Simultaneous classification and location of volcanic deformation in SAR interferograms using deep learning and the VolcNet database

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Abstract

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With the evolution of InSAR into a tool for active hazard monitoring, through its ability to detect ground deformation with low latency, new methods are sought to quickly and automatically interpret the large number of interferograms that are created. In this work, we present a convolutional neural network (CNN) that is able to both classify the type of deformation, and to locate the deformation within an interferogram in a single step. We achieve this through building a "two headed model", which is able to return both outputs after one forward pass of an interferogram though the network, and so does not require the use of a sliding window approach for localisation. We train our model by first creating a large dataset of synthetic interferograms

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which feature labels of both the type and location of any deformation, and we release the Python3 code for this as a package named SyInterferoPy. We find that our model's performance is improved through the inclusion of just a small amount of augmented real Sentinel-1 data, and retrain our model accordingly. We also release this set of labelled training data as a database named VolcNet. When building models of this type, it is common for some of the weights within the model to be transferred from other models designed for different problems. Consequently, we also investigate how to best organise interferograms such that the filters learned in models such as VGG16 are sensitive to the signals of interest in interferograms, but find that using different data in each of the three input channels significantly degrades performance when compared to the simple case of repeating wrapped and unwrapped phase across each channel. This implies that the inclusion of supplementary data, which we expect should improve the ability to distinguish deformation from noise, requires training of a network from scratch.

Keywords: volcano monitoring, CNN, InSAR, VGG16, VolcNet,

SyInterferoPy

1 1. Introduction

In recent years, work to extend volcano monitoring to all of the world's ~1400 subaerial volcanoes has resulted in the application of several machine
learning methods to ground deformation maps produced by interferometric
synthetic aperture radar (InSAR). Work presented in Anantrasirichai et al.
(2018, 2019a,b) and Valade et al. (2019) has used convolutional neural networks (CNNs) to determine if individual interferograms contain deformation,

whilst time series have been used by Gaddes et al. (2018) to detect signs of 8 unrest and by Sun et al. (2020) to detect subtle deformation signals. How-9 ever, in both of the examples detailed above, each algorithm demonstrates 10 very limited knowledge of the diverse types of deformation that may be mea-11 sured at volcanoes. The algorithm presented in Anantrasirichai et al. (2019a) 12 assigns all data containing deformation to one label, whilst the algorithm pre-13 sented in Gaddes et al. (2018) alerts users to changes in the signals present, 14 but does not identify the type of deformation present. Consequently, we seek 15 to improve upon these approaches by developing a CNN that is able to dif-16 ferentiate between different types of deformation, and to detect the spatial 17 extent of it. 18

Figure 1A shows the hierarchy of computer vision object/signal identification 19 methods. The algorithm presented in Anantrasirichai et al. (2018) contains a 20 model that performs classification and, by breaking larger images into smaller 21 tiles that are each classified, the algorithm as a whole is able to perform lo-22 calisation. This approach has the limitation that the deep learning model 23 used in this algorithm does not need to learn how to determine the location 24 or size of the object (or signal) of interest, and at a more fundamental level, 25 remains a classification and not localisation model. However, in the field of 26 computer vision, CNNs have been developed that are able to perform both 27 classification and localisation on images that contain either single or multiple 28 objects. The location of an object is either indicated through encompassing it 29 in a rectangle (e.g. localisation or object detection, Simonyan and Zisserman 30 (2014); Redmon et al. (2016)) or, in more complex algorithms, indicating 31 the exact outline of an object by identifying which pixels comprise it (e.g. 32

instance segmentation, He et al. (2017)). These approaches should provide more detailed information on the spatial extent of a signal of interest than a classification model that is repeatedly used on different areas of the representation. Consequently, we endeavour to advance the state of the art through developing a CNN that is able to both localise deformation within an interferogram, and to classify different types of deformation (the hierarchy of which we show in Figure 1B).

When constructing a CNN to perform both classification and localisation 40 with data derived from SAR satellites, a new CNN could be designed before 41 all the parameters within it are trained. However, this approach has the risk 42 of failing to utilise the successful applications of CNNs to other computer 43 vision problems. When reviewing methods aimed at incorporating previous 44 successful models, the two disparate parts of a CNN must be considered. 45 An example CNN is shown in Figure 1C, in which the convolutional part 46 comprises of filters that are convolved across an image to extract deep repre-47 sentations, whilst downsampling is performed simultaneously to reduce the 48 spatial extent of an image. In the case of the example network show in in 40 Figure 1C, a three channel (colour) image of size $(224 \times 224 \times 3)$ pixels is 50 transformed into a spatially smaller but deep $(7 \times 7 \times 512)$ representation 51 by this process. In the second part, this 3D representation is flattened into 52 a vector (which in this example would be of size $(7 \times 7 \times 512 = 25088)$), 53 before a traditional neural network comprising of interconnected neurons is 54 used to create the desired model outputs. The size of the last layer of this 55 second part is dependent on features such as the number of different classes 56 present in the data and, in this example case with two neurons in the last 57

⁵⁸ layer, would be used in a case in which there were only two different classes.

Consequently, when using an existing model on a new problem, any change in 59 the number or type of output classes will require changing the fully connected 60 part of the network. Therefore, it is common to retain the convolutional lay-61 ers (i.e. part one of the model) and design a new fully connected network (i.e. 62 part two of the model) that outputs the classes required by the new problem. 63 However, this approach still requires the training of a CNN that is likely to 64 contain tens of millions of parameters, which will be both computationally 65 expensive, and require a large volume of training data. AlexNet, a previously 66 state-of-the-art image classification CNN (named after one of the designers, 67 Alex Krizhevsky), has 60 million parameters, was trained on 1.2 million im-68 ages, and even when implemented on GPUs took around one week to train 69 (Krizhevsky et al., 2012). Therefore, a common approach termed transfer 70 learning is to retain both the structure and weights of the initial convolu-71 tional layers, and to train only the fully connected part of the network. This 72 approach was successfully used by Anantrasirichai et al. (2018), who used 73 the structure and weights of AlexNet, but created their own fully connected 74 classifier to output whether an interferogram contained deformation or not. 75

The weights learned in the convolutional filters of a CNN are of great importance to a network's ability to detect features, as the filters must be sensitive to the patterns that these features present in an image. As networks such as AlexNet (Krizhevsky et al., 2012) and VGG16 (Simonyan and Zisserman (2014), named after the University of Oxford Visual Geometry Group) were originally developed to compete in the ImageNet competitions (Deng et al., 2009), the filters have been trained to detect the type of features present in natural images (e.g. photographs of a person, or car). When performing transfer learning, it is these filters that must be sensitive to the patterns presented in a deformation signal if the network is to correctly classify and locate it. However, as interferograms can be expressed in differing formats we also seek to explore which of these formats allows for the filters in models trained on natural images to excel.

⁸⁹ 2. Classification with different data formats

As the most common CNNs for computer vision are trained on images com-90 prising of a channel for each of the red, green, and blue values for each pixel, 91 other data that are to be used with the network must also be three channel. 92 However, when considering an image of interferometric phase, these images 93 contain only a single value for each pixel, and so consist of only one channel, 94 and are analogous to a greyscale image. This difference in the number of 95 channels can be circumvented through duplicating the one channel interfer-96 ogram in each of the three input channels of a CNN, but in this section of 97 our study we wish to determine if this approach can be improved upon. 98

⁹⁹ When two SAR images are combined to form a single interferogram, the ¹⁰⁰ resulting image is a 2D array of complex numbers (Hanssen, 2001). Whilst ¹⁰¹ the magnitude of each of these complex numbers relates to the underlying ¹⁰² brightness and coherence of a given pixel, it is common for only the argument ¹⁰³ to be displayed, as these phase values can be used to infer ground movement. ¹⁰⁴ However, the phase values of an interferogram are wrapped in the range ¹⁰⁵ $[-\pi, \pi]$ as only the fractional part of the phase value can be measured, but



Figure 1: A) Introduction to the hierarchy of computer vision object/signal identification methods. The upper and lower rows show 12 day descending Sentinel-1 interferograms of Sierra Negra and Wolf volcano (Galapagos Archipelago, Ecuador), respectively. The Sierra Negra interferogram contains only one signal (an inflating sill), whilst the Wolf interferogram contains two signals (a deflating sill and an opening dyke). B) Proposed hierarchy for signals of interest in interferograms at volcanic centres. We propose a model that is able to classify interferograms into one of the three classes shown in blue: "no deformation", "Dyke", and ""Sill/Point". We envisage that future studies may add further classes which we mark in grey, such as those that differentiate between sills and point sources. C) Overview of a traditional convolutional neural network (CNN), showing how convolving filters and downsampling create a small but deep representation of an image (($224 \times 224 \times 3$) to ($7 \times 7 \times 512$)), which is then flattened and passed through a traditional neural network.

this ambiguity can be estimated to produce an unwrapped interferogram (Chen and Zebker, 2001). We postulate that in addition to the use of either wrapped or unwrapped data duplicated to fill three channels, the original complex numbers of an interferogram could be used in two channels, and so allow the network to use interferometric amplitude as an indicator of the reliability of the phase.

However, we can also consider external data to feed into the CNN. When 112 a human observer interprets an interferogram, they are likely to use data 113 such as a digital elevation model (DEM) as this can be used to help deter-114 mine if a signal is due to deformation, or due to a topographically-correlated 115 atmospheric phase screen. This problem is of particular importance at stra-116 tovolcanoes, as the cones typical of these volcanoes can be several kilometres 117 high, and therefore be capable of creating large and spatially stationary sig-118 nals in interferograms. The body of literature that covers the application of 119 InSAR to volcanic deformation is replete with studies that consider which of 120 the two mechanisms are responsible for the observed signals, and examples 121 include Beauducel et al. (2000); Rémy et al. (2015); Yip et al. (2019). When 122 considering previous attempts at the automatic detection of deformation sig-123 nals in Sentinel-1 interferograms, Anantrasirichai et al. (2019a) also reported 124 that many of the false positives recovered by their algorithm were caused 125 by signals correlated with topography. Consequently, we postulate that the 126 inclusion of a DEM in the inputs to our CNN will improve its ability to 127 differentiate between deformation signals and atmospheric signals that are 128 correlated with topography, and therefore seek to investigate its use as an 129 input into a multichannel model. 130

To perform this analysis, we first synthesise a dataset of labelled interfero-131 grams. To achieve this, we have created an open source Python3 package 132 named SyInterferoPy, which we make freely available to the community via 133 GitHub: https://github.com/matthew-gaddes/SyInterferoPy. The col-134 lection of enough labelled data to train a CNN is commonly time consuming 135 or expensive, and we find that the addition of localisation labels to our data 136 makes it more time consuming than in previous studies. Additionally, due to 137 the large number of data that are required to train CNNs and our expansion 138 to classification of different types of deformation, procuring enough real data 139 to do this may be not possible. Consequently, we perform this analysis using 140 only synthetic data. Following the hierarchy proposed in Figure 1B, we cre-141 ate interferograms that contain either no deformation, deformation due to an 142 opening dyke, or deformation due to a sill or point source. These sources were 143 chosen after reviewing the database of volcanic deformation events measured 144 using InSAR in Biggs et al. (2014) as we believe they cover the majority of the 145 observed signals that are of importance for volcano monitoring (i.e. we disre-146 gard signals due to processes such as the cooling of lava flows). We model the 147 dykes as vertical dislocations with uniform opening in an elastic half space 148 (Okada, 1985) with strikes in the range $[0, 359^\circ]$, dips in the range $[75, 90^\circ]$, 149 openings in the range [0.1, 0.7] m, top depths in the range [0, 2] km, bottom 150 depths in the range [0, 8] km, and lengths in the range [0, 10] km. We model 151 the sill/point sources as horizontal dislocations with uniform opening in an 152 elastic half space (Okada, 1985) with strikes in the range $[0, 359^{\circ}]$, dips in the 153 range $[0, 5^{\circ}]$, openings in the range [0.2, 1] m, depths in the range [1.5, 3.5]154 km, and widths and lengths in the range [2, 6] km. It should be noted that 155

¹⁵⁶ our proposed hierarchy of volcanic deformation signals also includes processes ¹⁵⁷ that could be modelled as a point pressure source (commonly referred to as ¹⁵⁸ a "Mogi" source (Mogi, 1958)) within the sill/point category, but given that ¹⁵⁹ we do not envisage that a deep learning model using satellite data from only ¹⁶⁰ one look angle (i.e. ascending or descending) would be able to differentiate ¹⁶¹ between these two models, we generate our synthetic data using only one of ¹⁶² them for simplicity.

These deformation patterns are then combined with a topographically cor-163 related atmospheric phase screen (APS), and a turbulent APS, which we 164 discuss generating in more detail in Gaddes et al. (2018). We calculate the 165 topographically correlated APS using the Shuttle Radar Topography Mission 166 (SRTM) 90m DEM (Farr et al., 2007), and use the coastline information con-167 tained within the product to mask areas of water. We also synthesise areas 168 of incoherence within our interferograms, which we mask in order for our 169 synthetic interferograms to be as similar as possible to the Sentinel-1 inter-170 ferograms automatically created by the LiCSAR processor (Lazecky et al., 171 2020). Figure 2 shows the results of mixing these different elements to cre-172 ate our synthetic interferograms, and the range of sizes of deforming regions 173 that the different deformation model parameters produce (e.g. Interferogram 174 2 versus Interferogram 3). 175

This process creates unwrapped data, which can be converted to wrapped data through finding modulo 2π of the unwrapped phase. However, to synthesise both the real and imaginary part of a complex interferogram requires knowledge of both the brightness of a pixel and its phase. To achieve this, we again use the SRTM DEM, and calculate the intensity of reflected electro-

magnetic radiation at the angles of incidence used by the Sentinel-1 satellites 181 $(29.1 - 46.0^{\circ})$, before adding speckle noise, and calculating the interferomet-182 ric amplitude between two images (i.e. the product of the two amplitudes). 183 As inputs to CNNs that are to be trained using transfer learning must be 184 rescaled to the inputs used in the original training data, we use only relative 185 values in the range [(-1), -1] for the synthetic intensities. With knowledge of 186 the modulus (relative intensity) and argument (wrapped phase) of each pixel 187 of our synthetic interferogram, the real/imaginary components are simply 188 the products of the modulus and cosine/sine of the argument, respectively. 189 Figure 3 shows five different ways we can represent an interferogram using 190 the three channels available. 191

The CNN we build to classify the synthetic interferograms uses the five con-192 volutional blocks of VGG16 (Simonyan and Zisserman, 2014), with our own 193 fully connected network after this. This network was chosen as, when used 194 in the field of computer vision for classifying natural images, it outperformed 195 older models such as AlexNet (Simonyan and Zisserman, 2014), which is used 196 in the algorithm presented in Anantrasirichai et al. (2018). Figure 4B shows 197 an overview of the model, in which interferograms of shape $(224 \times 224 \times 3)$ are 198 passed through the five convolutional blocks of VGG16 to create a tensor of 199 shape $(7 \times 7 \times 512)$. This is flattened to make a vector of size 25,088, before 200 being passed through fully connected layers of size 256, 128, and an output 201 layer of size three (i.e., dyke, sill/point, or no deformation). The localisa-202 tion output shown in the figure is not used in our preliminary exploration 203 of which channel format to use (Section 2), but is used in Section 3. To 204 produce a set of outputs that can be used as probabilities, we use a softmax 205

activation for the last layer (Bridle, 1990), but on the remaining layers we use rectified linear units (ReLus) to reduce computation time (Agostinelli et al., 2014). As our model seeks to solve a classification problem, we use categorical cross entropy for the loss function, which we seek to reduce using the Nadam optimizer as this does not require the choice of a learning rate (Dozat, 2016).

To train the model using the five different types of synthetic data, we perform 212 what is termed "bottleneck learning" in machine learning literature (e.g. Yu 213 and Seltzer (2011)). This is shown in Figure 4A, and comprises of first 214 computing the results from passing our entire dataset through the first five 215 blocks of VGG16, before then training only the fully connected parts of our 216 network (i.e. the classification output). This method is highly efficient as 217 we do not generally wish to update the weights in the convolutional blocks 218 of VGG16, yet passing the data through these blocks is computationally 219 expensive. By passing the data through the convolutional blocks just once, 220 we can then repeat only the relatively inexpensive passes of the data through 221 the fully connected parts of our network as we update the weights contained 222 within these layers. 223

A common problem of CNNs that are used for classification can be overfitting of the training data, which results in a model that generalises to new data poorly (Krizhevsky et al., 2012). We endeavour to limit this through the use of dropout (Srivastava et al., 2014) before both the 256 and 128 neuron layers, as through randomly removing some connections during each pass of the data through our model, this method aims to ensure that our model is forced to learn more robust representations of the training data. As we use synthetic data, we are not limited by the usual cost of collecting labelled
data, and therefore are able to generate 20000 unique interferograms that are
evenly distributed between classes without the use of data augmentation.

Figure 5 shows the results of training five models with each of the data 234 formats previously discussed. The highest classification accuracy achieved is 235 ~ 0.95 , which is achieved when the models are trained with either wrapped or 236 unwrapped data repeated across the three input channels. However, it should 237 be noted that the accuracy of the unwrapped phase model takes the full 20 238 epochs to achieve this performance, which contrasts with the wrapped phase 239 model which shows little change after the eighth epoch. Inclusion of the 240 DEM as the third channel appears to reduce classification accuracy, whilst 241 very low accuracies are achieved in the real and imaginary channel case. We 242 discuss these results in more detail in Section 4, but for the remainder of the 243 paper we choose to work with data that is unwrapped and repeated across the 244 three input channels. We choose this approach as no significant differences 245 are seen between the classification accuracy ultimately achieved with either 246 wrapped or unwrapped data, but the use of unwrapped data may allow for 247 a model to be used with unwrapped time series, and so detect subtle signals 248 produced by low strain rate processes. Additionally, a model that works with 249 unwrapped data may also provide the opportunity to be expanded to locate 250 and classify unwrapping errors automatically. 251



Figure 2: An example of the constituent parts of seven synthetic interferograms. Interferogram 5 does not feature deformation, interferograms 1, 4, and 6 feature deformation due to an sill/point source, and interferograms 2-3 feature deformation due to an opening dyke. These signals are geocoded and areas of water masked, before being combined with a topographically correlated APS, and a turbulent APS. Areas of incoherence are also synthesised, and these are used to mask the combination of the three signals to create the final synthetic interferograms.



Figure 3: Organisation of an interferogram into three channel form. Columns one and two feature unwrapped data that is repeated, and in column two the DEM is included as the third channel. In column three the real and imaginary elements of the complex values of each pixel of an interferogram occupy channels one and two, whilst the DEM is included in the third. Columns three and four feature wrapped data that is repeated, and in column five the DEM is included as the third channel.



Figure 4: A) Overview of our approach to creating a dataset of synthetic interferograms, arranging these into the five different three channel formats, computing the bottleneck features for each piece of data, and training the fully connected layers of a CNN B)Structure of our classification and localisation CNN. Input interferograms are first passed through the first five convolutional blocks of VGG16 to transform them from size $(224 \times 224 \times 3)$ to size (7×512) . These are flattened to create a large fully connected layer featuring 25088 neurons, which is connected to both the upper branch/head, which performs classification, and the lower branch/head, which performs localisation. We find the localisation problem more complex than classification, and consequentially our localisation branch/head features more layers, each with more neurons. The output of the localisation head is a vector of four values determining the position and ¹⁶Size of the deformation, whilst the output of the classification head is a vector of three values that indicate the probability for each class, and sum to one.



Figure 5: Accuracy of classifying validation data (10% of the total) during training using three channel data arranged in different formats. "u": unwrapped data, "w": wrapped data, "d": DEM, "r" real component of interferogram, "i": imaginary component of interferogram. Low accuracy is seen for the "rid" data, and in both the wrapped and unwrapped cases inclusion of the DEM in the third channel is seen to degrade classification accuracy. At the end of the 20 epochs of training, only a small difference is seen in accuracy between wrapped and unwrapped data, with both classifying ~95% of the validation data correctly, though the wrapped phase model is seen to achieve this level of accuracy more quickly (requiring only eight epochs of training).

252 3. Classification and localisation

253 3.1. Using synthetic data

In the previous section, we demonstrated that, when using VGG16 with con-254 volutional weights learned on ImageNet data, roughly optimal performance 255 for classifying synthetic interferograms is achieved when either the wrapped 256 or unwrapped phase is repeated across the three input channels. We choose 257 to progress with only the unwrapped phase model, as the computational 258 cost of unwrapping is often already met by automatic processing systems 259 (e.g. LiCSAR, Lazecky et al. (2020)), and the development of models that 260 use unwrapped phase may lead to benefits such as the ability to classify and 261 locate unwrapping errors. In this section, we build on the model used to 262 perform classification by adding localisation output. We also endeavour to 263 ascertain if the expense of collecting labelled data can be avoided entirely 264 through the continued use of synthetic data when training our model. 265

We achieve both classification and localisation through dividing the fully 266 connected section of our model to produce two distinct outputs. One output 267 returns the class of the input data in the manner described in Section 2, whilst 268 the second returns the location and size of any deformation within the scene. 269 In machine learning parlance, models of this type are termed double headed, 270 and we subsequently refer to either of the outputs and their corresponding 271 preceding layers as either the classification head or localisation head. Figure 272 4B shows the structure of the two heads, and how they diverge after the 273 output of the fifth block of VGG16 has been flattened. The localisation head 274 is structured in a similar manner to the model described in Simonyan and 275

Zisserman (2014), in which the model conveys the location of any deformation 276 through outputting a column vector containing four values. Two of these 277 values determine the centre of the deformation pattern and two display its 278 horizontal and vertical extent. Together, these four values can be used to 279 construct a box encompassing a deformation pattern. However, we find that 280 an acceptable level of localisation performance cannot be achieved with a fully 281 connected network with the same complexity as the classification head, and 282 were required to increase both the number and size of layers in the localisation 283 head's fully connected network. Experimentation finds that the simplest 284 model capable of achieving good performance has five layers consisting of 285 2048, 1024, 512, 128, and 4 neurons. 286

We use the mean squared error between the predicted location vector and 287 the labelled location vector as our localisation loss function, which we seek to 288 minimise. When using three arc second pixels (~ 90 m) with a loss function 289 of this type, a mean square error of 400 pixels would correspond to the 290 localisation being incorrect by around $\sqrt{400} = 20$ pixels, or ~ 2 km. However, 291 when using a double headed network, training is complicated by the fact 292 that the model's overall loss is now a combination of the classification and 293 localisation loss, which must be balanced using a hyperparameter commonly 294 termed loss weighting. We experiment with this hyperparameter, and find 295 that a value of 0.95 for the classification loss and 0.05 for the localisation 296 loss provides a good balance between the two outputs. This value proves 297 suitable as the localisation loss is significantly larger than the classification 298 loss, but by weighting them unequally they then contribute to the overall 299 loss approximately equally. 300

An overview of how we trained our model is provided in Figure 6A, but it 301 should be noted that in this step we use only synthetic data. To train our 302 model computationally efficiently, we again employ bottleneck learning, but 303 to improve the performance of our network, we also seek to improve the 304 filters learned within the convolutional blocks. We perform this by changing 305 the style of learning after the 10th epoch, and switch from updating only 306 the fully connected layers, to also including the 5th convolutional block in 307 our updates. However, in contrast to the computationally cheap process of 308 passing only the bottleneck features through the fully connected part of the 309 network, we must now pass the images through both the convolutional and 310 fully connected part of the network. Care is also required with the learning 311 rate when starting the new style of training after the 10th epoch, as too 312 large a learning rate would quickly destroy the finely tuned values in both 313 the convolutional blocks of VGG16, and our fully connected classification 314 and localisation heads. We circumvent this through switching the optimizer 315 to stochastic gradient descent (SGD) and setting the learning rate manually. 316 We find that a value of 1.5×10^{-8} does not degrade the performance already 317 gained during training, but still allows for the validation localisation loss 318 to decrease from ~ 800 to ~ 700 pixels (i.e. a mean error of ~ 2.6 km), and 319 the classification accuracy to increase from ~ 0.8 to ~ 0.85 . This increase in 320 model performance is shown in Figure 6B. 321

Figure 7 shows the results of applying our trained classification and localisation model to a random selection of the testing data (i.e., 10% of the data, to which the model was not exposed to during training). In the majority of cases, the classification can be seen to be accurate, and the localisation

approximately correct. When considering the entire test set of data (i.e. not 326 just the subset shown in Figure 7), the classification accuracy is 0.89, whilst 327 the localisation loss is \sim 700. It should be noted that we could also report the 328 classification loss (0.31), but we believe this is less useful than the accuracy. 329 However, in the localisation case, accuracy is not a meaningful measure of 330 the fidelity of the output, as it is instead a regression problem in which we 331 aim to approximate the correct values, which are continuous in nature. In a 332 manner similar to that reported for the validation data, the localisation loss 333 (mean squared error) of \sim 700 pixels corresponds to a mean error of \sim 2.6 km 334 (when using three arc second pixels). 335

336 3.2. Application to real data

Whilst the model described in the previous section achieved good perfor-337 mance when classifying and locating deformation in synthetic interferograms, 338 for use in automatic detection algorithms we require our CNN to work with 339 Sentinel-1 data. These data are of particular importance for volcano moni-340 toring, as the European Space Agency's data policy ensures that Sentinel-1 341 data are available quickly and at no cost, whilst the low revisit times ensure 342 that the majority of sub-aerial volcanoes are imaged at least every 12 days. 343 To test our model with Sentinel-1 data, we apply our CNN to a collection of 344 52 interferograms for which we have performed the time consuming task of 345 labelling both the class and location of deformation within them. However, 346 in some examples assigning a single class to a complex deformation pattern 347 is difficult, and we instead assign what we deem the dominant class to be, 348 whilst expecting that the network should assign some probability to other 349



Figure 6: A) Overview of our approach to training our model, in which bottleneck features are used to train only the fully connected network, before the original data are used to fine tune the 5th convolutional block and the fully connected network B) Summary of training the two headed model with synthetic data. The upper plot shows the accuracy of the classification head, whilst the lower plot shows the loss function for the localisation head. To the left of the vertical dashed line bottleneck learning occurred, and to the right traditional learning occurred. This extra learning stage allows the localisation loss for the validation data to decrease from ~800 to ~700, and for the classification accuracy of the validation data to increase from ~0.80 to ~0.85.



Figure 7: Results of our classification and localisation CNN on the (synthetic) testing data. Deformation units are centimetres, black class labels and location boxes were generated from the synthetic data and encompass all areas with over 5 cm of deformation, whilst red depicts those predicted by the CNN. As the model outputs a probability for each label, these are included as decimals for each of the predicted classes. Inspection of the results shows that in all but one of the randomly chosen cases, the localisation is broadly correct, and the classification is correct. Interferogram 2, which is classified incorrectly, features a relatively strong turbulent APS (seen as the spatially correlated noise) and a deformation pattern that extends into an area of incoherence, which may explain the misclassification.

classes. This is most evident in interferograms seven, nine and ten of Figure 8 that span the 2015 eruption of Wolf Volcano (Galapagos, Ecuador), in which signals were attributed to both the deflation of a sill and the opening of a dyke (Novellis et al., 2017; Xu et al., 2016).

The interferograms used come from either a collection of time series that were 354 created by the authors of this study, or by the LiCSAR automatic interfero-355 gram processor (https://comet.nerc.ac.uk/COMET-LiCS-portal/), and fea-356 ture the volcanoes Campi Flegrei, Agung, Wolf, Sierra Negra, and Alcedo. 357 We filtered the interferograms with a Goldstein filter (Goldstein and Werner, 358 1998), unwrapped using SNAPHU (Chen and Zebker, 2001), and masked pix-359 els with an average coherence below 0.7. For the Galapagos volcanoes (Wolf, 360 Sierra Negra, and Cerro Azul), deformation is visible in some of the 12 day 361 interferograms, but the deformation signal at Campi Flegrei is more sub-362 tle, and we are required to manually create interferograms with temporal 363 baselines of 24/36/48/60 days in order for the deformation to be visible in 364 a single interferogram. The deformation signal at Agung was attributed to 365 the opening of a dyke (Albino et al., 2019), but due to the short lived na-366 ture of this event, is only visible in a relatively small number of the "daisy 367 chain" of short temporal baseline interferograms. To increase the number of 368 interferograms available, we again produce a selection of 24/36/48/60 day 369 interferograms that span the event. 370

Figure 8 shows the results of applying our trained classification and localisation model to a quasi-random selection of Sentinel-1 interferograms. Interferograms such as Interferogram 3 show a very clear inflation signal at Sierra Negra, and are correctly classified by the CNN ("sill/point"), whilst the lo-

calisation is broadly correct. Other promising results include the labelling of 375 the three Wolf coeruptive interferograms (seven, nine and ten) as containing 376 a sill ("sill/point"), which is also localised well. However, some interfero-377 grams are poorly classified, such as the subtle signal seen in interferogram 378 zero. The divergent nature of our CNN's two heads also leads to outputs 379 that show disagreement between them. Interferogram 11 demonstrates this, 380 in which it is correctly classified as containing no deformation, but features 381 an incorrect localisation output. 382

³⁸³ Considering the entire real testing dataset, the classification accuracy is 0.65, ³⁸⁴ whilst the localisation loss is \sim 2017. We discuss the results of this model ³⁸⁵ more fully in Section 4, but in the following section we seek to improve ³⁸⁶ the performance of our model through the inclusion of real data during the ³⁸⁷ training stage.

388 3.3. Augmentation of training data with the VolcNet database of Sentinel-1 389 data

To increase the performance of our model further, we seek to incorporate 390 real data into the training. We do this through revisiting the time series 391 that were used to generate the test dataset of 52 interferograms (Section 392 3.2), and labelling a further 173 interferograms which we use for training, 393 whilst retaining the original set for further testing. This number was cho-394 sen as it was the largest that could be created from several time series that 395 were readily available and, whilst we acknowledge that more labelled real 396 data is likely to improve our model, the creation of a significantly larger 397 database remains outside the scope of this paper. Additionally, the use of 398



Figure 8: Results of our classification and localisation CNN on our testing set of Sentinel-1 interferograms when the CNN has been trained on synthetic data only. The labelling convention is as per the previous figure (n.b. deformation is in centimetres), but labels in black were manually created. Inspection of these results show that they vary between both the label and localisation being broadly correct (e.g. 3, 10), the localisation correct but the label incorrect (e.g. 2), the label correct but the localisation incorrect (e.g. 6), and both the label and localisation incorrect (e.g. 4). Interferograms 0 - 1 feature Campi Flegrei, 2 features Agung, 3 - 5 feature Sierra Negra, 6 - 10 feature Wolf, and 11 features Cerro Azul.

a relatively small number of real data allows for greater care to be taken in 390 their labelling, and so reduce the probability of labelling errors occurring. 400 We also make the combined database of 173 + 52 = 225 training and test-401 ing data and their labels freely available via GitHub, and term this database 402 VolcNet: https://github.com/matthew-gaddes/VolcNet. However, 20000 403 synthetic interferograms were used to train the previous model, and the in-404 clusion of 173 new interferograms is unlikely to impact the model significantly 405 as these could still be classified poorly with minimal increase in the loss func-406 tion. We therefore apply data augmentation, which involves creating random 407 flips, rotations, and translations of the interferograms to extend our set of 408 real training data to feature 20000 unique, though often highly correlated, 409 Sentinel-1 interferograms. With the exception of including real data, we train 410 our model in the same computationally efficient manner as described in the 411 previous section, which we show schematically in Figure 6B. 412

Figure 9 shows the results of applying our CNN to the same set of test 413 interferograms used in Section 3.2. Inspection shows greatly improved lo-414 calisation, with very small errors for interferograms zero, two and three. In 415 this selection of interferograms, false positives are not seen (i.e. cases of "no 416 deformation" that are labelled as dykes and sills), but several cases of false 417 negatives are seen, such as interferograms 4, 7, 9, and 10 (i.e. cases of dykes 418 and sills that are labelled as "no deformation". The misclassification of in-410 terferogram 4 may be explained through the relatively low signal-to-noise 420 ratio of the deformation signal (i.e. in contrast to interferogram 3), whilst 421 interferograms 7, 9, and 10 feature complex signals that span the 2015 erup-422 tion of Wolf and were attributed to both changes in the volume of a sill, and 423

⁴²⁴ propagation of magma to the surface (Xu et al., 2016). As the model was ⁴²⁵ not trained on data that contained multiple deformation signals, the errors ⁴²⁶ seen when this situation is encountered suggests that further work may be ⁴²⁷ needed to incorporate more complex deformation patterns that better reflect ⁴²⁸ the processes that occur at volcanoes.

Considering the entire real testing dataset, performance has now increased, 420 and the classification accuracy has risen to 0.83, whilst the localisation loss 430 has decreased to 522. Table 1 compares the two models in a more detailed 431 manner by considering the classification accuracy and localisation loss for 432 each class of interferogram. As this is our best performing network, we 433 name it VUDL-NET-21 ("Volcanic Unrest Detection and Localisation NET, 434 2021), and make all the code required to train it freely available on GitHub: 435 https://github.com/matthew-gaddes/VUDLNet_21 436

437 4. Discussion

From the analysis performed in Section 2 we conclude that the incorporation 438 of a DEM into our CNN could not be achieved through the relatively simple 439 step of using it as one channel in multichannel data. This is likely because 440 the weights in the first five convolutional blocks of our model were trans-441 ferred from VGG16 and, as VGG16 was trained using natural images, inputs 442 which are broadly similar across all three channels are required. It should be 443 noted that we rescaled our training data to lie in the same range as the data 444 that VGG16 was trained on (described further in Section 2), and therefore 445 the lack of similarity across channels we refer to is not due to different mag-44F



Figure 9: Results of our classification and localisation CNN on our testing set of Sentinel-1 interferograms after incoporating real data into the training. The labelling convention and interferograms are as per Figure 8. This model can be seen to outperform the CNN trained only on synthetic data, with improved classification and localisation. However, several errors remain; e.g., interferogram 4 features a comparatively subtle uplift signal in comparison to others that preceded the 2018 eruption of Sierra Negra and is classified as "no deformation" by the model, whilst the complex co-eruptive signal of interferogram 9 is not located or classified accurately.

Classification Accuracy $[0-1]$	Synthetic	Synthetic and Real
Dyke (3)	0.00	0.67
Sill/Point (17)	0.47	0.82
No deformation (32)	0.81	0.84
Combined (52)	0.65	0.83

Localisation Loss (pixels)	Synthetic	Synthetic and Real
Dyke (3)	702	100
Sill/Point (17)	3366	579
No deformation (32)	1423	531
Combined (52)	2017	522

Table 1: Summary statistics for CNNs trained either with synthetic data, or with synthetic and real data. Combined refers to the complete set of testing data. For both cases, the models can be seen to achieve good accuracy when classifying interferograms that contain either no deformation or deformation due a sill or point source, but to misclassify interferograms that contain deformation due to an opening dyke (accuracies of 0.00 and 0.67). Significant reduction in localisation loss is also seen for interferograms that contain no deformation (1423 to 531 pixels²), suggesting that the inclusion of real data improves the model's ability to refrain from interpreting atmospheric signals as the location of deformation.

nitudes, but rather, different spatial patterns. However, an approach where 447 the weights within the convolutional blocks of a classification and localisa-448 tion model were trained from scratch, may easily allow for the incorporation 449 of extra data in the different input channels. Should this approach not be 450 feasible, information such as the DEM may be best incorporated through 451 the use of a two input model, in which one set of convolutional filters are 452 applied to the phase information, whilst a second is applied to the DEM. 453 These two networks could then be merged at the fully connected stage, in 454 much the same way as our fully connected model diverges into two outputs. 455 Should this be successful, it may also provide a method to add further inputs 456 to a model, such as those outputted by a weather model, which may reduce 457 false positives due to occurrences such as a strong topographically correlated 458 APS. However, training the weights of a model from scratch and exploring 459 more complex multi-input model architectures remains beyond the remit of 460 this study. 461

The results presented in Figure 8 show that a model trained only with syn-462 thetic data is able to classify and locate deformation signals in Sentinel-1 463 data. However, it is only successful in cases with particularly clear defor-464 mation patterns, and in cases with more subtle signals generally erroneously 465 resorts to labelling these as not containing deformation. It is possible that 466 both of these limitations may be overcome through the use of more realistic 467 synthetic data, as our result suggests that our current methodology does not 468 describe processes well enough to be used without real data. The generation 460 of more realistic deformation patterns may be achieved through steps such as 470 more intelligent sampling of the parameters used in the forward models used 471

to generate the deformation patterns, the use of different types of deforma-472 tion models such as penny-shaped cracks (Fialko et al., 2001) or point/Mogi 473 sources (Mogi, 1958), and the superposition of multiple deformation patterns 474 in a single interferogram such as was observed prior to the 2005 eruption of 475 Sierra Negra (Jónsson, 2009). The generation of more realistic atmospheric 476 signals could be achieved through increasing the complexity of synthetic data, 477 such as through the use of phase-elevation ratios that are non-linear or spa-478 tially variable, or through using data from different sources. Interferograms 479 that image regions with little deformation could be used to increase the 480 complexity of the set of "no deformation" data, or combined with synthetic 481 deformation patterns to produce more complex semi-synthetic data. 482

The results presented in Figure 9 show the benefit of incorporating real data. 483 However, much scope for improvement remains, with several classification 484 and localisation errors visible in this figure. The majority of the localisation 485 errors are either in cases in which the deformation signal is slight (e.g. inter-486 ferogram four of Figure 9), or in interferograms that span the 2015 eruption 487 of Wolf volcano. In the former case, it is natural for a threshold in the signal 488 to noise ratio to exist below which a method is not able to identify the signal 489 of interest, and these interferograms appear to represent that. In the latter 490 case, the interferograms in question contain complex deformation patterns 491 due to both the opening of a dyke and the removal of magma from a sill below 492 the caldera (Novellis et al., 2017), and the inclusion of either real of synthetic 493 training data that contains multiple deformation patterns may alleviate this 494 shortcoming. 495

⁴⁹⁶ The divergent nature of the two heads (classification and localisation) of our

network also allows for discrepancies between their outputs. This is seen 497 in interferogram 10 of Figure 9, in which the localisation head produces a 498 broadly correct output, but the signal is incorrectly labelled as "no defor-499 mation", although with a relatively low confidence. However, we postulate 500 that it may be possible to avoid errors of this type by using more complex 501 model architectures. Models such as YOLO (Redmon et al., 2016) produce 502 bounding boxes and classifications in one step, and have the added bonus 503 of being able to work with images that contain multiple signals. If success-504 fully applied to interferograms, a model of this complexity may avoid the 505 discrepancy errors we encounter, and be able to handle interferograms that 506 contain multiple deformation patterns. In the case that multiple signals do 507 exist in a single interferogram, we do not envisage these to be difficult to 508 label as it is likely that these would be considered interesting events by the 509 scientific community and therefore be the subject of detailed study (e.g. the 510 multi-signal interferograms used in this study are analysed in detail in (Xu 511 et al., 2016)). 512

Our approach to localisation avoids the need for repeated classification using 513 a sliding window approach, and allows for our network to reason using the 514 entire image. Whilst this approach is beneficial in terms of advancing the 515 state-of-the-art towards that of a human interpreter, one caveat remains in 516 that building a network that is able to utilise large interferograms can be 517 complex. In our model, we use pixels of three arc second size and, with an 518 input size of 224×224 , the resulting model is able to "see" an approximately 519 20km square around a volcano. If we wish to proceed at this resolution, our 520 model's visual field could be increased through changing the input size to 521

around 400×400 which would not impact our ability to use VGG16's filters (or convolutional blocks), but would increase the size of the first layer of the fully connected part of our network.

At present, an input with side length 224 is reduced to a feature map with 525 side length 7 (shown in Figure 4) which, combined with a depth of 512, 526 produces a flattened layer of size $7 \times 7 \times 512 = 25088$. However, doubling 527 the input side length would double the feature map side length, increasing 528 the flattened layer to a size of $14 \times 14 \times 512 = 100352$. Whist our model 529 contains millions of free parameters, connecting this layer to a subsequent 530 layer would produce a significant increase in the total, and is likely to require 531 either more ingenuity or more data to be trained successfully. Analysis of the 532 offsets of deformation patterns at volcanic centres by Ebmeier et al. (2018) 533 finds that 8% of signals are located more than 10km from a volcanic edifice, 534 and would therefore be missed by our current model. Future models that 535 wish to perform localisation using a global approach may therefore require 536 slight increases in size in order to capture all signals of interest. 537

538 5. Conclusion

We find that either wrapped or unwrapped data are approximately equally suited for use with the weights of VGG16's filters trained on ImageNet data, whilst more complex use of the three channel format that these models support degrades performance. However, we expect this will not be the case if the weights within VGG16's filters are trained from scratch, as additional data such as topography should help to separate deformation from noise.. We combine the five convolutional blocks of VGG16 with two fully connected networks to perform both classification and localisation, which allows our network to reason using the whole interferogram (i.e. avoiding a sliding window approach), and therefore move a step closer to interpreting InSAR data in a manner similar to a human expert. Additionally, our network is able to differentiate between several different forms of deformation.

To minimise the costly nature of labelling data, we initially train our model using only synthetic data. We find that our model generalises well to some cases of Sentinel-1 data, but errors remain in cases such as subtle deformation signals, or unusual atmospheric signals. We alleviate this problem through the inclusion of a small amount of real data during the training phase, and present a model that is able to both classify and locate deformation within ~50 interferograms of ~20km side length.

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(Hunter, 2007), and all CNN work was carried out in KERAS using the
TensorFlow backend.

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