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VESIcal Part I: An open-source thermodynamic model engine for mixed volatile (H₂O-CO₂) solubility in silicate melts

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Key Points:

- The first comprehensive volatile solubility tool capable of processing large datasets automatically
- Seven built-in solubility models, with automatic calculation and plotting functionality
- Built in python and easily usable by scientists with any level of coding skill

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Abstract

Thermodynamics has been fundamental to the interpretation of geologic data and modeling of geologic systems for decades. However, more recent advancements in computational capabilities and a marked increase in researchers' accessibility to computing tools has outpaced the functionality and extensibility of currently available modeling tools. Here we present VESIcal (Volatile Equilibria and Saturation Identification calculator): the first comprehensive modeling tool for H₂O, CO₂, and mixed (H₂O-CO₂) solubility in silicate melts that: a) allows users access to seven of the most popular models, plus easy inter-comparison between models; b) provides universal functionality for all models (e.g., functions for calculating saturation pressures, degassing paths, etc.); c) can process large datasets (1,000's of samples) automatically; d) can output computed data into an excel spreadsheet for simple post-modeling analysis; e) integrates advanced plotting capabilities directly within the tool; and f) provides all of these within the framework of a python library, making the tool extensible by the user and allowing any of the model functions to be incorporated into any other code capable of calling python. The tool is presented within this manuscript, which is a Jupyter notebook containing worked examples accessible to python users with a range of skill levels. The basic functions of VESIcal can also be accessed via a web app (<https://vesical.anvil.app>). The VESIcal python library is open-source and available for download at <https://github.com/kaylai/VESIcal>.

Plain Language Summary

Geologists use numerical models to understand and predict how volcanoes behave during storage (pre-eruption), eruption, and the composition and amount of volcanic gas released into the atmosphere of Earth and other planets. Most models are made by performing experiments on a limited dataset and creating a model that applies to that dataset. Some models combine lots of these individual models to make a generalized model that can apply to lots of different volcanoes. Many of these different models exist, and they all have specific uses, limitations, and pitfalls. Here we present the first tool, VESIcal, which acts as a simple interface to seven of the most commonly used models. VESIcal is written in python, so users can use VESIcal as an application or include it in their own models. VESIcal is the first tool that allows geologists to easily model thousands of data points automatically and provides a simple platform to compare results from different models in a way never before possible.

1 Introduction

Understanding the solubility and degassing of volatiles in silicate melts is a crucial component of modeling volcanic systems. As dissolved components, volatiles (primarily H₂O and CO₂) affect magma viscosity, rheology, and crystal growth. In addition, due to the strong dependence of volatile solubility on pressure, measured volatile concentrations in preserved high-pressure melts (i.e., melt inclusions: liquid magma trapped within crystals at high pressure, then brought to the surface during an eruption) can be used to determine pre-eruptive magmatic storage pressures, and thus depths. Importantly, volatile exsolution-driven overpressure of a magmatic system is likely the trigger of many explosive volcanic eruptions (Blake, 1984; Stock, Humphreys, Smith, Isaia, & Pyle, 2016; Tait, Jaupart, & Vergnolle, 1989). Once triggered, further drops in magmatic pressure caused by ascent of magma within a volcanic conduit result in the continuous exsolution of volatiles from the melt. Volatile elements experience a large positive volume change when moving from a dissolved to exsolved free fluid state. This expansion fuels a dramatic increase in the

66 magma’s buoyancy, which can often lead to a runaway effect in which the ascent and
 67 degassing of volatile-bearing magma eventually erupts at the surface in an explosive
 68 fashion. Working in concert with seismic and gas monitoring data, pre-eruptive mag-
 69 matic volatile concentrations as well as solubility and degassing modelling can be
 70 used in forensic and sometimes in predictive scenarios, helping us to understand and
 71 potentially mitigate the effects of explosive eruptions.

72 All of these processes depend directly on the solubility – or the capacity of a
 73 magma to hold in solution – of volatile elements. Over the last several decades, a
 74 veritable explosion of new volatile solubility data has opened the door to a plethora
 75 of models to describe the solubility of H₂O, CO₂, or mixed H₂O-CO₂ fluid in mag-
 76 mas covering a wide compositional, pressure, and temperature range. Volatile solu-
 77 bility is highly dependent upon the composition of the host magma, making already
 78 challenging experiments more onerous to perform to encapsulate the range of mag-
 79 mas seen in nature. The most fundamental models (Dixon, Stolper, & Holloway,
 80 1995; Moore, Vennemann, & Carmichael, 1998; Stolper, 1982) focus on a specific
 81 range of magma bulk compositions (e.g., basalt or rhyolite only). Later studies filled
 82 in compositional gaps, some with an increased focus on mixed-volatile (H₂O-
 83 CO₂) studies, increasing the natural applicability of our models to more systems
 84 (Iacono-Marziano, Morizet, Trong, & Gaillard, 2012; Iacovino, Moore, Roggensack,
 85 Oppenheimer, & Kyle, 2013; Liu, Zhang, & Behrens, 2005). To date, there have
 86 been only a few significant efforts to create a holistic thermodynamic model cali-
 87 brated by a wide range of data in the literature. The most popular are MagmaSat
 88 (the mixed-volatile solubility model built into the software package MELTS v. 1.2.0;
 89 Ghiorso & Gualda, 2015) and the model of Papale, Morretti, and Barbato (2006).
 90 Both of these studies have made their source code available; the Papale et al. (2006)
 91 FORTRAN source code (titled Solwcad), web app, and a Linux program can be
 92 found at <http://www.pi.ingv.it/progetti/eurovolc/>, and very recently Mag-
 93 maSat has been made accessible via the ENKI thermodynamic python framework
 94 (<http://enki-portal.org/>).

95 Despite this communal wealth of solubility models, quantitative calculations of
 96 volatile solubility, and by extension saturation pressures, equilibrium fluid composi-
 97 tions, and degassing paths, remains a time-consuming endeavor. Modeling tools that
 98 are available are typically unable to process more than one sample at a time, requir-
 99 ing manual entry of the concentrations of 8-10 major oxides, temperature, as well as
 100 CO₂ and H₂O concentrations to calculate saturation pressures, or X_{H_2O} to calculate
 101 dissolved volatile contents. This is particularly problematic for melt inclusion stud-
 102 ies, where saturation pressures are calculated for hundreds of inclusions, each with
 103 different entrapment temperatures, CO₂, H₂O, and major element concentrations.
 104 For example, the saturation pressures from 105 Gakkel ridge melt inclusions cal-
 105 culated in MagmaSat by Bennett, Jenner, Millet, Cashman, and Lissenberg (2019)
 106 required the manual entry of 1,365 values! The potential for user error in this data
 107 entry stage should not be overlooked.

108 In many cases, newly published solubility models do not include an accompa-
 109 nying tool, requiring users to correctly combine and interpret the relevant equations
 110 (e.g., Dixon, 1997; Dixon et al., 1995; Liu et al., 2005; Shishkina et al., 2014). This
 111 is problematic from a perspective of reproducibility of the multitude of studies
 112 utilizing these models, especially given that some of the equations in the original
 113 manuscripts contain typos or formatting errors. For some models, an excel spread-
 114 sheet was provided, or available at request from the authors. For example, Newman
 115 and Lowenstern (2002) included a simplified version of the Dixon (1997) model as
 116 part of “VolatileCalc”, which was written in Visual Basic for Excel. Due to its sim-
 117 plicity, allowing users to calculate saturation pressures, degassing paths, isobars and
 118 isopleths with a few button clicks and pop-up boxes, this tool has proved extremely

119 popular (with 766 citations at the time of writing). However, to calculate saturation
120 pressures using VolatileCalc, the user must individually enter the SiO_2 , H_2O , CO_2
121 content and temperature of every single sample into pop-up boxes. Similarly, the excel
122 spreadsheet for the Moore et al. (1998) model calculates dissolved H_2O contents
123 based on the concentration of 9 oxides, temperature, and the fraction of $X_{\text{H}_2\text{O}}$ in the
124 vapor, which must be pasted in for every sample. Finally, Allison, Roggensack, and
125 Clarke (2019) provide an excel spreadsheet that allows users to calculate fugacities,
126 partial pressures, isobars, isopleths and saturation pressures. Again, parameters for
127 each sample must be entered individually, with no way to calculate large numbers of
128 samples automatically.

129 Some of these published models and tools are at risk of being lost to time,
130 since spreadsheet tools (particularly earlier studies published before journal-
131 provided hosting of data and electronic supplements was commonplace) must
132 be obtained by request to the author. Even if the files are readily available, pro-
133 grams used to open and operate them may not support deprecated file formats.
134 More recently, authors have provided web-hosted interfaces to calculating sat-
135 uration pressures and dissolved volatile contents (e.g., Iacono-Marziano et al.
136 2012; <http://calcul-isto.cnrs-orleans.fr/>, and Ghiorso and Gualda 2015;
137 http://melts.ofm-research.org/CORBA_CTserver/GG-H2O-CO2.html). Ghiorso
138 and Gualda (2015) also provide a Mac application. While more accessible in the
139 present time, this does not negate the issue of the longevity of these models. The
140 link provided in the Iacono-Marziano et al. (2012) manuscript returns an error “this
141 site cannot be reached”, although email contact with the author directed us towards
142 the newer link given above. Similarly, the link to the H_2O - CO_2 equation of state
143 web calculator that Duan and Zhang (2006) provided in their manuscript returns a
144 404 error.

145 While we certainly advocate for the continued refinement of solubility models,
146 including the completion of new experiments in poorly studied yet critical compo-
147 sitional spaces such as andesites (Wieser, Iacovino, Moore, Matthews, & Allison,
148 submitted), a perhaps more crucial step at this juncture is in the development of a
149 tool that can apply modern computational solutions to making our current knowl-
150 edge base of volatile solubility in magmas accessible and enduring.

151 Here we present VESICAL (Volatile Equilibria and Saturation Identification
152 calculator): a python-based thermodynamic volatile solubility model engine that
153 incorporates seven popular volatile solubility models under one proverbial roof.
154 VESICAL is capable of performing a wide array of calculations on large datasets au-
155 tomatically. But, importantly, VESICAL has been designed for practicality and ease
156 of use. It is designed to be used by anyone, from someone who is completely unfa-
157 miliar with coding to an adept programmer. The non-coder user can interact with
158 VESICAL through a webapp (<https://vesical.anvil.app>) or directly within this
159 manuscript, which utilizes the user-friendly Jupyter Notebook format, allowing them
160 to upload a file with data, execute the various example calculations provided below,
161 and save the results to an Excel file to work with outside of VESICAL. This notebook
162 also incorporates built-in plotting options for easy visualization of user data and
163 calculated results. More experienced programmers may wish to use the more ad-
164 vanced functionality provided by VESICAL, including the ability to hybridize models
165 (e.g., use one model for H_2O and another for CO_2) or write their own routines and
166 code calling VESICAL methods. VESICAL is an open source tool and as such is far less
167 prone to the preservation issues discussed above. Because the VESICAL code is hosted
168 on GitHub, every change to the code is tracked publicly (Perkel, 2016). VESICAL’s
169 current release (version 0.1.5) is also archived on Zenodo, which provides a static
170 citable DOI (10.5281/zenodo.4291043) for the current version of the code.

171 Models included in VESICAL are:

- 172 1. MagmaSat: VESICAL's default model. The mixed-volatile solubility model
 173 within MELTS v. 1.2.0 (Ghiorso & Gualda, 2015)
- 174 2. Dixon: The simplification of the Dixon (1997) model as implemented in
 175 VolatileCalc (Newman & Lowenstern, 2002)
- 176 • DixonWater and DixonCarbon are available as pure-fluid models
- 177 3. MooreWater: (Moore et al. 1998; water only, but H₂O fluid concentration can
 178 be specified)
- 179 4. Liu: (Liu et al., 2005)
- 180 • LiuWater and LiuCarbon are available as pure-fluid models
- 181 5. IaconoMarziano: (Iacono-Marziano et al., 2012)
- 182 • IaconoMarzianoWater and IaconoMarzianoCarbon are available as pure-
 183 fluid models
- 184 6. ShishkinaIdealMixing: (Shishkina et al., 2014) using pure-H₂O and pure-CO₂
 185 models and assuming ideal mixing. In general, the pure-fluid versions of this
 186 model should be used
- 187 • ShishkinaWater and ShishkinaCarbon are available as pure-fluid models
- 188 7. AllisonCarbon: (Allison et al. 2019, carbon only)
- 189 (a) AllisonCarbon_vesuvius (default; phonotephrite from Vesuvius, Italy)
- 190 (b) AllisonCarbon_sunset (alkali basalt from Sunset Crater, AZ, USA)
- 191 (c) AllisonCarbon_sfvt (basaltic andesite from San Francisco Volcanic Field,
 192 AZ, USA)
- 193 (d) AllisonCarbon_erebus (phonotephrite from Erebus, Antarctica)
- 194 (e) AllisonCarbon_etna (trachybasalt from Etna, Italy)
- 195 (f) AllisonCarbon_stromboli (alkali basalt from Stromboli, Italy)

196 A list of model names recognized by VESICAL can be retrieved by executing the
 197 command `v.get_model_names()`, assuming VESICAL has been imported as `v` as is
 198 demonstrated in worked examples below. Note that the above model names are
 199 given in terms of how to call them within VESICAL (e.g., `model='MooreWater'`).
 200 Allison et al. (2019) provides unique model equations for each of the six alkali-rich
 201 mafic magmas investigated in their study. The default model in VESICAL is that
 202 calibrated for Vesuvius magmas, whose calibration has the widest pressure range of
 203 the study (Table 1). Setting a model name of `'AllisonCarbon'` within VESICAL will
 204 thus result in calculations using the AllisonCarbon_vesuvius model equations.

205 As any individual model is only valid within its calibrated range (see below),
 206 and each model is parameterized and expressed differently (e.g., empirical vs. ther-
 207 modynamic models), it is impractical to simply combine them into one large model.
 208 Instead, VESICAL is a single tool that can access and utilize all of these models, with
 209 an extensive pressure-temperature-composition calibration range (Fig. 1). VESICAL
 210 represents the first volatile solubility tool with the ability to perform calculations
 211 for multiple samples at once, with built-in functionality for extracting data from an
 212 Excel file. In addition, the code is written such that it is flexible (sample, calculation
 213 type, and model type can be chosen discreetly) and extensible (VESICAL code can be
 214 easily imported for use in python scripts, and the code is formatted such that new
 215 volatile models can be easily added).

216 All of the calculations implemented in VESICAL can be performed using any of
 217 the models included. The code is structured by calculation rather than by model,
 218 which provides an intuitive way for users to interact with the code and compare
 219 outputs from multiple models. A python class is defined for each calculation. These

220 classes can be called as python methods, take the model name and any applicable
 221 data as arguments, and return the results of the calculation. Each class performs
 222 five key functions: 1) creates the requested model object and performs any nec-
 223 essary pre-processing (e.g., ensuring relevant data are present; normalizing data);
 224 2) takes user input and performs the mathematical calculation; 3) does any neces-
 225 sary processing of the output (e.g., normalizing totals); 4) checks that the model
 226 is being used within its calibrated range; and 5) returns calculated outputs in an
 227 intuitive and manipulatable format (e.g., a python dictionary, a figure, or a pandas
 228 DataFrame). Results of calculations can easily be saved to one or more Excel files
 229 (.xlsx). To demonstrate that VESICAL returns results which are comparable with
 230 pre-existing tools, we have performed a number of tests, which are described in the
 231 Supplementary Information (Text S2).

232 This tool has enormous potential to increase our understanding of igneous
 233 systems. A detailed history of volatile solubility modeling and the implications of
 234 VESICAL are explored in detail in the companion manuscript to this work, Wieser
 235 et al. (submitted). As discussed above, calculating saturation pressures for melt
 236 inclusions using existing tools is an incredibly time-consuming pursuit, requiring
 237 hundreds to thousands of individual numbers to be manually entered. As a result,
 238 very few studies have compared the sensitivity of their pressure estimates to the
 239 choice of solubility model, or propagated errors inherent to measurements of volatile
 240 concentrations in melts using SIMS, FTIR and Raman Spectroscopy into an error
 241 bar in terms of saturation pressure. In contrast, VESICAL allows users to import an
 242 excel spreadsheet with each row containing the major element and volatile contents
 243 of each inclusion, as well as a temperature at which to evaluate solubility. Using
 244 the batch calculation functions, VESICAL will automatically calculate the saturation
 245 pressure for each row, using a user-specified model. Thus, users can easily compare
 246 results from different solubility models, to robustly assess their applicability for
 247 the system of interest. Additionally, users could easily load a different spreadsheet,
 248 where the CO₂ and H₂O concentrations are adjusted to reflect the analytical uncer-
 249 tainty on the instrument used, allowing error bars on the saturation pressure to be
 250 calculated for every single inclusion. The open-source nature of VESICAL also allows
 251 the vast capabilities of Python3 to be applied to modeling of solubility in magmas.
 252 For example, users could utilize Markov chain Monte Carlo (MCMC) methods to
 253 robustly calculate error distributions for each sample.

254 **2 Research Methodology**

255 Navigating the array of models implemented in VESICAL can be challenging.
 256 How can a user determine which model best suits their needs? MagmaSat (the de-
 257 fault model in VESICAL) is the most widely calibrated in P-T-X space, and so we
 258 recommend it for the majority of cases. Where a user wishes to use the other imple-
 259 mented models, we provide some tools to help choose the most appropriate model
 260 (see Supplement). These tools are described in more detail in Section 3.2 on compar-
 261 ing user data to model calibrations.

262 **2.1 Model Calibrations and Benchmarking**

263 The pressure, temperature, and compositional calibration ranges of the seven
 264 models implemented in VESICAL are shown in Table 1 and Figure 1. VESICAL abides
 265 by statements of caution made by the authors of these models regarding their ex-
 266 trapolation by informing the user if a calculation is being performed outside of a
 267 model's calibrated range. In this case, the code returns a warning message, which is
 268 as specific as possible, along with the requested output. We provide these calibra-
 269 tions along with several Jupyter notebooks in the supplementary material (Supple-

Table 1. Calibration ranges of VESICAL models

Model/Reference	Species	P (bar)	T (°C)	Compositional range	Notes
MagmaSat <i>Ghiorso and Gualda, 2015</i>	H ₂ O	0-20,000 ¹	550-1420 ¹	Very broad compositional range of natural silicate melts: subalkaline picobasalts to rhyolites, including a variety of mafic and silicic alkaline compositions	¹ Ranges extracted from Fig. 2d of Ghiorso and Gualda, 2015
	CO ₂	0-30,000 ¹	1139-1400 ¹		
Dixon <i>Simplification of Dixon (1997) used in VolatileCalc (Newman and Lowenstern, 2002)</i>	H ₂ O - CO ₂	0-5000 ¹	800-1400 ¹	Alkali basalts: 40-49 wt% SiO ₂	¹ Warnings implemented in VolatileCalc (Newman and Lowenstern, 2002). ² Calibration range suggested by Lesné et al. (2011) ³ Calibration range suggested by Iacono-Marziano et al. (2012) ⁴ Calibration temperature of Dixon (1997)
		0-2000 ² 0-1000 ³	600-1500 ¹ (1200) ⁴		
MooreWater <i>Moore et al. 1998</i>	H ₂ O	0-3000 ¹	700-1200 ¹	Broad compositional range: subalkaline basalts to rhyolites, alkaline trachybasalts-andesites, foidites, phonolites	¹ Author-suggested calibration range. The calibration dataset spans 190 to 6067 bar, and 800-1200°C
Liu <i>Liu et al. 2005</i>	H ₂ O - CO ₂	0-5000 ¹	700-1200 ¹	Haplogranites and rhyolites	¹ Author-suggested calibration range for the mixed fluid model. The calibration dataset covers 750-5510 bar and 800-1150°C for the Carbon model, and 1-5000 bar and 700-1200°C for the water model
Iacono-Marziano <i>Iacono-Marziano et al., 2012</i>	H ₂ O - CO ₂	95-10,500 (mostly <5000) ¹	1100-1400 (preferably 1200-1300) ²	Predominantly mafic compositions: subalkaline and alkaline basalts-andesites	¹ Range of calibration dataset, as authors do not specifically state a calibration range. We note that the vast majority of experiments were conducted at <5000 bar. ² Authors state that most experiments were conducted between 1200-1300°C (whole range 1100-1400°C)
Shishkina <i>Shishkina et al. 2014</i>	H ₂ O ¹	0-5000 ²	1050-1400 (preferably 1150-1250) ^{2,3}	Mafic and intermediate compositions: Subalkaline basalts-basaltic andesites, alkali basanites-phonolites. SiO ₂ <65 wt%.	¹ Although their empirical expressions are for pure fluids, they were mostly calibrated on mixed CO ₂ -H ₂ O experiments. ² Author-suggested range ³ Note, this model contains no temperature term.
	CO ₂ ¹	500-5000 ²	1200-1250 ^{2,3}	Predominantly mafic compositions: subalkaline basalts, alkaline basanites, trachybasalts	
AllisonCarbon <i>Allison et al., 2019</i>	CO ₂	0-7000 ¹	1200 ² (~1000-1400)	Alkali-rich mafic magmas from 6 volcanic fields. Separate model coefficients for each composition.	¹ Author-suggested range. The calibration dataset spans: (SPVF-4133-6141 bar, Sunset Crater; 4071-6098 bar, Erebus; 4078-6175 bar, Vesuvius; 269-6175 bar, Etna-455-6199, Stromboli-524-6080) ² Note, all calculations performed at 1200 °C (the experimental temperature). Authors suggest results generally applicable between 1000-1400 °C

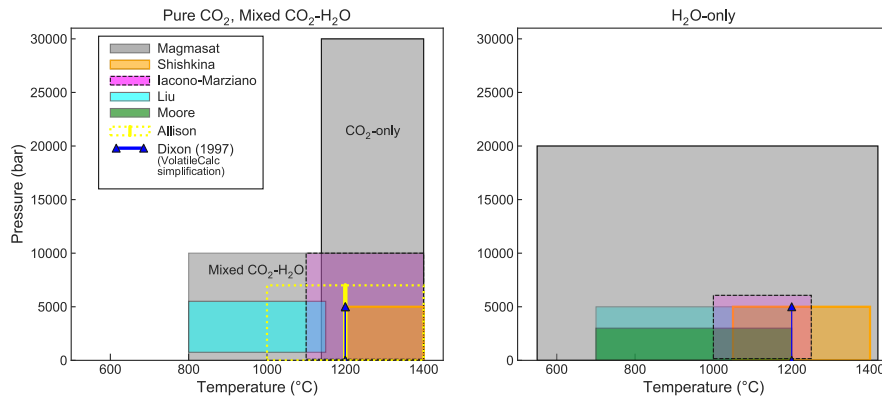


Figure 1. Illustrations showing the calibrated ranges of VESICAL models in pressure-temperature space. Due to difficulty in differentiating between pure-CO₂ and mixed fluid experiments in the literature, plots are subdivided into: experiments performed with pure-CO₂ or mixed (H₂O-CO₂) fluid; and pure-H₂O fluid.

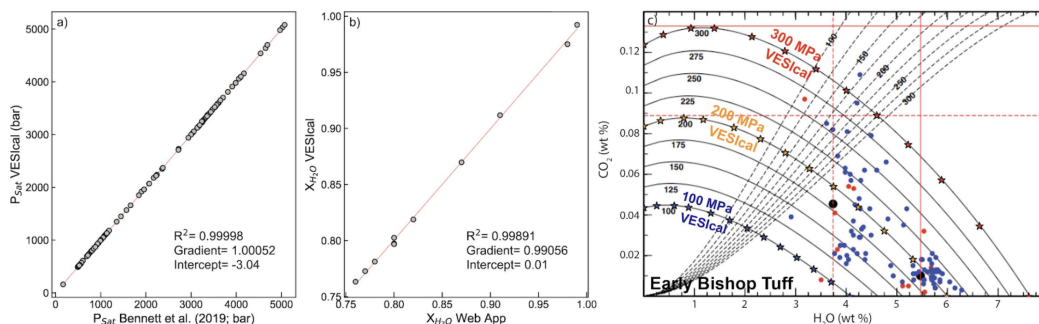


Figure 2. Benchmarking of VESIcal against MagmaSat. a. Comparison of saturation pressures calculated with VESIcal against those by Bennett et al. (2019) using the MagmaSat app for Mac. Samples are all MORB melt inclusions, and pressures were calculated at a temperature unique to each sample. b. Equilibrium fluid compositions calculated with VESIcal against those calculated with the MagmaSat web app. c. Individual points along the 1,000, 2,000, and 3,000 bar isobars for the Early Bishop Tuff rhyolite calculated with VESIcal (stars) and plotted atop isobars published in Fig. 14 of Ghiorso and Gualda (2015).

270 mentary Jupyter Notebooks S1-S7), which allow users to plot their data amongst
 271 the calibrations of the different models to assess their suitability for less objective
 272 measures (also see Section 3.2). Detailed descriptions of the seven solubility mod-
 273 els implemented in VESIcal, including information about their calibration range in
 274 terms of melt composition, pressure, and temperature, are given in this manuscript’s
 275 companion paper Wieser et al. (submitted).

276 Significant testing was undertaken to ensure that VESIcal faithfully repro-
 277 duces the results of all incorporated models. All models underwent multiple tests,
 278 the results of which are shown in the supplement (Supplemental Jupyter Note-
 279 books S1-S7). VESIcal reproduced the results from previous tools (e.g., web apps,
 280 Excel spreadsheets) to within $\pm 5\%$ relative. MagmaSat, VESIcal’s default model,
 281 underwent three tests, the results of which are shown in Fig. 2: 1. Comparison of
 282 saturation pressures from MORB melt inclusions in VESIcal to those published by
 283 Bennett et al. (2019), who used the MagmaSat Mac App ($R^2=0.99998$; Fig. 2a); 2.
 284 Comparison of fluid composition (X_{H_2O}) calculated with VESIcal and the web app
 285 ($R^2=0.999$, identical considering the web app returns 2dp; Fig. 2b); 3. Comparison
 286 of isobars for the Early Bishop Tuff calculated with VESIcal (star symbols) and
 287 isobars published in Fig. 14 of Ghiorso and Gualda (2015) (Fig. 2c).

288 2.2 Format of the python library

289 In this section, the basic organization and use cases of VESIcal are discussed.
 290 VESIcal relies heavily on python pandas, a python package designed for working
 291 with tabulated data. Knowledge of pandas is not required to use VESIcal, and
 292 we refer the user to the pandas documentation for an overview of the package
 293 (https://pandas.pydata.org/pandas-docs/stable/user_guide/index.html).

294 Specific details on how to perform model calculations are discussed in Section
 295 3 and include worked examples. The VESIcal library is written so that users can
 296 interact first and foremost with the calculation they want to perform. Five standard
 297 calculations can be performed with any model in the library:

- 298 1. `calculate_dissolved_volatiles()`
 299 2. `calculate_equilibrium_fluid_composition()`
 300 3. `calculate_saturation_pressure()`
 301 4. `calculate_isobars_and_isopleths()` (plus functionality for plotting; only
 302 for mixed volatiles models)
 303 5. `calculate_degassing_path()` (plus functionality for plotting; only for mixed
 304 volatiles models).

305 Fig. 3 illustrates the basic organization of the code. First, the user determines
 306 which calculation they wish to perform by accessing one of the five core calculation
 307 classes (listed above). In this step, the user specifies any input parameters needed
 308 for the calculation (e.g., sample composition in wt% oxides, pressure in bars, tem-
 309 perature in °C and fluid composition “X_{fluid}” in terms of XH₂O^{fluid}) as well as the
 310 model they wish to use. The default model is MagmaSat, but the user may spec-
 311 ify any model in the library. As an example, the code to calculate the saturation
 312 pressure of some sample using the MagmaSat model would be written as:

```
313     calculate_saturation_pressure(sample=mysample, temperature=850.0).  
314 result
```

315 where `mysample` is a variable (python dictionary or pandas Series) containing the
 316 composition of the sample in oxide wt%, and the temperature is given in °C. Exam-
 317 ples on how to create such a variable are given in Section 3. If a different model is
 318 desired, for example Dixon (1997), it can be passed as:

```
319     calculate_saturation_pressure(sample=mysample, temperature=850.0,  
320 model='Dixon').result
```

321 The core calculation classes each perform two functions: 1) a check is per-
 322 formed to ensure that the user input is within the model’s recommended calibration
 323 range; 2) the `calculate()` method sends the user input to the appropriate model.

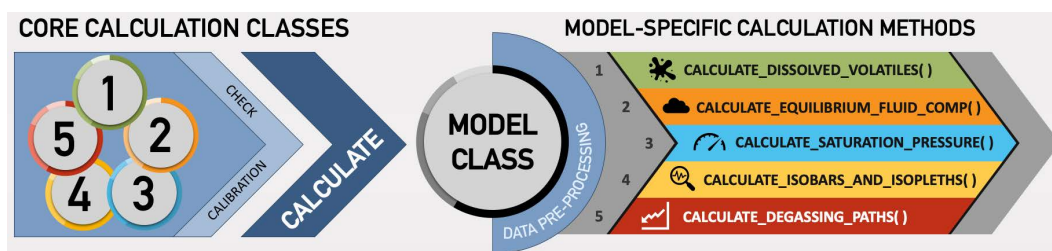


Figure 3. Flowchart illustrating the basic organization of the python library. First, a user chooses a calculation to perform and calls one of the five core calculation classes. Here, any necessary parameters are passed such as sample composition, pressure, and temperature. A check is run to ensure the calculation is being performed within model-specified limits. The `Calculate()` class then calls on one of the `Model()` classes. The default model is MagmaSat, but a user may specify a different model when defining the calculation parameters. Standard pre-processing is then performed on the input data, and this pre-processing step is unique to each model. The processed data are then fed into a model-specific method to perform the desired core calculation.

324 To facilitate both ease of use and flexibility in model application, we have
 325 structured the code such that users can follow one of two computational paths: a
 326 batch processing path and a single sample path (more advanced options). The level

327 of simplicity of either path is indirectly proportional to the level of customization
 328 and extensibility (Fig. 4).

329 The “simplest” way to interact with VESICAL within a python script (i.e., dis-
 330 counting the web app) is via the batch processing path. Here, the user provides
 331 input data in the form of a Microsoft Excel spreadsheet (.xlsx file) and instructs the
 332 model to perform whatever calculation is desired. The model returns data formatted
 333 like a spreadsheet (using the python pandas package), which contains the user’s orig-
 334 inal input data plus whatever model outputs were calculated. The user can continue
 335 to work with returned data by saving the result to a variable (as is shown in all ex-
 336 amples in this manuscript). Data can then be exported to an excel file with a simple
 337 command (see Section 3.10).

338 The more advanced calculation path is the most fundamental: the user has
 339 direct access to all model functions and can even hybridize models. This path al-
 340 lows the user to input information in a variety of ways without being constrained
 341 to formatting the input data in a particular way or naming scheme. This also gives
 342 the user more flexibility in integrating any VESICAL model function into some other
 343 python code.

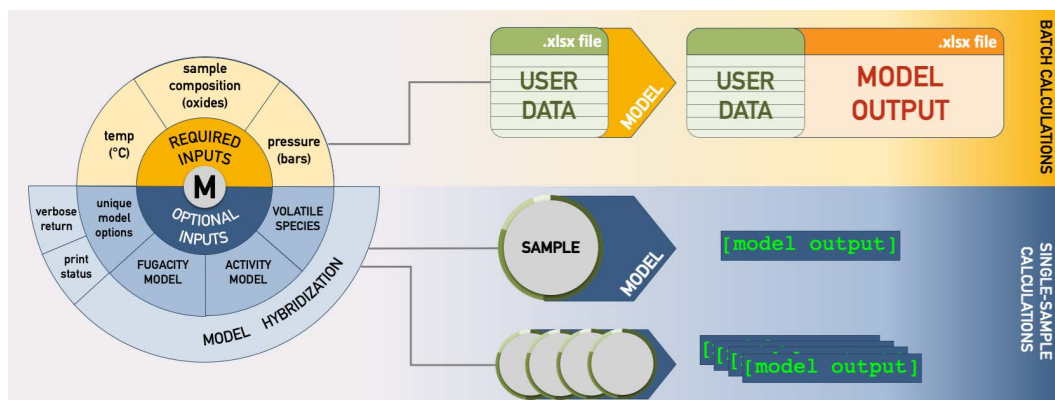


Figure 4. Flowchart illustrating the different operational paths. On top, batch calculation is shown, in which an Excel file with any amount of samples is fed into the model, calculations are performed, and the original user data plus newly calculated values are returned and can be saved as an Excel file. Below, single-sample calculation is shown. These methods can run calculations on one sample at a time, but multi-sample calculations can be performed iteratively with code written by the user. Calculated values are returned as a variable. For single-sample calculations, more advanced modeling options can be set, and hybridization of models can be performed.

344 2.3 Running the code

345 VESICAL can be used in a number of ways: via this Jupyter notebook, via the
 346 VESICAL web app, or by directly importing VESICAL into any python script.

347 VESICAL was born from functionality provided by ENKI and so all the files nec-
 348 essary to use VESICAL are hosted on the ENKI server (<http://enki-portal.org/>).
 349 A unique personal coding environment can be initiated by logging into the ENKI
 350 production server using a GitLab username and password (which is free to obtain;
 351 see directions on the ENKI website for specifics). The simplest way to use VESICAL
 352 while retaining all of its functionality is within this very manuscript, in the form of
 353 a Jupyter notebook. Because this manuscript and VESICAL python library files are

354 hosted on the ENKI server, code can be manipulated and executed in the code cells
 355 below. Making changes won't affect the public version of this manuscript. Likewise,
 356 any user can write their own python code using VESICAL by creating a Jupyter note-
 357 book on the ENKI server and importing VESICAL as is demonstrated in the code
 358 below.

359 Computation time on the ENKI server is limited by the server itself. VESICAL
 360 may run faster if installed locally. Advanced instructions on installing VESICAL on
 361 your own computer are provided in the Supplement (Supplementary Text S1).

362 The most limited but simplest method to interacting with VESICAL is through
 363 the web app (<https://vesical.anvil.app>). The web app can currently perform
 364 three of the five core calculations in batch process mode (via upload of an Excel
 365 spreadsheet). Some, but not all, optional parameters can be set.

366 **To run the code in this notebook**, nothing needs to be installed. Simply
 367 execute the code cells below, changing parameters as desired. Custom data may be
 368 processed by uploading an excel file into the same folder containing this notebook
 369 and then changing the filename in Section 3.1.

370 2.4 Documentation

371 This manuscript serves as an introduction to the VESICAL library aimed at
 372 python users of all levels. However, the code itself is documented with explanations
 373 of each method, its input parameters, and its returned values. This documentation
 374 can be accessed at our readthedocs website (<https://vesical.readthedocs.io/>).
 375 The documentation for any function can be viewed in a jupyter notebook by typ-
 376 ing the function followed by a question mark and executing the cell (e.g., “`v.
 377 calculate_saturation_pressure?`”).

378 Video tutorials are also available on the VESICAL YouTube ([https://
 379 www.youtube.com/channel/UCpvCCs5KMXzOxXWm0seF8Qw](https://www.youtube.com/channel/UCpvCCs5KMXzOxXWm0seF8Qw)). Currently, the first
 380 tutorial covers the basics of VESICAL. More videos for specific features and uses are
 381 planned.

382 2.5 Generic methods for calculating mixed-fluid properties

383 VESICAL provides a set of methods for calculating the properties of mixed
 384 CO₂-H₂O fluids, which can be used with any combination of H₂O and CO₂ solu-
 385 bility model. The use of generic methods allows additional models to be added to
 386 VESICAL by defining only the (simpler) expressions describing pure fluid solubility.
 387 Non-ideality of mixing in the fluid or magma phases can be incorporated by specify-
 388 ing activity and fugacity models. A complete description of these methods, including
 389 all relevant equations, can be found in the Supplement (Supplementary Text S2).

390 3 Workable example uses

391 In this section we detail how to use the various functions available in VESICAL
 392 through worked examples. The python code presented below may be copied and
 393 pasted into a script or can be edited and executed directly within the Jupyter note-
 394 book version of this manuscript. For all examples, code in sections 3.0.2 and 3.1
 395 must be executed to initialize the model and import data from the provided com-
 396 panion excel file. The following sections then may be executed on their own and do
 397 not need to be executed in order.

398 In each example below, a generic “method structure” is given along with def-
 399 initions of unique, required, and optional user inputs. The method structure is

400 simply for illustrative purposes and gives default values for every argument (input).
 401 In some cases, executing the method structure as shown will not produce a sensible
 402 result. For example, the default values for the `plot()` function (Section 3.8) contain
 403 no data, and so no plot would be produced. Users should replace the default values
 404 shown with values corresponding to the samples or conditions of interest.

405 All examples will use the following sample data by default (but this can be
 406 changed by the user):

- 407 • Dataset from `example_data.xlsx` loaded in Section 3.1.1 (variable name `myfile`
 408)
- 409 • Single composition defined in Section 3.1.2 (variable name `mysample`)
- 410 • Sample 10* extracted from `example_data.xlsx` dataset in Section 3.1.3 (vari-
 411 able name `sample_10`)

412 Calculations performed on single samples or on a dataset imported from an
 413 Excel file containing many samples are executed in two distinct ways. Note that sin-
 414 gle sample calculations require that the argument `sample` be defined and are always
 415 appended with `.result` at the end of the function call. Batch calculations are per-
 416 formed on the dataset itself, after that dataset is imported into VESIcal. Thus, the
 417 `sample` argument does not need to be defined discretely, since sample compositional
 418 information is stored within the dataset object. The two basic function calls (i.e.,
 419 how a user would write code to perform a calculation) are:

420 *Single sample calculations*

```
421 myvariable = v.name_of_the_core_calculation(sample=mysample ,
422                                           argument1=value1, argument2
423                                           =value2).result
424
425
```

426 *Batch calculations*

```
427 myvariable = myfile.name_of_the_core_calculation(argument1=value1 ,
428                                                  argument2=value2)
429
430
```

431 where VESIcal has been imported as `v`, `myvariable` is some arbitrary
 432 variable name to which the user wishes to save the calculated output,
 433 `name_of_the_core_calculation` is one of the five core calculations, `mysample` is
 434 a variable containing compositional information in wt% oxides, `myfile` is a variable
 435 containing an `ExcelFile` object created by importing an Excel file, and `argument1`,
 436 `argument2`, `value1`, and `argument2` are two required or optional arguments and
 437 their user-assigned values, respectively.

438 Workable examples detailed here are:

- 439 1. Loading, viewing, and preparing user data
 - 440 1.1 Loading an Excel file
 - 441 1.2 Defining a single sample composition
 - 442 1.3 Plotting user data
 - 443 1.4 Extracting a single sample from an Excel file
 - 444 1.5 Normalizing and transforming data
- 445 2. Calculating dissolved volatile concentrations
- 446 3. Calculating equilibrium fluid compositions

- 447 4. Calculating saturation pressures
 448 5. Calculating and plotting isobars and isopleths
 449 6. Calculating and plotting degassing paths
 450 7. Plotting multiple calculations
 451 8. Comparing results from multiple models
 452 9. Model hybridization (Advanced)
 453 10. Exporting data

454 ***3.0.1 Function arguments and their definitions***

455 Each section below details what arguments are required or optional inputs and
 456 gives examples of how to perform the calculations. Table 2 lists all arguments, both
 457 required and optional, used in the five core calculations. Many of the function argu-
 458 ments have identical form and use across all calculations, and so we list these here.
 459 Any special cases are noted in the section describing that calculation.

460 The most commonly used arguments are:

461 **sample** *Single sample calculations only* The composition of a sample. A single
 462 sample may be passed as a dictionary of values, with compositions of oxides
 463 in wt%. This argument is not needed for batch calculations since they are
 464 performed on ExcelFile objects, which already contain sample information.
 465 See examples for details.

466 **temperature, pressure, and X_fluid**: the temperature in °C, the pressure in
 467 bars, and the mole fraction of H₂O in the H₂O-CO₂ fluid, XH₂O^{fluid}. In all
 468 cases, X_fluid is optional, with a default value of 1 (pure H₂O fluid). Note
 469 that the X_fluid argument is only used for calculation of dissolved volatile
 470 concentrations.

471 *For single sample calculations*

472 Temperature, pressure, and X_fluid should be specified as a numerical value.

473 *For batch calculations*

474 Temperature, pressure, and X_fluid can either be specified as a numerical
 475 value or as strings referring to the names of columns within the Excel file
 476 containing temperature, pressure, or X_fluid values for each sample. If a nu-
 477 merical value is passed for either temperature, pressure, or X_fluid, that will
 478 be the value used for one or all samples. If, alternatively, the user wishes
 479 to use temperature, pressure, and/or X_fluid information in their ExcelFile
 480 object, the title of the column containing temperature, pressure, or X_fluid
 481 data should be passed in quotes (as a string) to **temperature, pressure,**
 482 and/or **X_fluid**, respectively. Note for batch calculations that if temperature,
 483 pressure, or XH₂O^{fluid} information exists in the ExcelFile but a single nu-
 484 merical value is defined for one or both of these variables, both the original
 485 information plus the values used for the calculations will be returned.

486 **verbose**: *Only for single sample calculations.* Always an optional argument
 487 with a default value of False. If set to True, additional values of interest,

488 which were calculated during the main calculation, are returned in addition
 489 to the results of the calculation.

490 **print_status:** *Only for batch calculations.* Always an optional argument,
 491 which sometimes defaults to True and other times defaults to False (see
 492 specific calculation section for details). If set to True, the progress of the cal-
 493 culation will be printed to the terminal. The user may desire to see the status
 494 of the calculation, as some calculations using MagmaSat can be somewhat
 495 slow, particularly for large datasets.

496 **model:** Always an optional argument referring to the name of the desired
 497 solubility model to use. The default is always “MagmaSat”.

Table 2. Matrix of all arguments used in the five core calculations, the nature of the argument (required or optional) and the input type or default value.

	dissolved_volatiles		equilibrium_fluid_comp		saturation_pressure		isobars_isopleths	degassing_path
	SS	Batch	SS	Batch	SS	Batch	SS	SS
sample	wt% oxides		wt% oxides		wt% oxides		wt% oxides	wt% oxides
temperature	°C	°C	°C	°C	°C	°C	°C	°C
pressure	bars	bars	bars	None				'saturation'
pressure_list							bars	
X_fluid	1	1						
isopleth_list							None	
verbose	False		False		False			
model	'MagmaSat'	'MagmaSat'	'MagmaSat'	'MagmaSat'	'MagmaSat'	'MagmaSat'	'MagmaSat'	'MagmaSat'
print_status		True		False		True	True	
smooth_isobars							True	
smooth_isopleths							True	
fractionate_vapor								0.0
init_vapor								0.0

SS = Single-sample. Batch = batch processing. Color of cells corresponds to the type of argument: green=required; orange=optional; gray=argument not used. Values in cells indicate the unit or type of data to input for required arguments or the default value in the case of optional arguments.

3.0.2 Initialize packages

498 For any code using the VESICAL library, the library must be imported for use.
 499 Here we import VESICAL as v. Any time we wish to use a function from VESICAL,
 500 that function must be preceded by 'v.' (e.g., v.calculate_saturation_pressure
 501). Specific examples of this usage follow. Here we also import some other python
 502 libraries that we will be using in the worked examples below.
 503

Input

```

504
505 import VESICAL as v
506 import pandas as pd
507
508
509 #The following are options for formatting this manuscript
510 pd.set_option('display.max_colwidth', 0)
511 from IPython.display import display, HTML
512 %matplotlib inline
513
    
```

3.1 Loading, viewing, and preparing user data

514 All of the following examples will use data loaded in the code cells in this sec-
 515 tion. Both batch processing of data in an Excel file and single-sample processing are
 516 shown. An example file called 'example_data.xlsx' is included with this manuscript.
 517 You can load in your own data by first ensuring that your file is in the same folder
 518 as this notebook and then by replacing the filename in the code cell below with the
 519

520 name of your file. The code cell below must be executed for the examples in the rest
 521 of this section to function properly.

522 **3.1.1 Batch processing**

523 Batch calculations are always facilitated via the `ExcelFile()` class, which the
 524 user uses to specify the filename corresponding to sample data. Loading in data is
 525 as simple as calling `ExcelFile(filename)`. Optionally, `input_type` can be used
 526 to specify whether the oxide data are in wt%, mol fraction, or mol%. Calculations
 527 will always be performed and returned with melt composition in wt% and fluid
 528 composition in mol fraction.

529 **Structure of the input file:** A file containing compositions (and optional
 530 pressure, temperature, or $\text{XH}_2\text{O}^{\text{fluid}}$ information) on one or multiple samples can be
 531 loaded into VESICAL. The loaded file must be a Microsoft Excel file with the exten-
 532 sion `.xls` or `.xlsx`. The file must be laid out in the same manner as the example file
 533 ‘example_data.xlsx’. The basic structure is also shown in Table 3.

534 Any extraneous columns that are not labeled as oxides or input parameters
 535 will be ignored during calculations. The first column titled ‘Label’ contains sample
 536 names. Note that the default assumption on the part of VESICAL is that this column
 537 will be titled ‘Label’. If no ‘Label’ column is found, the first non-oxide column name
 538 will be set as the index column, meaning this is how samples can be accessed by
 539 name (see Section 3.1.3). An index column can be specified by the user using the
 540 argument `label` (see documentation below). The following columns must contain
 541 compositional information as oxides. The only allowable oxides are: SiO_2 , TiO_2 ,
 542 Al_2O_3 , Fe_2O_3 , FeO , Cr_2O_3 , MnO , MgO , CaO , NiO , CoO , Na_2O , K_2O , P_2O_5 , H_2O ,
 543 and CO_2 . Currently, VESICAL can only read these oxide names exactly as written
 544 (e.g., with no leading or trailing spaces and with correct capitalization), but func-
 545 tionality to interpret variations in how these oxides are entered is planned (e.g., such
 546 that “sio2. ” would be understood as “SiO2”). All of these oxides need not be in-
 547 cluded; if for example your samples contain no NiO concentration information, you
 548 can omit the NiO column. Omitted oxide data will be set to 0 wt% concentration.
 549 If other oxide columns not listed here are included in your file, they will be ignored
 550 during calculations. Notably, the order of the columns does not matter, as they are
 551 indexed by name rather than by position. Compositions can be entered either in
 552 wt% (the default), mol%, or mole fraction. If mol% or mole fraction data are loaded,
 553 this must be specified when importing the file.

554 Because VESICAL may misread column headings, we highly recommend that
 555 users examine their data after loading into VESICAL and before performing calcula-
 556 tions. The user data, as it will be used by VESICAL, can be viewed at any time with
 557 `myfile.data` (see generation of Table 3 below).

558 Pressure, temperature, or $\text{XH}_2\text{O}^{\text{fluid}}$ data may optionally be included, if they
 559 are known. Column names for these data do not matter, as they can be specified by
 560 the user as will be shown in following examples.

561 The standard units used by VESICAL are always pressure in bars, temperature
 562 in °C, melt composition as oxides in wt%, and fluid composition as mol fraction
 563 (typically specified as `X.fluid`, the mol fraction of H_2O in an H_2O - CO_2 fluid, ranging
 564 from 0-1). Sample compositions may be translated between wt%, mol%, and mol
 565 fraction if necessary.

566 **Class structure:** `ExcelFile(filename, input_type='wtpercent', label='`
 567 `Label')`

568 **Required inputs:**

569 **filename:** A file name must be passed in quotes. This file must be in the
 570 same folder as the notebook or script that is calling it. This imports the data
 571 from the file name given and saves it to a variable of your choosing.

572 **Optional inputs:** By default, the ExcelFile class assumes that loaded data is in
 573 units of wt%; alternatively, data in mol% or mole fraction may be loaded. In that
 574 case, loaded data is converted into wt% values, since compositions must be in wt%
 575 when performing model calculations.

576 **input_type:** This is optional but must be specified if the data are input in
 577 mol% or mole fraction. In these cases, the data will be converted to wt%
 578 for the calculations. The user can pass `'molpercent'` for data in mol% or
 579 `'molfrac'` for data in mol fraction. The example below includes `input_type=`
 580 `'wtpercent'`. This is actually not necessary if data is in wt% but is included
 581 for clarity.

582 **label:** This is optional but can be specified if the column title referring to
 583 sample names is anything other than “Label”. The default value is “Label”.
 584 If no “Label” column is present and the label argument is not specified, the
 585 first column whose first row is not one of VESICAL’s recognized oxides will be
 586 set as the index column. The index column will be used to select samples by
 587 name.

588 **Outputs:**

589 A special type of python object defined in the VESICAL code known as an
 590 ExcelFile object.

591 **Input**

```
592 myfile = v.ExcelFile('Supplement/Example_Datasets/example_data.xlsx',
593                     input_type='wtpercent')
```

596 Once the ExcelFile object is created and assigned to a variable, the user can
 597 then access the data loaded from their file as `variable.data`. In this example, the
 598 variable corresponding to the ExcelFile object is named `myfile` and so the data
 599 in that file can be accessed with `myfile.data`. Below, `myfile.data` is saved to a
 600 variable we name `data`. The variable `data` is a pandas DataFrame object, which
 601 makes displaying the data itself quite simple and aesthetically pleasing, since pandas
 602 DataFrames mimic spreadsheets.

603 **Input**

```
604 data = myfile.data
605 data
```

608 **Output**

Table 3. User input data: Compositions, pressures, and temperatures for several silicate melts as supplied in the file ‘example_data.xlsx’

Label	CITATION	ROCK TYPE	SiO2	TiO2	Al2O3	Fe2O3	Cr2O3	FeO	MnO	MgO	NiO	CoO	CaO	Na2O	K2O	P2O5	H2O	CO2	Press	Temp
KI3-6_1a	Tucker et al. (2019)	Basalt	48.249207	2.222114	11.692194	0.00	0.0	0.000000	0.079999	14.183817	0.0	0.0	9.892732	1.810522	0.352014	0.210479	0.424695	0.002873	62.5	1299.094712
KI3-6_3a	Tucker et al. (2019)	Basalt	49.295691	2.165357	11.755584	0.00	0.0	0.000000	0.084045	13.403980	0.0	0.0	10.052578	2.208198	0.373328	0.204452	0.425984	0.006786	128.0	1283.419991
KI3-6_4a	Tucker et al. (2019)	Basalt	49.124079	2.360984	12.172833	0.00	0.0	0.000000	0.098809	11.997699	0.0	0.0	10.308188	2.001863	0.396512	0.238996	0.437758	0.004984	124.5	1255.153759
10*	Roggensack (2001)	Basalt	47.960000	0.780000	18.770000	0.00	0.0	10.920000	0.150000	6.860000	0.0	0.0	12.230000	1.850000	0.210000	0.170000	4.500000	0.047900	4000.0	1200.000000
19*	Roggensack (2001)	Basalt	49.640000	0.710000	18.050000	0.00	0.0	10.540000	0.190000	6.430000	0.0	0.0	12.090000	1.980000	0.200000	0.170000	5.100000	0.111300	4000.0	1200.000000
25	Roggensack (2001)	Basalt	50.320000	0.720000	18.030000	0.00	0.0	10.110000	0.140000	5.650000	0.0	0.0	12.780000	1.800000	0.240000	0.230000	5.200000	0.043700	4000.0	1200.000000
SAT-M12-1	Moore et al. (1998)	Andesite	62.600000	0.630000	17.300000	2.01	0.0	2.010000	0.060000	2.650000	0.0	0.0	5.640000	4.050000	1.610000	0.240000	2.620000	0.000000	703.0	1100.000000
SAT-M12-2	Moore et al. (1998)	Andesite	62.600000	0.630000	17.300000	2.01	0.0	2.010000	0.060000	2.650000	0.0	0.0	5.640000	4.050000	1.610000	0.240000	5.030000	0.000000	1865.0	1100.000000
SAT-M12-4	Moore et al. (1998)	Andesite	62.600000	0.630000	17.300000	2.01	0.0	2.010000	0.060000	2.650000	0.0	0.0	5.640000	4.050000	1.610000	0.240000	6.760000	0.000000	2985.0	1050.000000
samp. P1968a	Myers et al. (2019)	Rhyolite	76.974880	0.085516	3.110636	0.00	0.0	4.788883	0.000000	12.549439	0.0	0.0	1.207910	0.138963	1.133084	0.000000	4.340000	0.007000	2000.0	900.000000
samp. P1968b	Myers et al. (2019)	Rhyolite	76.943845	0.133125	3.169657	0.00	0.0	4.763435	0.000000	12.446403	0.0	0.0	1.231728	0.140993	1.170806	0.000000	5.850000	0.012300	2000.0	900.000000
samp. P1968c	Myers et al. (2019)	Rhyolite	77.187205	0.119506	3.167827	0.00	0.0	4.814076	0.000000	12.229534	0.0	0.0	1.184773	0.138201	1.158924	0.000000	5.754571	0.010663	2000.0	900.000000
samp. HPR3-1_XL-3	Mercer et al. (2015)	Rhyolite	75.413966	0.095164	14.077692	0.00	0.0	0.654992	0.125882	0.012003	0.0	0.0	0.636124	3.703110	5.128392	0.000000	5.943750	0.010000	2000.0	0.000000
samp. HPR3-1_XL-4_INCL-1	Mercer et al. (2015)	Rhyolite	76.613586	0.095943	13.476762	0.00	0.0	0.620769	0.113495	0.032069	0.0	0.0	0.624350	3.676972	4.579799	0.000000	5.340000	0.008000	0.0	900.000000
AW-6	Iacovino et al. (2016)	Phonotephrite	48.030000	2.840000	18.120000	0.00	0.0	9.600000	0.230000	3.080000	0.0	0.0	7.570000	6.040000	3.080000	1.410000	1.420000	0.129600	2000.0	1050.000000
AW-46	Iacovino et al. (2016)	Basaltic-Trachyandesite	52.980000	2.180000	20.490000	0.00	0.0	5.540000	0.200000	2.000000	0.0	0.0	7.100000	5.680000	3.160000	0.660000	4.760000	0.343900	4000.0	1000.000000
KI-07	Iacovino et al. (2016)	Basanite	44.610000	4.370000	14.410000	0.00	0.0	10.600000	0.170000	7.690000	0.0	0.0	11.550000	3.930000	1.740000	0.620000	2.900000	0.113100	2000.0	1100.000000

For the rest of this manuscript, data will be pulled from the example_data.xlsx file (Supplemental Dataset S1), which contains compositional information for basalts (Roggensack, 2001; Tucker et al., 2019), andesites (Moore et al., 1998), rhyolites (Mercer et al., 2015; Myers, Wallace, & Wilson, 2019), and alkaline melts (phonotephrite, basaltic-trachyandesite, and basanite from Iacovino, Oppenheimer, Scaillet, and Kyle 2016). Several additional example datasets from the literature are available in the Supplement (Supplementary Datasets S2-S5; Table 4). These include experimentally produced alkaline magmas from Iacovino et al. (2016, alkaline.xlsx), basaltic melt inclusions from Kilauea (Tucker et al., 2019) and Gakkel Ridge (Bennett et al., 2019, basalts.xlsx), basaltic melt inclusions from Cerro Negro volcano, Nicaragua (Roggensack, 2001, cerro_negro.xlsx), and rhyolite melt inclusions from the Taupo Volcanic Center, New Zealand (Myers et al., 2019) and a topaz rhyolite from the Rio Grande Rift (Mercer et al., 2015, rhyolites.xlsx). Where available, the calibration datasets for VESICAL models are also provided (Supplementary Datasets S6-S7).

Input

```
pd.read_excel("tables/Table_Example_Data.xlsx", index_col="Filename")
```

Output

Table 4. Example datasets included with VESICAL

Filename	Explanation	Compositions	Citations
example_data.xlsx	Example data used in this manuscript	Wide comp. range	Iacovino et al. (2016); Mercer et al. (2015); Myers et al. (2019); Roggensack (2001); Tucker et al. (2019)
alkaline.xlsx	Experimental glasses	Basanite to Tephriphonolite	Iacovino et al. (2016)
basalts.xlsx	Melt inclusion glasses	Basaltic	Tucker et al. (2019); Bennett et al. (2019)
cerro_negro.xlsx	Melt inclusion glasses	Basaltic	Roggensack (2001)
rhyolites.xlsx	Melt inclusion glasses	Rhyolitic	Mercer et al. (2015); Myers et al. (2019)

3.1.2 Defining a single sample

More advanced functionality of VESICAL is facilitated directly through the five core calculation classes. Each calculation requires its own unique inputs, but all calculations require that a sample composition be passed. We can pass in a sample either as a python dictionary or pandas Series. Below, we define a sample and name it `mysample`. Oxides are given in wt%. Only the oxides shown here can be used, but

635 not all oxides are required. Any extra oxides (or other information not in the oxide
636 list) the user defines will be ignored during calculations.

637 To manually input a bulk composition, fill in the oxides in wt% below:

638 Input

```
639 mysample = {'SiO2': 77.3,  
640            'TiO2': 0.08,  
641            'Al2O3': 12.6,  
642            'Fe2O3': 0.207,  
643            'Cr2O3': 0.0,  
644            'FeO': 0.473,  
645            'MnO': 0.0,  
646            'MgO': 0.03,  
647            'NiO': 0.0,  
648            'CoO': 0.0,  
649            'CaO': 0.43,  
650            'Na2O': 3.98,  
651            'K2O': 4.88,  
652            'P2O5': 0.0,  
653            'H2O': 6.5,  
654            'CO2': 0.05}
```

657 The oxides considered by VESICAL are:

658 Input

```
659 print(v.oxides)  
660  
661
```

662 Output

```
663 ['SiO2', 'TiO2', 'Al2O3', 'Fe2O3', 'Cr2O3', 'FeO', 'MnO', 'MgO', 'NiO', 'CoO', '  
664 CaO', 'Na2O', 'K2O', 'P2O5', 'H2O', 'CO2']  
665  
666
```

667 *3.1.3 Extracting a single sample from an Excel file*

668 Defined within the `ExcelFile()` class, the method `get_sample_oxide_comp()`
669 allows for the extraction of a melt composition from a loaded excel file.

670 **Method structure:** `myfile.get_sample_oxide_comp(samplename, norm='none')`
671)

672 **Required inputs:**

673 **samplename:** The name of the sample, as a string, as defined in the 'Label'
674 column of the input excel file.

675 **Optional inputs:**

676 **norm:** This is optional and determines the style of normalization performed
677 on a sample. The default value is `'none'`, which returns the value-for-value
678 un-normalized composition. Passing `'standard'` returns the composition
679 normalized to 100%, including any volatiles. Passing `'fixedvolatiles'`
680 normalizes the oxides to 100%, but volatiles remain fixed while other major

681 element oxides are reduced proportionally so that the total is 100 wt%. Pass-
 682 ing 'additionalvolatiles' normalizes oxides to 100% assuming the sample
 683 is volatile-free. If H₂O or CO₂ concentrations are passed to the function,
 684 their un-normalized values will be retained in addition to the normalized
 685 non-volatile oxides, summing to >100%.

686 **Outputs:**

687 The bulk composition stored in a dictionary, with values in wt%.

688 **Input**

```
689 """To get composition from a specific sample in the input data:"""
690 sample_10 = myfile.get_sample_oxide_comp('10*')
691
692
693 """To see the extracted sample composition, uncomment the line below by
694         removing the # and execute this code
695         cell"""
696 #sample_10
697
698 """To see the sum of the composition, uncomment the line below by removing
699         the # and execute this code cell"""
700 #sum(sample_10.values())
701
```

702 In some cases, it may be desired to simply retrieve a sample composition and
 703 use it elsewhere. In case normalization is desired, the 'norm' argument can be used.
 704 To specify a normalization style, for example the 'fixedvolatiles' normalization rou-
 705 tine, the above code could instead be written as:

```
706 sample_10 = myfile.get_sample_oxide_comp('10*', norm='fixedvolatiles')
707
708
```

709 **3.1.4 Normalizing and transforming data**

710 Before performing model calculations on your data, it may be desired to nor-
 711 malize the input composition to a total of 100 wt%. VESICAL has multiple methods
 712 for normalizing sample data using various routines. Normalization can be done auto-
 713 matically when retrieving a single sample from an Excel file, as detailed above. Each
 714 of the normalization routines can be accessed by the user at any time to normalize
 715 either a single sample or all samples in an ExcelFile object.

716 All three normalization functions can take in either a single composition as
 717 a dictionary or multiple compositions either as an ExcelFile object or a pandas
 718 DataFrame object (e.g., myfile or myfile.data). The three normalization routines
 719 are described in the previous section.

720 **Method structures:** `normalize(sample)`, `normalize_FixedVolatiles(sample)`,
 721 `normalize_AdditionalVolatiles(sample)`

722 **Required inputs:**

723 **sample** can be a dictionary containing compositional data for a single sample,
 724 an ExcelFile object containing compositional data for multiple samples, or a
 725 pandas DataFrame object containing compositional data for multiple samples.
 726 Examples are shown for all three cases below.

727 **Outputs:**

728 If a single composition is passed, a dictionary or pandas Series is returned. If
 729 multiple compositions are passed, a pandas DataFrame object is returned.

730 In any of the below examples, `myfile`, `myfile.data`, or `mysample` can all be passed
 731 to any function.

732 **Input**

```
733 """Standard normalization"""
734 standard = v.normalize(myfile)
735 #print(standard)
736
737
738 """FixedVolatiles normalization"""
739 fixed = v.normalize_FixedVolatiles(myfile.data)
740 #print(fixed)
741
742 """AdditionalVolatiles normalization"""
743 additional = v.normalize_AdditionalVolatiles(mysample)
744 #print(additional)
745
```

746 The user may wish to print extracted sample composition to a terminal or
 747 notebook cell to verify that the correct data was extracted. Using the current ex-
 748 ample, this can be done simply by typing `print(sample_10)`. However, VESICAL
 749 also has a built in function to display these values as a table, rather than as a list of
 750 values.

751 The `printTable()` function takes in any python dictionary and converts it
 752 to a pandas DataFrame, which can then be displayed in an aesthetically pleasing
 753 format in Jupyter notebooks.

754 **Method structure: printTable(myDict)**755 **Required inputs:**

756 `myDict` is any python dictionary such as `mysample` or `sample_10`

757 **Outputs:**

758 A pandas DataFrame is returned and printed in an aesthetically pleasing
 759 format.

760 **Input**

```
761 """Execute the following line to print the data as a list of values"""
762 print(sample_10)
763
764
765 """Execute the following line to display Table \ref{table_mysample} and print
766 the data as a table."""
767 v.printTable(sample_10)
768
```

Table 5. Viewing extracted sample composition

	value
SiO2	47.9600
TiO2	0.7800
Al2O3	18.7700
Fe2O3	0.0000
Cr2O3	0.0000
FeO	10.9200
MnO	0.1500
MgO	6.8600
NiO	0.0000
CoO	0.0000
CaO	12.2300
Na2O	1.9500
K2O	0.2100
P2O5	0.1700
H2O	4.5000
CO2	0.0479
Sum oxides	104.5479

3.2 Comparing User Data to Model Calibrations: Which Model Should I Use?

MagmaSat is the most thermodynamically robust model implemented in VESIcal, and thus it is the most generally appropriate model to use (n.b. that it is also the most computationally expensive). However, one of the strengths of VESIcal is its ability to utilize up to seven different solubility models. Each of these models is based on its own calibration dataset, meaning the pressure-temperature-composition space over which models are calibrated is quite variable from model to model. The individual model calibrations are discussed in detail in this manuscript’s companion paper (Wieser et al., in prep).

For the remainder of this section, all example calculations are carried out with MagmaSat, the default model of VESIcal. To use any other VESIcal model, simply add ‘model=’ and the name of the desired model in quotes to any calculation (e.g., `v.calculate_dissolved_volatiles(temperature=900, pressure=1000, model="Dixon")`). The model names recognized by VESIcal are: MagmaSat, ShishkinIdealMixing, Dixon, IaconoMarziano, Liu, AllisonCarbon, and MooreWater. For more advanced use cases such as hybridizing models (see Section 3.9), pure-H₂O and pure-CO₂ models from within a mixed-fluid model can be used by adding ‘Water’ or ‘Carbon’ to the model name (e.g., DixonCarbon; note that MagmaSat does not have this functionality).

Determination of the appropriate model to use with any sample is crucial to the correct application of these models, and so we stress the importance of understanding how a model’s calibration space relates to the sample at hand. VESIcal includes some built-in functionality for comparing melt compositions from user loaded data to those in the datasets upon which each of the VESIcal models is calibrated using the method `calib_plot`. This can be visualized as a total alkalis vs

795 silica (TAS) diagram (Fig. 5a) or as any x-y plot in which x and y are oxides (Fig.
796 5b).

797 **Method structure:** `calib_plot(user_data=None, model='all', plot_type='
798 TAS', zoom=None, save_fig=False)`

799 **Optional inputs:**

800 **user_data:** The default value is None, in which case only the model calibration
801 set is plotted. User provided sample data describing the oxide composition
802 of one or more samples. Multiple samples can be passed as an ExcelFile
803 object or pandas DataFrame. A single sample can be passed as a pandas
804 Series.

805 **model:** The default value is 'all', in which case all model calibration datasets
806 will be plotted. Otherwise, any model can be plotted by passing the name
807 of the model desired (e.g., 'Liu'). Multiple models can be plotted by passing
808 them as strings within a list (e.g., ['Liu', 'Dixon'])

809 **plot_type:** The default value is 'TAS', which returns a total alkalis vs sil-
810 ica (TAS) diagram. Any two oxides can be plotted as an x-y plot by setting
811 `plot_type='xy'` and specifying x- and y-axis oxides, e.g., `x='SiO2', y='Al2O3'`.

812 **zoom:** The default is None in which case axes will be set to the default of
813 $35 \leq x \leq 100$ wt% and $0 \leq y \leq 25$ wt% for TAS type plots and the best values to
814 show the data for xy type plots. The user can pass "user_data" to plot the
815 figure where the x and y axes are scaled down to zoom in and only show the
816 region surrounding the user_data. A list of tuples may be passed to manually
817 specify x and y limits. Pass in data as [(x_min, x_max), (y_min, y_max)]. For
818 example, the default limits here would be passed in as [(35,100), (0,25)].

819 **save_fig:** The default value is False, in which case the plot will be generated
820 and displayed but not saved. If the user wishes to save the figure, the desired
821 filename (including the file extension, e.g., .png) can be passed here. Note
822 that all plots in this Jupyter notebook can be saved by right clicking the plot
823 and choosing "Save Image As...".

824 **Outputs:**

825 A TAS or x-y plot of user data and model calibration data.

826 **Input**

```
827 v.calib_plot(user_data=myfile)
828
829 v.calib_plot(user_data=myfile, model='IaconoMarziano', plot_type='xy', x='
830 SiO2', y='K2O', save_fig=False)
831
```

832 **Output**

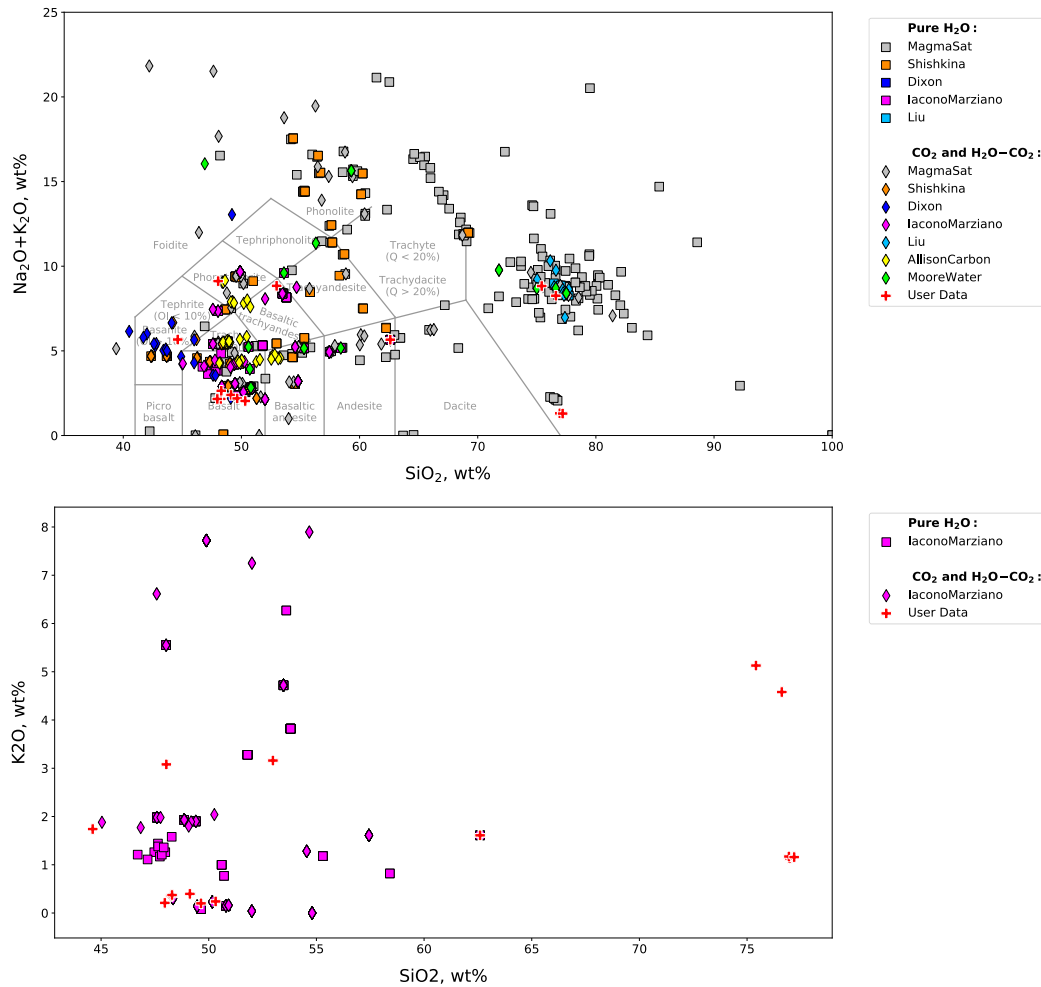


Figure 5. Example calibration plots. a. The default plot with user_data defined as myfile and no other options set. This produces a TAS digram with the user data plotted atop data from calibration datasets for all models. b. A plot with all options specified. This example produces an x-y plot for user_data (myfile) and the Iacono-Marziano calibration dataset where x and y are SiO_2 and K_2O concentration in wt%. Symbol shapes correspond to the volatile composition of experiments used to calibrate the model.

833 Using the functionality built into python and the matplotlib library, user data
 834 can be plotted on its own at any time, including before any calculations are per-
 835 formed. Almost any plot type imaginable can be produced, and users should refer
 836 to the matplotlib documentation (<https://matplotlib.org/3.2.1/index.html>) if
 837 more complex plotting is desired.

838 3.3 Calculating dissolved volatile concentrations

839 The `calculate_dissolved_volatiles()` function calculates the concentration
 840 of dissolved H_2O and CO_2 in the melt at a given pressure-temperature condition and
 841 with a given $\text{H}_2\text{O}-\text{CO}_2$ fluid composition, defined as the mole fraction of H_2O in an
 842 $\text{H}_2\text{O}-\text{CO}_2$ fluid ($X_{\text{H}_2\text{O}}^{\text{fluid}}$). The default MagmaSat model relies on the underlying
 843 functionality of MELTS, whose basic function is to calculate the equilibrium phase

844 assemblage given the bulk composition of the system and pressure-temperature con-
 845 ditions. To calculate dissolved volatile concentrations thus requires computing the
 846 equilibrium state of a system at fixed pressure and temperature over a range of bulk
 847 volatile concentrations until a solution is found that satisfies the user defined fluid
 848 composition.

849 First, the function makes an initial guess at the appropriate bulk volatile con-
 850 centrations by finding the minimum dissolved volatile concentrations in the melt
 851 at saturation, while asserting that the weight fraction of $\text{H}_2\text{O}/(\text{H}_2\text{O}+\text{CO}_2)$ in the
 852 system is equal to the user input mole fraction of $\text{H}_2\text{O}/(\text{H}_2\text{O}+\text{CO}_2)$ in the fluid.
 853 This is done by increasing the H_2O and CO_2 concentrations appropriately until a
 854 fluid phase is stable. Once fluid saturation is determined, the code then performs
 855 directional, iterative, and progressively more refined searches, increasing the pro-
 856 portion of H_2O or CO_2 in the system if the mole fraction of H_2O calculated in the
 857 fluid is greater than or less than that defined by the user, respectively. Four iterative
 858 searches are performed; the precision of the match between the calculated and de-
 859 fined $\text{XH}_2\text{O}^{fluid}$ increases from 0.1 in the first iteration to 0.01, 0.001, and finally to
 860 0.0001. Thus, the calculated dissolved volatile concentrations correspond to a system
 861 with $\text{XH}_2\text{O}^{fluid}$ within 0.0001 of the user defined value.

862 For non-MagmaSat models, dissolved volatile concentrations are calculated
 863 directly from model equations.

864 **Method structure:**

865 Single sample: `calculate_dissolved_volatiles(sample, temperature,`
 866 `pressure, X_fluid=1, verbose=False, model='MagmaSat').result`

867 ExcelFile batch process: `myfile.calculate_dissolved_volatiles(
 868 temperature, pressure, X_fluid=1, print_status=True, model='
 869 MagmaSat')`

870 **Standard inputs:**

871 `sample, temperature, pressure, X_fluid, model` (see Section 3.0.1).

872 **Unique optional inputs:**

873 `verbose`: *Only for single sample calculations.* Default value is False in which
 874 case H_2O and CO_2 concentrations are returned. If set to True, additional
 875 parameters are returned in a dictionary: H_2O and CO_2 concentrations in the
 876 fluid in mole fraction, temperature, pressure, and proportion of the fluid in
 877 the system in wt%.

878 `print_status`: *Only for batch calculations.* The default value is True, in
 879 which case the progress of the calculation will be printed to the terminal. The
 880 user may desire to see the status of the calculation, as this particular function
 881 can be quite slow, averaging between 3-5 seconds per sample.

882 **Calculated outputs:**

883 If a single sample is passed to `sample`, a dictionary with keys 'H2O' and
 884 'CO2' corresponding to the calculated dissolved H_2O and CO_2 concentra-
 885 tions in the melt is returned (plus additional variables 'temperature' in $^\circ\text{C}$,

886 'pressure' in bars, 'XH2O_fl', 'XCO2_fl', and 'FluidProportion_wtper' (the
887 proportion of the fluid in the system in wt%) if **verbose** is set to True).

888 If multiple samples are passed as an ExcelFile object, a pandas DataFrame
889 is returned with sample information plus calculated dissolved H₂O and CO₂
890 concentrations in the melt, the fluid composition in mole fraction, and the
891 proportion of the fluid in the system in wt%. Pressure (in bars) and Temper-
892 ature (in °C) columns are always returned.

893 Input

```
894 """Calculate dissolved volatiles for sample 10*"""
895 v.calculate_dissolved_volatiles(sample=sample_10, temperature=900.0, pressure
896 =2000.0, X_fluid=0.5, verbose=True).
897 result
898
899
```

900 Output

```
901 {'temperature': 900.0,
902  'pressure': 2000.0,
903  'H2O_liq': 2.69352739399806,
904  'CO2_liq': 0.0638439414375309,
905  'XH2O_fl': 0.500092686493868,
906  'XCO2_fl': 0.499907313506132,
907  'FluidProportion_wt': 0.18407321260435108}
908
909
```

910 Input

```
911 """Calculate dissolved for all samples in an ExcelFile object"""
912 dissolved = myfile.calculate_dissolved_volatiles(temperature=900.0, pressure=
913 2000.0, X_fluid=1, print_status=True)
914
915
```

916 Output

```
917 Calculating sample Kil3-6_1a
918 Calculating sample Kil3-6_3a
919 Calculating sample Kil3-6_4a
920 Calculating sample 10*
921 Calculating sample 19*
922 Calculating sample 25
923 Calculating sample SAT-M12-1
924 Calculating sample SAT-M12-2
925 Calculating sample SAT-M12-4
926 Calculating sample samp. P1968a
927 Calculating sample samp. P1968b
928 Calculating sample samp. P1968c
929 Calculating sample samp. HPR3-1_XL-3
930 Calculating sample samp. HPR3-1_XL-4_INCL-1
931 Calculating sample AW-6
932 Calculating sample AW-46
933 Calculating sample KI-07
934
935
```

936 Input

```
937 dissolved
938
939
```

940 Output

Table 6. Modeled dissolved volatile concentrations. *Note: This table has been truncated to display only the results of the calculation. The actual returned table would include all originally input user data in the leftmost columns followed by the calculation results. The complete table can be seen in the Jupyter notebook version of this manuscript.*

	User Input Data	H2O_liq_VESlcal	CO2_liq_VESlcal	Temperature_C_VESlcal	Pressure_bars_VESlcal	X_fluid_input_VESlcal	Model	Warnings
Label								
Kil3-6_1a	--	5.256561	0	900	2000	1	MagmaSat	
Kil3-6_3a	--	5.417720	0	900	2000	1	MagmaSat	
Kil3-6_4a	--	5.353421	0	900	2000	1	MagmaSat	
10*	--	4.984021	0	900	2000	1	MagmaSat	
19*	--	5.134419	0	900	2000	1	MagmaSat	
25	--	5.189068	0	900	2000	1	MagmaSat	
SAT-M12-1	--	5.810439	0	900	2000	1	MagmaSat	
SAT-M12-2	--	5.810439	0	900	2000	1	MagmaSat	
SAT-M12-4	--	5.810439	0	900	2000	1	MagmaSat	
samp. P1968a	--	6.484749	0	900	2000	1	MagmaSat	
samp. P1968b	--	6.473813	0	900	2000	1	MagmaSat	
samp. P1968c	--	6.482109	0	900	2000	1	MagmaSat	
samp. HPR3-1_XL-3	--	6.097630	0	900	2000	1	MagmaSat	
samp. HPR3-1_XL-4_INCL-1	--	6.138658	0	900	2000	1	MagmaSat	
AW-6	--	5.856636	0	900	2000	1	MagmaSat	
AW-46	--	5.879457	0	900	2000	1	MagmaSat	
KI-07	--	4.918430	0	900	2000	1	MagmaSat	

941

3.4 Calculating equilibrium fluid compositions

942

943

944

945

946

947

948

949

The `calculate_equilibrium_fluid_comp()` function calculates the composition of a fluid phase in equilibrium with a given silicate melt with known pressure, temperature, and dissolved H₂O and CO₂ concentrations. The calculation is performed simply by calculating the equilibrium state of the given sample at the given conditions and determining if that melt is fluid saturated. If the melt is saturated, fluid composition and mass are reported back. If the calculation finds that the melt is not saturated at the given pressure and temperature, values of 0.0 will be returned for the H₂O and CO₂ concentrations in the fluid.

950

Method structure:

951

952

```
Single sample: calculate_equilibrium_fluid_comp(sample, temperature,
pressure, verbose=False, model='MagmaSat').result
```

953

954

```
ExcelFile batch process: myfile.calculate_equilibrium_fluid_comp(
temperature, pressure=None, print_status=False, model='MagmaSat')
```

955

Standard inputs:

956

```
sample, temperature, pressure, model (see Section 3.0.1).
```

957

Unique optional inputs:

958 **verbose:** *Only for single sample calculations.* Default value is False, in which
 959 case H₂O and CO₂ concentrations in the fluid in mol fraction are returned.
 960 If set to True, additional parameters are returned in a dictionary: H₂O and
 961 CO₂ concentrations in the fluid, mass of the fluid in grams, and proportion of
 962 the fluid in the system in wt%.

963 **print_status:** *Only for batch calculations.* The default value is False. If True
 964 is passed, the progress of the calculation will be printed to the terminal.

965 **Calculated outputs:**

966 If a single sample is passed to **sample**, a dictionary with keys 'H2O' and
 967 'CO2' is returned (plus additional variables 'FluidMass_grams' and 'FluidPro-
 968 portion_wtper' if **verbose** is set to True).

969 If multiple samples are passed as an ExcelFile object, a pandas DataFrame
 970 is returned with sample information plus calculated equilibrium fluid compo-
 971 sitions, mass of the fluid in grams, and proportion of the fluid in the system
 972 in wt%. Pressure (in bars) and Temperature (in °C) columns are always
 973 returned.

974 **Input**

```
975 """Calculate fluid composition for the extracted sample"""  

976 v.calculate_equilibrium_fluid_comp(sample=sample_10, temperature=900.0,  

977                                 pressure=100.0).result  

978
```

980 **Output**

```
981 {'CO2': 0.00528661429366132, 'H2O': 0.994713385706339}  

982  

983
```

984 Below we calculate equilibrium fluid compositions for all samples at a single
 985 temperature of 900 °C and a single pressure of 1,000 bars. Note that some samples
 986 in this dataset have quite low volatile concentrations (e.g., the Tucker et al. (2019)
 987 basalts from Kilauea), and so are below saturation at this P-T condition. The fluid
 988 composition for undersaturated samples is returned as values of 0 for both H₂O and
 989 CO₂.

990 **Input**

```
991 """Calculate fluid composition for all samples in an ExcelFile object"""  

992 eqfluid = myfile.calculate_equilibrium_fluid_comp(temperature=900.0, pressure  

993                                                 =1000.0)  

994 eqfluid  

995  

996
```

Table 7. Isothermally modeled equilibrium fluid compositions. *Note: this table has been truncated to display only the results of the calculation. The actual returned table would include all originally input user data in the leftmost columns followed by the calculation results. The complete table can be seen in the Jupyter notebook version of this manuscript.*

Label	User Input Data	XH2O_fl_VESICAL	XCO2_fl_VESICAL	Temperature_C_VESICAL	Pressure_bars_VESICAL	Model	Warnings
Kii3-6_1a	--	0.000000	0.000000	900	1000	MagmaSat	Sample not saturated at these conditions
Kii3-6_3a	--	0.000000	0.000000	900	1000	MagmaSat	Sample not saturated at these conditions
Kii3-6_4a	--	0.000000	0.000000	900	1000	MagmaSat	Sample not saturated at these conditions
10*	--	0.984531	0.015469	900	1000	MagmaSat	
19*	--	0.974997	0.025003	900	1000	MagmaSat	
25	--	0.990107	0.009893	900	1000	MagmaSat	
SAT-M12-1	--	1.000000	0.000000	900	1000	MagmaSat	
SAT-M12-2	--	1.000000	0.000000	900	1000	MagmaSat	
SAT-M12-4	--	1.000000	0.000000	900	1000	MagmaSat	
samp. P1968a	--	0.977773	0.022227	900	1000	MagmaSat	
samp. P1968b	--	0.996799	0.003201	900	1000	MagmaSat	
samp. P1968c	--	0.997028	0.002972	900	1000	MagmaSat	
samp. HPR3-1_XL-3	--	0.997770	0.002230	900	1000	MagmaSat	
samp. HPR3-1_XL-4_INCL-1	--	0.997273	0.002727	900	1000	MagmaSat	
AW-6	--	0.261572	0.738428	900	1000	MagmaSat	
AW-46	--	0.897441	0.102559	900	1000	MagmaSat	
KI-07	--	0.826014	0.173986	900	1000	MagmaSat	

Below, we calculate equilibrium fluid compositions for the same dataset using temperatures and pressures as defined in the input data (Table 3). Note that Samples “samp. HPR3-1_XL-3” and “samp. HPR3-1_XL-4_INCL-1” have a user-defined value of 0.0 for temperature and pressure, respectively. VESICAL automatically skips the calculation of equilibrium fluids for these samples and returns a warning to the user, which are both printed to the terminal below and appended to the “Warnings” column in the returned data.

Input

```

1005 """Calculate fluid composition for all samples with unique pressure and
1006         temperature values for each sample.
1007     Pressure and temperature values are taken from columns named "Press" and "
1008         Temp" in the example ExcelFile"""
1009
1010
1011 eqfluid_wtemps = myfile.calculate_equilibrium_fluid_comp(temperature='Temp',
1012         pressure='Press')
1013
1014 eqfluid_wtemps

```

Output

```

1016 UserWarning: Temperature for sample samp. HPR3-1_XL-3 is <=0. Skipping sample.
1017 UserWarning: Pressure for sample samp. HPR3-1_XL-4_INCL-1 is <=0. Skipping sample.
1018
1019

```

Table 8. Modeled equilibrium fluid compositions with unique temperatures. Warnings “Bad temperature” and “Bad pressure” indicate that no data (or 0.0 value data) was given for the temperature or pressure of that sample, in which case the calculation of that sample is skipped. *Note: this table has been truncated to display only the results of the calculation. The actual returned table would include all originally input user data in the leftmost columns followed by the calculation results. The complete table can be seen in the Jupyter notebook version of this manuscript.*

	User Input Data	XH2O_fl_VESICAL	XCO2_fl_VESICAL	Model	Warnings
Label					
Kil3-6_1a	--	0.586164	0.413836	MagmaSat	
Kil3-6_3a	--	0.286160	0.713840	MagmaSat	
Kil3-6_4a	--	0.377439	0.622561	MagmaSat	
10*	--	0.892371	0.107629	MagmaSat	
19*	--	0.918888	0.081112	MagmaSat	
25	--	0.955803	0.044197	MagmaSat	
SAT-M12-1	--	1.000000	0.000000	MagmaSat	
SAT-M12-2	--	1.000000	0.000000	MagmaSat	
SAT-M12-4	--	1.000000	0.000000	MagmaSat	
samp. P1968a	--	0.998764	0.001236	MagmaSat	
samp. P1968b	--	0.998686	0.001314	MagmaSat	
samp. P1968c	--	0.998831	0.001169	MagmaSat	
samp. HPR3-1_XL-3	--	NaN	NaN	MagmaSat	Calculation skipped. Bad temperature.
samp. HPR3-1_XL-4_INCL-1	--	NaN	NaN	MagmaSat	Calculation skipped. Bad pressure.
AW-6	--	0.000000	0.000000	MagmaSat	Sample not saturated at these conditions
AW-46	--	0.492213	0.507787	MagmaSat	
KI-07	--	0.681758	0.318242	MagmaSat	

3.4.1 Converting fluid composition units

The fluid composition is always returned in units of mol fraction. Two functions exist to transform only the H₂O-CO₂ fluid composition between mol fraction and wt% and can easily be applied to returned data sets from calculations. Both functions require that the user provide the dataframe containing fluid composition information plus the names of the columns corresponding to the H₂O and CO₂ concentrations in the fluid. The default values for column names are set to those that may be returned by VESICAL core calculations, such that they need not be specified unless the user has changed them or is supplying their own data (e.g., imported data not processed through a core calculation).

Method structure:

```
Mol fraction to wt%: fluid_molfrac_to_wt(data, H2O_colname='
XH2O_fl_VESICAL', CO2_colname='XCO2_fl_VESICAL')
```

```
Wt% to mol fraction: fluid_wt_to_molfrac(data, H2O_colname='
H2O_fl_wt', CO2_colname='CO2_fl_wt')
```

Required inputs:

1036 data: A pandas DataFrame containing columns for H₂O and CO₂ concentra-
 1037 tions in the fluid.

1038 **Optional inputs:**

1039 H2O_colname and CO2_colname: The default values are 'XH2O_fl' and
 1040 'XCO2_fl' if input data are in mol fraction or 'H2O_fl_wt' and 'CO2_fl_wt'
 1041 if the data are in wt%. Strings containing the name of the columns corre-
 1042 sponding to the H₂O and CO₂ concentrations in the fluid.

1043 **Calculated outputs:**

1044 The original data passed plus newly calculated values are returned in a
 1045 DataFrame.

1046 **Input**

```
1047 """Converting from mol fraction to wt%"""
1048 eqfluid_wt = v.fluid_molfrac_to_wt(eqfluid)
1049 eqfluid_wt
1050
1051
```

Table 9. Equilibrium fluid compositions converted from mol fraction to wt%. *Note: this table has been truncated to display only the results of the calculation. The actual returned table would include all originally input user data in the leftmost columns followed by the calculation results. The complete table can be seen in the Jupyter notebook version of this manuscript.*

	User Input Data	XH2O_fl_VESical	XCO2_fl_VESical	Temperature_C_VESical	Pressure_bars_VESical	Model	Warnings	H2O_fl_wt	CO2_fl_wt
Label									
Kil3-6_1a	--	0.000000	0.000000	900	1000	MagmaSat	Sample not saturated at these conditions		
Kil3-6_3a	--	0.000000	0.000000	900	1000	MagmaSat	Sample not saturated at these conditions		
Kil3-6_4a	--	0.000000	0.000000	900	1000	MagmaSat	Sample not saturated at these conditions		
10*	--	0.984531	0.015469	900	1000	MagmaSat		96.3044	3.69556
19*	--	0.974997	0.025003	900	1000	MagmaSat		94.1062	5.89383
25	--	0.990107	0.009893	900	1000	MagmaSat		97.6179	2.38209
SAT-M12-1	--	1.000000	0.000000	900	1000	MagmaSat		100	0
SAT-M12-2	--	1.000000	0.000000	900	1000	MagmaSat		100	0
SAT-M12-4	--	1.000000	0.000000	900	1000	MagmaSat		100	0
samp. P1968a	--	0.977773	0.022227	900	1000	MagmaSat		94.7402	5.25979
samp. P1968b	--	0.996799	0.003201	900	1000	MagmaSat		99.2217	0.778256
samp. P1968c	--	0.997028	0.002972	900	1000	MagmaSat		99.2773	0.722709
samp. HPR3-1_XL-3	--	0.997770	0.002230	900	1000	MagmaSat		99.457	0.542973
samp. HPR3-1_XL-4_INCL-1	--	0.997273	0.002727	900	1000	MagmaSat		99.3367	0.6633
AW-6	--	0.261572	0.738428	900	1000	MagmaSat		12.6667	87.3333
AW-46	--	0.897441	0.102559	900	1000	MagmaSat		78.1798	21.8202
KI-07	--	0.826014	0.173986	900	1000	MagmaSat		66.0315	33.9685

1052 **Input**

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1055
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1057

```

"""Converting from wt% to mol fraction"""
eqfluid_mol = v.fluid_wt_to_molfrac(eqfluid_wt)
eqfluid_mol

```

Table 10. Equilibrium fluid compositions converted from wt% to mol fraction. *Note: this table has been truncated to display only the results of the calculation. The actual returned table would include all originally input user data in the leftmost columns followed by the calculation results. The complete table can be seen in the Jupyter notebook version of this manuscript.*

Label	User Input Data	XH2O_fl_VESical	XCO2_fl_VESical	Temperature_C_VESical	Pressure_bars_VESical	Model	Warnings	H2O_fl_wt	CO2_fl_wt	XH2O_fl	XCO2_fl
KII3-6_1a	--	0.000000	0.000000	900	1000	MagmaSat	Sample not saturated at these conditions				
KII3-6_3a	--	0.000000	0.000000	900	1000	MagmaSat	Sample not saturated at these conditions				
KII3-6_4a	--	0.000000	0.000000	900	1000	MagmaSat	Sample not saturated at these conditions				
10*	--	0.984531	0.015469	900	1000	MagmaSat		96.3044	3.69556	0.984531	0.0154691
19*	--	0.974997	0.025003	900	1000	MagmaSat		94.1062	5.89383	0.974997	0.0250027
25	--	0.990107	0.009893	900	1000	MagmaSat		97.6179	2.38209	0.990107	0.0098927
SAT-M12-1	--	1.000000	0.000000	900	1000	MagmaSat		100	0	1	0
SAT-M12-2	--	1.000000	0.000000	900	1000	MagmaSat		100	0	1	0
SAT-M12-4	--	1.000000	0.000000	900	1000	MagmaSat		100	0	1	0
samp. P1968a	--	0.977773	0.022227	900	1000	MagmaSat		94.7402	5.25979	0.977773	0.0222267
samp. P1968b	--	0.996799	0.003201	900	1000	MagmaSat		99.2217	0.778256	0.996799	0.0032013
samp. P1968c	--	0.997028	0.002972	900	1000	MagmaSat		99.2773	0.722709	0.997028	0.00297183
samp. HPR3-1_XL-3	--	0.997770	0.002230	900	1000	MagmaSat		99.457	0.542973	0.99777	0.00223037
samp. HPR3-1_XL-4_INCL-1	--	0.997273	0.002727	900	1000	MagmaSat		99.3367	0.6633	0.997273	0.00272658
AW-6	--	0.261572	0.738428	900	1000	MagmaSat		12.6667	87.3333	0.261572	0.738428
AW-46	--	0.897441	0.102559	900	1000	MagmaSat		78.1798	21.8202	0.897441	0.102559
KI-07	--	0.826014	0.173986	900	1000	MagmaSat		66.0315	33.9685	0.826014	0.173986

1058

3.5 Calculating saturation pressures

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The `calculate_saturation_pressure()` function calculates the minimum pressure at which a given silicate melt with known temperature and H₂O and CO₂ concentrations would be saturated with fluid. For MagmaSat, this is calculated by finding the pressure at which the smallest amount of vapor is present. This function also calculates the composition of the vapor in equilibrium with the melt at those conditions.

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The function works by calculating the equilibrium state of the given melt at very high pressure (20,000 bars) and then decreasing the pressure in steps of 1,000 bars until the mass of vapor is >0 grams. At this point, the pressure space is narrowed and searched in steps of 100 bars and then in steps of 10 bars until the saturation pressure is found. Thus, these calculations are accurate to 10 bars.

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For non-MagmaSat models, saturation pressure is calculated by repeatedly calculating the dissolved volatile concentration over a range of pressures and minimizing the difference between this computed concentration and the given concentration. This is only practical for non-MagmaSat models, where the dissolved volatiles calculation is extremely fast.

1075 **Method structure:**

1076 Single sample: `calculate_saturation_pressure(sample, temperature,`
 1077 `verbose=False, model='MagmaSat').result`

1078 ExcelFile batch process: `myfile.calculate_saturation_pressure(`
 1079 `temperature, print_status=True, model='MagmaSat')`

1080 **Standard inputs:**

1081 `sample, temperature, model` (see Section 3.0.1).

1082 **Unique optional inputs:**

1083 `verbose`: *Only for single sample calculations.* Default value is False in which
 1084 case the saturation pressure in bars is returned. If set to True, additional
 1085 parameters are returned in a dictionary: saturation pressure in bars, H₂O and
 1086 CO₂ concentrations in the fluid, mass of the fluid in grams, and proportion of
 1087 the fluid in the system in wt%.

1088 `print_status`: *Only for batch calculations.* The default value is True, in
 1089 which case the progress of the calculation will be printed to the terminal.

1090 **Calculated outputs:**

1091 If a single sample is passed to `sample`, the saturation pressure in bars is
 1092 returned as a numerical value (float) (plus additional variables 'XH2O_fl',
 1093 'XCO2_fl', 'FluidMass_grams', and 'FluidProportion_wtper' if `verbose` is set
 1094 to True).

1095 If multiple samples are passed as an ExcelFile object, a pandas DataFrame
 1096 is returned with sample information plus calculated saturation pressures,
 1097 equilibrium fluid compositions, mass of the fluid in grams, and proportion of
 1098 the fluid in the system in wt%. Temperature (in °C) is always returned.

1099 **Input**

```
1100 """Calculate the saturation pressure of the single sample we defined in
1101 Section 3.1.2 at 925 degrees C"""
1102 v.calculate_saturation_pressure(sample=mysample, temperature=925.0, verbose=
1103 True).result
1104
```

1106 **Output**

```
1107 {'SaturationP_bars': 2720,
1108 'FluidMass_grams': 0.0016655984224872,
1109 'FluidProportion_wt': 0.0015635017577088073,
1110 'XH2O_fl': 0.825802671679744,
1111 'XCO2_fl': 0.174197328320256}
1112
```

1114 **Input**

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```

"""Calculate the saturation pressure for all samples in an ExcelFile object
    at 925 degrees C"""
satPs = myfile.calculate_saturation_pressure(temperature=925.0)
satPs
    
```

Table 11. Isothermally modeled saturation pressures. *Note: this table has been truncated to display only the results of the calculation. The actual returned table would include all originally input user data in the leftmost columns followed by the calculation results. The complete table can be seen in the Jupyter notebook version of this manuscript.*

Label	User Input Data	SaturationP_bars_VESlcal	Temperature_C_VESlcal	XH2O_fl_VESlcal	XCO2_fl_VESlcal	FluidMass_grams_VESlcal	FluidSystem_wt_VESlcal	Model	Warnings
Kil3-6_1a	--	80	925	0.439592	0.560408	0.000026	0.000029	MagmaSat	
Kil3-6_3a	--	140	925	0.248725	0.751275	0.000620	0.000696	MagmaSat	
Kil3-6_4a	--	120	925	0.303412	0.696588	0.000332	0.000372	MagmaSat	
10*	--	2370	925	0.785443	0.214557	0.001277	0.001221	MagmaSat	
19*	--	3430	925	0.685666	0.314334	0.000226	0.000215	MagmaSat	
25	--	2580	925	0.825858	0.174142	0.000899	0.000854	MagmaSat	
SAT-M12-1	--	540	925	1.000000	0.000000	0.005197	0.005125	MagmaSat	
SAT-M12-2	--	1490	925	1.000000	0.000000	0.015744	0.015163	MagmaSat	
SAT-M12-4	--	2340	925	1.000000	0.000000	0.000981	0.000929	MagmaSat	
samp. P1968a	--	1030	925	0.970939	0.029061	0.005539	0.005308	MagmaSat	
samp. P1968b	--	1640	925	0.970540	0.029460	0.003193	0.003016	MagmaSat	
samp. P1968c	--	1590	925	0.972952	0.027048	0.000828	0.000783	MagmaSat	
samp. HPR3-1_XL-3	--	1920	925	0.946905	0.053095	0.001085	0.001026	MagmaSat	
samp. HPR3-1_XL-4_INCL-1	--	1600	925	0.947015	0.052985	0.002230	0.002120	MagmaSat	
AW-6	--	1200	925	0.229039	0.770961	0.000322	0.000317	MagmaSat	
AW-46	--	4640	925	0.439714	0.560286	0.000411	0.000391	MagmaSat	
KI-07	--	1450	925	0.678808	0.321192	0.002972	0.002886	MagmaSat	

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Input

```

"""Calculate the saturation pressure for all samples in an ExcelFile object,
    taking temperature
    values from a column named "Temp" in the ExcelFile"""
satPs_wtemps = myfile.calculate_saturation_pressure(temperature="Temp")
satPs_wtemps
    
```

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Output

```

Calculating sample Kil3-6_1a
Calculating sample Kil3-6_3a
Calculating sample Kil3-6_4a
Calculating sample 10*
Calculating sample 19*
Calculating sample 25
Calculating sample SAT-M12-1
Calculating sample SAT-M12-2
Calculating sample SAT-M12-4
Calculating sample samp. P1968a
Calculating sample samp. P1968b
Calculating sample samp. P1968c
    
```

```

1143 Calculating sample samp. HPR3-1_XL-3
1144 Calculating sample samp. HPR3-1_XL-4_INCL-1
1145 UserWarning: Temperature for sample samp. HPR3-1_XL-3 is <=0. Skipping sample.
1146 Calculating sample AW-6
1147 Calculating sample AW-46
1148 Calculating sample KI-07
1149 Done!
1150

```

Table 12. Modeled saturation pressures with unique temperatures. The warning “Bad temperature” indicates that no data (or 0.0 value data) was given for the temperature of that sample, in which case the calculation of that sample is skipped. *Note: this table has been truncated to display only the results of the calculation. The actual returned table would include all originally input user data in the leftmost columns followed by the calculation results. The complete table can be seen in the Jupyter notebook version of this manuscript.*

Label	User Input Data	SaturationP_bars _VESical	XH2O_fl _VESical	XCO2_fl _VESical	FluidMass_grams _VESical	FluidSystem_wt _VESical	Model	Warnings
KI13-6_1a	--	70	0.525553	0.474447	0.000710314	0.000797025	MagmaSat	
KI13-6_3a	--	130	0.281991	0.718009	0.000449053	0.00050435	MagmaSat	
KI13-6_4a	--	110	0.344636	0.655364	0.000370296	0.000415397	MagmaSat	
10*	--	2400	0.807034	0.192966	0.00029124	0.00027857	MagmaSat	
19*	--	3440	0.710745	0.289255	0.000584324	0.000555328	MagmaSat	
25	--	2660	0.845161	0.154839	0.000211825	0.000201233	MagmaSat	
SAT-M12-1	--	560	1	0	0.0229218	0.0226009	MagmaSat	
SAT-M12-2	--	1560	1	0	0.00331538	0.00319308	MagmaSat	
SAT-M12-4	--	2390	1	0	0.0186879	0.0177036	MagmaSat	
samp. P1968a	--	1020	0.971529	0.0284714	0.00694889	0.00666009	MagmaSat	
samp. P1968b	--	1630	0.970816	0.0291835	0.00258244	0.00243943	MagmaSat	
samp. P1968c	--	1580	0.973228	0.0267722	0.000412392	0.000389913	MagmaSat	
samp. HPR3-1_XL-3	--						MagmaSat	Calculation skipped. Bad temperature.
samp. HPR3-1_XL-4_INCL-1	--	1600	0.947004	0.0529965	0.00234923	0.0022335	MagmaSat	
AW-6	--	1270	0.224501	0.775499	4.1948e-05	4.13078e-05	MagmaSat	
AW-46	--	4740	0.441496	0.558504	0.000345244	0.00032851	MagmaSat	
KI-07	--	1530	0.673211	0.326789	0.0032638	0.00316864	MagmaSat	

1151 3.6 Calculating isobars and isopleths

1152 In this example, we demonstrate how isobars (lines of constant pressure) and
1153 isopleths (lines of constant fluid composition) can be calculated for any one com-
1154 position. A single melt composition can be extracted from a loaded excel file, or a
1155 composition can be entered by hand and stored within a dictionary. Due to com-
1156 putational intensity, isobars and isopleths can only be computed for one sample
1157 composition at a time.

1158 Once a single composition is defined, conditions over which to calculate isobars
1159 and isopleths must be specified. The generated plot is isothermal, so only one tem-
1160 perature can be chosen. Isobars and isopleths can be calculated for any number of
1161 pressures or $\text{XH}_2\text{O}^{fluid}$ values, respectively, passed as lists.

1162 The calculation is performed by iterating through possible concentrations of
1163 H_2O and CO_2 and calculating the equilibrium state for the system. The iteration
1164 begins at a fixed H_2O concentration, increasing the CO_2 concentration in steps of
1165 0.1 wt% until a fluid phase is stable. The H_2O concentration is then increased by 0.5

1166 wt% and CO₂ is again increased from 0 until a fluid phase is stable. This process is
 1167 repeated for H₂O values ranging from 0–15 wt%. The H₂O and CO₂ concentrations
 1168 from each system for which a fluid phase was found to be stable are saved and writ-
 1169 ten to a pandas DataFrame, which is returned upon completion of the calculation.

1170 Isobars and isopleths are computed at fixed H₂O-CO₂ points for any given
 1171 pressure. To generate curves using the MagmaSat model, polynomials are fit to
 1172 computed points using numpy’s polyfit method. This can be optionally disabled
 1173 by setting `smooth_isobars` or `smooth_isopleths` to False. The curvature of the
 1174 isobars depends strongly on the number of points used to fit a polynomial, deemed
 1175 “control points”, with curve fits becoming more accurate to the model as the num-
 1176 ber of control points increases. We found that above five control points, changes
 1177 to the shape of the curve fits becomes negligible. Thus, as a compromise between
 1178 accuracy and computation time, and to maintain consistency, MagmaSat isobars are
 1179 always computed with 5 control points at XH₂O^{fluid} values of 0, 0.25, 0.5, 0.75, and
 1180 1. Because non-MagmaSat models compute extremely quickly, all non-MagmaSat
 1181 models use 51 control points per isobar and do not utilize polynomial fits to the data
 1182 by default.

1183 **Method structure:**

```
1184 Only single sample calculations. calculate_isobars_and_isopleths(sample
1185     , temperature, pressure_list, isopleth_list=None, smooth_isobars=
1186     True, smooth_isopleths=True, print_status=True, model="MagmaSat").
1187     result
```

1188 **Standard inputs:**

1189 `sample`, `temperature`, `model` (see Section 3.0.1).

1190 **Unique required inputs:**

1191 `pressure_list`: A list of all pressures in bars at which to calculate isobars. If
 1192 only one value is passed it can be as float instead of list.

1193 **Unique optional inputs:**

1194 `isopleth_list`: The default value is None in which case only isobars will
 1195 be calculated. A list of all fluid composition values, in mole fraction H₂O
 1196 (XH₂O^{fluid}), at which to calculate isopleths. Values can range from 0–1. If
 1197 only one value is passed it can be as float instead of list. N.b. that, due to
 1198 the method of isobar smoothing using control points as outlined above, each
 1199 isopleth value passed here not equal to one of the five standard control point
 1200 values (0, 0.25, 0.5, 0.75, or 1) will result in an an additional control point
 1201 being used to smooth the isobars. Thus, entering additional isopleth values
 1202 results not only in more isopleth outputs but also in “smoother” (i.e., more
 1203 well constrained) isobars.

1204 `smooth_isobars` and `smooth_isopleths`: The default value for both of these
 1205 arguments is True, in which case polynomials will be fit to the computed data
 1206 points.

1207 `print_status`: The default value is True. If True, the progress of the calcula-
 1208 tions will be printed to the terminal.

1209 Calculated outputs:

1210 The function returns two pandas DataFrames: the first has isobar data, and
 1211 the second has isopleth data. Columns in the isobar dataframe are ‘Pressure’,
 1212 ‘H2O_{melt}’, and ‘CO₂_{melt}’, corresponding to pressure in bars and dissolved
 1213 H₂O and CO₂ in the melt in wt%. Columns in the isopleth dataframe are
 1214 ‘XH₂O_{fl}’, ‘H₂O_{liq}’, and ‘CO₂_{liq}’, corresponding to XH₂O^{fluid} and dis-
 1215 solved H₂O and CO₂ in the melt in wt%.

1216 Input

```
1217 """Define all variables to be passed to the function for calculating isobars
1218 and isopleths"""
1219
1220 """Define the temperature in degrees C"""
1221 temperature = 1200.0
1222
1223 """Define a list of pressures in bars: """
1224 pressures = [1000.0, 2000.0, 3000.0]
1225
```

1226 Next, the H₂O and CO₂ dissolved in the melt at saturation is calculated at the
 1227 specified temperature and over the range of specified pressures. Note that, because
 1228 this function calculates two things (isobars and isopleths), two variable names must
 1229 be given (below, “isobars, isopleths”). This calculation can be quite slow, and so it
 1230 is recommended to set `print_status` to True.

1231 Input

```
1232 isobars, isopleths = v.calculate_isobars_and_isopleths(sample=sample_10,
1233 temperature=temperature, pressure_list
1234 =pressures, isopleth_list=[0.25,0.5,0.
1235 75]).result
1236
1237
```

1238 Output

```
1239 Calculating isobar at 1000.0 bars
1240 Calculating isobar control point at XH2Ofluid = 0
1241 Calculating isopleth at XH2Ofluid = 0.25
1242 Calculating isopleth at XH2Ofluid = 0.5
1243 Calculating isopleth at XH2Ofluid = 0.75
1244 Calculating isobar control point at XH2Ofluid = 1
1245 Calculating isobar at 2000.0 bars
1246 Calculating isobar control point at XH2Ofluid = 0
1247 Calculating isopleth at XH2Ofluid = 0.25
1248 Calculating isopleth at XH2Ofluid = 0.5
1249 Calculating isopleth at XH2Ofluid = 0.75
1250 Calculating isobar control point at XH2Ofluid = 1
1251 Calculating isobar at 3000.0 bars
1252 Calculating isobar control point at XH2Ofluid = 0
1253 Calculating isopleth at XH2Ofluid = 0.25
1254 Calculating isopleth at XH2Ofluid = 0.5
1255 Calculating isopleth at XH2Ofluid = 0.75
1256 Calculating isobar control point at XH2Ofluid = 1
1257
```

1258

Done!

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3.7 Calculating degassing paths

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A degassing path is a series of volatile concentrations both in the melt and fluid that a magma will follow during decompression. In the calculation, the saturation pressure is computed, and then the system is equilibrated along a trajectory of decreasing pressure values at discrete steps. The default number of steps to calculate is 50, but this can be defined by the user by setting the argument `steps` to any integer value. A detailed explanation of how non-MagmaSat models handle the calculation of mixed-fluid composition can be found in the supplement (Supplementary Text S2). If so desired, this calculation can be performed for any initial pressure, but the default is the saturation pressure. If a pressure is specified that is above the saturation pressure, the calculation will simply proceed from the saturation pressure, since the magma cannot degas until it reaches saturation.

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Completely open-system, completely closed-system or partially open-system degassing paths can be calculated by specifying what proportion of the fluid to fractionate. The fluid fractionation value can range between 0 (closed-system: no fluid is removed, all is retained at each pressure step) and 1 (open-system: all fluid is removed, none is retained at each pressure step). Closed and partially open-system runs allow the user to specify the initial presence of exsolved fluid that is in equilibrium with the melt at the starting pressure.

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Method structure:

1280

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1282

```
Only single-sample calculations. calculate_degassing_path(sample,
    temperature, pressure='saturation', fractionate_vapor=0.0,
    init_vapor=0.0, steps=50, model='MagmaSat').result
```

1283

Standard inputs:

1284

`sample`, `temperature`, `model` (see Section 3.0.1).

1285

Unique optional inputs:

1286

1287

1288

1289

1290

pressure: The pressure at which to begin the degassing calculations, in bars. Default value is 'saturation', which runs the calculation with the initial pressure at the saturation pressure. If a pressure greater than the saturation pressure is input, the calculation will start at saturation, since this is the first pressure at which any degassing will occur.

1291

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1298

fractionate_vapor: Proportion of vapor removed at each pressure step. Default value is 0.0 (completely closed-system degassing). Specifies the type of calculation performed, either closed system (0.0) or open system (1.0) degassing. If any value between <1.0 is chosen, user can also specify the 'init_vapor' argument (see below). A value in between 0 and 1 will remove that proportion of vapor at each step. For example, for a value of 0.2, the calculation will remove 20% of the vapor and retain 80% of the vapor at each pressure step.

1299

1300

init_vapor: Default value is 0.0. Specifies the amount of vapor (in wt%) coexisting with the melt before degassing.

1301 **steps:** Default value is 50. Specifies the number of steps in pressure space at
 1302 which to calculate dissolved volatile concentrations.

1303 **Calculated outputs:**

1304 The function returns a pandas DataFrame with columns as: 'Pressure_bars',
 1305 'H2O_liq' and 'CO2_liq' (the concentration of H₂O and CO₂ in the melt,
 1306 in wt%), 'XH2O_fl' and 'XCO2_fl' (the composition of the H₂O-CO₂ fluid,
 1307 in mol fraction), and 'FluidProportion_wt' (the proportion of fluid in the
 1308 fluid-melt system, in wt%).

1309 **Input**

```

1310 temp = 1200 #temperature in degrees C
1311
1312
1313 """Calculate open, closed, and closed + 2 wt% initial vapor"""
1314 closed_df = v.calculate_degassing_path(sample=sample_10, temperature=temp).
1315             result
1316 open_df = v.calculate_degassing_path(sample=sample_10, temperature=temp,
1317                                     fractionate_vapor=1.0).result
1318 half_df = v.calculate_degassing_path(sample=sample_10, temperature=temp,
1319                                     fractionate_vapor=0.5).result
1320 exsolved_df = v.calculate_degassing_path(sample=sample_10, temperature=temp,
1321                                         init_vapor=2.0).result
1322
1323 """Calculate closed-system degassing starting from a pressure of 2000 bars"""
1324 start2000_df = v.calculate_degassing_path(sample=sample_10, temperature=temp,
1325                                           pressure=2000.0).result
1326

```

1327 **3.8 Plotting**

1328 After calculating isobars, isopleths, and degassing paths, any or all of these
 1329 may be plotted in an H₂O versus CO₂ plot with one simple function call. The
 1330 plot will be printed directly in the notebook or, if the code is run as script in a
 1331 command line, the plot will appear in its own window, at which point it can be
 1332 saved as an image file. VESICAL's `plot` function takes in lists of pandas DataFrames
 1333 with calculated isobar, isopleth, and degassing path information (e.g., output from
 1334 `calculate_isobars_and_isopleths` or `calculate_degassing_path()`) and plots
 1335 data as isobars (lines of constant pressure), isopleths (lines of constant fluid compo-
 1336 sition), and degassing paths (lines indicating the concentrations of H₂O and CO₂ in
 1337 a melt equilibrated along a path of decreasing pressure).

1338 Labels can be assigned to isobars, isopleths, and/or degassing paths separately.
 1339 Any or all of these data can be passed to the `plot` function. Multiple sets of plot-
 1340 table data can be passed. For example, isobars calculated with two different models
 1341 can be passed to the `isobars` argument as a list.

1342 VESICAL's plotting function is entirely based on python's matplotlib library,
 1343 which comes standard with many installations of python. With matplotlib, users
 1344 can create an almost immeasurable variety of plots (note that direct matplotlib
 1345 functionality is used to create custom plots in several of this manuscript's supple-
 1346 mentary Jupyter notebooks), and users should refer to the matplotlib documentation
 1347 (<https://matplotlib.org/3.2.1/index.html>) if more complex plotting is desired.
 1348 If preferred, VESICAL outputs can be saved to an excel file (see Section 3.10), and
 1349 plotting can be done in any plotting program desired (e.g., MS Excel).

1350 **Method structure:**

```

1351     plot(isobars=None, isopleths=None, degassing_paths=None, custom_H2O
1352          =None, custom_CO2=None, isobar_labels=None, isopleth_labels=None
1353          , degassing_path_labels=None, custom_labels=None, custom_colors=
1354          "VESIcal", custom_symbols=None, markersize=10, save_fig=False,
1355          extend_isobars_to_zero=True, smooth_isobars=False, smooth_isopleths
1356          =False)

```

1357 **Optional inputs:**

1358 **isobars:** DataFrame object containing isobar information as calculated by
 1359 `calculate_isobars_and_isopleths()`. Or a list of DataFrame objects.

1360 **isopleths:** DataFrame object containing isopleth information as calculated
 1361 by `calculate_isobars_and_isopleths()`. Or a list of DataFrame objects.

1362 **degassing_paths:** List of DataFrames with degassing information as gener-
 1363 ated by `calculate_degassing_path()`.

1364 **custom_H2O:** List of groups of H₂O concentration values to plot as points. For
 1365 example `myfile.data['H2O']` is one group of H₂O values. Must be passed
 1366 with `custom_CO2` and must be same length as `custom_CO2`.

1367 **custom_CO2:** List of groups of CO₂ values to plot as points. For example
 1368 `myfile.data['CO2']` is one group of CO₂ values. Must be passed with
 1369 `custom_H2O` and must be same length as `custom_H2O`.

1370 **isobar_labels:** Labels for the plot legend. Default is None, in which case
 1371 each plotted line will be given the generic legend name of “Isobars n”, with
 1372 n referring to the nth isobars passed. Isobar pressure is given in parentheses.
 1373 The user can pass their own labels as a list of strings. If more than one set
 1374 of isobars is passed, the labels should refer to each set of isobars, not each
 1375 pressure.

1376 **isopleth_labels:** Labels for the plot legend. Default is None, in which case
 1377 each plotted isopleth will be given the generic legend name of “Isopleth n”,
 1378 with n referring to the nth isopleths passed. Isopleth XH₂O values are given
 1379 in parentheses. The user can pass their own labels as a list of strings. If
 1380 more than one set of isopleths is passed, the labels should refer to each set of
 1381 isopleths, not each XH₂O value.

1382 **degassing_path_labels:** Labels for the plot legend. Default is None,
 1383 in which case each plotted line will be given the generic legend name of
 1384 “Pathn”, with n referring to the nth degassing path passed. The user can
 1385 pass their own labels as a list of strings.

1386 **custom_labels:** Labels for the plot legend. Default is None, in which case
 1387 each group of custom points will be given the generic legend name of “Cus-

1388 tomn”, with n referring to the nth degassing path passed. The user can pass
1389 their own labels as a list of strings.

1390 **custom_colors** and **custom_symbols**: Custom colors and symbol shapes can
1391 be specified for (**custom_H2O**, **custom_CO2**) points. A list of color values or
1392 symbol types readable by Matplotlib (see Matplotlib documentation) can be
1393 entered. The length of this list must be equal to the lengths of **custom_H2O**
1394 and **custom_CO2**. If nothing is specified for **custom_colors**, VESICAL’s default
1395 colors will be used. If nothing is specified for **custom_symbols**, all points will
1396 be plotted as filled circles.

1397 **markersize**: The size of the symbols can be specified here. If not specified,
1398 the default value is marker size 10.

1399 **save_fig**: Default value is False, in which case the figure will not be saved.
1400 If a string is passed, the figure will be saved with the string as the filename.
1401 The string must include the file extension.

1402 **Advanced inputs:** Most users will not need to use these inputs.

1403 **extend_isobars_to_zero**: If set to True (the default), isobars will be ex-
1404 tended to the plot axes, which are at x=0 and y=0, even if there is a finite
1405 solubility at zero partial pressure.

1406 **smooth_isobars** and **smooth_isopleths**: If set to True, isobar or iso-
1407 pleth data will be fit to a polynomial and plotted. If set to False (the
1408 default), the raw input data will be plotted. Note that MagmaSat
1409 **calculate_isobars_and_isopleths()** calculations return already
1410 “smoothed” data (that is, the raw data are fit to polynomials before be-
1411 ing returned). Raw “unsmoothed” data can be returned by MagmaSat
1412 **calculate_isobars_and_isopleths()** (see documentation on this method).

1413 **Calculated outputs:**

1414 The function returns a plot with x-axis as H₂O wt% in the melt and y-axis
1415 as CO₂ wt% in the melt. Isobars, or lines of constant pressure at which the
1416 sample magma composition is saturated, and isopleths, or lines of constant
1417 fluid composition at which the sample magma composition is saturated, are
1418 plotted if passed. Degassing paths, or the concentration of dissolved H₂O and
1419 CO₂ in a melt equilibrated along a path of decreasing pressure, is plotted if
1420 passed.

1421 *3.8.1 A simple example: Isobars and isopleths*

1422 Input

```
1423 v.plot(isobars=isobars, isopleths=isopleths)
```

1426 Output

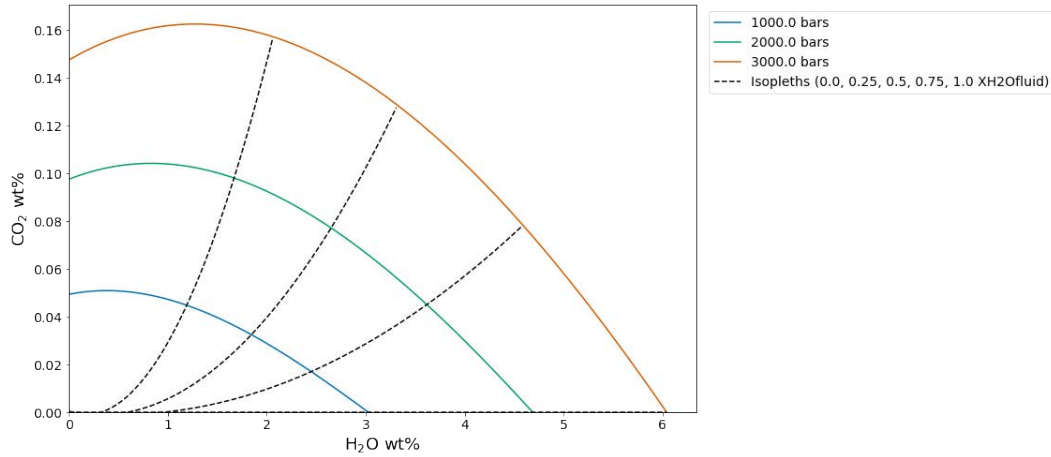


Figure 6. Isobars and isopleths calculated for the sample, temperature, pressures, $\text{XH}_2\text{O}^{fluid}$ values, and with the model as defined in Section 3.6. Manuscript default values are sample ‘10*’ at a 1,200 °C with isobars at 1,000, 2,000, and 3,000 bars, isopleths at $\text{XH}_2\text{O}^{fluid} = 0, 0.25, 0.5, 0.75, \text{ and } 1$ calculated with MagmaSat

1427 When plotting isobars and isopleths via MagmaSat, the values calculated by
 1428 `calculate_isobars_and_isopleths()` are used to calculate polynomial fits using
 1429 numpy’s ‘polyfit’. These polynomial fits, not the raw calculated data, are what have
 1430 been plotted above. This method of fitting polynomial curves to these data is com-
 1431 mon in the literature (e.g., Newman & Lowenstern, 2002; IaconoMarziano et al.,
 1432 2012; Iacovino et al., 2013) and is likely a very close approximation of the true sat-
 1433 uration surface. Non-MagmaSat models do not calculate polynomial fits by default,
 1434 but this can be done by passing `smooth_isobars=True` and `smooth_isopleths=`
 1435 `True` to `plot()`.

1436 A user may wish to apply custom formatting to the plot, in which case the
 1437 polynomial fits can be calculated and returned as a pandas DataFrame, which the
 1438 user can then plot up manually using Matplotlib, excel, or some other preferred
 1439 method. To calculate polynomial fits to isobar and isopleth data, isobars and iso-
 1440 pleths can be passed to `smooth_isobars_and_isopleths()`. For this advanced case,
 1441 we refer the reader to the documentation.

1442 *3.8.2 A simple example: Degassing paths*

1443 Input

```
1444 v.plot(degassing_paths=[open_df, half_df, closed_df, exsolved_df],
1445        degassing_path_labels=["Open", "Half",
1446                              "Closed", "Exsolved"])
1447
1448
```

1449 Output

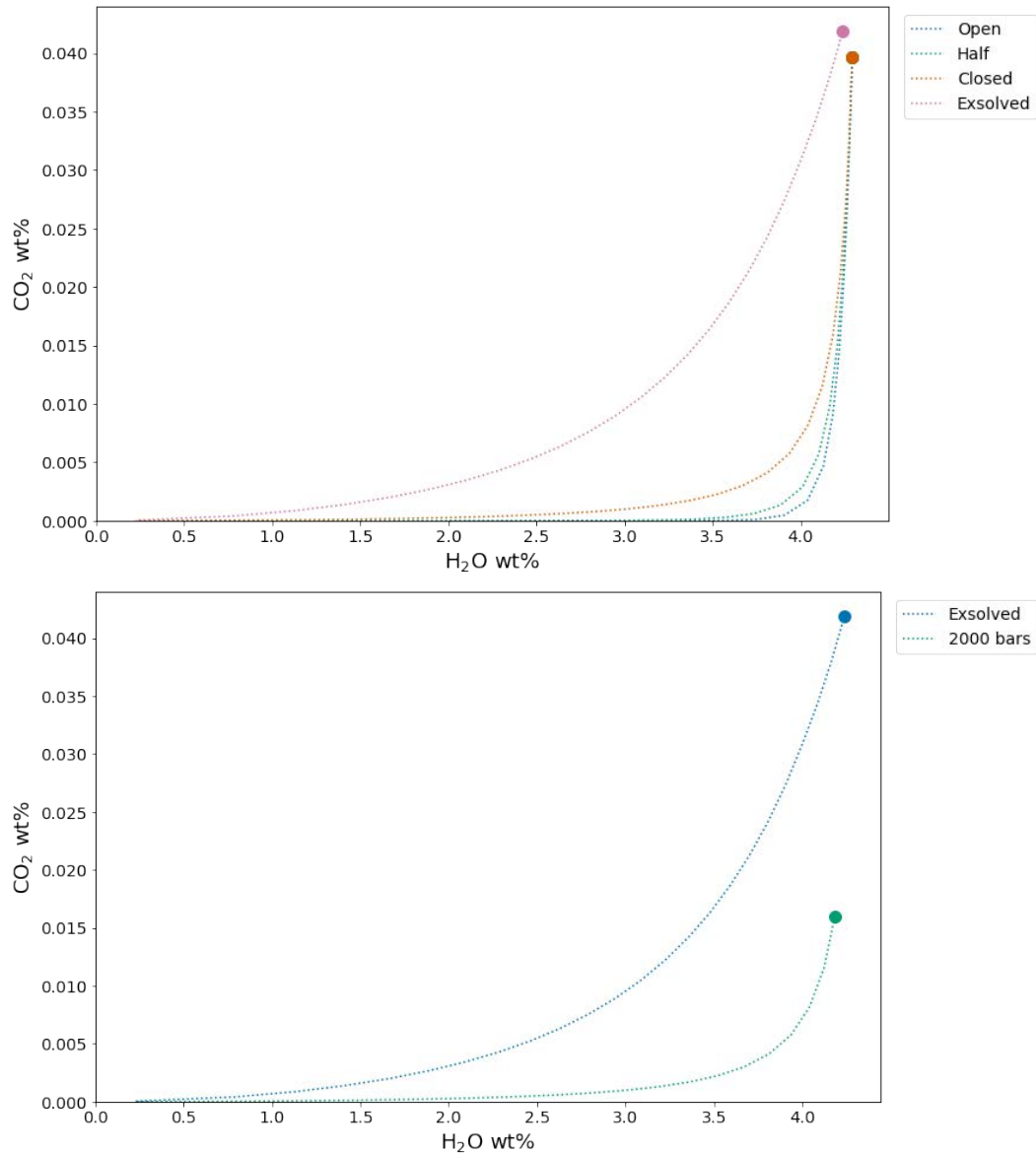


Figure 7. Degassing paths calculated for the sample, temperature, degassing style, initial exsolved fluid wt%, starting pressure, and model as designated in Section 3.6. Default manuscript values are sample ‘10*’ at 1,200 °C. “Open”, “Half”, and “Closed” curves in (a) represent open-system, partially open-system (50% fractionated fluid), and closed-system degassing paths, respectively, starting at the saturation pressure. The “Exsolved” curve in (b) represents closed-system degassing with an initial exsolved fluid wt% = 2.0. The “2000” curve in (b) represents closed-system degassing calculated starting at a pressure of 2,000 bars.

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3.8.3 Plotting multiple calculations

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One of the major advantages to VESICAL over any other modeling tool is the ability to quickly calculate and plot multiple calculations. VESICAL’s `plot()` function is very powerful and is designed to work with any VESICAL generated data. It can automatically plot and label one or multiple calculations. In addition, it can plot, as a scatter plot, any x-y points. The plot function always generates plots with H₂O on

1456 the x-axis and CO₂ on the y-axis. Functionality to plot other data (e.g. Harker style
 1457 diagrams) is already possible with Matplotlib, and so VESICAL does not duplicate
 1458 this functionality.

1459 It may be tempting to plot multiple calculations on multiple samples and
 1460 compare them, however we strongly caution against plotting data that do not corre-
 1461 spond. For example, isobars and isopleths are calculated isothermally. If degassing
 1462 paths are also plotted, the user should ensure that the degassing paths were calcu-
 1463 lated at the same temperature as the isobars and isopleths.

1464 *3.8.3.1 Isobars, isopleths, and degassing paths* In this example we will use
 1465 data imported in Section 3.1 and calculations performed in Sections 3.5 and 3.6. Of
 1466 course, all of the data calculated with VESICAL can be exported to an Excel file for
 1467 manipulation and plotting as desired. However, some examples of plotting that can
 1468 be done within this notebook or in a python script are shown below. Here we plot:

- 1469 • Isobars calculated at 1,200 °C and pressures of 1,000, 2,000, and 3,000 bars
 1470 for sample 10*
- 1471 • Isopleths calculated at 1200 °C and XH₂O^{fluid} values of 0, 0.25, 0.5, 0.75, and
 1472 1 for sample 10*
- 1473 • An open-system degassing path for sample 10*
- 1474 • A closed-system degassing path for sample 10*

1475 Input

```
1476 v.plot(isobars=isobars, isopleths=isopleths, degassing_paths=[open_df,  

  1477 closed_df], degassing_path_labels=["  

  1478 Open System", "Closed System"])
```

1481 Output

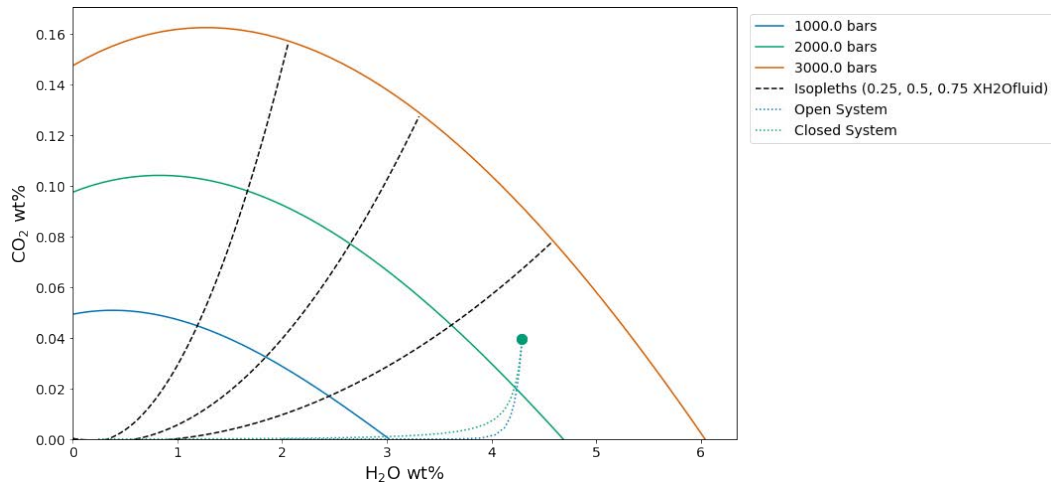


Figure 8. Example of plotting multiple calculations on one plot. Isobars and isopleths as defined in Section 3.6 and shown in Section 3.8.1 and degassing curves as defined in Section 3.7 and shown in Section 3.8.2. Default manuscript values are for sample ‘10*’ *at 1,200 °C with isobars at 1,000, 2,000, and 3,000 bars, isopleths at XH₂O^{fluid} values of 0, 0.25, 0.5, 0.75, and 1 with an open-system and a closed-system degassing path.

1482 *3.8.3.2 Isobars, isopleths, and degassing paths for multiple samples* First,
 1483 we will calculate some new data for two different samples: a basanite (sample KI-07
 1484 from Iacovino et al., 2016) and a rhyolite (sample samp. P1968a from Myers et al.,
 1485 2019). For both samples we will calculate and then plot:

- 1486 • Isobars and isopleths at 1100 °C, pressures of 1,000 and 2,000 bars and fluid
- 1487 compositions of $\text{XH}_2\text{O}^{fluid}$ of 0.25, 0.5, and 0.75
- 1488 • Closed-system degassing paths at 1100 °C

1489 Input:

```

1490 basanite_sample = myfile.get_sample_oxide_comp('KI-07')
1491 rhyolite_sample = myfile.get_sample_oxide_comp('samp. P1968a')
1492
1493
1494 basanite_isobars, basanite_isopleths = v.calculate_isobars_and_isopleths(
1495     sample=basanite_sample, temperature=
1496     1100, pressure_list=[1000, 2000],
1497     isopleth_list=[0.25,0.75]).result
1498
1499 rhyolite_isobars, rhyolite_isopleths = v.calculate_isobars_and_isopleths(
1500     sample=rhyolite_sample, temperature=
1501     1100, pressure_list=[1000, 2000],
1502     isopleth_list=[0.25,0.75]).result
1503
1504 basanite_degassing_path = v.calculate_degassing_path(sample=basanite_sample,
1505     temperature=1100).result
1506
1507 rhyolite_degassing_path = v.calculate_degassing_path(sample=rhyolite_sample,
1508     temperature=1100).result
1509

```

1510 Output:

```

1511 Calculating isobar control point at XH2Of fluid = 0
1512 Calculating isopleth at XH2Of fluid = 0.25
1513 Calculating isobar control point at XH2Of fluid = 0.5
1514 Calculating isopleth at XH2Of fluid = 0.75
1515 Calculating isobar control point at XH2Of fluid = 1
1516 Calculating isobar at 2000 bars
1517 Calculating isobar control point at XH2Of fluid = 0
1518 Calculating isopleth at XH2Of fluid = 0.25
1519 Calculating isobar control point at XH2Of fluid = 0.5
1520 Calculating isopleth at XH2Of fluid = 0.75
1521 Calculating isobar control point at XH2Of fluid = 1
1522 Done!
1523
1524 Calculating isobar at 1000 bars
1525 Calculating isobar control point at XH2Of fluid = 0
1526 Calculating isopleth at XH2Of fluid = 0.25
1527 Calculating isobar control point at XH2Of fluid = 0.5
1528 Calculating isopleth at XH2Of fluid = 0.75
1529 Calculating isobar control point at XH2Of fluid = 1
1530 Calculating isobar at 2000 bars
1531 Calculating isobar control point at XH2Of fluid = 0
1532 Calculating isopleth at XH2Of fluid = 0.25
1533 Calculating isobar control point at XH2Of fluid = 0.5
1534 Calculating isopleth at XH2Of fluid = 0.75
1535 Calculating isobar control point at XH2Of fluid = 1

```

1536

Done!

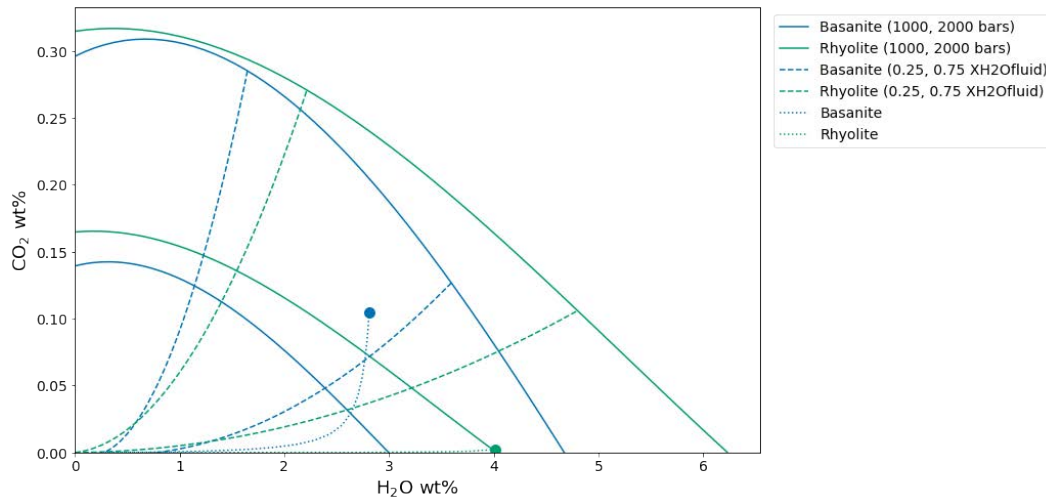


Figure 9. Example of plotting multiple calculations from multiple samples on the same plot. Note that the colors are automatically set to correspond to each sample for all plotted items (here, isobars, isopleths, and degassing paths). Samples, pressures, temperatures, $\text{XH}_2\text{O}^{\text{fluid}}$ values, and degassing path styles are defined above in this section. Manuscript default values are for a basanite (sample KI - 07) and a rhyolite (sample samp. P1968a) at 1,100 °C, 1,000 and 2,000 bars, and $\text{XH}_2\text{O}^{\text{fluid}} = 0.25$ and 0.75 and closed-system degassing.

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3.9 Model hybridization (Advanced)

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One of the advantages of implementing the solubility models in a generic python module is the flexibility this affords the user in changing the way solubility models are defined and used. In particular, the structure allows any combination of pure fluid models to be used together in modeling mixed fluids, and fugacity or activity models can be quickly changed without modifying code. This allows advanced users to see how changing a fugacity or activity model implemented in any particular solubility model would affect model results. Instructions for hybridizing models can be found in Supplemental Jupyter notebook S10.

1547

3.10 Exporting data

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Once batch calculations have been performed, they can be exported to an Excel file with the `save_excelfile()` command. This operation requires that the user define a filename (what to name your new file) and a list of the calculation results to save to this file.

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Note that this requires that calculations have been assigned to variable names, which has been done in all of the given examples. For example, to calculate saturation pressures of an imported file saved to the variable 'myfile' and simply print the output, the user can type `myfile.calculate_saturation_pressures([options])`, where `[options]` are the required and optional inputs. However, to save this result to a variable (e.g., called 'my_satPs') so that it can be accessed later, the correct python syntax would be `my_satPs = myfile.calculate_saturation_pressures([options])`.

1560 Multiple calculations can be saved to one Excel file, with each calculation be-
 1561 ing saved as its own sheet. If desired, the user can define the names of each of these
 1562 sheets. If not specified, the sheets will be named 'Original_User_Data', which con-
 1563 tains the original input data, and then 'CalcN' where N is the nth calculation in a
 1564 list of calculations.

1565 Advanced users note that any pandas DataFrame can be passed as a calcula-
 1566 tion, meaning this functionality is not limited to VESical's prescribed outputs.
 1567 The `save_excelfile()` method uses the pandas `to_excel` method, however not all
 1568 options are implemented here.

1569 **Method structure:**

```
1570     save_excelfile(self, filename, calculations, sheet_name=None)
```

1571 **Required inputs:**

1572 **filename:** Name of the file to create. The extension (.xlsx) should be in-
 1573 cluded along with the name itself, all in quotes (e.g., `filename='myfile.xlsx`
 1574 `'`).

1575 **calculations:** A list of variables containing calcula-
 1576 ted outputs from any of the core ExcelFile functions:
 1577 `calculate_dissolved_volatiles()`, `calculate_equilibrium_fluid_comp()`,
 1578 and `calculate_saturation_pressure()`. This must be passed as a list type
 1579 variable, even if only one calculation is given. This is done by enclosing the
 1580 variable in square brackets (e.g., `calculations=[my_calculation]`).

1581 **Optional inputs:**

1582 **sheet_name:** The default value is None, in which case sheets will be saved
 1583 as 'Original_User_data' (the data input by the user) followed by 'CalcN'
 1584 where N is the nth calculation in `calculations`. Otherwise, a list of names
 1585 for the sheets can be passed, with the names in quotes (e.g. `sheet_name=[`
 1586 `'SaturationPressures']`). 'Original_User_data' will always be saved as the
 1587 first sheet.

1588 **Calculated outputs:**

1589 An Excel file will be saved to the active directory (i.e., the same folder as this
 1590 manuscript notebook or wherever the code is being used).

1591 Here we save five of the calculations performed earlier in this manuscript that
 1592 were performed on imported user data. The user data was saved to the variable
 1593 'myfile'. Note that we execute the save command on the myfile variable. This is
 1594 necessary such that the original input user data may also be output with the results.

1595 **Input**

```
1596 myfile.save_excelfile(filename='testsave.xlsx',
1597                       calculations=[dissolved, eqfluid, eqfluid_wtemps, satPs
1598                                   , satPs_wtemps],
```

1600
1601
1602
1603

```
sheet_name=['dissolved', 'eqfluid', 'eqfluid_wtemps', '
SaturationPs', '
SatPs_wtemps'])
```

1604 Output

1605
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```
Saved testsave.xlsx
```

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3.10.1 Saving data for re-import into VESICAL

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In many cases, it may be preferable to compute large amounts of data using VESICAL and then reimport them, either to perform more analysis or to plot the data. Likewise, a user may wish to compute data in VESICAL and then send the results to a colleague, who can then re-import that data into VESICAL directly. For this case, we suggest using python’s pickle package (<https://wiki.python.org/moin/UsingPickle>). Any python object, such as the results of a VESICAL calculation, can be “pickled” or saved as a python-readable file. To use pickle, users must first import the pickle module, then “dump” the desired contents to a pickle file. The pickled data can be accessed by “loading” the pickled file.

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Below we pickle our computed dissolved volatile concentrations by dumping our variable `dissolved` to a pickle file that we name “dissolved.p”.

```
import pickle

pickle.dump(dissolved, open("dissolved.p", "wb"))
```

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In another python file or terminal session, `dissolved` can be loaded back in via:

```
import pickle

dissolved = pickle.load(open("dissolved.p", "rb"))
```

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4 Discussion and Conclusion

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4.1 Compositional Variation Within Datasets and Best Practices

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While not all solubility models incorporate significant bulk compositional parameters, it has been clearly shown that the composition of a melt plays a strong role in determining the solubility of H₂O and CO₂ in magmas (Ghiorso & Gualda, 2015; Moore, 2008; Papale et al., 2006; Wieser et al., submitted). Thus, compositional variance must be accounted for in any study examining solubility in multiple samples. A key use case where VESICAL can facilitate the adoption of this practice is in melt inclusion (MI) studies; specifically, where a single suite of MI with multiple melt compositions is examined using solubility models to interrogate magmatic degassing processes. Prior to the availability of VESICAL, the difficulty associated with performing multiple model calculations on multiple samples resulted in very few studies accounting for any compositional variance within their datasets. Indeed, until now, it has been difficult to even assess whether the potentially minimal compositional variance within a suite of melt inclusions from a single volcanic eruption would have any measurable effect on solubilities calculated for different MI.

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Using VESICAL, we can now easily address the question: what is the quantitative effect of compositional variation within a single suite of melt inclusions upon calculated melt inclusion saturation pressures? And, how does this affect conclusions

1650 that might be drawn regarding volcanic degassing and eruptive processes? To inves-
 1651 tigate this, we use a dataset of basaltic melt inclusions from Cerro Negro volcano,
 1652 Nicaragua (Roggensack, 2001). The compositional variation of these MI (Figure
 1653 10), while relatively restricted, results in quite variable mixed-fluid solubilities from
 1654 sample to sample. To determine the end-member compositions within the dataset
 1655 corresponding to the samples with the maximum and minimum combined H₂O-CO₂
 1656 solubilities, isobars were computed at 1200 °C and 3,000 bars for all samples using
 1657 the MagmaSat model in VESICAL. Maximum and minimum samples were taken as
 1658 the isobar curves with the smallest and largest integral (area under the curve). We
 1659 refer to this value as the “integrated mixed-volatile solubility” value, IMS, in units
 1660 of concentration squared. The samples that produced maximum and minimum in-
 1661 tegrated solubilities are shown in Figures 10 and 11 in blue and green, respectively
 1662 (sample 41b*, IMS=0.81 and 36a*, IMS=0.66 wt%² at 3,000 bars). A composi-
 1663 tion representing the average of all MI in the dataset is shown in orange (“Average
 1664 Sample”, IMS=0.70 wt%² at 3,000 bars). A jupyter notebook to reproduce these
 1665 calculations is provided in the supplement (Supplementary Jupyter Notebook S8).

1666 At all pressures, the integrated mixed-volatile solubility across the Cerro Ne-
 1667 gro dataset varies as much as 10% relative (Figure 11). For these MI, this results in
 1668 as much as 11.5% relative error in the calculation of saturation pressures (average
 1669 error for the entire dataset of 6.8% relative). It is noteworthy that this error is not
 1670 systematic either in terms of absolute value or sign. For example, when calculated
 1671 using their own compositions, saturation pressures for maximum and minimum sam-
 1672 ples 41b* and 36a* are 3050 and 3090 bars, respectively. But, saturation pressures
 1673 calculated for both of these MI using the dataset’s average composition are 3020
 1674 and 3250 bars, respectively. That is an error of -30 and +160 bars or -1% and +5%
 1675 respectively. Errors in these calculations, thus, may be quite small. But, in any case,
 1676 removing this error completely is a simple task using VESICAL, and so we recommend
 1677 that studies adopt the practice of calculating volatile solubilities (and associated
 1678 values) in melts using the composition unique to each melt investigated.

1679 Even in cases where solubility values (e.g., saturation pressures) are not calcu-
 1680 lated, the error highlighted above plagues any isobar diagram over which multiple
 1681 melt compositions are plotted (e.g., Figure 11). Alternative plots to the commonly
 1682 used H₂O-CO₂ diagram are shown in Figure 12, in which the same dataset is plot-
 1683 ted in terms of computed saturation pressure (at 1200 °C calculated with VESICAL
 1684 using MagmaSat) versus dissolved H₂O, dissolved CO₂, and fluid composition (as
 1685 XH₂O^{fluid} calculated with VESICAL using MagmaSat). These plots avoid the is-
 1686 sues discussed above as they are compositionally independent, since the saturation
 1687 pressure is calculated individually for each sample composition. Degassing trends
 1688 are more accurately represented; H₂O and CO₂ concentrations lie along expected
 1689 degassing trends with much less scatter than the H₂O-CO₂ plot. We can also see
 1690 from this figure that the fluid composition during this eruption at Cerro Negro re-
 1691 mained relatively constant at XH₂O^{fluid} ~0.8 from reservoir to surface, suggesting
 1692 a scenario approaching closed-system degassing (i.e., melt volatile concentrations are
 1693 buffered by the co-existing fluid composition).

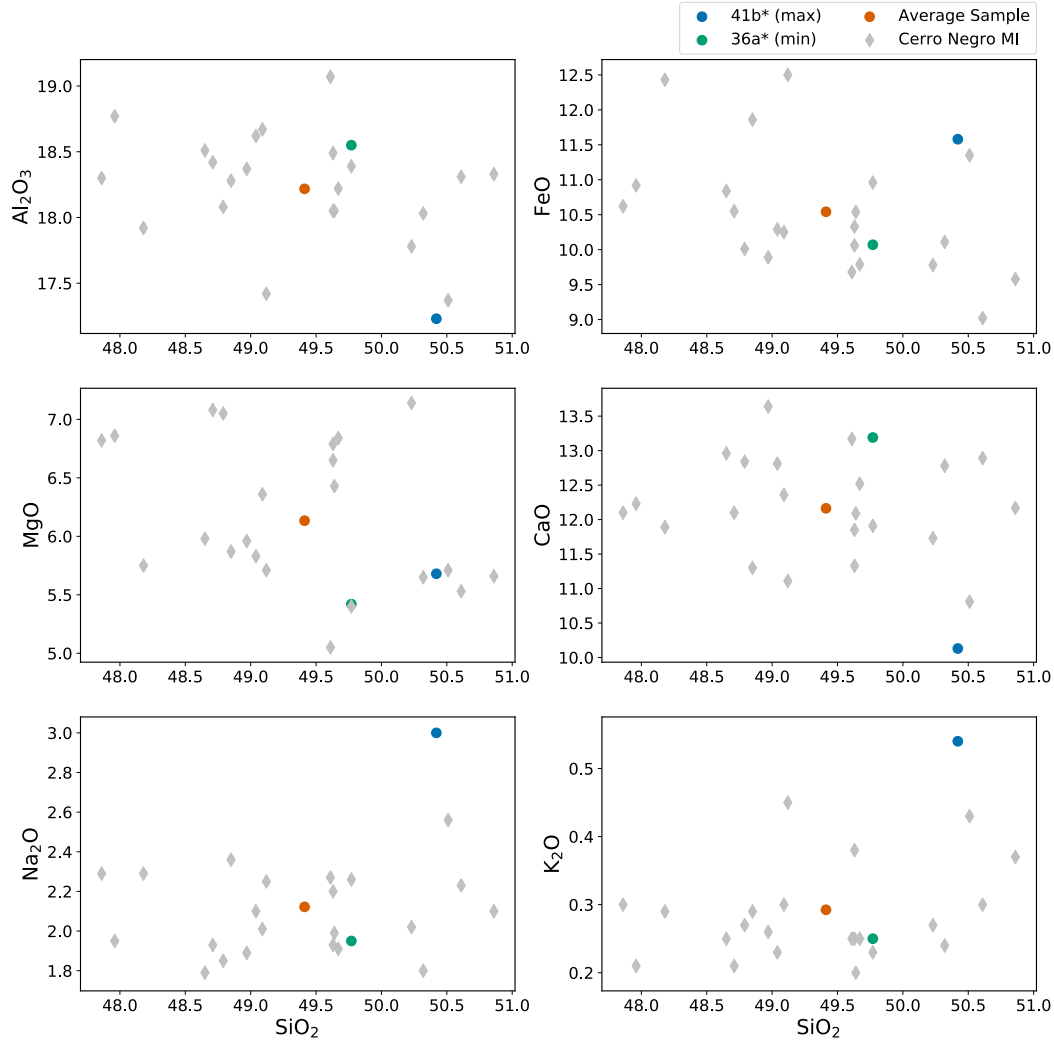


Figure 10. Harker style diagrams illustrating the compositional range of MIs from Cerro Negro volcano from Roggensack (2001). The “Average Sample” plotted as an orange dot represents a fictitious sample, calculated as the average of all MIs in the dataset. Sample 41b* and 36a* are the names of samples that produced isobars with maximum and minimum area under the curve, respectively (see text). Gray diamonds are all other data in the dataset.

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4.2 Model Comparisons

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One of the possible workflows enabled through VESICAL is the ability to easily compute and compare (numerically and graphically) results from several models at once. To illustrate this point, we will take two single samples within the calibrated compositional range of several models, calculate isobars at multiple pressures, and plot the results. This is a common way to compare the solubility surface computed by different models for a single melt composition, and it is particularly useful since it quickly highlights the significant variation that exists between published models. The results of this exercise are shown here, and a Jupyter notebook to reproduce the code and calibration checks is available in the Supplement (Supplementary Jupyter Notebook S9).

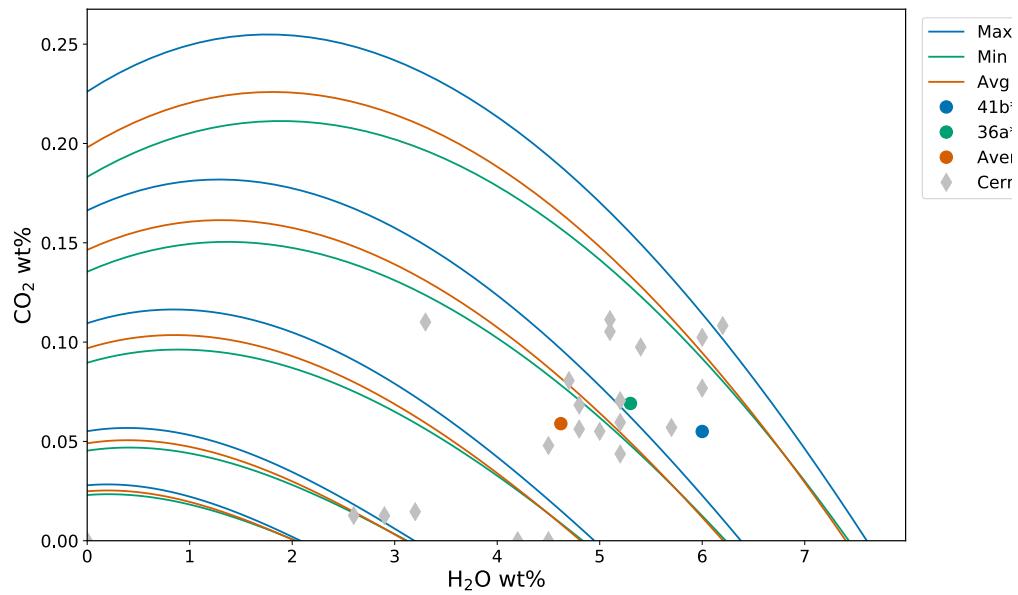


Figure 11. H₂O-CO₂ diagram with isobars for MI from Cerro Negro volcano (Roggensack, 2001) computed by VESical using MagmaSat at 1200 °C, pressures of 500, 1000, 2000, 3000, and 4,000 bars. Curves shown are polynomials fitted to data computed by VESical. Blue and green curves correspond to samples 41b* and 36a*, which produced isobars with maximum and minimum area under the curve, respectively. Orange isobars were those computed for a fictitious sample representing the average composition of the MI dataset. Gray diamonds are all other data in the dataset.

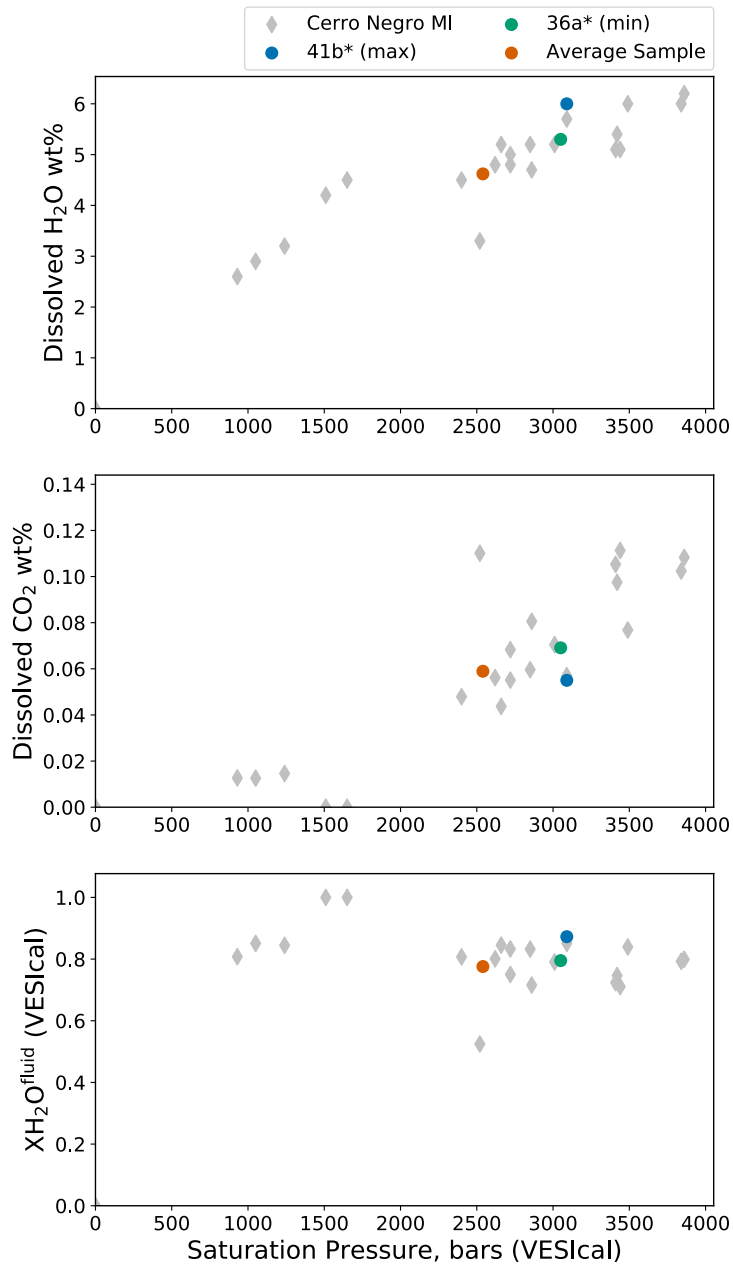


Figure 12. Saturation pressure at 1200 °C calculated using VESIcal with MagmaSat versus measured dissolved H₂O and CO₂ concentrations and calculated fluid composition in Cerro Negro melt inclusions. These plots meaningfully illustrate degassing processes while avoiding issues associated with commonly used H₂O-CO₂ diagrams, which occur with even minor compositional variation within a given dataset.

1705 We use a fictitious alkali basalt that we name “alkbasalt” and a fictitious rhy-
 1706 olite whose compositions are given in Table 13. The use of VESIcal’s `calib_plot()`
 1707 function (see supplement) illustrates that the composition of the alkali basalt is
 1708 within the compositional calibration ranges of four mixed-fluid solubility models:
 1709 MagmaSat, Iacono-Marziano, Dixon, and ShishkinaIdealMixing. The rhyolite is
 1710 within the ranges of MagmaSat and Liu. Isobars were calculated with these models
 1711 at 1200 °C for alkbasalt and 800 °C for rhyolite and pressures of 500, 1,000, and
 1712 2,000 bars, using the below code:

1713 Input

```
1714 model_comps = v.ExcelFile("tables/Table_Model_Comps.xlsx")
1715 model_comps.data
```

Table 13. Melt compositions used for modeling

	SiO ₂	TiO ₂	Al ₂ O ₃	Fe ₂ O ₃	FeO	MnO	MgO	CaO	Na ₂ O	K ₂ O	P ₂ O ₅	H ₂ O	CO ₂	Cr ₂ O ₃	NiO	CoO
Label																
Alkali Basalt	49.00	1.27	19.7	3.74	5.33	0.17	4.82	8.85	4.23	1.00	0.37	4.51	0.25	0.0	0.0	0.0
Rhyolite	77.19	0.06	12.8	0.00	0.94	0.00	0.03	0.53	3.98	4.65	0.00	0.26	0.05	0.0	0.0	0.0

1718 Input

```
1719 alkbasalt = model_comps.get_sample_oxide_comp("Alkali Basalt")
1720 rhyolite = model_comps.get_sample_oxide_comp("Rhyolite")
1721
1722
1723 alkbasalt_isobars, alkbasalt_isopleths = v.calculate_isobars_and_isopleths(
1724     sample=alkbasalt, temperature=1200,
1725     pressure_list=[500, 1000, 2000],
1726     isopleth_list=[0.5], print_status=True
1727 ).result
1728
1729 rhyolite_isobars, rhyolite_isopleths = v.calculate_isobars_and_isopleths(
1730     sample=rhyolite, temperature=800,
1731     pressure_list=[500, 1000, 2000],
1732     isopleth_list=[0.5]).result
1733
1734 Iac_alkbasalt_isobars, Iac_alkbasalt_isopleths = v.
1735     calculate_isobars_and_isopleths(sample
1736     =alkbasalt, temperature=1200,
1737     pressure_list=[500, 1000, 2000],
1738     isopleth_list=[0.5], model="
1739     IaconoMarziano").result
1740
1741 Dixon_alkbasalt_isobars, Dixon_alkbasalt_isopleths = v.
1742     calculate_isobars_and_isopleths(sample
1743     =alkbasalt, temperature=1200,
1744     pressure_list=[500, 1000, 2000],
1745     isopleth_list=[0.5], model="Dixon").
1746     result
1747
1748 Shish_alkbasalt_isobars, Shish_alkbasalt_isopleths = v.
1749     calculate_isobars_and_isopleths(sample
```

```

1750         =alkbasalt, temperature=1200,
1751         pressure_list=[500, 1000, 2000],
1752         isopleth_list=[0.5], model="
1753         ShishkinaIdealMixing").result
1754
1755 Liu_rhyolite_isobars, Liu_rhyolite_isopleths = v.
1756         calculate_isobars_and_isopleths(sample
1757         =rhyolite,
1758         temperature=800, pressure_list=[500, 1000, 2000], isopleth_list=[0.5], model=
1759         "Liu").result
1760

```

Output

```

1762 Calculating isobar at 500 bars
1763
1764 Calculating isobar control point at XH2Ofluid = 0
1765 Calculating isobar control point at XH2Ofluid = 0.25
1766 Calculating isopleth at XH2Ofluid = 0.5
1767 Calculating isobar control point at XH2Ofluid = 0.75
1768 Calculating isobar control point at XH2Ofluid = 1
1769 Calculating isobar at 1000 bars
1770 Calculating isobar control point at XH2Ofluid = 0
1771 Calculating isobar control point at XH2Ofluid = 0.25
1772 Calculating isopleth at XH2Ofluid = 0.5
1773 Calculating isobar control point at XH2Ofluid = 0.75
1774 Calculating isobar control point at XH2Ofluid = 1
1775 Calculating isobar at 2000 bars
1776 Calculating isobar control point at XH2Ofluid = 0
1777 Calculating isobar control point at XH2Ofluid = 0.25
1778 Calculating isopleth at XH2Ofluid = 0.5
1779 Calculating isobar control point at XH2Ofluid = 0.75
1780 Calculating isobar control point at XH2Ofluid = 1
1781 Done!
1782 Calculating isobar at 500 bars
1783 Calculating isobar control point at XH2Ofluid = 0
1784 Calculating isobar control point at XH2Ofluid = 0.25
1785 Calculating isopleth at XH2Ofluid = 0.5
1786 Calculating isobar control point at XH2Ofluid = 0.75
1787 Calculating isobar control point at XH2Ofluid = 1
1788 Calculating isobar at 1000 bars
1789 Calculating isobar control point at XH2Ofluid = 0
1790 Calculating isobar control point at XH2Ofluid = 0.25
1791 Calculating isopleth at XH2Ofluid = 0.5
1792 Calculating isobar control point at XH2Ofluid = 0.75
1793 Calculating isobar control point at XH2Ofluid = 1
1794 Calculating isobar at 2000 bars
1795 Calculating isobar control point at XH2Ofluid = 0
1796 Calculating isobar control point at XH2Ofluid = 0.25
1797 Calculating isopleth at XH2Ofluid = 0.5
1798 Calculating isobar control point at XH2Ofluid = 0.75
1799 Calculating isobar control point at XH2Ofluid = 1
1800 Done!
1801 RuntimeWarning: pressure exceeds 1000 bar, which Iacono-Marziano et al. (2012)
1802 suggest as an upper calibration limit of the Dixon (1997, Pi-SiO2 simpl.)
1803 Model
1804

```


1805 Input

1806

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1811

```

v.plot(isobars=[alkbasalt_isobars, Iac_alkbasalt_isobars,
               Dixon_alkbasalt_isobars,
               Shish_alkbasalt_isobars],
       isobar_labels=["MagmaSat", "Iacono-
                     Marziano", "Dixon", "Shishkina"])

```

1813 Output

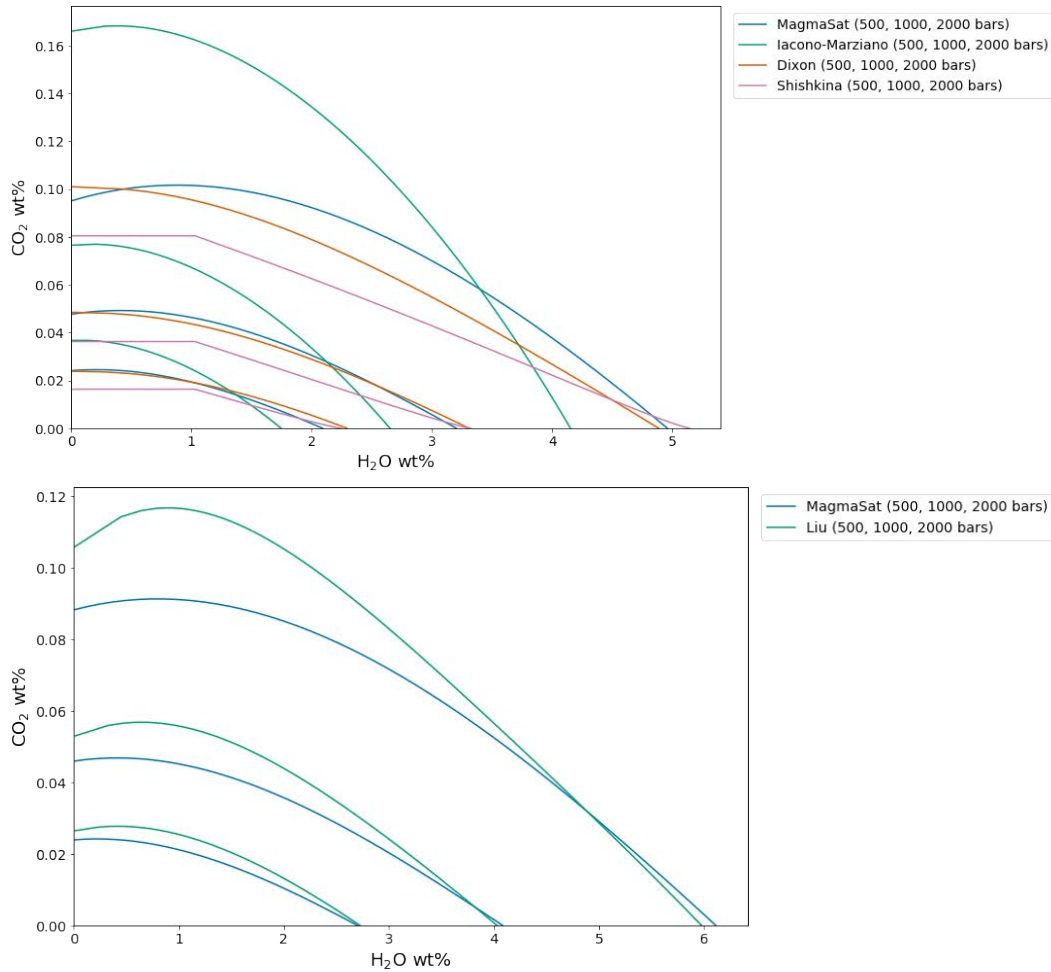


Figure 13. Isobars plotted for an alkali basalt (a) and rhyolite (b) with VESICAL for five mixed-fluid solubility models. For alkali basalt, MagmaSat, Iacono-Marziano, Dixon, and ShishkinaIdealMixing were used to create isobars at 1,200 °C. For rhyolite, MagmaSat and Liu were used to create isobars at 800 °C.

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It is immediately clear from Fig. 13 that major disagreement exists between these models. For the alkali basalt, MagmaSat and Dixon show the best agreement, particularly at pressures <2000 bars. However, the mismatch between these models (and, indeed, between all models) increases with pressure. The Iacono-Marziano model is calibrated for highly depolymerized alkali basalts resulting in an increased

1819 capacity of the melt to dissolve CO_2 . That may explain why this model predicts
1820 significantly higher CO_2 solubilities at $\text{XH}_2\text{O}^{\text{fluid}}$ values approaching 0.

1821 The ShishkinaIdealMixing model displays nearly linear isobars, with finite solu-
1822 bility below ~ 1 wt% dissolved H_2O . This is a consequence of the model calibration;
1823 the pure- H_2O solubility expression of ShishkinaIdealMixing is not calibrated with
1824 any experiments at low PH_2O . This results in a finite solubility at low dissolved
1825 H_2O concentrations, such that the zero-pressure solubility is not zero. This produces
1826 significant model error at low but non-zero values of $\text{XH}_2\text{O}^{\text{fluid}}$. Thus, we caution
1827 the user against using the Shishkina model at low but non-zero $\text{XH}_2\text{O}^{\text{fluid}}$ or when
1828 fluids deviate far from pure H_2O or pure CO_2 . In general, the Shishkina model
1829 should only be used for modeling pure- H_2O or pure- CO_2 fluids. This is discussed in
1830 more detail in Wieser et al. (submitted).

1831 The models of MagmaSat and Liu show a similar level of disagreement for
1832 H_2O - CO_2 solubility in the rhyolite, with Liu predicting much higher dissolved CO_2
1833 concentrations at low $\text{XH}_2\text{O}^{\text{fluid}}$ (< 20 relative% or ~ 220 ppm at $\text{XH}_2\text{O}^{\text{fluid}}=0.1$).

1834 4.3 Future development

1835 VESICAL represents the first comprehensive volatile solubility modeling tool
1836 of its kind, including the feature that VESICAL is extensible. VESICAL is written
1837 so that implementing new or yet-to-be-implemented solubility models is as simple
1838 as possible. To implement a new model, python code describing the model equa-
1839 tions needs to be written, and this model name needs to be added to a list of model
1840 names within the code. To make this as simple as possible such that the original au-
1841 thors of VESICAL are not the only people who can develop the code, planned future
1842 work includes the creation of detailed instructions (including instructional videos)
1843 illustrating this process.

1844 Likewise, new features can be added at any time, and enthusiastic members of
1845 the community who wish to help bring such features to VESICAL are very welcome.
1846 Users can contribute to VESICAL's code, implementing new models and new fea-
1847 tures, via github (<https://github.com/kaylai/VESICAL>). The repository is public,
1848 but we encourage users who wish to contribute to the code to fork the repository
1849 into their private workspace on github. Once edits to the code are complete, the
1850 new code can be added to VESICAL by creating a "Pull Request" inside of github.
1851 Changes and enhancements to VESICAL will correspond to a change in the code's
1852 version number. The published version of the code documented in this manuscript
1853 and archived on Zenodo is version 0.1.5 (DOI: 10.5281/zenodo.4291043). Planned
1854 features not implemented in this release include: 1. Models to calculate sample oxy-
1855 gen fugacity from $\text{Fe}^{2+}/\sum\text{Fe}$ and vice versa; 2. Additional volatiles such as sulfur; 3.
1856 More thermodynamic solubility models such as that of Papale et al. (2006).

1857 4.4 How to cite VESICAL and its models

1858 To cite computations done using VESICAL, please cite this manuscript, the
1859 VESICAL version number, as well as the model(s) used. Note that if a model was not
1860 specified during calculations, the default model of MagmaSat was used and should
1861 be cited as "MagmaSat Ghiorso and Gualda (2015)". For example: "Calculations
1862 were performed using VESICAL (v. 1.0.0; Iacovino et al., 2020) with the models of
1863 Shishkina et al. (2014) and Dixon (1997, "VolatileCalc")." The web-app always runs
1864 on the most up-to-date version of the VESICAL code, but it is best practice to note if
1865 the web-app was used ("Calculations were performed using the VESICAL web-app
1866 (v. 1.0.0; Iacovino et al., 2020)..."). We also encourage users to be as explicit as
1867 possible as to the conditions used for modelling. This includes stating the pressure,

1868 temperature, volatile concentration, and bulk magma composition used in modelling.
 1869 In the best case, VESICAL users will provide their code (e.g., as a jupyter notebook
 1870 or .py file) along with their publication such that it can be easily replicated.

1871 5 Conclusions

1872 VESICAL is a thermodynamic mixed-volatile solubility engine designed to meet
 1873 the growing computational needs of the igneous petrology community. Seven com-
 1874 monly used volatile solubility models are built into VESICAL, which employs the most
 1875 diversely calibrated (chemically and in P-T space) of the group, MagmaSat (Ghiorso
 1876 & Gualda, 2015), as the default model. VESICAL can perform five core calculations
 1877 with any mixed-fluid model and three core calculations with any model (mixed-fluid,
 1878 CO₂-only, H₂O-only). VESICAL allows for automatic calculation of large datasets and
 1879 robust built-in plotting capability.

1880 VESICAL represents the first stone on a path toward creating a generalized ther-
 1881 modynamic framework to model whole scale magmatic processes. Such a framework
 1882 builds upon the key tenets of VESICAL; namely: fundamental thermodynamic un-
 1883 derpinning; inclusion of existing modeling strategies; python powered, open-source,
 1884 and extensible code base; high usability at all levels; benchmarking and testing; and
 1885 power as a responsive and predictive tool.

1886 Data Availability Statement

1887 The VESICAL software is open source and is hosted on github ([https://](https://github.com/kaylai/VESICAL)
 1888 github.com/kaylai/VESICAL). The version of VESICAL used in this manuscript
 1889 is version 0.1.5 and is archived on zenodo (DOI: 10.5281/zenodo.4291043). VESICAL
 1890 runs on top of thermoengine, a python package that is a part of the ENKI frame-
 1891 work (<http://enki-portal.org/>). The thermoengine library is open source and is
 1892 available on GitLab (<https://gitlab.com/ENKI-portal/ThermoEngine>). VESI-
 1893 cal was written in Python3 and should be stable up to at least Python version
 1894 3.7.6. In addition to thermoengine, VESICAL requires the following standard li-
 1895 braries (with versions used for testing indicated in brackets): pandas (1.0.1), numpy
 1896 (1.18.1), matplotlib (3.1.2), cyclo (0.10.0), scipy (1.4.1), and sympy (1.5.1). The
 1897 VESICAL webapp interface runs through Anvil (anvil.works), which executes VESI-
 1898 cal code on a cloud server. The code that facilitates the link between the anvil
 1899 interface and the VESICAL code is available on the VESICAL github. VESICAL can
 1900 also be used within a jupyter notebook and is hosted on the ENKI jupyter hub
 1901 (<https://server.enki-portal.org/hub/login>) such that the code can be easily
 1902 accessed without installation on the user's local machine.

1903 All data sets used in this manuscript are available on the VESICAL github as
 1904 well as in the Supplementary Material of this manuscript. The example dataset used
 1905 for worked examples in Section 3 (example_data.xlsx file; Supplemental Dataset S1)
 1906 contains compositional information for basalts (Roggensack, 2001; Tucker et al.,
 1907 2019), andesites (Moore et al., 1998), rhyolites (Mercer et al., 2015; Myers et al.,
 1908 2019), and alkaline melts (phototephrite, basaltic-trachyandesite, and basanite from
 1909 Iacovino et al. 2016). Several additional example datasets from the literature are
 1910 available in the Supplement (Supplementary Datasets S2-S5; Table 4). These include
 1911 experimentally produced alkaline magmas from Iacovino et al. (2016, alkaline.xlsx),
 1912 basaltic melt inclusions from Kilauea (Tucker et al., 2019) and Gakkel Ridge (Ben-
 1913 nett et al., 2019, basalts.xlsx), basaltic melt inclusions from Cerro Negro volcano,
 1914 Nicaragua (Roggensack, 2001, cerro_negro.xlsx), and rhyolite melt inclusions from
 1915 the Taupo Volcanic Center, New Zealand (Myers et al., 2019) and a topaz rhyolite
 1916 from the Rio Grande Rift (Mercer et al., 2015, rhyolites.xlsx). Where available, the

1917 calibration datasets for VESICAL models are also provided (Supplementary Datasets
1918 S6-S7).

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1929 ciously provided by DeviantArt user Twai.

1930 References

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