* Preprint uploaded to EarthArxiv. This article is in press with G3. Please cite the published version*

Reconstructing Magma Storage Depths for the 2018 Kilauean Eruption from Melt inclusion CO₂ Contents: The Importance of Vapor Bubbles

P. E. Wieser¹, H. Lamadrid², J. Maclellan¹, M. Edmonds¹, S. Matthews³, K. Iacovino⁴, F.E. Jenner⁵, C. Gansecki⁶, F. Trusdell⁷, R.L. Lee⁷ and E. Ilyinskaya⁸

¹Department of Earth Sciences, University of Cambridge, UK.
²Geological Sciences, University of Missouri, 65211, US.
³Johns Hopkins University, Department of Earth and Planetary Sciences, Baltimore, MD 21218, USA.
⁴Jacobs, NASA Johnson Space Center, Houston, TX 77058, USA.
⁵School of Environment, Earth and Ecosystem Sciences, The Open University, MK7 6AA, UK
⁶Department of Geology, University of Hawaii at Hilo, Hilo, HI 96720, USA
⁷USGS Hawaiian Volcano Observatory, Hilo, HI 96720, USA
⁸School of Earth and Environment, University of Leeds, UK

Key Points:

- Petrological, gaseous and geophysical observations can be reconciled by a model where Fissure 8 was supplied from two storage reservoirs (∼1–2 and 3–5 km depth)
- Extensive post-entrapment crystallization of melt inclusions within High-Fo olivines (Fo>81.5) caused ∼90% of the CO₂ to enter the vapor bubble.
- Raman analyses of vapor bubbles combined with choice of a suitable H₂O-CO₂ solubility model is required to accurately determine magma storage depths.

Corresponding author: P. Wieser, penny.wieser@gmail.com
Abstract

The 2018 lower East Rift Zone (LERZ) eruption and the accompanying col-
lapse of the summit caldera marked the most destructive episode of activity at
Kilauea Volcano in the last 200 years. The eruption was extremely well-monitored,
with extensive real-time lava sampling as well as continuous geodetic data capturing
the caldera collapse. This multi-parameter dataset provides an exceptional oppor-
tunity to determine the reservoir geometry and magma transport paths supplying
Kilauea’s LERZ. The forsterite contents of olivine crystals, together with the de-
gree of major element disequilibrium with carrier melts, indicates that two distinct
crystal populations were erupted from Fissure 8 (termed High- and Low-Fo). Melt
inclusion entrapment pressures reveal that Low-Fo olivines (close to equilibrium with
their carrier melts) crystallized within the Halema’uma’u reservoir (∼2 km depth),
while many High-Fo olivines (>Fo81.5; far from equilibrium with their carrier melts)
crystallized within the South Caldera reservoir (∼3–5 km depth). Melt inclusions
in High-Fo olivines experienced extensive post-entrapment crystallization following
their incorporation into cooler, more evolved melts. This favoured the growth of a
CO₂-rich vapor bubble, containing up to 99% of the total melt inclusion CO₂ budget
(median=93%). If this CO₂-rich bubble is not accounted for, entrapment depths
are significantly underestimated. Conversely, reconstructions using equation of state
methods rather than direct measurements of vapor bubbles overestimate entrap-
ment depths. Overall, we show that direct measurements of melts and vapor bubbles
by SIMS and Raman Spectroscopy, combined with a suitable H₂O-CO₂ solubility
model, is a powerful tool to identify the magma storage reservoirs supplying volcanic
eruptions.

Plain Language Summary

Pockets of frozen magma trapped within olivine crystals, termed “melt inclusions”,
can provide information about the depths at which magma is stored beneath
the surface prior to a volcanic eruption. This is because the amount of CO₂ and
H₂O that can be dissolved in a melt is dependent on the pressure, and therefore
the depth. We examine melt inclusions from lava flows produced during the 2018
eruption of Kilauea Volcano. Previous geophysical work has shown that magma is
stored in two main reservoirs at Kilauea, located at ∼1–2 km and ∼3–5 km depth.
However, because many melt inclusions host almost all of their CO$_2$ within a vapor bubble, which is rarely measured, previous petrological estimates of magma storage depths at Kilauea do not align with the depths of these reservoirs identified by geophysics. In this study, we measure the amount of CO$_2$ in the glass and the bubble using Secondary Ion Mass Spectrometry (SIMS) and Raman Spectroscopy respectively. By adding these two measurements together, we can reconstruct the amount of CO$_2$ that was present when melt inclusions were trapped. Calculated depths align remarkably well with geophysical estimates, and demonstrate that the 2018 eruption was supplied by both magma storage reservoirs.

1 Introduction

The 2018 lower East Rift Zone (LERZ) eruption was the largest and most destructive in the last 200 years of activity at Kilauea Volcano, Hawai‘i (Neal et al., 2019), accompanied by the highest co-eruptive fluxes of SO$_2$ ever measured at Kilauea (up to 200 kt a day; Kern et al., 2020; Whitty et al., 2020), and very high lava effusion rates (100-300 m$^3$/s; Neal et al., 2019; Patrick, Orr, et al., 2019). Before the onset of this new eruptive episode in May 2018, Kilauea had been erupting near-continuously for 35 years on the middle East Rift Zone (ERZ) at Pu‘u ‘Ō‘ō cone and surrounding vents, located approximately ~20 km east of Kilauea’s summit (1983–2018), and ~24 km uprift of the 2018 eruption site (Fig. 1b). From 2008 to 2018, a persistently active lava lake was also present within Halema‘uma‘u (HMM) pit crater, located in the south west area of Kilauea’s summit caldera (Fig. 1b).
The 2018 eruption was preceded by swarms of lower-crustal earthquakes at ~6–12 km depth beneath Kīlauea’s summit area on March 7th, April 11th, and April 18th, 2018 (Flinders et al., 2020). This inflation has been variably interpreted to result from a short-term increase in magma supply (Flinders et al., 2020), or a decrease in the output of magma along the ERZ to Pu‘u ʻO‘o, leading to magma backing up within the summit reservoir (Patrick et al., 2020). On March 13th, 2018, inflation was recorded by tiltmeters located at Kīlauea’s summit. Inflationary
ground deformation also began at Pu‘u ‘Ō‘ō, suggesting that excess magma was accumulating beneath this vent (Neal et al., 2019). The pressurization at these two locations continued throughout March and April, demonstrated by the rise of the lava pond at Pu‘u ‘Ō‘ō, and overflows of the summit lava lake in mid-late April. On April 30th, the crater floor at Pu‘u ‘Ō‘ō collapsed, followed by an eastward migration of seismicity along the rift zone, consistent with the propagation of a dyke (Neal et al., 2019). A hazard notice released early in the morning of May 1st warned the residents of Lower Puna to be alert, as a large area along the ERZ east of Pu‘u ‘Ō‘ō was at risk from a new outbreak of lava. Following the appearance of ground cracks in the Leilani Estates subdivision (Fig. 1c) on May 2nd, lava reached the surface just before 5 pm on May 3rd (Neal et al., 2019). Over the next few days, multiple fissures opened, preceded by gas emissions and ground cracking. In all, 24 fissures opened between the 3rd and 27th of May 2018.

Activity between the 3rd and 9th of May, classified as Early Phase 1 by Gansecki et al. (2019), was characterized by the eruption of spatter mounds and sluggish, slow-moving lava flows. This relatively evolved magma (mean SiO$_2$=51 wt% and MgO=4 wt%; Lee et al., 2019; Gansecki et al., 2019) is thought to have formed by differentiation within LERZ storage reservoirs over decades to centuries (Neal et al., 2019). Throughout May, the compositions of erupted melts and crystals became increasingly primitive as summit-derived magma flushed out the LERZ storage reservoirs, with the exception of the involvement of an andesitic composition erupted in mid to late May (Gansecki et al., 2019). The eruption of hotter, less viscous lava led to the generation of fast-moving lava flows on May 18th, which reached the coast five days later (Neal et al., 2019, Fig. 1c). By May 28th, activity had localized at Fissure 8 (F8), with the effusion of fast-flowing magma as a channelized flow (Patrick, Dietterich, et al., 2019). Activity ended abruptly on August 4th, by which time F8 had erupted $\sim$1.5 km$^3$ of lava (Kauahikaua & Trusdell, 2020).

Despite the abundant geophysical and geochemical observations made during the LERZ eruption, the source of the magma erupted at F8 from late May-August 2018 has not yet been established. It is generally accepted that two main reservoirs are located beneath Kilauea’s summit. The shallower Halema‘uma‘u (HMM) reservoir is recognised as an inflation source located beneath the eastern rim of the HMM crater, and is thought to be centred at $\sim$0.5–2 km depth (Anderson et al., 2019;
Cervelli & Miklius, 2003; Baker & Amelung, 2012; Fiske & Kinoshita, 1969), while the deeper South Caldera (SC) reservoir manifests as an inflation source located beneath the southern portion of the caldera, at ∼3–5 km depth (Baker & Amelung, 2012; Poland et al., 2015). The 2018 LERZ eruption was accompanied by large-scale subsidence of the caldera floor centred around the HMM crater (500 m in certain locations; Neal et al., 2019), which has been attributed to magma withdrawal from the underlying HMM reservoir to feed the effusion of lava from F8 (Anderson et al., 2019). However, recent estimates of the total SO\textsubscript{2} emissions requires the erupted volume to be approximately twice the modelled volume loss from the HMM reservoir, suggesting that a second magma source was involved (Kern et al., 2020).

Additionally, the erupted crystal cargo from F8 contained some of the most forsteritic olivines (Fo\textsubscript{88–89}) erupted at Kīlauea since 1974, which must have grown in melts with 13–14 wt% MgO (Gansecki et al., 2019). Some of these crystals also contain prominent kink bands (Gansecki et al., 2019), indicating that their crystal lattices have been deformed (Wieser, Edmonds, et al., 2020). Previous work has suggested that highly forsteritic, deformed olivines are derived from the deeper, SC reservoir at 3–5 km depth (Helz et al., 2014, 2015; Wieser et al., 2019; Wieser, Edmonds, et al., 2020), or Kīlauea’s deep rift zones at 6–9 km depth (Clague & Deningler, 1994; Vinet & Higgins, 2010). Alternatively, Lynn et al. (2017) suggest that highly forsteritic olivines from the Keanaakākō'i Tephra may originate from deeper crustal storage reservoirs, perhaps located near the base of the volcanic pile at ∼8-10 km depth.

Our study utilizes the strong pressure dependence of the solubility of CO\textsubscript{2} (and H\textsubscript{2}O) in silicate melts to determine the pressures at which pockets of melt, termed melt inclusions, were trapped within olivine crystals. Through prior constraints on the density profile of the crust, entrapment pressures from F8 melt inclusions erupted in late May, mid-July and early August 2018 can be converted into entrapment depths. In turn, these depths can be compared to geophysical estimates of the depths of the main magma storage regions at Kīlauea to determine the source(s) of magma erupted at F8.
2 Melt Inclusion Entrapment Pressures

2.1 The Importance of Vapor Bubbles

The solubility of pure CO$_2$ and H$_2$O in silicate melts is dependent on the pressure, the major element content of the melt, and the melt temperature. Assuming that a melt was saturated in a CO$_2$-H$_2$O fluid phase at the time of melt inclusion formation, the pressure at which a melt inclusion was trapped can be calculated by reconstructing its initial volatile and major element composition. In relatively water-poor systems like Kilauea, where melts contain <1 wt% H$_2$O (Dixon et al., 1991; Clague et al., 1995; Sides, Edmonds, Maclellan, Swanson, & Houghton, 2014; Sides, Edmonds, Maclellan, Houghton, et al., 2014; Tucker et al., 2019; Wallace & Anderson, 1998), the entrapment pressure is most sensitive to the CO$_2$ content of the melt, and its major element composition. Variations in melt H$_2$O content between 0–1 wt% have a relatively small effect on the entrapment pressure (except at very low CO$_2$ contents; see Supporting Information Fig. S1; Newman & Lowenstern, 2002).

However, estimating the CO$_2$ content of a melt inclusion at the point of entrapment is not straightforward. The host crystal may experience a period of cooling after the melt inclusion was trapped, leading to the growth of olivine on the walls of the inclusion (termed post-entrapment crystallization, or PEC; Roedder, 1984; Danyushevsky et al., 2000; Anderson & Brown, 1993). The precipitation of denser olivine from the silicate melt, combined with the differential thermal contraction of the melt phase and the host olivine, causes the internal pressure of the melt inclusion to drop, driving the growth of a vapor bubble (Roedder, 1979; Anderson, 1974; Anderson & Brown, 1993). Combined with a reduction in the solubility of CO$_2$ associated with major element changes during PEC, these processes cause CO$_2$ to migrate from the melt phase into the bubble (Steele-Macinnis et al., 2011; Sides, Edmonds, Maclellan, Houghton, et al., 2014; Maclellan, 2017; Aster et al., 2016). An additional phase of bubble growth is caused by the differential thermal contraction of the melt inclusion and the host olivine during syn-eruptive cooling from high magmatic temperatures (∼1150°C at F8; Helz & Thornber, 1987; Gansecki et al., 2019) to the glass transition temperature (∼725°C; Ryan & Sammis, 1981).
Unfortunately, the vast majority of published volatile contents in melt inclusions globally, and at Kīlauea, only measured CO$_2$ in the glass phase, using techniques such as secondary-ion mass spectrometry (SIMS), or Fourier transform infrared spectroscopy (FTIR; Bennett et al., 2019; Ruth et al., 2018; Sides, Edmonds, Macleman, Houghton, et al., 2014; Sides, Edmonds, Macleman, Swanson, & Houghton, 2014). Given that recent work has shown that $\sim$40–90% of the total CO$_2$ budget of melt inclusions may be held within the vapor bubble (Hartley et al., 2014; Wallace et al., 2015; Moore et al., 2015; Rasmussen et al., 2020), entrapment pressures from studies neglecting vapor bubble carbon must be viewed as minimum estimates (Anderson & Brown, 1993; Ruth et al., 2018).

### 2.2 Reconstructing Vapor Bubble CO$_2$

Several approaches have been used to explore the contribution of vapor bubbles to the CO$_2$ budget of Hawaiian melt inclusions. Anderson and Brown (1993) theoretically reconstruct vapor bubble CO$_2$ by assuming that the melt and vapor bubble were in chemical equilibrium at high magmatic temperatures prior to syn-eruptive quenching. Specifically, they calculated melt inclusion internal pressures from glass CO$_2$ contents, and used these pressures to determine the molar volume of CO$_2$ in vapor bubbles using the CO$_2$ equation of state (EOS). They converted their molar volumes into CO$_2$ concentrations assuming that bubbles occupied 0.5 vol% of the melt inclusion prior to quenching, and added these values to measurements of glass CO$_2$ concentrations. Riker (2005) used a similar method to reconstruct bubble carbon for melt inclusions from the 1859 eruption of Mauna Loa. However, instead of using a fixed bubble volume, they account for the differential amounts of cooling and PEC experienced by erupted crystals, and calculate the bubble volumes prior to quench-induced expansion as a function of the drop in temperature ($\Delta T$) between the melt inclusion at the point of entrapment and eruption ($\text{VB} \text{ vol}\% = 0.0162 \Delta T - 0.0016$). More recently, Tucker et al. (2019) theoretically reconstructed bubble carbon contents for a large suite of melt inclusions from several Hawaiian volcanoes, including 167 from Kīlauea. However, instead of estimating the size of the vapor bubble prior to syn-eruptive quenching as in Anderson and Brown (1993) and Riker (2005), they used observed bubble volumes to convert CO$_2$ densities obtained from the EOS into bubble CO$_2$ concentrations. This approach is problematic because ex-
pansion of the bubble during syn-eruptive cooling and quenching continues until the glass transition temperature, while CO$_2$ diffusion through the melt into the bubble may effectively cease at a higher temperature. Thus, the final stages of bubble expansion will occur without concurrent CO$_2$ diffusion from the glass into the bubble, meaning that the EOS method will overpredict the amount of CO$_2$ in the bubble (Anderson & Brown, 1993; Maclennan, 2017; Rasmussen et al., 2020).

The total amount of CO$_2$ within melt inclusions can also be determined using experimental homogenization techniques, where crystals containing melt inclusions are heated to magmatic temperatures. This drives the dissolution of the olivine rim precipitated during PEC, which changes the chemistry and volume of the melt inclusion so that CO$_2$ held within the vapor bubble dissolves back into the melt. Following rapid quenching, the glass phase of these rehomogenized melt inclusions can be analyzed by SIMS or FTIR (Esposito et al., 2012; Rasmussen et al., 2020; Skirius et al., 1990; Tuohy et al., 2016; Wallace et al., 2015). However, experimental homogenization can lead to H$_2$O loss, excess dissolution of olivine on the walls of the melt inclusion, and loss of mineral and melt inclusion zoning, which degrades the overall utility of the melt inclusion record (Rasmussen et al., 2020; Tuohy et al., 2016). Additionally, it is not always possible to fully dissolve the original bubbles, and new bubbles containing CO$_2$ may nucleate upon quench (Wallace et al., 2015; Tuohy et al., 2016; Skirius et al., 1990; Rasmussen et al., 2020).

Most recently, the density of CO$_2$ in vapor bubbles has been measured directly using Raman Spectroscopy (Esposito et al., 2011; Steele-Macinnis et al., 2011; Hartley et al., 2014; Moore et al., 2015, 2018; Aster et al., 2016; Taracsák et al., 2019). The Raman spectrum of CO$_2$ consists of two peaks nominally at 1285 cm$^{-1}$ and 1388 cm$^{-1}$ at 1 bar (see Supporting Information Fig. S2), resulting from the interaction of a symmetrical stretching mode and an active bending mode in the CO$_2$ molecule by a process known as Fermi resonance (Rosso & Bodnar, 1995; Lamadrid et al., 2017; Fermi, 1931). Hence, collectively, these peaks are referred to as the Fermi diad (FD), and the distance between the peak centres is the Fermi diad splitting ($\Delta$). However, while it is well accepted that $\Delta$ correlates with CO$_2$ density ($\rho_{CO_2}$), there are a number of different parameterizations for this relationship in the literature (Wang et al., 2019; Rosso & Bodnar, 1995; Lamadrid et al., 2017; Kawakami et al., 2003, and refs. within). The diversity of published densimeters
reflects different instrument hardware, as well as the choice of analytical conditions (Lamadrid et al., 2017). Thus, the approach used by a number of studies where a densimeter is chosen from the literature to convert measurements of $\Delta$ to $\rho_{CO_2}$ on a different Raman instrument from the one used to calibrate the densimeter results in large systematic uncertainties in the absolute density of CO$_2$ (e.g., Venugopal et al., 2020; Taracsák et al., 2019; Hartley et al., 2014). For example, $\Delta$=102.8 cm$^{-1}$ yields $\rho_{CO_2}$=0.0281 g/cm$^3$ using the densimeter of Wang et al. (2019), but $\rho_{CO_2}$=0.1397 g/cm$^3$ using the densimeter of Kawakami et al. (2003). For a bubble volume of 5% (the 80th percentile of bubble volume proportions at Kilauea from Tucker et al., 2019) and a melt density of 2.75 g/cm$^3$, these different densimeters predict a contribution of 538 ppm vs. $\sim$2674 ppm CO$_2$ to the reconstructed total CO$_2$ budget of the melt inclusion. For a melt inclusion with SiO$_2$=49 wt%, and H$_2$O=0.5 wt%, these CO$_2$ contents correspond to entrapment pressures of $\sim$1.2 kbar vs. 4.8 kbar (at 1200°C; Newman & Lowenstern, 2002), and entrapment depths of $\sim$4 km vs. $\sim$18 km respectively for a crustal density of 2700 kg/m$^3$. This demonstrates that the development of an instrument-specific calibration is essential to be able to differentiate between lower and upper crustal storage at ocean island volcanoes, let alone fingerprinting the involvement of different reservoirs identified by geophysical techniques.

An additional source of error affecting both Raman measurements and EOS methods arises during the conversion of $\rho_{CO_2}$ into the equivalent amount of CO$_2$ in ppm held within the vapor bubble ([CO$_2$]$^{VB}$):

$$[CO_2]^{VB} = 10^6 \times \frac{\rho_{CO_2} V_{VB}}{\rho_{Melt} V_{Melt}}$$

Where $V_{VB}$ and $V_{Melt}$ are the volume of the vapor bubble and the melt phase of the inclusion respectively, and $\rho_{Melt}$ is the density of the silicate melt calculated here using DensityX (Iacovino & Till, 2019). Total CO$_2$ contents are obtained by summing the equivalent amount of CO$_2$ in the vapor bubble with the concentration of CO$_2$ measured in the melt phase ([CO$_2$]$^{Melt}$) by SIMS or FTIR:

$$[CO_2]^{Tot} = [CO_2]^{VB} + [CO_2]^{Melt}$$

The volumes of the vapor bubble and melt inclusion are typically determined from 2D transmitted light images, estimating the length of the third, unmeasurable
dimension from the major and minor axes of the plan view of the inclusion. Tucker et al. (2019) simulate this process by randomly intersecting ellipses and show that the smallest errors are achieved by calculating the third dimension as the arithmetic mean of the two measured axes. However, this approach is still associated with a $1\sigma$ error of -47 to +37% (Tucker et al., 2019). Although important, we note that this random error is entirely overwhelmed by the systematic error of up to a factor of 4 in literature datasets which have arbitrarily chosen a literature densimeter.

To mitigate the systematic error associated with Raman calibration, we determine the relationship between $\Delta$ and $\rho_{\text{CO}_2}$ for the specific instrument and acquisition conditions used in this study through the analysis of synthetic fluid melt inclusions with known CO$_2$ densities. Analysis of both the melt phase (using SIMS) and the vapor bubble (using a calibrated Raman system) yields the first extensive dataset critically evaluating the contribution of vapor bubbles to the total CO$_2$ budget of specific melt inclusions at Kilauea. Combined with a rigorous examination of the suitability of different CO$_2$ - H$_2$O solubility models, these measurements place accurate constraints on entrapment depths of olivine-hosted melt inclusions from the 2018 LERZ eruption. This dataset, combined with quantitative models of bubble growth, also allows assessment of the relative importance of post-entrapment crystallization and syn-eruptive quenching on the partitioning of CO$_2$ between the melt and vapor phase. In turn, this allows the accuracy of EOS methods as an alternative to direct measurements of $\rho_{\text{CO}_2}$ using Raman Spectroscopy to be evaluated.

3 Materials and Methods

3.1 Sample Details, Preparation and Analytical Methods

We examine three samples erupted at F8 (square symbols; Fig. 1c):

1. May-18 (erupted May 30th, 2018; USGS code KE62–3293; blue symbols), comprising vesicular reticulite and scoria which landed in a bucket placed near the F8 vent ($19^\circ 27.7486' \text{ N}, 154^\circ 54.8636' \text{ W}$).

2. July-18 (erupted Mid-July 2018; red symbols), from the selvages of a naturally-quenched, and highly vesicular proximal overflow from the F8 channel ($<50 \text{ m from the vent}; 19^\circ 27.879' \text{ N}, 154^\circ 54.645' \text{ W}$).
3. Aug-18 (erupted Aug 1st; USGS code KE62–3321F; orange symbols), which was sampled directly from the F8 channel using a metal rod and chain, and rapidly quenched in water. Direct lava sampling took place on a stable channel levee (19° 28.31508’ N, 154° 54.51426’ W), ~700 m downstream of the position of the July-18 overflow.

Samples were jaw crushed and sieved into three size fractions (250–840, 840–1000 and >1000 µm). Olivines were picked under a binocular microscope, and individually mounted in CrystalBond™ on glass slides. Care was taken to prepare melt inclusions hosted within olivine crystals from all three size fractions. Melt inclusions were exposed by grinding with 250–3000 grade wet and dry paper, allowing embayments to be avoided, and melt inclusions containing vapor bubbles to be identified. Melt inclusions without vapor bubbles were ground down with progressively finer wet and dry paper until the center of the inclusion was exposed. Melt inclusions containing vapor bubbles were ground down to just above the top of the melt inclusion of interest (to avoid intersecting the bubble, and releasing the trapped CO₂). A photo was taken of the melt inclusion and vapor bubble using a transmitted light microscope to allow estimation of melt inclusion and bubble volumes. For larger melt inclusions, two images were acquired: one where the bubble was in focus, and one where the melt inclusion outline was in focus. The outline of the bubble and melt inclusion were traced using ImageJ (Schneider et al., 2012), and a best fit ellipse was fitted to each. Volumes were calculated by assuming that the third (non-measurable dimension) was equal to the arithmetic mean of the two measured dimensions (Tucker et al., 2019). Several melt inclusions contained large spinel crystals that were likely co-entrapped. The volume of these spinels (assuming a cuboid shape, with the third dimension also equal to the arithmetic mean of the visible dimensions) was subtracted from the volume of the melt inclusion.

Following optical measurements, crystals were ground down until the vapor bubble was within ~30 µm of the surface. Depending on the optical quality after fine grinding (using 2000-7000 grade wet and dry paper), melt inclusions were variably polished using 9 µm diamond pastes prior to Raman analysis. Raman spectra of vapor bubbles were collected using a confocal LabRAM 300 (Horiba Jobin Yvon) Raman spectrometer in the Department of Earth Sciences at the University of Cam-
bridge. The two CO$_2$ Fermi Diads were fitted with Gaussians (see Supporting Information Fig. S4). The relationship between the $\Delta$ and $\rho_{CO_2}$ for the specific Raman acquisition condition used in this study was determined by analyzing 16 synthetic CO$_2$ – H$_2$O fluid melt inclusions with a range of densities (\(~0.04 \text{ g/cm}^3\), \(~0.08 \text{ g/cm}^3\) and \(~0.14 \text{ g/cm}^3\)) hosted in quartz, as well as three Kilauean melt inclusion vapor bubbles. The densities of all 19 of these primary standards were measured using a JY Horiba LabRam HR in the Fluids Research Laboratory at Virginia Tech Raman, which has been specifically calibrated for low CO$_2$ densities using a high-pressure optical cell (Lamadrid et al., 2017). A linear regression through repeated measurements of standards yielded the following relationship with 95% confidence intervals on the regression (see Supporting Information Fig. S3):

$$\rho_{CO_2} (\text{g/cm}^3) = 0.3217 \pm 0.026 \Delta (\text{cm}^{-1}) - 32.995 \pm 2.7$$

(3)

Further analytical details are presented in the Supporting Information (Text S1). Following Raman analyses, individual crystals were ground down to expose the center of each melt inclusion to maximize the available analyzable area. The bubble was exposed in approximately half of bubble-bearing inclusions. Following sonication to remove polishing residue, exposed bubble walls were examined on the FEI Quanta 650FEG SEM at the University of Cambridge in low vacuum mode prior to the application of any coatings. Crystals were then mounted in epoxy in groups of 20–40, and polished with progressively finer diamond pastes (9, 6, 3, 1, 0.25 $\mu$m).

Following the application of a gold coat, the concentrations of H$_2$O and CO$_2$ (as well as MgO and SiO$_2$ for normalization) in melt inclusions and co-erupted matrix glasses were determined using the Cameca IMS-7f GEO at the NERC Ion Microprobe Facility, University of Edinburgh. SIMS analysis was performed prior to EPMA analysis to avoid volatile migration under the electron beam, and to avoid contamination of measured carbon concentrations by a carbon coat. Epoxy stubs were placed in the sample chamber at vacuum for a minimum of 6 hours before analysis to allow them to outgas. A wide variety of standards were analyzed to create calibration curves for H$_2$O and CO$_2$ (N71, M10, 519-4-1, M5, M40, M36, M21, M47, M36; see Supporting Information S5; Shishkina et al., 2010; Hauri, 2002). Additional information regarding calibration, background and drift corrections are provided in the Supporting Information (Text S2).
Following SIMS analyses, the Au coat was removed by polishing on a 0.25 µm diamond polishing pad, and a carbon coat was applied for electron microprobe analyzer (EPMA) analyses. Spot analyses of melt inclusions, matrix glasses and host olivines were obtained using a Cameca SX100 EPMA in the Department of Earth Sciences, University of Cambridge following the two-condition analytical set up described in Wieser et al. (2019). Spectrometer configurations, count times, calibration materials, and estimates of precision and accuracy calculated from repeated analyses of secondary standards (San Carlos Olivine, VG2 and A99; Jarosewich, 2002) are presented in the Supporting Information (Text S3, Tables S2-4).

Melt inclusions were corrected for the effects of post-entrapment crystallization using the Olivine MI tool in Petrolog3 (Danyushevsky & Plechov, 2011). This requires the user to specify the initial FeOT and the host Fo content of each inclusion. FeOT was set at 11.33 wt% for melt inclusions hosted in olivines with forsterite contents ([Fo=Mg2+//(Mg2+ + Fe2+), atomic]) > 79 mol% based on the liquid line of descent at Kilauea, and for consistency with previous studies (Wieser et al., 2019; Sides, Edmonds, Maclennan, Swanson, & Houghton, 2014). For olivine crystals with Fo<79 mol%, the initial FeO content was estimated from the relationship between the equilibrium olivine forsterite content and melt FeOT contents in a fractional crystallization model computed in MELTS for MATLAB (Supporting Information Fig. S5 Antoshechkina & Ghiorso, 2018).

4 Results

F8 melt inclusions are hosted in olivine crystals with a wide range of core compositions (Fo77−89; Fig. 2a). Core compositions in all three samples show a peak at ~Fo88−89 (Fig. 2b-d), which lies significantly above the equilibrium field calculated from the Mg# of co-erupted matrix glasses [Mg#=Mg2/+(Mg2++Fe2+), atomic], even considering a wide range of experimentally-determined values for K\text{Fe}^{3+}/Mg2+ (black lines, Fig. 2a; 0.270–0.352; Roeder & Emslie, 1970; Matzen et al., 2011). Fourteen melt inclusions from May-18, but only six melt inclusions from July-18 and one from Aug-18 are hosted in olivines which lie within the equilibrium field. F8 olivines have some of the highest Fo contents ever reported at Kilauea (Fig. 2a-d vs. Fig. 2e-f; Sides, Edmonds, Maclennan, Swanson, & Houghton, 2014; Wieser et al., 2019), but relatively low carrier melt Mg#s (51–57 mol%; assuming Fe3+/FeT
In turn, this juxtaposition produces some of the most extreme degrees of olivine-carrier melt Fe-Mg disequilibrium seen at Kilauea (Fig. 2a). Crystals with high forsterite cores show strong normal zoning, while those with core compositions plotting closer to the equilibrium field on Fig. 2a are not visibly zoned in rapid EDS acquisitions (see Supporting Information Figs. S7-9).

The majority of F8 melt inclusions exhibit lower measured FeO$_T$ contents than co-erupted matrix glasses and the composition of Kilauean melt inclusions from the literature (grey dots; Wieser et al., 2019; Tucker et al., 2019; Sides, Edmonds, Maclellan, Houghton, et al., 2014; Sides, Edmonds, Maclellan, Swan- son, & Houghton, 2014). Melt inclusion MgO contents are more similar to those of co-erupted matrix glasses (Fig. 3a). Following a correction for the effects of post-entrapment crystallization, F8 melt inclusions have MgO contents between 6.4 and 13.7 wt%, and FeO$_T$ contents between 11.3 and 12 wt% (Fig. 3a, Supporting Information Fig. S5). Despite the high degree of Mg# disequilibrium between olivine crystals and their carrier melts (Fig. 2a), measured melt inclusion Mg#s (uncor- rected for the effects of PEC) mostly lie within, or close to the equilibrium field calculated from the core compositions of their host olivines (Fig. 3b). The distance from the equilibrium field degree is largest in the July-18 sample, but still smaller than the vast majority of melt inclusions data from other Kilauean eruptions, particularly those hosted in olivines with higher Fo contents (Fig. 3b). Melt inclusions hosted in olivine crystals which have the highest degree of disequilibrium with their carrier melts (calculated by subtracting the equilibrium Fo content of the co-erupted matrix glass from the Fo content of each olivine) have experienced the most PEC (Fig. 3c) and have the lowest measured FeO$_T$ contents (Fig. 3d).

To encapsulate the variable degrees of olivine-melt disequilibrium, and to aid comparisons between different crystal populations, we subdivide F8 olivines into two groups. The first group contains olivines which lie within, or close to the equilibrium field calculated from the Mg# of the co-erupted matrix glass (Fig. 2a). For the May-18 sample, the division was placed at Fo$_{81.5}$, based on the near continuous distribution of olivines from slightly above to within the equilibrium field (which can easily be generated by slight cooling between crystallization and eruption), and the slight gap between these olivines and those with higher Fo contents (Fig 2b). The second group contains olivines which lie outside the equilibrium field. For brevity,
Figure 2. Olivine populations and olivine-melt relationships at F8 compared to literature data. a) Core olivine forsterite content versus matrix glass Mg# for Fe$^{3+}/Fe_T=0.15$ (Moussallam et al., 2016; Helz et al., 2017). Olivines lying between the black lines ($K_D=0.270–0.352$) are in equilibrium with their carrier melts considering the range of experimentally-determined Fe-Mg partition coefficients (Roeder & Emslie, 1970; Matzen et al., 2011). F8 olivines have some of the highest Fo contents observed at Kilauea, yet are hosted in carrier liquids with some of the lowest Mg#. Literature data from Wieser et al. (2019), Sides, Edmonds, Maclennan, Houghton, et al. (2014), Sides, Edmonds, Maclennan, Swanson, and Houghton (2014). b-d) Histograms of olivine Fo contents from this study, e) Kilauea Iki (Sides, Edmonds, Maclennan, Houghton, et al., 2014; Sides, Edmonds, Maclennan, Swanson, & Houghton, 2014), and f) the compilation of literature analyses presented in Wieser et al. (2019) combined with new measurements from Tucker et al. (2019). The strong bimodality in F8 forsterite contents, along with the degree of olivine-melt disequilibrium was used to subdivide melt inclusions into those hosted within High-Fo olivines (black dotted outline) and Low-Fo olivines (red dotted outline). Olivines are further subdivided into those hosting a melt inclusion without a vapor bubble (no VB), with a vapor bubble which produces a Fermi diad (VB with FD), those with a vapor bubble that does not produce a Fermi diad (VB without FD). Melt inclusions which are cracked, and have a vapor bubble without a FD, are indicated with a white dot.

these groups are referred to as Low-Fo and High-Fo olivines, although this classification evaluates the forsterite content of the olivine relative to the Mg# of the co-erupted matrix glass, rather than the absolute Fo content (see Fig. 3c).
ilar classification for the eruptions on Fig. 2 with higher glass Mg#s would place
the boundary between groups at higher Fo contents (e.g., the Fo$_{84}$ division used by
Wieser et al., 2019).
Figure 3. Measured major element systematics for F8 melt inclusions (uncorrected for the effects of PEC). a) High-Fo F8 melt inclusions have significantly lower FeO₀ contents than liquid line of descent defined by Kilauean matrix glasses from (this study, Wieser et al., 2019; Sides, Edmonds, Maclennan, Houghton, et al., 2014), and a MELTS for MATLAB (Antoshechkina & Ghiorso, 2018) fractionation path following the onset of clinopyroxene and plagioclase fractionation (green line) which recreates glass compositions erupted from earlier, more evolved fissures during the 2018 eruption (4-5 wt% MgO, white triangles). Despite highly variable FeO₀ contents, the MgO contents of melt inclusions mostly align with those of their co-erupted matrix glasses. b) In contrast to the prominent disequilibrium between High-Fo olivine compositions and co-erupted matrix glasses (Fig. 1a), melt inclusion Mg#s uncorrected for the effects of PEC (for Fe³⁺/Fe=0.15) plot close to the equilibrium field with their host olivines (particularly melt inclusions from the May-18 and Aug-18 samples). Melt inclusions from previous Kilauean eruptions (Wieser et al., 2019; Tucker et al., 2019; Sides, Edmonds, Maclennan, Houghton, et al., 2014; Sides, Edmonds, Maclennan, Swanson, & Houghton, 2014, grey dots) lie much further below the equilibrium field. c) The amount of PEC (calculated in Petrolog3; Danyushevsky & Plechov, 2011) is strongly correlated with the degree of ol-melt disequilibrium, calculated by subtracting the equilibrium olivine composition of the co-erupted matrix glass (for K_D=0.3) from the measured Fo content. d) The FeO₀ contents of F8 melt inclusions also shows a strong negative correlation with the amount of PEC, extending to lower values than the vast majority of
All High-Fo melt inclusions contain a vapor bubble (Fig. 3c), 73% (N=53) of which produce a Fermi diad (FD) during Raman analysis. Vapor bubbles which do not produce a FD may contain no CO$_2$, or CO$_2$ densities below the detection limit of Raman spectroscopy. While the detection limit will depend on the exact depth of the bubble below the surface, as well as the transparency of the host crystal, the distribution of densities in vapor bubbles which produced a FD indicates that the detection limit lies between 0–0.02 g/cm$^3$ (light green bar in Fig. 4c). Nine of the bubbles without a FD are hosted within cracked melt inclusions, which may have resulted in CO$_2$ loss from the bubble (diamonds with white dots; Fig. 3 and 4, see Supporting Information Fig. S10 Aster et al., 2016). In contrast, only 50% (N=15) of Low-Fo melt inclusions contain a vapor bubble, and only 20% (N=3) of these produce a FD (Fig. 3c). Only 1 of the bubbles without a FD is hosted within a cracked melt inclusion.

Bubble-bearing melt inclusions show a correlation between the volume % of the bubble and the amount of PEC, despite the large random errors associated with measuring bubble proportions from 2D images (grey error bars; Fig. 4a). There is a substantial drop in glass CO$_2$ contents with increasing PEC, and melt inclusions containing vapor bubbles with a FD show significantly lower glass CO$_2$ contents than bubble-free melt inclusions (Fig. 4b, \(p=10^{-7}\); Kolmogorov Smirnov test). There is no obvious correlation between the CO$_2$ density in vapor bubbles and the amount of PEC (Fig. 4c, \(R^2=10^{-5}\)), the CO$_2$ density and the glass CO$_2$ content \((R^2=0.1)\) or the CO$_2$ density and the volume of the bubble \((R^2=0.0004)\). The median and mean proportion of the total melt inclusion CO$_2$ budget hosted within the bubble is 93% and 87% respectively (black histogram; Fig. 4d). This exceeds the proportions calculated by Moore et al. (2015) for melt inclusions from the 1959 and 1960 eruptions of Kilauea (median=67%, mean=65%; blue histogram). This discrepancy reflects the fact that Moore et al. (2015) did not measure the CO$_2$ content of the glass in each melt inclusion, so they calculated proportions assuming a glass CO$_2$ content of 300 ppm (the maximum measured in the same suite of samples by Tuohy et al., 2016). Our new data shows the importance of measuring CO$_2$ in the glass and bubble of a specific melt inclusion; while bubble-free melt inclusions have CO$_2$ contents up to 417 ppm in the glass phase, those with vapor bubbles producing a FD have median CO$_2$ contents of only 45 ppm (mean=54 ppm; Fig. 4b).
contrast to the highly variable CO₂ contents in melt inclusion glasses, H₂O contents are remarkably constant within a given eruption, despite significant variation in the contents of incompatible elements such as Na₂O and K₂O (Fig. 5a). Excluding two degassed melt inclusions (∼0.09 wt% H₂O), F8 melt inclusions have between 0.19–0.33 wt% H₂O, which is lower than most of the Kīlauean melt inclusions measured by Sides, Edmonds, Maclennan, Houghton, et al. (2014); Sides, Edmonds, Maclennan, Swanson, and Houghton (2014) and almost all of those measured by Tucker et al. (2019) (Fig. 5b).

5 Discussion

5.1 Mineral-melt disequilibrium drives the growth of a CO₂-rich bubble

The prominent Mg# disequilibrium between the core compositions of High-Fo olivines from F8 and their carrier melts has been observed in a number of historic eruptions at Kīlauea (Fig. 2; Tuohy et al., 2016; Wieser et al., 2019; Sides, Edmonds, Maclennan, Houghton, et al., 2014; Sides, Edmonds, Maclennan, Swanson, & Houghton, 2014). Based on major and trace element disequilibrium between melt inclusions and their carrier melts (e.g., Nb/Y ratios), as well as microstructures consistent with deformation of the crystal lattice (also observed in some High-Fo olivines from F8 by Gansecki et al., 2019), Wieser, Edmonds, et al. (2020) and Wieser et al. (2019) suggested that highly forsteritic olivines are scavenged from long-lived plastically-deforming mush piles at the base of the SC reservoir, and incorporated into cooler, lower Mg# carrier melts with different trace element signatures just prior to eruption. In contrast, these studies suggest that olivines with lower forsterite contents exhibiting small amounts of olivine-melt disequilibrium (similar to the Low-Fo olivines in this study), no lattice distortions, and a high degree of trace element equilibrium may have crystallized from their carrier melts as true phenocrysts.

Kīlauean melts with greater than ∼6.8 wt% MgO are saturated in only olivine and minor chrome-spinel (Wright & Fiske, 1971), so show a strong correlation between temperature and the MgO content of the melt (Helz & Thornber, 1987). The remarkably constant FeO contents of these high MgO melts (Fig. 3a) means that
glass Mg\# is strongly correlated with MgO, and therefore temperature. As glass Mg\# is closely related to the olivine forsterite content through the Fe-Mg olivine-liquid exchange coefficient, equilibrium olivine forsterite contents are also strongly correlated with temperature. Thus, the difference in Mg\# between the measured olivine core composition, and the equilibrium olivine forsterite content calculated from the composition of co-erupted matrix glasses (termed the degree of olivine-melt disequilibrium) is proportional to the amount of cooling experienced by the inclusion prior to syn-eruptive quenching (Wieser et al., 2019). The close relationship between the amount of cooling experienced by an inclusion, and the amount of PEC (Danyushevsky et al., 2000) accounts for the excellent correlation between the degree of olivine-melt disequilibrium and the amount of PEC (Fig. 3c).

F8 melt inclusions are hosted in some of the most forsteritic olivines erupted at Kilauea, yet were erupted in carrier melts with some of the lowest Mg\#s (Fig. 2a). Consequently, they have experienced some of the largest amounts of cooling following entrapment, and, by extension, some of the largest amounts of PEC ever reported at Kilauea (up to \(\sim 33\%\); Fig. 3c). These PEC extents are also significantly larger than those reported from other volcanic systems; olivine-hosted melt inclusions from Holuhraun (Iceland), Piton de la Fournaise (Réunion) and Erebus (Antarctica) have experienced \(~5\%, <12\%\) and \(0-4.2\%\) PEC respectively (Hartley et al., 2015; Collins et al., 2012; Moussallam et al., 2014). The small amounts of cooling (and therefore PEC) experienced by Low-Fo olivines, which are close to equilibrium with their carrier melts, likely occurred during fractionation between the formation and eruption of these crystals (Fig. 3c). However, progressive fractionation and cooling of a batch of melt cannot account for the peak at \(~\text{Fo}_{88-89}\) in F8 samples (Wieser et al., 2019; Maaløe et al., 1988), nor the paucity of olivines with Fo contents in equilibrium with the co-erupted matrix glasses (particularly in the July and Aug samples; Fig. 2a). Based on the similarities between the High-Fo olivines from F8 and previous studies (large amounts of olivine-melt disequilibrium, presence of lattice distortions; Gansecki et al., 2019), we appeal to the process proposed by Wieser et al. (2019), where cooling is not a gradual process during progressive differentiation of a given magma batch (Maaløe et al., 1988), but occurs over short timescales, when High-Fo olivine crystals residing in hot mush piles are mixed into...
significantly cooler, lower Mg# melts (Wieser et al., 2019; Sides, Edmonds, Maclennan, Houghton, et al., 2014), see also Shea et al. (2019).

Melt inclusion MgO and FeO\(_T\) contents are strongly affected by the crystallization of olivine on the walls of the melt inclusion (PEC), and subsequent diffusive re-equilibration. Based on the strong coupling between MgO content and temperature in olivine-saturated liquids (Helz & Thornber, 1987), thermal equilibration of a hot olivine crystal with a cooler carrier melt drives the crystallization of a zoned olivine rim from the melt inclusion, causing the MgO content of the melt inclusion to drop to match that of the carrier melt (Fig. 3a). This zoned olivine rim begins to re-equilibrate with the host crystal, and, in turn, the melt inclusion re-equilibrates with the changing rim composition (Danyushevsky et al., 2000). The melt inclusion loses FeO by diffusion to achieve Mg# equilibration with the host olivine following the large initial drop in MgO during cooling. As the MgO content of the melt inclusion is a function of the temperature, FeO diffusion is countered by MgO diffusion in the opposite direction, which is sequestered by further post-entrapment crystallization of olivine on the wall of the melt inclusion.

This FeO-loss process accounts for the negative correlation between melt inclusion FeO\(_T\) contents and the amount of PEC (Fig. 3d). For a given amount of PEC, F8 melt inclusions have lower FeO\(_T\) contents and display a smaller degree of Mg# disequilibrium with their olivine host than the vast majority of literature data (Fig. 3b, d). It is important to note that methods calculating the amount of PEC based on the degree of Mg# disequilibrium between the melt inclusion and the host crystal (e.g., Tucker et al., 2019; Neave et al., 2017) will significantly underestimate the true amount of PEC in melt inclusions where extensive FeO-loss has occurred compared to the Petrolog3 method used here where the user specifies an initial FeO\(_T\) content. For example, the May-18 melt inclusions with Fo>85 have lost sufficient quantities of FeO by diffusive re-equilibration such that their Mg#s are in equilibrium with the composition of the host olivine. Thus, methods based on Mg# comparisons would indicate that these melt inclusions have experienced very minor amounts of PEC. However, their FeO contents lie ~ 4 wt% below the composition of co-erupted matrix glasses, indicating that their compositions have been heavily altered by the PEC process (Fig. 3a).
The higher degrees of diffusive FeO-loss for a given amount of PEC for F8 melt inclusions compared to literature data (Fig. 3d) indicates that there was a longer time lag between the entrainment of crystals into cooler melts and their eventual eruption. Danyushevsky et al. (2002) quantitatively model Fe-Mg re-equilibration to estimate this time lag: their Fig. 4c shows that a melt inclusion with a ∼50 μm radius that has experienced ΔT=100–150°C and undergone FeO loss at T=1150–1200°C achieves 98% equilibrium in ∼2 years. These extents of cooling and temperatures of re-equilibration are representative of F8 inclusions. However, Danyushevsky et al. (2002) assume isotropic diffusion of Fe through the host olivine crystal with \( D_{\text{Fe, Mg}} \approx 3–6 \times 10^{-17} \, \text{m}^2/\text{s} \) at 1150–1200°C. In reality, FeO loss will be dominated by diffusion along the fast c-direction in olivine (\( D_{\text{Fe, Mg}} \approx 1–4 \times 10^{-16} \, \text{m}^2/\text{s} \) for Fo₈₀–₈₉, T=1150–1200°C, and QFM to QFM+0.3; Chakraborty, 2010; Barth et al., 2019). Thus, complete re-equilibration could be achieved almost an order of magnitude faster, in a matter of months. Considering the substantial uncertainties in this method associated with the fact the model of Danyushevsky et al. (2002) does not account for diffusional anisotropy, and the fact the degree of re-equilibration is very sensitive to the choice of \( K_D \) (Fig. 3b), the FeO-T-systematics of melt inclusions within High-Fo olivines erupted on May 28th (∼70–100% re-equilibration) indicate that entrainment into cooler carrier melts occurred approximately a month to a year prior to eruption.

### 5.2 Diffusive H₂O-loss

Given that H₂O in melt inclusions diffusively re-equilibrates over hours to days (Hartley et al., 2015; Le Voyer et al., 2014; Gaetani et al., 2012), the timescales inferred from Fe-Mg disequilibrium are more than sufficient for H₂O contents within F8 melt inclusions to be fully reset to the H₂O content of the melt which carried them to the site of the eruption. This re-equilibration accounts for the remarkably uniform H₂O contents of F8 melt inclusions in each sample, despite substantial variation in the concentration of other incompatible elements (e.g., Na₂O; Fig. 5a).

The approximately constant H₂O contents in melt inclusions from each sample indicates that F8 carrier melts erupted in late May had H₂O contents of 0.29 wt%, while those erupted in July and August had slightly lower H₂O contents (∼0.22–0.23 wt%). These carrier melts are relatively H₂O-poor compared to the composition.
of previously-erupted Kilauean melts (inferred from published melt inclusion data; Fig. 5). The presence of more H$_2$O-poor carrier melts in 2018 likely results from the extensive mixing of magmas which had partially degassed their H$_2$O at the summit lava lake with undegassed melts within the plumbing system between 2008 and 2018 (similar to the mechanism proposed for Puna Ridge magmas by Dixon et al., 1991).
Figure 4. Vapor bubble and melt inclusion CO$_2$ systematics. a) There is a positive correlation between the volume proportion of the vapor bubble (VB) and the amount of PEC. Only melt inclusions which have experienced <10% PEC are bubble-free. Error bars show the 1σ errors associated with estimating bubble volume proportions from 2D images (-45% and +37% Tucker et al., 2019). b) With increasing amounts of PEC, the amount of CO$_2$ within the glass phase of the melt inclusion declines. The highest glass CO$_2$ contents are observed in melt inclusions with no vapor bubbles (squares), and melt inclusion with bubbles that did not produce a FD (diamonds). In contrast, the vast majority of melt inclusions with low glass CO$_2$ contents have vapor bubbles which produced a FD (circles), or vapor bubbles without a FD that were hosted within cracked melt inclusions (diamonds with white dots). c) There is no correlation between the CO$_2$ density in vapor bubble measured using Raman Spectroscopy and the amount of PEC. Error bars show the ±1σ deviation of three repeated measurements of each vapor bubble. The green bar shows our estimate of the detection limit (Det. Lim.) of Raman analyses based on the distribution of measured bubble densities. d) The black histogram shows the proportion of CO$_2$ held within the vapor bubble for F8 melt inclusions that produced a FD (mean=87%, median=93%). Estimates by Moore et al. (2015) for Kilauean melt inclusions from the 1959 and 1960 eruptions are also shown.
**Figure 5.** H$_2$O systematics of F8 melt inclusions relative to literature data from Kilauea. a) F8 melt inclusion H$_2$O contents are remarkably constant within each sample, despite substantial variations in Na$_2$O. This indicates that melt inclusion H$_2$O contents were reset by diffusive re-equilibration with their carrier liquid. The precision of SIMS measurements (±1.5%) is smaller than the symbol size, so error bars are not shown. b) F8 melt inclusions have lower H$_2$O contents than the majority of Kilauean melt inclusions measured by Sides, Edmonds, Maclennan, Swanson, and Houghton (2014); Sides, Edmonds, Mackenna, Houghton, et al. (2014) (yellow histogram) and almost all of the melt inclusions measured by Tucker et al. (2019). H$_2$O contents from submarine ERZ glasses with 7–16 wt% H$_2$O from Dixon et al. (1991); Clague et al. (1995) are shown with red dashed lines. c) Relationship between the molar fraction of H$_2$O in the vapor phase (X$_{H_2O}$) and the melt H$_2$O content for five different melt CO$_2$ contents (50, 100, 200, 500 and 750 ppm; using VolatileCalc-Basalt; Newman and Lowenstern, 2002). X$_{H_2O}$ ratios for the co-existing vapor in equilibrium with the measured concentration of CO$_2$ and H$_2$O in the melt phase of the bubble-bearing inclusions from this study and Tucker et al. (2019) (triangles) are overlain, with symbols colored by the CO$_2$ content of the glass phase. The relatively low H$_2$O contents of F8 melt inclusions mean that X$_{H_2O}$ is generally <0.1. However, a number of inclusions from Tucker et al. (2019) with glass CO$_2$ contents <100 ppm have much higher X$_{H_2O}$ ratios. This causes the CO$_2$ densities predicted using the EOS method to fall below the trend line defined by F8 melt inclusions on Fig. 8a.
5.3 PEC and melt-vapor CO$_2$ partitioning

It is well recognized that extensive PEC drives the growth of a CO$_2$-rich vapor bubble (Steele-Macinnis et al., 2011; Sides, Edmonds, Macleman, Houghton, et al., 2014; Sides, Edmonds, Macleman, Swanson, & Houghton, 2014; Aster et al., 2016; Macleman, 2017). Thus, studies measuring only the CO$_2$ in the melt phase using SIMS or FTIR will yield spuriously low entrapment depths for melt inclusions which have undergone extensive PEC (e.g., Sides, Edmonds, Macleman, Houghton, et al., 2014). Our concurrent measurements of CO$_2$ in the melt and bubble phase of a large number of melt inclusions which have experienced a wide range of PEC amounts (Fig. 3c-d) provides a unique opportunity to interrogate the various processes causing CO$_2$ to partition into the vapor bubble.

To investigate the effects of compositional changes in the melt inclusion associated with PEC, we use the CO$_2$ solubility model of Shishkina et al. (2014):

$$\ln[CO_2] = 1.15\ln(P) + 6.71\Pi^* - 1.345$$

(4)

Where $[CO_2]$ is the concentration of CO$_2$ in ppm, and $P$ is the pressure in MPa. The $\Pi^*$ term accounts for the compositional dependence on CO$_2$ solubility, expressed in terms of the cation fractions of 7 major element species:

$$\Pi^* = \frac{Ca^{2+} + 0.8K^+ + 0.7Na^+ + 0.4Mg^{2+} + 0.4Fe^{2+}}{Si^{4+} + Al^{3+}}$$

(5)

We calculate the change in $\Pi^*$ during PEC, $\Delta \Pi^*$, by subtracting the $\Pi^*$ value of the PEC-corrected major element composition of each melt inclusion from the $\Pi^*$ value of the measured composition. $\Delta \Pi^*$ becomes progressively more negative with increasing amounts of PEC, showing that CO$_2$ becomes progressively less soluble (red dots; Fig. 6b, see also Macleman, 2017). Changes in $\Pi^*$ are dominated by a decrease in $X_{Mg}$, and increase in $X_{Si}$ and $X_{Al}$ resulting from the crystallization of olivine on the walls of the inclusion. These changes are partially counteracted by an increase in $X_{Ca}$ (as Ca is incompatible in olivine). To quantify the magnitude of this drop in $\Pi^*$ in terms of CO$_2$ partitioning between the melt and bubble, we consider the 8 melt inclusions which have experienced >30% PEC (all of which contain bubbles which produce a FD). The mean $\Pi^*$ value of the measured compositions of
these melt inclusions is 0.33, while the mean Π° of their PEC-corrected compositions is 0.39 (∆ Π°=-0.068). For P=0.76 kbar, which is the average entrapment pressure for the PEC-corrected compositions of these melt inclusions calculated using equation 4, CO₂ solubility drops by ~192 ppm. As melts at Kilauea are CO₂ saturated at crustal storage depths (Gerlach et al., 2002), this extra CO₂ will partition into the vapor bubble.

However, the mean amount of CO₂ sequestered within the vapor bubbles of these 8 melt inclusions is 657±231 ppm (calculated using equation 1). This reflects three additional processes which enhance CO₂ partitioning into the bubble during PEC. Firstly, the crystallization of olivine, which contains negligible quantities of CO₂, drives up the total concentration of the CO₂ in the remaining melt by a factor of 1 plus the amount of PEC (1.3 to 1.33× for these 8 melt inclusions). As mentioned above, because Kilauea melt inclusions are CO₂ saturated (Gerlach et al., 2002), this excess partitions into the bubble (mean 145 ppm, up to 230 ppm CO₂).

Secondly, the preferential contraction of the melt phase relative to the olivine during thermal re-equilibration leads to a reduction in the volume of the melt phase. This is enhanced by the third process; the crystallization of denser olivine on the rim of the melt inclusion. A drop in the internal pressure of the melt inclusion causes the CO₂ solubility to decrease further, driving more CO₂ into the vapor bubble (equation 5). Evidence for these volume changes is provided by the correlation between the amount of PEC and the volume of the vapor bubble (Fig. 4a), as well as the observation that all melt inclusions without a vapor bubble have experienced <10% PEC (Fig. 4a), while all melt inclusions that have experienced >10% PEC have a vapor bubble.
Figure 6. Evaluating the compositional sensitivity of CO$_2$ solubility. a) Comparison of the MgO vs. Al$_2$O$_3$ systematics of PEC-corrected F8 inclusions to the glass compositions used to calibrate each solubility model. The North Arch lavas which define the simplified $\Pi$ vs. SiO$_2$ relationship presented in Dixon (1997) and implemented in VolatileCalc-Basalt (Newman & Lowenstern, 2002) are also shown (blue circles). The MagmaSat dataset (Ghiorso & Gualda, 2015) includes the experiments in the calibration datasets of Shishkina et al. (2014), Iacono-Marziano et al. (2012) and Dixon et al. (1995) (so is not shown, as it would cover all these symbols). b) $\Delta X$ (triangle and star symbols) and $\Delta \Pi^*$ (red dots Shishkina et al., 2014) for F8 melt inclusions plotted against the amount of PEC. $\Delta X$ and $\Delta \Pi^*$ were calculated by subtracting the values of $X$ and $\Pi^*$ for PEC-corrected melt inclusions from the values of $X$ and $\Pi^*$ for measured compositions. For example, inclusion LL8,156 has experienced 33% PEC, and has a PEC-corrected MgO content of 13.5 wt% and a measured MgO content of 5.4 wt%. Thus, $\Delta X_{MgO}$ is strongly negative. c) The compositional parameter $\Pi$ of Dixon (1997) calculated for PEC-corrected F8 melt inclusion compositions varies substantially with SiO$_2$, following an offset trend to that defined by North Arch Glasses (Dixon et al., 1997, blue dots and linear regression). VolatileCalc-Basalt effectively treats all melt inclusions with $>$49 wt% SiO$_2$ as if $\Pi$ is constant (red line). d) The compositional parameter $\Pi^*$ from Shishkina et al. (2014), and therefore the solubility of CO$_2$, is significantly higher for High-Fo melt inclusions (which have the highest PEC-corrected MgO, and lowest SiO$_2$ and Al$_2$O$_3$ contents). The color of the symbols for F8 melt inclusions in c) and d) represents the amount of PEC.
Overall, changes in melt chemistry, the incompatible behaviour of CO$_2$, and a drop in the internal pressure of the melt inclusion accounts for the rapid decrease in glass CO$_2$ contents with increasing PEC (Fig. 4b). Our concurrent measurements of glass and bubble CO$_2$ provide the first opportunity to see through these convoluting effects of PEC to robustly determine total CO$_2$ contents, and therefore entrapment depths of Kilauean melt inclusions. To account for the uncertainty regarding the amount of CO$_2$ held within bubbles that did not produce a FD (diamond symbols), particularly those hosted within cracked olivines (diamond symbols with white dot), we only calculate total CO$_2$ contents and entrapment depths for melt inclusions which had no bubble, or a bubble that produced a FD. These total CO$_2$ were corrected for the incompatible behaviour of CO$_2$ during PEC to determine the total CO$_2$ content at the point of melt inclusion entrapment.

Total PEC-corrected CO$_2$ contents in melt inclusions hosted within High-Fo olivines are offset to significantly higher values compared to those hosted within Low-Fo olivines (Fig. 7a), indicating that these two olivine populations crystal-lized at distinct depths within Kilauea’s plumbing system. It is also interesting to compare our total CO$_2$ contents to previously published data on Kilauean melt inclusions. Although these studies investigate products from different eruptions, the apparent stability in the geometry of Kilauea’s plumbing system since at least the 1950s (Helz et al., 2014; Poland et al., 2015; Eaton & Murata, 1960) means such comparisons are still useful (and particularly relevant for studies of the 1959–1960 eruptive period, where activity at the summit was followed by a large LERZ eruption; e.g., Tuohy et al., 2016; Moore et al., 2015; Sides, Edmonds, Maclennan, Houghton, et al., 2014; Sides, Edmonds, Maclennan, Swanson, & Houghton, 2014). Unsurprisingly given our findings that ~90% of CO$_2$ is held within the vapor bubble (Fig. 4d), CO$_2$ contents in F8 melt inclusions are significantly higher than measurements of just the glass phase by Sides, Edmonds, Maclennan, Swanson, and Houghton (2014); Sides, Edmonds, Maclennan, Houghton, et al. (2014) (Fig. 7c). F8 melt inclusions are also offset to higher CO$_2$ contents than experimentally-rehomogenized melt inclusions (Tuohy et al., 2016, Fig. 7d). Tuohy et al. (2016) note similar offsets between their measurements and Raman reconstructions of bubble CO$_2$ by Moore et al. (2015) in the same sample set. They suggest that their analyses may have been biased towards melt inclusions with smaller bubbles that
fully disappear upon heating, lower pressure inclusions that do not fracture during heating, and larger inclusions that can be analysed by FTIR.

Interestingly, our distribution of total CO₂ contents for melt inclusions which possessed bubbles are indistinguishable using the Kolmogorov-Smirnov (KS) test \((p=0.1)\) from the CO₂ contribution of just the vapor bubbles in melt inclusions from the 1959 and 1960 eruptions of Kilauea (Moore et al., 2015, Fig. 7c). This demonstrates that in olivine populations which have experienced extensive PEC, measurements of glass CO₂ contents are of subordinate importance to measurements of bubble CO₂. Furthermore, the contribution of CO₂ from the melt phase for the majority of High-Fo melt inclusions from F8 is entirely overwhelmed by the errors on the amount of CO₂ in the bubble associated with estimating bubble volume proportions from 2D images. However, it is worth noting that only measuring CO₂ in vapor bubble would have failed to identify the population of Low-Fo olivines which host almost all of their CO₂ within the glass phase. Thus, we suggest that future studies use a small number of SIMS or FTIR analyses of melt inclusions, combined with EPMA analyses of host crystals and melt inclusions, to determine the relationship between glass and bubble CO₂ contents and the amount of PEC in different subpopulations of melt inclusions. If the vast majority of CO₂ in a given population is held in the vapor bubble, a limited analytical budget would be better spent accurately measuring bubble volumes (using MicroCT or 3D Raman mapping; Pamukcu et al., 2013; Venugopal et al., 2020) to combine with Raman measurements of CO₂ density in the rest of the sample set, instead of precisely quantifying the insignificant amount of CO₂ held within the glass phase using SIMS or FTIR.

Importantly, we also observe that the distribution of total CO₂ contents in bubble-bearing melt inclusions is significantly higher than bubble-free melt inclusions (Fig. 7b). This result invalidates the approach of preferentially targeting bubble-free melt inclusions to avoid having to account for CO₂ within the vapor bubbles (e.g., Helo et al., 2011; Esposito et al., 2011) in systems where erupted crystals have experienced extensive PEC prior to eruption. Crucially, analysis of only bubble-free melt inclusions by SIMS or FTIR, or analyses of just vapor bubbles using Raman, would have failed to identify that crystals are supplied from two distinct storage regions within Kilauea’s plumbing system.
Figure 7. Histograms of melt inclusion CO$_2$ contents from this study and the literature (all corrected for the effects of PEC). a) Total CO$_2$ contents (bubble+glass) for High and Low-Fo melt inclusions are statistically distinguishable at $p=0.05$ using the Kolmogorov Smirnov (KS) test (p value and test statistic k shown on the figure). b) Similarly, melt inclusions which contain a vapor bubble (VB) with a FD have significantly higher total CO$_2$ contents than bubble-free melt inclusions. c) Melt inclusion CO$_2$ contents from a suite of eruptions at Kilauea between 1500 and 2008 AD where only the glass phase was measured (Sides, Edmonds, Maclennan, Swanson, & Houghton, 2014; Sides, Edmonds, Maclennan, Houghton, et al., 2014). d) CO$_2$ contents of experimentally-homogenized melt inclusions from the
1959 Kilauea Iki and 1960 Kapoho eruptions (Tuohy et al., 2016). e) Bubble CO\textsubscript{2} contents from Moore et al. (2015) in the same suite of samples as in d). For consistency, these bubble CO\textsubscript{2} contents were corrected for PEC using the average amount of PEC reported by Tuohy et al. (2016) (13%). f) Cumulative distribution plots for these datasets. g) Total inclusion CO\textsubscript{2} contents from Tucker et al. (2019) where the contribution from bubble CO\textsubscript{2} was estimated using the EOS method (excluding inclusions with bubble volumes >8% that the authors suggest were co-entrapped). 35 melt inclusions have CO\textsubscript{2} >1500 ppm. Note the change in x axis scale from plots a-f). For literature data, all melt inclusions are shown, as Fo contents were not reported by Moore et al. (2015), and matrix glass Mg#s were not reported in Tucker et al. (2019), so it was not possible to classify data based on the degree of olivine-melt disequilibrium as for F8 samples.

5.4 Analytical versus theoretical constructions of vapor bubble CO\textsubscript{2}

In contrast to the good agreement between our estimates of total CO\textsubscript{2} contents from combined SIMS and Raman measurements from F8 and the bubble-only measurements of Moore et al. (2015), the total CO\textsubscript{2} contents estimated by Tucker et al. (2019) for a range of Kilauean eruptions using the EOS method are displaced to significantly higher values (Fig. 7g). To assess the cause of this discrepancy, we follow the EOS method they describe to calculate CO\textsubscript{2} bubble densities for F8 melt inclusions to compare to our Raman measurements. The simplification of the Dixon (1997) solubility model implemented in the excel workbook VolatileCalc (hereafter VolatileCalc-Basalt Newman & Lowenstern, 2002) was used to calculate the internal pressure of the melt inclusion based on the measured SiO\textsubscript{2}, CO\textsubscript{2} and H\textsubscript{2}O contents of the glass phase. The pure CO\textsubscript{2} EOS of Span and Wagner (1996) implemented in Python3 through CoolProp (Bell et al., 2014) was used to calculate the CO\textsubscript{2} density at this internal pressure and 725 °C, which was the presumed glass transition temperature of Tucker et al. (2019) based on Ryan and Sammis (1981). The Duan and Zhang (2006) EOS utilized by Tucker et al. (2019) yields identical densities to the fourth decimal place (see Supporting Information Fig. S11). The more significant source of error involves the choice of the glass transition temperature. This is fixed at 725 °C in Tucker et al. (2019) and 825 °C in Moore et al. (2015)(dashed and solid magenta line; Fig. 8a) for simplicity, but in reality, varies as a function of
cooling rate and melt viscosity (and, by extension, melt composition; Giordano et
al., 2005; Maclellan, 2017). The average glass transition temperatures predicted by
the bubble-growth python code MIMiC (which uses the model of Giordano et al.,
2005; Rasmussen et al., 2020) for bubble-bearing F8 melt inclusions for cooling rates
of 10 °C/s is 680 °C (dotted magenta line; Fig. 8a). Following Tucker et al. (2019),
we multiply the density obtained from the pure-CO₂ EOS by the mole fraction of
CO₂ (X_{CO₂}) in the vapor phase determined in VolatileCalc (Newman & Lowenstern,
2002). This correction neglects the non-ideal mixing of H₂O and CO₂ at magmatic
temperatures compared to the use of a mixed H₂O-CO₂ EOS (e.g., Moore et al.,
2015) but is probably a reasonable approximation for relatively dry systems such as
Kilauea (Fig. 5a-b).

The dominant control of the glass CO₂ content on the internal pressure of the
inclusion in relatively anhydrous melts, and the positive relationship between the in-
ternal pressure and ρ_{CO₂} from the EOS evaluated at a constant temperature, means
that predicted ρ_{CO₂} values increase with increasing glass CO₂ contents (Fig. 8a). Predicted CO₂ densities from Tucker et al. (2019) plot on or below the quadratic fit
through the EOS predictions for F8 melt inclusions at 725 °C (magenta solid line),
because of the higher values of X_{H₂O} (and thus lower X_{CO₂}) for a number of melt
inclusions which possess high glass H₂O, but low glass CO₂ contents (Fig. 5c). How-
ever, unlike the predictions from the EOS method, there is no correlation between
ρ_{CO₂} measured using Raman spectroscopy and glass CO₂ contents (R²=0.11). Inter-
estingly, all melt inclusions with >200 ppm CO₂ in the glass have vapor bubbles
which did not produce a FD (diamond symbols; Fig. 8a), indicating that their CO₂
densities were below the detection limit of Raman Spectroscopy (~0–0.02 g/cm³;
green bar in Fig. 4c). It seems implausible that these bubbles could possess the high
CO₂ densities predicted by the EOS (ρ_{CO₂} >0.2 g/cm³) and fail to produce a FD.
Furthermore, melt inclusions with ρ_{CO₂} > 0.2 g/cm³ will consist of an outer shell of
liquid CO₂, and an inner sphere of vapor CO₂ at room temperature (~21–22 °C).
For ρ_{CO₂}=0.4 g/cm³, this liquid phase will comprise 26% of the radius of the bub-
ble, and the motion of the inner sphere of vapor because of Brownian motion would
be readily observable under an optical microscope. Yet, we observe no two-phase
bubbles, and there are no reports of two-phase bubbles in the Kilauean literature.
Figure 8. Comparisons of bubble CO$_2$ densities calculated using the EOS with those measured by Raman Spectroscopy. a) Calculated $\rho_{CO_2}$ correlates strongly with glass CO$_2$. Bubbles within F8 melt inclusions are shown as white circles and diamonds (FD and no FD), bubbles within melt inclusions from Tucker et al. (2019) are shown as beige hollow circles. Magenta lines shows quadratic fits through calculated bubble densities for F8 melt inclusions for the EOS evaluated at 680°C, 725°C and 825°C. A number of inclusions with low inclusion CO$_2$ contents and high H$_2$O contents from Tucker et al. (2019) lie below this line, because of their higher X$_{H_2O}$ values (Fig. 5c). Measured $\rho_{CO_2}$ in this study are shown as colored circles, with error bars showing the 1σ of repeated acquisitions of each bubble. Colored diamonds (no FD, not cracked) are plotted at 0.02 g/cm$^3$ (the presumed detection limit of Raman Spectroscopy; see Fig. 4c). b) The absolute discrepancy between predicted and measured $\rho_{CO_2}$, $\Delta \rho_{CO_2}$, correlates strongly with glass CO$_2$ content. The 95% confidence interval on a linear regression for measured bubble densities is shown with red dotted lines. Bubbles which did not produce a FD lie within error of the extrapolated confidence interval (assuming $\rho_{CO_2}$=0.02 g/cm$^3$). c) To allow comparison with bubble growth models in Fig. 9, the discrepancy between EOS methods and Raman measurements are shown as a factor (as above, VB without a FD assumed to contain 0.02 g/cm$^3$). The proportion of the total bubble volume grown during quench for the High- and Low-Fo models shown in Fig. 9 are shown with red and cyan lines respectively. Error bars in b) and c) for VB with FD show the 1σ uncertainty of repeated Raman measurements, and those for VB without FD are calculated for DL between 0-0.02 g/cm$^{-3}$ (hence they extend to infinity in c).
The fundamental tenet of the EOS method used by Tucker et al. (2019) is that $\text{CO}_2$ continues to partition between the vapor bubble and the melt until the bubble stops growing at the glass transition temperature. However, during syn-eruptive quenching, the strong temperature dependence of $\text{CO}_2$ diffusivity means that the diffusion of $\text{CO}_2$ from the melt into the bubble may cease before the bubble reaches its final volume (Anderson and Brown, 1993). Continued bubble growth without concurrent diffusion causes the density of $\text{CO}_2$ within the bubble to drop below that predicted from the EOS (Aster et al., 2016; Moore et al., 2015; Maclennan, 2017). Non-equilibrium bubble expansion has been proposed to account for the presence of vapor bubbles in Icelandic melt inclusions with $\text{CO}_2$ concentrations below the detection limit of Raman Spectroscopy (Neave et al., 2014).

The discrepancy between EOS predictions and Raman measurements ($\Delta \rho_{\text{CO}_2}$) increases linearly with glass $\text{CO}_2$ content ($R^2=0.75$; shown as an absolute discrepancy, Fig. 8b) and decreases with the amount of PEC (shown as a factor, Fig. 8c). Melt inclusions containing bubbles without a FD lie within the confidence interval of the regression through bubbles which produced a FD if the Raman detection limit (0.02 g/cm$^3$) is subtracted from $\text{CO}_2$ densities calculated from the EOS (Fig. 8b). To investigate these correlations, we assess the relative contribution of bubble growth at high magmatic temperatures during PEC and ascent (where $\text{CO}_2$ diffusion and bubble growth are coupled) compared to bubble growth during quench (where $\text{CO}_2$ diffusion is temperature-limited, and therefore decoupled from the mechanical expansion of the bubble).

We model melt inclusions from the point of entrapment to the glass transition temperature using the model of Maclennan (2017; Fig. 9). Quench rates of 10°C/s were used based on video footage of the sampling and quenching of the Aug-18 sample; $\sim$40 s elapsed between the sample being pulled from the channel ($\sim$1150°C) and becoming brittle at the glass transition temperature ($\sim$725 °C Tucker et al., 2019). At these cooling rates, there is negligible transfer of $\text{CO}_2$ from the melt to the bubble during syn-eruptive quenching. Two end-member cooling histories were modelled. The red melt inclusion in Figure 9a experienced large amounts of cooling ($\Delta T=150^\circ\text{C}$) and PEC at high magmatic temperatures and pressures, representative of the PT path followed by melt inclusions hosted within the most forsteritic olivines. The blue melt inclusion in Figure 9b experiences no cooling and post-
entrapped crystallization prior to ascent and syn-eruptive quenching, representative
of Low-Fo melt inclusions which form in carrier melts with similar temperatures to
the ones in which they were erupted.

The High-Fo melt inclusion (red) grows a considerable proportion of its final
bubble volume (58%) during PEC at high magmatic temperatures (square to star
symbol; Fig. 9a). The diffusion of CO$_2$ into this growing bubble causes the CO$_2$
content of the melt phase to drop rapidly (Fig. 9c). During syn-eruptive quenching,
there is no further CO$_2$ diffusion between the melt and bubble (Fig. 9c). This stage
of bubble growth accounts for 42% of the final volume, with $\rho_{CO_2}$ decreasing from
0.10 to 0.06 g/cm$^3$ (Fig. 9a, d). As the EOS method effectively predicts the density
of CO$_2$ in the vapor bubble prior to the final, quench-induced stage of bubble ex-
pansion, the EOS method overpredicts the CO$_2$ density by a factor of 1.7× in this
example. This lies well within the deviation between measured and predicted CO$_2$
contents for High-Fo F8 melt inclusions which have experienced >10% PEC (red line
on Fig. 8c). In this case, the proportion of the bubble grown at high temperatures
will be substantially greater, as the model of Macleman (2017) does not account for
the FeO-loss process, which greatly increases the amount of PEC for a given $\Delta T$.
The volume of the bubble grown during syn-eruptive quench is determined by the
difference between the temperature at the initiation of syn-eruptive quenching, and
the glass transition temperature, so is almost constant for different PT paths. In
contrast, with increasing amounts of PEC, the volume of the bubble grown at high
temperatures gets progressively larger, so the relative expansion of the bubble during
quench (and therefore the change in CO$_2$ density) gets progressively smaller. For
example, in models with $\Delta T=200^\circ$C instead of $\Delta T=150^\circ$C, the amount of PEC
increases from 18% to 25%, and the proportion of the bubble grown at high temper-
ature increases from 58% to 68%. In turn the bubble density drops from only 0.073
to 0.052 g/cm$^3$ during syn-eruptive quenching (so the EOS method would only over
predict by a factor of $\sim1.4$×).

In contrast, the Low-Fo melt inclusion (blue) grows a very small proportion of
its total bubble volume at high temperatures (10%), with 90% of the final bubble
volume growing upon quench (Fig. 9b). Substantial bubble expansion upon quench
without concurrent CO$_2$ diffusion causes $\rho_{CO_2}$ to drop substantially (Fig. 9d). Ef-
fectively, the EOS method calculates the density of the bubble at the initiation of
the quench stage ($\rho_{CO_2}=0.205 \text{ g/cm}^3$; star symbol), while the true bubble density is $11.9\times$ lower ($\rho_{CO_2}=0.021 \text{ g/cm}^3$; circle symbol), close to the detection limit of Raman spectroscopy. This calculated discrepancy is very similar to that for vapor bubbles in Low-Fo inclusions which do not have Fermi diads (assuming the detection limit=$0.02 \text{ g/cm}^3$, cyan line, Fig. 8c).

In summary, the EOS substantially overestimates $\rho_{CO_2}$ for melt inclusions which have experienced small amounts of PEC and retain high CO$_2$ contents (Fig. 8b,c), because bubble growth in these melt inclusions is dominated by the quenching process where there is no diffusion of CO$_2$ into the bubble. In contrast to these very large discrepancies (factors of $\sim$10), bubble densities in melt inclusions which have experienced extensive PEC are broadly matched by the EOS method (within a factor of $\sim$2; Fig. 8c).
Figure 9. Model of CO$_2$ partitioning between the melt and bubble for PT scenarios representative of inclusions hosted within High and Low-Fo olivines (red and blue colors, respectively). a) The red melt inclusion experiences considerable cooling (ΔT=150°C) and post-entrapment crystallization at high temperatures and pressures (square to diamond symbol), driving the growth of a vapor bubble. This high temperature phase of bubble growth is accompanied by CO$_2$ diffusion from the melt to the bubble, causing the glass CO$_2$ content to drop substantially (c). This inclusion then ascends to the surface (diamond to star symbol), and experiences a second stage of vapor bubble growth during syn-eruptive quenching (star to circle symbol). b) The blue melt inclusion follows an end-member PT path representative of an inclusion hosted within a Low-Fo olivine. It experiences no cooling and post-entrapment crystallization at high temperature. A bubble only begins to grow during ascent to the surface, with 90% of the total bubble volume of this inclusion occurs during syn-eruptive quenching (star to circle). At the quenching rates of 10°C/s used in this model, there is negligible CO$_2$ transfer from the glass to the bubble during this low temperature phase of bubble growth. The large amount of bubble expansion without concurrent CO$_2$ diffusion causes the density of CO$_2$ in the vapor bubble to drop close to the detection limit of Raman Spectroscopy (green line, d), while the CO$_2$ of the glass phase remains unchanged (c).

These bubble-growth models show that the magnitude of the discrepancy between measured bubble densities and those predicted by the EOS relates to the proportion of the bubble grown during syn-eruptive quenching. In contrast, Tucker et al. (2019) suggest that Raman measurements may underestimate $\rho_{CO_2}$ relative to
EOS methods because of the sequestration of significant quantities of CO$_2$ as thin films of solid carbonate on bubble walls. Carbonate phases have been identified in a number of melt inclusion vapor bubbles from subduction zone settings based on the presence of a distinctive peak in the Raman spectra at $\sim$1090 cm$^{-1}$ (Venugopal et al., 2020; Moore et al., 2015). However, while Moore et al. (2015) report relatively abundant carbonate phases in vapor bubbles from Seguam and Fuego, only four of the 142 Kilauean vapor bubbles they examined contained carbonates, all of which were hosted within a single olivine crystal. This suggests that vapor bubble carbonates are significantly less common in H$_2$O-poor ocean island systems. We observe no carbonate peaks in Raman spectra from F8 bubbles, nor during optical observations made prior to the exposure of bubbles during polishing. Additionally, no carbonate phases were identified during detailed examination of exposed bubble walls using backscatter and secondary electron imaging, and Energy-Dispersive Spectroscopy (EDS) maps on a FEG-SEM. These EDS maps reveal that bubble wall coatings with a “dotted” appearance identified by Tucker et al. (2019) (see their Fig. 2F) consist of Fe-Cu sulfides, rather than carbonates (see also Venugopal et al., 2020; Moore et al., 2015; Wieser, Jenner, et al., 2020). Finally, even if carbonates in bubble walls remained undetected, our observations regarding the systematic relationship between PEC amounts, CO$_2$ contents, and the discrepancy between Raman measurements and the EOS would necessitate that only bubbles hosted in melt inclusions which had undergone negligible PEC contain carbonate phases.

5.5 Reconstructing Magma Storage Depths

Under the assumption that any reservoir from which a substantial proportion of the crystal cargo was derived must also have supplied melt (in order to entrain these crystals, and carry them to the surface), the depths of the main magma reservoirs supplying F8 can be estimated from melt inclusion entrapment pressures (for a known crustal density). Entrapment pressures were calculated from PEC-corrected total CO$_2$ and major element contents, and temperatures calculated using the MgO-liquid thermometer of Helz and Thornber (1987) for PEC-corrected MgO contents. As melt inclusion H$_2$O contents have been reset by diffusive re-equilibration, saturation pressures were calculated assuming H$_2$O=0.5 wt%, based on the distribution of measured H$_2$O contents in literature studies of Kilauean melt inclusions and un-
degassed submarine glasses from the ERZ (Fig. 5b; Sides, Edmonds, Maclellan, Houghton, et al., 2014; Sides, Edmonds, Maclellan, Swanson, & Houghton, 2014; Clague et al., 1995; Dixon et al., 1991; Tucker et al., 2019). Entrapment pressures for measured water contents are also shown in the Supplementary Information. Entrapment pressures were converted into magma storage depths assuming $\rho=2400$ kg/m$^3$ (for consistency with modelling of the geodetic signals from the 2018 summit collapse by Anderson et al., 2019). Initially, we consider melt inclusions with no vapor bubble, or a vapor bubble which produced a FD, due to the uncertainty in the CO$_2$ density of vapor bubbles which do not contain a FD.

Literature studies of Kilauean melt inclusions have mostly calculated saturation pressures using the CO$_2$-H$_2$O solubility model of Dixon et al. (1995) and Dixon (1997), implemented in the excel workbook VolatileCalc (Newman & Lowenstern, 2002, e.g., Tuohy et al. 2016; Sides et al. 2014a, b; Moore et al., 2015; Tucker et al., 2019). VolatileCalc-Basalt uses a simplified relationship for the compositional dependence of CO$_2$ solubility expressed in terms of just the melt SiO$_2$ content, rather than the full compositional parameter $\Pi$ which accounts for the abundance of seven cations (Dixon, 1997, Fig. 6c). In this simplification the parameter $X_{CO_2^-}(P_0,T_0)$, which representing the solubility of CO$_2$ at 1200 $^\circ$C and 1 bar for a specified fluid CO$_2$ fugacity in the thermodynamic expression of Dixon et al. (1995), is expressed as:

$$X_{CO_2^-}(P_0,T_0) = 8.7 \times 10^{-6} - 1.7 \times 10^{-7}[SiO_2]$$  \hspace{1cm} (6)

This relationship derives from the excellent linear correlation between $\Pi$ and SiO$_2$ in a suite of lavas with 40–49 wt% from the North Arch Volcanic field (blue regression line; Fig. 6c; Dixon et al., 1997). However, extrapolation of Equation 6 beyond 51.2 wt% SiO$_2$ returns a negative value for $X_{CO_2^-}(P_0,T_0)$, which, in turn, predicts that the solubility of CO$_2$ is negative at all pressures. To avoid these extrapolation issues, VolatileCalc-Basalt does not let users enter a SiO$_2$ content >49 wt%, so most studies simply calculate the CO$_2$ solubility for melts with >49 wt% SiO$_2$ using the expression for SiO$_2$=49 wt% (e.g., Tucker et al., 2019; Sides, Edmonds, Maclellan, Houghton, et al., 2014; Sides, Edmonds, Maclellan, Swanson, & Houghton, 2014). Newman and Lowenstern (2002) suggest that this approxima-
tion should return accurate entrapment pressures for basaltic compositions with up
to 52 wt% SiO$_2$ contents. However, the simplified compositional parameter used in
VolatileCalc-Basalt is only valid for melt compositions which define the same tra-
jectories in II vs. SiO$_2$ space as the North Arch Lavas. F8 melt inclusions which
have undergone >10% PEC are offset to substantially higher II values at a given
SiO$_2$ (Fig. 6c), so VolatileCalc-Basalt underestimates the solubility of CO$_2$. Addi-
tionally, while F8 melt inclusions show a large drop in II with increasing SiO$_2$, all
but four melt inclusions have SiO$_2$ >49 wt%, so are treated as if they had the same
composition in VolatileCalc-Basalt (red line; Fig. 6c). Thus, VolatileCalc-Basalt not
only underestimates CO$_2$ solubility, and therefore overestimates entrapment pres-
sures for F8 melt inclusions hosted in High-Fo olivines, it also neglects compositional
variations in CO$_2$ solubility within this suite (Fig. 6c).

To demonstrate the importance of evaluating the suitability of different solu-
bility models, we compare entrapment pressures from VolatileCalc-Basalt with the
models of Ghiorso and Gualda (2015), hereafter MagmaSat, Iacono-Marziano et
al. (2012) with hydrous coefficients, hereafter IM-2012, and Shishkina et al. (2014),
hereafter S-2014, using the open-source python tool VESIcal (Iacovino et al., 2020).
These three models utilize more than a decade of additional experiments on basaltic
compositions compared to the expressions implemented in VolatileCalc-Basalt. By
extension, these models are calibrated on a significantly larger compositional range
(Fig. 6a), so more effectively encapsulate variability in CO$_2$ solubility as a function
of melt composition.

Entrapment pressures for melt inclusions hosted in Low-Fo olivines from F8
calculated using VolatileCalc-Basalt, S-2014, and IM-2012 are statistically indistin-
guishable using the KS test at p=0.05 (Fig. 10a), likely because the major element
compositions of these melt inclusions lie within the calibration range of all four sol-
ubility models (Fig. 6a). MagmaSat returns slightly lower pressures, although these
are not statistically distinguishable (p=0.1 vs. S-2014). These slight discrepancies
likely reflect the differential treatment of mixing between H$_2$O and CO$_2$ fluids in
these different models (e.g., non-ideal mixing in MagmaSat and IM-2012 vs. ideal
mixing in S-2014 and VolatileCalc-Basalt; see Supporting Information Fig. S1).
As only 2 Low-Fo melt inclusions have vapor bubbles producing a FD (N=2), the
distribution of entrapment pressures calculated using just glass CO$_2$ contents are
indistinguishable from those using total CO$_2$ contents (dotted magenta vs. solid red lines; Fig. 10a).

In contrast, there are substantial differences between the entrapment pressures obtained from different solubility models for High-Fo melt inclusions (>Fo$_{81.5}$), with MagmaSat and S-2014 plotting to significantly lower pressures than IM-2012 and VolatileCalc-Basalt (both pairs are statistically indistinguishable from one another at p=0.05; Fig. 10b). As discussed above, the simplification of the compositional dependence in VolatileCalc-Basalt means that this model underestimates CO$_2$ solubility, and therefore overestimates entrapment pressures for High-Fo melt inclusions (Fig. 6c). Similarly, Iacono-Marziano et al. (2012) warn that their semi-empirical model poorly incorporates the compositional effect of melt MgO contents on CO$_2$ solubility, as the vast majority of melts in their calibration dataset have ~6–8 wt% MgO. In contrast, High-Fo PEC-corrected melt inclusions have MgO contents ranging from 7.8–13.7 wt% (Fig. 6a). The calibration dataset for the S-2014 model incorporates a significantly broader range of basaltic compositions, including melts with MgO contents similar to PEC-corrected High-Fo melt inclusions (Fig. 6a). The MagmaSat calibration dataset is similarly extensive (including the experiments used to calibrate S-2014, IM-2012 and VolatileCalc-Basalt). As for Low-Fo melt inclusions, MagmaSat is offset to slightly lower pressures than S-2014 (median offset of 0.1 kbar).

Overall, we favour entrapment pressures from MagmaSat (Fig. 11, as it has the largest calibration dataset, and is a full thermodynamic model (whereas S-2014 is purely empirical). Additionally, the S-2014 model predicts ~1 wt% H$_2$O at 0 bar, meaning that it is effectively evaluating the solubility of pure CO$_2$ for the H$_2$O contents considered here (so shows no change in saturation pressure with variation in H$_2$O contents between 0–1 wt% H$_2$O, see Supporting Information Fig. S1). As shown in Fig. 10, differences between Shishkina and MagmaSat are relatively small. For High-Fo inclusions, the differences between these models are statistically insignificant, and easily overwhelmed with the errors associated with bubble volumes (error bars on Fig. 11a). For completeness, Supporting Information Fig. S12 shows forsterite vs. depth plots similar to those shown in Fig. 11 for reconstructions using Shishkina, and for measured and fixed H$_2$O contents.
Using MagmaSat, Low-Fo melt inclusions yield median entrapment depths (assuming ρ=2400 kg/m$^3$) of 1.44 km (lower and upper 68%=0.89–1.74 km). The median centroid depth, aspect ratio and reservoir volume derived from modelling of the first stage of the 2018 caldera collapse by Anderson et al. (2019) suggests that the HMM reservoir spans depths of 0.82–3.1 km, which aligns well with our entrapment depths, which mainly cluster in the top half of that range (perhaps suggesting melt inclusion formation was favoured in the upper half of the reservoir). The low PEC amounts experienced by these melt inclusions, the absence of cracks, and the fact that the two Low-Fo inclusions which did yield a diad had very low CO$_2$ densities (Fig. 4c), suggests that melt inclusions with a vapor bubble which did not produce a FD likely contained very small quantities of CO$_2$ (because the bubble predominantly forming during syn-eruptive quench; Fig. 9). Thus, we also consider entrapment depths from these melt inclusions (diamond shapes on Fig. 11a). This extends the distribution of entrapment depths to slightly deeper depths, which show an even better overlap with the depths of the HMM reservoir suggested by Anderson et al. (2019).

Considering only High-Fo melt inclusions with a measurable Fermi diad (due to the uncertainty in the amount of CO$_2$ held within vapor bubbles which did not produce a FD in melt inclusions which have undergone extensive PEC), the distribution of entrapment depths (KS test, p=1.6×10$^{-7}$) and means (ANOVA, p=2.5×10$^{-6}$) are offset to significantly higher pressures than Low-Fo melt inclusions (Fig. 11a). Considering the error associated with reconstructing bubble CO$_2$ contents from bubble volumes estimated from 2D images (shown in pink on Fig. 10b), the distribution of entrapment depths for High-Fo olivines overlaps remarkably well with geophysical estimates of the depth of the SC reservoir (3–5 km; Poland et al., 2015). In detail, High-Fo olivines seem to form two main groups, one located at ∼2 km depth, and a second located at 3–5 km depth (Fig. 11a).

The quench-dominated mechanism of bubble growth in Low-Fo olivines means that very little CO$_2$ is held within the vapor bubble. Thus, entrapment depths calculated using glass-only measurements are statistically indistinguishable from those combining bubble and glass measurements (Fig. 10a). In contrast, entrapment depths calculated using just glass CO$_2$ contents in High-Fo olivines are anomalously shallow (median=0.38 km, lower and upper 68%=0.3–0.51 km; Fig. 11b), because
bubble growth at high temperatures during PEC has resulted in the vast majority of
the CO$_2$ entering the vapor bubble (Fig. 9).

Use of EOS techniques to reconstruct CO$_2$ contents of vapor bubbles yields
very high entrapment depths for Low-Fo olivines (median=3.3 km, lower and upper
68%=0.89–10.8 km). Crucially, 13 inclusions yield entrapment depths >5 km (the
inferred base of the SC reservoir), because the EOS method drastically overestimates
bubble CO$_2$ densities in inclusions which have experienced minimal PEC (Fig. 8b-c).
For High-Fo olivines, there is a better overlap between entrapment depths calculated
using EOS methods, and Raman measurements, and EOS methods get closer to the
true distribution of entrapment pressures than measurements of only the glass phase
(Fig. 10b). However, EOS methods still predict that 23 melt inclusions crystallized
at >5 km depth, with one forming at 26.4 km, compared to only two entrapment
depths at 6.3 and 8.8 km using Raman reconstructions of bubble CO$_2$. 
**Figure 10.** Cumulative distribution functions of entrapment pressures from different solubility models (major elements and CO₂ abundances corrected for the effects of PEC), with p values and test statistics from the KS test shown for different comparisons. a) Entrapment pressures for melt inclusion hosted in Low-Fo olivines (for melt inclusions with no VB, or a VB with a FD). Assuming $p=2400$ kg/m$^3$, the median depths for all solubility models align well with the depth range of the HMM reservoir from modelling of the first stage of the 2018 caldera collapse by Anderson et al. (2019) (upper and lower limits calculated from their median volume, centroid depth, and aspect ratio; cyan bar). The distributions of entrapment pressures from MagmaSat calculated from total carbon contents (bubbles+glass; red line) vs. glass only measurements (pink dotted line) are statistically indistinguishable. Entrapment pressures from MagmaSat where bubble CO₂ contents are calculated using the EOS method lie to significantly higher pressures (deep red dotted line). b) Entrapment pressures calculated for melt inclusions hosted in High-Fo olivines (for melt inclusions with a VB producing a FD). The light red region shows the error on MagmaSat entrapment pressures resulting from uncertainty in estimating bubble proportions from 2D images (Tucker et al., 2019). This aligns well with geophysical estimates of the depth of the SC reservoir (3–5 km, magenta bar; Poland et al., 2015). Entrapment pressures from MagmaSat calculated using only glass CO₂ contents (dotted magenta line) are offset to very low pressures extremely low pressures. Entrapment pressures calculated from bubble reconstructed using the EOS method are also offset to anomalously high pressures. In a-b), all melt inclusions are shown for glass-only measurements and EOS calculations, because studies which do not perform Raman measurements cannot distinguish between bubbles with and without a FD.
5.6 Summit-Rift Connectivity

Melt inclusion entrapment depths indicate that olivine crystals erupted at F8 crystallized within both the shallower HMM reservoir (Low-Fo olivines) and the deeper, SC reservoir (High-Fo olivines). The low degrees of olivine-melt disequilibrium and limited amounts of PEC experienced by melt inclusions hosted within Low-Fo olivines implies that these crystals grew in a melt with a similar Mg#, and therefore temperature, to the carrier melt in which they were erupted. In contrast, the high degrees of olivine-melt disequilibrium and large amounts of PEC indicates that High-Fo crystals were mixed into a significantly lower Mg# (and therefore cooler) carrier liquid than the liquid in which they crystallized. Based on reports of lattice distortions (Gansecki et al., 2019) in some F8 olivines, high core forsterite contents, and the clustering of entrapment pressures between 3–5 km (Fig. 11), we suggest that these olivines grew in the SC reservoir, and then settled into mush piles at the base of this reservoir where they were stored for prolonged periods (perhaps as long as centuries to millennia; Wieser, Edmonds, et al., 2020).

Seismic swarms and the initiation of inflationary tilt in March to April 2018 have been interpreted to record the injection of new melts into the South Caldera reservoir (Neal et al., 2019; Flinders et al., 2020), which may have disturbed the olivine mush pile. These new melts (along with the High-Fo olivines they scavenged) would then have mixed into the cooler, lower Mg# melts present within the middle to upper parts of the SC reservoir. Alternatively, if inflationary signals were generated by a reduction in the amount of magma flowing along the ERZ to Pu‘u ‘O‘o (Patrick et al., 2020), progressive internal pressurization of the SC reservoir could also disturb piles of settled crystals. Rapid cooling of mush-derived olivines following their mixing into more evolved melts would have initiated large amounts of PEC. Using the method of Danyushevsky et al. (2002, 2000), the degrees of Mg# re-equilibration between melt inclusions and host olivine crystals (≈70-100%) indicate that crystals were resident in these cooler melts for timescales of approximately a month to a year prior to their eruption at Fissure 8. This is consistent with the time lag between geophysical signals indicating increasing pressurization of the magmatic system in March, and the eruption of crystals between late May and August.
The fact that only two melt inclusions record entrapment depths > 5 km rules out models where high forsterite olivines grew in deeper magma storage reservoirs near the base of the volcanic pile (as suggested for Kilauea’s prehistoric explosive period by Lynn et al., 2017), or within Kilauea’s deep rift zones at ~ 6–9 km (Fig 11 Clague & Denlinger, 1994).
Figure 11.

Caption Fig. 11. Schematic diagram of Kilauea’s plumbing system, informed by entrapment depths from MagmaSat for PEC-corrected melt inclusion compositions (assuming \( \rho = 2400 \text{ kg/m}^3 \) following Anderson et al. (2019)). a) Preferred entrapment depths from this study (all melt inclusions for Low-Fo olivines, only those with a FD for High-Fo olivines). Error bars on bubble-free melt inclusions from SIMS analyses are smaller than the symbol size. Error bars for bubble-bearing melt inclusions were calculated from the minimum and maximum possible total \( \text{CO}_2 \) content using the 1\( \sigma \) error calculated from repeated Raman analyses of each bubble, and the 1\( \sigma \) estimated by Tucker et al. (2019) associated with calculating 3D bubble...
volume proportions from 2D images (-48 to 37%). b) Entrapment depths estimated from analyses of only the glass phase are anomalously shallow for High-Fo olivines. c) Entrapment depths using the EOS method to reconstruct bubble CO$_2$ contents are anomalously deep, with large numbers of inclusions plotting at >5 km depth (note change in scale). Error bar reflects the uncertainty associated with calculating 3D bubble volume proportions from 2D images. d) Cross section showing the three hypothesized magma transport paths supplying rift zone eruptions.

The mechanism by which crystal populations grown in the HMM and SC reservoirs were mixed into a single carrier melt encapsulates an ongoing debate at Kilauea regarding the geometry of the connection between the rift zone conduit and the summit reservoir system. This connection has been variably described as a Y-shaped feeder system with the SC reservoir feeding both the HMM reservoir and the ERZ conduit with two discrete conduits (Pietruszka et al., 2018; Poland et al., 2015, Model 2, Fig. 11d), or a Γ-shaped feeder system with a vertical conduit between the HMM and the SC reservoir, and a single, near-horizontal conduit from the HMM reservoir into the ERZ (Cervelli & Miklius, 2003, Model 3, Fig. 11d). Cervelli and Miklius (2003) suggest that the Γ-shaped model is more plausible because a shallow conduit (which is subject to less lithostatic pressure) is more likely to remain open during pauses in eruptive activity than a deep conduit, and because shallow intrusions into the upper ERZ influence both the HMM reservoir and activity at Pu’u ‘Ō’ō. However, Poland et al. (2015) favour the Y-shaped model based on earthquake and InSAR observations that dyke intrusions into the ERZ in 2007 and 2011 ascended from a depth of ~2–3 km.

For both reservoir geometries, the olivine mush pile at the base of the SC reservoir may have been disturbed by the input of new magma into Kilauea’s summit inferred from geophysical signals (Neal et al., 2019; Flinders et al., 2020), or progressive internal pressurization due to a drop in magma output to Pu’u ‘Ō’ō. In the Γ-shaped model, High-Fo crystals sourced from the SC mush pile may have ascended into the HMM reservoir, and then been transported along a shallow rift zone conduit to the site of the eruption along with Low-Fo olivines. However, the Y-shaped model provides an additional mechanism by which to disturb the SC mush pile. In this geometry, melts from the HMM reservoir carrying Low-Fo olivine crystals would have drained down through the SC reservoir before passing out onto
the rift zone, with significant potential for this downward flow, aided by the large scale collapse of Kīlauea’s caldera, to erode the SC mush pile. Interestingly, the proportion of crystals which are out of equilibrium with their carrier melts increases substantially between May-August 2018 (Fig. 2a), and the degree of re-equilibration between melt inclusions and host crystals decreases (Fig. 3b).

If the disturbance to the mush pile was solely the result of pressurization of the volcanic plumbing system, it might be expected that the majority of High-Fo olivines were disturbed from their mush piles in mid-March to April 2019, when inflationary signals were the strongest (Patrick et al., 2020; Neal et al., 2019). In this scenario, High-Fo olivines might be expected to be more dominant in the May-18 vs. July and Aug-18 samples. In contrast, increasing erosion and scavenging of High-Fo olivines during the downdraining of melts from the HMM reservoir into the SC reservoir during the summit collapse could account for the increase in the proportion of High-Fo olivines with time, similar to the mechanism suggested by Teasdale et al. (2005) for the 1998 eruption of Cerro Azul, Galápagos. Erosion of the mush pile by down-draining from the shallower HMM reservoir, into which the summit caldera was collapsing, also accounts for the fact that High-Fo olivines were extremely rare during the 35 year Pu‘u ‘Ō‘ō eruption.

Another possibility is that some melt inclusions were trapped during the 40 km of transport down the ERZ to the site of the eruption (Patrick, Dietterich, et al., 2019). Assessing this hypothesis requires assumptions regarding the depth of magma transport. Given that the dyke to the LERZ propagated downrift from Pu‘u ‘Ō‘ō, we assume that the dyke had a similar depth to intrusions within the proximity of Pu‘u ‘Ō‘ō between 1997–2007, which have been studied in detail, and shown to rise from the ERZ conduit at depths of ~2–2.4 km (Owen et al., 2000; Montgomery-Brown et al., 2011, and refs within). Thus, it is plausible that some of the Low-Fo olivines with entrapment depths near ~2 km may have growth in the rift zone. However, crystallization within the ERZ conduit and dyke would likely occur throughout the eruption, yet the abundance of Low-Fo olivine crystals declines as the eruption proceeds.

The cluster of High-Fo olivines at ~2 km could also represent crystallization during down-rift transport. These olivine crystals have Fo contents between 84 and
89, which must have grown from melts with MgO contents between 8.5–13.1 wt%
(for K_D=0.3, FeO_T=11.3 wt%, with Fe^{3+}/Fe_T=0.15). Yet, the highest erupted
glass MgO content during the 2018 LERZ eruption is 6.74 wt% MgO (Fig. 3a and
Gansecki et al., 2019). Moreover, glass MgO contents during the 35-year Pu‘u ‘O‘o
eruption did not exceed 8 wt% MgO (see Fig. 8.2 Thornber et al., 2015), suggesting
that high MgO melts may not have been present in the rift zone conduit since the
early phases of the Mauna Ulu eruption in 1969 (Wieser et al., 2019). In contrast,
based on the occurrence of high MgO glass shards in a number of eruptions around
the summit caldera, Helz et al. (2015) suggest that melts with 6.5–11 wt% MgO are
present in the summit reservoir over many centuries. This supports our inference
that the High-Fo olivines erupted at F8 crystallized from high MgO melts supplied
from the Hawaiian mantle plume within the SC reservoir. These high MgO melts are
very rarely erupted at the surface as they rapidly mix with more evolved, resident
melts within the reservoir, so the only record of their existence are the olivines they
crystallize. Given the rarity of these high MgO melts at the surface, it is difficult to
imagine a situation where these melts would avoid mixing with resident magmas in
the summit reservoir, and manage to ascend prolonged distances along the ERZ con-
duit (which must be dominated by low MgO melts based on the composition of the
co-erupted carrier liquid at F8). Finally, if these High-Fo olivines crystallized in the
rift zone, they must have been resident for between a month and a year before they
erupted at F8 (based on the degree of Mg# re-equilibration between melt inclusions
and host olivine crystals).

Interestingly, the May-18 sample does not show the distinctive clustering of
High-Fo entrapment depths at ~2 km seen in the July and Aug-18 sample. This
may result from the relatively small number of measurements of High-Fo olivines
in this sample (N=12). Alternatively, it may suggest that the two reservoirs be-
came increasingly connected during the collapse of the summit caldera, allowing
remobilized High-Fo crystals from the SC mush pile to be transported up into the
shallower HMM reservoir. The juxtaposition of these hot crystals with cooler melts
within this reservoir may have led to dissolution or rapid growth (Shea et al., 2019;
 Mourey et al., 2020), favouring the formation of embayments. Perhaps due to the
mixing with a hotter, and higher Mg# melt, growth may have resumed, sealing off
melts inclusions recording shallower entrapment depths, before the crystal cargo was

-52-
drained back down in the SC reservoir, and out along the ERZ conduit. It is also possible that the two reservoir systems always have a higher degree of connectivity than indicated by schematic diagrams such as Fig. 11, with frequent cycling of melt and crystals between the two reservoirs (and it is simply chance that these lower P inclusions were not seen in the May-18 sample). Further investigation of geophysical datasets from the 2018 eruption should provide tighter constraints on the depth of rift zone transport and dike propagation, allowing more rigorous assessments of the magma transport geometries indicated by our barometric estimates. Additionally, more detailed work on timescales from diffusive re-equilibration of Fe-Mg in both melt inclusions and host crystals will help evaluate differences between the High-Fo crystal cargo erupted at F8 between May and August.

6 Conclusion

Detailed investigations of melt inclusion volatile systematics from the 2018 eruption of Kilauea reveal that the erupted crystal cargo originated from both the Halema’uma’u reservoir (Low-Fo olivines; ∼1–2 km depth) and the South Caldera reservoir (High-Fo olivines, ∼3–5 km depth). This demonstrates that in addition to the supply of magma from the HMM reservoir inferred from geophysical modelling of the summit collapse (Anderson et al., 2019), a substantial volume of magma must also have been derived from the SC reservoir in order to transport these High-Fo crystals to the surface. This supports recent estimates of the total amount of SO$_2$ emitted from F8 (Kern et al., 2020), which requires the erupted volume to have been approximately twice that inferred to have drained from the HMM reservoir by Anderson et al. (2019).

High-Fo Melt inclusions, which mostly yield entrapment depths aligned with geophysical estimates of the depth of the SC reservoir (∼3–5 km), host the vast majority of their CO$_2$ budget in the vapor bubble (∼90%). This is a consequence of the large amounts of PEC experienced by these melt inclusions following their entrainment into cooler, lower Mg# melts. Based on the textural and chemical similarities of these High-Fo crystals and those observed at previous eruptions at Kilauea (Wieser, Edmonds, et al., 2020; Wieser et al., 2019), we suggest that these olivines grew from high MgO melts present at the base of the SC reservoir (Helz et al., 2015), and settled into mush piles for prolonged time periods. Based on the
degree of Mg# re-equilibration between melt inclusions and host olivines, we sug-
124 suggest that these olivines were mobilized from mush piles and mixed into lower Mg#
carrier melts approximately a month to a year before they erupted at Fissure 8.
125 This disturbance may correspond with the onset of geophysical signals of inflation
126 in March-April, 2018, interpreted to represent the injection of new melts into the
127 plumbing system, or a reduction in output from the summit reservoir (Flinders et
128 al., 2020; Patrick et al., 2020). Because of the large amount of CO$_2$ in the vapour
bubbles of these inclusions, entrapment depths calculated using only glass CO$_2$ con-
tents would yield anomalously low entrapment depths (~0.3–0.5 km), and fail to
129 recognise that the SC reservoir supplied significant volumes of magma to Fissure 8.
130
In contrast, Low-Fo melt inclusions are closer to equilibrium with their carrier
131 melts, so have experienced smaller amounts of PEC. Where present, the vapor bub-
132 ble in these melt inclusions is very CO$_2$-poor, and grew most of its volume during
during syn-eruptive quenching (~90%). As the quench rates of these samples mean
133 that there was almost no diffusion of CO$_2$ between the melt and bubble during this
growth phase, reconstructions of bubble CO$_2$ using equation of state methods yield
134 anomalously high entrapment depths (4.5–16.1 km; Fig. 11c).

Careful choice of a CO$_2$-H$_2$O solubility model is also vital to obtain accurate
135 entrapment pressures, and therefore depths. Importantly, the basaltic functions of
VolatileCalc, which has been used the majority of previous Kilauean melt inclusion
136 studies, overpredict entrapment pressures for High-Fo melt inclusions, due to the
137 simplified relationship between CO$_2$ solubility and melt composition in this model.
Like EOS methods, use of this model would indicate that ~50% of melt inclusions
crystallized deeper than the base of the SC reservoir at >5 km (requiring the pres-
138 1ence of a previously unrecognised storage reservoir; Fig. 10).

Overall, our study highlights the importance of measuring bubble densities us-
ing Raman Spectroscopy in addition to measurements of the melt phase by SIMS or
139 FTIR. We also emphasise the importance of carefully evaluating the compositional
range of different solubility models relative to the melt composition of interest. The
140 strong agreement between our entrapment depths and models of magma storage
inferred from geophysical datasets at Kilauea shows that melt inclusion records are
a powerful tool to accurately constrain the location of magma storage reservoirs
supplying volcanic eruptions.

Acknowledgments
This work was funded through a NERC DTP studentship to PW (NE/L002507/1),
a NERC ion microprobe grant (IMF675/1118), two Cambridge University Leave to
Work away grants, and a grant from the NERC Centre for Observation and Modelling of Earthquakes, Volcanoes and Tectonics (COMET). We thank Iris Buisman
for help collecting EPMA data, Cees-Jan de Hoog and John Craven at the Edinburgh Ion Microprobe Facility for their assistance collecting SIMS data, and Richard
Taylor (Zeiss) for collecting the EDS maps shown in the Supporting Information.
We thank Emily Mason, Emma Liu, and Dave Schneider for help collecting samples
in the field. We are very grateful to Jonathon Tucker to helping us to reproduce the
EOS calculations in his paper, and for helpful discussions about bubble walls. Fi-
ally, we thank Paul Wallace, Kendra Lynn and one anonymous reviewer, along with
the editor Ken Rubin for their helpful comments that greatly improved the quality
of this manuscript.

Data Availability The melt inclusion and glass compositions presented in
this paper are provided as an excel spreadsheet. This data has been uploaded to
the Cambridge University Repository https://doi.org/10.17863/CAM.60202, and
is also available on Github https://github.com/PennyWieser/G3-2018-MI. This
spreadsheet also contains the results of the bubble growth models shown in Fig. 9.

References
Anderson. (1974). Evidence for a picritic, volatile-rich magma beneath Mt. Shasta,
Kilauean melt inclusions. American Mineralogist, 78(7-8), 794–803.
Anderson, Johanson, I. A., Patrick, M., Gu, M., Segall, P., Poland, M. P., . . . Mik-
lius, A. (2019). Magma reservoir failure and the onset of caldera collapse at
Antoshechkina, P. M., & Ghiorso, M. S. (2018). MELTS for MATLAB: A new edu-
cational and research tool for computational thermodynamics. AGUFM, 2018,


Fiske, R. S., & Kinoshita, W. T. (1969). Inflation of kilauea volcano prior to its...


positional ranges in coeval melts erupted from kilauea’s summit reservoir.

*Hawaiian Volcanoes: from Source to Surface*, 125–145.


210–222.


Patrick, M., Dietterich, H., Lyons, J., Diefenbach, A., Parcheta, C., Anderson, ...


Wang, W., Caumon, M.-C., Tarantola, A., Pironon, J., Lu, W., & Huang, Y. (2019). Raman spectroscopic densimeter for pure CO_{2} and CO_{2}-H_{2}O-NaCl fluid systems over a wide pt range up to 360 c and 50 mpa. *Chemical Geology, 528*, 119281.


