

1 **Numerical models of P–T, time and grain-size controls on Ar diffusion in biotite: an aide to**  
2 **interpreting  $^{40}\text{Ar}/^{39}\text{Ar}$  ages**

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10

11 **Abstract**

12

13  $^{40}\text{Ar}/^{39}\text{Ar}$  dating of biotite is used extensively to determine the timing of cooling and  
14 exhumation in metamorphic terranes.  $^{40}\text{Ar}/^{39}\text{Ar}$  age interpretations commonly assume that  $^{40}\text{Ar}$   
15 diffuses out of biotite through temperature-dependent volume diffusion, and therefore that the  
16 age represents the time at which biotite cooled through the nominal closure temperature. Several  
17 processes or scenarios affect the reliability of the interpretation of  $^{40}\text{Ar}/^{39}\text{Ar}$  ages as representing  
18 the timing of cooling through a nominal closure temperature, including incomplete re-setting of  
19 Ar systematics, incorporation of excess Ar, crystal defects acting as Ar traps or fast-pathways, or  
20 fluid-present recrystallization/dissolution. We present a series of numerical diffusion model  
21 results that show the percentage of radiogenic Ar that should theoretically be retained in biotite  
22 with different grain radii residing for various periods over a range of P–T conditions in a perfect  
23 open system that loses Ar via volume diffusion alone. A second set of models demonstrate the  
24 effects of crustal residence temperatures, residence timescales, and subsequent cooling rates, on  
25 ‘perfect open system’ biotite  $^{40}\text{Ar}/^{39}\text{Ar}$  age and intra-grain Ar distributions. The model results are

26 useful for constraining cooling and exhumation histories from  $^{40}\text{Ar}/^{39}\text{Ar}$  biotite data in a variety  
27 of metamorphic settings. They also provide baseline data for biotite Ar retention,  $^{40}\text{Ar}/^{39}\text{Ar}$  ages  
28 and intra-grain age distributions that would theoretically be produced from volume diffusion  
29 acting alone. Consequently, the models can help evaluate the plausibility of alternative scenarios  
30 that may have affected biotite  $^{40}\text{Ar}/^{39}\text{Ar}$  ages, including extraneous Ar contamination or Ar loss  
31 via processes other than diffusion. In conjunction with well-constrained petrogenetic histories,  
32 numerical diffusion models are a powerful tool for interpreting  $^{40}\text{Ar}/^{39}\text{Ar}$  biotite ages, especially  
33 when linked with intra-grain  $^{40}\text{Ar}/^{39}\text{Ar}$  age profiles.

#### 34 **Keywords**

35  $^{40}\text{Ar}/^{39}\text{Ar}$  thermochronology, biotite, diffusion, numerical model, pressure-temperature, crustal  
36 residence

#### 37 **1. Introduction**

38  $^{40}\text{Ar}$  is produced from radioactive decay of  $^{40}\text{K}$ , and has been shown to diffuse efficiently in  
39 biotite at temperatures above  $\sim 300^\circ\text{C}$  (Harrison et al., 1985; McDougall and Harrison, 1999). It  
40 is assumed that Ar strongly partitions from minerals into the grain boundary (fluid-bearing)  
41 network, consistent with open-system behaviour (e.g., Kelley, 2002). Therefore,  $^{40}\text{Ar}/^{39}\text{Ar}$   
42 ‘dates’ yielded by biotite are typically assumed to relate to temperature-dependent diffusional Ar  
43 loss and thus constrain the timing of cooling following metamorphism.  $^{40}\text{Ar}/^{39}\text{Ar}$  dating of biotite  
44 has been used for decades to constrain the timing of cooling, exhumation and low-temperature  
45 geological events worldwide (e.g., Berger, 1975; Hanson et al., 1975; Steltenpohl et al., 1993;  
46 Hodges and Bowring, 1995; McDougall and Harrison, 1999; Schneider et al., 1999, 2013;  
47 Willigers et al., 2001). For detailed discussion and calculations of Ar diffusion in biotite and the

48 closure temperature concept, we refer the reader to previous studies (Dodson, 1973, 1986;  
49 Harrison et al., 1985; Wheeler, 1996; McDougall and Harrison, 1999).

50 Several studies have identified complexities of  $^{40}\text{Ar}$  concentration in mica that call into  
51 question traditional interpretations of metamorphic  $^{40}\text{Ar}/^{39}\text{Ar}$  ages as resulting solely from  
52 temperature-controlled volume diffusion (Heizler and Harrison, 1988; Lee, 1995; Kelley, 2002;  
53 Villa, 2010; Warren et al., 2011; Camacho et al., 2012; Cossette et al., 2015; Stübner et al.,  
54 2017). These studies suggest that alternative processes or scenarios affected the  $^{40}\text{Ar}$   
55 concentrations in biotite.  $^{40}\text{Ar}/^{39}\text{Ar}$  dates that are older than the timing of cooling through the  
56 nominal closure temperature of  $^{40}\text{Ar}$  ( $T_c$ ) can be produced by: (i) incomplete re-setting of mica  
57 during metamorphism, resulting in retention of “inherited” (pre-thermal peak)  $^{40}\text{Ar}$  (Warren et  
58 al., 2012a); (ii) incorporation and retention of excess Ar, which refers to parentless  $^{40}\text{Ar}$  that is  
59 incorporated in the grain via diffusion from an Ar-rich grain boundary fluid network or contained  
60 within mineral/fluid inclusions (Kelley, 2002); (iii) planar defects in the crystal structure serving  
61 as  $^{40}\text{Ar}$  traps (proposed in trioctohedral mica; Camacho et al., 2012); or (iv) recrystallization in a  
62 closed Ar-rich system, adding  $^{40}\text{Ar}$  to grain rims (Warren et al., 2011).  $^{40}\text{Ar}/^{39}\text{Ar}$  dates that are  
63 younger than the age of cooling through the nominal  $T_c$  can result from: (i) crystallization of the  
64 grain at or below the nominal  $T_c$  (e.g., Warren et al. 2012); (ii) planar defects in the crystal  
65 structure, such as those produced during deformation, serving as fast-pathways through which  
66  $^{40}\text{Ar}$  can escape (Lee, 1995; Hodges and Bowring, 1995); and (iii) isotopic resetting ( $^{40}\text{Ar}$  loss)  
67 due to fluid-present retrograde reactions / recrystallization / dissolution (Villa, 2010).

68 Metamorphic biotite is infamous for yielding  $^{40}\text{Ar}/^{39}\text{Ar}$  ages that are older than those  
69 expected from volume diffusion during residence at high temperatures or cooling through the  
70 nominal  $^{40}\text{Ar}$   $T_c$ . Despite the higher nominal Ar  $T_c$  for muscovite (~420–450°C; Harrison et al.,

71 2009), biotite in some cases yields  $^{40}\text{Ar}/^{39}\text{Ar}$  dates that are substantially older than those of  
72 muscovite from the same rock, and may also pre-date U/Pb ages of metamorphic monazite or  
73 zircon. Such age relationships have been documented in several orogens, including the  
74 Paleoproterozoic Trans-Hudson (Skipton et al., 2017), Mesoproterozoic Grenville (Dallmeyer  
75 and Rivers, 1983; Cosca et al., 1991; Smith et al., 1994), Neoproterozoic Capricorn (Occhipinti  
76 and Reddy, 2009), Mesozoic Alpine (Brewer, 1969; Pickles et al., 1997) and Himalaya (Mottram  
77 et al., 2015; Stübner et al., 2017).

78 In the event that biotite yields an  $^{40}\text{Ar}/^{39}\text{Ar}$  date that defies independent geological or  
79 isotopic evidence, the anomalous  $^{40}\text{Ar}/^{39}\text{Ar}$  ratio is typically attributed to processes other than (or  
80 in addition to) volume diffusion, involving inherited or excess  $^{40}\text{Ar}$ , crystal defects,  
81 recrystallization, dissolution, as described above, or dehydroxylation during vacuum heating  
82 (Harrison et al., 1985; Gaber et al., 1988; McDougall and Harrison, 1999). The degree of  
83 potential interpretational inaccuracy in such biotite ages is difficult to quantify, especially  
84 without models of Ar retention for different biotite radii and P–T histories. This has resulted in  
85 non-uniform interpretations of biotite  $^{40}\text{Ar}/^{39}\text{Ar}$  data – which may be arbitrary without conclusive  
86 evidence for the process being invoked – and a general distrust and avoidance of biotite  
87  $^{40}\text{Ar}/^{39}\text{Ar}$  ages in recent metamorphic studies.

88 Here we present numerical models for volume diffusive loss of  $^{40}\text{Ar}$  out of biotite over a  
89 range of geologically relevant temperatures (200–650°C) and pressures (0–2 GPa), and for  
90 different grain radii (0.1–5 mm) and residence times (1–1000 Myr). These models provide a  
91 baseline for ideal  $^{40}\text{Ar}$  diffusion behaviour in biotite, according to experimentally established  
92 diffusion parameters, and demonstrate theoretical  $^{40}\text{Ar}$  retentivity for various P–T scenarios to  
93 help interpret cooling/exhumation histories. Our models also enable comparisons with equivalent

94 models for muscovite (Warren et al., 2012a) to aid age interpretations of co-existing biotite and  
95 muscovite. The calculated percentage of  $^{40}\text{Ar}$  retention in biotite that would be expected from  
96 volume diffusion acting alone provides constraints on whether or not alternative processes may  
97 have affected the sample  $^{40}\text{Ar}/^{39}\text{Ar}$  age. The models illustrate the significance of grain size, P–T  
98 and crustal residence time on  $^{40}\text{Ar}$  diffusion, and demonstrate that excess Ar or changes to mica  
99 structure do not necessarily have to be invoked to explain  $^{40}\text{Ar}/^{39}\text{Ar}$  ages that seem to conflict  
100 with other geochronometers. Our models also help to rule-in or rule-out certain scenarios, such  
101 as whether or not an  $^{40}\text{Ar}/^{39}\text{Ar}$  age could reflect the timing of biotite growth, or the retention of  
102 pre-thermal peak radiogenic  $^{40}\text{Ar}$ . Ar loss via dissolution-recrystallization would be faster than  
103 via diffusion, and assessing Ar retentivity as a function of temperature in biotite affected by  
104 dissolution-recrystallization would be invalid (Villa, 2010). Our models still apply in these cases,  
105 but only if the initial (“starting”) temperature of the model is taken to be the temperature of  
106 recrystallization.

## 107 **2. Methodology: numerical modeling of $^{40}\text{Ar}$ diffusion in biotite**

108 Numerical models of  $^{40}\text{Ar}$  diffusion in biotite were run using the MATLAB<sup>TM</sup> program  
109 DiffArgP (Wheeler, 1996; Warren et al., 2012a). The following parameters were used for the  
110 models (excluding uncertainties): activation energy ( $E_a$ ) =  $47 \pm 2$  kcal mol<sup>-1</sup> (196 648 J mol<sup>-1</sup>;  
111 Harrison et al., 1985); diffusion coefficient ( $D_0$ ) =  $0.077 \frac{+0.21}{-0.06}$  cm<sup>2</sup> s<sup>-1</sup> (Harrison et al., 1985); and  
112 activation volume ( $V_{\text{act}}$ ) = 14 cm<sup>3</sup> mol<sup>-1</sup> (Harrison et al., 1985; Grove and Harrison, 1996;  
113 Harrison et al., 2009). Harrison et al. (1985) indicate a  $1\sigma$  uncertainty of  $\pm \sim 0.1$  log(D) units for  
114 diffusion coefficients calculated from experimental data. Including this uncertainty produced no  
115 significant difference to our model results.

116           The models were run using a cylindrical geometry because diffusive Ar loss in mica  
117 mainly occurs through in-plane diffusion in the crystal, which is typically modeled using  
118 cylindrical symmetry (Hames and Bowring, 1994). There has been some debate about the  
119 detailed geometry used to model these systems, but detailed analysis of diffusion coefficients has  
120 shown that the symmetry effects (e.g. cylindrical vs. spherical) on the diffusion coefficients can  
121 be expected to be substantially smaller than the measurement uncertainties listed above (Forster  
122 and Lister 2014). A Crank-Nicholson solver was used for the time integration with a time step  
123 that is 10 times larger than that required for the fully explicit model (following Wheeler, 1996;  
124 Warren et al., 2012a). It was assumed that volume diffusion occurred in an open system where  
125 the Ar concentration at the grain boundary was negligible (i.e., no excess  $^{40}\text{Ar}$  in the grain  
126 boundary network) and the grain radius was equivalent to the diffusion radius. Numerical  
127 accuracy on the bulk ages was achieved following the methods outlined in Warren et al. (2012a,  
128 b). Representative model output data (integrated or "bulk"  $^{40}\text{Ar}/^{39}\text{Ar}$  age for each model and a  
129 core-to-rim  $^{40}\text{Ar}/^{39}\text{Ar}$  age profile), bulk age regression plots, and core-to-rim age profiles are  
130 shown in Supplementary File 1.

131           Models were run for a range of biotite grain radii (0.1, 0.5, 1, 2 and 5 mm) that are  
132 representative of the grain sizes typically analyzed for  $^{40}\text{Ar}/^{39}\text{Ar}$  thermochronology. The models  
133 simulated residence times at peak conditions of 1, 5 and 20 Myr, which appear to be  
134 characteristic residence timescales for metamorphism in both modern and ancient orogens (e.g.,  
135 1–10 Myr, ca. 470 Ma Grampian Orogen, Scotland, Viete et al., 2011; 20–40 Myr, ca. 1830 Ma  
136 Trans-Hudson Orogen, Canada, Skipton et al., 2016;  $\leq$ 1–5 Myr, ca. 10.5–21 Ma Sikkim  
137 Himalaya, Mottram et al., 2015). Residence times of 100, 500 and 1000 Myr were also modeled  
138 for grain radii of 0.1 to 1 mm to illustrate how Ar retention might be affected by long-term

139 crustal residence such as expected / considered likely in Precambrian orogens. Coarser grain  
140 sizes were not considered because the high expected volumes of  $^{40}\text{Ar}$  given their age are  
141 inhibitive for  $^{40}\text{Ar}/^{39}\text{Ar}$  analyses. For a given biotite grain radius and residence time, models  
142 were run for a range of temperatures at  $10^\circ\text{C}$  increments to cover the full spectrum of Ar  
143 retentivity from 0% (complete  $^{40}\text{Ar}$  loss) to 100% (all  $^{40}\text{Ar}$  retained). Models were run using a  
144 pressure of 0.5 GPa; Ar retention at different pressures (0–2 GPa) was calculated using  
145 established values of  $E_a$ ,  $P_0$  and  $V_{\text{act}}$  (above) to map out equivalent diffusion coefficients across  
146 the entire pressure range. These model results were used to construct P–T diagrams showing  
147 %Ar retention in biotite for temperatures of 200–650°C and pressures up to 2 GPa (Figs. 1–3).

148         A second set of models was run to simulate the effect of various cooling/exhumation  
149 histories on Ar retention in 0.5 mm radius biotite (Figs. 4–6). For these models, biotite was first  
150 maintained at a temperature of 250°C, 350°C or 450°C and pressure of 0.7 GPa for different  
151 residence times (1, 20, 100, 500 or 1000 Myr). These conditions correspond to the red, blue and  
152 intermediate zones in the P-T-retention plots in Figs. 1–3. Following the defined residence  
153 periods, the modeled biotite was cooled at rates of 1.5, 10 or 30°C/Myr, which are representative  
154 cooling rates documented/suggested in Proterozoic and modern orogens (e.g., Dunlap, 2000).  
155 Decompression was modelled linearly with cooling, such that 0°C and 0 GPa were attained  
156 simultaneously in each model. A start time of 1500 Ma was used for this set of models to present  
157 all the modeled residence periods, temperatures and cooling rates from a common point in time,  
158 enabling straightforward comparison between models results shown in Figs. 4–6. The start time  
159 is otherwise arbitrary; the key detail is the amount of time that went unrecorded in the mica due  
160 to low Ar retentivity, i.e., the difference between the time at which the model started and the

161 bulk age calculated by DiffArgP. In effect, the models can be applied to any period of geological  
162 interest.

### 163 **3. Model results and interpretation**

#### 164 **3.1. Plots of pressure–temperature–%Ar retention**

165 Model results are shown on pressure–temperature plots with colour shading  
166 corresponding to percentages of  $^{40}\text{Ar}$  retention (Figs. 1–3). As with equivalent models  
167 constructed for muscovite (Warren et al., 2012a), the blue zones represent P–T conditions of low  
168 Ar retention, the red zones represent conditions of high Ar retention, and orange-to-light blue  
169 zones reflect conditions of intermediate or partial Ar retention. Biotite that crystallized in or  
170 experienced peak metamorphism in the blue P–T zones would not theoretically retain any pre-  
171 thermal peak (inherited) radiogenic Ar. It is therefore capable of constraining the timing of  
172 cooling and exhumation. Due to high Ar retention in the red P–T zones, the  $^{40}\text{Ar}/^{39}\text{Ar}$  age of  
173 biotite that crystallized at these conditions should, in an ideal system, reflect the timing of  
174 crystallization. Biotite that crystallised at lower conditions and subsequently experienced peak  
175 metamorphism in the red P–T zones would not have had the opportunity to lose its inherited  
176 (pre-thermal peak)  $^{40}\text{Ar}$  before cooling initiated. Even if such a grain lost some Ar during  
177 cooling, it would still yield an older  $^{40}\text{Ar}/^{39}\text{Ar}$  date than a grain that had crystallised at peak  
178 conditions, potentially resulting in overestimation of interpreted cooling rates. An  $^{40}\text{Ar}/^{39}\text{Ar}$  age  
179 of biotite that crystallized in or experienced peak metamorphism in the “intermediate” P–T zones  
180 must also be interpreted with caution due to incomplete pre-peak degassing of  $^{40}\text{Ar}$ .

181 The plots illustrate the significant dependence of  $^{40}\text{Ar}$  retentivity on grain size and  
182 residence time, even for relatively short residence times of 1–20 Myr (Figs. 1, 2). For a given set



183 of crustal residence conditions (temperature, pressure, time) within the intermediate zone, a 0.1  
184 mm-radius grain is ~35% less retentive of Ar than a 1 mm-radius grain, which is ~25% less  
185 retentive than a 5 mm-radius biotite. For a biotite grain with a given radius residing at fixed P–T  
186 conditions in the intermediate zone, a grain residing for 20 Myr is ~35% less retentive than  
187 biotite residing for 1 Myr.

188 The plots simulating long-term crustal residence of 100–1000 Myr demonstrate the  
189 effects of geologic time on  $^{40}\text{Ar}$  concentrations in biotite, especially in Precambrian orogens  
190 (Fig. 3). For a 1 mm-radius biotite, Ar retentivity is ~20, 40 or 60% lower for residence times of  
191 100, 500 or 1000 Myr, respectively, compared to residence of 20 Myr. Time exerts the most  
192 extreme effects on Ar systematics in fine-grained, 0.1 mm-radius biotite: during 1 Ga residence  
193 at upper-crustal conditions of 250°C ( $<T_c$ ) and  $P \leq 0.5$  GPa, models suggest that the grain would  
194 lose at least ~50% radiogenic Ar through diffusion (Fig. 3i) before exhumation starts.

### 195 **3.2. Models of cooling and exhumation histories for 0.5 mm radius biotite**

196 Model results are shown as core-to-rim  $^{40}\text{Ar}/^{39}\text{Ar}$  age profiles with corresponding bulk ages,  
197 calculated using a model start time of 1500 Ma (Figs. 4–6). For models in which biotite resided  
198 at 250°C for 1–100 Myr prior to cooling, bulk ages are  $\leq 1$  Myr younger than the onset of crustal  
199 residence (i.e., the model start time), and core-to-rim age profiles are relatively flat regardless of  
200 cooling rate (Figs. 4a–b, 5a). These model results reflect insignificant Ar diffusion in biotite at  
201 250°C, as expected so far below the nominal  $T_c$ . For residence times of 500 Myr and 1 Gyr at  
202 250°C, modelled core-to-rim age profiles exhibit diffusive Ar loss at outer grain edges and yield  
203 significantly lower bulk ages that are 28–30 Myr and 81–84 Myr, respectively, younger than the  
204 onset of crustal residence (Figs. 5b, 6a). This implies that low-temperature Ar ‘leakage’ from the

205 outermost  $\leq 50$   $\mu\text{m}$  of grain edges may be possible during long-term crustal residence of 0.5 mm-  
206 radius biotite in Precambrian orogens, and may affect  $^{40}\text{Ar}/^{39}\text{Ar}$  step-heating or total fusion ages  
207 beyond analytical uncertainty.

208 For models in which biotite crystallised and resided at relatively cool temperatures of  $350^\circ\text{C}$   
209 for various periods prior to cooling, slower cooling rates produce younger bulk ages and greater  
210 core-to-rim age decreases than those produced by faster cooling rates. This relationship reflects  
211 relatively efficient Ar diffusion at  $350^\circ\text{C}$ , which is more pronounced in grains that remained  
212 hotter for longer and/or that cooled more slowly. For a residence time of 1 Myr at  $350^\circ\text{C}$ , model  
213 ages are up to 10 Myr younger than the time of the onset of cooling below  $350^\circ\text{C}$  in each model.  
214 However, for all other residence periods modeled (20 Myr to 1 Gyr), resultant ages are older than  
215 the onset of cooling or, in the case of cooling at  $1.5^\circ\text{C}$  after 20 Myr residence, only 4 Myr  
216 younger than the onset of cooling. Therefore, these models illustrate the possible partial retention  
217 of  $^{40}\text{Ar}$  in biotite during residence within the 'intermediate' P–T zone, and the importance of  
218 knowing the P–T conditions of biotite growth as well as its subsequent P–T path for interpreting  
219 the measured  $^{40}\text{Ar}/^{39}\text{Ar}$  date.

220 Models of biotite crystallising then residing at higher temperatures (e.g.,  $450^\circ\text{C}$ ) for various  
221 periods followed by cooling at different rates all yielded ages younger than the time of onset of  
222 cooling, in accordance with highly efficient  $^{40}\text{Ar}$  diffusion at  $450^\circ\text{C}$ . The slower the cooling rate,  
223 the younger the bulk age and the steeper the core-to-rim age profile, with all ages younger than  
224 those of equivalent models run with  $350^\circ\text{C}$  residence conditions. This is consistent with  
225 sustained diffusion of  $^{40}\text{Ar}$  out of biotite that remains hotter than  $T_c$  for longer. Notably, for  
226 residence periods of 20 Myr and longer, core-to-rim age profile slopes of the  $350^\circ\text{C}$  models are  
227 steeper than those of  $450^\circ\text{C}$  models with equivalent cooling rates. This is inferred to reflect the

228 less efficient diffusion of Ar at 350°C, hindering transport of Ar from the grain cores to the grain  
229 rims. Conversely, biotite residing at 450°C would experience more efficient Ar loss, such that  
230 the core-to-rim age gradient is controlled solely by the subsequent cooling rate. This is supported  
231 by our 450°C models: each cooling rate produced a distinct core-to-rim age gradient that is  
232 unaffected by residence time or when cooling began.

## 233 **4. Discussion**

### 234 **4.1. Applicability of experimentally-determined Ar diffusion parameters to natural samples**

235 Few studies have successfully conducted experimental measurements of  $^{40}\text{Ar}$  diffusivity  
236 in biotite, in part due to the difficulty of maintaining the stability of hydroxyl-bearing minerals  
237 over the necessary temperature range. Harrison et al. (1985) addressed this issue by measuring  
238 radiogenic  $^{40}\text{Ar}$  loss from biotite samples after hydrothermal-isothermal treatment; for each  
239 temperature run, biotite was heated at constant temperature in the presence of water to help  
240 maintain the mineral's stability. The biotite samples were ~56% annite, with radii of 56–202  $\mu\text{m}$ ,  
241 typical of biotite in granite and in most metamorphic rocks dated using  $^{40}\text{Ar}/^{39}\text{Ar}$  (e.g., meta-  
242 granite, pelite, psammite). Equivalent experiments conducted on biotite richer in Fe provided  
243 nearly identical diffusion parameters (Grove and Harrison, 1996). For these reasons, in the  
244 absence of other reliable experimental values, and in consistency with most interpretations of  
245  $^{40}\text{Ar}/^{39}\text{Ar}$  biotite data we used the  $E_a$  and  $D_0$  of Harrison et al. (1985) here (a comprehensive  
246 review is provided by McDougall and Harrison, 1999).

247 It has been argued that lab-measured diffusivities of hydrous minerals (biotite,  
248 phlogopite, muscovite) are too high compared to those affecting natural resetting of  
249 geochronometers due to greater artificially-induced  $^{40}\text{Ar}$  loss during heating experiments (Villa,  
250 1994, 2010). During initial heating, insufficient water activity in the experimental capsule leads

251 to dehydroxylation, whereas excessive water activity can result in aqueous dissolution. Both  
252 processes may create pathways through which  $^{40}\text{Ar}$  can escape more rapidly than in nature,  
253 resulting in overestimation of the measured volume diffusivities (Villa, 2010). Corrected  
254 activation energies and diffusion coefficients have been estimated for phlogopite (Villa, 2010),  
255 however, correction factors are based on an assumed percentage (~6%) of initial fast-pathway  
256  $^{40}\text{Ar}$  loss required to fit lines through measured data. As such, the amount of fast-pathway  $^{40}\text{Ar}$   
257 loss from biotite during diffusion experiments is not reliably quantifiable, and corrections for  
258 fast-pathway  $^{40}\text{Ar}$  loss in experimentally determined  $E_a$  and  $D_0$  are not built into our models.  
259 This may represent a source of uncertainty in the calculated percentages of  $^{40}\text{Ar}$  retention, such  
260 that biotite may retain more  $^{40}\text{Ar}$  in reality than the modeled percentages. Nonetheless,  $^{40}\text{Ar}/^{39}\text{Ar}$   
261 mica dates have, in many settings, been documented to align with those predicted by measured  
262 Ar diffusivities and other isotopic systems (i.e., the  $^{40}\text{Ar}/^{39}\text{Ar}$  age of biotite < muscovite <  
263 hornblende < U/Pb ages; e.g., Van Schmus et al., 2007; Schneider et al., 2013; Willigers et al.,  
264 2001), suggesting that the measured diffusivities are likely close to those operating in nature.

265 It is important to note that every biotite grain has a P–T region for which it would retain  
266 most, if not all of its radiogenic  $^{40}\text{Ar}$ , and this P–T region covers broader temperatures at higher  
267 pressures. This point remains valid for any set of diffusion parameters ( $D_0$ ,  $E_a$ ,  $V_0$ ), and our  
268 numerical uncertainty analysis has shown that Ar retention/release regions in P–T space are  
269 robust against changes in diffusion coefficients.

## 270 **4.2. Interpreting exhumation and cooling**

271 By illustrating how Ar retentivity in biotite varies with pressure, temperature, grain size and  
272 residence time, our modeled P–T–% retention plots can be used to help interpret cooling  
273 histories from  $^{40}\text{Ar}/^{39}\text{Ar}$  data in a variety of metamorphic terranes. Our modeled ages and core-

274 to-rim age profiles of hypothetical cooling/exhumation scenarios may also inform tectonic  
275 interpretations, especially when linked with in-situ  $^{40}\text{Ar}/^{39}\text{Ar}$  data, such as provided by laser  
276 ablation.

277 Mica intra-grain age maps from UV laser spot analyses reveal abundant information, together  
278 with step-heating or total-fusion  $^{40}\text{Ar}/^{39}\text{Ar}$  data to provide context. Previous studies have  
279 matched measured core-to-rim age profiles with diffusion model results to constrain cooling  
280 rates and cooling/exhumation histories (e.g., Kelley and Wartho, 2000; Wartho et al., 2003;  
281 Warren et al., 2011, 2012b; Skipton et al., 2017). Interpretations of cooling histories from UV  
282 laser age maps may be limited by the spatial resolution (at least 30–50  $\mu\text{m}$  laser spot size usually  
283 required) and analytical errors of UV laser spot ages. Intra-grain age complexities and break-off  
284 of crystal edges during sample preparation present additional challenges, and the uncertainties  
285 inherent in DiffArgP modeling and biotite diffusion parameters (discussed above) necessitate  
286 caution when comparing  $^{40}\text{Ar}/^{39}\text{Ar}$  dates with model results. Even so, we consider such  
287 comparisons to be the currently best available approach for interpreting  $^{40}\text{Ar}/^{39}\text{Ar}$  dates as related  
288 to cooling, crystallisation or excess  $^{40}\text{Ar}$  contamination.

#### 289 4.2.1. *High-grade metamorphism*

290 The models suggest that biotite from medium- to high-grade terranes where the thermal  
291 peak is  $\geq 600^\circ\text{C}$  would completely lose any pre-peak (inherited) radiogenic Ar, even if peak  
292 metamorphism lasted for only 1 Myr (Figs. 1g, 2a, 2d). Possible exceptions include coarse-  
293 grained biotite (2–5 mm radii) residing at pressures of  $\sim 1$  GPa and higher (Fig. 1a, d). Efficient  
294 Ar diffusion  $\geq 600^\circ\text{C}$  – even during short-lived thermal maximums – is supported by analyses of  
295 Himalayan biotite grains (0.25–0.5 mm radii) metamorphosed at  $\geq 650^\circ\text{C}$  for  $\sim 5$  Myr, which

296 yielded dates consistent with cooling ages (Mottram et al., 2015). Therefore, our results indicate  
297 that biotite that experienced amphibolite- to granulite-facies metamorphism is a candidate for  
298 yielding  $^{40}\text{Ar}/^{39}\text{Ar}$  cooling and exhumation ages (clearly an open grain boundary system is also  
299 required). In this, our models are in agreement with long-held protocol for interpreting cooling  
300 ages from biotite in high-grade metamorphic terranes.

#### 301 4.2.2. *Low-grade and/or short-lived metamorphism*

302         Temperatures attained during peak greenschist or sub-greenschist-facies metamorphism  
303 approach, or are lower than, the nominal closure temperature of Ar in biotite ( $T_c \approx 300^\circ\text{C}$ ;  
304 McDougall and Harrison, 1999). Biotite that crystallised along the prograde path may therefore  
305 retain a percentage of pre-thermal peak  $^{40}\text{Ar}$  (i.e., its Ar systematics are not fully reset) and  
306 produce an  $^{40}\text{Ar}/^{39}\text{Ar}$  date that is older than the cooling age that would be predicted had the  
307 biotite crystallised at, and cooled from, peak temperatures. Our models provide graphical  
308 representation of this scenario, allowing a quantitative estimate of whether or not inherited Ar  
309 could be a factor in biotite of a variety of grain sizes residing at a variety of conditions. For  
310 example, a 1 mm-radius biotite grain metamorphosed at  $375^\circ\text{C}$  ( $P > 0.5$  GPa) would need to  
311 remain at those conditions for  $>20$  Myr to retain none of its pre-peak Ar (Figs. 1g–i, 3a–c). If  
312 metamorphosed at  $375^\circ\text{C}$  for 20 Myr, a coarser-grained crystal (2–5 mm radius) would retain at  
313 least ~50% inherited Ar, regardless of pressure (Fig. 1c, f). The models show that biotite grains  
314 with smaller radii (~0.1–0.5 mm) are the safest choice for constraining the cooling age following  
315 peak greenschist-facies metamorphism. Biotite grains that experienced thermal peak at sub-  
316 greenschist-facies ( $\leq 300$ – $350^\circ\text{C}$ ) are capable of yielding  $^{40}\text{Ar}/^{39}\text{Ar}$  crystallization ages, but not  
317 cooling ages. This relationship can potentially be used to date low-temperature events such as

318 fluid-assisted biotite neo- or recrystallization, as has been demonstrated for white mica (e.g.,  
319 Cossette et al., 2015; Kellett et al., 2016).

320 Rapid metamorphic cycles, and short residence times at peak conditions, such as appears  
321 to be the case in many modern orogens, also present challenges for interpreting  $^{40}\text{Ar}/^{39}\text{Ar}$  ages.  
322 Without sufficient time to diffuse out of biotite, pre-peak radiogenic Ar may be retained even in  
323 0.1 mm-radius grains that experienced moderate temperatures. For instance, during 1 Myr  
324 residence at medium pressures, our models suggest that a 0.1 mm-radius biotite grain would only  
325 be fully reset (retain 0% pre-peak Ar) if temperatures were sustained at  $\geq 400^\circ\text{C}$  (Fig. 2d).

326 In the eastern Himalaya, biotite ages from an inverted metamorphic sequence (garnet to  
327 kyanite-sillimanite grades; 0.4–0.8 GPa) provide empirical evidence of  $^{40}\text{Ar}$  inheritance resulting  
328 from short-lived metamorphism at moderate temperatures (Mottram et al., 2015). Biotite grains  
329 with 0.25 and 0.5 mm radii were dated from the highest-grade part of the sequence, which was  
330 metamorphosed at  $\geq 650^\circ\text{C}$  for  $\sim 5$  Myr, and yielded narrow age populations indicative of cooling  
331 ages. In contrast, biotite grains with equivalent radii were analyzed from lower-grade rocks that  
332 experienced peak temperatures of  $400\text{--}580^\circ\text{C}$  for  $\leq 1$  Myr. These grains produced discordant  
333 heating spectra and dispersed  $^{40}\text{Ar}/^{39}\text{Ar}$  dates that were both older and younger than those of co-  
334 existing muscovite (Mottram et al., 2015). The authors attributed this trend to incomplete re-  
335 setting of Ar systematics (Ar inheritance) resulting from short residence times at low  
336 temperatures. In support of this interpretation, our models illustrate that a 0.5 mm-radius biotite  
337 grain experiencing peak temperatures at  $400^\circ\text{C}$  and pressures of 0.4–0.8 GPa would need to  
338 remain at those conditions for  $>20$  Myr to achieve complete loss of pre-peak  $^{40}\text{Ar}$  (Fig. 2b). For a  
339 temperature of  $580^\circ\text{C}$ , the same grain would lose all pre-peak  $^{40}\text{Ar}$  if it remained at those  
340 conditions for  $\geq 1$  Myr (Fig. 2a).

### 341 4.2.3. Precambrian orogens

342 The models highlight key factors in interpreting  $^{40}\text{Ar}/^{39}\text{Ar}$  ages in Precambrian orogens  
343 where rocks are known to have resided at lower-, mid- and/or upper-crustal conditions for 10s to  
344 100s of Myr, or even Gyr timescales. In Precambrian terranes, slow cooling rates of  $\leq 10^\circ\text{C}/\text{Myr}$   
345 are typically deduced from comparisons between  $^{40}\text{Ar}/^{39}\text{Ar}$  and U–Pb ages (e.g., Schneider et al.,  
346 2007; Rivers, 2008; Willigers et al., 2001; Skipton et al., 2017). Alternatively, it has been  
347 proposed that  $^{40}\text{Ar}/^{39}\text{Ar}$  ages in Precambrian terranes may be artificially young due to gradual  
348 diffusive Ar loss during long-term crustal residence below nominal Ar closure temperatures  
349 (Dunlap, 2000). As a result, rates of cooling and exhumation in Precambrian terranes may have  
350 been faster than current estimations. Our modeled P–T–%retention plots support limited Ar loss  
351 during long-term, low-temperature crustal residence of fine-grained biotite. For instance, a 0.1  
352 mm-radius biotite grain may lose ~25% of its Ar during 1 Gyr of residence at  $200^\circ\text{C}$  and 0.3  
353 GPa, and ~70% at  $275^\circ\text{C}$  (Fig. 3i). However, models of 0.5 mm-radius biotite that resided at  
354  $250^\circ\text{C}$  for 500 Myr and 1 Gyr exhibit flat core-to-rim age profiles with Ar loss evident only in  
355 the outermost ~50  $\mu\text{m}$  of grain edges (Figs. 5b, 6a). The bulk ages of these models are up to 84  
356 Myr younger than the onset of crustal residence at  $250^\circ\text{C}$ . Our modeling therefore implies that  
357 long-term crustal residence at  $T < T_c$  may produce a bulk  $^{40}\text{Ar}/^{39}\text{Ar}$  date several Myr younger  
358 than the age of cooling through  $T_c$ , and that diffusive Ar loss may be detectable within the grain  
359 edge using UV laser  $^{40}\text{Ar}/^{39}\text{Ar}$  spot core-to-rim transects.

360 UV age transects have been compared with DiffArgP models to test cooling rates and  
361 low-temperature Ar loss in muscovite from the Paleoproterozoic Trans-Hudson Orogen (Skipton  
362 et al., 2017). In that case, core-to-rim age profiles generated by DiffArgP models of 1 Gyr  
363 isothermal residence at  $220^\circ\text{C}$  exhibited minor Ar loss at muscovite grain edges, which



364 coincided with dates of UV laser spots. Due to the 50  $\mu\text{m}$  UV spot size and analytical (and  
365 model) uncertainties, this relationship was not definitive, but supports the plausibility of gradual  
366 Ar loss during long-term isothermal residence at  $T < T_c$ . Importantly, in that study, DiffArgP  
367 models simulating various initial cooling rates (1–10°C/Myr) showed that any slow Ar loss that  
368 may have occurred during a subsequent 1 Gyr isothermal period in the crust (at  $T = 220^\circ\text{C}$ )  
369 would have been insufficient to change cooling ages beyond uncertainties, or to erase Ar  
370 evidence of early rapid ( $\geq 10^\circ\text{C}/\text{Myr}$ ) cooling. Therefore, the muscovite likely cooled at 1–  
371 2.5°C/Myr following peak metamorphism, in line with ‘slow’ cooling rates determined in other  
372 Precambrian orogens (Skipton et al., 2017).

373 UV laser spot intra-grain  $^{40}\text{Ar}/^{39}\text{Ar}$  age maps also revealed evidence of slow cooling in  
374 biotite from a ca. 1680 Ma synorogenic monzogranite in the Yavapai orogen in the southwestern  
375 United States (Hodges and Bowring, 1995). The authors concluded that core-to-rim age  
376 decreases of  $\sim 200$  Myr (from ca. 1240 to 1040 Ma) over 0.5–0.7 mm grain radii resulted from  
377 slow cooling following magmatic crystallization, in agreement with independent geological  
378 evidence. They used the closure temperature algorithm (Dodson, 1986) to estimate a cooling rate  
379 of 0.5 K/Myr. This estimate is supported by our DiffArgP models: models using a faster cooling  
380 rate of 1.5°C/Myr yielded more shallowly sloped core-to-rim age gradients ( $\sim 100$  Myr; Figs. 4e–  
381 f, 5e–f, 6c) than that of the Yavapai biotite.

382 In some Proterozoic orogens, faster cooling rates have been interpreted from  $^{40}\text{Ar}/^{39}\text{Ar}$   
383 ages that are nearly equivalent to metamorphic U/Pb ages. Mid-crustal blocks in the Grenville  
384 orogen appear to have cooled at rates up to 11°C/Myr during late-orogenic extension (Cosca et  
385 al., 1995; Rivers, 2008; Schneider et al., 2013). Gravity-driven extensional collapse has been  
386 proposed in the Variscan orogen, based on rapid cooling and exhumation deduced in part from

387  $^{40}\text{Ar}/^{39}\text{Ar}$  ages (e.g., Steltenpohl et al., 1993). “Old” biotite dates that are similar to U/Pb ages of  
388 peak metamorphism, suggesting fast cooling, may be reliable if Ar inheritance is ruled out. This  
389 can be evaluated using our model results, together with the known P–T history: the dated biotite  
390 must have resided for sufficient time at temperatures in the ‘blue’ P–T zones (in Figs. 1–3).  
391 Theoretically, it would also exhibit a flat core-to-rim age profile indicating rapid cooling (e.g.,  
392 age profiles for cooling rates of 10°C/Myr and 30°C/Myr in Figs. 4e–f, 5e–f, 6c). However, such  
393 an interpretation assumes no excess Ar contamination, a completely open grain boundary and no  
394 trapping of Ar within grain defects; these assumptions are challenging to quantify (discussed  
395 below).

#### 396 **4.3. Effects of extraneous Ar and fast-pathway Ar loss**

397 By showing the ages that would be expected following volume diffusion acting alone, our  
398 models can help determine whether a biotite  $^{40}\text{Ar}/^{39}\text{Ar}$  date is likely to represent the timing of  
399 cooling at a particular rate or if it could have been produced or reset by other processes.

400 The effects on  $^{40}\text{Ar}/^{39}\text{Ar}$  cooling ages of crystal defects serving as Ar traps (e.g., Camacho et  
401 al. 2012) or Ar-loss pathways (e.g., Lee, 1995; Hodges and Bowring, 1995) cannot be directly  
402 tested using DiffArgP models. Instead, P–T–%retention plots (Figs. 1–3) provide theoretical  
403 constraints on alternative scenarios: e.g., an anomalously young biotite age may result from late,  
404 low-temperature biotite crystallization within the ‘red zones’, and not necessarily from Ar loss  
405 through grain defects. UV laser spot analyses are important for investigating possible effects of  
406 crystal defects on Ar ages; anomalously young zones within biotite may be attributed to grain  
407 defects allowing rapid Ar loss (e.g., Hodges and Bowring, 1995; Skipton et al., 2017).

408 The P–T–% retention plots (Figs. 1–3) can be used to assess the likelihood of retention of  
409 inherited Ar: biotite that experienced peak conditions within the red or intermediate P–T zones is  
410 at risk for containing pre-thermal peak radiogenic Ar, producing an  $^{40}\text{Ar}/^{39}\text{Ar}$  age that may  
411 predate the timing of post-thermal peak cooling through  $T_c$ . Conversely, if biotite experienced  
412 peak P–T in the blue zone, yet yields an  $^{40}\text{Ar}/^{39}\text{Ar}$  age that is older than that expected from  
413 independent data, the biotite may have been contaminated by excess  $^{40}\text{Ar}$  ( $^{40}\text{Ar}_e$ ).

414 In some cases,  $^{40}\text{Ar}_e$  contamination can be identified from step-heating analyses (review in  
415 Kelley, 2002).  $^{40}\text{Ar}_e$  has been suggested as the cause of saddle-shaped gas release spectra  
416 (Lanphere and Dalrymple, 1976; Harrison and McDougall, 1981; McDougall and Harrison,  
417 1999); the shape arising from the suggested release of  $^{40}\text{Ar}$  trapped in fluid or melt inclusions at  
418 low temperature and from the breakdown of solid inclusions at high temperature (Kelley, 2002).

419 A linear array of step-heating data on an inverse isochron plot may also show the presence of  
420 trapped  $^{40}\text{Ar}_e$  with a distinct non-atmospheric composition (Heizler and Harrison, 1988).  
421 However, identification of an  $^{40}\text{Ar}_e$  component on an isochron plot may be prevented by  
422 scattered data, which results from  $^{40}\text{Ar}_e$  with an inhomogeneous isotopic ratio (e.g., inclusions;  
423 Reddy et al., 1997) or, possibly, clustered data resulting from homogenization with radiogenic  
424 Ar produced in situ (at  $T > T_c$ ). Additionally, anomalously old biotite ages are commonly  
425 calculated from flat ‘plateau’ gas release spectra (e.g., Pankhurst et al., 1973; Roddick et al.,  
426 1980; Sherlock et al., 1999; Skipton et al., 2017). In such cases, there is currently no definitive  
427 test for  $^{40}\text{Ar}_e$  contamination, and DiffArgP modeling does not provide one.

428 DiffArgP can, however, be used to model diffusion of excess Ar from the grain boundary  
429 network into the grain, and comparisons with intra-grain UV laser age spots can shed light on

430 how/when excess Ar may have been incorporated. For example, in white mica from the Oman  
431 high-pressure terrane, UV laser spot transects revealed Ar enrichment in grain rims (Warren et  
432 al., 2011). The authors ran DiffArgP models in which excess Ar was introduced to the grain  
433 boundary network (the ‘edge age’ in Wheeler, 1996) at different times along the cooling path.  
434 When excess Ar was introduced in the models at ‘low’ temperatures (i.e., temperatures  
435 approaching  $T_c$ ), the modeled core-to-rim age profiles exhibited Ar-enriched grain rims with  
436 anomalously old bulk ages. This led the authors to conclude that the anomalously old white mica  
437 could have incorporated excess Ar late in the cooling history from grain boundary fluids in a  
438 closed system, through diffusion or incorporation during recrystallization (Warren et al., 2011).  
439 In a similar case,  $^{40}\text{Ar}/^{39}\text{Ar}$  UV laser transects conducted across biotite grains from the Italian  
440 Alps yielded dates that increased from core to rim, ranging from ca. 161 to 514 Ma in individual  
441 crystals (Pickles et al., 1997). This age pattern was attributed to diffusion of excess Ar into the  
442 grains at temperatures less than 300°C, as supported by theoretically derived curves for volume  
443 diffusion of Ar (Pickles et al., 1997).

444 Incorporation of  $^{40}\text{Ar}_e$  at high temperatures ( $>T_c$ , in blue zones in Figs. 1–3), at which Ar  
445 diffusion is highly efficient, would theoretically result in diffusive within-grain homogenization  
446 of the excess Ar with radiogenic  $^{40}\text{Ar}$  produced *in situ*. As such, the mica would yield an  
447 anomalously old age and a smoothly decreasing core-to-rim age profile; this has been illustrated  
448 by DiffArgP models of white mica (Warren et al., 2011). Therefore, biotite that yields an  
449 anomalously old age but a smoothly decreasing core-to-rim age profile with no evidence of  $^{40}\text{Ar}$ -  
450 enrichment at grain rims may still contain excess Ar. In this case, biotite would have had to have  
451 incorporated  $^{40}\text{Ar}_e$  during (or prior to) peak P–T conditions in the blue zones in Figs. 1–3, either  
452 via diffusion from  $^{40}\text{Ar}$ -enriched metamorphic fluids, or incorporation during crystallisation in

453 the presence of  $^{40}\text{Ar}$ -enriched fluids. In contrast, excess Ar enrichment of rims is likely to have  
454 occurred at maximum P–T conditions in the red or intermediate zones, such as via low-  
455 temperature diffusion from a  $^{40}\text{Ar}$ -enriched grain boundary network in a closed system. Our P–  
456 T–% retention plots can thus be used in conjunction with the established P–T history to evaluate  
457 scenarios of  $^{40}\text{Ar}_e$  contamination.

458 Figs. 1i, 2c and 2f compare modeled Ar retentivity in biotite (this study) and muscovite  
459 (Warren et al., 2012a) for grain radii of 0.1, 0.5 and 1 mm with 20 Myr residence. The model  
460 data reiterate previously established points: muscovite requires higher temperatures than biotite  
461 to achieve diffusional loss of pre-thermal peak Ar and resetting of  $^{40}\text{Ar}/^{39}\text{Ar}$  systematics, and has  
462 a higher nominal closure temperature. Therefore, the  $^{40}\text{Ar}/^{39}\text{Ar}$  cooling age of biotite should be  
463 younger than that of muscovite in the same rock, provided both minerals grew during the same  
464 metamorphic event within the ‘blue’ P–T zones modeled for biotite (Figs. 1–3) and muscovite  
465 (Figs. 3 and 4 in Warren et al., 2012a). Nonetheless, as discussed above, some paired biotite and  
466 muscovite ages defy this theoretical relationship. In such cases, muscovite may have crystallized  
467 or recrystallized at low temperatures, following cooling through the biotite nominal closure  
468 temperature, i.e., within the ‘red’ P–T zones. A known P–T history is crucial for interpreting this  
469 scenario, together with petrographical evidence of late white mica growth/recrystallization. Mica  
470 chemistry can also be used to elucidate recrystallized, compositionally distinct muscovite rims  
471 (e.g., Cossette et al., 2015). Still, muscovite with no apparent evidence of low-temperature ( $<T_c$ )  
472 growth, compositional zoning or recrystallization has been shown to yield ages younger than  
473 those of co-existing biotite in some cases (e.g., Mottram et al., 2015; Skipton et al., 2017). Due  
474 to the higher solubility of Ar in biotite than muscovite, biotite may preferentially incorporate  
475  $^{40}\text{Ar}_e$  (Roddick et al., 1980; Dahl, 1996; review in Kelley, 2002). Anomalously old biotite ages

476 may result from planar defects in the crystal acting as Ar traps (Camacho et al., 2012). In cases  
477 where biotite yields an older  $^{40}\text{Ar}/^{39}\text{Ar}$  age than co-existing muscovite, obtaining UV laser spot  
478 transects on both minerals would inform considerations of  $^{40}\text{Ar}_e$ , particularly if localized  $^{40}\text{Ar}$ -  
479 enriched zones were revealed. Notably, there are currently few intra-grain age data for biotite  
480 (Hodges and Bowring, 1995; Pickles et al., 1997) or for co-existing muscovite, which might  
481 otherwise be used to further constrain this discussion.

## 482 **5. Conclusions**

483 The models presented here provide numerical and visual illustration of the percentage of Ar  
484 that should theoretically be retained in biotite with a variety of grain radii (0.1 to 5 mm) residing  
485 for various periods (1 Myr to 1 Gyr) over a range of P–T conditions (Figs. 1–3). The models also  
486 demonstrate the effects of different crustal residence temperatures (250–450°C) and durations (1  
487 Myr to 1 Gyr), and of various subsequent cooling rates (1.5–30°C/Myr), on the  $^{40}\text{Ar}/^{39}\text{Ar}$  age and  
488 core-to-rim age profile of biotite (Figs. 4–6). Consequently, the models are effective for  
489 interpreting metamorphic  $^{40}\text{Ar}/^{39}\text{Ar}$  ages and corresponding cooling/exhumation histories in  
490 modern and ancient orogens. As they represent a baseline for %Ar retention,  $^{40}\text{Ar}/^{39}\text{Ar}$  ages and  
491 intra-grain age profiles of biotite that are expected from volume diffusion acting alone, the  
492 models are useful for evaluating the likelihood of extraneous  $^{40}\text{Ar}$  contamination and non-  
493 diffusional  $^{40}\text{Ar}$  loss.

494 The models presented here demonstrate the importance of interpreting  $^{40}\text{Ar}/^{39}\text{Ar}$  ages within  
495 an established P–T–t framework: the dated crystal must have attained peak P–T conditions  
496 within the ‘blue’ zones (Figs. 1–3) in order to yield a cooling age. Petrographic analyses, mineral  
497 chemical maps and an understanding of the P–T evolution are also key to assessing whether mica

498 recrystallization or dissolution may have reset Ar systematics. An  $^{40}\text{Ar}/^{39}\text{Ar}$  biotite age should be  
499 supplemented by a muscovite age from the same rock when possible, which provides an  
500 additional constraint on the cooling/exhumation history, especially in conjunction with P–T–  
501 %retention plots for biotite (this study) and muscovite (Warren et al., 2012a). Paired biotite–  
502 muscovite ages may also provide insights into excess  $^{40}\text{Ar}$  contamination.

503 The modeled core-to-rim age profiles for biotite presented here strongly support the UV laser  
504 spot technique for  $^{40}\text{Ar}/^{39}\text{Ar}$  thermochronological studies. Intra-grain age maps have the potential  
505 to yield a wealth of information, including diffusional core-to-rim age profiles from which  
506 cooling histories can be interpreted, particularly when compared with diffusion models, as  
507 demonstrated in previous studies. UV laser age maps also enable assessment of: excess  $^{40}\text{Ar}$ ;  
508 inherited  $^{40}\text{Ar}$ ;  $^{40}\text{Ar}$  loss via fast-diffusion pathways (anomalously young ages in grain centre);  
509 and, possibly, low-temperature ( $<T_c$ ) diffusional Ar loss from grain rims during long-term crustal  
510 residence.

511 Cooling/exhumation histories, as classically interpreted from  $^{40}\text{Ar}/^{39}\text{Ar}$  data, must be  
512 grounded in theoretical diffusional behaviour, as quantified by DiffArgP modeled bulk ages and  
513 core-to-rim age profiles. The temperature, pressure, time and grain-size parameters used in our  
514 models correspond to many geological scenarios, and the models can therefore be compared with  
515  $^{40}\text{Ar}/^{39}\text{Ar}$  biotite ages to inform interpretations of cooling/exhumation. For geological parameters  
516 beyond those modeled here, we recommend using DiffArgP to model proposed cooling histories  
517 for comparisons with  $^{40}\text{Ar}/^{39}\text{Ar}$  results.

518 The models presented here contain several sources of uncertainty. They are therefore best  
519 used in conjunction with  $^{40}\text{Ar}/^{39}\text{Ar}$  biotite data to provide approximate P–T–t constraints on

520 interpreted cooling/exhumation histories or to highlight alternative scenarios, rather than to  
521 provide a single ‘answer’. Further research to improve constraints on Ar behaviour in biotite will  
522 increase confidence in biotite  $^{40}\text{Ar}/^{39}\text{Ar}$  ages as relating to geological phenomena linked to time,  
523 rather than contamination. In particular, new UV laser  $^{40}\text{Ar}/^{39}\text{Ar}$  spot maps of biotite from  
524 various metamorphic terranes would provide a more complete library of intra-grain Ar  
525 distributions in biotite for comparison with diffusion models, and are an important step toward  
526 developing methodology for identifying and quantifying excess Ar and Ar trapped or lost via  
527 grain defects in biotite.

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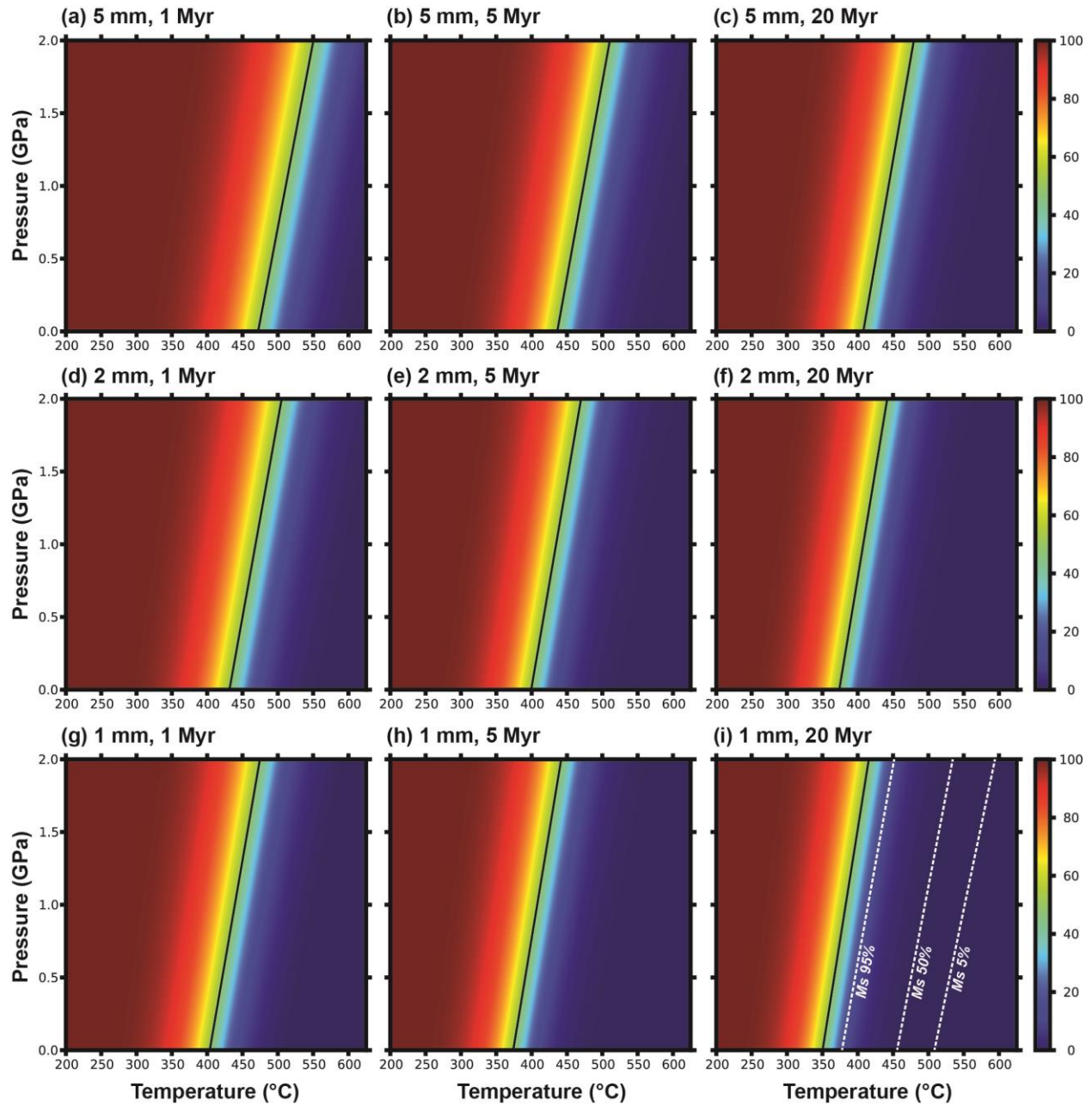
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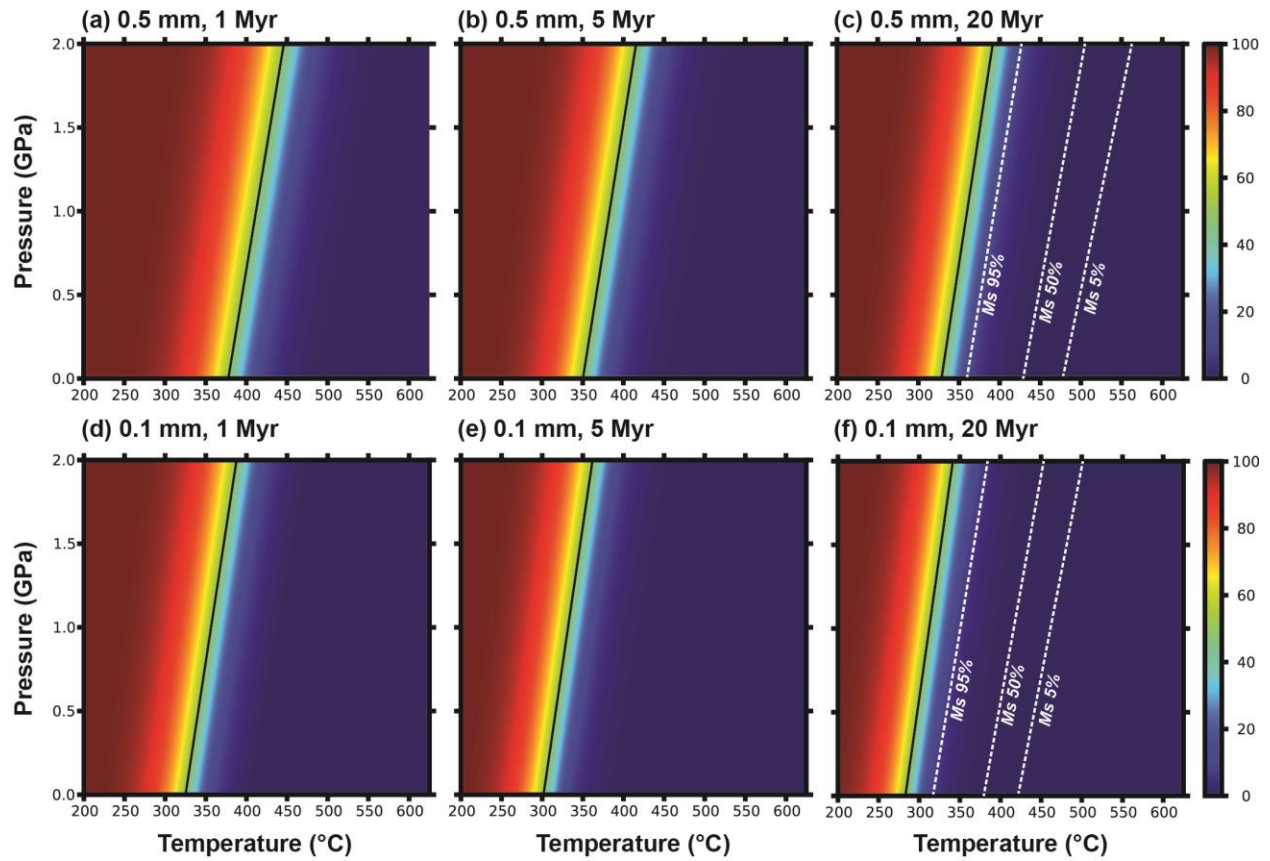
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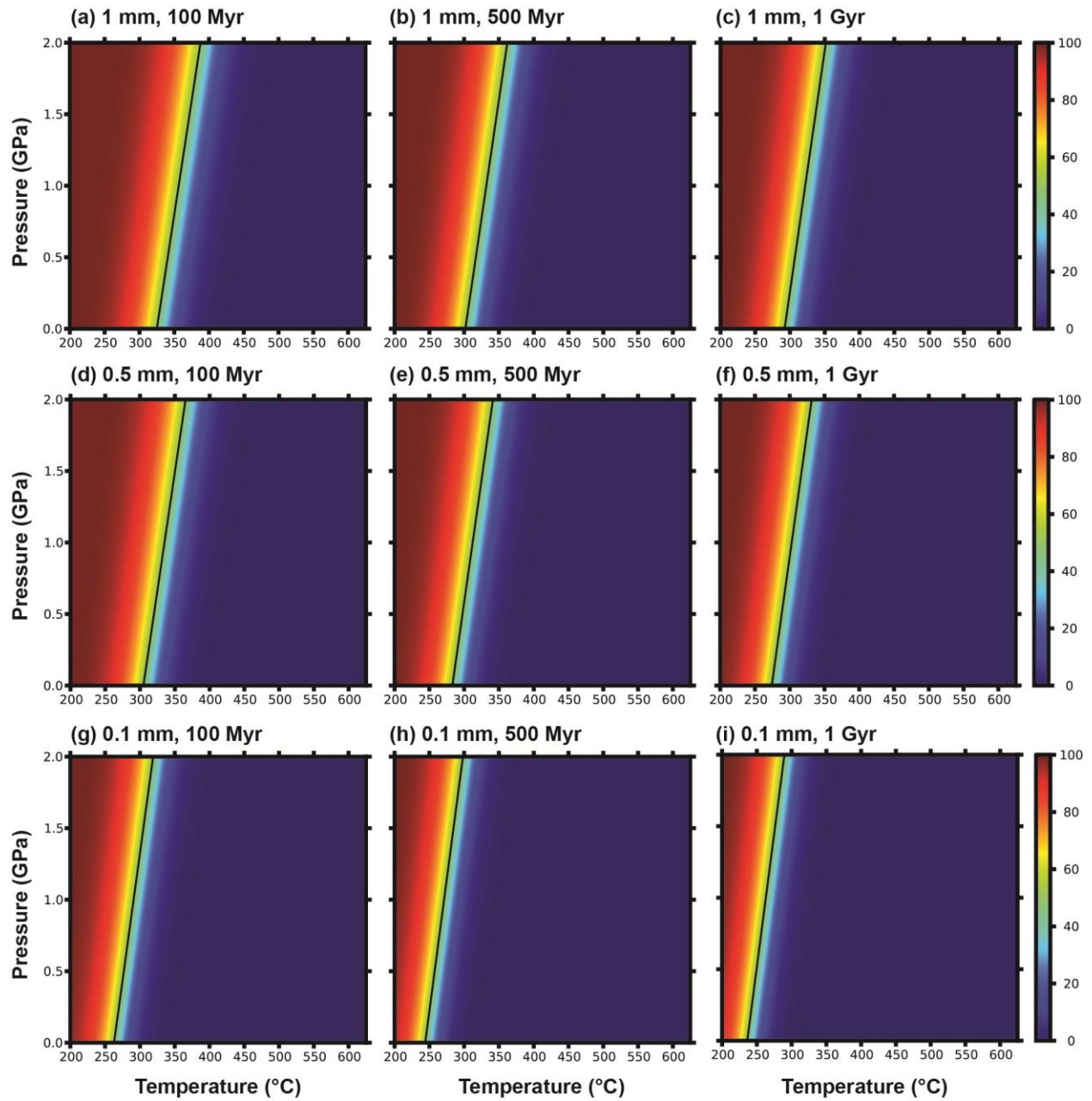
## Figures



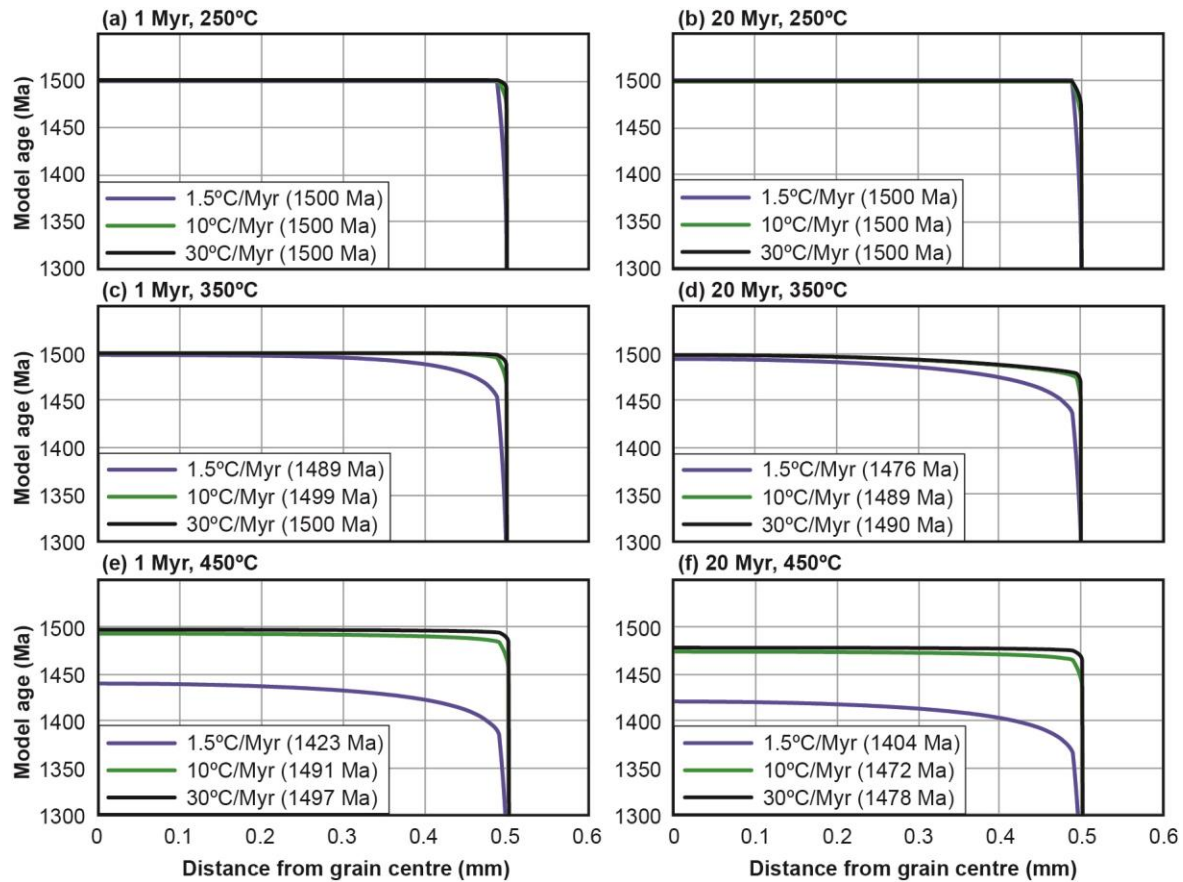
**Fig. 1:** Pressure–temperature diagrams colour coded with percentages of radiogenic Ar retained in biotite, as calculated from numerical diffusion models for biotite grains with radii of 1, 2 and 5 mm residing at the given P–T conditions for periods of 1, 5 and 20 Myr. White dashed lines indicate percentages of radiogenic Ar retained in muscovite, modelled by Warren et al. (2012).



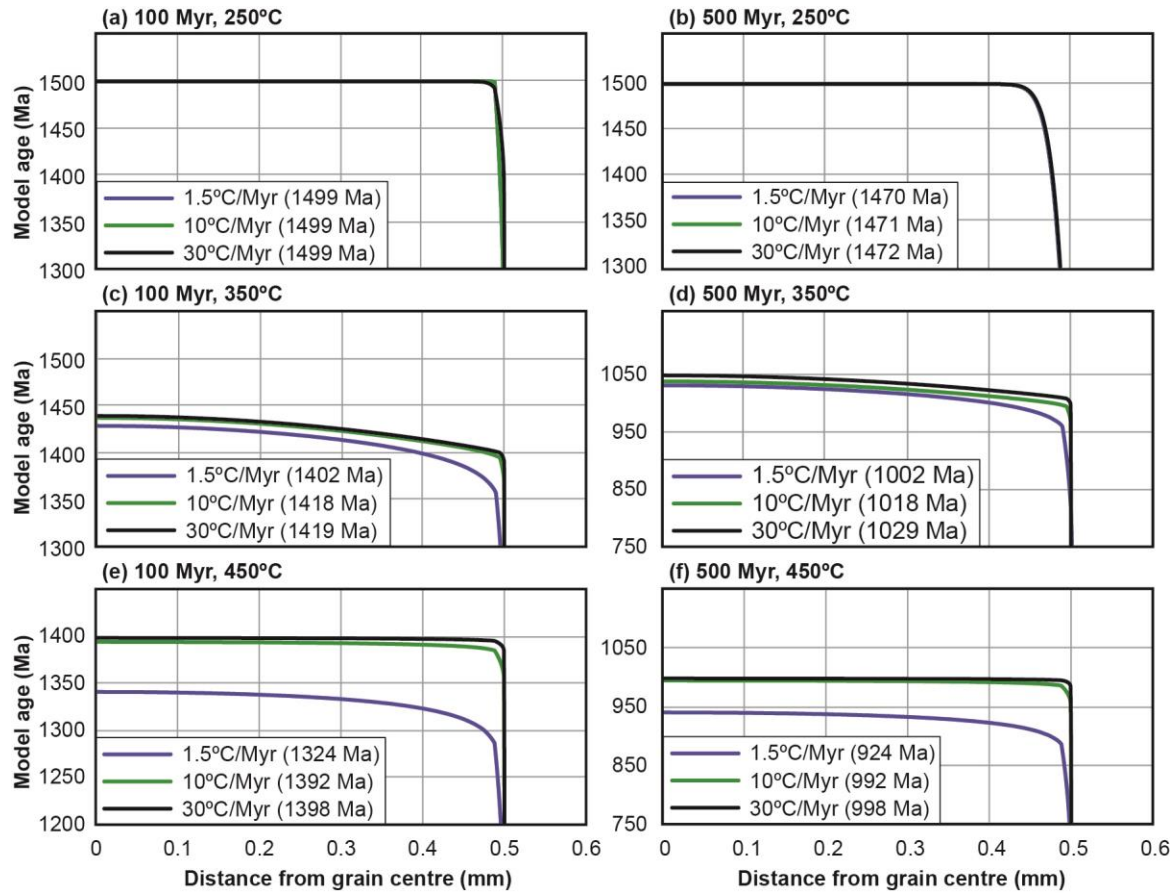
**Fig. 2:** Pressure–temperature diagrams colour coded with percentages of radiogenic Ar retained in biotite, as calculated from numerical diffusion models for biotite grains with radii of 0.5 and 0.1 mm residing at the given P–T conditions for periods of 1, 5 and 20 Myr. White dashed lines indicate percentages of radiogenic Ar retained in muscovite, modelled by Warren et al. (2012).



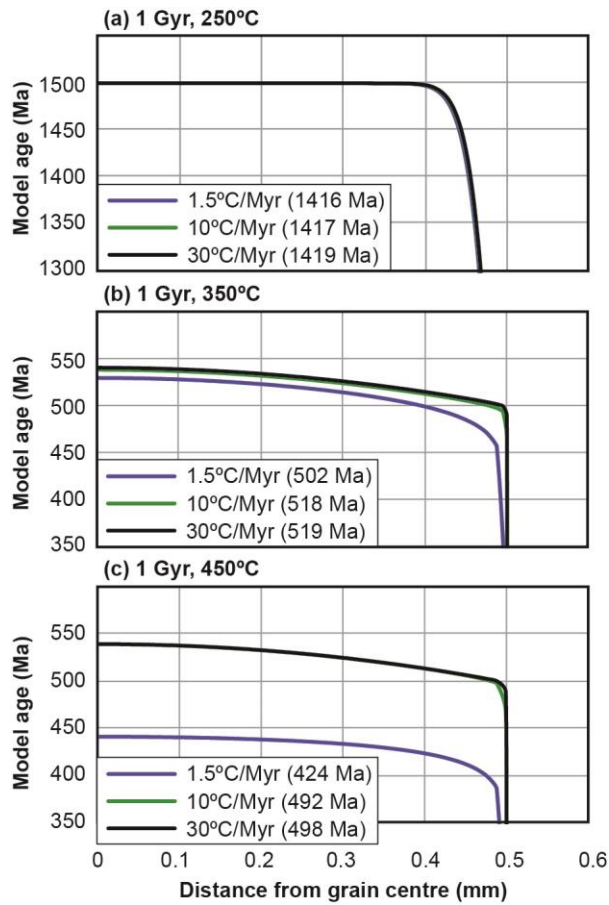
**Fig. 3:** Pressure–temperature diagrams colour coded with percentages of radiogenic Ar retained in biotite, as calculated from numerical diffusion models for biotite grains with radii of 1, 0.5 and 0.1 mm residing at the given P–T conditions for periods of 100 Myr, 500 Myr and 1 Gyr.



**Fig. 4:** Modelled core-to-rim  $^{40}\text{Ar}/^{39}\text{Ar}$  age profiles for 0.5 mm-radius biotite that remained at temperatures of 250°C, 350°C or 450°C for 1 Myr or 20 Myr, then cooled at rates of 1.5°C/Myr, 10°C/Myr or 30°C/Myr. All models were run with an initial pressure of 0.7 GPa, followed by decompression that occurred simultaneously with cooling. Models were run from an arbitrary starting time of 1500 Ma; see text for details. Model bulk ages are shown in parentheses for each cooling rate.



**Fig. 5:** Modelled core-to-rim  $^{40}\text{Ar}/^{39}\text{Ar}$  age profiles for 0.5 mm-radius biotite that remained at temperatures of 250°C, 350°C or 450°C for 100 Myr or 500 Myr, then cooled at rates of 1.5°C/Myr, 10°C/Myr or 30°C/Myr. All models were run with an initial pressure of 0.7 GPa, followed by decompression that occurred simultaneously with cooling. Models were run from an arbitrary starting time of 1500 Ma; see text for details. Model bulk ages are shown in parentheses for each cooling rate.



**Fig. 6:** Modelled core-to-rim  $^{40}\text{Ar}/^{39}\text{Ar}$  age profiles for 0.5 mm-radius biotite that remained at temperatures of 250°C, 350°C or 450°C for 1 Gyr, then cooled at rates of 1.5°C/Myr, 10°C/Myr or 30°C/Myr. All models were run with an initial pressure of 0.7 GPa, followed by decompression that occurred simultaneously with cooling. Models were run from an arbitrary starting time of 1500 Ma; see text for details. Model bulk ages are shown in parentheses for each cooling rate.