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Seismic observation of tsunami at island broadband stations

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Key Points:

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- For quantification of seismic observation of tsunami, we evaluate scattering of an incident tsunami for an axisymmetric structure.

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- Ground deformation due to the tsunami loading is modeled using static Green's functions.

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- By fitting the modeled displacement to observed seismic data, the incident tsunami is inferred from the seismic observation.

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Abstract

16
17 Previous studies have reported seismic observations of tsunami recorded at island broad-
18 band stations. Coastal loading by the tsunami can explain them. For further quantifi-
19 cation, we model tsunami propagation assuming an axisymmetric structure: a conical
20 island with a flat ocean floor. The total tsunami wavefield can be represented by super-
21 position between an incident tsunami wave and the scattering. The ground deformation
22 due to the total tsunami wavefield at the center is calculated using static Green's func-
23 tions for elastic half-space with a first-order correction for bathymetry. By fitting the
24 modeled displacement to observed seismic data, we can infer the incident tsunami wave,
25 which can be interpreted as the virtual tsunami amplitude without the conical island.
26 First, we apply this new method to three components of seismic data at a volcano is-
27 land, Aogashima, for the 2015 Torishima-Oki tsunami earthquake. The estimated tsunami
28 amplitude from the vertical component is consistent with the offshore array observation
29 of absolute pressure gauges close to the island (1.5–20 mHz). The estimated incident az-
30 imuth from the three components is also consistent with ray theory. Second, we apply
31 this method to seismic data at four island broadband stations in the Indian ocean for
32 the 2010 Mentawai tsunami earthquake in Indonesia. Despite the limited observed fre-
33 quency range from 0.5–2.0 mHz, the amplitudes and incident azimuths are consistent with
34 past studies. These observations can complement offshore tsunami observations. More-
35 over, this method is applicable not only for a tsunami but also for background ocean in-
36 fragravity wave activity.

1 Introduction

38 Crustal deformation beneath the ocean due to a massive shallow earthquake gener-
39 erates tsunami (e.g. Satake, 2015). Physically, these are also known as ocean infragrav-
40 ity waves or ocean external gravity waves. Although tsunami amplitudes are usually small
41 in the deep ocean, they increase drastically as tsunami approaches the coast. Such large
42 amplitudes cause severe damage in coastal areas. Understanding tsunami propagation
43 is important for effectively evaluating the risk. Tsunami observations are also crucial for
44 characterizing the source processes of an earthquake (e.g. Satake, Fujii, Harada, & Namegaya,
45 2013). Observations by offshore ocean bottom pressure gauges (*e.g.* Deep-ocean Assess-
46 ment and Reporting of Tsunamis (DART) (Bernard & Meinig, 2011)) are typically used
47 for source inversion because of simple wave propagation in the pelagic environment.

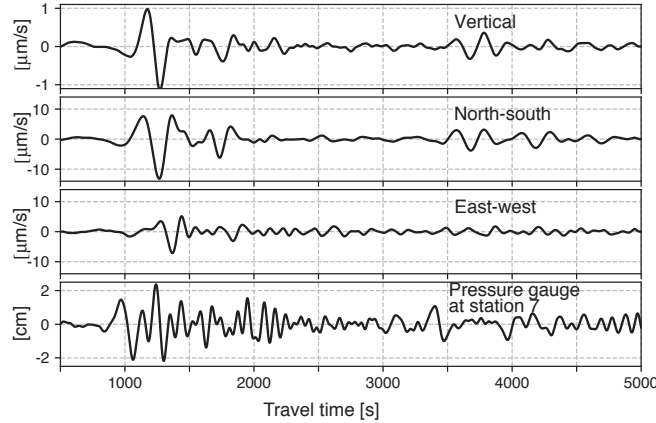


Figure 1. The upper three records show 3 components of the ground velocity recorded by a broadband seismometer at Aogashima (N.AOGF). The lowest record shows tsunami height at an offshore pressure gauge (station 7 shown in Figure 2). All the records are bandpass-filtered from 2 to 20 mHz.

48 Loading on the seafloor by tsunami causes ground deformation of the ground, and
 49 vice versa, which is detectable by land-based broadband seismic stations. For example,
 50 when the 2010 Maule earthquake hit Chile, a high-density tiltmeter network in Japan
 51 recorded ground tilt motions with a typical period of approximately one hour over a broad
 52 inland area facing the Pacific coast (Kimura, Tanaka, & Saito, 2013). Simple 2-D mod-
 53 eling for the deformation induced by the Chilean tsunami explained the observed tilt mo-
 54 tions in the Japanese island arc (Kimura et al., 2013). During the 2004 Sumatra–Andaman
 55 earthquake, tilt motions from 0.3–0.6 mHz were recorded by a broadband seismometer
 56 at Showa station at the mouth of a bay in Antarctica (Nawa et al., 2007), and tilt mo-
 57 tions with typical periods of approximately 1000 s were recorded by broadband seismome-
 58 ters at stations on islands in the Indian ocean (Yuan, Kind, & Pedersen, 2005). Although
 59 the order of observed amplitudes can be explained by tilt motions caused by tsunami load-
 60 ing, the mechanism is not yet fully understood.

61 Figure 1 shows an example of broadband seismic records at a volcano island, Ao-
 62 gashima, associated with tsunami when the 2015 Torishima earthquake (see section 5
 63 for details). The observed larger amplitudes in horizontal components suggest the effect
 64 of tilt motions is dominant. All the seismic records lack the higher-frequency content.

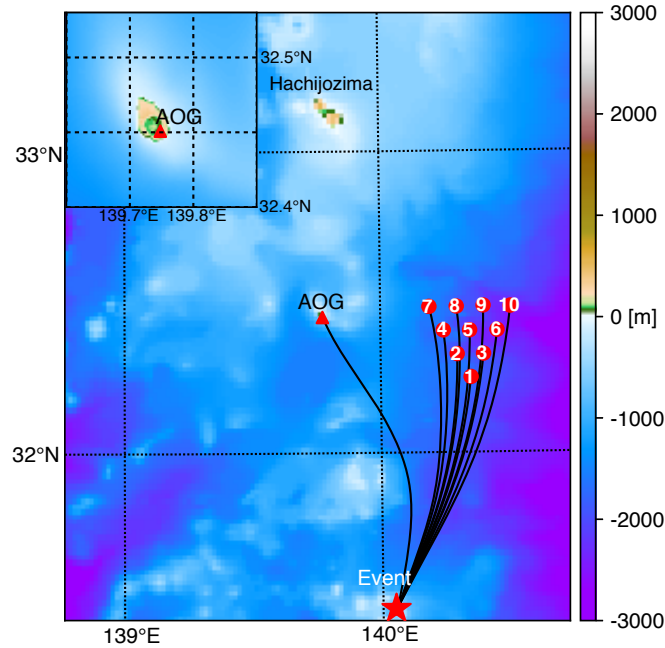


Figure 2. Station distribution of an array of 10 offshore pressure gauges (triangles). The inset shows an enlarged map of Aogashima (AOG). The star symbol shows the hypocenter of the earthquake near Torishima on May 2, 2015. At approximately 33.1°N , Hachijojima north to Aogashima is also shown. The station numbers are shown in red circles.

65 To quantify ground motions at islands, we model the sloping effects in a semi-analytic
 66 manner for an axisymmetric conical island with a flat ocean floor (Fujima & Goto, 1994;
 67 K anođlu & Synolakis, 1998; Smith & Sprinks, 1975). Although the model is simple, it
 68 can express the complex wave propagation close to the shoreline. This simple model can
 69 explain the spatial pattern of coastal tsunami amplification around islands.

70 In section 2, we present a theory of tsunami propagation when an arbitrary tsunami
 71 wavefield enters a conical island. In section 3, we then estimate the ground deformation
 72 at the center of the island due to tsunami loading, which can be related to the incident
 73 tsunami wavefield. In section 4, using the axisymmetric assumption, we propose a new
 74 technique for estimating virtual tsunami amplitude without a conical island, which could
 75 be a proxy for offshore tsunami amplitude. In section 5, this method is applied to two
 76 examples: the 2015 Torishima earthquake in Japan and the 2010 Mentawai tsunami earth-
 77 quake in Indonesia.

2 Theory of tsunami propagation for a conical island with a flat ocean floor

In this study, we consider scattering of tsunami around an axisymmetric conical island. For simplicity, we assume that the tsunami can be approximated as a linear long-wave because dispersion effects should be less important than topographic effects in this case. Following (Gill, 1982), we consider shallow-water equations derived using the hydrostatic approximation. The displacement amplitude of the sea surface disturbance $\eta(r, \theta; t)$ satisfies the following governing equation in time domain:

$$\frac{\partial^2 \eta(r, \theta; t)}{\partial t^2} = g_0 \nabla_h [D(r) \nabla_h \eta(r, \theta; \omega)], \quad (1)$$

where r is the radius, θ is the azimuth (Figure 3), g_0 is the gravity constant, ∇_h represents the spatial gradient in 2-D, and $D(r)$ is an axisymmetric water depth given by

$$D(r) = \begin{cases} 0 & \text{if } r < r_0, \\ m(r - r_0) & \text{if } r_0 \leq r < r_1, \\ D_0 & \text{if } r_1 \leq r, \end{cases} \quad (2)$$

where r_1 is the radius of the root of the island, r_0 is the radius of the island, D_0 is the sea surface height of the flat ocean from the sea bottom, and m is the slope given by $D_0/(r_1 - r_0)$. The frequency-domain representation $\eta(r, \theta; \omega)$ satisfies the following equation:

$$-\omega^2 \eta(r, \theta; \omega) = g_0 D(r) \nabla_h^2 \eta(r, \theta; \omega) + g_0 \nabla_h D(r) \cdot \nabla_h \eta(r, \theta; \omega), \quad (3)$$

where ω is the angular frequency.

We note that, for negative frequency, $\eta(r, \theta, -\omega)$ is defined as the complex conjugate by $\eta^*(r, \theta; \omega)$ because the time domain representation should be a real function. A Fourier component at a negative frequency $-\omega$ is, thus, defined by the complex conjugate of that at a positive frequency ω . Here, we use the Fourier convention:

$$F(\omega) = \int_{-\infty}^{\infty} f(t) e^{-i\omega t} dt, \quad (4)$$

where f is an arbitrary function as a function of time, t , and F is its Fourier component.

At high frequency, tsunami velocity $\sqrt{g_0 D(r)}$ near the coast decreases towards zero because the second term of the right-hand side becomes negligible. The coastal low-velocity region traps tsunami energy, which enhances tsunami run-up height (e.g. Liu, Cho, Briggs, Lu, & Synolakis, 1995; Satake, 2015). Zero velocity at the coast makes the governing equation singular. By using the axisymmetric approximation, however, an analytic evaluation of the singularity becomes possible (Fujima & Goto, 1994).

107 Because the governing equation is axisymmetric, tsunami wavefield $\eta(r, \theta; \omega)$ can
 108 be expanded by a Fourier series with respect to the azimuth, in general, as:

$$109 \quad \eta(r, \theta; \omega) = \frac{1}{2} \phi_0(r; \omega) \\
 110 \quad + \sum_{n=1}^{\infty} [\phi_n(r; \omega) \cos(n\theta) + \phi_{-n}(r; \omega) \sin(n\theta)], \quad (5) \\
 111$$

112 where $\phi_n(r; \omega)$ is the radial function of azimuthal order n . We assume that an arbitrary
 113 incident tsunami wave $\eta^{in}(r, \theta; \omega)$ enters the island and is scattered in the sloping bot-
 114 tom (region II in Figure 3); thus, the total wavefield $\eta(r, \theta; \omega)$ in the flat ocean (region
 115 I in Figure 3) can be represented by superposition between the incident wave and the
 116 scattered wave (Fujima & Goto, 1994; Kânoğlu & Synolakis, 1998; Smith & Sprinks, 1975).
 117 In the following subsections, we evaluate $\phi_n(r; \omega)$ by considering the scattering for an
 118 arbitrary incident wave field using a semi-analytic method (Fujima & Goto, 1994; Kânoğlu
 119 & Synolakis, 1998).

120 2.1 Incident tsunami wavefield

121 First, let us consider an arbitrary incident arbitrary wavefield $\eta^{in}(r, \theta; \omega)$ in a flat
 122 ocean without the conical island virtually. The incident wavefield in a flat ocean η^{in} can
 123 be expanded by a Fourier series with respect to the azimuth and Bessel functions of the
 124 first kind with respect to the radial direction as follows:

$$125 \quad \eta^{in}(r, \theta; \omega) = \frac{1}{2} \zeta_0^{in}(\omega) J_0(k_0 r) \\
 126 \quad + \sum_{n=1}^{\infty} [\zeta_n^{in}(\omega) \cos(n\theta) + \zeta_{-n}^{in}(\omega) \sin(n\theta)] J_n(k_0 r), \quad (6) \\
 127$$

128 where J_n is the n th order Bessel function of the first kind, k_0 is the wavenumber given
 129 by $\omega/\sqrt{g_0 D_0}$, and $\zeta_n^{in}(\omega)$ is the coefficient.

130 2.2 Wave scattering by a conical island in a flat ocean (I)

131 The incident wave $\eta^{in}(r, \theta; \omega)$ enters the conical island area and the scattered wave
 132 amplitude is represented by $\eta^{sc}(r, \theta; \omega)$. The total tsunami amplitude η can be written
 133 as

$$134 \quad \eta(r, \theta; \omega) = \eta^{in}(r, \theta; \omega) + \eta^{sc}(r, \theta; \omega). \quad (7)$$

135 Let us consider the scattered wavefield $\eta^{sc}(r, \theta; \omega)$ for the flat ocean floor (I) (see
 136 Figure 3). The scattered wavefield $\eta^{sc}(r, \theta; \omega)$ can be represented by an outgoing wave

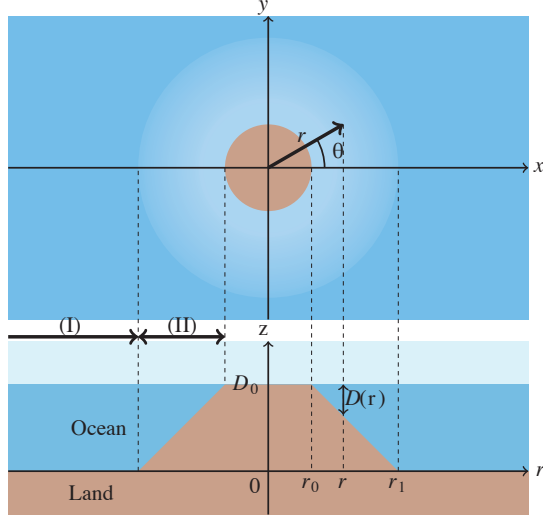


Figure 3. Schematic figure of the conical island. The upper panel shows the plan view of the island, and the lower panel shows the cross-section. The radius on the surface is r_0 and that of the base is r_1 .

137 in the flat ocean according to the causality of the scattered wave. For a positive angular
 138 frequency ω , the scattered wavefield can be written as

$$\begin{aligned}
 139 \quad \eta^{sc}(r, \theta; \omega) &= \frac{1}{2} B_0(\omega) \zeta_0^{in}(\omega) H_0^{(2)}(k_0 r) \\
 140 \quad &+ \sum_{n=1}^{\infty} [B_n(\omega) \zeta_n^{in}(\omega) \cos(n\theta) + B_{-n}(\omega) \zeta_{-n}^{in}(\omega) \sin(n\theta)] H_n^{(2)}(k_0 r), \quad (8) \\
 141
 \end{aligned}$$

142 where $H_n^{(2)}(\omega)$ is the n th order Hankel function of the second kind, which represents out-
 143 going waves, and B_n shows the relative amplitudes of the scattered wave.

144 In summary, $\phi_n(r; \omega)$ (equation (5)) in this region (I) is given by

$$145 \quad \phi_n(r; \omega) = \left(B_n(\omega) H_n^{(2)}(k_0(\omega)r) + J_n(k_0(\omega)r) \right) \zeta_n^{in}(\omega). \quad (9)$$

146 We note that the Bessel functions represent the incident waves and the Hankel functions
 147 represent the outgoing scattered waves.

148 **2.3 Tsunami wavefield above the sloping bottom in region (II)**

149 For the numerical calculation of $\phi_n(r; \omega)$ within region (II) ($r_0 \leq r \leq r_1$), we
 150 define the amplitude A_n and the normalized radial function R_n as:

$$151 \quad \phi_n(r; \omega) = A_n(\omega) R_n(r; \omega) \zeta_n^{in}(\omega), \quad (10)$$

152 where R_n is normalized so that $R_n(r_0; \omega) = 1$ and A_n is the amplitude factor of ϕ_n at
 153 $r = r_0$. Equation (5) in region (II) can be rewritten as follows:

$$154 \quad \eta(r, \theta; \omega) = \frac{1}{2} A_0(\omega) \zeta_0^{in}(\omega) R_0(r; \omega) \\
 155 \quad + \sum_{n=1}^{\infty} [A_n(\omega) \zeta_n^{in}(\omega) \cos(n\theta) + A_{-n}(\omega) \zeta_{-n}^{in}(\omega) \sin(n\theta)] R_n(r; \omega). \quad (11) \\
 156$$

157 Inserting $\eta(r, \theta; \omega)$ into the governing equation (equation (3)) leads to the following equa-
 158 tion of R_n :

$$159 \quad \frac{d^2 R_n(r; \omega)}{dr^2} + \left(\frac{1}{r} + \frac{1}{D(r)} \frac{dD(r)}{dr} \right) \frac{dR_n(r; \omega)}{dr} + \left(\frac{\omega^2}{g_0 D(r)} - \frac{n^2}{r^2} \right) R_n(r; \omega) = 0. \quad (12)$$

160 Following Fujima and Goto (1994), we define the following dimensionless param-
 161 eters, ξ and β , to characterize this system. $\xi(r)$ is the radial phase defined as

$$162 \quad \xi(r) \equiv \int_{r_0}^r k(r') dr' = 2\omega \sqrt{\frac{(r - r_0)}{g_0}} \quad \text{if } r_0 \leq r \leq r_1, \quad (13)$$

163 where $k(r)$ is the local wave number given by

$$164 \quad k(r) \equiv \frac{\omega}{\sqrt{g_0 D(r)}}. \quad (14)$$

165 β is the azimuthal number along a circle with a radius of $2r_0$ defined by

$$166 \quad \beta \equiv \left. \frac{2\pi r}{\lambda(r)} \right|_{r=2r_0}, \quad (15)$$

167 where $\lambda(r)$ is wavelength defined by $2\pi/k(r)$. The reason for choosing this radius is dis-
 168 cussed in section 6.

169 The change of variables from r and h to ξ and β leads to the following equation:

$$170 \quad \frac{d^2 R_n(\xi; \omega)}{d\xi^2} + \left(\frac{2\xi}{\xi^2 + \beta^2} + \frac{1}{\xi} \right) \frac{dR_n(\xi; \omega)}{d\xi} + \left(1 - \left(\frac{2\xi}{\xi^2 + \beta^2} \right)^2 n^2 \right) R_n(\xi; \omega) = 0. \quad (16)$$

171 Only in two extreme cases of the radius of the island ($r_0 = 0$ and $r_0 = \infty$) (Fu-
 172 jima & Goto, 1994) can we obtain the analytical solutions of $R(\xi)$, which are crucial for
 173 understanding the behavior of $R(\xi)$. Two independent solutions exist according to the
 174 governing equation; the only one satisfies the physical requirement, which is a finite am-
 175 plitude of η at the shoreline. First, let us consider the analytical solution for an infinite
 176 radius of the island, which also represents a flat sloping bottom. Because β becomes in-
 177 finite, $R_n(0)$ is given by

$$178 \quad R_n(\xi) \sim J_0(\xi). \quad (17)$$

179 Next, let us consider the analytical solution for the zero island radius case $r_0 = 0$. Be-
 180 cause β becomes 0, $R_n(\xi)$ can be given by

$$181 \quad R(\xi) \sim \frac{J_{\sqrt{1+4n^2}}(\xi)}{\xi}. \quad (18)$$

182 Here, we choose a solution that has a finite amplitude at $\xi = 0$. At $\xi = 0$, only $R_0(\xi)$
 183 has a non-zero value, whereas $R_n(0) = 0$ for $n \neq 0$. In general, $R_n(\xi)$ has a signifi-
 184 cant value at $\xi = 0$ when $n \leq \beta$ (Fujima & Goto, 1994). Since the evaluation of the
 185 ground deformations requires only R_n for $n = 0, \pm 1$, as discussed in the following sec-
 186 tions, all the $R_n(\xi)$ have significant values at around $\xi = 0$

187 This ordinary differential equation can be solved using the numerical Livermore Solver
 188 for Ordinary Differential Equations (LSODE) (Radhakrishnan & Hindmarsh, 1993). Al-
 189 though R_n is integrated from $\xi = 0$ outward with respect to ξ , the governing equation
 190 at $\xi = 0$ is a singularity. For this reason, $R_n(\xi)$ is integrated from $\xi = \Delta\xi$ numeri-
 191 cally. $R_n(\Delta\xi)$ can be evaluated analytically by the asymptote (Fujima & Goto, 1994).
 192 $R_n(\Delta\xi)$ can be represented by Taylor expansion up to the second order when $\Delta\xi \ll 1$
 193 and $\beta \neq 0$ (Fujima & Goto, 1994):

$$194 \quad R_n(\Delta\xi) \approx \left(1 - \frac{1}{4}\Delta\xi^2\right). \quad (19)$$

195 Accordingly, the first order initial boundary conditions of R_n at $\xi = \Delta\xi$ are given by

$$196 \quad R_n(\Delta\xi) = 1, \quad (20)$$

$$197 \quad \left. \frac{dR_n(\xi)}{d\xi} \right|_{\xi=\Delta\xi} = -\frac{1}{2}\Delta\xi. \quad (21)$$

199 2.4 Boundary condition between (I) and (II)

200 We evaluate the boundary condition between (I) and (II) at $r = r_1$ for this equa-
 201 tion. Continuity of the amplitude for each azimuthal order, n , and the first derivative
 202 at the boundary between regions (I) and (II) leads to the following boundary condition:

$$203 \quad A_n(\omega)R_n(\xi_1) = J_n(k_0r_1) + B_n(\omega)H_n^{(2)}(k_0r_1), \quad (22)$$

$$204 \quad A_n(\omega) \left(\frac{dR_n(\xi)}{d\xi} \frac{d\xi}{dr} \right) \Big|_{\xi=\xi_1} = \frac{dJ_n(k_0r)}{dr} \Big|_{r=r_1} + B_n(\omega) \frac{dH_n^{(2)}(k_0r)}{dr} \Big|_{r=r_1}, \quad (23)$$

205 where $\xi_1 \equiv \xi(r_1)$. We can estimate A_n and B_n by solving this equation.
 206

207 Figure 4 shows the induced tsunami wavefield with azimuthal order 0 for the unit
 208 amplitude of the incident wave ($\phi_0(r, \omega)/\zeta_0^{in}(\omega)$) at 4 mHz. The parameters are those

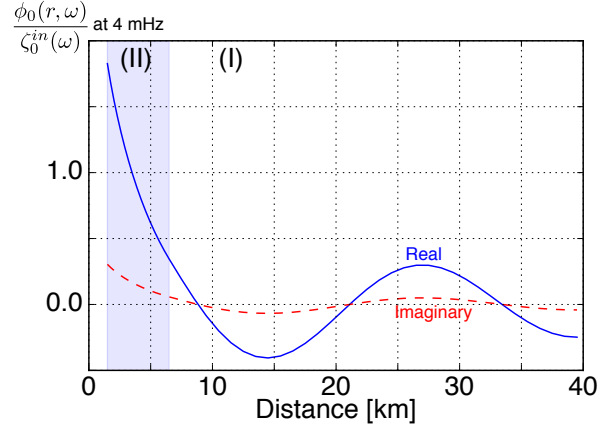


Figure 4. $\phi_0(r; \omega)/\zeta_0(\omega)$ at 4 mHz for Aogashima, the parameters of which are given in Table 1. The blue line shows the real part and the red dashed line shows the imaginary part.

209 for Aogashima given in Table 1. At approximately $r = r_0$, $\phi_0(r; \omega)/\zeta_0^{in}(r; \omega)$ is larger
 210 than 1, which indicates amplification due to confinement along the coast. We discuss this
 211 in detail in section 6.

Table 1. Parameters (radius of the island r_0 , slope m , and ocean depth D_0) used in this study based on ETOPO1 (Amante & Eakins, 2009). These parameters were estimated by the non-linear least-squares technique using MINPACK (Moré et al., 1984) with trial and error. f_β is a reference frequency used as $\beta = 1$ in equation (15).

station	radius r_0 [km]	slope m	ocean depth D_0 [km]	f_β [mHz]
AOG	1.5	0.20	1.0	2.9
RER	29	0.070	4.2	0.39
AIS	4.9	0.18	2.0	1.5
DGAR	12	0.017	4.2	0.29
CRZF	10	0.034	3.0	0.45

212 3 Ground deformation by tsunami loading

213 To estimate ground motions due to tsunami, we assume that they can be repre-
 214 sented by static deformation caused by tsunami loading (e.g. Sorrells & Goforth, 1973)
 215 because the phase velocity of seismic waves (on the order of 4 km/s) is much faster than

216 that of a tsunami (on the order of 0.01 km/s) in coastal areas. Loading on the seafloor
 217 by the modeled tsunami wavefield is convolved with static Green's functions in a semi-
 218 infinite medium with the following correction for bathymetric effects. Because the ra-
 219 dius of the island, r_0 , is much smaller than r_1 in most cases, we evaluate the deforma-
 220 tion, $\mathbf{u}(\omega)$, at the center of the island for simplicity. Note that the tilt motion at the cen-
 221 ter is also calculated because the horizontal component of a broadband seismometer is
 222 sensitive to tilt motion in this frequency range (Aki & Richards, 1980).

223 To evaluate the bathymetric correction for the Green's functions in a semi-infinite
 224 medium, the displacement $\mathbf{u}(x, y, z)$ and stress $\boldsymbol{\sigma}(x, y, z)$ in a Cartesian coordinate sys-
 225 tem (x, y, z) is expanded by the powers of slope, m , up to the first order (Segall, 2010;
 226 Williams & Wadge, 2000):

$$227 \quad u_i(x, y, z; \omega) = u_i^{(0)}(x, y, z; \omega) + u_i^{(1)}(x, y, z; \omega)m + \mathcal{O}(m^2), \quad i = x, y, z \quad (24)$$

$$228 \quad \sigma_{ij}(x, y, z; \omega) = \sigma_{ij}^{(0)}(x, y, z; \omega) + \sigma_{ij}^{(1)}(x, y, z; \omega)m + \mathcal{O}(m^2), \quad i, j = x, y, z, \quad (25)$$

230 where \mathcal{O} indicates "order of", u_i is the displacement, σ_{ij} is the stress, $^{(0)}$ shows the 0th
 231 order term, and $^{(1)}$ shows the first order terms. Based on the estimation of the first or-
 232 der terms described in appendix A, the first order terms with respect to the slope, m ,
 233 becomes comparable to the second order terms. Therefore, we neglect the first order terms
 234 below.

235 The displacement and tilt on the surface ($z = D_0$) and at the center ($x = y =$
 236 0) are corrected for elevation from $z = 0$ as follows:

$$237 \quad u_\alpha(0, 0, D_0) = u_\alpha^{(0)}(0, 0, 0) - D_0 \left. \frac{\partial u_z^{(0)}}{\partial \alpha} \right|_{z=0}, \quad \alpha = x, y, \quad (26)$$

$$238 \quad u_z(0, 0, D_0) = u_z^{(0)}(0, 0, 0), \quad (27)$$

$$239 \quad \left. \frac{\partial u_z}{\partial \alpha} \right|_{x=y=0, z=D_0} = \left. \frac{\partial u_z^{(0)}}{\partial \alpha} \right|_{x=y=z=0}, \quad \alpha = x, y. \quad (28)$$

241 The first-order corrections of horizontal displacement according to the location change
 242 are related to the corresponding 0th-order tilt motions. The correction of vertical dis-
 243 placement and tilt motion according to the location change is negligible in the first or-
 244 der because the surface pressure causes a vertical strain $\partial u_z^{(0)}/\partial z = 0$ at the free sur-
 245 face in a half space (Farrell, 1972).

246 Static Green's functions $g_r^z(r)$, $g_\theta^z(r)$, and $g_z^z(r)$ at a surface point $\mathbf{r} = (r, \theta, 0)$ for
 247 a vertical force at the origin in a semi-infinite medium are given by (Jaeger, Cook, & Zim-

248 merman, 2007; Segall, 2010)

$$249 \quad g_r^z(r) = \frac{1}{4\pi} \frac{1}{\lambda + \mu} \frac{1}{r}, \quad (29)$$

$$250 \quad g_\theta^z(r) = 0, \quad (30)$$

$$251 \quad g_z^z(r) = \frac{1}{4\pi\mu} \frac{\lambda + 2\mu}{\lambda + \mu} \frac{1}{r}, \quad (31)$$

252

253 where r is the radius in a cylindrical coordinate system (Figure 3), μ , and λ are Lamé's
 254 constant of the ground, the superscript on the Green's tensors refers to the direction of
 255 the point force, and the subscript refers to the direction of displacement. By convolv-
 256 ing forcing by the total tsunami wavefield and the static Green's functions with bathy-
 257 metric corrections, we can estimate the displacement and tilt at the center.

258 4 Virtual tsunami amplitude and direction without a conical island

259 Based on the total tsunami wavefield (section 2) and the Green's functions (sec-
 260 tion 3), we can relate the ground particle velocity at the center to the incident tsunami
 261 using a transfer function. The axisymmetric assumption of the island simplifies the trans-
 262 fer function concerning the azimuthal dependence. By deconvolving the transfer func-
 263 tion from observed seismic data in the vertical component, we can infer the incident tsunami
 264 amplitude, η^v , at the center assuming that the island is virtually removed. By decon-
 265 volving the transfer function from observed seismic data in the horizontal component,
 266 we can estimate the spatial gradient of η^v , which shows the propagation direction together
 267 with a single plane wave assumption.

268 4.1 Transfer function of the vertical component

269 The vertical ground velocity at the origin $v_z(\omega)$ due to the tsunami deformation
 270 can be represented by convolution between tsunami loading and the static Green's func-
 271 tion as:

$$272 \quad v_z(\omega) = -\rho g_0 \omega e^{i\pi/2} \int_{r_0}^{\infty} \int_0^{2\pi} \eta(r, \theta; \omega) g_z^z(r) r dr d\theta, \quad (32)$$

273 where $v_z(\omega)$ is the particle velocity in the z component given by $i\omega u_z(\omega)$. Let us eval-
 274 uate the integration using equations (5), (9), and (10). Because the integrand is axisym-
 275 metric, the higher order contributions with respect to azimuthal order ($n \geq 1$) such as:

$$276 \quad -\rho g_0 \omega e^{i\pi/2} \int_{r_0}^{\infty} \phi(r; \omega) g_z^z(r) r dr \int_0^{2\pi} \cos(n\theta) d\theta \quad (33)$$

277 are canceled out. Here, we define the virtual tsunami amplitude, $\eta^v(\omega)$, without the is-
 278 land as

$$279 \quad \eta^v(\omega) \equiv \eta^{in}(r, \theta; \omega)|_{r=0}. \quad (34)$$

280 The virtual tsunami amplitude can be related to the particle velocity v_z using a trans-
 281 fer function $T_{\eta z}$:

$$282 \quad v_z(\omega) = T_{\eta z}(\omega)\eta^v(\omega), \quad (35)$$

283 where $T_{\eta z}(\omega)$ is the transfer function of the tsunami to vertical ground velocity, defined
 284 as

$$285 \quad T_{\eta z}(\omega) \equiv -e^{i\pi/2}\pi\omega\rho g_0 (I_1^z(\omega) + I_2^z(\omega)), \quad (36)$$

286 The integrals I_1^z and I_2^z are defined as

$$287 \quad I_1^z(\omega) \equiv \int_{r_1}^{\infty} \left(B_0(\omega)H_0^{(2)}(k_0r) + J_0(k_0r) \right) g_z^z(r)rdr, \quad (37)$$

$$288 \quad I_2^z(\omega) \equiv \int_{r_0}^{r_1} A_0(\omega)R_0(r)g_z^z(r)rdr, \quad (38)$$

290 respectively. Figure 5a shows an example of the vertical transfer function $T_{\eta z}(\omega)$ for Ao-
 291 gashima. Below 5 mHz, the transfer function is flat. At 0 frequency, the amplitude and
 292 phase of the transfer function can be explained by the theoretical solution for a flat ocean
 293 (Ben-Menahem & Singh, 2000) as discussed in section 6. The amplitude decreases with
 294 a frequency above 5 mHz because tsunami wavelength becomes smaller than the island
 295 scale r_0 .

296 4.2 Transfer function of the horizontal component

297 Let us consider the transfer function of the horizontal component for tsunami in-
 298 cidence in the same manner. The horizontal ground velocity at the origin $\mathbf{v}_h(\omega)$ due to
 299 tsunami deformation can be represented by

$$300 \quad \mathbf{v}_h(\omega) \equiv \begin{pmatrix} v_x(\omega) \\ v_y(\omega) \end{pmatrix} = -\rho g_0 \omega e^{i\pi/2} \int_{r_0}^{\infty} \int_0^{2\pi} \eta(r, \theta; \omega) \left(g_r^z - D_0 \frac{\partial g_z^z}{\partial r} \right) \begin{pmatrix} -\cos \theta \\ -\sin \theta \end{pmatrix} r dr d\theta. \quad (39)$$

301 Because $\cos \theta$ and $\sin \theta$ have orthogonality with respect to the azimuthal integration, only
 302 $n \pm 1$ in terms of η contributes to the integration, as follows:

$$303 \quad \begin{pmatrix} v_x(\omega) \\ v_y(\omega) \end{pmatrix} = \frac{i}{2} T_{\eta h}(\omega) \begin{pmatrix} \zeta_1^{in} \\ \zeta_{-1}^{in} \end{pmatrix} = i \frac{T_{\eta h}(\omega)}{k_0} \nabla_h \eta^{in}(r, \theta; \omega)|_{r=0}. \quad (40)$$

304 Here, $T_{\eta h}(\omega)$ is given by,

$$305 \quad T_{\eta h}(\omega) = 2\pi\omega\rho g_0 (I_1^h(\omega) + I_2^h(\omega)), \quad (41)$$

306 where integrals I_1^h and I_2^h are defined as

$$307 \quad I_1^h(\omega) \equiv \int_{r_1}^{\infty} \left(B_1(\omega)H_1^{(2)}(k_0r) + J_1(k_0r) \right) \left(g_r^z - D_0 \frac{\partial g_z^z}{\partial r} \right) r dr, \quad (42)$$

$$308 \quad I_2^h(\omega) \equiv \int_{r_0}^{r_1} A_1(\omega)R_1(r) \left(g_r^z - D_0 \frac{\partial g_z^z}{\partial r} \right) r dr. \quad (43)$$

310 The spatial gradient of the surface displacement $\nabla_h \eta|_{r=0}$ can be related to the flow rate,

311 \mathbf{Q} (Satake, 2015), at the origin defined as

$$312 \quad \mathbf{Q} = \int_{D_0-D(r)}^{D_0} \mathbf{v}_h dz = \frac{ig_0}{\omega}, \nabla_h \eta^{in}|_{r=0} \quad (44)$$

313 $D(r)$ is water depth at r and D_0 is water depth of the flat ocean floor (Figure 3).

314 For simplicity, we assume that η can be represented by a single plane wave inci-

315 dence with the relative travel time, $\mathcal{T}(r, \theta)$, to the origin. The gradient can be written

316 as

$$317 \quad \nabla_h \eta^{in}(r, \theta; \omega) = -i\omega \eta^{in}(0, \theta; \omega) \nabla_h \mathcal{T}(r, \theta) = \eta^{in}(0, \theta; \omega) (-ik_0) \mathbf{e}_r, \quad (45)$$

318 where \mathbf{e}_r is the propagation direction of the tsunami. Then, we obtain the following re-

319 lationship:

$$320 \quad \mathbf{v}_h(\omega) = T_{\eta h}(\omega) \eta^v(\omega) \mathbf{e}_r. \quad (46)$$

321 $T_{\eta h}$ represents the transfer function from the tsunami incidence to horizontal ground ve-

322 locity at the center. This result shows that the observed ground velocity is parallel to

323 the tsunami propagation direction under the single plane-wave assumption. Figure 5a

324 shows an example of the horizontal transfer function $T_{\eta z}(\omega)$ for Aogashima. The trans-

325 fer function has a broad peak at 5 mHz. At 0 frequency, the amplitude and phase of the

326 transfer function can be explained by the theoretical solution for a flat ocean (Ben-Menahem

327 & Singh, 2000) as discussed in section 6. The amplitude also decreases with a frequency

328 above 5 mHz.

329 Below 1 mHz, tilt motion induced by tsunami is dominant in the horizontal com-

330 ponent of seismic sensors (Kimura et al., 2013; Nawa et al., 2007). The horizontal ac-

331 celeration contribution due to tilt motion ($\nabla_h u_z$, where u_z is the vertical displacement)

332 is given by $g_0 \nabla_h u_z$ (e.g. Rodgers, 1968; Wielandt & Forbriger, 1999). Then, the tilt mo-

tion at the origin, $v(\omega)$, due to deformation by the tsunami can be represented by

$$\mathbf{v}_h^{tilt}(\omega) = \frac{g_0 \nabla_h u_z}{i\omega} = \frac{-\rho g_0}{i\omega} \int_{r_0}^{\infty} \int_0^{2\pi} \eta(r, \theta; \omega) \frac{\partial g_r^z}{\partial r} \begin{pmatrix} -\cos \theta \\ -\sin \theta \end{pmatrix} r dr d\theta. \quad (47)$$

The higher order contributions ($n \neq \pm 1$) are again canceled out.

$$\mathbf{v}^{tilt}(\omega) = \frac{i}{2} T_{\eta h}(\omega) \begin{pmatrix} \zeta_1^{in} \\ \zeta_{-1}^{in} \end{pmatrix} = i \frac{T_{\eta h}^{tilt}(\omega)}{k_0} \nabla_h \eta^{in}(r, \theta; \omega)|_{r=0}. \quad (48)$$

Here, the transfer function due to tilt, $T_{\eta h}^{tilt}(\omega)$, of the tsunami to horizontal ground velocity is given by,

$$T_{\eta h}^{tilt}(\omega) = \frac{2\pi \rho g_0}{\omega} (I_1^t(\omega) + I_2^t(\omega)), \quad (49)$$

where integrals I_1^t and I_2^t are defined by

$$I_1^t(\omega) \equiv \int_{r_1}^{\infty} (B_1(\omega) H_1^{(2)}(k_0 r) + J_1(k_0 r)) \frac{\partial g_h^r(r)}{\partial r} r dr, \quad (50)$$

$$I_2^t(\omega) \equiv \int_{r_0}^{r_1} A_1(\omega) R_1(r) \frac{\partial g_z^z(r)}{\partial r} r dr. \quad (51)$$

Then, we also obtain the following relationship:

$$\mathbf{v}_h^{tilt}(\omega) = T_{\eta h}^{tilt}(\omega) \eta^v(\omega) \mathbf{e}_r. \quad (52)$$

Figure 5b shows that the tilt effects of the horizontal transfer function are dominant, specifically at low frequencies. Below 1 mHz, the transfer function approaches the theoretical solution for a flat ocean (Ben-Menahem & Singh, 2000), which is proportional to ω^{-1} . With increasing frequency, the contribution of the tilt effect decreases. Although the amplitudes of horizontal components are an order of magnitude larger than those of vertical components, the estimated virtual tsunami amplitude from horizontal components is more ambiguous. This is because tilt motions, which are the spatial derivative of vertical motion, are more sensitive to small-scale bathymetric changes and crustal heterogeneity.

5 Comparison with observations

During huge shallow earthquakes, the horizontal components of broadband seismometers located on an island often record tilt motion associated with tsunami (e.g., the 2004 Sumatra earthquake (Yuan et al., 2005)), although the contribution of low-frequency seismic waves excited by the earthquake (Kimura et al., 2013; Yuan et al., 2005) disturbs

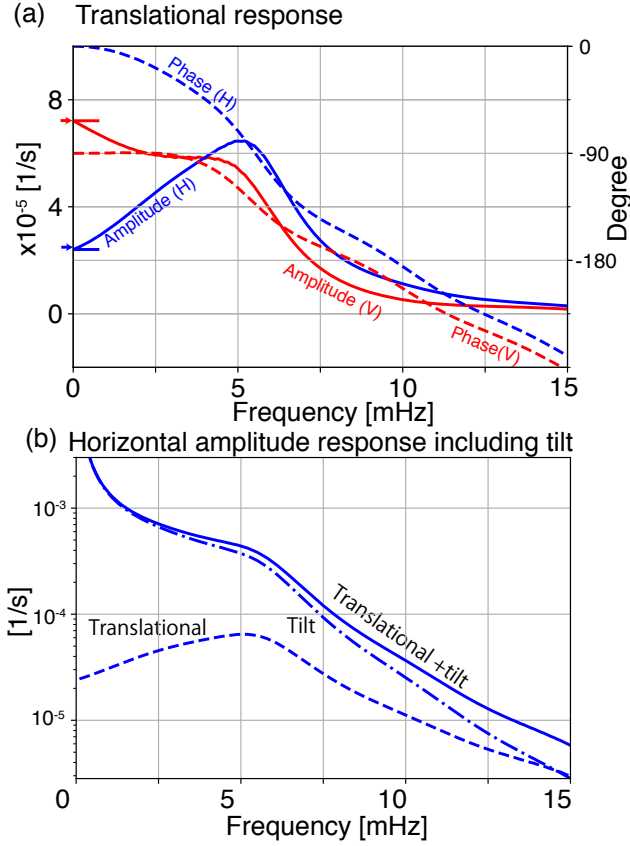


Figure 5. (a) Transfer function of translational motions against frequency. The dashed lines show the phases and the solid lines show the amplitudes, where (V) in the figure represents the vertical component and (H) shows the horizontal component. The red and blue lines show the vertical and horizontal transfer functions, respectively. Red and blue arrows at 0 mHz show the theoretical amplitudes for a flat ocean (Ben-Menahem & Singh, 2000) in vertical and horizontal components respectively. The phase shift can be explained by the arrival delay (approximately 70 s). (b) Amplitude of the transfer function of the horizontal component against frequency according to the contribution of translational motion, tilt motion, and both. The contribution of tilt motion is dominant below 5 mHz. We note that phases of the transfer function due to tilt are analytically the same as those of horizontal transfer function at all frequencies.

360 the tsunami signal. The amplitudes of vertical components are too small to detect be-
361 cause the vertical response is much smaller than the tilt response, as shown in Figure
362 5.

363 In order to suppress the noise, we apply this method to tsunami earthquakes, which
364 cause a much larger tsunami than expected from the seismic moment. We determine the
365 virtual tsunami amplitude and direction for two tsunami earthquakes: (1) the 2015 vol-
366 canic tsunami earthquake near Torishima, Japan, and (2) the 2010 Mentawai tsunami
367 earthquake in Indonesia. These results are verified by ray theory and other geophysical
368 observations.

369 5.1 Torishima 2015 Earthquake in Japan

370 A compensated-linear-vector-dipole (CLVD) type earthquake occurred on May 2,
371 2015, near Torishima island, Izu–Bonin arc, Japan (Figure 2), generating an abnormally
372 large tsunami (*e.g.* 0.5 m at Hachijozima 180 km north of the epicenter) for the moment
373 magnitude of M_w 5.7, determined by the U.S. Geological Survey. The tsunami was caused
374 by large deformation in a shallow part of a submarine volcanic body (Fukao et al., 2018).
375 A triangular array of ocean bottom pressure (OBP) gauges recorded an off-shore tsunami
376 (Sandanbata et al., 2017). They were deployed 100 km northeast of the epicenter with
377 a station separation of approximately 10 km (Figure 2). All tsunami waveforms with am-
378 plitudes of approximately 2 cm are similar to each other (Figure 6). A tsunami earth-
379 quake with a surface wave magnitude of M_s 5.6 in the same area occurred on June 13,
380 1984 (Kanamori, Ekström, Dziewonski, Barker, & Sipkin, 1993; Satake & Kanamori, 1991);
381 their focal mechanisms suggest magma injection with the submarine volcano (Fukao et
382 al., 2018; Kanamori et al., 1993).

383 At Aogashima island, close to the array, a broadband seismometer (STS2) of F-
384 net (Okada et al., 2004) was deployed by the National Research Institute for Earth Sci-
385 ence and Disaster Prevention (NIED). Because seismic waves from tsunami earthquakes
386 were relatively small at a low-frequency of 1.5-20 mHz, the broadband seismometer recorded
387 clear ground motions associated with the tsunami (Figure 1). We can compare the es-
388 timated virtual tsunami amplitudes from the seismic observations with near deep ocean
389 bottom pressure gauge.

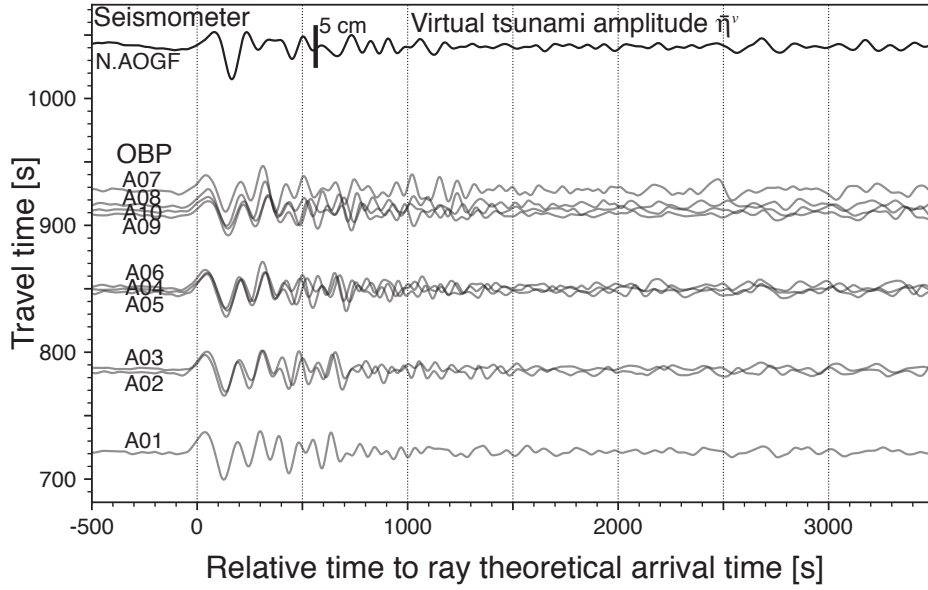


Figure 6. Estimated virtual tsunami amplitude with array observations by absolute pressure gauges. The vertical axis shows travel time predicted by ray theory and the horizontal axis shows relative time to the ray theoretical arrival time. Here, travel times are calculated by fast marching (Rawlinson, 2005; Rawlinson & Sambridge, 2005) using the long wave approximation. The uppermost record shows the virtual tsunami amplitude estimated from the vertical ground velocity at Aogashima (N.AOGF). The lower record shows 10 records of ocean bottom pressure gauges. These records are bandpass filtered from 1.5 to 20 mHz (4th order Butterworth, zero phase). The amplitude scales are the same throughout all records. The maximum amplitudes are approximately 2 cm.

390 Using the vertical component of the broadband seismometer, we infer the virtual
 391 tsunami amplitude. The modeled parameters of the conical island are given in Table (1).
 392 Using the transfer function, $T_{\eta z}(\omega)$, shown by Figure 5a, we estimate the virtual tsunami
 393 amplitude $\bar{\eta}^v(\omega)$ by deconvolution:

$$394 \quad \bar{\eta}^v(\omega) = \frac{T_{\eta z}^*(\omega)}{T_{\eta z}^*(\omega)T_{\eta z}(\omega) + w} v_z(\omega), \quad (53)$$

395 where w is the water level, which is 5×10^{-3} of the squared amplitude of $T_{\eta z}$ at 5 mHz.
 396 The $\bar{\eta}^v$ is converted in time domain. Figure 6 shows the comparison of $\bar{\eta}^v(t)$ with ob-
 397 served tsunami amplitudes by the pressure gauges against the relative travel time. The
 398 estimated amplitude of approximately 2.5 cm and the relative travel times are consis-
 399 tent with the offshore observations. The ray theoretical arrival times should coincide with

400 the peak time, but the figure shows slight delays in the peak time, which are attributed
 401 to dispersion due to the finite wavelength. This result verifies the feasibility of this method.

402 Next, let us consider the propagation direction from the observed horizontal com-
 403 ponents shown in Figure 5b. Using the transfer function, $T_{\eta h}$, for horizontal components,
 404 the tsunami amplitude with a propagation direction of $(\bar{\eta}_x^v, \bar{\eta}_y^v)$ can be defined as,

$$405 \begin{pmatrix} \bar{\eta}_x^v(\omega) \\ \bar{\eta}_y^v(\omega) \end{pmatrix} \equiv \frac{T_{\eta h}^*}{T_{\eta h}^*(\omega)T_{\eta h}(\omega) + w} \begin{pmatrix} v_x(\omega) \\ v_y(\omega) \end{pmatrix}, \quad (54)$$

406 where w is the water level, which is 1×10^{-3} the squared amplitude of $T_{\eta h}$ at 5 mHz.
 407 With the single plane wave assumption, $(\bar{\eta}_x^v, \bar{\eta}_y^v)$ can be interpreted as $\eta^{in} \mathbf{e}_r$ (equation
 408 (46)). Figure 7a shows the comparison among $\bar{\eta}_x^v$, $\bar{\eta}_y^v$, and $\bar{\eta}^v$. The waveforms at approx-
 409 imately 1000 s are consistent with each other.

410 The particle motions of the horizontal components (Figure 7b) shows a linear po-
 411 larization, which is consistent with the ray path shown in Figure 2. The consistency sug-
 412 gests that the assumptions related to the approximations of the conical island and the
 413 single plane wave are appropriate. Although the horizontal amplitude is slightly larger
 414 than the vertical amplitude, the discrepancy can be attributed to the slightly off-center
 415 station to the southwest. Phases of the later arrival at approximately 3000 s in Figure
 416 7 are different in different components because they are composed of multiple scatter-
 417 ing waves.

418 To quantitatively estimate the propagation direction, we assume that the virtual
 419 tsunami amplitude is given by $\bar{\eta}^v$ from the vertical component. Then, equation (46) leads
 420 to

$$421 \begin{pmatrix} \bar{\eta}_x^v(\omega) \\ \bar{\eta}_y^v(\omega) \end{pmatrix} = \bar{\eta}^v \begin{pmatrix} \sin \varphi \\ \cos \varphi \end{pmatrix}, \quad (55)$$

422 where φ is the propagation azimuth, which, in this case, can be estimated by

$$423 \varphi = \frac{\pi}{2} - \arctan 2 \left(\int_{t_0}^{t_1} \bar{\eta}_y^v(t) \bar{\eta}^v(t) dt, \int_{t_0}^{t_1} \bar{\eta}_x^v(t) \bar{\eta}^v(t) dt \right), \quad (56)$$

424 where $\arctan 2$ is 2-argument arc-tangent, t_0 is 0 s, and t_1 is 5000 s. The red arrow in Fig-
 425 ure 7 shows the propagation direction φ , whose length shows the root mean squared am-
 426 plitude from 0 to 5000 s. Because the integration in the above equation, which repre-
 427 sents covariance between the vertical and horizontal components, suppress incoherent
 428 parts, which originate from the higher noise level and scattered wavefield, the estima-

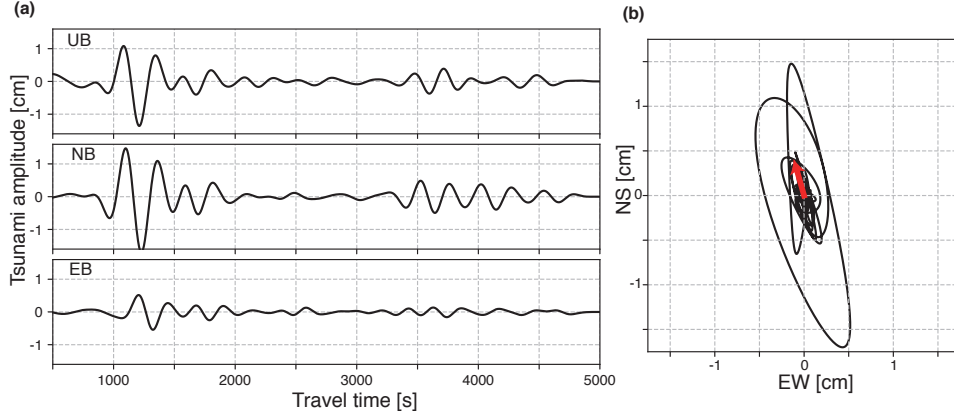


Figure 7. (a) The three components of the estimated tsunami waveform. The first is 2–5 mHz with a 6th order Butterworth filter. (b) Particle motions of the horizontal components from 2 to 5 mHz. The red arrow shows the estimated propagation direction with root mean squared amplitudes from 0 to 500 s.

429 tion is expected to be robust. Figure 8 shows the comparison between the estimated az-
 430 azimuth and the ray azimuth at the station. This figure shows that they are consistent within
 431 10 degrees. We also note that the above method enables us to estimate the propagation
 432 direction without introducing a 180° uncertainty (e.g. Takagi, Nishida, Maeda, & Obara,
 433 2018).

434 5.2 Mentawai 2010 in Indonesia

435 The 2010 Mentawai earthquake (Mw 7.8) caused a destructive tsunami in the Mentawai
 436 Islands, west of Sumatra in Indonesia (Satake, Nishimura, et al., 2013). The tsunami am-
 437 plitude reached 9.3 m on the west coasts of North and South Pagai Island. Seismolog-
 438 ical data analyses show that the earthquake was a tsunami earthquake (e.g. Lay et al.,
 439 2011). For the analysis, we use four broadband stations located on islands DGAR, RER,
 440 CRZF, and AIS shown in Figure 9. For the estimation of tsunami amplitude, we use the
 441 water level (see equations (53) and (54)), which is 5% of the maximum squared ampli-
 442 tude in a frequency range from 0.7 to 2 mHz.

443 Because most island radii (Table 1) are larger than that of Aogashim, as shown in
 444 Figure 10, their transfer functions are not sensitive to tsunami above 1 mHz, as shown
 445 in Figure 11. Hence, we focus on a signal with a typical frequency of 1 mHz. The esti-

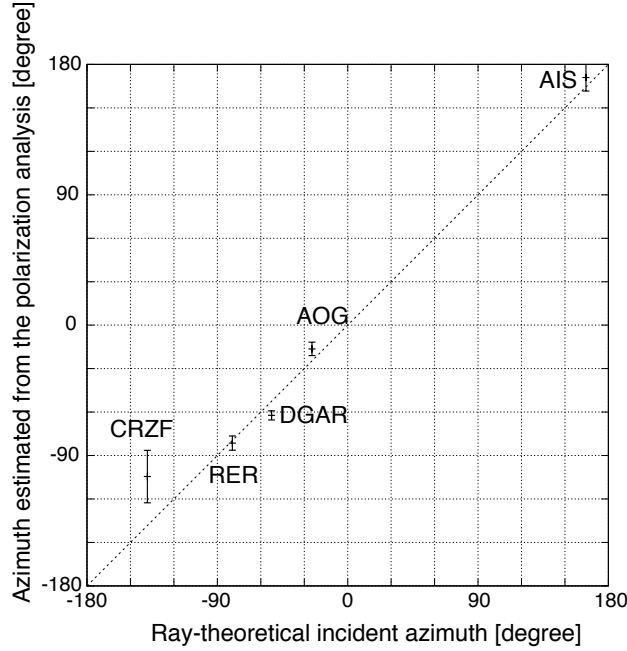


Figure 8. Propagation azimuths at stations. The horizontal axis shows the propagation azimuths estimated by this method utilizing broadband seismic data, whereas the vertical axis shows azimuths based on ray theory. To estimate the error of the propagation azimuth, we made 10^5 bootstrap samples and we estimated the error bars of 1σ by the use of moving block bootstrap resampling (Vogel & Shallcross, 1996). We made 10^5 bootstrap samples with a block length of 50 s at Aogashima and that of 100 s at the other stations respectively.

446 mated virtual tsunami amplitudes were 0.4 cm at DGAR, 1.3 cm at AIS, 0.9 cm at CRZF,
 447 and 0.6 cm at RER. Arrival times of the estimated waveforms are consistent with the
 448 ray theoretical values. The arrival time at DGAR is advanced because the simple sym-
 449 metric model is too simple to model a large island with a larger root size r_1 of approx-
 450 imately 260 km (see Table 1). Although DART station 5601 recorded a maximum tsunami
 451 amplitude of 1 cm (Satake, Nishimura, et al., 2013), it is located 1,600 km south to the
 452 epicenter. Because there are no offshore stations close to the four seismic broadband sta-
 453 tions, we compare the virtual tsunami heights $\bar{\eta}^v$ with numerical results by NOAA Cen-
 454 ter for Tsunami Research, which are maximum tsunami heights at an offshore points close
 455 to the stations based on the NOAA forecast method using MOST model with the tsunami
 456 source inferred from DART data (Gica, Spillane, Titov, Chamberlin, & Newman, 2008).

457 The calculated maximum wave heights of about 5 mm for RER, about 14 mm for AIS,
 458 about 14 mm, and about 8 mm for CRZF are consistent with our estimations.

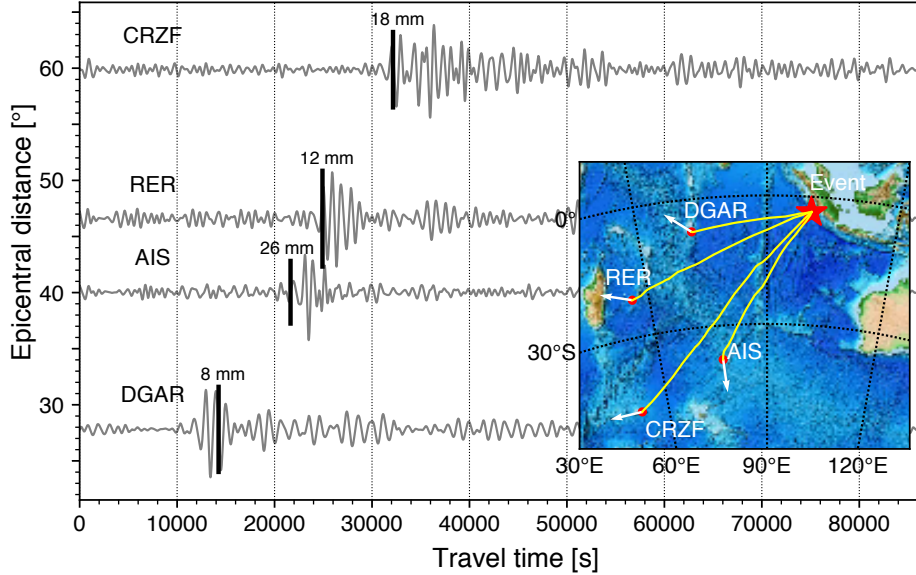


Figure 9. Virtual tsunami amplitudes at four stations for the 2010 Mentawai earthquake (Oct 25, 2010). 0.7–2 mHz (order 6). The map in the inset shows the station locations and the earthquake location. The bold black bars show the corresponding ray theoretical arrival times with amplitude scales.

459 The map in Figure 9 shows the estimated propagation directions using three components of broadband seismometers, as shown in the previous subsection. Although the
 460 estimated azimuths are slightly different from the ray paths on this large scale, the difference
 461 can be attributed to strong refraction close to the islands. Indeed, the relationship
 462 between the propagation azimuths estimated from the seismic stations can be explained
 463 by the azimuths predicted by ray theory, as shown in Figure 8. These are consistent with ray paths
 464 within 10 degrees except for CRZF. The deviation could be explained by scattering due to the
 465 neighboring island (Figure 10), which may break the single plane wave approximation.
 467

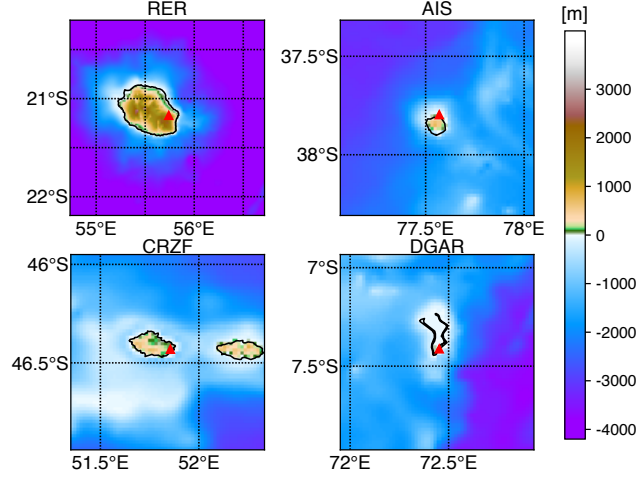


Figure 10. Enlarged maps of the islands. Stations are indicated by red triangles.

6 Characteristics of the transfer function according to the slope and radius

Tsunami trapping in the coastal slope of a conical island is crucial for characterizing the transfer functions. This section describes the amplification characteristics due to trapping in coastal areas, where the trapping condition (Longuet-Higgins, 1967) is given by,

$$\frac{\partial}{\partial r} \left(\frac{D(r)}{r^2} \right) \geq 0. \quad (57)$$

For the case of a conical island, the condition can be simplified as

$$r \leq 2r_0. \quad (58)$$

This relationship indicates that a larger conical island will trap more inshore areas.

β defined in equation (15) is crucial for characterizing the trapping effect. β can be interpreted as the ratio of the circumference, $4\pi r_0$ at $r = 2r_0$, to the wavelength, λ . In other words, β shows the azimuthal number of the trapped mode. Here, we define the cut-off frequency f_β as $\beta = 1$. Above this frequency, the tsunami is trapped in inshore areas. f_β is also a good proxy for ground deformation at the center because the deformation becomes significant when the radius of the island becomes larger than the wavelength. Consequently, the ground deformation becomes small with increasing frequency above the frequency. The f_β value, therefore, characterizes the cut-off frequency of the transfer functions. Table 1 shows f_β for the islands, which correspond to the cut-off frequency shown in Figure 11.

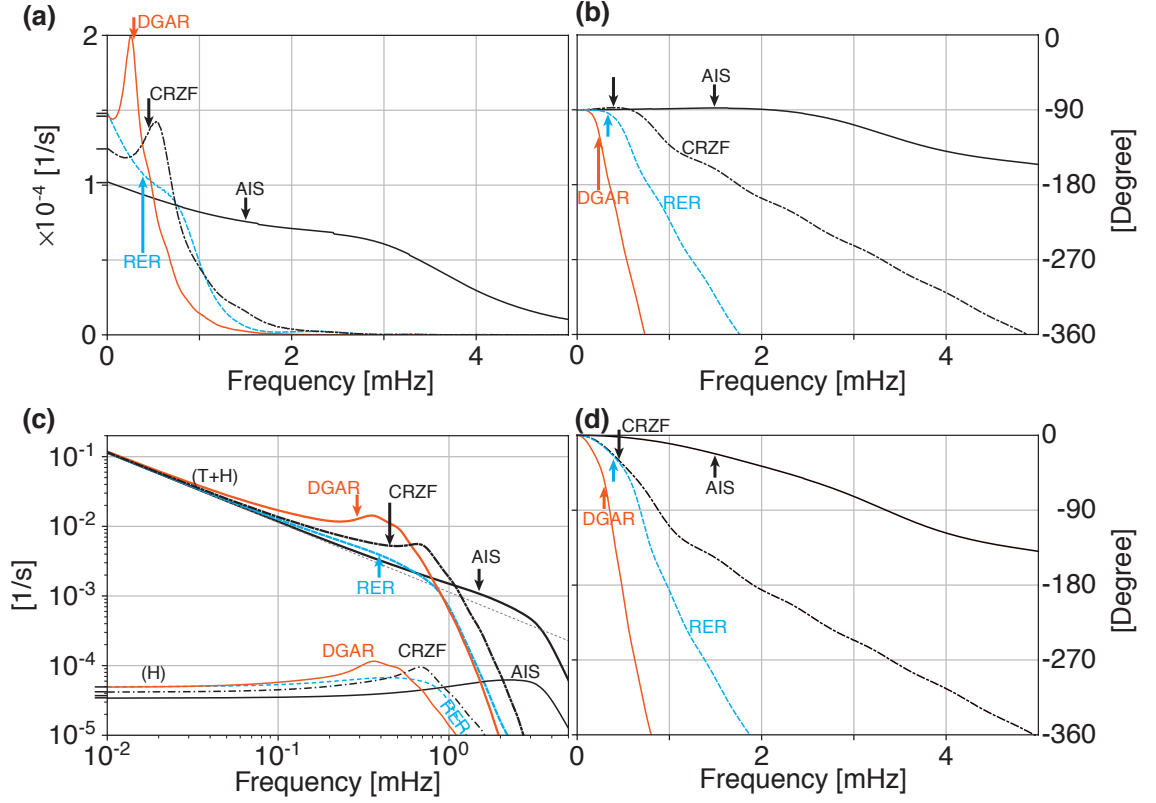


Figure 11. (a) Amplitudes of transfer functions for vertical components against frequency at the four broadband stations, composed of one IRIS IDA station, DGAR (Diego Garcia, Chagos islands), and three GEOSCOPE stations RER (La Réunion Island, France), CRZF (Port Alfred - Ile de la Possession - Crozet Islands, France), and AIS (Nouvel Amsterdam, TAAF, France). Station locations are shown in Figure 9. Black tick marks at 0 mHz show theoretical amplitudes for a flat ocean (equation (59)) in vertical components. The f_β values are shown by arrows. (b) Phases of the transfer functions for vertical components against frequency. (c) Amplitudes of transfer functions for horizontal components against frequency. Labels (H) shows the horizontal components due to translational motion, and (H+T) shows the horizontal component including the tilt effect. Black tick marks at 0 mHz show the theoretical amplitudes for a flat ocean (equation (60)) in horizontal components, and the straight dot-line in gray shows the theoretical amplitudes caused by the tilt motion for a flat ocean (equation (61)). (d) Phases of the transfer functions for horizontal components against frequency.

488 With a smaller slope m , more tsunami energy is trapped in the inshore area due
 489 to the slow propagation speed. In this case, the transfer function exhibits a peak at ap-
 490 proximately f_β . The translational transfer functions of DGAR and CRZF with smaller
 491 slope, m , show peaks at approximately f_β .

492 At much lower frequencies than f_β , we can neglect scattering by the island because
 493 the wavelength of the tsunami becomes much larger than the island scale. Moreover, the
 494 contribution of ground deformation in the inshore area becomes negligible. In this limit,
 495 the transfer functions are approximated by those of a semi-infinite medium loaded by
 496 pressure fluctuations on the surface given by Ben-Menahem and Singh (2000):

$$497 \quad \lim_{\omega \rightarrow 0} T_{\eta z}(\omega) = \frac{e^{-i\pi/2} \sqrt{g_0 D_0}}{2(\lambda + \mu)} \frac{\lambda + 2\mu}{\mu} \rho g_0, \quad (59)$$

$$498 \quad \lim_{\omega \rightarrow 0} T_{\eta h}(\omega) = \frac{\sqrt{g_0 D_0}}{2(\lambda + \mu)} \rho g_0, \quad (60)$$

$$499 \quad \lim_{\omega \rightarrow 0} T_{\eta h}^{tilt}(\omega) = \frac{\lambda + 2\mu}{2(\lambda + \mu)\mu} \rho \frac{g_0^2}{\omega}. \quad (61)$$

501 Figure 5a and Figure 11 show that the transfer functions approaching zero frequency also
 502 approach the above values. Figure 11 (d) also shows that $T_{\eta h}^{tilt}(\omega)$ actually approaches
 503 equation (61) in the low frequency limit.

504 At frequencies higher than about $10f_\beta$, the wavelength of tsunami becomes much
 505 smaller than the island scale. Consequently, the scattering by small scale bathymetric
 506 changes breaks the basic assumption of this method. Thus, f_β could be a proxy for the
 507 characteristics when evaluating the transfer function.

508 **7 Potential applications for ocean infragravity waves**

509 Although tsunami in this frequency range is ocean infragravity waves excited by
 510 an earthquake, ocean infragravity waves are also excited by the other geophysical pro-
 511 cesses. For example, they are excited persistently along shorelines by incident ocean swell
 512 through nonlinear processes and travel across the ocean with a typical height on the or-
 513 der of 1 cm in pelagic regions (Rawat et al., 2014; Tonegawa et al., 2018). The background
 514 ocean infragravity-wave activities are also key for understanding background seismic wave-
 515 fields know as seismic hum because they are the primary excitation source (Ardhuin, Gualtieri,
 516 & Stutzmann, 2015; Nishida, 2013, 2017; Rhie & Romanowicz, 2004). Observed equipar-
 517 tition of energy between Love and Rayleigh waves (Fukao, Nishida, & Kobayashi, 2010;
 518 Nishida, Kawakatsu, Fukao, & Obara, 2008) suggests a topographic coupling between

519 ocean infragravity waves and seismic surface waves. Seismic observations at island broad-
 520 band stations could be used to understand the excitation mechanisms because model-
 521 ing of ocean infragravity waves requires further researches (Ardhuin et al., 2015; Ard-
 522 huin, Rawat, & Aucan, 2014).

523 Our proposed technique for estimating virtual tsunami amplitude is applicable not
 524 only for tsunami but also for random wavefields of the background ocean infragravity
 525 waves. Seismic observations at islands could elucidate ocean infragravity wave activities.
 526 The wave action model WAVEWATCH III has recently been extended from the swell
 527 band to ocean infragravity waves (Ardhuin et al., 2014) and recovers the observed en-
 528 ergy of wave height within 50%. Our method could be used to improve such models.

529 8 Conclusions

530 In this study, we consider that an arbitrary tsunami in a flat ocean floor enters a
 531 conical island. The scattering wavefield is evaluated using a semi-analytical method, which
 532 is an extension of the theory of Fujima and Goto (1994). Then, we calculate ground de-
 533 formation due to tsunami loading at the center of the conical island using static Green's
 534 functions with a first-order correction for bathymetry. In this formulation, the ground
 535 motions can be represented by convolution between the transfer functions and the in-
 536 cident tsunami amplitudes at the station. The transfer functions are characterized by
 537 a cutoff frequency, f_β , and they approach those given by Ben-Menahem and Singh (2000)
 538 for a semi-infinite medium loaded by pressure on the surface without an island. By de-
 539 convolving the transfer functions from seismic data, we can infer the incident tsunami
 540 wavefield, which can be interpreted as the virtual tsunami amplitude without the island.
 541 Thus, we propose a new technique for estimating the virtual tsunami amplitude and prop-
 542 agation direction from seismic data using the assumption of a single plane wave.

543 First, we apply this technique to seismic records from Aogashima volcanic island
 544 when the Torishima Oki earthquake hit on May 2, 2015. The estimated tsunami ampli-
 545 tude is quantitatively consistent with an array observation of pressure gauges close to
 546 the island from 1.5 to 20 mHz. The incident angle estimated from the seismic data is
 547 also consistent with the ray-theoretical value. We also apply this method to seismic data
 548 at four broadband stations located on islands in the Indian ocean for the tsunami earth-
 549 quake in Mentawai, Indonesia on October 25, 2010. Although the observed frequency

550 range is limited from 0.5 to 2.0 mHz, the incident angles are consistent with ray theo-
551 retical values. This method can, therefore, complement offshore tsunami observations.

552 Because this technique is formulated for an arbitrary incident wavefield, it could
553 be employed not only for tsunami but also for background ocean infragravity waves, which
554 are excited along shorelines by incident ocean swell through nonlinear processes. Fur-
555 ther research should develop this method in order to elucidate background ocean infra-
556 gravity wave activities using broadband seismic stations located on islands.

A Correction of ground deformation for tilt

Following Segall (2010), we estimate the first order correction of displacements $u_i^{(1)}$ ($i = x, y, z$) for the bathymetry as induced displacement by the first order stress $\sigma_{ij}^{(1)}$ in a cylindrical coordinate (r, θ, z) , given by

$$\sigma_{zz}^{(1)} = 0, \quad (\text{A.1})$$

$$\sigma_{rz}^{(1)} = -\frac{dh}{dr}(\sigma_{zz}^{(0)} - \sigma_{rr}^{(0)}), \quad (\text{A.2})$$

$$\sigma_{\theta z}^{(1)} = -\frac{dh}{dr}\sigma_{r\theta}^{(0)} \quad (\text{A.3})$$

at $z = 0$. Here, the 0th-order terms in Cartesian coordinates satisfy

$$\frac{\partial \sigma_{ij}^{(0)}}{\partial x_j} = 0 \quad (\text{A.4})$$

with boundary conditions given by

$$\sigma_{zz}^{(0)} = -p(x, y), \sigma_{zx}^{(0)} = 0, \sigma_{zy}^{(0)} = 0. \quad (\text{A.5})$$

We note the following relationships:

$$\left. \frac{\partial \sigma_{rz}^{(0)}}{\partial z} \right|_{z=0} = \left. \frac{\partial \sigma_{\theta z}^{(0)}}{\partial z} \right|_{z=0} = \left. \frac{\partial \sigma_{zz}^{(0)}}{\partial z} \right|_{z=0} = 0, \quad (\text{A.6})$$

on the free surface of the island. This result is obtained by representing the stress in terms of the Newtonian potential functions (Love, 1929, section 1.1).

The first order displacement can be calculated by convolution between the Green's function in a semi-infinite medium and $\sigma_{ij}^{(1)}$ on the surface. The corresponding components ($\sigma_{rz}^{(1)}$ and $\sigma_{r\theta}^{(1)}$) can be calculated by convolution between $-p$ and static Green's functions of surface traction for normal traction in a semi-infinite space (Jaeger et al., 2007; Segall, 2010). The Green's functions $g_{xx}^{\sigma z}, g_{xy}^{\sigma z}, g_{yy}^{\sigma z}$ in a Cartesian coordinate system are given by

$$g_{xx}^{\sigma z} = \frac{1}{2\pi} \frac{\mu}{\lambda + \mu} \frac{-x^2 + y^2}{r^4} + \frac{1 + 2\nu}{2} \delta(r), \quad (\text{A.7})$$

$$g_{xy}^{\sigma z} = -\frac{1}{2\pi} \frac{\mu}{\lambda + \mu} \frac{2xy}{r^4}, \quad (\text{A.8})$$

$$g_{yy}^{\sigma z} = \frac{1}{2\pi} \frac{\mu}{\lambda + \mu} \frac{x^2 - y^2}{r^4} + \frac{1 + 2\nu}{2} \delta(r). \quad (\text{A.9})$$

Note that Jaeger et al. (2007) does not include two terms of $\delta(r)$ because they are defined outside the source regions. The two terms can be estimated as the limit of a disk load given by Farrell (1972) as r approaches 0, as shown in the next section. For the convolution between $g_{ij}^{\sigma z}$ and $\sigma_{ij}^{(0)}$, calculation in the wavenumber domain is convenient (Segall,

587 2010). $G_{ij}^{\sigma z}$, which is the Fourier component of $g_{ij}^{\sigma z}$ in the wavenumber domain, is given
 588 by

$$589 \quad G_{xx}^{\sigma z} = \frac{1}{2} \frac{\mu}{\lambda + \mu} \frac{-k_x^2 + k_y^2}{k_x^2 + k_y^2} + \frac{1 + 2\nu}{2} \quad (\text{A.10})$$

$$590 \quad G_{xy}^{\sigma z} = \frac{1}{2} \frac{\mu}{\lambda + \mu} \frac{-2k_x k_y}{k_x^2 + k_y^2} \quad (\text{A.11})$$

$$591 \quad G_{yy}^{\sigma z} = \frac{1}{2} \frac{\mu}{\lambda + \mu} \frac{k_x^2 - k_y^2}{k_x^2 + k_y^2} + \frac{1 + 2\nu}{2} \quad (\text{A.12})$$

593 Figure A.1 shows a typical example of induced 0th-order stress $\sigma_{zz}^{(0)} - \sigma_{rr}^{(0)}$ and $\sigma_{r\theta}^{(0)}$,
 594 which is stress induced by the tsunami wavefield with an azimuthal order of 1 ($\zeta_1^{in} =$
 595 1) for Aogashima at 4 mHz. Because $\sigma_{zz}^{(0)} - \sigma_{rr}^{(0)}$ and $\sigma_{r\theta}^{(0)}$ are an order of magnitude smaller
 596 than $\sigma_{zz}^{(0)}$ at the surface, we can neglect the first order stress $\sigma_{ij}^{(1)}$. Consequently, the first
 597 order displacement $u^{(1)}$ is also negligible. Although the first order correction of normal
 598 traction $\sigma_{zz}^{(1)}$ is negligible, those of shear traction, $\sigma_{zx}^{(1)}$ and $\sigma_{zy}^{(1)}$, are significant.

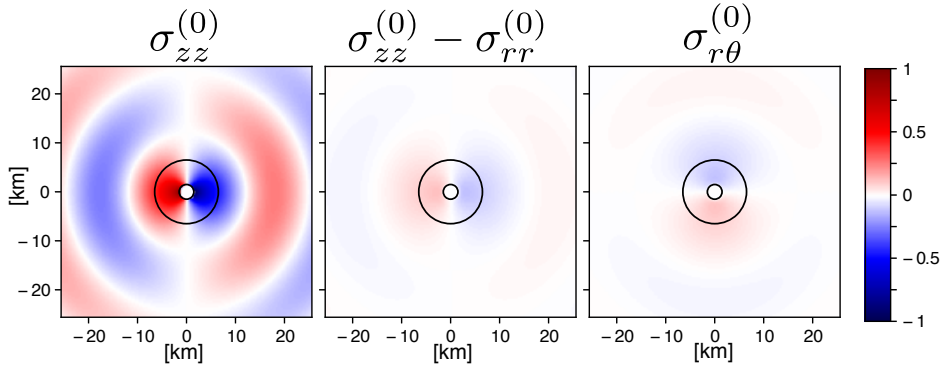


Figure A.1. Stress σ_{zz} is imposed on the surface. σ_{rr} is the induced principle stress on the surface, which is one order of magnitude smaller than the imposed stress. The inner circle shows the radius of the island at sea level, r_0 , and the outer circle shows the radius of the island on the seafloor r_1 .

B Stress components by surface loads on a half-space

Stress components by surface loads on a half-space are given Jaeger et al. (2007)

as

$$\sigma_{xx} = \frac{1}{2\pi} \left[\frac{3x^2z}{r^5} + \frac{(1-2\nu)(y^2+z^2)}{r^3(z+r)} - \frac{(1-2\nu)z}{r^3} - \frac{(1-2\nu)x^2}{r^2(z+r)^2} \right] \quad (\text{B.1})$$

$$\sigma_{xy} = \frac{1}{2\pi} \left[\frac{3xyz}{r^5} - \frac{(1-2\nu)xy(z+2r)}{r^3(z+r)^2} \right] \quad (\text{B.2})$$

$$\sigma_{yy} = \frac{1}{2\pi} \left[\frac{3y^2z}{r^5} + \frac{(1-2\nu)(x^2+z^2)}{r^3(z+r)} - \frac{(1-2\nu)z}{r^3} - \frac{(1-2\nu)y^2}{r^2(z+r)^2} \right]. \quad (\text{B.3})$$

Because the surface values are singular, we derive the simplified form on the surface below.

Let us consider that stress components by a disk load (Love, 1929; Lubarda, 2013) are given by

$$\sigma_{rr} = \frac{p}{2} \begin{cases} 1+2\nu, & r < R \\ -(1-2\nu)\frac{R^2}{r^2}, & r \geq R \end{cases} \quad (\text{B.4})$$

$$\sigma_{\theta\theta} = \frac{p}{2} \begin{cases} 1+2\nu, & r < R \\ (1-2\nu)\frac{R^2}{r^2}, & r \geq R \end{cases} \quad (\text{B.5})$$

where R is the radius of the disk and p is the pressure applied uniformly over the disk area. The limits of stress as R approaches 0 have the following forms:

$$\sigma_{xx} = \frac{1}{2\pi} \frac{\mu}{\lambda + \mu} \frac{-x^2 + y^2}{r^4} + \frac{1+2\nu}{2} \delta(r) \quad (\text{B.6})$$

$$\sigma_{xy} = -\frac{1}{2\pi} \frac{\mu}{\lambda + \mu} \frac{2xy}{r^4} \quad (\text{B.7})$$

$$\sigma_{yy} = \frac{1}{2\pi} \frac{\mu}{\lambda + \mu} \frac{x^2 - y^2}{r^4} + \frac{1+2\nu}{2} \delta(r). \quad (\text{B.8})$$

These representations are also given by the limit of equation B.1 as z approaches 0.

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632 **References**

- 633 Aki, K., & Richards, P. G. (1980). *Quantitative Seismology* (Vol. 1). W. H. Free-
 634 man, San Francisco.
- 635 Amante, C., & Eakins, B. W. (2009). *ETOPO1 Global Relief Model con-*
 636 *verted to PanMap layer format* [data set]. PANGAEA. doi: 10.1594/
 637 PANGAEA.769615
- 638 Ardhuin, F., Gualtieri, L., & Stutzmann, E. (2015). How ocean waves rock the
 639 Earth: Two mechanisms explain microseisms with periods 3 to 300 s. *Geophys.*
 640 *Res. Lett.*, *42*(3), 765–772. doi: 10.1002/2014GL062782
- 641 Ardhuin, F., Rawat, A., & Aucan, J. (2014, may). A numerical model for free in-
 642 fragravity waves: Definition and validation at regional and global scales. *Ocean*
 643 *Model.*, *77*, 20–32. doi: 10.1016/j.ocemod.2014.02.006
- 644 Ben-Menahem, A., & Singh, S. J. (2000). *Seismic Waves and Sources* (2nd ed.).
 645 Dover Publications, Incorporated.
- 646 Bernard, E. N., & Meinig, C. (2011, sep). History and future of deep-ocean tsunami
 647 measurements. In *Ocean. mts/ieee kona* (pp. 1–7). IEEE. doi: 10.23919/
 648 OCEANS.2011.6106894
- 649 Farrell, W. E. (1972). Deformation of the Earth by surface loads. *Rev. Geophys.*,
 650 *10*(3), 761. doi: 10.1029/RG010i003p00761
- 651 Fujima, K., & Goto, C. (1994). Characteristics of long waves trapped by conical is-
 652 lands, in japanese. *The Japan Society of Civil Engineers, 1994* (497), 101-110.
 653 doi: 10.2208/jscej.1994.497_101
- 654 Fukao, Y., Nishida, K., & Kobayashi, N. (2010). Seafloor topography, ocean in-
 655 fragravity waves, and background Love and Rayleigh waves. *J. Geophys. Res.*
 656 *Solid Earth*, *115*(4), 1–10. doi: 10.1029/2009JB006678
- 657 Fukao, Y., Sandanbata, O., Sugioka, H., Ito, A., Shiobara, H., Watada, S., & Sa-
 658 take, K. (2018). Mechanism of the 2015 volcanic tsunami earthquake near
 659 Torishima, Japan Mechanism of volcanic tsunami earthquake. *Sci. Adv.*.
- 660 Gica, E., Spillane, M., Titov, V., Chamberlin, C., & Newman, J. (2008). *Develop-*
 661 *ment of the forecast propagation database for NOAA’s Short-Term Inundation*
 662 *Forecast for Tsunamis (SIFT)* (Tech. Rep.).
- 663 Gill, A. (1982). *Atmosphere-ocean dynamics*. Elsevier Science. Retrieved from
 664 https://books.google.co.jp/books?id=8kFPh_SvnAIC

- 665 Jaeger, J., Cook, N., & Zimmerman, R. (2007). *Fundamentals of rock mechanics*.
666 Wiley.
- 667 Kanamori, H., Ekström, G., Dziewonski, A., Barker, J. S., & Sipkin, S. A. (1993).
668 Seismic radiation by magma injection: An anomalous seismic event near
669 Tori Shima, Japan. *J. Geophys. Res. Solid Earth*, *98*(B4), 6511–6522. doi:
670 10.1029/92JB02867
- 671 Kânoğlu, U., & Synolakis, C. E. (1998). Long wave runup on piecewise lin-
672 ear topographies. *J. Fluid Mech.*, *374*(November 1998), 1–28. doi:
673 10.1017/S0022112098002468
- 674 Kimura, T., Tanaka, S., & Saito, T. (2013). Ground tilt changes in Japan caused by
675 the 2010 Maule, Chile, earthquake tsunami. *Journal of Geophysical Research:*
676 *Solid Earth*, *118*(1), 406–415. doi: 10.1029/2012JB009657
- 677 Krischer, L., Megies, T., Barsch, R., Beyreuther, M., Lecocq, T., Caudron, C., &
678 Wassermann, J. (2015). ObsPy: A bridge for seismology into the scientific
679 Python ecosystem. *Comput. Sci. Discov.*, *8*(1). doi: 10.1088/1749-4699/8/1/
680 014003
- 681 Lay, T., Ammon, C. J., Kanamori, H., Yamazaki, Y., Cheung, K. F., & Hutko, A. R.
682 (2011). The 25 October 2010 Mentawai tsunami earthquake (M w 7.8) and
683 the tsunami hazard presented by shallow megathrust ruptures. *Geophys. Res.*
684 *Lett.*, *38*(6), 2–6. doi: 10.1029/2010GL046552
- 685 Liu, P. L.-F., Cho, Y.-S., Briggs, M. J., Lu, U. K., & Synolakis, C. E. (1995).
686 Runup of solitary waves on a circular island. *Journal of Fluid Mechanics*,
687 *302*(10), 259–285. doi: 10.1017/S0022112095004095
- 688 Longuet-Higgins, M. S. (1967). On the trapping of wave energy round islands. *J.*
689 *Fluid Mech.*, *29*(04), 781–821. doi: 10.1017/S0022112067001181
- 690 Love, A. E. H. (1929). The Stress Produced in a Semi-Infinite Solid by Pressure
691 on Part of the Boundary. *Philos. Trans. R. Soc. A Math. Phys. Eng. Sci.*,
692 *228*(659-669), 377–420. doi: 10.1098/rsta.1929.0009
- 693 Lubarda, V. A. (2013). Circular loads on the surface of a half-space: Displace-
694 ment and stress discontinuities under the load. *Int. J. Solids Struct.*, *50*(1), 1–
695 14. doi: 10.1016/j.ijsolstr.2012.08.029
- 696 Moré, J. J., Sorensen, D. C., Hillstrom, K. E., & Garbow, B. S. (1984). *The MIN-*
697 *PACK Project, in Sources and Development of Mathematical Software*. Upper

- 698 Saddle River, NJ, USA: Prentice-Hall, Inc.
- 699 Nawa, K., Suda, N., Satake, K., Fujii, Y., Sato, T., Doi, K., . . . Shibuya, K. (2007).
700 Loading and gravitational effects of the 2004 Indian Ocean tsunami at Syowa
701 Station, Antarctica. *Bull. Seismol. Soc. Am.*, *97*(1A), S271–S278. doi:
702 10.1785/0120050625
- 703 Nishida, K. (2013). Earth’s Background Free Oscillations. *Annu. Rev. Earth Planet.*
704 *Sci.*, *41*(1), 719–740. doi: 10.1146/annurev-earth-050212-124020
- 705 Nishida, K. (2017). Ambient seismic wave field. *Proc. Japan Acad. Ser. B*, *93*(7),
706 423–448. doi: 10.2183/pjab.93.026
- 707 Nishida, K., Kawakatsu, H., Fukao, Y., & Obara, K. (2008, aug). Background Love
708 and Rayleigh waves simultaneously generated at the Pacific Ocean floors. *Geo-*
709 *phys. Res. Lett.*, *35*(16), L16307. doi: 10.1029/2008GL034753
- 710 Okada, Y., Kasahara, K., Hori, S., Obara, K., Sekiguchi, S., Fujiwara, H., & Ya-
711 mamoto, A. (2004). Recent progress of seismic observation networks in Japan
712 Hi-net, F-net, K-NET and KiK-net. *Earth, Planets Sp.*, *56*(8), xv–xxviii. doi:
713 10.1186/BF03353076
- 714 Radhakrishnan, K., & Hindmarsh, A. C. (1993, dec). *Description and use of*
715 *LSODE, the Livermore Solver for Ordinary Differential Equations* (Tech.
716 Rep.). Livermore, CA: Lawrence Livermore National Laboratory (LLNL).
717 doi: 10.2172/15013302
- 718 Rawat, A., Arduin, F., Ballu, V., Crawford, W., Corela, C., & Aucan, J. (2014,
719 nov). Infragravity waves across the oceans. *Geophys. Res. Lett.*, *41*(22),
720 7957–7963. doi: 10.1002/2014GL061604
- 721 Rawlinson, N. (2005). *FMST: Fast Marching Surface Tomography package Research*
722 (Tech. Rep.). Aust. Natl. Univ.
- 723 Rawlinson, N., & Sambridge, M. (2005). The fast marching method: An effective
724 tool for tomographic imaging and tracking multiple phases in complex layered
725 media. *Explor. Geophys.*, *36*(4), 341–350. doi: 10.1071/EG05341
- 726 Rhie, J., & Romanowicz, B. (2004, sep). Excitation of Earth’s continuous free oscil-
727 lations by atmosphereoceanseafloor coupling. *Nature*, *431*(7008), 552–556. doi:
728 10.1038/nature02942
- 729 Rodgers, P. W. (1968). The response of the horizontal pendulum seismometer to
730 Rayleigh and Love waves, tilt, and free oscillations of the earth. *Bull. Seismol.*

- 731 *Soc. Am.*, 58(5), 1385–1406.
- 732 Sandanbata, O., Watada, S., Satake, K., Fukao, Y., Sugioka, H., Ito, A., & Shiobara,
733 H. (2017). Ray Tracing for Dispersive Tsunamis and Source Amplitude Es-
734 timation Based on Green’s Law: Application to the 2015 Volcanic Tsunami
735 Earthquake Near Torishima, South of Japan. *Pure Appl. Geophys.* doi:
736 10.1007/s00024-017-1746-0
- 737 Satake, K. (2015). Tsunamis. In *Treatise geophys.* (pp. 477–504). Elsevier. doi: 10
738 .1016/B978-0-444-53802-4.00086-5
- 739 Satake, K., Fujii, Y., Harada, T., & Namegaya, Y. (2013). Time and space dis-
740 tribution of coseismic slip of the 2011 Tohoku earthquake as inferred from
741 Tsunami waveform data. *Bull. Seismol. Soc. Am.*, 103(2 B), 1473–1492. doi:
742 10.1785/0120120122
- 743 Satake, K., & Kanamori, H. (1991). Abnormal tsunamis caused by the June 13,
744 1984, Torishima, Japan, earthquake. *J. Geophys. Res. Solid Earth*, 96(B12),
745 19933–19939. doi: 10.1029/91JB01903
- 746 Satake, K., Nishimura, Y., Putra, P. S., Gusman, A. R., Sunendar, H., Fujii, Y., ...
747 Yulianto, E. (2013). Tsunami Source of the 2010 Mentawai, Indonesia Earth-
748 quake Inferred from Tsunami Field Survey and Waveform Modeling. *Pure*
749 *Appl. Geophys.*, 170(9-10), 1567–1582. doi: 10.1007/s00024-012-0536-y
- 750 Segall, P. (2010). *Earthquake and Volcano Deformation*. Princeton University Press.
- 751 Smith, R., & Sprinks, T. (1975, nov). Scattering of surface waves by a conical island.
752 *J. Fluid Mech.*, 72(02), 373. Retrieved from `papers://2ebf624a-5397-4902`
753 `-a637-e1c2a5c19c2c/Paper/p1173http://www.journals.cambridge.org/`
754 `abstract{_}S0022112075003424` doi: 10.1017/S0022112075003424
- 755 Sorrells, G. G., & Goforth, T. T. (1973). Low-Frequency Earth Motion Gener-
756 ated By Slowly Propagating Partially Organized Pressure Fields. *Bull. Seis-*
757 *mol. Soc. Am.*, 63(5), 1583–1601.
- 758 Takagi, R., Nishida, K., Maeda, T., & Obara, K. (2018). Ambient seismic noise
759 wavefield in Japan characterized by polarization analysis of Hi-net records.
760 *Geophys. J. Int.*, 215(3), 1682–1699. doi: 10.1093/gji/ggy334
- 761 Tonegawa, T., Fukao, Y., Shiobara, H., Sugioka, H., Ito, A., & Yamashita, M.
762 (2018). Excitation Location and Seasonal Variation of Transoceanic Infra-
763 gravity Waves Observed at an Absolute Pressure Gauge Array. *J. Geophys.*

- 764 *Res. Ocean.*, 40–52. doi: 10.1002/2017JC013488
- 765 Vogel, R. M., & Shallcross, A. L. (1996, jun). The moving blocks bootstrap
766 versus parametric time series models. *Water Resour. Res.*, 32(6), 1875–
767 1882. Retrieved from [http://engineering.tufts.edu/cee/people/vogel/
768 documents/moving-blocks.pdf](http://engineering.tufts.edu/cee/people/vogel/documents/moving-blocks.pdf)<http://doi.wiley.com/10.1029/96WR00928>
769 doi: 10.1029/96WR00928
- 770 Wielandt, E., & Forbriger, T. (1999). Near-field seismic displacement and tilt asso-
771 ciated with the explosive activity of Stromboli. *Ann. Geophys.*, 42(3), 407–416.
772 doi: 10.4401/ag-3723
- 773 Williams, C. A., & Wadge, G. (2000). An accurate and efficient method for includ-
774 ing the effects of topography in three-dimensional elastic models of ground
775 deformation with applications to radar interferometry. *J. Geophys. Res.*,
776 105(B4), 8103–8120. doi: 10.1029/1999JB900307
- 777 Yuan, X., Kind, R., & Pedersen, H. (2005). Seismic monitoring of the Indian Ocean
778 tsunami. *Geophys. Res. Lett.*, 32(15), L15308. doi: 10.1029/2005GL023464