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Slow-moving arctic soils commonly organize into striking large-scale spatial patterns called solifluction terraces and lobes. Though these features impact hillslope stability, carbon storage and release, and landscape response to climate change, no mechanistic explanation exists for their formation. Everyday fluids—such as paint dripping down walls—produce markedly similar fingering patterns resulting from competition between viscous and cohesive forces. Here we use a scaling analysis to show that soil cohesion and hydrostatic effects can lead to similar large-scale patterns in arctic soils. A large new dataset of high-resolution solifluction lobe spacing and morphology across Norway supports theoretical predictions and indicates a newly observed climatic control on solifluction dynamics and patterns. Our findings provide a quantitative explanation of a common pattern on Earth and other planets, illuminating the importance of cohesive forces in landscape dynamics. These patterns operate at length and time scales previously unrecognized, with implications toward understanding fluid-solid dynamics in particulate systems with complex rheology.

solifluction | fluid instabilities | climate | granular fingering | periglacial

Periodically frozen soil—a temporally evolving mixture of granular material, fluid, and ice—is one of the most complex natural materials found on planetary surfaces. While its rheology is not well understood, arctic soil deformation commonly produces large, distinctive meters-to-tens of meters-scale spatial patterns visible in aerial images (Figure 1A,B). Patterns are organized in both the downslope and cross-slope directions. Regular downslope-oriented terraces of soil are characterized by raised fronts that protrude 1-2 meters above the surrounding topography (Figure 1A,C). Terrace fronts are commonly broken into finger-like lobes evenly spaced cross-slope (Figure 1A,B). Known as solifluction features, these patterns form due to a combination of frost heave, in which segregation ice growth lofts soil upwards, and gelifluction, a slow flow-like relaxation of partially saturated soil once it thaws in the summer (1, 2). While a rich history of experimental and global field observations over the past century have characterized solifluction processes and velocities ($\sim 10^{-1} - 10^1$ cm/year) (2, 3), there exists no agreed-upon rheological model for solifluction that can offer quantitative and qualitative explanations for the striking patterns it produces. Renewed interest in these features primarily stems from a need to predict arctic landscape response to climate change and storage and release of permafrost carbon, as well as to predict and mitigate arctic slope instabilities due to thawing permafrost (4).

Strikingly similar patterns develop in simple fluids, where competition between viscous and cohesive forces drives a suite of common instabilities in thin films. For example, the evenly spaced fluid fingers that form when painting a wall, icing a cake, or sloshing oil in a frying pan are known as “contact line instabilities” at fluid fronts (7, 11) (Figure 1A). Only recently

have soft solids (12) and granular materials (13–18) been shown to exhibit patterns and morphology that resemble those of thin-film fluids. Notably, (13) found that small cohesive forces between sand grains produce an effective surface tension relevant at macroscopic length scales, causing a steady stream of sand to break into droplets similar to a Rayleigh-Plateau instability. However, connections between fluid and granular instabilities—especially regarding the role of cohesion—remain a frontier in materials science.

Here we take the first step toward utilizing quantitative connections with fluid and granular mechanics to better understand solifluction processes and patterns. We present a conceptual model of solifluction pattern formation in which solifluction lobes (resembling fluid fingers) arise as a cross-slope instability on the fronts of terraces (resembling waves) formed during an initial downslope instability (Figure 1A,B). While we present data for both instabilities, we focus mainly on the cross-slope patterns. First, we discuss how key ingredients that control fluid contact line instabilities—viscosity, velocity, fluid thickness, and surface tension—may translate to soil. By adopting an analogy between fluid and soil dynamics, we suggest a formal scaling analysis relating solifluction wavelengths to active soil thickness, topographic slope, and cohesion-drive effects at the soil front. Using high-resolution topographic data from over 3000 solifluction lobes across 25 sites in Norway, we show that scaling between solifluction wavelengths and slope, lobe thickness, and lobe front angle generally agrees with our theoretical analysis. Data from these sites show that lobe morphology is strongly correlated with elevation, which likely represents a climate control on solifluction processes due

Significance Statement

Slow-moving arctic soils form patterns resembling those found in common fluids, such as paint and cake icing drips. Inspired by fluid instabilities, we develop a new conceptual model for soil patterns and use mathematical analysis to predict their wavelength. In particular, we propose that soil patterns arise due to competition between gravity and cohesion, or the “stickiness” of soil grains. We compare our theoretical predictions with a new data set of soil features from Norway, finding that soil patterns are controlled by fluid-like properties as well as climate. Our work provides the first physical explanation for a common pattern on both Earth and Mars, with implications for our understanding of landscapes and complex materials composed of both granular and fluid components.

R.C.G., M.F., and J.R. designed research; M.F. and R.C.G. analyzed data; all authors contributed to development of theory and writing of paper

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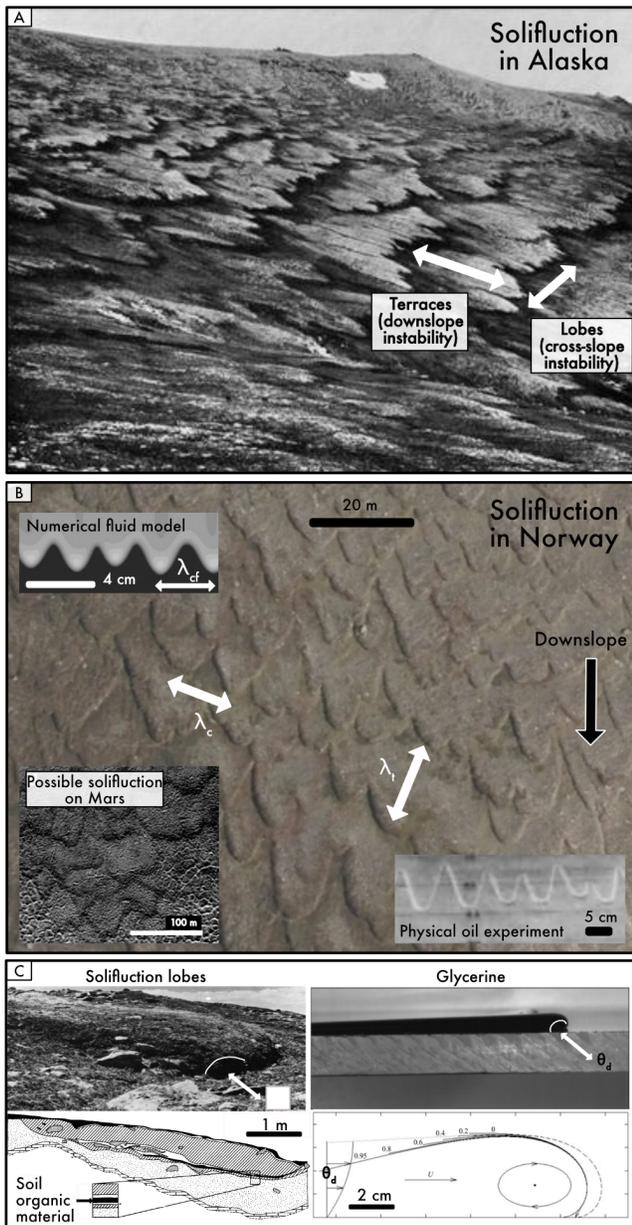


Fig. 1. A) Solifluction terraces and lobes in Chicken Creek, Alaska. Photo by Philip S. Smith, reprinted from the USGS Photographic Library. B) Examples of solifluction and fluid patterns. Background: Orthophoto of solifluction lobes in Norway, copyright Kartverket. Upper left: Numerical model image reprinted from (5). Lower left: Possible solifluction on Mars, reprinted from (6). Lower right: Photo of front of oil flowing down plane, reprinted from (7). Cross-slope wavelengths for fluids λ_{cf} and solifluction lobes λ_c are shown, as well as the downslope solifluction terrace wavelength λ_t . C) Morphology and dynamics of solifluction lobes vs. surface tension-dominated flows. Upper left: Solifluction lobe in Colorado, reprinted from (8) (copyright Taylor and Francis). Lower left: Map of trenched lobe in Norway, with soil organic layer showing rollover motion. Adapted from (9). Upper right: Gravity driven glycerine front. Lower right: schematic of glycerine front showing rollover motion. Shape of nose derived from Young-Laplace equation for surface tension effects. Numbers indicate profile evolution through time, and dashed line illustrates profile at next moment in time. Dynamic contact angle θ_d is shown for both a solifluction lobe and a fluid finger. Both reprinted from (10).

to the dependence of frost heave on mean annual temperature amplitude (T_a) and mean annual air temperature (MAAT). We discuss how cohesion not only slows down soil motion but results in a state change in soil behavior, with implications for Arctic landscape response to climate change and interpretation of past climates on Earth and other planets. Our work shows that even in creeping granular-fluid-ice materials, competition between driving stress and cohesion can result in large-scale patterns similar to those found in fluids, with implications for our understanding of the rheological behavior of complex materials.

Fluid Fingering Instabilities

First, we briefly describe fingering instabilities in fluid films. The qualitative explanation for contact line instabilities is simple: at a fluid interface in a thin film, cohesive forces in the form of surface tension hold back the flow, allowing the front to thicken into a capillary ridge. With a slight initial perturbation, competition between body forces, which cause thicker zones to move faster, and surface tension, which induces transverse flow under bumps, drives the growth of fingers with a regular wavelength. Experiments (e.g., (7, 19, 20)), linear stability analysis (e.g. (11, 21)), and numerical models (e.g. (5, 22)) have determined that the cross-slope wavelength λ_{cf} of fluid contact line instabilities scales as:

$$\lambda_{cf} \sim h \left(\frac{\sigma}{3v\mu} \right)^{1/3} \quad [1]$$

where h is the fluid thickness, μ is the fluid dynamic viscosity, v is a characteristic velocity, σ is the surface tension, and $\sigma/v\mu$ is the inverse capillary number Ca . This means that flows with greater thickness or surface tension produce larger wavelengths, while more viscous or faster moving flows produce smaller wavelengths. While absolute finger wavelengths may differ depending on rheology, contact line instabilities have been shown to exhibit the scaling shown in Eqn. 1 regardless of rheology (e.g., (19, 22)). Note that v depends on both μ and h ; therefore, for a laminar Newtonian fluid with density ρ flowing down a plane with slope angle ϕ , in which we use a characteristic average velocity $v = \rho gh^2 \sin \phi / 2\mu$, Eqn. 1 becomes:

$$\lambda_{cf} \sim \left(\frac{2h\sigma}{3\rho g \sin \phi} \right)^{1/3} \quad [2]$$

Ca has also been shown to control the dynamic contact angle θ_d at the fluid front (Figure 1C) according to the Voinov-Tanner-Cox law, such that $\theta_d^2 \sim Ca^m$, where $m = 1$ for a Newtonian fluid (23), $m > 1$ for a viscoelastic fluid (24) and $m < 1$ for shear thinning fluids (25). The positive relationship between θ_d and Ca shows that the steeper the contact angle, the faster/more viscous the flow (or the lower the cohesion/surface tension). This provides a link between finger morphology and dynamics, and because both wavelength and contact angle depend on Ca , we would expect a power law trend between the two of the form $\frac{\lambda_{cf}}{h} \sim \theta_d^{-1/m}$.

Solifluction Lobes as Fluid-like Instabilities

We argue that the solifluction phenomenon qualitatively exhibits all the necessary ingredients for a fluid-like instability. Here we describe how each ingredient may translate to soil,

117 resulting in a new conceptual model of solifluction pattern
118 formation (Figure 2C).

119 Contact line instabilities initiate at a raised fluid front.
120 For solifluction, we propose that a downslope instability
121 forms evenly spaced solifluction terraces that operate sim-
122 ilarly to a fluid front. With raised fronts $\sim 1 - 2m$ tall and
123 downslope wavelengths λ_t much larger than soil thickness
124 ($\lambda_t \sim 10^1 - 10^2m$) (Figure 1A; 2C, 3E), this downslope in-
125 stability features prominently in the landscape. Though the
126 cause of the downslope instability is unclear, we argue it is
127 likely a result of soil rheology, similar to non-inertial waves
128 recently observed in shear thickening fluids or fluids with re-
129 sisting forces at the free surface (26) (see Discussion). With
130 enough heterogeneity in topography, soil properties (such as
131 moisture, cohesion, and grain size), or vegetation, smooth
132 terrace fronts may break into solifluction lobes evenly spaced
133 cross-slope (Figure 1A,B; 2C) with cross-slope wavelengths
134 λ_c on the order of $1 - 10^2m$. Although the thickness, h , of
135 these features is large relevant to fluid thin films, $\sim 1m$, the
136 hillslope-wide lateral length scale of motion supports the idea
137 that they may behave like thin films (27).

138 While solifluction rheology and mechanistic relationships
139 between velocity and depth are still unclear, data and models
140 show that velocity likely increases with total active soil thick-
141 ness due to freeze-thaw processes (2, 28). Field measurements
142 across the globe have found solifluction velocities ranging from
143 $10^{-1} - 10^1$ cm/yr (2). Considering the soil as a slow-moving
144 fluid, these slow velocities suggest very high viscosities. We
145 compile every available field-measured and experimental ver-
146 tical velocity profile from the literature and find that most
147 exhibit an exponential decrease in velocity with depth (Fig-
148 ure 2A) while a few studies exhibit more complex profiles
149 (SI Appendix, Fig S2). We then calculate effective viscosity
150 μ_{eff} as the ratio between shear stress τ and strain rate du/dz ,
151 where u is the downslope velocity and z is the vertical depth
152 into the soil profile: $\tau = \mu_{eff} \frac{du}{dz}$. We find large μ_{eff} ranging
153 from $10^5 - 10^{12}$ Pa-s. In contrast to a Newtonian fluid with
154 constant viscosity, velocity profiles show that effective viscosity
155 increases with depth (Figure 2B), indicating a non-Newtonian-
156 like flow behavior. While a proper description of solifluction
157 rheology should explicitly take into account granular physics,
158 our first order assumption of non-Newtonian fluid-like behav-
159 ior is likely acceptable for a wet granular material (e.g., (29))
160 (see Discussion).

161 Surface tension at the front is the last key ingredient for a
162 contact line instability, as it allows the fluid to thicken and be-
163 come unstable. Recent studies have shown that intergranular
164 cohesion can produce an effective surface tension in granu-
165 lar materials at small length scales (e.g.(13)); analogous to
166 molecular surface tension, an effective granular surface ten-
167 sion can be calculated as the work required to separate two
168 grains divided by their cross sectional area (13). While this
169 effect may exist in soils, it is likely not physically relevant for
170 $\sim 1m$ thick solifluction lobes in which overburden pressure
171 vastly outweighs any possible pressure due to effective surface
172 tension. However, there are many sources of cohesion that
173 can lend substantial strength to soils, including microbes (e.g.,
174 (30)), permafrost, vegetation (e.g., (31)), capillary bridges
175 due to moisture content (e.g., (32)), clay composition, and
176 solid bridging due to polydispersity ((33)). Additionally, com-
177 monly documented retrograde motion uphill in solifluction

lobes points toward strong effects of cohesion in arctic soils
(2, 34), likely resulting from temporally evolving strength of
capillary bridges. We argue that strong soil cohesion and
corresponding low soil velocities at solifluction fronts allow
soil buildup and transverse flow due to hydrostatic pressure,
similar to the behavior of surface tension-dominated fluids.
This increased cohesion at the front allows the lobe to main-
tain its thickness without diffusing away, especially given the
steep (often overhanging) slope angle at the front. While to
our knowledge no field measurements of soil cohesion trends
across a lobe exist, field velocity and morphology measure-
ments support the idea of cohesive, stalled terrace and lobe
fronts. Displacement markers in the field show soil buildup
behind solifluction lobe fronts and transverse flow toward the
middle/front of lobes, similar to behavior in fluid fingers (8).
Solifluction terrace and lobe morphology (thickened front and
steep, sometimes overhanging contact angle) (e.g., (8)) and
dynamics (tractor tread-style rollover motion at the front)
(8, 9, 35) resemble those of surface-tension dominated flows
(Figure 1C). Though the stalling of solifluction fronts is clear
from observations, existing field data are not sufficient to de-
termine the physical mechanisms for this observation (however,
see Discussion for potential mechanisms). We proceed with
our analysis based on the observation of stalled lobe fronts,
but without any assumptions of the mechanism for increased
cohesion at the front.

204 Conceptual Model

205 We propose that the solifluction lobe instability is initiated
206 and controlled by competition between these elements: 1)
207 the body force due to gravity, which moves thicker material
208 downhill faster 2) cohesion at the front, which resists flow, and
209 3) lateral flow due to hydrostatic pressure under topographic
210 bumps (Figure 2B), with cross-slope wavelengths set by these
211 competing processes (Figure 2B). This is similar to fluid con-
212 tact line fingering in that competition between a body force
213 and resisting force due to cohesion at the front initiates and
214 controls the preferred wavelength of the instability, where in-
215 creased cohesion at the front takes the place of surface tension.
216 Finally, while formulations of fluid contact line instabilities
217 ignore hydrostatic effects because surface tension dominates,
218 here we include hydrostatic pressure that drives lateral flow
219 in the presence of inevitable topographic roughness in natural
220 landscapes.

221 We develop our analysis to be as general as possible, with-
222 out assuming a specific source of cohesion at the front of
223 the lobe. While vegetation has been shown to be important
224 for solifluction patterns (36), the existence of non-vegetated
225 lobes precludes vegetation as a necessary ingredient for their
226 formation. Here we focus on solifluction lobes without large
227 boulders; however, stone-banked lobes exhibit grain size segre-
228 gation with large boulders at the front and sides of the lobe (8).
229 This likely leads to a similar effect in which boulder jamming
230 at the front of the lobe stalls flow. Thus our general conceptual
231 model should apply to both turf-banked and stone-banked
232 lobes on Earth and Mars, as well as unvegetated lobes with
233 relatively homogeneous grain sizes as are observed on Mars
234 (37).

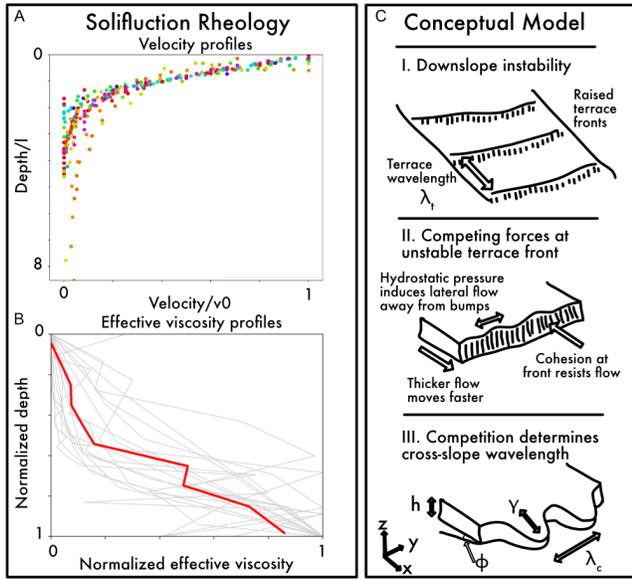


Fig. 2. A) Vertical velocity profiles compiled from the literature, observed both in the field (35, 38–43) and laboratory experiments (1, 44). Data are normalized by the e-folding depth of exponential fits to each profile (see Methods). See non-normalized plots in SI Appendix Figure S3. B) Vertical viscosity profiles computed from velocity profile show general increase in effective viscosity with depth. The grey lines show individual profiles, while the red line shows the viscosity value averaged all profiles. Data are normalized by max and min values in order to plot between 0 and 1. See non-normalized plots in SI Appendix Figure S4. C) Conceptual model of solifluction lobe pattern formation, with variables used in the wavelength scaling analysis defined in part III.

Wavelength scaling analysis

Inspired by fluid theory for contact line instabilities, we take the first step toward deriving an expression for solifluction lobe wavelengths. Because solifluction rheology is uncertain (but certainly nonlinear, see Figure 2), our analysis avoids assumptions of Newtonian flow. In contrast to instabilities in surface-tension dominated fluids, we allow for hydrostatic effects given the likelihood of natural topographic roughness in the field. We examine laminar flow down a plane, accounting for hydrostatic pressure in both the downslope (x) and cross-slope (y) directions. Cohesion has been shown to control effective viscosity in granular materials (e.g., (29, 45)). Therefore, to account for cohesion at solifluction fronts, we allow effective viscosity to vary in the (x) direction. Here we present the simplest approach to scaling; see SI Appendix Section I for alternative approaches that produce similar results.

For a laminar fluid flowing down an inclined plane, under hydrostatic conditions upstream from the front, the basal shear stress is:

$$\tau_0 = -\rho gh \sin \phi + \rho gh \frac{\partial h}{\partial x} \quad [3]$$

where ρ is the bulk density, g is gravity, h is the fluid thickness, and ϕ is the underlying slope. To avoid assumptions of Newtonian rheology, but without assuming a particular form of a power-law fluid, we define a bulk viscosity μ such that $\tau_0 = -\mu U/h$, where U is the vertically averaged velocity in the x (downhill) direction. This is akin to using a characteristic viscosity as done in previous non-Newtonian fluid fingering studies in which viscosity varies with depth (e.g., (19)). To

account for cohesion at the front, we allow viscosity to change in the x direction. Solving for the downslope velocity and assuming that cross-slope velocity arises only from the hydrostatic pressure gradient, we can solve the continuity equation at steady-state and retain only first-order terms (see methods) to find:

$$\frac{3 \sin \phi}{\mu} \frac{\partial h}{\partial x} - \frac{h \sin \phi}{\mu^2} \frac{\partial \mu}{\partial x} - \frac{h}{\mu} \frac{\partial^2 h}{\partial x^2} + \frac{h}{\mu} \frac{\partial^2 h}{\partial y^2} = 0 \quad [4]$$

where the first two terms represent the body force, the third term is the downslope hydrostatic component (x direction), and the fourth term is the cross-slope hydrostatic component (y direction). Now we can scale terms by dimensionless quantities (indicated with hats) as follows:

$$\begin{aligned} h &= h_0 \hat{h} \\ \mu &= \mu_0 \hat{\mu} \\ x &= \gamma \hat{x} \\ y &= \lambda \hat{y} \end{aligned} \quad [5]$$

where h_0 is a characteristic thickness, μ_0 is a characteristic viscosity, γ is a characteristic length scale in the x direction that describes a distance over which the viscosity varies, and λ is a characteristic length scale in the y direction. Retaining only the dimensional leading coefficients and simplifying:

$$\frac{2 \sin \phi}{\gamma} - \frac{h_0}{\gamma^2} + \frac{h_0}{\lambda^2} = 0 \quad [6]$$

We note that the viscosity cancels out, and its only effect lies in γ ; thus the large range of effective viscosity values found in 2B does not influence the expected scaling proposed here. We are mainly interested in λ , which we assume to be equivalent to the cross-slope wavelength λ_c between solifluction lobes (analogous with the wavelength of fluid fingers at a contact line as shown in Eqn. 2). Assuming the body force (first term) dominates over the hydrostatic pressure gradient (second term), we find:

$$\lambda_c \sim \sqrt{\frac{h_0 \gamma}{2 \sin \phi}} \quad [7]$$

This suggests that the cross-slope wavelength increases with soil thickness and the characteristic length over which viscosity changes due to dynamics at the front, and decreases with basal slope (which we assume to be equivalent to x directed topographic slope averaged over a distance \gg length of a lobe). Though the particular scaling differs from that for fluids in Eqn. 1, our relationship is similar in that cross-slope wavelength is projected to exhibit a power law increase with thickness and cohesion and a decrease with topographic slope. These fundamental similarities between solifluction lobe and fluid finger wavelengths also suggest that while we do not yet have a prediction for the contact angle at the front of lobes, we might expect an inverse relationship between cross-slope wavelength normalized by thickness and the contact angle as described above for fluids.

Solifluction patterns in Norway

To explore these ideas in real landscapes, we collected high resolution morphologic and topographic data from 26 highly-patterned solifluction sites across Norway (Figure 3). We manually measured 3000 individual lobes from submeter LiDAR-derived digital elevation models (DEMs) (freely available at

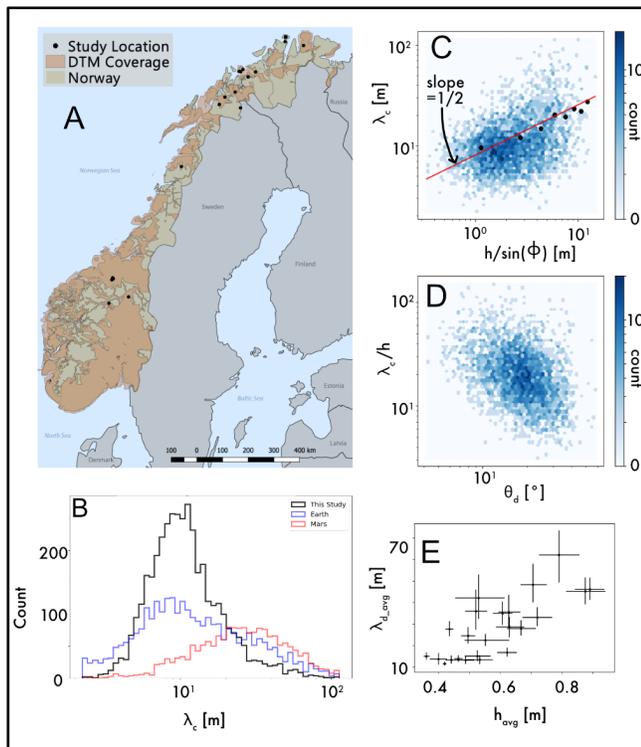


Fig. 3. A) Map of Norway showing study sites used in this paper and DTM coverage. B) Cross-slope wavelength (λ_c) distributions measured in this study, shown with distributions for Earth and Mars from (37). C) Cross-slope wavelength (λ_c) vs. lobe thickness h /topographic slope s . Due to a large number of data points, data are collected into hexagonal bins with color representing the count in each bin. Darker blue indicates a larger number of data points. The red line shows theoretical prediction from Eqn. 6, not a fit to the data; however, vertical position of line is determined by the best fit power law intercept on the raw data. Black dots show average wavelength split into 10 bins of $h/\sin\phi$ values. We omit the highest bin because it contains only 1 data point and therefore is not a meaningful average. D) Cross-slope wavelength (λ_c) normalized by thickness h vs. contact angle θ_d at the front of the lobe. Data are collected into hexagonal bins with color representing the count in each bin. Darker blue indicates a larger number of data points. E) Downslope terrace wavelength (λ_t) averaged at each site vs. average lobe thickness for each site.

Hoydedata) to obtain cross-slope lobe wavelength λ_c , thickness h , lobe length L , and lobe front/riser angle θ_d (hereafter referred to as contact angle), terrace (downslope) wavelength λ_t , and topographic slope angle ϕ (see Methods). We find that cross-slope wavelengths range from 2-100 m, with a mean of 13m. This range agrees with previous studies (37), and values are generally smaller but overlap with those found on Mars (Figure 3B). Trends between lobe morphology metrics and topography agree with theoretical predictions. Cross-slope wavelength increases with lobe thickness/topographic slope, as expected from our scaling analysis (Eqn. 6). Though the data include a large amount of scatter, binned average wavelengths show that our theoretical prediction describes the general trend well (Figure 3C). Note that in order to better explain the data we would need constraints on γ , which may also depend on lobe thickness and explain the jelly bean shape of the data. A better understanding of rheology could also be incorporated in our analysis to improve predictions. Our theory predicts only scaling rather than absolute wavelengths; however, we calculate the best fit power law coefficient on the raw data (≈ 8) to empirically estimate a coefficient for Eqn. 6. Adding a factor of 8 to the front of Eqn. 6 and simplifying suggests that cross-slope wavelength $\lambda_c \approx 6\sqrt{h_0\gamma}/\sin\phi$.

As expected from theory, we see a negative power law trend between wavelength/thickness and contact angle. This observation is consistent with theory for dynamic contact angle of a droplet rolling down a flat substrate. However, to properly predict the relationship between cross-slope wavelength and contact angle, we would need theory equivalent to the Voinov-Tanner-Cox law that accounts for cohesion rather than surface tension. We also find that lobe aspect ratio (L/W) slightly increases with topographic slope, as observed in fluid experiments (SI Appendix, Fig S5) (46). Most lobes are wider than they are long, exhibiting a sawtooth shape similar to that observed for fluids on gently sloping planes (SI Appendix, Fig. S5) (Figure 1B). Finally, we observe a positive relationship between downslope terrace wavelength and lobe thickness averaged by site (Figure 3E), but no clear relationship with topographic slope is discerned (SI Appendix, Fig S6). While we currently lack a prediction for the scaling of downslope wavelength, our data provide the first step toward developing a better understanding of the phenomenon (see Discussion).

Large amounts of scatter in the field data likely contain interesting information about lithology, vegetation, climate, and other unknown parameters that differ between sites. However, that average wavelength trends agree with our theory inspired by simple fluids is remarkable and supports the idea that solifluction patterns operate similarly to fluid contact line instabilities.

Climate controls

Our data show a meaningful increase in solifluction lobe thickness and cross-slope wavelengths with elevation (Figure 4), pointing toward a climate control on lobe morphology and pattern formation due to the lapse rate, or change in temperature with thickness in the atmosphere. Though solifluction features are traditionally thought to be climate-controlled and have often been used to interpret past climate, limited data exist for co-located climate metrics and solifluction lobe morphology and dynamics (47). However, recent work on frost cracking in rock (48–50) illuminates the climatic conditions

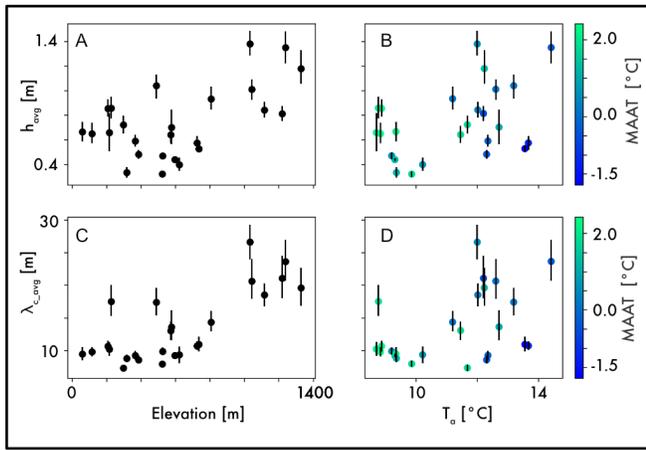


Fig. 4. Relationships between lobe morphology, elevation, and climate indices. Climate data are drawn from daily observations between the years 2000-2020. h_{avg} and λ_{cavg} are the average lobe thickness and cross-slope wavelength at each site, respectively. Elevation is given with reference to sea level. T_a is the mean annual temperature amplitude, and MAAT is the mean annual air temperature. Vertical bars represent 95 % confidence intervals from the field data averaged at each site.

terraces, which we argue promote the growth of solifluction lobes as a contact line instability, deserves further inspection. While terraces resemble roll waves seen in inertial fluid flows (e.g., (56)), buckling instabilities seen in multilayer flows (57) like rock glaciers (58) and lava flows (59), or wrinkling instabilities found in multilayer solids like pumpkins and human skin (60), our observations of solifluction terrace wavelengths do not fit within these frameworks. Exceedingly slow solifluction velocities exist in a non-inertial regime, which precludes a comparison with roll waves (56). While the positive relationship between downslope wavelength and lobe thickness is similar to that seen in buckling and wrinkling instabilities, absolute terrace wavelengths can be much larger than lobe thickness, which is unusual for buckling and wrinkling instabilities; our data show that terrace wavelengths are 1-2 orders of magnitude larger than lobe thicknesses (Figure 2E). Further, the observed low effective viscosities at the surface do not align with buckling instabilities, which typically require a more rigid flow on top (e.g. (58)). However, recent work describes a newly-observed non-inertial instability in shear-thickening flows (e.g., cornstarch mixed with water) that can produce wavelengths much larger than flow thickness (26). These instabilities are shown to result from flow rheology alone, and simply require a rheological curve that exhibits shear-thickening behavior. Our observations of soil velocity profiles, in which effective viscosity increases with depth and therefore shear stress, may align well with a shear-thickening type rheology. Further, our proposed increase in cohesion at soil fronts may also result in an added free surface stabilizing force, which could allow the instability even without shear thickening behavior (26). Further study of these "oobleck waves" may inform the critical conditions necessary for solifluction terrace formation; in turn, field studies of solifluction may provide a natural example of similar instabilities at exceedingly low Reynolds Number, illuminating our understanding of subcritical fluid instabilities.

While we treat solifluction as a non-Newtonian fluid for a first approach, more study is needed to understand the complex rheology of soliflucting soil from a granular perspective. Granular flow rheology is currently understood within the $\mu(I)$ framework, a dimensionless form of the classic shear stress/strain rate relationship that accounts for confining pressure relevant for granular materials (61, 62). In essence, $\mu(I)$ is very similar to fluid rheology, but allows for the role of changing confining pressure with depth. However, the extremely low solifluction velocities observed in the field indicate that solifluction occurs not as a granular flow but well within the granular creep regime (63) that has been shown to describe soil transport velocities on temperate hillslopes (64, 65). Granular creep rheology is still at the forefront of granular physics research. Experiments have shown that creep occurs below the assumed static coefficient of friction (63). While creep rheology is still uncertain, new models for creep indicate that rather than a viscous-like flow rule, an elastoplastic model may be physically relevant (66). Interestingly, a similar type of model was found to best describe solifluction experiments, rather than a viscous model (67). Experimental and field work is needed to understand whether solifluction is best described as a creeping granular material, a highly viscous non-Newtonian fluid, or some combination of the two, especially given the complex, temporally changing processes (frost heave, gelifluction) that are known to drive it.

required for segregation ice growth and frost heave, the main drivers of solifluction (2, 51). (49) find that the depth and intensity of frost cracking increases with annual temperature amplitude and decreases with MAAT. To explore this idea, we compare high temporal resolution climate metrics from extensive monitoring stations in Norway over the last 20 years (52) with solifluction lobe morphology for each site shown in Figure 3A. Consistent with frost cracking predictions, we find an increase in finger wavelength and lobe thickness with annual temperature amplitude, corresponding with a general decrease in MAAT (Figure 4). Other differences between high and low elevations may explain observed morphology trends. While we do not see strong relationships with mean annual snowfall, precipitation, or time spent in the frost cracking window (SI Appendix, Figs 7-9), shortwave radiation or vegetation coverage may be important. We interpret the data to show that climate primarily affects the depth of solifluction processes, which in turns affects the wavelengths. This is supported by a much weaker relationship between elevation and wavelength normalized by thickness (SI Appendix, Fig 10). We acknowledge that we have no constraints on the age or current activity of the features at our sites; therefore, modern climate conditions may not reflect conditions at the time of formation. However, modern studies have found that solifluction processes are active on the Norway mainland (e.g., (53-55)).

Discussion

Our work suggests that even extremely slow-moving soils may exhibit subcritical fluid-like instabilities, but at length and time scales orders of magnitude larger than those observed in thin films. Our new conceptual model for solifluction pattern formation provides a framework for further study. Here we provide some discussion on the most interesting questions resulting from this study, with suggestions for the most promising avenues of exploration.

The initial downslope instability that forms solifluction

Our results also suggest strong connections between climate and solifluction lobe morphology. While much more detailed work is needed to quantitatively understand the role of climate in setting solifluction patterns and lobe morphology, these results suggest that lobe morphology metrics measurable from remote sensing data may contain information about present and past climate, both on Earth and other planets. Additionally, these data show that a changing climate may have substantial effects on solifluction dynamics and morphologies. This relates to a fundamental, yet unanswered question: why do we only see solifluction patterns in cold places? We argue that solifluction provides an example of a contact line instability in a parameter space well outside that of previous studies, with the potential to help shed light on recently observed subcritical fluid instabilities (e.g., (26, 46)) and unstable behavior of soft materials (62). Strong heterogeneity in topography and material properties may be required for the instability to form, as is observed in subcritical fluid fingering over rough substrates (46, 68); it is notable that many hillslopes exhibit solifluction terraces with smooth fronts that are not broken into fingers; (8) qualitatively noted that terraces seem to form in areas with homogeneous snow cover and smooth topography, further supporting the idea that solifluction lobes grow as a secondary instability on top of the downslope instability and require heterogeneity to form. We do acknowledge that isolated solifluction lobes are also observed in areas with increased soil moisture (8), perhaps behaving similarly to an isolated droplet moving down a plane (69). Numerical and appropriately scaled physical experiments may be used to explore required thresholds for the onset of both the downslope and cross-slope instabilities under different rheological regimes and to test the idea that competition between gravity and cohesion is needed to initiate the instability. A better understanding of critical conditions for the onset of the instabilities would also inform our understanding of solifluction lobes seen on Mars, whether they require a cold climate to form, and what explains the larger wavelengths seen on Mars (6, 37). Our findings may also have relevance for earthflows, temperate, slow-moving landslides that exhibit similar morphologic and dynamic characteristics to solifluction lobes (70).

More work is needed to understand soil cohesion and velocity trends across solifluction features and how they relate to the onset of instability. We highlight three potential mechanisms for observed spatial gradients in soil velocities, all related to soil moisture: capillary suction, ice lens formation, and vegetation. Studies of soil moisture trends across lobes are limited and find conflicting results that may point toward different mechanisms for increased cohesion at the front; (8) and (71) find that lobes are drier at the front due to drainage, while (72) and (36) find increased soil moisture at lobe fronts due to lower permeability and funneling of water along lobes. Either case may lead to increased cohesion at the front. In the dry front case, decreased soil moisture may induce high capillary suction and therefore higher cohesion (e.g., (73–75)). Lower soil moisture may also inhibit the formation of ice lenses, which drive frost heave and need moisture to grow (76), (77). (8) found that the water table was lowest at the boundaries of solifluction lobes during the fall freeze up, which he interpreted limited the formation of ice lenses and explained low soil velocities at the front. In contrast, increased soil moisture may promote preferential growth of vegetation at the front

(e.g., (36)) that adds cohesion through root strength. It is also noteworthy that soil moistures recorded by (72) fall in the $\sim 5\text{--}10\%$ range, corresponding to strong capillary suction (73–75). Finally, compaction of the front may reduce porosity and permeability (72, 78), altering the rheology of the soil and decreasing the efficiency of ice lensing if permeability is low enough (77). It is possible that all of these effects occur and are important at different points in the season; for example, increased soil moisture at the front may promote vegetation growth in the spring, and decreased moisture after drainage decreases ice lens formation in the fall. Targeted field studies are needed to uncover spatial and temporal changes in soil cohesion across lobes and its effects on stalling the lobe front.

Our analysis is targeted at behavior at the onset of the solifluction lobe instability. Once initiated, the pattern will be self-enhanced as the increased resistance at the raised lobe fronts will further stagger the flow. Nevertheless, more work is needed to understand the evolution of these features through time, as well as possible merging of lobes that would skew measurements toward larger wavelengths. Field studies could examine how disparate lobes interact; for example, once formed, the presence of lobes can redirect water flow through the landscape, influencing lobe development and initiation upslope/downslope (72). For the downslope instability, studies that examine downslope patterns in terrace front exposure dates could determine whether these waves form all at once or initiate at the bottom of a slope and propagate upward. The presence of lobes may also exert a weathering feedback on the underlying bedrock and permafrost, as soil thickness changes substantially along the length of a lobe.

Finally, our results highlight the importance of cohesion in landscape evolution. Rather than simply increasing shear strength, as typically assumed in Mohr-Coulomb soil mechanics models, we suggest that the presence of cohesion can lead to non-linear dynamics that cause large-scale instabilities in landscapes. While further field and experimental work is needed to better understand the rheology of arctic soils, we suggest that incorporating formulations of cohesion into soil transport models is key to accurately predict landscape evolution and response to climate change.

Materials and Methods

Velocity and viscosity profiles. We used WebPlotDigitizer (<https://automeris.io/WebPlotDigitizer/>) to digitize solifluction lobe velocity profile data from the literature, both from field (35, 38–43) and laboratory experiments (1, 44). To make the plots shown in 2, we compile the data in python and ensure all data are in the same units. For velocity profiles we attempt to fit an exponential line to the data; if the fit is arbitrarily better than 0.85 (most profiles), then we calculate an e-folding depth to collapse the data onto a normalized plot. If the fit is worse than 0.85, we present those profiles non-normalized in the Supplementary Material. To calculate effective viscosity, we calculate the change in velocity with depth between each data point to obtain the strain rate. We calculate shear stress as $\tau = \rho g z s$, where we use a constant bulk density ρ of 2500 kg/m^3 ; $g = 9.8$; z = depth in meters; and slope values given in each individual study from which the data are obtained. We then calculate effective viscosity as the ratio between shear stress and strain rate. Finally, we average over all profiles by 10cm wide depth bins to calculate an average effective viscosity profile for all the data.

Lobe wavelength data. Wavelength calculations: Study sites were selected using a combination of high resolution orthophotos and

592 a hillshade of the digital elevation model. We selected 30 hill- 661
 593 slopes on the order of 500 to 1000m long where solifluction was the 662
 594 dominant topographic pattern throughout the domain. Sites with 663
 595 exposed bedrock, gullies, or ponds were avoided. Using a gradient 664
 596 and hillshade map, cross-hillslope groups of solifluction lobes were 665
 597 manually delineated (Figure S1). To streamline and standardize 666
 598 the delineation process, we represent each lobe as a georeferenced 667
 599 triangle. The three vertices defining the triangle were placed along 668
 600 the riser of the lobe at the apex and the two points on either side 669
 601 of the apex where adjacent lobes begin (Figure S1). Lobes were 670
 602 not delineated when riser edges and transitions into adjacent lobes 671
 603 were ambiguous. In addition, some sites contained smaller lobes 672
 604 superimposed on larger terraces or lobes. In these instances we 673
 605 delineated the smaller scale feature. In addition to individual lobes, 674
 606 a minimum of 5 downslope transects were delineated at each study 675
 607 site. Transects were oriented in the direction of the lobes with 676
 608 vertices added each time the transect crossed the riser of a lobe. 677
 609 Over 3500 individual lobes were delineated across 28 hillslopes. 678

610 For each lobe we used the triangle vector to estimate several 679
 611 planform morphological metrics including lobe orientation, width, 680
 612 and length. To determine orientation we first calculated the line 681
 613 bisecting the interior angle at the apex of the lobe. Lobe orientation 682
 614 was taken to be the direction of this line. Lobe width was calculated 683
 615 as the distance between the two endpoints on either side of the apex. 684
 616 Lobe length was calculated as the minimum distance between the 685
 617 apex and the line connecting the two endpoints. At each lobe a local 686
 618 transect was extracted from the elevation data using a 50m window 687
 619 centered at the lobe apex and in the direction of the bisecting line. 688
 620 Elevation profiles along the transect were extracted using linear 689
 621 interpolation with the number of points in the profile determined by 690
 622 the length of the transect and the DEM resolution (length/cell-size) 691
 623 (figure S1b,c). 692

624 From the profile, lobe thickness and contact angle (referred to as 693
 625 riser angle in the solifluction literature) were determined. Transects 694
 626 were first detrended by finding the best fit line to the entire 50m 695
 627 transect in a least squares sense. The slope of the trend line was 696
 628 taken to be the parent slope. To calculate lobe thickness and contact 697
 629 angle, the detrended profile is subset to only include the portion 698
 630 of the profile representing the manually delineated lobe and 2m 699
 631 down slope of the lobe apex (figure S1d). Thickness is calculated 700
 632 as the elevation range in the subsetted profile. Contact angle is 701
 633 calculated as the maximum derivative along the subsetted profile 702
 634 using a central differencing scheme (numpy gradient citation). 703

635 To compare data in Figure 2 with our theoretical prediction, we 704
 636 plot a 1/2 power law on top of the data and use the best fit power 705
 637 law intercept to position it. Data are split into 12 x-axis bins and 706
 638 averaged to give the black data points in 2. 707

639 **Climate data.** We use SeNorge2, a gridded meteorological data 708
 640 set with a spatial resolution of 1 square kilometer and 709
 641 a temporal resolution of 1 hour to estimate typical cli- 710
 642 mate conditions for each study site. Data comes from 711
 643 the Norway Meteorological Organization and can be found 712
 644 at <https://thredds.met.no/thredds/catalog/senorge/catalog.html>. 713
 645 While hourly data is available, in this study we used products re- 714
 646 leased at the daily timescale. The variables include maximum daily 715
 647 temperature, minimum daily temperature, mean daily temperature, 716
 648 and daily precipitation. The gridded data is interpolated from 717
 649 monitoring stations throughout Norway and is corrected to account 718
 650 for elevation. For full description of the climate data see (52). We 719
 651 identified each grid cell containing a study site and extracted the 720
 652 previous 20 years of daily climate data. We grouped the mean daily 721
 653 temperature data for each site by year, then calculated the yearly 722
 654 temperature amplitude as the difference between max and min mean 723
 655 daily temp for each year. We then report mean yearly temperature 724
 656 amplitude T_a as the mean temperature amplitude averaged over 725
 657 all 20 years of data for each site bounded within the 5th and 95th 726
 658 percentile of the data. We calculated the number of frost cycles per 727
 659 year at each site where a frost cycle was defined as a zero crossing 728
 660 of the temperature data. Since the hourly data is summarised at 729

the daily scale this is equivalent to a change in sign between the 661
 maximum daily temperature and the minimum daily temperature. 662
 We used the surface temperature data as a proxy for ground tem- 663
 perature (i.e. no corrections/adjustments are made). Justification 664
 comes from experimental studies measuring soil movement due to 665
 frost heave and gelifluction. We averaged the morphology data at 666
 each site in order to compare with the number of frost cycles, and 667
 bootstrapped 95 confidence intervals for the means. 668

Data Archival. All data and code used to produce figures are 669
 available at the NGEE Arctic Data Repository (79). Norwegian 670
 LiDAR data are available for download [here](#). Norwegian 671
 climate data are available [here](#). Additional figures and supple- 672
 mentary information are provided in the SI Appendix. 673

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