

1 Time-dependent forecast of large earthquakes  
2 from physics-informed probabilistic approach  
3

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23 **Abstract**

24 **The elastic energy that fuels large earthquakes accumulates hetero-**  
25 **geneously along faults, resulting in complex earthquake occurrence**  
26 **patterns. Although earthquake cycle simulations help capture such**  
27 **complexity in seismic hazard models, their high computational cost**  
28 **prevents widespread use and uncertainty quantification. Here, we**  
29 **propose a physics-based probabilistic method to forecast the timing**  
30 **and magnitude of large earthquakes. The method combines fracture**  
31 **mechanics theory and observational constraints on seismic coupling,**

32 historical seismicity and fracture energy to forecast the arrest loca-  
33 tions of long ruptures that have saturated the seismogenic depth. We  
34 apply this approach to estimate the time-dependent probability of  
35 earthquakes exceeding M8.5 across the entire Chilean subduction zone.  
36 Sensitivity analysis shows the most critical model parameter relates to  
37 the scaling between fracture energy and slip. We constrain the model  
38 parameters by matching the time between mega-earthquakes on the  
39 Valdivia segment, validate the constrained model based on the seis-  
40 micity of other segments, then apply it prospectively over the whole  
41 Chile megathrust. Our results highlight how earthquake potential on  
42 a given megathrust segment can be altered by earthquakes on neigh-  
43 boring segments, which reduce the energy available for multi-segment  
44 ruptures. The proposed physics-informed framework constitutes a new  
45 approach for time-dependent seismic hazard analysis on large faults.

## 46 1 Introduction

47 Estimating the frequency and size of future earthquakes is critical for seismic hazard  
48 assessment. This requires defining not only where and when earthquakes can start,  
49 but also where their ruptures will stop, which is not trivial on very long faults with  
50 multiple segments that might rupture simultaneously [1].

51 Current time-dependent models used in seismic hazard assessment are a statisti-  
52 cal description of the expected time of the next earthquake depending on the time  
53 elapsed since the previous one [2]. Point process models are often applied on individ-  
54 ual fault segments, assumed disconnected and hosting characteristic earthquakes of  
55 a certain size [e.g. 3, 4]. Their controlling parameters, including the mean recurrence  
56 time and the deviation from periodic recurrence, can be constrained by past seismicity  
57 [5–7]. However, due to their oversimplified assumptions, such models poorly describe  
58 sequences of earthquakes with rupture extents that might breach segment barriers and  
59 overlap [2, 8].

60 One important factor controlling the propagation and final size of earthquakes is  
61 the elastic energy available around the fault [9], which is generally space- and time-  
62 dependent due to tectonic stress accumulation, non-planar fault geometry, and the

63 continuous stress redistribution by seismic activity and fault creep. Interseismic cou-  
64 pling maps inferred from geodetic observations [10, 11] allow to identify areas that  
65 accumulate slip deficit, thus elastic energy, and can potentially host future large earth-  
66 quakes [12, 13]. Although slip deficit informs about the maximum slip that future  
67 earthquakes can release at any given point on the fault, it does not directly inform  
68 about where a rupture will stop, hence its final magnitude. Coulomb stress change  
69 analyses of interactions between fault segments [e.g. 14, 15] have been used to assess  
70 whether a rupture can jump from one segment to another, but they do not allow  
71 to evaluate whether a jumping rupture will propagate further along the receiving  
72 segment.

73 Incorporating the physics of earthquake rupture dynamics is a promising avenue to  
74 advance earthquake hazard assessment [16, 17]. A recent extension of fracture mechan-  
75 ics theory to elongated ruptures (length  $>$  width), relevant for large earthquakes that  
76 saturate the seismogenic width, provides a framework to evaluate whether a section  
77 of a fault tends to hinder or fuel rupture propagation [9]. Important implications of  
78 this theory were discussed for a segment of the Chilean subduction zone [18] and  
79 for a crustal fault system in China [19] using coupling maps to constrain the elas-  
80 tic energy available along the fault. Here, we take a major step towards integrating  
81 this theoretical framework into seismic hazard analysis by developing a method that  
82 generates millions of earthquake scenarios, enabling the probabilistic assessment of  
83 time-dependent earthquake potential across the entire length of a fault with exhaustive  
84 uncertainty quantification.

85 In this study, we apply this extension of fracture mechanics to assess the rupture  
86 potential of the entire Chilean subduction megathrust. Its historical earthquake record  
87 spans 500 hundred years (Fig. 1a) [e.g. 20–24], its paleo-seismological record at least  
88 two millennia [e.g. 25, 26], and available interseismic coupling maps cover the entire  
89 region (Fig. 1b) [e.g. 12, 20, 27–29]). The available dataset is therefore adequate to

90 calibrate and validate the framework. Additionally, coupling ratio and seismogenic  
91 depth vary along strike allowing us to examine the influence of the segmentation of  
92 the seismogenic megathrust on the earthquake potential (Fig. 1c).

93 We evaluate the sensitivity of our framework to parameter uncertainties, revealing  
94 that the key parameter is the coefficient that controls the scaling of fracture energy  
95 with slip. We constrain the model parameters by confronting our model to the observed  
96 earthquake record of the well-studied Valdivia segment, which hosted the giant M9.5  
97 1960 earthquake. Using this constrained model, we evaluate the spatial and temporal  
98 evolution of the probability of occurrence of an earthquake of a certain size along the  
99 whole Chile subduction, for retrospective validation and prospective forecasting. These  
100 results illustrate how a physics-based model can inform probabilities of earthquake  
101 occurrence, hence seismic hazard studies, especially in current seismic gaps where large  
102 earthquakes are overdue [30–32].

## 103 **2 Determining the rupture extent of elongated** 104 **earthquakes**

105 Once a rupture has saturated the seismogenic width of a fault ( $W$ ), it can only con-  
106 tinue growing by propagating horizontally. In the fracture mechanics theory of such  
107 elongated ruptures [9, 18], the propagation and arrest of a rupture are controlled by  
108 the ratio  $G_c/G_0$  between fracture energy  $G_c$  and elastic energy release rate  $G_0$ . A fault  
109 section hinders rupture propagation if it satisfies  $G_c/G_0 > 1$ ; otherwise, it fuels the  
110 rupture. This energy ratio varies along the fault and evolves through the interseismic  
111 period. Given the spatial distribution of  $G_c/G_0$  along a fault, the rupture arrest loca-  
112 tions are determined by a criterion based on a “rupture potential”,  $\Phi$ , defined at any

113 along-strike location  $L$ , relative to an arbitrary reference location, 0:

$$\Phi(L) = \int_0^L \frac{1 - G_c/G_0}{W} dL. \quad (1)$$

114 An elongated bilateral rupture starting at position  $L_0$  will stop at the positions  $L_-$   
115 and  $L_+$  where the rupture potential is the same as that of the hypocentral region, i.e.  
116 where  $\Phi(L_0) = \Phi(L_-) = \Phi(L_+)$ , as illustrated in Fig. S6.

117 Our estimates of the energy ratio are constrained by the slip deficit derived from  
118 maps of interseismic coupling ( $\chi$ ). As a conservative approach, we assume that ruptures  
119 involve a coseismic slip  $D$  equal to the whole slip deficit accumulated at a time  $t$  since  
120 the last large event,  $D = \chi V_{plate} t$ , where  $V_{plate}$  is the long-term slip rate. At each  
121 location on the fault, the oldest known large event sets the onset time for our modeling  
122 (e.g., in Chile, 1575 for the Valdivia segment and 1995 for the Antofagasta segment;  
123 Fig. 1a).

124 For sub-shear ruptures, the elastic energy release rate is approximately [18]

$$G_0 \approx C(\theta, \nu) ((1 - \nu)^{-1} \cos^2 \theta + \sin^2 \theta) \mu (\chi V_{plate} t)^2 / W \quad (2)$$

125 where  $\mu$  is the shear modulus,  $\theta$  the rake angle,  $C(\theta, \nu)$  a geometric factor of order  
126 1 given by Eq. 3, and  $\nu = 0.25$  the Poisson's ratio. The parameters involved in this  
127 equation are quite well constrained by geophysical observations in Chile (Methods),  
128 and only the coupling ratio  $\chi$  and seismogenic width  $W$  are considered here to vary  
129 along-strike.

130 We relate fracture energy  $G_c$  to coseismic slip  $D$  using a compilation of estimates  
131 derived from laboratory experiments, geological measurements, seismological data, and  
132 numerical modeling [33] (Fig. S1). Since we focus on large megathrust earthquakes, we  
133 consider estimates obtained from seismological data for  $D > 0.1$  m. We fit a scaling

134 law of the form  $G_c \approx BD^n$ , where  $G_c$  is in  $\text{MJ.m}^{-2}$  and  $D$  is in meters, yielding  
135  $B = 2.60$  and  $n = 1.02$ . The value of  $n$  is close to 1, consistent with models of dynamic  
136 rupture with off-fault inelastic dissipation [34, 35].

137 Using these local estimates of  $G_c$  and  $G_0$  based on the slip deficit  $D$  accumulated  
138 since the last rupture, we evaluate the time- and space-dependent seismogenic poten-  
139 tial. We assume earthquakes can nucleate anywhere on the seismogenic zone and, at  
140 a given time  $t$ , we examine a comprehensive set of earthquake scenarios spanning all  
141 possible hypocenter locations on the megathrust (Fig. S5). In each scenario, we con-  
142 sider a "saturating earthquake", i.e. one whose rupture has already grown enough to  
143 saturate the seismogenic zone, and use our model to predict where the rupture will  
144 stop and the final earthquake magnitude. In particular, for a given epicenter location,  
145 we compute the rupture potential  $\Phi(L)$  along the fault and then use it to determine  
146 the rupture arrest points  $L_-$  and  $L_+$  (e.g., Fig. S6). A more detailed description of  
147 the procedure is provided in the Method section. Owing to the small computational  
148 cost of our approach, we can thoroughly consider millions of earthquake scenarios at  
149 any given time, as needed for probabilistic analysis and uncertainty quantification.

### 150 3 Parameter Sensitivity Analysis

151 We evaluate how the uncertainties in model input parameters affect model results, by  
152 focusing on a key model outcome: the "critical time"  $T_c$  when a fault section reaches  
153 the condition  $G_0 > G_c$  required to fuel rupture propagation. Since  $G_c/G_0 \propto D^{n-2}$   
154 with  $n - 2 < 0$ , the energy ratio decreases over time as slip deficit  $D$  accumulates,  
155 from very high values ( $G_c/G_0 \gg 1$ ) soon after a large earthquake to values promoting  
156 rupture propagation ( $G_c/G_0 < 1$ ) after a finite time  $T_c$  given by Eq. 4 (Methods). For  
157 a given distribution of model parameters (Fig. 2), characteristic of those constraining  
158 our model in Chile, we compute the corresponding distribution of  $T_c$ . This approach

159 allows us to evaluate the effect of the chosen parameter values on the transition time  
160 at a given position along the fault.

161 Two sensitivity analyses are performed: (1) we fix the value of one parameter and  
162 evaluate the effect of the uncertainties of the remaining ones (Fig. 2g); (2) we fix all  
163 parameters but one and evaluate the effect of the uncertainty of this single parameter  
164 (Fig. 2h). In the first analysis, the coefficient  $B$  of the scaling between fracture energy  
165 and slip is the only parameter that, if fixed, leads to a significant change in the  
166 probability density function (PDF) of  $T_c$  (Fig. 2g). In the second analysis, the PDF of  
167  $T_c$  obtained when varying only  $B$  is very similar to the PDF obtained by varying all  
168 the parameters. Thus, the distribution of  $T_c$  is primarily controlled by the uncertainty  
169 on  $B$ , which in turn is likely due to the high uncertainties in estimates of  $G_c$  for  
170 natural earthquakes and their intrinsic variability [33]. The other parameters have a  
171 significantly smaller effect on  $T_c$ . For instance, for this example, varying  $B$  modulates  
172  $T_c$  between  $\sim 30$  and 1610 yrs, while varying  $W$  modulates  $T_c$  between  $\sim 200$  and 280  
173 yrs and varying  $\theta$  has almost no impact.

174 Given the critical role of  $B$ , it is crucial to continue collecting and improving  
175 estimates of  $G_c$  and  $D$  for large earthquakes. Next, we show how to further constrain  
176  $B$  using historical data.

## 177 **4 Constraining the scaling relation between fracture** 178 **energy and slip**

179 To better constrain  $B$ , we confront the results of the time and space-dependent seis-  
180 mogenic potential model with the sequence of major earthquakes on the Valdivia  
181 segment in southern Chile (Fig. 1a). Paleo-seismological evidence indicates an earth-  
182 quake recurrence time of 250-350 years during the last 2 millennia, with the latest  
183 major events being the 1960  $M_w$  9.5 event and a large megathrust earthquake in 1575

184 [25, 36]. Two other relatively large events occurred in 1737 and 1837, but likely rup-  
185 tured only a limited portion of the segment [25]. The slip deficit accumulated since  
186 1575 is consistent with the slip estimated for the 1960 earthquake ( $\sim 20\text{-}35$  m; [37]).

187 At any given time after 1575, we use our model to test whether hypothetical satu-  
188 rating earthquakes that contain the 1960 Valdivia earthquake epicenter can propagate  
189 further and rupture the portion of the Valdivia segment south of latitude  $38^\circ\text{S}$ . This  
190 procedure allows to avoid using the portion of the Valdivia segment that overlaps with  
191 the Maule earthquake of 1751 as a constraint, as the lateral extent of this earthquake  
192 is uncertain. For the 1960 earthquake to occur in our model, the segment needs to be  
193 ready to break before this date. The subset of  $B$  values consistent with this constraint  
194 is shown in Fig. 3 (dark blue PDF). The result for all parameters is shown in Fig. S2.  
195 If we assume that the 1960 earthquake occurred immediately after the segment was  
196 ready, the subset of admissible  $B$  values is even tighter (light blue PDF; Fig. S2). This  
197 constrained PDF aligns well with the  $G_c - D$  scaling data (gray histogram in Fig. 3)  
198 and its fit (Section 2; Fig. S1). This cross-validation comforts us that the range of  $B$   
199 constrained by assuming the fault is ready exactly in 1960 is reasonable; therefore, we  
200 use it in the remainder of this study.

## 201 **5 The seismogenic potential of the Chile subduction** 202 **megathrust**

203 We now assess the time- and space-dependent seismogenic potential along the whole  
204 Chile subduction zone. We account for the spatial variation and uncertainties of the  
205 parameters (Methods), focusing on scenarios consistent with the 1960 earthquake  
206 occurring immediately after the southern portion of the Valdivia segment is ready.  
207 This approach constrains the values of  $B$  explored as well as the other parameters in

208 a self-consistent way (Fig. S2). At each time, 19 million scenarios are evaluated, con-  
209 sidering 915 potential initial rupture and nucleation positions and probing parameter  
210 uncertainties using 21,000 random samples (Fig. S5).

211 We first evaluate the PDF of the critical time  $T_c$  at each latitude (Fig. 4b) and  
212 find an overall consistency with the activity of the major segments of the Chilean sub-  
213 duction zone. Along the Valdivia segment, the mode of  $T_c$  (red line in Fig. 4b) falls  
214 slightly before the occurrence of the 1960 earthquake, by design of our calibration of  
215 model parameters. Along the Maule segment, the mode of  $T_c$  roughly matches the  
216 timing of the 2010 earthquake. Its spatial variation reflects changes in coupling, yield-  
217 ing larger  $T_c$  values (i.e. later readiness) in the northern part of the Maule segment,  
218 which may explain why the 2010 event did not extend further north. To the south,  
219 the low available potential energy due to the 1960 Valdivia earthquake contributes to  
220 hinder the southward propagation of the Maule earthquake.

221 Along the Valparaiso segment, when the 2015 Illapel earthquake broke the seg-  
222 ment only partially, the model indicates that a full-segment rupture was most likely  
223 but partial-segment ruptures remained significantly probable. Along the Iquique seg-  
224 ment, the 2014 earthquake occurs when the segment is not completely ready, which  
225 is consistent with the fact that the event saturated the seismogenic zone but did not  
226 propagate further. The rough timing constraints derived from  $T_c$  highlight that our  
227 model captures to first order relevant factors governing rupture propagation and tim-  
228 ing in these segments. Other interpretations of the sequence of old earthquakes might  
229 lead to different results, as discussed in the Method section, which could be handled  
230 by accounting for uncertainties on paleo-seismic data in our approach.

231 Moving forward from the analysis of the critical time  $T_c$ , we evaluate whether  
232 saturating earthquakes can propagate further and become very large earthquakes.  
233 Considering the moment-area scaling law [38], saturating ruptures in Chile have a  
234 minimum magnitude  $M_{SAT} \approx 8.0-8.3$  (Methods). We hence consider our results for

235 events with magnitude above 8.3. We compute the probability  $P_{M>X|SAT,t}$  that a fault  
 236 location can participate in a saturating event that grows to a magnitude exceeding  
 237  $X$ , at time  $t$  (Methods). Fig. 4c shows the space-time evolution of  $P_{M>8.5|SAT,t}$  while  
 238 Fig. 4d shows the temporal evolution of its mean within each segment. This analy-  
 239 sis reveals the influence of the interconnection between segments. If a fault segment  
 240 were isolated from the rest of the fault, its  $P_{M>8.5|SAT,t}$  would increase gradually (e.g.  
 241 black dashed line in Fig. 4e). Because ruptures can break through segment bound-  
 242 aries, the evolution of the rupture potential of a segment influences the evolution of  
 243  $P_{M>8.5|SAT,t}$  on other segments (Fig. 4d). For instance, along the Copiapo segment,  
 244  $P_{M>8.5|SAT,t}$  decreases after the 1960 Valdivia, 2010 Maule and 2015 Illapel earth-  
 245 quakes because these events reduce the energy available in their segments, which in  
 246 turn reduces the likelihood of multi-segment ruptures reaching the Copiapo segment.  
 247 Furthermore, the increase in  $P_{M>8.5|SAT,t}$  on the Copiapo segment at the beginning  
 248 of the loading period (between 1906 and 1960) is faster than if the segment was iso-  
 249 lated (see Fig. 4e). High values of  $P_{M>8.5|SAT,t}$  initially concentrated at the southern  
 250 border of the Copiapo segment gradually expand northward over time (Fig. 4c). This  
 251 results from the progressive loading of the Valparaiso, Maule and Valdivia segments  
 252 which increases the likelihood of a large earthquake initiating within these regions and  
 253 propagating through the Copiapo segment.

## 254 **6 Towards Efficient Physics-Based Seismic Hazard** 255 **Assessment**

256 While we do not attempt to predict the exact time and magnitude of the next large  
 257 earthquake, our model provides a probabilistic forecast based on a physical and statis-  
 258 tical approach that is consistent with the observed earthquake history. It specifically  
 259 accounts for the spatial variability of energy along a fault due to differences in coupling  
 260 and the timing of previous large earthquakes.

261 In particular, our approach yields the conditional probability  $P_{M>X|SAT,t}$  of the  
262 occurrence of an earthquake above magnitude  $X$  at time  $t$ , provided that it has already  
263 developed into a saturating event. The probability of occurrence of an elongated earth-  
264 quake above magnitude  $X$  is  $P_{M>X} \cap SAT = P_{M>X|SAT,t} \times P_{SAT}$ , where  $P_{SAT}$  is  
265 the inter-event time probability of saturating events since their last occurrence, eval-  
266 uated over a specified time interval centered at time  $t$ .  $P_{SAT}$  depends on the rate of  
267 occurrence of saturating events and we propose in the Method section two alternative  
268 approaches to evaluate it.

269 Our model can incorporate possible dependencies of  $P_{SAT}$  on location along the  
270 fault and on time since the last large earthquake. For example, Fig. S3 shows  $P_{SAT}$ ,  
271  $P_{M>X|SAT,t}$  and  $P_{M>X} \cap SAT$  for a mean rate of saturating events of  $1/90 \text{ yrs}^{-1}$ ,  
272 assuming the occurrence of saturating events follows a random Poisson process.

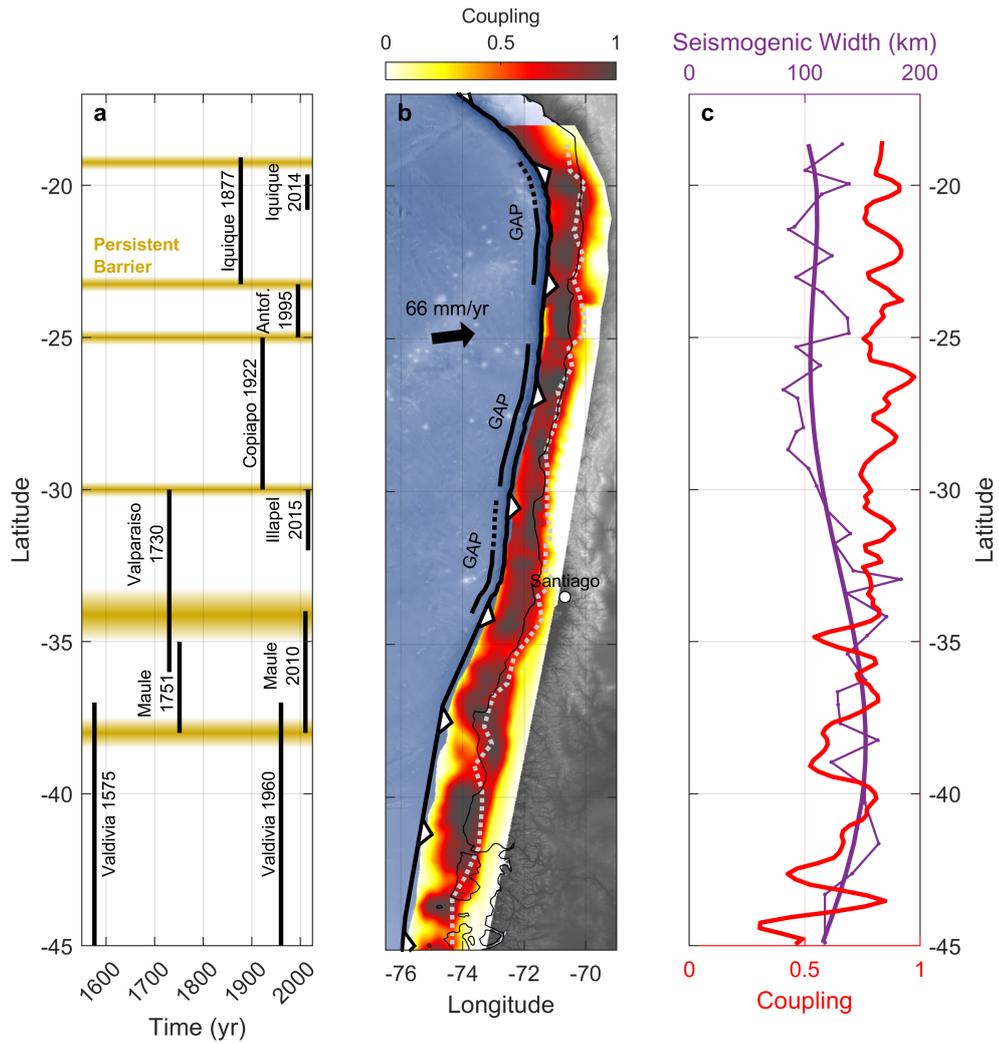
273 The rate of occurrence of saturating events is a crucial model input to assess  
274 seismic hazard. If it is very low, the fault will remain unbroken until it is ready to host  
275 full-segment events, and ruptures will rarely stay at  $M_w = M_{SAT}$ , they will rather  
276 propagate into large events. Conversely, if the rate of saturating events is extremely  
277 high, the fault will rarely be ready to host large events, and magnitudes will remain  
278 close to  $M_{SAT}$ . Examples of these end-member behaviors might be the Cascadia [39]  
279 and Vanuatu [40] subduction zones, respectively. Thus, the rate of saturating events  
280 is expected to control the shape of the magnitude-frequency distribution of very large  
281 earthquakes.

282 Beyond the probabilities discussed above, our framework provides a generative  
283 model of earthquake scenarios for practical hazard assessment. This framework can  
284 be used to generate catalogs of large earthquakes, in particular their rupture location,  
285 rupture history and final slip distribution. These rupture scenarios can be readily  
286 combined with ground motion models to evaluate site-specific hazard and produce  
287 regional (time-dependent) hazard maps.

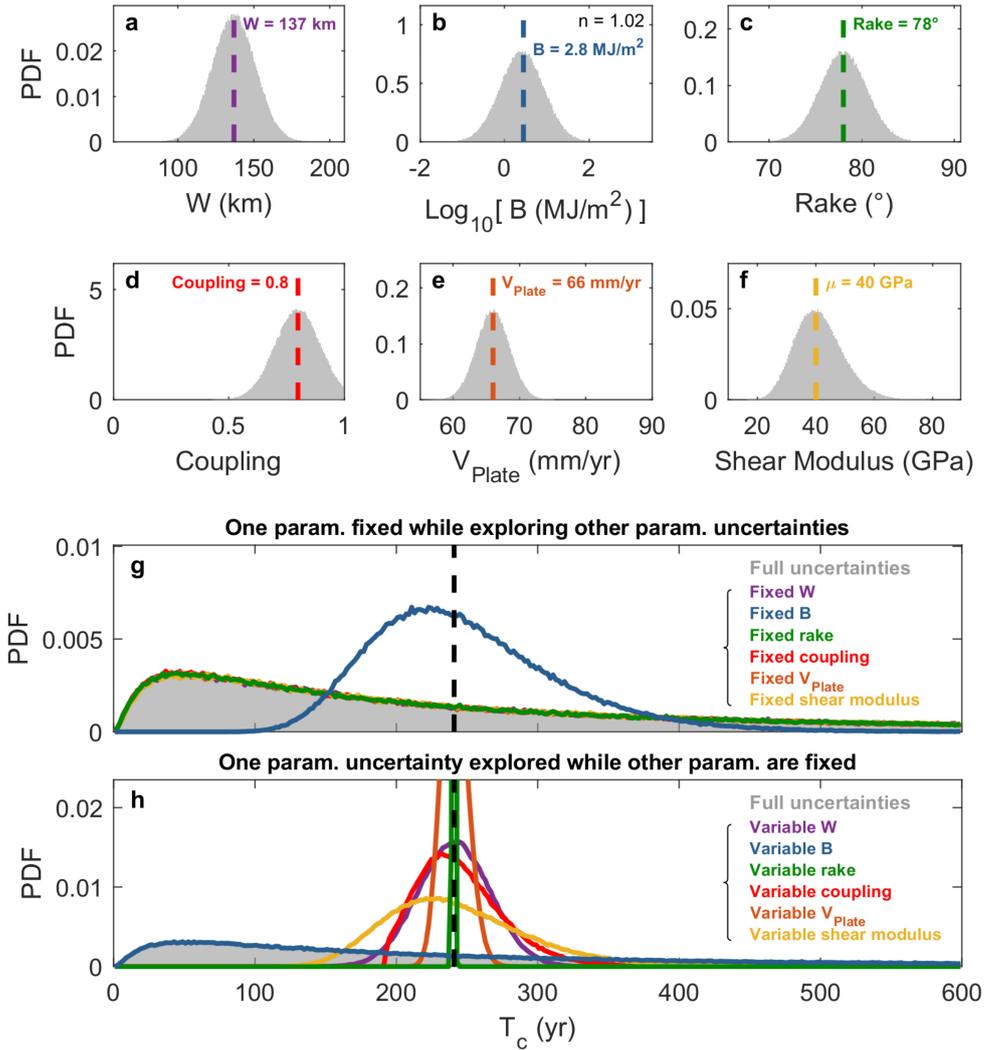
288 As a compromise to develop a computationally-efficient model, strong assumptions  
289 are made to simplify the complex and evolving behavior of natural faults. We assume  
290 that slip deficit accumulates over interseismic periods at a steady rate that is spatially  
291 prescribed by a coupling distribution inverted from recent (~30 years) geodetic data.  
292 We also assume that this slip deficit is fully released by large earthquakes, ignoring  
293 static and viscoelastic stress transfer after each earthquake [41], the occurrence of  
294 slow slip events [42–44], and super-cycle behavior with coseismic slip undershooting or  
295 overshooting the slip deficit [45]. Moreover, the model does not currently consider non-  
296 planar fault geometry, frictional heterogeneities or other types of obstacles that could  
297 hinder the propagation of earthquakes [e.g. 46–49]. Last but not least, uncertainties in  
298 the occurrence time and rupture extent of old large earthquakes in the historical and  
299 paleoseismic records are substantial [22–24] and remain to be integrated in our model.

300 Although crucial, many of these limitations are partially accounted for by paramete-  
301 ter uncertainties. Moreover, most of these biases and missing elements can be addressed  
302 through future research and each ingredient of the framework can be refined. Ongo-  
303 ing and continuous efforts to improve our knowledge of faults —in particular fracture  
304 energy, fault coupling and seismogenic width —and past earthquakes are critical for  
305 seismic hazard assessment. Applying the approach to other subduction zones would  
306 further constrain and test the model. Such efforts could lead, for instance, to establish  
307 relations between model parameters controlling fault behavior, in particular the energy  
308 scaling coefficient  $B$ , and observable physical properties along subduction zones, such  
309 as seafloor roughness, sediment thickness or seismic wave speeds. The approach could  
310 also be tested prospectively on Slow Slip Events [50], owing to their short recurrence  
311 times, and for which many earthquake cycles involving multiple megathrust segments  
312 have been recorded.

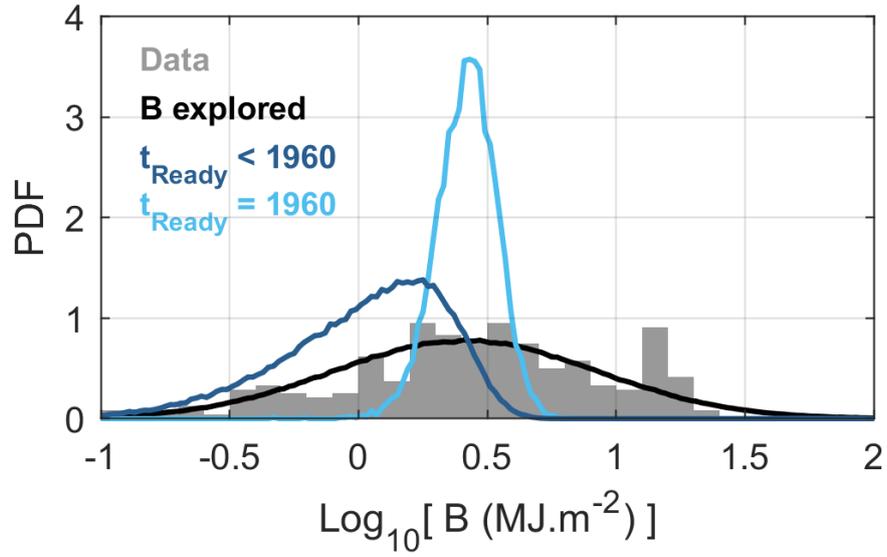
313 Our study demonstrates that combining a physics-based model with statistical  
314 analysis provides a quantitative framework to assess the seismogenic potential of sub-  
315 duction zones. The application to the Chile subduction zone highlights how fault  
316 interactions can modulate the seismogenic potential in space and time, offering a new  
317 perspective on space- and time-dependent seismic hazard assessment. The framework  
318 can reveal regions that are more susceptible to host large earthquakes, helping to  
319 establish hazard mitigation measurements in a more effective and organized manner.  
320 It could also potentially be used in early warning systems as prior information to  
321 forecast the final size of a rupture that has just saturated the seismogenic zone.



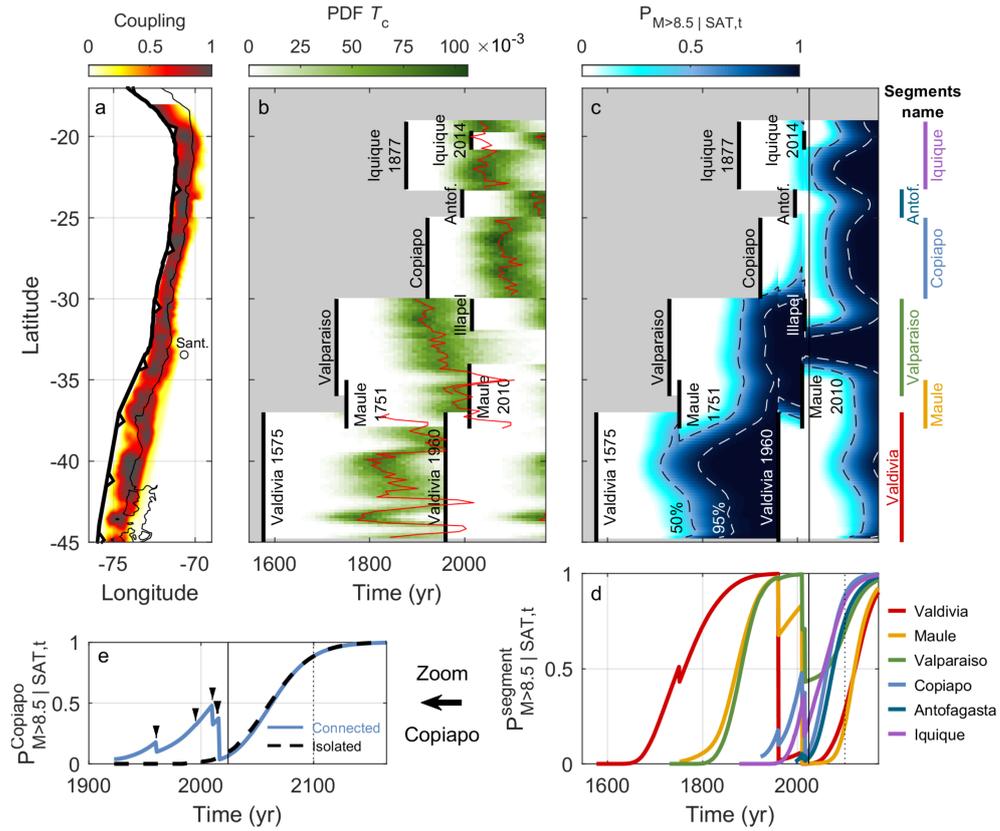
**Fig. 1 Overview of the Chilean subduction zone. (a)** Past seismicity and fault segmentation (modified from [20]). Rupture extent and occurrence time of historic earthquakes are indicated by black bars. Areas identified as persistent barriers to the propagation of earthquakes are shown in yellow. **(b)** Interseismic coupling along the Chilean subduction interface (yellow to brown shading, [12, 20, 27–29]), seismogenic depth estimated from seismicity distribution (light gray dotted curve) and current seismic gaps. Thin and thick black lines indicate the coast and the subduction trench, respectively. **(c)** Lateral distributions of seismogenic width (thick purple curve), its smoothed version (thin blue curve), and depth-averaged interseismic coupling (red curve).



**Fig. 2 Sensitivity of critical time  $T_c$  to uncertainties in model parameters.** (a-f) PDF prescribed for each parameter, uniformly along strike. We draw randomly 300,000 combinations of parameters from these PDFs. (g) PDFs of  $T_c$  accounting for the uncertainties of all parameters but one. (h) PDFs of  $T_c$  accounting for the uncertainty of a single parameter. The colored vertical dashed lines in panels (a) to (f) indicate the fixed parameter values selected for the sensitivity tests. The gray histograms in (g) and (h) are the PDFs of  $T_c$  accounting for the uncertainties of all parameters.



**Fig. 3 Constraint on the fracture energy versus slip scaling coefficient  $B$  based on the Valdivia segment earthquake sequence.** (Gray) empirical distribution of  $B$  based on estimates of  $G_c$  and  $D$  from seismological data compilation [33] (Fig. S1) and (black) its smooth approximation. Distribution of  $B$  according to different constraints: assuming the Valdivia segment is ready to host full-segment ruptures (dark blue) any time before the 1960 Mw 9.5 earthquake and (light blue) right in 1960.



**Fig. 4 Seismogenic potential of the Chilean subduction.** (a) Coupling map of the Chilean subduction zone ([12, 20, 27–29]). The black thick and thin lines represent the trench and coast, respectively. The white dot indicates the city of Santiago. (b) PDF of critical time  $T_c$  (green color scale) and its mode (red curve) at each latitude. (c) Spatio-temporal evolution of  $P_{M>8.5|SAT,t}$ , the probability of a portion of the fault to host  $M_w > 8.5$  events, knowing they already succeeded to saturate the seismogenic zone. The 50% and 95% iso-probabilities are indicated by the black and white dashed lines, respectively. The vertical thin black line indicates the year 2025. The gray shaded areas in panels (b) and (c) indicate the spatio-temporal zones that are not considered in the analysis, and where seismic events are not allowed to propagate. The colored vertical lines on the right of panel (c) indicates the extent of the segments considered. (d) Temporal evolution of the mean  $P_{M>8.5|SAT,t}$  along each segment. (e) Zoom of the temporal evolution of mean  $P_{M>8.5|SAT,t}$  of the Copiapó segment. The solid blue and dashed black lines correspond, respectively, to the scenarios where the Copiapó segment is fully connected to all other segments and completely isolated from them. The inverted black triangles indicate the occurrence of large earthquakes on neighboring segments. The vertical full and dashed black lines in panels (d) and (e) indicate the years 2025 and 2100, respectively.

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## 334 **Methods**

### 335 **Determination of model parameters and their uncertainties**

336 We present here the data used to evaluate the distributions of  $G_0$  and  $G_c$  along the  
337 Chilean subduction zone.

338 The seismogenic width ( $W$ ) of the Chilean megathrust is defined at any position  
339 along-strike as the along-dip distance between the trench location and the down-  
340 dip limit of shallow interplate thrust events in the instrumental seismicity record.  
341 From the CMT Harvard Catalog, we select the events consistent with slab interface  
342 faulting by applying two criteria: (1) a plunge of the tension axis larger than 45  
343 degrees, corresponding to thrust events, and (2) depth between 20 km above and 25 km  
344 below the plate interface given by the Slab 2.0 model, to discard crustal thrust events  
345 while accounting for the vertical uncertainty of earthquake locations. In addition,  
346 for a more complete coverage of the entire margin, we consider focal mechanisms of  
347 small earthquakes, mainly on the Southern Andes [51]. The combined catalog contains  
348 500 earthquakes. For each 0.6 degrees latitude bin, we define the down-dip limit of  
349 interplate seismicity by the location of the easternmost event. Based on the distance  
350 between this boundary and the trench ( $dt$ ), we estimate the seismogenic width as

351  $W = dt/\cos(dip)$ . We find a down-dip limit between 40 and 60 km depth, based on  
 352 the pattern of seismicity and focal mechanisms ([52]; Fig. S4). We observe a lateral  
 353 change at about 30°S (Fig. 1c):  $W$  is roughly 100 km north of this latitude and  
 354 increases to 150 km to the south. These results agree well with previous estimates of  
 355  $W$  [53] and help explain why Chile hosted larger earthquakes in the south than in the  
 356 north. We represent the uncertainties on  $W$  by a Gaussian distribution centered on  
 357 the spatially smoothed version of  $W$  (Fig. 1c) with standard deviation of 14 km (i.e.  
 358 the standard deviation of the difference between the rough and smoothed distributions  
 359 of  $W$ ). Smoothing is achieved by fitting a polynomial function of degree 3 to the  $W$   
 360 distribution along strike.

361 The plate rate  $V_{plate}$  and rake  $\theta$  are assumed uniform along the whole subduction  
 362 and their distributions are prescribed as follows. The PDF of  $V_{plate}$  is a Gaussian  
 363 function with a mean and standard deviation equal to  $66 \pm 2.5$  mm/yr, roughly the  
 364 convergence rate between the Pacific and South American plates [e.g. 54, 55]. The  
 365 PDF of  $\theta$  is also taken as Gaussian with a mean and standard deviation of  $78 \pm 2.5^\circ$ ,  
 366 oblique to the subduction trench.

367 The distribution of coupling,  $\chi$ , along strike is estimated by depth-averaging across  
 368 the seismogenic width an interseismic coupling map compiled from various geodetic  
 369 studies [20] (Fig. 1). We take trench-perpendicular profiles of  $\chi$  spaced every 0.05  
 370 degrees, and calculate the average along each profile. Uncertainties on  $\chi$  are described  
 371 by a Gaussian distribution, with a mean value based on available coupling models (ref;  
 372 Fig. 1c) and standard deviation of 0.1, truncated between 0 and 1.

373 The shear modulus  $\mu$  is assumed constant over the whole subduction. Its PDF is  
 374 described as a log-normal distribution with mean of 55 GPa and standard deviation  
 375 of 8 GPa, from which we then subtract 14 GPa. This distribution increases at  $\sim 20$   
 376 GPa, peaks at 40 GPa, and then decreases down to  $\sim 70$  GPa. We set  $\nu = 0.25$ ,  
 377 and corresponding uncertainties are not explored. The geometric coefficient  $C(\theta, \nu)$  is

378 estimated as [18]

$$C(\theta, \nu) = \frac{\pi}{4} \sqrt{(1 - \nu)^2 \cos^2 \theta + \sin^2 \theta} \quad (3)$$

379 For the sensitivity analysis and to constrain the fracture energy-slip scaling, we  
380 explore the uncertainties of the scaling law by fixing the exponent  $n = 1.02$  and  
381 exploring the uncertainty of the prefactor  $B$ . The PDF of  $\text{Log}_{10}[B]$  is set as a Gaussian  
382 distribution with mean 6.41 and standard deviation of 0.51, based on the spread of  
383 available seismological data [33] (Fig. S1).

384 For the sensitivity analysis, we evaluate the effect of parameter uncertainties on  
385 the critical time  $T_c$  for a given point on the fault. The uncertainties of the PDFs  
386 are prescribed as explained previously. We do not explore the effect of the spatial  
387 variability of parameters and consider a mean coupling of 0.8 and mean seismogenic  
388 width of 137 km, the mean values along the Chilean subduction. The PDF of each  
389 parameter is shown in Figs. 2a-f.

390 In Section *The seismogenic potential of the Chile subduction megathrust*, the  
391 parameters, including  $B$ , follow different distributions that are based on the constraint  
392 developed in Section *Constraining the scaling relation between fracture energy and slip*  
393 (Fig. S2).

## 394 **Time and space-dependent evaluation of the seismogenic** 395 **potential**

396 We evaluate the seismogenic potential of a fault over time using the following procedure  
397 (Fig. S5). We discretize the fault along strike into a set of 20 km long subfaults, each  
398 spanning the whole seismogenic depth. At each time and for each possible hypocen-  
399 ter position along strike, we consider a set of ruptures that have initially saturated

400 the seismogenic width (initial length equal to initial width). We consider all possi-  
 401 ble positions of the saturating ruptures relative to the hypocenter. For each rupture,  
 402 we determine its final extent using the theoretical arrest criterion (see Section *Deter-*  
 403 *mining the rupture extent of elongated earthquakes*; Figs. S5 and S6). The seismic  
 404 moment of each earthquake is calculated as  $M_0 = \int \mu DWdL$ , integrated over its final  
 405 rupture extent.

406 From the ensemble of scenarios, we can compute various probabilities, for instance  
 407 the probability of an event exceeding a certain magnitude or breaking a whole segment  
 408 or breaking through a barrier. Here, we focus on the probability at time  $t$  of a subfault  
 409 to host earthquakes exceeding a certain magnitude, given that those earthquakes have  
 410 already saturated the seismogenic zone,  $P_{M>X|SAT,t}$ . At any given time, we compute  
 411 the probability  $P_{M>X|SAT,t}$  that a fault location can participate in an event of magni-  
 412 tude exceeding  $X$  as the ratio, among the earthquake scenarios that rupture this fault  
 413 location, between the number of events with  $M > X$  and the total number of events.

414 The magnitude  $M_{SAT}$  above which our model's assumption of elongated ruptures  
 415 is valid corresponds to the size at which earthquakes start to saturate the seismo-  
 416 genic zone. Here, we assume that such saturating earthquakes have a square rupture  
 417 area, with length and width equal to the seismogenic width. Considering the range of  
 418 seismogenic widths in Chile (thick purple line in Fig. 1c), from 104 to 153 km, and  
 419 using an empirical moment-area scaling relationship for dip-slip earthquakes [38], we  
 420 estimate that  $M_{SAT} \approx 8.0-8.3$ .

421 The critical time  $T_c$  after which a fault section promotes rupture propagation  
 422 instead of hindering it, derived from the condition  $G_c/G_0 = 1$ , is

$$T_c = \frac{1}{\chi V_{plate}} \left[ \frac{\mu C(\theta, \nu) ((1 - \nu)^{-1} \cos^2 \theta + \sin^2 \theta)}{BW} \right]^{1/(n-2)}. \quad (4)$$

## 423 **Determining the recurrence time of saturating events**

424 To evaluate  $P_{SAT}$ , we propose two alternative approaches. In the first approach, for  
425 a given segment, we directly take the observed rate of  $M_w \geq M_{SAT}$  events from  
426 the catalog, including events that started in other segments and propagated into the  
427 segment of interest. We further assume that their occurrence follows a Poisson process.  
428 In the second approach, we still assume that saturating events follow a Poisson process,  
429 but we match the rate of  $M_w = M_{SAT}$  events predicted by our model with their  
430 observed rate. This approach requires a generative model of earthquakes, based on  
431  $P_{M>X} \cap SAT$ , to extract the rate of  $M_w = M_{SAT}$  events.

## 432 **Discussion on the historical catalog**

433 The quality of the historical catalog used has an impact on the results. The catalog  
434 selected for this study is a simplified one, a choice discussed here. As an example  
435 of the influence of the catalog, we provide estimates using a catalog that includes  
436 three additional events: the 1835 Maule, 1819 Copiapo and 1943 Illapel earthquakes  
437 (Fig. S7). With this catalog,  $P_{M>X|SAT,t}$  on the Copiapo segment is close to 0 after  
438 the 1922 event because the 1943 Illapel earthquake has isolated the Copiapo segment  
439 from the energy available on the rest of the Valparaiso segment (Fig. S7c).

440 We assume that each event releases all the accumulated slip deficit. As a result,  
441  $P_{M>X|SAT,t}$  depends entirely on the most recent events that have occurred on each  
442 segment. After the 2015 Illapel earthquake, the evolution of  $P_{M>X|SAT,t}$  is identical  
443 for both the initial and updated catalogs since both contain the same most recent  
444 earthquakes on each segment (Fig. S7c). If, instead, we allowed a residual slip deficit  
445 after each event, the evolution of  $P_{M>X|SAT,t}$  after the 2015 Illapel earthquake might  
446 differ between the two catalogs.

447 The framework can also shed light on the interpretation of historical earthquakes.  
448 For example, it has been suggested that Copiapo's presumed-full-segment ruptures in

449 1819 and 1922 were actually due to multiple earthquakes [24]. Considering the short  
450 inter-event time between those two sequences, the model suggests that the fault did not  
451 have enough time to reload, which favors the interpretation of sequences of multiple  
452 ruptures rather than full-segment ruptures.

453 Finally, in our study, although along-strike heterogeneity in  $W$  and  $\chi$  was explored,  
454 the parameter  $B$  was held constant over the whole subduction. In our model, this  
455 parameter quantifies the fault strength, which can be spatially heterogeneous. Incorporating  
456 additional constraints from observed earthquake sequences might help constrain  
457 along-strike variation in the naturally tunable parameter  $B$ , and improve the model's  
458 forecast capability.

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## Supplementary Information

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### Time-dependent forecast of large earthquakes from

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### physics-informed probabilistic approach

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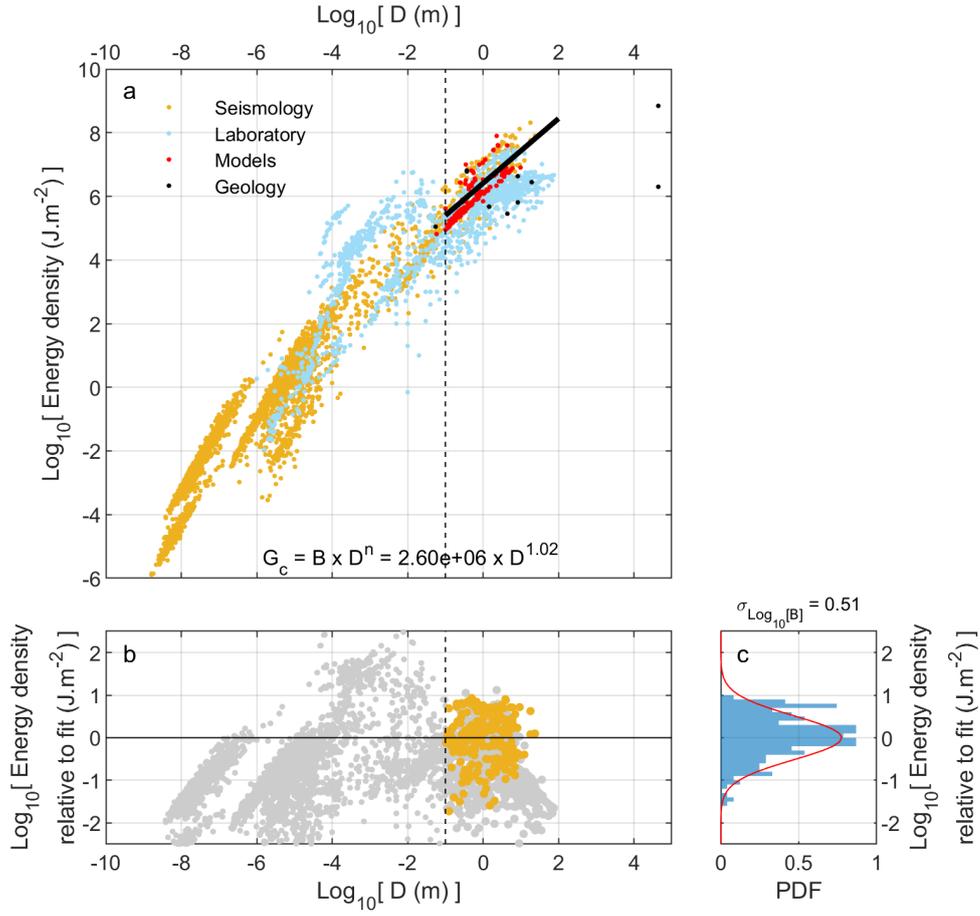
#### Text S1 Comparison between forecast and observed magnitudes

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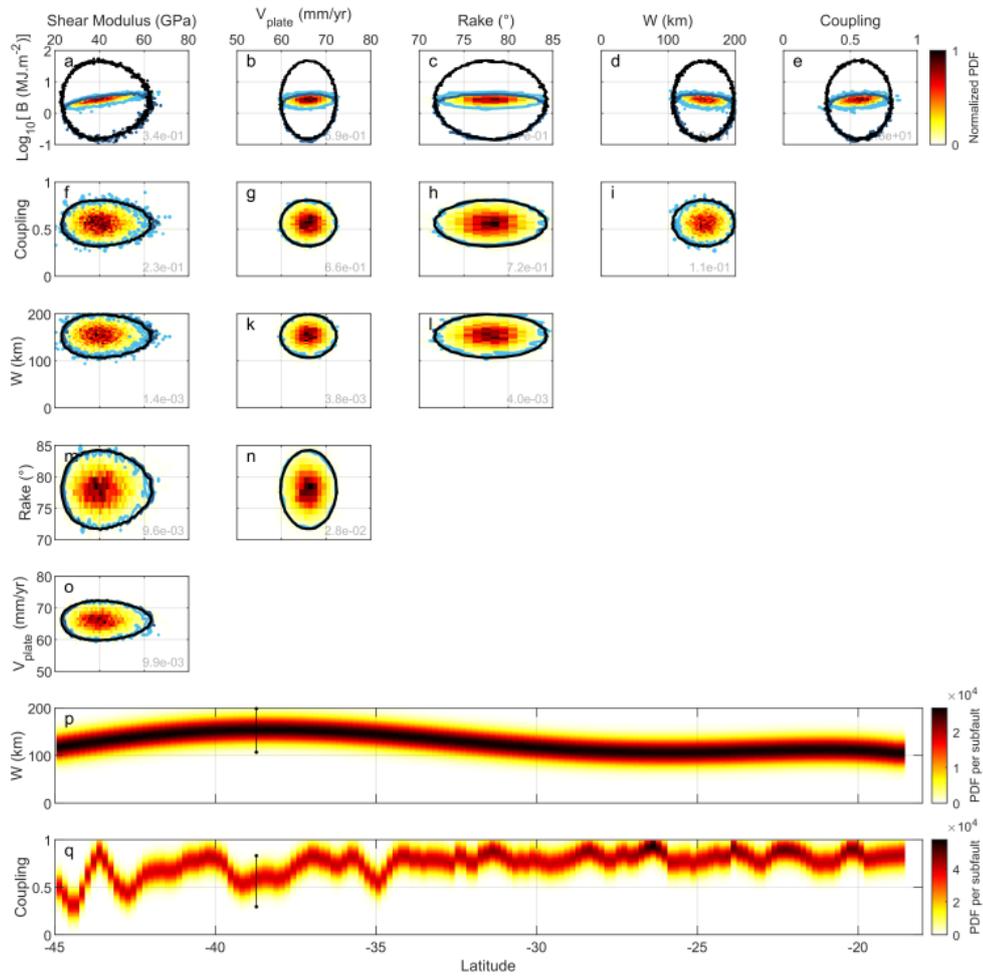
Here, we compare the forecast of the magnitude of past events with their observed values in the original catalog (Fig. S8) and in the updated catalog (Fig. S9). The magnitude forecast for the Valdivia 1960 earthquake is slightly lower than the observed one. This discrepancy can be partly explained by a maximum slip deficit of  $\sim 25$  m accumulated between the 1575 and 1960 events (assuming a loading rate of 66 mm/yr), which is further decreased when accounting for coupling (Fig. 1c), and therefore does not reach the observed 20-35 m slip of the 1960 event. For the 2010 Maule earthquake, the magnitude probability is multimodal, with the two largest peaks located at  $M_w \sim 8.6$  and 9.1 based on the original catalog. The latter corresponds to scenarios in which the event rupture extends to the Valparaiso segment. The model forecasts a  $M_w \sim 8.9$  for the 2015 Illapel earthquake which was actually a  $M_w \sim 8.3$  event. This overestimation arises because, in the original catalog, no earthquakes are recorded between the 1730 Valparaiso event and 2015, resulting in a large accumulated slip deficit. Moreover, most of the forecast ruptures involve the rest of the Valparaiso segment. The inclusion of the 1943 event in the updated catalog (Fig. S7) helps correct this overestimation to some extent (Fig. S9). Finally, the 2014 Iquique earthquake, along with its main aftershock, falls within the forecast magnitudes, although some debate remains about the overlap between the 1877 and 2014 events [23, 56]. When additional earthquakes are incorporated - as in the updated catalog - the forecast magnitudes change because each added event resets the available elastic energy within its rupture extent and can isolate certain segments from available elastic energy on neighboring segments.

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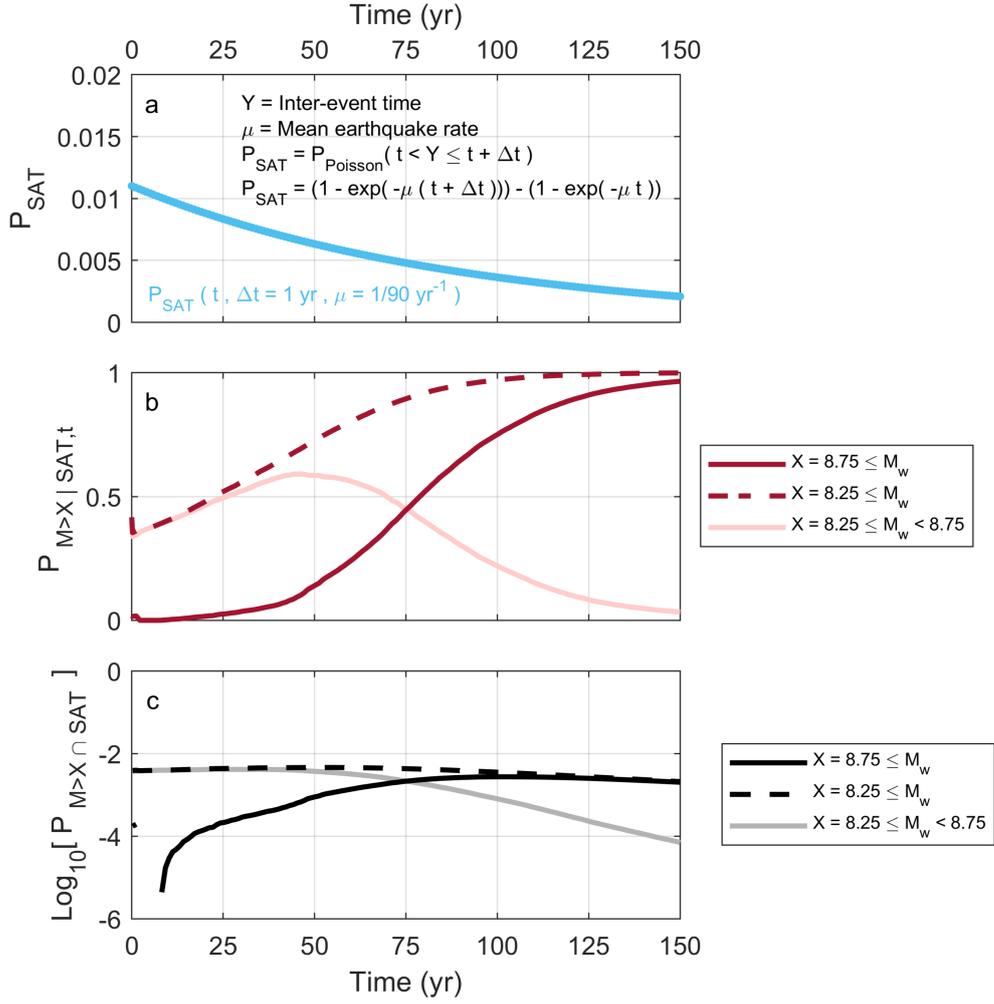
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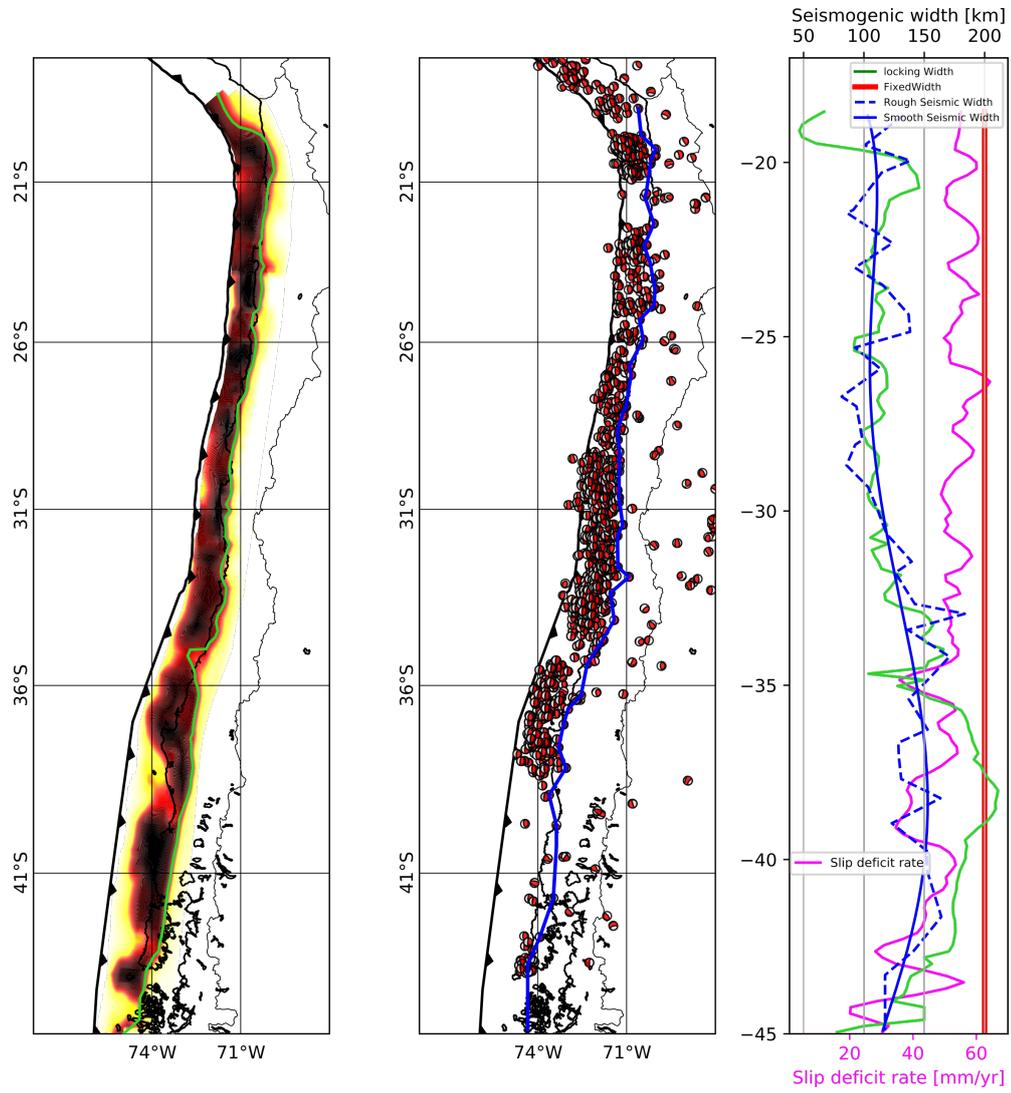
**Fig. S1 Scaling relation between fracture energy and final slip.** (a) Estimates of fracture energy,  $G_c$ , and earthquake slip,  $D$ , compiled by [33]. Colors indicate different types of  $G_c$  estimates. Solid black line: best-fitting scaling relation (power law equation at the bottom) for  $D > 0.1$  m (vertical black dashed line) using only seismological data (yellow dots). (b) Residuals between  $G_c$  estimates and the best-fitting scaling relation. Gray and yellow dots represent the data that are disregarded and used, respectively, to determine the scaling relation. (c) Histogram of the residuals (blue) and a Gaussian approximation to it (red, with a standard deviation of  $0.51 \text{ Log}_{10}[\text{J.m}^{-2}]$ ) used in this study to represent the uncertainty of  $B$ .



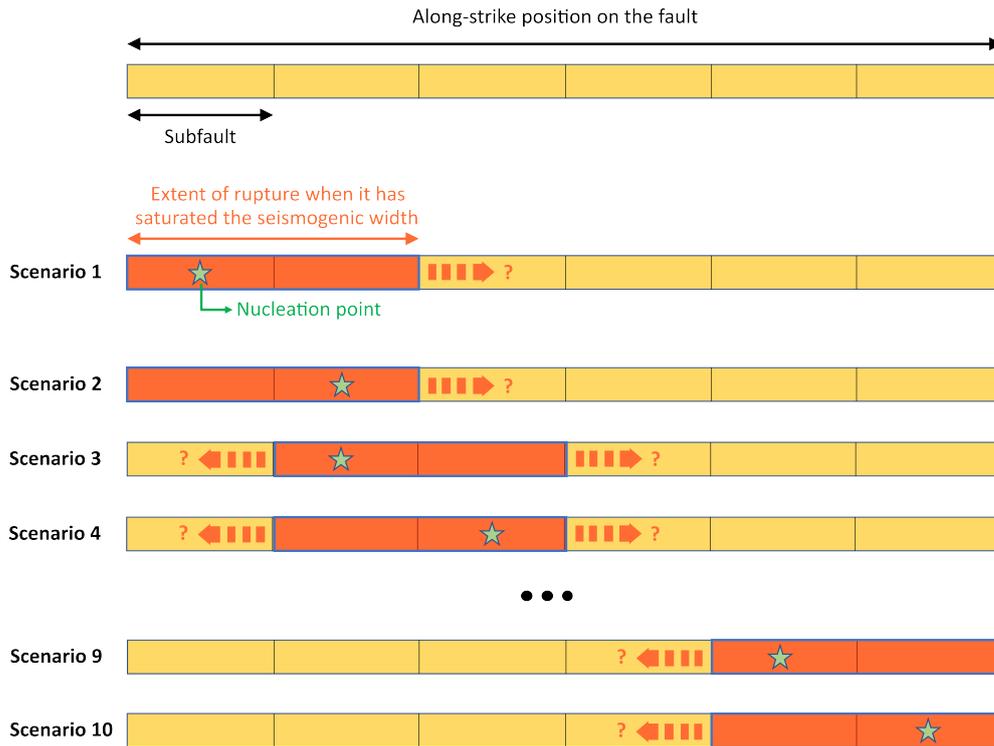
**Fig. S2 Constraints on model parameters based on the Valdivia segment's inter-event time.** (a)-(o) Normalized PDFs of each model parameter, constrained by the assumption that the 1960 M9.5 Valdivia earthquake occurs immediately after the whole southern portion of the Valdivia segment (south of latitude 38°S) is ready to rupture (Section 4). Maximum value of the PDFs are indicated in gray at the bottom right of each panel. Contours of 5% of the maximum PDF value are shown for different constraints imposed: (black) initial parameter distribution described in the Method section [Determination of model parameters and their uncertainties](#), parameter distribution assuming the portion of the Valdivia segment south of latitude 38°S is ready to rupture fully (dark blue) any time before the 1960 earthquake and (light blue) exactly at the occurrence time of the 1960 earthquake. The distributions of  $W$  and coupling are taken from a location on the fault shown by the vertical black line in panels (p) and (q). (p) PDF of the seismicogenic width  $W$  for each subfault. (q) PDF of the interseismic coupling for each subfault.



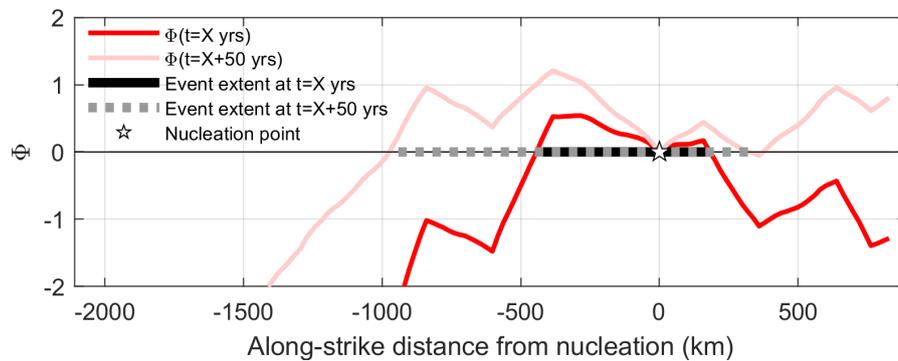
**Fig. S3 Evaluation of the probability of an earthquake to saturate the seismogenic zone and to reach a certain magnitude.** (a) Probability of the inter-event time of saturating earthquakes,  $P_{SAT}$ , assuming their occurrence follows a Poisson process with a mean rate of  $\mu = 1/90 \text{ yrs}^{-1}$ . (b) Probability  $P_{M>X|SAT,t}$  that an earthquake will exceed magnitude  $X$  given that its rupture has already saturated the seismogenic width at time  $t$ . We show here the case for the Iquique and Antofagasta segments combined, with  $t = 0$  corresponding to the occurrence of the 2014 Iquique earthquake. (c) Probability of occurrence of an earthquake exceeding magnitude  $X$  within an interval of 1 year around time  $t$ ,  $P_{M>X} \cap SAT = P_{M>X|SAT,t} \times P_{SAT}$ .



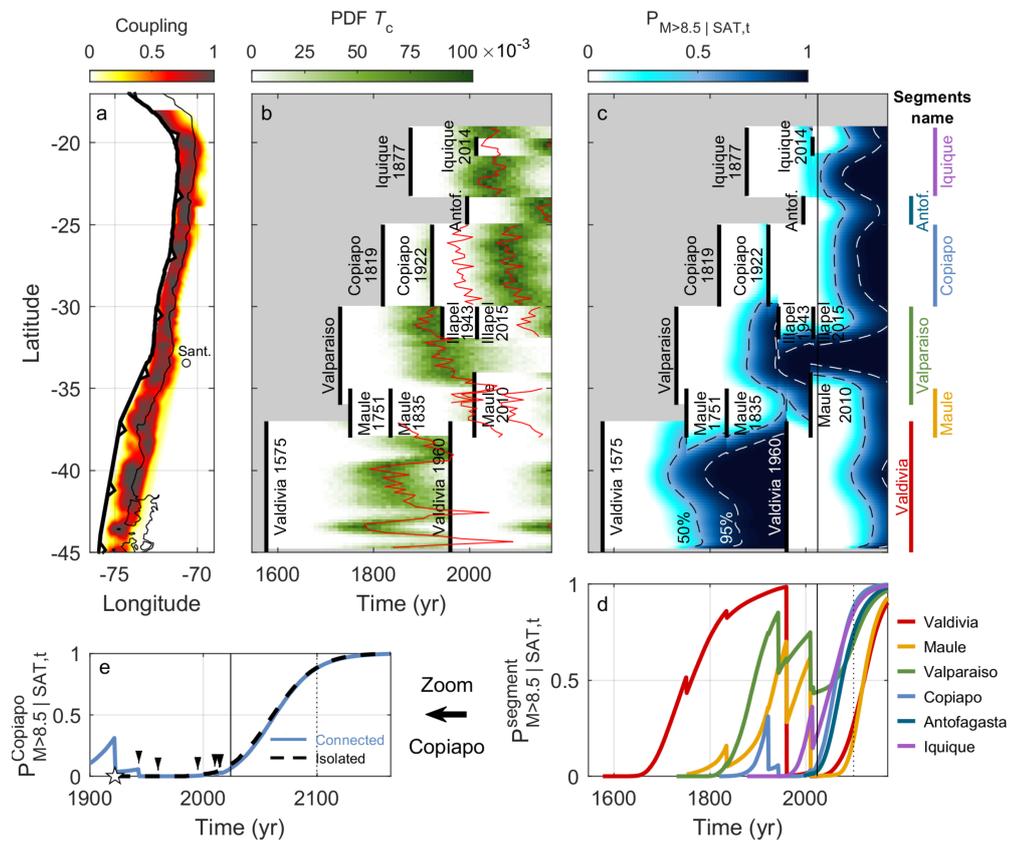
**Fig. S4** (a) Interseismic coupling along the Chilean subduction megathrust [12, 20, 27–29]. (b) Focal mechanisms of earthquakes in Chile from 1980 to 2022 [52], used to estimate the seismogenic depth. (c) Comparison between seismogenic widths estimated from interseismic coupling and seismicity.



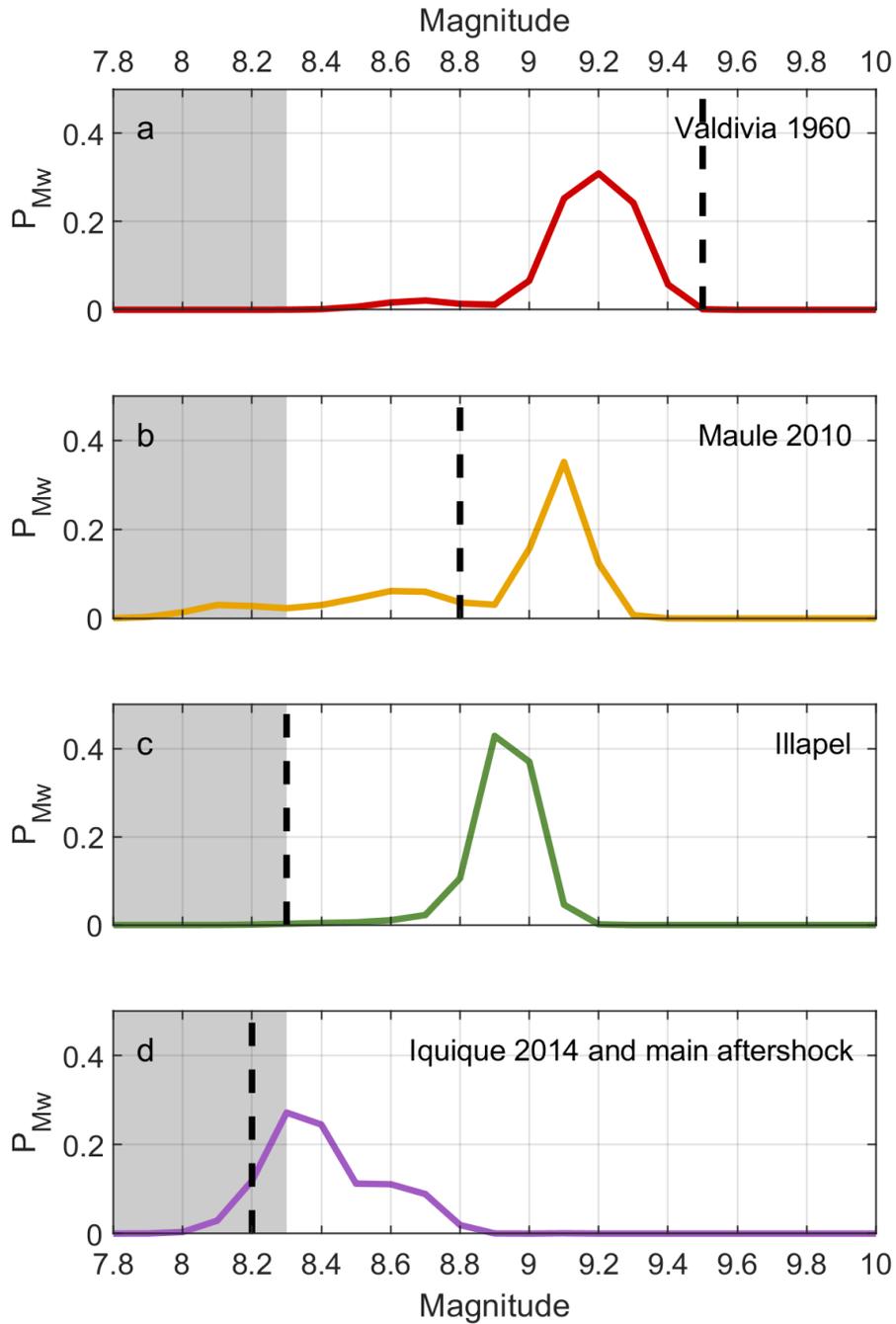
**Fig. S5** Cartoon illustrating the different earthquake scenarios tested to evaluate the seismogenic potential at a time  $t$ .



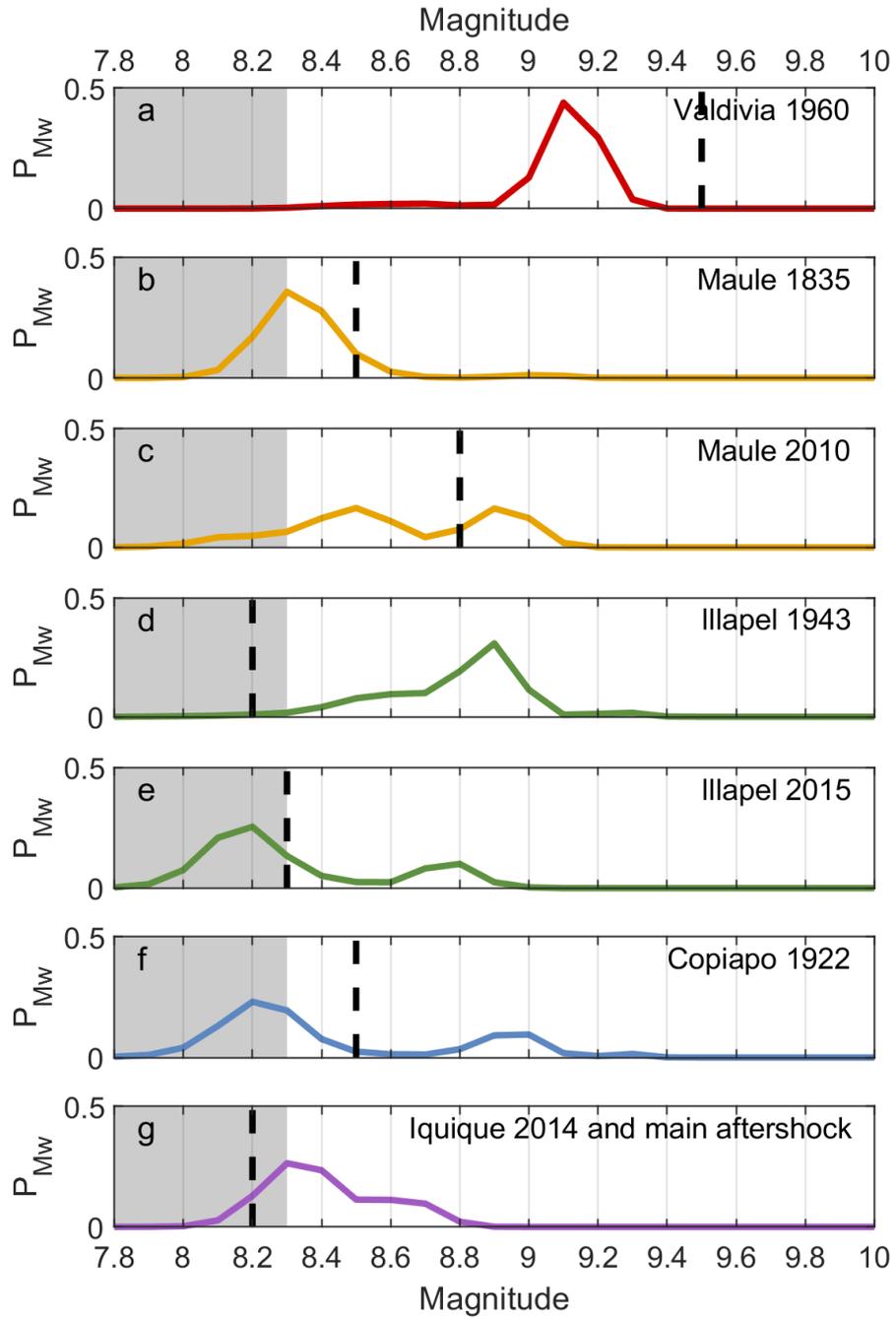
**Fig. S6** Example of distribution of rupture potential  $\Phi$  for a specific earthquake scenario (see Fig. S5) and at two different times. The white star indicates the hypocenter location tested, which is also used here as reference point for  $\Phi$  without loss of generality. At time  $X$ , the earthquake propagates until  $\Phi$  (red curve) passes below its hypocentral value; its final rupture extent is indicated by the thick horizontal black line. At time  $X + 50$  yrs, the fault has been loaded further, thus modifying  $\Phi$  (pink curves). The earthquake can now propagate further, as indicated by the thick dotted gray line.



**Fig. S7** Same as Fig. 4 but using an alternative historical earthquake catalog that includes the 1819 Copiapo, 1943 Illapel and 1835 Maule earthquakes. The white star in panel (e) indicates the timing of the 1922 earthquake on the Copiapo segment.



**Fig. S8** Forecast of earthquake magnitude at the location and time of known events. The vertical black dashed line indicates the observed magnitude. The gray-shaded area represents a magnitude range that should not be interpreted, as events within those magnitudes are unlikely to saturate the seismicogenic zone. Curve colors correspond to the segments shown in Fig. 4.



**Fig. S9** Same as Fig. S8, but for the updated catalog (Fig. S7).