

1 **“Empirical pre-whitening” spectral analysis detects periodic but inconsistent signals in abyssal hill**  
2 **morphology at the southern East Pacific Rise**

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11 Key Points:

- 12 1. A new algorithm is formulated to detect periodicities embedded in an aperiodic process using  
13 “empirical pre-whitening” spectral analysis
- 14 2. Periodicities are detected at the southern East Pacific Rise, but are spatially and temporally  
15 inconsistent
- 16 3. The dominant aperiodic signal is likely fault-constructed, while ephemeral periodic signals may  
17 relate to internal melt supply variations

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**Abstract.** The existence, or not, of periodicities in abyssal hill morphology has been vigorously debated in recent publications, and some have hypothesized that such periodicities are evidence of the impact of Milankovitch cycle-caused sea level fluctuations on the volcanic construction process at mid-ocean ridges. Periodicities are detected by the presence of spectral peaks that rise significantly above the random variations of sample power spectra associated with an aperiodic, continuous spectrum process, typically modeled as a band-limited fractal (von Kármán model). Here I formulate and test a new algorithm to “empirically pre-whiten” the sample power spectrum which, without needing to model the continuous spectrum, flattens it to a zero-mean process. This greatly simplifies definition of the null hypothesis, and additional modeling approximates standard deviation levels that provide a conservative basis for detecting peaks that may be indicative of periodicity. The algorithm is applied to extensive bathymetric data flanking the southern East Pacific Rise. Significant periodicities are detected on many profiles analyzed, but the periods vary widely, and do not cluster at Milankovitch periods. The most substantial harmonic signals detected exhibit periods  $\sim 0.082\text{-}0.216$  my, with root-mean square (RMS) heights approximately a quarter to a third of the RMS height for the aperiodic signal. It is hypothesized that the dominant aperiodic component of abyssal hills corresponds to morphology constructed by faults that follow a random distribution governed by scaling laws, whereas longer-scale periodic signals are associated with crustal thickness variations controlled internally by variations in melt supply.

Key Words: Mid-ocean ridge, faulting, melt supply, von Kármán model, stochastic processes, autocovariance

## 43 1. Introduction

44 A number of recent publications have endeavored to identify peaks in the sample power spectra  
45 (periodograms) of abyssal hill bathymetry profiles, presumably indicative of periodicities that could be  
46 interpreted as systemic temporal variations in mid-ocean ridge (MOR) processes (Crowley et al., 2015;  
47 Tolstoy, 2015; Olive et al., 2016; Shinevar et al., 2019). Discovery of topographic periodicities would  
48 greatly impact our understanding of variability in MOR processes, whether externally forced, such as  
49 proposed Milankovitch Cycle dependence (Crowley et al., 2015; Tolstoy, 2015), or internally forced, such  
50 as via modulations of mantle upwelling (Shinevar et al., 2019; Parnell-Turner et al., 2020). There are,  
51 however, a number of potential pitfalls in these analyses, and it is quite possible that the spectral peaks  
52 that have been discerned are instead typical random fluctuations of a sample power spectrum  
53 estimated from an aperiodic time series, particularly if detection thresholds are not sufficiently  
54 conservative.

55 As described in Priestley (1981), there are two end-member time series spectra: discrete and  
56 continuous. Discrete spectra are those with one or more periodicities, detected by peaks on the sample  
57 power spectrum at individual frequencies. Well-known methods are established for determining the  
58 significance of those peaks as observed on a sample power spectrum in the presence of a background  
59 white noise process. In contrast, continuous spectra processes are those that are characterized by a  
60 smooth, continuous power spectral function  $P(f)$  across a range of frequencies,  $f$ , and do not contain any  
61 periodicities. However, sample power spectra derived from continuous-spectra time series are, in  
62 Priestley's (1981) words, "erratic and wildly fluctuating", which is a result of two well-known properties:  
63 (1) the variance of the sample power spectrum does not approach zero as the number of sample points  
64 ( $N$ ) approaches infinity, and (2) the correlation between two sample power spectrum points decreases  
65 as  $N$  increases. Because of this erratic property, application of discrete-spectrum tests to continuous-  
66 spectra processes "may indicate the existence of a large number of spurious periodic components",

67 according to Priestley (1981); the methods are not invalid, he states, but rather are misapplied when  
68 used on time series with continuous spectra. Furthermore, since the variance of the sample power  
69 spectrum scales with  $P^2(f)$ , such false detections are more likely where  $P(f)$  is larger.

70 Between the discrete and continuous spectrum end members, Priestley (1981) describes a “mixed”  
71 spectrum derived from the blending of time series of both periodic and aperiodic character, which is an  
72 apt model for hypothesizing the existence of periodicities in abyssal hill morphology (Goff et al., 2018).  
73 Abyssal hills are formed primarily by normal faults (McDonald et al., 1996; Durant et al., 1996;  
74 Macdonald, 2015), whose throw and spacing can be modeled as random distributions that follow scaling  
75 laws (Malinverno and Cowie, 1993; Bohnenstiehl and Carbotte, 2001). Abyssal hill morphology  
76 statistical properties have been successfully characterized using a von Kármán functional form (von  
77 Kármán, 1948), a continuous (aperiodic) spectrum that can also be described as a band-limited fractal  
78 model (Goff and Jordan, 1988, Goff and Tucholke, 1997). Any periodic component of the seafloor  
79 topography, such as might be caused by variations in crustal thickness, independent of the abyssal hill  
80 faulting process, could be modeled as a superposition of periodic and aperiodic signals.

81 If we consider the aperiodic time series with continuous power spectrum,  $P(f)$ , to be a null  
82 hypothesis, rejection of the null hypothesis would be established by observation of a spectral peak that  
83 greatly exceeds the normal variation of the continuous sample power spectrum. However, to do this,  
84 the null hypothesis must be defined, which requires either knowing  $P(f)$  *a priori*, or modeling  $P(f)$  by  
85 fitting a functional form (e.g., Goff and Jordan, 1988). Vaughan (2005), for example, formulated a  
86 methodology for detecting periodicities in the presence of a red (negative trend with frequency)  
87 background noise, which can be fit with simple power-law, and where the null hypothesis variability  
88 about this trend is characterized by a  $\chi^2$  distribution. Vaughan (2005) noted, however, that the  
89 modeling fit itself adds additional uncertainty, leading him to strongly suggest that confidence levels 3-4  
90 times the standard deviation ( $\sigma$ ) should be applied when determining the significance of a spectral peak

91 in indicating a periodic component of a mixed spectrum, rather than the oft-assumed  $2\sigma$  confidence  
92 level.

93 Pre-whitening is another approach to assisting in the detection of periodicities in a mixed spectrum;  
94 the general idea is to divide the sample power spectrum by  $P(f)$  so that the overall trend is flat; i.e., it  
95 emulates a discrete spectrum in the presence of white noise. In this construction, standard tests for the  
96 significance of observed peaks can be applied (Priestley, 1981). The spectral analysis methodology  
97 employed by Crowley et al. (2015) and emulated by others (Olive et al., 2016; Shinevar et al., 2019),  
98 does indeed attempt to apply pre-whitening to the spectrum. However, no attempt was made in these  
99 analyses to estimate  $P(f)$ , applying instead simple  $f^2$  multiplicative factor that fails to flatten the  
100 spectrum. Rather, because abyssal hills are band-limited in their power-law (i.e., fractal) behavior, this  
101 attempt at pre-whitening causes the spectrum to arc, artificially enhancing positive spectral fluctuations  
102 near the apex of the arc to appear more significant than they likely are. Although modeling the  
103 spectrum using the von Kármán function would undoubtedly improve pre-whitening, Priestley (1981)  
104 argues against pre-whitening in this way because, if there is indeed a periodic component, it will distort  
105 the modeling of  $P(f)$  in a way that adversely affects both that estimation and the ultimate detection of  
106 periodic signals.

107 Harmonic components of a mixed spectrum profile can also be detected using multitaper techniques  
108 (Thomson, 1990; Percival and Walden, 1993; Mann and Lees, 1996; Crowley et al., 2015). Multitaper  
109 spectral estimation applies an orthogonal series of tapers to a time series, Fourier transforms each and  
110 then adds the results together to form a sample power spectrum. This technique is widely used to  
111 reduce the variability of the power spectrum estimate in comparison to the periodogram, and eliminate  
112 spectral leakage (e.g., McCoy et al., 1998; Babadi and Brown, 2014). An embedded harmonic signal may  
113 be detected by an F-test for phase-coherent variability at any one frequency across taper components  
114 (Thomson, 1990; Mann and Lees, 1996). However, phase coherence does not necessarily imply

115 significance with respect to the variability associated with the aperiodic component of the process at  
116 that frequency (Mann and Lees, 1996). Alternatively, or in addition to the F-test, the height of a spectral  
117 peak can be compared against an assumed  $\chi^2$  distribution on local variability about the null hypothesis,  
118 which is represented by the best estimate of  $P(f)$  for the multitaper estimate of the power spectrum  
119 (Percival and Walden, 1993; Mann and Lees, 1996; Crowley et al., 2015). This test is akin to the  
120 procedure Vaughan (2005) utilized for the periodogram.

121 To obviate the need to model  $P(f)$  for defining the null hypothesis and/or for pre-whitening,  
122 Priestley (1981; Chapter 8) proposed an ingenious and simple solution that he termed the “ $P(\lambda)$ ” test.  
123 The method utilizes the sample autocovariance function, which is the Fourier transform pair of the  
124 sample power spectrum. The sample autocovariance consists of two components: (1) a central,  
125 decaying portion that includes all information about the functional nature of the continuous, aperiodic  
126 spectrum  $P(f)$ , and (2) a long tail that randomly fluctuates about 0 and, should they be present, also  
127 includes harmonic fluctuations associated with periodic components of the time series because they do  
128 not decay to zero with increasing lag. Priestley’s (1981) method consists of zeroing-out the central,  
129 decaying portion of the sample autocovariance (which can be determined by simple inspection rather  
130 than modeling), and then Fourier-transforming the remaining tails; the result will be a zero-mean (null  
131 hypothesis), randomly fluctuating function, with positive spikes at frequencies if and where periodic  
132 signals are present (deviation from null hypothesis). Despite the relative simplicity and elegance of the  
133  $P(\lambda)$  test, a literature search found very few examples of its application (e.g., Bhansali, 1977; Garrido and  
134 Garcia, 1992). For clarity in terminology, I propose the term “empirical pre-whitening” to describe this  
135 simple technique.

136 In this paper I present a new algorithm for utilizing Priestley’s (1981) “ $P(\lambda)$ ”/empirical pre-whitening  
137 method to detect periodic signals in a mixed-spectra process. I first test the algorithm on synthetic  
138 profiles generated by adding cosine functions of various amplitude and frequency to an aperiodic time

139 series corresponding to the von Kármán statistical model (Goff and Jordan, 1988). The algorithm is able  
 140 to accurately detect the periodic components provided the amplitude is sufficient to rise significantly  
 141 above the random fluctuations associated with the aperiodic component of the spectrum at that  
 142 frequency. I then apply this algorithm to twelve bathymetric profiles of abyssal hill morphology along  
 143 the southern East Pacific Rise (EPR) to test for the presence of periodicities. A portion of this region was  
 144 also used by Tolstoy (2015) in a spectral analysis that discerned a ~100 ky periodicity, which is one of the  
 145 Milankovitch periods. The profiles are converted from distance to crustal age versus depth using an  
 146 existing, high-resolution age model for the region (Goff et al., 2018).

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## 148 2. Formulation

149 The following formulation is based on Priestley (1981; Section 8.4). Consider a discrete time or space  
 150 series  $X_i$ ,  $1 \leq i \leq N$ , evenly space by  $\Delta X$ . Consider further that  $X_i$  represents the summation of two  
 151 independent, zero-mean, stationary processes  $Y_i$  and  $Z_i$ , where  $Y_i$  is an aperiodic process with a  
 152 continuous spectrum, and  $Z_i$  is represented by one or more sinusoidal forms. The autocovariance of  $X_i$ ,  
 153  $R_X(s)$ , is then represented by:

$$154 \quad E[X_i X_{i+s}] = R_X(s) = R_Y(s) + R_Z(s), \quad (1)$$

155 where  $E[\ ]$  is the expectation operator,  $s$  is the lag index, and  $R_Y(s)$  and  $R_Z(s)$  are the autocovariances of  $Y_i$   
 156 and  $Z_i$ , respectively. Because  $Y_i$  is aperiodic,  $R_Y(s)$  will decay monotonically with increasing  $|s|$ . Because  
 157  $Z_i$  has periodic elements,  $R_Z(s)$  will also vary sinusoidally for all  $s$ ; each sinusoidal element, defined by a  
 158 frequency  $f$  amplitude and amplitude  $\alpha$ , will contribute a term  $\frac{1}{2} \alpha^2 \cos(2\pi s f)$  to  $R_Z(s)$ . The sample  
 159 autocovariance, i.e., estimation of  $R_X(s)$  based on samples  $X_i$ , is given by:

$$160 \quad \hat{R}_X(s) = \frac{1}{N-s} \sum_{i=1}^{N-s} X_i X_{i+s}, \quad 0 \leq s \leq N/2$$

$$161 \quad \hat{R}_X(-s) = \hat{R}_X(s). \quad (2)$$

162 The power spectrum of  $X_i$ , denoted by  $P_X(f)$ , is the Fourier transform conjugate of  $R_X(s)$ , and we can  
 163 likewise define the power spectra of  $Y_i$  and  $Z_i$  in the same way such that

$$164 \quad P_X(f) = P_Y(f) + P_Z(f). \quad (3)$$

165 The sample power spectrum can be computed in two equivalent ways:

$$166 \quad \hat{P}_X(f) = DFT[\hat{R}_X(s)], \text{ or} \quad (4)$$

$$167 \quad \hat{P}_X(f) = |DFT[X_i]|^2, \quad (5)$$

168 where DFT indicates the discrete Fourier transformation. Equation (5) is far more commonly utilized since  
 169 it does not require the extra step of computing the sample autocovariance as in Equation (2). However,  
 170 Equation (4) is utilized here because it provides a mechanism for separating periodic from aperiodic  
 171 components of the spectrum. Priestley (1981) proposes in his “ $P(\lambda)$ ” test to first inspect  $\hat{R}_X(s)$  after  
 172 computing it in order to identify a value  $m$  such

$$173 \quad R_Y(s) \sim 0, |s| \geq m. \quad (6)$$

174 In other words, we seek to identify that portion of the sample autocovariance which is monotonically  
 175 decaying, and which contains all the structural information that constrains the continuous portion of the  
 176 power spectrum  $P_Y(f)$ . The remainder, or “tail,” is a zero-mean signal that, if there are no periodic  
 177 elements in  $X_i$ , will fluctuate randomly (and which, after DFT, contributes to the erratic fluctuations of  
 178  $\hat{P}_X(f)$ ). If, however, there are periodic elements, then those will be present in the tail, as noted above.

179 The next step in Priestley’s (1981) method is thus to remove the monotonically decaying portion of  
 180  $\hat{R}_X(s)$  by zeroing it out for  $|s| < m$ :

$$181 \quad \hat{R}_X^m(s) = \begin{cases} 0, & |s| < m \\ \hat{R}_X(s), & |s| \geq m \end{cases}. \quad (7)$$

182 Finally, this altered sample autocovariance is transformed to create the “empirically pre-whitened”  
 183 spectrum

$$184 \quad \hat{P}_X^m(f) = DFT[\hat{R}_X^m(s)]. \quad (8)$$



185 In practice, the “cut” edges at  $|\pm s| = m$ , as well as the ends of the function at  $|\pm s| = N/2$ , need to be  
186 tapered prior to the DFT in order to minimize spectral leakage.

187 In the case of the null hypothesis, where no periodicity is present and  $P_X(f) = P_Y(f)$ , Priestly (1981)  
188 demonstrates that

$$189 \quad E[\hat{P}_X^m(f)] = 0, \quad (9)$$

190 and

$$191 \quad VAR[\hat{P}_X^m(f)] \sim \frac{N-2m}{2} P_Y^2(f), \quad (10)$$

192 where VAR indicates the variance. Therefore, the standard deviation on the null hypothesis,  $\sigma$ , is  
193 estimated by the square root of Equation (10). Deviation from the null hypothesis can be established by  
194 observation of spectral peaks that significantly deviate from the typical erratic variability associated with  
195 the continuous component of the spectrum. For this purpose, a conservative criterion must be applied.  
196 Depending on  $N$ , the empirically pre-whitened spectrum could have hundreds or thousands of peaks  
197 and valleys, so that numerous peaks are expected to surpass a  $2\sigma$  (95%) threshold, and even several are  
198 likely to surpass a  $3\sigma$  (99%) threshold without the presence of a periodic signal. In the following  
199 analyses, a value of  $3.5\sigma$  will be used as a minimum detection threshold.

200 Equation (10) does require knowledge of the underlying continuous spectrum  $P_Y(f)$ . Where  $P_Y(f)$  is  
201 not known *a priori*, it must be modeled by fitting a smooth functional form to the sample  
202 autocovariance or sample power spectrum. This will be demonstrated in Section 4. Addition of periodic  
203 components will increase the overall variance of the profile compared to the null hypothesis, thus  
204 increasing the modeled value of  $P_Y(f)$  and subsequent estimation of  $\sigma$ . Fortunately, this has the effect of  
205 increasing the confidence in detection of periodic contributions, since the level of significance of a  
206 spectral peak should be considered a minimum value.

207

208 **3. Synthetic Test**

209 To test the ability of an empirically pre-whitened spectrum to detect periodic elements of a mixed  
 210 spectrum process, I constructed a series of synthetic profiles consisting of the addition of an aperiodic  
 211 time series, generated from the von Kármán statistical model, and cosine functions of varying amplitude  
 212 and frequency. The von Kármán statistical model can be expressed equivalently in either  
 213 autocovariance or power spectral form (Goff and Jordan, 1988; Goff and Tucholke, 1997). For the  
 214 autocovariance:

$$215 \quad R_{VK}(s) = H^2 G_\nu[k_0 s] / G_\nu(0) \quad (11)$$

216 where  $H$  is the RMS height,  $k_0$  is a scaling parameter with dimensions  $\text{time}^{-1}$  (or  $\text{distance}^{-1}$ ), and  $G_\nu$  is  
 217 defined by

$$218 \quad G_\nu(x) = x^\nu K_\nu(x). \quad 0 \leq x < \infty. \quad (12)$$

219  $K_\nu$  is the modified Bessel function of the second kind and order  $\nu$ . At  $\nu = 1/2$ ,  $R_{VK}(s)$  is an exponential  
 220 function. The functional form of the von Kármán power spectrum for a profile is given by:

$$221 \quad P_{VK}(f) = \frac{\Gamma\left(\nu + \frac{1}{2}\right)}{\Gamma(\nu)} \frac{2H^2 \sqrt{\pi} (k_0/2\pi)^{2\nu}}{((k_0/2\pi)^2 + f^2)^{\nu + \frac{1}{2}}}$$

222 (13)  
 224

225 where  $\Gamma$  is the gamma function. In the power spectral formulation,  $k_0/2\pi$  serves as a corner frequency:  
 226 for  $f \gg k_0/2\pi$ ,  $P_{VK}(f)$  is a power-law form (i.e., red spectrum, or fractal), while for  $f \ll k_0/2\pi$ ,  $P_{VK}(f)$  is a  
 227 constant (i.e., white spectrum). The order parameter  $\nu$  determines the Hausdorff, or fractal dimension:

$$228 \quad D = E + 1 - \nu, \quad (14)$$

229 where  $E$  is the Euclidian dimension (i.e.,  $E = 1$  for a profile).

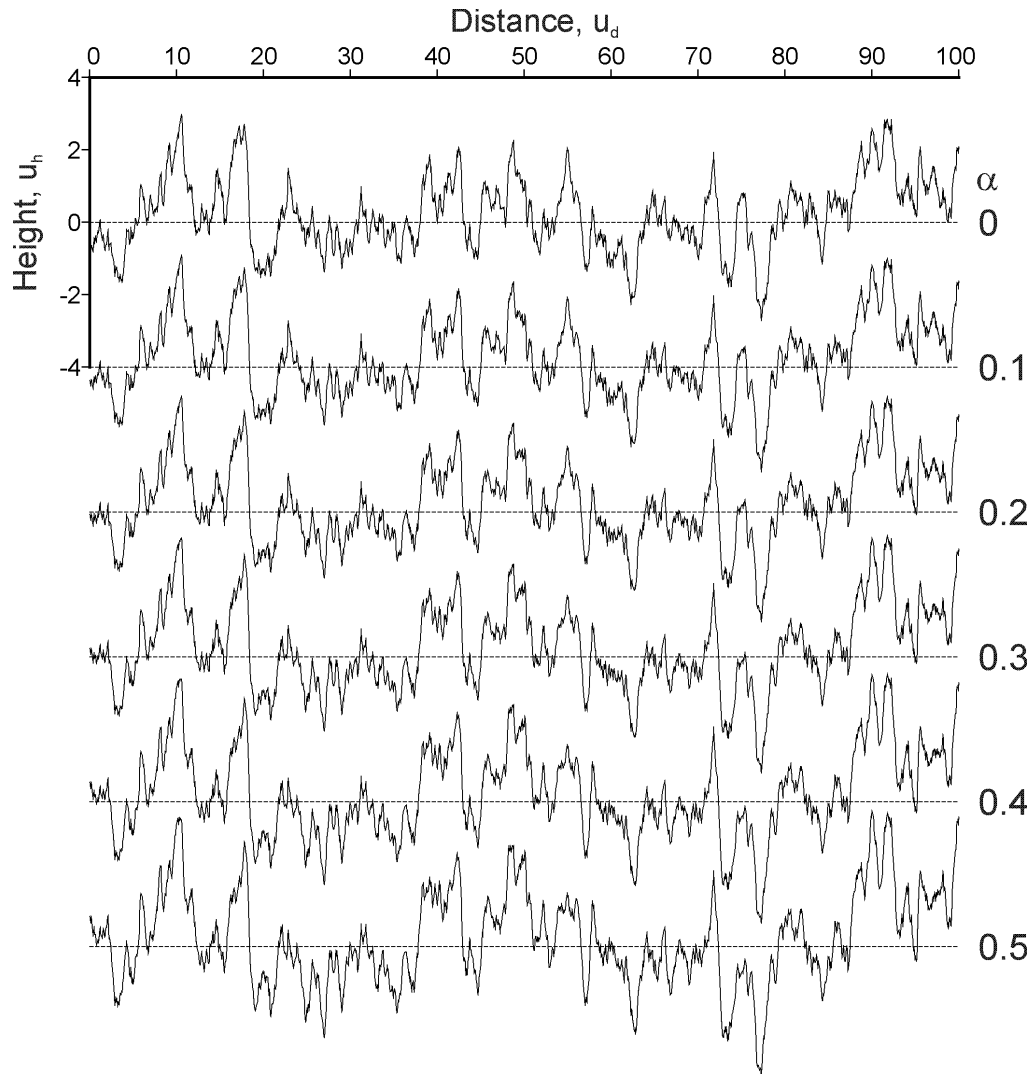
230 A synthetic profile conforming to the von Kármán statistical model can be generated by: (1)  
 231 multiplying the amplitude spectrum (square root of Equation (13)) by a random phase  $\exp(i\phi)$ , where  $\phi$   
 232 is a uniform random value distributed on  $(0, 2\pi]$ , (2) enforcing Hermetian symmetry over negative

233 frequencies, and (3) transforming to the space domain by DFT (Goff and Jordan, 1988; Goff, 1995). The  
234 uniform random phase results in a Gaussian distribution of profile values. In practice, a larger profile  
235 than required should be generated, and then cropped to size in order to fully randomize the sample  
236 power spectrum of the synthetic profile.

237 For the synthetic experiment, parameters chosen were:  $H = 1 u_h$ ,  $k_0 = 1 u_d^{-1}$ , and  $\nu = 0.8$ , where  $u_h$   
238 and  $u_d$  are arbitrary units of height and distance (or time), respectively. The profile length is 10,000  
239 points with a node spacing of  $\Delta X = 0.05 u_d$ . The top profile of Figure 1 displays the profile generated  
240 with these parameters. To generate a mixed-spectrum profile,  $X_M(i\Delta X)$ , I superpose cosine functions on  
241 the von Kármán profile using:

$$242 \quad X_M(i\Delta X) = X_{VK}(i\Delta X) + \alpha[\cos(i\Delta X 2\pi f_1) + \cos(i\Delta X 2\pi f_2) + \cos(i\Delta X 2\pi f_3)] , \quad (15)$$

243 where  $X_{VK}(i\Delta X)$  is the profile generated with the von Kármán statistical model, and  $f_1, f_2$  and  $f_3$  are  
244 frequencies chosen to be 0.02, 0.1, and 0.5 cycles/ $u_d$ , respectively. Figure 1 displays the results of  
245 Equation (15) for values of  $\alpha$  ranging from 0 to 0.5. A surprising observation regarding these profiles is  
246 that they look very similar; i.e., that the harmonic components are not visually self-evident, even at the  
247 largest value of  $\alpha$ . This observation can be understood by considering the contribution of each  
248 sinusoidal component to the overall RMS height. For example, at  $\alpha = 0.3 u_h$ , the variance is of the  
249 sinusoidal component is  $\frac{1}{2}\alpha^2$ , or  $0.045 u_h^2$ . Added to the aperiodic variance of  $1 u_h^2$ , the combined  
250 variance is  $1.045 u_h^2$ , and taking the square root yields an overall RMS of  $1.022 u_h$ . Thus, the addition of  
251 one sinusoidal component of amplitude  $0.3 u_h$  increases the RMS by only 2.2%.



252

253 Figure 1. Synthetic profiles constructed using Equation (15) and parameters listed in the text. The  
 254 vertical scale corresponds to the  $\alpha = 0$  profile; all others are offset a constant distance for visualization.  
 255 The first 100  $u_d$  of each synthetic profile, out of a total distance of 500  $u_d$ , are plotted.

256

257 In contrast to the profiles, the sample autocovariances of these profiles (Figure 2) display clear visual

258 evidence of the harmonic components, which come to dominate the tails as  $\alpha$  increases because they do

259 not decorrelate as lag increases, as the aperiodic signal does. This is a clear visual confirmation of the

260 utility of the sample autocovariance to isolate the harmonic components of a mixed spectrum process

261 from the aperiodic components. Using these sample autocovariances, I have conducted a spectral

262 analysis where I compare (1) the sample power spectrum computed by DFT of the full sample

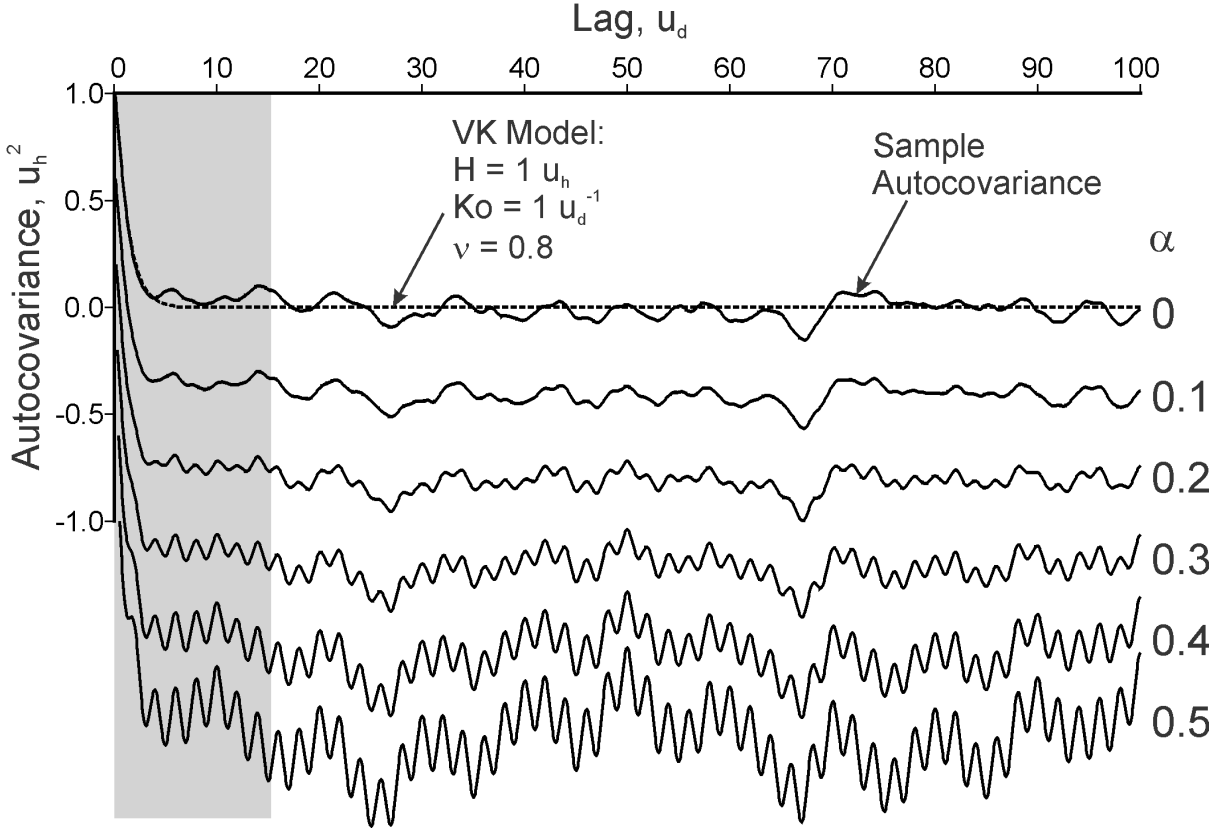
263 autocovariance, and (2) the empirically pre-whitened spectrum computed by DFT of the sample

264 autocovariance after zeroing-out the shaded regions shown in Figure 2, which self-evidently includes the  
265 full span of the monotonically-decaying portion of the function. In addition, a  $\cos^2$  taper is applied over  
266 10% of the profile at each edge to suppress spectral leakage. The full suite of results is presented in the  
267 Supplementary Material, and cases  $\alpha = 0 u_h$  and  $\alpha = 0.3 u_h$  are presented in Figures 3 and 4, respectively,  
268 to illustrate key findings.

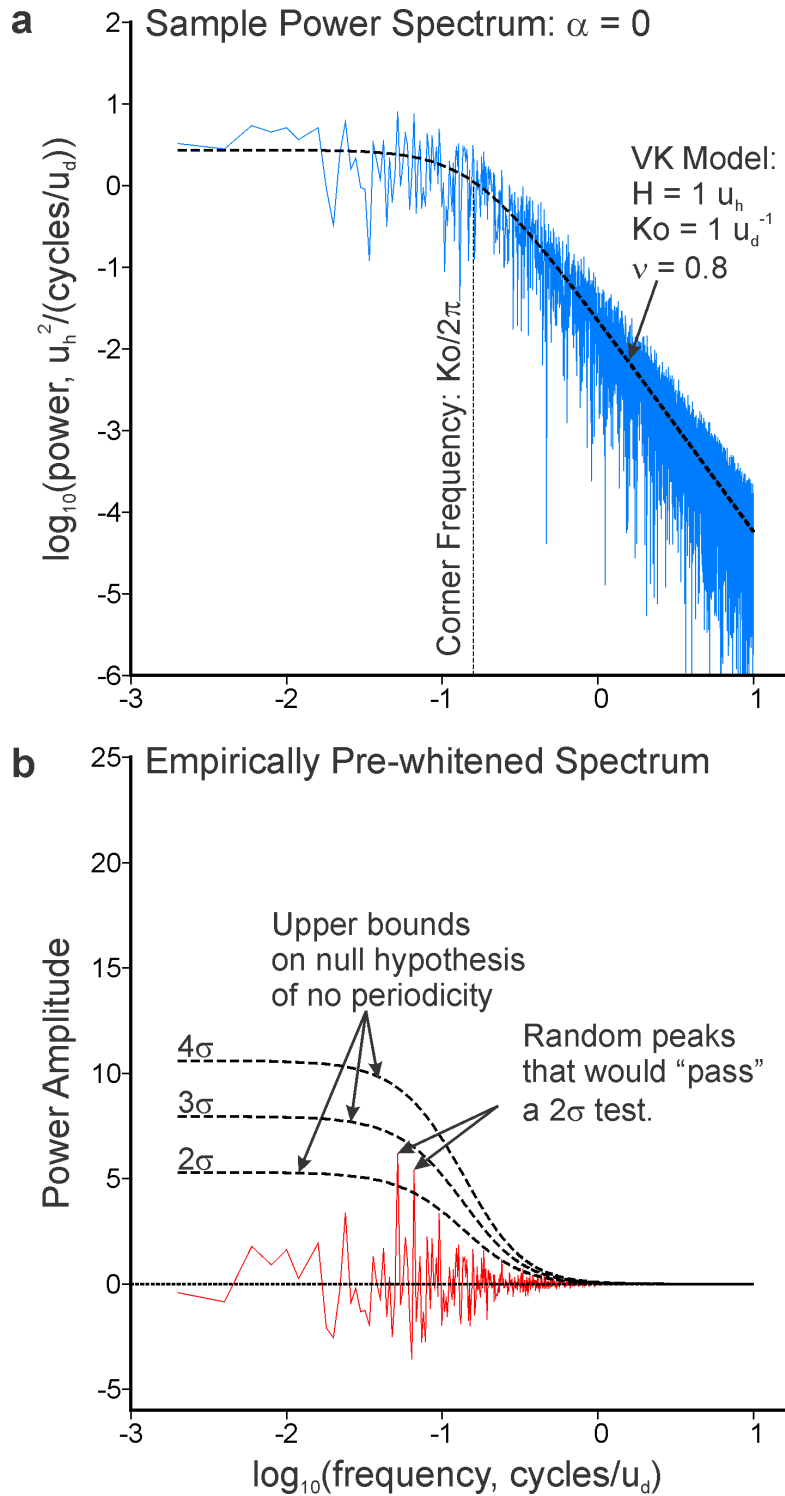
269 The null ( $\alpha = 0 u_h$ ) case is presented in Figure 3. As noted earlier, the von Kármán statistical model is  
270 a band-limited fractal, following a power-law form (negative linear trend on a log-log plot) at high  
271 frequencies, and flat at low frequencies, with the transition governed by the corner frequency. The  
272 sample power spectrum from the synthetic profile (Figure 3a) closely follows this functional form, as  
273 expected, but with the highly erratic variability that is characteristic of continuous-spectrum, aperiodic  
274 profile. The empirically pre-whitened spectrum for the null case (Figure 3b), is also highly erratic, but  
275 with a mean of zero which indicates success in removing the structural form of the continuous power  
276 spectrum. Comparison between Figures 3a and 3b demonstrates that the variations of the sample  
277 power spectrum about the model function are retained in the variation of the empirically pre-whitened  
278 spectrum about zero. The  $2\sigma$  upper bound does well in characterizing the envelope of variability, which  
279 increases as  $f$  decreases, but is not a hard limit; at least two peaks are observed to exceed  $2\sigma$ , which is  
280 expected statistically.

281 The  $\alpha = 0.3 u_h$  case is presented in Figure 4. Frequency  $f_3$  (0.5 cycles/ $u_d$ ) is detectable at  $\alpha = 0.1 u_h$   
282 (Supplementary Material) owing to the fact that the variations of the aperiodic component of the profile  
283 are very small at this frequency. Frequencies  $f_1$  (0.02 cycles/ $u_d$ ) and  $f_2$  (0.1 cycles/ $u_d$ ), however, are only  
284 detectable at  $>3.5\sigma$  for  $\alpha = 0.3 u_h$  (Figure 4b) and larger (Supplementary Material). Because they all  
285 have the same amplitude, the peaks at all three frequencies are expected to be of the same height on  
286 the empirically pre-whitened spectrum. However, the peak at  $f_2$  is observed to be less than the peaks at  
287  $f_1$  and  $f_3$  by about 25% (Figure 4b). This emphasizes an important point: the height of the discrete

288 spectral peaks are modulated by the random highs and lows of the continuous spectrum upon which it is  
 289 superposed, leading to uncertainty in detection and measurement of amplitude (which will be  
 290 considered in the next section).

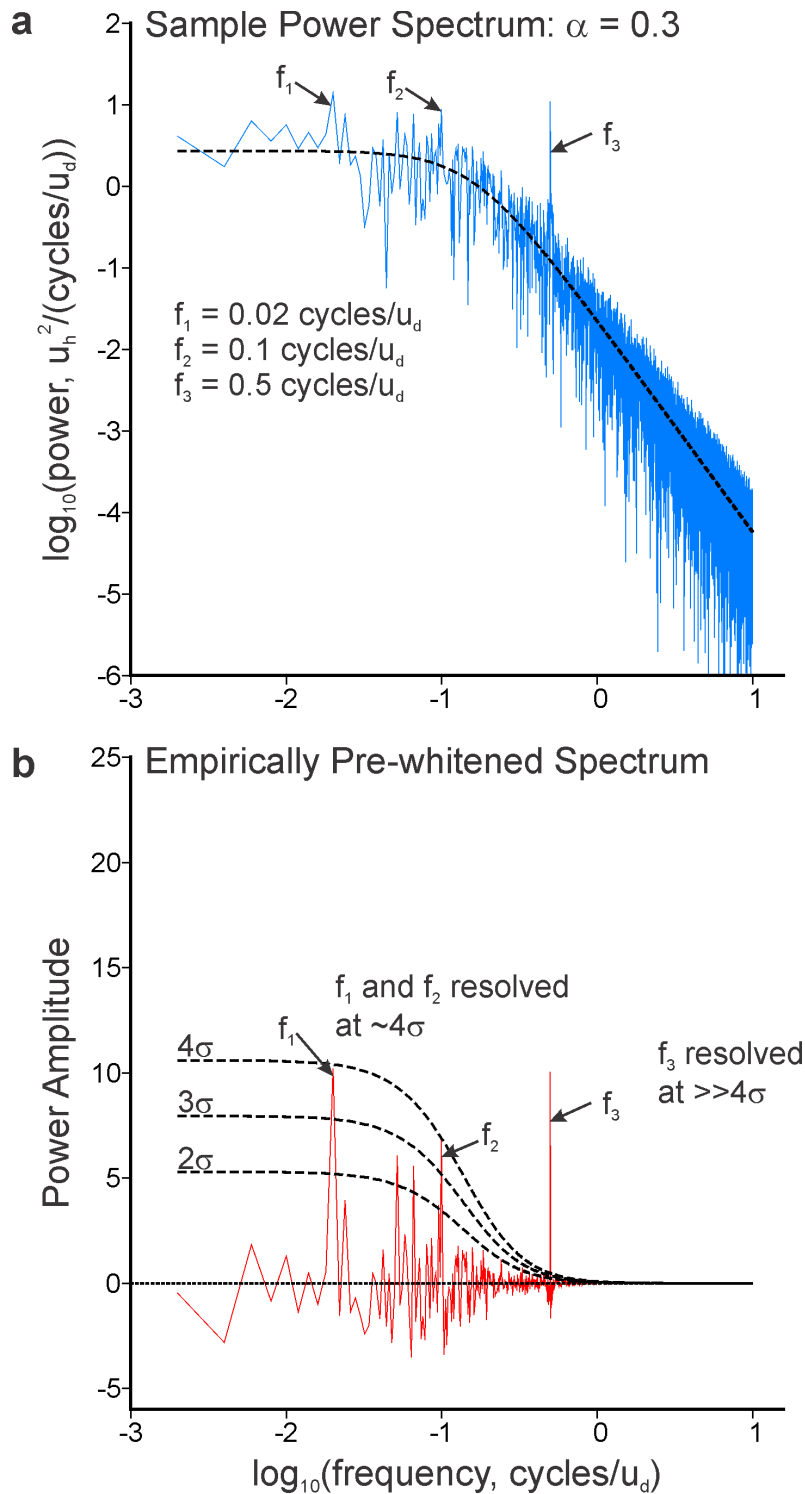


291  
 292 Figure 2. Sample autocovariance functions (solid) computed from profiles shown in Figure 1, plotted to a  
 293 lag of  $100 u_d$ . The von Kármán (VK) statistical model autocovariance, from which the synthetic profiles  
 294 were generated, is overlain (dashed). The vertical scale corresponds to the  $\alpha = 0$  function; all others are  
 295 offset a constant distance for visualization. For Figures 3 and 4, the discrete Fourier transformation of  
 296 the sample autocovariance (with Hermetian symmetry) is used to compute the sample spectral density,  
 297 while the empirically pre-whitened spectrum is computed in the same way after values in the shaded  
 298 region are zeroed out. The number of values zeroed out is determined by inspection, ensuring that the  
 299 full span of the decaying portion of the autocovariance is removed and leaving only a fluctuating, zero-  
 300 mean tail. A value of  $\alpha = 0$  is the null condition of no periodic component to the sample profile. Periodic  
 301 components come to dominate the tail of the autocovariance with increasing  $\alpha$ , compared to the far  
 302 more subtle visual impact evidenced in the synthetic profiles of Figure 1.



303

304 Figure 3. (a) Sample power spectrum and (b) empirically pre-whitened spectrum calculated from the  $\alpha =$   
 305 0 sample autocovariance shown in Figure 2. The von Kármán model is overlain on the power spectral  
 306 density, and the  $2\sigma$ ,  $3\sigma$ , and  $4\sigma$  upper bounds on the null hypothesis are overlain on the empirically pre-  
 307 whitened spectrum. Examples of "false positive" detection of periodic components are observed in the  
 308 if the  $2\sigma$  bound is used as a threshold.



309

310 Figure 4. (a) Sample power spectrum and (b) empirically pre-whitened spectrum calculated from the  $\alpha =$   
 311 0.3 sample autocovariance shown in Figure 2. The von Kármán model is overlain on the power spectral  
 312 density, and the  $2\sigma$ ,  $3\sigma$ , and  $4\sigma$  upper bounds on the null hypothesis are overlain on the empirically pre-  
 313 whitened spectrum. All three harmonic components are resolved at  $> 3.5\sigma$  in this example.  
 314

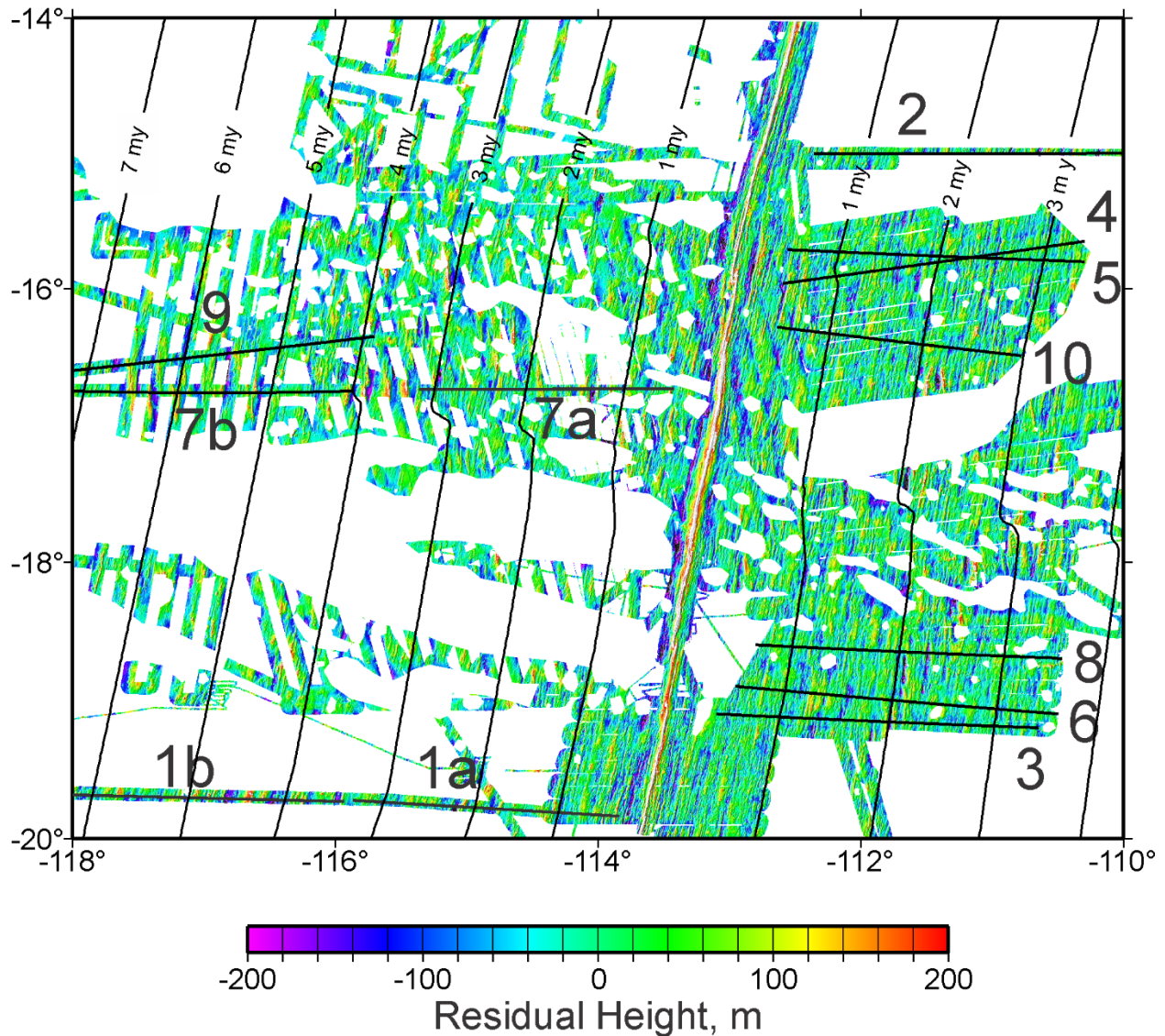


315 This synthetic experiment demonstrates the efficacy of the empirically pre-whitened spectrum in  
316 detecting periodic components of a mixed spectrum profile. Even with a conservative detection  
317 criterion of  $3.5\sigma$ , positive identification was made of harmonic signals that add only 2.2% each to the  
318 overall RMS variability. The certainty of detection increases as the amplitude of the sinusoidal  
319 component increases (Supplementary Material), providing confidence that any substantial harmonic  
320 component to the profile will be detected. The empirical pre-whitening algorithm has the potential for a  
321 wide variety of applications.

322

#### 323 **4. Application to the Southern East Pacific Rise**

324 The southern East Pacific Rise (Figure 5) is the site of some of the most extensive publically-available  
325 multibeam bathymetric coverage in the world of a mid-ocean ridge (MOR) and its flanks (Scheirer et al.  
326 1996). The region also exhibits some of the fastest MOR spreading rates ( $\sim 7.7$ - $7.8$  cm/yr half rates  
327 DeMets et al., 1990). Tolstoy (2015) applied a spectral analysis in a limited area of this region and found  
328 a spectral peak at a period of  $\sim 100$  ky, inferring that Milankovitch cycles may be influencing volcanic  
329 construction at the MOR. Goff et al (2018) further fine-tuned the Müller et al. (2016) age model for this  
330 region, and applied a stacking analysis to identify any temporal variations in bathymetry that were  
331 coherent across the region, which would be expected if the rise and fall of sea-level associated with  
332 Milankovitch cycles, and external forcing, were controlling abyssal hill construction. They found,  
333 however, that there was no evidence for spatially coherent temporal signals, periodic or otherwise.  
334 Nevertheless, lack of synchronicity does not imply lack of periodicity. Rather than an external forcing  
335 that affects the MOR uniformly either globally or regionally, variations in volcanic output might be  
336 internally forced within the mantle (Shinevar et al., 2019; Parnell-Turner et al., 2020), which could be  
337 periodic (or at least episodic) and which may vary in period, phase and amplitude from one segment to  
338 the next. If so, then the stacking analysis of Goff et al. (2018) would not detect such signals.



340

341 Figure 5. Multibeam bathymetry along the flanks of the southern East Pacific Rise, high-pass filtered  
 342 with a 40 km box filter and masked to removed seamounts (modified from Goff et al., 2018). Crustal  
 343 ages are contoured at 1 my increments (Muller et al., 2016; Goff et al., 2018). Profiles used for analysis  
 344 are indicated by thick black lines and numbered identifiers.

345

346 To search for possible temporal periodicities, I have selected 12 profiles of residual height (Figure 5)  
 347 and converted to age versus residual height using the crustal age model presented in Goff et al. (2018).  
 348 Each profile is ~2.5-3 my long, resampled at a uniform interval of 0.0025 my, and linearly interpolated  
 349 over any gaps in coverage. Such gaps were few as profiles were carefully selected to correspond to

350 swaths of nearly complete coverage and no seamounts. Profiles were also restricted to ages > 0.5 my to  
351 avoid the MOR axial high and associated negative sidelobes that form with the high-pass filter of the  
352 original bathymetry.

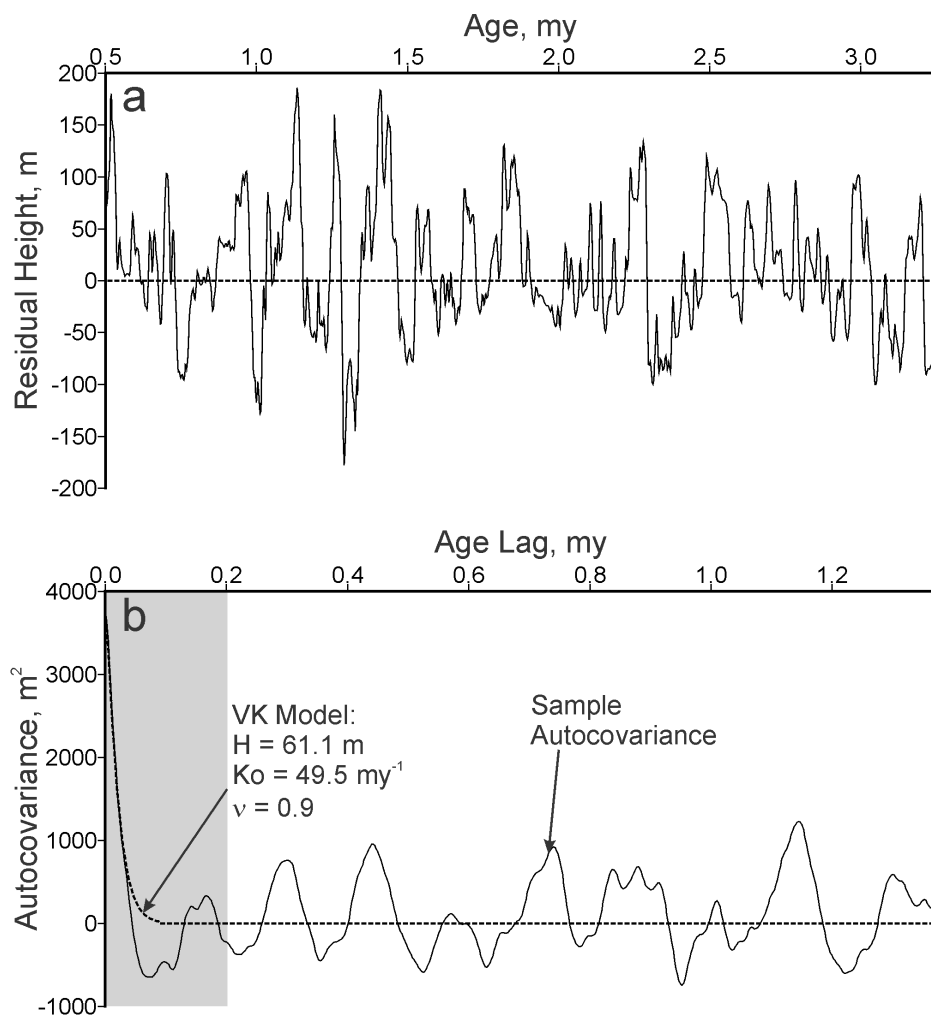
353 For example purposes, I present here the full analysis of Profile 7a (Figures 6 and 7), which is one of  
354 the more convincing detections of a periodic component. The full suite of profiles analyses are  
355 presented in the Supplementary Material, with results listed in Table 1. The age-versus-residual height  
356 values for Profile 7a are shown in Figure 6a, and its sample autocovariance function is shown in Figure  
357 6b. A von Kármán model is fit to the sample autocovariance (Figure 6b) via weighted, least-squares  
358 inversion as formulated in Goff and Jordan (1988). The estimated value for RMS height,  $H$ , is  $61.1 \pm 4.7$   
359 m, and the scale parameter,  $k_0$ , is  $68.3 \pm 13.8 \text{ my}^{-1}$ . Estimation of the parameter  $\nu$  tends to become  
360 unstable as it approaches its upper limit of 1 (Goff, 1991); that was the case here and in most of the  
361 estimations in this analysis, and was assumed to be 0.9. A characteristic time,  $\lambda_0$ , can be defined by the  
362 width, or second moment of the autocovariance model (Goff and Jordan, 1988):

$$363 \quad \lambda_0 = \frac{\sqrt{2(\nu+1/2)}}{k_0}. \quad (16)$$

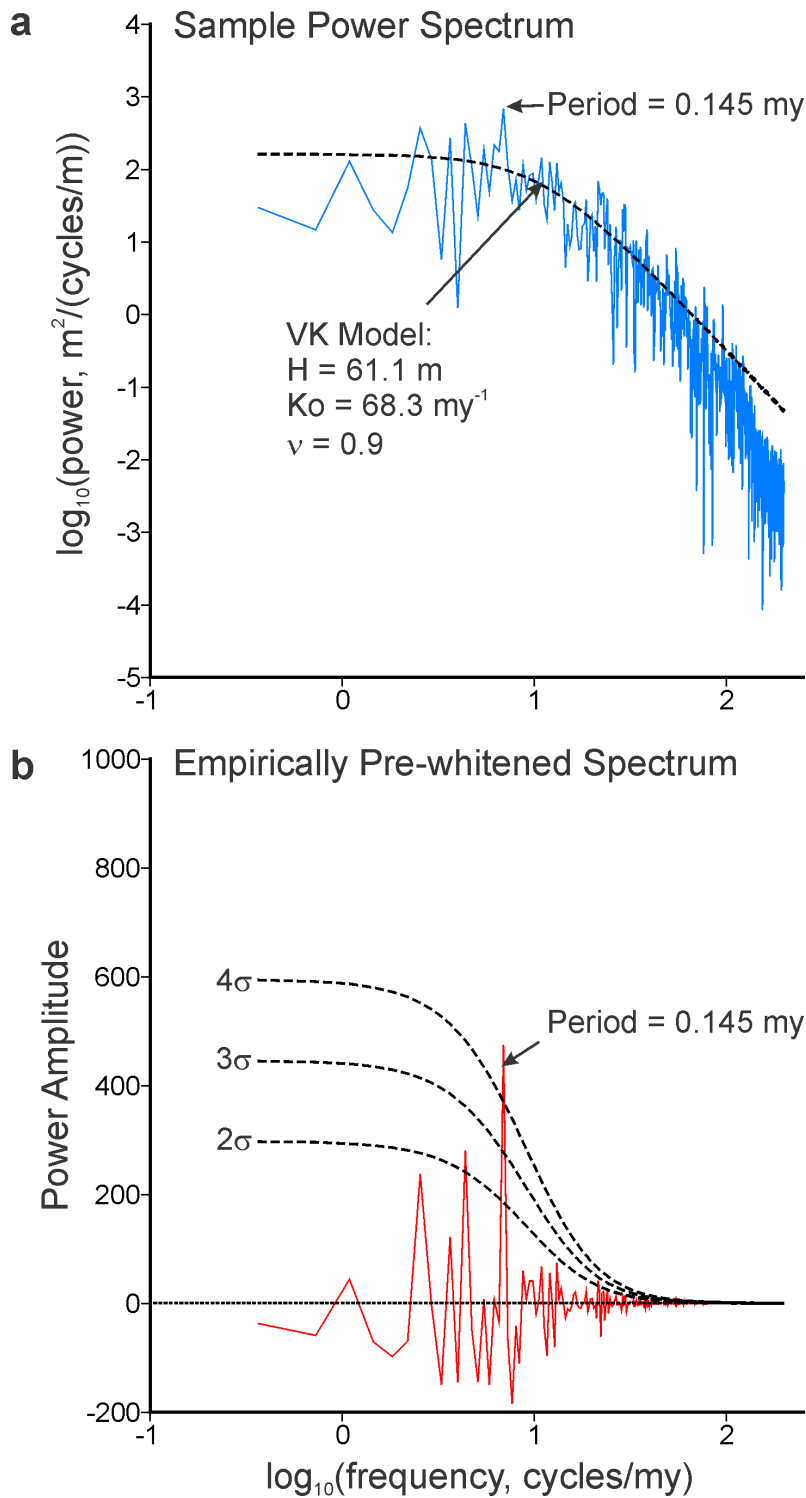
364 The characteristic time roughly corresponds to the visually dominant (on average) peak-to-peak distance  
365 (Goff, 1991), and thus is an important point of comparison for any potential identification of a harmonic  
366 component. For Profile 7a,  $\lambda_0 = 0.049 \pm 0.010 \text{ my}$  (which equates to  $\sim 3.8 \text{ km}$ ). The tail of the sample  
367 autocovariance (Figure 6b) exhibits a number of evidently regularly-space peaks and troughs that  
368 strongly suggest the presence of a harmonic component to the profile.

369 The spectral analysis of Profile 7a is shown in Figure 7. The sample power spectrum (Figure 7a)  
370 follows the modeled von Kármán power spectrum well at lower frequencies, but deviates at the higher  
371 frequencies. This deviation from the power law trend is a phenomenon noted by Goff and Jordan  
372 (1988), who attributed it to the “response”, or beam width of the multibeam echosounder being larger  
373 than the sample interval. This effect may also be caused by the averaging associated with the gridding

374 process. In any case, it is not a concern in this analysis because any periodic elements at that scale  
 375 would exhibit very small amplitudes. In addition to the overall von Kármán-like trend, a noticeable peak  
 376 is observed corresponding to a period of 0.145 my, approximately three times the characteristic time of  
 377 the best-fitting von Kármán model. That same peak is shown on the empirically pre-whitened spectrum  
 378 (Figure 7b) to be significant at a very high level of confidence:  $5.1\sigma$ . Therefore, it can be stated that a  
 379 periodic signal, with period of 0.145 my, is present in Profile 7a with a very high degree of certainty.



380  
 381 Figure 6. (a) Bathymetric profile 7a converted from distance to age on the x-axis using the age model of  
 382 Goff et al. (2018); location shown in Figure 5. (b) Sample autocovariance (solid) computed from (a), with  
 383 best-fit von Kármán model (dashed). The power spectral density in Figure 7a is computed by discrete  
 384 Fourier transform of the full sample autocovariance (with Hermetian symmetry), whereas the  
 385 empirically pre-whitened spectrum in Figure 7b is computed in the same way after zeroing out the  
 386 shaded region that fully encompasses the structural (non-zero mean) portion of the autocovariance and  
 387 tapering the edges.



388

389 Figure 7. (a) Sample power spectrum and (b) empirically pre-whitened spectrum calculated from the  
 390 sample autocovariance of Profile 7a shown in Figure 6b. The best-fit von Kármán model is overlain on  
 391 the power spectral density, and the  $2\sigma$ ,  $3\sigma$ , and  $4\sigma$  upper bounds on the null hypothesis are overlain on  
 392 the empirically pre-whitened spectrum. One harmonic component at a period of 0.145 my is detected  
 393 at  $5.1\sigma$  confidence

394 Having identified a likely periodic signal, the next step is to estimate its amplitude,  $\alpha$ . That value can  
395 be estimated from the amplitude of the peak observed on the empirically pre-whitened spectrum,  
396 which is proportional to  $\alpha^2$  (Priestley, 1981). However, the coefficient is a complex function of  $N$ ,  $m$  and  
397 the tapers used prior to DFT of  $\hat{P}_X^m(f)$ . Priestly (1981) calculated closed-form approximations for linear  
398 or no tapers, neither of which I found appropriate to the application at hand. Rather than attempt the  
399 same calculation for the  $\cos^2$  tapers used here, a far simpler method is to generate a simple cosine  
400 function and pass it through the same spectral analysis applied to the data profile. Then,  $\alpha$  is adjusted  
401 until the height of the resulting spectral peak matches what is observed on the empirically pre-whitened  
402 spectrum. With this procedure I estimated  $\alpha$  to be  $\sim 30$  m for the 0.145 my period peak detected for  
403 Profile 7b. The variance of this sinusoidal contribution is  $\alpha^2/2 = 450 \text{ m}^2$ , which equates to an RMS of 21.2  
404 m. The overall variance of Profile 7a is  $H^2 = 3730 \text{ m}^2$ . Therefore,  $3730 \text{ m}^2 - 450 \text{ m}^2$ , or  $3280 \text{ m}^2$  of the  
405 total variance of Profile 7a, is attributed to the aperiodic component of the profile. This equates to an  
406 RMS of 57.3 m, and which is 2.7 times the RMS of the sinusoidal component. Thus, while significant in  
407 its measurability, the sinusoidal contribution at 0.145 my period represents a relatively minor  
408 component of Profile 7a compared to the aperiodic signal.

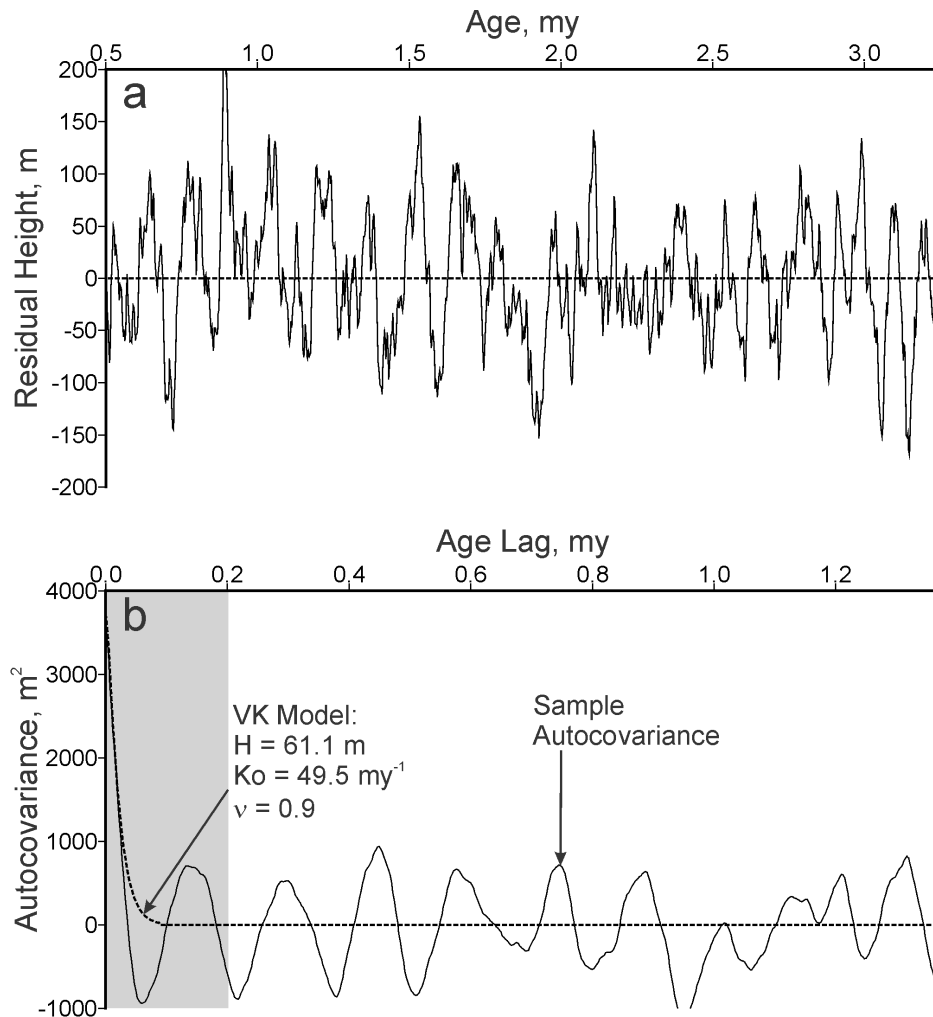
409 I next test the ability of the mixed spectrum statistical model, of the form presented in Equation  
410 (15), to match these observations. To do so I formulated a synthetic profile composed of: (1) a von  
411 Kármán aperiodic component using the parameters  $H = 57.3$  m (the estimated RMS height of the  
412 aperiodic component, rather than the overall RMS), and  $k_0$  and  $\nu$  as derived from the best-fit model, and  
413 (2) an added cosine function corresponding to amplitude 30 m and period 0.145 my. Initially this  
414 created a spectral peak that was too large, so the amplitude was reduced to 24 m to match the height  
415 exactly. This reiterates the point that the estimation of harmonic amplitude has significant uncertainties  
416 owing to modulation by the random, aperiodic component of the spectrum. The level of uncertainty will  
417 depend on the variation of the empirically pre-whitened continuous spectrum in proportion to the

418 height of the discrete spectral peak at the frequency of interest. The synthetic profile and sample  
419 autocovariance are shown in Figure 8, and the resulting spectral analysis is shown in Figure 9. The  
420 similarity of these plots to Figures 6 and 7, respectively, is very strong, particularly in the self-evident  
421 harmonic component in the tail of the sample autocovariance (Figure 8b), and in the size spectral peaks  
422 noted both on the sample power spectrum (Figure 9a) and the empirically pre-whitened spectrum  
423 (Figure 9b). The only notable difference between real and synthetic is in the power at the highest  
424 frequencies (Figures 7a versus 9a), which causes the real profile (Figure 6a) to have a smoother  
425 appearance than the synthetic profile (Figure 8a) at the smallest scales.

426 Spectral analysis plots for all twelve profiles are presented in the Supplementary Material. Estimated  
427 von Kármán and cosine function parameters from each analysis are listed in Table 1. Periodicities were  
428 detected in all but three of the profiles, and in several there were multiple periodicities detected. The  
429 periods detected were highly variable, however, ranging at least an order of magnitude from 0.02 my  
430 (the minimum considered for inclusion in Table 1) to 0.216 my. There is no evident clustering of values  
431 at the Milankovitch periods of 0.100 my, 0.041 my or 0.026 my, although there are several detected  
432 periods that are equal or close to those values. More importantly, there is no evidence of spatial or  
433 temporal consistency. For example, Profiles 3, 6 and 8 are quite proximal (Figure 5), but exhibit no  
434 consistency in the periods of their harmonic components (Table 1). The same inconsistency is also true  
435 of Profiles 1a and 1b, and Profiles 7a and 7b (Table 1), although each pair is sited along the same flow  
436 line (Figure 5) and so were generated at the same ridge crest segment but at different times.

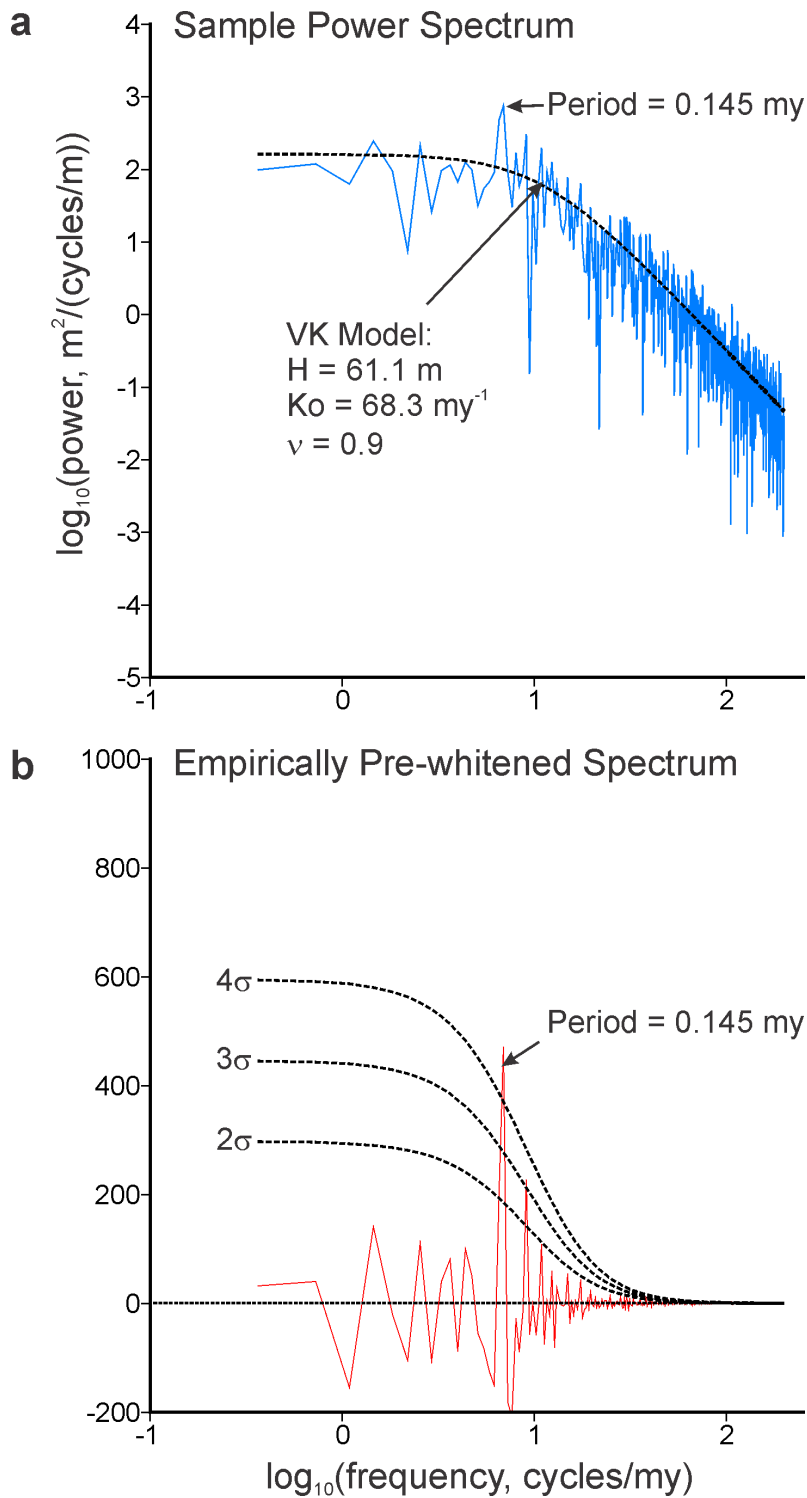
437 To gauge the significance of each detected periodicity to variability of each profile, I calculate a  
438 value  $R$  as the ratio of RMS heights of the periodic to aperiodic components, respectively. By this  
439 measure (Table 1), there is a clear separation of significance between those harmonic detections with  
440 periods greater than or less than the characteristic time of the best-fitting von Kármán model. Those  
441 periods greater than the characteristic time, seven in all, exhibit  $R$  values ranging from 0.19 to 0.38, with

442 all but the smallest of those  $>0.27$ . In contrast, periods less than the characteristic time exhibit  $R$  values  
 443 ranging from 0.03 to 0.11, with only the largest  $> 0.08$ . In all cases, however, the aperiodic component  
 444 of the profiles is the dominant source of variability.  
 445



446  
 447 Figure 8. (a) Synthetic profile formed from the summation of (1) an aperiodic von Kármán profile, with  
 448 parameters as noted in the text, and (2) a cosine function of amplitude 24 m and period 0.145 my. (b)  
 449 Sample autocovariance (solid) computed from (a), with best-fit von Kármán model for Profile 7a  
 450 (dashed). The power spectral density in Figure 9a is computed by discrete Fourier transform of the full  
 451 sample autocovariance (with Hermitian symmetry), whereas the empirically pre-whitened spectrum in  
 452 Figure 9b is computed in the same way after zeroing out the shaded region that fully encompasses the  
 453 structural (non-zero mean) portion of the autocovariance and tapering the edges.  
 454





455

456 Figure 9. (a) Sample power spectrum and (b) empirically pre-whitened spectrum calculated from the  
 457 sample autocovariance of the synthetic profile shown in Figure 8. The best-fit von Kármán model is  
 458 overlain on the power spectral density, and the 2 $\sigma$ , 3 $\sigma$ , and 4 $\sigma$  upper bounds on the null hypothesis are  
 459 overlain on the empirically pre-whitened spectrum. The height of the spectral peak at 0.145 my period,  
 460 observed in spectral analysis of Profile 7a (Figure 7), is successfully reproduced by the synthetic profile.

461

## 462 **5. Conclusions and Discussion**

463 Application of an “empirical pre-whitening” spectral analysis, based on the “ $P(\lambda)$  test”  
464 formulated by Priestly (1981), has enable detection of temporal periodicities at high confidence in a  
465 number of profiles sampled from multibeam bathymetric data along the southern EPR. However, these  
466 harmonic signals are relatively minor components of the overall variability of the profiles, which are  
467 instead dominated by an aperiodic signal conforming to a continuous, rather than discrete spectrum.  
468 Furthermore, the periods expressed by the harmonic signals are widely variable, and do not exhibit any  
469 spatial or temporal consistency. This behavior makes the origin of harmonic signals in abyssal hill  
470 morphology enigmatic, but does rule out external forcing such as may be applied by Milankovich cycle-  
471 based variability in sea level. Rather, the forcing must be internal, highly localized, and subject to  
472 changing conditions over time.

473 Abyssal hills generated at fast spreading rates are predominantly fault-bounded, horst-and-graben  
474 structures (e.g., Macdonal et al., 1996; Macdonald, 2015). Furthermore, fault scaling parameters  
475 (spacing, length, throw) are successfully modeled as random distributions constrained by scaling laws  
476 (Malinverno and Cowie, 1993; Bohnenstiehl, and Carbotte, 2001). The dominant aperiodic component  
477 of abyssal hills can thus reasonably be assumed to be associated with this fault-generated morphology,  
478 characterized statistically by a von Kármán model defined by parameters RMS height, characteristic  
479 time, and fractal dimension. The most significant harmonic contributions to abyssal hills, typically with  
480 RMS heights around a quarter to a third of the aperiodic RMS, exhibit periods that are larger than the  
481 characteristic time. Such variations in bathymetry could plausible be associated with variations in crustal  
482 thickness associated with temporal variations in magma supply (Canales et al., 2000; Shinevar et al.,  
483 2019; Parnell-Turner et al, 2020). Parnell-Turner et al. (2020), in a spectral analysis of abyssal hill  
484 morphology on the flanks of the medium-spreading-rate Southeast Indian Ridge, also discerned a scale

485 of morphology (although no clear indication of periodicity) that was larger than the characteristic  
486 time/width of abyssal hills. They hypothesize that variations in melt supply at <0.2 my time scales could  
487 be associated either with time-varying, melt rich “porosity waves” in the mantle, or by small-scale  
488 mantle heterogeneities. Investigating whether these or other mechanisms could apply to the super-fast  
489 spreading southern EPR would be an important avenue of investigation for a modeling effort (though  
490 beyond the scope of this paper). These results provide key observations that need to be accounted for  
491 in any such effort, including the range of periods observed, their spatio-temporal variability, and their  
492 topographic amplitudes.

493

494 **Acknowledgements.** The southern East Pacific Rise multibeam data used in this analysis are available  
495 from the Global Multi-Resolution Topography Data Synthesis (<https://www.gmrt.org/>).

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559  
560

561 Table 1. Modeled aperiodic and detected periodic components of southern EPR profiles

562

563	Profile	H, m	$\lambda_0$ , my	Period, my (min 0.02)	$Z_\sigma$ (> 3.5)	$\alpha$ , m	R
566	1a	65.5	0.065	0.112	4.6	25	0.28
567				0.021	3.9	3	0.03
568	1b	83.8	0.089	0.037	3.9	7	0.06
569	2	74.1	0.050	0.143	5.3	35	0.35
570				0.042	4.0	11	0.11
571	3	51.3	0.038	0.111	3.9	19	0.27
572				0.082	6.2	20	0.29
573	4	50.4	0.049	-	-	-	-
574	5	50.3	0.043	0.032	3.7	6	0.08
575				0.027	6.2	6	0.08
576	6	48.2	0.056	0.216	4.2	24	0.38
577				0.022	4.8	3	0.05
578	7a	68.3	0.049	0.145	5.1	30	0.33
579	7b	80.3	0.068	-	-	-	-
580	8	41.3	0.034	0.047	4.1	11	0.19
581	9	58.4	0.065	0.040	3.7	7	0.08
582				0.030	4.0	5	0.06
583				0.025	7.4	5	0.06
584				0.020	6.0	4	0.05
585	10	55.5	0.034	-	-	-	-

586

587 H: RMS height of best-fit von Kármán model

588  $\lambda_0$ : Characteristic time of best-fit von Kármán model

589  $Z_\sigma$ : Height of spectral peak expressed as multiple of standard deviation  $\sigma$ .

590  $\alpha$ : Estimated amplitude of harmonic component.

591 R: Ratio of periodic to aperiodic RMS

592 -: No detection of harmonic component