Modelling cross-shore shoreline change on multiple timescales and their interactions

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¹⁶ Key Points:	
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17	•	Implementation of multiple shoreline response factors to consider different
18		timescales and their interplay in equilibrium shoreline models.
19	•	Extreme forcing events can have a persistent impact on the longer term state
20		of the beach.
21	•	The long term shoreline location can modulate extreme event impacts.

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22 Abstract

Understanding and predicting shoreline changes is paramount to coastal managers to 23 anticipate potential threats. These shoreline changes are often driven by complex 24 processes at multiple timescales. In this paper, a new approach to model 25 wave-driven, cross-shore shoreline change incorporating multiple timescales is 26 introduced. As a base we use the equilibrium shoreline prediction model ShoreFor 27 that accounts for a single timescale only. High resolution data collected at four 28 distinctly different study-sites is used to train the new data driven model. The four 29 data-sets together cover sites that are mid latitude storm-dominated, under the 30 influence of tropical cyclones and monsoons, and equatorial storm-free dominated by 31 seasonal climate variability. In addition to the direct forcing approach used in most 32 models, here two additional terms are introduced: 1) a time-upscaling and 2) a 33 time-downscaling approach. The upscaling approach accounts for the persistent 34 effect of short term events, such as storms, on the shoreline position. The 35 downscaling approach accounts for the effect of long term shoreline modulation on 36 shorter event impacts. The multi-timescale model shows considerable improvement 37 compared to the direct-forcing approach in the original ShoreFor model at the four 38 contrasted sites. 39

40 **1 Introduction**

Sandy beaches are constantly adapting to changing wave forcing over a variety 41 of temporal scales (Larson & Kraus, 1995; Pianca et al., 2015; Almar et al., 2017), 42 which can be traced in cross-shore shoreline changes. Coastal variability, and 43 particularly erosion, can expose human- and ecosystems in the littoral zone to risk, 44 which implies that understanding and predicting shoreline evolution is of paramount 45 importance. However, it is not straightforward to predict shoreline variability at a 46 multitude of natural temporal scales from storm events to seasonal and inter-annual 47 evolution due to intrinsic limitations of current observation strategies. These 48 observational strategies generally focus on a particular spatial-temporal scale (Plant 49 et al., 2007; Bergsma & Almar, 2020). The same is true for many of the 50 equilibrium-based shoreline models (Montaño et al., 2020) that are optimized during 51 the calibration process for the single most dominant timescale of shoreline variability 52 in the training set. Quite often this results in models being skillful at either the 53 short-term (storm) timescale or optimized for the longer (seasonal to inter-annual) 54 timescales. Addressing all the timescales together is a major challenge and as a 55 result, current understanding on how the shorelines respond to different timescales 56 and how these timescales influence shoreline change is limited. In addition to these 57 temporal limitations, spatial restrictions exist. Most of the research on shoreline 58 change over the last decades has been conducted at storm-dominated mid-latitudes, 59 obscuring understanding to various mechanisms that play a role at different latitudes 60 (e.g Takbash & Young, 2019). In the mid-latitudes, winter storms or the seasonality 61 in the storms dominate the wave regime. Conversely, in the Tropics seasonal 62 monsoons can dominate the wave climate and shoreline changes instead of 63 paroxysmal storms such as tropical cyclones. At the equator, storm-free coasts are 64 seen, where inter-annual changes of wave regimes predominate. In the two latter 65 areas, climate modes exert a strong modulation of waves on inter-annual-, seasonal-66 and event-timescales such as tropical cyclones or monsoon pulses (Ondoa et al., 67 2017; Marchesiello et al., 2020). 68

Recent studies identified the persistent nature of short wave events on longer beach response timescales (Frazer et al., 2009; Anderson et al., 2010; Karunarathna et al., 2014; Angnuureng et al., 2017; Almar et al., 2017). This link between the different timescales is often missing when modelling the seasonal to inter-annual evolution of the coastline and storm impact persistence. For example, extremes (e.g.

storms and tropical cyclones) have both transient and persistent impact, individually 74 or in sequence (Anderson et al., 2010). Moreover, Angnuureng et al. (2017) showed 75 the influence of average winter storms on beach response and revealed that not only 76 the storm energy is important, but also the frequency of recurrence, highlighting 77 interactions between short-term storms and long-term evolution. They showed the 78 importance of the recurrence-frequency of extremes to beach erosion and post-event 79 reconstruction; such that the shoreline retreat was most governed by the first storm 80 in the sequence, while the impact of subsequent forcing events was less pronounced 81 (low cumulative impact), something that is also observed in Bergsma et al. (2019) 82 and follows the general equilibrium response of a beach (Yates et al., 2009; Davidson 83 et al., 2013; Splinter et al., 2014). Furthermore, a main outcome of recent studies in 84 tropical South East Asia (Almar et al., 2017; Thuan et al., 2019) is the long lag 85 (50–60 days) observed between monthly-averaged waves and shoreline location, while 86 the envelope of intra-seasonal monsoon events is in closer phase with the shoreline 87 location. Hence, the shoreline variation appears to be in equilibrium with energetic 88 wave conditions, rather than the monthly-averaged waves. This is in line with 89 observations by Jackson et al. (2002) at low-energy environments where the beach is 90 assumed to be in equilibrium with previous energetic wave events rather than with 91 current conditions. The beach is considered inactive the rest of the time. It is the 92 particularly long duration of winter monsoon events that presumably drive most of 93 the shoreline changes, with very gentle wave conditions in between which limit the 94 recovery potential, as observed elsewhere. 95

The understanding and prediction of coastal evolution is often simulated using 96 models that simulate hydrodynamics linked to morphodynamics that can roughly be 97 divided into three categories: the more complex and time-consuming process-based 98 models (Walstra et al., 2012, 2016; Callaghan et al., 2013; Roelvink et al., 2009), qq hybrid models (usually based on the equilibrium concept (Montaño et al., 2020)) 100 and more recently, machine learning models (Goldstein et al., 2019). Each of these 101 models are typically bound to the dominant spatial- and temporal scales of key 102 processes to model, and as a result they struggle, or become too computational 103 expensive, to account for dynamics at different timescales. Hybrid (equilibrium) 104 models are generally more computationally efficient in comparison to process-based 105 models and have been proven reliable on inter-annual timescales to simulate 106 shoreline behaviour (Miller & Dean, 2004; Yates et al., 2009; Davidson et al., 2013; 107 Splinter et al., 2014; Splinter et al., 2017). However, they typically account for a 108 single dominant physical process and need a large, site-specific, dataset for 109 calibration purposes (Splinter et al., 2013). A limitation to these models however, is 110 that only coastal processes observed during the calibration time-frame are accounted 111 for (Vitousek et al., 2017). Moreover, hybrid models do not explicitly account for all 112 113 individual processes that drive shoreline change but seek an overall behaviour pattern as response to the different processes. 114

In this paper we evaluate to what extent multiple timescales of dominant forcing- and beach response behavior co-exist and to what extent such behaviors can interact with different timescales of forcing and response. We aim to improve cross-shore multi-timescale shoreline predictions by using the single timescale ShoreFor model (SF-ST, see Appendix A for a model description) as a baseline model. The research uses data from four datasets with contrasting timescales and characteristics.

¹²² 2 Model training sites covering different wave environments

To train the SF-ST model, shoreline location and wave measurements are required. A source of shoreline data are shore-based video cameras that generally collect data during daylight on a 30-min basis (Holman & Stanley, 2007). In comparison to shoreline-walking GPS surveys, these video-based shorelines provide
 significantly better temporal resolution, which makes video-derived shorelines
 particularly suitable to study the importance of different, multiple, response
 timescales (Ondoa et al., 2020; Pianca et al., 2015).

In order to make the video-data suitable for SF-ST and to cover a wide range 130 of timescales (1 day to inter-annual timescales), all shoreline and wave forcing 131 datasets are interpolated (upsampled, corresponding to the value every 24-hours), 132 such that they have a temporal resolution of 1 day. Moreover, the raw shoreline 133 position data is detrended by a second order polynomial, to filter out shoreline 134 trends which have a larger temporal scale than the duration of the dataset. The 135 importance of multiple beach response timescales will be investigated at four 136 different study sites: Narrabeen (Australia), Nha Trang (Vietnam), Tairua (New 137 Zealand) and Grand Popo (Benin). These sites were chosen to cover different wave 138 environments and for the availability of daily shoreline data. All four beaches are 139 subjected to a small tidal range (microtidal, <2.0 m, <1.6 m, <2.0 m and <1.8 m, 140 respectively), such that SF-ST has an optimal model performance (Harley et al., 141 2011; Almar et al., 2017; Blossier et al., 2017; Ondoa et al., 2017), respectively. 142 Moreover, the beach dynamics are either dominated or largely influenced by 143 cross-shore processes. Furthermore, major differences between the wave conditions 144 are present at the four study sites. The wave climate at Narrabeen consists of small 145 (daily) timescale storms (and swell waves) and a larger temporal scale, but less 146 intense seasonal cycle. At Nha Trang, three distinct wave forcing timescales are 147 present: typhoons (daily), monsoons (monthly) and a seasonal variation (annual). 148 At Tairua, the wave climate is largely influenced by small timescale storm- and swell 149 waves (Bradshaw et al., 1991). At Grand Popo two timescales in the wave forcing 150 are present: on the one hand, wind- and swell waves (daily) and on the other hand a 151 considerable seasonal variation. 152

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2.1 Narrabeen-Collaroy, Australia

The Narrabeen-Collaroy beach (34^0 S) is situated near Sydney in the southeast 154 of Australia (Figure 1). The embayed beach is bound at the north and south by two 155 headlands. Narrabeen beach is situated in the north of the embayment and Collaroy 156 beach is situated in the south. In 2004, an ARGUS system (Holman & Stanley, 157 2007; Turner et al., 2016) was installed. In this paper, alongshore averaged shoreline 158 data a bit southwards of the center of the embayment is used (2400 m to 2800 m 159 from the northern edge of the embayment), in line with previous studies at this 160 beach (Davidson et al., 2013; Phillips et al., 2017). Narrabeen beach is characterised 161 by sand with a D50 of 0.4 mm. The wave climate is largely influenced by swells from 162 the SSE (mean $H_s = 1.6$ m and mean $T_p = 10$ s). Additionally, the wave climate 163 consists of larger waves $(H_s = 3 \text{ m})$ that originate from storm events and can hit the 164 coastline in any direction. Furthermore, a small seasonal cycle is present with on 165 average higher waves in the Australian winter- and milder waves in the Australian 166 summer months (Davidson et al., 2017). On larger timescales, effects of El-Nino 167 Southern Oscillation (ENSO) can play a role as well (Turner et al., 2016; 168 Ranasinghe et al., 2004; Harley et al., 2009). In this study, nearshore wave 169 time-series at the 10 m depth contour are used. 170

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2.2 Nha-Trang beach, Vietnam

A video system (Lefebvre et al., 2014; Thuan et al., 2016) was installed in 2013 at Nha Trang beach in Vietnam (12⁰ N) (Figure 1). The camera location is considered far enough for the beach not to be influenced by the edges of the bay (Almar et al., 2017). Cross-shore shoreline positions are estimated from this camera data on a daily basis. The shoreline location used in this paper is retrieved by



Figure 1. Overview of the model training sites and positions of the camera-stations from which high-resolution shoreline data is extracted. Top left: Narrabeen- and Colleroy beach embayment. Top center: the Nha Trang beach in Vietnam. Bottom left: Grand Popo beach in Benin. Right: Tairua beach in New Zealand.

alongshore averaging the video-derived shoreline data (over 75 m) from the northern 177 part of the bay relative to the camera location. Nha Trang beach is characterised by 178 sand with a D50 of 0.3 mm. Interestingly, the tropical wave climate at Nha Trang is 179 characterized by multiple wave conditions with a distinct timescale, of which the 180 seasonal variation is the most pronounced. The offshore annual mean significant 181 wave height H_s is 0.95 m, with an associated averaged peak period T_p of 6.2 s. 182 Typhoons typically occur on average 4-6 times per year between August and 183 November. The wave climate is also characterized by summer- and winter monsoons, 184 where the summer monsoons mainly consist of wind waves and the winter monsoons 185 of swell waves. The winter monsoons (October to April), which do not occur at the 186 same time as the typhoons, can generate waves up to 4.0 m, which can heavily affect 187 shoreline change. During fall and winter (October to April) the mean H_s is 1.2 m 188 and T_p is 6.8 s, while during spring and summer (May to September) the mean H_s is 189 reduced to 0.6 m with a shorter T_p below 5 s (Thuan et al., 2019). 190

¹⁹¹ 2.3 Tair

2.3 Tairua beach, New-Zealand

Tairua Beach is situated at the east coast of New Zealand's northern island 192 (37^0 S) (Figure 1). This 1.2 km long beach is situated in between two headlands, 193 where on the southern headland a video camera was installed in 1998. In this study, 194 high resolution shoreline data (alongshore averaged over the bay: 1050 m, see 195 Montaño et al. (2020)) is used, which is extracted from those camera images. Tairua 196 beach is characterised by sand with a D50 of 0.3 mm. The beach is subjected to 197 easterly and northeasterly swell and storm waves (Blossier et al., 2017). The offshore 198 wave climate has a mean H_s of 1.4 m, with up to 6 m during storm events (Smith & 199 Bryan, 2007). 200

201 2.4 Grand Popo beach, Benin

A video system was installed in 2013 at Grand Popo (6^0 N), Benin, situated in 202 the equatorial Gulf of Guinea, West Africa (Figure 1). It is an open-ocean, sandy 203 stretch of coast which is situated far from any anthropological influences. The 204 nearest one (20 km updrift) is a field of groynes, constructed in the last five years 205 (Ondoa et al., 2020; Anthony et al., 2019). Grand Popo beach is characterised by 206 sand with a D50 of 0.6 mm. Overall, the Gulf of Guinea can be considered as a 207 storm free region with only distant swells and wind seas locally generated in the 208 tropical band (6° N to 15° S) (annual mean $H_s = 1.36$ m, $T_p = 9.4$ s). Beach 209 dynamics are dominated by long swells that originate from the southern hemisphere 210 at high latitudes (Almar et al., 2015). Therefore, the wave climate consists of clear 211 seasonal (and inter-annual) variations, with more energetic waves during the 212 April-October period and less energetic waves during the November-March period. 213

3 Implementing multiple timescales and links between timescales in cross-shore shoreline model

We propose four steps to implement multiple dominant forcing and beach 216 response timescales within the SF-ST model and to assess its performance. The first 217 step is to distinguish timescales in the measured data using a filter function and 218 subsequently determine which timescales are dominant in the raw forcing and 219 shoreline position signals (Section 3.1). Then an approach to implement these 220 multiple dominant timescales in the SF-ST model is proposed (Section 3.2). This 221 implementation uses a threefold correspondence between the isolated timescales of 222 the wave data to the isolated timescales in shoreline data where the timescales that 223 are smaller, identical or larger are linked in a direct forcing, upscaling and 224 downscaling procedure (Sections 3.2.1, 3.2.2 & 3.2.3, respectively). The combined 225 model is referred to as ShoreFor Multiple Timescales (SF-MT). Subsequently, the 226 modelling calibration and validation phases are elaborated in Section 3.3. In 227 Appendix B model skill assessment and performance is discussed. 228

3.1 Distinguishing multiple timescales

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To distinguish timescales, the raw shoreline position and wave forcing (H_s, T_p) 230 data is filtered using a running average filter with varying (enlarging) window sizes. 231 The running average filter is used to allow for data-gaps in the datasets. Per 232 window, and hence timescale (i.e. 1 until the length of the time-series, with steps of 233 1 day), a residual variance of the shoreline position and wave forcing time-series is 234 calculated. With residual variance of the filtered signals a temporal spectrum is 235 constructed. In other words, we can plot the temporal spectrum as the (remaining) 236 variance of all filtered signals as a function of the timescale. Dominant timescales 237 are defined by the largest variance. In contrast to, for example Fourier spectra, the 238 linear superposition of all filtered signals is not equal to the raw signal since the 239 filter function is shape-preserving but not energy-conserving. By dividing the filtered 240 signals by a weighting value proportional to the window size of the running average 241 filter, energy is conserved and the raw signal can be reconstructed through linear 242 superposition. As a consequence, the energy (i.e. variability) for each filtered signal 243 reduces, where the difference is largest for the largest timescales, because the 244 window width increases with increasing timescales. A second temporal spectrum can 245 be constructed from the resulting signals, which is used to construct 246 timescale-clusters by dividing the spectrum into bins (i.e. bands). 247

When filtered wave-forcing and shoreline position signals are directly related (i.e. on a corresponding timescale) using SF-ST, the corresponding calibration parameters and resulting modelled shoreline position signals are partly dependent on

the variability of the related (input) signals. For example, the response value (i.e. c, 251 Equation A1), becomes smaller if the variability of the wave forcing becomes larger 252 (for the same shoreline signal), because the rate parameter (c) and wave energy flux 253 (P) determine the magnitude of the shoreline response (Splinter et al., 2014). Hence, 254 the variability of all (filtered) input signals has to be identical, when considering an 255 inter-comparison of modelled shoreline position signals on multiple timescales. 256 Therefore, timescale-clusters are used of which each cluster has an identical 257 variability. To that end, the previously obtained spectrum is employed and will 258 determine the number of timescale-clusters that is used for the multi-timescale 259 implementation. Timescale-clusters are formed by dividing the obtained temporal 260 spectrum into bins. Within such a bin a particular number of filtered signals can be 261 found. The linear superposition of all filtered signals within a bin results in a 262 time-series which represents a particular timescale (i.e. a timescale-cluster). The 263 bin-distribution is based on an equal amount of shoreline response variation within 264 each bin. In this way, all resulting timescale-clusters, which represent certain 265 timescales, will have the same variance. The variability within a bin is equal to the 266 signal with the largest variability in the spectrum, otherwise the variability of that 267 signal does not fit within the bin. This means that only one filtered signal fits within 268 the bin at the point corresponding to the peak of the spectrum. For other bins, 269 multiple filtered signals can fit in a bin, because the variability of those individual 270 signals is lower. The lower the variability of the spectrum, the wider the bins, the 271 more filtered signals fit within a bin. Hence, the bin distribution is determined by 272 adding up filtered signals (starting with the signal that has a timescale of 1 day), 273 until that summation reaches the maximum variability of the bins. For the 274 remaining filtered signals, a new bin is used. This procedure is continued up to the 275 point where all filtered signals fall within a bin. 276

In the wave forcing spectra (i.e. the individual spectra for H_s and T_p), an 277 identical bin-distribution is used as such that corresponding timescale-clusters are 278 formed. Thereafter, the different timescale-clusters in the wave forcing data (H_s and 279 T_p) are related to ones in the shoreline data on multiple scales. The interactions 280 between the wave forcing and shoreline position timescale-clusters on multiple 281 timescales are based on three approaches: the direct forcing-, the upscaling- and 282 downscaling approach. The combined model is referred to as ShoreFor Multiple 283 Timescales (SF-MT). 284

3.2 Implementing multiple timescales

In this section the multi-timescale implementation within the SF-ST model is 286 governed by introducing the three separate terms: the direct forcing-, upscaling- and 287 downscaling approach (Section 3.2.1, 3.2.2, 3.2.3, respectively). The direct forcing 288 approach relates corresponding timescale-clusters in the wave and shoreline position 289 data. The upscaling approach accounts for the persistent effect of short wave events 290 on the shoreline position. The downscaling approach accounts for the effect of the 291 longer timescales in beach variation on the impact to shorter forcing events by 292 introducing a time-dependent response factor. 293

²⁹⁴ 3.2.1 Direct Forcing

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In the direct forcing approach all timescale-clusters in the wave forcing data $(H_s \& T_p)$ are related to corresponding timescale-clusters in the shoreline position data, following:

$$\frac{dx_i}{dt} = c(F(\phi)_i^+ + rF(\phi)_i^-) \tag{1}$$

in which i is an indicator of the fact that corresponding timescale-clusters are linked 298 to each other. Note that the standard single timescale ShoreFor model (SF-ST, see 299 Appendix A) is adapted in the direct forcing approach (except for the linear trend 300 term), but it is applied multiple times: for each timescale-cluster with a distinct 301 timescale. The linear trend term (b) is omitted from the model, because otherwise a 302 linear trend will be present for every predicted shoreline signal (for every band). 303 Within each band, no linear trend is present as the filter function only captures 304 timescales which are smaller than the full length of the dataset. Hence, b should be 305 zero when the full time-frame is considered. However, during the calibration phase 306 only part of the entire dataset is used such that a (small) trend can be present. 307 Subsequently, this trend will be assigned to b. As this linear trend will be 308 extrapolated during the validation phase, it will result in a wrong shoreline 309 prediction as no trend is present over the full period. 310

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3.2.2 Upscaling: the long-term persistence of short-timescales

To include the relation between small wave forcing timescales and larger timescales in shoreline response, as small timescale wave forcing events (e.g. storms) can have a considerable and persistent effect on larger beach response timescales (e.g., Frazer et al., 2009; Anderson et al., 2010; Almar et al., 2017), an upscaling approach is proposed. This is described mathematically as follows:

$$\frac{dx_j}{dt} = c(F(\phi)_{i \to j}^+ + rF(\phi)_{i \to j}^-) \tag{2}$$

wherein the subscript indices i and j indicate the timescales: i is the small timescale and j the larger one (j>i). The upscaling effect is indicated with an arrow. In this model improvement step the ShoreFor model equation has kept its original form (Equation A1), while only the forcing is represented differently.

This upscaling effect is evaluated by using an envelope (based on spline 321 interpolation) of wave forcing timescale clusters that links the two different 322 timescales. Figure 2 shows an example of an envelope (black-dashed) of a significant 323 wave height timescale-cluster (black-solid), where it is clearly visible that the 324 envelope has a larger timescale than the wave height signal. A similar approach is 325 followed for the wave period. The envelopes representing the wave height and wave 326 period will be related to the corresponding shoreline timescale-cluster (red-solid). 327 The resulting modelled shoreline is represented by the red-dashed time-series in 328 Figure 2. 329

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3.2.3 Downscaling: the changing efficiency of short timescales due to long-term variations

The incorporation of the effect of large timescale shoreline variations on the efficiency with which smaller timescale wave-forcing events induce cross-shore sediment transport is achieved by a so-called downscaling approach. This step ensures that smaller beach response timescales can be accounted for, if larger ones dominate. The downscaling approach is compared to SF-ST slightly adapted and can be mathematically described as follows:

$$x_i(t) = c_j(t) \int_0^t (F(\phi, t)_i^+ + rF(\phi, t)_i^-) dt$$
(3)

in which the subscript indices i and j indicate the timescales, where j > i.

³³⁹ Downscaling can be further explained by the time-series in Figure 3. The dynamic



Figure 2. The upscaling approach: modelling the persistent effect of extreme forcing events on the longer term state of the beach. The effect of the small timescale wave height time-series (black-solid) on a larger shoreline position timescale (red-solid) is modelled using the envelope of the wave height time-series (black-dashed), which creates the timescale link. A similar approach is followed for the wave period. The resulting modelled shoreline is given by the dashed red line.



Figure 3. The downscaling approach: modelling the effect of long term shoreline trends on extreme event impacts. The solid black time-series represents the wave height. The effect of the larger timescales in shoreline variation on the efficiency with which smaller timescale wave-forcing events induce cross-shore sediment transport is modelled by using a dynamic response factor (black-dashed), which has the shape of the larger timescale shoreline variation signal. The shoreline signal with a smaller timescale is indicated by the solid red time-series and the resulting modelled shoreline signal is indicated by the red dashed line. Hence, if the shoreline on a larger timescale is accreted (e.g. October 2013, high dynamic response factor), the relative (compared to the wave forcing) shoreline response on a smaller timescale is large (higher sediment transport efficiency).

response factor $(c_i(t))$ (black-dashed) has the shape of the considered large timescale 340 shoreline variation to account for a variable sediment transport efficiency, because 341 beach response to small timescale high-intensity wave forcing events (red-solid) can 342 depend on this larger timescale shoreline variation (i.e. the initial state of the 343 beach). The figure shows that if the shoreline on a larger timescale is accreted (e.g. 344 October 2013, high dynamic response factor), the relative (compared to the wave 345 forcing, black-solid) shoreline response on a smaller timescale (red-solid) is large 346 (higher sediment transport efficiency). Conversely, if it is eroded (e.g. January 2014, 347 low dynamic response factor), the relative shoreline response is low (limited 348 sediment transport efficiency). The resulting modelled shoreline time-series is 349 indicated by the dashed red line in Figure 3B. 350

The justification of the downscaling approach consists of three components: 1) the influence of large timescale shoreline variations on beach response to small timescale high-intensity forcing events as observed in measurements, 2) modelling of small beach response timescales with the direct forcing approach and 3) modelling of small beach response timescales with the downscaling approach.

When a forcing event of a small temporal scale (e.g. storm/monsoon) impacts 356 the coastline, the beach response can depend on whether that coastline is eroded or 357 accreted on a larger temporal scale (e.g. due to a seasonal variation). Or stated 358 otherwise, on the initial state of the beach (Aagaard et al., 2005). For a beach in the 359 state of erosion, a minor retreat of the shoreline location is expected due to the 360 presence of an erosion profile. For an accreted beach a larger beach response is 361 expected. If the period between two similar high-intensity forcing events is very 362 small compared to the calibrated memory decay factor $(\langle 2\phi \rangle)$, the direct forcing 363 approach is already able to model the fact that the subsequent forcing events 364 correspond to a different beach response. The (modelled) response to the second 365 forcing event is lower, because the coastline is already closer to the equilibrium with the high-intensity forcing conditions. This is due to the dynamic equilibrium 367 condition (Equation A4) which introduces a negative feedback mechanism: the 368 disequilibrium between the present and the antecedent forcing is lower during the 369 second forcing event. This mechanism ensures that if two high-intensity forcing 370 events approach the coastline shortly after each other, the cumulative shoreline 371 recession is limited (Davidson et al., 2013). However, if the period between two 372 similar high-intensity forcing events is considerably larger than the memory decay 373 factor $(>2\phi)$, the direct forcing approach is not able to model a different beach 374 response due to a different initial state of the beach (i.e. a varying shoreline on a 375 larger timescale). Due to the constant response factor (i.e. c; Equation 1) and the 376 large period between the two short high-intensity forcing events, the direct forcing 377 approach will model two beach responses with the same erosional amplitude. Hence, 378 no connection is present between the larger timescale shoreline variation and the 379 modelled small timescale beach response to high-intensity forcing conditions. 380

To implement the dependency of small timescale beach response (to short 381 high-intensity forcing events) on large timescale beach variations, a time-varying 382 response factor is used (i.e. c(t); Equation 3). This dynamic response factor 383 represents the changing efficiency over time with which waves induce cross-shore 384 sediment transport and is a function of the spatial separation between the shoreline 385 and the offshore sediment source (e.g. sand bars(s)). This spatial separation 386 normally scales with the surfzone width imposed by the antecedent waves, with 387 lower response rates for erosion profiles (wide surfzone) due to the inefficient transfer 388 of sediment between the offshore region and the beach face. Conversely, as the 389 offshore sand supply is migrated closer to the shoreline (narrow surfzone; accreted 390 beach), the sediment transport efficiency increases, facilitating faster response. 391 Therefore, the dynamic response factor has the shape of a large timescale shoreline 392 signal. Now, the response to a short high-intensity forcing event is higher (large 303 sediment transport efficiency) when the beach (on a larger time scale) is accreted and lower (small efficiency) when the beach is already eroded. 395

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3.3 Model calibration and validation

The modelling of cross-shore shoreline change on multiple timescales is divided in two phases: model calibration and model validation. During model calibration the site-specific model free parameters $(c_i \& \phi_i)$ are determined using the wave forcing- $(H_{s,i} \text{ and } T_{p,i})$ and shoreline data $(x_{s,i})$, where the subscript *i* indicates the multiple predictions from the direct forcing-, upscaling- and downscaling approaches. At the time of model validation, wave forcing data is used as model input only and

Dataset	Calibration time-frame	Validation time-frame	Data-gaps shoreline position [%]
Narrabeen	01-08-2004 /	11-07-2010 /	25
	10-07-2010	19-04-2015	
Nha Trang	27-07-2013 /	01-01-2015 /	20
	31-12-2014	01-11-2015	
Tairua	02-01-1999 /	01-01-2009 /	0
	31-12-2008	31-12-2013	
Grand Popo	20-02-2013 /	23-11-2015 /	40
	22 - 11 - 2015	22-06-2016	

 Table 1.
 Calibration- and validation time-frames of the Narrabeen-, Nha Trang-, Tairua and

 Grand Popo dataset, as well as the percentages of data-gaps in the shoreline position data (based on daily data).

together with the calibrated parameters shoreline predictions are generated. Table 1

⁴⁰⁴ presents the calibration and validation time-frames for all four datasets.

⁴⁰⁵ Furthermore, note the difference in the percentages of data-gaps in the shoreline

⁴⁰⁶ position data (the wave forcing data is continuous for all four study sites).

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3.3.1 Calibration of the downscaling approach

While the calibration method for the direct forcing and upscaling approach is 408 similar to that of the SF-ST model, the calibration method for the downscaling 409 approach is slightly different considering that the dynamic response factor (c(t)) has 410 the shape of a larger timescale shoreline signal. However, this dependency poses a 411 problem as during validation the model must generate shoreline predictions which 412 are solely based on wave forcing (shoreline data is not available). Hence, a different 413 approach is needed to generate the shape of the dynamic response factor. To that 414 end, note that the modelled signals from the direct forcing and upscaling approach 415 are available before applying the downscaling approach and will therefore be used to 416 capture the total shoreline response to come up with a shoreline signal. 417 Subsequently, that shoreline signal will be filtered to generate timescale-clusters that 418 can be used as dynamic response factors. However, during the direct forcing and 419 upscaling approach multiple shoreline time-series with different timescales are 420 generated (Equations 1 and 2) and not all those signals will equally contribute to 421 the total shoreline change prediction at the considered site; some will have no 422 contribution at all. Therefore, a linear least-squares solver with bounds is used (after 423 the determination of the model free parameters) to find which summation of 424 predicted shoreline signals fits best to the raw measured shoreline position data. The 425 procedure can be written down in the following manner: 426

$$\min_{k} \frac{1}{2} ||\mathbf{C} \cdot \underline{k} - \underline{d}||^2 \text{ with } 0 \le \underline{k} \le 1$$
(4)

In which the matrix \mathbf{C} contains all the individual modelled shoreline signals 427 (time-series) with a distinct timescale that are generated using the direct forcing and 428 upscaling approach, d the vector containing the measured shoreline data, the double 429 vertical lines represent the mathematical norm and \underline{k} the calculated vector 430 containing values between the lower (zero) and upper (one) bound. Individual 431 modelled shoreline signals (resulting from Equations 1 and 2) which are not 432 important for the total shoreline prediction attain a zero value, whereas the most 433 important signals attain a value of one. The matrix C only contains modelled 434 shoreline signals that have a relatively high correlation with the corresponding 435

measured time-series. Modelled shoreline signals with a relatively low correlation 436 (with the corresponding measured time-series) result from a poor relation between 437 the wave forcing and shoreline data and are therefore not used. The thresholds 438 indicating a low/high correlation are determined through the fitting of a normal 439 distribution to all correlation values per model improvement step. The thresholds 440 indicating a high correlation are set to an optimized probability of exceedance of 441 90%, for both the direct forcing and upscaling approach. This ensures that most 442 signals will be used as input for the linear least-squares solver and only the poorest 443 modelled shoreline signals are omitted. Subsequently, the resulting total shoreline 444 signal is filtered and timescale-clusters are generated following the same 445 bin-distribution as was used to determine the timescale-clusters for the direct forcing 446 and upscaling approach. These timescale-clusters are used as the dynamic response 447 factor, such that all shoreline predictions in the validation phase, using the three 448 modelling approaches, can be generated by the wave forcing only. Note that this 449 procedure implies that shoreline predictions generated with the downscaling 450 approach are partly based on shoreline predictions generated with the direct forcing 451 and upscaling approach. 452

3.3.2 Predicting the total shoreline change

Now, the procedure following Equation 4 is applied again, but with modelled 454 shorelines of all three approaches. The thresholds were adapted, which resulted in 455 the P90, P75 and P50 probability of exceedance for the direct forcing, upscaling and 456 downscaling approach, respectively. The probability of exceedance is higher for the 457 direct forcing approach as there are less shoreline signals generated using that 458 approach (N in case of N timescale-clusters, while for the up- and downscaling 459 approach $(N^2 - N)/2$ signals are generated). Note that the summation of modelled 460 shoreline signals that will model the total shoreline change during the calibration 461 phase $(\sum \mathbf{C} \cdot \mathbf{k})$, is also responsible for modelling shoreline change during model 462 validation ($\sum \mathbf{D} \cdot \mathbf{k}$, where **D** is the matrix containing the individual predicted 463 shoreline signals for the validation phase). 464

465 4 Results

453

In this section, calibration (Section 4.1) and validation (Section 4.2) results are presented, when SF-ST and the multi-timescale model (SF-MT) are applied to all four datasets. An overview of model results assessed by four different model skill indicators (correlation, NMSE, BSS & AIC), is presented in Section 4.3.

Table 2 provides information regarding the four datasets at the model training 470 sites used in this study: Narrabeen, Nha Trang, Tairua & Grand Popo. The number 471 of timescale bins is presented, which represents the number of timescale-clusters used 472 in the multi-timescale implementation. Or stated otherwise, in how many bins the 473 temporal spectra are divided. Note that at Grand Popo a limited number of 474 timescale bins is used (i.e. 9): this is the maximum number of bins for which the 475 requirement of identical shoreline variability within each bin (Section 3.1) can be 476 met. The most striking difference between the datasets is the number of dominant 477 timescales in the shoreline position and wave forcing data (i.e. local maximums in 478 the temporal spectra, Section 3.1 and Figure C1). 479

At Narrabeen, only one dominant timescale is found in the shoreline position signal that is related to the seasonal variation (i.e. 322 days, Table 2). Besides the seasonal variation, the storm/swell timescale is dominant in the wave forcing data (i.e. 2-14 days). At Nha Trang, two dominant timescales are present in the wave forcing: the monsoon- and seasonal timescale, which implies that typhoons are not dominant. In the shoreline position signal, only the seasonal variation is dominant.

Dataset	Timescale bins	Dominant timescale shoreline position [days]	Dominant timescale wave forcing [days]
Narrabeen	45	322	2-14 & 350
Nha Trang	35	302	10-26 & 314-342
Tairua	23	34 & 434-806	2-10
Grand Popo	9	6 & 46 & 326	10 & 94 & 358

Table 2. Information of the Narrabeen-, Nha Trang-, Tairua and Grand Popo dataset.Dominant timescales are defined as local maximums in the temporal spectra (see Appendix C).

At Tairua, a monthly- and seasonal- to inter-annual timescale is dominant in the shoreline position signal, while storms/swells dominate the wave climate. At Grand Popo even more dominant timescales are found in the shoreline position data: a storm/swell-, an approximately monthly- and a seasonal timescale. In the wave forcing data three dominant timescales can be found as well: a storm/swell data three dominant timescales are been as the found as well: a storm/swell

timescale, a timescale of approximately 3 months and a seasonal timescale.

4.1 Calibration

492

Figure 4 presents the results (calibration and validation) when SF-ST (black) 493 and SF-MT (red) are applied to the datasets at Narrabeen (top), Nha Trang (second), Tairua (third) and Grand Popo (bottom). The transition between the 495 calibration and validation time periods is indicated with a dashed black line. Figure 496 5 presents the contribution of each model improvement step over time (left, in 497 similar order) and the corresponding relative contribution of each model 498 improvement step (right) for the calibration period only. The blue, orange and 499 purple lines correspond to the direct forcing, upscaling and downscaling approaches, 500 respectively. In Figure 6 the standard deviation per timescale-cluster is shown (left 501 panels) for the shoreline position data (green), the SF-ST (black) and SF-MT (red) 502 model result (calibration + validation) for all datasets (in similar order as Figure 4 503 and 5). In the middle panel the correlation between the SF-MT model result (and 504 SF-ST) and the shoreline position data is presented on all different timescales. In 505 the right panels, a model score is given for each of the three model improvement 506 steps for all different timescales. The score for every timescale consists of the 507 correlation coefficient (model result - data on that particular timescale) multiplied 508 by standard deviation of that modelled signal, timescale and model improvement 509 step. Using this modelling result score means that 1) if the correlation between the 510 data - model is high, the model is able to reproduce shoreline change at this 511 timescale, 2) if the standard deviation of the model result is high, that particular 512 shoreline signal is important in determining shoreline change according to Equation 513 4. 514

For the Narrabeen dataset (top panel in Figure 4) SF-ST (black) is able to 515 capture the smaller timescale storm/swell response (order of days), but the larger 516 timescale shoreline variations are captured to a lesser extent ($\phi = 3$ days and c =517 $10^{-7} (m/s)/(W/m)^{0.5}$). The SF-MT model (red) also captures the storm 1.96* 518 timescale to a certain extent, but yields a considerable increase in skill (BSS of 0.61) 519 by better capturing shoreline change on larger timescales (larger than the storm 520 timescale). This occurs for example in 2009, where first the large erosion period 521 halfway through 2009 is captured well by the SF-MT model and poorly by SF-ST, 522 while the same occurs for the accretive period during the second half of 2009. 523 Overall the SF-MT model yields a better fit to the data, compared to SF-ST, which 524 seems to underestimate the amplitude of shoreline accretion/erosion most of the 525

time. This is emphasized by the NMS error between the data and model result, 526 which is 0.71 for SF-ST and reduces to 0.29 for the SF-MT model. This corresponds 527 to a 'fair' and 'excellent' rating for SF-ST and SF-MT, respectively. The standard 528 deviation and correlation plot per timescale (Figure 6A) shows that for storm/swell 529 timescales (1-12 days) SF-ST has a higher standard deviation and a similar 530 correlation. Hence, the smaller storm timescales are better captured by the SF-ST 531 model. However, for SF-MT the standard deviation multiplied with the correlation 532 is higher for timescales larger than 33 days (up to 2285 days). Hence, the dominant 533 seasonal timescale is better captured by the SF-MT model, which contributes most 534 to the model improvement. Moreover, the upscaling approach contributes 535 considerably (73%) to the total shoreline signal (orange lines in Figure 5A). The 536 larger timescales are captured by the upscaling and downscaling (purple, Figure 6A) 537 approaches whereas the smaller (storm) timescales are captured by the downscaling 538 approach as well. The direct forcing approach (blue) has a limited contribution to 539 the total model result (7%, Figure 5A), compared to the upscaling (73%) and 540 downscaling (20%) approach. 541

At Nha Trang considerable improvement is made by implementing multiple 542 timescales within the SF-ST model (Figure 4B), which is emphasized by a BSS of 543 10^{-8} 0.62 (i.e. an 'excellent' rating). Where SF-ST ($\phi = 180$ days and c = 4.61 * 544 $(m/s)/(W/m)^{0.5}$ only partially captures the seasonal timescale (the most dominant 545 timescale, see Table 2 and Figure C1), the SF-MT model captures both the response 546 to monsoons and the seasonal variation in wave data (i.e. the two dominant 547 timescales in the wave data). The NMS errors for SF-ST and SF-MT with the data 548 is 0.31 ('good') and 0.13 ('excellent'), respectively. Figure 6B shows that the 549 standard deviation and correlation per timescale for SF-MT (red) are high and 550 relatively uniformly distributed across the different timescales. This states that all 551 timescales are well captured. For SF-ST (black) the correlation is lower for all 552 timescales except for the seasonal variation, where the correlation is similar. The 553 standard deviation is lower/higher for timescales smaller/larger than 78 days. If 554 both indicators are combined, it becomes clear that the largest contributor to the 555 model improvement of SF-MT are the smaller timescales (i.e. the monsoons). 556 Furthermore, note that an improvement is already made by using the upscaling 557 approach only (orange line Figure 5B). However, in that case, only the response to 558 the seasonal variation is captured. The response to monsoons (timescale of ≈ 20 559 days) is captured by the downscaling approach (purple). The relative contribution of 560 each model improvement step indicates as well that the seasonal timescale 561 (upscaling) is the most dominant (70%) in determining coastline evolution, followed 562 by the monsoon response (downscaling, 23%). Figure 6B implies as well that the 563 downscaling approach captures the smaller timescales (monsoons), while the larger 564 565 timescales (seasonal variation) are captured by the upscaling approach.



Figure 4. Model calibration and validation results using SF-ST (black) and SF-MT (red) for the dataset at Narrabeen (top), Nha Trang (second), Tairua (third) and Grand Popo (bottom). Note that the measured data is indicated in blue. The black dashed line indicates the discrimination between the calibration- and validation period.



Figure 5. Contribution of each model improvement step over time (left panels) for the dataset at Narrabeen (top), Nha Trang (second), Tairua (third) and Grand Popo (bottom). Note that the measured data is indicated in black and the direct forcing-, upscaling- and downscaling approach are indicated in blue, orange and purple, respectively. Right: the corresponding relative contribution of the three model improvement steps.

566	From Figure 4C it becomes clear that the SF-ST (black, $\phi = 150$ days and $c =$
567	$1.03 * 10^{-7} (m/s)/(W/m)^{0.5}$) and SF-MT (red) model both capture shoreline change
568	well for the dataset at Tairua and at first sight model differences are less pronounced
569	than for the dataset at Narrabeen and Tairua. The NMS error indicates that there
570	are differences: 0.51 for SF-ST and 0.36 for SF-MT. However, they both correspond
571	to a 'good' rating, although the error is considerably lower for SF-MT. This
572	difference is also emphasized by the BSS of 0.3, indicating that the SF-MT is a
573	'good' improvement compared to SF-ST. The better model capability of SF-MT to
574	capture shoreline change is emphasized as well in Figure 6C: both the standard
575	deviation and the correlation for storm to monthly dominant timescales are higher
576	for SF-MT. Those figures show as well that for the dominant seasonal to
577	inter-annual timescales shoreline change is captured well by both models. However,
578	there are certain moments in time where the SF-MT model outperforms SF-ST.
579	This occurs for example at the end of 2006/beginning of 2007, where the accretion
580	period is not well captured by SF-ST (Figure 4C). From Figure 5C and Figure 6C



Figure 6. Standard deviation of the shoreline signals per timescale-cluster (left) for the data (green), SF-ST (black) and SF-MT (red), considering the dataset at Narrabeen (top), Nha Trang (second), Tairua (third) and Grand Popo (bottom). The second column indicates the correlation coefficient between the model result and data for SF-ST (black) and SF-MT (red) for every timescale-cluster and dataset. The third column shows a modelling score per timescale-cluster and model improvement step. The score consists of the correlation coefficient (data-model result) multiplied by the standard deviation (of the model result) at every timescale-cluster and for every model improvement step. The blue-, orange- and purple lines represent the direct forcing-upscaling and downscaling approach, respectively.

becomes clear that the larger dominant seasonal to inter-annual timescales are
modelled using the upscaling approach (orange, 57%), the smaller timescales are
modelled using the downscaling (monthly timescale, purple, 27%) and direct forcing
approach (storm/swell timescale, blue, 16%).

At Grand Popo the difference in capturing shoreline change between SF-ST (ϕ = 7 days and $c = 7.63 * 10^{-8} (m/s)/(W/m)^{0.5}$) and the SF-MT model is minor (Figure 4D). The NMS error between the data and SF-ST model result is 0.62 (a 'fair' rating), while it is 0.52 (a 'good' rating) for SF-MT. The BSS is 0.18, which corresponds to a 'fair' model improvement. The small difference between the two model results arises from the fact that the most dominant seasonal timescale is

captured moderately better using SF-MT. This is emphasized in Figure 6D, where 591 the correlation and standard deviation is similar and/or higher for SF-MT for the 592 seasonal timescale. The daily to monthly timescales are captured with similar skill, 593 or perhaps better using SF-ST as in particular more variability is present at those timescales, while the correlation is more or less the same. Figure 5D and Figure 6D 595 show that the seasonal timescale is modelled by the direct forcing (blue) and 596 upscaling (orange) approach and the storm/swell to monthly timescales by the direct 597 forcing approach as well. The direct forcing approach contributes most to capturing 598 shoreline change (47%), while the upscaling approach is responsible for modelling 599 36% of the shoreline variability. Signals generated with the downscaling approach 600 have little contribution to the total modelled shoreline change signal (17%). It can 601 be that this is due to the storm-free wave climate, for which the response could 602 normally be captured by the downscaling approach. Nevertheless, the swell timescale 603 is predicted poorly, even though this is a dominant mode of shoreline response 604 (Table 2). 605

4.2 Validation

606

During model validation wave data in combination with the calibrated free parameters found in Section 4.1 are used to predict shoreline evolution. However, measured shoreline data is still available and is used to compare with the shoreline predictions. For the validation phase, shoreline predictions are shown in Figure 4 as well.

The validation results at Narrabeen reveal that the result of SF-MT 612 outperforms that of SF-ST, but differences are less pronounced as for the calibration 613 phase (BSS of 0.26 or a 'good' rating, compared to 0.61 or an 'excellent' rating for 614 the calibration phase). From the time-series in Figure 4A, it becomes clear that 615 especially after 2013, the prediction of SF-MT is closer to the data than the 616 prediction of SF-ST. The NMS error between the data and model prediction is 0.83617 for the SF-ST model, which reduces to 0.61 for the SF-MT model. This corresponds 618 to a 'poor' and 'fair' rating, respectively. The overall variability of the beach is 619 better represented by the SF-MT model, which is emphasized by the correlation 620 coefficient (0.45 compared to 0.62, for SF-ST and SF-MT, respectively). 621

The model validation phase at Nha Trang shows similar characteristics as for 622 the calibration phase as the seasonal variation and the response to summer- and 623 winter monsoons are well predicted by SF-MT, while the SF-ST model only partially 624 captures the seasonal variation (Figure 4B). The NMS error for SF-ST and the 625 SF-MT model is 0.63 and 0.26, which corresponds to a 'fair' and 'excellent' rating, 626 respectively. The similar characteristics for the calibration and validation phase are 627 also emphasized by the BSS, which is 0.61 for the validation phase while it was 0.62628 for the calibration phase (i.e. an 'excellent' rating). 629

A comparison of the validation results for both models at Tairua (Figure 4C) shows that some improvement is made by implementing multiple timescales in SF-ST, especially during the last 2 to 3 years of the dataset (BSS of 0.18 or a 'fair' model improvement). Overall, the SF-MT model predicts shoreline change better than SF-ST, which results in a decrease in the NMS error of 18% and an increase in the correlation coefficient of 8% (Table 3). The rating of the NMS error for SF-ST and SF-MT is 'fair' and 'good', respectively.

For the validation phase at Grand Popo a considerable improvement is made, which results in a NMS error of 0.47 for the SF-MT model (a 'good' rating), compared to 0.65 for SF-ST (a 'fair' rating). Signals generated by the direct forcing and upscaling approach contribute most to the improvement as those signals that

Site	Indicator	Calibration			Validation		
		SF-ST	SF-MT	%	SF-ST	SF-MT	%
Narrabeen	R	0.52	0.85	63	0.45	0.62	38
	NMSE	0.71	0.29	-59	0.83	0.61	-27
	BSS	-	0.61	-	-	0.26	-
	ΔAIC	-	>1	-	-	<1	-
Nha Trang	R	0.83	0.94	13	0.86	0.89	3
	NMSE	0.31	0.13	-58	0.63	0.26	-59
	BSS	-	0.62	-	-	0.61	-
	ΔAIC	-	>1	-	-	<1	-
Tairua	R	0.70	0.85	21	0.60	0.65	8
	NMSE	0.51	0.36	-29	0.71	0.58	-18
	BSS	-	0.3	-	-	0.18	-
	ΔAIC	-	>1	-	-	<1	-
Grand Popo	R	0.62	0.73	18	0.47	0.60	28
	NMSE	0.62	0.52	-16	0.65	0.47	-28
	BSS	-	0.18	-	-	0.30	-
	ΔAIC	-	<1	-	-	<1	-

Table 3.Model skill during the calibration and validation phase, for the SF-ST and SF-MTmodel, at all four sites, using four model skill indicators.

make sure that the dominant seasonal variation is better captured (as observed in Section 4.1). The BSS is 0.30, which corresponds to a 'good' rating.

4.3 Overview model improvement

Table 3 presents the modelling skill of the SF-ST and SF-MT model, per study site, for the calibration and validation phase by using four different model skill indicators: the correlation coefficient, the NMS error, the BSS score and Δ AIC.

For the dataset at Narrabeen the model improvement during the calibration 647 phase is considerable (BSS of 0.61 or an 'excellent' rating), while it is less 648 pronounced for the validation phase (BSS of 0.26 or a 'good' rating). The 649 correlation coefficient is substantially larger for SF-MT during the calibration as well 650 as for the validation phase (63% and 28%, respectively). The ΔAIC score (difference 651 in AIC score between SF-ST and SF-MT) is larger than 1 for the calibration phase 652 and smaller than 1 for the validation phase. This indicates that a considerable 653 model improvement is acquired during the calibration phase. Conversely, during the 654 validation phase the SF-ST model is preferred according to this score, due to the 655 trade-off between the model's simplicity and goodness of fit. The ΔAIC score 656 indicates that for the SF-MT model the number of calibration parameters (i.e. 657 decreased model simplicity), which is penalized for by the AIC score (Equation B3), 658 is too large compared to the goodness of fit (relative to SF-ST). 659

Considering the Nha Trang dataset, model improvement is large for the 660 calibration phase as well as for the validation phase, as the NMS error rating 661 increases from a 'good' rating to an 'excellent' rating and a 'fair' to 'excellent' rating 662 for the calibration and validation phase, respectively. The correlation coefficient is 663 improved less considering the calibration and validation phase (13% and 3%)664 respectively) when comparing SF-MT to SF-ST. This is due the fact that both 665 models capture and correlate with the (most) dominant seasonal response. The BSS 666 also indicates substantial model improvement during model calibration and 667 validation, corresponding to an 'excellent' rating for both phases. The ΔAIC score is 668 larger/smaller than 1 for the calibration/validation phase. This implicates that 669 during the calibration phase the larger number of calibration parameters in the 670 SF-MT model is justified by a considerably better model fit (relative to SF-ST), 671 while this is not the case for the validation phase. 672

At Tairua, the NMS error is moderately decreased by using SF-MT compared 673 to SF-ST during the calibration and validation phase (29% and 18%, respectively). 674 The same is true for the correlation coefficient, with increases of 21% and 8%, while 675 the BSS corresponds to a 'good' and 'fair' rating for the calibration and validation 676 phase, respectively. The moderately increased performance of SF-MT over SF-ST 677 can partly be explained by the fact that both models capture the most dominant 678 seasonal to inter-annual response, while the SF-MT model better captures shoreline 679 change on the dominant monthly timescale. The ΔAIC score is larger than 1 for the 680 calibration phase and smaller than 1 for the validation phase. This indicates that a 681 considerable model improvement is acquired during the calibration phase, while 682 during the validation phase the SF-ST model is preferred due to the model's 683 simplicity compared to the relative goodness of fit. 684

For the calibration phase at Grand Popo, model improvement is less impressive 685 compared to other sites as the NMS error reduces from 0.62 (a 'fair' rating) to 0.52686 (a 'good' rating) for SF-ST and SF-MT, respectively. For the validation phase the 687 improvement is more pronounced (28%). For both modelling phases the correlation coefficient is increased as well, when comparing SF-ST to SF-MT (18% and 28% for 689 the calibration and validation phase, respectively). The BSS for the calibration 690 phase yields a 'fair' rating. The BSS for the validation phase yields a 'good' rating, 691 which indicates that the model result of SF-MT is considerably closer to the 692 measured data than the baseline prediction (i.e. the SF-ST model). Note that all 693 scores are larger for the validation phase than for the calibration phase, which is 694 probably due to the fact that the validation time-frame is rather short (Table 1). 695 The ΔAIC score is smaller than 1 for both modelling phases, indicating that SF-ST 696 is the preferred model because of the model's simplicity relative to the goodness of 697 fit. 698

5 Discussion

This work was motivated by the fact that single memory decay models fail to 700 reproduce shoreline evolution at equatorial West-African and tropical Vietnamese 701 sites over timescales of 2-3 years, where multiple forcing timescales are present, such 702 as seasonal and monsoon forcing. In this paper, we focused on a single memory 703 decay hybrid model that predicts temporal changes of the shoreline location due to 704 varying wave conditions. Although there are hybrid models that account for 705 shoreline change due to for example cross-shore and longshore processes, sea level 706 rise and include the beach-dune system (e.g., Antolínez et al., 2019; Vitousek et al., 707 2017; Robinet et al., 2018, 2020), here the focus was on shoreline changes due to 708 cross-shore processes only. The hybrid model used here as a base is the ShoreFor 709 model (SF-ST; Shoreline Forecast - Single Timescale - see description in Appendix 710 A), by Davidson et al. (2013). This model uses a holistic understanding of how a 711

beach responds to several high-intensity forcing event characteristics (duration, 712 intensity, clustering and recovery, see Appendix A). The key model free parameter is 713 the memory decay factor (ϕ) , which indicates the single most dominant response 714 time of cross-shore sediment exchange. However, due to this single memory decay 715 factor, model skill deteriorates considerably if multiple dominant forcing and beach 716 response timescales are present (Vitousek et al., 2017; Almar et al., 2017; Splinter et 717 al., 2017). Recent work by Splinter et al. (2017) and Ibaceta et al. (2020) also 718 showed that timescales of beach change and forcing may be temporally dependent, 719 with beaches undergoing rapid adjustment to the changes in the dominant wave 720 forcing over time and where single memory decay models can fail to capture the 721 observed shoreline signal. 722

Besides the literature mentioned in Section 2, the temporal spectra (Section 3.1 723 and Figure C1) reveal the presence of multiple dominant timescales. These spectra 724 can be considered before model application and can be used to determine if the 725 SF-MT model is more favorable to use with respect to SF-ST (considering model 726 complexity): multiple dominant forcing timescales lead to a substantial improvement 727 (e.g. Narrabeen and Nha Trang, BSS of 0.61 and 0.62, respectively), while if a single 728 timescale is present a less substantial improvement can be expected (Tairua, BSS of 729 (0.30). At Grand Popo model improvement is also less substantial (BSS of (0.18)), 730 while there are multiple dominant forcing timescales present. However, it should also 731 be mentioned that in terms of forcing, this site is very unique (other than multiple 732 dominant forcing components): see for example Ondoa et al. (2020), in which they 733 reveal that intra-seasonal sea level variations impact the beach profile, which is a 734 process that is not accounted for in the model. Moreover, at Narrabeen, Nha Trang 735 and Tairua, the ΔAIC score is larger than 1 for the calibration phase, indicating a 736 considerable model improvement is acquired when accounting for model skill and 737 complexity. However, for the validation phase the ΔAIC score is smaller than 1. In 738 case of a low/negative ΔAIC score and a limited number of observed dominant 739 timescales, a reduced number of bins can also be tested to increase the ΔAIC score. 740 Nevertheless, SF-MT currently handles a large number of 'blind' bins by giving 741 low/no weight to timescale-clusters where low variability is observed to have an 742 unbiased result regarding timescale interactions (rather than hardwire on dominant 743 timescales before model application). The multi-timescale model outperforms SF-ST 744 at sites where short-term (2-3 years) and long-term (10-14 years) data is available. 745 Interestingly, for longer period simulations, climate variability induces changes in 746 wave regimes at all scales, storminess of storm tracks in mid-latitudes, tropical 747 cyclones, but also monsoons and seasonal to inter-annual average conditions 748 (Vitousek et al., 2017; Melet et al., 2020). Moreover, as a variable climate is 749 expected, multiple timescales of shoreline adjustment to forcing likely exist almost 750 751 everywhere. In that context, the humble simplified approach developed in SF-MT can be an attractive way to capture shoreline change to climate modes, climate 752 change and their timescale-interactions. 753

Apart from a considerable increase in model prediction skill (Table 3), 754 compared to SF-ST, the SF-MT model also gains insight in how a beach responds to 755 the considered wave-forcing on multiple scales. The contribution of each model 756 improvement step to shoreline evolution (Figure 5 & 6), illustrates for example that 757 at all sites extreme forcing events have a considerable and persistent shoreline 758 impact (i.e. upscaling approach). It showed that these forcing events are responsible 759 for 36 to 73% of the variability of shoreline evolution. At Narrabeen, Nha Trang and 760 Tairua, long term shoreline trends affect short term forcing event impacts (i.e. 761 downscaling approach). These affected short term forcing event impacts are 762 responsible for 17 to 27% of the variability of shoreline evolution. At Grand Popo 763 those mechanisms are not the main driver of shoreline variability. There the wave 764 forcing drives, for a large part, shoreline change on corresponding timescale-clusters 765

(i.e. direct forcing approach), which could be one of the causes why the model result 766 of SF-MT it is closest to the SF-ST model performance. Moreover, the distribution 767 of shoreline variability over the different modelling approaches and timescale-clusters 768 in SF-MT (last column in Figure 6), showed that the upscaling approach is 769 responsible for capturing shoreline change on the largest timescales in the dataset, as 770 this approach is modelling the persistent effect of short high-intensity wave forcing 771 events on larger timescale shoreline response. Conversely, the modelled shorelines 772 generated with the downscaling approach correspond better to shoreline data on 773 smaller timescales, as this approach is modelling the effect of the larger timescales in 774 shoreline variation on the efficiency which with smaller timescale wave-forcing events 775 induce cross-shore sediment transport. The direct forcing approach does not account 776 for particular shoreline response timescales as it seems to be dataset dependent. 777

The SF-MT model generates multiple individual signals, in which each signal 778 (i.e. timescale-cluster) has a unique timescale relation between the wave forcing and 779 shoreline signal. A certain selection of all these generated signals make up the total 780 shoreline signal (Section 3.3). To visualize these unique timescale relations of all 781 chosen modelled signals, a grid of timescale interactions is presented (Figure 7). In 782 those grids the percentage to the total shoreline signal per individual modelled signal 783 (i.e. timescale-cluster) is plotted, revealing the most important timescale 784 interactions per dataset. The axes can be used to check which timescales are 785 considered and the diagonal, upper left corner and lower right corner correspond to 786 signals generated with the direct forcing, upscaling, and downscaling approach, 787 respectively. Figure 7 presents the timescale interactions at Narrabeen (top), Nha 788 Trang (middle) and Tairua (bottom). Due to the limited number of timescale-bins, 789 the grid of timescale interactions will not be shown for the dataset at Grand Popo. 790

The interactions between timescales shown in Figure 7A show that at 791 Narrabeen the short-term high-intensity forcing events with a timescale of 792 approximately 1 to 6 days have a large and persistent impact on the large timescale 793 shoreline variation (quasi-seasonal). Moreover, shoreline variability on inter-annual 794 timescales is driven by variations in the wave climate with a similar timescale, but it 795 is sensitive to whether the coastline is eroded or accreted on a mildly larger 796 timescale of approximately 860-1134 days (i.e. downscaling approach). This means 797 that the impact to inter-annual forcing events is dependent on whether that 798 coastline is eroded or accreted on a similar to larger timescale. 799

In contrast, Figure 7B shows that at Nha Trang small(er) timescales in the 800 wave forcing (especially those with a timescale of 123-197 days) have a persistent 801 and considerable effect on coastline evolution, and which is together with the 802 persistent effect of monsoons the cause of the seasonal variability (i.e. upscaling). 803 Furthermore, as indicated by the time-series in Figure 5B, shoreline response to both 804 summer and winter monsoons is affected by longer term shoreline variations (i.e. 805 downscaling). This means that the response to these monsoons is not equal 806 throughout the year. Beach response to monsoons (with a timescale of 807 approximately 10-30 days) is larger when the shoreline is already accreted on a 808 larger timescale (3 months or 1.5 year, see Figure 7B). This supports the fact that 809 due to an overall accreted beach state, the offshore sand supply is close to the 810 shoreline, which yields a high sediment transport efficiency and faster response to 811 monsoons. Conversely, when the coastline is already eroded on a larger timescale, 812 the monsoon response is relatively smaller: a large spatial separation between the 813 shoreline and the offshore sediment source yields an inefficient transfer of sediment 814 between the offshore region and beach face, causing a lower response rate. Hence, at 815 Nha Trang the beach response to winter monsoons is relatively smaller than the 816 response to summer monsoons. 817



Figure 7. Timescale interactions at Narrabeen (top), Nha Trang (middle) and Tairua (bottom) and the corresponding legend (bottom). The diagonal represents signals modelled with the direct forcing approach where the black axes (from x to y) can be used to check which timescales are involved. For the upscaling approach (all patches in the upper left corner) the black axes can be used as well. The lower right corner of the grid represents signals generated with the downscaling approach. For those patches the red axes need to be used (from x to y). The colour indicates the percentage of those signals to the total modelled shoreline. A smooth function is used to visually highlight the most dominant timescale interactions.

Figure 7C visualizes the timescale interactions at Tairua. It shows that the 818 wave forcing with an annual timescale has a large and persistent impact on the 819 inter-annual shoreline response (852-1355 days). Moreover, shoreline response on the 820 smallest (storm/swell) timescales (6-9 days) is driven by wave forcing events on a 821 similar timescale (i.e. direct forcing). Furthermore, the inter-annual shoreline change 822 has an influence on how the beach responds to the short timescale wave forcing 823 events with a timescale of approximately 9 to 26 days. 824

6 Conclusions 825

In this study, a new approach is presented to allow for multiple wave forcing-826 and beach response timescales within the single timescale- equilibrium shoreline 827 prediction model ShoreFor (SF-ST; Shoreline Forecast - Single Timescale). While 828 SF-ST was capable of accurately predicting shoreline change only on the single most 829 dominant beach response timescale, multiple dominant timescales can determine 830 shoreline evolution. The multi-timescale implementation (SF-MT; Shoreline Forecast 831 - Multiple Timescales) is governed by filtering and identifying all of the wave forcing 832 and shoreline response timescales. Subsequently, timescales in the wave forcing and 833 shoreline signals are linked through three new terms in the model which are direct 834 forcing, upscaling and downscaling. In the direct forcing term, the shoreline is forced 835 by waves on the corresponding timescales (e.g. a beach erodes and recovers to an 836 individual storm). The upscaling term accounts for the persistent effect of short(er) 837 forcing timescales on longer shoreline response timescales (e.g. seasonal persistence 838 of summer- and winter monsoons). This is modelled using the envelope of the 839 filtered wave signals, which provides the timescale link. The downscaling approach 840 governs the effect of long(er) timescales of shoreline evolution on shoreline response 841 to short(er) wave forcing timescales (e.g. storm impact during accreting or eroding 842 trends). The effect is modelled by introducing a time-dependent response factor 843 from a longer timescale shoreline evolution signal. The multi-timescale model 844 showed considerable improvement compared to SF-ST at the four contrasted sites 845 used in this study. This combined approach leads to several interests when 846 considering interplay between climate modes and storminess under climate change 847 when forecasting future shoreline evolution. 848

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https://doi.org/10.5281/zenodo.3669126. The data at Tairua can be accessed 859 through: https://coastalhub.science/data. 860

Appendix A ShoreFor (SF-ST), the original single timescale model 861

ShoreFor (SF-ST; Shoreline Forecast - Single Timescale) (Davidson et al., 862 2013) is an equilibrium shoreline prediction model, which employs the concept of 863 (dis-)equilibrium of shoreline location following Wright et al. (1985), to predict 864 shoreline change. The SF-ST model takes the following form to estimate temporal 865 shoreline change (Splinter et al., 2014; Splinter et al., 2017): 866

$$\frac{dx_s}{dt} = c(F(\phi)^+ + rF(\phi)^-) + b \tag{A1}$$

Wherein dx_s/dt is the rate of shoreline change, t the time, c a response rate

parameter, ϕ the memory decay factor, r the erosion/accretion ratio, b the linear trend term and F the wave forcing term. The forcing term is divided into an accretionary (F^+) and erosional component (F^-) , because the accretionary and erosion responses are governed by different processes.

The SF-ST model describes the wave forcing using the dimensionless fall velocity (Ω , see e.g. Gourlay (1968); Dean (1973)):

$$\Omega = \frac{H_s}{w_s T_p} \tag{A2}$$

- wherein H_s and T_p being respectively the deep-water significant wave height and
- peak period and w_s the sediment fall velocity.
- ⁸⁷⁶ Both forcing terms in equation A1 are determined by:

$$F = P^{0.5} \frac{\Delta\Omega}{\sigma_{\Delta\Omega}} \tag{A3}$$

⁸⁷⁷ Where P is the wave power ($\propto H_s^2 T_p$ in deep water), $\Delta \Omega$ the disequilibrium of

- dimensionless fall velocity $(\Omega_{eq} \Omega)$ with Ω_{eq} being a dynamic equilibrium term, Ω 878 the instantaneous dimensionless fall velocity and $\sigma_{\Delta\Omega}$ the standard deviation of the 879 disequilibrium. The disequilibrium term $(\Delta \Omega)$ determines whether the coastline is 880 accreting or eroding (plus and minus, respectively (Davidson et al., 2013)) and 881 dividing by the standard deviation of the disequilibrium makes sure that only the 882 wave energy flux (P) and response rate parameter (c) determine the rate of 883 shoreline change, rather than the magnitude of disequilibrium. The dynamic 884 equilibrium term accounts for the fact that future shoreline positions can be strongly 885 dependent on past hydrodynamic conditions (Davidson et al., 2013) and can be, 886
- following Wright et al. (1985), defined as follows:

$$\Omega_{eq} = \frac{\sum_{i=1}^{2\phi} \Omega_i 10^{\frac{-i}{\phi}}}{\sum_{i=1}^{2\phi} 10^{\frac{-i}{\phi}}}$$
(A4)

in which i is the number of days in the wave forcing time-series prior to the day of

observation, Ω_i the dimensionless fall velocity and ϕ the memory decay factor. A large memory decay factor (>>100 days) generates a large timescale shoreline response (e.g. a seasonal variation), while a small decay factor (<100 days) produces a shoreline prediction where smaller (storm) timescales are dominant (Splinter et al., 2014).

The linear trend term in equation A1 captures shoreline changes that do not result from wave driven- cross-shore sediment transport processes (e.g. gradients in long-shore sediment transport). Furthermore, note that c and ϕ are site-specific calibration parameters, while r is not a model free parameter. In absence of the erosion parameter (r), a strong erosive trend would be predicted as negative disequilibrium conditions (e.g. storms) often have a higher associated wave power (Stokes et al., 2015). This erosion ratio parameter is based on the assumption that
 the detrended erosion and accretion forcing are assumed equal: it maintains a
 long-term shoreline equilibrium if no trend in the wave forcing data is present.

The SF-ST model seeks the best relation between the raw wave forcing- and 903 raw shoreline position data through the fitting of several calibration parameters (c &904 ϕ) using the knowledge of how the beach responds to incoming wave forcing. For 905 example, a beach in equilibrium with the current and antecedent (calm) forcing 906 conditions will try to adapt to a new equilibrium if wave conditions change, like in 907 the case of a high-intensity forcing event (e.g. a storm) impacting the coastline. 908 During such event, the beach will erode and the shoreline moves landward. The new 909 established shoreline is then more in equilibrium with the prevailing forcing. 910 However, several characteristics of the high-intensity forcing event play a role in how 911 the (modelled) shoreline position responds to the considered wave forcing. The first 912 aspect is the forcing duration: only if the duration is long enough (i.e. stationary 913 conditions), a new equilibrium is established. Secondly, the intensity of the wave 914 forcing determines how far the beach retreats. Thirdly, in case of multiple 915 high-intensity forcing events, the sequence of these forcing events (e.g. a storm 916 cluster) determines to a large extent the shoreline change. Here, the first wave 917 forcing event in the cluster is more effective in eroding the shoreline, because the 918 disequilibrium is the largest (Yates et al., 2009). A prerequisite, for the sequencing 919 to be important, is that the beach has no time to fully recover in between the 920 high-intensity forcing events that make up the cluster (Angnuureng et al., 2017; 921 Karunarathna et al., 2014). To what extent a beach recovers from the antecedent 922 high-intensity forcing conditions mainly depends on the characteristics of the 923 post-storm hydrodynamic conditions relative to the antecedent conditions (Morton 924 et al., 1994). The SF-ST model is only applicable on locations where wave driven-, 925 cross-shore processes dominate sediment transport and where anthropological 926 influences are minimal (Davidson et al., 2013). SF-ST was originally established 927 using data in micro-tidal environments (see Davidson et al. (2013)), but the 928 subsequent model of Splinter et al. (2014) was established covering a wide range of 929 tidal ranges. Moreover, Dodet et al. (2019) showed that the model yields significant 930 skill in reproducing post-storm recovery in a macro-tidal environment as well. 931 However, here model training sites with a limited tidal range are used, to minimize 932 the influence of the tide on the shoreline location. 933

⁹³⁴ Appendix B Model skill assessment

To evaluate model prediction skill, the total shoreline prediction for both the 035 calibration- and validation phase is compared to the corresponding measured 936 shoreline location data. The first model skill indicator that is used is the correlation 937 coefficient. The correlation coefficient indicates the strength of the relationship 938 between the modelled- and measured shoreline data. The other three model skill 939 indicators are: 1) the normalized mean square error (NMSE) between the modelled 940 and measured data and 2) the Brier Skill Score (BSS), which can take measurement 941 errors into account and 3) the ΔAIC value, which accounts for model complexity. 942 The NMSE (Miller & Dean, 2004; Splinter et al., 2013) compares the error variance 943 to the observed variance and is chosen to allow for easier skill comparison between 944 each site, compared to the Root Mean Squared Error (RMSE). The NMSE can be 945 written down as: 946

$$NMSE = \frac{\sum (x_m - x)^2}{\sum x_m^2} \tag{B1}$$

In which x_m is the measured shoreline and x the modelled shoreline. A NMSE of 0-0.3, 0.3-0.6, 0.6-0.8, 0.8-1.0 is labeled as 'excellent', 'good', 'fair' and 'poor', respectively (Splinter et al., 2014).

The Brier Skill Score (van Rijn et al., 2003; Sutherland et al., 2004) compares the performance of two models to the observed shoreline location and has the following form (adopted after Bosboom and Reniers (2017)):

$$BSS = \frac{\langle (x_b - x_m)^2 \rangle - \langle (x - x_m)^2 \rangle}{\langle (x_b - x_m)^2 \rangle - 2\delta^2} \tag{B2}$$

Wherein x_m is the measured shoreline, x the modelled shoreline, δ the measurement 953 error and x_b the baseline model. In this paper, SF-ST will be used as a baseline 954 model. The triangle brackets indicate the mean. Positive BSS indicate a significant 955 model improvement relative to this baseline model where values between 0-0.1, 956 0.1-0.2, 0.2-0.5 and 0.5-1.0 are labeled as 'poor', 'fair', 'good' and 'excellent', 957 respectively. Note that the formulation of the BSS has been adopted after Bosboom 958 and Reniers (2017). They advise the use of the skill formulation according to 959 Sutherland et al. (2004) in combination with a classification that is not adjusted for 960 measurement error as is used here. A constant measurement error of 0.5 meter is 961 used, as for all sites the shoreline location time-series are extracted from 962 video-images. 963

By using SF-MT, the total predicted shoreline signal consists of multiple 964 signals with different timescales. For each individual modelled signal using the direct 965 forcing- and upscaling approach (Equations 1 and 2), two calibration parameters are 966 present: the memory decay factor (ϕ) and the response factor (c). For the 967 downscaling approach (Equation 3) only one calibration parameter is present: the 968 memory decay factor. Therefore, the fourth model skill indicator that will be used is 969 the Akaike's information criterion (AIC) (Akaike, 1974) as it is specifically designed 970 to compare models with a different number of calibration parameters (m): 971

$$AIC = n * (log(2\pi) + 1) + n * log(\sigma^2) + 2m$$
(B3)

In which *n* is the total number of samples and σ^2 the variance of the model or baseline residuals. Hence, it deals with the trade-off between the goodness of fit and model simplicity. If the difference between the baseline and model AIC (Δ AIC) exceeds 1.0, a considerable model improvement is acquired (Davidson et al., 2013). In this study SF-ST will be used as a baseline model.

⁹⁷⁷ Appendix C Temporal spectra of the wave- and shoreline data

This Appendix shows how the dominant timescales in the shoreline- and wave forcing time-series were determined (Table 2). Dominant timescales were obtained by determining local peaks (using a peak analysis tool) in the temporal spectra. The temporal spectra for the shoreline position, wave height and wave period are shown in Figure C1 for each dataset. The most dominant timescale per spectrum is indicated with a red circle, while other dominant timescales can be identified by other local peaks in the temporal spectra.

985 References

Aagaard, T., Kroon, A., Andersen, S., Sørensen, R. M., Quartel, S., & Vinther,
 N. (2005). Intertidal beach change during storm conditions; egmond, the
 netherlands. *Marine Geology*, 218, 65-80.



Figure C1. Temporal spectra of the shoreline position (dotted), wave height (crosses) and wave period (diamonds), for all datasets. The red circle indicates the most dominant timescale. The top left, top right, bottom left and bottom right panel is corresponding to the dataset at Narrabeen, Nha Trang, Tairua and Grand Popo, respectively.

989	Akaike, H. (1974). A new look at the statistical model identification. <i>IEEE</i>
990	Transactions on Automatic Control, 19(6), 716-723.
991	Almar, R., Kestenare, E., Reyns, J., Jouanno, J., Anthony, E., Laibi, R.,
992	Ranasinghe, R. (2015, November). Response of the bight of benin (gulf of
993	guinea, west africa) coastline to anthropogenic and natural forcing, part1:
994	Wave climate variability and impacts on the longshore sediment transport.
995	Continental Shelf Research, 110, 48–59. Retrieved from https://doi.org/
996	10.1016/j.csr.2015.09.020 doi: 10.1016/j.csr.2015.09.020
997	Almar, R., Marchesiello, P., Almeida, L. P., Thuan, D. H., Tanaka, H., & Viet,
998	N. T. (2017). Shoreline response to a sequence of typhoon and monsoon
999	events. Water, $9(52)$.
1000	Anderson, T. R., Frazer, L. N., & Fletcher, C. H. (2010, April). Transient and
1001	persistent shoreline change from a storm. Geophysical Research Letters,
1002	<i>37</i> (8). Retrieved from https://doi.org/10.1029/2009g1042252 doi:
1003	10.1029/2009gl 042252
1004	Angnuureng, D. B., Almar, R., Senechal, N., Castelle, B., Addo, K. A., Marieu, V.,
1005	& Ranasinghe, R. (2017). Shoreline resilience to individual storms and storm
1006	clusters on a meso-macrotidal barred beach. Geomorphology, 290, 265 - 276.
1007	Retrieved from http://www.sciencedirect.com/science/article/pii/
1008	S0169555X17301496 doi: https://doi.org/10.1016/j.geomorph.2017.04.007
1009	Anthony, E., Almar, R., Besset, M., Reyns, J., Laibi, R., Ranasinghe, R., Vacchi,
1010	M. (2019, February). Response of the bight of benin (gulf of guinea, west
1011	africa) coastline to anthropogenic and natural forcing, part 2: Sources and
1012	patterns of sediment supply, sediment cells, and recent shoreline change.
1013	Continental Shelf Research, 173, 93–103. Retrieved from https://doi.org/
1014	10.1016/j.csr.2018.12.006 doi: 10.1016/j.csr.2018.12.006
1015	Antolínez, J. A. A., Méndez, F. J., Anderson, D., Ruggiero, P., & Kaminsky, G. M.
1016	(2019, June). Predicting climate-driven coastlines with a simple and efficient

1017 1018	multiscale model. Journal of Geophysical Research: Earth Surface, 124(6), 1596–1624. Retrieved from https://doi.org/10.1029/2018jf004790 doi:
1019	10.1029/2018jf 004790
1020	Bergsma, E., & Almar, R. (2020, June). Coastal coverage of ESA' sentinel 2 mission.
1021	Advances in Space Research, 65 (11), 2636–2644. Retrieved from https://doi
1022	.org/10.1016/j.asr.2020.03.001 doi: 10.1016/j.asr.2020.03.001
1023	Bergsma, E., Conley, D., Davidson, M., OHare, T., & Almar, R. (2019, March).
1024	Storm event to seasonal evolution of nearshore bathymetry derived from
1025	shore-based video imagery. Remote Sensing, $11(5)$, 519. Retrieved from
1026	https://doi.org/10.3390/rs11050519 $doi: 10.3390/rs11050519$
1027	Blossier, B., Bryan, K. R., Daly, C. J., & Winter, C. (2017, October). Shore and
1028	bar cross-shore migration, rotation, and breathing processes at an embayed
1029	beach. Journal of Geophysical Research: Earth Surface, 122(10), 1745–
1030	1770. Retrieved from https://doi.org/10.1002/2017jf004227 doi:
1031	10.1002/2017if004227
1032	Bosboom, J., & Reniers, A. (2017). The deceptive simplicity of the brier skill
1022	score Handbook of Coastal and Ocean Engineering: Ernanded Edition 2-2
1033	
1034	Bradshaw B. Hoaly T. P. Doll P. M. & Bolstad W. (1001) Inner shalf
1035	dimension of a storm dominated coast contracted how gooland Lewrold
1036	dynamics on a storm-dominated coast, east coromander, new zearand. Journal of Coastal Bassarah $\gamma(1)$ 11.20 Detrieved from https://www.istor.org/
1037	of Coastat Research, 7(1), 11-50. Retrieved from https://www.jstor.org/
1038	stable/4297802
1039	Callaghan, D. P., Ranasinghe, R., & Roelvink, D. (2013). Probabilistic estimation of
1040	storm erosion using analytical, semi-empirical, and process based storm erosion
1041	models. Coastal Engineering, 82, 64-75.
1042	Davidson, M. A., Splinter, K. D., & Turner, I. L. (2013). A simple equilibrium
1043	model for predicting shoreline change. Coastal Engineering, $73(52)$, 191-202.
1044	Davidson, M. A., Splinter, K. D., Turner, I. L., & Harley, M. D. (2017). Annual
1045	prediction of shoreline erosion and subsequent recovery. Coastal Engineering.
1046	Dean, R. G. (1973). Heuristic models of sand transport in the surfzone. Proc. of the
1047	1st Australian Conference on Coastal Engineering, Engineering Dynamics in
1048	The Surf Zone, Sydney, Australia, 209-214.
1049	Dodet, G., Castelle, B., Masselink, G., Scott, T., Davidson, M., Floc'h, F.,
1050	Suanez, S. (2019). Beach recovery from extreme storm activity during the
1051	2013-14 winter along the atlantic coast of europe. Earth Surface Processes and
1052	Landforms, 1/4, 393-401.
1052	Frazer I. N. Anderson T. B. & Fletcher C. H. (2009 October) Modeling
1053	storms improves estimates of long-term shoreline change Geophysical Research
1054	Lettere $\frac{26}{20}$ Batriovad from https://doi.org/10.1020/2009g1040061
1055	doi: 10.1020/2000gl040061
1056	Coldatein E. D. Cose C. & Diant N. C. (2010 July) A review of machine
1057	Goldstein, E. D., Coco, G., & Plant, N. G. (2019, July). A review of machine
1058	Earth Griener Devices 10/ 07 100 Detrieved from https://doi.org/
1059	Larth-Science Reviews, 194, 97–108. Retrieved from https://doi.org/
1060	10.1016/j.earscirev.2019.04.022 doi: 10.1016/j.earscirev.2019.04.022
1061	Gourlay, M. R. (1968). Beach and dune erosion tests. <i>Delft Hydraulics Laboratory</i>
1062	Report m935/m936, Delft, The Netherlands.
1063	Harley, M. D., Turner, I., Short, A., & Ranasinghe, R. (2011). A reevaluation of
1064	coastal embayment rotation: the dominance of cross-shore versus alongshore
1065	sediment transport processes in se australia. Journal Of Geophysical Research,
1066	116(16).
1067	Harley, M. D., Turner, I. L., Short, A. D., & Ranasinghe, R. (2009). Interannual
1068	variability and controls of the sydney wave climate. International Journal of
1069	Climatology, n/a-n/a. Retrieved from https://doi.org/10.1002/joc.1962
1070	doi: 10.1002/joc.1962
1071	Holman, R. A., & Stanley, J. (2007). The history and technical capabilities of argus.

1072	$Coastal \ Engineering, \ 54 (6-7), \ 477-491.$
1073	Ibaceta B Splinter K D Harley M D & Turner I L (2020 November)
1074	Enhanced coastal shoreline modeling using an ensemble kalman filter to
1075	include nonstationarity in future wave climates Geophysical Research Letters
1075	$\gamma(22)$ Betrieved from https://doi org/10.1029/2020g1090724 doi:
1076	47(22). Reflected from https://doi.org/10.1020/2020g1000724 doi.
1077	10.1029/2020g1090724
1078	Jackson, N., Nordstrom, K., Ellot, I., & Masselink, G. (2002). "Iow energy" sandy
1079	beaches in marine and estuarine environments: A review. Geomorphology, 48,
1080	147-162.
1081	Karunarathna, H., Pender, D., Ranasinghe, R., Short, A. D., & Reeve, D. E.
1082	(2014). The effects of storm clustering on beach profile variability. Marine
1083	Geology, 348, 103 - 112. Retrieved from http://www.sciencedirect.com/
1084	science/article/pii/S0025322713002624 doi: https://doi.org/10.1016/
1085	j.margeo.2013.12.007
1086	Larson, M., & Kraus, N. C. (1995). Prediction of cross-shore sediment transport at
1087	different spatial and temporal scales. Marine Geology, 126(1-4), 111-127.
1088	Lefebvre, JP., Almar, R., Viet, N. T., Thuan, D. H., Binh, L. T., Ibaceta, R., &
1089	Duc, N. V. (2014). Contribution of swash processes generated by low energy
1000	wind waves in the recovery of a beach impacted by extreme events: Nha trang
1000	vietnam Journal of Coastal Research $70(\text{sp1})$
1091	Marchosialla P. Kostanara F. Almar B. Boucharal I. & Neuvon N. M. (2020)
1092	November) I ongehere drift produced by alimete modulated monocone and
1093	typhoong in the south shine son I aurol of Marine Systems 011, 102200
1094	Detrieved from https://doi.org/10.1016/j.jmanauz.2020.102200
1095	to 1016 /: imagene 2020 102200
1096	10.1016/J.Jinarsys.2020.103399
1097	Melet, A., Almar, R., Hemer, M., Cozannet, G. L., Meyssignac, B., & Ruggiero,
1098	P. (2020, August). Contribution of wave setup to projected coastal sea level
1099	changes. Journal of Geophysical Research: Oceans, 125(8). Retrieved from
1100	https://doi.org/10.1029/2020jc016078
1101	Miller, J. K., & Dean, R. G. (2004). A simple new shoreline change model. <i>Coastal</i>
1102	Engineering, 51, 531-556.
1103	Montaño, J., Coco, G., Antolínez, J. A. A., Beuzen, T., Bryan, K. R., Cagigal,
1104	L., Vos, K. (2020, Feb 07). Blind testing of shoreline evolution models.
1105	Scientific Reports, $10(1)$, 2137.
1106	Morton, R. A., Paine, J. G., & Gibeaut, J. C. (1994). Stages and durations of
1107	post-storm beach recovery, southeastern texas coast, u.s.a. Journal of Coastal
1108	Research, 10, 884-908.
1109	Ondoa, G. A., Almar, R., Jouanno, J., Bonou, F., Castelle, B., & Larson, M. (2020)
1110	may). Beach adaptation to intraseasonal sea level changes. <i>Environmental</i>
1111	Research Communications 2(5) 051003 Betrieved from https://doi.org/10
1112	1088%2F2515-7620%2Fab8705_doi: 10.1088/2515-7620/ab8705
1112	Ondoa C. A. Bonou F. Tomaty F. du Ponhoat V. Parrat C. Dorba C. k
1113	Alman P. (2017) Peach response to wave forcing from event to inter annual
1114	Annai, R. (2017). Deach response to wave forcing from event to inter-annual time scales at grand none, hence $(gulf of guinea)$. Water $O(6)$
1115	Dhilling M.C. Harley M.D. Thurrey I.L. Calinter K.D. & Cars D. I. (2017)
1116	Phillips, M. S., Harley, M. D., Turner, I. L., Spinter, K. D., & Cox, R. J. (2017,
1117	March). Shoreline recovery on wave-dominated sandy coastlines: the role
1118	or sandbar morphodynamics and nearshore wave parameters. Marine
1119	<i>Geology</i> , 385, 146–159. Retrieved from https://doi.org/10.1016/
1120	j.margeo.2017.01.005 doi: 10.1016/j.margeo.2017.01.005
1121	Pianca, C., Holman, R., & Siegle, E. (2015). Shoreline variability from days to
1122	decades: Results of long-term video imaging. Journal Of Geophysical Research
1123	$Oceans, \ 120, \ 2159-2178.$
1124	Plant, N. G., Aarninkhof, S. G. J., Turner, I. L., & Kingston, K. S. (2007,
1125	May). The performance of shoreline detection models applied to video
1126	imagery. Journal of Coastal Research, 233, 658–670. Retrieved from

1127	https://doi.org/10.2112/1551-5036(2007)23[658:tposdm]2.0.co;2
1128	doi: $10.2112/1551-5036(2007)23[658:tposdm]2.0.co;2$
1129	Ranasinghe, R., McLoughlin, R., Short, A., & Symonds, G. (2004, March).
1130	The southern oscillation index, wave climate, and beach rotation. Marine C_{1} is a contract of C_{2} and C_{2} is a contract of C_{2} is a contract of C_{2} in the contract of C_{2} is a contract of C_{2} in the contract of C_{2} is a contract of C_{2} in the contract of C_{2} is a contract of C_{2} in the contract of C_{2} is a contract of C_{2} in the contract of C_{2} is a contract of C_{2} in the contract of C_{2} is a contract of C_{2} in the contract of C_{2} in the contract of C_{2} is a contract of C_{2} in the contract of C_{2} is a contract of C_{2} in the contract of C_{2} is a contract of C_{2} in the contract of C_{2} is a contract of C_{2} in the contract of C_{2} is a contract of C_{2} in the contract of C_{2} is a contract of C_{2} in the contract of C_{2} is a contract of C_{2} in the contract of C_{2} is a contract of C_{2} in the contract of C_{2} is a contract of C_{2} in the contract of C_{2} in the contract of C_{2} is a contract of C_{2} in the contract of
1131	Geology, 204 (3-4), 273-287. Retrieved from https://doi.org/10.1016/
1132	$s_{0025-3227(04)00002-7}$ doi: 10.1016/ $s_{0025-3227(04)00002-7}$
1133	Robinet, A., Castelle, B., Idier, D., Harley, M., & Splinter, K. (2020). Controls of
1134	local geology and cross-shore/longshore processes on embayed beach shoreline
1135	variability. Marine Geology, 422, 106118.
1136	Robinet, A., Idier, D., Castelle, B., & Marieu, V. (2018). A reduced-complexity
1137	shoreline change model combining longshore and cross-shore processes: the
1138	Ix-shore model. Environ. Model. Softw., 109, 1-16.
1139	Roelvink, D., Reniers, A., van Dongeren, A., van Thiel de Vries, J., McCall, R.,
1140	& Lescinski, J. (2009, November). Modelling storm impacts on beaches,
1141	dunes and barrier islands. Coastal Engineering, 56(11-12), 1133–1152.
1142	Retrieved from https://doi.org/10.1016/j.coastaleng.2009.08.006
1143	doi: 10.1016/j.coastaleng.2009.08.006
1144	Smith, R. K., & Bryan, K. R. (2007, July). Monitoring beach face volume with
1145	a combination of intermittent profiling and video imagery. Journal of Coastal
1146	Research, 234, 892-898. Retrieved from https://doi.org/10.2112/04-0287
1147	.1 doi: 10.2112/04-0287.1
1148	Splinter, K. D., Turner, I., Reinhardt, M., & Ruessink, B. (2017). Rapid adjustment
1149	of shoreline behaviour to changing seasonality of storms: observations and
1150	modelling at an open-coast beach. Earth Surf. Process. Landf., 42, 1886-1194.
1151	Splinter, K. D., Turner, I. L., & Davidson, M. A. (2013, July). How much data
1152	is enough? the importance of morphological sampling interval and duration
1153	for calibration of empirical shoreline models. Coastal Engineering, 77, 14–27.
1154	Retrieved from https://doi.org/10.1016/j.coastaleng.2013.02.009 doi:
1155	10.1016/j.coastaleng.2013.02.009
1156	Splinter, K. D., Turner, I. L., Davidson, M. A., Patrick, B., Castelle, B., &
1157	Oltman–Shay, J. (2014). A generalized equilibrium model for predicting
1158	daily to interannual shoreline response. Geophys. Res. Earth Surf., 119(52),
1159	1936-1958.
1160	Stokes, C., Davidson, M., & Russell, P. (2015). Observation and prediction of three-
1161	dimensional morphology at a high-energy macrotidal beach. <i>Geomorphology</i> ,
1162	243, 1-13.
1163	Sutherland, J., Peet, A., & Soulsby, R. (2004). Evaluating the performance of
1164	morphological models. Coastal Engineering, 51, 917-939.
1165	Takbash, A., & Young, I. R. (2019, September). Global ocean extreme wave heights
1166	from spatial ensemble data. Journal of Climate, 32(20), 6823–6836. Retrieved
1167	from https://doi.org/10.1175/jcli-d-19-0255.1 doi: 10.1175/jcli-d-19
1168	-0255.1
1169	Thuan, D. H., Almar, R., Marchesiello, P., & Viet, N. (2019). Video sensing of
1170	nearshore bathymetry evolution with error estimate. J. Mar. Sci. Eng., 7,
1171	
1172	Thuan, D. H., Binh, L. T., Viet, N. T., Hanh, D. K., Almar, R., & Marchesiello,
1173	P. (2016). Typhoon impact and recovery from continuous video monitoring:
1174	a case study from nha trang beach, vietnam. Journal of Coastal Research, $\frac{77}{10}$
1175	
1176	Turner, I. L., Harley, M. D., Short, A. D., Simmons, J. A., Bracs, M. A., Phillips,
1177	M. S., & Splinter, K. D. (2016, April). A multi-decade dataset of monthly
1178	beach profile surveys and inshore wave forcing at narrabeen, australia.
1179	scientific Data, 5(1). Retrieved from https://doi.org/10.1038/
1180	saata.2010.24 dol: 10.1058/sdata.2010.24
1181	van rujn, L., waistra, D., Grasmeijer, B., Sutherland, J., Pan, S., & Sierra, J.

1182	(2003). The predictability of cross-shore bed evolution of sandy beaches at the
1183	time scale of storms and seasons using process-based profile models. Coastal
1184	Engineering, 47, 295-327.
1185	Vitousek, S., Barnard, P. L., Limber, P., Erikson, L., & Cole, B. (2017). A model
1186	integrating longshore and cross-shore processes for predicting long-term
1187	shoreline response to climate change. Journal of Geophysical Research: Earth
1188	Surface, 122(4), 782-806.
1189	Walstra, D. J. R., Reniers, A. J. H. M., Ranasinghe, R., Roelvink, J. A., &
1190	Ruessink, B. G. (2012). On bar growth and decay during inter-annual net
1191	offshore migration. Coastal Engineering, 60, 190-200.
1192	Walstra, D. J. R., Wesselman, D. A., van der Deijl, E. C., & Ruessink, G. (2016).
1193	On the intersite variability in inter-annual nearshore sandbar cycles. Marine
1194	Science and Engineering, $4(15)$.
1195	Wright, L. D., Short, A. D., & Green, M. O. (1985). Short-term changes in the
1196	morphodynamic states of beaches and surf zones; an empirical predictive
1197	model. <i>Marine Geology</i> , $62(52)$, 339-364.

Yates, M. L., Guza, R. T., & O'Reilly, W. C. (2009). Equilibrium shoreline response: Observations and modeling. *Journal Of Geophysical Research*, 114.