_{target}})^{20}) \quad \text{Equation 21}$$

1002 Applying this equation required approximating pH_{lab} because the model was designed to
1003 calculate the in-situ field pH, while laboratory pH was estimated as a post-processing step at
1004 some computational cost. To address this, we derived empirical linear relationships between the
1005 in-situ pH and the laboratory pH prior to running cropland simulations, with a separate
1006 relationship fitted for carbonate-buffered and carbonate free soils. These regressions explained
1007 >90% of the variation in pH_{lab} and could be used to solve Equation 21 without explicitly
1008 estimating this quantity at every model iteration, speeding up computations substantially.

1009 After applying Equation 21, we partitioned lime added into calcitic and dolomitic
1010 components. In general, crop Mg removal exceeded inputs, and so we satisfied Mg demand first.
1011 Mg demand ($\text{mol m}^{-2} \text{y}^{-1}$) was set equal to the cropland partial Mg budget (crop removal –
1012 manure inputs) where removal exceeded inputs and set to zero elsewhere. Dolomitic lime
1013 addition ($\text{mol m}^{-2} \text{y}^{-1}$) was then set to equal to Mg demand. Where Mg demand could not be met

1014 because the mass of dolomite added exceeded Lime_{max} , the cropland Mg budget was set equal to
1015 zero and it was assumed the Mg came from other unknown sources. Calcitic lime addition was
1016 calculated as the difference between the mass of dolomite added and Lime_{tot} . Ca and Mg added
1017 in lime were obtained from dolomitic and calcitic lime based on the chemical formulae for
1018 calcite and dolomite (Table S6).

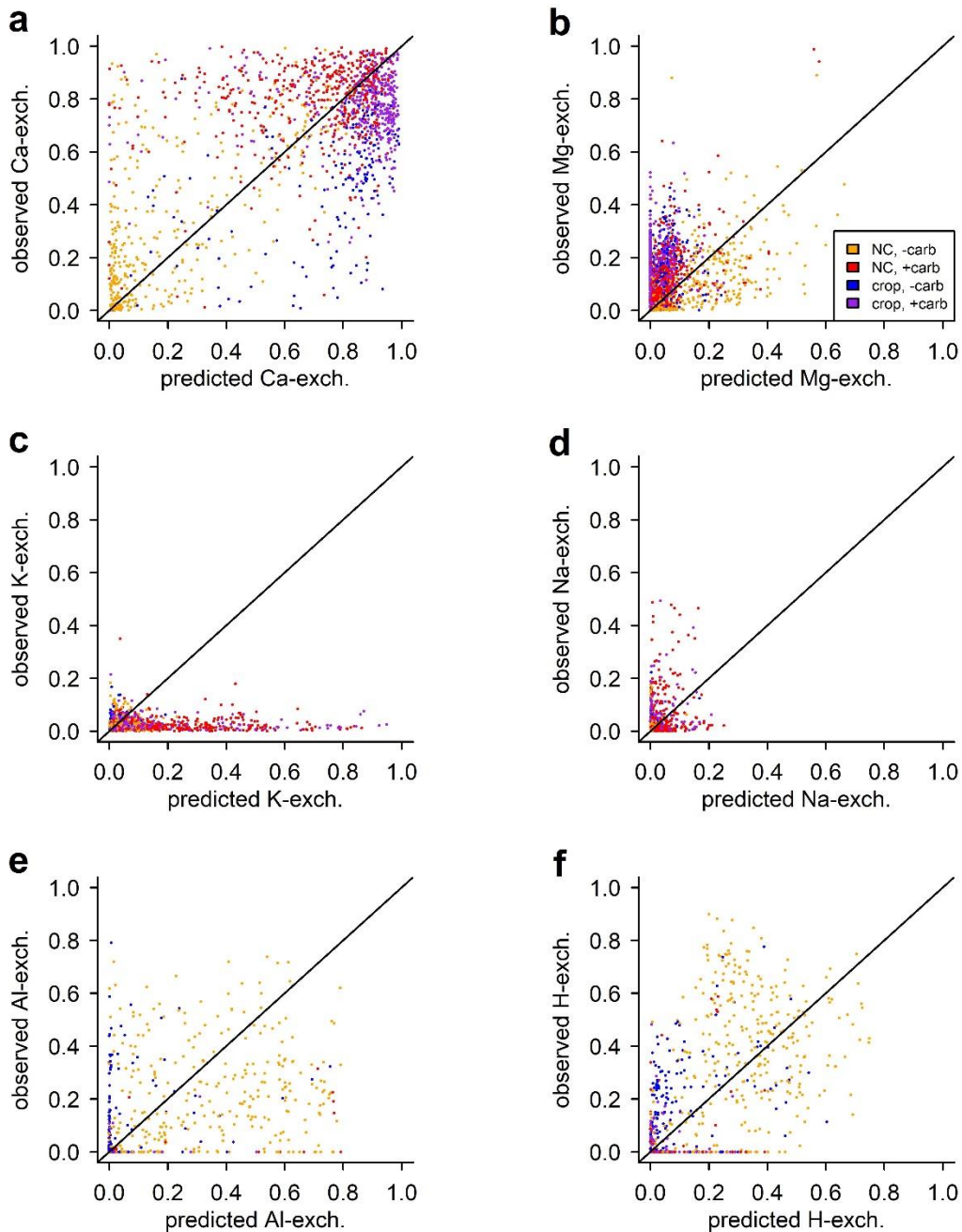
1019



1020

1021 **Figure S1. Model performance matching soil pH.** (a) shows observed depth-weighted average
1022 soil pH of the top 100 cm at 4,247 unique locations used for model training and validation. (b)
1023 shows pH simulated by the calibrated model at the same locations, and (c) shows the model
1024 residuals (predicted – observed pH). (d) shows a plot of predicted versus observed pH, with
1025 colors representing different combinations of land use and soil carbonate status (NC, -carb =
1026 non-cropland, carbonate free; NC, +carb = non-cropland, carbonates present; crop, -carb =
1027 cropland, carbonate free; crop, +carb = cropland, carbonates present). RMSE is the root mean
1028 squared error.

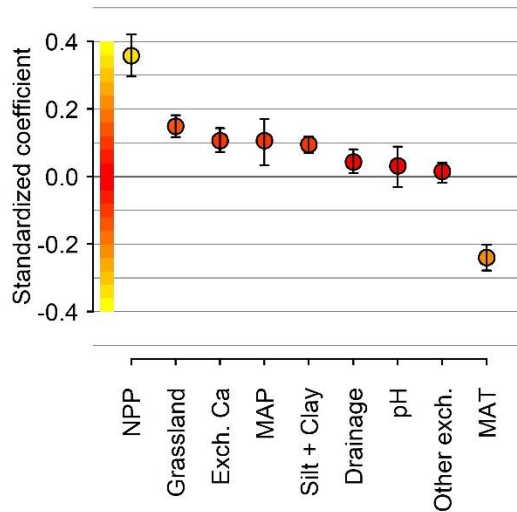
1029



1030

1031 **Figure S2. Model performance for exchangeable ions.** (a) – (f) show predicted versus
 1032 observed exchange fractions for Ca, Mg, K, Na, Al, and H⁺. Observed values represent depth-
 1033 weighted averages to 100 cm taken from the NCSS database³⁵ (n = 2,563 unique profiles).
 1034 Values are normalized by total cation exchange capacity (moles cation charge / CEC). Colors
 1035 represent different combinations of land use and soil carbonate status (NC, -carb = non-cropland,
 1036 carbonate free; NC, +carb = non-cropland, carbonates present; crop, -carb = cropland, carbonate
 1037 free; crop, +carb = cropland, carbonates present). Diagonal lines show the 1:1 relationship.

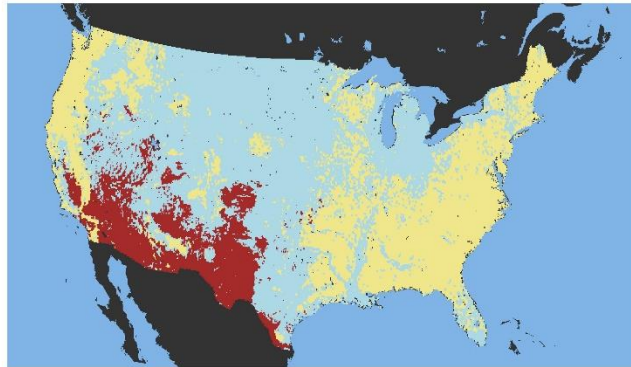
1038



1039

1040 **Figure S3. Controls on Mollisol distribution and A-horizon soil organic carbon stocks in the**
 1041 **USA with alternative predictors.** Standardized regression coefficients were derived from a
 1042 multivariate linear regression model, where A-horizon organic carbon stocks were predicted as a
 1043 function of the eight variables listed on the horizontal axis. In (a) exchangeable Ca fraction was
 1044 included in the regression rather than base saturation as in the main text. In (b) cation exchange
 1045 capacity was corrected for the contribution from soil organic matter prior to calculating
 1046 exchangeable ion pools. In both panels, whiskers show 95% confidence intervals derived from a
 1047 spatial blocked bootstrapping procedure (see Methods). The absolute value of each regression
 1048 coefficient is an index of how strongly related each variable is to the response variable, and is
 1049 shown with a relative color scale: yellow = maximum, red = zero. Abbreviations: NPP = net
 1050 primary productivity, MAT = mean annual soil temperature, MAP = mean annual precipitation,
 1051 Exch. Ca = total exchangeable Ca, Other exch. = sum of non-Ca exchangeable ions.

1052



Carbonate Ca source/sink status

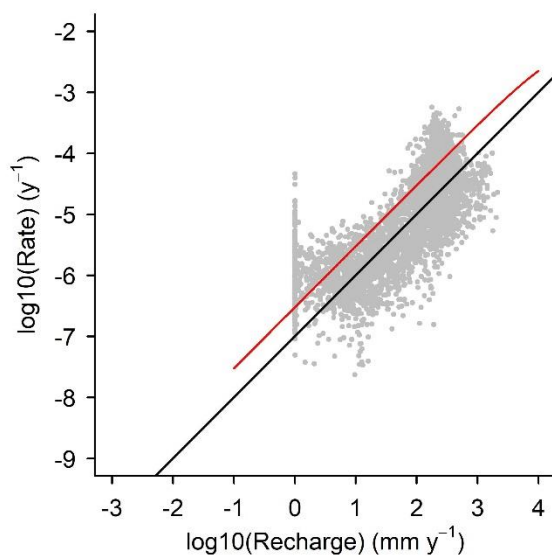
■ source ■ absent ■ sink

1053

1054 **Figure S4. Modeled carbonate source / sink status.** Data show model simulations under
1055 preindustrial late Holocene conditions. Areas mapped in yellow are carbonate free, areas mapped
1056 in blue are releasing Ca via carbonate weathering, and areas mapped in red are a sink for Ca via
1057 carbonate formation.

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1061 **Figure S5. Modeled plagioclase feldspar weathering rate versus recharge.** Gray points show
1062 modeled feldspar weathering rates normalized by the feldspar stock versus the recharge
1063 parameter. The red line shows the non-linear fit to a compilation of field and lab weathering rates
1064 from Maher 2010,^[3] and the black line shows a fit to the same compilation from Yu and Hunt
1065 2018^[4].

1066

1067

	R²	RMSE
Ca ²⁺	0.40	0.26
Mg ²⁺	0.06	0.15
Na ⁺	0.08	0.06
K ⁺	0	0.18
Al ³⁺	0.30	0.15
H ⁺	0.51	0.14
All	0.66	0.17

1068

1069 **Table S1. Validation statistics for exchangeable ion fractions.** R² values are derived by
1070 regressing observations on predictions; root mean squared error (RMSE) was calculated as the
1071 square root of the mean of the squared residuals (geochemical model predictions – observations).
1072 Statistics for all cations were obtained by treating all observed and predicted cation fractions as
1073 independent values and pooling them. Observed values represent depth-weighted averages to 100
1074 cm taken from the NCSS database³⁵ (n = 2,563 unique profiles; 3,423 total including repeats
1075 from spatially weighted resampling).

1076

1077

	value	CI
intercept	-0.05	[-0.065, -0.036]
grassland	0.139	[0.106, 0.171]
exch. Ca	0.144	[0.109, 0.178]
other exch.	0.011	[-0.018, 0.039]
MAT	-0.229	[-0.265, -0.188]
silt + clay	0.032	[0.000, 0.065]
Drainage	0.088	[0.062, 0.111]
log NPP	0.347	[0.289, 0.411]
MAP	0.105	[0.030, 0.168]
pH	0.009	[-0.055, 0.064]

1078

1079 **Table S2. Results of multiple regression analysis for A-horizon SOC.** Statistics are derived
1080 from a multivariate logistic regression, where log-transformed A-horizon organic carbon stocks
1081 were modeled as a function of potential grassland and savanna vegetation (grassland),
1082 exchangeable Ca (Ca exch.), non-Ca exchangeable ions (other exch.), soil silt + clay content, net
1083 primary productivity (NPP), USDA drainage class (drainage), Mean annual soil temperature
1084 (MAT), and mean annual precipitation (MAP). Continuous predictors were scaled by their
1085 standard deviations prior to fitting, whereas the binary predictor (grassland) was scaled by two
1086 times its standard deviation. Model $R^2 = 0.30$ and residual standard error was 0.4188. Confidence
1087 intervals were derived from a spatially blocked bootstrapping procedure (see Methods).

Ion or algebraic constraint	Equation
Ca ²⁺	$dCa/dt = D_{Ca} + A_{Ca} + C_{Ca} + R_{Cc,Ca} + R_{Do,Ca} + R_{Pl,Ca} + R_{Hb,Ca} + R_{Py,Ca} - L_{Ca}$
Mg ²⁺	$dMg/dt = D_{Mg} + A_{Mg} + C_{Mg} + R_{Do,Mg} + R_{Hb,Mg} + R_{Py,Mg} + R_{Cl,Mg} - L_{Mg}$
Na ⁺	$dNa/dt = D_{Na} + R_{Pl,Na} - L_{Na}$
K ⁺	$dK/dt = D_K + C_K + M_K + R_{Ks,K} + R_{Il,K} - L_K$
NO ₃ ⁻	$dN/dt = D_N + C_N + F_N - V_N - L_N$
SO ₄ ²⁻	$dS/dt = D_S + C_S - L_S$
Cl ⁻	$dCl/dt = D_{Cl} - L_{Cl}$
Charge Balance	$0 = (2[Ca^{2+}] + 2[Mg^{2+}] + [K^+] + [Na^+] + 3[Al^{3+}] + 2[Al(OH)^{2+}] + [Al(OH)_2^+] + 2[AlHOrg^{2+}] + [AlH_2Org^+] + [H^+]) - ([OH^-] + [HCO_3^-] + 2[CO_3^{2-}] + [H_2Org^-] + 2[HOrg^{2-}] + 3[Org^{3-}] + [Al(OH)_4^-] + 2[SO_4^{2-}] + [NO_3^-] + [Cl^-])$
Exchange	$1 = fCa + fMg + fNa + fK + fAl + fH$

1088 **Table S3 Governing equations.** Capital letters indicate rates: D = deposition (wet + dry); A =
1089 agricultural liming, C = cropland nutrient budget (inputs – uptake); R = weathering; L =
1090 leaching; F = fixation; V = volatilization. Weathering rates (mol mineral y⁻¹) were multiplied by
1091 the molar concentration of each element the mineral to yield the flux of each element from the
1092 mineral; this is indicated in the subscripts, with the mineral listed first and then the
1093 corresponding element. Minerals: Cc = calcite; Do = dolomite; Pl = plagioclase; Hb =
1094 hornblende; Py = pyroxene; Cl = chlorite; Ks = K-feldspar; Il = illite.

1095

Mineral	Abbr.	Type	Formula	Density
Plagioclase	Pl	tectosilicate	$\text{Na}_{(1-f_{\text{An}})}\text{Ca}_{f_{\text{An}}}\text{Al}_{(1+f_{\text{An}})}\text{Si}_{(3-f_{\text{An}})}\text{O}_8$	$2.75f_{\text{An}} + 2.625(1-f_{\text{An}})$
K-feldspar	Ks	tectosilicate	KAlSi_3O_8	2.59
Pyroxene	Py	inosilicate	$\text{MgCa}(\text{SiO}_3)_2$	3.3
Hornblende	Hb	inosilicate	$\text{Ca}_2(\text{Mg}_2\text{Fe}_2\text{Al})\text{Si}_7\text{AlO}_{22}(\text{OH})_2$	3.1735
Chlorite	Cl	phyllosilicate	$\text{Mg}_5\text{Al}_2\text{Si}_3\text{O}_{18}\text{H}_8$	2.915
Illite	Il	phyllosilicate	$\text{K}(\text{Al}_2)(\text{Si}_3\text{Al})\text{O}_{10}(\text{OH})_2$	2.795
Calcite	Cc	carbonate	CaCO_3	2.7102
Dolomite	Do	carbonate	$\text{CaMg}(\text{CO}_3)_2$	2.85

1096 **Table S4 Mineral properties.** f_{An} = anorthite molar fraction. Densities are midpoints of reported
1097 ranges from Mindat.org.

1098

1099

Parameter	Description	Value	Units	Source
E _{asil}	Silicate weathering activation energy	74	kJ mol ⁻¹ K ⁻¹	²
H _r	Reference [H ⁺] value	10 ⁻⁵	mol l ⁻¹	This study
n _H	Silicate weathering reaction order for H ⁺	0.6667	-	This study
RRPl	Relative reaction rate, plagioclase	1	-	¹
RRKs	Relative reaction rate, K-feldspar	0.63	-	¹
RRHb	Relative reaction rate, hornblende	0.25	-	¹
RRPy	Relative reaction rate, pyroxene	1	-	This study
log(A _{acid,Cc})	Acid mechanism preexponential factor, calcite	-0.3	mol m ⁻² s ⁻¹	⁶
log(A _{neut,Cc})	Neutral mechanism preexponential factor, calcite	-5.81	mol m ⁻² s ⁻¹	⁶
log(A _{CO₂,Cc})	CO ₂ mechanism preexponential factor, calcite	-3.48	mol m ⁻² s ⁻¹	⁶
log(A _{acid,Do})	Acid mechanism preexponential factor, dolomite	-3.19	mol m ⁻² s ⁻¹	⁶
log(A _{neut,Do})	Neutral mechanism preexponential factor, dolomite	-7.53	mol m ⁻² s ⁻¹	⁶
log(A _{CO₂,Do})	CO ₂ mechanism preexponential factor, dolomite	-5.11	mol m ⁻² s ⁻¹	⁶
E _{aacid,cc}	Acid mechanism activation energy, calcite	14.4	kJ mol ⁻¹ K ⁻¹	⁶
E _{a_{neut,cc}}	Neutral mechanism activation energy, calcite	23.5	kJ mol ⁻¹ K ⁻¹	⁶
E _{aCO₂,cc}	CO ₂ mechanism activation energy, calcite	35.4	kJ mol ⁻¹ K ⁻¹	⁶
E _{aacid,do}	Acid mechanism activation energy, dolomite	36.1	kJ mol ⁻¹ K ⁻¹	⁶
E _{a_{neut,do}}	Neutral mechanism activation energy, dolomite	52.2	kJ mol ⁻¹ K ⁻¹	⁶
E _{aCO₂,do}	CO ₂ mechanism activation energy, dolomite	34.8	kJ mol ⁻¹ K ⁻¹	⁶
n _{H_{Cc}}	Reaction order for H ⁺ , calcite	1	-	⁶
n _{CO₂,Cc}	Reaction order for CO ₂ , calcite	1	-	⁶
n _{H_{Do}}	Reaction order for H ⁺ , dolomite	0.5	-	⁶
n _{CO₂,Do}	Reaction order for CO ₂ , dolomite	0.5	-	⁶

1100 **Table S5 Weathering rate parameters**

1101

Reaction	ΔS (kJ K ⁻¹ mol ⁻¹)	ΔH (kJ mol ⁻¹)	logK	source
$\text{CO}_2(\text{g}) \leftrightarrow \text{CO}_2(\text{aq})$	-0.09617	-20.28822		8,9
$\text{CO}_2(\text{aq}) + \text{H}_2\text{O} \leftrightarrow \text{HCO}_3^- + \text{H}^+$	-0.08905	9.701672		8,9
$\text{HCO}_3^- \leftrightarrow \text{CO}_3^{2-} + \text{H}^+$	-0.14845	14.69839		8,9
$\text{H}_2\text{O} \leftrightarrow \text{OH}^- + \text{H}^+$	-0.08064	55.81354		8,9
$\text{Al}(\text{OH})_3(\text{s}) \leftrightarrow \text{Al}(\text{OH})_3(\text{aq})$	-0.00909	50.45804		8,9
$\text{Al}(\text{OH})_3(\text{aq}) + 3\text{H}^+ \leftrightarrow \text{Al}^{3+} + 3\text{H}_2\text{O}$	-0.18933	-153.61150		8,9
$\text{Al}(\text{OH})_3(\text{aq}) + 2\text{H}^+ \leftrightarrow \text{Al}(\text{OH})_2^+ + 2\text{H}_2\text{O}$	-0.10063	-98.86893		8,9
$\text{Al}(\text{OH})_3(\text{aq}) + \text{H}^+ \leftrightarrow \text{Al}(\text{OH})_2^{2+} + \text{H}_2\text{O}$	-0.01697	-39.97106		8,9
$\text{Al}(\text{OH})_3(\text{aq}) + \text{H}_2\text{O} \leftrightarrow \text{Al}(\text{OH})_4^- + \text{H}^+$	-0.02573	25.43200		8,9
$\text{CaCO}_3(\text{s}) \leftrightarrow \text{Ca}^{2+} + \text{CO}_3^{2-}$	-0.19821	-11.49904		8,9
$\text{CaMgC}_2\text{O}_6(\text{s}) \leftrightarrow \text{Ca}^{2+} + \text{Mg}^{2+} + 2\text{CO}_3^{2-}$	-0.44944	-34.26448		8,9
$(1/5)\text{Mg}_5\text{Al}_2\text{Si}_3\text{O}_{18}\text{H}_8(\text{s}) + 2\text{H}^+ \leftrightarrow (2/5)\text{Al}(\text{OH})_3(\text{aq}) + \text{Mg}^{2+} + (3/5)\text{SiO}_2(\text{aq}) + (6/5)\text{H}_2\text{O}$	-0.072267	-50.73344		8,9
$\text{KAl}_3\text{Si}_3\text{O}_{12}\text{H}_2(\text{s}) + \text{H}^+ + 3\text{H}_2\text{O} \leftrightarrow 3\text{Al}(\text{OH})_3(\text{aq}) + \text{K}^+ + 3\text{SiO}_2(\text{aq})$	-0.00210	227.67055		8,9
$\text{SiO}_2(\text{amorph}) \leftrightarrow \text{SiO}_2(\text{aq})$	0.01531	20.05391		8,9
$\text{H}_3\text{Org} \leftrightarrow \text{H}_2\text{Org}^- + \text{H}^+$			-2.653	14
$\text{H}_2\text{Org}^- \leftrightarrow \text{HOrg}^{2-} + \text{H}^+$			-6.233	14
$\text{HOrg}^{2-} \leftrightarrow \text{Org}^{3-} + \text{H}^+$			-7.467	14
$\text{AlH}_2\text{Org}^{2+} \leftrightarrow \text{H}^+ + \text{AlHOrg}^+$			-4.963	14
$\text{AlHOrg}^+ \leftrightarrow \text{H}^+ + \text{AlOrg}$			-4.040	14
$\text{AlOrg} \leftrightarrow \text{Al}^{3+} + \text{Org}^{3-}$			-10.020	14
$3\text{Ca-X} + 2\text{Al}^{3+} \leftrightarrow 2\text{Al-X} + 3\text{Ca}^{2+}$			2.026 (s); 1.195 (lo); 0.106 (cl)	16
$3\text{Mg-X} + 2\text{Al}^{3+} \leftrightarrow 2\text{Al-X} + 3\text{Mg}^{2+}$			2.811 (s); 1.244 (lo); 0.599 (cl)	16
$3\text{Na-X} + \text{Al}^{3+} \leftrightarrow \text{Al-X} + 3\text{Na}^+$			1.811 (s); 0.646 (lo); 1.045 (cl)	16
$3\text{K-X} + \text{Al}^{3+} \leftrightarrow \text{Al-X} + 3\text{K}^+$			-0.917 (s); -2.413 (lo); -3.561 (cl)	16
$3\text{H-X} + \text{Al}^{3+} \leftrightarrow \text{Al-X} + 3\text{H}^+$			-6.924 (s); -7.532 (lo); -9.923 (cl)	16

1102 **Table S6 Equilibrium reactions and thermodynamic parameters.** For exchange reactions
1103 logK values are for sand, loess, and clay respectively based on reference [9].

1104

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