How do normal faults grow?

Atle Rotevatn\textsuperscript{a}, Christopher A.-L. Jackson\textsuperscript{b}, Anette B.M. Tvedt\textsuperscript{c}, Rebecca E. Bell\textsuperscript{b},
Ingvild Blækkan\textsuperscript{a}

\textsuperscript{a}Department of Earth Science, University of Bergen, PO Box 7800, 5020 Bergen, Norway
\textsuperscript{b}Basins Research Group (BRG), Department of Earth Science & Engineering, Imperial College, Prince Consort Road, London, SW7 2BP, UK
\textsuperscript{c}Petrolia NOCO AS, Espehaugen 32, 5258 Blomsterdalen, Norway

*corresponding author: atle.rotevatn@uib.no (A. Rotevatn), phone: +47 48109959.

Keywords: normal fault; fault growth; isolated fault model; propagating fault model; coherent fault model; constant-length fault model; fault scaling

Abstract

Normal faults grow via synchronous increase in displacement and length (‘propagating fault model’, also known as the ‘isolated fault model’), or by rapid length establishment and subsequent displacement accrual (constant-length fault model). We here use time-series displacement (D) and length (L) data from natural and experimental faults to elucidate growth styles and D-L trajectories throughout fault life, and to assess the applicability of the two fault models. We show that the growth of most faults is characterized by two stages, with the first defined by fault lengthening (20-30\% of fault lifespan) and the second by displacement accrual (70-80\% of fault lifespan). Although broadly adhering to the constant-length model, fault growth throughout the lengthening stage, during which significant displacement (10-60\% of the total end-of-life fault displacement) may also accumulate, is achieved through rapid tip propagation, relay breaching, and segment linkage, characteristics perhaps most intuitively thought to reflect growth in accordance with the propagating model. The subsequent growth stage is dominated by displacement accrual with limited lateral tip propagation, a phenomenon best described by the constant-length model. We also show that, despite being used primarily in support of the propagating
1. Introduction

There are currently two often-used models describing the growth of normal faults, herein termed the ‘propagating’ and ‘constant-length’ fault models (e.g., Walsh et al., 2002; Walsh et al., 2003; Nicol et al., 2005; Jackson and Rotevatn 2013; Henstra et al., 2015; Fossen and Rotevatn 2016; Hemelsdaël and Ford 2016; Nicol et al., 2016; Tvedt et al., 2016; Childs et al., 2017; Jackson et al., 2017) (Fig. 1). The propagating model (also referred to as the ‘isolated fault model’; see e.g. Jackson & Rotevatn 2013; Childs et al., 2017) suggests fault growth occurs via a synchronous increase in fault length and displacement (e.g., Walsh and Watterson 1988; Dawers et al., 1993; Cartwright et al., 1995; Walsh et al., 2003), whereas the constant-length model suggests faults establish their near-final lengths early in their slip history, after which they grow mainly by displacement accrual (e.g., Walsh et al. 2003; Nicol et al., 2005; Jackson and Rotevatn 2013). To our knowledge, structural geology textbooks do not consider the constant-length model in their treatment of normal fault growth; instead, they focus entirely on propagation models (e.g., Davis et al., 2011; Fossen 2016). In the authors’ opinion, it is therefore fair to say that the constant-length model is less well-known to the general structural community, outside of those specialising in fault growth. Because of this, we suggest there is a bias in favour of the propagating model in the earth science community overall, despite the mounting body of evidence to support the constant-length fault model (e.g., Nicol et al., 2010; Giba et al., 2012; Jackson et al., 2017; Rotevatn et al., 2018).

Understanding how normal faults grow is important for a range of earth science disciplines, with the styles and rate of tip propagation controlling, for example, the tectono-stratigraphic development of sedimentary basins (e.g., Gawthorpe and Leeder 2000; Ge et al., 2017; Henstra et al., 2017; Jackson et al., 2017), and the location, magnitude, and recurrence interval of potentially hazardous earthquakes (Walsh et al., 2003; Nicol et al., 2005; Soliva et al., 2008; Nicol et al., 2010). Despite mounting evidence in support of the constant-length model, the character of the initial lengthening stage remains unclear, including its duration (relative to the total lifespan of the fault) and its structural evolution (including growth pattern of faults), since few
studies have been able to provide insight to the details of this early, relatively short-lived stage of fault growth (Schlagenhauf et al., 2008; Nixon et al., 2016).

Motivated by this, we here review the wealth of data published on fault length and displacement over the last 40 years and interpret new data from natural and experimental fault systems to investigate how a fault migrates through displacement-length (D-L) space as it grows. Using this data compilation we compare and contrast how these real and simulated faults behave in comparison to the often-used normal fault growth models described above. Using time-series fault displacement and length (D-L) data, we demonstrate that both models are applicable to the growth of normal faults, with each describing temporally distinct aspects of fault behaviours observed in nature and experiments. We conclude that most ancient normal faults, for which appropriate kinematic constraints are available, are characterized by: (i) an initial stage of length establishment (occurring over a time period of 20-30% of the total fault lifespan), characterized by rapid tip propagation, relay formation, breaching and segment linkage, best described by the propagating model; this stage typically also involves accumulation of 10-60% of the final fault displacement; (ii) a subsequent stage of displacement accrual without significant further fault lengthening, best described by the constant-length model (occurring over a time period of ~70-80% of the total fault lifespan). We also show that, despite being implicitly or explicitly used in support of the propagating fault model, in the scientific literature (e.g., Cartwright et al., 1995; Dawers and Anders 1995) and structural geology textbooks alike (e.g., Fossen 2016), global displacement-length (D-L) datasets (e.g., Marrett and Allmendinger 1991; Cowie and Scholz 1992b; Cowie and Scholz 1992a) are equally compatible with the constant-length fault model.

Using natural examples to document the structural and kinematic characteristics of the initial stage of fault propagation and lengthening may achieve significant future advances in our understanding of how normal faults grow. This stage is presently poorly documented and thus insufficiently understood due to: (i) a lack of reliable, preserved constraints from syn-kinematic growth strata; and/or (ii) the fact that any growth strata deposited during the initial, relatively short-lived state of fault growth may simply be too thin to detect using all but the highest-resolution geophysical methods (Jackson et al., 2017).

2. The propagating fault model
The term ‘propagating fault model’ (Fig. 1A) describes the conventional model by which faults grow via a synchronous increase in their displacement and length (Fig. 1C), i.e. the view that when faults accrue displacement they also lengthen by tip propagation and linkage via relay formation and breaching (e.g., Cartwright et al., 1995; Cowie et al., 2000; Kim and Sanderson 2005; Bergen and Shaw 2010). The propagating model is preferred, explicitly or implicitly, by numerous studies using observations from natural fault systems (e.g., Peacock and Sanderson 1991, 1994; Trudgill and Cartwright 1994; Wojtal 1996; Marchal et al., 1998; Morewood and Roberts 1999; Dawers and Underhill 2000; Gawthorpe and Leeder 2000; McGill et al., 2000; McLeod et al., 2000; Young et al., 2003; Soliva and Benedicto 2004; Commins et al., 2005; Hus et al., 2006; Bastesen and Rotevatn 2012), numerical modelling (e.g. Crider and Pollard 1998; Gupta et al., 1998; Cowie et al., 2000) and analogue models (e.g., McClay 1990; McClay and White 1995; Ackermann et al., 2001; Clifton and Schlische 2001; Mansfield and Cartwright 2001; Acocella et al., 2005; Bellahsen and Daniel 2005). What we herein refer to as ‘the propagating model’ is also sometimes referred to as the ‘isolated model’ (e.g., Jackson & Rotevatn 2013; Childs et al. 2017), despite this term originally being used by Walsh et al. (2003) to describe the degree of kinematic and geometric coherency within a fault system, and not the presence or absence of tip propagation.

The propagating model is largely based on the observation that, when plotted in log-log space, fault displacement and length data appear strongly positively correlated across several orders of magnitude. This empirical relationship is described as \( D = cL^n \), where \( D \) is maximum fault displacement, \( L \) fault-trace length, \( c \) a constant, and \( n \) falls between 1 and 1.5 (e.g., Walsh and Watterson 1988; Marrett and Allmendinger 1990; Marrett and Allmendinger 1991; Cowie and Scholz 1992b; Marrett and Allmendinger 1992; Dawers et al., 1993; Schlische et al., 1996; Schultz et al., 2008; Torabi and Berg 2011; Rotevatn and Fossen 2012). Regardless of the exact value of \( n \), the empirical relationship between \( D \) and \( L \) has historically been assumed to suggest that an increase in fault displacement (\( D \)) is associated with a corresponding increase in fault length (\( L \)) (Watterson 1986; Morley et al., 1990; Peacock and Sanderson 1991; Cowie and Scholz 1992b; Cowie and Scholz 1992a; Cartwright et al., 1995; Dawers and Anders 1995; Huggins et al., 1995; Peacock and Sanderson 1996; McLeod et al., 2000; Mansfield and Cartwright 2001; Rykkelid and Fossen 2002; Kim and Sanderson 2005; Baudon and Cartwright 2008). In addition to fault
displacement and length being positively correlated, support for the propagating fault model includes: (i) the occurrence of breached relays and multiple displacement minima along strike of normal faults (e.g., Gawthorpe and Leeder 2000); and (ii) theoretical fracture mechanics, which predicts that for a given rock shear strength, displacement and length must increase linearly (e.g., Cowie and Scholz 1992b). The view that fault growth is achieved chiefly by lengthening and amalgamation of individual segments means the propagating model is also commonly referred to as ‘fault growth by segment linkage’, or derivations thereof (e.g., Cartwright et al., 1995; Cartwright et al., 1996; McGill et al., 2000; Jackson et al., 2002). It would be fair to say that the propagating model has dominated the structural geology and tectonics literature for decades, providing the basis for descriptions of normal fault growth in textbooks (e.g., Davis et al., 2011; Fossen 2016).

Despite the fact it offers a relatively simple and thus appealing explanation of global D-L scaling relationships, there are a number of challenges to the propagating model. First, we know of no examples of presently active or extinct (i.e. ancient) natural fault system, for which robust kinematic constraints have been presented (e.g. growth strata or geomorphic evidence documenting tip propagation and fault lengthening), that present compelling evidence faults are growing or grew in accordance with the propagating fault model over geological timespans (i.e. $10^4-10^6$ years; Jackson et al., 2017). Second, the propagating model appears incompatible with the (generally much lower) displacement-length ratios of individual earthquakes (e.g., Wells and Coppersmith 1994; Walsh et al., 2002; Nicol et al., 2005).

3. The constant-length fault model

The notion that major, through-going normal faults can ‘rapidly’ form was first fully discussed in the seminal paper by Cowie (1998). A similar, rapid-establishment theme is characteristic of the ‘constant-length fault model’ (Fig. 1B), which was conceived and developed in a series of papers published from 2002 onwards. At least partly motivated by the incompatibility between fault and earthquake D-L scaling properties, Walsh et al. (2002) presented what was initially termed an “alternative model” for the growth of normal faults. They argued that, contrary to the propagating model, in which displacement and length increase in concert, “(…)fault lengths are near constant from an early stage and growth is achieved mainly by increase in cumulative displacement” (Fig. 2D). The term ‘constant fault-length model’ was
subsequently coined by Nicol et al. (2005), to explicitly capture the fact that, for much of their life, the studied faults experienced displacement accumulation rather than lengthening (Walsh et al., 2002).

Most early work on the constant-length model was based on the analysis of growth strata preserved next to relatively large (e.g., several kilometres in length, several hundreds of metres of displacement), ancient faults imaged in 3D seismic reflection data (Meyer et al., 2002; Walsh et al., 2002). Mounting support for the constant-length fault model came from similar, seismic reflection-based studies (e.g., Giba et al., 2012; Jackson and Rotevatn 2013; Tvedt et al., 2016; Jackson et al., 2017), as well as from numerical models (e.g., Finch and Gawthorpe 2017) and analogue models (e.g., Schlagenhauf et al., 2008). Recent work has also used damage zone geometry, and the scaling properties of exposed, relatively small-scale (i.e. up to several metres of displacement) faults, to provide additional support for the constant-length model (Nicol et al., 2016).

The constant-length model is attractive in that it offers a more dynamic view of D-L scaling relationships (i.e. D-L scaling may change over time as a fault grows; see Cladouhos and Marrett 1996; Rotevatn and Fossen 2012; Nicol et al., 2016), as well as offering an explanation for the apparent mismatch between fault and earthquake-rupture scaling relationships (Nicol et al., 2005). However, the constant-length model initially appears at odds with the observation that relatively few ancient faults plot below the regression trendline plotted in global D-L compilations; such faults should at least theoretically occur if we assume some ancient faults became inactive early in their development, shortly after the initial stage of lengthening, or, in the case of still-active faults that are relatively immature.

Summarized, the constant-length model is built on the main premise that faults propagate to their near-full lengths relatively rapidly (Walsh et al., 2002; Nicol et al., 2016), after which further lengthening is typically retarded due to mechanical fault interactions between adjacent faults and an associated reduction of tip stresses (see also Cowie 1998; Gupta and Scholz 2000). It remains unclear, however, how D and L accumulation during fault growth is partitioned in time. Furthermore, existing work on the constant-length model has focused predominantly structural characteristics and timescales associated with the near-vertical D-L growth paths defining the displacement accrual stage once the (near-)final fault length is established (e.g.,
Motivated by the above review, and the fact the two models have co-existed for ~15 years, we find it timely to critically assess their applicability to describe the growth of normal faults. We therefore address the following key questions: i) how is fault lengthening partitioned in time?; ii) how is displacement accrual partitioned in time?; iii) what is the role of tip propagation and fault linkage throughout fault life? Essentially, these questions all revolve around understanding fault behaviour in D-L space through their lifespans. To address this, we study seismically imaged natural normal faults, in addition to faults generated in analogue models, to extract D-L data through time. D-L data for individual faults through time is key to understanding fault growth, since the global D-L database really only shows a static view, where each data point represents the final stage of what is essentially a fault’s unknown journey through D-L space (Nicol et al., 2010; Rotevatn and Fossen 2012; Nicol et al., 2016).

With these data, and by addressing the above questions, we specifically aim to: (i) elucidate the poorly-documented early lengthening stage of faults exhibiting a broadly constant-length model-type behaviour; (ii) reassess the propagating and constant-length models in an attempt to clarify their applicability to the growth of faults in nature and experiments; and (iii) to suggest some key questions to be addressed in future research.

4. Fault behaviour in D-L space through time

To reveal how faults grow in space and time, we present D-L data extracted at several points in the growth history of natural and experimentally reproduced faults (Fig. 2). Data from natural faults are derived from throw backstripping of, and analysis of growth strata from, syn-sedimentary growth faults from the Egersund Basin, offshore Norway (Tvedt et al., 2013; Tvedt et al., 2016) and the Santos Basin, offshore Brazil (Tvedt 2016) (see cited papers and Jackson et al. 2017 for backstripping method used and justification). Additional D-L data from natural faults were extracted from Meyer et al. (2002), and experimental fault data from published sandbox models (Schlagenhauf et al., 2008) and new plaster models (Blækkan 2016).

The plots of D-L evolution through time (Fig. 2) clearly show that only few natural and experimental faults behave according to the predictions of the propagating
model, i.e. exhibiting a corresponding increase in length as displacement is accrued (see inset i in Fig. 2A). This observation, in concert with those from previous studies (e.g., Cartwright et al., 1996; McLeod et al., 2000; Commins et al., 2005; Hemelsdaël and Ford 2016), suggests that fault growth according to the propagating fault model does occur, but is an end-member behaviour rather than the norm.

Much more commonly, faults exhibit two-part growth trajectories in D-L space that can be split into an early, relatively low-gradient part, and a subsequent, relatively high-gradient part, separated by a moderately well-defined, fairly abrupt inflection point (see inset ii in Fig. 2A). The high-gradient part is typical of fault behaviour according to the constant-length fault model, with the near-vertical growth trends in D-L space representing displacement accrual without significant fault lengthening (Meyer et al., 2002; Walsh et al., 2002). However, the initial, relatively low-gradient parts of the D-L graphs (Fig. 2A) exhibit great variability. For example, the D-L plots in Figure 2 show that the initial lengthening stage often involves not only lengthening, but may also involve (periods of) significant displacement accrual (up to 40-60% of the total end-of-life displacement). The amount of displacement accrual varies, and the gradients in D-L space during this early stage of growth therefore also vary greatly, from relatively gentle, near-flat, constant-length-like gradients to steeper, propagating-like gradients (Fig. 2). These data thus document that, for faults that otherwise behave broadly in accordance with the constant-length model, a wide spread of D-L trajectories is seen during the initial lengthening stage. Such variability and complexity of the initial lengthening stage has, to our knowledge, not previously been demonstrated in other studies advocating the constant-length model (e.g., Walsh et al., 2002). This leads to the question “what style of growth (i.e. instantaneous length establishment vs. lengthening by tip propagation and linkage) characterizes the relatively low-gradient stage seen in the D-L paths, and is this ‘lengthening’ stage adequately captured and understood in the present models for normal fault growth?”.

As discussed by Childs et al. (2017) and Jackson et al. (2017), seismic reflection-based studies may show that faults establish their lengths within the first resolvable time increment but that, because this first resolvable time increment may be longer than the lengthening stage, the lengthening goes undetected. To investigate the lengthening stage further we therefore return to analogue models, in which this early stage of fault growth may be closely monitored and captured. In the following we discuss a plaster experiment (Figs. 3 and 4) of Blækkan (2016), first showing images
of the experiment at relatively long (5-second) time-steps (Fig. 3), before showing the
early stages of the experiment at much shorter (0.5-second) time-steps (Fig. 4). We do
this to mimic having different temporal resolutions of data (i.e. low-resolution data at
5 sec time-steps vs. high-resolution data at 0.5 sec time-steps), which may impact our
understanding of fault growth. For information about the experimental setup, see
Blækkan (2016).

Consider Figure 3, where we show a map-view image showing the evolution of a
large (relative to the scale of the experiment) normal fault (F1) at 5 second intervals
(timesteps T1-T4). Even after the first timestep (T2), F1 has grown across the width
of the model. The faults tips are pinned laterally at the experiment boundary, thus
emulating natural reasons for lateral fault tip pinning, such as the interaction with
other faults (e.g., Nicol et al., 2010). Further timesteps (T3 and T4) are characterised
by displacement accrual, accompanied by relay breaching. Based on viewing the
experiment at a relatively low temporal resolution (i.e. 5 sec timesteps), which we
compare to the limitations of the lowest resolvable time increment from growth strata
when analysing fault growth in the subsurface using reflection seismic and well data,
F1 thus appears to grow in accordance with the constant-length model.

By making the observational increments shorter (i.e. 0.5 secs) we can now
investigate the geometric and kinematic characteristics of the lengthening stage
between timesteps T1 and T2 (i.e. T1a-d; Fig. 4). A fault segment (termed main
core main segment S1; Fig. 4) that nucleates or at least breaches the surface in the western part
of the model during timestep T1a, propagates eastward and lengthens during
timesteps T1b and T1c. Fault lengthening during this stage is largely achieved by the
nucleation, propagation, and linkage of new, smaller segments ahead of the
propagating eastern tip of segment S1. In timestep T1c, a second segment (termed
main segment S2; Fig. 4) nucleates in the eastern part of the model, clearly separate
from the main S1 structure in the west. From timestep T1c to T1d, both tips of S2
propagate. Eastward propagation of S2 is arrested at the model boundary; the western
tip approaches the oncoming and now-rapidly eastward-propagating tip of S1. At
timestep T1d, the two main segments (S1 and S2) remain unlinked, but are
underlapping and approaching one another (sensu Peacock et al., 2017). The final, 0.5
second-long timestep between T1d and T2 sees hard-linkage of smaller S2 segments,
which were soft-linked during T1d, but hard-linked by T2. By T2, S1 and S2 have
overlapped and soft-linked, bounding a relay zone that is eventually breached by T3.
The style of fault growth documented in time steps T1a through T1d (Fig. 4) is similar to that observed in some natural fault systems (e.g., Jackson et al., 2002; Gawthorpe et al., 2003; Young et al., 2003), typified by tip-propagation and segment linkage. These observations demonstrate that for a fault appearing to broadly behave according to the constant-length fault model, tip propagation and segment linkage govern the early, transient, relatively rapid lengthening stage of the fault (cf. Peacock and Sanderson 1991; Cartwright et al., 1995; Walsh et al., 2003). This offers insights into the structural characteristics of the early length-establishment stage, which has rarely or never been fully captured in natural fault systems (see Hemelsdaël and Ford 2016; Nixon et al., 2016).

The example above also highlights that for a given fault, D-L ratios may change abruptly as the fault lengthens by linkage of precursor segments. More specifically, in our case an abrupt increase occurs between T1d (D-L ratio = c. 1.1) and T2 (D-L ratio = c. 1.35) (Fig. 4 and Fig 3) (cf. Cowie 1998). As such, the kinematic significance of D-L ratios recorded on active and inactive faults should be treated with care since they: (i) may change with time on a single structure; and (ii) vary depending on the length-scale considered (i.e. individual segment length immediately before, vs. full fault length immediately after, linkage and establishment of the full fault length) (Rotevatn and Fossen 2012; Nicol et al., 2016).

We now return to the D-L plots discussed initially in this section and shown in Figure 2. The complex D-L paths observed in the lengthening stage may seem very different to the well-known, sub-vertical D-L growth trends presented by Meyer et al. (2002), which were used by Walsh et al. (2002) in support of the constant-length model. However, the extracted D-L paths from Meyer et al. (2002) show that, although sub-vertical growth trends are seen in the right hand part of the curves (Fig. 2D), there is an unresolved precursor stage that involves (i) not only lengthening, but a variable amount of displacement accrual (10-60% of total end-of-life displacement; Fig. 2D) and (ii) overall lower-gradient (compared to the subsequent displacement accrual stage), but somewhat variable trajectories through D-L space (Fig. 2D). This important element of the early-stage growth of normal faults may previously have been gone unnoticed, since D-L data from Walsh et al. (2002) and Meyer et al. (2002) were presented only in log-log space. Plotting such data in log-log space is inherently problematic, as it may unintentionally mask variability and statistical spread. Interestingly, although the D-L paths presented in our study vary greatly, most of the
D-L paths shown in Figure 5 fall within the cloud of the global D-L dataset when plotted in log-log space. This highlights the danger of plotting data on logarithmic scales, and demonstrates how radically different D-L trajectories of faults may effectively ‘hide’ in log-log space. It also shows that one cannot infer ‘typical’ fault growth trajectories in D-L space based on the often-cited correlation of fault displacement and -length over several orders of magnitude. This is so because each fault in the global data base is represented by a single, static, present-day D-L data point, which contains no dynamic information whatsoever about the D-L trajectory throughout the active life of each particular fault (cf. Cladouhos and Marrett 1996).

5. Conclusions and future research challenges

By using D-L data from a range of natural and experimentally reproduced faults, we have demonstrated that propagating (synchronous D-L growth) and constant-length (L-dominated followed by D-dominated growth) fault behaviours occur in nature. The critical point is that the different models appear to describe kinematic behaviours associated with specific times in the evolution of a fault; i.e. the propagating model, defined by tip propagation and segment linkage, characterises the initial, rapid and transient part of the lifespan of most faults, when its growth is dominated by lengthening, whereas the constant-length model characterises the latter part of the faults’ evolution, when growth is dominated by displacement accrual (also see Nicol et al., 2016; Nixon et al., 2016; Finch and Gawthorpe 2017; Jackson et al., 2017; Rotevatn et al., 2018). Importantly, the constant-length model appears to be overall most applicable in the sense that a stage length of establishment is followed by a stage of displacement accrual without further fault lengthening. Our data uncover great variability in the fault D-L gradient paths during the initial lengthening stage; such variability has previously not been shown as previous studies have plotted D-L data in only log-log space.

We thus conclude that normal faults are generally characterized by hybrid growth behaviours whereby a rapid stage of fault propagation, linkage, and lengthening (Stage 1; lengthening stage) is followed by a stage of constant-length displacement accrual (Stage 2; displacement accrual stage); the two stages are generally separated by a relatively abrupt inflection on the D-L curve (Fig. 6). Importantly, the lengthening stage may also involve displacement accrual, and the gradient of the
growth path during this stage may range from sub-vertical (‘constant-length’-type gradient; trajectory ‘a’ in Fig. 6) to sub-horizontal (‘propagating’-type gradient; trajectory ‘e’ in Fig. 6). The detailed growth behaviours seen in the first stage is most adequately captured by the propagating model, in that it involves tip propagation, segment linkage, overall fault lengthening and a variable amount of displacement accrual. The second stage is characterized by displacement accrual and limited fault lengthening. The D-L trajectory during this growth stage is typically sub-vertical, which is characteristic of growth according to the constant-length model (Meyer et al., 2002; Walsh et al., 2002). Fault behaviours demonstrated herein, whereby propagating and constant-length fault growth characterize successive stages of fault evolution, are identified in previous studies (Cowie 1998; Walsh et al., 2002; Jackson and Rotevatn 2013; Horne 2016; Nicol et al., 2016; Finch and Gawthorpe 2017; Rotevatn et al., 2018), although the lengthening stage remains to be more widely elucidated from natural examples.

The duration of each stage presented above remains uncertain. Normal faults analysed by Walsh et al. (2002) and Jackson et al. (2017) established their near-final lengths within 20-33% of their slip history; similarly, the majority of experimental faults in Schlagenhauf et al. (2008) grew to near-final lengths within c. 30% of their model durations. We therefore tentatively conclude that, irrespective of their final size, faults typically spend 20-30% of their lifespan in the lengthening stage (Stage 1), before accruing displacement for the remainder of their slip histories (Stage 2). Similar behaviours are seen in experimental strike-slip fault systems, where establishment of distributed faulting along the full final-length of the slip zone is near-instant, whereas the formation and slip localization onto a fully through-going fault occurs at c. 30-35% of total fault duration (Hatem et al., 2017).

A critical research task to deepen our understanding of normal fault growth lies in undertaking more displacement backstripping studies of seismically imaged growth faults in order to investigate faults’ D-L trajectories through time. Furthermore, new insight may be gained from reassessing the global D-L dataset to sort, examine, and analyse these data based on variables such as tectonic setting, strain rate, and host lithology; this may help us further elucidate setting-specific factors controlling fault behaviour.

A key future research challenge related to the growth of normal faults is to better document the initial lengthening stage described above. Insights may be gained by
integrating high-resolution geophysical imaging techniques (e.g. reflection, sparker, pinger, boomer, and chirp profiling), which allow mapping of fault structure and associated growth strata, and borehole data, which may constrain the age of the growth strata and thus the timescale of fault development (e.g., Taylor et al., 2004; Nicol et al., 2005). Note that, in some active rifts, such as the Gulf of Corinth, Greece (e.g., Nixon et al., 2016; Bell et al., 2017; Gawthorpe et al., 2017), basin underfilling represents a drawback to the investigation of normal fault growth based on the analysis of growth strata (see discussion by Jackson et al. 2017).

Despite our tentative conclusion that the lengthening stage typically endures for 20-30% of fault lifespan, the duration remains uncertain, and more research is needed to fully understand what the notion of ‘rapid’ lengthening (e.g., Walsh et al., 2002) really entails. We speculate that the significant variability of D-L trajectories demonstrated for the lengthening stage (Stage 1) may translate to a similar variability in its duration. We further suggest that investigations into the (relative) duration of the lengthening stage should encompass the full spectrum of fault sizes in nature and experiments, to rigorously test whether duration is linked to fault size, despite the fact that we herein have tentatively concluded that it is not.

Acknowledgements

The geology department at the University of Otago, New Zealand, is thanked for hosting the first author for a research sabbatical, during which time this paper was written. We are grateful for well-considered, constructive, and elaborate comments from journal reviewers Nancye Dawers and Tom Manzocchi, which helped clarify and improve the final version of this paper. The authors would also like to thank colleagues who commented on a preprint version of this paper. We are particularly grateful to Michele Cooke for her insightful review of the preprint, and for enlightening Twitter discussions on fault growth.

FIGURE TEXT CAPTIONS:

Figure 1. Conceptual models for the development of surface-breaching, syn-sedimentary normal fault systems: (a) the propagating fault model (Walsh and Watterson 1988; Cartwright et al., 1995; Dawers and Anders 1995; Huggins et al.,
and (b) the constant-length fault model (Childs et al., 1995; Walsh et al., 2002; Walsh et al., 2003; Giba et al., 2012). The (i) plan-view, (ii) strike-projection and (iii) displacement–length (D–L) plots are shown to illustrate the key geometrical and evolutionary aspects of each model. The black arrows in (ii) show the fault level of the map shown in (i). F1-3, faults 1–3; T1-3, time-steps 1–3. Note that, based on the final fault length (i.e. T3 in i), shape (i.e. T3 in ii) and throw distribution (i.e. T3 in iii), it is difficult to determine which growth model best describes its evolution. (c) Schematic D-L plots through fault life according to the propagating fault model; time steps correspond to those shown in (a). (c) Schematic D-L plots through fault life according to the constant-length fault model; time steps correspond to those shown in (b). (a) and (b) are from Jackson et al. (2017); (c) and (d) are modified from Nicol et al. (2016).

**Figure 2.** Normalized maximum displacement (D) versus normalized fault length (L) plots though fault life for a series of faults. (A) shows data from all faults studied herein, whereas (B), (C), and (D) show selections of the data. The data includes natural faults from Tvedt et al. (2013, 2016), Tvedt (2016), Meyer et al. (2002), faults from plaster experiments by Blækkan (2016) and faults from sandbox experiments by Schlagenhauf et al. (2008). Note that the data from Meyer et al. (2002) carries some uncertainty as the data were manually extracted from the log-log D-L plots in that paper. Inset (i) shows D-L graphs for select faults that exhibit sympathetic D-L growth, i.e. propagating fault growth. Inset (ii) shows D-L graphs from select faults that show clearly separate low-gradient and high-gradient parts, separated by clear inflection points. (B) shows data from natural faults extracted from Tvedt (2016) and Tvedt et al. (2013, 2016). (C) shows data from faults produced in physical analogue models from Schlagenhauf et al. (2008) and Blækkan (2016). (D) shows the data extracted from Meyer et al. (2002); note however that we have added (x, y) = (0, 0) to all the D-L curves, in order to illustrate that each of the vertical D-L graphs in Meyer et al. (2002) have an additional unrecorded and unknown growth stage that is illustrated by dashed lines. See text for full discussion.

**Figure 3.** Plaster experiment of normal fault evolution. Four timesteps, T1 through T4 at 5-second intervals, are shown. Timestep T1 is the experiment at the onset of extension. To the right, displacement-length plots for the fault evolving in the
experiment are shown for timesteps T2 (green), T3 (blue) and T4 (red). Note that the fault seen in T2 already at that stage has established itself across the extent of the model. See Figure 4 for four additional, shorter, 0.5-second timesteps immediately prior to timestep T2, which show the lengthening stage of the fault.

Figure 4. Plaster experiment of normal fault evolution; 4 timesteps are shown at 0.5 second intervals; T1a through T1d. These timesteps cover the 2 seconds leading up to timestep T2 in Figure 3; see Figure 3 caption for further explanation.

Figure 5. Global D-L dataset (grey data points) for faults plotted in log-log space (D-L data extracted from Krantz 1988; Gudmundsson and Bäckström 1991; Cowie and Scholz 1992a, and references therein; Dawers et al., 1993; Cartwright et al., 1995; Schlische et al., 1996; Schultz and Fossen 2002). The D-L paths shown in Figure 2 of this study are also shown. Note most of the different D-L paths from this study plot within the global dataset, despite that these growth paths show a wide range of behaviours (see text for full discussion). This demonstrates that the global correlation of D and L cannot be invoked to support ‘propagating’ fault growth, since ‘constant-length’ and hybrid growth patterns are all fully consistent with, and may hide within, the global D-L database as shown here.

Figure 6. Schematic illustration showing idealized D-L growth trajectories of the end member ‘propagating’ (green) and ‘constant-length’ (blue) fault models, as well as a series of hybrid fault growth trajectories (black). As shown in this paper, few faults follow the propagating or constant-length trajectories; most faults follow D-L growth paths that fall between the end-member models and are characterized by two stages. The first stage is characterized by rapid fault lengthening and a variable amount of displacement accrual, and is best described by the propagating model since it is associated with lengthening achieved by tip propagation, relay formation and breakdown, segment linkage and amalgamation to ultimately establish near-full fault lengths at the end of Stage 1. The second stage (Stage 2), is best described as ‘constant-length’ fault behaviour, i.e. displacement accrual without significant tip propagation or further fault lengthening. The fault growth trajectory in D-L space during Stage 1 of the fault growth varies significantly, from sub-horizontal coherent-like trajectories with limited displacement accrual (graph a), to steep and propagating-
like trajectories with significant displacement accrual during Stage 1 (graph e). See text for full discussion.

REFERENCES


displacement gradient variations controlled by strain softening versus hardening;

Rotevatn, A., Kristensen, T. B., Ksienzyk, A. K., Wemmer, K., Henstra, G. A.,
Midtkandal, I., Grundvåg, S. A. & Andresen, A. 2018. Structural Inheritance and
Rapid Rift-Length Establishment in a Multiphase Rift: The East Greenland Rift

Rykkelid, E. & Fossen, H. 2002. Layer rotation around vertical fault overlap zones:
observations from seismic data, field examples and physical experiment. *Marine and

growth of normal faults: Insights from a laser-equipped analog experiment. *Earth and

Schlische, R. W., Young, S. S., Ackermann, R. V. & Gupta, A. 1996. Geometry and
scaling relations of a population of very small rift-related normal faults. *Geology*
**24**(8), 683-686.

Schultz, R. A. & Fossen, H. 2002. Displacement-length scaling in three dimensions:
the importance of aspect ratio and application to deformation bands. *Journal of
Structural Geology* **24**, 1389-1411.

Dependence of displacement-length scaling relations for fractures and deformation
bands on the volumetric changes across them. *Journal of Structural Geology* **30**(11),
1405-1411.


Displacement and interaction of normal fault segments branched at depth:
Implications for fault growth and potential earthquake rupture size. *Journal of
Structural Geology* **30**(10), 1288-1299.

and linkage in the Whakatane Graben, New Zealand, during the last 1.3 Myr. *Journal

Petroleum Geology* **28**(8), 1444-1460.

Trudgill, B. D. & Cartwright, J. A. 1994. Relay ramp forms and normal fault linkages,


Fig. 1

(A) (i) map-view

○ = fault tip at T1
□ = fault tip at T2
□ = relay zone length
● = fault tip at T3
= tip propagation

(ii) strike-projection

‘incidental’ fault overlap (i.e. relay zone)

(iii) D-L profiles

length (L)
displacement (D)

(B) (i) map-view

= fault tip location at T2
○ = fault tip location at T1
= relay zone length

(ii) strike-projection

fault overlap (i.e. relay zone)

(iii) D-L profiles

length (L)
displacement (D)

(C) (D)
Timestep T1: T=0 sec

Timestep T2: T=5.0 sec

Timestep T3: T=10.0 sec

Timestep T4: T=15.0 sec

5 second intervals
Timestep T1a: T=5.5 sec

Timestep T1b: T=6.0 sec

Timestep T1c: T=6.5 sec

Timestep T1d: T=7.0 sec
Length

Maximum displacement

Fault death

Synchronous D-L ('propagating') fault growth

Stage 1: rapid fault lengthening; 20-30% of fault lifespan

Typified by 'propagating' fault growth - tip propagation and segment link-up

Stage 2: displacement accrual; 70-80% of fault lifespan

Typified by constant-length fault growth no or only limited fault lengthening

Hybrid growth patterns

'Constant-length' fault growth

dcbe

a