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Relative humidity gradients as a key constraint on terrestrial water and energy fluxes

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1 **Abstract:**

2 Earth's climate and water cycle are highly dependent on the latent heat flux (LE) associated with
3 terrestrial evapotranspiration. While the widely-used Penman-Monteith LE model is useful to
4 explore vegetative controls on LE , land-atmosphere interactions are difficult to interpret due to
5 the complex role of biological controls on underlying physical processes. Here, we present a
6 novel LE model that defines LE as a combination of diabatic (heat-driven) and adiabatic (relative
7 humidity (rh) gradient-driven) processes using only abiotic variables. This approach yields new
8 insights on the fundamental characteristics of LE . Here we show that the ratio of LE to available
9 energy is mainly controlled by vertical rh gradients, but the spatiotemporal variability
10 in rh gradients are small due to equilibration at the land-atmosphere boundary. Consequently, the
11 global mean vertical rh gradient is near zero, implying land-atmosphere equilibrium at the
12 global-scale. As a result, the spatiotemporal variability of LE is largely determined by the
13 diabatic term, which can be readily determined by standard meteorological measurements. Our
14 proposed model and findings provide a fundamental benchmark for LE predictions. By
15 demonstrating how land surface conditions become encoded in the atmospheric state, our model
16 will also help to improve our understanding of Earth's climate system and water cycle.

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Main text:

Latent heat flux (LE) associated with plant transpiration and evaporation from soil and intercepted water is the key component linking the water cycle and the terrestrial energy budget. More than half of the incoming radiation energy at the land surface is consumed as LE , making evapotranspiration (i.e., the sum of evaporation and transpiration) the second largest flux in the terrestrial water balance after precipitation ¹, and a key driver of Earth’s climate system ². However, because the land surface is heterogeneous and mainly unsaturated, our ability to predict LE remains inadequate, as evidenced by poorly constrained representations of LE in the current generation of climate models ³. While most research has been devoted to developing and improving rate-limiting parameters constraining LE such as García, et al. ⁴, exploring the governing physics of LE has received less attention following earlier pioneering work ⁵⁻⁸. Understanding the governing physics is especially important in the era of the Anthropocene since the variability of LE has become more unpredictable ^{9,10}.

A traditional way to understand the governing physics is to partition LE into diabatic and adiabatic processes using the Penman-Monteith (PM) equation ⁷, as proposed by Monteith ¹¹. The PM equation combines the energy balance equation with mass-transfer theory for water vapour and sensible heat, resulting in diabatic (radiative energy-related) and adiabatic (vapour pressure deficit-related) processes for a parcel of air in contact with a saturated surface ¹¹.

$$LE = \underbrace{\frac{S}{S+\gamma\left(\frac{r_a+r_s}{r_a}\right)} \cdot Q}_{\text{Diabatic process}} + \underbrace{\frac{\rho c_p}{S+\gamma\left(\frac{r_a+r_s}{r_a}\right)} \cdot \frac{e^*(T_a)-e_a}{r_a}}_{\text{Adiabatic process}} \quad (1)$$

38 where S is the linearized slope of saturation vapour pressure versus temperature (hPa K^{-1}), γ is
39 the psychrometric constant (hPa K^{-1}), ρ is the air density (kg m^{-3}), c_p is the specific heat capacity
40 of air at constant pressure ($\text{MJ kg}^{-1} \text{K}^{-1}$), and Q is available radiative energy (i.e., difference
41 between net radiation and soil heat flux and expressed in units of W m^{-2}). $e^*(T_a)$ is the saturation
42 vapour pressure (hPa) at air temperature (T_a) measured at a reference height, and e_a is vapour
43 pressure (hPa) at the reference height. The term $[e^*(T_a) - e_a]$ is known as atmospheric vapour
44 pressure deficit (VPD, expressed in units of hPa). r_a is total aerodynamic resistance to heat and
45 water vapour transfer (s m^{-1}), and r_s is surface resistance to water vapour transfer (s m^{-1})
46 representing drying soil and/or plant stomatal closure.

47 In principle, high VPD at the reference height increases the adiabatic term in Eq. (1) ¹².
48 Yet, this “high VPD leads to high LE ” interpretation cannot be generalized because r_s increases
49 with VPD due to stomatal closure by vegetation under high VPD conditions ¹³⁻¹⁵. While the PM
50 equation is useful to explore biological control of LE through r_s ⁵, physical mechanisms of each
51 term in Eq. (1) are less intuitive due to the sensitivity of r_s to VPD.

52 Is there a way to mathematically express the physical mechanisms of LE without
53 requiring r_s ? Helpfully, Monteith ¹¹ provided another form of the LE model for the case when the
54 surface does not reach saturation (i.e., the relative humidity (rh) of the surface is less than unity),
55 and for which r_s is not required. Here, we further find that there are two mathematical
56 expressions of LE which are capable of accounting for the vertical gradients in rh . The following
57 pair of equations allow us to capture the thermodynamic process governing turbulent heat
58 exchange between the land surface and the atmosphere, including under unsaturated land surface
59 conditions (derivation in [Appendix A](#)).

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$$61 \quad LE = \underbrace{\frac{rh_s S}{rh_s S + \gamma} \cdot Q}_{\text{Diabatic process: } LE_Q} + \underbrace{\frac{\rho c_p e^*(T_a)}{rh_s S + \gamma} \cdot \frac{rh_s - rh_a}{r_a}}_{\text{Adiabatic process: } LE_G} = LE_Q + LE_G \quad (2)$$

$$62 \quad LE = \underbrace{\frac{rh_a S}{rh_a S + \gamma} \cdot Q}_{\text{Diabatic process: } LE_{Q'}} + \underbrace{\frac{\rho c_p e^*(T_s)}{rh_a S + \gamma} \cdot \frac{rh_s - rh_a}{r_a}}_{\text{Adiabatic process: } LE_{G'}} = LE_{Q'} + LE_{G'} \quad (3)$$

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64 where rh_s and rh_a are rh at the land surface and the reference height, respectively. Equations (2)
 65 and (3) include rh_s to compensate for eliminating r_s from the original PM equation. Since the
 66 adiabatic process in Eqs. (2) and (3) are controlled by the vertical difference of rh , we refer to
 67 Eqs. (2) and (3) as the proposed PM_{rh} model (Penman-Monteith equation expressed using rh) to
 68 distinguish it from the original PM model. The two equations represent different thermodynamic
 69 paths which will be discussed in the next section. Arguably, applying PM_{rh} can provide new
 70 insights into the fundamental mechanisms of LE , particularly when it is decomposed into its
 71 energy driven diabatic component (LE_Q or $LE_{Q'}$) and its adiabatic component (LE_G or $LE_{G'}$) that
 72 is driven by the gradient in rh .

73 In this paper, we first present the theory of our PM_{rh} model, and apply it empirically to an
 74 eddy-covariance observation site. Also, the proportion of net available energy consumed in
 75 evapotranspiration, known as the evaporative fraction ($EF = \frac{LE}{Q}$) is decomposed into $\frac{LE_Q}{Q}$ and $\frac{LE_G}{Q}$.
 76 Finally, we apply the decomposition approach to a global LE dataset ¹⁶ to understand how LE_Q
 77 and LE_G vary spatiotemporally in different regions of the world, and discuss how these patterns
 78 can help to understand land-atmosphere interactions and potential responses under future
 79 climatic conditions.

80

81 **Theory and observational evidence.**

82 Before discussing PM_{th} in-depth, we revisit the Penman equation ⁶ to help with the physical
 83 reasoning behind our proposed framework. The widely recognized form of the Penman equation,
 84 which was developed as an *LE* model for a saturated surface, is as follows:

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$$86 \quad LE = \underbrace{\frac{s}{s+\gamma} \cdot Q}_{\text{Diabatic process}} + \underbrace{\frac{\rho c_p [e^*(T_a) - e_a]}{[s+\gamma] r_a}}_{\text{Adiabatic process}} \quad (4)$$

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88 We rearrange this original formulation to derive Eq. (5) by factoring out $e^*(T_a)$ and introducing
 89 $rh_a = \frac{e_a}{e^*(T_a)}$ into the second term.

90

$$91 \quad LE = \underbrace{\frac{s}{s+\gamma} \cdot Q}_{\text{Diabatic process}} + \underbrace{\frac{\rho c_p e^*(T_a)}{s+\gamma} \cdot \frac{1-rh_a}{r_a}}_{\text{Adiabatic process}} \quad (5)$$

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93 Equations (4) and (5) are mathematically equivalent, but their interpretations are quite
 94 different. In Eq. (4), the adiabatic process is controlled by VPD at the reference height. However,
 95 in Eq. (5), the adiabatic process acts over the vertical rh difference from the surface to the
 96 reference height. Since the Penman equation is a model for saturated surfaces, $1 - rh_a$ in Eq. (5)
 97 indicates the vertical rh difference. Arguably, Eq. (5) is more thermodynamically sound
 98 compared to Eq. (4) since rh is an ideal-gas approximation to the water activity ¹⁷ which
 99 represents the chemical potential of water (μ_w) ^{12,18}. When the vertical gradient of rh dissipates,
 100 the land surface and the atmosphere are in thermodynamic equilibrium ¹⁹. Therefore, taking Eq.
 101 (5) instead of Eq. (4) allows us to view the adiabatic process of the Penman model as a

102 reequilibration process driving land-atmosphere equilibrium by bringing the surface μ_w to that of
103 the atmosphere.

104 As with our interpretation of the Penman model, we can view Eq. (2), as a generalized
105 form of the Penman model. Here, the $LE_G (= \frac{\rho c_p e^*(T_a)}{r_{h_s S + \gamma}} \frac{r_{h_s} - r_{h_a}}{r_a})$ term of Eq. (2) is an
106 reequilibration process between the land and the atmosphere when the land surface is not
107 saturated. It is worth noting that LE_G can be negative when r_{h_s} is less than r_{h_a} . Thus, the LE_G
108 term acts to reduce the vertical rh gradient. This physical interpretation is consistent with recent
109 findings that the variance of the rh gradient tends to be minimized over the course of the day
110 ^{20,21}. The diabatic $LE_Q (= \frac{r_{h_s S}}{r_{h_s S + \gamma}} Q)$ term can be understood as equilibrium LE for an unsaturated
111 surface as was recently suggested by McColl, et al. ²², which we discuss later in this section.

112 How then can we interpret the two formulas of PM_{rh} in Eqs. (2) and (3)? To explain the
113 two forms, we use the psychrometric relationship applied to a parcel of air near an unsaturated
114 land surface that is under constant pressure and steadily receiving radiation energy ¹¹. The initial
115 thermodynamic state of the air parcel can be represented by its temperature and water vapour
116 pressure such as point A in [Figure 1](#). The initial state is changed by two processes as follows: (1)
117 equilibrating between the land surface (r_{h_s}) and the air parcel (r_{h_a}), and (2) increasing enthalpy
118 forced by the incoming energy.

119 In the equilibrating process, the air parcel is adiabatically cooled (or heated when $r_{h_s} <$
120 r_{h_a}), while the enthalpy of the parcel is not changed. Therefore, the increase (decrease) in latent
121 heat content in the parcel is exactly balanced by a decrease (increase) in sensible heat ($A \rightarrow B$ in
122 [Figure 1](#): trajectory along constant enthalpy line). This process is equivalent to the LE_G term in
123 Eq. (2). Now, the air parcel is in thermodynamic equilibrium with the land surface (point B in

124 [Figure 1](#)). Then, the air parcel receives energy while the equilibrium is sustained (i.e., rh_s is
125 steady), which increases both the temperature and absolute water vapour content of the air parcel
126 ($B \rightarrow C$ in [Figure 1](#)). This process can be expressed as LE_Q of Eq. (2). Consequently, the
127 thermodynamic state of the air parcel approaches point C in [Figure 1](#).

128 However, we should recognize that temperature and vapour pressure are “state” variables
129 meaning that they do not depend on the thermodynamic path by which the system arrived at its
130 final state²³. In the above example, we conceptually followed the adiabatic process first and then
131 the diabatic process (Path 1 in [Figure 1](#)), but one can imagine the opposite order. If we choose
132 Path 2 in [Figure 1](#), the diabatic process comes the first, and thus rh_a instead of rh_s is preserved
133 while enthalpy increases (i.e., LE_Q'), and the adiabatic process is followed at temperature of T_S
134 (i.e., LE_G'). Path 2 is described by Eq. (3).

135 Therefore, one can interpret the two forms of PM_{rh} in Eqs. (2) and (3) as two
136 thermodynamic paths where the diabatic and adiabatic processes occur simultaneously. It should
137 be noted that the diabatic and adiabatic processes in PM_{rh} are “path” functions and thus they vary
138 by path. For instance, LE_Q is slightly higher than LE_Q' when $rh_s > rh_a$. However, as shown by
139 [Figure 2 \(a1\) and \(a2\)](#), observational data from around the world represented in the
140 FLUXNET2015²⁴ dataset indicate that differences between LE_Q and LE_Q' , as well as differences
141 between LE_G and LE_G' , are marginal at daily time scale. This is an important point since LE_Q'
142 can be determined simply and directly using by reference height meteorological measurements,
143 while LE_Q is required to know rh_s .

144 Another distinct characteristic of the PM_{rh} model is the way it defines equilibrium at the
145 land-atmosphere interface. Unlike many previous studies which focused on the vertical gradient
146 of VPD^{8,25,26}, land-atmosphere equilibrium is achieved in the PM_{rh} model when the vertical rh

147 gradient (i.e., the μ_w gradient) dissipates. That is, if $rh_s \approx rh_a$, then it follows that LE_G (or LE_G')
148 is zero and thus LE becomes

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$$150 \quad LE \approx \frac{rh_a S}{rh_a S + \gamma} Q \quad (6)$$

151

152 Equation (6), is identical to the “surface flux equilibrium (SFE)” theory recently introduced by
153 McColl, et al. ²². They hypothesized that in many continental regions, the near surface
154 atmosphere is in state of SFE, where the surface moistening and surface heating terms are
155 balanced in the rh budget, especially at longer time scales. Equation (6) successfully predicted
156 observed LE at daily and multiday time scales for inland regions ²⁷, which implies the vertical rh
157 gradient tends to zero. This is logical in that LE_G itself operates to diminish the vertical rh
158 gradient. Our analysis in [Figure 2](#) also indicates that the mean value of daily LE_G of all
159 FLUXNET2015 sites is close to zero, implying global-scale land-atmosphere equilibrium.
160 Importantly, LE is primarily determined by LE_Q ($R^2 = 0.65$) instead of LE_G ($R^2 = 0.18$).
161 Nevertheless, FLUXNET2015 data suggests that LE_G is the main driver of local-scale variability
162 of EF at the daily time scale ([Figure 2 \(c1\) and \(c2\)](#)).

163

164 **Time series of decomposed LE .**

165 In order to explore the influence of varying conditions on individual decomposed LE terms and
166 identify land-atmosphere equilibrium conditions, we applied the PM_{th} model to multi-year
167 observational eddy-covariance data collected at an irrigated sugarcane farm in Costa Rica. The
168 site has wet-dry tropical climate with a dry season from December to March. The decomposition

169 analysis of LE shows that while LE_Q is the major component of LE , LE_G variability plays a major
170 role in seasonal behavior of LE , which is confirmed by wavelet analysis (Fig. 3 d1-d2).
171 Interestingly, the annual mean LE_G was the highest in 2015, a drought year in which rh_a was
172 generally lower than for the other years, while the annual mean LE_G was close to zero only in
173 2016 when there was no application of dry season irrigation.

174 To explore the diurnal behaviour of decomposed LE , we selected different surficial and
175 atmospheric conditions when LE_G was zero, positive, or negative in Fig. 3 (c1) - (c4). In the 2016
176 dry season, LE_G was close to zero as a daily average value, as a result of negative daytime and
177 positive nighttime LE_G values due to dry air and dry soil conditions (no irrigation) and
178 undeveloped vegetation canopy (Fig. 3 (c1)). Daily LE_G was also close to zero during wet season
179 conditions (e.g., Fig. 3 (c2)). In this case, LE_G was near zero during both daytime and nighttime
180 periods due to near saturated atmospheric and land surface conditions. These two cases show that
181 dry land-dry air or wet land-wet air conditions can each lead to daily scale land-atmosphere
182 equilibrium (i.e., $LE_G \approx 0$), although the diurnal pattern of LE_G is starkly different for dry land-
183 dry air vs. wet land-wet air conditions.

184 Meanwhile, when rh_a was low (≈ 0.55) and the canopy was well-developed, LE_G was
185 found to be positive during both daytime and nighttime periods (Fig. 3 (c3)). On the other hand,
186 during post-harvest conditions when vegetative canopy cover was minimal and air and soil
187 moisture levels were low, daily LE_G was found to be negative as a result of negative daytime and
188 positive nighttime LE_G values (Fig. 3 (c4)). Regarding the overall diurnal pattern, LE_G generally
189 declined during the morning and increased in the afternoon, which is consistent with the well-
190 known diurnal pattern of EF^{28,29} (Fig. 3 (c5)).

191

192 **Spatial pattern of decomposed LE .**

193 We then applied the PM_{rh} model to the FLUXCOM dataset, a benchmark global LE data product
194 ¹⁶. As shown in Fig 4 (a) and (c), the spatial patterns of the annual mean LE and LE_Q were
195 similar. The monthly time series of global LE and its two components in Fig 4 (e1) show that
196 LE_G is consistently close to zero and that LE is mostly determined by LE_Q ($R^2 = 0.85$) instead of
197 LE_G ($R^2 = 0.18$) (Fig 4 (f1) and (f2)). This result is consistent with Eq. (6) and the SFE theory. In
198 other words, the land surface is generally under thermodynamic equilibrium with the atmosphere
199 at the global-annual scale (i.e., $rh_s \approx rh_a$).

200 However, while mean annual LE_G was close to zero in broad areas (particularly in high
201 latitude regions), it was distinctly positive or negative in many regions (Fig 4 (d)). In humid
202 tropical regions like the Amazon basin where moisture convergence is large, LE_G was generally
203 positive, whereas arid regions such as Australia where characterized by negative LE_G (Fig 4 (e3)
204 and (e4)). The spatial pattern of LE_G is similar to the spatial pattern of EF (Fig 4 (b)). The finding
205 that that the spatial variation of EF is primarily controlled by LE_G instead of LE_Q was supported
206 by correlation analyses ($R^2 = 0.60$ for $EF \sim LE_G$ and $R^2 = 0.28$ for $EF \sim LE_Q$; Fig 4 (f3) and (f4)).

207

208 **Discussion.**

209 As described in the theory section, land-atmosphere equilibrium is achieved when LE_G
210 approaches zero and thus LE reduces to Eq. (6). The decomposed terms derived from both the
211 empirical FLUXNET and model-based FLUXCOM datasets show that the global mean for LE_G
212 is near zero, implying global-scale land-atmosphere equilibrium (Fig 2 and Fig 4). This result
213 extends the SFE theory of McColl, et al. ²². Although, LE_G is not always near zero particularly in
214 low latitude regions where the influence of the ocean and atmospheric on rh_a is significant³⁰,

215 moisture convergence and divergence at the global-scale tend to balance each other, out resulting
216 global-scale land-atmosphere equilibrium. Moisture convergence and divergence drives
217 spatiotemporal variability of EF at local scales, with moisture convergence vs. divergence
218 appearing encoded as the sign of LE_G . Indeed, the spatial pattern in Fig 4 (d) clearly
219 distinguishes atmospheric moisture convergence regions such as South Atlantic convergence
220 zone (SACZ) of southeastern Brazil (25°S, 55°W).

221 Salvucci and Gentine²⁰ found that the variance of the rh gradient tends to be minimized
222 over the course of the day, and they developed an approach to predict LE based on this finding.
223 However, its physical mechanisms remain elusive. Our PM_{rh} model provides theoretical support
224 for Salvucci and Gentine's approach²⁰ in that LE_G acts to reduce the rh gradient. Indeed, the
225 diurnal cycles of the LE_G in Fig 3 are aligned with their findings with respect to the sign of LE_G
226 during daytime and nighttime. Over the course of the day, rh_a coevolves with rh_s through the
227 equilibration process (i.e., LE_G), and thus the land surface moisture status is linked to rh_a . This
228 interpretation also can explain the widely-accepted Bouchet's complementary hypothesis³¹ in
229 that land wetness can be parameterized based on rh_a such as Priestley-Taylor (PT) JPL LE
230 prediction model^{4,32}.

231 In summary, we have shown that our novel PM_{rh} model provides a new opportunity to
232 understand the governing physics of the terrestrial energy budget. Our findings suggest that
233 while LE_G is a primary component determining EF, spatiotemporal variability of LE_Q alone can
234 adequately represent the variability of LE . Our analyses reveal global-scale land-atmosphere
235 equilibrium which can be a fundamental benchmark against which LE predictions derived from
236 climate models can be assessed. Also, our analysis shows how the land surface conditions
237 become encoded to the atmospheric state. Questions remain regarding how LE_Q and LE_G will be

238 influenced in relation to changing climatic and land surface conditions, and how these changes
239 might affect the climate system at differing spatial and temporal scales through positive or
240 negative feedbacks.
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Methods.

FLUXNET2015. The daily scale FLUXNET2015 dataset, which includes 212 empirical eddy-covariance flux tower sites around globe, was used in this study²⁴. The turbulent heat fluxes, net radiation, soil heat flux, air temperature, relative humidity, wind speed, friction velocity, and barometric pressure were obtained from the dataset and then quality-controlled (details in [Appendix B](#)). In order to decompose daily LE into LE_Q and LE_G , we first estimated daily aerodynamic resistance (r_a) by considering aerodynamic resistance to momentum transfer and the additional boundary layer resistance for heat and mass transfer (or excess resistance)^{12,33,34}.

$$r_a = \frac{u_*^2}{u(z_r)} + 6.2u_*^{-0.67} \quad (7)$$

The first term on the right hand side of Eq. (7) is the aerodynamic component and the second term is the boundary layer component. Here, u_* is friction velocity and $u(z_r)$ is reference height wind speed. r_a was estimated using the bigleaf R package³³.

By rearranging Eq. (2), rh_s can be calculated using.

$$rh_s = \frac{\gamma LE r_a / \rho c_p + e_a}{SH r_a / \rho c_p + e^*(T_a)} \quad (8)$$

LE_Q and LE_Q' were calculated using rh_a and rh_s following Eqs. (2) and (3), and then LE_G and LE_G' were calculated by subtracting LE_Q and LE_Q' from LE . To calculate LE_Q and LE_Q' , we define Q as $LE + H$, but it should be noted this approach can include systematic uncertainty since the sum of LE and H measured by eddy-covariance system is typically lower than the difference

264 between net radiation (R_n) and the soil heat flux (G) (i.e., conditions referred to as the energy
265 balance closure problem³⁵). To investigate the effect of energy balance closure problem, we
266 provide [Figure S1](#) that was generated by 1) defining Q as $R_n - G$, and 2) correcting LE and H
267 based on the assumption that the Bowen ratio ($B = H/LE$) is correct²⁴. We found that [Figure S1](#)
268 and [Figure 2](#) are almost identical, implying that the lack of surface energy balance closure does
269 not significantly impact our analyses and interpretations.

270

271 In-situ dataset. In-situ half-hourly eddy-covariance observations used in this study were made
272 from 2015 to 2018 on a ratoon sugarcane farm in the province of Guanacaste, Costa Rica
273 ($10^{\circ}25'07.60''N$; $85^{\circ}28'22.22''W$). The site has a wet-dry tropical climate with a dry season from
274 December to March and a median monthly air temperature ranging from $27^{\circ}C$ to $30^{\circ}C$. The
275 study site experienced drought in 2015³⁶. The site was irrigated occasionally during dry seasons
276 via furrow irrigation events, except for 2016 when there was no irrigation due to crop replanting.
277 Due to ratooning practice (detailed explanation in [Appendix B](#)), the sugarcane growing seasons
278 varied by year, which provided an opportunity to explore distinct and varied combinations of
279 land cover fraction and atmospheric aridity conditions.

280 The measurement data were quality controlled following Morillas, et al.³⁶ (details in
281 [Appendix B](#)). Half-hourly r_a was then estimated by Eq. (9) instead of Eq. (7) in order to
282 explicitly include atmospheric stability and canopy height dynamics³³.

283

$$284 \quad r_a = \frac{\ln\left[\frac{z_r - d}{z_{om}}\right] - \psi_h}{k u_*} + 6.2 u_*^{-0.67} \quad (9)$$

285

286 where, k is the von Kármán constant (0.41), d is the zero-plane displacement height ($d = 0.7z_h$),
287 z_{0m} is the roughness length for momentum ($z_{0m} = 0.1z_h$), ψ_h is the integrated form of the stability
288 correction function. z_h is canopy height based on manual measurements taken during regular
289 maintenance visits. r_a was estimated using bigleaf R package³³ and rh_s was calculated from Eq.
290 (8). Negative H and inaccurate r_a modelling sometimes yielded negative rh_s or values greater
291 than one, especially at nighttime. In these cases, rh_s was assigned the value of one following the
292 approach described in the bigleaf R package³³. We then estimated LE_Q and LE_G from Eq. (2).

293
294 FLUXCOM LE dataset decomposition. The FLUXCOM dataset¹⁶ is a global-scale machine
295 learning ensemble product which upscales FLUXNET observations³⁷ using Moderate
296 Resolution Imaging Spectroradiometer (MODIS) satellite data and reanalysis meteorological
297 data. In this study we used the monthly LE dataset (0.5° resolution) modelled using MODIS and
298 ECMWF ERA5 reanalysis data.

299 From our analyses of the FLUXNET2015 global empirical data we learned that LE_Q and
300 LE_Q' are almost identical. Therefore, instead of trying to model LE_Q , we simply estimated LE_Q as
301 LE_Q' . Here, Q was obtained from the FLUXCOM output, and air temperature and relative
302 humidity were retrieved from ERA5-Land monthly averaged data (2 m height). LE_G was then
303 estimated by subtracting LE_Q from LE .

304

305

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315 Y.K., L.M., and M.S.J. performed research; Y.K. analyzed data; Y.K., M.G., L.M., T.A.B, and
316 M.S.J. wrote the paper.

317 **Competing interests:** Authors declare no competing interests.

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References:

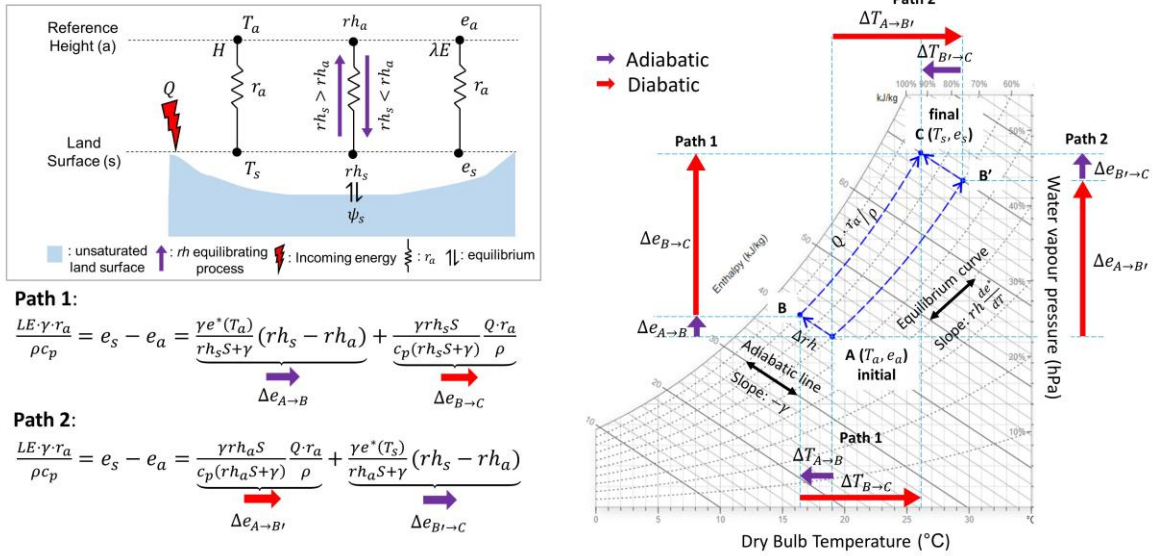
- 321 1 Oki, T. & Kanae, S. Global hydrological cycles and world water resources. *Science* **313**,
322 1068-1072 (2006).
- 323 2 Willett, K. *et al.* HadISDH land surface multi-variable humidity and temperature record
324 for climate monitoring. *Climate of the Past* **10** (2014).
- 325 3 Ma, H.-Y. *et al.* CAUSES: On the Role of Surface Energy Budget Errors to the Warm
326 Surface Air Temperature Error Over the Central United States. *Journal of Geophysical*
327 *Research: Atmospheres* **123**, 2888-2909, doi:10.1002/2017jd027194 (2018).
- 328 4 García, M. *et al.* Actual evapotranspiration in drylands derived from in-situ and satellite
329 data: Assessing biophysical constraints. *Remote Sensing of Environment* **131**, 103-118,
330 doi:10.1016/j.rse.2012.12.016 (2013).
- 331 5 Jarvis, P. G. & McNaughton, K. G. in *Advances in ecological research* Vol. 15 1-49
332 (Elsevier, 1986).
- 333 6 Penman, H. L. Natural evaporation from open water, bare soil and grass. *Proceedings of*
334 *the Royal Society of London. Series A. Mathematical and Physical Sciences* **193**, 120-145
335 (1948).
- 336 7 Monteith, J. L. in *Symposia of the society for experimental biology*. 205-234 (Cambridge
337 University Press (CUP) Cambridge).
- 338 8 Priestley, C. H. B. & Taylor, R. J. On the Assessment of Surface Heat Flux and
339 Evaporation Using Large-Scale Parameters. *Monthly Weather Review* **100**, 81-92,
340 doi:10.1175/1520-0493(1972)100<0081:otaosh>2.3.co;2 (1972).
- 341 9 Milly, P. C. D. *et al.* Stationarity Is Dead: Whither Water Management? *Science* **319**,
342 573-574, doi:10.1126/science.1151915 (2008).
- 343 10 Marvel, K. *et al.* Twentieth-century hydroclimate changes consistent with human
344 influence. *Nature* **569**, 59-65, doi:10.1038/s41586-019-1149-8 (2019).
- 345 11 Monteith, J. L. Evaporation and surface temperature. *Quarterly Journal of the Royal*
346 *Meteorological Society* **107**, 1-27, doi:10.1002/qj.49710745102 (1981).
- 347 12 Monteith, J. & Unsworth, M. *Principles of environmental physics: plants, animals, and*
348 *the atmosphere*. (Academic Press, 2013).
- 349 13 Novick, K. A. *et al.* The increasing importance of atmospheric demand for ecosystem
350 water and carbon fluxes. *Nat Clim Change* **6**, 1023, doi:10.1038/nclimate3114 (2016).
- 351 14 Tan, C. S., Black, T. A. & Nnyamah, J. U. A Simple Diffusion Model of Transpiration
352 Applied to a Thinned Douglas-Fir Stand. *Ecology* **59**, 1221-1229, doi:10.2307/1938235
353 (1978).
- 354 15 Massmann, A., Gentine, P. & Lin, C. When Does Vapor Pressure Deficit Drive or
355 Reduce Evapotranspiration? *Journal of Advances in Modeling Earth Systems* **11**, 3305-
356 3320, doi:10.1029/2019ms001790 (2019).
- 357 16 Jung, M. *et al.* The FLUXCOM ensemble of global land-atmosphere energy fluxes.
358 *Scientific Data* **6**, 74, doi:10.1038/s41597-019-0076-8 (2019).
- 359 17 Lovell-Smith, J. W. *et al.* Metrological challenges for measurements of key
360 climatological observables. Part 4: atmospheric relative humidity. *Metrologia* **53**, R40-
361 R59, doi:10.1088/0026-1394/53/1/r40 (2015).
- 362 18 Kleidon, A. & Schymanski, S. Thermodynamics and optimality of the water budget on
363 land: A review. *Geophysical Research Letters* **35**, doi:10.1029/2008gl035393 (2008).

- 364 19 Kleidon, A., Schymanski, S. & Stieglitz, M. in *Bioclimatology and Natural Hazards*
365 (eds Katarína Štřelcová *et al.*) 107-118 (Springer Netherlands, 2009).
- 366 20 Salvucci, G. D. & Gentine, P. Emergent relation between surface vapor conductance and
367 relative humidity profiles yields evaporation rates from weather data. *Proceedings of the*
368 *National Academy of Sciences* **110**, 6287-6291, doi:10.1073/pnas.1215844110 (2013).
- 369 21 Rigden, A. J. & Salvucci, G. D. Evapotranspiration based on equilibrated relative
370 humidity (ETRHEQ): Evaluation over the continental U.S. *Water Resources Research*
371 **51**, 2951-2973, doi:10.1002/2014wr016072 (2015).
- 372 22 McColl, K. A., Salvucci, G. D. & Gentine, P. Surface Flux Equilibrium Theory Explains
373 an Empirical Estimate of Water-Limited Daily Evapotranspiration. *Journal of Advances*
374 *in Modeling Earth Systems* **0**, doi:10.1029/2019ms001685 (2019).
- 375 23 Iribarne, J. V. & Godson, W. L. *Atmospheric thermodynamics*. Vol. 6 (Springer Science
376 & Business Media, 2012).
- 377 24 Pastorello, G. *et al.* The FLUXNET2015 dataset and the ONEFlux processing pipeline
378 for eddy covariance data. *Scientific Data* **7**, 225, doi:10.1038/s41597-020-0534-3 (2020).
- 379 25 McNaughton, K. G. & Jarvis, P. G. Predicting effects of vegetation changes on
380 transpiration and evaporation. *Water deficits and plant growth* **7**, 1-47 (1983).
- 381 26 Raupach, M. R. Combination theory and equilibrium evaporation. *Quarterly Journal of*
382 *the Royal Meteorological Society* **127**, 1149-1181, doi:10.1002/qj.49712757402 (2001).
- 383 27 McColl, K. A. & Rigden, A. J. Emergent simplicity of continental evapotranspiration.
384 *Geophysical Research Letters* **n/a**, e2020GL087101, doi:10.1029/2020gl087101 (2020).
- 385 28 Gentine, P., Entekhabi, D. & Polcher, J. The Diurnal Behavior of Evaporative Fraction in
386 the Soil–Vegetation–Atmospheric Boundary Layer Continuum. *Journal of*
387 *Hydrometeorology* **12**, 1530-1546, doi:10.1175/2011jhm1261.1 (2011).
- 388 29 Gentine, P., Entekhabi, D., Chehbouni, A., Boulet, G. & Duchemin, B. Analysis of
389 evaporative fraction diurnal behaviour. *Agricultural and Forest Meteorology* **143**, 13-29,
390 doi:10.1016/j.agrformet.2006.11.002 (2007).
- 391 30 Byrne, M. P. & O’Gorman, P. A. Trends in continental temperature and humidity directly
392 linked to ocean warming. *Proceedings of the National Academy of Sciences* **115**, 4863-
393 4868, doi:10.1073/pnas.1722312115 (2018).
- 394 31 Bouchet, R. J. Evapotranspiration réelle et potentielle, signification climatique. *IAHS*
395 *Publ* **62**, 134-142 (1963).
- 396 32 Fisher, J. B., Tu, K. P. & Baldocchi, D. D. Global estimates of the land–atmosphere
397 water flux based on monthly AVHRR and ISLSCP-II data, validated at 16 FLUXNET
398 sites. *Remote Sensing of Environment* **112**, 901-919, doi:10.1016/j.rse.2007.06.025
399 (2008).
- 400 33 Knauer, J., El-Madany, T. S., Zaehle, S. & Migliavacca, M. Bigleaf—An R package for
401 the calculation of physical and physiological ecosystem properties from eddy covariance
402 data. *PLOS ONE* **13**, e0201114, doi:10.1371/journal.pone.0201114 (2018).
- 403 34 Thom, A. S. Momentum, mass and heat exchange of vegetation. *Quarterly Journal of the*
404 *Royal Meteorological Society* **98**, 124-134, doi:10.1002/qj.49709841510 (1972).
- 405 35 Wilson, K. *et al.* Energy balance closure at FLUXNET sites. *Agricultural and Forest*
406 *Meteorology* **113**, 223-243, doi:10.1016/S0168-1923(02)00109-0 (2002).

407 36 Morillas, L., Hund, S. V. & Johnson, M. S. Water Use Dynamics in Double Cropping of
408 Rainfed Upland Rice and Irrigated Melons Produced Under Drought-Prone Tropical
409 Conditions. *Water Resources Research* **0**, doi:10.1029/2018wr023757 (2019).
410 37 Baldocchi, D. *et al.* FLUXNET: A new tool to study the temporal and spatial variability
411 of ecosystem-scale carbon dioxide, water vapor, and energy flux densities. *Bulletin of the*
412 *American Meteorological Society* **82**, 2415-2434, doi:10.1175/1520-
413 0477(2001)082<2415:FANTTS>2.3.CO;2 (2001).
414 38 Marsh, A. *Psychrometric Chart*, <<https://drajmarsh.bitbucket.io/psychro-chart2d.html>>
415 (2018).
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Figures:



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Fig. 1. Schematic conceptualization of the PM_{rh} model and psychrometric relationship of PM_{rh}.

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The psychrometric chart is modified from Marsh³⁸. Path 1 represents Eq. (2) divided by $\frac{\rho c_p}{\gamma r_a}$

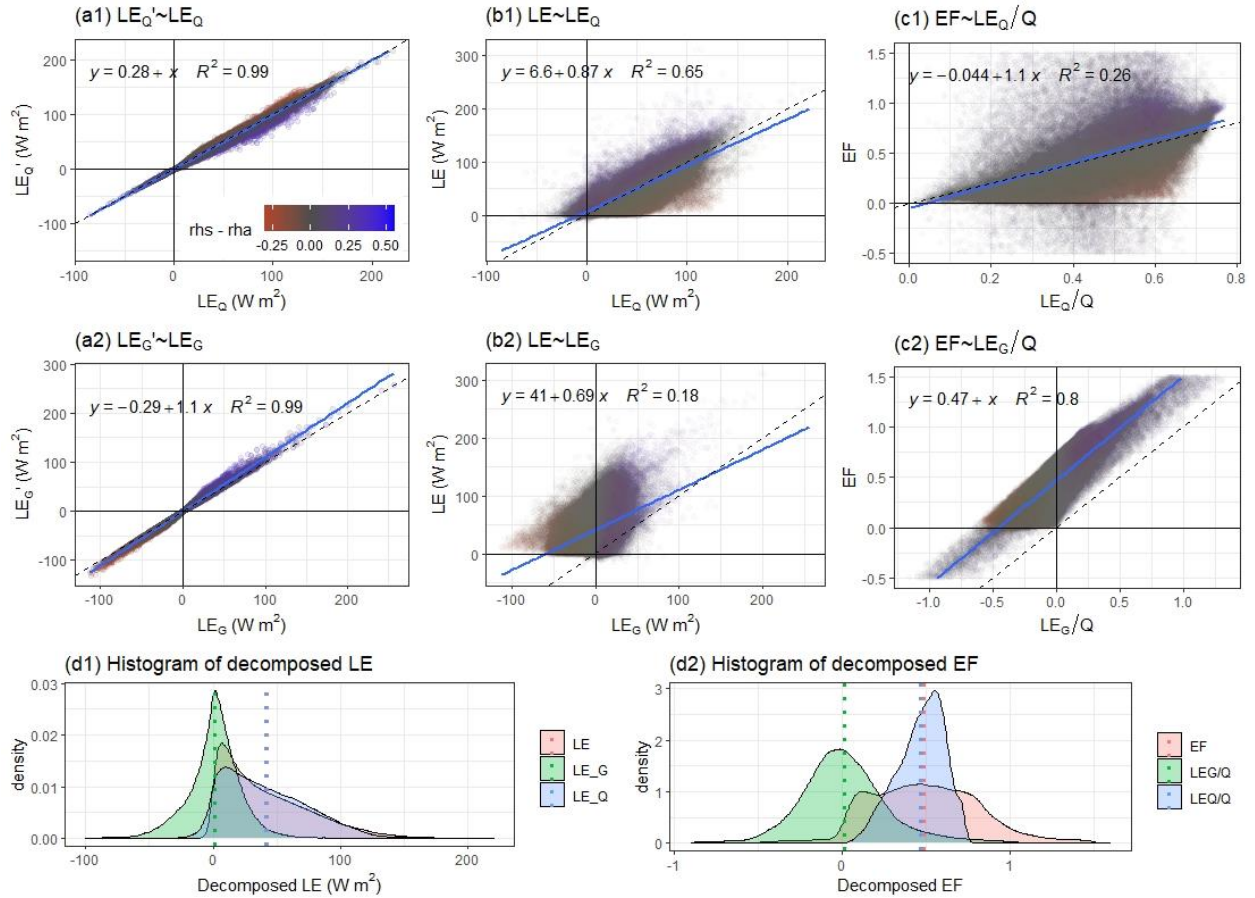
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while Path 2 represents Eq. (3) divided by $\frac{\rho c_p}{\gamma r_a}$. Here, the enthalpy change of the air parcel is

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defined as $\frac{Q \cdot r_a}{\rho}$ (kJ kg⁻¹).

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Fig. 2. FLUXNET2015²⁴ daily LE , LE_Q , and LE_G for 212 sites and 1532 site-years. Panels (a1)

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and (a2) are linear regressions of LE_Q' on LE_Q and LE_G' on LE_G . Panels (b1) and (b2) are linear

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regressions of LE on LE_Q and LE on LE_G . Panels (c1) and (c2) are linear regressions of EF on

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LE_Q/Q and EF on LE_G/Q . In these panels, daily EF data within a range from -1 to 1.5 are only

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shown. Here, dashed lines are one-to-one lines, blue lines are regression lines, and color

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represents $rhs - rha$. Panel (d1) and (d2) are histograms of decomposed LE and EF with mean

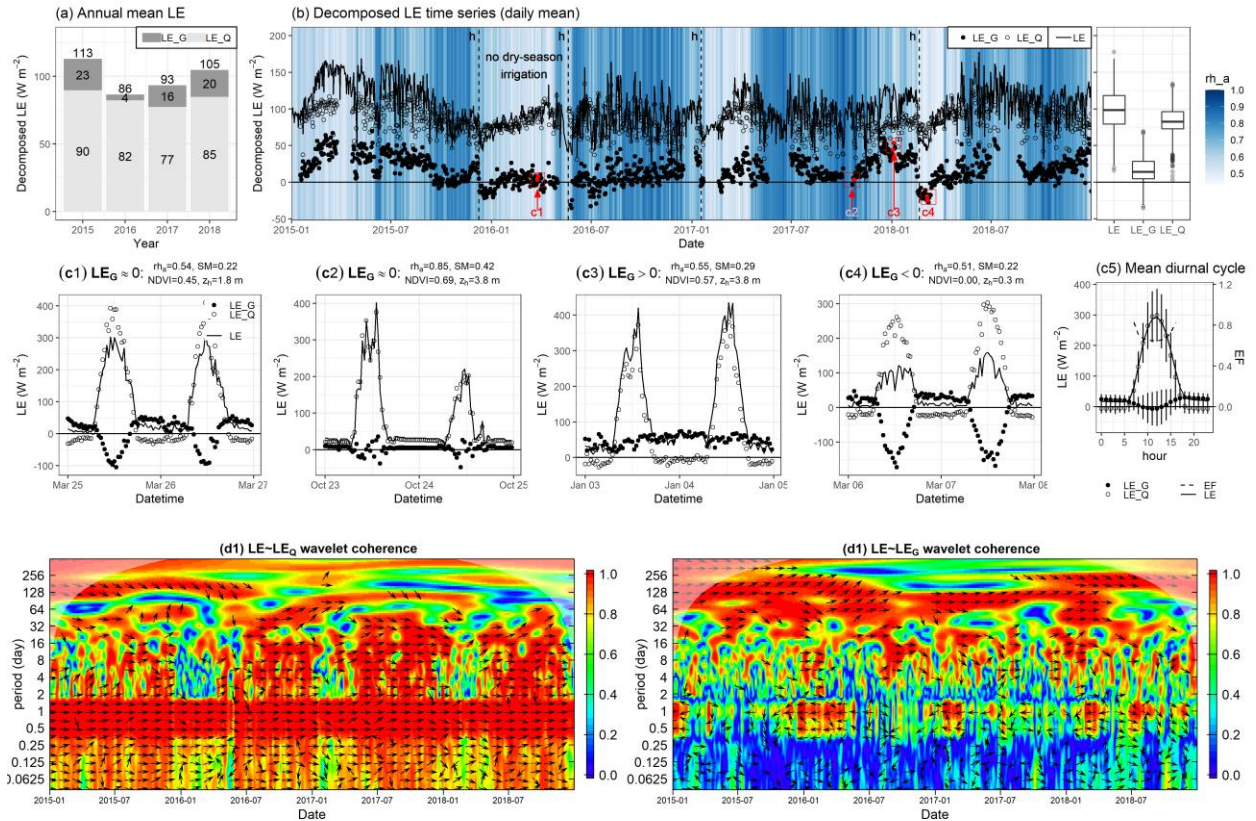
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values (dotted lines). To correct for lack of energy balance closure, in all calculations Q was set

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equal to $LE + H$.

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Fig. 3. Time series of LE , LE_Q , and LE_G for the sugarcane eddy-covariance tower site in Costa

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Rica. Panel (a) is mean annual LE and its components and (b) is a time series of daily mean

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values with a background color of rh_a . Dashed lines with “h” in panel (b) indicate sugarcane

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harvest. Panels (c1) ~ (c4) are half-hourly time series indicated in panel (b). Here, SM is

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volumetric soil water content, NDVI is normalized difference vegetation index, and z_h is canopy

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height. Panel (c5) presents the long-term mean diurnal cycle of decomposed LE and EF. Panels

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(d1) and (d2) are wavelet coherence of LE with LE_Q and LE with LE_G . Red and blue colors

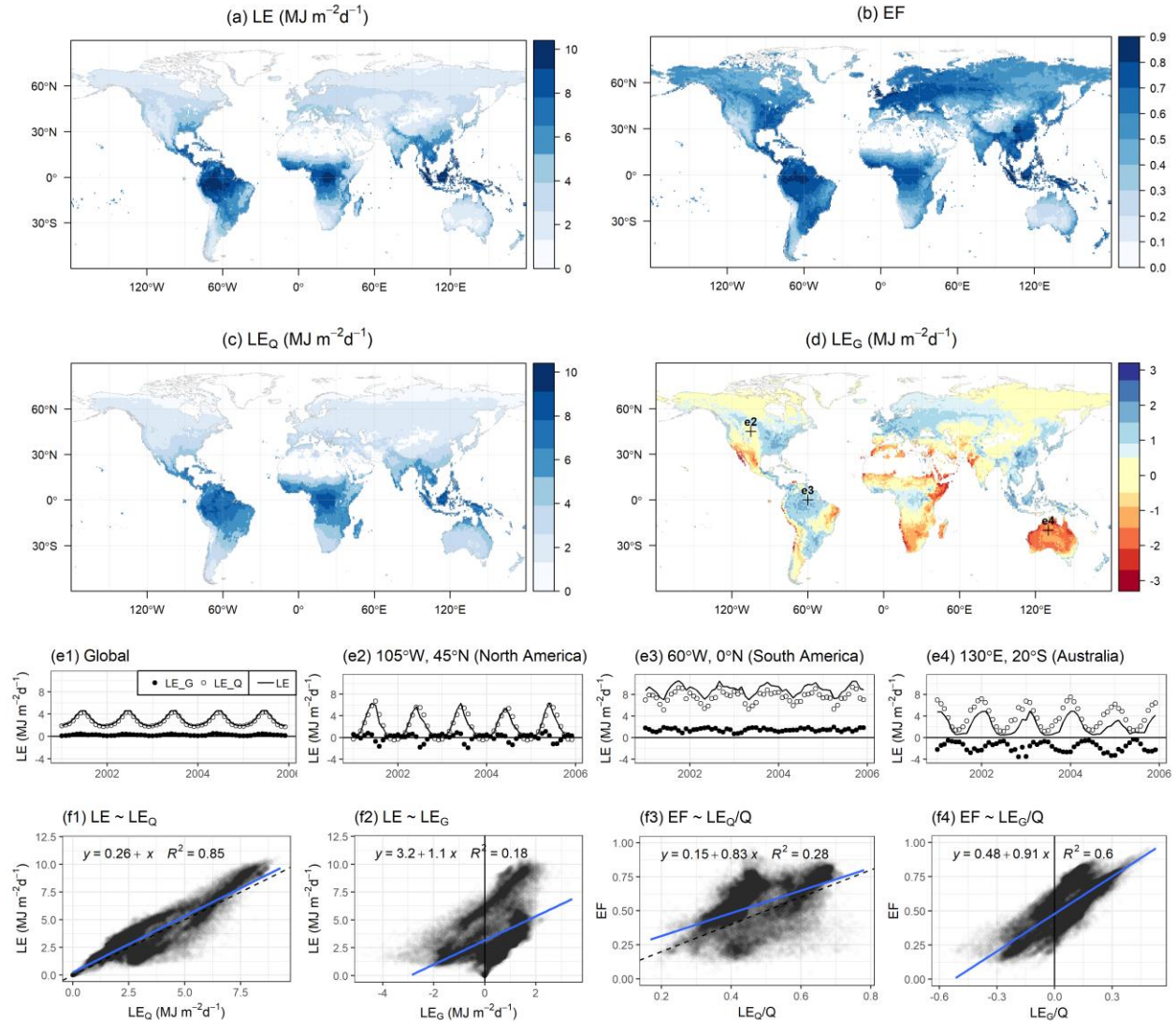
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indicate high and low correlation, respectively. Arrows (pointing right: in-phase; left: antiphase)

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only appear when the coherence is significant ($p < 0.01$).

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Fig. 4. Mean annual LE , EF , LE_Q , and LE_G from 2001 to 2005 (panels (a), (b), (c), and (d), respectively). Panel (e1) is a time series of monthly global average LE and the two components, LE and LE_Q . Panels (e2), (e3), and (e4) are time series at specific locations highlighted in panel (d). Panels (f1), (f2), (f3), and (f4) are spatial linear regressions of LE on LE_Q , LE on LE_G , EF on LE_Q/Q , and EF on LE_G/Q , respectively.

Supplemental Information for

Relative humidity gradients as a key constraint on terrestrial water and energy fluxes

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Appendix A: Two forms of PM_{rh}

Derivation of Equation (2)

LE and H can be written using aerodynamic resistance for water vapour (r_{av}) and sensible heat (r_{aH}) as follows

$$LE = \frac{\rho c_p r h_s e^*(T_s) - r h_a e^*(T_a)}{\gamma r_{av}} \quad (\text{A1})$$

$$H = \rho c_p \frac{T_s - T_a}{r_{aH}} \quad (\text{A2})$$

To express LE as a function of T_a and rh_s , adding $-rh_s e^*(T_a) + rh_s e^*(T_a)$ to the numerator of (A1) yields:

$$LE = \frac{\rho c_p r h_s e^*(T_s) - r h_s e^*(T_a) + r h_s e^*(T_a) - r h_a e^*(T_a)}{\gamma r_{av}} = \frac{\rho c_p r h_s}{\gamma} \frac{e^*(T_s) - e^*(T_a)}{r_{av}} + \frac{\rho c_p}{\gamma} e^*(T_a) \frac{r h_s - r h_a}{r_{av}} \quad (\text{A3})$$

Next, we use the linearized slope of e^* ($\frac{e^*(T_s) - e^*(T_a)}{T_s - T_a} \approx \frac{de^*}{dT} |_{T=T_a} = S$) to give

$$LE = \frac{\rho c_p}{\gamma} r h_s S \frac{T_s - T_a}{r_{av}} + \frac{\rho c_p}{\gamma} e^*(T_a) \frac{r h_s - r h_a}{r_{av}} \quad (\text{A4})$$

If we assume $r_{aH} \approx r_{av} \approx r_a$, Eq. (A4) becomes

$$LE = r h_s \frac{S}{\gamma} H + \frac{\rho c_p}{\gamma} e^*(T_a) \frac{r h_s - r h_a}{r_a} \quad (\text{A5})$$

Then, substituting the surface energy balance ($H = Q - LE$) into the first term of Eq. (A5):

$$LE = \underbrace{\frac{r h_s S}{r h_s S + \gamma} Q}_{\text{Diabatic}} + \underbrace{\frac{\rho c_p e^*(T_a)}{r h_s S + \gamma} \frac{r h_s - r h_a}{r_a}}_{\text{Adiabatic}} \quad (\text{A6})$$

Derivation of Equation (3)

LE and H can be written using aerodynamic resistance for water vapour (r_{av}) and sensible heat (r_{aH}) as follows

$$LE = \frac{\rho c_p r h_s e^*(T_s) - r h_a e^*(T_a)}{\gamma r_{av}} \quad (\text{A#7})$$

$$H = \rho c_p \frac{T_s - T_a}{r_{aH}} \quad (\text{A#8})$$

To express LE as a function of T_s and rh_a , adding $-rh_a e^*(T_s) + rh_a e^*(T_s)$ to the numerator of (A#1) yields:

$$LE = \frac{\rho c_p r h_s e^*(T_s) - r h_a e^*(T_s) + r h_a e^*(T_s) - r h_a e^*(T_a)}{\gamma r_{av}} = \frac{\rho c_p}{\gamma} e^*(T_s) \frac{r h_s - r h_a}{r_{av}} + \frac{\rho c_p}{\gamma} r h_a \frac{e^*(T_s) - e^*(T_a)}{r_{av}} \quad (\text{A#9})$$

Next, we use the linearized slope of e^* ($\frac{e^*(T_s) - e^*(T_a)}{T_s - T_a} \approx \frac{de^*}{dT} |_{T=T_a} = S$) to give

$$LE = \frac{\rho c_p}{\gamma} e^*(T_s) \frac{r h_s - r h_a}{r_{av}} + \frac{\rho c_p}{\gamma} r h_a S \frac{T_s - T_a}{r_{av}} \quad (\text{A#10})$$

If we assume $r_{aH} \approx r_{av} \approx r_a$, Eq. (A#4) becomes

$$LE = \frac{\rho c_p}{\gamma} e^*(T_s) \frac{r h_s - r h_a}{r_a} + r h_a \frac{S}{\gamma} H \quad (\text{A#11})$$

Then, substituting the surface energy balance ($H = Q - LE$) into the second term of Eq. (A#5):

$$LE = \underbrace{\frac{\rho c_p e^*(T_s)}{r h_a S + \gamma} \frac{r h_s - r h_a}{r_a}}_{\text{Adiabatic}} + \underbrace{\frac{r h_a S}{r h_a S + \gamma} Q}_{\text{Diabatic}} \quad (\text{A#12})$$

Appendix B: Detailed data processing

FLUXNET2015. We only included daily FLUXNET2015 data ¹ for periods for which the quality control (QC) flag indicated more than 80 % half-hourly data were present (i.e., measured data in general, or good quality gap-filled data in cases of partially missing data). Detailed description on QC flag can be found in Pastorello, et al. ¹.

The sum of LE and H measured by eddy-covariance system is typically lower than the difference between net radiation (R_n) and the soil heat flux (G), resulting in a known condition referred to as the surface energy imbalance (e.g., energy balance closure problem) ^{2,3}. In order to apply the PM_{th} model, energy balance closure should be assumed. To generate [Figure 2](#), we attributed the energy imbalance to unmeasured heat storage term, which means that Q was defined as $LE+H$. We also investigated the impact of “forcing” energy balance closure by setting $LE + H$ equal to $R_n - G$ and weighting LE and H based on the assumption that the Bowen ratio ($B = H/LE$) is correct ¹. This resulted in [Figure S1](#), which shows almost identical results as those presented in [Figure 2](#).

In-situ dataset. The sugar cane eddy-covariance tower site has a wet-dry tropical climate, with median monthly air temperature ranging from 27 °C to 30 °C at the nearest climate station in Santa Cruz, 25 km away from our study site, from 1996 to 2018. The dry season lasts from December to March (7 mm/month on average at the climate station in Santa Cruz) and the wet season from April to November (203 mm/month at the climate station in Santa Cruz). The Province of Guanacaste experienced drought in 2015 ⁴, the first year of eddy-covariance observational data (1127 mm/year in 2015 at the study plot vs. 1652 mm/year long-term average at the climate station).

A ratooning practice is applied in growing sugarcane, a perennial plant. Ratooning means cutting most of the above-ground portion when harvesting the crop, but leaving the roots intact to allow the sugarcane to regrow from the established roots. This ratooning is conducted once a year at the study site. About 5 years after initial planting, regrowth becomes less vigorous and new sugarcane plants are planted. In the middle of 2016, a new planting was started in the flux tower footprint area. The growing season length at the site is about a year, but it varies with regrowth times after the initial planting. Therefore, harvest timing varied from December to May during the study period (Fig. 3 (b)). Crop canopy height varied from 0.01 m to 3.8 m above ground during each harvest cycle. Sugarcane was watered in the dry season via furrow irrigation events, with the exception of 2016 when there was no irrigation due to the replanting.

An eddy-covariance (EC) flux tower was installed 6 m above ground inside a sugarcane plot. The study plot is located in a homogenous landscape where about 200 km² around study site is devoted to sugarcane agriculture. The EC system included an open-path infrared gas analyzer (LI-7500A, LI-COR Biosciences, Lincoln, NE, USA) and a sonic anemometer (model 81000, R.M. Young, Traverse City, MI, USA). A soil heat flux plate (HFP01SC-L, Campbell Scientific, Logan, UT, USA) was installed 8 cm below ground, and two net radiometers (2015-2016: NR-LITE, Campbell Scientific, Logan, UT, USA; 2017-2018: SN-500, Apogee Instruments, Logan, UT, USA) were sequentially installed at 5.7 m height. For complementary meteorological measurements, two Vaisala WXT520 weather transmitters (Vaisala Inc. Helsinki, Finland) were installed at 3.6 m and 1.6 m heights. The 1.6 m height Vaisala transmitter was installed within the canopy next to the tower while the 3.6 m height Vaisala weather transmitter located about 25 m from the EC tower but sharing the same patch with the EC system. The volumetric soil water content and soil temperature were measured at several depths at the site

(GS3, Decagon Devices, Pullman, WA, USA); here we report only values at the 8 cm depth.

Normalized difference vegetation index (NDVI) was also measured by proximal tower-mounted sensors (SRS, Decagon Devices) beginning in 2017. NDVI values presented for context in Fig. 3 (c2), (c3), and (c4) were measured at the tower, while the NDVI value in Fig. 3 (c1) was

5 retrieved from Landsat7 as that time interval preceded installation of the proximal NDVI sensor.

High frequency raw EC data were processed, and block averaged with EddyPro software (versions 6.0.0 to 6.2.1, LI-COR Biosciences, Lincoln, NE, USA). The processes includes double rotation coordinate correction ⁵, frequency response correction ⁶, and density correction ⁷. Block averaged fluxes at 30-min intervals went through a quality control procedure from which

10 fluxes were removed when any of the following conditions occurred, following Morillas, et al. ⁴: periods of heavy rain, low signal strength (signal strength < 60%), measurements flagged as low quality by the EddyPro software, or during conditions with low friction velocity (u_*) based on moving point method ^{8,9}. Subsequently, the resulting gaps in 30-min turbulent fluxes were gap-filled using the marginal distribution sampling method ^{9,10}.

15 Vapour pressure (e_a) measured by the open-path infrared gas analyzer (IRGA) was used to calculate rh_a . To ensure data quality of e_a , data were also filtered out when any of the following conditions occurred: periods of heavy rain, low signal strength (signal strength <60%), measurements flagged as low quality by the EddyPro software, and unrealistic values recorded by the IRGA compared to Vaisala measurements (more than 20% difference when calculating

20 relative humidity). The resulting IRGA gaps in the e_a time series were replaced by the corresponding measurements made using the Vaisala sensor at the 3.6 m height.

For the study period, the surface energy balance closure of 30 min data was 86 %, which is typical of high-quality eddy-covariance data sets ². When canopy height was less than 1 m, the

surface energy balance was almost closed (97%), whereas the closure was 83 % when canopy height was higher than 1 m. Considering a possible significant role of unmeasured canopy and soil heat storages ^{11,12} and the homogenous landscape of the study site ^{3,13}, we did not force the energy closure. Therefore, for PM_{rh} application, we defined Q as a sum of LE and H instead of the difference between net radiation and soil heat flux by attributing the cause of the surface energy imbalance to unmeasured heat storage terms following Moon, et al. ¹⁴.

In order to explore the time scale of the covariances for $LE \sim LE_Q$ and $LE \sim LE_G$ in the frequency domain, we applied wavelet coherence analysis using WaveletComp R package ¹⁵.

The package is designed to apply the continuous wavelet transform using Morlet wavelet, which is a popular approach to analyze hydrological and micrometeorological datasets ^{16,17}. A total time series of half-hourly decomposed LE for the 4-year measurement period was used to estimate localized coherence and phase angle. The wavelet coherence can be interpreted as the local correlation between two variables in the frequency-time domain (see Fig. 3, where red indicates high correlation). 0° phase angle (arrow pointing right) indicates periods of positive correlation while 180° phase angle (arrow pointing left) indicates periods of negative correlation.

References:

- 1 Pastorello, G. *et al.* The FLUXNET2015 dataset and the ONEFlux processing pipeline
for eddy covariance data. *Scientific Data* **7**, 225, doi:10.1038/s41597-020-0534-3 (2020).
- 2 Wilson, K. *et al.* Energy balance closure at FLUXNET sites. *Agricultural and Forest
5 Meteorology* **113**, 223-243, doi:10.1016/S0168-1923(02)00109-0 (2002).
- 3 Stoy, P. C. *et al.* A data-driven analysis of energy balance closure across FLUXNET
research sites: The role of landscape scale heterogeneity. *Agricultural and Forest
Meteorology* **171-172**, 137-152, doi:10.1016/j.agrformet.2012.11.004 (2013).
- 4 Morillas, L., Hund, S. V. & Johnson, M. S. Water Use Dynamics in Double Cropping of
10 Rainfed Upland Rice and Irrigated Melons Produced Under Drought-Prone Tropical
Conditions. *Water Resources Research* **0**, doi:10.1029/2018wr023757 (2019).
- 5 Wilczak, J. M., Oncley, S. P. & Stage, S. A. Sonic Anemometer Tilt Correction
Algorithms. *Boundary-Layer Meteorology* **99**, 127-150, doi:10.1023/A:1018966204465
(2001).
- 15 6 Moncrieff, J. B. *et al.* A system to measure surface fluxes of momentum, sensible heat,
water vapour and carbon dioxide. *Journal of Hydrology* **188-189**, 589-611,
doi:10.1016/S0022-1694(96)03194-0 (1997).
- 7 Webb, E., Pearman, G. & Leuning, R. Correction of flux measurements for density
effects due to heat and water vapour transfer. *Quarterly Journal of the Royal
20 Meteorological Society* **106**, 85-100 (1980).
- 8 Papale, D. *et al.* Towards a standardized processing of Net Ecosystem Exchange
measured with eddy covariance technique: algorithms and uncertainty estimation.
Biogeosciences **3**, 571-583, doi:10.5194/bg-3-571-2006 (2006).
- 9 Wutzler, T. *et al.* Basic and extensible post-processing of eddy covariance flux data with
25 REddyProc. *Biogeosciences Discussions*, doi:10.5194/bg-15-5015-2018 (2018).
- 10 Reichstein, M. *et al.* On the separation of net ecosystem exchange into assimilation and
ecosystem respiration: review and improved algorithm. *Global Change Biology* **11**, 1424-
1439, doi:10.1111/j.1365-2486.2005.001002.x (2005).
- 11 Leuning, R., van Gorsel, E., Massman, W. J. & Isaac, P. R. Reflections on the surface
30 energy imbalance problem. *Agricultural and Forest Meteorology* **156**, 65-74,
doi:10.1016/j.agrformet.2011.12.002 (2012).
- 12 Eshonkulov, R., Poyda, A., Ingwersen, J., Pulatov, A. & Streck, T. Improving the energy
balance closure over a winter wheat field by accounting for minor storage terms.
Agricultural and Forest Meteorology **264**, 283-296, doi:10.1016/j.agrformet.2018.10.012
35 (2019).
- 13 Foken, T. The energy balance closure problem: an overview. *Ecological Applications* **18**,
1351-1367, doi:10.1890/06-0922.1 (2008).
- 14 Moon, M., Li, D., Liao, W., Rigden, A. J. & Friedl, M. A. Modification of surface energy
balance during springtime: The relative importance of biophysical and meteorological
40 changes. *Agricultural and Forest Meteorology* **284**, 107905,
doi:10.1016/j.agrformet.2020.107905 (2020).
- 15 Roesch, A. & Schmidbauer, H. WaveletComp: Computational Wavelet Analysis. (2014).
- 16 Hatala, J. A., Detto, M. & Baldocchi, D. D. Gross ecosystem photosynthesis causes a
diurnal pattern in methane emission from rice. *Geophysical Research Letters* **39**, 1-5,
45 doi:10.1029/2012GL051303 (2012).

- 17 Johnson, M. S. *et al.* Soil CO₂ Dynamics in a Tree Island Soil of the Pantanal: The Role of Soil Water Potential. *PLOS ONE* **8**, e64874, doi:10.1371/journal.pone.0064874 (2013).

Supplement Figures:

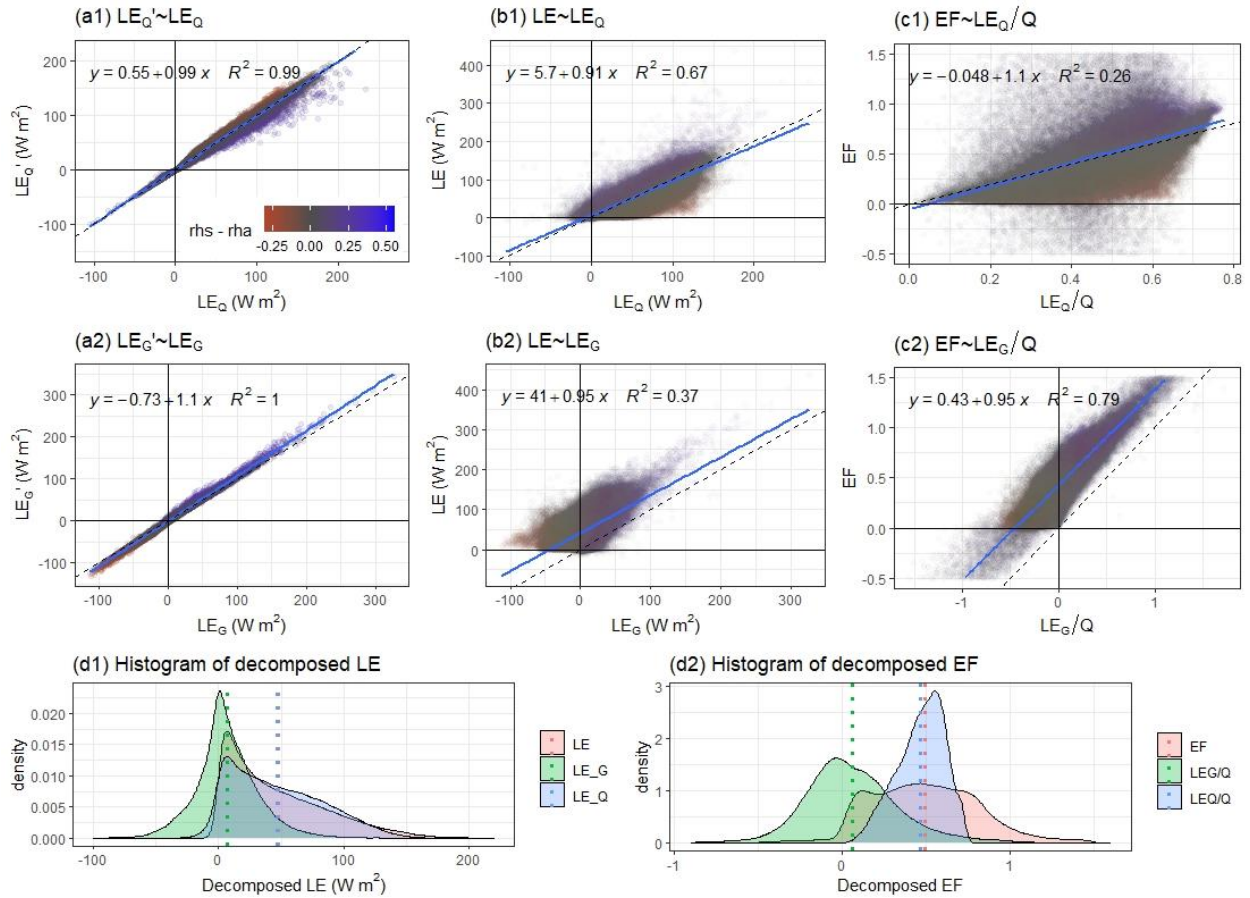


Figure S1. FLUXNET2015¹ daily LE , LE_Q , and LE_G (energy balance corrected). Panels (a1) and (a2) are linear regressions of LE_Q' on LE_Q and LE_G' on LE_G . Panels (b1) and (b2) are linear regressions of LE on LE_Q and LE on LE_G . Panels (c1) and (c2) are linear regressions of EF on LE_Q/Q and LE on LE_G/Q . Here, dashed lines are one-to-one lines, blue lines are regression lines, and color represent $rh_s - rh_a$. Panel (d1) and (d2) are histograms of decomposed LE and EF with mean values (dotted line).