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ABSTRACT

Conventional topographic terms in ground motion models (GMMs) typically characterize topographic effects using site-specific parameters such as relative elevation, curvature, or slope. This study demonstrates that topographic response is influenced by source-to-site geometry, specifically the incidence direction with respect to the slope aspect. Utilizing 15,189 records from 641 Kiban–Kyoshin network (KiK-net) stations in Japan, we analyze the corrected within-event residuals from which path, source, and site effects are eliminated. We introduce the azimuthal difference (α) between slope aspect and epicentral direction alongside the relative elevation (h_r) to capture the directional influences of incoming seismic waves on topographic response. Our empirical findings reveal that topographic effects (amplification or deamplification) are determined by the interplay between h_r and α , where facing slopes ($\alpha = 0^\circ$) at ridges exhibit maximum amplification, while back slopes ($\alpha = 180^\circ$) can induce deamplification. These responses exhibit a period-dependence, appearing prominently at short-to-intermediate periods ($T \leq 0.3$ s) where the seismic wavelength is comparable to the topographic scale, but diminishing at longer periods as the wavelength exceeds the topographic scale. By parameterizing this azimuthal dependence into a topographic term (f_{topo}), the model effectively reduces the standard deviation of the residuals.

1. INTRODUCTION

Topographic effects refer to the amplification or deamplification of ground motions due to

30 the geometric characteristics of irregular terrain. It is particularly well known that ground
31 motions are predominantly amplified at sites located on convex terrains, such as ridges, crests,
32 and hills, relative to the surrounding area. These effects have been empirically documented
33 over several decades through numerous field observations. Early instrumental evidence was
34 captured during the 1971 San Fernando earthquake and its subsequent aftershocks, where
35 pronounced amplification was recorded at the Pacoima Dam and several Californian mountain
36 crests (Davis & West, 1973; Perez, 1973). Similar observations were subsequently reported
37 worldwide, including Osakayama Hill in Japan (Nishimura & Morii, 1984), Canal Beagle in
38 Chile (Çelebi, 1987), and Robinwood Ridge in California (Hartzell *et al.*, 1994). More
39 catastrophic evidence emerged from the 1994 Northridge earthquake, where extreme
40 topographic amplification contributed to severe structural failure at the Tarzana station in
41 California, USA (Spudich *et al.*, 1996), and more recently, at the IBRH11 station in Japan
42 during the 2011 Tohoku earthquake (Sato *et al.*, 2014). Contemporary studies continue to
43 report such topographic effects across diverse regions and geometries, including Tarzana Hill
44 in California, USA (Graizer, 2009); Little Red Hill in New Zealand (Buech *et al.*, 2010); Narni
45 Village in Italy (Massa *et al.*, 2010); Mt. Dong in China (Luo *et al.*, 2020); Gokgang-ri in South
46 Korea (Kang *et al.*, 2019); and embankments of reservoirs in South Korea (Lee *et al.*, 2025).

47 Beyond empirical observations, numerical simulations have been extensively employed to
48 identify the controlling parameters of topographic amplification. Bouchon and Barker (1996)
49 examined the topographic amplification in the frequency range from 2 to 15 Hz at Tarzana hill
50 in California, USA. Paolucci (2002) compared two-dimensional (2D) and three-dimensional
51 (3D) topographic effects at various sites in Italy. Assimaki *et al.* (2005) parameterized various
52 factors such as the dominant frequency of input motion, the bedrock-soil impedance ratio, the
53 depth-to-bedrock ratio, and the relative thickness and flexibility of a surface layer to explain
54 topographic effects in Athens, Greece. Lee *et al.* (2009) investigated peak ground acceleration
55 (PGA) amplification considering variations in source frequency, source depth, wave-field type,
56 and subsurface models in the Yangminshan region of Taiwan. Assimaki and Jeong (2013)
57 conducted a parametric study on surface soil stiffness, soil thickness, and soil–bedrock
58 impedance, inspired by the observations from the 2010 Haiti earthquake. Maufroy *et al.* (2015)
59 introduced parameters such as the curvature smoothing range and the S-wave wavelength to
60 evaluate topographic effects. Mohammadi and Asimaki (2017) analyzed the soil–topography
61 coupling effects by parameterizing slope height, slope depth, thickness of surface layer, and
62 shear wave velocity. Luo *et al.* (2020) evaluated the influence of stratigraphy and topography

63 by modeling 2D and 3D representations of Mt. Dong in China with various subsurface
64 structures. Li *et al.* (2022) investigated topographic amplification on slopes by considering soil
65 type, slope height, slope angle, and the peak acceleration of input motion. Fang *et al.* (2023)
66 examined the influence of soil property on topographic effects. Furthermore, several studies
67 have proposed predictive models for topographic effects based on surface geometry parameters
68 such as the relative elevation (h_r), curvature, and slope angle (Kim *et al.*, 2024; Park *et al.*,
69 2022; Rai *et al.*, 2017; Rai *et al.*, 2016). While these frameworks have demonstrated a
70 significant correlation between site-specific parameters and topographic effects, they have
71 primarily treated these responses as site-specific stationary properties, overlooking the
72 azimuthal interaction between the incoming wavefield and terrain geometry. Consequently,
73 there remains a lack of empirical evaluations that incorporate the seismic incidence direction
74 as a predictive variable alongside conventional site-specific parameters.

75 This azimuthal dependence originates from the complex interaction between the incident
76 wavefield and the three-dimensional terrain geometry, where the ground motion is significantly
77 modulated by the slope orientation relative to the source. The seismic wavefield can be altered
78 depending on whether the slope aspect is oriented toward or away from the source. This
79 directional effect is empirically supported by observations from the 2017 Pohang earthquake,
80 where Kang *et al.* (2019) reported that structures located on slopes facing the epicenter
81 sustained severe damage compared to those on the back slopes. Based on these observations,
82 Lee *et al.* (2026) demonstrated that ground motion amplification is modulated by the combined
83 effects of relative elevation (h_r) and the azimuthal difference between slope aspect and
84 epicentral direction (α), using localized data from Pohang, South Korea. Their results showed
85 that for $\alpha < 90^\circ$ (i.e., the slope facing the epicenter) ground motions were deamplified when h_r
86 < -18 m and amplified when $h_r > 14$ m. In contrast, for $\alpha > 90^\circ$ (i.e., the slope facing away
87 from the epicenter) ground motions were deamplified when $h_r > 14$ m. However, their findings
88 remain constrained to small-scale topographic environments, localized micro-earthquakes (i.e.,
89 local magnitude ranging from -1.1 to 1.7), with pronounced effects observed only in the short-
90 period range of 0.01 – 0.1 s, leaving the generalizability of this directional effect unresolved.
91 This direction-dependent topographic behavior has not yet been sufficiently incorporated into
92 existing GMMs, due to the scarcity of empirical quantifications across diverse topographic
93 scales and periods.

94 Motivated by the need to examine the generality of the azimuth-dependent topographic

95 effects reported by Lee et al. (2026), this study investigates the variability of ground motion
96 response throughout Japan. Unlike that study, which was limited to a localized topographic
97 environment and a relatively small topographic scale, this study considers diverse and large-
98 scale topographic configurations and evaluates the azimuth-dependent topographic effects by
99 jointly considering h_r and α . To evaluate these topographic effects in Japan, we utilize the
100 Kiban-Kyoshin Network (KiK-net) dataset compiled by Dawood *et al.* (2016), which provides
101 a comprehensive collection of seismic metadata and spectral accelerations across a range of
102 periods. To systematically isolate topographic effects, we first account for the source and path
103 effects by employing the reference GMM derived by Kotha *et al.* (2018), which incorporates
104 moment magnitude (M) and the Joyner–Boore distance (R_{JB}). Subsequently, we partition the
105 residuals into between-event and within-event residuals and eliminate the site effect governed
106 by the time-averaged shear wave velocity in the upper 30 m (V_{S30}) from the within-event
107 residuals. The remaining residuals are analyzed with respect to topographic parameters (h_r and
108 α). These parameters were derived from a Digital Elevation Model (DEM) using ArcGIS, as
109 described in the section “Topographic parameters”. Finally, we develop a comprehensive
110 GMM that incorporates a novel topographic term dependent on both h_r and α , alongside path,
111 source, and site effects.

112 2. DATA

113 2.1. Ground motions in Japan

114 Dawood et al. (2016) compiled a comprehensive dataset that includes earthquake
115 magnitude and location, station location, V_{S30} , source-to-station distance, and pseudo spectral
116 acceleration (PSA) at various periods (i.e., $T = 0.01\text{--}10$ s), etc. The data selection process
117 followed the five criteria outlined by Kotha et al. (2018) to ensure the inclusion of high-quality
118 records: 1) Category A, representing the strictest error margin; 2) Active Shallow Crustal events
119 (ACRsh); 3) focal depth ≤ 35 km; 4) surface recordings with measured V_{S30} available; and 5)
120 all six-component (two horizontal and one vertical components at both borehole and surface)
121 of ground motions with signal-to-noise ratio (SNR) ≥ 3 within a frequency bandwidth range
122 from high-pass corner frequency (f_c) to 30 Hz. The initial dataset of approximately 157,000
123 records was reduced to 15,189 records through the data selection process. The final dataset
124 utilized in this study is illustrated in Figure 1, which shows the locations of 641 stations and
125 the magnitudes and epicenters of 838 events. As summarized in Figure 2(a–d), the selected

126 15,189 records span R_{JB} values from 0 to 600 km. The 838 events have focal depth ranging
 127 from 5 to 35 km and M ranging from 3.4 to 6.9. The stations have V_{S30} values ranging from
 128 106 to 2,100 m/s.

129 2.2. Topographic parameters

130 We utilized a Digital Elevation Model (DEM) with a 1 arc-second (~30 m) spatial
 131 resolution from the Shuttle Radar Topography Mission (SRTM), provided by the United
 132 States Geological Survey (USGS). Two primary topographic parameters were derived using
 133 ArcGIS: relative elevation (h_r) and azimuthal difference between slope aspect and epicentral
 134 direction (α).

135 h_r quantitatively indicates the difference between the elevation of a station and its
 136 surrounding mean elevation (h_{mean}). To account for the multiscale nature of topography, h_r was
 137 calculated using different search radii. For a given radius, h_r^{radius} is defined as the difference
 138 between the station elevation (h) and the mean elevation within that radius (h_{mean}^{radius}) in meters:

$$h_r^{radius} = h - h_{mean}^{radius} \quad (1)$$

139 A positive h_r indicates convex regions such as ridges, whereas a negative h_r indicates concave
 140 regions such as valleys. Figure 3(a and b) shows a satellite image and elevation map of Japan,
 141 respectively. Figure 3(c and d) shows an example of a mean elevation within a radius of 1,000
 142 m (h_{mean}^{1000}) and a relative elevation at a 1,000 m-scale (h_r^{1000}), respectively.

143 To account for the azimuthal dependence of the topographic effects, we introduced α , which
 144 represents the angular difference between the azimuth of the slope aspect (ϕ_{slope}) and the
 145 station-to-source azimuth (ϕ_{epi}). Both azimuths are measured in degrees clockwise from North.
 146 Specifically, α was constrained to range from 0° to 180° , where $\alpha = 0^\circ$ indicates that the slope
 147 faces toward the epicenter (facing slope), whereas $\alpha = 180^\circ$ indicates that the slope faces away
 148 from the epicenter (back slope). Furthermore, to reflect the topographic scale of the terrain
 149 geometry, we computed the smoothed α (α^{radius}) using the ϕ_{slope} derived from the mean
 150 elevation for a specified radius (ϕ_{slope}^{radius}) as follows:

$$\alpha^{radius} = \begin{cases} |\phi_{slope}^{radius} - \phi_{epi}| & \text{if } |\phi_{slope}^{radius} - \phi_{epi}| \leq 180^\circ \\ 360^\circ - |\phi_{slope}^{radius} - \phi_{epi}| & \text{if } |\phi_{slope}^{radius} - \phi_{epi}| > 180^\circ \end{cases} \quad (2)$$

151 Here, α for ϕ_{slope} derived from the native-resolution DEM is denoted as α^{DEM} . Figure 3(e and f)
 152 shows examples of the native-scale ϕ_{slope} and α^{DEM} .

153 The distributions of the topographic parameters are shown in Figure 2. Figure 2(e) shows
 154 that most of the 641 KiK-net stations are concentrated at relatively low elevations, particularly
 155 below approximately 300 m. Similarly, the distribution of h_r^{1000} , as shown in Figure 2(f), is
 156 concentrated near zero with a slight tendency toward negative, showing that most sites are not
 157 on hilltops or ridges. Figure 2(g and h) illustrates the distributions of ϕ_{epi} and ϕ_{slope} . The
 158 distribution of α at a 100 m-scale (α^{100}), derived from both ϕ_{slope}^{100} and ϕ_{epi} , is shown in Figure
 159 2(i). In the subsequent section, we employed h_r^{radius} and α^{radius} as topographic parameters to
 160 develop a topographic term.

161 3. RESIDUAL DECOMPOSITION USING A MIXED-EFFECTS

162 MODEL

163 3.1. Source and path effects

164 To quantify topographic response from the ground motions, we developed a base GMM by
 165 performing a regression analysis. We adopted the functional forms for source and path effects
 166 proposed by Kotha et al. (2018) (hereafter Ko18). The analysis was conducted using pseudo-
 167 spectral acceleration (PSA) at 12 periods (i.e., $T = 0.01, 0.02, 0.03, 0.05, 0.075, 0.1, 0.2, 0.3,$
 168 $0.5, 0.75, 1$ and 2 s), calculated as the geometric mean of two horizontal components. (i.e.,
 169 East-West (EW) and North-South (NS) components). The numbers of records available for
 170 analysis were 15,189 for periods of 0.01–0.5 s, 13,802 for periods of 0.75–1 s, and 6,646 for a
 171 period of 2 s, because the maximum usable period for each record was defined as $T_{max} = 0.5/f_c$
 172 (Dawood et al., 2016). Although the initial dataset included response spectra up to 10 s, only
 173 periods of $T \leq 2$ s were considered in this study due to the data sparsity at longer periods. The
 174 form of Ko18 that incorporates a mixed-effects model is conceptualized as follows:

$$\ln(\text{PSA}) = f_R(\mathbf{M}, R_{JB}) + f_M(\mathbf{M}) + \delta B_e + \delta W_{es} \quad (3)$$

175 where PSA is 5% damped pseudo spectral acceleration at a period, \mathbf{M} is moment magnitude,
 176 R_{JB} is the Joyner–Boore distance, f_R and f_M are the distance and magnitude scaling terms, δB_e
 177 is the between-event residuals for e^{th} event, and δW_{es} is the within-event residuals for e^{th} event
 178 at s^{th} site. The specific functional forms for f_R and f_M adapted from Ko18 are described in
 179 APPENDIX.

180 3.2. Site-effect correction

181 Following the framework of Ko18, we first calculated the total residuals by removing the

182 source and path effects utilizing f_R and f_M . These total residuals were subsequently partitioned
 183 into between-event and within-event components. As illustrated in Figure A1, the between-
 184 event residuals exhibit no systematic trends with respect to \mathbf{M} , and the within-event residuals
 185 show no systematic dependence on R_{JB} .

186 Using the within-event residuals, we accounted for site effects by evaluating the V_{S30} -
 187 dependent trends. The V_{S30} -correction process was conducted in two sequential stages to ensure
 188 that the site-specific effect was captured across the 12 spectral periods.

189 In the first stage, for each period, we computed the site-averaged within-event residuals for
 190 each station. This average represents the systematic bias of a particular site at a given period.
 191 We then modeled the relationship between these station-averaged residuals and V_{S30} using the
 192 LOESS (Locally Weighted Regression and Smoothing Scatterplots) function (Cleveland, 1979),
 193 as illustrated in Figure A2. The site term modeled by the LOESS fit, denoted as $f_{\text{site}}(V_{S30})$,
 194 captures the systematic site response associated with V_{S30} for each period.

195 In the second stage, we derived the V_{S30} -corrected within-event residual (δW_{es}^*) by
 196 subtracting the corresponding V_{S30} -dependent site term (f_{site}) value from the within-event
 197 residuals as follows:

$$\delta W_{es}^* = \delta W_{es} - f_{\text{site}}(V_{S30}) \quad (4)$$

198 where δW_{es} represents the within-event residual for e^{th} event at s^{th} site. These corrected
 199 residuals, δW_{es}^* , from which the dominant V_{S30} influence has been eliminated, are used to
 200 quantify topographic responses in the subsequent section.

201 4. CHARACTERIZATION OF AZIMUTH-DEPENDENT 202 TOPOGRAPHIC EFFECTS

203 4.1. Azimuth-dependent topographic response

204 We evaluated the remaining variability (i.e., δW_{es}^*) using two key topographic parameters,
 205 h_r^{radius} and α^{radius} , across a range of radius scales. To identify the optimal topographic scale that
 206 best captures the topographic response, we calculated h_r for scale radius ranging from 100 to
 207 3,000 m, while α for native resolution (i.e., α^{DEM}) and scale radius of 50 and 100 m. We then
 208 classified the ground motion data into high- and low-relative elevation groups based on the
 209 upper and lower 1% of h_r^{radius} , respectively. This threshold was selected to isolate sites with
 210 the strongest relative topographic contrast, corresponding to pronounced ridge-like and valley-

211 like geometries where topographic effects are expected to be most clearly observed.

212 Conventional GMMs typically employed h_r as a sole parameter to account for topographic
213 effect, assuming a monotonic amplification occurs at ridges characterized by high h_r values. In
214 contrast, valley sites characterized by low h_r values experiences deamplification. However, our
215 empirical findings show that the ground motion response is significantly modulated by the
216 incidence direction with respect to the slope aspect, consistent with the findings of Lee et al.
217 (2026). Figure 4 conceptually depicts 4 representative cases characterized by h_r (high versus
218 low) and α (0° versus 180°) under oblique incidence. At the ridge facing toward the epicenter
219 ($h_r > 0, \alpha = 0^\circ$), the incident seismic wave propagates along the slope surface, facilitating the
220 generation of surface waves that maximize seismic amplification. Conversely, at the ridge
221 facing away from the epicenter ($h_r > 0, \alpha = 180^\circ$), the incident seismic wave experiences
222 attenuation due to its longer path compared to the ridge facing toward the epicenter. At the
223 valley facing toward the epicenter ($h_r < 0, \alpha = 0^\circ$), the terrain geometry causes scattering and
224 energy dispersion due to its convexity, leading to seismic deamplification. These inferences are
225 consistent with the empirical trends observed in the actual seismic dataset and underscore the
226 necessity of incorporating azimuthal parameters into the topographic term of GMMs.

227 We evaluated h_r scales ranging from 100 to 3000 m and α scales from the DEM resolution
228 to 100 m. For clarity, Figure 5 illustrates δW_{es}^* versus α^{100} for the high- and low- h_r groups
229 defined using h_r^{500} , h_r^{1000} , and h_r^{1500} at $T = 0.02, 0.2,$ and 2 s. These scales were selected to
230 illustrate how the azimuth-dependent topographic response varies with the spatial scale of
231 relative elevation. For h_r^{1000} , 151 out of 15,189 ground motions were categorized into high- h_r
232 ($h_r^{1000} > 45$ m), whereas 161 out of 15,189 ground motions were categorized into low- h_r
233 elevation ($h_r^{1000} < -150$ m), for $T = 0.02$ and 0.2 s, as illustrated in Figure 5(b and e). For $T =$
234 2 s, 59 and 46 out of 6,646 records were classified into high and low h_r^{1000} groups, respectively
235 (Figure 5(h)). The same method for classification of high- and low- h_r groups was applied to
236 other scales of h_r^{radius} . In contrast, the intermediate- h_r groups exhibited no discernible trend
237 with respect to α^{radius} , as shown in Figure A3 and were consequently excluded from the
238 topographic correction model.

239 Among the combinations of various scales of h_r^{radius} and α^{radius} , pronounced trends of
240 topographic effect were primarily observed for h_r^{radius} scales of 1,000 m or larger and α^{radius}
241 scales 50 m or larger for $T \leq 0.3$. Specifically, as shown in Figure 5(b and e), the high h_r groups

242 defined by h_r^{1000} show the mean residuals of 0.49 and 0.57 at $\alpha^{100} = 9^\circ$ for $T = 0.02$ and 0.2 s,
243 respectively. These values gradually decrease to -0.33 and -0.24 as α^{100} increases to 171° . This
244 indicates that seismic amplification at ridge is maximized when the slope aspect is oriented
245 toward the epicenter (i.e., facing slope) whereas deamplification occurs as the slope faces away
246 from the epicenter (i.e., back slope). Conversely, for $T = 0.02$ and 0.2 s, the low h_r groups
247 defined by h_r^{1000} show that the mean residual of -0.47 and -0.44 at $\alpha^{100} = 9^\circ$, respectively.
248 These values increase to approximately 0 near $\alpha^{100} = 90^\circ$ and remain close to zero thereafter.
249 This indicates that deamplification at low relative elevation is dominant for facing slopes. The
250 same azimuth-dependent trends for both high- and low- h_r groups were observed at the h_r^{1500}
251 scale. This behavior aligns with the findings of Lee et al. (2026) in Pohang, South Korea, where
252 a similar azimuth-dependence was reported using a localized seismic network. However, while
253 their topographic term was optimized for the h_r^{300} scale due to the smaller topographic scale of
254 that region, the azimuth-dependent topographic effects in our empirical observations are
255 identified for the h_r^{1000} scale, reflecting the larger topographic scale of Japan.

256 Figure 5(a and d) shows a substantially weaker azimuth-dependent trend for h_r^{500} . This
257 scale-dependence implies that for the present dataset, the azimuthal modulation of ground
258 motion is more evident when larger-scale topographic features are considered. The selection
259 process of optimal spatial resolution for topographic parameters is described in the subsequent
260 section.

261 For both high- and low- h_r , the azimuthal dependence of topographic effects is distinct at
262 short-to-intermediate periods, particularly at $T = 0.02$ and 0.2 s. In contrast, the azimuthal
263 dependence diminishes significantly at $T = 2$ s, as illustrated in Figure 5(h and i). Similar
264 behavior is observed across other scale combinations, where azimuth-dependent topographic
265 effects are evident primarily for h_r^{radius} scales equal to or greater than $1,000$ m and α^{radius} scales
266 greater than 50 m. Together, these observations indicate that the topographic effects are period-
267 dependent. The significant trends at short-to-intermediate periods ($T \leq 0.3$ s) suggest a loss of
268 sensitivity to terrain geometry in the long-period range. This period-dependency is governed
269 by the physical relationship between the seismic wavelength and the characteristic scale of the
270 terrain. When the wavelength of long-period waves significantly exceeds the topographic scale,
271 the influence of local topographic irregularities on wave propagation becomes progressively
272 weaker, and scattering and interference effects become less pronounced. Consequently, the

273 azimuthal orientation of the slope becomes irrelevant to the ground motion amplification or
274 deamplification.

275 4.2. Development of a topographic term

276 Based on empirical observations in the previous section, we developed the topographic
277 correction term at periods ranging from 0.01 to 2 s. We proposed the linear relationship between
278 the V_{S30} -corrected within-event residuals (δW_{es}^*) and the aspect-to-source azimuthal difference
279 (α) in case of high- and low- h_r groups, respectively. The thresholds for each case of high- and
280 low- h_r were set to divide the upper and lower 1% h_r .

281 Equation (5) shows the proposed functional form developed separately for each high-and
282 low- h_r^{1000} cases.

$$f_{\text{topo}}(h_r^{1000}, \alpha^{100}) = \begin{cases} e_1 + e_2 \times \alpha^{100} & \text{for } h_r^{1000} > 45 \text{ m} \\ e_3 + e_4 \times \alpha^{100} & \text{for } h_r^{1000} < -150 \text{ m} \end{cases} \quad (5)$$

283 e_1 , e_2 , e_3 , and e_4 represent the period-dependent regression coefficients, summarized in Table
284 1. Examples of the proposed model at periods of 0.02, 0.2, and 2 s are shown as the regression
285 lines in Figure 5(b, e, and h), respectively.

286 To determine the optimal spatial resolution for the topographic parameters, we examined
287 the standard deviation (SD) after the topographic correction in all combinations of h_r^{radius} and
288 α^{radius} for each period. Since the azimuth dependence on topographic effects was observed at
289 short-to-intermediate periods ($T \leq 0.3$ s), our evaluation focused on the residual SD after the
290 topographic correction within this range. The combination of h_r^{1000} and α^{100} yielded the lowest
291 residual SD at $T = 0.01$ – 0.1 s, as summarized in Table 2. This suggests that h_r^{1000} and α^{100} is
292 the optimal scale for describing the azimuth-dependent topographic effects. Therefore, we
293 adopted h_r^{1000} and α^{100} as the topographic parameters to construct the azimuth-dependent
294 topographic term. As illustrated in Figure 6, the topography-corrected residuals ($\delta W_{es}^* -$
295 $f_{\text{topo}}(h_r^{1000}, \alpha^{100})$) demonstrate a significant reduction in the systematic azimuthal trends
296 previously observed. This reduction in uncertainty indicates that incorporating α effectively
297 accounts for systematic topographic effects that were previously unmodeled in the topographic
298 term of existing GMMs.

299 Lee et al. (2026) proposed topographic term (f_{topo}) coefficients considering both h_r and α^{DEM}
300 at short-to-intermediate periods ($T \leq 0.5$ s) through a linear function formulated for high- and

301 low- h_r groups, using α derived from a DEM with 30 m resolution. For high- h_r groups, the slope
302 coefficients for f_{topo} are -7.68×10^{-3} and 4.50×10^{-4} at $T = 0.02$ and 0.2 s, respectively (Lee et al.,
303 2026). Comparing these values with the results of this study indicates that both studies exhibit
304 highly consistent azimuthal dependencies at $T = 0.02$ s. Specifically, the same physical trend is
305 observed where ground motions amplify on slopes facing toward the epicenter and deamplify
306 on slopes facing away. However, the azimuthal effect becomes significantly more pronounced
307 in Japan at $T = 0.2$ s, which means that azimuth-dependent topographic effects extend into the
308 longer period. This phenomenon occurs because larger terrain geometries interact more
309 strongly with longer seismic wavelengths, which physically justifies our adoption of broader
310 topographic scales (h_r^{1000} and α^{100}) than those used by Lee et al. (2026). For low- h_r groups, the
311 slope coefficients from Lee et al. (2026) are 8.20×10^{-3} and 6.49×10^{-3} at $T = 0.02$ and 0.2 s,
312 respectively, showing that a consistent azimuth-dependent mechanism is verified for valley-
313 like sites as well. Specifically, both studies confirm that deamplification in valleys remains
314 dominant for facing slopes and systematically diminishes for the back slopes.

315 As shown in Figure 7, we compared the GMM from the base model ($f_R + f_M$) with those
316 from the proposed GMM incorporating the azimuth-dependent topographic term ($f_R + f_M + f_{topo}$).
317 All predictions are conditioned on a fixed Magnitude (**M** 5.0) across $\alpha^{100} = 30^\circ, 90^\circ,$ and 150° .
318 For $\alpha^{100} = 30^\circ$, the proposed GMM exhibited a 9–26% amplification in PSA for high- h_r group
319 at $T = 0.01$ – 0.3 s where the topographic response is most pronounced. Conversely, for the low-
320 h_r group at the same period range, the proposed GMM yields 5–31% deamplification. For α^{100}
321 $= 90^\circ$, no distinct amplification or deamplification was captured between the two GMMs. For
322 $\alpha^{100} = 150^\circ$ within the same period range, high- h_r group exhibits an 18–41% deamplification
323 in PSA.

324 As shown in Figure 8, we also compared the base GMM with the proposed GMM across
325 the entire evaluated period range ($T = 0.01$ – 2 s) under a fixed magnitude and source-to-site
326 distance (**M** 4.0, $R_{JB} = 150$ km). For $\alpha^{100} = 30^\circ$, an amplification at short-to-intermediate
327 periods ($T = 0.01$ – 0.3 s) was captured for high- h_r group however, this amplification diminished
328 at longer periods ($T > 0.3$ s) as the predictions converge toward the baseline GMM. Conversely,
329 a deamplification for low- h_r group was captured at the same period range, demonstrating that
330 the azimuth-dependent topographic effects are confined to short-to-intermediate periods. For
331 $\alpha^{100} = 90^\circ$, the proposed GMM yielded similar predictions to the base GMM across all periods
332 for high- and low- h_r group. For $\alpha^{100} = 150^\circ$, a deamplification occurred for high- h_r group at T

333 = 0.01–0.3 s, which diminishes at $T > 0.3$ s.

334

5. CONCLUSIONS

335 This study investigated the azimuth-dependent topographic effects using 15,189 ground
336 motion records from 641 KiK-net stations across Japan. By removing the source, path, and V_{S30}
337 -dependent site effects using a reference GMM, the remaining residuals were analyzed with
338 respect to topographic parameters. We identified the relative elevation scaled at a radius (h_r^{radius})
339 and the scaled azimuthal difference between slope aspect and epicentral direction (α^{radius}) as
340 the topographic parameters.

341 Our findings demonstrate that topographic amplification is not a monotonic function of the
342 relative elevation (h_r), as suggested by previous studies (e.g., Kim et al. (2024); Rai et al. (2016);
343 Rai et al. (2017)), but is significantly modulated by the relative orientation between the slope
344 aspect and the epicenter. At ridge-like sites (high- h_r), amplification is maximized for facing
345 slopes ($\alpha = 0^\circ$), whereas deamplification occurs for back slopes ($\alpha = 180^\circ$). At valley-like sites
346 (low- h_r), pronounced deamplification is observed for facing slopes. These results indicate that
347 topographic effects depend on the incidence direction, even at the same site. Therefore,
348 conventional topographic terms based solely on relative elevation are insufficient to fully
349 describe topographic amplification patterns. The results highlight the necessity of jointly
350 considering both h_r and α when parameterizing topographic effects in empirical GMMs.

351 The spatial scale of the topographic parameters also proved critical. In the study area, the
352 most distinct ground motion responses were captured at h_r^{1000} and α^{100} . While we propose a
353 topographic term based on these specific scales, it is important to note that the optimal scale
354 and thresholds (e.g., $h_r^{1000} > 45$ m or < -155 m) are likely region-dependent and may vary
355 with local terrain geometry. This scale dependence suggests that the characteristic dimensions
356 of regional topography should be considered when defining topographic parameters for
357 ground-motion prediction.

358 The consistent identification of azimuth-dependent topographic effects across different
359 regions reinforces the reliability of this phenomenon. The empirical observation that ground
360 motion amplification and deamplification are modulated by h_r and α directly aligns with
361 independent regional studies in the literature (Lee et al., 2026). However, whereas Lee et al.
362 (2026) demonstrated this behavior using a localized seismic network in Pohang, South Korea,

363 the present study confirms that the same mechanism is observable across a nationwide dataset
364 encompassing diverse topographic environments, a broader range of earthquake magnitudes,
365 and a substantially larger number of earthquakes and recording stations. This consistency
366 demonstrates that despite differences in regional topographic settings, earthquake magnitude
367 ranges, and dataset sizes, the azimuthal dependence represents a fundamental and reproducible
368 characteristic of topographic effects.

369 The observed topographic trends were prominent at short-to-intermediate periods ($T \leq 0.3$
370 s) but disappeared at longer periods. This suggests a period-dependent mechanism where the
371 topography-azimuth dependence diminishes as the seismic wavelength exceeds the physical
372 scale of the terrain geometry. By incorporating this azimuthal influence, the proposed model
373 effectively reduces uncertainty, providing a more refined framework for regional seismic
374 hazard assessments.

375 **ACKNOWLEDGEMENTS**

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TABLES

490 Table 1. Regression coefficients of the topographic term proposed in this study for 12 periods
 491 ranging from 0.01 to 2 s.

Period (s)	e_1	e_2	e_3	e_4
0.01	1.92×10^{-1}	-3.57×10^{-3}	-1.60×10^{-1}	1.78×10^{-3}
0.02	1.91×10^{-1}	-3.61×10^{-3}	-1.63×10^{-1}	1.78×10^{-3}
0.03	1.77×10^{-1}	-3.58×10^{-3}	-1.67×10^{-1}	1.75×10^{-3}
0.05	1.41×10^{-1}	-3.60×10^{-3}	-1.55×10^{-1}	1.65×10^{-3}
0.075	1.38×10^{-1}	-4.49×10^{-3}	-9.63×10^{-2}	1.27×10^{-3}
0.1	2.54×10^{-1}	-4.64×10^{-3}	-1.20×10^{-1}	2.43×10^{-3}
0.2	3.39×10^{-1}	-3.59×10^{-3}	-2.39×10^{-1}	1.76×10^{-3}
0.3	2.48×10^{-1}	-3.13×10^{-3}	-4.52×10^{-1}	2.90×10^{-3}
0.5	4.79×10^{-2}	-8.55×10^{-4}	-4.96×10^{-1}	2.83×10^{-3}
0.75	-7.93×10^{-2}	6.44×10^{-4}	-4.62×10^{-1}	2.68×10^{-3}
1	-2.18×10^{-2}	2.70×10^{-4}	-4.55×10^{-1}	2.77×10^{-3}
2	-5.91×10^{-2}	6.92×10^{-4}	-1.88×10^{-1}	1.20×10^{-3}

492

493 Table 2. Standard deviations (SD) of residuals after the topographic correction across various spatial scales of h_r and α , computed for high- and
 494 low- h_r topographic groups for 12 periods ranging from 0.01 to 2 s.

495

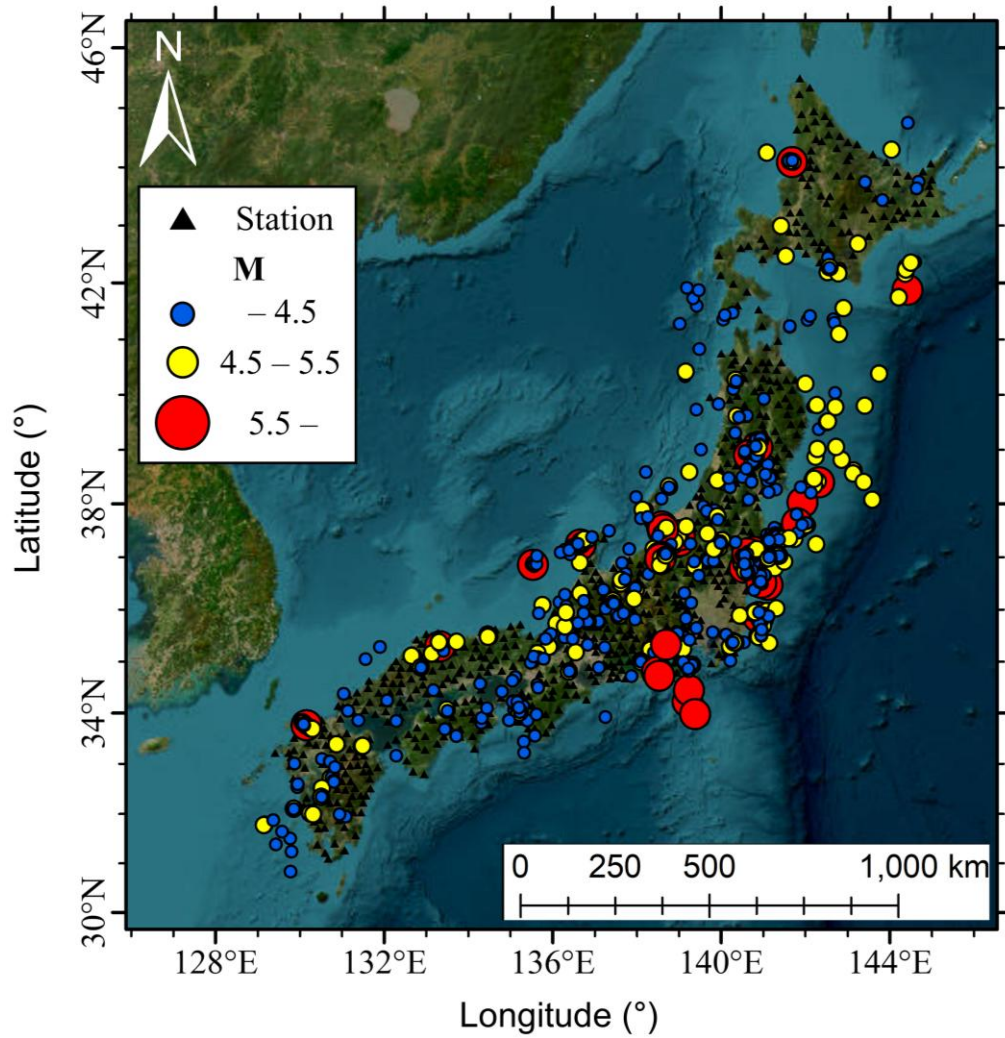
Period (s)	h_r^{500}			h_r^{1000}			h_r^{1500}		
	α^{DEM}	α^{50}	α^{100}	α^{DEM}	α^{50}	α^{100}	α^{DEM}	α^{50}	α^{100}
0.01	0.661	0.667	0.666	0.603	0.597	0.591	0.616	0.613	0.609
0.02	0.661	0.667	0.667	0.603	0.597	0.591	0.616	0.613	0.609
0.03	0.656	0.662	0.662	0.599	0.594	0.588	0.614	0.611	0.607
0.05	0.686	0.694	0.694	0.611	0.606	0.601	0.620	0.618	0.615
0.075	0.733	0.737	0.736	0.657	0.647	0.640	0.660	0.653	0.649
0.1	0.728	0.731	0.730	0.657	0.646	0.640	0.668	0.661	0.658
0.2	0.741	0.744	0.743	0.688	0.682	0.677	0.703	0.699	0.696
0.3	0.670	0.675	0.675	0.676	0.671	0.666	0.696	0.688	0.683
0.5	0.586	0.593	0.594	0.649	0.649	0.647	0.672	0.670	0.668
0.75	0.578	0.583	0.584	0.623	0.626	0.626	0.637	0.639	0.638
1	0.551	0.558	0.559	0.573	0.578	0.577	0.582	0.587	0.586
2	0.496	0.500	0.500	0.509	0.516	0.518	0.482	0.488	0.489

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FIGURES

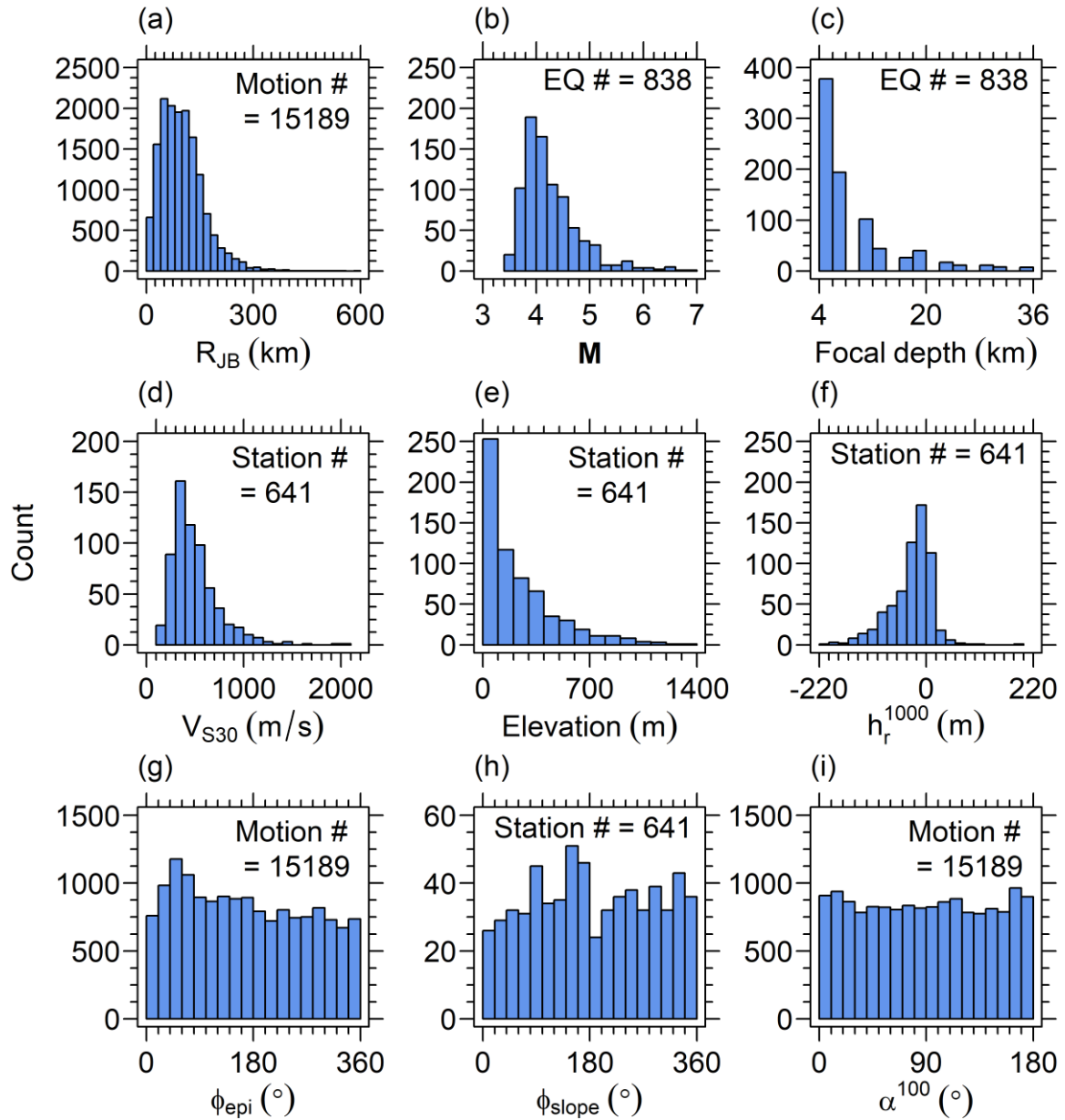
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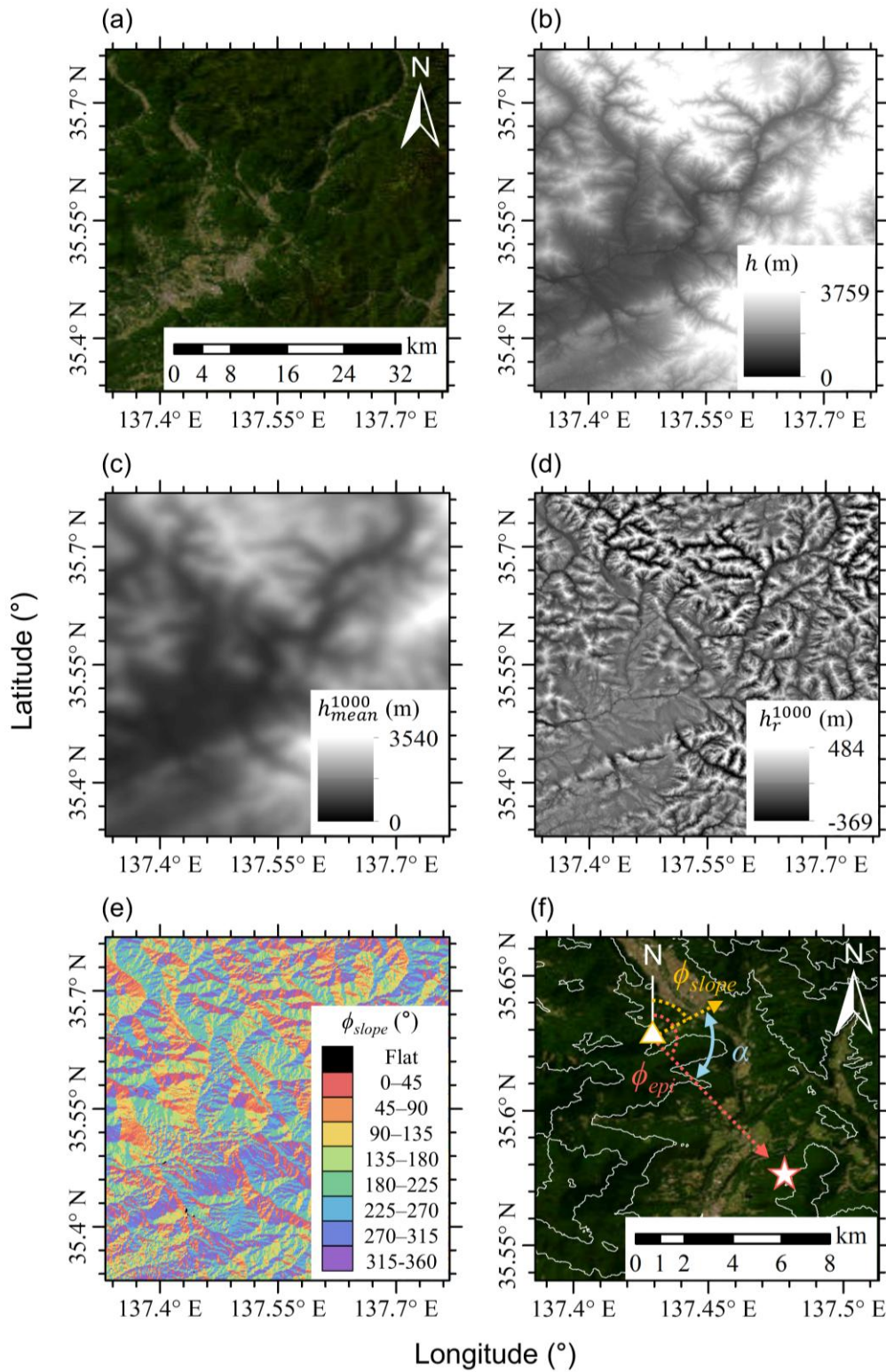
500 Figure 1. Location of the selected KiK-net stations and earthquakes. Color and size of markers

501 denote moment magnitude.



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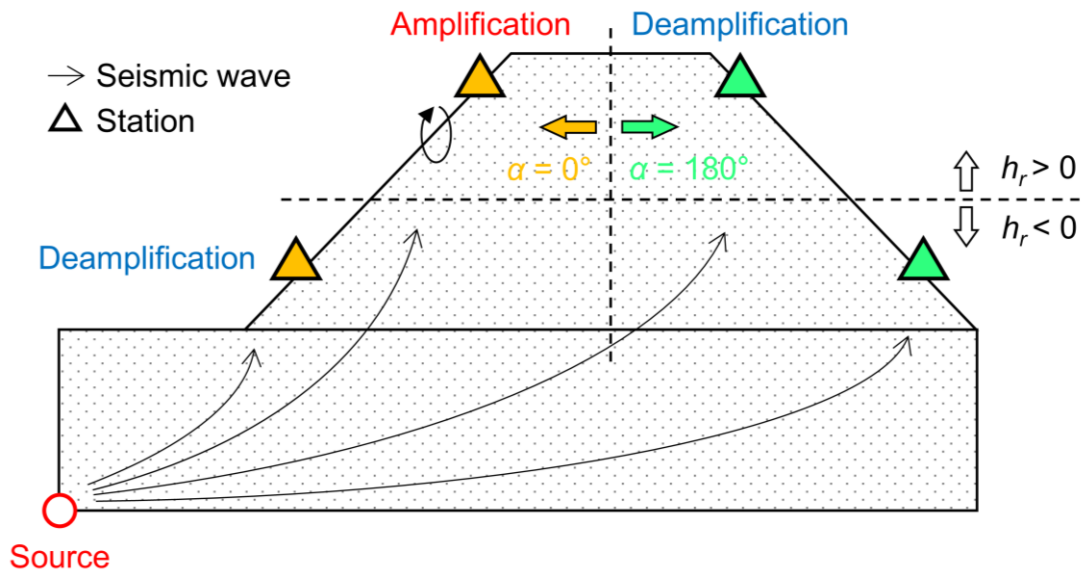
503 Figure 2. The data distributions of (a) the Joyner–Boore distance (R_{JB}), (b) moment magnitude,
 504 (c) focal depth, (d) V_{S30} , (e) elevation, (f) h_r^{1000} , (g) ϕ_{epi} , (h) ϕ_{slope} , and (i) α^{100} .



505

506 Figure 3. Maps of (a) satellite image, (b) digital elevation model (DEM), (c) mean elevation
 507 within 1000 m, (d) the relative elevation at a 1,000 m-scale, (e) ϕ_{slope} , and (f) an example of α .

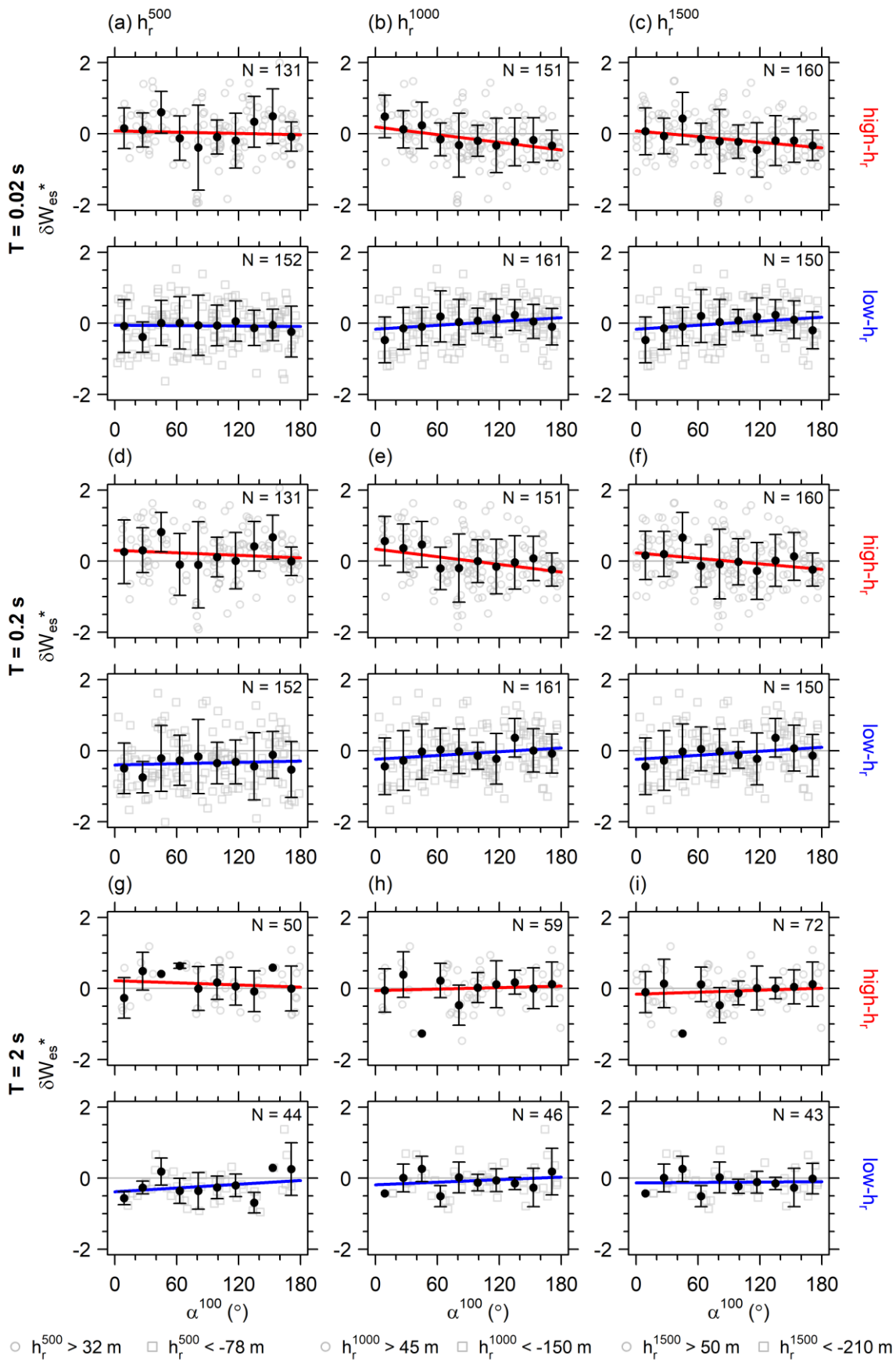
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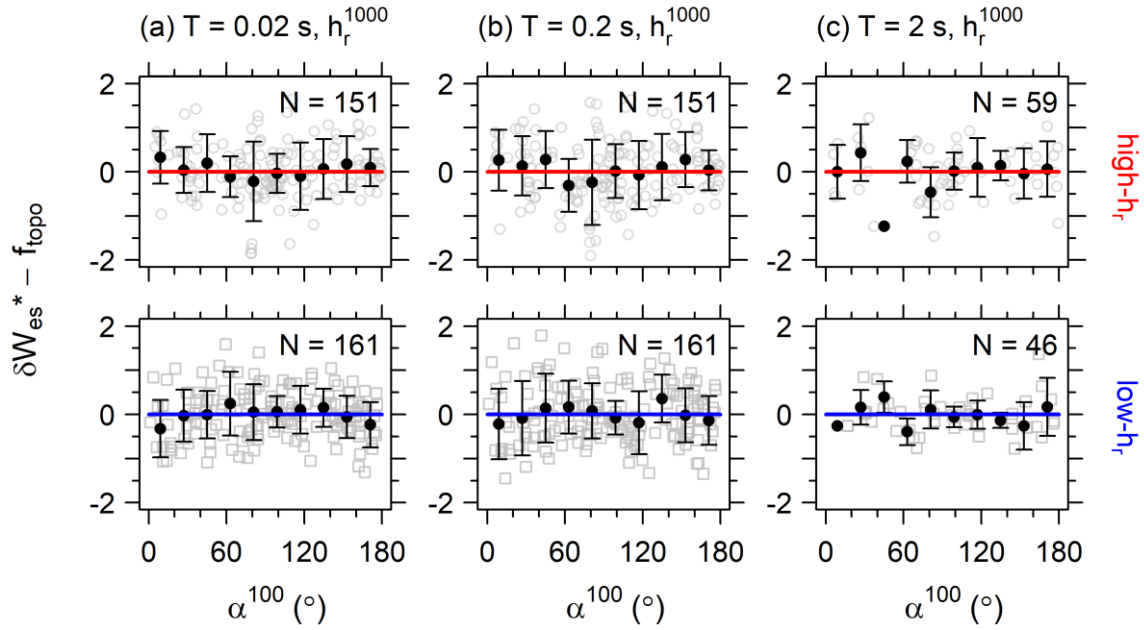
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510 Figure 4. Conceptual schematic illustrating the interaction between terrain geometry (h_r) and
 511 seismic incidence direction (α) on ground motion response. The diagram identifies four distinct
 512 topographic configurations based on h_r and α .

513



515 Figure 5. The V_{S30} scaled within-event residual (δW_{es}^*) against the smoothed α at a 100 m-scale
 516 (α^{100}). Rows and columns correspond to spectral periods (0.02, 0.2, and 2 s) and radii of the
 517 relative elevation, respectively. High-(gray circles, red lines) and low- h_r groups (gray squares,
 518 blue lines) are shown with their corresponding fits. Error bars denote grouped mean \pm one
 519 standard deviation.



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521 Figure 6. Topography-corrected residuals against α^{100} . Gray circles and squares denote high-
 522 and low- h_r for a 1000 m-scale, respectively. Error bars represent grouped mean \pm one standard
 523 deviation.

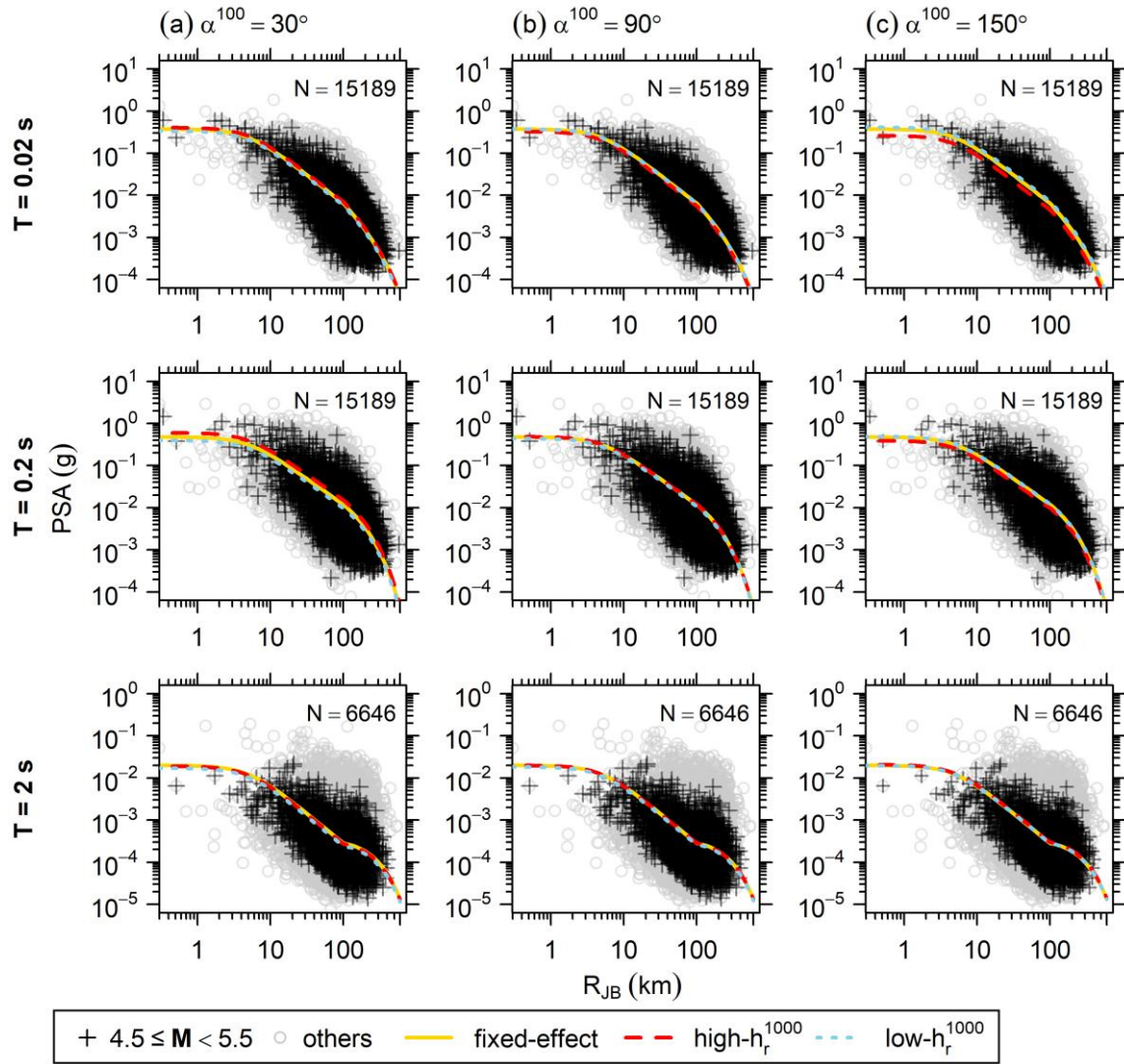
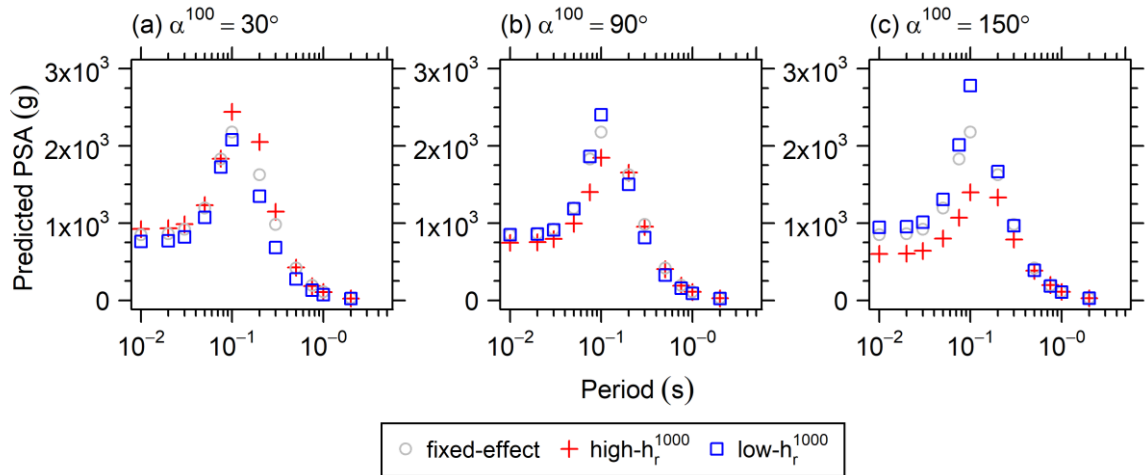


Figure 7. Measured geometric-mean horizontal PSA versus R_{JB} at $T = 0.02, 0.2,$ and 2 s across variations in α^{100} : (a) 30° , (b) 90° , and (c) 150° . Black crosses denote events with magnitudes between 4.5 and 5.5 , while gray circles denote all other events. The predictions are conditioned on a fixed magnitude (M 5.0). Yellow solid lines denote the predictions from the base model including f_R and f_M . Red dashed lines and blue dotted lines represent the predictions from the proposed GMM incorporating $f_R, f_M,$ and f_{topo} .



531

532 Figure 8. Predicted geometric-mean horizontal PSA from the base and proposed GMMs versus
 533 various periods across variations in α^{100} : (a) 30° , (b) 90° , and (c) 150° . The predictions are
 534 conditioned on a fixed magnitude (M 4.0) and source-to-site distance ($R_{JB} = 150$ km). Gray
 535 circles denote the predictions from the base model including f_R and f_M . Red crosses and blue
 536 squares represent the predictions from the proposed GMM incorporating f_R , f_M , and f_{topo} .

537

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APPENDIX

539

The specific functional forms for f_R and f_M were adapted from Ko18, as follows:

$$f_R(\mathbf{M}, R_{JB}) = \begin{cases} c_1 \ln \sqrt{R_{JB}^2 + h^2} & R_{JB} < 100 \text{ km} \\ c_1 \ln \sqrt{100^2 + h^2} + c_2 \ln \left(\frac{R_{JB}}{100} \right) + c_3 (R_{JB} - 100) & R_{JB} \geq 100 \text{ km} \end{cases} \quad (\text{A1})$$

$$\ln(h) = 2.303(\max[(-0.05 + 0.15\mathbf{M}), (-1.72 + 0.43\mathbf{M})]) \quad (\text{A2})$$

$$f_M(\mathbf{M}) = \begin{cases} a + b_1(\mathbf{M} - M_{\text{ref}}) & \mathbf{M} < M_{\text{ref}} \\ a + b_2(\mathbf{M} - M_{\text{ref}}) & M_{\text{ref}} \leq \mathbf{M} < M_h \\ a + b_2(M_h - M_{\text{ref}}) + b_3(\mathbf{M} - M_h) & M_h \leq \mathbf{M} \end{cases} \quad (\text{A3})$$

540

where $c_1, c_2, c_3, a, b_1, b_2,$ and b_3 are regression coefficients. The reference magnitude (M_{ref}) is

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set to 4.5, while the period-dependent hinge magnitude (M_h) is fixed at 5.5 for spectral periods

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up to 0.1 s and increases linearly with the logarithmic period for those exceeding 0.1 s, as

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described in Ko18. Although the functional forms follow Ko18, all regression coefficients ($c_1,$

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$c_2, c_3, a, b_1, b_2, b_3$) were calibrated through a regression analysis using our dataset. The

545

regression coefficients for f_R and f_M are listed in

546 Table A1.

547 As illustrated in Figure A1, between-event residuals and within-event residuals exhibit no
548 systematic trends with respect to \mathbf{M} and R_{JB} , respectively.

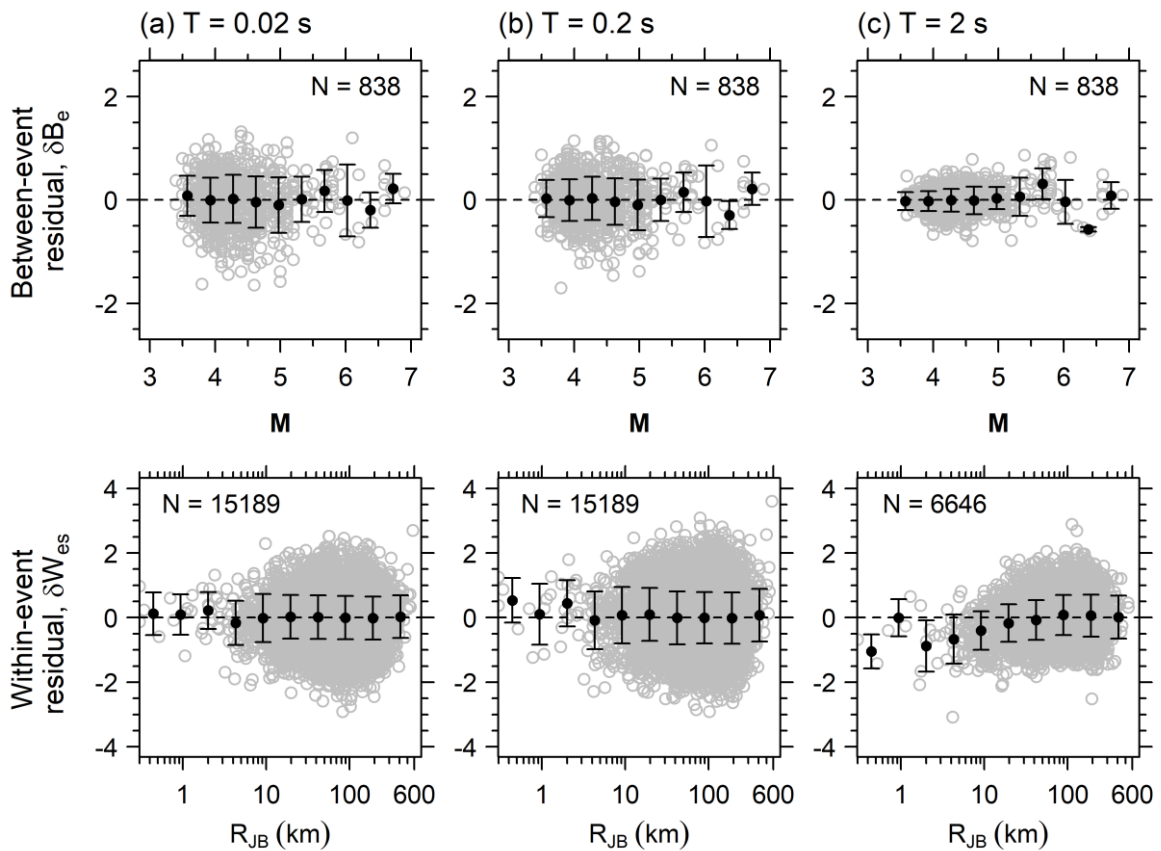
549 Figure A2 illustrates the relationship between station-averaged within-event residuals and
550 V_{S30} for each spectral period. A LOESS regression was applied to the data to capture the V_{S30} -
551 dependent site effects, which was subsequently used to correct the within-event residuals.

552 Figure A3 shows δWes^* versus α^{100} for the intermediate- h_r groups identified using h_r^{500} ,
553 h_r^{1000} , and h_r^{1500} . As illustrated in Figure A3, these intermediate groups do not exhibit any
554 apparent azimuthal dependence, maintaining a residual trend close to zero regardless of α^{100}
555 across the h_r scales.

556 Table A1. Regression coefficients for the reference ground motion model (GMM) covering the
 557 distance and magnitude scaling terms. These coefficients are derived from following the
 558 parametric regression form by Kotha et al. (2018).

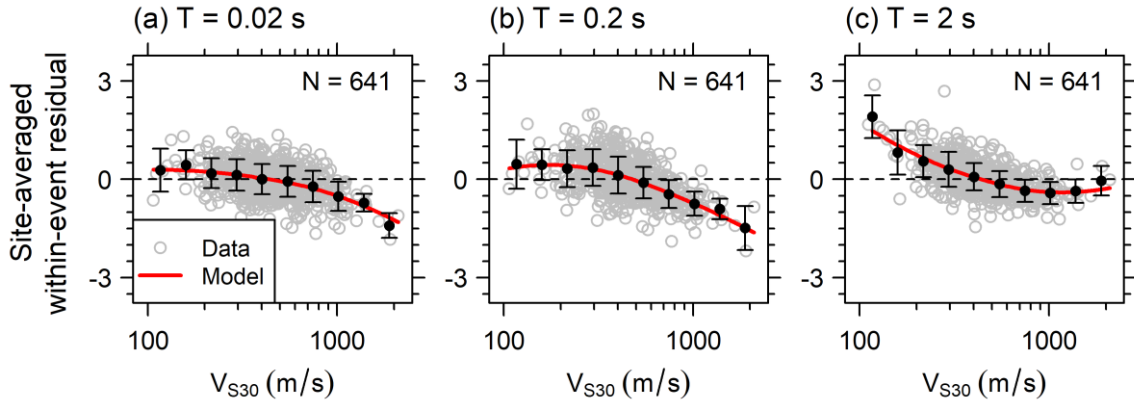
Period (s)	c_1	c_2	c_3	a	b_1	b_2	b_3
0.01	-1.355	-1.353	-0.0053	0.486	0.999	1.402	0.900
0.02	-1.354	-1.388	-0.0052	0.497	0.995	1.398	0.902
0.03	-1.350	-1.609	-0.0042	0.572	0.968	1.379	0.894
0.05	-1.316	-2.164	-0.0021	0.756	0.893	1.313	0.864
0.075	-1.239	-2.282	-0.0022	0.877	0.879	1.263	0.837
0.1	-1.216	-1.797	-0.0046	0.893	0.929	1.294	0.852
0.2	-1.233	-0.421	-0.0098	0.516	1.194	1.462	0.782
0.3	-1.298	0.228	-0.0118	0.267	1.438	1.557	0.752
0.5	-1.373	0.894	-0.0137	-0.246	1.787	1.736	0.619
0.75	-1.385	1.028	-0.0132	-0.923	1.993	1.880	0.431
1	-1.340	0.973	-0.0121	-1.689	2.113	2.022	0.200
2	-1.419	0.503	-0.0079	-2.757	2.141	2.241	-0.149

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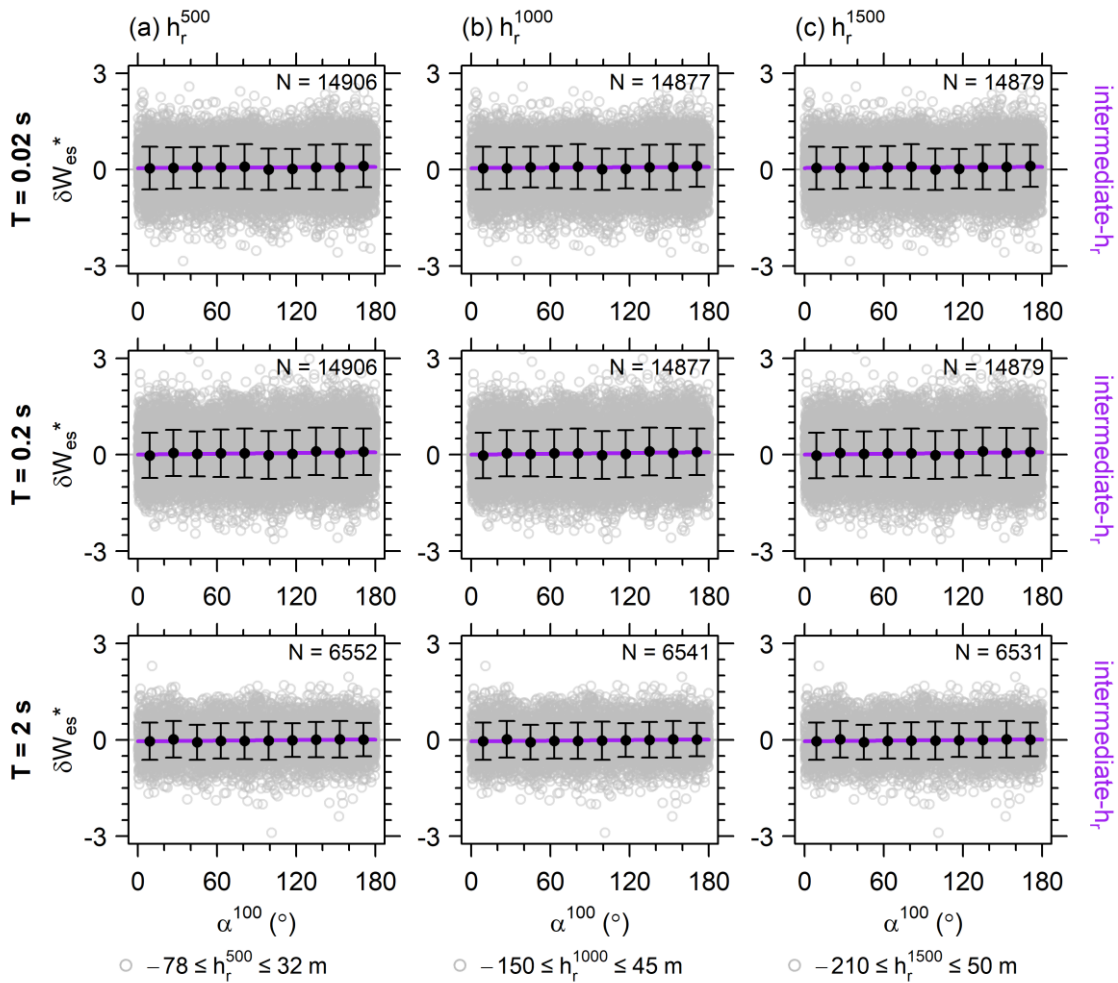
561
 562 Figure A1. Between-event residuals versus M and within-event residuals versus R_{JB} . The black

563 circles and error bars represent grouped mean \pm one standard deviation.



564

565 Figure A2. Site-averaged within-event residual versus V_{S30} . The red solid line represents the
 566 LOESS regression fit and black circles with error bars represent grouped mean \pm one standard
 567 deviation.



568

569 Figure A3. The V_{S30} scaled within-event residual (δW_{es}^*) against the smoothed α at a 100 m-

570 scale (α^{100}). Rows and columns correspond to spectral periods (0.02, 0.2, and 2 s) and radii of
571 the relative elevation, respectively. Intermediate- h_r groups (gray circles) are shown with its
572 corresponding fits (purple lines). Error bars denote grouped mean \pm one standard deviation.