

Time-dependent compaction as a mechanism for regular stick-slips

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Abstract

Owing to their destructive potential, earthquakes receive considerable attention from laboratory studies. In friction experiments, stick-slips are studied as the laboratory equivalent of natural earthquakes, and numerous attempts have been made to simulate stick-slips numerically using the Discrete Element Method (DEM). However, while laboratory stick-slips commonly exhibit regular stress drops and recurrence times, stick-slips generated in DEM simulations are highly irregular. This discrepancy highlights a gap in our understanding of stick-slip mechanics, which propagates into our understanding of earthquakes. In this work, we show that regular stick-slips emerge in DEM when time-dependent compaction by pressure solution is considered. We further show that the stress drop and recurrence time of stick-slips is directly controlled by the kinetics of pressure solution. Since compaction is known to operate in faults, this mechanism for frictional instabilities directly relates to natural seismicity.

Plain Language Summary

Earthquakes have a big impact on society, and are therefore intensively studied in laboratory settings. The study of laboratory-scale earthquakes, the so-called stick-slips, generates new insights into the origin and behaviour of earthquakes in nature. At present, computer simulations of stick-slips have not been able to reproduce prominent laboratory observations, which shows that the origin of stick-slips, and of natural earthquakes, is not yet fully understood. In this work, we present computer simulations that succeed to reproduce the laboratory observations, thereby revealing that time-dependent compaction is of great importance to stick-slips and natural earthquakes. These results help to further understand the complex behaviour of earthquakes in nature.

1 Introduction

The risk to society posed by earthquakes world-wide calls for a thorough understanding of the mechanisms driving earthquake nucleation and rupture propagation. Stick-slips have long been recognised as being the laboratory analogue for natural earthquakes (*Brace and Byerlee, 1966*), and are therefore intensively studied to uncover the processes involved in unstable frictional sliding of rock interfaces and of fault gouges, the granular product of rock wear due to fault motion (*Anthony and Marone, 2005; Leeman et al., 2016; Scuderi et al., 2014*). The frictional strength and stability of gouges is often interpreted in a framework of granular flow and force transmission within the aggregate. Most notably, models describing the stability of the so-called “force chains” (discrete groups of grains that support the majority of the imposed load; *Cates et al., 1998; Farr et al., 1997*) have received much attention (e.g. *Rechenmacher et al., 2010; Tordesillas et al., 2011*). During the ‘stick’-phase, when the sample is locked and accumulates elastic strain, the force chains support the external load and sliding of grains is prohibited. When the yield strength of the aggregate is reached, force chains start to collapse or buckle, and a cascade of these events results in macroscopic sample failure, followed by accelerated (unstable) slip. This cycle of formation and destruction of force chains is thought to explain the existence of frictional instabilities (*Daniels and Hayman, 2008; Tordesillas et al., 2009*).

The presence of force chains within dry granular aggregates has been demonstrated both experimentally (*Daniels and Hayman, 2008; Hayman et al., 2011*) and numerically (*Aharonov and Sparks, 2002, 2004; Mair and Hazzard, 2007*), and force chain collapse has been positively correlated with the onset of frictional instabilities (*Daniels and Hayman, 2008*). Many numerical studies employ the Discrete Element Method (DEM) for this particular problem (e.g. *Ferdowsi et al., 2013; Morgan, 2004; Tordesillas et al., 2011*), a numerical technique that is ideally suited to investigate the behaviour of aggregates with a large number of degrees of freedom. By implementing the appropriate physical interactions between

particles, DEM can be employed to simulate and generalise the complex behaviour observed in the laboratory, and test hypotheses regarding the mechanisms of stick-slips. Since the conceptual model of force chain collapse described above is entirely seated on elastic-frictional interactions between discrete particles, standard DEM formulations incorporating these interactions ought to be capable of reproducing the stick-slip behaviour as observed in the laboratory. However, many DEM studies report only irregular stick-slip behaviour, i.e. stress drops of highly variable magnitude and recurrence time (Aharonov and Sparks, 2004; Dorostkar et al., 2017; Ferdowsi et al., 2013; Morgan, 2004), while most laboratory studies report regular stick-slips (Anthony and Marone, 2005; Leeman et al., 2016; Mair et al., 2002; Scuderi et al., 2016; Tinti et al., 2016). This discrepancy reveals a gap in our understanding of stick-slip and earthquake mechanics, and calls for a reappraisal of the force chain conceptual model.

In this study, we show that regular stick-slips with near-constant recurrence time and stress drop can be reproduced in DEM when fluid-rock interactions are incorporated. Following Niemeijer and Spiers (2007) and Chen and Spiers (2016), we consider the interplay between dilatant granular flow and compaction by intergranular pressure solution, which has been proposed by these authors as a mechanism for velocity-weakening behaviour, a requirement for stick-slip behaviour (Gu et al., 1984; Ruina, 1983). By employing the implementation of pressure solution in DEM by Van den Ende et al. (2018), we simulate unstable frictional sliding of fault gouges while systematically varying the kinetics of pressure solution, and we investigate the effect of these fluid-rock interactions on the frictional behaviour of the gouge. Simulations with appreciable pressure solution kinetics display stick-slips with regular recurrence time and stress drop, demonstrating that the interplay between dilatant granular flow and time-dependent compaction leads to periodic unstable sliding. We subsequently relate the frictional properties of the aggregate to the internal distribution of force and stress, and show that compaction by pressure solution leads to a more diffuse transmission of stress so that the stability of individual force chains no longer controls the overall sliding stability of the aggregate. Instead, the stress drop and recurrence time of stick-slips (and earthquakes by analogy) are directly controlled by compaction induced by pressure solution. These results imply that the analysis of force chains may not provide the necessary insights relevant for understanding the frictional behaviour of natural faults that undergo fluid-rock interactions.

2 Numerical methods

To investigate the effect of pressure solution creep on stick-slip behaviour, we simulate laboratory biaxial shear tests numerically using the Discrete Element Method (DEM; Cundall and Strack, 1979). We employ the open-source 3D DEM software package granular LAMMPS (Landry et al., 2003; Plimpton, 1995), which was modified by Marketos (2013) and by Van den Ende et al. (2018). The basic DEM approach is summarised in Supporting Information SI1 (Guo and Morgan, 2006; Hanley et al., 2015; Jiang et al., 2010; Mair and Abe, 2008; Scholtès and Donzé, 2012). For a detailed description of the numerical method and the implementation of intergranular pressure solution in DEM, the reader is referred to Van den Ende et al. (2018). All simulation parameters reported below and in Supplementary Table SI2 are presented in their physical dimensions for easy comparison with laboratory values (see Van den Ende et al. (2018) for details of the adopted scaling procedure).

2.1 Model set-up

First, a sample is generated consisting of 10000 particles, sampled from a uniform size distribution in the range of 10 to 20 μm , enclosed in the vertical direction by two rigid toothed pistons (see Fig. 1). In the horizontal directions, periodic boundaries are employed. During the simulations, a constant, servo-controlled normal stress of $\sigma_n = 5 \text{ MPa}$ is imposed onto the gouge by the top piston. After application of the normal load, the top piston is pulled by a virtual spring in the x -direction at a rate of $10 \mu\text{m s}^{-1}$ to simulate gouge deformation in a biaxial shear configuration. The shear force exerted by the aggregate on the top piston is calculated each time step, from which the shear stress τ is obtained as the shear force divided by the nominal top surface area of the piston.

Each simulation consists of two phases: in the presliding phase, the sample is deformed for 100 s with a high stiffness of the virtual spring, so that sliding is stable and a steady-state shear stress is achieved. Then, the stiffness of the spring is

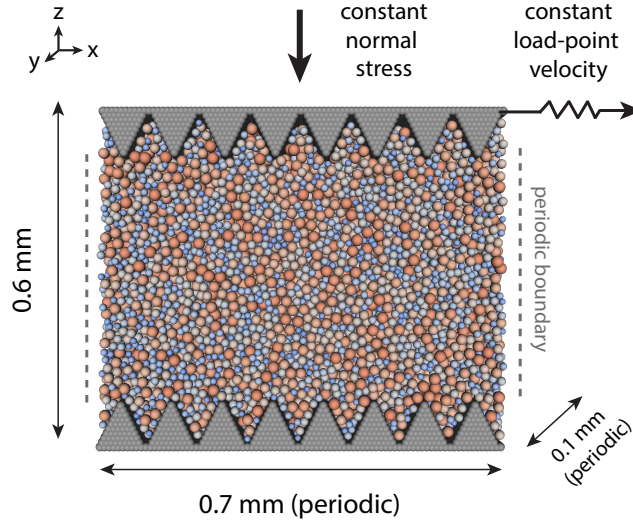


Figure 1: Visualisation of the DEM sample prior to the presliding phase. The gouge particles are colour coded according to their diameter (in the range of 10 to 20 μm).

instantaneously lowered to a value that permits unstable sliding (see *Gu et al.*, 1984; *Ruina*, 1983), and deformation is continued for another 1000 s, during which stick-slips are generated. This procedure is repeated for different values of the pressure solution kinetic constant Z_{ps} of 0, 1.05×10^{-28} , 1.05×10^{-27} , and $5.25 \times 10^{-27} \text{ m}^3 \text{ Pa}^{-1} \text{ s}^{-1}$. A value of $Z_{ps} = 0$ indicates that pressure solution is inactive, and corresponds to previous DEM studies where only elastic-frictional interactions have been considered. Higher values of $Z_{ps} > 0$ indicate faster rates of pressure solution creep, with the maximum value of $5.25 \times 10^{-27} \text{ m}^3 \text{ Pa}^{-1} \text{ s}^{-1}$ corresponding to the kinetics of halite (NaCl) at room temperature (*Spiers et al.*, 1990). A summary of the DEM parameter values is given in Supplementary Table SI2.

During each simulation, the volumetric sample response is continuously monitored. This is done by calculating the bulk sample porosity ϕ from the total mass of the particles present in the system, and the total volume occupied by the sample enclosed by the simulation domain boundaries. The total sample volume is corrected for the volume occupied by the pistons, so that estimates of porosity represent the porosity of the gouge layer itself.

2.2 Contact stress distributions

To better apprehend the effect of non-zero Z_{ps} on the state of the aggregate, it is useful to consider the local distribution of particle contact stresses. To this end, we calculate for each particle contact the maximum compressive force in the direction of shear as $f_c = \sqrt{f_x^2 + f_z^2}$, where f_i is the component of force along the i -coordinate, with $i = x$ being the direction of shear, and $i = z$ being the vertical (shear plane normal) direction. The contact stress is accordingly calculated as $\sigma = f_c/A_c$, with A_c being the area of the circular intersection between two overlapping spheres. Furthermore, the orientation of force/stress is calculated with respect to the direction of shear as $\cos \theta = f_x/f_c$.

3 Results

3.1 Steady-state deformation (preshear)

During the presliding stage (at high spring stiffness), it is observed that the steady-state macroscopic coefficient of friction ($\mu = \tau/\sigma_n$) increases with increasing pressure solution kinetics (Z_{ps}), concurrent with a decreasing overall porosity (see Fig. 2). Furthermore, simulations with higher values of Z_{ps} display smoother friction curves, with fewer and smaller load drops during sliding. For all simulations with $Z_{ps} > 0$, the nett volumetric behaviour is compactive, with only the simulation with $Z_{ps} = 0$ being dilatant. It should be taken into account, however, that these simulations experience localisation of shear strain. In the simulation with $Z_{ps} = 0$, the passive region of the sample is stationary, so that the

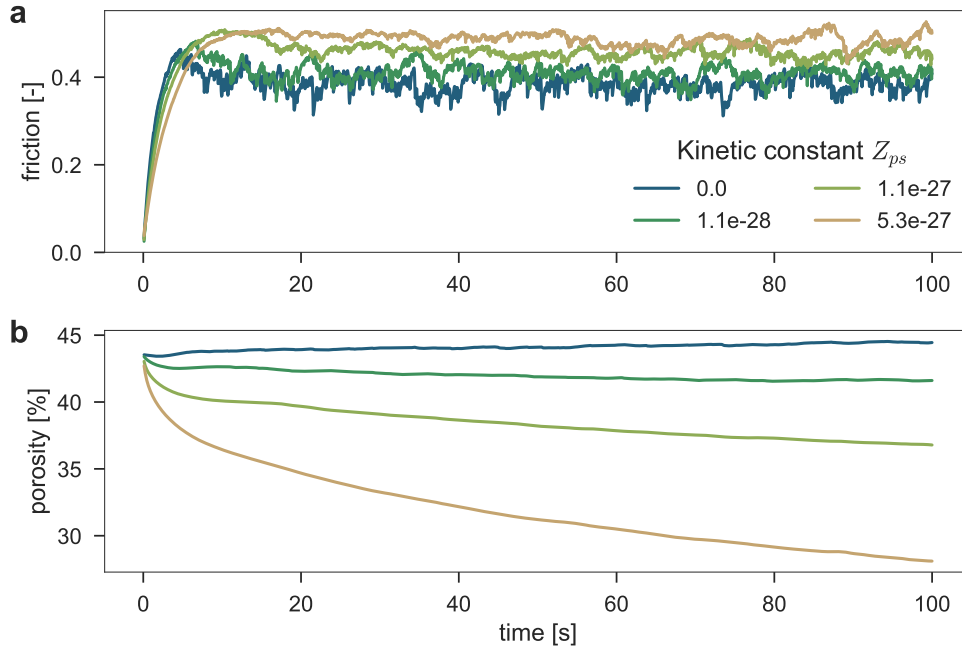


Figure 2: Timeseries of the presliding phase, for different values of the pressure solution kinetic constant Z_{ps} . a) Apparent coefficient of friction ($\mu = \tau/\sigma_n$); b) The volumetric response of each sample, represented by the bulk-averaged porosity.

observed dilatancy is fully attributable to granular flow in the active region. In the simulations with $Z_{ps} > 0$, the passive region continues to compact by pressure solution in the absence of dilatant granular flow, so that the volumetric signal of the active region is obscured by the compaction of the bulk sample.

3.2 Unstable sliding behaviour

When the loading spring stiffness is instantaneously lowered, all samples begin to undergo stick-slip cycles (Fig. 3). The stick-slip behaviour of the simulation with $Z_{ps} = 0$ is exemplary to stick-slips commonly observed in DEM, exhibiting stress drops of highly variable recurrence time and magnitude. This is similarly reflected by the volumetric response of the sample, showing irregular and non-systematic timing of compaction and dilatation at porosities near 45 %. There is no indication that the stick-slip behaviour of the simulation with $Z_{ps} = 0$ will eventually evolve towards a more regular, repeating stick-slip sequence.

By contrast, all simulations with $Z_{ps} > 0$ show a pattern of periodically repeating stick-slips, all exhibiting a near-constant stress drop after a brief run-in of a few cycles. Simulations with higher values of Z_{ps} show longer recurrence times and correspondingly larger stress drops. The sample volumetric behaviour mirrors that of the friction coefficient, showing compaction during the stick-phase, and rapid dilatation during the slip-phase. Due to localisation, the behaviour is nett compactive, but the repetitive succession of compaction during the stick and dilatation during slip is persistent. As compaction of the bulk gouge decelerates with decreasing porosity, volumetric response of the active zone becomes more prominent in the porosity evolution (Fig. 3h). Overall, the volumetric behaviour of the passive zone does not influence the stick-slip cycle behaviour.

The sample stick-slip behaviour can be characterised by considering the friction drop $\Delta\mu$, the preceding stick duration Δt , and the maximum dilatancy $\Delta\phi$ associated with each slip event (Fig. 4). Particularly for the two simulations with the lowest values of Z_{ps} , there is substantial scatter present in the data set, but the median values of each data set consistently show positive relations between each of the aforementioned quantities. What is also clearly noticeable in Fig. 4b and d, is that there is no clear relationship between stress drop and recurrence time on the one hand, and dilatation on the other for the simulation with $Z_{ps} = 0$, as noted earlier (see Fig. 3a and b). With increasing value of $Z_{ps} > 0$, the amount of compaction (and accordingly the amount of dilatation) increases, leading to a larger friction drop and recurrence time.

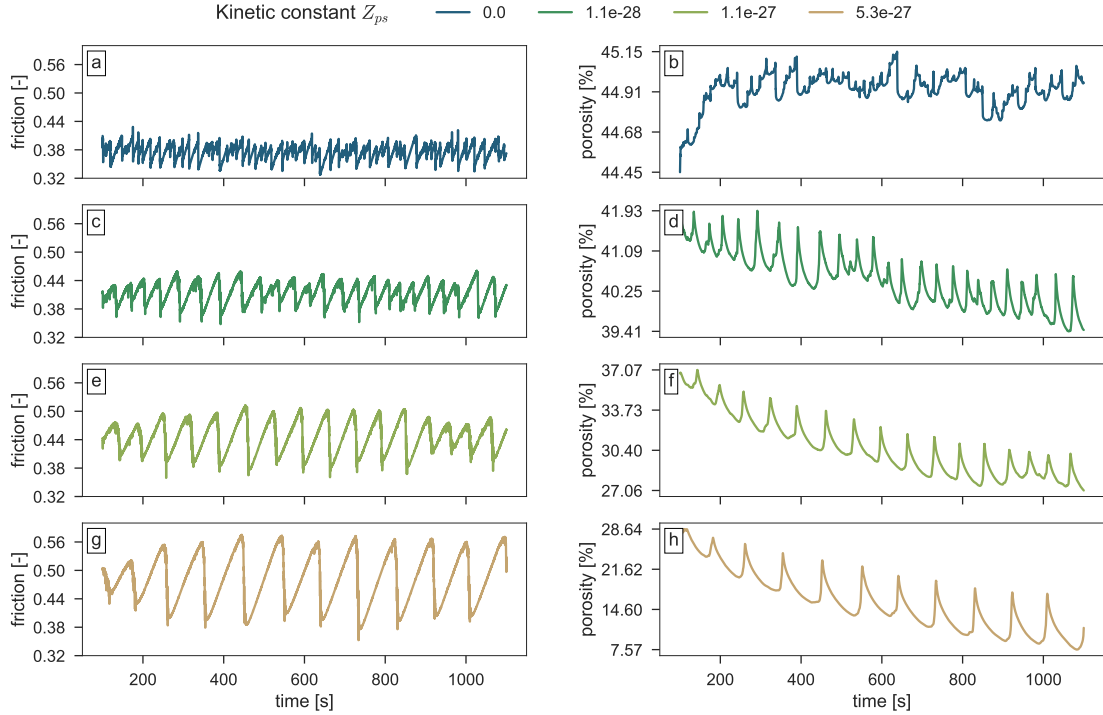


Figure 3: Timeseries of stick-slip behaviour for all simulations. Left panels: coefficient of friction (τ/σ_n); Right panels: sample porosity. The values of the pressure solution kinetic constant Z_{ps} are as indicated in the figure legend. Note that the porosity data is plotted on different vertical scales.

4 Discussion

4.1 Comparison with previous work

Most commonly, 3D DEM studies of biaxial shear deformation of dry aggregates observe a macroscopic friction coefficient in the range of 0.2-0.5 (e.g. *Dorostkar et al., 2017; Guo and Morgan, 2004; Mair and Hazzard, 2007*). This value has been found to be controlled by geometric quantities such as particle dimensionality (*Frye and Marone, 2002*) and particle shape (*Guo and Morgan, 2004*). Our values of friction fall within this range, though our results also show that higher values of Z_{ps} systematically produce higher friction values. Likewise, the volumetric sample response for the simulation with $Z_{ps} = 0$ is broadly similar to previous DEM studies, exhibiting irregular excursions in sample porosity around a given mean value during stick-slip (e.g. *Dorostkar et al., 2017; Morgan, 2004*). By contrast, the simulations with $Z_{ps} > 0$ show a much clearer relation between stress and porosity during each stick-slip cycle, in a way that has not been previously reported.

4.2 Contact stress distribution

To compare the stress distributions for the different simulations, each exhibiting vastly different values of porosity ϕ and mean particle contact area, we compute probability density functions of the particle contact stress σ normalised by its bulk mean value $\langle\sigma\rangle$, as well as the orientation distribution of σ (Fig. 5). As opposed to absolute probability, the probability density may exceed a value of 1, with higher values indicating a larger proportion of particle contacts exhibiting a particular value of stress.

When compaction by pressure solution is absent ($Z_{ps} = 0$), the contact stresses cluster narrowly around the mean value (Fig. 5a), largely independent of the stress orientation (as evidenced by a discrete band in Fig. 5b). The contact stress distributions as seen in simulations with $Z_{ps} > 0$ are markedly different from that seen in the simulation with $Z_{ps} = 0$. Instead of exhibiting a peak near the mean value, the contact stress distribution is wide and near-monotonically decreasing

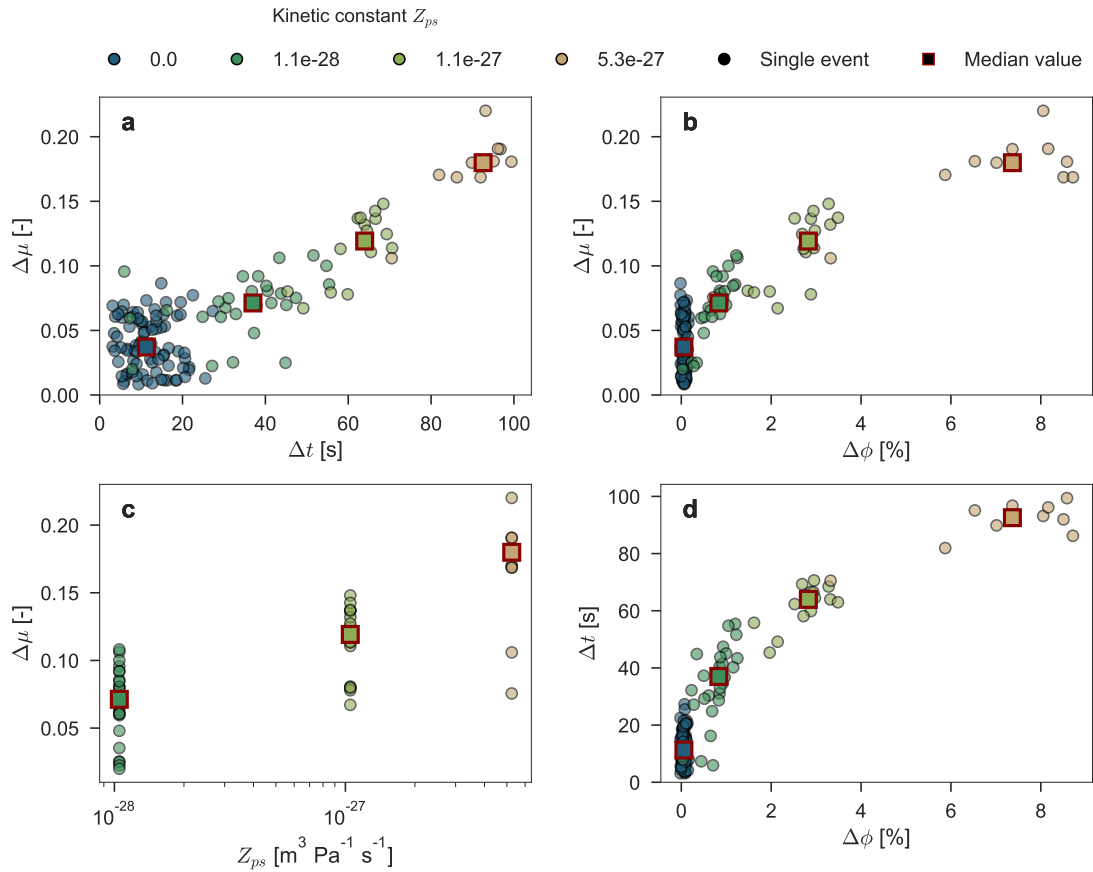


Figure 4: Overview of stick-slip characteristics. a) Friction drop $\Delta\mu$ as a function of preceding stick duration Δt ; b) Friction drop $\Delta\mu$ as a function of the maximum dilatancy $\Delta\phi$ during slip; c) Friction drop $\Delta\mu$ as a function of pressure solution kinetic constant Z_{ps} ; d) Stick duration Δt as a function of the maximum dilatancy $\Delta\phi$ during slip.

towards higher stress values. This suggests that the stress is rather diffusely distributed throughout the aggregate, which has been argued to stabilise force chains present in the system and to inhibit unstable sliding (*Mair et al., 2002*).

The distribution of contact stresses when pressure solution is active can be explained by considering the negative feedback loop induced by pressure solution creep: when the stress on the contact is locally high, the rate of pressure solution is fast and so the contact area grows rapidly due to particle convergence. As a result, local concentrations of contact stress diminish and cease to exist. This has been demonstrated quantitatively by *Van den Ende et al. (2018)* for uniaxially compacting aggregates. Overall, pressure solution negatively impacts the formation of isolated force chains, so that force chain collapse is unlikely to constitute the observed stick-slip behaviour.

4.3 The origin of regular stick-slips

Classically, conceptual models for the occurrence of (repeating) earthquakes revolve around the notion that faults strengthen during interseismic times, and that the instability (the earthquake) occurs when the tectonic stress exceeds the shear strength of the fault. If laboratory stick-slips are truly analogous to natural earthquakes, then the same mechanism is expected to apply for stick-slips. However, at the scale of a laboratory aggregate, the force chain collapse model is generally preferred, which does not involve time-dependent strengthening as envisioned for natural seismic cycles.

In our DEM simulations, we observe prominent compaction during the stick-phase, and dilatation during slip. As has been demonstrated by laboratory friction tests (*Karner and Marone, 2001; Richardson and Marone, 1999*) and by analytical models (*Chen and Spiers, 2016*), densification is positively correlated with aggregate strength, and so the observed compaction translates into a time-dependent increase in shear strength. Due to continuous loading at the

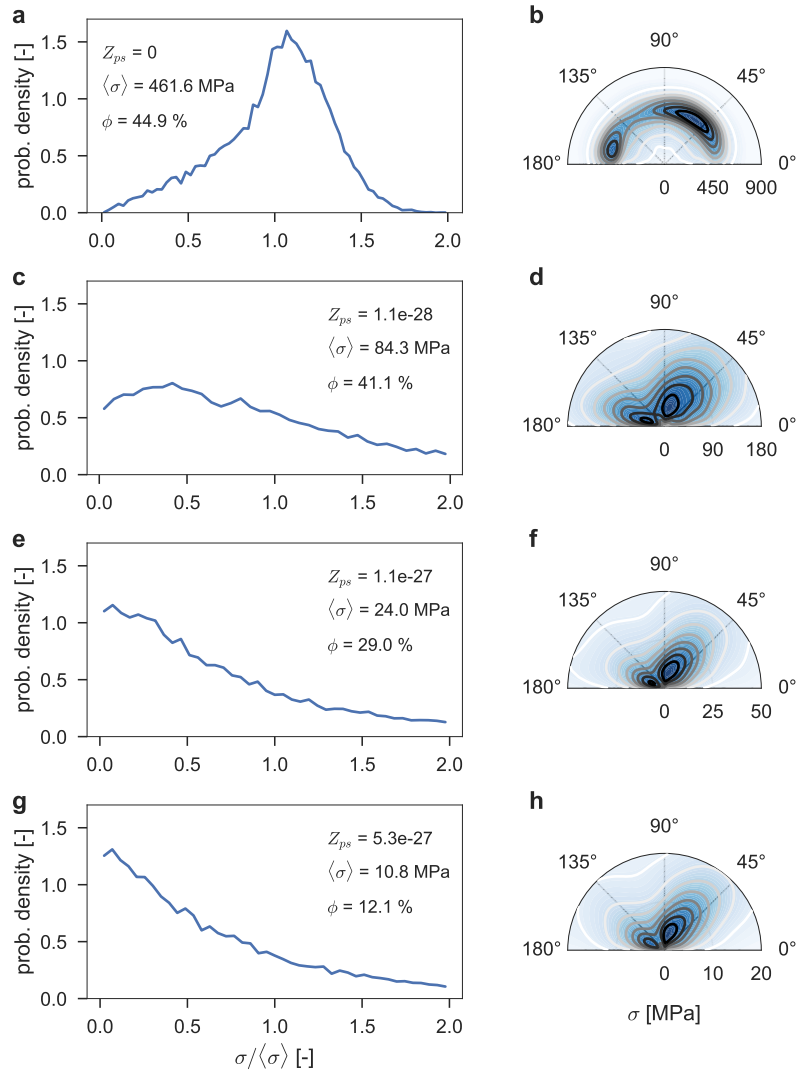


Figure 5: Contact stress distributions (left panels) and orientations (right panels) defined relative to the direction of shear. The value of the kinetic constant Z_{ps} , mean stress $\langle \sigma \rangle$, and porosity ϕ are as indicated for each simulation in the left panels.

load-point, the stress exerted on the aggregate increases during the stick-phase. When the shear stress acting on the gouge exceeds the aggregate strength, an instability is triggered and the sample slips. During accelerated slip, granular flow induces dilatation and weakening in the sample, and the cycle repeats. This conceptual model of a stick-slip cycle is generally compatible with present models for the natural seismic cycle (*Sleep and Blanpied, 1992; Van den Ende et al., 2017*), and is an outcome of the microphysical models proposed by *Niemeijer and Spiers (2007)* and *Chen and Spiers (2016)*, which are seated on the same physical principles (pressure solution and granular flow) as the DEM simulations presented here. One key aspect in this conceptual model is the process of gouge compaction during the stick-phase.

When pressure solution is operative, time-dependent strengthening of the aggregate by compaction is expected to dominate over local variations in packing density and stress distribution, so that the overall stress drop and recurrence time are one-sidedly controlled by the volumetric evolution of the aggregate (i.e. compaction during the stick-phase, and dilatation during slip). As a result, the stress drop and recurrence time are regular in magnitude. Conversely, in the absence of compaction by pressure solution, local variations in packing density and contact stress (and correspondingly the presence of isolated force chains) are expected to determine the irregular stick-slip behaviour as seen when $Z_{ps} = 0$, as there exists no mechanism to counteract or dominate over the local random fluctuations.

The results presented here indicate that a time-dependent strengthening mechanism is required to explain the stick-slip

behaviour observed in laboratory experiments. In our DEM simulations, this strengthening mechanism is provided by time-dependent compaction by pressure solution, but alternative processes, such as microcracking (Atkinson, 1984; Brantut *et al.*, 2013), or plastic creep (Dieterich and Kilgore, 1994; Scuderi *et al.*, 2014), could be considered depending on the test material and conditions. Our results further imply that time-dependent strengthening mechanisms, rather than time-independent force chain dynamics, likely constitute the frictional behaviour of natural faults. Laboratory and DEM studies should therefore focus on the quantification and analysis of micro-scale processes that facilitate gouge strengthening, like the ones mentioned above.

5 Implications and concluding remarks

Numerous field geological studies have convincingly demonstrated that pressure solution creep and granular flow are dominant deformation mechanisms within faults at seismogenic depths (Chester *et al.*, 1993; Hadizadeh *et al.*, 2012; Holdsworth *et al.*, 2011; Smeraglia *et al.*, 2017). These deformation mechanisms have similarly been identified in laboratory friction experiments performed under (seismogenic) conditions that favour pressure solution creep (Bos *et al.*, 2000; Chen *et al.*, 2015; Niemeijer and Spiers, 2006), and have been argued to govern velocity-weakening behaviour and stick-slip instability nucleation (Chen and Spiers, 2016; Niemeijer and Spiers, 2007). Our simulations show that the interplay between dilatant granular flow and non-dilatant pressure solution indeed generates stick-slips as reported by laboratory studies, as envisioned in microphysical models, and supported by field observations.

Encouraged by the above, we will now broaden our interpretation of the mechanics of stick-slip to discuss the implications for natural seismicity. In our simulations with constant displacement rate, the kinetics of pressure solution control the recurrence time and stress drop of the unstable slip events through the amount of compaction achieved during the interseismic period and correspondingly the amount of dilatation during accelerated slip. This offers important constraints on the stress drop in the absence of dynamic weakening (see Tullis, 2007), which is highly relevant for slow slip events (Gomberg, 2010; Rogers and Dragert, 2003) and (induced) microseismicity. Furthermore, if the kinetics of pressure solution control the recurrence interval of natural earthquakes, spatial variations in pressure solution rates due to variable temperature, mineralogy, and pore fluid chemistry will produce spatially heterogeneous seismicity distributions. Therefore, laboratory experiments designed to quantifying the rate of gouge compaction (such as uniaxial compaction tests; e.g. *Pluymakers and Spiers*, 2014), will provide constraints on the amount of compaction expected during interseismic times under in-situ fault conditions, which in turn may grant important insights into spatial and/or temporal variability of natural earthquakes. Laboratory estimates of the kinetics of pressure solution (i.e. Z_{ps}) can be used as direct input for numerical models.

Lastly, the capability of DEM to capture the mechanics of earthquake nucleation strongly solicits for a detailed investigation of the nucleation process using this numerical method. Among others, two potential venues of investigation are the study of precursory phenomena (e.g. *Ferdowsi et al.*, 2013), and the mechanical effects of an (undrained) fluid phase (e.g. *Catalano et al.*, 2014; *Dorostkar et al.*, 2017). Both of these subjects are challenging to address in laboratory experiments, as details of the local microstructure, state of stress, and fluid pressure are generally not available. In this way, the DEM approach presented in this work offers means to complement previous field, laboratory, and model studies concerning earthquake nucleation.

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