



# Evaluation of H<sub>2</sub>O-CO<sub>2</sub> solubility models in silicate melts: Precision and accuracy of vapor saturation pressure and composition

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Conceptualization: E.C. Hughes, L.M. Saper

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Methodology: E.C. Hughes, L.M. Saper

Visualization: E.C. Hughes

Writing – original draft: E.C. Hughes

Writing – review & editing: E.C. Hughes, L.M. Saper

## Data, code, and outputs

The experimental data compilation (no new experimental data is associated with this manuscript); all calculation outputs and figures; and the Jupyter Notebook and Python files for running the

31 calculations and plotting the figures are available at [https://github.com/eryhughes/evaluation\\_H2O-](https://github.com/eryhughes/evaluation_H2O-)  
32 [CO2-solubility-models](https://github.com/eryhughes/evaluation_H2O-CO2-solubility-models).

## 33 Abstract

34 Solubility models for H<sub>2</sub>O and CO<sub>2</sub> in silicate melt are crucial in igneous petrology and volcanology, in  
35 particular for calculating the pressure of vapor saturation of melts from their dissolved volatile  
36 content as a barometer, as well as melt and vapor compositions and proportions during degassing.  
37 We assessed the accuracy and precision of the calculated pressure of vapor saturation and  
38 equilibrium vapor composition using various H<sub>2</sub>O-CO<sub>2</sub> solubility models implemented in VESical  
39 (Dixon, Liu, IaconoMarziano, ShishkinaIdealMixing, and MagmaSat) using a dataset containing 770  
40 vapor-saturated experimental glasses. Experimental and analytical uncertainties were included but  
41 model errors were not considered. Across each models' full calibration range, pressure of vapor  
42 saturation calculations using IaconoMarziano and MagmaSat are accurate, whilst Dixon, Liu, and  
43 ShishkinaIdealMixing, are quite inaccurate, and all are relatively imprecise. Most models except  
44 ShishkinaIdealMixing are accurate for vapor composition, but all are relatively imprecise. Both  
45 accuracy and precision for each model tend to be better for specific melt compositions within the  
46 range of experimental pressure-temperature conditions. Hence, for application to natural systems, it  
47 is important to assess the accuracy and precision of H<sub>2</sub>O-CO<sub>2</sub> solubility models using experimental  
48 data that are closely matched to the system of interest.

## 49 Introduction

50 Water (H<sub>2</sub>O) and carbon dioxide (CO<sub>2</sub>) are typically the most abundant volatiles in many  
51 terrestrial silicate melts prior to extensive degassing or crystallisation (e.g., Edmonds et al., accepted;  
52 Wallace, Plank, et al., 2015). The concentration of dissolved volatiles has a major influence on the  
53 viscosity and density of magmas; phase equilibria at a given pressure ( $P$ ) and temperature ( $T$ ); and  
54 the chemical composition of melt and vapor during degassing (e.g., Dixon & Stolper, 1995; Feig et al.,  
55 2006; Giordano et al., 2008). Crucially, the dissolved volatile content of silicate melt is often used as a  
56 barometer based on the pressure of vapor saturation ( $P_{\text{sat}}^v$ ), often applied to melt inclusion and  
57 matrix glass data (e.g., Anderson et al., 1989; Blundy & Cashman, 2008; Hughes et al., 2024). Hence,  
58 accurate and precise models of H<sub>2</sub>O-CO<sub>2</sub> solubility are critical when trying to petrologically image the  
59 plumbing system of a particular volcano or estimate the eruption depth from submarine tephra,

60 especially if comparing to geophysical estimates (e.g., Hughes et al., 2023; Kilgour et al., 2013;  
61 Wieser, Kent, Till, et al., 2023). Additionally, the vapor composition ( $x_{\text{H}_2\text{O}}^v$  and  $x_{\text{CO}_2}^v$  – mole fraction in  
62 the vapor) is often used to calculate the compositions of melt inclusion-hosted bubbles when these  
63 bubbles cannot be analysed and therefore to reconstruct the true volatile content of melt inclusions  
64 at their time of entrapment (e.g., Rasmussen et al., 2020; Wallace, Kamenetsky, et al., 2015). Water  
65 and CO<sub>2</sub> solubility models form the basis of multi-volatile degassing model, which are used to  
66 interpret both melt inclusion and volcanic gas data (e.g., Burgisser et al., 2015; Ding et al., 2023;  
67 Hughes et al., 2025; Liggins et al., 2020; Moretti et al., 2003; Sun & Lee, 2022). The H<sub>2</sub>O content of  
68 the melt has a major influence on melt density and viscosity, and therefore H<sub>2</sub>O solubility models  
69 impact the accuracy of conduit models of volcanic ascent (e.g., La Spina et al., 2022; Mastin, 2002).  
70 Accurate CO<sub>2</sub> solubility models are required to estimate magma depth from the C/S ratio of volcanic  
71 gases, which is often used in volcano monitoring (e.g., Aiuppa et al., 2007; Kern et al., 2022). Hence,  
72 accurate and precise solubilities of H<sub>2</sub>O and CO<sub>2</sub> in silicate melts are important for a variety of  
73 applications in igneous petrology and volcanology.

74 In the literature there are a variety of H<sub>2</sub>O-CO<sub>2</sub> solubility models, as well as tools for calculating  
75  $P_{\text{sat}}^v$ ,  $x_{\text{H}_2\text{O}}^v$ , and  $x_{\text{CO}_2}^v$  from a specified melt composition using these models (see review by Wieser et  
76 al., 2022). Solubility model uncertainties are often assessed by comparing the calculated and  
77 measured volatile content of the melt from experiments at known conditions, either graphically or  
78 numerically (e.g., Duan, 2014; Ghiorso & Gualda, 2015; Iacono-Marziano et al., 2012; Jiménez-Mejías  
79 et al., 2022; Liu et al., 2005; Papale et al., 2022; Shishkina et al., 2014). However, the parameter of  
80 interest for users is often the calculated  $P_{\text{sat}}^v$ ,  $x_{\text{H}_2\text{O}}^v$ , and/or  $x_{\text{CO}_2}^v$  from the dissolved H<sub>2</sub>O and CO<sub>2</sub>,  
81 melt composition, and  $T$ . Hence, sometimes isobars are calculated and graphically compared to  
82 experimental data at experimental  $P$  to assess model accuracy ( $P_{\text{exp}}$ : e.g., Ghiorso & Gualda, 2015;  
83 Jiménez-Mejías et al., 2022; Newman & Lowenstern, 2002; Wieser et al., 2022; Yoshimura, 2023).  
84 Occasionally, calculated  $P_{\text{sat}}^v$  is compared to  $P_{\text{exp}}$  from experiments graphically (e.g., Duan, 2014;

85 Newman & Lowenstern, 2002; Papale et al., 2006) or the deviation between them is reported (e.g.,  
86 Jiménez-Mejías et al., 2022; Papale et al., 2006).

87 This study builds upon these efforts to investigate the accuracy and precision of existing H<sub>2</sub>O-  
88 CO<sub>2</sub> solubility models for calculating  $P_{\text{sat}}^v$ ,  $x_{\text{H}_2\text{O}}^v$ , and  $x_{\text{CO}_2}^v$  from the dissolved H<sub>2</sub>O and CO<sub>2</sub> content of  
89 silicate melt by leveraging: (1) the large number of experiments on H<sub>2</sub>O-CO<sub>2</sub> solubility that have been  
90 published since 2015, when the most recent of the models used in this study was developed  
91 (MagmaSat; Ghiorso & Gualda, 2015), and (2) the creation of the Python package VESlcal (Iacovino et  
92 al., 2021) that enables large numbers of calculations of  $P_{\text{sat}}^v$  and equilibrium vapor composition to be  
93 done accurately, easily, and quickly using a variety of different H<sub>2</sub>O-CO<sub>2</sub> solubility models.

## 94 Methods

95 The aim is to evaluate the accuracy and precision of existing H<sub>2</sub>O-CO<sub>2</sub> solubility models by  
96 comparing calculated  $P_{\text{sat}}^v$ ,  $x_{\text{H}_2\text{O}}^v$ , and  $x_{\text{CO}_2}^v$  to  $P_{\text{exp}}$  and measured vapor composition from vapor-  
97 saturated melt experiments (e.g., Duan, 2014; Jiménez-Mejías et al., 2022; Newman & Lowenstern,  
98 2002; Papale et al., 2006).

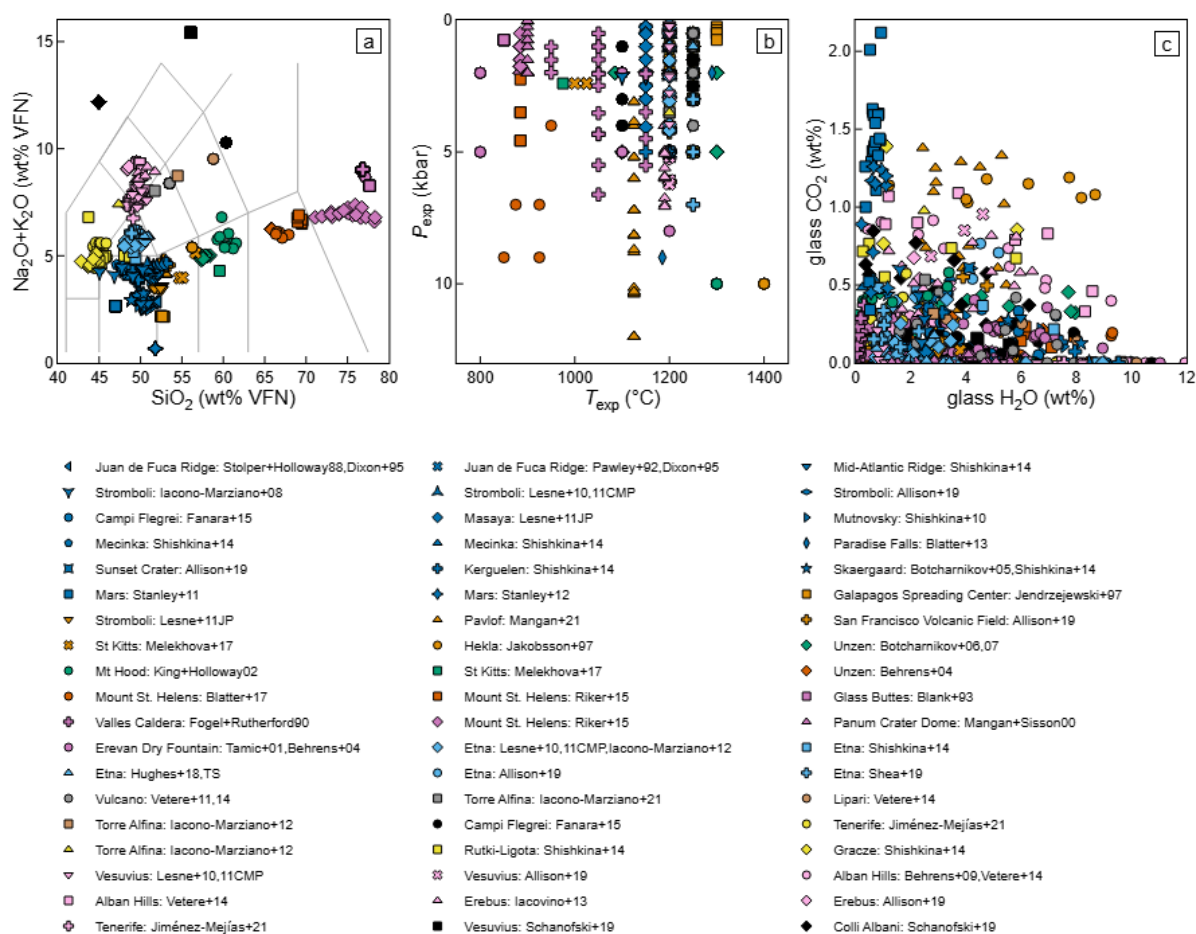
## 99 Experimental data in the literature

100 Experimental data was collated from the literature where there was vapor-saturated silicate  
101 melt at known  $P$  and  $T$  with measured major/minor oxide, H<sub>2</sub>O, and CO<sub>2</sub> concentrations in the  
102 quenched glasses. These data mostly come from superliquidus experiments (i.e., melt and vapor  
103 only), but some data are from crystallisation experiments. Data collation focussed on studies where  
104 the vapor is mixed H<sub>2</sub>O-CO<sub>2</sub>: however, if experiments on pure-H<sub>2</sub>O or -CO<sub>2</sub> with the same melt  
105 composition are available, these were also included. If major and minor oxide concentrations are not  
106 available for each experimental glass, the average glass composition is used if reported, or, as a last  
107 resort, the starting composition was used for superliquidus experiments. As the vapor is assumed to  
108 contain only H<sub>2</sub>O and CO<sub>2</sub> and the melt only molecular H<sub>2</sub>O, hydroxyl ions (OH<sup>-</sup>), molecular CO<sub>2</sub>,

109 and/or carbonate ions ( $\text{CO}_3^{2-}$ ) in most models and tools that calculate  $P_{\text{sat}}^v$  and vapor composition,  
110 we chose to focus on experiments that are sufficiently oxidising such that  $\text{H}_2$ ,  $\text{CO}$ , and  $\text{CH}_4$  are not  
111 important species in the melt or vapor ( $\text{O}_2$  is always a small proportion of the vapor phase under  
112 geological conditions such that its effect on  $P$  can be ignored). Additionally, experiments with other  
113 volatiles (e.g.,  $\text{Cl}$  and  $\text{S}$ ) were only included if non- $\text{H}_2\text{O}$ - $\text{CO}_2$  vapor species were a minor component of  
114 the vapor. If  $x_{\text{H}_2\text{O}}^v$  and/or  $x_{\text{CO}_2}^v$  are reported, these are included in the dataset: for mixed  $\text{H}_2\text{O}$ - $\text{CO}_2$   
115 experiments, if only one of  $x_{\text{H}_2\text{O}}^v$  or  $x_{\text{CO}_2}^v$  are reported, the other is calculated assuming the vapor  
116 contains only  $\text{H}_2\text{O}$  and  $\text{CO}_2$ . If uncertainties are not reported, the following are assumed:  $\pm 10$  °C for  
117 experimental  $T$  ( $T_{\text{exp}}$ );  $\pm 1\%$  relative for major/minor oxide glass chemistry; and  $\pm 10\%$  relative for glass  
118  $\text{H}_2\text{O}$  and  $\text{CO}_2$  concentrations.

119 The collated literature dataset contains 770 individual experimental glasses from 39 studies,  
120 covering a wide range of melt compositions and  $P$ - $T$  space (Figure 1; Allison et al., 2019; Behrens et al.,  
121 2009; Behrens, Ohlhorst, et al., 2004; Behrens, Tamic, et al., 2004; Blank et al., 1993; Blatter et al.,  
122 2013, 2017; Botcharnikov et al., 2005, 2006, 2007; Dixon et al., 1995; Fanara et al., 2015; Fogel &  
123 Rutherford, 1990; Hughes et al., 2018; Iacono Marziano et al., 2007; Iacono-Marziano et al., 2012;  
124 Iacovino et al., 2013; Jakobsson, 1997; Jendrzewski et al., 1997; Jiménez-Mejías et al., 2022; King &  
125 Holloway, 2002; Lesne, Kohn, et al., 2011; Lesne, Scaillet, Pichavant, & Brey, 2011; Lesne, Scaillet,  
126 Pichavant, Iacono-Marziano, et al., 2011; Mangan et al., 2021; Mangan & Sisson, 2000; Melekhova et  
127 al., 2017; Pawley et al., 1992; Riker et al., 2015; Schanofski et al., 2019; Shea et al., 2025; Shishkina et  
128 al., 2010, 2014; Stanley et al., 2011, 2012; Stolper & Holloway, 1988; Tamic et al., 2001; Vetere et al.,  
129 2011, 2014). Most of the experiments were conducted at 800–1300 °C and <10 kbar, with two studies  
130 on Martian basalts at 1400–1650 °C and 10–25 kbar (Stanley et al., 2011, 2012) (Figure 1b). Roughly  
131 57 different melt compositions are covered in the dataset: most of the experiments are conducted on  
132 basalts/basaltic andesites (36%) and alkali-rich compositions (41%, particularly phonotephrites at  
133 14%), with far fewer on more evolved compositions (6% on andesites, 3% on dacites, and 14% on  
134 rhyolites) (Figure 1a and Figure 2). Around 17% have measured  $\text{Fe}^{3+}/\text{Fe}_T$  (Figure 3c), which is sometimes

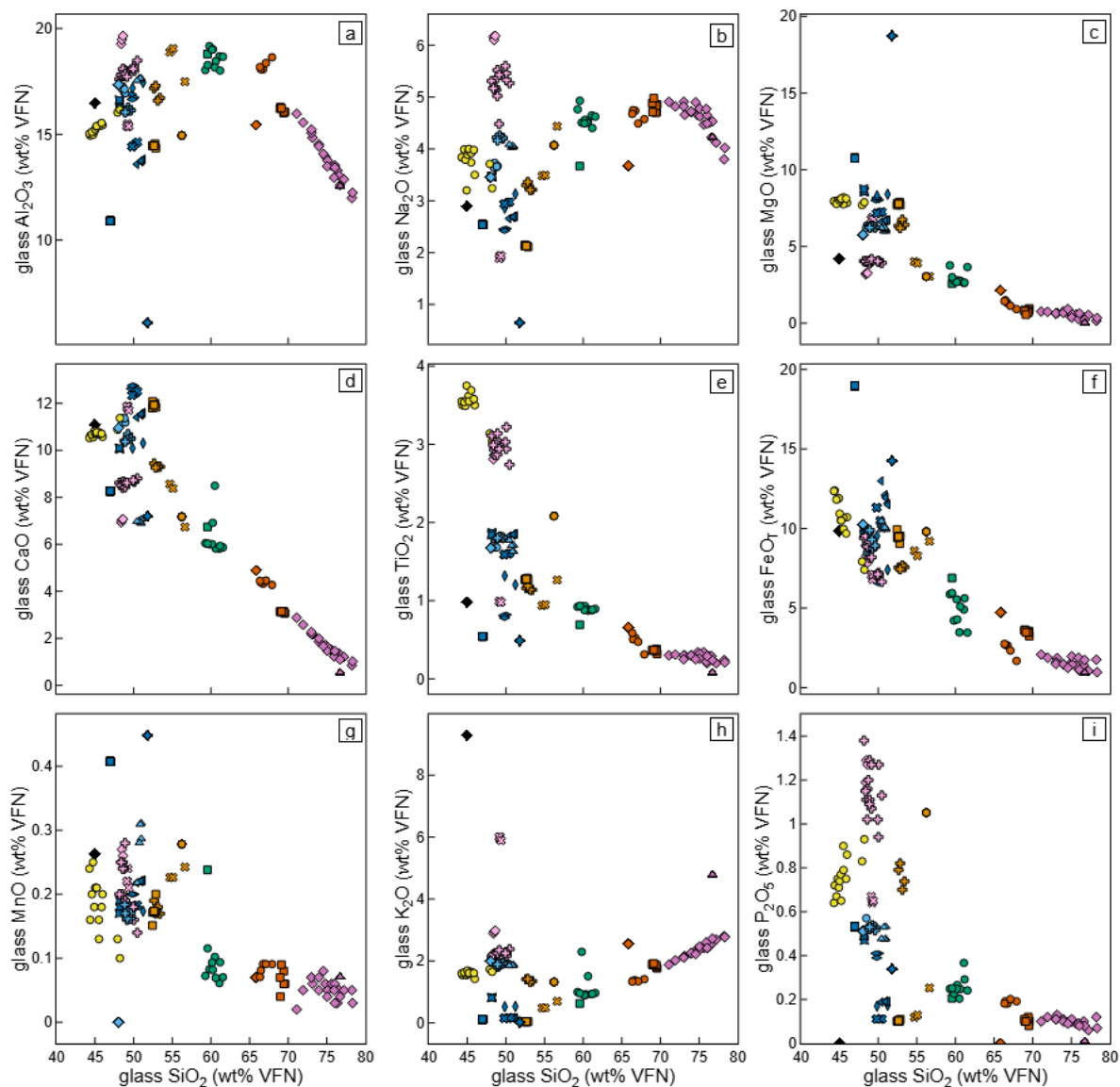
135 used in H<sub>2</sub>O-CO<sub>2</sub> solubility models (e.g., Ghiorso & Gualda, 2015). Most of the experiments are mixed  
 136 H<sub>2</sub>O-CO<sub>2</sub> (82%), 18% are H<sub>2</sub>O-only, and one experiment is CO<sub>2</sub>-only (Figure 1c). The maximum H<sub>2</sub>O  
 137 content of the melt is 11.95 wt% and maximum CO<sub>2</sub> is 2.12 wt%, but ~75% of the experiments have <5  
 138 wt% H<sub>2</sub>O or <3000 ppmw CO<sub>2</sub> (Figure 1c), with 63% of experiments reporting the fluid composition  
 139 (Figure 3a and b). Just over 30% of the experiments were published since 2015, the year the most  
 140 recent model tested in this study was published (Ghiorso & Gualda, 2015).



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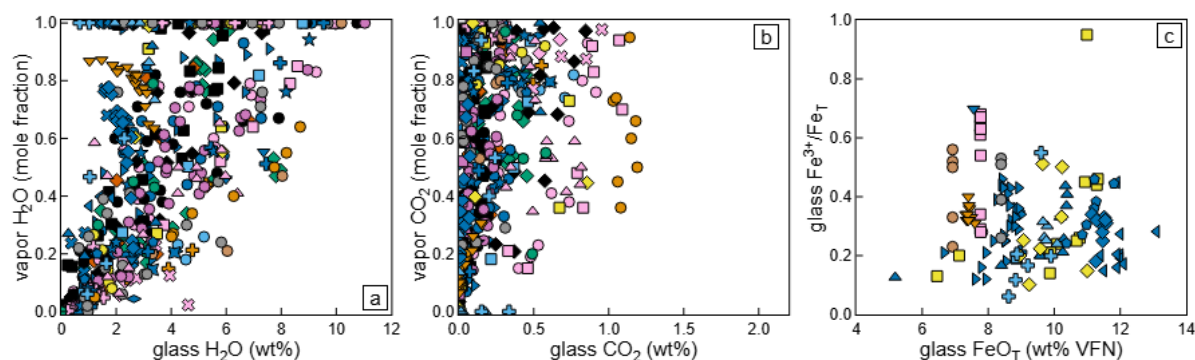
142 **Figure 1:** Glass composition and experimental conditions for vapor-saturated silicate melt  
 143 experiments collated from the literature ( $n = 770$ ). (a) Total alkalis (Na<sub>2</sub>O+K<sub>2</sub>O) vs. SiO<sub>2</sub> (both volatile-  
 144 free normalised: VFN) with TAS classification fields indicated by grey lines. (b) Experimental pressure  
 145 ( $P_{exp}$ ) vs. temperature ( $T_{exp}$ ): Martian basalts from Stanley et al. (2011) and Stanley et al. (2012),  
 146 which are at higher  $P$ - $T$ , are not shown for clarity. (c) Glass CO<sub>2</sub> vs. H<sub>2</sub>O. In all panels, symbol colour  
 147 indicates the TAS classification and shape (within a TAS classification) indicates specific melt  
 148 composition (and study/studies) as detailed in the legend. Uncertainties are not plotted for clarity.  
 149 References: Allison et al. (2019), Behrens et al. (2009), Behrens, Tamic, et al. (2004), Behrens,

150 *Ohlhorst, et al. (2004), Blank et al. (1993), Blatter et al. (2013), Blatter et al. (2017), Botcharnikov et*  
151 *al. (2005), Botcharnikov et al. (2006), Botcharnikov et al. (2007), Dixon et al. (1995), Fanara et al.*  
152 *(2015), Fogel & Rutherford (1990), Hughes et al. (2018), Iacono Marziano et al. (2007), Iacono-*  
153 *Marziano et al. (2012), Iacovino et al. (2013), Jakobsson (1997), Jendrzejewski et al. (1997), Jiménez-*  
154 *Mejías et al. (2022), King & Holloway (2002), Lesne, Scaillet, Pichavant, & Brey (2011), Lesne, Scaillet,*  
155 *Pichavant, Iacono-Marziano, et al. (2011), Lesne, Kohn, et al. (2011), Mangan & Sisson (2000),*  
156 *Mangan et al. (2021), Melekhova et al. (2017), Pawley et al. (1992), Riker et al. (2015), Schanofski et*  
157 *al. (2019), Shea et al. (2025), Shishkina et al. (2010), Shishkina et al. (2014), Stanley et al. (2011),*  
158 *Stanley et al. (2012), Stolper & Holloway (1988), Tamic et al. (2001), Vetere et al. (2011), and Vetere*  
159 *et al. (2014). All figures were created using Plotly's Python Library.*



160

161 **Figure 2:**  $\text{SiO}_2$  vs. oxide concentration (both volatile-free normalised, VFN) for all experimental glasses  
 162 in the dataset.  $\text{FeO}_T$  refers to total Fe as FeO. Uncertainties are not plotted for clarity. Symbol  
 163 shapes/colours and references as in Figure 1.



164

165 **Figure 3:** Vapor composition and iron speciation for experimental glasses in the dataset where it is  
 166 measured. Vapor composition against glass volatile concentration for (a) H<sub>2</sub>O and (b) CO<sub>2</sub>. (c) Iron  
 167 oxidation state (Fe<sup>3+</sup>/Fe<sub>T</sub>) against total iron as FeO in the glass (FeO<sub>T</sub>). Uncertainties are not plotted  
 168 for clarity. Symbol shapes/colours and references as in Figure 1.

### 169 Calculations of the vapor saturation pressure and composition

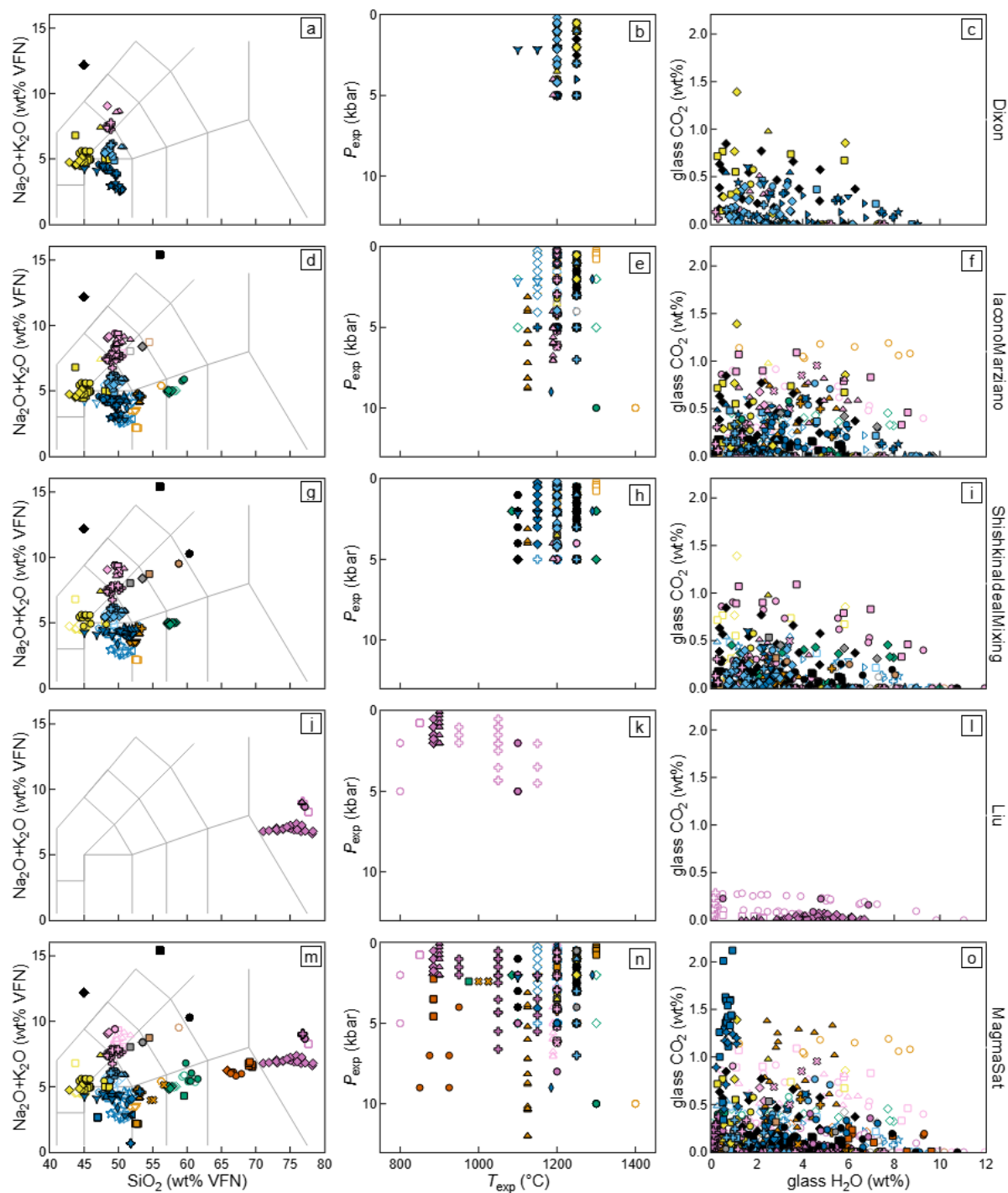
170 The Python package VESical (v1.2.10, Iacovino et al., 2021) including ThermoEngineLite  
 171 (v2.0.0.dev7, Wolf et al., 2026) was used to calculate  $P_{\text{sat}}^v$ ,  $x_{\text{H}_2\text{O}}^v$ , and  $x_{\text{CO}_2}^v$  for experiments from the  
 172 dataset within the reported calibration ranges (Iacovino et al., 2021; Wieser et al., 2022) for the  
 173 following H<sub>2</sub>O-CO<sub>2</sub> solubility models (Table 1 and Figure 4), which are referred to as they are in  
 174 Iacovino et al. (2021): Dixon (aka VolatileCalc-Basalt: Dixon, 1997; Newman & Lowenstern, 2002); Liu  
 175 (Liu et al., 2005); IaconoMarziano (Iacono-Marziano et al., 2012); ShishkinaIdealMixing (Shishkina et  
 176 al., 2014); and MagmaSat (Ghiorso & Gualda, 2015). These models were chosen because they have  
 177 solubility models for both H<sub>2</sub>O and CO<sub>2</sub>; are individually applicable to a relatively wide range of melt  
 178 compositions; are commonly used by the community; are incorporated into external degassing  
 179 models; and are available in VESical that crucially makes conducting tens of thousands of calculations  
 180 trivial. Broadly, Dixon is applicable to alkali basalts; IaconoMarziano and ShishkinaIdealMixing to sub-  
 181 alkaline and alkaline basalts through andesites; Liu to rhyolites; and MagmaSat to all natural silicate  
 182 melts. Given the wealth of experiments containing vapor-saturated silicate melt published since  
 183 Ghiorso & Gualda (2015), many of the experimental glasses in the dataset were *not* used during  
 184 calibration of these models, enabling independent evaluation: i.e., data included in a model's  
 185 calibration are shown as open symbols, whereas data not included in a model's calibration are shown

186 as filled symbols, in Figure 4. Some interpretation was required when deciding if an experiment was  
 187 included during model calibration due to ambiguities in the original publications.

188 **Table 1:** Calibration range and calculation options for each model.

Model	$T$ (°C) <sup>1</sup>	$P$ (bar) <sup>1</sup>	SiO <sub>2</sub> (wt%) <sup>1</sup>	Normalisation <sup>2</sup>	Redox <sup>3</sup>
Dixon	600–1500	<5000	40–49	None	N/A
IaconoMarziano	1100–1400	<10,000	<57.5	Additional	N/A
ShishkinaIdealMixing	1050 – 1400	<5000	<65	Fixed	No
Liu	700–1200	<5000	Rhyolite	Fixed	N/A
MagmaSat	All	All	Natural	Fixed	Yes

189 *Notes:* 1 Calibration ranges as described in Iacovino et al. (2021) and Wieser et al. (2022). 2 Melt  
 190 composition normalisation routine as described in Iacovino et al. (2021), as suggested in Iacovino et  
 191 al. (2021) and Wieser et al. (2022). 3 Whether Fe<sup>3+</sup>/Fe<sub>T</sub> is used to calculate H<sub>2</sub>O-CO<sub>2</sub> solubility within  
 192 the H<sub>2</sub>O-CO<sub>2</sub> solubility model.



193

194 **Figure 4:** Glass compositions and experimental conditions for literature experiments used for  
 195 evaluating  $H_2O$ - $CO_2$  solubility models (labelled on the right-hand side) within their calibration ranges:  
 196 **(a–c)** Dixon, **(d–f)** IaconoMarziano, **(g–i)** Shishkin al dealMixing, **(j–l)** Liu, and **(m–o)** MagmaSat. **(a, d,**  
 197 **g, j, m)** Total alkalis ( $Na_2O+K_2O$ ) vs.  $SiO_2$  (both normalised volatile-free: VFN) with TAS classification  
 198 fields indicated by grey lines. **(b, e, h, k, n)** Experimental pressure ( $P_{exp}$ ) vs. temperature ( $T_{exp}$ ):  
 199 Martian basalts from Stanley et al. (2011) and Stanley et al. (2012) are not shown for clarity. **(c, f, i, l,**  
 200 **o)** Glass  $CO_2$  vs.  $H_2O$ . Symbols, colours, and references as in Figure 1. Uncertainties are not plotted for

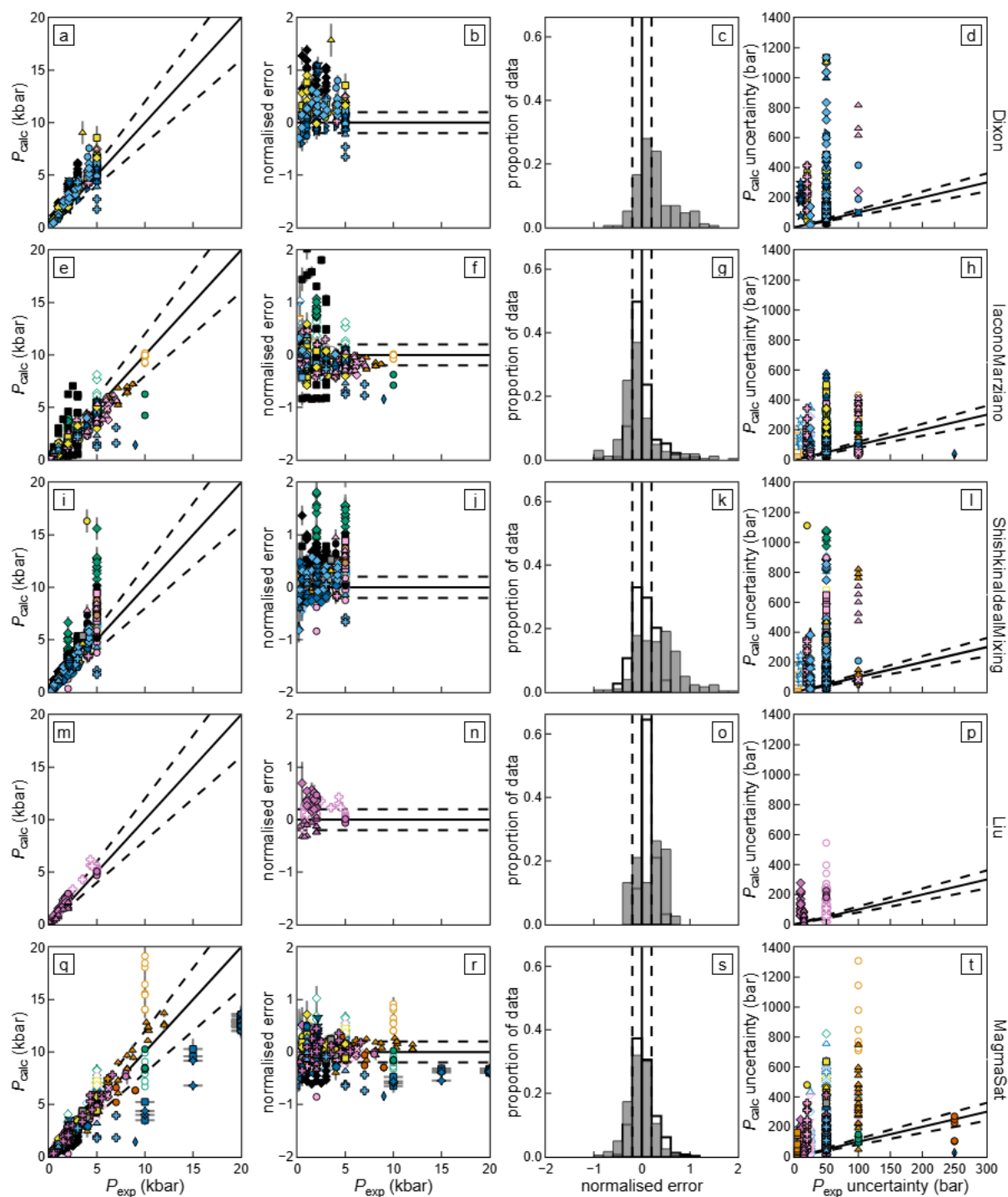
201 *clarity. Open symbols are experiments used to calibrate the model, whereas closed symbols are*  
202 *experiments not used to calibrate the model but within the calibration range of the model (Table 1).*

203 As highlighted in Iacovino et al. (2021) and Wieser et al. (2022), how the glass composition is  
204 normalised can affect the results depending on the model. Data was not normalised when using  
205 Dixon, as recommended by Wieser et al. (2022); ‘additionalvolatiles’ was used for IaconoMarziano  
206 and ‘fixedvolatiles’ for MagmaSat as stated in Iacovino et al. (2021); and ‘fixedvolatiles’ for Liu and  
207 ShishkinaIdealMixing (see Iacovino et al., 2021, for definitions of the different normalisation  
208 routines; Table 1). The oxidation state of Fe can also effect the results depending on the model  
209 (Wieser et al., 2022): Dixon and Liu are unaffected by  $Fe^{3+}/Fe_T$ ; IaconoMarziano only has an  $FeO_T$   
210 term; all Fe is treated as FeO (i.e.,  $FeO_T$ ) for ShishkinaIdealMixing as in the model’s calibration; and  
211 MagmaSat is sensitive to  $Fe^{3+}/Fe_T$ , so measured  $Fe^{3+}/Fe_T$  is used where it is reported but all Fe is  
212 assumed to be FeO if it is not reported (Table 1).

213 To include experimental and analytical uncertainty on calculated  $P_{sat}^v$ ,  $x_{H_2O}^v$ , and  $x_{CO_2}^v$ , a  
214 Monte Carlo approach using 1000 iterations was applied, except for MagmaSat where 100 iterations  
215 were used because it is computationally more expensive and therefore takes longer to run (Iacovino  
216 et al., 2021). The composition of each glass (i.e., major/minor oxide,  $H_2O$ , and  $CO_2$  concentrations)  
217 and  $T_{exp}$  were varied within their analytical/experimental uncertainties assuming uncertainties are  
218 independent from each other and normally distributed about a specified mean and standard  
219 deviation. For each iteration,  $P_{sat}^v$ ,  $x_{H_2O}^v$ , and  $x_{CO_2}^v$  were calculated using the  
220 *calculate\_equilibrium\_fluid\_comp* function in VESICAL, from which the average and standard  
221 deviation of each output parameter was calculated and reported for each experimental glass. This  
222 unfortunately does *not* include the effect of model uncertainty, which would require varying the  
223 model parameters for each  $H_2O$ - $CO_2$  solubility model within their uncertainties, which is not  
224 currently implemented in VESICAL (or any available tool), but will be critical to properly assess  
225 systematic uncertainties in these models in the future. The normalised error distribution (i.e.,  
226 [calculated – known]/known) was calculated for  $P_{sat}^v$ ,  $x_{H_2O}^v$ , and  $x_{CO_2}^v$ .

## 227 Results

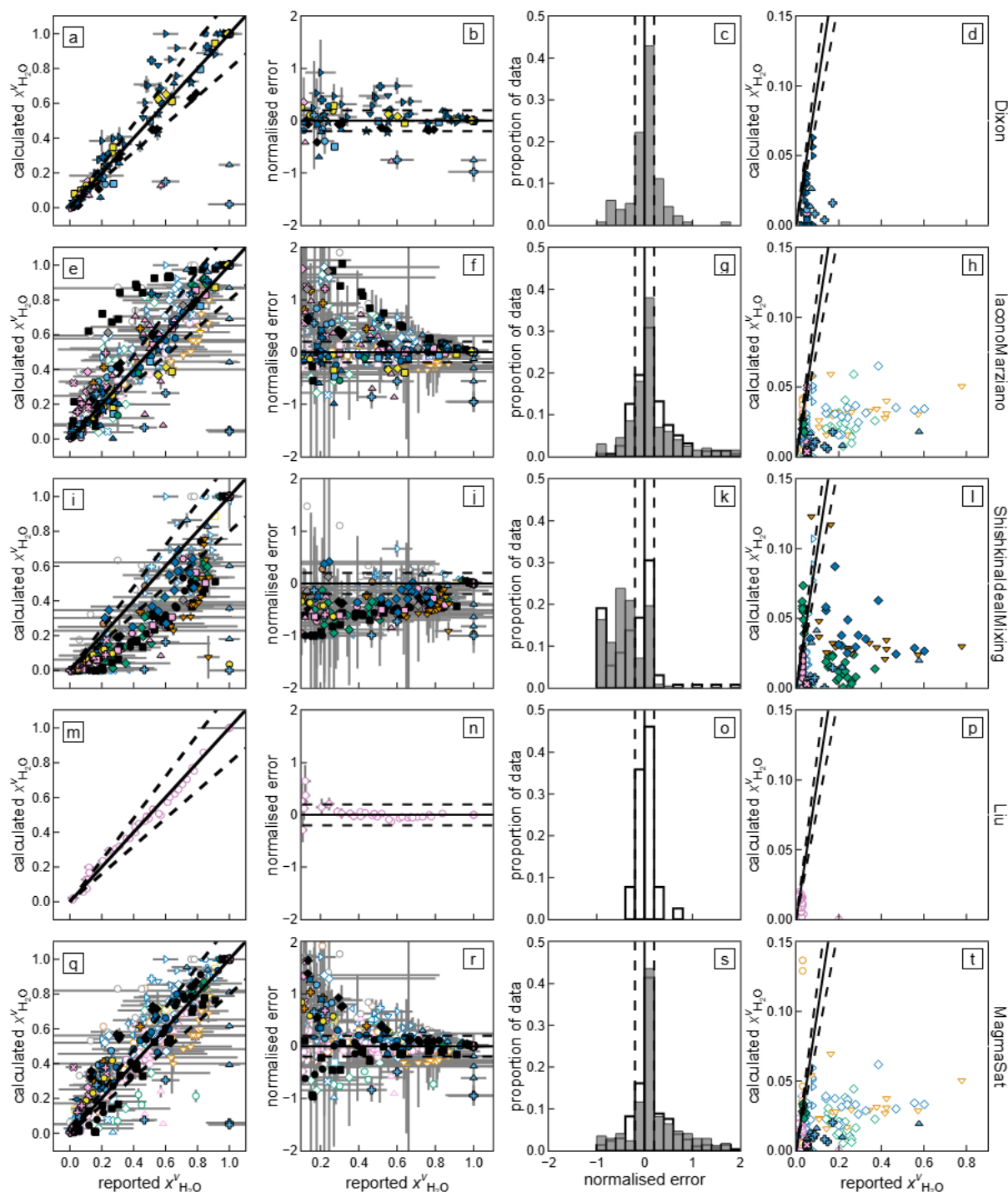
228 Figure 5 is a comparison of  $P_{\text{exp}}$  and calculated  $P_{\text{sat}}^v$  ( $P_{\text{calc}}$ ) for each model, whilst measured  
229 (where available) and calculated  $x_{\text{H}_2\text{O}}^v$  and  $x_{\text{CO}_2}^v$  are shown in Figure 6 and Figure 7, respectively.  
230 Both experimental data not included in the calibration of each model but within its calibration range  
231 (i.e., filled symbols and bars in Figure 5, Figure 6 and Figure 7), as well as experimental data used for  
232 calibrations, are plotted (see Table 2 for number of experiments for each model). Some  $P_{\text{sat}}^v$  values  
233 and their uncertainties derived using laconoMarziano are very large ( $>10,000$  bars  $P_{\text{sat}}^v$  and/or 1000–  
234 30,000 bars uncertainty,  $n = 21$ ), which are all for experiments with 0 ppmw  $\text{CO}_2$ . These values are  
235 not considered further (and are not plotted in Figure 5) because they result from the mathematical  
236 limit of the laconoMarziano model that cannot calculate  $p_{\text{CO}_2} = 0$  when  $\text{CO}_2 = 0$  ppmw (lacono-  
237 Marziano et al., 2012).



238

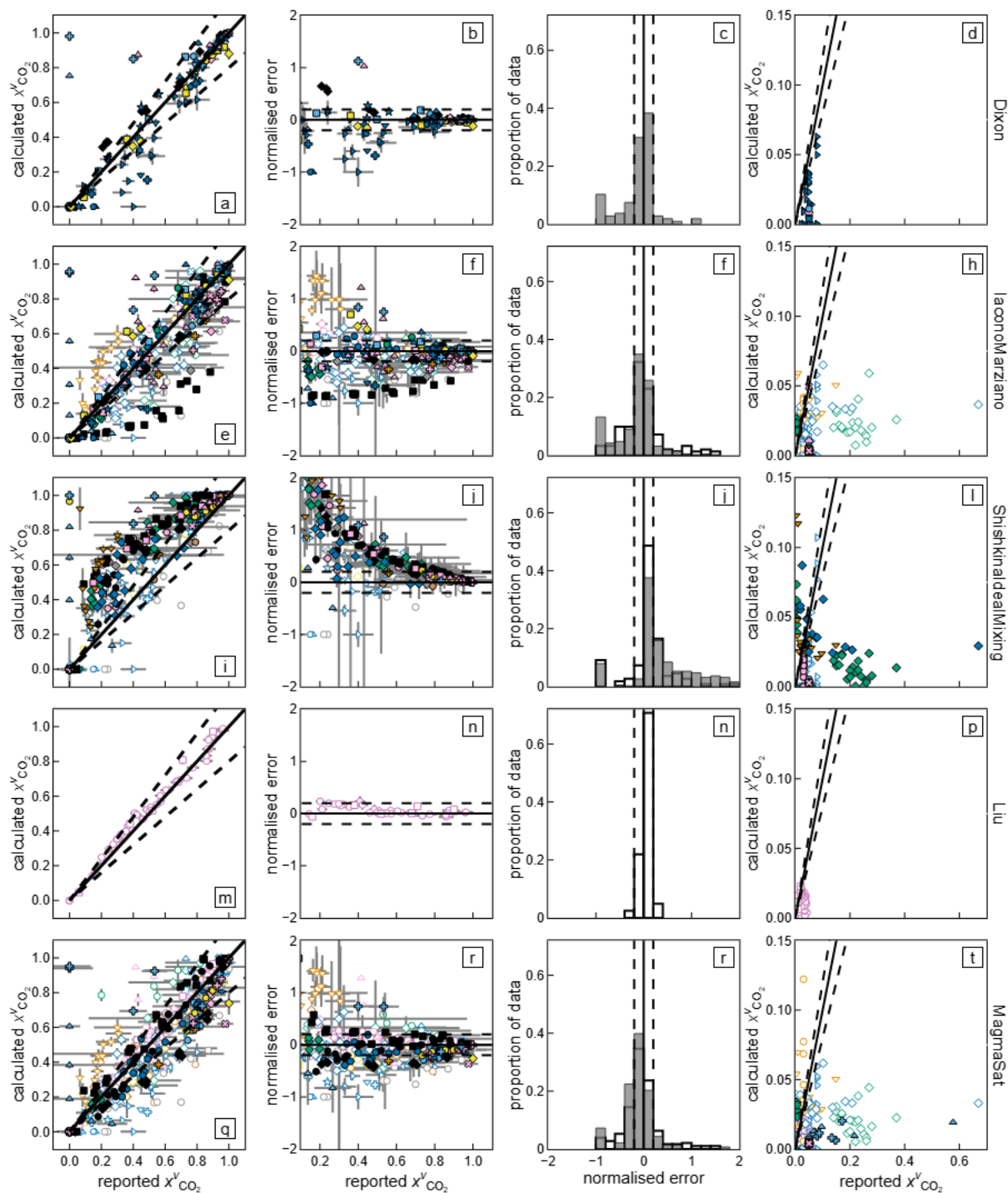
239 **Figure 5:** Evaluating the accuracy and precision of  $P_{Sat}^v$  calculated with  $H_2O-CO_2$  solubility models  
 240 using VEScal (labelled along the right-hand side): **(a–d)** Dixon, **(e–h)** IaconoMarziano, **(i–l)**  
 241 ShishkinaldealMixing, **(m–p)** Liu, and **(q–t)** MagmaSat. **(a, e, i, m, q)** Calculated  $P$  ( $P_{calc}$ , i.e.,  $P_{Sat}^v$ ) vs.  
 242 experimental  $P$  ( $P_{exp}$ ). **(b, f, j, n, r)** Normalised error in  $P_{calc}$  (i.e.,  $[P_{calc} - P_{exp}]/P_{exp}$ ) vs.  $P_{exp}$ . **(c, g, k, o, s)**  
 243 Histogram of normalised error in  $P_{calc}$  by proportion of data. **(d, h, l, p, t)** Calculated uncertainty in  
 244  $P_{calc}$  vs. experimental uncertainty in  $P_{exp}$  (Martian basalts from Stanley et al. (2011) and Stanley et al.  
 245 (2012) are not shown as  $P_{exp} = 1000$  bars). In all panels, the black solid line is perfect agreement and

246 the black dashed lines are  $\pm 20\%$ . Symbols and colours as in Figure 1, except open symbols (or the  
 247 open bars in the histograms) are data used in calibration of the model, whereas filled symbols (or the  
 248 grey histograms) are for data not used in calibration of the model.



249  
 250 **Figure 6:** Evaluating the accuracy and precision of  $x_{H_2O}^v$  calculated with  $H_2O$ - $CO_2$  solubility models  
 251 using VESICAL (labelled along the right-hand side): (a–d) Dixon, (e–h) IaconoMarziano, (i–l)  
 252 ShishkinaldealMixing, (m–p) Liu, and (q–t) MagmaSat. (a, e, i, m, q) Calculated  $x_{H_2O}^v$  vs. reported

- 253  $x_{\text{H}_2\text{O}}^{\text{v}}$ . **(b, f, j, n, r)** Normalised error in  $x_{\text{H}_2\text{O}}^{\text{v}}$  (i.e., [calculated  $x_{\text{H}_2\text{O}}^{\text{v}}$  – reported  $x_{\text{H}_2\text{O}}^{\text{v}}$ ]/reported  $x_{\text{H}_2\text{O}}^{\text{v}}$ ) vs.
- 254 reported  $x_{\text{H}_2\text{O}}^{\text{v}}$ . **(c, g, k, o, s)** Histogram of normalised error in  $x_{\text{H}_2\text{O}}^{\text{v}}$  by proportion of data. **(d, h, l, p, t)**
- 255 Calculated uncertainty in calculated  $x_{\text{H}_2\text{O}}^{\text{v}}$  vs. analytical uncertainty in reported  $x_{\text{H}_2\text{O}}^{\text{v}}$  (one value at
- 256 calculated  $x_{\text{H}_2\text{O}}^{\text{v}}$  uncertainty = 0.35 is excluded in t). In all panels, the black solid line is perfect
- 257 agreement and the black dashed lines are  $\pm 20\%$ . Symbols and colours as in Figure 1 and Figure 5.



258

259 **Figure 7:** Evaluating the accuracy and precision of  $x_{\text{CO}_2}^v$  calculated with  $\text{H}_2\text{O}-\text{CO}_2$  solubility models  
 260 using VESical (labelled along the right-hand side): **(a–d)** Dixon, **(e–h)** IaconoMarziano, **(i–l)**  
 261 ShishkinaIdealMixing, **(m–p)** Liu, and **(q–t)** MagmaSat. **(a, e, i, m, q)** Calculated  $x_{\text{CO}_2}^v$  vs. reported  
 262  $x_{\text{CO}_2}^v$ . **(b, f, j, n, r)** Normalised error in  $x_{\text{CO}_2}^v$  (i.e.,  $[\text{calculated } x_{\text{CO}_2}^v - \text{reported } x_{\text{CO}_2}^v] / \text{reported } x_{\text{CO}_2}^v$ ) vs.  
 263 reported  $x_{\text{CO}_2}^v$ . **(c, g, k, o, s)** Histogram of normalised error in  $x_{\text{CO}_2}^v$  by proportion of data. **(d, h, l, p, t)**  
 264 Calculated uncertainty in calculated  $x_{\text{CO}_2}^v$  vs. analytical uncertainty in reported  $x_{\text{CO}_2}^v$ . In all panels, the

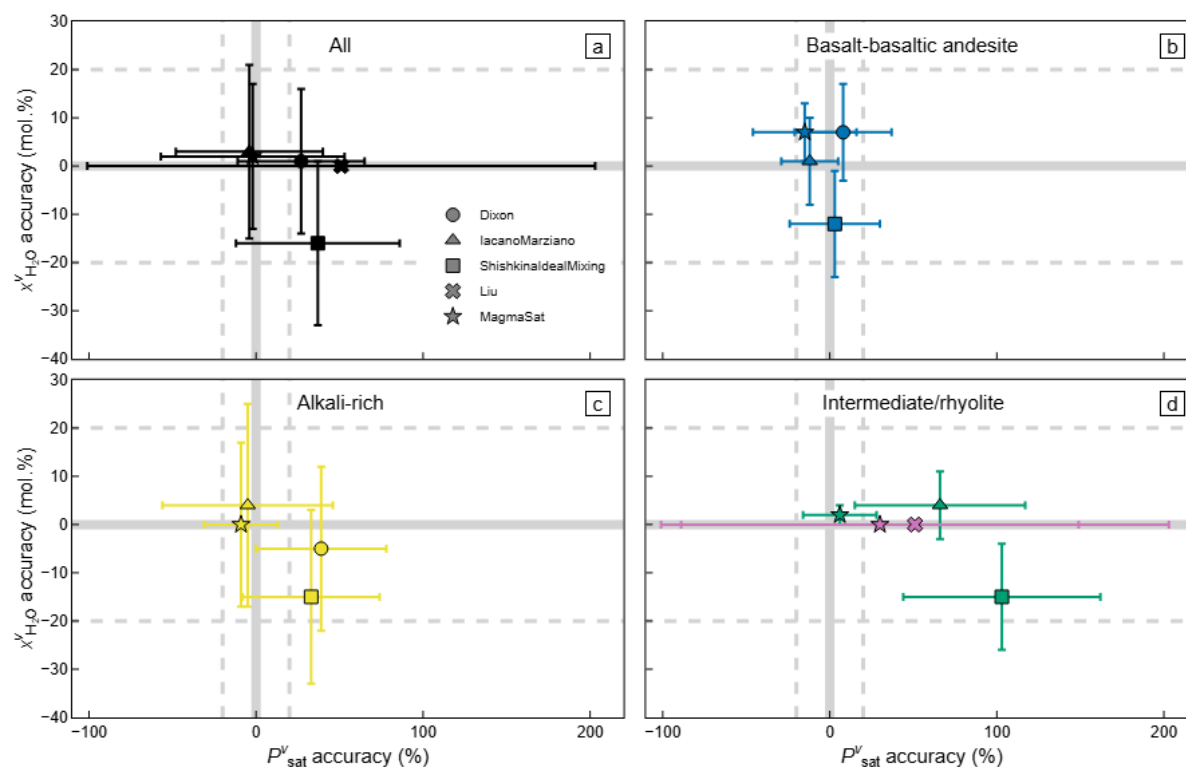
265 *black solid line is perfect agreement and the black dashed lines are ±20%. Symbols and colours as in*  
 266 *Figure 1 and Figure 5.*

267 **Table 2:** *Number of experiments and calculated accuracy and precision of  $P_{\text{sat}}^v$  and  $x_{\text{H}_2\text{O}}^v$  across all*  
 268 *compositions within each models calibration range.*

Model	Dixon		IaconoMarziano		ShishkinIdealMixing		Liu		MagmaSat	
$P_{\text{sat}}^v$										
<i>n</i>	175	<i>0</i>	270	<i>237</i>	306	<i>188</i>	40	<i>62</i>	365	<i>405</i>
accuracy (%)	27		-4	<i>1</i>	37	<i>3</i>	51	<i>12</i>	-2	<i>5</i>
precision (%)	38		44	<i>25</i>	49	<i>21</i>	152	<i>12</i>	55	<i>27</i>
$x_{\text{H}_2\text{O}}^v$										
<i>n</i>	136	<i>0</i>	215	<i>164</i>	239	<i>133</i>	0	<i>39</i>	174	<i>313</i>
accuracy (mol.%)	<1		3	<i>4</i>	-16	<i>-5</i>		<i>&lt;1</i>	2	<i>3</i>
precision (mol.%)	15		18	<i>14</i>	17	<i>12</i>		<i>3</i>	18	<i>13</i>

269 *Notes:* Data on experiments not used for calibration are normal type, whereas data for experiments  
 270 used for calibration are in *italics*.

271 To evaluate the overall accuracy for each H<sub>2</sub>O-CO<sub>2</sub> solubility for  $P_{\text{sat}}^v$ , the mean of the  
 272 normalised error is compared for experimental data not included for calibration (Table 2 and Figure  
 273 8a – the same analyses are reported for experimental data used for calibration for interest, but not  
 274 discussed). Dixon, ShishkinIdealMixing and Liu all overestimate  $P_{\text{sat}}^v$  on average by +27–51%;  
 275 whereas IaconoMarziano and MagmaSat slightly underestimate  $P_{\text{sat}}^v$  by 4 and 2%, respectively  
 276 (Figure 5c, f, j, n, r, Table 2, and Figure 8a). To evaluate overall precision for each H<sub>2</sub>O-CO<sub>2</sub> solubility  
 277 model, the standard deviation of the normalised error for each model is compared for data not  
 278 included during model calibration (Table 2 and Figure 8a). The precision of  $P_{\text{sat}}^v$  for all models is poor,  
 279 ranging between ±38–55% except Liu which is ±152% (Figure 5c, f, j, n, r, Table 2, and Figure 8a).  
 280 Uncertainties in  $P_{\text{sat}}^v$  incorporating experimental and analytical uncertainties for all models (<1400  
 281 bars) are typically much larger than the uncertainty in  $P_{\text{exp}}$  (typically 20–100 bar: Figure 5 g, k, o, s).



282

283 **Figure 8:** Comparison of model accuracy and precision for different melt compositions (labelled for  
 284 each panel):  $x_{\text{H}_2\text{O}}^{\text{v}}$  accuracy vs.  $P_{\text{sat}}^{\text{v}}$  accuracy, where the error bar indicates precision (based on  
 285 experiments not used during model calibration): (a) all melt compositions within the calibration  
 286 range; (b) basalt-basaltic andesites; (c) alkali-rich compositions; and (d) intermediate (green) and  
 287 rhyolites (pink). Symbol shape indicates model and symbol colour indicates melt composition. The  
 288 accuracy and precision of  $x_{\text{H}_2\text{O}}^{\text{v}}$  could not be calculated for Liu and MagmaSat for rhyolites due to a  
 289 lack of experimental data with reported  $x_{\text{H}_2\text{O}}^{\text{v}}$  that was not used to calibrate these models – hence  
 290 they are arbitrarily plotted at  $x_{\text{H}_2\text{O}}^{\text{v}}$  accuracy = 0 mol.%. The grey solid lines indicate perfect accuracy  
 291 and the grey dotted lines  $\pm 20\%$  accuracy.

292 As  $x_{\text{H}_2\text{O}}^{\text{v}}$  or  $x_{\text{CO}_2}^{\text{v}}$  can equal 0, the absolute mean and standard deviation (mol.%) rather than  
 293 normalised error are compared to evaluate accuracy and precision: values are calculated for  $x_{\text{H}_2\text{O}}^{\text{v}}$   
 294 and assumed to be of similar magnitude (but opposite sign for accuracy) for  $x_{\text{CO}_2}^{\text{v}}$  (Table 2 and Figure  
 295 8a, although normalised errors are shown in Figure 6 and Figure 7c, f, j, n, and r). For Liu, there is no  
 296 experimental data with reported  $x_{\text{H}_2\text{O}}^{\text{v}}$  not used for calibration and therefore independent accuracy  
 297 and precision cannot be evaluated. Dixon, IaconoMarziano, and MagmaSat have high accuracy (-1 to  
 298 +3 mol.%), whereas ShishkinaIdealMixing underestimates by 16% (Figure 6, Figure 7, Table 2, and

299 Figure 8a). All models have a similar precision of 15–18 mol.%  $x_{\text{H}_2\text{O}}^v$ . In contrast to  $P_{\text{sat}}^v$  uncertainties  
300 in calculated  $x_{\text{H}_2\text{O}}^v$  and  $x_{\text{CO}_2}^v$  are typically smaller than measurement uncertainties (<15 vs. <100  
301 mol.%; Figure 6 and Figure 7g, k, o, s).

## 302 Discussion

303 Overall, IaconoMarziano and MagmaSat are accurate for  $P_{\text{sat}}^v$  within their calibration range (-4  
304 and -2%, respectively), whilst the other models are quite inaccurate (+30–50%) and the precision for  
305 all models is quite poor for  $P_{\text{sat}}^v$  (38–151%) (Table 2 and Figure 8a). Because H<sub>2</sub>O and CO<sub>2</sub> solubility  
306 models are equations that calculate the concentration of H<sub>2</sub>O and CO<sub>2</sub> under a set of conditions, the  
307 uncertainties in these models are typically quoted in reference to how well the models reproduce  
308 the measured H<sub>2</sub>O and CO<sub>2</sub> concentrations of experiments, which are normally ±10–20% precision:  
309 Dixon: 8–15 % for H<sub>2</sub>O and ~15% for CO<sub>2</sub> and (Dixon, 1997; Duan, 2014); IaconoMarziano: average  
310 error for H<sub>2</sub>O is 8–17% and CO<sub>2</sub> is 12–13% (Duan, 2014; Iacono-Marziano et al., 2012);  
311 ShishkinIdealMixing: 78% are within ±10% for H<sub>2</sub>O and 70% are within 20% for CO<sub>2</sub> (Shishkina et al.,  
312 2014); Liu: 6–8% for H<sub>2</sub>O and 10–26% for CO<sub>2</sub> (Duan, 2014; Liu et al., 2005); and MagmaSat: ~25% for  
313 H<sub>2</sub>O and ~10% for CO<sub>2</sub> (Ghiorso & Gualda, 2015). The poorer precision in  $P_{\text{sat}}^v$  compared to replicating  
314 the dissolved H<sub>2</sub>O and CO<sub>2</sub> concentrations highlights that uncertainties in both H<sub>2</sub>O and CO<sub>2</sub> solubility  
315 contribute to uncertainty in  $P_{\text{sat}}^v$ . The accuracy in vapor composition is good for most models (1–3  
316 mol.%), except ShishkinIdealMixing (16 mol.%), but precision is quite poor (15–18 mol.%).  
317 Unfortunately, this highlights that previous models are not particularly accurate (Dixon,  
318 ShishkinIdealMixing, Liu) and/or precise (all models) in predicting  $P_{\text{sat}}^v$  or the vapor composition  
319 even within their stated calibration ranges (Figure 8a).

## 320 Accuracy and precision for different melt compositions

321 The accuracy and precision of different H<sub>2</sub>O-CO<sub>2</sub> solubility models may differ for different  
322 compositions within their calibration ranges, which are reported for basalt-basaltic andesites, alkali-  
323 rich, intermediates, and rhyolites in Table 3 and Figure 8b–d. Basalt-basaltic andesite melts are very

324 common across a wide variety of tectonic settings and are relatively well represented in the  
 325 experimental dataset (Figure 4). For basalt-basaltic andesites (Table 3 and Figure 9b), the accuracy  
 326 and precision in  $P_{\text{sat}}^v$  improves significantly compared to the full calibration range for Dixon and  
 327 ShishkinaldealMixing (8/29 and 3/27% for accuracy/precision, respectively), whereas for  
 328 IaconoMarziano and MagmaSat the accuracy reduces slightly (-12 to -15%), but the precision  
 329 improves (31 to 17%). There are slight improvements in the accuracy of  $x_{\text{H}_2\text{O}}^v$  for IaconoMarziano,  
 330 ShishkinaldealMixing, and MagmaSat, but the accuracy for Dixon gets worse (7 mol.%). Precision in  
 331  $x_{\text{H}_2\text{O}}^v$  improves for Dixon, IaconoMarziano, and ShishkinaldealMixing (10–11 mol.%) and remains  
 332 similar for MagmaSat. Overall, for all models, accuracy and precision in  $P_{\text{sat}}^v$  and  $x_{\text{H}_2\text{O}}^v$  (except  $P_{\text{sat}}^v$   
 333 accuracy for IaconoMarziano and MagmaSat) are better for basalt-basaltic andesites compared to  
 334 their full calibration ranges (Figure 8a and b).

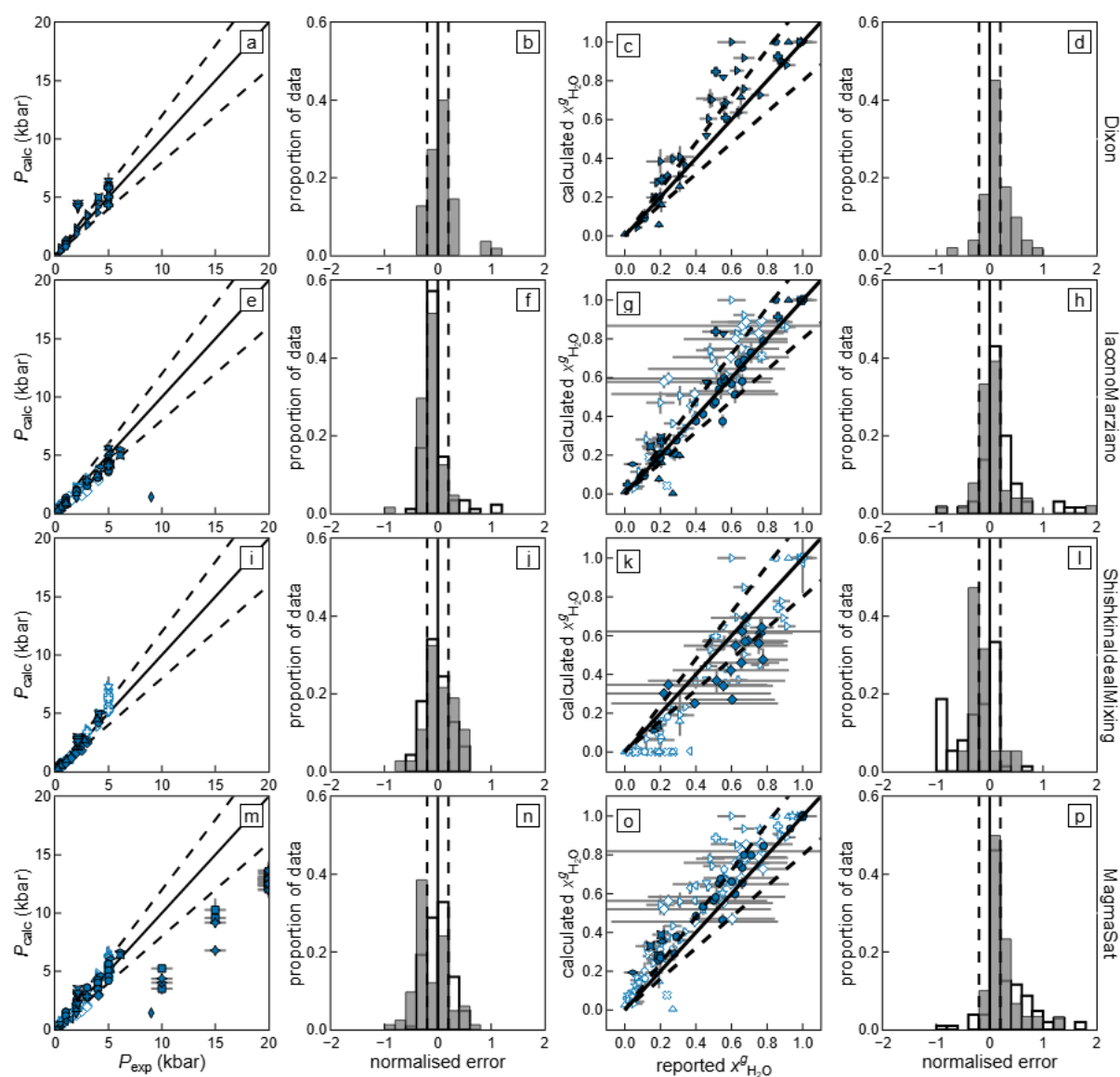
335 **Table 3:** Number of experiments and calculated accuracy and precision of  $P_{\text{sat}}^v$  and  $x_{\text{H}_2\text{O}}^v$  for  
 336 difference melt compositions.

Model	Dixon	IaconoMarziano	ShishkinaldealMixing	Liu	MagmaSat					
Basalt-basaltic andesite										
$P_{\text{sat}}^v$ n	55	0	64	89	37	94	0	0	83	125
$P_{\text{sat}}^v$ accuracy (%)	8		-12	-4	3	-1			-15	1
$P_{\text{sat}}^v$ precision (%)	29		17	25	27	23			31	21
$x_{\text{H}_2\text{O}}^v$ n	52	0	53	65	19	76	0	0	31	107
$x_{\text{H}_2\text{O}}^v$ accuracy (mol.%)	7		1	7	-12	-6			7	9
$x_{\text{H}_2\text{O}}^v$ precision (mol.%)	10		9	11	11	12			6	11
Alkali-rich										
$P_{\text{sat}}^v$ n	98	0	155	57	204	35	0	0	149	134
$P_{\text{sat}}^v$ accuracy (%)	39		-5	-6	33	5			-9	4
$P_{\text{sat}}^v$ precision (%)	39		51	15	41	17			22	18
$x_{\text{H}_2\text{O}}^v$ n	67	0	134	20	161	14	0	0	131	68
$x_{\text{H}_2\text{O}}^v$ accuracy (mol.%)	-5		4	-2	-15	-9			<1	1
$x_{\text{H}_2\text{O}}^v$ precision (mol.%)	17		21	7	18	11			17	13
Intermediate										
$P_{\text{sat}}^v$ n	0	0	13	22	37	0	0	0	28	46
$P_{\text{sat}}^v$ accuracy (%)			66	34	103				-6	3

$P_{\text{sat}}^v$ precision (%)			51	25	59				22	26
$x_{\text{H}_2\text{O}}^v n$	0	0	13	22	37	0	0	0	8	46
$x_{\text{H}_2\text{O}}^v$ accuracy (mol%)			4	10	-15				2	-4
$x_{\text{H}_2\text{O}}^v$ precision (mol%)			7	15	11				2	14
Rhyolite										
$P_{\text{sat}}^v n$	0	0	0	0	0	0	40	62	60	47
$P_{\text{sat}}^v$ accuracy (%)							51	12	30	1
$P_{\text{sat}}^v$ precision (%)							152	12	119	12
$x_{\text{H}_2\text{O}}^v n$	0	0	0	0	0	0	0	39	0	39
$x_{\text{H}_2\text{O}}^v$ accuracy (mol%)								<1		<1
$x_{\text{H}_2\text{O}}^v$ precision (mol%)								3		4

337 Notes: Data for experiments not used for calibration are normal type, whereas data for experiments

338 used for calibration are in *italics*.

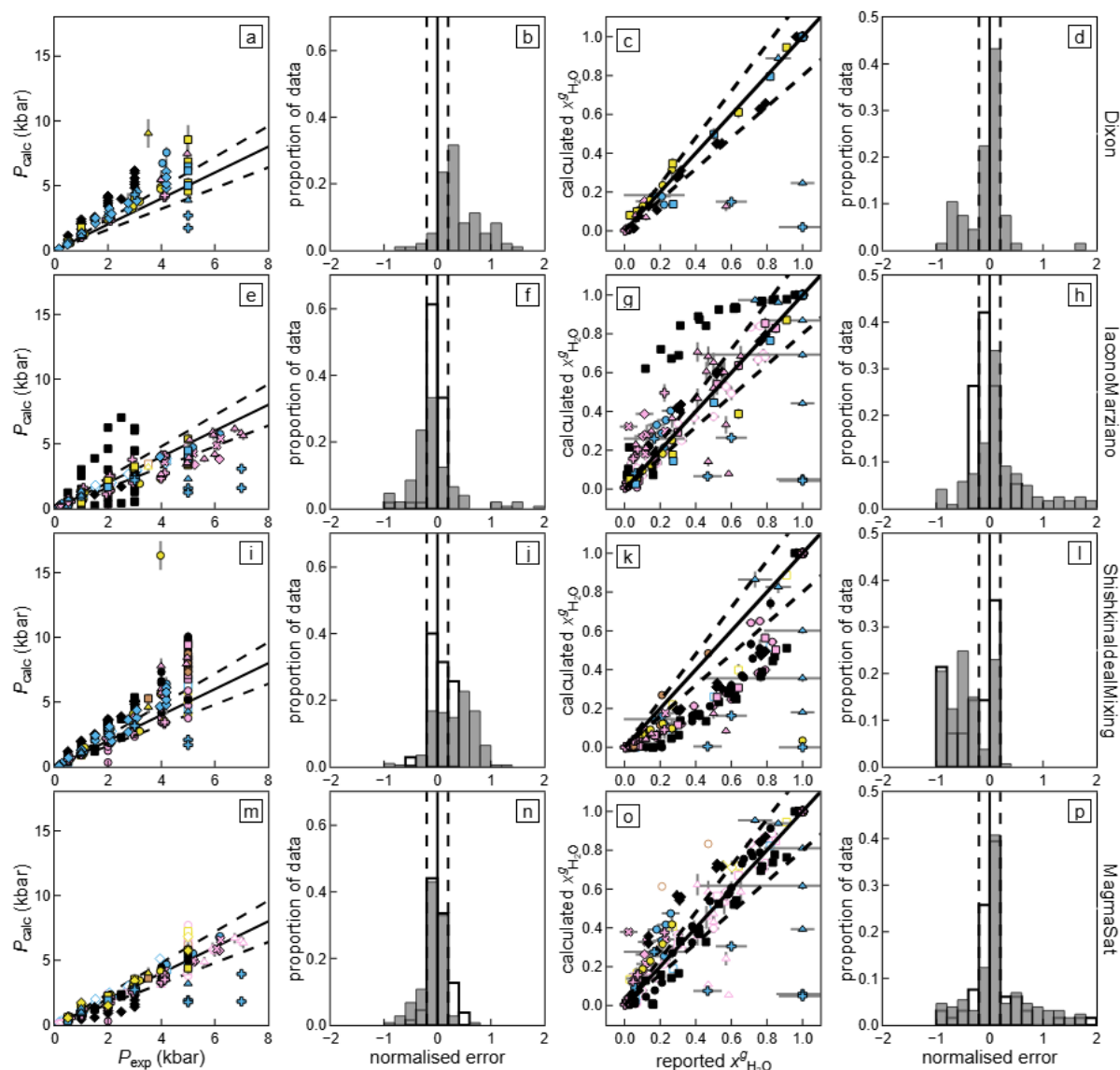


339

340 **Figure 9:** Evaluating the accuracy and precision of  $P_{sat}^v$  and  $x_{H_2O}^v$  calculated with  $H_2O$ - $CO_2$  solubility  
 341 models using VESIcal (labelled along the right-hand side) for basalt and basaltic andesite melts: **(a–d)**  
 342 Dixon, **(e–h)** IaconoMarziano, **(i–l)** ShishkinaIdealMixing, and **(m–p)** MagmaSat. **(a, e, i, m)**  
 343 Calculated  $P$  ( $P_{calc}$ , i.e.,  $P_{sat}^v$ ) vs. experimental  $P$  ( $P_{exp}$ ). **(b, f, j, n)** Histogram of normalised error in  $P_{calc}$   
 344 by proportion of data. **(c, g, k, o)** Calculated  $x_{H_2O}^v$  vs. reported  $x_{H_2O}^v$ . **(d, h, l, p)** Histogram of  
 345 normalised error in  $x_{H_2O}^v$  by proportion of data. In all panels, the black solid line is perfect agreement  
 346 and the black dashed lines are  $\pm 20\%$ . Symbols and colours as in Figure 1 and Figure 5.

347 Alkali-rich melts have been targeted experimentally due to being present at a quite a few well-  
 348 studied volcanoes and their large effect on  $CO_2$ -solubility. For alkali-rich melts (Table 3 and Figure 10),  
 349 the precision is similar but the accuracy worse for both  $P_{sat}^v$  and  $x_{H_2O}^v$  for Dixon (accuracy drops to  
 350 39% and -5 mol.%, respectively). IaconoMarziano has similar accuracy but slightly worse precision

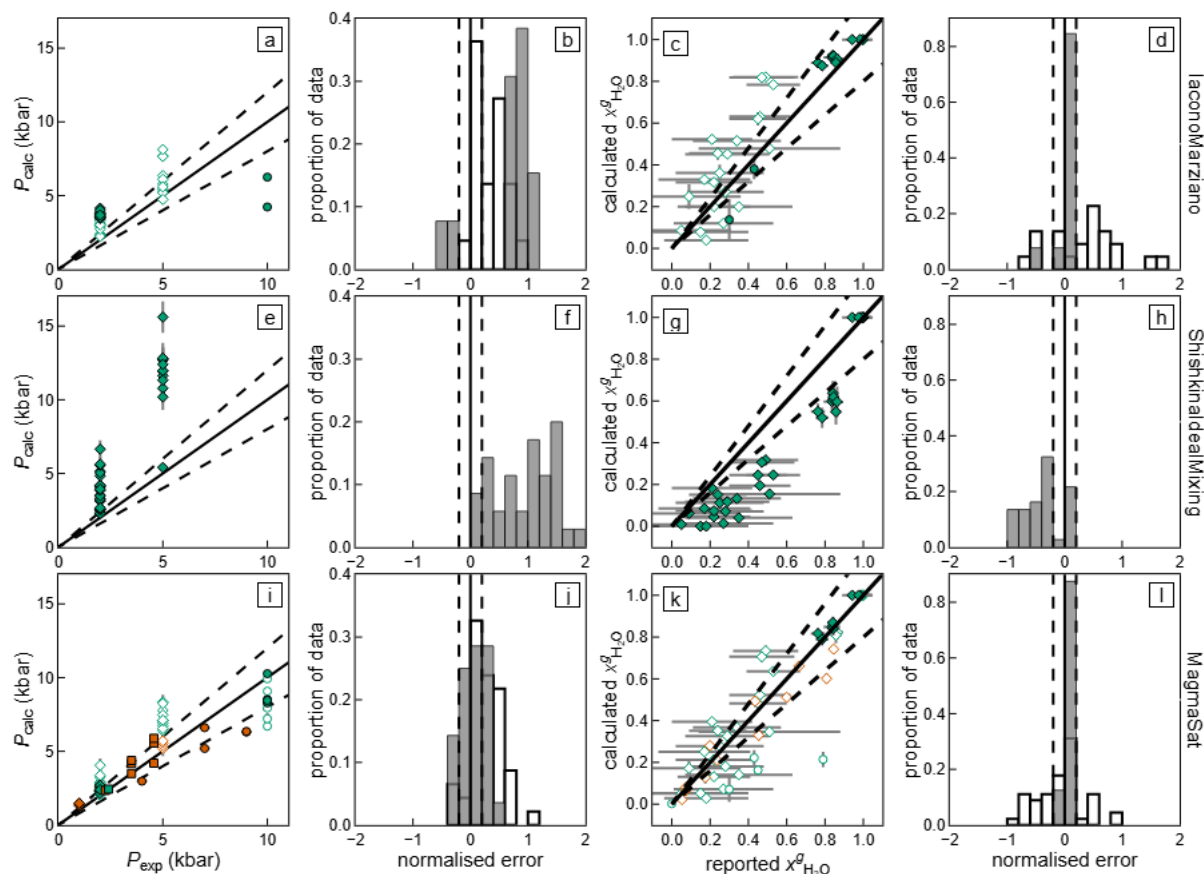
351 for both  $P_{\text{sat}}^v$  and  $x_{\text{H}_2\text{O}}^v$ . For ShishkinaldealMixing, the precision and accuracy of  $P_{\text{sat}}^v$  are slightly  
 352 better for alkali-rich melts, and similar for  $x_{\text{H}_2\text{O}}^v$ . Precision and accuracy of  $x_{\text{H}_2\text{O}}^v$  are the same for  
 353 MagmaSat, similar for  $P_{\text{sat}}^v$  accuracy, but there is a marked improvement for  $P_{\text{sat}}^v$  precision (down to  
 354 22%). Overall, alkali-rich melts are well reproduced by IaconoMarziano and ShishkinaldealMixing,  
 355 and particularly well by MagmaSat (Figure 8a and c).



356  
 357 **Figure 10:** Evaluating the accuracy and precision of  $P_{\text{sat}}^v$  and  $x_{\text{H}_2\text{O}}^v$  calculated with  $\text{H}_2\text{O}-\text{CO}_2$  solubility  
 358 models using VESlcal (labelled along the right-hand side) for alkali-rich melts: **(a–d)** Dixon, **(e–h)**  
 359 IaconoMarziano, **(i–l)** ShishkinaldealMixing, and **(m–p)** MagmaSat. **(a, e, i, m)** Calculated  $P$  ( $P_{\text{calc}}$ , i.e.,  
 360  $P_{\text{sat}}^v$ ) vs. experimental  $P$  ( $P_{\text{exp}}$ ). **(b, f, j, n)** Histogram of normalised error in  $P_{\text{calc}}$  by proportion of data.  
 361 **(c, g, k, o)** Calculated  $x_{\text{H}_2\text{O}}^v$  vs. reported  $x_{\text{H}_2\text{O}}^v$ . **(d, h, l, p)** Histogram of normalised error in  $x_{\text{H}_2\text{O}}^v$  by

362 *proportion of data. In all panels, the black solid line is perfect agreement and the black dashed lines*  
363 *are  $\pm 20\%$ . Symbols and colours as in Figure 1 and Figure 5.*

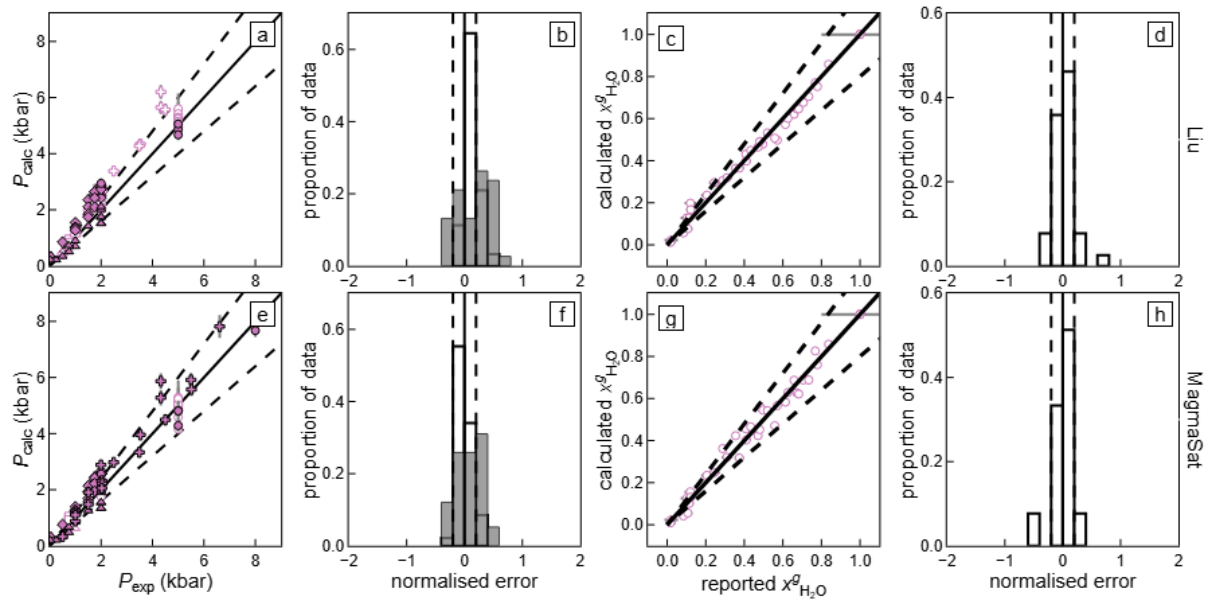
364 Wieser et al. (2022) explored the accuracy of H<sub>2</sub>O-CO<sub>2</sub> solubility models for intermediate  
365 (andesite and dacite) melts given their dominance in subduction zones and hazardous volcanoes.  
366 Wieser et al. compared isobars calculated using various models through VESical and Solwcad (Papale  
367 et al., 2006) with  $P_{\text{exp}}$  (their Figure 16) and concluded MagmaSat was the most accurate model,  
368 predicting volatiles contents within  $\pm 20\%$  of reported values. For intermediate melts (Table 3 and  
369 Figure 11), the accuracy and precision of  $P_{\text{sat}}^v$  is much worse for IaconoMarziano and  
370 ShishkinaIdealMixing (66–100% accuracy), but there are slight improvements in  $x_{\text{H}_2\text{O}}^v$  precision and  
371 accuracy compared to their full calibration range. The accuracy of  $P_{\text{sat}}^v$  and  $x_{\text{H}_2\text{O}}^v$  are slightly worse for  
372 MagmaSat compared to its full calibration, but the precision is better (22% for  $P_{\text{sat}}^v$ ). Overall, as  
373 suggested by Wieser et al. (2022), MagmaSat has the best accuracy and precision for intermediate melts  
374 (Figure 8d). However, the lack of experimental studies on intermediate melts severely limits the  
375 applicability of any H<sub>2</sub>O-CO<sub>2</sub> solubility model to such magmas due to a lack of calibration data (e.g.,  
376 Wieser et al., 2022). Interestingly, there are a large number of experimental studies investigating  
377 vapor-saturated calc-alkaline intermediate magmas in the literature that have unfortunately not  
378 measured H<sub>2</sub>O and/or CO<sub>2</sub> in the glass (e.g., Alonso-Perez et al., 2008; Blatter et al., 2023; Blatter &  
379 Carmichael, 1998; Krawczynski et al., 2012; Marxer et al., 2021; Nandedkar et al., 2014). These (and  
380 new) experiments could fill crucial gaps in H<sub>2</sub>O and/or CO<sub>2</sub> solubility model compositional space in the  
381 future.



382

383 **Figure 11:** Evaluating the accuracy and precision of  $P_{sat}^v$  and  $x_{H_2O}^v$  calculated with  $H_2O-CO_2$  solubility  
 384 models using VESlcal (labelled along the right-hand side) for intermediate (andesite and dacite)  
 385 melts: **(a–d)** laconoMarziano, **(e–h)** ShishkinaldealMixing, and **(i–l)** MagmaSat. **(a, e, i)** Calculated  $P$   
 386 ( $P_{calc}$ , i.e.,  $P_{sat}^v$ ) vs. experimental  $P$  ( $P_{exp}$ ). **(b, f, j)** Histogram of normalised error in  $P_{calc}$  by proportion of  
 387 data. **(c, g, k)** Calculated  $x_{H_2O}^v$  vs. reported  $x_{H_2O}^v$ . **(d, h, l)** Histogram of normalised error in  $x_{H_2O}^v$  by  
 388 proportion of data. In all panels, the black solid line is perfect agreement and the black dashed lines  
 389 are  $\pm 20\%$ . Symbols and colours as in Figure 1 and Figure 5.

390 For rhyolites (Table 3 and Figure 12), only the accuracy and precision of  $P_{sat}^v$  can be  
 391 evaluated as all experimental data with reported vapor composition was used for calibrating both Liu  
 392 and MagmaSat.  $P_{sat}^v$  accuracy and precision are much worse for MagmaSat compared to the whole  
 393 calibration range (31% and 119%, respectively), which likely reflects the low pressure of these  
 394 experiments and therefore large relative errors for small absolute differences.



395

396 **Figure 12:** Evaluating the accuracy and precision of  $P_{sat}^v$  and  $x_{H_2O}^v$  calculated with  $H_2O$ - $CO_2$  solubility  
 397 models using VESlcal (labelled along the right-hand side) for rhyolite melts: **(a-d)** Liu and **(e-h)**  
 398 MagmaSat. **(a, e)** Calculated  $P$  ( $P_{calc}$ , i.e.,  $P_{sat}^v$ ) vs. experimental  $P$  ( $P_{exp}$ ). **(b, f)** Histogram of  
 399 normalised error in  $P_{calc}$  by proportion of data. **(c, g)** Calculated  $x_{H_2O}^v$  vs. reported  $x_{H_2O}^v$ . **(d, h)**  
 400 Histogram of normalised error in  $x_{H_2O}^v$  by proportion of data. In all panels, the black solid line is  
 401 perfect agreement and the black dashed lines are  $\pm 20\%$ . Symbols and colours as in Figure 1 and  
 402 Figure 5.

403 This approach of calculating the accuracy and precision of  $P_{sat}^v$  and vapor composition can be  
 404 used to evaluate how well existing solubility models reproduce new experimental data in the future  
 405 and can be repeated on new  $H_2O$ - $CO_2$  solubility models as they are published to ensure the best  
 406 estimates of accuracy and precision are available. Given  $\sim 30\%$  of the experimental dataset was  
 407 published after these models were published, improved  $H_2O$ - $CO_2$  solubility models may be possible  
 408 using these 'new' data.

#### 409 Influence of analytical uncertainty

410 Using a Monte Carlo approach to incorporate experimental uncertainty in  $T_{exp}$  and analytical  
 411 uncertainty in glass composition (majors/minors,  $H_2O$ , and  $CO_2$ ) enables a comparison between the  
 412 uncertainties in experimental  $P$  and the precision in calculated  $P_{sat}^v$ , and the analytical uncertainties  
 413 in measured and precision in calculated vapor composition, for an individual glass measurement (i.e.,

414 what is the spread in calculated  $P_{\text{sat}}^v$  and vapor composition due to experimental and analytical  
415 uncertainties). This is a minimum estimate in the precision in calculated  $P_{\text{sat}}^v$  and vapor composition  
416 for an individual glass composition because model uncertainty is not included. Calculated  $P_{\text{sat}}^v$   
417 precision for an individual experimental glass composition is typically larger than experimental  
418 uncertainty in  $P_{\text{exp}}$  (Figure 5g, k, o, s). This suggests improved precision in  $P_{\text{sat}}^v$  for natural samples  
419 (e.g., melt inclusions and matrix glass) will require reduced uncertainties in measured H<sub>2</sub>O and CO<sub>2</sub>.  
420 However, similar uncertainties in measured H<sub>2</sub>O and CO<sub>2</sub> exist in the calibration datasets for the H<sub>2</sub>O-  
421 CO<sub>2</sub> solubility models themselves, which would be reflected in model error. Conversely, calculated  
422 precision in vapor composition from an individual glass composition is typically better than analytical  
423 uncertainty (Figure 6 and Figure 7g, k, o, s), highlighting the analytical challenges of measuring  
424 experimental vapor composition.

425 A similar Monte Carlo approach can be applied to natural sample data to account for analytical  
426 uncertainty in calculated  $P_{\text{sat}}^v$  and vapor composition (e.g., Hughes et al., 2025). Inclusion of  
427 analytical uncertainties will result in worse calculated precision for natural samples (i.e., melt  
428 inclusions and matrix glasses) than the experimental glasses explored here (assuming melt inclusion  
429 compositions at entrapment can be faithfully reconstructed: Rose-Koga et al., 2021). Firstly, for these  
430 experiments,  $T$  is known with a small uncertainty (e.g.,  $\pm 10$  °C), whereas for natural samples,  $T$  is not  
431 known independently and is typically calculated from the glass composition, which is associated with  
432 larger uncertainties (e.g.,  $>30$  °C depending on the thermometer; Wieser et al., 2025). This is likely to  
433 cause a small change in the calculated precision because H<sub>2</sub>O-CO<sub>2</sub> solubility is typically not strongly  $T$ -  
434 dependent (e.g., Wieser et al., 2022). Secondly, for melt inclusions, CO<sub>2</sub> is often hosted in a vapor  
435 bubble in addition to the glass (e.g., Hartley et al., 2014; Moore et al., 2015; Wallace, Kamenetsky, et  
436 al., 2015), which leads to larger analytical uncertainties in CO<sub>2</sub> compared to experiments (see Wieser  
437 et al. (2025) for a discussion on this topic). Thirdly, uncertainties in the melt composition will be  
438 larger for melt inclusions where corrections for post-entrapment crystallisation and melting have

439 been applied (although the difference in calculated  $P_{\text{sat}}^v$  is small when these corrections are included:  
440 van Gerve et al., 2025).

#### 441 Using experimental data to select the most appropriate model

442 Ultimately, users of H<sub>2</sub>O-CO<sub>2</sub> solubility models wish to use the model that will produce the most  
443 accurate and precise results for their application of interest – whether that is calculating the  
444 composition of vapor bubbles in melt inclusions to reconstruct the true dissolved volatile content at  
445 entrapment;  $P_{\text{sat}}^v$  from melt inclusion or matrix glass data to estimate magma storage or eruption  
446 depth; or the melt and vapor compositions and proportions during degassing to compare to natural  
447 data or as an input to conduit flow models. Comparison to the calibration dataset for a model is  
448 typically the first step in choosing the most appropriate model (e.g., Iacovino et al., 2021). However,  
449 the accuracy and precision of the H<sub>2</sub>O-CO<sub>2</sub> solubility models explored here must also be taken into  
450 consideration when making inferences about natural systems and comparison to other datasets (e.g.,  
451 geophysical estimates of magma storage depth). One option is to use the spread of results from  
452 different H<sub>2</sub>O-CO<sub>2</sub> solubility models as an indication of uncertainty (e.g., Wieser et al., 2025).  
453 However, as each model has different accuracy and precision for different melt compositions within  
454 their calibration range, the most appropriate model to use depends on the system of interest.

455 The most appropriate model to select can be evaluated by calculating accuracy (mean of the  
456 difference between calculated and known values) and precision (standard deviation of the difference  
457 between calculated and known values) of calculated  $P_{\text{sat}}^v$  and vapor composition using experiments  
458 that are close in composition to the system of interest (e.g., Wieser et al., 2025; Wieser, Kent, & Till,  
459 2023). For instance, if one were interested in modelling a basaltic andesite with similar composition  
460 to Pavlof (Alaska, USA), you could calculate the accuracy and precision of  $P_{\text{sat}}^v$  using the experimental  
461 data of Mangan et al. (2021) (no measured vapor compositions are reported). This would require  
462 using the melt composition (including H<sub>2</sub>O and CO<sub>2</sub>), experimental conditions ( $P$  and  $T$ ), and their  
463 uncertainties to calculate  $P_{\text{sat}}^v$  (and vapor composition) using different H<sub>2</sub>O-CO<sub>2</sub> solubility models  
464 through a tool like VESIcal (or using the results from the calculations in this paper) and from this

465 calculating accuracy and precision. In this example, IaconoMarziano has -19% accuracy and 10%  
466 precision; ShishkinaIdealMixing 18% and 23%; and MagmaSat 2% and 16% for  $P_{\text{sat}}^v$ . This provides  
467 both an evidence-based choice and an assessment of uncertainty for the modelling results.

## 468 Conclusions

469 The accuracy and precision of five commonly-used H<sub>2</sub>O-CO<sub>2</sub> solubility models (VolatileCalc-  
470 Basalt/Dixon, 1997/Newman & Lowenstern, 2002; MagamSat/Ghiorso & Gualda, 2015; Iacono-  
471 Marziano et al., 2012; Liu et al., 2005; Shishkina et al., 2014) were evaluated by calculating the vapor  
472 saturation pressure and composition using the Python packages VESlcal (Iacovino et al., 2021) and  
473 ThermoEngineLite (Wolf et al., 2026) on a literature dataset of 770 vapor-saturated silicate melt  
474 experiments with measured glass (and vapor) H<sub>2</sub>O and CO<sub>2</sub> compositions. The calculated pressure of  
475 vapor saturation was compared to the experimental pressure, and the calculated vapor composition  
476 to reported vapor composition where available, for experimental data not used for calibration of  
477 each model. For the pressure of vapor saturation, models vary from being accurate across their  
478 stated calibration ranges (IaconoMarziano and MagmaSat) to quite inaccurate (Dixon, Shishkina, and  
479 Liu), and all are quite imprecise. Most models are accurate for the vapor composition (except  
480 ShishkinaIdealMixing) but all are relatively imprecise. The accuracy and precision can be better for  
481 different melt compositions within each models stated calibration range. For a system of interest, the  
482 most appropriate model can be chosen by evaluating the accuracy and precision for calculated vapor  
483 saturation pressure and composition when applied to experiments covering similar melt and  $P$ - $T$   
484 conditions, which is especially important when applying to natural data.

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## 491 Competing interests

492 The author declares no competing interests.

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