Orbital, the Box – an Interactive Educational Tool for In-depth Understanding of Astronomical Climate Forcing

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ABSTRACT

"Orbital, the Box" provides an interactive tool with graphical user interface (GUI) for stimulating active, visual learning for understanding of astronomical climate forcing. This cross-platform tool can be run locally on a personal computer using a standard web browser environment with no need for plugins, thus maximising accessibility for students and teachers alike. The tool facilitates in the development of a holistic and quantitative understanding of astronomical climate forcing by allowing students to independently vary orbital parameters, after which they can instantaneously see the resulting effect upon the seasonal and latitudinal distribution of solar irradiance arriving at the top of the Earth's atmosphere. Such an approach follows a classic controlled experimental design whereby one parameter can be changed while all others are kept constant. This experimental tool can be deployed as a virtual laboratory, including within a flipped classroom setting, to promote active learning of traditionally challenging concepts such as the roles of eccentricity and precession in astronomical climate forcing, and in particular their interaction with Kepler's second law and the subsequent consequences for season length.

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when implemented within, e.g. a "flipped classroom" (Bykerk-Kauffman, 1995; Huguet et al., 2020). In the case of astronomical climate forcing, it is obviously not possible to apply the traditional interactive methods used within geosciences, e.g. a fieldwork or laboratory element. However, an interactive tool with graphical user interface (GUI) can be developed to offer a virtual laboratory element (Kostadinov and Gilb, 2014). Here, *Orbital, the Box* is presented, which can be used to help impart an understanding of orbital parameters upon the distribution of irradiance across latitudes and seasons, with the aim of developing both a conceptual (specifically, a sense of the physical mechanism) and quantitative understanding of processes. Quantitative understanding is particularly important and is often overlooked within the geosciences (Manduca et al., 2008). Such a holistic and quantitative understanding of the effect of orbital parameters upon the Earth's irradiance profile is vital before the student can proceed on to other related subjects, such as learning about the millennial-scale time frequencies of past changes in eccentricity, obliquity and precession, and how they may or may not be present in the palaeoclimate record across vast timescales.

2 METHOD
2.1 GUI INTERFACE
The user is presented with a control panel in the form of three slider controls: (1) eccentricity, (2) obliquity and (3) ω, the geocentric solar longitude (λ) at which perihelion occurs, changes of which are caused by precessional processes. The user can set 15 unique values for eccentricity (covering a range of typical Earth values from 0.001 to 0.058), 15 unique values for obliquity (covering a range of typical Earth values between 21.8° and 24.5°) and 13 unique values for ω (from 0° to 360°). Each time a slider is adjusted, the image to the right displaying the irradiance distribution and orbital information (distance from sun, orbital speed) is updated instantaneously, helping to facilitate rapid active learning. Each of the three controls can be set independently, meaning that there are a total of $15 \times 15 \times 13 = 2925$ possible unique combinations to be explored. The reason the results can be loaded instantaneously on a standard personal computer is because the images containing the irradiance distributions are not computed live, instead, the respective images for all 2925 unique combinations have been pre-computed and can thus be instantly called upon when required. The control panel system used to call the images is written in HTML, CSS and Javascript, all of which are included with the major web browsers on all major computing platforms. As such, the tool can be run on desktop computers, laptops or tablets. Publicly available tutorials were used to design the CSS and Javascript elements (w3schools.com, 2020).

2.2 COMPUTATION OF SOLAR IRRADIANCE
The 2925 unique irradiance scenarios were computed in Matlab 2019a using scripts based on established methodologies. These scripts were specifically written for the development of this educational tool, but could be used in other settings (e.g. research), and have therefore been made publicly available on Github (http://www.github.com/bryanlougheed/orbital_the_box/).

Each image of annual irradiance distribution is calculated as follows, using the orbital parameters of Laskar et al. (2004) as input. For each unique combination of eccentricity, obliquity and ω, a 180° latitude by 365.2 day grid of irradiance is produced, using a respective resolution of 0.5° and 0.2 days. For the centre of each grid cell, 24 hr mean irradiance (daily Q_{mean}) is calculated in Wm^{-2} following Berger (1978), using a solar constant of 1361 Wm^{-2}. The aforementioned procedure requires λ as input, and I have calculated the λ associated with each 0.2 day increment following the standard Keplerian methods outlined by Meeus (1998) involving a binary search solution for the Kepler equation developed by Sinnott (1985). To the best of my knowledge, this computational procedure for the Kepler equation was first highlighted within the geosciences by Kostadinov and Gilb (2014). The Berger (1978) irradiance procedure furthermore calls for geocentric latitude as input, but I have substituted it here by geographic latitude to account for the ellipsoidal shape of the Earth (using the WGS84 reference ellipsoid). I validated this substitution approach against the incoming irradiance angle correction approach of Van Hemelrijck (1983). In order to better facilitate visual interpretation of the irradiance grid showing daily Q_{mean}, it is contoured at 25 Wm^{-2} intervals from 0 to 650 Wm^{-2}. The annual Q_{mean} for each latitude is calculated by taking the mean of all 24 hr Q_{mean} values calculated for each 0.2 day increment. Earth's distance from the Sun for each λ increment is calculated following the standard Keplerian methods outlined in Meeus (1998), assuming a semi-major axis of 1 AU. The corresponding orbital speed is calculated following the law of orbital energy invariance.

3 OVERVIEW OF THE GUI TOOL
3.1 GRAPHICAL REPRESENTATION
Within palaeoclimate teaching, current representations of the effect of orbital parameters upon the distribution of irradiance are sometimes not described correctly (Wampler, 2000a, b), possibly due to the limitations of the text format. Here, I have created a graphical representation that captures many complex concepts in one glance, shown in Figure 1 for the orbital configuration of the 21st century (eccentricity: 0.0167, obliquity: 23.4°, geocentric longitude of perihelion: 283°). This static graphical representation already allows a student to develop an understanding of the effects of eccentricity
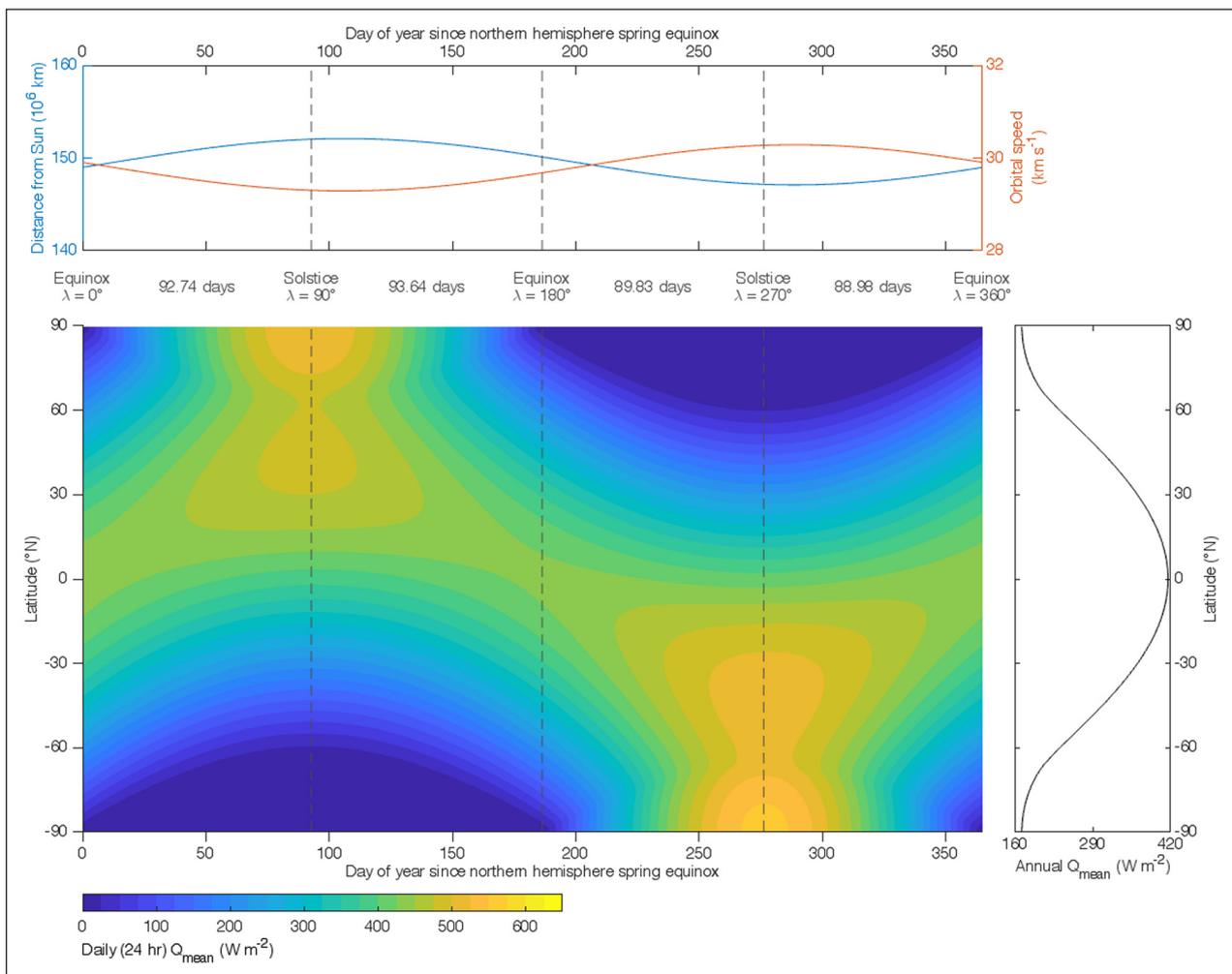
Figure 1 Graphical representation of the Earth's irradiance profile in the early 21st century (eccentricity: 0.0167, obliquity: 23.4°, geocentric longitude of perihelion: 283°). **Top panel**: The Earth's distance from the sun and the speed of its orbit throughout the tropical year, starting on the day of the spring equinox. Equinox and solstice days are indicated by dashed lines. **Bottom-left panel**: Distribution of irradiance (24-hour mean irradiance in Wm^{-2}) for the latitudes of Earth throughout the tropical year, also starting on the day of the spring equinox. Equinox and solstice days are indicated by dashed lines. **Bottom-right panel**: The mean irradiance received at each latitude throughout the course of the entire tropical year.

and precession upon the Earth's irradiance profile. For example, one sees that nowadays the Earth is closest to the Sun (i.e. at perihelion) approximately near the 280th day of the tropical year, approximately coinciding with southern hemisphere summer. This means that southern hemisphere summer receives slightly higher peak irradiance than the northern hemisphere summer does, as is visualised in the figure. However, one can also see how the Earth's orbital speed is slightly faster during southern hemisphere summer, which translates to southern hemisphere summer being slightly shorter than northern hemisphere summer (as indicated by the day durations indicated in the figure). The season length compensates for the difference in irradiance received, meaning that any latitude will receive the same mean irradiance throughout the course of the entire tropical year as its corresponding latitude in the opposite hemisphere (as can be seen in the right panel).

In addition to the graphical representation of the irradiance distribution reaching the Earth, a scale drawing

of the elliptical orbit of the Earth, with the Sun at the focal point, is also provided (Figure 2). This figure allows the student to visually analyse the aphelion and perihelion distances, and how the tropical year is oriented with regards to the orbit due to general precession.

3.2 INTERACTIVE REPRESENTATION

The graphical representations shown in Figure 1 and Figure 2 are a static representation of a single orbital configuration corresponding to the orbital parameters of the early 21st century. Here, this graphical representation is used to form the basis of the interactive tool. It has previously been demonstrated that such interactive tools with real-time updated results help students to more thoroughly build a conceptual understanding of a complex process, especially when the student is allowed to independently explore the possibilities provided by the tool (National Research Council, 2015; Wieman et al., 2008). In the case of *"Orbital, the Box"*, the student can experiment by using a control panel (Figure 3) to
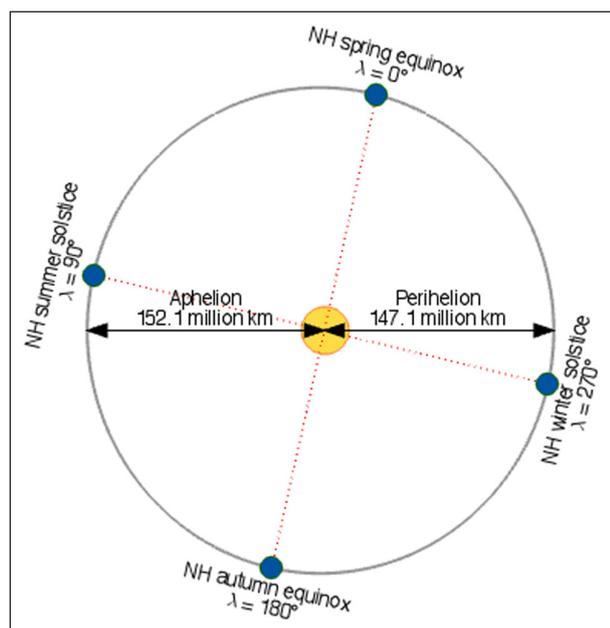
Figure 2 Graphical representation of the Earth's orbital configuration in the early 21st century (eccentricity: 0.0167, geocentric longitude of perihelion: 283°). The orbital shape has been drawn to scale. The size of the Earth and Sun have been increased for visual clarity.
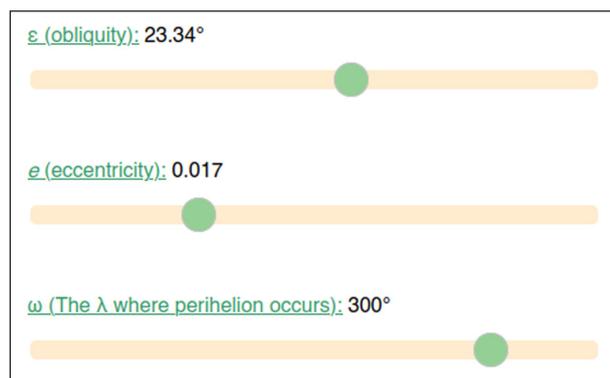

Figure 3 The slider control panels used to control the graphical representations.

independently change orbital parameters and see how such changes influence the following: (1) the variation in Earth's orbital speed and distance from the Sun throughout the year; (2) the irradiance distribution across the Earth's latitudes and throughout the year; (3) the day length of the astronomical seasons; (4) the mean annual irradiance received at each latitude; (5) the shape and positioning of the Earth's orbit relative to the Sun. This setup constitutes a classic experimental environment with multiple variables (in this case three), whereby one variable is changed while the other two are kept constant.

3.3 DIGITAL TEXTBOOK

Included in the interactive GUI is access to a basic digital textbook explaining the concepts of obliquity, eccentricity and geocentric longitude of perihelion (which is governed by precession). The hyperlinks above the

slider controls in Figure 3 will take the students to pages with basic information about the orbital parameters and a tutorial containing example calculations and figures demonstrating basic principles. In the obliquity section, students learn how to calculate the declination latitude of the Sun, as well as the midday angle of the Sun for the solstices at their city, given a specific obliquity. In the eccentricity section, there is a tutorial on how to calculate aphelion and perihelion distances given a specific eccentricity, as well as information on how to calculate the speed of the Earth's orbit at aphelion and perihelion. Geocentric longitude of perihelion is explained and its cause (general precession) is explained using animations.

4 CONCLUSION AND REUSE POTENTIAL

The GUI tool has great potential to be integrated into geosciences curricula, particularly within a classic experimental environment allowing for the isolated study of the individual effects of orbital parameters upon the seasonal and latitudinal distribution of irradiance. The tool provides an experimental environment that can be deployed within a flipped classroom setting with jigsaw activities, as has previously been successfully deployed in geosciences the case of, e.g. plate tectonics (Sawyer et al., 2005). An example lesson plan is to split students into three groups, with each group focussing on learning the effect of one (or all) of the three orbital parameters (obliquity, eccentricity and precession). Each group could investigate the effect (if any) of their parameter(s) upon orbital distance, speed, seasonal irradiance distribution, length of season, and mean annual irradiance received at each latitude. Afterwards, groups can rotate members and/or hold discussions to teach each the other groups about the particular orbital parameter that they studied.

It should be noted that the GUI tool developed here exclusively includes realistic values for the orbital parameters of planet Earth. A useful additional exercise/ challenge is assigning groups unrealistic orbital values for Earth (such as an obliquity value of 45°) and asking them to then sketch the irradiance profile that they would expect to be associated with such a parameter, as well as what latitude the polar circle and tropics would be. Such a task can promote metacognitive thinking, as it challenges the students to extrapolate an extreme hypothetical scenario, which can in turn help them better understand the functioning of more realistic scenarios. Example teaching instructions and material for a group learning activity are included in the Supplement.

Planet Earth's irradiance distribution and its relation to orbital parameters is a very challenging subject to teach. Geosciences has traditionally relied upon fieldwork and/or laboratory settings to stimulate active