Simulating fully-integrated hydrological dynamics in complex Alpine headwaters: potential and challenges

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Key Points:

- An integrated model of two adjacent steep, snow-dominated, geologically complex Alpine headwaters was developed and calibrated automatically
- Spatio-temporal dynamics and interdependencies of snow, surface water, groundwater, and evapotranspiration processes were represented
- Employing alternative, commonly used subsurface simplifying assumptions strongly affected simulated dynamics
Abstract

Highly simplified approaches continue to underpin hydrological climate change impact assessments across the Earth’s mountainous regions. Fully-integrated surface-subsurface models may hold far greater potential to represent the distinctive regimes of steep, geologically-complex headwater catchments. However, their utility has not yet been tested across a wide range of mountainous settings. Here, an integrated model of two adjacent calcareous Alpine headwaters that accounts for 2D surface flow, 3D variably-saturated groundwater flow, and evapotranspiration is presented. An energy balance-based representation of snow dynamics contributed to the model’s high-resolution forcing data, and a sophisticated 3D geological model helped to define and parameterize the subsurface structure. In the first known attempt to calibrate a catchment-scale integrated model of a mountainous region automatically, numerous uncertain model parameters were estimated. The salient features of the hydrological regime could ultimately be satisfactorily reproduced – over an 11-month evaluation period, the Nash-Sutcliffe efficiency of simulated streamflow at the main gauging station was 0.76. Spatio-temporal visualization of the forcing data and simulated responses further confirmed the model’s broad coherence. Presumably due to unresolved local subsurface heterogeneity, closely replicating the somewhat contrasting groundwater level signals observed near to one another proved more elusive. Finally, we assessed the impacts of various common model simplifications and assumptions on key simulated outputs, finding strongly affected model performance in many cases. Although certain outstanding challenges must be overcome if the global uptake of integrated models in mountain regions is to increase, our work demonstrates the feasibility and benefits of their application in such complex systems.

Key words: Mountain hydrology; integrated hydrological modelling; snow; geology; calibration; spatio-temporal
1. Introduction

Mountainous water resources are crucial for many human societies and ecosystems around the world (Immerzeel et al., 2020; Viviroli et al., 2020). However, in the European Alps as elsewhere, two key hydrological system components – the glaciers and snowpacks – are declining rapidly due to ongoing warming (Beniston et al., 2018). Reliable projections of Alpine hydrological system behavior are therefore urgently required to design and implement sound mitigation and adaptation measures.

In terms of their complexity and dynamics, mountain hydrological systems have few equivalents. For instance, considerable elevation gradients and rugged topography drive pronounced spatio-temporal variability in meteorological conditions, and inherently complex bedrock and unconsolidated sediment architectures can strongly influence subsurface flow patterns and storage dynamics, and therefore broader hydrological system functioning. Contemporaneous changes in other system components such as forests and permafrost could modulate more direct climate-driven hydrological changes (e.g. Evans et al., 2015). Unfortunately, the quantity and spatial representativeness of environmental data in such environments is often notoriously limited (Thornton, Palazzi, et al., 2021).

Despite this high complexity, but probably also partly due to limited data, most mountainous hydrological climate change impact assessments rely on highly simplified “box-type” conceptual hydrological models (e.g. Jenicek et al., 2018; Wagner et al., 2017). More physically-based models such as the Cold Regions Hydrology Model (CRHM) and Alpine3D are now being increasingly applied (e.g. DeBeer and Pomeroy, 2017; Brauchli et al., 2017). However, both model classes have important limitations with respect to the representation of subsurface flows and exchanges between surface and groundwaters. Typically, only shallow “soil zones” are represented, combined with spatially lumped “groundwater reservoirs”. Storage-discharge relationships are generally assumed to be linear, and both lateral flows and subsurface-surface exchanges are routinely neglected (Gallice et al., 2016; Fatichi et al., 2015).

Elsewhere, partial differential equation-based, spatially distributed, fully-integrated (or fully-coupled) surface-subsurface models are becoming more popular; reported applications now span a considerable range of research questions, environmental settings, and spatial scales (Ala-aho et al., 2015; Hwang et al., 2018; Jaros et al., 2019; Maxwell et al., 2015; Smerdon et al., 2007; Sulis et al., 2011; Tolley et al., 2019). These codes can mechanistically simulate most relevant hydrological processes including 2D surface flow, 3D variably-saturated groundwater flow, and evapotranspiration in a physically-based, distributed, transient, and internally coherent fashion. In contrast to traditional groundwater models, recharge does not have to be prescribed externally. Runoff generation can arise from arbitrary combinations of infiltration overland flow, saturation excess overland flow, and groundwater discharge), meaning that dominant runoff generation mechanisms need not be assumed a priori.

Integrated models would appear to be especially well-suited to simulating distinctive mountain hydrological regimes. As 3D information on the arrangement of subsurface formations can be incorporated, they should be able to explicitly capture the influence of complex Alpine geologies on broader hydrological dynamics. Surface water flows, which are important in terms of flood risk and sediment transport in steep terrain, are simultaneously accounted for. In addition, the free, bi-directional exchange between the surface and subsurface domains can be represented. As such, unlike most hydrological models which require fixed stream locations to be defined, fully-integrated codes like HydroGeoSphere (HGS; Aquanty Inc., 2016) allow the stream network to evolve dynamically according to the topography, boundary conditions, and surface and subsurface properties prescribed. This could be useful because many headwater torrents and streams are intermittent (Durighetto et al., 2020; Van Meerveld et al., 2019) and/or demonstrate strong spatio-temporal variability in patterns of loss and gain more generally.

Several progressively comprehensive and complex studies seeking to exploit the capabilities of advanced coupled and integrated surface-subsurface models in mountainous contexts have emerged over recent years (Gleeson and
Manning, 2008; Huntington & Niswonger, 2012; Voeckler et al., 2014; Markovich et al., 2016; Pribulick et al., 2016; Ala-aho et al., 2017; Penn et al., 2016; Carroll et al., 2019; Maina & Siirila-Woodburn, 2020). Whilst these examples attest to much progress, they predominantly focused on crystalline or other low permeability/storage bedrock catchments in western North America, and generally still involved substantial structural simplifications.

For instance, some previous studies simply assumed bedrock to be entirely impermeable (i.e. a no-flow boundary was imposed at its upper surface; Ala-aho et al., 2017; Camporese et al., 2019). Alternatively, single bedrock zones with homogeneous hydraulic conductivity (Markovich et al., 2016; Voeckler et al., 2014) or a few sub-parallel geological layers (Huntington & Niswonger, 2012) were considered sufficient, although Engdahl and Maxwell (2015) employed a more detailed representation. Even where bedrock flow was permitted, domains were typically limited vertically to only a few tens of meters below the surface, potentially limiting groundwater circulation depth. Although hydraulic conductivity may indeed decline strongly with depth in crystalline settings (Welch & Allen, 2014), field evidence for deep flows is increasing (Frisbee et al., 2017).

The uptake of integrated models in other, potentially even more complex, mountainous regions remains extremely limited. For instance, the topographic, geological, and process complexity of hydrological systems in the European Alps is arguably higher than that of mountainous basins in the Western U.S. and Canada, partly because the range is geologically younger. As such, certain assumptions made in previous mountain integrated modelling studies may be even more strongly challenged by Alps’ steep, snow-dominated, and geologically complex nature. Indeed, in calcareous parts, sequences of limestones, shales, and marls have been folded and faulted into complex arrangements. In these regions, groundwater flowpaths can be deep, with patterns strongly influenced by aquifer-aquitard interface geometries (Thornton et al., 2018). Consequently, integrated models here should ideally be based on 3D representations of structural geology, but 3D datasets possessing the requisite attributes for hydrological/hydropgeological modelling have traditionally been lacking (e.g. Thornton et al., 2018).

Similarly, in steep, rugged terrain, forcing datasets should be highly resolved in space and time (i.e. on the order of 10s – 100s of meters, and at hourly time-steps). However, running complex integrated models of real-world catchments with such highly-resolved spatially distributed and transient boundary conditions remains uncommon, and so its feasibility is unclear. On this note, it is worth mentioning that fully-integrated model generally lack the convenient pre-processing routines to correct (e.g. for precipitation undercatch) and spatially interpolate meteorological station data. As reanalysis products are generally still too coarse and unreliable to be applied directly in small, rugged headwaters, this may hinder their usability. Other code limitations may pose further problems; for example, GSFLOW (Markstrom et al., 2008) runs exclusively at daily time-steps.

Adequately representing snow dynamics, and therefore spatio-temporal patterns of meltwater arrival at the land surface, is also imperative. The main challenges in this regard are associated with high process variability and complexity alongside limited and uncertain meteorological data. Integrated models generally offer only index-based snowmelt estimation approaches (an exception is ParFlow.CLM which supports an energy-balance scheme). For example, the study of Voeckler et al. (2014), alongside other integrated model applications in less mountainous but nevertheless strongly snow-influenced settings (Cochand et al., 2019; Schilling, Park et al., 2019) involved such empirical schemes, while Ala-aho et al. (2017) neglected snow processes altogether. Integrated surface-subsurface code do not yet incorporate snow redistribution processes. As such, advancements in distributed snowpack simulations – for example using physics-based, multi-layered snow models (Brauchli et al, 2017), more hybrid physical-empirical models conditioned on various snow observations (Thornton, Brauchli, et al., 2021), and other similar efforts (e.g. Griessinger et al., 2019; Schattan et al., 2020) – have yet to be combined with integrated descriptions of surface-subsurface flow dynamics.

Finally, integrated models are notoriously computationally intensive. Long runtimes (often days to weeks; Miller et al. 2018) can confound formal automated calibration and uncertainty analyses, which require many forward
iterations (von Gunten et al., 2014). Of all the mountainous integrated modelling studies discussed hitherto, only Ala-aho et al. (2017) attempted automated calibration, with others relying on – if anything – manual calibration and/or simple sensitivity analyses (see also Foster and Maxwell, 2019). Nonetheless, because “mountains do not give up their secrets easily” (Klemeš, 1990), the importance of calibration is arguably higher here than elsewhere.

In summary, meeting the goal of developing robust and informative simulations of Alpine systems using fully-integrated models would appear to require progress beyond established practices in several areas. In this context, we sought to develop and calibrate a fully-integrated model of two adjacent steep, snow-dominated, and geologically-complex headwater catchments in Switzerland to gain insights into two initial research questions:

1. How feasible is the development and application of integrated models employing minimal structural simplification in complex Alpine terrain?
2. To what extent can such models be calibrated automatically using streamflow and groundwater level time-series data?

Then, bearing in mind the structural simplifications applied in previous studies (and the general neglect of structural uncertainty), we developed several structurally simplified model versions (mimicking common approaches) which were applied in a series of sensitivity experiments to address a further research question:

3. Taking the calibrated “full complexity” model as a reference, to what extent do structural simplifications affect model performance, and what can be inferred about the degree of model complexity required in such settings?

Being able to address this third question is a key corollary benefit of developing holistic, complex models in the first instance. Pursing this research theme more extensively could help to close the gap between simpler and coarser models that can be applied efficiently across large areas and timescales but which may not yield locally meaningful or useful predictions, and more detailed and sophisticated models that able to exploit multiple local datasets but which are currently less amenable to extension across larger areas.

2. Methods
2.1. Study area and field instrumentation

The ~37 km² study area encompasses two adjacent headwater catchments in the western Swiss Alps – the Vallon de Nant and the Vallon de La Vare (Figure 1). Elevations range from 950 m to >3,050 m a.s.l, slopes are steep, and the topography is rugged. The Vallon de Nant has been designated a Natural Reserve since 1969, and the wider area remains in a highly natural state. Land cover is varied; with increasing elevation, dense forest progressively gives way to open alpine pastures, regions of unconsolidated rock, and bedrock outcrops/cliffs. Debris flows and avalanches occur frequently. Apart from in the valley bottoms, soils are generally thin or non-existent, whilst small glaciers persist in the highest sheltered, north-facing sections. Some permafrost is present at the highest elevations (Giaccone et al., 2019), but is unlikely to be extensive. Various unconsolidated Quaternary sedimentary features overlie the bedrock in places and are thought to function as aquifers.

Approximately 40% of annual precipitation (≥1400 mm) falls as snow. Snowmelt dominates total annual streamflow and contributes significantly to groundwater recharge. Intensive convective storms occur regularly in summer. The surface hydrology of the Vallon de Nant is characterized by numerous temporary torrents, whose discharge responds rapidly to rainfall and snowmelt. Streams and other surface water features are less conspicuous in the upper part of the Vallon de La Vare, probably because of its more permeable near-surface bedrock. Lack of long-term, systematic hydrometeorological observations and severely restricted vehicular access (due to environmental regulations) represented challenges to model development.
Geologically, the region lies within the Nappe de Morcles; the lowest of a series of large nappe thrust folds that together constitute the Helvetic Nappes. Alternating sequences of fairly permeable and – in places – probably karstified limestones are interspersed with much lower permeability marls and shales (Badoux, 1971). These Mesozoic sequences have been folded and faulted into complex arrangements by tectonic forces, such that the geometries of the various (non-planar) aquifer-aquitard interfaces are expected to strongly influence groundwater flow patterns. As alluded to above, the two sub-catchments lie within different zones of the first-order fold structure. Thornton et al. (2018) provide further information on the area’s geology and known or hypothesized hydrological / hydrogeological functioning.

Figure 1. The study area and its location within Switzerland. Stream discharge (S1-S3) and groundwater level (N1-N4) measurement station locations are indicated. Coordinates are in the CH1903 system (m). The catchment center is at approximately: N46.23, E7.10. A concrete weir exists downstream of Pont de Nant (S2 in Figure 1, see also Figure S1a). Such gauging stations are rare on low-order Alpine streams, especially upstream of any anthropogenic influences. Automatic water level measurements were combined with a salt-dilution derived rating curve (Ceperley et al., 2018) to generate a fairly complete record of hourly discharge from April 2016 onwards. Shifting streambed configurations immediately upstream of the regular cross-section undermine the consistency of the record somewhat, leading to potential biases
and/or uncertainties affecting both high and low flow estimates. Stream level measurements were also made at two additional locations, S1 and S3, but the resultant discharge series here are shorter and more uncertain as the cross-sections were not fixed.

Four small-diameter shallow (up to 6.5 m deep) groundwater piezometers (or observation wells) were installed in the vicinity of the large alluvial fan system in the central part of the Vallon de Nant (N1-N4 in Figure 1; see also Figure S1). The piezometers were screened over at least their lower halves, and were equipped with the pressure loggers in June 2017. They yield half-hourly observations, although at three of the four sites groundwater levels fell below the piezometer base elevations for considerable periods.

2.2. Model setup

HGS (Aquancy Inc., 2016) is a fully-integrated simulator that simultaneously solves the diffusion wave approximation to the Saint-Venant equations for shallow 2D surface flow and a modified form of Richards’ equation for 3D variably-saturated subsurface flow. The surface-subsurface coupling was conceptualized here using the first-order-exchange method (Ebel et al., 2009). Although some formations are expected to be karstified and soil macropores also likely present, the subsurface was treated as an Equivalent Porous Media (EPM). As such, parameters values must be considered effective at the elemental scale. Interception and evapotranspiration are simulated according to Kristensen and Jensen (1975) as a function of atmospheric demand (i.e. potential evapotranspiration; \(ET_p\)), surface and near-surface moisture conditions, and vegetation properties. HGS was chosen over possible alternatives on account of its support for (partially, in this case) unstructured finite element meshes which – compared with regular discretization schemes – allow better representation of the study area’s complex topography and other physical features than regular discretization schemes. Additionally, as noted earlier, the stream network is free to evolve “naturally” in HGS.

2.2.1. Finite element mesh generation

Several meshes were initially developed and tested to achieve an appropriate balance between the representation of physical features, good numerical convergence, and the total number of nodes/elements. Catchment boundary and theoretical stream polylines generated via a terrain analysis acted as the primary geometrical constraints. In the final 2D triangular surface mesh (Figure S2), which was generated using multi-level optimization and Delaunay refinement in Algomesh (HydroAlgorithmics, 2016), nodes were spaced at approximately 20-25 m intervals along the streamlines to capture the morphology of the incised watercourses, with separation distance then increasing away from riparian areas. The mesh was further refined in very steep areas, and nodes were placed at precisely the same locations as the in situ instruments. Overall, a fairly high surface mesh resolution was required to minimize potential biases that can be induced in such terrain if low-order streams and ridges are smoothed out (Wang et al., 2018). Typical terrain pre-processing (Käser et al., 2014) was not carried out due to the presence of topographically closed basins in the limestone landscape of the Vallon de La Vare. Rather, surface node elevations were simply extracted directly from the swissALTI3D Digital Terrain Model (DTM) (horizontal resolution = 2 m). Thereafter, the mesh was extruded vertically in 23 layers, resulting in a 3D mesh comprised of 272,376 nodes (507,771 prismatic elements) (Figure 2). (Note: under the “dual nodes” approach applied, HGS automatically creates a duplicate surface node sheet).
Figure 2. The partially-unstructured 3D prismic mesh. The Z-variable denotes elevation in meters above sea level (a.s.l.). The surface mesh was refined close to the streams and in very steep areas. Discretization in the vertical plane was finest near the surface and coarsened with depth. Coordinates are in the projected CH1903 system (m).

Vertical resolution was maximal near the surface, with sheets created at 0.25, 0.5, 1.0, 2.0, 4.0, and 6.0 m depths to ensure that near-surface wetting / drying fronts could be captured, that layers coincided with the assumed soil thicknesses (see next subsection), and that nodes were located at the approximate depths of the groundwater pressure transducers. The next three layers were spaced at 5 m intervals everywhere, except within the extents of major unconsolidated features (in these areas, the lowermost of these layers corresponds to the estimated feature base geometries – that is, depth to bedrock in all apart from the Nant alluvial fan – and the remaining two layers equally divided the remaining distance up to the 6.0 m deep layer; see also Supplementary Text S1). Across the entire domain, the spacing between the 14 remaining sub-parallel layers increased with depth until the constant specified base elevation of 800 m a.s.l. was reached. Given the regional geology (folded and faulted sequences of hydraulically contrasting formations, including some thin layers), such an extensive and highly resolved vertical mesh sought to ensure that potential deep flow paths were not artificially curtailed, and that loss of structural information during the transfer of the continuous 3D geological model onto the mesh was minimized.

2.2.1. Definition of surface and subsurface zones

A land cover map developed from swisstopo data (see Figure S3) defined the surface and evapotranspiration zones (i.e. spatial regions assigned uniform parameter values). As the map resolution exceeded that of the mesh, faces were assigned to distinct zones according to the dominant land cover classes (Tables S1 and S2). Estimated permafrost extent in both consolidated and unconsolidated sediments, mapped using the methodology of Deluigi et al. (2017), was superimposed upon this classification (i.e. permafrost presence was treated as a sub-category in the
zonation scheme). The consolidated component of the permafrost map was binary because permafrost presence in rock walls depends strongly on air temperature and can therefore generally be determined confidently. Predicting the spatial distribution of permafrost occurrence in unconsolidated sediments is much more demanding, and so the map of permafrost occurrence in unconsolidated sediments was probabilistic. Only pixels with probabilities > 0.5 were treated as permafrost in the model, however.

Subsurface zones were defined according to three sources. The first was a 3D model of bedrock geology that represents 18 distinct formations and associated features like faults and secondary folds (Thornton et al., 2018; Figure S4). To transfer the bedrock information on the mesh, geological formation identifiers (see Table S3) at each element centroid were extracted. As with the land cover map, some information loss was inevitable during this process. The second source was estimated geometries of five unconsolidated Quaternary features likely to be important aquifers. These geometries were derived via a simple geomorphometrical method, which was complemented by inferences from geophysics for the main alluvial fan aquifer (Nant) feature (see Supplementary Text S1). The formation identifiers of any elements whose centroids fell within these volumes were overwritten with those of the respective Quaternary formation, this reassignment being necessary because all elements were initially assigned an identifier from the bedrock model (i.e. the bedrock model was “filled” to the surface). Wherever bedrock did also not outcrop according to surficial geological maps beyond these major unconsolidated formation extents, a generic “cover” layer with an assumed thickness of 2 m was defined to represent the thin superficial cover.

The third information source – a simple assumed soil depth map (Figure S5) – was prepared in the absence of more detailed information on the spatial distribution of soil depths and their associated textural or hydraulic properties; the existing “official” spatially distributed soil data (OFAG, 1980) were considered dated and of questionable suitability. Soils were considered as a single, homogenous zone, and the same “overwriting” process as described above was applied. Whilst the soil zone is very small compared to the unconsolidated and consolidated geological formations volumetrically, it likely exerts a disproportionately strong hydrological influence via its influence on the partitioning of incident liquid water at the surface. In total, 24 distinct subsurface zones were defined. The main remaining structural uncertainties relate to the soil and unconsolidated aquifer volumes. All these zones were considered fixed in the full complexity reference model.

2.2.3. Boundary conditions

HGS currently provides no meteorological station data pre-processing capabilities, and offers only a simple temperature-index snow module. We therefore elected to apply forcing datasets that were generated externally, but specifically for use in this model (Thornton, Brauchli, et al., 2021). For the snow component, a spatially distributed energy balance-based model that additionally accounts for gravitational snow redistribution from steep slopes was used to generate hourly snowmelt data at 25 m resolution. In that model, several uncertain snow parameters were optimized against snow extent maps derived from Landsat 8 imagery and reconstructed snow water equivalent (SWE) time-series. Commensurate datasets pertaining to glacier melt, rain falling on snow / ice free surfaces, and $ET_p$ (based on the Penman-Monteith method) datasets were also produced. For further details, readers are referred to (Thornton, Brauchli, et al., 2021). The datasets corresponding to the period 1 October 2014 – 30 September 2019, and therefore partially coinciding with the streamflow and groundwater level observations, were compiled to give grided representations of i) “all liquid water arriving at the land surface” (i.e. snowmelt, ice melt, firn melt, and rain), and ii) $ET_p$, which were then applied in HGS as “rain” and “potential evapotranspiration” boundary conditions, respectively. Aggregations to daily and monthly values were also produced.

To allow water to leave the domain, a “critical depth” boundary condition was applied to all surface boundary nodes (Aquanty, 2016). This condition forces the flow depth at these locations to be equal to the critical depth, which is the depth at which specific energy is minimal for a given discharge. It corresponds to the condition of critical flow for which the Froude number is equal to one (Hornberger et al., 2014). The base and sides of the domain were treated as “no flow” boundaries (i.e. flow across these faces was assumed to be negligible).
2.2.4. Initialization

The initialization of catchment-scale integrated models can be time-consuming and challenging (Ajami et al., 2015). Beginning from a prescribed set of initial conditions, the model must be run – using either steady or recursive transient forcing data – until a state of equilibrium (or “dynamic equilibrium”, in transient cases) is attained. Traditional initial condition options are a water table coincident with the surface (a so-called “wet start”), a completely dry domain (a “dry start”), or a water table configured to some shallow but arbitrary constant depth beneath the surface (e.g. 1-5 m; Seck et al., 2015). In HGS, an initial water table surface can also be generated as a function of elevation. However, being influenced not only by topography but also by geology, the mean water table distribution in our study area was expected to be complex (with thick unsaturated zones beneath some mountain ridges, for instance). As such, employing the traditional approaches would likely have resulted in extremely lengthy spin-up times. A customized initial water table was therefore generated by interpolating (in 3D) coordinates \((x,y,z)\) sampled at perennial steam, spring, and wetland locations (i.e. where the water table is at / near the surface) using a spline function. As the hydrological regime under consideration is highly transient, the model (with the initial parameter estimates) was then initialized by applying the monthly frequency forcings corresponding to the 2014/2015 hydrological year recursively. Initialization was deemed complete when the simulated surface water hydrographs and groundwater levels at the various observation points ceased to demonstrate marked inter-annual trends.

2.3. Calibration strategy and historical runs

Many of the model’s parameters were highly uncertain, at least at the elemental scales. Those relating to the inaccessible mountain block subsurface were essentially unknown. Thus, some form of calibration was required. Whilst manual trial-and-error procedures are sometimes applied in the integrated modelling literature, this approach is subjective and would have been confounded by the large number of parameters involved here (which itself arises due to the complex geology and diverse land cover). An automated approach was therefore pursued.

Based on a combination of lithological descriptions (for the bedrock formations), relevant previous studies, and informed judgement, an initial parameterization scheme was devised. A subset of 46 potentially sensitive parameters were then identified as calibration targets (see Tables S1 to S3). The model was linked with PEST_HP (v17) (Doherty, 2020) – a code-independent, gradient-based parameter estimation tool that employs the Levenberg-Marquardt (L-M) algorithm to minimize an objective function (in a least-squares sense). Being a gradient-based method, the L-M algorithm may converge to local minima. Nevertheless, its efficiency in terms of the number of forward runs required is attractive when seeking to optimize computationally intensive models. For every PEST model run (i.e. alternative parameter set proposed), a “re-initialization period” beginning on 1 October 2014 (approximately 18 months before the first available observations) was simulated to try and equilibrate the system state to the new parameters. All available hourly (mean) streamflow measurements and half-hourly (instantaneous) groundwater level measurements from 9 April 2016 (i.e. the start of measurements at S2) until 31 October 2017 were used in the calibration, although depending on the site there were data gaps of varying length. Following a split-sample strategy, the remaining observations (from November 2017 to September 2018 inclusive) were retained for independent evaluation.

The objective function (OF) was:

\[
\text{OF} = \sum_{i=1}^{20409} [w_{\text{GWL}} (GWL_{\text{sim}} - GWL_{\text{obs}})^2] + \sum_{i=1}^{13184} [w_{\text{QS2}} (QS_{2\text{sim}} - QS_{2\text{obs}})^2] + \sum_{i=1}^{60533} [w_{\text{QS1,3}} (QS_{1,3\text{sim}} - QS_{1,3\text{obs}})^2]
\]

[Eq. 1]
where \( w_{GWL} \), \( w_{QS2} \), and \( w_{QS1,3} \) are the relative weights that were assigned to each “observation group”, i.e. the groundwater levels, the streamflows at S2, and the streamflows at S1 and S3, respectively. Here, \( w_{GWL} = 0.38 \), \( w_{QS2} = 5.50 \times 10^{-5} \), and \( w_{QS1,3} = 9.00 \times 10^{-5} \). \( GWL_{sim} \) and \( GWL_{obs} \), \( QS2_{sim} \) and \( QS2_{obs} \), and \( QS1,3_{sim} \) and \( QS1,3_{obs} \) are the corresponding simulated and observed values at N1-4, S2, and S1 and S3, respectively.

Given the contrasting number, magnitudes, and units of observations within the different groups, as well as the unknown degree of initial mismatch, the final weighting scheme used in the OF (i.e. the weights to apply to the observations in each of the three groups) could only be determined after running the model once with the initial parameters and arbitrary weights, and is inherently somewhat subjective. Usually, one would seek to roughly equilibrate the respective contributions of each observation group to the OF. Although the streamflow measurements (being spatially integrated) and groundwater level measurements (being spatially explicit) can be considered complementary (Paniconi & Putti, 2015), in complex unconsolidated settings, groundwater levels can be heavily influenced by extremely local phenomena. In this case, because the four piezometers were located within a single model zone, we realized that it would be essentially impossible to reproduce the distinctly different groundwater responses observed in these nearby wells without introducing sub-zone heterogeneity, which was beyond the present scope. Therefore, to prevent the calibration process magnifying this deficiency in model structure, the groundwater levels were weighted relatively lightly such that their combined contribution to the initial OF was only around 11%.

In other words, whilst each observation group maintained at least some “visibility” in the calibration, most emphasis was placed on streamflows.

Various additional model simplifications were necessary to facilitate automated calibration (cf. Ala-aho et al. 2017). Firstly, the re-initialization and calibration periods described above were relatively short. Whilst this naturally facilitated the multiple runs required, longer periods would of course have been preferable. That said, the length of the calibration period specifically was largely dictated by observational data availability and a desire to maintain an independent evaluation period. That said, given the pronounced seasonality of the catchments’ hydrological regimes, it was considered crucial that the calibration period should exceed one year.

Runtimes were found to increase substantially with the forcing data’s temporal resolution. Therefore, in a second simplification, the calibration runs were undertaken using only monthly (but still distributed, 25 m) forcings. Perhaps slightly surprisingly, simulated seasonal dynamics were not highly sensitive to monthly vs. daily data (Figures S8 and S9), which provides some justification for this strategy. In another simplification aimed at reducing runtimes, the unsaturated zone (pressure head–saturation, and saturation–relative hydraulic conductivity) relationships for all subsurface zones except the soil were made less non-linear and represented in tabular form using a small number of data points. The poorly understood nature of these relationships in consolidated, potentially fractured, and/or karstified bedrock supports this approach. For the soil, van Genuchten parameters (van Genuchten, 1980) were applied (see Table S1).

The slope term in the surface water flow equations was assumed equal to the topographic slope, and thereby also linearized. Furthermore, the HGS model’s convergence criteria were relaxed for calibration (Newton absolute = \( 1 \times 10^{-3} \) m, Newton residual = 500 m) before being re-tightened for the subsequent runs with optimized parameters (Newton absolute = \( 1 \times 10^{-3} \) m, Newton residual = 150 m). The latter settings led to a mean mass balance error, expressed as a percentage of liquid water input, of \( \leq 5\% \). Finally, the “coupling length” parameter for all surface zones except the streambed was set to a somewhat higher (and fixed) value (0.1 m) than is ordinarily the case; values closer to zero are generally recommended to approximate the Continuity of Pressure (COP) approach, but typically increase runtimes (Liggett et al., 2012). Tests revealed model outputs of interest to be fairly insensitive to this choice. To represent the enhanced surface-subsurface disconnection that the fine silty streambed sediments we observed in the field could induce, the streambed zone coupling length was fixed to 1.0 m.
The calibration runs were carried out on a Windows machine (Intel(R) Xeon(R) CPU E-2699 v4 @ 2.20 GHz, 64.0 GB RAM, 44 cores with 12 agents running in parallel). Each HGS instance was also distributed across two cores. Despite the simplifications and calibration challenges, parameters from all three “domains” could be calibrated, and the value of the multi-component OF was reduced somewhat, indicating modest success. Two runs were then made using the optimized model: i) the full four-year period was simulated with daily forcing, and ii) the final two-year period was simulated with hourly forcing. The latter enabled the impact of forcing frequency on simulated hydrological responses to be further assessed.

2.4. Systematically simplifying the reference model

A series of sensitivity experiments were then undertaken to investigate the impacts of making various structural and process simplifications or assumptions on key model predictions. In each case, simulated streamflow and groundwater levels were compared to those generated by the reasonably calibrated full complexity model forced with daily data (the reference model). In this sense, the reference model parameters should simply be considered reasonable values that can be applied in conjunction with changed structures. The modified model elements are listed below; all other aspects remained as per the reference model. No re-calibration of these simplified models was undertaken because this could have allowed parameters to take on surrogate values to compensate for flawed model structures. In other words, we sought to isolate the influences of the selected model structural and process assumptions (see also Wen et al., 2021). We could have addressed the alternative question of how does optimal model performance and/or how do parameter values change as a function of simplification? by re-calibrating each of the simplified models, but that was not the intention here.

Impermeable subsurface, no ET (Scenario A): This extreme end-member scenario simply assumes that the subsurface is entirely impermeable (i.e. no infiltration or groundwater processes can occur), and additionally that no water is returned to the atmosphere via ET. As such, all liquid water incident at the surface (i.e. rainfall + snowmelt + ice melt) flows directly overland according to the discretized topography and surface parameters.

Limited vertical extent (Scenario B): This scenario involves limiting the vertical extent (or “watershed thickness”) of the reference integrated model (with ET) to a uniform of 30 m. All elements with centroids beneath this depth were deactivated, which is equivalent to applying a “no flow” boundary condition at 30 m depth. Whilst such shallow model configurations are fairly common in both catchment and larger scale modelling studies (e.g. Foster & Maxwell, 2019), a need has been identified to further elucidate the consequences of such choices in terms of simulated hydrological dynamics (Condon et al., 2020).

Spatially uniform forcing (Scenario C): Catchment-scale integrated models are sometimes forced with spatially uniform meteorological boundary conditions (e.g. Ala-aho et al., 2017). Where distributed meteorological/snowmelt data are unavailable, measurements made at a single station within or near a given study catchment might be considered representative of conditions across it. Alternatively, depending on its size, an entire individual catchment may correspond to only a single pixel of a given historical reanalysis product or climate model projection. This uniform assumption is likely to be reasonable in very small and/or fairly flat catchments, but is likely to be less appropriate in larger and more topographically complex mountain headwaters. Thus, for this scenario, the distributed (25 m resolution) daily forcings of the reference model were averaged across the Vallon de Nant sub-catchments. (Note this was only done for the Vallon de Nant).

Near-surface geology from global maps (Scenario D): Several very coarse resolution, continental- to global-scale integrated modelling efforts have applied global hydrogeological maps to define subsurface hydraulic properties (de Graaf et al., 2019; Reinecke et al., 2019). Whilst it is becoming increasingly clear that predictions made in this way are often severely limited with respect to local and perhaps even regional observations (Reinecke et al., 2020), the role of the subsurface representation itself has not yet been isolated, especially in mountainous terrain. We therefore
substituted subsurface information from the GLHYHMPS 2.0 (Huscroft et al., 2018) dataset into our otherwise
detailed and high resolution model.

Specifically, we used this dataset to define hydraulic conductivities and effective porosities in the uppermost 10 m.
To parameterize deeper elements/layers, previous larger scale studies using such datasets have typically employed
an exponential decline in conductivity with depth whose rate is dependent upon the surface slope (Fan et al., 2013).
However, as the parameters of this empirical function are highly scale-dependent, they cannot be directly transferred
to the present, high-resolution model. To mimic the decline in conductivity traditionally imposed nevertheless, the
conductivities of all elements below the uppermost 10 m were set to half their near-surface values. As such, under
this scenario, the detailed 3D structures of the reference model were entirely removed.

No permafrost (Scenario E): A “no permafrost” simulation was undertaken in which the coupling length parameter
in permafrost areas was set back (from 50 m) to the value of 0.1 m assigned elsewhere.

3. Results

3.1. Full complexity integrated model

3.1.1. Daily forcing data

Figures 3 and 4 show streamflow and groundwater level time-series simulated by the calibrated, “full complexity”
integrated model using daily forcing data against the corresponding observations. The annual water balance
dynamics of the areas contributing to S1 and S2 seems to have been well captured, although the onset of high spring
flows does sometimes appear delayed, most notably at S2 during spring 2016. While baseflow levels are replicated
very closely at S1, they appear slightly overestimated at S2. It should be remembered, however, that even at the
concrete weir of S2, low flow measurements (which are really only estimates) can be associated with considerable
uncertainty due to shifting channel configurations immediately upstream, the relative effects of which are greater
than at higher flows. At the principal gauging station (S2), the Nash-Sutcliffe Efficiency (NSE) obtained over the
evaluation period (November 2017 – September 2018 inclusive) was 0.76 (see Table 1). At S3, the fit is noticeably
poorer; this is discussed further shortly.

The observed groundwater levels (Figure 4) at N3 and N4 especially also demonstrate strong seasonality, with
pronounced snowmelt-driven peaks being followed by more gradual recessions at each site. Importantly, although the
four sites are situated fairly close to one another, their respective observed dynamics are quite contrasting. In
comparison, the simulated groundwater level dynamics across the four sites are too consistent or similar. More
specifically, whilst the general observed seasonality is represented in the simulations at all sites, the distinctive
signals at N2 and to a lesser extent N1 could not be reproduced well. At N4, the groundwater level trends, if not the
precise levels themselves, are generally satisfactorily captured. At N3, the simulated head is above the land surface,
which corresponds to exfiltration (also discussed in due course). Despite these differences, Figure S7 suggests that
overall, water table elevations across the alluvial fan zone were approximated reasonably well by the model.
Figure 3. Streamflows simulated by the fully-integrated model using daily 25 m resolution forcing data at the three gauging station locations and daily mean observations for the period 1 October 2014 – 1 October 2018. The dashed green line distinguishes the calibration (left) and evaluation (right) periods.
Figure 4. Groundwater levels at the four piezometer locations simulated by the fully-integrated model using daily 25 m resolution forcing data and daily mean observations for the period 1 October 2014 – 1 October 2018. The horizontal brown line corresponds to the surface elevation. The dashed green line distinguishes the calibration (left)
and evaluation (right) periods. Gaps in observations occur when groundwater levels fell below the bases of the shallow piezometers.

Although the groundwater level fits are not exceptional, Figures 3 and 4 together underline the unique capabilities of integrated models to yield predictions of both streamflows and groundwater levels from a single consistent framework. In this sense, integrated models are clearly far more suited than traditional surface water models to simulate groundwater levels and vice versa. In simulating such a large range of variables, where additional in situ measurements exist (e.g. \( ET_a \) and/or soil moisture), further point-scale comparisons can readily be made.

Another key advantage of comprehensive integrated models is that comparisons and diagnostics are not limited to time-series or scatterplots at observation point locations. Rather, spatio-temporal patterns in forcing data and numerous simulated state variables pertaining to the different “domains” (i.e. the surface, subsurface, and evapotranspiration) can be visualized and/or extracted as required. Visualizing these model datasets and evaluating their consistency with prior knowledge of the system enables the coherency of the numerical representation can be assessed at a conceptual level. In addition, comparisons can be made with independent spatially distributed (or spatially integrated datasets), either in calibration itself or simply for evaluation, further demonstrating the potential of such a simulation approach. To illustrate these varied possibilities, three brief examples from the integrated model forced with daily data are considered.

Firstly, Movie S1 (see Supporting Information) shows the spatio-temporal dynamics of the model’s meteorological boundary conditions (“all liquid water” and potential evapotranspiration) and two important simulated response variables – surface water depth and actual evapotranspiration \( (ET_a) \) – over the hydrological year 2017/2018. During the initial period, dynamics are subdued as the catchment gradually drains. As snowmelt onset occurs at progressively higher locations, the surface water network begins to expand. A strong elevational influence is visible in both the prescribed \( ET_p \) and the simulated \( ET_a \). Some surface water bodies do still form in parts of the Vallon de Le Vare, including at the locations of a high elevation lakes/wetland (e.g. 578653, 123594).

Secondly, Movie S2 shows the interplay between simulated saturation, both at the surface and (using slices) at depth, and the simulated surface water level response in the stream at S2. Throughout the snowmelt period, near-surface saturation levels gradually increase, followed by the arrival of the annual simulated water level peak. These patterns correspond closely with our general knowledge and understanding of the system. Movie S2 also clearly shows that the water table is generally lower in the Vallon de La Vare than the Vallon de Nant, and so could indicate a possible cause of the poorer performance at S3.

Finally, a thermal image of the central part of the Vallon de Nant obtained by drone early in the morning on 7 December 2016 is introduced. No precipitation had fallen in the preceding 10 days, and – unusually for the time of year – the ground remained snow free. As such, all water in the channel could be confidently and exclusively identified as emergent groundwater. As groundwater is several degrees warmer than the dry land surface under these circumstances (i.e. early morning in winter), the region of groundwater exfiltration from the streambed into the channel can be clearly identified (Figure 5a). A comparison can thus be made between this image and the simulated spatial patterns of exchange flux and surface water presence on the same day (Figures 5b and c). Groundwater is seen to emerge at approximately the same location in the model as in reality. Moreover, surface water is present from this point downstream in the simulation, which is again consistent with the thermal image (in which the discrete “warm” region continues northwards downstream). This demonstrates that integrated models are uniquely suited to answer questions such as “where do significant volumes of groundwater exfiltration, or streamflow generation, occur?”
Figure 5. Spatial patterns of (a) relative surface temperature in the distal part of the Nant alluvial fan in the early morning of 7 December 2016 from which “observed” subsurface-surface exchange flux and surface water presence were inferred (note that the stream appears warmer than the surroundings, and that red circular patterns correspond to trees that also appear warmer because of solar illumination), (b) subsurface-surface exchange flux simulated by the fully-integrated model on the same date (positive values correspond to surface water exfiltration), and (c) simulated surface water presence, indicated by the simulated surface water depth, again on the same data. The dashed green box indicates the common area.

Further exploiting the many possibilities that exist to extract and/or visualize data from integrated models offers a viable path to developing improved understanding of complex hydrological systems. For instance, such an approach may help the identification of the regards in which, or reasons for which, a given numerical representation may remain deficient.

3.1.2. Hourly forcing data

Figure 6 presents streamflows and groundwater levels simulated by the calibrated integrated model forced with hourly data at S2 and N4, respectively. In this case, the NSE coefficient attained over the evaluation period at S2, 0.73 (Table 1), was slightly lower than in the daily forcing case, but still denotes good performance. Sharp flow peaks associated with convective thunderstorms are represented a little better than in the daily case (in which the rainfall totals are distributed evenly over 24-hour periods) but remain insufficiently accentuated compared with the observations. To illustrate the high frequency variability more clearly, Figure 7 focuses on a reduced period (spring and summer 2018); one observes that diurnal variations in both streamflow and groundwater levels associated with spring snowmelt (and potentially also ice melt and evapotranspiration) can be reproduced.

Figure 8 shows the catchment water balance over spring and summer 2018; this is another informative type of output that can be obtained from integrated models. (In HGS, the water balance can also be obtained for spatial subsets of the domain by specifying shapefile extents, but that here we look at the entire catchment). The rate of incoming liquid water is seen to exceed the rate of simulated infiltration during the early melt season, causing accumulation in the overland domain. With time, the rate of groundwater exfiltration also increases. Later in the season, the infiltration begins to exceed that of incoming liquid water, which presumably corresponds to infiltration from surface water bodies that can occur as near surface saturation levels decline from their snowmelt induced peaks. Groundwater exfiltration declines a little but remains noticeable.
Figure 6. Streamflow and groundwater levels at S2 and N4, respectively, simulated by the fully-integrated model using hourly 25 m resolution forcing data and hourly mean observations for the period 1 October 2016 – 1 October 2018. The light blue are in the upper pane reflects a potential uncertainty range of +/- 30% around the observations, whilst the pink shading beneath the simulated line in shown simply to enable the two time-series to be compared more easily.
Figure 7. Streamflow and groundwater levels simulated by the fully-integrated model using hourly 25 m resolution forcing at S2, S1, and N4, respectively, and hourly mean observations for the period 1 October 2016 – 1 October 2018.
3.2. Simplified models

3.2.1. Impermeable subsurface, no ET (Scenario A)

Figure 9 presents streamflows simulated under the “impermeable matrix” assumption (with ET also deactivated), using daily forcing data. Close correspondence between simulated and observed peak timing is observed, which provides further reassurance that the previously generated liquid water inputs (Thornton, Brauchli, et al., 2021) are reasonable. Entirely expectedly, simulated flows under this assumption are overestimated with respect to observations during high flow periods and underestimated during lower flow periods. Interestingly, the degree of overestimation is much more pronounced at S3 than S1 and S2, which clearly demonstrates that the actual runoff ratio of this geologically complex sub-catchment is considerably lower than that of the others in reality. The spatial
outputs from this simulation (not shown) reveal that, again unsurprising, a substantial lake forms in the topographic
depression of La Varre (~576859,123516). No such lake exists in reality, although a wetland is located in this area.
Figure 9. Simulated streamflow at each of the three gauging stations under the “impermeable matrix” assumption (i.e. “surface only”, with infiltration, subsurface flow, and evapotranspiration (ET) all deactivated) using daily 25 m resolution data, and daily mean observations.

3.2.2. Limited vertical extent (Scenario B)

Compared with the reference simulation, limiting the model’s vertical extent to 30 m accentuates peak flows appreciably, reduces baseflows, and leads to more pronounced recessions (i.e. the regime becomes “flashier”; Figure 10). Minimum groundwater levels are lower under this scenario than in the reference case. As in Scenario A, the streamflow simulations at S3 are extreme overestimations, most especially during 2018. Annual peak groundwater levels in the Vallon de Nant piezometers are hardly affected, but recession rates are noticeably more rapid and annual minima are lower (Figure 11). Figure S16 shows the main catchment water balance fluxes for this scenario with respect to the baseline model. One observes in particular that, as expected, both overland flow and groundwater exfiltration are more pronounced under Scenario B.
Figure 10. Streamflows simulated with a version of the fully integrated model whose depth (i.e. vertical extent) was limited to a uniform thickness of 30 m below the surface. Daily 25 m resolution forcing data were applied, and daily mean observations are also plotted.
Figure 11. Groundwater levels simulated with a version of the fully integrated model whose depth (i.e. vertical extent) is limited to a uniform thickness of 30 m below the surface. Daily 25 m resolution forcing data were applied, and daily mean observations are also plotted.
3.2.3. Spatially-uniform forcing (Scenario C)

Applying spatially uniform forcing data across the Vallon de Nant sub-catchment produces noticeably lower spring peaks, especially at the higher elevation site (S1; Figure 12), compared with the reference model (see also Table 1). The impact on groundwater levels is both more modest and less variable over the annual cycle, and is therefore not shown.
Figure 12. Comparison of simulated streamflows generated using 25 m resolution spatially distributed forcing data and spatially uniform (i.e. sub-catchment-averaged) forcing data. In both cases, the frequency was daily.

3.2.4. Geology from global maps (Scenario D)

Figure 13 illustrates the simulations that result from using the GHLYMPS 2.0 map to define 2D near surface porosity and hydraulic conductivity values, with conductivities decreased by a factor of two for all elements with centroids greater than 10 m beneath the surface.

Figure 13. Comparisons between simulated streamflows at groundwater levels at S2 and N4 generated from the full complexity reference model and the model whose key subsurface parameters were derived from GLHYMPS 2.0. In both cases, the forcing data was of daily frequency.

In this case, the simulations bear little resemblance to either the observations, with seasonal streamflow and groundwater level dynamics being far too subdued and groundwater levels generally too low, leading to no streamflow whatsoever being simulated at S1.
3.2.5. No permafrost (Scenario E)

Compared with the reference model, the final simplification – “no permafrost” – led no discernible visual or statistical differences with the reference model at the various observation points. As such, no plots are presented here. An additional “end member” simulation (also not shown) in which the coupling length parameter was set to the “permafrost value” of 50 m across the entire catchment produced only relatively minor differences with the reference simulation.

3.2.5. Statistical comparison of the scenarios

Table 1 presents a statistical comparison of the various scenarios against observations.

<table>
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<th>S1 (NSE)</th>
<th>S2 (NSE)</th>
<th>S3 (NSE)</th>
<th>N1 (SE)</th>
<th>N2 (SE)</th>
<th>N3 (SE)</th>
<th>N4 (SE)</th>
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Table 1. Statistical comparison of correspondence between simulations and observations for the various model scenarios. The Nash Sutcliffe Efficiency (NSE) is used to compare the model fits for streamflow, whilst the standard error (SE) is used for groundwater levels. “EP” denotes “entire period”, whilst “EV” denotes “evaluation period only”. Because the simplified versions were not calibrated, it does not make sense to consider the results only over the evaluation period. In addition, when interpreting these results across sites for a given scenario, it should be remembered that the number and temporal coverage of observations differ.
The streamflow performance metrics of the (uncalibrated) simplified models are universally lower than those of their full complexity (calibrated) counterparts. This is generally also the case for the groundwater levels, and the exceptions (Scenario C at N2, Scenario B at N3, and Scenario C and N4) could simply be down to chance. Whilst the fit scores of the simplified models with respect to both streamflow and groundwater levels could probably have been improved somewhat via calibration, because the model structures employed in these scenarios are either obviously (Scenarios A and C) or very likely (Scenarios B and D) unrealistic in such terrain, parameter values would likely have had to take on implausible values or surrogate roles to achieve this; a situation that would inevitably have adverse consequences for any subsequent predictions. The fits are worst for Scenario D. Overall, these results can be taken to demonstrate the relative value of the full complexity reference model.

4. Discussion

4.1. Assessing the historical time-series simulated by the full complexity model

In light of the study region’s characteristics, in the initial phase of model development, we sought to establish a forcing configuration and model structure that was as comprehensive and constrained as possible. Specifically, all the processes and components omitted in the early synthetic study of Gleeson and Manning (2008) – that is, “evapotranspiration, the role of the orographic effects on precipitation, the seasonal effects of snow accumulation and melting, … transient conditions, such as perched ground-water conditions…[and] the role of alpine glaciers or permeable surficial geology units” – were incorporated. Parameterization and calibration were then conducted “given” this preferred structure.

Each of the main phases, from obtaining the extensive data necessary to build the model, ensuring its smooth and sufficiently fast execution, and finally calibrating it such that the available observations could be reproduced with some skill, were challenging. In addition, because it is possible to constrain the parameters of integrated models to physically plausible values (as was done here), it is to be expected that the levels of fit attainable are often lower than those that can be achieved with simpler, more data-driven alternatives (Mendoza et al., 2015) in which these constraints are less strong or entirely lacking. More generally, since simulating mountain hydrological systems using integrated models remains an emerging discipline, we argue that statistical benchmark levels of fit (corresponding to “good”, “acceptable”, “poor”, etc.) remain to be established for different variables and different types of physical setting. Catchment size also likely influences expected performance levels. For instance, simulating streamflow presence, absence, and level using integrated models in relatively small and steep alpine headwaters is more challenging than in larger catchments. This is because in larger catchment, variability is more “smoothed out”. In other words, outputs would be expected to demonstrate far less sensitivity to small scale (changes in) model structure and parameterisation.

Accordingly, it is satisfying that using the daily forcing data, observed streamflow dynamics at S1 and S2 were generally reproduced acceptably (Figure 3). The improved correspondence between observations and simulations over the evaluation period compared with the calibration period may seem slightly counterintuitive, but could simply be explained by the forcing data having been better estimated over this period (e.g. due to more complete/local input data being available) (Thornton et al., 2021). Another interesting feature of Figure 3, providing it is not a reflection of bias in the observations, is that baseflows appear to be overestimated more at S2 than S1. This could indicate some issue or scope for improvement in the geometries and/or parameterizations of zones (surface or subsurface) that influence flow exclusively (or proportionally more) downstream of S1.

The lower fit at S3 is likely due to the great geological complexity of this sub-catchment, on which data remains lacking, being insufficiently represented in the model. In reality, the high, topographically closed basin of La Varre, which is naturally dammed to a height of around 20 m, must drain through the subsurface. This is because no lake is present in the depression in reality, but merely a wetland (576859,123516). It is possible that, in attempting to
prevent a lake forming here in our model, we set the initial effective hydraulic conductivities in this region too high, which led to an unduly low water table across much of the Vallon de La Vare sub-catchment. Such a water table state naturally favors infiltration and recharge at the expense of more rapid surface and shallow subsurface runoff, ultimately leading to an overly stable hydrograph. In other words, it seems that the model was unable to capture these both aspects (no deep lake but still a rather flashy streamflow response) in a single conceptualization. The problem is therefore likely a structural one. In fact, La Varre is believed to drain via a discrete fracture that bypasses several otherwise impermeable formations, as well as potentially the site of S3 (Lugeon & Gagnebin, 1928). To represent flows through such fractures or karstic conduits, it would probably be necessary to superimpose discrete fractures or conduits on the porous media domain. Whilst this is theoretically possible in HGS, obtaining data to locate and parameterize these features is difficult in remote Alpine settings.

Another possible (or perhaps partial) explanation is simpler. At S3, observed flow levels are much lower in 2018 than 2017. However, the opposite situation occurs at S1 and S2, and winter 2017/2018 was known to be remarkably snow rich more generally. Given that these catchments are adjacent, there could simply be a hitherto undiagnosed issue in the calibration period measurements at S3 (simply measuring streamflow reliably in such settings is often difficult). Of course, it would be undesirable for model calibration to compensate for, and thereby “hide”, and such possible structural or data issues, meaning the mismatch could be less concerning than it may initially appear.

The nature and practical implementation of the inversion algorithm could represent additional limiting factors. It is possible that the solution to the inverse problem (i.e. the calibration) reached a local minimum, and/or that the bounds imposed on the effective parameter values of subsurface formations in the Vallon de La Vare region were too restrictive. It is furthermore conceivable that even if improved within-bound parameter values (i.e. those which would ordinarily have produced a more rapid streamflow response and hence a better match at S3) were proposed by PEST, the 18-month re-initialization period simulated prior to each calibration run may have been too short to allow the internal storages to fully re-equilibrate with the adjusted parameters. Ideally, a longer re-initialization period would have followed every change in parameter values, strictly continuing until a (close to) perfect “dynamic steady state” was re-established. However, given the model’s runtimes (which, incidentally, also depend on the parameter values), such an approach would have precluded automated calibration altogether in this case. The interplay between initial conditions, parameter updates, and re-equilibration within automated optimization frameworks have received very little attention in the integrated modelling literature to date, and should be investigated more thoroughly. The availability of longer time-series could also have led to a more reliable calibration, but would again have increased the computational load. In any case, longer timeseries could not be obtained within the scope of this project, which followed a concurrent “measure and model” philosophy. In summary, some combination of deficient model structure, limitations associated with the parameter estimation approach, and relatively short and perhaps even uncertain observations could explain the difficulties the full complexity model has to reproduce the observations at S3. Nevertheless, as is discussed shortly, these results are still far superior to those generated in the simplified cases, which underlines the challenging nature of this sub-catchment.

Of the four groundwater observation points, N4 can probably be considered the most spatially representative, since it is located closest to the main gravelly part of the alluvial aquifer. It is therefore reassuring that the simulated dynamics at N4 generally correspond with observations, even if the simulated level is slightly higher (Figure 4). Besides the general points related to the calibration discussed above, the influence of local-scale heterogeneity in hydraulic properties is probably the main reason why the agreement between simulated and observed groundwater levels is relatively limited. Whilst all the piezometers are located nearby one another (and moreover in only a small part of the entire model domain), as highlighted already, the observed signals at each are rather contrasting. The flashy response of groundwater above a constant lower level at S2, for instance, probably arises because the piezometer samples a former stream channel comprised of coarse sediments with a relatively impermeable underlying clay-rich layer. Crucially, since all the piezometers are situated within a single model zone (the “Nant” alluvial fan system), to which homogenous material properties were assigned, it is unsurprising that the contrasting
responses observed at each could not be reproduced. Indeed, as mentioned earlier, the groundwater level data were
deliberately de-weighted to reduce the chance of the calibration process compensating for this structural deficiency
at the expense of the broader coherence of the model. Improving these fits would require the introduction of sub-
zone heterogeneity. One way to achieve this could be using the Iterative Ensemble Smoother (IES) method of White
(2018), which theoretically enables a very large number of parameters to be estimated (e.g. hydraulic conductivity
per element) with relatively few model runs. Additional fine-scale heterogeneity may not substantially affect
simulated catchment-scale dynamics, however.

At N3, groundwater levels are overestimated by approximately 3 m, which places the simulated level above the land
surface. However, N3 is extremely near the significant zone of exfiltration shown in Figure 5, so lack of small scale
topographic or subsurface feature representation could be responsible for the difference. The general overestimation
of the groundwater levels in this zone also explains why the zone of exfiltration occurs at a slightly higher elevation
in the model than in reality (Figure 5).

Whilst using extremely highly resolved (hourly) forcing data, which is rarely done with integrated models, brings
some benefits in terms of reproducing diurnal fluctuations and sharp streamflow peaks (Figures 6 and 7), the overall
performance metrics are slightly lower than in the daily forcing case. This is presumably because the model was
 calibrated at a highly contrasting frequency (monthly). Had the simplified Scenario A simulation not been
conducted, one could have hypothesized that the underestimation of sharp peaks by the hourly model could be due
either to intense localized convective rainfall events having been “missed” by the gauge network from which the
forcing datasets were generated, or the geometries of the many small torrents that are able to rapidly transmit rainfall
and snowmelt to the main channel not having been represented sufficiently in the mesh (cf. Ala-aho et al., 2017).
However, the fact that streamflow peak timing is reproduced even with only daily forcing under Scenario A (Figure
9) largely eliminates these possibilities; this is an example of the insights that employing complex and simplified
models in combination can yield. Instead, it would appear more likely that in the hourly reference model, surface
and near-surface permeabilities generally remain too high, and/or interception and evaporative losses are
overestimated (both leading to insufficient overland flow generation). Whatever the reason, Movie S1 indeed
suggests that small flowing torrents do not appear to form extensively enough in the model compared with field
experience, at least with daily forcing data. A clear limitation of the present study is that the monthly data used for
calibration did not contain information on these high-frequency dynamics, which prevented improved peak flow
matching. Resolving the topography of small torrents in even more detail could certainly have also helped, but
would have resulted in an even larger mesh and hence longer runtimes.

Finally, the relatively low observed and simulated water levels / discharges during baseflow periods at all sites (see
e.g. Figure 3 and Movie S2) suggest that even under present climatic conditions, the stream network is fairly close to
becoming (more) intermittent or ephemeral. Small shifts in climate and vegetation conditions could induce
threshold-like responses in terms of stream intermittency which would have important implications for ecosystems
and human societies (e.g. via reduced hydropower production) alike.

4.2. Insights from the simplified models

The simplifications in the final phase to assess output sensitivity pertain to both subsurface representation and
spatio-temporal forcing data resolution. Whilst commonly made, they have not previously been extensively tested.
Only by developing complex models as reference cases is it possible to assess the impacts of subsequent
simplifications via sensitivity analyses (see also Rapp et al., 2020; Schreiner-McGraw & Ajami, 2020). One
example along these lines was already mentioned in the previous section. Here, we further discuss each of the
simplified scenarios in turn.
In Scenario A (Impermeable subsurface, no ET; Figure 9), the temporal pattern under/overestimation with respect to the observations are as expected; with infiltration and subsurface storage and discharge precluded, the simulated spring and summer rainfall peaks are higher than their observed counterparts, whilst baseflows later in the year (which are of course sustained by groundwater discharge in reality) are underestimated. Indeed, these results unambiguously demonstrate that even ignoring any ET losses, streamflow would frequently become negligible in summers/autumns following snow-poor winters such as 2016/2017 were it not for the sustaining influence of groundwater discharge. As such, they confirm the importance of groundwater discharge to sustaining baseflows in this catchment (Figure 5).

Although incomplete observed time-series preclude temporally integrated volumetric comparisons, the general tendency for overestimation at S1 and S2 under Scenario A make sense as the fraction of incident precipitation that in reality is returned to the atmosphere via ET, and hence never becomes streamflow is neglected in this scenario. The most remarkable result, though, is the extreme overestimation of streamflow relative to observations at S3 when all water is forced to flow overland. This result clearly indicates that the runoff-ratio of the Vallon de La Vare is considerably lower than that of the Vallon de Nant. As the land cover in the two catchments is broadly comparable (Figure S3), the difference can be confidently attributed to the presence of more permeable bedrock types in the Vallon de La Vare (see also Thornton et al., 2018). In reality, subsurface flow paths (in the upper part especially) must be longer and deeper. Indeed, the early tracer test by Lugeon and Gagnebin (1928) mentioned earlier proved a hydrogeological connection between the topographically closed basin of La Varre and La Chambrette – a spring which joins the main channel below S3. This means that some water must actually bypass the station entirely, although the relative volumes remain unclear. In light of these results and evident complexity, the results of the reference model at S3 seem less disappointing. This further underscores the importance of considering the context, including climatic and geological conditions, catchment size, and model type, when evaluating statistical fit metrics of hydrological model (Seibert et al., 2018).

The shift in dynamics due to the imposition of a “no flow” boundary at 30 m depth (Scenario B; Limited vertical extent; Figures 10, 11, and S16) (enhanced runoff during snowmelt and intense rainfall, more pronounced recessions, etc.) can be explained by reduced maximum subsurface storage volumes. Although less so that in Scenario A, that streamflow is still grossly overestimated at S3 (Figure 10) indicates that under both Scenarios A and B, simulated streamflow dynamics are far too rapid and overestimate discharge considerably (and moreover almost certainly involve incorrect flowpaths). In contrast, in the reference case, the simulated dynamics were too suppressed; improved simulations must therefore lie somewhere in between. Whilst it is impossible to state definitively whether the full depth model structure in the Vallon de La Vare is preferable to that of Scenario B, our prior understanding of the region's geology, plus these results, suggest that it is likely the case. More generally, because it is common for vertical domain extents to be limited when applying computationally intensive integrated hydrological models to real mountainous catchments, the degree of sensitivity demonstrated represents an important finding. In some previous studies, manual calibration may have (fully or partially) compensated for this effect, but such action could compromise any subsequent predictions. The sensitivity of integrated model outputs to assumed vertical extent should therefore be assessed more routinely (see also Condon et al., 2020).

The noticeable differences between the respective simulations during spring periods in Figure 12 (Scenario C; Spatially-uniform forcing) suggest that it is necessary to employ spatially distributed forcing to reproduce annual flow peaks, especially at higher points along mountain stream networks. This makes sense because while the elevations and slope aspects at which snowmelt is generated naturally evolve over time, these spatial patterns are lost when catchment-averaged data are applied. In even larger catchments, these differences would be exacerbated. It should also be emphasized that the spatially uniform forcing dataset used here was generated by averaging the distributed outputs produced by Thornton et al. (2021) at each time-step. As such, the differences may have been larger if “truly uniform” forcing dataset had been applied.
Meanwhile, Scenario D (Geology from global maps) reveals that one cannot parameterize groundwater and integrated models based directly on global map products – as is currently done in many global-scale groundwater and integrated modelling studies – and obtain acceptable simulation results at local, management-relevant scales. The considerable challenge of how to define sufficiently good 3D subsurface structures and associated parameter values must therefore be addressed if the goal of developing practically useful global groundwater predictions is ever to be realized.

Finally, the results of Scenario E (No permafrost; not shown) suggest that, probably due to its limited extent in this region, permafrost thaw is not expected to have a major impact on streamflows. However, a full “thermally enabled” simulation that accounts for pore water freeze-thaw and thermally modified hydraulic conductivities, rather than the simple coupling length approach used here, would probably be necessary undertaken to verify this assertion.

4.3. Main novelties

The full complexity integrated model presented is associated with several novelties. Firstly, in incorporating an accurate, high-resolution 3D model of bedrock geology (Thornton et al., 2018) – supplemented by a dedicated analysis of unconsolidated sediment geometries and represented on a vertically-extensive and fairly finely resolved mesh – the model’s subsurface structure is more refined than that of previous integrated models of mountainous catchments. Yes given the extreme geological complexity of La Vare, further detail may still be required.

Secondly, the snowmelt component of the model’s forcing dataset – generated in a prior study using an energy balance-based snow model that additionally accounts for gravitational redistribution and was conditioned upon two complementary types of snow observations (Thornton, Brauchli, et al., 2021) – extends well beyond the approaches usually taken to develop forcing data for integrated surface-subsurface models. The highly spatially and temporally resolved nature of the forcing datasets more generally can be regarded as a further novelty. Besides enabling the pronounced spatio-temporal dynamics that characterize such environments to be represented more faithfully in the hourly version of the full model than is typically the case, it was also possible to quantify the impacts of downgrading the forcing data’s temporal frequency and spatial resolution.

Detailed HGS models of real (as opposed to synthetic) mountainous catchments have not previously been presented in the literature. This is important because in contrast to some other integrated codes, HGS permits the free evolution of surface water network. HGS also supports flexible tetrahedral meshes, which arguably enable the representation of complex topography more efficiently than the regular, structured meshed employed by other popular integrated codes (but see Maxwell, 2013). Equally importantly, this study represents the first known attempt to calibrate any integrated hydrological model of a mountainous catchment in an automated fashion.

Finally, in contrast to many related previous studies (e.g. Carroll et al., 2019; Engdahl & Maxwell, 2015; Markovich et al., 2016; Penn et al., 2016; Pribulick et al., 2016), explicit time-series comparisons between simulations and historical observations, and associated statistical metrics, are presented. This goes beyond the status quo in much integrated modelling whereby simulated historical hydrological baselines are only compared with projections made under modified conditions (rather than with historical observations as well). Whilst the physical basis of the models involved means that such an approach is not invalid, actually demonstrating that (with plausible parameter values) historical observations can be reproduced satisfactorily by carefully developed integrated models, as is done here, enhances confidence in the robustness and suitability of the approach. The spatio-temporal visualization of different aspects of the simulations was also helpful in this regard. Integrated model results should be presented using both techniques (i.e. time-series comparisons and full visualization) more routinely.
4.4. Fully-integrated hydrological models in complex mountainous settings: potential next steps

Based upon this work, numerous recommendations for future research, some of which have already been alluded to, can be made. Firstly, the interplay between initial conditions, parameter updates, and (minimum) re-initialization period length (i.e. the period that should be (re)simulated with every new set of parameters prior to the commencement of calibration) in the automated calibration of integrated hydrological models should be investigated more systematically. Secondly, when employing integrated model codes that support unstructured meshes in such topographically and geologically complex settings, there is likely scope to increase mesh efficiency. The mesh employed here – in which the same (surface constrained) layer was replicated vertically – was a limiting factor. Ideally, fully-unstructured meshes that are constrained / refined according to surface features (streams, topography, etc.) in the upper few meters only, but then transition to being exclusively concordant with geological formation interfaces beneath this, could be developed and applied. To ensure numerical stability, high quality element shapes would have to be maintained, however, which is unlikely to be trivial (depending on the degree of surface and subsurface complexity). If possible, the attendant runtime improvements could open many more possibilities for automatically calibrating such models, including over longer periods and using higher frequency forcing data.

Accurate, spatially continuous (3D) data pertaining to the subsurface remains severely lacking in both mountain regions and elsewhere. This is a major impediment to the more widespread uptake of integrated models involving detailed subsurface structures. Few catchment- or regional-scale 3D bedrock models with appropriate attributes for groundwater or integrated hydrological models currently exist in mountain regions, although they can now be developed (Thornton et al., 2018). Improved approaches to estimate the geometries and properties of numerous unconsolidated sedimentary features (i.e. across entire rugged, inaccessible headwaters) are also required (see Supplementary Text S1). With continued developments in satellite remote sensing, the already considerable disparity between the amount and quality of data available pertaining to the surface and that pertaining to the subsurface is widening. 3D (or even 2D) data on soil hydraulic properties are also scarce, even in relatively densely populated and developed mountain ranges such as the European Alps. As already noted, soils control water partitioning at the land surface, and so high-quality soil representations data are crucial for reliable simulations.

As we have hopefully helped to demonstrate, the extensive (2D-3D) visualization capabilities of integrated models enable users to evaluate the coherence of a given numerical representation to be assessed in a conceptual sense, for instance in relation to known theory and/or understanding of a given system developed in the first. This approach can enable users to identify where a given model may require or benefit from the introduction of additional data, the reappraisal of the conceptual model, or other improvements as part of an iterative development process. More formally, the considerable number of simulated variables that can be extracted at any point(s) in space and time from within the model domain provide enormous scope for a much wider variety of observational datasets, both in situ and remotely sensed, to be introduced in their calibration and evaluation (in a multi-objective fashion).

Such datasets could include remotely-sensed ET maps (e.g. Allen et al., 2007; Li et al., 2009) or gravimetric estimates of seasonal groundwater storage (e.g. Arnoux et al., 2020). The latter in particular would provide more spatially integrated, representative information than the piezometer measurements used here (see also Schilling, Cook et al., 2019). One could also constrain integrated models using snapshot maps of the evolving steam network extent (e.g. captured using drone photography) (see also Stoll & Weiler, 2010). Combining integrated models and many diverse datasets in this fashion should ultimately reduce the extent to which equifinality afflicts model predictions, and thus help to finally realize the vision of Grayson & Blöschl (2001). However, what constitutes an acceptable level of model-data fits for such models, given the characteristics of such terrain and in a metric-specific fashion, must be established by the community. As noted above, we recommend these evaluation activities include time-series comparisons where relevant.
5. Conclusions

We have presented a fully-integrated surface-subsurface hydrological model of a steep, snow-dominated mountainous catchment that incorporates a dedicated 3D model of bedrock geology and an energy balance-based representation of snow processes; two structural advancements over previous mountain integrated modelling efforts that, given the study area’s characteristics, were deemed important. Establishing and running such a model was found to be feasible, if challenging. In the first known attempt for an integrated model of a mountainous catchment, automated calibration was undertaken with respect to observed streamflows and groundwater levels.

Following calibration, the system’s hydrological dynamics could generally be satisfactorily replicated, suggesting that integrated models do indeed have utility in complex Alpine settings. When high-frequently (hourly) forcing data were applied, diurnal fluctuations in streamflows and groundwater levels could be reproduced, suggesting that such temporal resolution is necessary for certain applications. Visualizing the model’s forcings and simulated response variables in time and space, and the outcome of a “soft evaluation”, in which simulated patterns of surface-subsurface exchanges flux was compared with a flux pattern inferred from a thermal drone image, further reinforced our view of the model’s broad coherence and ability to capture observed surface-subsurface flow dynamics.

The model struggled to closely replicate observed streamflows at one location (S3). This can be attributed with reasonable confidence to fact that our model does not explicitly represent the discrete karstic features of the upstream sub-catchment, although unreliable streamflow observations could be a factor in the poor correspondence. Replicating the distinctive signals of groundwater levels that were observed nearby one another also proved elusive, likely due to unrepresented local scale heterogeneities in subsurface hydraulic properties. This suggests that in such settings, local-scale variability in shallow in situ groundwater level observations can adversely affect their utility in the catchment-scale groundwater and integrated model calibration. Even notwithstanding any such data issues or data-model scale mismatch, as with most calibration exercises, a risk of post-calibration non-uniqueness remains. This could not be addressed with the present scope, with the long model runtimes representing the main impediment.

Subsequently simplifying the full complexity reference model in a series of sensitivity tests revealed that:

- In this study area, without groundwater discharge, streamflow would frequently become negligible in summers following snow-poor winters;
- Limiting the model’s vertical extent significantly increased the “flashiness” of simulated streamflows and groundwater levels, indicating that care should be taken to ensure that simulation domains are sufficiently deep – especially in more permeable geological settings (otherwise, the risk of overestimating streamflow peaks could be considerable);
- Applying spatially uniform forcing data led to reduced simulated annual (snowmelt-related) streamflow peaks, most noticeably at higher elevation points along the stream network;
- Satisfactory simulations (with respect to observations) were not obtained when we substituted the model’s subsurface structure and parameterization with information derived from existing, global-scale maps, thereby demonstrating the importance of carefully defining locally meaningful subsurface structures and calibrating their associated parameters within physically plausible limits; as such, the suitability of global products for large-scale groundwater/integrated modelling efforts which nevertheless require locally meaningful predictions, especially without model calibration, requires further detailed assessment across many different settings; and,
- Complete permafrost thaw would be expected to have an almost indistinguishable impact on hydrological variables such as streamflows and groundwater levels, although the fairly simplistic way in which permafrost was represented in the reference model limits our confidence in this assertion somewhat.
Relative to the simpler alternatives tested, the value of our full complexity model lies not only in the generally improved fit metrics, but crucially in the fact that they were generated via a more plausible model structure. In addition, considering the relatively complex and more simplified approaches alongside one another yielded insights that could not have been obtained using either approach independently. We therefore conclude that physically-based integrated flow models provide a strong basis for exploring the impacts of different simplifications, assumption, and other approaches that are used across the full spectrum of hydrological model, including those implemented in more widely used tools.

Several recommendations for future integrated modelling research in climatologically, topographically, and geologically complex mountainous settings have emerged, including the needs to develop dedicated methods to generate more efficient, fully-unstructured meshes; develop and apply improved methods describe the 3D geometries and hydraulic properties of unconsolidated subsurface formations; routinely test the sensitivity of model predictions to assumed watershed base depth or thickness; investigate the interplay between initial conditions and re-initialization simulation times in automated calibration; better exploit the possibilities to introduce a range of complementary variables (in situ and remotely sensed, spatially distributed and spatially integrated, fully quantitative and “softer” data, etc.) into multi-objective calibration and evaluation; and establish more refined model performance criteria, for several variables and associated metrics, that account for factors such as catchment type, catchment area, model type, plausibility of simulated spatial patterns, and credibility of subsurface structure for use in model evaluation and intercomparison exercises.

In summary, our contribution both attests to the considerable potential of fully-integrated models in complex mountain settings and elucidates several outstanding challenges (especially those concerning data requirements and calibration). Even despite these challenges, the strong physical basis of integrated models should already facilitate hydrological climate change impact assessments across the European Alps and other rapidly changing mountain regions that are more reliable and holistic (e.g. include both plausible future climate and vegetation scenarios) than those hitherto possible. For practical reasons, initial applications could focus on exceptionally important or ecologically sensitive catchments, or else catchments for which much of the requisite data already exists.

Acknowledgments, Samples, and Data

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Author contributions

J.M.T. conducted the majority of the work, including making the groundwater measurements, sourcing the inputs datasets, setting up and calibrating the model, planning and executing the subsequent simulations, preparing the figures (except Figure S12), and writing the manuscript. R.T. provided advice and technical contributions regarding HydroGeoSphere. N.L. enabled the geophysics fieldwork and conducted the geophysical inversion. P.B. and G.M.
were responsible for funding acquisition and provided support and advice at all stages. All authors contributed to the finalization of the manuscript.

References


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**Supporting References**


Supporting Information for

Simulating fully-integrated hydrological dynamics in complex Alpine headwaters

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Contents of this file

Figures S1 to S16
Text S1

Additional Supporting Information (Files uploaded separately)

Captions for Tables S1 to S3
Captions for Movies S1 to S3

Introduction

This file contains supplementary figures, describes the methods taken to estimate unconsolidated sedimentary formation geometries, and provides captions for supplementary tables and animations.
Figure S1. Photographs showing a) the concrete weir gauging station S2, and b) the installation of piezometer N4.
Figure S2. The 2D surface triangular mesh, underlain by a high-resolution aerial photograph (Source: ©swisstopo). Refinement is highest in the riparian zone and in steep areas. Care was also taken to ensure that nodes were placed at the precise coordinates of the observation points (piezometers, denoted by N, and streamflow gauging stations, denoted by S).
Figure S3. Land cover map of the study area, including estimated (present) permafrost distribution, that was used to define surface and evapotranspiration zones in the integrated model.
Figure S4. Illustration of the 3D bedrock geological model that contributed to the definition of subsurface zones in the integrated flow model. Source: Thornton et al. (2018).
Figure S5. The spatial distribution of soil depth that was assumed in the integrated model in the absence of any detailed, high-resolution spatial information on soil depths and properties. Where the underlying aerial imagery is visible, no soil layer is represented.
Figure S6. Cross-section through the 3D bedrock geological model showing the possibility for groundwater exportation across the topographic divide on the eastern flank of the Vallon de Nant, which is illustrated using the dashed white line (i.e. across the no-flow boundary in the model).
Figure S7. Pairwise plot of observed and simulated groundwater levels. The simulated levels were generated using the version of the model forced by daily frequency data. Model outputs were interpolated in time onto the half-hourly observation time-step to facilitate the plot.
Figure S8. The impact of moving from monthly to daily frequency forcing on streamflow predictions generated by the fully-integrated model.
Figure S9. The impact of moving from monthly to daily frequency forcing on groundwater level predictions generated by the fully-integrated model.
Figure S10. The major unconsolidated sedimentary feature extents considered in this study. The locations of electrodes that were placed during the geophysics campaign and the topographical cross-sections that were established as a basis for interpolating the bedrock interfaces are also shown. N denotes Nant, M Martinets, C La Chaux, and VU Vare Upper, and VL Vare Lower. The underlying hillshade map was generated from the swissALTI3D digital terrain model © swisstopo).
Figure S11. The arrangement of electrodes along the three transects in the Nant alluvial fan that were surveyed using electrical resistivity tomography (ERT). The profiles were named N1, N2, and N3, and the electrodes were numbered sequentially along each profile.
**Figure S12.** Inverted electrical resistivity fields for each of the three surveyed profiles in the Nant alluvial fan. A common resistivity scale is used. Annotations indicate the inferred bedrock interface and other interpretations, which in some cases are only tentative.
Figure S13. Interpolated 2D cross-sections for each of the 13 topographical transects. For the three profiles pertaining to Nant, interfaces derived from the geophysical surveys were included in addition to the topographic points immediately outside the sedimentary features in order to constrain the estimated 2D bedrock interface. Elsewhere, the 2D interpolations were informed solely by the bedrock gradients immediately beyond the sedimentary feature in question.
Figure S14. 3D points forming the input to the Thin Plate Spline (TPS) interpolation of the bedrock interface beneath the moraines of Les Martinets, looking due south.
Figure S15. Estimated depth to bedrock within unconsolidated sedimentary features that were identified as potentially to host important aquifers. In the case of Nant, the result was generated by combining bedrock interfaces inferred from electrical resistivity images along the three profiles and the results from the geomorphometric method. The remaining features could not be practically surveyed with geophysics, and so the purely desk-based geomorphometric method was used here.
Figure S16. Comparison of the catchment water balance simulated under the fully-complexity integrated model with daily data, and the model whose vertical extent was limited to 30 m (Scenario B).
Text S1. Estimating geometries of potential unconsolidated Quaternary aquifers

Recent dedicated field campaigns have elucidated the hydrological importance – in the sense of having the capacity to store and then subsequently release substantial quantities of groundwater – of various individual unconsolidated Quaternary sedimentary features, such as talus slopes, moraines, alluvial fans, and rock glaciers, that are commonly encountered in alpine settings (Hayashi, 2019; Somers & McKenzie, 2020). However, researchers have few practical, cost-effective methods at their disposal to accurately estimate the 3D geometries of several such features across entire rugged, largely inaccessible mountainous headwater catchments. This is problematic because model structures should ideally be constrained as tightly as possible initially in order to limit the potential for parameter values to take on values that compensate for poor structures to reproduce the “right answers”, but for the “wrong reasons” (which could have severe implications for subsequent predictions).

In absence of borehole information, geophysical methods (e.g. Sass, 2006; McClymont et al., 2011, 2012) generally yield the strongest geometrical constraints. Whilst therefore recommendable in principle, they are also very labour intensive. Given this and the fact that the routinely generated resultant data 2D, it is generally not possible to survey more than perhaps one or two such features with sufficient density to provide meaningful 3D insights. In addition, environmental protection measures in sensitive mountain regions may preclude the use of certain geophysical techniques (e.g. seismic methods).

Traditional desk-based geomorphometrical methods, meanwhile, are certainly more efficient across larger areas, but the accuracy of the resultant estimate may be compromised, especially in light of the distinctive characteristics of alpine terrain. Several geomorphometrical approaches to estimating the sediment/bedrock interface along 2D cross-sections perpendicular to the main valley axis have been considered. Perhaps the most straightforward approach involves simply projecting hillslope gradients into the subsurface (Hinderer, 2001). The fitting of power laws (Svensson, 1959) and quadratic functions (Wheeler, 1984) to empirical cross-section data have also proved rather popular (James, 1996; Li et al., 2001), even if much of this work was undertaken in attempts to try to better understand valley formation processes, whereby the fitted parameter values are interpreted (e.g. a power law exponent, \( b \), approaching two is taken to be indicative of parabolic “U-shaped” glacial valleys, whilst values closer to one are considered to signify fluvially-incised “V-shaped” valleys), rather than current geometries.

Nevertheless, if elevation points along the profiles corresponding to the sedimentary fill are removed prior to curve fitting, erosional upper bedrock surfaces can be reconstructed (Harbor & Wheeler, 1992). A fairly dense array of cross-sections must usually be considered to capture any longitudinal variability in the 2D profiles, and a final interpolation undertaken to produce a 3D result. Schrott et al. (2003), for instance, took such an approach in a small catchment in the Bavarian Alps, Germany, but found that the surfaces produced by polynomial fitting overestimated sediment thicknesses compared to coincident seismic refraction surveys. Not dissimilarly, Rogger et al. (2017) used a geomorphometrical approach to augment geophysical insights; sediment thicknesses were estimated at many different cross-sections by “extending the bare rock surface below the sediment deposit through a parabola fitted to the bedrock slopes at the outcrop boundaries”.

Major drawbacks have been identified with both the power law and quadratic methods, however (Harbor & Wheeler, 1992; Pattyn & Van Huele, 1998). Specifically, power law functions must be fitted to both sides of a given valley cross-section independently, since the variable representing horizontal distance cannot
take negative values. Additionally, power law functions must pass through the origin of the coordinate system used, yet where this location should be is generally unknown at the outset—above all when the very aim is to interpolate the bedrock surface beneath sedimentary fill deposits. This issue renders the results sensitive to the choice of origin. The logarithmic transformation that is typically applied to solve for the constants of power law equations compounds the problem, since it causes more weight to be placed upon those points located near the origin than those towards the profile’s extremities. Quadratic functions, meanwhile, assume that the cross-sectional form is parabolic and symmetrical, and are hence poorly suited to representing any form of asymmetry in such profiles.

A more modern but related approach to the estimation of glacial valley bedrock forms is the Sloping Local Base Level (LSBL) method (Jaboyedoff & Derron, 2005). This technique requires a digital terrain model (DTM) as input. Via the iterative calculation of quadratic parabolas, the topographic surface within the region of sedimentary fill is then progressively “excavated”, leaving a curved 3D bedrock surface. A crucial impediment to the wider implementation of this technique is that the maximum expected depth to bedrock, must be specified a priori (Otto et al., 2009), yet this is typically a key unknown to be determined. More recently, Mey et al. (2015) presented an approach to the estimation of valley fill thickness/bedrock surface topography that revolves around training a machine learning algorithm using geometrical landscape data—specifically, the sectoral distance to the nearest bedrock hillslope, with the training data being generated by artificially filling DTMs. The approach hinges on the morphological similarity of the hillslope above the valley fill and the bedrock interface beneath it. Whilst results were promising with respect to estimating the thicknesses of sediments stored in the floor of large, almost horizontal intermontane valleys, the method would appear to be less immediately applicable to smaller alpine headwater catchments with their steeper sloping deposits.

As this last point alludes to, a further limitation of all the aforementioned geomorphometrical methods—and one which is particularly important given the complex nature of the bedrock geology at the present study site—is that geometric similarity above and below the fill level is assumed. In other words, no account is taken of lithological contrasts which, where present, bring about discontinuities in the cross-sectional profiles and terrain morphology more generally. The geostatistical approach developed by Castilla-Rho et al. (2014) used splines—a geomorphometrical technique that is better able to account for cross-sectional variability—in conjunction with various other datasets to estimate the bedrock interfaces of fluvial valleys.

As a consequence of these issues, it remains challenging to establish the extent to which the combination of these unconsolidated features contributes to the hydrological functioning of the broader catchment systems within which they are embedded, including their contributions to streamflow. Indeed, in integrated and other similar numerical model applications in mountainous areas, it remains common to rely on extremely simplified representations of potential unconsolidated aquifers (e.g. spatially uniform thicknesses) to be applied (Floriancic et al., 2018; Smoorenburg, 2015).

From this brief review, it seems unlikely that any ideal solution to this challenge presently exists, and that a combination of a geomorphological approach with constraints from geophysics might therefore represent a pragmatic compromise. As such, with a view to informing development of the integrated model described in the main paper, a simple 2D and 3D spline-based geomorphometrical approach involving the targeted extraction of digital terrain and geological map data is presented. This is fairly similar to the approach of Castilla-Rho et al. (2014), but without stochastic quantification of uncertainty (which fell beyond our scope). It is shown that, where available, bedrock interface constraints inferred from
geophysics – in the case of an electrical resistivity tomography (ERT) survey – can easily be incorporated. Ultimately, it is hoped that the approach provides a means by which catchment-scale groundwater and integrated surface-subsurface model structures can be refined compared to present practices.

The first step of the methodology involved identifying any major sedimentary features with the potential to act as aquifers (i.e. can store and subsequently release meaningful quantities of water) and establishing their surficial extents. This step required some general understanding of the hydrogeological system – especially qualitative knowledge of where the major aquifers are located. This understanding was developed by basic field measurements and reviewing various existing datasets.

More specifically, feature identification placed reliance on existing detailed (pre-digitised) surface geological maps (the swisstopo GeoCover25 dataset; https://shop.swisstopo.admin.ch/en/products/maps/geology/GC_VECTOR) and a high (2 m) resolution terrain “hillshade” map which was developed from the swissALTI3D dataset (https://shop.swisstopo.admin.ch/en/products/height_models/alti3D). Unconsolidated sedimentary deposits were marked on the geological maps, and are furthermore clearly discernible in the “hillshade” map. Previous studies pertaining to the hydrogeological function of certain types of features (e.g. proglacial moraines) were also consulted as necessary. In this way, the following five principal features were identified:

- A large alluvial fan system, referred to henceforth as Nant;
- High proglacial moraine sediments of the Glacier des Martinets – Les Martinets;
- Glacial drift sediments – La Chaux;
- Generic unconsolidated fill sediments in a karstic, topographically closed depression (i.e. a doline) – Vare Upper, and;
- Generic unconsolidated fill sediments – Vare Lower.

These five features were treated as distinct zones so that in the subsequent integrated model, different hydraulic properties reflecting their specific histories and constituent materials could be assigned to each in the integrated flow model. The spatial extents of these features were extracted as shapefiles from the GeoCover25 maps and verified with reference to the hillshade map. The resultant areas are presented in Figure S10. In a final preliminary step, the \(x, y\), and surface elevation, \(z\), attributes of points spaced at 5 m intervals along the feature boundaries (i.e. where sediment thickness = 0) were extracted from the DTM, and the resultant coordinate triplets recorded along with an identifier of the feature to which they correspond.

As previously discussed, in seeking to estimate Quaternary aquifer geometries, as much geophysics as possible should ideally be conducted. That said, the practical and monetary constraints to such approaches are elevated in rugged alpine terrain. With such considerations in mind, and within the very broad scope of this study, only one geophysical technique could be deployed here, and only a single unconsolidated formation surveyed. Since the main alluvial fan in the central part of the Vallon de Nant (i.e. Nant) was believed to constitute the most important unconsolidated formation in hydrological terms, attention was focussed here. This feature also happened to be comparatively accessible; having obtained the necessary special permissions, off-road vehicular access was possible as far as Chalet Nant – a now uninhabited farm building in the alpine pasture.
The survey’s primary objective was to determine the spatial distribution of depth to bedrock; any potential insights that could be gleaned with regards to internal structure would be considered a bonus. Seismic methods (used by Schrott et al., 2003, amongst many others) were discounted due to the Natural Reserve’s regulations, whilst the depth of information provided by ground-penetrating radar is too limited. Finally, we decided to rely on ERT, which we expected could provide information about the lithological structure down to depths ~100-200 m. A four-day long field campaign was conducted in favourable meteorological (dry and sunny conditions) in September 2018 – the first attempt to image the subsurface of this pristine Alpine valley.

With the objectives in mind, the intended profile layouts and electrode spacings were planned in advance. Three separate profiles were identified; one long one of 1,780 m running approximately parallel to the main valley axis (N1), and two shorter perpendicular profiles of 700 m each (N2 and N3) (Figure S11). The former sought to capture any longitudinal variability in the bedrock interface (i.e. along the valley axis), for instance due to glacial over-deepening, which is common in such settings. The two intersecting transverse profiles sought to provide some 3D constraints on the morphology of the upper bedrock surface (and hence the unconsolidated sediment thickness); the ultimate goal being to develop a 3D flow model after all. In order to image comparatively deep, a 20-m electrode spacing was chosen.

Once in the field, where conditions allowed, the stainless-steel electrodes were hammered in to a depth of 10-20 cm. The length of N1 necessitated a “roll-along” technique. At locations without soil cover (see e.g. Figure 4.8b), electrodes were positioned firmly in the silty sediments between larger boulders and pebbles, and sponges dampened with salt water were applied to decrease the contact resistance. Typically, contact resistances between electrodes of less than 5 kOhm were achieved. The electrode positions were measured accurately using a Leica Differential GPS device; these are plotted in Figure S11. Relatively straight profiles could be maintained, and so any corresponding 3D distortive effects in the results should be minimal.

The apparent resistivity measurements were acquired in both dipole-dipole and Wenner-Schlumberger configurations using an IRIS Syscal Pro instrument. The current injection cycles (500 ms) were repeated four times and the measurements were stacked in order to improve the signal-to-noise ratios. Prior to inversion, the data from the Wenner-Schlumberger and dipole-dipole surveys were combined, giving a total of 3,353 measurements for N1, and 793 measurements for N2 and N3, before any measurements whose standard deviation exceed 3% were removed. The inversions were performed in a fairly standard fashion using the code BERT (Günther, Rücker and Spitzer, 2006). Robust data reweighting and compact inversion using iteratively-reweighted least-squares were employed to reduce the influence of outliers and to image sharper interfaces, respectively. The inversion process converged in 10 iterations, with a final relative root-mean square error of <5%.

The three resultant resistivity images (Figure S12) were interpreted both independently and in combination. To facilitate the latter, they were georeferenced and visualised in conjunction with the surface topography within a virtual environment (Movie 3). This step also enabled the coherence of the inversion results near the profiles’ intersection points to be verified. Next, a plausible bedrock interface was tentatively identified and annotated on the images (along with other possible interpretations). Finally, the spatial coordinates \((x,y,z)\) of points placed at regular intervals along the identified subsurface interface were extracted.
The next phase of the methodology was to make a series of 2D interpolations at the various cross-sections. To achieve this, the geophysical transects and other topographical profiles were first extended, points were generated at 5 m intervals along the full profiles, the surface elevation ($z$) extracted from the DTM, and the horizontal distance from the respective profile start points calculated. Then, for each feature independently, the surface elevation points were plotted against the horizontal distances, and any points falling within the unconsolidated sediment extents (identified via spatial intersection with the feature shapefiles) were removed. These points are represented in red in Figure S13.

Following that, cubic splines were fitted to interpolate between the remaining points. As a class of functions, splines are local interpolators which seek to fit the empirical data points exactly (or extremely closely, by minimising the sum of the squared residuals) whilst simultaneously maximising smoothness, by penalising roughness (Mitas and Mitasova, 1999). They are generally favoured over high-order polynomials because the latter can result in strong oscillations. The specific technique of cubic spline fitting involves establishing piecewise third-order polynomials that pass through all of the control points. In this way, the upper bedrock surfaces along each transect were estimated. For the three profiles in the Nant feature, the additional subsurface interface derived from the geophysics results were included in the 2D interpolations in the same fashion as the topographic points beyond feature extents.

The smoothness of the resultant interpolations makes splines well-suited to the task of reconstructing "U-shaped" glacial valleys; the smooth interfaces they propose beneath the sediment-obscured regions correspond to the simplest possible models. Simultaneously, in being able to follow sharp elevation discontinuities in the bedrock outcrops, which arise here due to lithological contrasts, these points do not influence the reconstructed interfaces. In other words, the upper bedrock surface estimates along each transect were consistent with the bedrock gradients immediately beyond the feature extents. It follows that should any lithological "steps" occur beneath the zones of sediment fill, these would not be captured. Such "steps" are generally not too problematic in this case, however.

In certain instances, the interpolated interfaces did demonstrate a fairly high degree of sensitivity to the elevation gradients immediately beyond the sedimentary feature extents, and hence to the inclusion/exclusion of sampled points near the sediment/bedrock interfaces. This is similar to the finding of Mey et al. (2015), who also noted a certain sensitivity to the accuracy of the mapped feature “mask”. In fact, here, there was no hard condition to stipulate that the resultant interpolated surface should remain beneath the topographic surface. That said, the original surficial extent mapping (and hence the distinction between which points lay within the unconsolidated region and which lay beyond it) was certainly not perfect. This observation justified the manual additional removal of a few points in certain cases in these boundary regions, leading to interface profiles that were i) more consistent with prior expectations, and ii) were sufficiently coherent with others in the same feature. The final resultant splines are shown as the light blue lines in Figure S13.

The surface coordinates (i.e. $x, y$) of regular points along the interpolated spline function beneath the sedimentary fill were calculated using trigonometry and recorded along with the elevation estimates ($z$). Finally, the triplets $(x, y, z)$ were grouped by feature, and pooled with the corresponding surficial extent triplets (i.e. where thickness = 0) that had been generated already. For illustration, Figure S11 shows all points prior to 3D interpolation for the Les Martinets feature.
Finally, the 3D interpolations could be undertaken. For each feature independently, all 3D (i.e. $x, y, z$) points which corresponded to an observed or estimated sediment thickness of zero (i.e. the bedrock interface) were interpolated using Thin Plate Spline (TPS) functions – which imitate thin steel sheets forced to pass through the points – to give a spatially continuous 3D surface (with 10 m horizontal resolution). The smoothing parameter was identified automatically by generalised cross-validation. Where necessary, the resultant raster dataset was clipped to the feature boundaries. The final estimated unconsolidated sediment thickness distribution is shown in Figure S12.

Given the relative ambiguity of the bedrock interface from the geophysical results (essentially due to their being no strong contrasts in resistivity – the clay rich Flysch bedrock apparently having fairly similar properties to the unconsolidated materials), as well as the potential for the internal structure, which could not be determined using the large electrode-spacing used here, having potentially high hydrological importance (for instance, a very shallow clay layer could be observed in the field in regions of the main alluvial fan aquifer at Nant after an erosive flow event), the entire depth to bedrock beneath the alluvial fan was not defined as being eminently permeable for the purposes of the subsequent numerical modelling. Instead, only the upper third of the total thickness was considered as such, with the lower permeability till/clay assumed to comprise the remaining volume. This is essentially akin to defining the alluvial fan base according to a lower resistivity isosurface than the bedrock interface in S12; somewhere in the light blue region. Such an approach is justified by the fact the ERT appears to be mapping the fan and the till as a common low-resistivity feature above the bedrock interface. The technique is also known to have a tendency to somewhat overestimate the size of conductive anomalies – in this case the coarse gravel region of the fan. Since the geomorphometrical method provided no insight whatsoever in the other formations, they were assumed “hydrologically active” to their full depth.

For an extended description of the method and results, readers are directed to Chapter 4 of Thornton (2020). This doctoral thesis is currently under embargo but can be provided confidentially by the corresponding author upon request.

References


**Table S1.** Evapotranspiration parameter values in the integrated model, rounded to two significant figures. $d_e$ is evaporation depth, $d_r$ root depth, LIA range gives the annual minimum and maximum Leaf Area Index (with monthly variability between these values), $C_1$, $C_2$, and $C_3$ are transpiration fitting parameters, and $H_{wp}$, $H_{fc}$, $H_{ol}$, and $H_{al}$ are the pressure heads at the wilting point, field capacity, oxic limit, and anoxic limits, respectively. $H_{ets}$ is the pressure head below which evaporation is zero, and $H_{ets}$ the pressure head above which full evaporation can occur. $C_{int}$ is the canopy storage parameter. For parameters that were subjected to calibration, the initial values, lower and upper bounds permitted, and the final value obtained are specified. Evaporation from the bedrock, glaciers, unconsolidated rock, and streambed zones was deactivated in the model. All free parameters were log-transformed to improve the numerical robustness of the process.

**Table S2.** Surface parameter values in the integrated model, rounded to two significant figures. $n_{xy}$ is the Manning's roughness coefficient, $h_{d}$ is the depression (or rill) storage height, $h_o$ is the obstruction storage height, $l_{exch}$ is the surface-subsurface coupling length. For parameters that were subjected to calibration, the initial values, lower and upper bounds permitted, and the final value obtained are specified. *Except where permafrost, in which case $l_{exch}$ was assigned a value of 50 m. All free parameters were log-transformed to improve the numerical robustness of the process.

**Table S3.** Subsurface parameter values in the hydrological model, rounded to an appropriate degree of precision. $k_{xy}$ is horizontal saturated hydraulic conductivity, $k_z$ is vertical saturated hydraulic conductivity, $\theta$ is effective porosity, $S_s$ is specific storage, and $\alpha$ and $\beta$ are parameters of the Van Genuchten unsaturated retention functions. These functions were simplified for all subsurface formations except soils. For parameters that were subjected to calibration, the initial values, lower and upper bounds permitted, and the final value obtained are specified. The “subsurface.mprops” file in the Supplementary Materials details the simplified unsaturated parameterization applied in non-soil zones. $k_z = k_{xy}$, except where indicated. All free parameters were log-transformed to improve the numerical robustness of the process.

**Movie S1.** Upper: The evolution the daily frequency forcing data prescribed to the fully-integrated model (left: all liquid water inputs, i.e. rain + snowmelt + icemelt, and right: potential evapotranspiration). Lower: actual evapotranspiration (right) and surface water depth (left) simulated using the fully integrated model with daily frequency forcing data. The period shown is the 2017/2018 hydrological year, and the time-step of the animation is half-daily. The “days” are days from 1 October 2014. Note that the $ET_p$ and $ETa$ scales are inverted because HGS writes the latter as a negative flux by default.
**Movie S2.** The evolution of catchment (surface) saturation (left) and the response of water level at gauging station S2 (right) over the course of the 2017/2018 hydrological year simulated using the fully-integrated model with daily frequency forcing. The time-step of the animation is half-daily (the “days” are days from 1 October 2014).

**Movie S3.** Animation illustrating the three electrical resistivity profiles that were obtained for the Nant feature. To provide additional context to the georeferenced profiles, the surface topography according to the Alti3D digital terrain model is also represented. The bedrock interface was interpreted to be located around the transition from an upper region of lower resistivity to a lower region of higher resistivity (see the annotations on the profiles). This interface, which appears to be consistent between the profiles, was digitized (pink dots).