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11	This is a non-peer reviewed preprint submitted to EarthArXiv.
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20	Two Pixel Reference Algorithm
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27	Abstract: Object based image analysis (OBIA) has a unique process requirement: relate all
28	the pixels in the segmented images to the vectorized polygons (pixel in polygon). The existing
29	solutions are very slow in finding the pixels in a polygon. This paper proposes a novel
30	algorithm called Two-Pixel-Reference to speed up the process. The algorithm is initially
31	designed for segmented remote sensing images. It avoids most multiple-layer loops in
32	existing methods and trims many redundant comparison among pixels. Thus it has literal
33	lower Big O algorithm complexity. We implemented the algorithms in C++ and made more
34	than seventy tests on two different machines to compare the algorithm with three other
35	existing algorithms. The results show that it significantly decreases the time cost of the
36	process. In every single test, the proposed algorithm costs much less time than other
37	algorithms. Specifically, the average duration is reduced from 3.96 seconds to 0.15 second on
38	machine #1 and from 3.647 seconds to 0.073 second on machine #2. This paper makes a good
39	example for researching time-efficient algorithms to accelerate the overall process of OBIA in
40	such a big data era.

- Keywords: object based image analysis; pixel in polygon; complexity; remote sensing; image
 classification; vectorization.

47 **1. Introduction**

48 Object based image analysis (OBIA) is one of the state-of-the-art techniques in RS [1-6]. 49 It first segments an image into objects, which are also called patches, segments or regions. 50 Then the post processes are conducted on the objects rather than pixels (as shown in Fig. 1). 51 Many study cases have proven that OBIA is more advantageous on enhancing the 52 classification accuracy than pixel based image analysis (PBIA) [7-10]. However, due to the 53 new object layer, OBIA has more steps than PBIA and the overall time cost of OBIA is 54 generally higher. More efforts on speeding up OBIA are needed to increase the time value of 55 OBIA results.



Figure 1. A segmented RS image and some sample segments

According to our experiences in building and using OBIA system [3, 11], a large block of time of an OBIA analysis is spent on sorting pixels in each region after an image is segmented. The existing methods have high time complexity and are very inefficient for time saving purpose. Thus, this paper proposes a new algorithm of sorting pixels to decrease the duration

62 into a senseless level. The algorithm avoids most multiple-layer loops in existing methods and 63 trims many redundant comparison among pixels. Finally it evolves into an extremely concise 64 method with very low time complexity.

65 To test the algorithm, we compared four algorithms, including three existing algorithms, 66 on two machines. The inputs include an image and a vector containing polygons generated 67 from the image by raster-to-vector conversion. The output is an image, in which each pixel 68 value is set as the identifier of the vector feature the pixel belongs to. In all the experiments, 69 the input files and the output files are exactly the same. The only difference is the duration of 70 algorithm execution. We recorded the execution time and made an analysis. The results show 71 that the proposed algorithm significantly decrease the time cost. Specifically, the average 72 duration is reduced from 3.96 seconds to 0.15 second on machine #1 and from 3.647 seconds 73 to 0.073 second on machine #2.

74 The remainder of this paper is organized as follows. Section 2 introduces the background 75 knowledge. Section 3 details the new algorithm and three existing algorithms. In section 4 the 76 experiments are described and the results are evaluated. Section 5 discusses our original 77 contribution to the community. Section 6 concludes the paper and gives the future work.

78

2. Background

79 A large amount of RS data has been obtained by satellite-based or in-situ (e.g., airborne) 80 sensors in the last few decades. Today the amount is still aggressively growing [12, 13]. For 81 example, the NASA Earth Observing System Data and Information System (EOSDIS) [14] 82 has archived over 3.5 million individual Landsat scenes totaling around 1 petabyte of imagery 83 [15, 16]. There are many other RS products and data archive centers around the world.

Comparing to the speed of obtaining RS images, the speed of processing and analyzing images is relatively slow [17, 18]. The complexity of applied algorithms, especially time complexity, has big influences on the speed, and certainly the time value of the information extracted from RS images [19]. Lowering algorithm complexity can reduce the time cost of image analysis and enhance our capability of timely discovering valuable information within the huge RS data.

90 OBIA, one of the current researched hot topics in RS, is comprised of three major steps: 91 image segmentation, post process and object analysis [20] (as shown in Fig. 2). Each step has 92 a set of algorithm choices. Image segmentation filters RS images into a collection of regions 93 [21]. The pixels in one region have the same value. The algorithms for this step have k-means 94 [22], ISODATA [23], mean shift [24], etc. The segmented image goes through a post process 95 including band combination, vectorizing and pixel sorting. The band combination process 96 merges all the bands into only one band. To ensure the mappings between image objects and 97 vector features are bijection, the combination should be reversible which means the one band 98 can be decomposed back to the original bands. The one band is then vectorized into a vector 99 file which outlines the image objects with polygons. Each polygon is managed as a vector 100 feature in geographic information systems. A sorting process will take the segmented image 101 and the vector features as inputs, figure out the containing relationships between the vector 102 features and the image pixels and output a image in which each pixel's value is set as the 103 identifier of the feature it belongs to (Fig. 3).

104 The post process is essential for the next process in the third step such as calculating the 105 properties of image objects. The properties of image objects have three major categories: spatial, spectral and texture [25-27]. The spectral and texture properties of a feature are calculated based on the original values of the contained pixels. Once the property values are generated, people will be able to do some object analysis on them, e.g., supervised classification or feature extraction (buildings, rivers, roads, forests, lakes, lawns, planes, etc) [28-30].



Figure 2. The workflow of OBIA

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Figure 3. Sorting pixels located in vectorized polygons

115 **3. Algorithms**

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116 This section will first list three existing algorithms as comparison and then introduce a 117 new algorithm called two-pixel-reference algorithm. All the algorithms are able to complete

118 the pixel sorting task. But their algorithm complexity is different.

119 **3.1 Shared parameters and variables**

120 Given the inputted image is a one-band image containing X columns and Y rows of pixels.

121 The value of the pixel at column x and row y is represented by function $F_{(x, y)}$. The value of

- 122 variable x ranges from 1 to X. The value of variable y ranges from 1 to Y. The corresponding
- 123 inputted vector file has *M* features/polygons whose identifiers are assigned in sequence from
- 124 1 to *M*. The features are represented by *VF*.





Figure 4. Example inputted image and vector parameters and variables

127 **3.2 Existing algorithms**

128 1) Algorithm #1: This algorithm is based on the widely used four direction seed spreading 129 algorithm. The basic idea is finding a pixel located in a feature and adding it as a seed into a 130 list. Then iterate all its neighbor pixels to find if there is any pixels belonging to the same 131 feature. Four direction means only the pixels located on the east, west, south and north are 132 considered as neighbor pixels. If a neighbor pixel is identified within the feature, it will be 133 taken as a new seed and added to the list. The spreading process is repeated on the new seeds 134 until all the pixels in the list have been processed. Finally, the list will contain all the pixels 135 within the feature. The core steps of this algorithm are detailed below.

1. Get the first seed pixel SP_i for each feature f_i in VF.

2. For each feature f_i , add its seed SP_i to list L.

- 3. Compare SP_i with its four neighbors. If a neighbor has the same value with the seed, add it
- to L. After all the neighbors are compared, mark SP_i as checked.
- 4. Repeat Step 3 on the unchecked seed in L until all the seeds in L are checked. The pixels in

L will be the pixels contained in f_i .

5. Repeat Step 1~4 to sort all the features in VF.

Because the deepest step (Step 3) in the loops could be run by up to $M \times (X \times Y)^4$ times,

- 137 the Big-O complexity of this algorithm is:
- 138 $T_{algorithm1} = O_{(M \times (X \times Y)^4)}$

139 *M* is not a constant variable so it can NOT be ignored.

140 2) Algorithm #2: This algorithm is an improved version of algorithm #1. It takes advantage of

- 141 a characteristics of the segmented image. If the first seed's pixel value of a feature is unique
- among the first seeds of all the features, then all the pixels with this value directly belongs to
- 143 the feature. The steps of algorithm #2 are:

1. Get the first seed pixels for all the features in VF.

2. If the first seed pixel value of f_i is unique, find all the pixels with this value and belong

them to f_i .

3. For those features whose first seed pixel values are not unique, apply Algorithm #1.

144 Suppose the number of the features having unique first seed pixel values is K, then the

- 145 complexity of algorithm #2 is:
- 146 $T_{algorithm} = O_{((M-K)\times(X\times Y)^4)}$

147 3) Algorithm #3: This algorithm is a mutation of algorithm #1. Algorithm #1 and #2 stand on

the position of features, while this algorithm is in the perspective of pixels. The steps are

- 149 described below.
 - 1. Get the first seed pixels for all the features in VF. Add them to a list L_1 .
 - 2. All the pixels are initially marked as unchecked. Scan the pixels line by line.

3. For each unchecked pixel P(x, y), use it as a seed and apply Algorithm #1 to get a list of pixels L_2 .

4. Search L_1 to get the first seed which is listed in L_2 . Get the feature corresponding to the seed. Belong L_2 to the feature.

5. Mark all the pixels in L_2 as checked.

6. Repeat 3~5 until all the pixels in the image are checked.

150 The complexity of this algorithm is:

151 $T_{algorithm3} = O_{((X \times Y)^4)}$

152 **3.3 Two-Pixel-Reference (TPR) Algorithm**

This algorithm avoids most loops in the above three algorithms and trims redundant comparison among pixels to speed up the process. It fully takes advantage of the boundaries of vector features and uses two direction comparison to prevent duplicated comparison. Only three steps are performed in this algorithm. In each step, the loop has no more than two layers to ensure the complexity stays low. The steps are detailed below.

1. For each feature f_i in VF, mark the pixels adjacent to its boundary and locating within f_i by f_i 's identifier. Repeat this step until all the pixels adjacent to feature boundaries are marked. 2. Scan the image row by row. If a pixel $P_{(x, y)}$ is not marked, compare its value $F_{(x, y)}$ with $F_{(x-1, y)}$ and $F_{(x, y-1)}$. If equal to one of them, mark P with the equal one's feature identifier. Repeat this step until all the pixels are marked.

3. Set the identifier values to corresponding pixels and output the image.

This algorithm will be referred to as Algorithm #4 hereafter in this paper. The complexityof this algorithm is:

 $O_{algorithm4} = O_{(X \times Y)}$

161 According to the Big O algorithm complexity rules [31, 32], The four algorithms are

162 placed in order from high complexity to low complexity as:

163 $O_{algorithm} > O_{algorithm2} > O_{algorithm3} > O_{algorithm4}$

164 Therefore, TPR algorithm has the lowest algorithm complexity literally. Next section will

test the physical influences on time cost through experiments.

166 4. Implementation, Experiment and Results

167 We implement the four algorithms using C++ language with support from GDAL library

- 168 [33]. The code is available in a public GitHub repository
- 169 <u>https://github.com/VirginiaJRS/PixelsInSegment.</u>

We run the code on a test image on two machines. Fig. 5a shows the original test image,
a high resolution optical remote sensing image of the Dallas Love Field Airport at Texas, U.S.
Fig. 5b and 5c are the input files of the algorithms and Fig. 5d is the outputted image. One test
machine is a HP laptop with Windows 7 64-bit system, Intel Core i5-2450M CPU (2.50GHz)
and 6 gigabytes RAM memory. The other machine is a HP Proliant DL180 G6 rack server
with Ubuntu Linux 12.04 LTS system, 8 core Intel(R) Xeon(R) CPU E5606 (2.13GHz) and 8
gigabytes RAM memory.

As the operating systems are in parallel processing mode, other running threads at the same time will definitely impact the duration of each execution of the algorithms. To reduce the uncertain impacts of the external factors and create a fair test environment, we killed as many threads as possible before the tests are conducted. During the test, both machines are dedicated and not be used for any other tasks. The execution time is automatically recorded

- 182 by the code and exported to tables by a Shell script. We visualized the time cost data into
- 183 multiple plots as shown in Fig. 6.



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(a)



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199 the same algorithm. For example, the time cost of Algorithm #1 on machine #1 ranges from

200	300 seconds to 550 seconds, while the time cost on machine #2 ranges from 260 seconds to
201	300 seconds. Generally for all the four algorithms, the time cost on machine #2, which is a
202	rack server, is more stable than machine #1 which is a laptop. But the differences on time cost
203	among algorithms are still very apparent. The range of time cost of the four algorithms is
204	listed in Table 1. All the ranges are never overlapped with each other and have a clear
205	high-to-low sequence which completely agrees with the literal order analyzed in Section 3.
206	The time cost of the TPR algorithm (#4) is obviously the lowest on both machines. We also
207	calculated the average time cost of each algorithm on the two machines (Table 2). The time
208	cost of algorithm #4 is always below 0.2 second. Such an interval is actually senseless by
209	human beings. Comparing to the time cost of 3 seconds (algorithm #3), 200 seconds
210	(algorithm #2) and 270 seconds (algorithm #1), TPR algorithm significantly compressed the
211	time cost of this process into a very satisfying level.

The dimension of the test image is 800 pixels (X) by 538 pixels (Y) and the number of features is 900 (M). If the inputted image is changed to a larger one and the feature number also increases, the time cost of each algorithm will definitely increase. According to the Big-O algorithm complexity rules, the time cost of algorithm #4 will remain the lowest among the four.

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Table 1. The ranges of time cost for the four algorithms (unit: second)

	Algorithm #1	Algorithm #2	Algorithm #3	Algorithm #4
Machine #1	300~550	200~280	2~10	0.07~0.3
Machine #2	260~300	197~207	3.63~3.66	0.06~0.08

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Table 2. The average time costs of the four algorithms on two machines (unit: second)

	Algorithm #1	Algorithm #2	Algorithm #3	Algorithm #4
Machine #1	350.321	235.810	3.96	0.15
Machine #2	276.823	200.578	3.647	0.073

219 **5. Discussion**

220 5.1 Performance

221 TPR algorithm can help speed up the process of OBIA and shorten the interval between 222 the image acquired date and the image analyzed date. A direct impact on service providers 223 and endpoint users is the data processing time is reduced. There are three major modes for RS 224 image analysis: manual, semi-automatic and automatic. The semi-automatic mode allows 225 image analysts to use GIS/RS software such as ArcGIS, ENVI, ERDAS, eCognition for automatic assistance and is the most used one. The workflow is sequential. Once an analyst 226 227 submits a request to the systems, (s) he will have to wait until the segmentation is completed. 228 If one process like the pixel sorting process becomes faster, the time that analyzers spend on 229 waiting will decrease respectively. The time for analyzing an image will lower too. Eventually 230 the interval between the image acquiring date and the date when endpoint users receive the 231 analyzed products will shrink. This is very meaningful in urgent cases such as earthquake, 232 flooding, wild fire, debris flow and typhoon when every second counts.

233 5.2 Application Vision

This algorithm provides a good example for researchers to develop optimal complexity algorithms for time saving purposes. Most current researchers in RS mainly focus on improving result accuracy and show less care on time costs. In many researches, the efficiency of algorithms is sacrificed to pursue for a more accurate result such as Neural Network and SVM based image analysis techniques. Their outputs may have higher accuracy but take much longer than basic analysis techniques. In other words, more recent researches are engaged in augmenting the information value of RS products but ignore the time value. This work try to display the power of time-efficient algorithms in RS and make the overall duration of an analysis on a RS image into an endurable level.

243 **6. Conclusion and Future Work**

244 This paper proposes a novel algorithm, named TPR algorithm, to speed up the process of 245 sorting pixels in segmented RS images. It avoids most multiple-layer loops in existing 246 methods and trims many redundant comparison among pixels. It fully leverages the 247 boundaries of vector features and uses two direction comparison to prevent duplicated 248 comparison. Its Big O algorithm complexity is very lower than existing algorithms. We 249 implemented the algorithm in C++ and published the code onto GitHub. Experiments have 250 been made by running the code with a high resolution optical RS test image on two different 251 machines. In every single test, the time cost of TPR algorithm is always the lowest. The 252 results prove that the new algorithm significantly decreases the time cost of the process. The 253 average duration is reduced from 3.96 seconds to 0.15 second on machine #1 and from 3.647 254 seconds to 0.073 second on machine #2. The algorithm sets a good example for time-efficient 255 algorithms to speed up the overall process of OBIA in the big data era.

To make TPR algorithm able to serve as a robust building block in OBIA, we will maintain and update the code on GitHub. Besides, the current test image is a high resolution optical image. We will apply the algorithm on high spectral images in our next stage of work. In addition, how to fasten the other steps in OBIA while keeping the accuracy not going down 260 will be studied too.

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