

# Post-critical *SsPmp* and Its Applications to Virtual Deep Seismic Sounding (VDSS)

## 1. Sensitivity to Lithospheric 1D and 2D Structure

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### Abstract

Virtual Deep Seismic Sounding (VDSS) has recently emerged as a novel method to image the Moho and potentially other lithospheric boundaries. The behavior of *SsPmp*, the post-critical reflection phase at the Moho that is utilized in VDSS, is rich with complexities not yet widely utilized. Here, motivated by observations from the Ordos Plateau in North China, we use synthetic seismograms computed with a broad range of models to evaluate how different parts of the lithosphere along the ray path of *SsPmp* affect its phase, amplitude, and arrival time. If the crust-mantle boundary is a sharp discontinuity, the *SsPmp* phase shift relative to the direct S wave varies from  $\sim 180^\circ$  to  $\sim 0^\circ$  with increasing values of lower-crustal  $V_p$ , upper-mantle  $V_p$  and ray parameter. This property indicates the possibility of using *SsPmp* to constrain  $V_p$  in the lower crust and uppermost mantle. If the crust-mantle boundary is a velocity-gradient zone with thickness smaller than the dominant wavelength of the converted P wave ( $\sim 25$  km), the *SsPmp* phase and amplitude do not differ significantly from the case with a discontinuity that has the same velocity increase. However, in such cases *SsPmp* arrival times vary as different functions of ray parameter from the cases with sharp crust-mantle boundary, because different rays turn at different depths, allowing measurement of the vertical velocity gradient in the crust-mantle transition zone. If the virtual source (location of S-to-P conversion at the free surface) is in a sedimentary basin, *SsPmp* amplitude can be significantly reduced due to low S-to-P reflected energy at the virtual source. This may cause the absence of *SsPmp* despite appropriate source-receiver geometry. The *SsPmp* arrival time relative to direct S is not only controlled by crustal thickness at the reflection point, but also by lateral variation of  $V_s$  beneath the virtual source and the receiver. The accuracy of crustal-thickness measurements from *SsPmp* arrival times thus

depends on our knowledge of the variability of lithospheric  $V_s$  and crustal  $V_p$  across a broad region.

## 1. Introduction

For a quarter-century the seismic community has relied heavily on receiver function (RF) techniques, which use teleseismic P-to-S ( $Pms$  or PRF) or S-to-P ( $Smp$  or SRF) conversion phases, to image discontinuities in the lithosphere (Fig. 1) (e.g. Kind et al., 1995; Langston, 1979; Owens and Taylor, 1984). In recent years, Virtual Deep Seismic Sounding (VDSS) has emerged as a novel method to image the crust-mantle boundary (CMB) and has been successfully applied to multiple datasets from different areas as a complement to RF techniques (e.g. Kang et al., 2016; Parker et al., 2016; Tseng et al., 2009; Yu et al., 2016, 2012). Here we use  $CMB$  to denote the geological transition from crust to mantle, whether abrupt or a “velocity-gradient zone” spanning many kilometers; and  $Moho$  to denote a seismological inference about this transition, typically given as single depth.  $SsPmp$ , the seismic phase used in VDSS, originates when upcoming teleseismic S waves convert to down-going P waves at the free surface (the virtual source), which then undergo post-critical reflection at or within the CMB and finally reach the receiver (Fig. 1). The arrival time of  $SsPmp$  relative to the direct S arrival (or  $Ss$ ), hereafter  $T_{VDSS}$ , is used to estimate the Moho depth at the reflection point, normally assumed to be the midpoint between the virtual source and receiver. Because VDSS uses teleseismic events, the incident S wave can be approximated as a plane wave with constant ray parameter. To enable post-critical reflection of  $SsPmp$  at the Moho, appropriate epicentral distances are  $\sim 40\text{--}50^\circ$ , corresponding to ray parameter  $p = \sim 0.1256\text{--}0.1345$  s/km for a focal depth of 0 km ( $1/p = \sim 7.96\text{--}7.43$  km/s), and slightly smaller  $p$  for larger focal depths (Fig. 2). Due to post-critical reflection at the Moho,  $SsPmp$  usually has amplitude comparable to  $Ss$  (Fig. 3a), making it possible to construct a seismic profile with a single event recorded by an array (Figs. 4b,c). Because  $SsPmp$  undergoes post-critical reflection at the Moho, its phase is changed relative to  $Ss$  (e.g. Aki and Richards, 1980) (Fig. 3a; hereafter referred to as phase shift for simplicity and denoted  $\Phi_{VDSS}$ ), making it difficult to directly pick  $T_{VDSS}$  from raw records. Previous studies (e.g. Tian et al., 2015; Tseng et

al., 2009; Yu et al., 2016;) have used 1D waveform fitting to measure  $T_{VDSS}$ , and then find the trade-off relation between crustal  $V_p$  and thickness  $H$  using the equation:

$$T_{VDSS} = 2H \sqrt{\frac{1}{V_p^2} - p^2} \quad (1)$$

where  $p$  is the ray parameter of the incident waves. In the process of waveform fitting, the upper mantle has commonly been assumed to be a half space and its  $V_p$  (or  $V_p^{um}$ ) has been fixed based on *a priori* knowledge of  $V_p^{um}$  of the study area due to the recognized effect of  $V_p^{um}$  on  $SsPmp$  waveforms (e.g. Tian et al., 2015; Yu et al., 2016). Similarly, previous VDSS studies have commonly assumed for the purposes of waveform fitting that the CMB is a discontinuity at which  $V_p$  jumps from typical crustal values ( $\sim 6.5$  km/s) to typical upper mantle values ( $\sim 8.1$  km/s). Tseng et al. (2009) and Yu et al. (2012) discussed the case in which the CMB is a velocity gradient zone and showed that the  $SsPmp$  waveforms appeared similar to the case in which the CMB is a discontinuity. Multiples (reverberations) generated in sedimentary basins severely contaminate receiver-function waveforms and have presented a long-standing challenge to the utility of receiver functions (e.g. Bao and Niu, 2017; Guan and Niu, 2017; Langston, 2011; Tao et al., 2014; Yu et al., 2015). In contrast, the manner in which sedimentary basins affect  $SsPmp$  waveforms is not widely understood. Parker et al., 2016 showed that  $SsPmp$  responds differently to a vertically homogeneous basin and to a basin with velocity increasing downward.

Here we present as motivation a dataset from the Ordos Plateau in North China in which significant changes in  $SsPmp$  phase shift, amplitude relative to direct S, and travel time delay ( $\Phi_{VDSS}$ ,  $A_{VDSS}$ ,  $T_{VDSS}$ ) are observed across the recording array. We first use synthetic waveforms to demonstrate that, when the CMB is a sharp discontinuity,  $\Phi_{VDSS}$  decreases from  $\sim 180^\circ$  to  $\sim 0^\circ$  as the lower crustal  $V_p$  (hereafter  $V_p^{lc}$ ) or upper mantle  $V_p$  (hereafter  $V_p^{um}$ ) or ray parameter  $p$  increases. Additionally, when  $p$  is small ( $1/p$  is close to  $V_p^{um}$ )  $\Phi_{VDSS}$  is more sensitive to  $V_p^{um}$  than  $V_p^{lc}$ , whereas when  $p$  is large ( $1/p$  is close to  $V_p^{lc}$ )  $\Phi_{VDSS}$  is more sensitive to  $V_p^{um}$  than  $V_p^{um}$ . We next show that when the CMB is a velocity gradient zone with thickness up to the dominant wavelength of incident S wave ( $Ss$ ), neither  $\Phi_{VDSS}$  nor  $A_{VDSS}$  varies significantly with  $p$ , but  $T_{VDSS}$  varies as different functions of  $p$  from the case with sharp CMB, because rays with different ray parameters turn at different depths within the velocity-gradient zone. This feature should make VDSS an ideal method to study CMB structure in areas such as the Colorado Plateau, where a

sharp Moho is not observed by traditional methods based on pre-critical reflections and conversions (Hauser and Lundy, 1989; Shen et al., 2013). We also demonstrate that although  $A_{VDSS}$  is largely insensitive to CMB structure,  $A_{VDSS}$  is significantly decreased by low near-surface velocity at the virtual source, which may explain cases of the absence of  $SsPmp$  from records with otherwise proper observation geometries. Finally, we use 2D synthetic seismograms to show that  $T_{VDSS}$  is affected not only by crustal thickness at the reflection point, but also by heterogeneity in  $V_s$  structure beneath the virtual source and receiver, for instance lateral variation in lithospheric thickness, which must be accounted for when using  $T_{VDSS}$  to estimate crustal thickness. Our analyses qualitatively explain the variation of  $\Phi_{VDSS}$  and  $A_{VDSS}$  in our example from the Ordos Plateau. In our companion paper (Liu et al., unpublished manuscript, hereafter “Part 2”), we quantitatively analyze a more comprehensive dataset from the Ordos Plateau in order to demonstrate the use of post-critical  $SsPmp$  in imaging lithospheric structure.

## 2. Data

The Ordos Plateau in northern China (Fig. 3c) is a site of considerable interest, as it is the surviving remnant of the Archean North China Craton (Liu et al., 1992). It is unknown why this region preserved its lithospheric root while the eastern part of the craton underwent significant modification (decratonization) in Mesozoic time (Gao et al., 2008; Griffin et al., 1998; Menzies et al., 1993). To study the lithospheric structure of the Ordos Plateau, a W–E linear seismic array was deployed across the Ordos Plateau at  $\sim 37.5^\circ$  N during 2006–2008 by Peking University (Yu et al., 2012), and recorded abundant intermediate to deep seismicity in the west-Pacific subduction zones at epicentral distances of  $40\text{--}50^\circ$ , making the dataset ideal for observing post-critical  $SsPmp$  (Fig. 4a). Because the western and eastern parts of the array were deployed in two different time periods, we use two nearby events ( $\sim 400$  km separation) in the Banda Sea to make a single record section (Figs. 4b,c). The traces are bandpass filtered from  $0.04\text{--}0.5$  Hz, separated into pseudo-P (motion associated with incoming P waves) and pseudo-SV (motion associated with incoming SV waves) components (hereafter referred to as P and S for simplicity) with a particle-motion analysis algorithm (Yu et al., 2013), aligned along their direct S ( $Ss$ ) arrival times. The  $Ss$  arrival times are picked at the zero-crossings of the  $Ss$  wavelets, which closely resemble a first-order Hermitian wavelet (first derivative of Gaussian wavelet; Figs. 4b-f), because for a first-order Hermitian wavelet the peak of its envelope function is at its zero-

crossing and does not change after an arbitrary phase shift. The sensitivity of measured arrival time to the addition of noise could make the use of the zero-crossing less appropriate for real data than for these synthetics. Our synthetic waveforms are normalized to the peak amplitudes of the corresponding direct S arrivals.

We observe significant variation in  $A_{VDSS}$  across the array. For instance,  $A_{VDSS}$  of JB09 is only about half of JB13 (Figs. 4d,e), despite a station separation of only  $\sim 60$  km. Because the traces are normalized by the peak amplitudes of  $S_s$ , the effects of source radiation pattern are removed (and should anyway be minor since the aperture of the array is small compared to the epicentral distance). The rapid change of  $A_{VDSS}$  across the array thus must be due to structure near the stations.  $\Phi_{VDSS}$  also varies rapidly across the array. At JB13,  $S_sPmp$  has a  $\sim 90^\circ$  phase advance relative to  $S_s$  (Fig. 4e), as commonly assumed for post-critical  $S_sPmp$  (Tseng et al., 2009). However, only  $\sim 120$ -km distant, at FY03 the  $S_sPmp$  waveform closely resembles  $S_s$ , indicating a  $\sim 0^\circ$  phase shift (Fig. 4f).  $\Phi_{VDSS}$  is unrelated to the source and should be primarily controlled by structure close to the stations.  $A_{VDSS}$  and  $\Phi_{VDSS}$  are crucial properties that need to be correctly modeled in order to measure  $T_{VDSS}$ . If the signal-to-noise ratio of  $S_sPmp$  is very small, it will be difficult to measure its arrival time. Even when  $S_sPmp$  amplitude is high, as for JB13 and FY03, improperly modeling the phase of  $S_sPmp$  will cause up to  $\sim 1$  s error in  $T_{VDSS}$ , which corresponds to  $\sim 5$  km error in the resulting crustal thickness estimation, a nontrivial error in most applications. The phenomenon of significant spatial variation of  $A_{VDSS}$  and  $\Phi_{VDSS}$  has not been systematically explored by previous studies. Another unexpected feature of the Ordos dataset is that  $T_{VDSS}$  varies significantly across the array (Fig. 4a). Using the arrival time of the strongest peaks on the P component as an approximation of  $T_{VDSS}$  (equivalent to assuming a  $90^\circ$  phase shift), we find that  $T_{VDSS}$  reaches its maximum of  $\sim 12$  s at  $\sim 110.5^\circ$  E, nominally corresponding to a crustal thickness of  $\sim 60$  km, and then decreases rapidly eastward, reaching  $\sim 6$  s at  $\sim 113^\circ$  E, which corresponds to a crustal thickness of  $\sim 30$  km (Yu et al., 2012). This change in travel-time is far greater than possible phase delays that are limited to  $0$ – $180^\circ$ , or  $\sim 2$  s for these  $\sim 4$  s period arrivals. The unexpectedly deep Moho was previously interpreted as preservation of a  $\sim 20$ -km thick, mafic lower-crustal layer beneath the Ordos Plateau, relict from craton formation (Yu et al., 2012). However, the recent recognition that lateral variation in  $V_s$  structure affects  $T_{VDSS}$  (Yu et al., 2016) makes the direct relation of  $T_{VDSS}$  to crustal thickness problematic. Therefore, it is important to evaluate quantitatively how realistic lateral variations of  $V_s$  affect  $T_{VDSS}$ . In the

following sections, we use synthetic seismograms to examine possible lithospheric structures that may affect  $A_{VDSS}$ ,  $\Phi_{VDSS}$  and  $T_{VDSS}$ .

### 3. Synthetic Tests

#### 3.1. Sensitivity to $V_p$ across the crust-mantle boundary (CMB)

In this section, we first assume that the lithosphere consists of three homogeneous layers separated by abrupt discontinuities: the upper crust, lower crust and upper mantle (Figs. 5a, 6a). The  $SsPmp$  waveform is affected by  $V_p$  of the lower crust and upper mantle, therefore we first vary  $V_p^{lc}$  with fixed  $V_p^{um}$  (Fig. 5a), and then vary  $V_p^{um}$  with  $V_p^{lc}$  fixed (Fig. 6a), to test the sensitivity of the  $SsPmp$  waveform to the two parameters. As  $V_p$  varies, we vary  $V_s$  to keep Poisson's ratio constant at 0.25, and vary density to satisfy the Nafe-Drake relation (Brocher, 2005). We compute waveforms using the reflectivity algorithm in a layered medium (Randall, 1989), in which the incident S wave has a constant ray parameter  $p = 0.127$  s/km ( $1/p = 7.87$  km/s). The source time function is assumed to be a first-order Hermitian wavelet (first derivative of a Gaussian wavelet) with a half width of  $\sim 2$  s, which has similar shape and frequency to observed  $Ss$  of deep or intermediate-depth earthquakes (Fig. 3).

Fig. 5b shows synthetic seismograms computed with  $V_p^{lc}$  ranging from 7.0–7.8 km/s and  $V_p^{um}$  fixed at 8.0 km/s. This range of  $V_p^{lc}$  is characteristic of continental lower crust made of predominantly mafic rocks (Christensen and Mooney, 1995). As  $V_p^{lc}$  increases,  $SsPmp$  arrives earlier ( $T_{VDSS}$  decreases) and becomes closer to the reflection phase at the top of the lower crust ( $SsPip$  with  $i$  standing for intra-crustal interface; Fig. 5b), with little change in  $A_{VDSS}$  and  $\Phi_{VDSS}$  (Fig. 5d). The amplitude of  $SsPip$  grows as  $V_p^{lc}$  increases (Fig. 5c), interfering with  $SsPmp$  and distorting its waveform (Fig. 5b). The different responses of  $SsPip$  and  $SsPmp$  to velocity changes indicate their different natures. As a pre-critical reflection, the amplitude of  $SsPip$  grows as the velocity contrast at the intra-crustal interface increases. In contrast, as a post-critical reflection phase, the amplitude of  $SsPmp$  ( $A_{VDSS}$ ) stays constant despite changes of velocity contrast across the Moho, because all incident energy is reflected upwards at the CMB ( $V_p^{um}$  exceeds the ray parameter  $p$ ).

Fig. 6 shows the sensitivity of  $SsPmp$  waveforms to  $V_p^{um}$ . We compute synthetic seismograms using models with  $V_p^{um}$  ranging from 7.9–8.5 km/s and  $V_p^{lc}$  fixed at 7.0 km/s (Fig.

6a). The range of  $V_p^{um}$  used here covers most of the observed range for the continental uppermost mantle (Christensen and Mooney, 1995), and also ensures post-critical reflection of  $SsPmp$  at the CMB for our chosen ray parameter ( $1/p=7.87$  km/s). Our synthetic seismograms show the strong dependence of  $\Phi_{VDSS}$  on  $V_p^{um}$  (Fig. 6b). When  $V_p^{um} = 7.9$  km/s,  $\Phi_{VDSS}$  is close to  $180^\circ$  (corresponding to the source wavelet multiplied by -1), and the waveform is very similar to the pre-critical reflection. As  $V_p^{um}$  increases,  $\Phi_{VDSS}$  first decreases to  $\sim 90^\circ$ , and then further drops towards  $0^\circ$  (Fig. 6b). Another important observation is that despite the significant change in phase,  $A_{VDSS}$  stays the same as  $V_p^{um}$  increases, because all incident energy is post-critically reflected. Because  $\Phi_{VDSS}$  (the  $SsPmp$  waveform) is sensitive to  $V_p^{um}$ , one must know  $V_p^{um}$  in order to correctly measure  $T_{VDSS}$ . An example is shown in Fig. 6c, in which we assume the  $SsPmp$  wavelet to be phase-shifted by  $90^\circ$  from  $Ss$ , and cross-correlate it with synthetic waveforms computed with models in Fig. 6a in order to find  $T_{VDSS}$ . The resulting  $T_{VDSS}$  for each model is then converted to estimated crustal thickness (Moho depth) using Eq. 1 with the true average crustal  $V_p$ . We observe that a  $90^\circ$  phase shift is only a good approximation when  $V_p^{um} = 8.3$  km/s, whereas for  $V_p^{um} = 7.9$  km/s the estimated Moho depth is  $\sim 5$  km larger than the true value (Fig. 6c). This example highlights the importance of using the correct  $V_p^{um}$  in measuring  $T_{VDSS}$  and estimating Moho depth.

To explore the effect of ray parameter  $p$  on  $\Phi_{VDSS}$  and its sensitivity to  $V_p^{lc}$  and  $V_p^{um}$ , we calculate  $\Phi_{VDSS}$  as functions of  $V_p^{lc}$  and  $V_p^{um}$  for  $p = 0.127$  and  $0.130$  s/km. When  $p = 0.127$  s/km ( $1/p = 7.87$  km/s),  $\Phi_{VDSS}$  is largely controlled by  $V_p^{um}$  (Fig. 7a; also Figs. 5, 6). However, when  $p = 0.130$  s/km ( $1/p = 7.69$  km/s),  $\Phi_{VDSS}$  depends more on  $V_p^{lc}$  than  $V_p^{um}$  (Fig. 7b). Besides,  $\Phi_{VDSS}$  decreases for all  $V_p^{lc}$  and  $V_p^{um}$  when  $p$  increases from  $0.127$  s/km to  $0.130$  s/km (Fig. 7). This example indicates that increasing  $p$  not only reduces  $\Phi_{VDSS}$ , but also makes  $\Phi_{VDSS}$  more sensitive to  $V_p^{lc}$  and less sensitive to  $V_p^{um}$ . Combining the above examples, we conclude that increasing  $V_p^{lc}$ ,  $V_p^{um}$  and  $p$  decreases  $\Phi_{VDSS}$ , and that when  $p$  is small ( $1/p$  is close to  $V_p^{um}$ )  $\Phi_{VDSS}$  is more sensitive to  $V_p^{um}$  than  $V_p^{lc}$ , whereas when  $p$  is large ( $1/p$  is close to  $V_p^{lc}$ )  $\Phi_{VDSS}$  is more sensitive to  $V_p^{lc}$  than  $V_p^{um}$ .

### 3.2. Sensitivity to CMB Thickness

To understand how CMB thickness affects *SsPmp* waveforms, we model the CMB as a transition from  $V_p = 6.5$  km/s, typical of crustal rocks, to  $V_p = 8.1$  km/s, typical of uppermost-mantle rocks. As before,  $V_s$  and density are varied simultaneously with  $V_p$  to keep Poisson's ratio at 0.25 and to satisfy the Nafe-Drake relation (Brocher, 2005). We model the transition zone as a stack of 1-km-thick layers and vary the transition thickness from 0–20 km below a fixed top at 40 km (Fig. 8a). As the CMB becomes thicker, there is little change in either  $A_{VDSS}$  or  $\Phi_{VDSS}$  (Fig. 8b). This behavior is distinct from that of pre-critical reflected and converted phases at the CMB, which become broader and weaker as the CMB thickens. The clear change in Fig. 8b is that  $T_{VDSS}$  becomes larger as the post-critical reflection occurs at greater depth, because in each case the incident wave turns at the depth within the CMB where  $V_p = 1/p$ , so the turning depth becomes larger as the CMB thickness increases (Fig. 8a).

Fig. 9 compares the responses of PRF and VDSS to different CMB thicknesses (Figs. 9a,b). The model in Fig. 9b is identical to the model with a 20-km-thick CMB in Fig. 8a, whereas Fig. 9a is the 0-km-thick CMB model in Fig. 8a with the discontinuity shifted from 40 km to 50 km, so that the centers of the CMBs are at the same depth in Fig. 9a and b. When the incident waves are plane P waves with ray parameters in the range 0.04–0.08 s/km, the computed PRFs are strong and narrow for a discontinuous CMB (Fig. 9c), but broad and weak for a transitional CMB (Fig. 9d) (even the strongest *Pms* on the PRFs shown here is only ~20% the amplitude of the first arrival). As the CMB thickens, high-frequency components of the incident P waves with wavelengths shorter than the scale of the CMB become insensitive to it, eliminating high-frequency components of *Pms*. The *Pms* waveforms stay unchanged as the ray parameter varies from 0.04–0.08 s/km for both a sharp CMB (Fig. 9c) and a broad CMB (Fig. 9d). Theoretical *Pms* arrival times (calculated assuming that conversion occurs at the center of the CMB) closely match the centers of observed *Pms*, and are very similar at the same ray parameter, for both sharp and broad CMBs (Figs. 9c,d). The above behaviors would also be observed for pre-critical *Pmp* and *SsPmp* reflections.

In contrast, post-critical *SsPmp* is a strong phase whether the CMB is a discontinuity or a broad transition zone, and has similar amplitude to *Ss* (Figs. 9f, 8b). The reason that post-critical *SsPmp* remains strong as the CMB thickens is that all frequency components of the down-going P wave are reflected (or turned) at the depth where, for that ray parameter,  $V_p$  reaches the critical velocity. As a result,  $T_{VDSS}$  predicted using the reflection depth as the depth where the critical



velocity is reached follows the move-out of  $SsPmp$  closely in the transitional model (Fig. 9f) but differs significantly from  $T_{VDSS}$  in the sharp CMB case (Fig. 9e).

When an incident plane wave turns in a medium with positive vertical velocity gradient, the turning wave will have a  $90^\circ$  phase shift relative to the incident wavelet (Shearer, 1999). However, our synthetic waveforms show that, for CMB thickness  $< 20$  km,  $\Phi_{VDSS}$  of the transitional models are similar to the discontinuity model with the same  $p$  (Figs. 8b, 9e,f), instead of  $90^\circ$ . The reason is that the dominant wavelength of down-going P wave in the CMB ( $\sim 25$  km for a dominant frequency of  $\sim 0.25$  Hz) is similar to the CMB thickness ( $< 20$  km), causing  $\Phi_{VDSS}$  to be insensitive to the presence of the transition zone. Since the transitional models have the same total velocity increase across the CMB as the discontinuity model,  $\Phi_{VDSS}$  of the transitional models are similar to the discontinuity model at a given  $p$ . To further test our hypothesis, we computed  $\Phi_{VDSS}$  for CMB thicknesses up to 60 km with the total velocity increase across the CMB the same as the discontinuity model (Fig. 8c). The results show that as CMB thickness exceeds  $\sim 20$  km,  $\Phi_{VDSS}$  starts to deviate significantly from the discontinuity model ( $\Phi_{VDSS} = 119^\circ$ ), and gradually approaches  $90^\circ$  as CMB thickness further increases (Fig. 8c). This supports our hypothesis that  $\Phi_{VDSS}$  is similar in both transitional and discontinuity models due to finite-frequency effects. In principal, higher-frequency incident waves would show a more pronounced difference between  $\Phi_{VDSS}$  produced by a sharp and a broad CMB, though recorded teleseismic S waves seldom have energy above 1 Hz. Therefore, we conclude that, for CMB thickness smaller than  $\sim 25$  km, no significant difference exists between  $\Phi_{VDSS}$  caused by a sharp CMB and by a broad CMB, though the two models cause distinct move-out of  $T_{VDSS}$  with  $p$  (Fig. 9f).

### 3.3. Sensitivity to Sedimentary Basins

In the presence of sedimentary basins, we expect the waveforms of  $SsPmp$  to be affected by the thickness, velocity, Poisson's ratio (or  $V_p/V_s$  ratio), and velocity gradient of the sedimentary layer. We next test the sensitivity of  $SsPmp$  waveforms to sedimentary basins by varying each of these four parameters, one at a time (Figs. 10a-d). Our reference basin model is a homogeneous layer with  $V_p = 4.5$  km/s, Poisson's ratio = 0.25, and thickness = 6 km. For simplicity, we assume the basin has uniform properties both at the virtual source and at the receiver (Fig. 10j).

#### 3.3.1. Sedimentary-layer thickness

To test the effects of sedimentary-layer thickness on  $SsPmp$  waveforms, we vary thickness from 0 km (bed-rock case), 3 km (shallow-basin) to 6 km (deep-basin) (Fig. 10a). Both basin cases have similar  $A_{VDSS}$ , clearly lower than the bed-rock case (Fig. 10e).  $SsPmp$  arrives increasingly later ( $T_{VDSS}$  increases) as the basin becomes deeper, because the basin has lower velocities than the bed rock (Fig. 10e). Also visible in the two basin cases are the seismic arrivals  $Sbp$  (S-to-P conversion phase at the basin-basement interface  $b$ ) and  $SsPbp$  (pre-critical P reflection phase at the basin-basement interface after S-to-P reflection at the free surface) (Fig. 10e), both delayed slightly from  $Ss$ . As the basin becomes thicker,  $Sbp$  and  $SsPbp$  are increasingly delayed from  $Ss$  (Fig. 10e).  $SsbPmp$  (S-to-P reflection at the basin-basement interface followed by post-critical reflection at the Moho) is not observed because the velocity contrast at the basin-basement interface is not large enough to generate strong S-to-P reflections (Fig. 10e).

The reduced  $A_{VDSS}$  in the presence of sedimentary cover has profound significance, as none of the parameters previously examined ( $V_p^{lc}$ ,  $V_p^{um}$  and CMB thickness) have significant effects on  $A_{VDSS}$ , thus cannot explain observations of highly variable  $SsPmp$  amplitude (Figs. 4d,e). We interpret the low  $SsPmp$  amplitude in the presence of a sedimentary basin as caused by the low  $V_s$  at the virtual source, which reduces the incident angle of the incoming S wave at the free surface and lowers the reflection coefficient between the incident S wave and reflected P wave. (In an extreme case, a vertically incident S wave produces no reflected P wave.) Because it is the reflected P wave at the free surface that is later reflected at the Moho to form  $SsPmp$ , the sedimentary layer reduces  $A_{VDSS}$ . In other words, the “efficiency” of the virtual source decreases due to the sedimentary basin at the virtual source. Because the dominant wavelength of the incident S wave is  $\sim 10$  km in the sedimentary layer, significantly larger than 3 and 6 km, the increase of basin thickness from 3 to 6 km does not profoundly increase the affected spectrum. Therefore,  $A_{VDSS}$  does not vary significantly when the basin deepens from 3 to 6 km (Fig. 10e).

### 3.3.2. Sedimentary-layer velocities

To test the effects of sedimentary-layer velocities on  $SsPmp$  waveforms, we vary  $V_p$  in our homogeneous basin from 4.5 km/s (high- $V_p$  case), 3.5 km/s (intermediate- $V_p$ ), to 2.5 km/s (low- $V_p$  case) (Fig. 10b). Because we hold the Poisson’s ratio constant,  $V_s$  of the basin changes accordingly. As sedimentary  $V_p$  drops, we observe a dramatic decrease in  $SsPmp$  amplitude (Fig. 10f). In the high- $V_p$  case  $SsPmp$  is still the dominant phase, whereas in the intermediate and low-

$V_p$  cases  $A_{VDSS}$  becomes so low that it is hard to distinguish it from other basin phases (Fig. 10f). Another important observation is that in the low- $V_p$  case a strong P phase arrives at  $\sim 4.5$  s,  $\sim 5$  s earlier than predicted  $T_{VDSS}$  (Fig. 10f), and could be easily misinterpreted as  $SsPmp$  due to its high amplitude. We interpret this strong P arrival as a superposition of  $SsPbp$  and  $SsbPmp$  that arrive at approximately the same time. As the velocity contrast at the basin-basement interface increases, the S-to-P reflection at the interface becomes stronger, further increasing  $SsbPmp$  amplitude. If we increase the CMB depth to 60 km, the temporal separation between  $SsPbp$  and  $SsbPmp$  will increase so that they appear as two distinct arrivals (Fig. S1), thereby supporting our interpretation that the strong P phase at  $\sim 4.5$  s in the low- $V_p$  case is the superposition of  $SsPbp$  and  $SsbPmp$ . In summary, when basin velocity is relatively low and basin thickness is large enough (dominant frequency component of the incident wave is sensitive to the basin),  $SsPbp$  and  $SsbPmp$  become the dominant P phases and can be easily misidentified as  $SsPmp$ , which may cause significant errors in Moho depths inferred from  $T_{VDSS}$ .

The above examples show that  $SsPmp$  amplitude is strongly controlled by basin velocity (Figs. 10a-f), which we interpret as a result of reduced S-to-P reflection coefficient at the virtual source in the presence of sedimentary basins. To further validate our interpretation, we calculate the maximum amplitude in a 4-s time window around the theoretical  $T_{VDSS}$  as a proxy for  $A_{VDSS}$  for models with basin  $V_s$  varied from 1.45-3.75 km/s (sedimentary-layer thickness and Poisson's ratio remain fixed at 6 km and 0.25) (Fig. 10i). We also calculate the S-to-P reflection coefficient at the free surface for a half-space (i.e. no basin) for the same  $V_s$  range and Poisson's ratio = 0.25 (Fig. 10i). A comparison of the two values shows near equivalence for  $V_s > 2.25$  km/s, suggesting the S-to-P reflection ratio is a primary control on  $A_{VDSS}$  (Fig. 10i). As  $V_s$  decreases from 2.15–2.05 km/s,  $A_{VDSS}$  drops faster than the S-to-P reflection ratio probably due to interference with other sedimentary phases, but for  $V_s < 2.05$  km/s,  $SsPmp$  amplitude again decreases at about the same rate as S-to-P reflection ratio (Fig. 10i). Other factors causing the small discrepancy between  $A_{VDSS}$  and S-to-P reflection ratio likely include transmission loss at the basin-basement interface and finite-frequency effects.

### 3.3.3. Sedimentary-layer $V_p/V_s$

To test the effects of sedimentary Poisson's ratio on  $SsPmp$  waveforms, we vary Poisson's ratio from 0.25, 0.275 to 0.3 (Fig. 9c). Increasing Poisson's ratio  $\nu$  corresponds to increasing  $V_p/V_s$  ratio as:

$$V_p/V_s = \sqrt{\frac{2(1-\nu)}{1-2\nu}} \quad (2)$$

Because we hold basin  $V_p$  constant, increasing Poisson's ratio causes basin  $V_s$ , thus S-wave incident angle, to decrease. Therefore, the amplitude of  $SsPmp$  decreases with increasing sedimentary Poisson's ratio (Fig. 10g). Although the range of Poisson's ratio used here is quite large and covers most sedimentary rocks (Brocher, 2005), the effect of basin Poisson's ratio on  $A_{VDSS}$  is quite limited (Fig 10g). Because  $T_{VDSS}$  is only related to  $V_p$  in the crust (Eq. 1), despite changes of  $A_{VDSS}$ ,  $SsPmp$  arrive at identical times in all three cases (Fig. 10g).

### 3.3.4 Sedimentary-layer velocity gradient

To test how vertical velocity gradient in sedimentary basins affects  $SsPmp$  waveforms, we compare results for a constant-velocity basin (homogeneous case) with results from a basin formed of six 1-km-thick layers with velocity linearly increasing from 2.5 km/s at the surface to 6.5 km/s at the basin-basement interface (gradient case) (Fig. 10d). Although the basins in both cases have the same average velocity, our synthetic seismograms show that  $A_{VDSS}$  is further reduced in the gradient case (Fig. 10h). This is because the multiple sub-layers strongly scatter short-wavelength components of incident  $Ss$  (both forward and backward), while the long-wavelength components of the incident S wave only respond to the average properties of the basin that are the same as in the homogeneous case. As the result of normal S-to-P reflection ratio for long-wavelength components but reduced S-to-P reflection ratio for short-wavelength components at the virtual source,  $SsPmp$  in the gradient case is depleted in high frequencies and has lower amplitude than  $SsPmp$  for the homogeneous case (Fig. 10h). Because sedimentary basins commonly have velocities increasing with depth, this example explains why in some cases observed  $A_{VDSS}$  can be even lower than  $A_{VDSS}$  predicted for homogeneous sedimentary layers.

## 3.4. Sensitivity to Lateral Heterogeneity in the Mantle

Yu et al. (2016) discussed the effects of local-scale lateral heterogeneity in the crust and the uppermost mantle (i.e. deviations from 1D Earth models) that causes travel-time differences between up-going S legs of  $SsPmp$  and  $Ss$ , thereby causing significant errors in interpretations of  $T_{VDSS}$  using 1D assumptions (Eq. 1). A simple example would be the juxtaposition of thick Archean lithosphere (>200 km) and Phanerozoic lithosphere of normal thickness (~80 km),

putatively the case at the boundaries of the Ordos Block (Fig. 4) (Yu et al., 2012). We would like to quantify the effects of such lateral heterogeneity on *SsPmp* waveforms.

We create a 2D model with a constant crustal thickness of 40 km, in order to explore only the effect of mantle heterogeneity on *SsPmp* waveforms (Fig. 11a). The lithosphere comprising both the crust and lithospheric mantle is 80-km thick at each end, and 200-km thick in the center of the model. The 200-km thick lithosphere linearly shallows to 80 km across 200 km, forming two straight ramps dipping at  $31^\circ$  (Fig. 11a). The velocity of the lithospheric mantle is  $\sim 5\%$  faster than the asthenosphere (Fischer et al., 2010). We use the SPECFEM2D software package to compute the surface-recorded seismograms of a plane S wave with ray parameter 0.1275 s/km (incident angle of  $35^\circ$  in the asthenosphere) incident on the bottom-left of the model (Komatitsch et al., 2001; Komatitsch and Vilotte, 1998; Tromp et al., 2008). Despite a constant crustal thickness in our model, the synthetic seismograms show significant variation of  $T_{VDSS}$  across the recording array (Fig. 11b). On the far left of the array, where both virtual sources and receivers are located above thin lithosphere, *SsPmp* arrives at  $\sim 6.9$  s (Fig. 11b), in agreement with the 1D prediction. When the receiver is located at the edge of the area with thick lithosphere (blue triangle in Fig. 11a), with the corresponding virtual source (blue star in Fig. 11a) above thinner lithosphere,  $T_{VDSS}$  increases to  $\sim 8$  s, significantly later than the 1D prediction (blue traces in Figs. 11b,c). In the center of the area with thick lithosphere, where receivers and corresponding virtual sources are both in areas with thick lithosphere, observed  $T_{VDSS}$  returns to the time predicted for the 1D model (black virtual source, receiver, traces in Figs. 11a-c). At the right edge of the area with thick lithosphere, where the receivers are located above thinner lithosphere than their virtual sources,  $T_{VDSS}$  rapidly decreases to  $\sim 5.5$  s, significantly earlier than the 1D prediction (red triangle, star and traces in Figs. 11a-c). If this observed  $T_{VDSS}$  is used to infer crustal thickness with an 1D assumption, the 1.5 s difference from the theoretical  $T_{VDSS}$  will cause  $\sim 9$  km error in Moho depth! The explanation for the anomalous  $T_{VDSS}$  is that when the up-going S wave leg of *Ss* travels through a velocity anomaly that is not present on the path of *SsPmp* (Fig. 11d), the travel-time difference between the two ray paths deviate from predictions made by assuming 1D Earth structure, and the residual will be included in the observed  $T_{VDSS}$ . Therefore, when applying VDSS to data collected in areas with significant variation in lithosphere thickness, it is vital to correct for S travel-time residuals before converting observed  $T_{VDSS}$  to crustal thickness. A practical approach to this correction is presented in Part 2.

Another interesting feature of our synthetic seismograms is that the  $Ss$  observed above the right margin of the thick lithosphere is significantly stronger than that observed along the rest of the profile (red traces in Figs. 11b,c). The increase in  $Ss$  amplitude cannot be due to crustal structure as it is uniform along the profile. A probable explanation is that the lithosphere ramp on the right edge of the thick lithosphere causes energy to be focused (multi-pathing effect). Note that we apply no normalization to the traces in Figs. 10b,c. If the traces are normalized with the peak  $Ss$  amplitude of each trace, a common practice in VDSS data processing, the red trace at the right edge of thick lithosphere will have a low  $A_{VDSS} = 0.83$  due to its high  $Ss$  amplitude. In contrast, the blue trace at the left edge of thick lithosphere (Fig 11a-c) will have  $A_{VDSS} = 1.23$ . Thus, lateral heterogeneity in the mantle can affect  $A_{VDSS}$ , as well as  $T_{VDSS}$ , by changing the energy distribution across the incident S wavefront.

#### 4. Discussion

The nature of  $SsPmp$  as a post-critical, thus wide-angle, reflection phase brings both advantages and disadvantages in using  $T_{VDSS}$  to infer Moho depth. A clear advantage of  $SsPmp$  compared with narrow-angle phases (e.g.  $Pms$  used in PRF) is its high amplitude, which makes it possible to constrain crustal thickness with a single record. In addition, the long ray path of  $SsPmp$  in the crust causes  $T_{VDSS}$  to have a stronger dependence on ray parameter (or higher “move-out”) than  $Pms$ , making it feasible to use the move-out of  $SsPmp$  to simultaneously constrain crustal thickness and crustal average  $V_p$  (Kang et al., 2016). In addition, given a uniform azimuthal distribution of earthquakes, it is possible to measure crustal thickness on a circle with ~60-km radius centered at the receiver, a much broader range than the CMB depth sampled by PRFs that is usually within 15 km from the receiver. Moreover, post-critical reflection causes a phase shift  $\Phi_{VDSS}$  between  $SsPmp$  and  $Ss$ , which can be used to determine  $V_p^{lc}$  and  $V_p^{um}$ , though this inference requires particularly high-quality waveform data (see Part 2).

Disadvantages of the long crustal ray path of  $SsPmp$  include its sensitivity to lateral variation over a wide area, both in basins near the surface and at mantle depths. For instance, Fig. 10 shows that sedimentary basins at virtual sources can significantly reduce  $A_{VDSS}$ , making it difficult to measure  $T_{VDSS}$ . Sedimentary basins may also generate phases ( $SsPbp$ ,  $SsbPmp$ , etc.) that are stronger than  $SsPmp$ , and can easily be misidentified as  $SsPmp$ , thus causing large errors in inferred Moho depths (Fig. 10) (though offering the ability to study basin structure). Dense 1D

or 2D arrays that cover both basins and adjacent exposed basement are key to avoiding such mistakes, because the gradual transition in waveforms allows recognition of sedimentary effects. In a second example, Fig. 11 shows the effect of heterogeneous mantle velocity structure on  $A_{VDSS}$  and  $T_{VDSS}$ , which can be partially overcome by application of “static” corrections given data collected by a dense 2D array (Yu et al., 2016). In general, future work using  $SsPmp$  to study crustal properties should leverage the power of dense arrays to alleviate challenges posed by its long ray path in the crust.

When the CMB is a transition zone,  $SsPmp$  is a turning wave with post-critical reflection at the depth where  $V_p$  reaches the critical velocity ( $1/p$ ). Because  $SsPmp$  is high amplitude even for a transitional CMB, it is possible to use  $SsPmp$  with different ray parameters, which turn at different depths, to constrain the interior structure of the CMB (Fig. 9). In contrast, conversion phases such as  $Pms$  (and pre-critical reflection phases) may be too weak to image a transitional CMB. In areas with poorly-defined or absent PRF Moho, such as the Colorado Plateau, analysis of post-critical  $SsPmp$  may reveal more details of the CMB.

The Ordos Plateau is overlain by thick west-dipping Phanerozoic strata, with the age of exposed rocks decreasing westward (Xia et al., 2017; Yang et al., 2005). The virtual source of JB09 is west of the virtual source of JB13 (Fig. 4c), so is above younger, thus likely lower-velocity sedimentary rocks. A wide age range of sedimentary rocks may also cause significant velocity gradients across the basin. These factors may explain the significantly reduced  $A_{VDSS}$  at JB09 compared to JB13. In contrast to the change in  $A_{VDSS}$  between JB09 and JB13, the change in  $\Phi_{VDSS}$  between JB13 and FY03 may have a more complicated origin. As shown in Figs. 5,6, elevated  $V_p^{lc}$  and  $V_p^{um}$  reduce  $\Phi_{VDSS}$ , and may cause  $\Phi_{VDSS} \approx 0^\circ$  at FY03. In addition, if the CMB is dipping from the virtual source towards the station, the incident angle of  $SsPmp$  at the Moho is increased, thus increasing ray parameter  $p$  and decreasing  $\Phi_{VDSS}$  (Fig. 7). Because the virtual source of FY03 is closer than station JB13 to the actively extending Shanxi Graben System (Fig 4a), the crust at the virtual source is likely thinner than at the station, causing a dipping CMB that may also contribute to the very small  $\Phi_{VDSS}$  at FY03. Quantitative analysis of change in  $A_{VDSS}$  and  $\Phi_{VDSS}$  across the Ordos Plateau is beyond the scope of this paper and will be presented in detail in Part 2.

## 5. Conclusion

Using synthetic seismograms, we find that  $\Phi_{VDSS}$  is negatively related to  $V_p^{lc}$ ,  $V_p^{um}$  and  $p$ , making it possible to constrain  $V_p^{lc}$  and  $V_p^{um}$  with observed *SsPmp* waveforms.  $A_{VDSS}$  is insensitive to CMB thickness but is strongly affected by near-surface velocity at the virtual source. If the CMB is a velocity gradient zone, *SsPmp* is a turning wave within the CMB, with turning depth determined by the ray parameter, thereby offering the potential to image the CMB in areas where methods based on conversion and pre-critical reflection phases fail to show a clear Moho. We also show that  $T_{VDSS}$  is affected not only by crustal thickness, but also by crustal and upper-mantle heterogeneity, which require array data for proper analysis.

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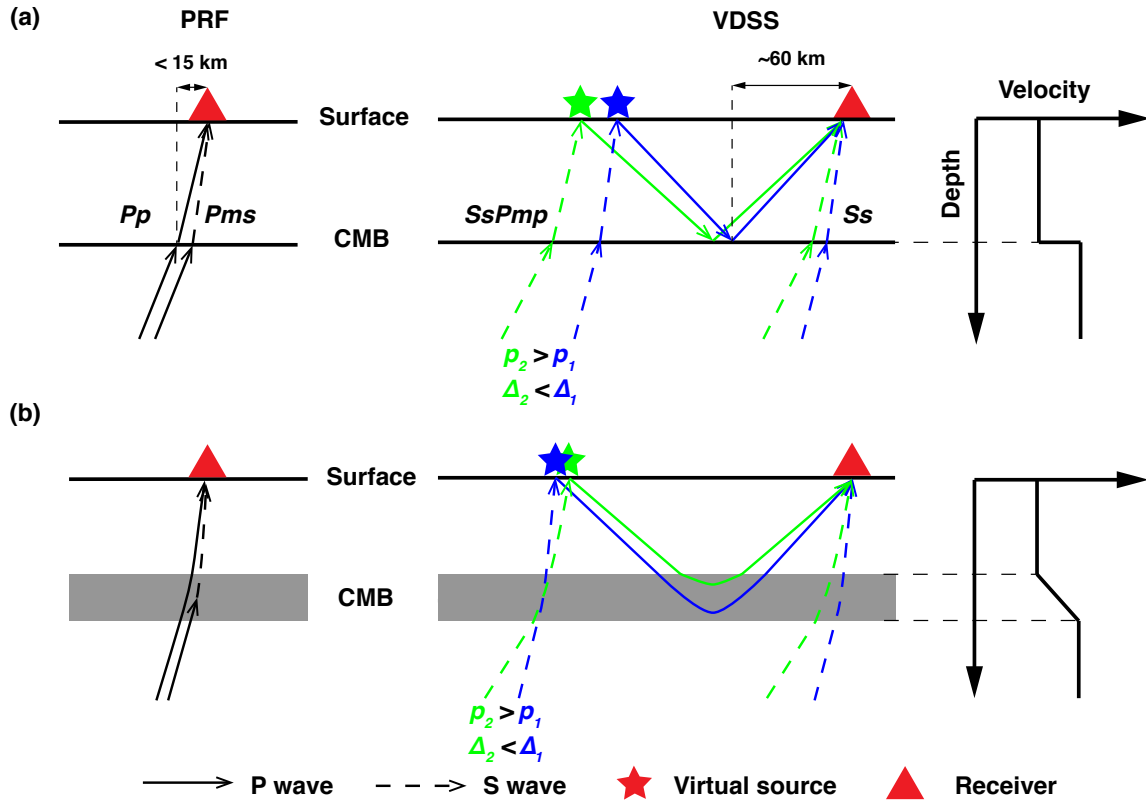


Figure 1. Comparison between ray paths for P receiver functions (PRF; left column) and Virtual Deep Seismic Sounding (VDSS; right column) (a) for an abrupt velocity discontinuity at the crust-mantle boundary (CMB) and (b) for a velocity gradient zone at the CMB. For VDSS, blue and green rays and virtual sources are from earthquakes with epicentral distance  $\Delta_1 > \Delta_2$  and ray parameter  $p_1 < p_2$ .

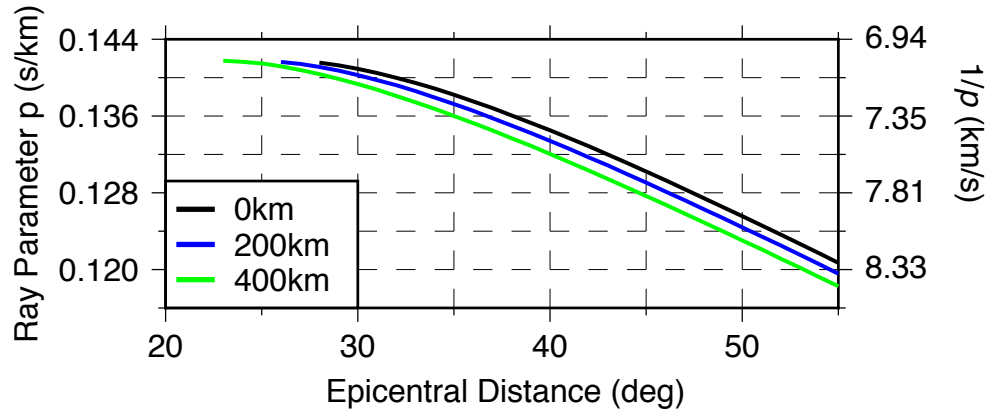


Figure 2. Ray parameters of teleseismic S waves ( $S_s$ ) and corresponding  $S_sPmp$  as functions of epicentral distance and focal depth, calculated using the IASP91 model. Note the ray parameter does not exceed 0.143 s/km due to triplication at the bottom of the mantle transition zone.

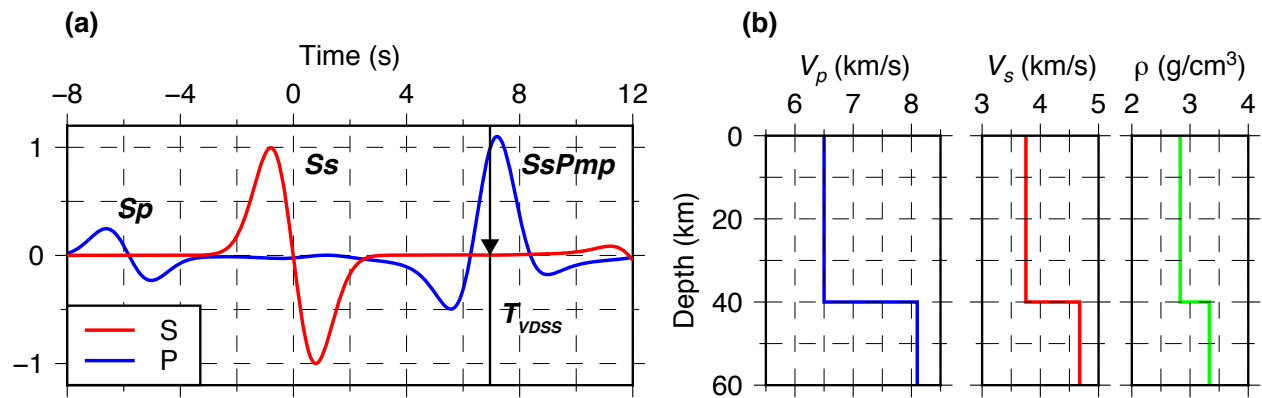


Figure 3. (a): P and S components of the synthetic waveforms computed using the models in (b) and aligned to *Ss* arrival. Ray parameter of the incident S wave is  $p = 0.127$  s/km ( $1/p=7.87$  km/s). The source time function has a dominant frequency of  $\sim 0.25$  Hz. The *Ss* arrival is picked at the zero-crossing of the source wavelet, the peak of the envelope function. Black inverted triangle: *SsPmp* arrival time relative to *Ss* ( $T_{VDSS}$ ) predicted with ray theory. Large amplitude and phase shift of *SsPmp* are due to post-critical reflection at the Moho. (b): 1D velocity and density model of a homogeneous crust over a half-space mantle that are used to compute waveforms in (a).

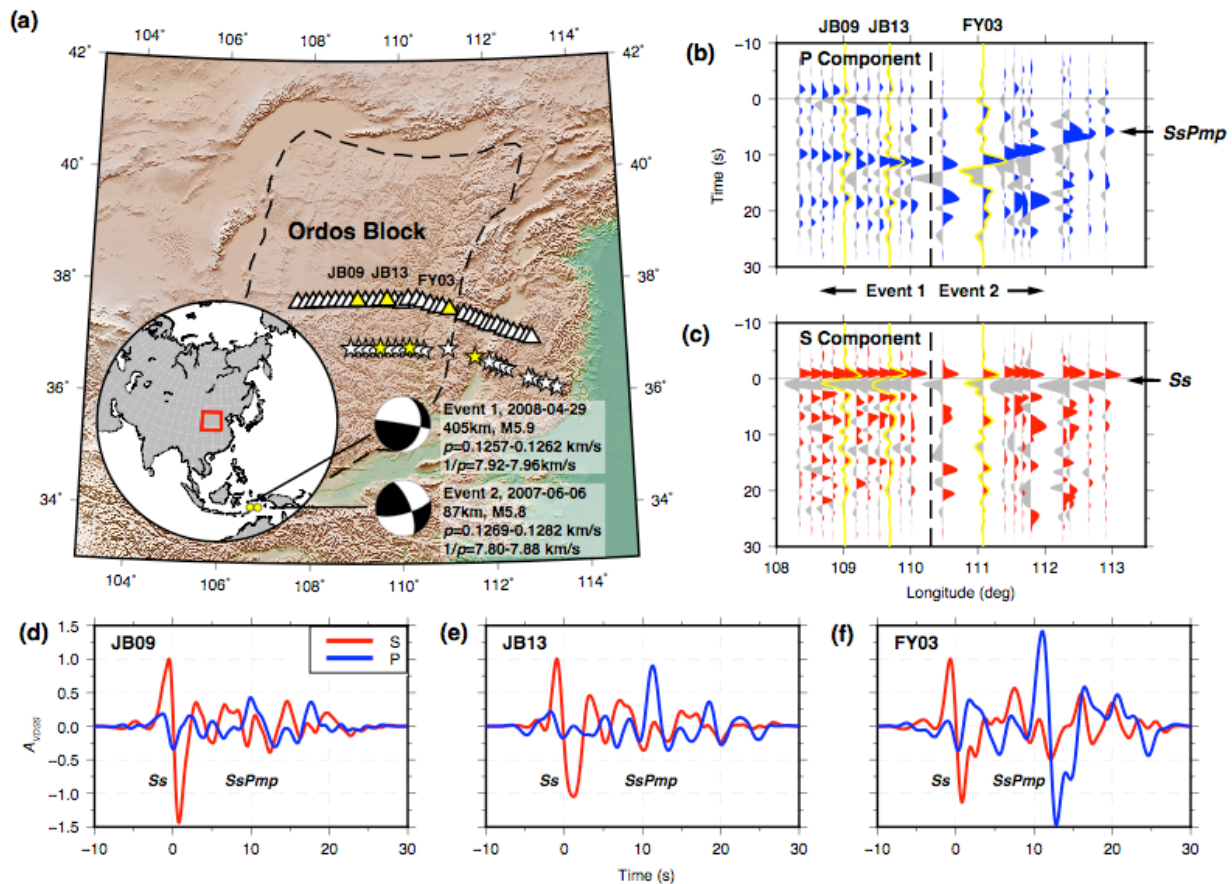


Figure 4.  $SsPmp$  observations from the Ordos plateau, North China. (a): Geometry of the dataset. Triangles: stations. Stars: virtual sources calculated for a crustal thickness of 40 km and  $V_p = 6.3$  km/s. The range of ray parameters ( $\rho$ ) are for the entire array shown on the map. Yellow triangles and stars correspond to yellow-highlighted traces in (c) and (d). Inset map marks the station map; yellow circles are the epicenters of the two earthquakes. (b) and (c):  $Ss$  phase from two deep-focus Banda Sea earthquakes recorded by the broadband array shown in (c). Blue and red wiggles: P and S-component waveforms respectively aligned to  $Ss$  arrival time (0s, picked at the zero-crossing) and normalized by the maximum positive amplitude of  $Ss$ . Dashed vertical lines separate the two events shown in (c). The traces highlighted with yellow are recorded at yellow triangles in (a). (d-f): Waveforms recorded at JB09, JB13 and FY03. Blue and red: P and S-components waveforms respectively aligned to  $Ss$  arrival time and normalized by the maximum positive amplitude of  $Ss$ . Note the  $\sim$ factor-of-two difference in  $A_{VDSS}$  between JB09 and JB13, and the difference in  $\Phi_{VDSS}$  between JB13 ( $\sim 90^\circ$  phase shift from  $Ss$ ) and FY03 ( $\sim 0^\circ$  phase shift).

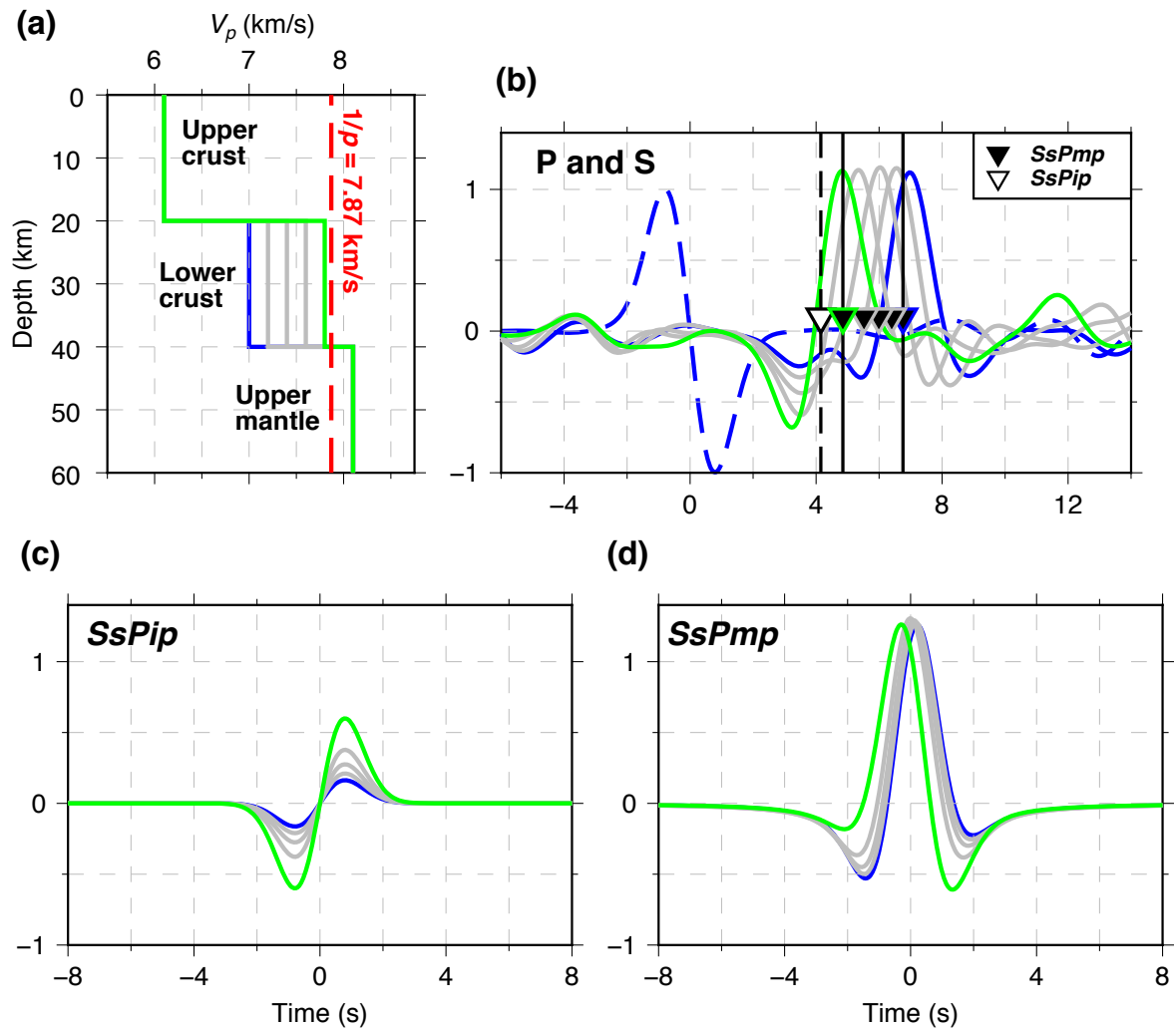


Figure 5. *SsPmp* waveforms computed for ray parameter  $p = 0.127$  s/km and  $V_p^{lc}$  ranging from 7.0–7.8 km/s. (a):  $V_p$  models used to compute the *SsPmp* synthetic seismograms. Blue:  $V_p^{lc} = 7.0$  km/s. Green:  $V_p^{lc} = 7.8$  km/s. Gray: intermediate models. Red dashed line: critical  $V_p$  of incident wave ( $1/p = 7.87$  km/s). (b): Blue, gray and green curves: P-component synthetic seismograms colored as in (a). Dashed blue curve: S-component synthetic seismogram computed with  $V_p^{lc} = 7.0$  km/s. Black inverted triangles with blue, gray and green edges: ray-theory-predicted  $T_{VDSS}$  of models in (a) colored as in (a). Open inverted triangle: ray-theory-predicted arrival time of the pre-critical reflection phase at the top of the lower crust (*SsPip*), constant for all models. Vertical solid and dashed lines: ray-theory-predicted arrival times of *SsPip* and *SsPmp* ( $V_p^{lc} = 7.0$  and 7.8 km/s). (c) and (d): *SsPip* and *SsPmp* waveforms respectively, colored as in (b), aligned on their ray-theory-predicted arrival times.

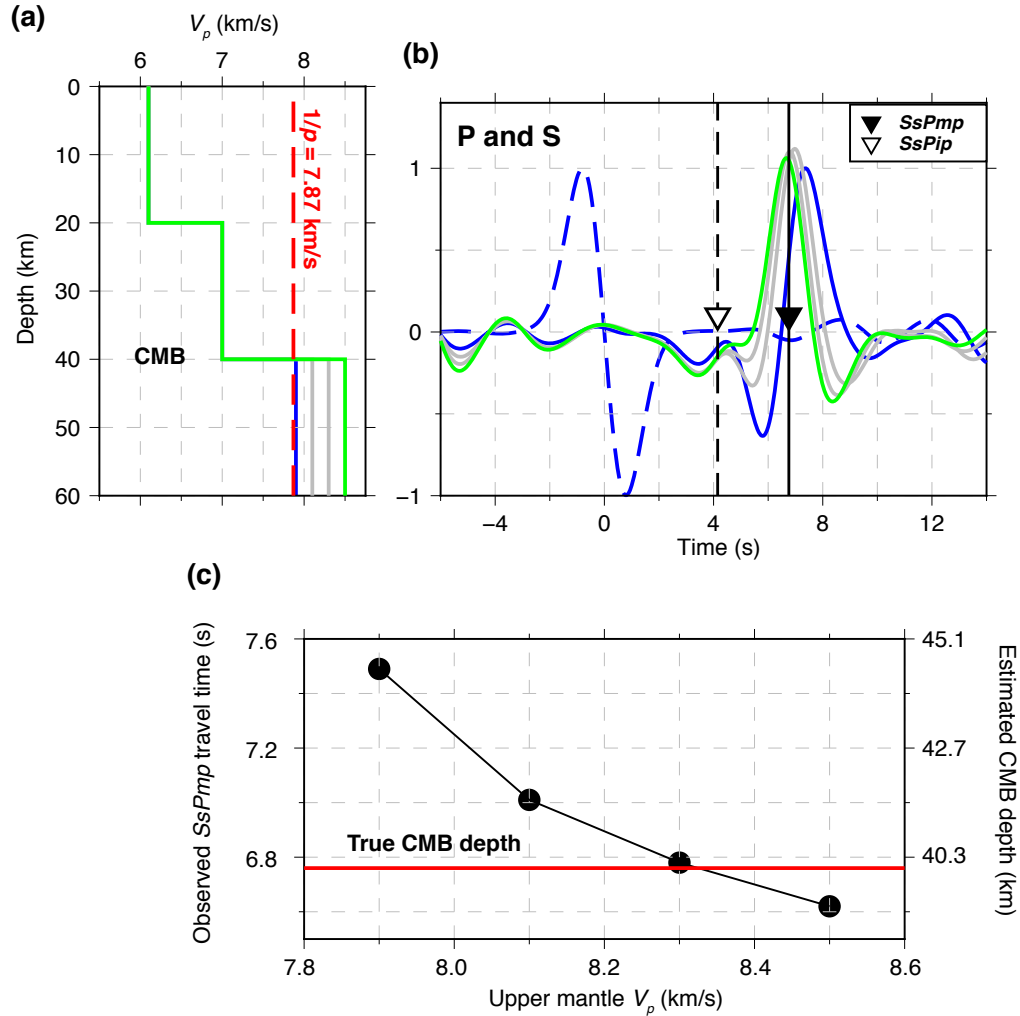


Figure 6. *SsPmp* waveforms for  $7.9 \leq V_p^{um} \leq 8.5$  km/s. (a):  $V_p$  models. Blue:  $V_p^{um} = 7.9$  km/s. Green:  $V_p^{um} = 8.5$  km/s. Gray: intermediate models. Red dashed line: critical  $V_p$  of the incident wave ( $1/p = 7.87$  km/s). (b): Blue, gray and green curves: P-component synthetic seismograms colored as in (a). Dashed blue curve: S-component synthetic seismogram for  $V_p^{um} = 7.9$  km/s. Black (and open) inverted triangles: theoretical  $T_{VDSS}$ , (and  $T_{SsPip}$ ), constant for all models. (c): Observed  $T_{VDSS}$  and estimated Moho depth for waveforms in (b) assuming a  $90^\circ$  phase shift of *SsPmp* relative to *Ss*. The observed  $T_{VDSS}$  are found by cross-correlating the  $90^\circ$ -phase-shifted wavelet with the waveforms in (b). The estimated Moho depths are derived from observed  $T_{VDSS}$  using Eq. 1 and the true average crustal  $V_p$  of the models. Red line: true CMB depth of 40 km.



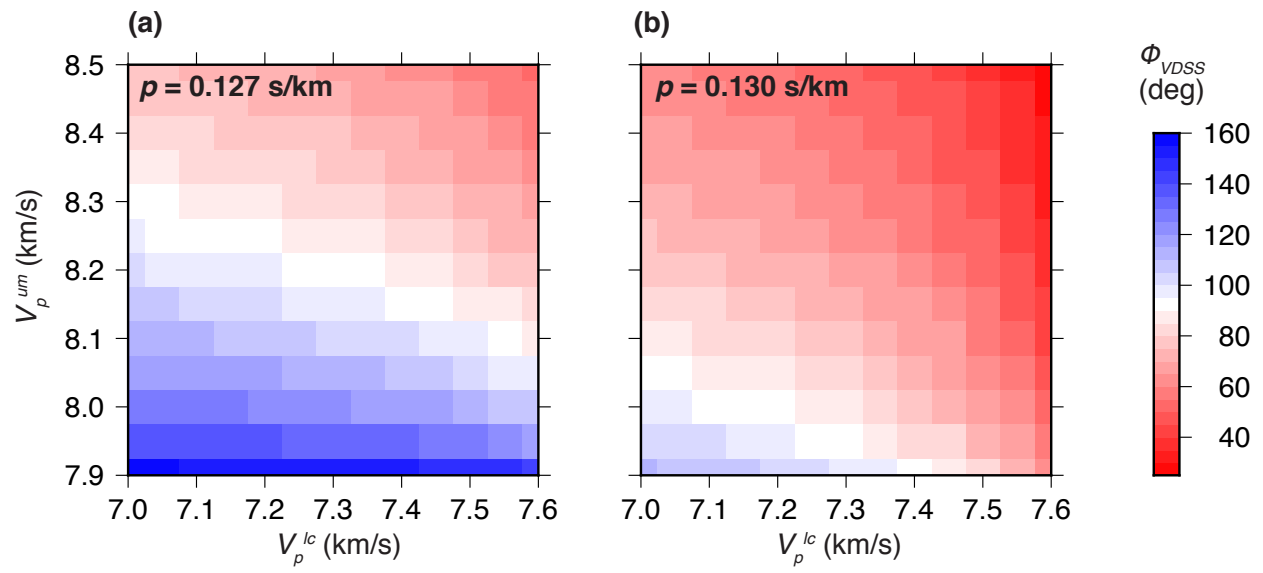


Figure 7.  $\Phi_{VDSS}$  as a function of  $V_p^{lc}$  and  $V_p^{um}$  for two different  $p$ . The  $V_s$  and densities are varied to keep a constant Poisson's Ratio of 0.25, and to satisfy the Nafe-Drake relation (Brocher, 2005). (a)  $\Phi_{VDSS}$  as a function of  $V_p^{lc}$  and  $V_p^{um}$  when  $p = 0.127$  s/km. (b)  $\Phi_{VDSS}$  as a function of  $V_p^{lc}$  and  $V_p^{um}$  when  $p = 0.130$  s/km. Note that when  $p = 0.127$  s/km  $\Phi_{VDSS}$  is primarily controlled by  $V_p^{um}$ , whereas when  $p = 0.130$  s/km  $\Phi_{VDSS}$  is affected by both  $V_p^{lc}$  and  $V_p^{um}$ .

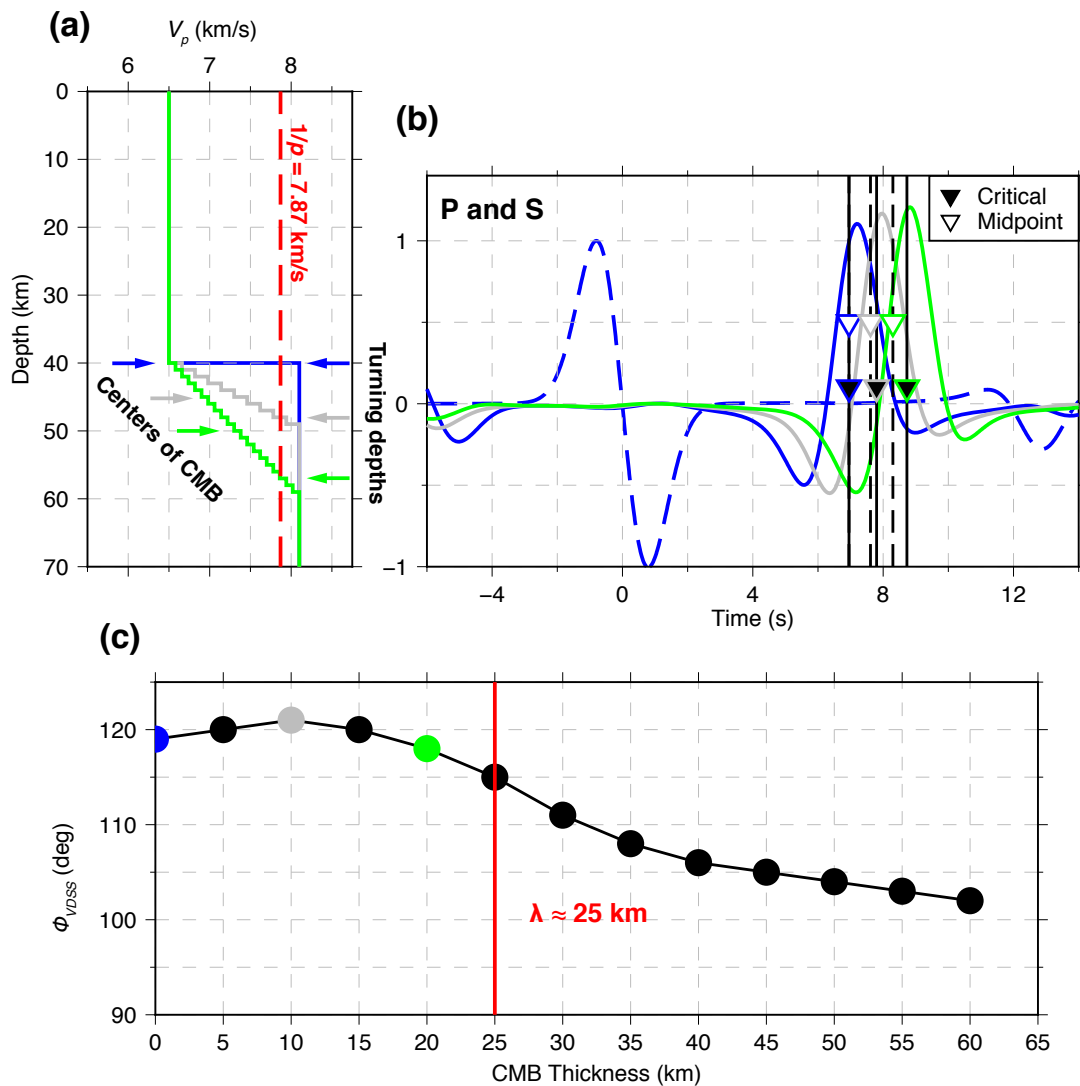


Figure 8. *SsPmp* waveforms for a CMB thickness of 0 (velocity discontinuity), 10 and 20 km. (a)  $V_p$  models. Blue: CMB as a velocity discontinuity at 40-km depth. Grey: 10-km thick CMB. Green: 20-km thick CMB. Red dashed line: critical  $V_p$  of the incident wave ( $1/p = 7.87$  km/s). (b) Blue, grey and green curves: P-component synthetic seismograms colored as in (a). Dashed blue curve: S-component synthetic seismogram computed with the discontinuous CMB model plotted for reference. Black inverted triangles with blue, grey and green edges: theoretical  $T_{VDSS}$  of the models colored as in (a), calculated for the depths at which  $V_p = 7.87$  km/s, i.e. at which  $V_p$  equals the critical velocity (the reciprocal ray parameter). Open inverted triangles with blue, grey and green edges: theoretical  $T_{VDSS}$  of the models colored as in (a), calculated for the depths to the center of the CMB. (c)  $\phi_{VDSS}$  as a function of CMB thickness.  $V_p$  at the top and bottom of the CMB are fixed at 6.5 and 8.1 km/s. Blue, gray and green circles: models colored as in (a). Red line: dominant wavelength  $\lambda$  of P waves with dominant frequency 0.25 Hz in the CMB. Note that as CMB thickness becomes larger than  $\lambda$ ,  $\phi_{VDSS}$  deviates significantly from the value with a velocity discontinuity.

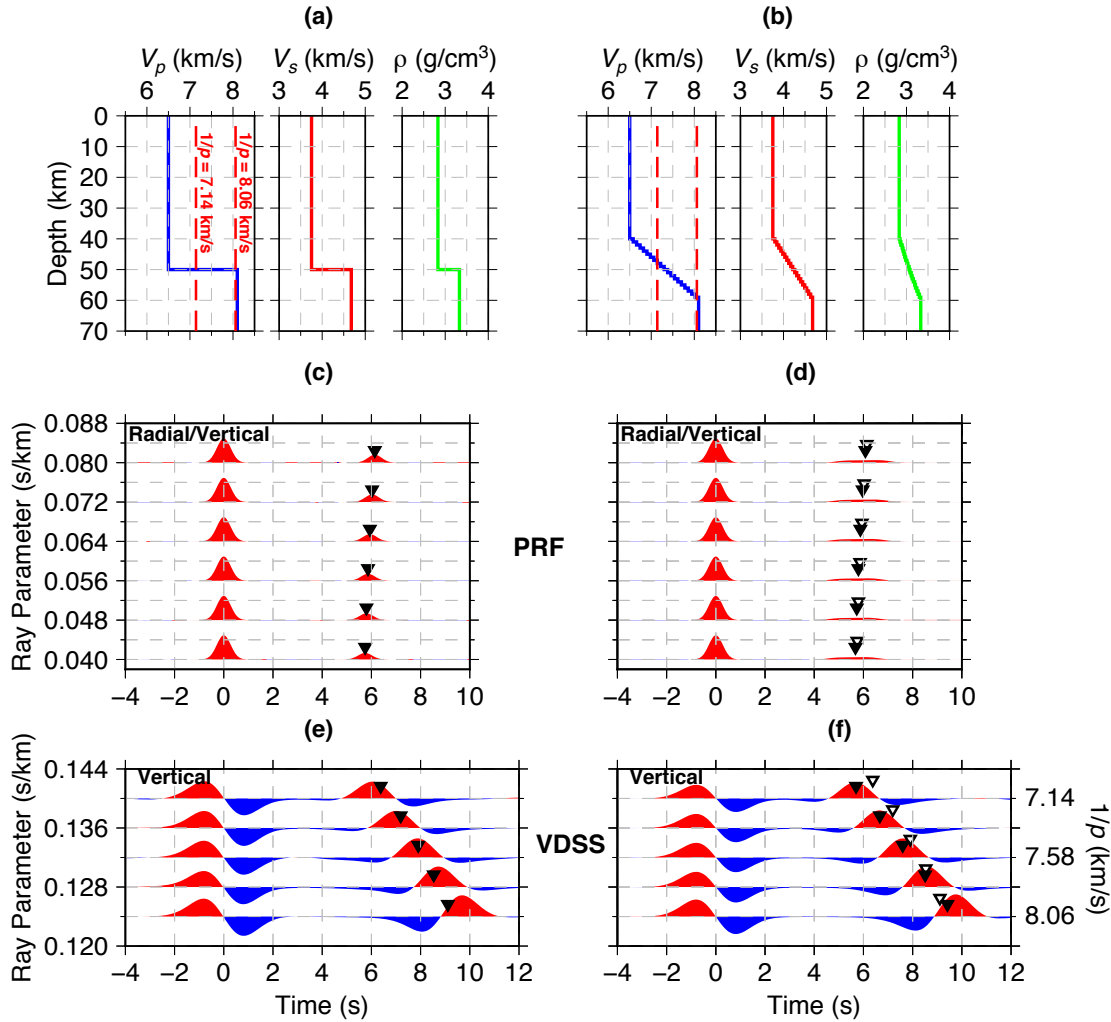


Figure 9. Synthetic RF and  $SsPmp$  waveforms with different ray parameters for different CMB thicknesses but the same total velocity change across the CMB. (a) and (b): 1D Models in which the CMB is represented by either a discontinuity in  $V_p$ ,  $V_s$  and density, or by a 20-km thick transition zone. (c) and (d): Synthetic PRFs (radial components deconvolved by vertical components) computed with the models in (a) and (b), respectively, and ray parameters ranging from 0.04-0.08 s/km. Black inverted triangles are theoretical  $Pms$  travel times for a conversion depth at 50 km, i.e. at the abrupt discontinuity (model a) or at the center of the transition zone (model b). Open triangles in (d) show the theoretical arrival times in model a, offset vertically to be visible. (e) and (f): Vertical-component synthetic  $SsPmp$  waveforms computed with model a and b respectively, and ray parameters ranging from 0.124-0.140 s/km. The corresponding turning velocities ( $1/p$ ) are labeled on the right. Black inverted triangles in (e) are theoretical  $T_{VDSS}$  for reflections at the discontinuity, and in (f) are theoretical  $T_{VDSS}$  computed for reflections at the depth where  $V_p = 1/p$ . Open inverted triangles in (f) show  $T_{VDSS}$  in (e), offset vertically to be visible. Note that theoretical  $T_{VDSS}$  in (e) and (f) form distinct move-out curves with respect to  $p$ , and that  $\Phi_{VDSS}$  varies with  $p$

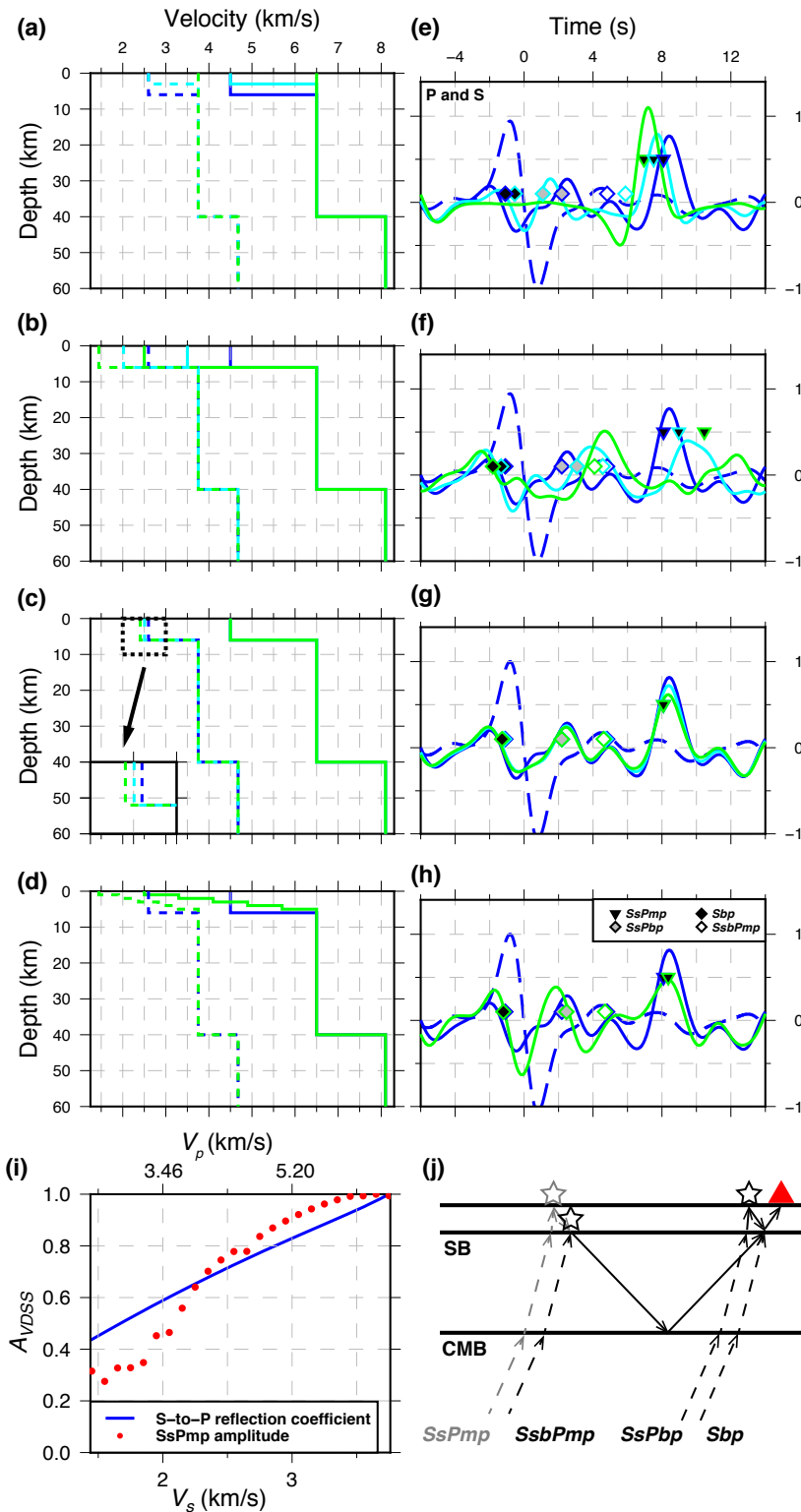


Figure 10. *SsPmp* waveforms for different sedimentary basins on top of the same crust with 40-km-deep Moho. (a), (b), (c) and (d):  $V_p$  (solid lines) and  $V_s$  (dashed lines) models of simple sedimentary basins. Blue lines in each part: our 'standard model', a 6-km thick sedimentary layer ( $V_p = 4.5$  km/s) above basement ( $V_p = 6.5$  km/s) and a CMB discontinuity at 40 km depth above  $V_p^{um} = 8.1$  km/s; Poisson's ratio = 0.25. In (a) we vary sedimentary thickness between 6 km (blue), 3 km (cyan), and 0 km (no sedimentary layer, green). In (b) we vary sedimentary  $V_p$  between 4.5 km/s (blue), 3.5 km/s (cyan) and 2.5 km/s (green);  $V_s$  is also varied to keep Poisson's ratio at 0.25. In (c) we vary sedimentary Poisson's ratio between 0.25 (blue), 0.275 (cyan), and 0.3 (green), while keeping the sedimentary  $V_p$  at 4.5 km/s (The inset figure shows the zoom-in plot of  $V_s$  in the basin). In (d), we vary the velocity gradient in the sedimentary basin between a constant velocity (blue) and a stack of six 1-km thick layers with  $V_p$  linearly increasing with depth from 1.5-6.5 km/s (green). (e), (f), (g), and (h): Solid curves: P-component synthetic seismograms for velocity models (a), (b), (c) and (d) respectively, and colored as in these velocity models. Dashed blue curves: S-component synthetic seismograms for standard model. Black inverted triangles with edges colored corresponding to the velocity models mark theoretical  $T_{VDSS}$ . Black, gray and white diamonds with edges colored corresponding to the velocity models mark theoretical arrival times of  $Sbp$ ,  $SsPbp$ , and  $SsbPmp$ . (i): Effects of sedimentary basin on  $A_{VDSS}$ . Red circles: maximum amplitude in a 4-s time window around the theoretical  $T_{VDSS}$  as a proxy for  $A_{VDSS}$  for models with sedimentary  $V_s$  ranging from 1.45-3.75 km/s (basin thickness and Poisson's ratio are fixed at 6 km and 0.25). Blue curve: S-to-P reflection ratio at the free surface for a half-space (i.e. no basin) for the same  $V_s$  range and Poisson's ratio = 0.25. Both the red circles and blue curve are normalized with their maximum values for the convenience of plotting. The corresponding sedimentary  $V_p$  are plotted on the top. (j): Ray paths of  $SsPmp$ ,  $SsbPmp$ ,  $SsPbp$  and  $Sbp$ .

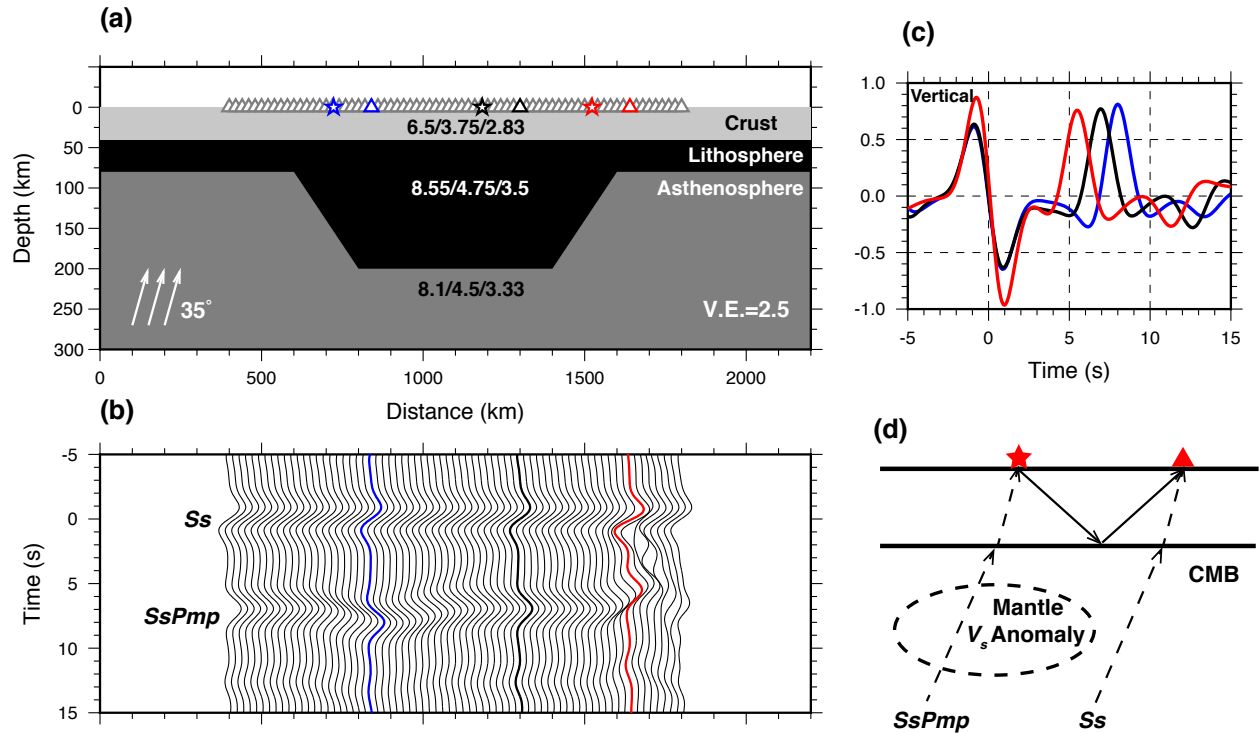


Figure 11. Effects of lateral variation in mantle  $V_s$  on  $T_{VDSS}$ . (a): 2D model used to compute synthetic seismograms, with a vertical exaggeration of 2.5. Light gray: crust. Black: lithospheric mantle. Dark gray: asthenosphere. Material properties of model layers are listed as  $V_p$  (km/s)/ $V_s$  (km/s)/ $\rho$  (g/cm<sup>3</sup>). Incident angle of the plane S wave is 35°, and the dip of the lithosphere-asthenosphere boundary is 31°. The seismograms of the stations highlighted with blue, black and red are shown in (b) and (c). Stars show the virtual sources of the stations highlighted with the same colors. (b): Vertical-component synthetic seismograms recorded by stations in (a). Black, blue and red traces: traces recorded by highlighted stations in (a) and colored accordingly. Note the significant lateral variation of  $T_{VDSS}$  despite homogeneous crustal thickness. (c): Vertical-component synthetic seismograms recorded by highlighted stations in (a) and colored accordingly. (d): Schematic showing  $V_s$  anomaly in the mantle affects  $T_{VDSS}$  by changing the relative travel times of Ss and the S legs of SsPmp.

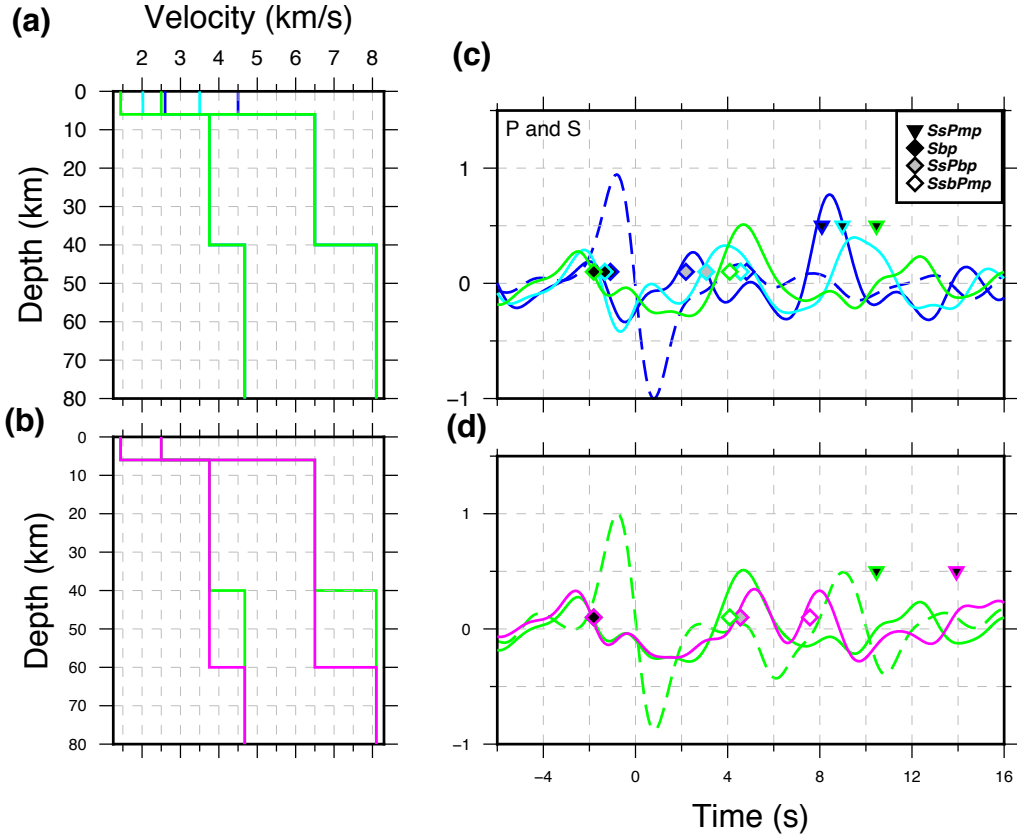


Figure S1. (a): The same as Fig. 8b. (b):  $V_p$  and  $V_s$  models with the same sedimentary layer thickness (6 km),  $V_p$  (4.5 km/s) and Poisson's ratio (0.25), but with Moho thickness varied between 40 km (green curve) and 60 km (magenta curve). The green model is the same as the green one in (a). (c): The same as Fig. 8f. (d): Solid curves: P-component synthetic waveforms calculated from velocity models in (b) and colored as in (b). Dashed green curves: S-component synthetic seismograms computed with the green model in (b).