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3 **Decomposing the Drivers of Polar Amplification with a Single Column**

4 **Model**

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ABSTRACT

19 The precise mechanisms driving Arctic amplification are still under debate.
20 Previous attribution methods based on top-of-atmosphere energy budgets have
21 assumed all forcings and feedbacks lead to vertically-uniform temperature
22 changes, with any departures from this collected into the lapse-rate feedback.
23 We propose an alternative attribution method using a single column model
24 that accounts for the forcing-dependence of high latitude lapse-rate changes.
25 We test this method in an idealized General Circulation Model (GCM), find-
26 ing that, even though the column-integrated carbon dioxide (CO₂) forcing
27 and water vapor feedback are stronger in the tropics, they contribute to polar-
28 amplified surface warming as they lead to bottom-heavy warming in high lati-
29 tudes. A separation of atmospheric temperature changes into local and remote
30 contributors shows that, in the absence of polar surface forcing (e.g., sea-ice
31 retreat), changes in energy transport are primarily responsible for the polar
32 amplified pattern of warming. The addition of surface forcing substantially
33 increases polar surface warming and reduces the contribution of atmospheric
34 dry static energy transport. This physically-based attribution method can be
35 applied to comprehensive GCMs to provide a clearer view of the mechanisms
36 behind Arctic amplification.

37 **1. Introduction**

38 The Arctic amplification of surface temperature change is a robust feature of observations
39 (Stocker et al. 2013) and comprehensive climate model simulations (Pithan and Mauritsen 2014).
40 A number of mechanisms are thought to contribute to Arctic amplification, including the surface
41 albedo feedback, increased atmospheric energy transport convergence (Hwang and Frierson 2010),
42 and the temperature feedback (Pithan and Mauritsen 2014); however, the precise contribution of
43 each mechanism is still unclear. Clarifying how these different factors contribute to Arctic ampli-
44 fication is essential for reducing the uncertainty in the rate of Arctic warming through improved
45 process-level understanding.

46 The tropics differ from the high latitudes in that they are close to radiative-convective equilib-
47 rium: heating by convection is balanced by radiative cooling, and the vertical temperature profile
48 is mostly determined by surface temperature and humidity. The high latitudes, on the other hand,
49 are close to radiative-advective equilibrium: warming from horizontal atmospheric heat trans-
50 port is balanced by cooling from radiation. This means that different forcings and feedbacks
51 induce different lapse rate responses. For example, an increase in longwave optical depth leads to
52 bottom-heavy warming (Cronin and Jansen 2016; Henry and Merlis 2019), whereas atmospheric
53 energy transport is thought to primarily affect the midtroposphere at high latitudes (Laliberté and
54 Kushner 2013; Feldl et al. 2017a). This implies that the ratio between surface warming and top-
55 of-atmosphere (TOA) net radiation changes at the high latitudes is different for each forcing and
56 feedback. Surface temperature change attributions based on TOA budget analyses (Pithan and
57 Mauritsen 2014) and moist energy balance models (Roe et al. 2015) assume a linear relationship
58 between surface temperature change and TOA net radiation change that is independent of forcing.
59 Hence these attribution methods neglect the dependence of the vertical structure of warming on

60 the perturbation type at high latitudes, and may produce misleading attributions of the drivers of
61 Arctic amplification.

62 Process oriented and mechanism denial experiments are useful tools for studying the mecha-
63 nisms responsible for Arctic amplification. For example, the analysis from Stuecker et al. (2018)
64 suggests that local forcings and feedbacks dominate the polar-amplified pattern of surface temper-
65 ature change in a comprehensive GCM in which CO₂ concentrations are increased in restricted
66 latitudinal bands. Using the conventional TOA budget-based attribution method, they suggest that
67 the lapse rate feedback is a main contributor to this surface temperature change pattern. Screen
68 et al. (2012) attribute near-surface warming to local forcings and feedbacks and warming aloft to
69 atmospheric energy transport increases by prescribing local and remote sea surface temperature
70 (SST) and sea ice concentration (SIC) changes in two comprehensive atmospheric GCMs. How-
71 ever, fixing SST where the model would otherwise warm (or cool) the surface is akin to imposing
72 a surface heat sink (or source), hence the results are not easily interpretable.

73 While these comprehensive GCM studies provide important insights into the mechanisms of
74 Arctic amplification, a hierarchy of models is required for a complete understanding of the drivers
75 of Arctic amplification in climate models and observations. Previous work using single column
76 model representations of the high latitude atmosphere suggested that the high latitude temperature
77 response is sensitive to the forcing type (Abbot and Tziperman 2008; Payne et al. 2015). Cronin
78 and Jansen (2016) have developed a 1-dimensional model of an atmosphere in radiative-advective
79 equilibrium for the high latitudes, which led to the important insight that high latitude lapse rate
80 changes are forcing-dependent. The present work seeks to bridge the gap between their simple
81 radiative-advective column model and complex climate model simulations in order to advance our
82 understanding of the drivers of Arctic amplification.

83 Using an idealized moist atmospheric GCM with aquaplanet surface boundary conditions, no
84 clouds, and no sea ice (hence no surface albedo feedback), we qualitatively reproduce the pattern
85 of surface temperature change from comprehensive GCMs. To simulate the effect of melting sea
86 ice, we impose a polar surface heat source, ranging from 0 to 24 W m^{-2} . Then, we use a single
87 column model (SCM) to emulate the tropics and high latitudes of the idealized GCM. This allows
88 us to calculate the response to each individual forcing and feedback and thus decompose the drivers
89 of tropical and polar temperature change. By accounting for each forcing and feedback's impact
90 on the vertical structure of temperature change, this physically-based attribution method does not
91 assume a universal high latitude lapse rate feedback, and, therefore, does not ignore how the
92 vertical structure of temperature change depends on the perturbation. The idealized GCM acts as a
93 test-case for the attribution method, which could potentially be used to untangle the contributions
94 of the various mechanisms of polar amplification in comprehensive models or in observations.

95 **2. Idealized atmospheric GCM**

96 We use an idealized moist atmospheric GCM based on the Geophysical Fluid Dynamics Lab-
97 oratory (GFDL) spectral dynamical core and the comprehensive radiation scheme of the GFDL
98 AM2 GCM, with no sea ice or clouds. This is similar to the setup in Merlis et al. (2013) and to
99 the Model of an Idealized Moist Atmosphere (MiMA, Jucker and Gerber (2017)). These GCMs
100 follow the moist idealized GCM described in Frierson et al. (2006), but use comprehensive clear-
101 sky radiation instead of grey radiation. In the MiMA setup, the surface albedo is globally uniform
102 and increased to compensate for the cooling effect of clouds. In Merlis et al. (2013), an idealized
103 cloud distribution is prescribed for the radiative transfer calculation. Here, there are no clouds and
104 we set the surface albedo to a hemispherically symmetric analytic distribution similar to Earth's
105 northern hemisphere TOA albedo, as estimated from the Cloud and the Earth's Radiant Energy

106 System data (Loeb et al. (2018), see supplemental figure S1), in order to produce an Earth-like
107 meridional surface temperature gradient. The model uses the comprehensive radiation scheme de-
108 scribed in Anderson et al. (2004) with annual mean solar insolation and a solar constant equal to
109 1365 W m^{-2} .

110 The surface boundary condition is a slab mixed layer ocean aquaplanet with no representation
111 of ocean heat transport and the heat capacity of 1m of water. We use annual-mean insolation and
112 the small mixed layer depth allows the model to run quickly without meaningfully affecting the
113 model's climate, as we only consider annual-mean quantities. The GCM was run at T42 spectral
114 truncation, for a nominal horizontal resolution of $2.8^\circ \times 2.8^\circ$, and with 30 vertical levels. The skin
115 temperature is interactively computed using the surface radiative and turbulent fluxes, which are
116 determined by bulk aerodynamic formulae. A k-profile scheme with a dynamically determined
117 boundary layer height is used to parameterize the boundary layer turbulence. The GCM uses a
118 simplified Betts-Miller convection scheme (Frierson 2007), and large scale condensation is pa-
119 rameterized such that the relative humidity does not exceed one and condensed water is assumed
120 to immediately return to the surface. As there is no representation of sea ice, there is no surface
121 albedo feedback. To mimic the presence of the surface albedo feedback, we run perturbation ex-
122 periments with an added polar surface heat source. All simulations are run for 20 years with time
123 averages over the last 10 years shown, when all climate states have reached a statistical steady
124 state.

125 We perform four simulations: a control run in which the atmospheric CO_2 concentration is set
126 to 300 ppm, a run with quadrupled (1200 ppm) CO_2 concentration, and two runs with quadrupled
127 CO_2 concentrations and constant surface heat sources Q_s of 12 W m^{-2} and 24 W m^{-2} poleward
128 of 80° in both hemispheres. The heat sources simulate surface heating through the surface albedo
129 feedback or increased oceanic energy transport convergence. Given that the polar surface tempera-

130 ture change under $4xCO_2$ is approximately 8K, a 12 (24) $W m^{-2}$ surface heat source is equivalent
131 to a 1.5 (3) $W m^{-2} K^{-1}$ local feedback. This can be compared to the locally defined surface
132 albedo feedback from the models participating in the fifth coupled model intercomparison project
133 (CMIP5) which is approximately $1 W m^{-2} K^{-1}$ in the Arctic and $2 W m^{-2} K^{-1}$ in the Antarctic
134 (Feldl and Bordoni 2016, their figure 1).

135 Figure 1a shows the zonal-mean surface skin temperature differences between the control and
136 three perturbation simulations, in addition to the zonal-mean surface temperature responses of
137 abrupt $4xCO_2$ experiments with 7 models participating in the sixth Coupled Model Intercom-
138 parison Project (CMIP6) listed in the legend of figure 1 (Eyring et al. 2016). Figure 1b shows the
139 surface temperature changes normalized by their global mean. The patterns of surface temperature
140 change from the idealized model experiments (black) approximately span the CMIP6 model re-
141 sponses (colors). The amount of Arctic amplification is underestimated in the $4xCO_2$ experiment,
142 but adding a polar surface heat source brings the idealized GCM closer to CMIP6 in the Arctic,
143 with high latitude warming of 2 to 3 times the global-mean surface temperature change. Note that
144 the CMIP6 temperature changes are not fully equilibrated, and, at equilibrium, the Antarctic is
145 also expected to have amplified warming, but this warming is transiently delayed by ocean heat
146 uptake (Manabe et al. 1991; Rugenstein et al. 2019).

147 **3. Single column model**

148 To emulate the tropical and high-latitude atmosphere of the idealized GCM, we use the single
149 column model (SCM) from the ClimLab python package for process-oriented climate modeling
150 Rose (2018). The temperature tendency budgets for atmospheric and surface temperature are given
151 by the following equations:

$$\frac{\partial T_{atm}(p)}{\partial t} = \frac{\partial T_{atm}(p)}{\partial t} \Big|_{rad} + \frac{\partial T_{atm}(p)}{\partial t} \Big|_{conv} + \frac{\partial T_{atm}(p)}{\partial t} \Big|_{adv} + \frac{\partial T_{atm}(p)}{\partial t} \Big|_{cond} \quad (1)$$

$$\frac{\partial T_s}{\partial t} = \frac{\partial T_s}{\partial t} \Big|_{rad} + \frac{\partial T_s}{\partial t} \Big|_{SH} + \frac{\partial T_s}{\partial t} \Big|_{LH}, \quad (2)$$

152 where t is time and p is pressure (with 40 pressure levels). The subscripts ‘rad’, ‘conv’, ‘adv’, and
 153 ‘cond’, ‘SH’, ‘LH’ refer to radiative, convective, advective, condensation, sensible heat flux, and
 154 latent heat flux temperature tendencies, respectively. The radiative, convective, sensible heat flux,
 155 and latent heat flux temperature tendencies are computed interactively. The RRTMG radiation
 156 scheme is used for the computation of shortwave and longwave radiative temperature tendencies.
 157 The surface albedo and control insolation are set such that the upwelling and downwelling TOA
 158 shortwave radiation match the idealized GCM simulations in the tropics (10°S to 10°N) and pole-
 159 ward of 80°. Convection is implemented as an adjustment of the temperature profile to the moist
 160 adiabat, whereas the idealized GCM uses a simplified Betts-Miller convection scheme (Frierson
 161 2007). Note that at high latitudes, horizontal atmospheric energy transport induces a temperature
 162 structure stable to convection, hence convection has no effect. The surface sensible and latent heat
 163 fluxes are computed using bulk aerodynamic formulae with 5×10^{-2} drag coefficient and 5 ms^{-1}
 164 near surface wind speed (Rose 2018).

165 Values from the idealized GCM experiments averaged in the tropics (10°S to 10°N) and pole-
 166 ward of 80°N are used to prescribe the specific humidity profile, which affects the radiation and
 167 surface latent heat flux. In addition, the time-mean advection and condensation temperature ten-
 168 dency profiles from the idealized GCM simulations are added as external temperature tendency
 169 terms to simulate the dry and moist components of atmospheric energy transport convergence,
 170 respectively (see supplementary figure S2 for the temperature tendency profiles). The advective

171 temperature tendency term is calculated in the GCM as the difference in temperature tendency be-
172 fore and after running the dynamics module, hence it contains the horizontal and vertical advection
173 temperature tendencies.

174 The climatological temperature profiles of the idealized GCM and SCM are similar (figure 2),
175 though the SCM has an overly strong near-surface temperature inversion compared to the GCM.
176 This may be due to the absence of boundary layer scheme in the SCM, which would smooth dif-
177 ferences between the surface and lower atmospheric layers. Similarities between the temperature
178 profiles simulated by the idealized GCM and by the SCM still hold when the latitudinal bounds of
179 the tropics are set to 20°S-20°N and the high latitudes to 60° (see supplementary figure S3).

180 **4. Attribution of idealized GCM tropical and polar lapse rate changes to forcings and feed-** 181 **backs.**

182 As discussed in the introduction, the forcing dependence of the high latitude lapse rate feedback
183 makes a TOA budget approach to attributing the polar surface warming to different forcings and
184 feedbacks ambiguous (see next section). The SCM allows us to attribute the idealized GCM's
185 tropical and polar lapse rate changes to the different forcings and feedbacks. We individually
186 perturb CO₂, water vapor, and atmospheric energy transport (moist and dry components) in the
187 tropics and high latitudes to attribute the total warming to each of these individual components.

188 Figure 3 shows the decomposition of (a) tropical and (b,c,d) polar lapse rate changes of the
189 three idealized GCM perturbation experiments: 4xCO₂ (a,b), 4xCO₂ with $Q_s=12 \text{ W m}^{-2}$ (a,c) and
190 $Q_s=24 \text{ W m}^{-2}$ (a,d); Table 1 summarizes the surface temperature change attributions.

191 The tropical lapse rate changes for the three experiments are similar enough to be plotted in the
192 same figure 3a: the $Q_s = 12 \text{ W m}^{-2}$ and $Q_s = 24 \text{ W m}^{-2}$ experiment changes are shown in dashed
193 and dash-dotted respectively, and fall close to each other. They are decomposed into the tempera-

194 ture change from the CO₂ forcing (red), water vapor feedback (blue), and energy transport (green).
195 For each GCM experiment, the SCM's response to applying all of the perturbations simultaneously
196 (black) is exactly the same as the sum of the responses to the individual perturbations and fits the
197 idealized GCM's response well throughout the troposphere (grey), demonstrating the accuracy of
198 the attribution method. Differences in the stratosphere between the SCM and idealized GCM may
199 be due to the different radiation schemes or ozone distributions. Since convection is triggered in
200 the tropics, the temperature profiles are moist adiabatic and the vertical structure of tropospheric
201 temperature change ($\Delta T/\Delta T_S$) is approximately the same for all SCM experiments. The energy
202 transport is slightly reduced in the experiments with surface heat sources.

203 The polar lapse rate changes (b,c,d) are decomposed into the temperature changes from the CO₂
204 forcing (red), water vapor feedback (blue), the 'local' water vapor feedback (blue dashed, see
205 section 6), the energy transport (dry component in orange and moist component in cyan), and
206 surface heat source (yellow). Again, for each GCM experiment, the SCM's response to applying
207 all of the perturbations simultaneously (black) is exactly the same as the sum of the responses to the
208 individual perturbations, and fits the idealized GCM's response well throughout the troposphere
209 (grey), showing the accuracy of the attribution method. The increase in longwave absorbers (CO₂
210 and water vapor) leads to bottom-heavy warming, the dry component of energy transport leads to
211 top-heavy warming, the moist component of energy transport leads to mid-troposphere enhanced
212 warming, and the surface heat source leads to very bottom-heavy warming.

213 The polar surface temperature change is 3.6K and 7.6K higher in the $Q_s = 12\text{W m}^{-2}$ and $Q_s =$
214 24W m^{-2} cases respectively, which is caused mainly by 4.6K and 8.9K warming, respectively,
215 due to the surface heat source. The reduction in the dry component of energy transport causes
216 a 2.1K and 4.1K cooling respectively versus no warming in the simulation with $Q_s = 0\text{W m}^{-2}$.
217 There are also slight increases in warming due to the water vapor feedback (discussed in section

218 6) and moist component of the energy transport compared to the 4xCO₂ experiment (Table 1).
 219 This is consistent with Hwang et al. (2011), who found that enhanced Arctic warming due to
 220 local feedbacks weakens the equator-to-pole temperature gradient and reduces the dry component
 221 of the atmospheric energy transport, which outweighs the increase in the moist component of
 222 atmospheric energy transport that arises from the enhanced warming.

223 5. Surface temperature change attribution method comparison

224 The conventional surface temperature change attribution method (Pithan and Mauritsen 2014;
 225 Stuecker et al. 2018) assumes forcings and feedbacks lead to vertically uniform temperature
 226 changes. The deviation from vertically uniform temperature change is then accounted for in the
 227 lapse rate feedback. One can decompose the surface temperature change as follows (equation 3 in
 228 the Methods section of Stuecker et al. (2018)):

$$\Delta T_S(\phi) = \left(-\frac{1}{\lambda_P}\right) \{ \Delta T_S(\phi) [\lambda'_P(\phi) + \lambda_{LR}(\phi) + \lambda_{WV}(\phi) + \lambda_{AL}(\phi)] + \mathcal{F}(\phi) + \Delta(\nabla \cdot \vec{F}(\phi)) \} \quad (3)$$

229 where ϕ is the latitude. The surface temperature change attributions are then given by the average
 230 of $\Delta T_S(\phi)$ over the tropics and Arctic. The Planck feedback is decomposed into its global-mean
 231 $\overline{\lambda_P}$ and its deviation λ'_P , λ_{LR} is the lapse rate feedback, λ_{WV} is the water vapor feedback, λ_{AL} is the
 232 surface albedo feedback and λ_{CL} is the cloud feedback.

233 To apply the conventional attribution method to the GCM simulations, we use aquaplanet ker-
 234 nels from Feldl et al. (2017b) (available at <https://github.com/nfeldl/aquakernels>) to calculate the
 235 feedbacks. The CO₂ forcing \mathcal{F} is computed as the change in TOA net radiation between the con-
 236 trol simulation and an idealized GCM simulation where sea surface temperatures (SST) are fixed
 237 to the control SST and CO₂ concentrations are quadrupled (Hansen et al. 2005). The change in

238 atmospheric energy transport convergence $\Delta(\nabla \cdot \vec{F})$ is computed as the change in net TOA radia-
239 tion (minus the surface forcing) between the control and perturbed simulations. This method of
240 attributing surface temperature changes to forcings and feedbacks then tells us how much surface
241 temperature change is required to balance the TOA energy imbalance caused by each forcing or
242 feedback, assuming the atmospheric temperature change is vertically uniform (except for the lapse
243 rate feedback).

244 Figure 4 compares this TOA energy budget surface temperature change attribution method
245 (crosses) with the single column model based attribution method (filled circles) for the $4\times\text{CO}_2$
246 (a), $4\times\text{CO}_2$ with $Q_s = 12\text{W m}^{-2}$ (b) and $Q_s = 24\text{W m}^{-2}$ (c). The tropical (x-axis, 10°S to 10°N)
247 and polar (y-axis, 80°N to 90°N) attributions are plotted against each other. If a point falls above
248 (below) the one-to-one line, the forcing or feedback contributes to polar (tropical) amplification.
249 As in Pithan and Mauritsen (2014), the TOA attribution method suggests that the Planck and lapse
250 rate feedbacks contribute to polar amplification. The lapse rate feedback contributes to more po-
251 lar amplification in the surface heat source experiments. The single column model attribution
252 method, in contrast, has no temperature feedback in its decomposition. Since the TOA energy
253 budget method assumes that the temperature response to a TOA energy imbalance is vertically
254 uniform, it will attribute a larger (smaller) amplitude change in surface temperature than the sin-
255 gle column model if the response to the forcing or feedback is top-heavy (bottom-heavy). In the
256 tropics, all temperature changes are top-heavy as they follow the moist adiabat, hence the SCM
257 attributions are all closer to the y-axis than the corresponding TOA method attributions. In the
258 high latitudes, the SCM temperature changes from increases in CO_2 , water vapor, and surface
259 heat source are bottom-heavy, hence they all contribute a larger surface temperature change than
260 is diagnosed from the TOA method. The energy transport convergence change leads to top-heavy

261 warming, hence the warming attributed to it by the SCM method is smaller than the warming
262 attributed by the TOA method, and even negative in the surface heat source cases.

263 In summary, we underline two main points from this comparison of the single column model
264 and TOA-based surface temperature change attribution methods:

265 • The increase in longwave absorbers (CO₂ and water vapor) go from contributing to tropical
266 amplification in the TOA attribution method to contributing to polar amplification in the SCM
267 attribution method. The forcing from CO₂ and the water vapor feedback are stronger in
268 the tropics than the high latitudes, but since the tropical SCM attribution includes the effect
269 of convection, the warming maximum is pushed to the upper-troposphere and there is less
270 surface warming. In the high latitudes however, an increase in longwave absorbers leads to
271 bottom-heavy warming (Cronin and Jansen 2016; Henry and Merlis 2019). Russotto and
272 Biasutti (2020) analyze the response of atmospheric GCMs using a moist energy balance
273 model, and similarly find that a tropically amplified CO₂ forcing and water vapor feedback
274 lead to a polar amplified temperature response.

275 • Since the increase in atmospheric energy transport convergence preferentially affects the mid-
276 troposphere, it leads to less surface warming at high latitudes, and even surface cooling in the
277 surface heat source experiments.

278 **6. Local and remote drivers of temperature change.**

279 The SCM attribution method can also be used to decompose the drivers of polar amplification
280 into local and remote drivers. The CO₂ and surface heat source perturbations are local drivers,
281 while the energy transport can be considered as a remote driver. The water vapor feedback includes
282 both local and remote contributions. First, the change in specific humidity can be decomposed

283 into a temperature-dependent change and a change due to relative humidity: $\Delta q = \Delta q|_{fixedRH} +$
 284 $\Delta RH \times q^*|_{clim}$ where $q^*|_{clim}$ is the climatological saturation specific humidity. Since the relative
 285 humidity in the idealized GCM stays relatively constant (supplementary figure S4), we ignore
 286 the second term of this equation. Using fixed relative humidity (RH) SCM experiments, we can
 287 decompose the temperature-dependent changes in specific humidity into the ‘local’ changes in
 288 response to the temperature changes forced by increased CO₂ and the surface heat source, and
 289 the ‘remote’ changes in response to the temperature change forced by altered energy transports:
 290 $\Delta q \approx \Delta q|_{fixedRH} = \Delta q|_{fixedRH, \Delta CO_2, \Delta Q_s} + \Delta q|_{fixedRH, \Delta ET}$.

291 This local versus remote decomposition of the water vapor concentration increase is not perfect,
 292 as it assumes the energy transport simply affects the humidity of the high latitudes by changing
 293 its temperature and activating the local water vapor feedback, whereas the general circulation can
 294 directly advect water vapor. The energy transport term also contains vertical advection, which can
 295 change as a result of local diabatic forcings (shown in magenta in supplementary figure S2). More-
 296 over, GCM experiments where the forcing from a CO₂ increase is constrained to the high latitudes
 297 show changes in energy transport, which would also affect the water vapor feedback (Stuecker
 298 et al. 2018). Since energy transport is affected by both temperature and humidity gradients, it is
 299 not clear that any perfect local / remote decomposition exists. Nevertheless, our definition of ‘lo-
 300 cal’ recovers traditional SCM treatments of fixed relative humidity water vapor feedback (Manabe
 301 and Wetherald 1967) in the limit of no energy transport change.

302 The fixed-RH SCM simulations have the same modules and parameters as the standard SCM
 303 simulations, but instead of prescribing the idealized GCM’s specific humidity, they have fixed rel-
 304 ative humidity and the specific humidity is free to evolve with the temperature. The climatological
 305 temperature of the fixed RH SCMs have a warm bias (supplementary figure S5) and the climato-
 306 logical specific humidity is biased high (supplementary figures S6). We do two sets of fixed-RH

307 SCM experiments: the first ('local') experiment is forced with the increase in CO₂ concentration
308 (and surface heat source), and the second is forced with increased CO₂ concentration (and surface
309 heat source) and perturbed energy transport. The latter has less tropical warming and similar polar
310 warming compared to the idealized GCM (red lines in supplementary figure S7 for the 4xCO₂
311 experiment), and similar changes in specific humidity in the tropics and a higher increase in high
312 latitudes compared to the idealized GCM (red lines in supplementary figures S8 for the 4xCO₂
313 experiment). The 'local' increase in water vapor, $\Delta q|_{fixedRH,\Delta CO_2,\Delta Q_s}$, is taken to be the change in
314 water vapor from the first set of fixed-RH SCM experiments (blue lines in figure S8 for the 4xCO₂
315 experiment), and the 'remote' increase in water vapor, $\Delta q|_{fixedRH,\Delta ET}$, is taken to be the residual
316 between the total change in water vapor and the 'local' change in water vapor. We then force the
317 original SCM with the 'local' and 'remote' specific humidity changes to deduce the 'q (local)' and
318 'q (remote)' temperature changes (shown in table 2). The 'q (local)' experiments are comparable
319 to the fixed RH experiments in Payne et al. (2015). The temperature changes from the high latitude
320 'q (local)' experiments are shown in figure 3 (blue dashed).

321 Table 2 summarizes the result of this local / remote decomposition of surface temperature
322 change. In the three perturbation experiments, the warming from CO₂ alone is 1.8K in the tropics
323 and 3.1K at high latitudes, hence increasing CO₂ leads to polar amplification in the absence of any
324 feedbacks. The addition of the 'local' water vapor feedback increases the tropical surface warm-
325 ing to 7.5K and the polar surface warming to 4.0K in the 4xCO₂ experiment, and thus cancels
326 the polar amplification from CO₂ alone. Payne et al. (2015) also found a tropical amplification of
327 surface temperature change in their fixed-RH SCM simulations, though with somewhat different
328 magnitude. Finally, adding the atmospheric energy transport and its implied water vapor change
329 decreases the tropical surface warming to 3.7K, and increases the polar surface warming to 9.0K
330 in the 4xCO₂ experiment, thus leading to polar amplification. The polar surface heat source gen-

331 erally increases the amount of polar amplification despite the partial compensation by a reduction
332 in dry energy transport. For the $4\times\text{CO}_2$ experiment, approximately half of the polar warming is
333 due to local sources (4.0K out of 9K of total warming), but the polar amplified pattern of warming
334 is primarily caused by the increase in atmospheric energy transport which cools the tropics and
335 warms the high latitudes. The high latitude warming is then strongly enhanced by the increased
336 water vapor from remote sources. When a polar surface heat source is added, almost all of the
337 polar surface warming is due to local sources because of the surface heat source and the compen-
338 sating reduction in the dry component of energy transport: 10.2K and 16.1K from local sources
339 for a total warming of 12.6K and 16.6K for the $Q_s = 12\text{W m}^{-2}$ and $Q_s = 24\text{W m}^{-2}$ experiments,
340 respectively.

341 **7. Summary and discussion**

342 Unlike the tropics which are close to radiative-convective equilibrium, the high latitudes are
343 in radiative-advective equilibrium: different forcings and feedbacks induce different lapse rate
344 responses. Previous surface temperature attributions have assumed that different forcings and
345 feedbacks induce vertically homogeneous warming, and attributed the deviation from vertically
346 uniform warming to the lapse rate feedback. In these attributions, the lapse rate feedback functions
347 as a residual that cannot be clearly ascribed to any particular physical process.

348 We introduce a surface temperature change attribution method based on a single column model,
349 which accounts for the vertically inhomogeneous temperature change contributions of each forc-
350 ing and feedback. We find that the warming from increased longwave absorbers (CO_2 and water
351 vapor) is bottom-heavy and accounts for most of the surface warming in the absence of a surface
352 heat source. By contrast, the warming from atmospheric heat transport preferentially warms the
353 mid and upper troposphere. When a polar surface heat source is added, there is a reduction in the

354 dry component of atmospheric energy transport which partially compensates for the extra surface
355 warming from the polar surface heat source. Compared to the conventional surface temperature
356 change attribution method, the increase in longwave absorbers (CO₂ and water vapor) goes from
357 contributing to tropical amplification to polar amplification. In addition, the polar warming contri-
358 bution from the increase in atmospheric energy transport convergence is reduced as it preferentially
359 warms the mid and upper troposphere. Finally, we separated the drivers of atmospheric tempera-
360 ture change into local and remote contributors and found that, in the absence of a polar surface heat
361 source, the change in energy transport was primarily responsible for the polar amplified pattern of
362 warming. The addition of a polar surface heat source increases the contribution of local drivers to
363 polar warming at the expense of remote drivers, as the dry energy transport is reduced.

364 It is important to note that clouds and sea ice were ignored in this analysis (aside from the surface
365 heat source that mimics the effects of shortwave cloud feedbacks and sea ice), though they may
366 play an important role in explaining the pattern of surface temperature change in comprehensive
367 climate model simulations. Arctic amplification also has seasonality — it is strong in winter and
368 suppressed in summer — which has been suggested to result from the increased polar ocean heat
369 uptake in summer and ocean heat release in winter from the melting sea ice (Manabe and Stouffer
370 1980; Bintanja and Van der Linden 2013; Dai et al. 2019). Nevertheless, we believe that the single-
371 column model can be a stepping stone for connecting simple physical models with comprehensive
372 climate models: clouds and seasonality can be prescribed in the SCM, which would be a valuable
373 extension of the present work. This would allow us to understand the basic mechanisms driving
374 Arctic amplification and reduce the uncertainty in the rate of Arctic warming.

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376 figures will be made available at https://github.com/matthewjhenry/HMLR19_SCM. Documenta-
377 tion for the python ClimLab package can be found at <https://climlab.readthedocs.io/>. The top-of-
378 atmosphere albedo data from the Cloud and the Earth’s Radiant Energy System (CERES) can be
379 found at <https://ceres.larc.nasa.gov/>. The CMIP6 data is available on the Earth System Grid Fed-
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451 **LIST OF TABLES**

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456 ture and is decomposed into its dry and moist components in the pole. ‘Q_s’
457 denotes the effect of the surface heat source on the surface temperature change. . . . 24

458 **Table 2.** Surface temperature change attribution based on the single column model de-
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460 perature change attributions are sufficiently similar to be in a single column.
461 The three successive values separated by a comma refer to the the 4xCO₂,
462 Q_s = 12W m⁻², and Q_s = 24W m⁻² experiments respectively. Slight discrep-
463 ancies between the total and the sum of local and remote totals occur as the total
464 is the surface temperature change from the experiment with all perturbations. . . . 25

Forcing (W m^{-2}) / Feedback ($\text{W m}^{-2} \text{K}^{-1}$)	4xCO ₂	4xCO ₂ + 12 W m^{-2}	4xCO ₂ + 24 W m^{-2}
Tropics			
CO ₂	1.8	1.8	1.8
Water Vapor	2.8	2.9	2.9
ET	-0.8	-0.5	-0.5
Tropics total	3.7	4.0	4.1
Pole			
CO ₂	3.1	3.1	3.1
Water Vapor	4.3	4.8	5.5
ET (dry)	0	-2.1	-4.1
ET (moist)	1.4	2.0	2.8
Q_s	0	4.6	8.9
Pole total	9.0	12.6	16.6

465 TABLE 1. Surface temperature change attribution based on the single column model decomposition for the
466 three perturbation experiments. ‘CO₂’ and ‘Water Vapor’ denote the radiative effect of their increase on surface
467 temperature, whereas ‘ET’ denotes the effect of the change in energy transport on surface temperature and is
468 decomposed into its dry and moist components in the pole. ‘ Q_s ’ denotes the effect of the surface heat source on
469 the surface temperature change.

Forcing / feedback	Tropics	Pole (4xCO ₂)	Pole (4xCO ₂ +12)	Pole (4xCO ₂ +24)
CO ₂	1.8	3.1	3.1	3.1
q (local)	5.7	0.9	2.5	4.1
Q_s	0	0	4.6	8.9
Local total	7.5	4.0	10.2	16.1
q (remote)	-2.9,-2.8,-2.8	3.4	2.3	1.4
ET	-0.8,-0.5,-0.5	1.5	-0.1	-1.4
Remote total	-3.8,-3.4,-3.4	4.9	2.2	0
Total	3.7,4.0,4.1	9.0	12.6	16.6

470 TABLE 2. Surface temperature change attribution based on the single column model decomposition for the
471 three perturbation experiments. The tropical surface temperature change attributions are sufficiently similar to
472 be in a single column. The three successive values separated by a comma refer to the the 4xCO₂, $Q_s = 12\text{W m}^{-2}$,
473 and $Q_s = 24\text{W m}^{-2}$ experiments respectively. Slight discrepancies between the total and the sum of local and
474 remote totals occur as the total is the surface temperature change from the experiment with all perturbations.

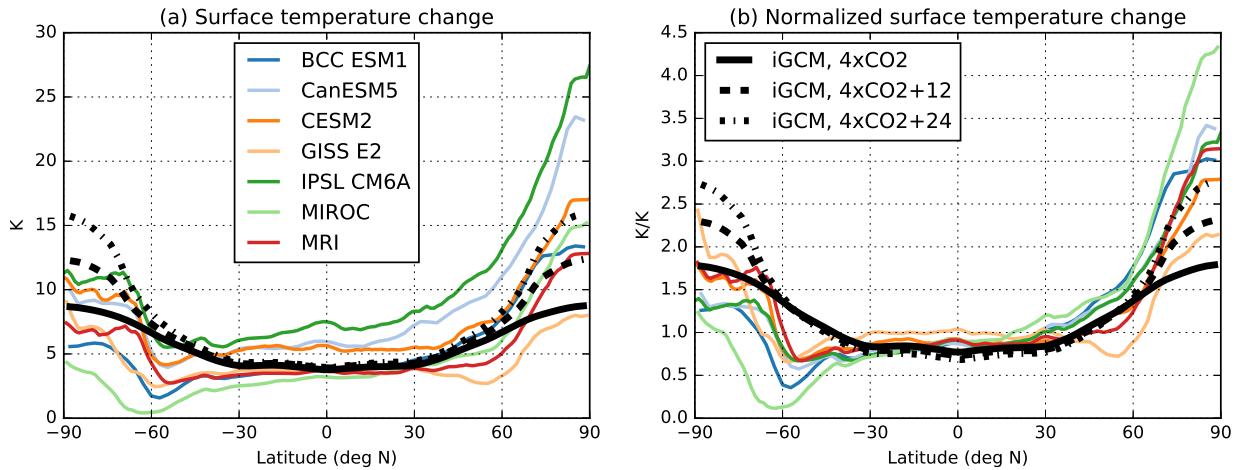
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479 source poleward of 80° using an idealized moist atmospheric GCM with no clouds or sea
480 ice. These are compared to CMIP6 abrupt 4xCO₂ surface temperature changes in simula-
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482 MIROC, MRI. (b) Same as (a), but the temperature changes are normalized by global mean
483 surface temperature change. 27

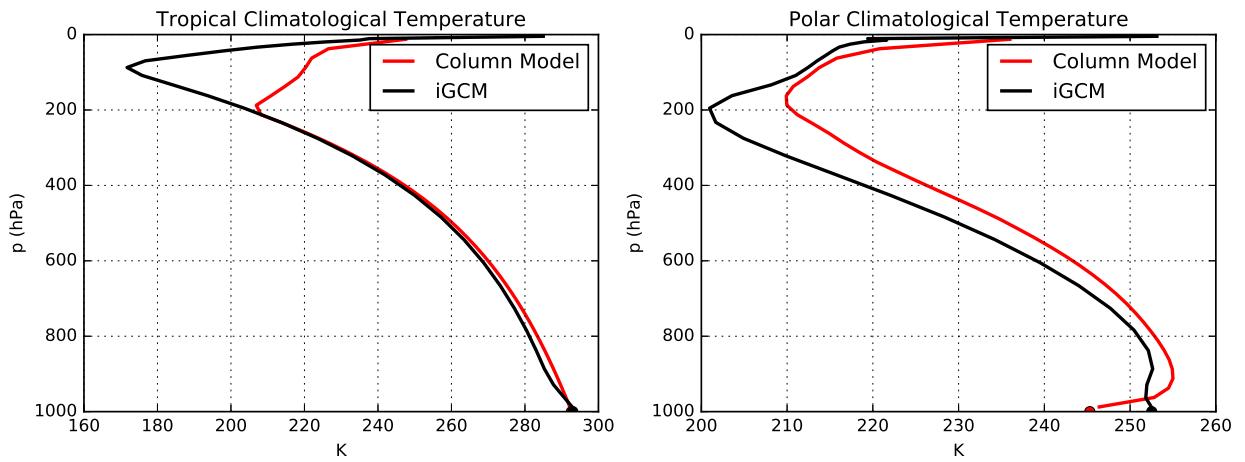
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491 the same as the sum of individual changes and fit the idealized GCM (grey) well. The in-
492 dividual forcing and feedback contributions are calculated by individually perturbing them
493 in the single column model (colors). They include the CO₂ increase (red), the water vapor
494 feedback (blue), the ‘local’ water vapor feedback (blue dashed, see section 6), the energy
495 transport (green in tropics, separated into dry (orange) and moist (cyan) in high latitudes),
496 and the surface heat source (yellow). The tropical temperature changes of the three experi-
497 ments (a) are similar enough to be plotted together (12 W m⁻² in dashed lines and 24 W m⁻²
498 in dash-dotted lines). Surface temperature change attributions are summarized in table 1. 29

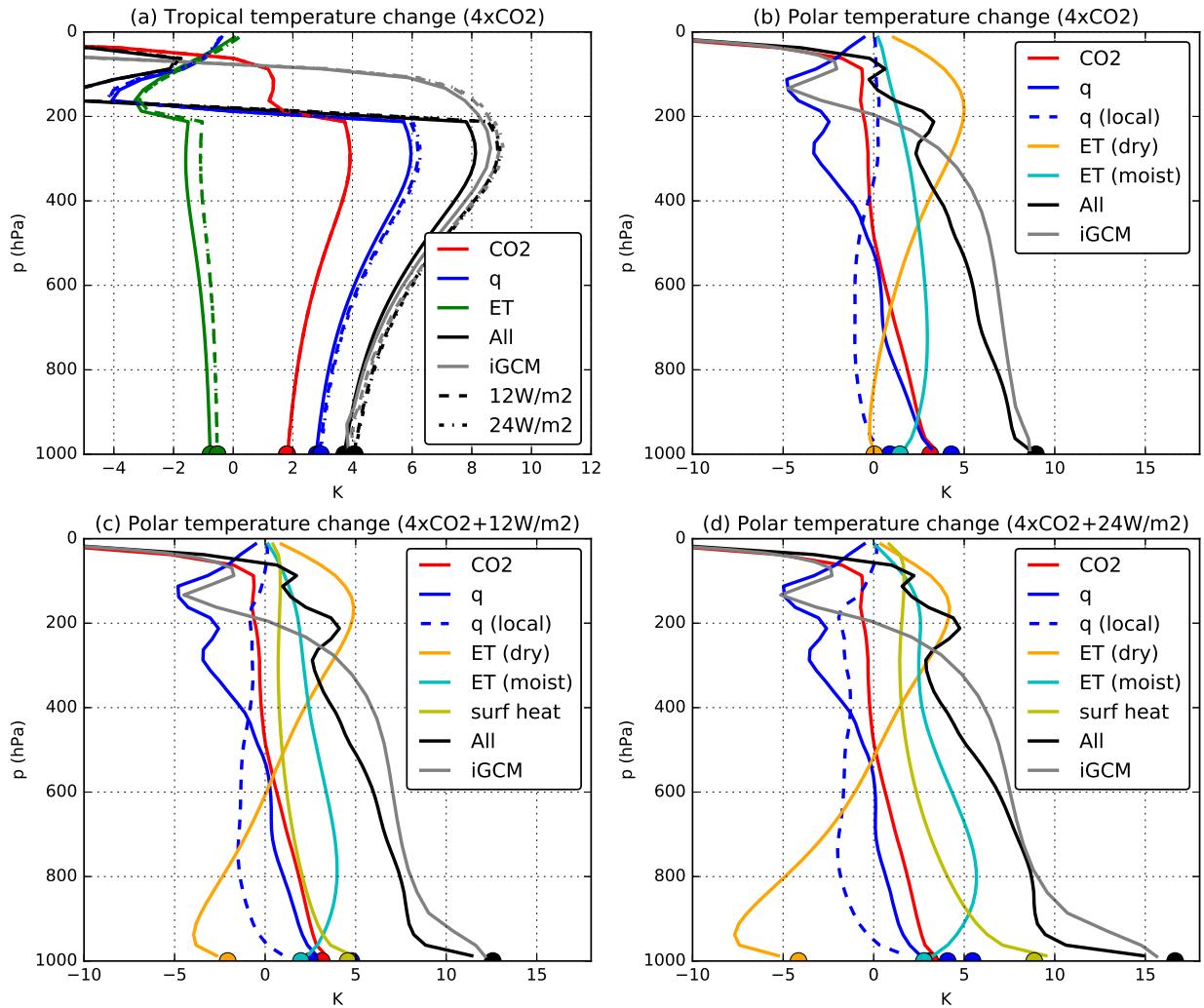
499 **Fig. 4.** Surface temperature change attributions for the 4xCO₂ (a) and 4xCO₂ with $Q_s = 12\text{W m}^{-2}$
500 (b) and $Q_s = 24\text{W m}^{-2}$ (c) using the TOA energy budget method (crosses) and the SCM
501 method presented in this paper (dots). Presented are the surface temperature change attri-
502 butions to the increase in CO₂ (red), water vapor (blue), energy transport (green), surface
503 heat source (yellow) for both methods. The Planck (magenta) and lapse rate (cyan) feed-
504 back contributions are also shown for the TOA energy budget method. When the point is
505 above (below) the one-to-one line, the forcing or feedback contributes to polar (tropical)
506 amplification. 30



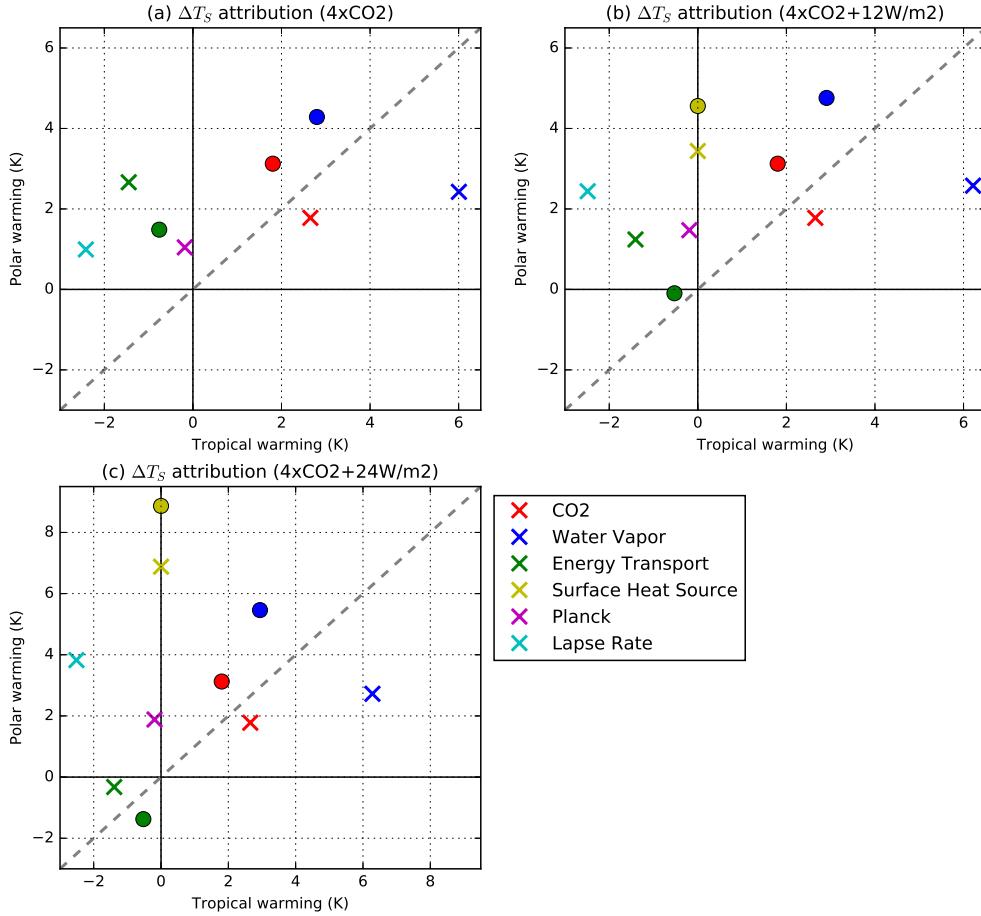
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 511 changes in simulations with the following models: BCC-ESM1, CanESM5, CESM2, GISS-E2, IPSL CM6A,
 512 MIROC, MRI. (b) Same as (a), but the temperature changes are normalized by global mean surface temperature
 513 change.



514 FIG. 2. Comparison between the single column model (red) and idealized GCM (black) for the (a) tropical
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516 FIG. 3. Tropical (a) and polar (b,c,d) temperature change for the idealized GCM (grey) and three perturbation
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 528 (dots). Presented are the surface temperature change attributions to the increase in CO_2 (red), water vapor (blue),
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