



### Backprojection to image slip

Journal:	<i>Geophysical Journal International</i>
Manuscript ID	Draft
Manuscript Type:	Research Paper
Date Submitted by the Author:	n/a
Complete List of Authors:	Okuwaki, Ryo; University of Tsukuba, Graduate School of Life and Environmental Sciences Kasahara, Amato; Independent Researcher Yagi, Yuji; University of Tsukuba, Graduate School of Life and Environmental Sciences Hirano, Shiro; Ritsumeikan University, College of Science and Engineering Fukahata, Yukitoshi; Kyoto University, Disaster Prevention Research Institute
Keywords:	Image processing < GEOPHYSICAL METHODS, Time series analysis < GEOPHYSICAL METHODS, Earthquake dynamics < SEISMOLOGY, Earthquake source observations < SEISMOLOGY, Theoretical seismology < SEISMOLOGY

1  
2  
3 submitted to *Geophys. J. Int.*  
4  
5  
6  
7  
8

## 9 **Backprojection to image slip**

10  
11  
12  
13 Ryo Okuwaki,<sup>1</sup> Amato Kasahara,<sup>2,\*</sup> Yuji Yagi,<sup>3</sup> Shiro Hirano,<sup>4</sup> and Yukitoshi Fukahata<sup>5</sup>  
14

15  
16 <sup>1</sup>*Graduate School of Life and Environmental Sciences, University of Tsukuba, Tsukuba, Ibaraki 305-8572, Japan.*

17  
18 *E-mail: rokuwaki@gmail.com*

19  
20 <sup>2</sup>*Independent Researcher.*

21  
22 <sup>3</sup>*Faculty of Life and Environmental Sciences, University of Tsukuba, Tsukuba, Ibaraki 305-8572, Japan.*

23  
24 <sup>4</sup>*College of Science and Engineering, Ritsumeikan University, Kusatsu, Shiga 525-8577, Japan.*

25  
26 <sup>5</sup>*Disaster Prevention Research Institute, Kyoto University, Uji, Kyoto 611-0011, Japan.*  
27  
28  
29  
30  
31

### 32 **SUMMARY**

33  
34 Waveform backprojection is a key technique of earthquake-source imaging, which has  
35 been widely used for extracting information of earthquake source evolution that cannot  
36 be obtained by kinematic source inversion. The technique enjoys considerable popularity,  
37 owing to the simplicity of its implementation and the robustness of its processing, but  
38 the physical meaning of backprojection images has remained elusive. In this study, we  
39 reviewed the mathematical representation of backprojection (BP) and hybrid backprojec-  
40 tion (HBP) methods, following the pioneering work of Fukahata et al. (*Geophys. J. Int.*  
41 (2014) 196, 552–559), to clarify the physical implications of BP images. We found that  
42 signal intensity in BP and HBP images is scaled with the amplitude of the Green's func-  
43 tion that corresponds to a unit-step slip, which results in the signal intensity being depth  
44 dependent. We propose variants of BP and HBP, which we call kinematic BP and HBP,  
45 respectively, to relate the BP signal intensity to slip motion of an earthquake by modify-  
46 ing the normalizing factors used in the original BP and HBP methods. The original BP  
47 and HBP images remain useful for assessing the spatiotemporal strength of the wave ra-  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60

2 *R. Okuwaki, A. Kasahara, Y. Yagi, S. Hirano, and Y. Fukahata*

3  
4  
5 diation, which scales with the amplitude of the Green's function, whereas the kinematic  
6  
7 BP and HBP methods are suitable for imaging the slip motion that is responsible for the  
8  
9 high-frequency radiation produced during the source-rupture process.  
10

11 **Key words:** Image processing; Time series analysis; Earthquake dynamics; Earthquake  
12  
13 source observations; Theoretical seismology  
14  
15  
16

## 17 1 INTRODUCTION

18  
19  
20 Waveform backprojection (BP) is a technique for tracking the source evolution of specific seismic  
21  
22 phases (e.g. the *P* phase) during an earthquake (see Kiser & Ishii 2017, for a comprehensive re-  
23  
24 view of BP). Owing to its robustness and applicability to high-frequency waveforms, BP has been  
25  
26 used for extracting information about earthquake-rupture evolution that is missed by the analyses of  
27  
28 low-frequency waveforms by kinematic source inversion, including, for example, multiple branching  
29  
30 ruptures (Meng et al. 2012b; Satriano et al. 2012; Fan et al. 2016, 2017), triggering ruptures of very  
31  
32 early aftershocks (D'Amico et al. 2010; Kiser & Ishii 2013; Fan & Shearer 2016), cascading asperity  
33  
34 ruptures (Okuwaki et al. 2014, 2016), mechanisms of deep-focused earthquakes (Suzuki & Yagi 2011;  
35  
36 Kiser et al. 2011; Ye et al. 2013), frequency-dependent wave radiation of subduction zone megathrust  
37  
38 earthquakes (Kiser & Ishii 2011; Wang & Mori 2011; Yao et al. 2013; Satriano et al. 2014; Yin et al.  
39  
40 2016, 2018), and complex rupture evolution associated with the geometric features of a fault system  
41  
42 (Meng et al. 2012a; Uchide et al. 2013; Vallée & Satriano 2014; Okuwaki & Yagi 2018).

43  
44 According to theoretical studies and dynamic numerical simulations of rupture evolution, high-  
45  
46 frequency waves are generated by abrupt changes of slip velocity or rupture velocity, or both (Madariaga  
47  
48 1977; Bernard & Madariaga 1984; Spudich & Frazer 1984; Madariaga et al. 2006; Beresnev 2017).  
49  
50 Such changes can be caused by barriers or asperities, including fault roughness (Das & Aki 1977; Aki  
51  
52 1979; Dunham et al. 2011; Shi & Day 2013; Bruhat et al. 2016; Mai et al. 2017). By applying the  
53  
54 BP technique, studies have imaged intense high-frequency radiation just before the rupture penetrates  
55  
56 a large-slip area or geometric barriers (e.g. Uchide et al. 2013; Yagi & Okuwaki 2015; Okuwaki &  
57  
58 Yagi 2018), a finding that is consistent with our theoretical understanding of the generation of high-  
59  
60 frequency radiation. In the case of some subduction-zone megathrust earthquakes, however, a distinct  
anti-correlation with respect to depth has been reported, between a shallow large-slip area and the  
deep sources of intense high-frequency radiation; this finding leads to the idea that rupture properties  
within these subduction zones are segmented along depth (Koper et al. 2012; Lay et al. 2012; Ye et al.

\* Contribution was mostly made at the time affiliated with University of Tsukuba<sup>1</sup>.

2016). This idea may be useful for a unified understanding of subduction-zone megathrust earthquakes involving the apparent diversity of source rupture evolution.

However, these considerations raise an intriguing question: why is the intense high-frequency signal captured by the BP technique always located around the down-dip edge of the large-slip zone, even though the rupture front often goes along both up-dip and down-dip directions (e.g.  $M_W$  9.0 2011 Tohoku-oki, Japan and  $M_W$  8.3 2015 Illapel, Chile, earthquakes; Meng et al. 2011; Melgar et al. 2016; Meng et al. 2018)? If high-frequency radiation reflects the kinematic features of source process, given that the BP technique is designed to track the high-frequency radiation, the high-frequency signals in the BP image should be seen around the rupture tip or the healing front (e.g. Madariaga et al. 2006) but not necessarily in the down-dip part of the seismogenic zone. Thus, the view of the high-frequency radiation derived from observations through application of the BP technique seems to be inconsistent with the one derived from the theoretical knowledge. In fact, as we will show in Section 2, the BP image has an inherent bias that is proportional to the amplitude of the Green's function. In other words, the BP image is not just a simple representation of the kinematic features of the source process.

In this study we propose an alternative BP technique that enables us to extract kinematic features of rupture evolution from high-frequency waveform data. We first review the mathematical representation of the BP method, following the pioneering work of Fukahata et al. (2014), who have clarified the theoretical background of the BP techniques and showed that a BP image can represent slip motion as either slip velocity or slip acceleration. However, because Fukahata et al. (2014) basically considered the case of a point source, they did not discuss in detail the normalizing factor adopted for the BP method. We point out the importance of the normalizing factor, which plays a critical role in the resultant signal intensity for the case of multiple-point sources. We consider both the original time-domain BP method (e.g. Ishii et al. 2005) and the Hybrid backprojection (HBP) method (Yagi et al. 2012; Okuwaki et al. 2014). The latter is a variant of the BP technique that introduces the Green's function to enhance the depth resolution of the projected images by using depth phases. We clarify the theoretical meaning of the signal intensity obtained by the BP and HBP methods, which depends on the amplitude of the Green's function and is not directly related to the slip motion. We examine this theoretical outcome through numerical tests using synthetic waveforms, and confirm that the images obtained by the BP and HBP methods have an inherent depth dependence, which is due to the normalizing factor. We propose new variants of the BP and HBP methods (which we call kinematic BP and HBP methods) that, by taking the effect of the normalizing factor into account, allow us to remove the depth-dependent bias in the original BP and HBP images and retrieve signal intensities that are related to slip velocity or slip acceleration. We test the methods through numerical experiments and

4 *R. Okuwaki, A. Kasahara, Y. Yagi, S. Hirano, and Y. Fukahata*

5 application to the observed data of the  $M_W$  8.3 2015 Illapel, Chile, earthquake, and confirm that the  
6 relative signal intensity is related to the slip motion by the kinematic BP and HBP methods.  
7  
8  
9

## 10 2 DEPTH DEPENDENCE IN BP AND HBP IMAGES

11 In this section, we investigate the mathematical expressions of the BP and HBP methods (Ishii et al.  
12 2005, 2007; Yagi et al. 2012; Fukahata et al. 2014). Particularly, we consider the role of the normal-  
13 izing factors in the implementations and their effect on the resultant signal intensity, which was not  
14 addressed in detail by Fukahata et al. (2014). We then perform a numerical test by using synthetic  
15 waveforms to demonstrate that both the BP and HBP images have an inherent depth dependence that  
16 is proportional to the amplitude of the Green's function for a unit-step slip.  
17  
18  
19  
20  
21  
22  
23  
24  
25

### 26 2.1 Representation of BP

27 A BP image is made by stacking observed waveforms as follows:  
28  
29

$$30 s_i^{\text{BP}}(t) = \sum_j w_j \frac{u_j(t + t_{ij}^p)}{A_j}, \quad (1)$$

31 where  $s_i^{\text{BP}}(t)$  is the signal intensity of the BP image at the  $i$ th source location at hypocentral time  $t$   
32 (where  $t = 0$  corresponds to the origin time of the earthquake), and  $u_j(t + t_{ij}^p)$  is the observed waveform  
33 at the  $j$ th station that is time-shifted by the theoretical travel time of the  $P$  phase  $t_{ij}^p$  between the  $i$ th  
34 source location and the  $j$ th station. For simplicity, we neglect the calibration of travel time error (Ishii  
35 et al. 2007; Fan & Shearer 2017) and the slowness correction (Meng et al. 2016).  $w_j$  is a weighting  
36 factor for each waveform, which is introduced to avoid spatial bias due to the station distribution;  $w_j$   
37 is usually designed to be negatively correlated with station density and sums to 1, that is,  $\sum_j w_j = 1$   
38 (details are shown in Section 2.3). The normalizing term  $A_j$  is given by the root-sum-square of the  
39 observed waveform,  
40  
41  
42  
43  
44  
45  
46  
47  
48

$$49 A_j = \text{pol}(u_j) \cdot \sqrt{\int_0^T u_j^2(\tau + t_j^p) d\tau}, \quad (2)$$

50 where  $\text{pol}(u_j) \in \{-1, +1\}$  is the polarity of the first motion of waveform  $u_j$ ,  $t_j^p$  is the  $P$ -phase arrival  
51 time at the  $j$ th station, and  $T$  is the waveform length. The normalizing factor can also be represented  
52 by the maximum amplitude of the observed waveform, although these forms of the normalizing factor  
53 were not presented explicitly in the relevant papers. In this study, we use the representation in eq. (2),  
54 because of its similarity to the normalizing factor in the HBP method defined in eq. (8). The observed  
55  
56  
57  
58  
59  
60

waveform  $u_j$  can be expressed as

$$\begin{aligned} u_j(t) &= \sum_{i'} (a_{i'} * G_{i'j})(t) \\ &= (a_i * G_{ij})(t) + \sum_{i'(\neq i)} (a_{i'} * G_{i'j})(t), \end{aligned} \quad (3)$$

where  $a_i$  is the slip motion at the  $i$ th source location on the fault surface,  $*$  denotes convolution, and we neglect the background noise of the observed waveform for simplicity. The Green's function  $G_{ij}$  in eq. (3) is the deformation at the  $j$ th station due to a unit-step slip on the  $i$ th subfault. For the velocity data  $u_j$ , slip motion  $a_i$  may represent slip velocity if the Green's function is a propagator from slip velocity to far-field velocity, or slip acceleration if the Green's function is a propagator from slip velocity to far-field displacement (Fukahata et al. 2014). Hereafter, we refer to the slip motion  $a_i$  as slip velocity, considering together that the waveform  $u_j$  is velocity data and the Green's function  $G_{ij}$  is for unit-step slip velocity. By substituting eq. (3) into eq. (1), we get the following expression for the signal intensity,

$$s_i^{\text{BP}}(t) = \sum_j \frac{w_j}{A_j} \left( (a_i * G_{ij})(t + t_{ij}^p) + \sum_{i'(\neq i)} (a_{i'} * G_{i'j})(t + t_{ij}^p) \right). \quad (4)$$

As shown in eq. (4), eq. (1) is divided into two terms: the first term is the signal that corresponds to the contribution from the  $i$ th source, and the second term is noise, which is the contribution from other  $i'$ th locations. If the noise term can be assumed to be suppressed by stacking (Fukahata et al. 2014) as,

$$\sum_j \frac{w_j}{A_j} \left( \sum_{i'(\neq i)} (a_{i'} * G_{i'j})(t + t_{ij}^p) \right) \approx 0, \quad (5)$$

then the signal intensity at the  $i$ th location can ideally be represented as

$$s_i^{\text{BP}}(t) \approx \sum_j \frac{w_j}{A_j} (a_i * G_{ij})(t + t_{ij}^p), \quad (6)$$

where the signal intensity at the  $i$ th source location  $s_i^{\text{BP}}$  represents the slip velocity at the  $i$ th source location  $a_i$ , which scales with the normalizing factor  $A_j$  and the Green's function  $G_{ij}$ . Hence, the signal intensity  $s_i^{\text{BP}}$  is not uniquely determined by the amplitude of the slip velocity at the  $i$ th source location  $a_i$ , but is additionally controlled by a scaling factor composed of  $A_j$  and  $G_{ij}$ , which depends on the source location because its numerator includes  $G_{ij}$ .

6 *R. Okuwaki, A. Kasahara, Y. Yagi, S. Hirano, and Y. Fukahata*

## 2.2 Representation of HBP

The HBP image is made by stacking cross-correlation functions of the observed waveform and the Green's function:

$$s_i^{\text{HBP}}(t) = \sum_j w_j \frac{(u_j \hat{\times} G_{ij}^p)(t)}{A_{ij}} = \sum_j w_j \frac{\int_0^T u_j(\tau) G_{ij}^p(\tau - t) d\tau}{A_{ij}} \quad (7)$$

where  $\hat{\times}$  denotes cross-correlation, and  $G_{ij}^p$  is the theoretical Green's function that corresponds to the deformation due to a unit-step slip velocity.  $T$  is the time period of the cross-correlation function of the waveform and the Green's function. The weighting factor  $w_j$  is the same as in eq. (1), and the normalizing factor  $A_{ij}$  is represented as

$$A_{ij} = \sqrt{\int_0^T u_j^2(\tau + t_j^p) d\tau} \cdot \sqrt{\int_0^T G_{ij}^{p2}(\tau + t_j^p) d\tau}, \quad (8)$$

which is designed to normalize the cross-correlation function in the numerator of eq. (7). Eq. (3) can be used to expand eq. (7) into signal and noise terms as follows:

$$s_i^{\text{HBP}}(t) = \sum_j \frac{w_j}{A_{ij}} \left[ ((a_i * G_{ij}) \hat{\times} G_{ij}^p)(t) + \sum_{i'(\neq i)} ((a_{i'} * G_{i'j}) \hat{\times} G_{ij}^p)(t) \right]. \quad (9)$$

If the noise term can be assumed to be suppressed by stacking (Fukahata et al. 2014) as

$$\sum_j \frac{w_j}{A_{ij}} \left( \sum_{i'(\neq i)} (a_{i'} * G_{i'j}) \hat{\times} G_{ij}^p \right)(t) \approx 0, \quad (10)$$

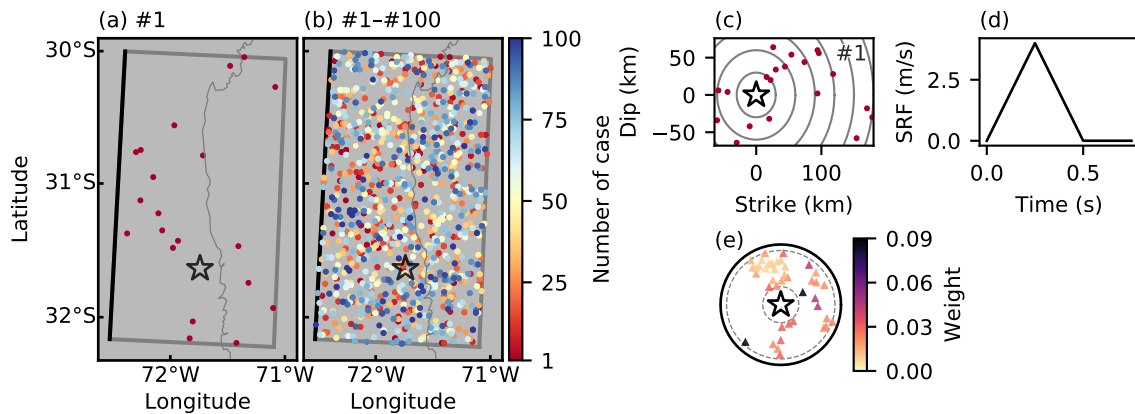
the final form of the signal intensity is

$$s_i^{\text{HBP}}(t) \approx \sum_j \frac{w_j}{A_{ij}} ((a_i * G_{ij}) \hat{\times} G_{ij}^p)(t). \quad (11)$$

The resultant signal intensity at the  $i$ th source location  $s_i^{\text{HBP}}$  represents the slip velocity  $a_i$  scaled with a weighting factor  $w_j$ , the normalizing factor  $A_{ij}$  and the cross-correlation function of the Green's functions. Eq. (11) indicates that the resultant signal intensity of the HBP method is also expected to correlate with the source location because the scaling factor includes the Green's functions.

## 2.3 Numerical test

As seen in eqs. (6) and (11), the signal intensity of the BP and HBP images is not a simple representation of the slip motion at the specific source location; but rather, it includes additional contributions from the normalizing factors and the Green's functions. We performed a numerical test with synthetic waveforms computed using a known slip velocity  $a$  to empirically show how the scaling factors in eqs. (6) and (11) affect the resultant BP and HBP images. First, we generated synthetic waveforms using 20 point sources that were randomly distributed on a dipping model plane in the Chilean subduction zone



**Figure 1.** Model setting for the numerical test. (a) Map view of the distribution of randomly selected point sources for the case 1 (#1) and (b) all the point sources through the cases 1–100 (#1–#100). The color of point sources represents the index of the case. The gray rectangle outlines the model fault plane with a dip angle of  $15^\circ$ , the black line on the west side is the up-dip limit of the fault area, and the star denotes the nucleation point (hypocentre). The thin gray curved line shows the coastline. (c) Relation between the point-source location (red dot) and the rupture front for the case 1. The star denotes the nucleation point. Gray circles represent the constantly propagating rupture front snapshotted at 10 s interval. (d) Slip-rate function (SRF) built in each point source. (e) Observation station distribution denoted as triangles. The star denotes the nucleation point, and the gray dashed circles show epicentral distances at  $30^\circ$  and  $90^\circ$ . Color of each triangle represents the weight defined in eq. (12).

(Fig. 1a). Each point source has a uniform potency of  $4 \times 10^6 \text{ m}^3$  ( $2 \times 2 \text{ km}^2$  area  $\times$  1 m slip for pure thrust motion against the relative plate motion; DeMets et al. 2010), which is composed of a triangular slip-rate function with a half-rise time of 0.25 s computed at a sampling frequency of 20 Hz (Fig. 1d). The model plane is a  $190 \times 130 \text{ km}^2$  rectangle with strike and dip angles of  $2.7^\circ$  and  $15^\circ$ , respectively, that has been discretized for point sources with a spatial resolution of  $2 \text{ km} \times 2 \text{ km}$  in both strike and dip directions. The initial rupture point (hypocentre) is located at  $31.637^\circ\text{S}$ ,  $71.741^\circ\text{W}$ , and 25-km depth. Each point source is triggered to rupture by the expanding circular rupture front propagating at a constant speed of 3 km/s from the hypocentre (Fig. 1c). The Green's function that is convolved with the slip-rate function to generate the synthetic waveforms is calculated by the method of Kikuchi & Kanamori (1991). Near the source area, a layered medium (Table 1) is used for calculating the Haskell propagator matrix for the Green's function, and the ak135 model (Kennett et al. 1995) is used to calculate geometrical spreading factors, ray parameters, and travel times. The synthetic waveforms were calculated for the stations at teleseismic distances between  $30^\circ$ – $90^\circ$  (Fig. 1e), and the weighting factor



8 *R. Okuwaki, A. Kasahara, Y. Yagi, S. Hirano, and Y. Fukahata*

**Table 1.** Near-source structure used to calculate Green's function.

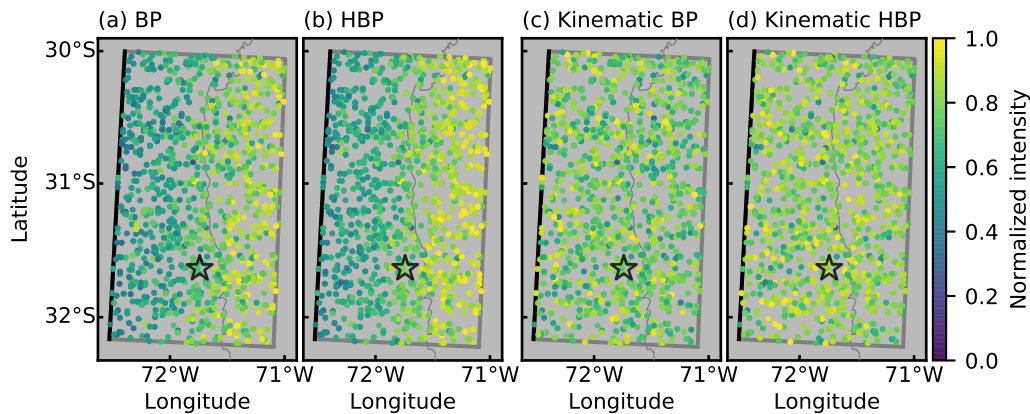
$V_P$	$V_S$	Density	Thickness
(km/s)	(km/s)	( $10^3\text{kg/cm}^3$ )	(km)
1.50	0.00	1.02	4.00
4.80	2.77	2.72	4.00
5.50	3.18	2.72	4.00
6.00	3.46	2.86	4.00
6.40	3.70	2.86	6.00
6.80	3.93	3.03	8.00
7.80	4.32	3.42	0.00

$w_j$  in eqs. (1) and (7) is calculated according to the following rules:

$$\begin{aligned}
 w_j &= \frac{r_j}{\sum_j r_j}, \\
 r_j &= \frac{1}{\sum_{j'} m_{jj'}}, \\
 m_{jj'} &= \begin{cases} 1 & (\Delta_{jj'} \leq 20^\circ) \\ 0 & (\Delta_{jj'} > 20^\circ), \end{cases} \quad (12)
 \end{aligned}$$

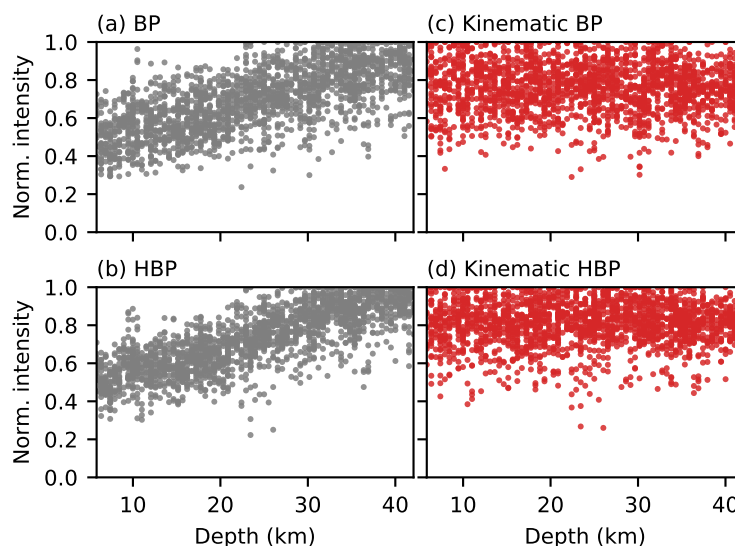
where  $\Delta_{jj'}$  is the epicentral distance between a pair of stations. In the BP method, this weighting factor is based on globally distributed stations (e.g. Fan & Shearer 2015), whereas when the BP method is applied to an array of stations, the weighting factor is represented by, for example, a cosine function (Ishii et al. 2007), and the weight given to the waveform decays with distance from the centre of the station array. Note that in this test, the hypocentre, fault geometry, station configuration, and near-source velocity structures are those used in seismic source study of the  $M_W$  8.3 2015 Illapel, Chile, earthquake (Okuwaki et al. 2016). We used the BP and HBP methods to backproject the synthetic waveforms onto the fault. To show systematic bias independent of specific point-source distributions, we computed backprojection images for 100 cases of 20 randomly selected point sources (Fig. 1b).

We then plotted the backprojected signal intensities at the locations of point sources shown in Fig. 1(b) both in map view (Figs. 2a and b) and along depth (Figs. 3a and b). The result shows a clear depth dependence of the backprojected signal intensity on the model fault plane, where the signal intensity increases with the depth of the point sources even though we generated the synthetic waveforms by assuming the same potency at all the point sources. This depth dependence in both the BP and HBP images reflects the depth dependence of the fractions in eqs. (6) and (11), which have the Green's functions as their numerator and the normalizing factor as their denominator. In the assumed dipping model fault plane embedded in a layered medium (Table 1), the Green's function displays a



**Figure 2.** Map view of the result with the (a) original BP, (b) original HBP, (c) kinematic BP, and (d) kinematic HBP methods. Color represents the maximum intensity of the backprojected signal among the source duration, which is normalized by the maximum intensity among backprojected images for each case of #1–#100. The gray rectangle outlines the model fault plane, the black line is the up-dip limit of the fault area, and the star denotes the nucleation point (hypocentre). The thin gray curved line shows the coastline.

depth dependence related to the rigidity of the medium and to geometrical spreading factors, both of which become larger with depth. Thus, we can conclude that the BP and HBP methods are inherently designed to retrieve contributions of wave radiation to entire waveforms, which should be proportional to the amplitude of the Green's functions. Note that the weighting factor  $w_j$  fluctuates at most 9% for



**Figure 3.** Depth view of the normalized intensity of images obtained by the (a) original BP, (b) original HBP, (c) kinematic BP, and (d) kinematic HBP methods. Abscissa is the depth of point sources, and the ordinate is the normalized intensity of the backprojected images.

1  
2  
3  
4 10 *R. Okuwaki, A. Kasahara, Y. Yagi, S. Hirano, and Y. Fukahata*

5 the station configuration adopted in this numerical test (Fig. 1e), and it does not significantly affect the  
6 signal intensity. The numerical test presented in this study extends the result of Fukahata et al. (2014)  
7 that did not rigorously consider the effect of a scaling factor due to the amplitude of the Green's  
8 function, because they basically considered the case of a single point source. However, for the case  
9 of multiple-point sources (Fig. 1), the dependence of the signal intensity on the source location has  
10 been clearly revealed (Figs. 2a and b and 3a and b), because the scaling factor is proportional to the  
11 amplitude of the Green's function which depends on the source location shown in eqs. (6) and (11).  
12  
13  
14  
15  
16  
17  
18

### 19 3 NEW SCALING FACTORS FOR BP AND HBP METHODS TO IMAGE SLIP MOTION

20 The depth dependence of the BP and HBP images (Figs. 2a and b and 3a and b) highlights the inherent  
21 design of the BP and HBP methods, which extracts the relative strength of the wave radiation scaled  
22 by the amplitude of the Green's function; as a result, the BP and HBP images are biased when they are  
23 interpreted as the slip motion. However, BP and HBP methods are potentially useful for investigating  
24 the details of rupture properties or slip motion recorded in high-frequency waveforms. Therefore, it  
25 would be convenient if we can design BP and HBP methods to retrieve the slip motion on a fault plane  
26 from the backprojected images. For this purpose, we propose variants of the BP and HBP methods in  
27 which the normalizing factors in eqs. (1) and (7) of the original BP and HBP methods are appropriately  
28 modified. We then test the proposed methods in the same situation as described in Section 2.3 and also  
29 apply them to real waveforms of the  $M_W$  8.3 2015 Illapel, Chile, earthquake.  
30  
31  
32  
33  
34  
35  
36  
37  
38

#### 39 3.1 Modification in kinematic BP and HBP methods and synthetic test

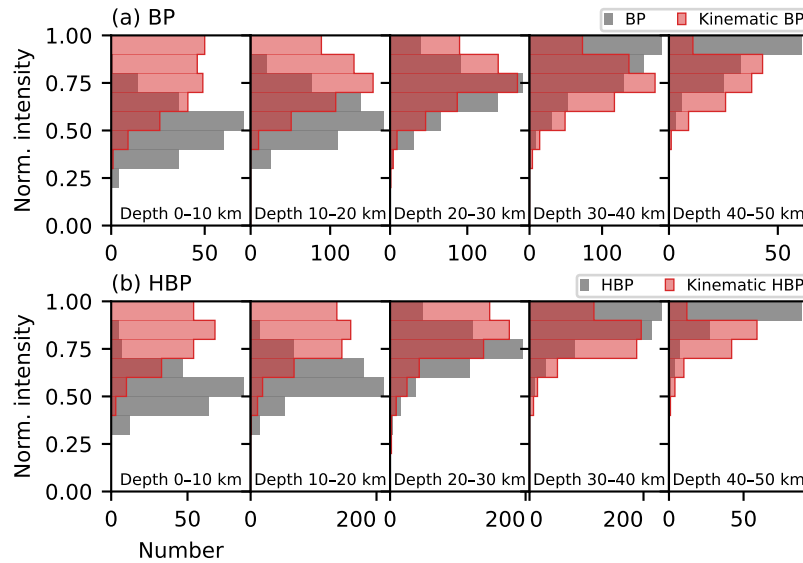
40 In order to retrieve the slip motion from the signal intensity, we modify the BP and HBP methods by  
41 changing the normalizing factors to cancel out the numerators of the signal terms,  $G_{ij}$  in eq. (6) and  
42  $G_{ij} \hat{\times} G_{ij}^p$  in eq. (11). For the BP method, we propose a normalizing factor  $A_{ij}^{\text{kBP}}$  as  
43  
44  
45

$$46 A_{ij}^{\text{kBP}} = g_{ij}^p, \quad (13)$$

47 where  $g_{ij}^p$  is the amplitude of the first motion of the theoretical Green's function. For the HBP method,  
48 we modify the normalizing factor  $A_{ij}$  in eq. (8) by using the theoretical Green's function  $G_{ij}^p$ :  
49  
50  
51

$$52 A_{ij}^{\text{kHBP}} = \int_0^T G_{ij}^{p,2}(\tau + t_{ij}^p) d\tau. \quad (14)$$

53 The bias in the original BP and HBP images (Section 2.3) is expected to be corrected by this modi-  
54 fication of the normalizing factors. Thus, the kinematic BP and HBP images should be more directly  
55 related to the slip motion on a fault.  
56  
57  
58  
59  
60



**Figure 4.** Histograms of the normalized intensity of the signals obtained by (a) the original and kinematic BP methods, and (b) the original and kinematic HBP methods.

The same numerical test that we carried out in Section 2.3 is performed to examine how the proposed normalization factors modify the resultant signal intensity. As shown in Figs. 2–4, the depth dependence seen in the original BP and HBP images has mostly disappeared; basically uniform distribution of signal intensity with depth is obtained by the kinematic BP and HBP methods. These results indicate that the input potency used for generating the synthetic waveforms is backprojected onto the point source without the depth-dependent bias.

### 3.2 Theoretical background of kinematic BP and HBP methods

Here, we consider the theoretical background of the kinematic BP and HBP methods, which successfully suppressed the depth-dependent bias, following the procedure taken in Fukahata et al. (2014) with the modified normalizing factors of eqs. (13) and (14).

In the kinematic BP method as well as in the original BP method, we first assume that the Green's function in eq. (6) is an impulsive response function (Fukahata et al. 2014), which can be represented by Dirac's delta function with the amplitude of the first motion of the Green's function as a scale factor on the basis that later phases and inelastic attenuation can be neglected:

$$G_{ij}(t + t_{ij}) \approx g_{ij}\delta(t), \quad (15)$$

where  $g_{ij}$  is the amplitude of the first motion of the true Green's function, and  $t_{ij}$  is the true travel time of the  $P$  phase. If we can further assume that the true travel time  $t_{ij}$  is approximately equal to the

12 *R. Okuwaki, A. Kasahara, Y. Yagi, S. Hirano, and Y. Fukahata*

theoretical travel time of  $t_{ij}^p$ ,

$$t_{ij}^p \approx t_{ij}, \quad (16)$$

eq. (15) becomes

$$G_{ij}(t + t_{ij}^p) \approx g_{ij}\delta(t). \quad (17)$$

Substituting Eq. (17) into eq. (6), we obtain

$$s_i^{\text{kBP}} = \sum_j \frac{w_j}{A_j} a_i g_{ij}(t). \quad (18)$$

If we can compute a Green's function for the  $P$  phase that satisfies

$$g_{ij}^p \approx g_{ij}, \quad (19)$$

the fraction of the Green's function and the normalizing factor in eq. (18) is canceled out in the kinematic BP method because we now have defined the normalizing factor as in eq. (13). Hence, the modified signal intensity at the  $i$ th source location  $s_i^{\text{kBP}}$  becomes

$$s_i^{\text{kBP}}(t) \approx a_i(t), \quad (20)$$

where we used  $\sum_j w_j = 1$ . In eq. (20) the signal intensity in the kinematic BP method,  $s_i^{\text{kBP}}$ , directly corresponds to the slip velocity  $a_i$ . Which of the Green's function due to unit-step slip velocity or displacement can well satisfy the assumption of eq. (17) is hard to be determined (Fukahata et al. 2014), but we note if the effect of the attenuation for the teleseismic body waves can be neglected, the slip motion  $a_i$  corresponds to the slip acceleration for the velocity data  $u_j$ .

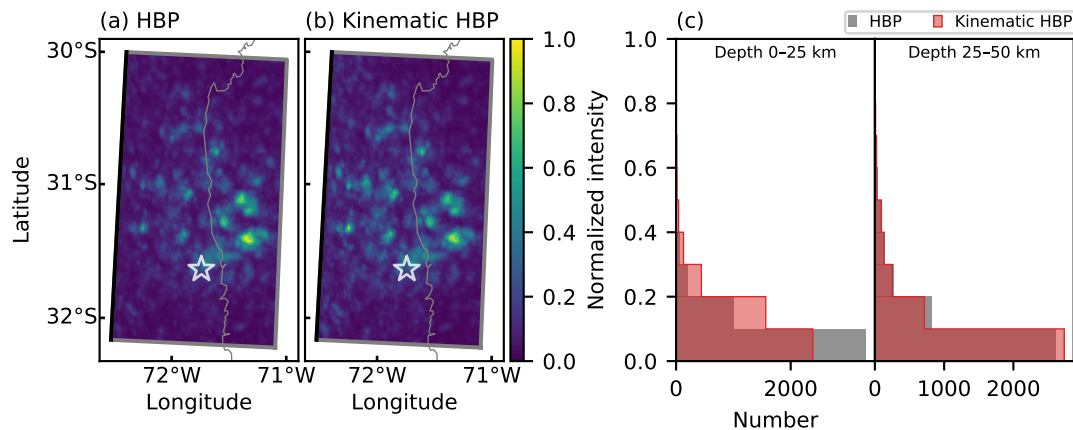
In the kinematic HBP method as well as in the original HBP method, we first assume that the theoretical Green's function is a good approximation of the true Green's function as

$$G_{ij}^p(t) \approx G_{ij}(t). \quad (21)$$

Substituting eq. (21) into eq. (11), we obtain

$$s_i^{\text{kHBP}}(t) \approx \sum_j w_j \frac{((a_i * G_{ij}^p) \hat{\times} G_{ij}^p)(t)}{A_{ij}}. \quad (22)$$

If we use the normalizing factor defined by eq. (14), the fraction that is composed of the cross-correlation of the Green's functions and the normalizing factor in eq. (22) results in the normalized auto-correlation function of the Green's function. Therefore, if we can assume that the stacked auto-correlation functions is like the Dirac's delta function with certain amplitude (Fukahata et al. 2014),



**Figure 5.** Comparison of (a) the original and (b) the kinematic HBP images. Color represents the normalized intensity of the backprojected signal. The gray rectangle outlines the model fault plane with a dip angle of  $15^\circ$ , the black line on the west side is the up-dip limit of the fault area, and the star denotes the nucleation point (hypocentre). The thin gray curve shows the coastline. (c) Histograms of the normalized intensity of the signals obtained by the original and the kinematic HBP methods.

eq. (22) becomes

$$\sum_j w_j \frac{(G_{ij}^p \hat{\times} G_{ij}^p)(t)}{\int_0^T G_{ij}^{p2}(\tau + t_{ij}^p) d\tau} \approx \delta(t), \quad (23)$$

where we used  $\sum_j w_j = 1$ . Then, the modified signal intensity at the  $i$ th source location  $s_i^{\text{kHBP}}$  is finally expressed as

$$s_i^{\text{kHBP}}(t) \approx a_i(t). \quad (24)$$

In eq. (24) the signal intensity of the kinematic HBP image,  $s_i^{\text{kHBP}}$ , directly corresponds to the slip velocity  $a_i$ .

### 3.3 Application to the real data

In order to demonstrate how the relative signal intensity is modified by the kinematic HBP method for the real case, we applied it to the waveforms of the  $M_W$  8.3 2015 Illapel, Chile, earthquake with the same procedure adopted by Okuwaki et al. (2016), which used the original HBP method (Fig. 5). Therefore, except for the normalizing factor, both methods are the same. Here, 4th root stacking (e.g. McFadden et al. 1986) was used to enhance the signal-to-noise ratio of the image, and the data were filtered in the 0.3–2.0 Hz frequency band. Compared with the original HBP method, the application of the kinematic HBP method increased signal intensity in the region shallower than 25 km (Fig. 5c). Based on the numerical test, we can consider that the depth-dependent bias included in the original

1  
2  
3  
4 14 *R. Okuwaki, A. Kasahara, Y. Yagi, S. Hirano, and Y. Fukahata*

5 HBP method is successfully suppressed by the kinematic HBP method. The source models of the 2015  
6 Illapel earthquake showed a complex rupture evolution along both the up-dip and down-dip directions  
7 (Melgar et al. 2016; An et al. 2017; Yin et al. 2018; Meng et al. 2018), which is more consistent with  
8 the image obtained by the kinematic HBP method. The increased signal in the shallow part should  
9 reflect the source of high-frequency radiation from the up-dip rupture propagation.  
10  
11  
12  
13

#### 14 **4 DISCUSSION**

15  
16  
17 In this study, we proposed the variants of the BP and HBP methods in order to directly retrieve the slip  
18 motion from the backprojected images by modifying the normalizing factors adopted in the original BP  
19 and HBP methods, which suppresses the depth-dependent bias in the original BP and HBP methods.  
20 However, for subduction zone megathrust earthquakes, the depth dependence of the signal intensity in  
21 the original BP and HBP images is still crucial information for assessing future-earthquake damage  
22 due to strong shaking, because buildings have resonant frequencies that lie in the frequency band used  
23 for the BP analyses (e.g. Snieder & Şafak 2006; Meng et al. 2012a). The contribution from high-  
24 frequency wave radiation by a unit slip in the deeper part of the seismogenic zone tends to be larger  
25 than that from the radiation in the shallower part of the fault, provided that the fault is dipping and  
26 the rigidity of the medium increases with depth. Both the mathematical representations and numerical  
27 test indicate that in the original BP and HBP methods the signal intensity does not directly correspond  
28 to the slip behaviour. As a result, the slip heterogeneity that causes high-frequency radiation (e.g.  
29 Spudich & Frazer 1984) is not easily be resolved by the original BP and HBP methods.  
30  
31  
32  
33  
34  
35  
36  
37

38 We verified through numerical tests that the kinematic BP and HBP methods worked well for  
39 suppressing depth dependence of the signal intensity and extracting slip motion on a fault surface,  
40 which should be useful for unbiased interpretation of high-frequency signals in the context of the  
41 source-rupture evolution. However, even if we use the kinematic BP and HBP methods, in the ideal  
42 model setting to generate the synthetic waveforms, the input sources were still imperfectly recovered,  
43 and the normalized backprojection intensity ranged from about 0.5 to 1.0 (Figs. 3 and 4). One possible  
44 reason for this spread in the distribution is due to the noise given in the second terms in eqs. (4) and  
45 (9). We assumed for both the original and kinematic BP and HBP methods that the noise terms can be  
46 suppressed by stacking as eqs. (5) and (10) based on Fukahata et al. (2014). However, in our numerical  
47 test, where the multiple-point sources with a uniform slip-rate function are randomly distributed (Fig.  
48 1), the interference of the noise and signal terms cannot be neglected when the sources are close to  
49 each other since the convolution functions of the slip velocity and the Green's function get similar  
50 among the neighbouring locations. As a result, the signal intensity may be intensified or decreased by  
51 the noise. This imperfect recovery of the input sources is a common feature in both the original and  
52  
53  
54  
55  
56  
57  
58  
59  
60

kinematic BP and HBP methods, irrespective of the implementation of the normalizing factor because this comes from the resemblance of the Green's function at sources (Fukahata et al. 2014). We also note that the assumptions we made in eqs. (19) and (21) may not work efficiently for the analysis of real data, because of the limitation to calculate the Green's function accurately (e.g. Yagi & Fukahata 2011).

We have discussed the depth dependence of the signal intensity in the original BP and HBP methods by only considering that the scaling factors include the Green's functions in the numerators of the signal terms in eqs. (4) and (9). However the normalizing factors adopted in the original BP and HBP methods also include the slip motion  $a_i$  since the normalizing factors are composed of the waveform data  $u_j$  (eq. 3). For example, eq. (6) can be rewritten as

$$s_i^{\text{BP}}(t) \approx \sum_j w_j \frac{(a_i * G_{ij})(t + t_{ij}^p)}{\text{pol}(u_j) \cdot \sqrt{\int_0^T [\sum_{i'} (a_{i'} * G_{i'j})(\tau + t_j^p)]^2 d\tau}}, \quad (25)$$

for the original BP method, in which  $a_i$  is included in both the numerator and denominator. Thus, the relationship between the resultant signal intensity and the slip motion  $a_i$  is essentially non-linear in the original BP and HBP method, which makes it difficult to understand the effect of the Green's function on the depth dependence of the signal intensity. On the other hand, the normalizing factors in the kinematic BP and HBP methods are designed to include the Green's function alone. Because of that, the signal intensity is directly related to the slip motion, which establishes a linear relation between the signal intensity and the slip motion.

## 5 CONCLUSION

Through the mathematical reviews and numerical tests of the time-domain BP and HBP methods, we confirmed that the signal intensity in the original BP and HBP methods was designed to retrieve the relative strength of wave radiation. Therefore, the signal intensity is proportional to the amplitude of the Green's function, which leads to clear depth dependence of the signal intensity. The depth dependence of the BP and HBP images gives a bias when the signal intensity of the image is interpreted as the rupture property. On the other hand, the kinematic BP and HBP methods, the variants of the BP techniques proposed in this paper, can directly relate the signal intensity to slip motion on a fault surface, which is free from the depth dependence. The proposed methods are useful for quantifying the depth dependence of the high-frequency sources, which would deepen our understanding of the high-frequency radiation and its role on the rupture property during an earthquake.



16 R. Okuwaki, A. Kasahara, Y. Yagi, S. Hirano, and Y. Fukahata

## ACKNOWLEDGMENTS

We appreciate the editor and the reviewers for their handling and reviewing our paper. This work was supported by Grant-in-aid for Japan Society for the Promotion of Science (JSPS) Research Fellowship (JP16J00298) and JSPS Grants-in-aid for Scientific Research (JP16K05529, JP16H01842, and JP16K05539). The authors thank Hisahiko Kubo, Lingsen Meng, Takahiko Uchide, and Wenyuan Fan for their valuable comments on the early stage of this study. Teleseismic waveforms from the networks; Antarctic Seismographic Argentinean Italian Network (AI; <https://doi.org/10.7914/SN/AI>), Canadian National Seismograph Network (CN; <https://doi.org/10.7914/SN/CN>), GEOSCOPE (G; <https://doi.org/10.18715/GEOSCOPE>), Global Telemetered Seismograph Network (USAF/USGS, GT; <https://doi.org/10.7914/SN/GT>), Global Seismograph Network (GSN IRIS/IDA, II; <https://doi.org/10.7914/SN/II>), and Global Seismograph Network (GSN IRIS/USGS, IU; <https://doi.org/10.7914/SN/IU>) are downloaded through the IRIS-DMC (<https://ds.iris.edu/ds/nodes/dmc/>). The figures are generated with matplotlib (Hunter 2007, Version v2.2.2; <https://doi.org/10.5281/zenodo.1202077>). All the data and results shown in this study are stored in Github (<https://github.com/rokuwaki>).

## REFERENCES

- Aki, K., 1979. Characterization of barriers on an earthquake fault, *J. Geophys. Res.*, **84**(B11), 6140.
- An, C., Yue, H., Sun, J., Meng, L., & Báez, J. C., 2017. The 2015 Mw 8.3 Illapel, Chile, Earthquake: Direction-Reversed Along-Dip Rupture with Localized Water Reverberation, *Bull. Seismol. Soc. Am.*, **107**(5), 2416–2426.
- Beresnev, I. A., 2017. Factors controlling high-frequency radiation from extended ruptures, *J. Seismol.*, **21**(5), 1277–1284.
- Bernard, P. & Madariaga, R., 1984. A new asymptotic method for the modeling of near-field accelerograms, *Bull. Seismol. Soc. Am.*, **74**(2), 539–557.
- Bruhat, L., Fang, Z., & Dunham, E. M., 2016. Rupture complexity and the supershear transition on rough faults, *J. Geophys. Res. Solid Earth*, **121**(1), 210–224.
- D’Amico, S., Koper, K. D., Herrmann, R. B., Akinci, A., & Malagnini, L., 2010. Imaging the rupture of the Mw 6.3 April 6, 2009 L’Aquila, Italy earthquake using back-projection of teleseismic P-waves, *Geophys. Res. Lett.*, **37**(3), 1–5.
- Das, S. & Aki, K., 1977. Fault plane with barriers: A versatile earthquake model, *J. Geophys. Res.*, **82**(36), 5658–5670.
- DeMets, C., Gordon, R. G., & Argus, D. F., 2010. Geologically current plate motions, *Geophys. J. Int.*, **181**(1), 1–80.
- Dunham, E. M., Belanger, D., Cong, L., & Kozdon, J. E., 2011. Earthquake Ruptures with Strongly Rate-Weakening Friction and Off-Fault Plasticity, Part 2: Nonplanar Faults, *Bull. Seismol. Soc. Am.*, **101**(5), 2308–2322.

- 1  
2  
3  
4  
5  
6 Fan, W. & Shearer, P. M., 2015. Detailed rupture imaging of the 25 April 2015 Nepal earthquake using  
7 teleseismic P waves, *Geophys. Res. Lett.*, **42**(14), 5744–5752.
- 8  
9 Fan, W. & Shearer, P. M., 2016. Local near instantaneously dynamically triggered aftershocks of large earth-  
10 quakes, *Science*, **353**(6304), 1133–1136.
- 11  
12 Fan, W. & Shearer, P. M., 2017. Investigation of Backprojection Uncertainties With M6 Earthquakes, *J.*  
13 *Geophys. Res. Solid Earth*, **122**(10), 7966–7986.
- 14  
15 Fan, W., Shearer, P. M., Ji, C., & Bassett, D., 2016. Multiple branching rupture of the 2009 Tonga-Samoa  
16 earthquake, *J. Geophys. Res. Solid Earth*, **121**(8), 5809–5827.
- 17  
18 Fan, W., Bassett, D., Jiang, J., Shearer, P. M., & Ji, C., 2017. Rupture evolution of the 2006 Java tsunami  
19 earthquake and the possible role of splay faults, *Tectonophysics*, **721**, 143–150.
- 20  
21 Fukahata, Y., Yagi, Y., & Rivera, L., 2014. Theoretical relationship between back-projection imaging and  
22 classical linear inverse solutions, *Geophys. J. Int.*, **196**(1), 552–559.
- 23  
24 Hunter, J. D., 2007. Matplotlib: A 2D Graphics Environment, *Comput. Sci. Eng.*, **9**(3), 90–95.
- 25  
26 Ishii, M., Shearer, P. M., Houston, H., & Vidale, J. E., 2005. Extent, duration and speed of the 2004 Sumatra-  
27 Andaman earthquake imaged by the Hi-Net array, *Nature*, **435**(7044), 933–936.
- 28  
29 Ishii, M., Shearer, P. M., Houston, H., & Vidale, J. E., 2007. Teleseismic P wave imaging of the 26 December  
30 2004 Sumatra-Andaman and 28 March 2005 Sumatra earthquake ruptures using the Hi-net array, *J. Geophys.*  
31 *Res. Solid Earth*, **112**(11), 1–16.
- 32  
33 Kennett, B. L. N., Engdahl, E. R., & Buland, R., 1995. Constraints on seismic velocities in the Earth from  
34 traveltimes, *Geophys. J. Int.*, **122**(1), 108–124.
- 35  
36 Kikuchi, M. & Kanamori, H., 1991. Inversion of complex body waves-III, *Bull. Seismol. Soc. Am.*, **81**(6),  
37 2335–2350.
- 38  
39 Kiser, E. & Ishii, M., 2011. The 2010 mw 8.8 Chile earthquake: Triggering on multiple segments and  
40 frequency-dependent rupture behavior, *Geophys. Res. Lett.*, **38**(7).
- 41  
42 Kiser, E. & Ishii, M., 2013. Hidden aftershocks of the 2011 Mw 9.0 Tohoku, Japan earthquake imaged with  
43 the backprojection method, *J. Geophys. Res. Solid Earth*, **118**(10), 5564–5576.
- 44  
45 Kiser, E. & Ishii, M., 2017. Back-Projection Imaging of Earthquakes, *Annu. Rev. Earth Planet. Sci.*, **45**(1),  
46 271–299.
- 47  
48 Kiser, E., Ishii, M., Langmuir, C. H., Shearer, P. M., & Hirose, H., 2011. Insights into the mechanism of  
49 intermediate-depth earthquakes from source properties as imaged by back projection of multiple seismic  
50 phases, *J. Geophys. Res. Solid Earth*, **116**(6), 1–26.
- 51  
52 Koper, K. D., Hutko, A. R., Lay, T., & Sufri, O., 2012. Imaging short-period seismic radiation from the 27  
53 February 2010 Chile (MW 8.8) earthquake by back-projection of P, PP, and PKIKP waves, *J. Geophys. Res.*  
54 *Solid Earth*, **117**(B2), 1–16.
- 55  
56 Lay, T., Kanamori, H., Ammon, C. J., Koper, K. D., Hutko, A. R., Ye, L., Yue, H., & Rushing, T. M.,  
57 2012. Depth-varying rupture properties of subduction zone megathrust faults, *J. Geophys. Res. Solid Earth*,  
58 **117**(B4), 1–12.
- 59  
60

18 R. Okuwaki, A. Kasahara, Y. Yagi, S. Hirano, and Y. Fukahata

- Madariaga, R., 1977. High-frequency radiation from crack (stress drop) models of earthquake faulting, *Geophys. J. Int.*, **51**(3), 625–651.
- Madariaga, R., Ampuero, J. P., & Adda-Bedia, M., 2006. Seismic radiation from simple models of earthquakes, in *Earthquakes Radiated Energy Phys. Faulting*, no. 1999, pp. 223–236.
- Mai, P. M., Galis, M., Thingbaijam, K. K. S., Vyas, J. C., & Dunham, E. M., 2017. Accounting for Fault Roughness in Pseudo-Dynamic Ground-Motion Simulations, *Pure Appl. Geophys.*, **174**(9), 3419–3450.
- McFadden, P. L., Drummond, B. J., & Kravis, S., 1986. The Nth-root stack: Theory, applications, and examples, *Geophysics*, **51**(10), 1879–1892.
- Melgar, D., Fan, W., Riquelme, S., Geng, J., Liang, C., Fuentes, M., Vargas, G., Allen, R. M., Shearer, P. M., & Fielding, E. J., 2016. Slip segmentation and slow rupture to the trench during the 2015, M w 8.3 Illapel, Chile earthquake, *Geophys. Res. Lett.*, **43**(3), 961–966.
- Meng, L., Inbal, A., & Ampuero, J.-P., 2011. A window into the complexity of the dynamic rupture of the 2011 Mw 9 Tohoku-Oki earthquake, *Geophys. Res. Lett.*, **38**(7), 1–6.
- Meng, L., Ampuero, J.-P., Sladen, A., & Rendon, H., 2012a. High-resolution backprojection at regional distance: Application to the Haiti M 7.0 earthquake and comparisons with finite source studies, *J. Geophys. Res. Solid Earth*, **117**(B4), 1–16.
- Meng, L., Ampuero, J.-P., Stock, J., Duputel, Z., Luo, Y., & Tsai, V. C., 2012b. Earthquake in a Maze: Compressional Rupture Branching During the 2012 Mw 8.6 Sumatra Earthquake, *Science*, **337**(6095), 724–726.
- Meng, L., Zhang, A., & Yagi, Y., 2016. Improving back projection imaging with a novel physics-based aftershock calibration approach: A case study of the 2015 Gorkha earthquake, *Geophys. Res. Lett.*, **43**(2), 628–636.
- Meng, L., Bao, H., Huang, H., Zhang, A., Bloore, A., & Liu, Z., 2018. Double pincer movement: Encircling rupture splitting during the 2015 mw 8.3 illapel earthquake, *Earth Planet. Sci. Lett.*, **495**, 164 – 173.
- Okuwaki, R. & Yagi, Y., 2018. Role of geometric barriers in irregular-rupture evolution during the 2008 Wenchuan earthquake, *Geophys. J. Int.*, **212**(3), 1657–1664.
- Okuwaki, R., Yagi, Y., & Hirano, S., 2014. Relationship between High-frequency Radiation and Asperity Ruptures, Revealed by Hybrid Back-projection with a Non-planar Fault Model, *Sci. Rep.*, **4**(1), 7120.
- Okuwaki, R., Yagi, Y., Aránguiz, R., González, J., & González, G., 2016. Rupture Process During the 2015 Illapel, Chile Earthquake: Zigzag-Along-Dip Rupture Episodes, *Pure Appl. Geophys.*, **173**(4), 1011–1020.
- Satriano, C., Kiraly, E., Bernard, P., & Vilotte, J.-P., 2012. The 2012 Mw 8.6 Sumatra earthquake: Evidence of westward sequential seismic ruptures associated to the reactivation of a N-S ocean fabric, *Geophys. Res. Lett.*, **39**(15), 1–6.
- Satriano, C., Dionicio, V., Miyake, H., Uchida, N., Vilotte, J. P., & Bernard, P., 2014. Structural and thermal control of seismic activity and megathrust rupture dynamics in subduction zones: Lessons from the Mw 9.0, 2011 Tohoku earthquake, *Earth Planet. Sci. Lett.*, **403**, 287–298.
- Shi, Z. & Day, S. M., 2013. Rupture dynamics and ground motion from 3-D rough-fault simulations, *J.*

- Geophys. Res. Solid Earth*, **118**(3), 1122–1141.
- Sniieder, R. & Şafak, E., 2006. Extracting the building response using seismic interferometry: Theory and application to the Millikan Library in Pasadena, California, *Bull. Seismol. Soc. Am.*, **96**(2), 586–598.
- Spudich, P. & Frazer, L., 1984. Use of ray theory to calculate high-frequency radiation from earthquake sources having spatially variable rupture velocity and stress drop, *Bull. Seismol. Soc. Am.*, **74**(6), 2061–2082.
- Suzuki, M. & Yagi, Y., 2011. Depth dependence of rupture velocity in deep earthquakes, *Geophys. Res. Lett.*, **38**(5), 1–5.
- Uchide, T., Yao, H., & Shearer, P. M., 2013. Spatio-temporal distribution of fault slip and high-frequency radiation of the 2010 El Mayor-Cucapah, Mexico earthquake, *J. Geophys. Res. Solid Earth*, **118**(4), 1546–1555.
- Vallée, M. & Satriano, C., 2014. Ten year recurrence time between two major earthquakes affecting the same fault segment, *Geophys. Res. Lett.*, **41**(7), 2312–2318.
- Wang, D. & Mori, J., 2011. Frequency-dependent energy radiation and fault coupling for the 2010 Mw8.8 Maule, Chile, and 2011 Mw9.0 Tohoku, Japan, earthquakes, *Geophys. Res. Lett.*, **38**(22), 1–7.
- Yagi, Y. & Fukahata, Y., 2011. Introduction of uncertainty of Green's function into waveform inversion for seismic source processes, *Geophys. J. Int.*, **186**(2), 711–720.
- Yagi, Y. & Okuwaki, R., 2015. Integrated seismic source model of the 2015 Gorkha, Nepal, earthquake, *Geophys. Res. Lett.*, **42**(15), 6229–6235.
- Yagi, Y., Nakao, A., & Kasahara, A., 2012. Smooth and rapid slip near the Japan Trench during the 2011 Tohoku-oki earthquake revealed by a hybrid back-projection method, *Earth Planet. Sci. Lett.*, **355–356**, 94–101.
- Yao, H., Shearer, P. M., & Gerstoft, P., 2013. Compressive sensing of frequency-dependent seismic radiation from subduction zone megathrust ruptures, *Proc. Natl. Acad. Sci.*, **110**(12), 4512–4517.
- Ye, L., Lay, T., Kanamori, H., & Koper, K. D., 2013. Energy release of the 2013 Mw 8.3 Sea of Okhotsk earthquake and deep slab stress heterogeneity, *Science*, **341**(6152), 1380–1384.
- Ye, L., Lay, T., Kanamori, H., & Rivera, L., 2016. Rupture characteristics of major and great ( $M_w \geq 7.0$ ) megathrust earthquakes from 1990 to 2015: 2. Depth dependence, *J. Geophys. Res. Solid Earth*, **121**(2), 845–863.
- Yin, J., Yang, H., Yao, H., & Weng, H., 2016. Coseismic radiation and stress drop during the 2015 Mw 8.3 Illapel, Chile megathrust earthquake, *Geophys. Res. Lett.*, **43**(4), 1520–1528.
- Yin, J., Denolle, M. A., & Yao, H., 2018. Spatial and Temporal Evolution of Earthquake Dynamics: Case Study of the Mw 8.3 Illapel Earthquake, Chile, *J. Geophys. Res. Solid Earth*, pp. 1–24.