

1 **The Sediment Budget Estimator (SBE): a process-model for the stochastic estimation**  
2 **of fluxes and budgets of sediment through submarine channel systems.**

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21 **ABSTRACT**

22 Turbidity currents transport vast amounts of sediment through submarine channels onto deep-  
23 marine basin floor fans. There is a lack of quantitative tools for the reconstruction of the sediment  
24 budget of these systems. The aim of this paper is to construct a simple and user-friendly model that  
25 can estimate turbidity-current structure and sediment budget based on observable submarine  
26 channel dimensions and general characteristics of the system of interest. The requirements for the  
27 model were defined in the spirit of the source-to-sink perspective of sediment volume modeling: a  
28 simple, quantitative model that reflects natural variability and can be applied to ancient systems with  
29 sparse data-availability. The model uses the input conditions to parameterize analytical formulations  
30 for the velocity and concentration profiles of turbidity currents. Channel cross-section and temporal  
31 punctuation of turbidity-current activity in the channel are used to estimate sediment flux and  
32 sediment budget. The inherent uncertainties of geological sediment budget estimations motivate a  
33 stochastic approach, which results in histograms of sediment budget estimations, rather than  
34 discrete values. The model is validated against small-scale experimental turbidity currents and the  
35 1929 Grand Banks turbidity current. It is found to perform within acceptable margins of error for  
36 sediment flux predictions at these smallest and largest scales of turbidity currents possible on Earth.  
37 This success motivates application of the model to a reconstruction of the sediment budget related  
38 to Cretaceous slope-channel deposits (Tres Pasos Formation, Chile). The results give insight into the  
39 likely highly stratified concentration profile and the flow velocity of the Cretaceous turbidity currents  
40 that formed the deposits. They also yield estimates of the typical volume of sediment transported  
41 through the channels while they were active. These volumes are demonstrated to vary greatly  
42 depending on the geologic interpretation of the relation between observable deposit geometries and  
43 the dimensions of the flows that formed them. Finally, the shape of the probability density functions  
44 of predicted sediment budgets is shown to depend on the geological (un)certainty ranges. Correct  
45 geological interpretations of deep marine deposits are therefore indispensable for quantifications of  
46 sediment budgets in deep marine systems.

47

## INTRODUCTION

48 The rationale in studies about turbidity currents and their deposits often refers to submarine fans  
49 being the most voluminous sedimentary bodies on Earth (Middleton, 1993) and turbidity currents  
50 the most prolific transport agents on the planet (Talling *et al.*, 2012), yet no study has succeeded in  
51 presenting a process model that can be used to relate the turbidity currents responsible for the flux  
52 of sediment to the volumes of submarine fan deposits (Jobe *et al.*, 2018). The budget of sediment  
53 transported onto submarine fans is governed by geological mechanisms that operate on thousands  
54 to millions of years involving climate, tectonics, and sea level variations, and it is measured in cubic  
55 kilometers [km<sup>3</sup>]. The flux of sediment in turbidity currents is governed by complex particle-fluid  
56 dynamics operating on milliseconds to hours, and it is measured in cubic meters per second [m<sup>3</sup>/s].  
57 This disparate spread in scales and types of controls makes calculation of geological sediment  
58 budgets from flow processes one of the big challenges in marine geosciences.

59 The source-to-sink approach to studying the entire geological chain of sediment production and  
60 transport has gained prominence in the past decade. It holistically tracks the budget of sediment  
61 from weathering of bedrock in mountainous or hilly catchment areas (the source), through the  
62 various depositional environments along the transport path, all the way to the terminal depositional  
63 sink in the deep oceans (Somme *et al.*, 2009a; Walsh *et al.*, 2016). A strength of the source-to-sink  
64 approach has been that it made the ultimate simplification of the process of sediment transport,  
65 while still yielding robust and informative answers to geological problems. Sediment is simply  
66 distributed from the source to the sink, and the various depositional sub-systems that are passed  
67 along the pathway (rivers, deltas, the continental shelf) act to extract a certain fraction of the  
68 available sediment budget (Paola & Martin, 2012). This success may be counterintuitive when  
69 observed parallel to the development of process-based modelling efforts that seek increasingly more  
70 detailed and complex treatments of the dynamics of sediment transport (Cantero *et al.*, 2011; Abd El-  
71 Gawad *et al.*, 2012; Basani *et al.*, 2014; Kneller *et al.*, 2016). Herein we explore how turbidity-current  
72 processes can be incorporated in a source-to-sink approach without decreasing its robustness and

73 viability. Such incorporation of process-modelling into source-to-sink studies is one of four key areas  
74 for future advances called for by Walsh et al. (2016) in their review of the past, present, and future of  
75 the source-to-sink perspective. Geological uncertainties in source-to-sink analyses are commonly  
76 large, which means that boundary conditions for model simulations are defined as probable ranges,  
77 rather than specific, discrete, values. We argue that this necessitates application of stochastic  
78 process-modelling approaches to predictions of fluxes of sediment into deep water. Furthermore, a  
79 successful geological tool should be a simple, quantitative model that reflects natural variability and  
80 can be applied to ancient systems (Sømme and Martinsen, 2017).

81 The aim of this study is to construct a simple and user-friendly model that can estimate turbidity  
82 current parameters and sediment budgets based on observable submarine channel parameters.  
83 The result is the Sediment Budget Estimator (SBE), a process-based turbidity-current model that  
84 predicts sediment budget transferred through submarine channels from the continental slope to  
85 submarine fans over geological timescales.

86 Three geometrical geological inputs are required: Submarine channel dimension (depth and width),  
87 the size of the median and coarsest sediment particles present on the bed, and submarine channel  
88 gradient. These can be derived from subsurface datasets such as reflection seismic data, core, or  
89 well-logs (Samuel *et al.*, 2003), from chosen outcrop analogues or architectural data-stores (Baas *et al.*,  
90 2005; Cullis *et al.*, 2019), modern oceanographic analogues (Covault *et al.*, 2011; Prather *et al.*,  
91 2016), or source-to-sink predictions based on system style (Helland-Hansen *et al.*, 2016). An  
92 additional estimation of the range of depth average sediment concentration needs to be supplied.  
93 Input can be constrained by narrow bounds of uncertainty where reliable data is available, or broad  
94 ranges of values where estimates are poorly constrained.

95 The SBE uses these input ranges to parametrize analytical formulations for the velocity and  
96 concentration profiles of turbidity currents that are typical of the chosen system geometries. These  
97 currents will be referred to as “characteristic turbidity currents” in this paper. The sediment flux is  
98 determined by multiplying the velocity and concentration profiles. The first type of output of the SBE

99 are illustrative examples of the size, velocity, and concentration distribution of characteristic  
100 turbidity currents, and a histogram of sediment fluxes [ $\text{m}^3/\text{s}$ ] transported through the channel cross  
101 sections. These histograms reflect the range of possible outcomes given the uncertainties in the  
102 input boundary conditions, and embody the stochastic character of the SBE.

103 Secondly, the SBE estimates the system-scale sediment budgets on geological timescale. To obtain  
104 these, the user can input turbidity current recurrence time (Pirmez & Imran, 2003; Clare *et al.*, 2014;  
105 Allin *et al.*, 2018; Jobe *et al.*, 2018; Stacey *et al.*, 2019), event duration (Pirmez & Imran, 2003; Xu,  
106 2011; Cooper, 2013; Clarke, 2016; Azpiroz-Zabala *et al.*, 2017), and geological system activity (Pirmez  
107 *et al.*, 2012). These inputs can be based on the user's understanding of their particular system, or on  
108 default values for system styles suggested in literature. Output of this module is a histogram of  
109 sediment budgets [ $\text{km}^3$ ] on geological timescale.

110 The essence of this approach of estimating sediment budgets is similar to the paleohydrologic  
111 "fulcrum approach" to fluvial sediment-budget estimation as proposed by (Holbrook & Wanas, 2014)  
112 and applied by (Lin & Bhattacharya, 2017; Sharma *et al.*, 2017). The fulcrum method perceives a  
113 fluvial channel cross section as the pivot between the sediment load received from the up-stream  
114 domain and transmitted to a downstream domain. It analyzes the relation between local channel-fill  
115 deposit architecture and this expected sediment throughput. In this paper we will describe this  
116 model-approach with special emphasis on the connection between flow structures of turbidity  
117 currents, their specific geological basin setting, and the geometry of of submarine channels. Due  
118 consideration will eb given to deep-marine concepts that can be used to constrain simulations. The  
119 model is then validated against the smallest and largest scales of sediment delivery into deep basins  
120 for which accurate dynamic data are available: laboratory scale turbidity currents (de Leeuw *et al.*,  
121 2016, 2018a) and the 1929 Grand Banks turbidity current (Heezen & Ewing, 1952; Kuenen, 1952;  
122 Stevenson *et al.*, 2018). The model is then be applied to estimate the sediment budget associated  
123 with Cretaceous submarine channel deposits exposed in the Tres Pasos Formation in Southern Chile  
124 (Hubbard *et al.*, 2010, 2014; Macauley & Hubbard, 2013; Hubbard *et al.*, 2020). This application

125 demonstrates the importance of geological models derived from stratigraphic observations for  
126 sediment budget estimations. The statistical uncertainties in sediment budget estimates on geologic  
127 time-scales can be decreased by narrowing the confidence bounds through strict scrutiny of the  
128 geologic record. Hence, the predictability of source-to-sink transfer of sediment to the terminal  
129 depositional sink in the deep oceans depends on the strength and confidence of geological models.

130

### 131 **FORMULATION OF THE TURBIDITY CURRENT FLOW-STRUCTURE MODEL**

132 The backbone of the SBE is formed by analytical formulations for vertical profiles of velocity,  $u(z)$ , and  
133 concentration,  $c(z)$ , in turbidity currents (Fig. 1a). These are coupled by two closure equations that  
134 relate the velocity and concentration in the flow: 1) a sediment bypass condition that relates the bed  
135 shear stress to the basal sediment concentration (Eggenhuisen *et al.*, 2017); and 2) a conventional  
136 formulation that relates the average sediment concentration to the bed shear stress (Kneller, 2003;  
137 García, 2008). Three boundary conditions need to be set by the user to be able to solve the system of  
138 equations: Submarine channel dimension (depth and width), the size of the median and coarsest  
139 sediment particles present on the bed, and submarine slope gradient.

140

#### 141 *Velocity Profile*

142 The velocity profile of turbidity currents has been recognized to display robust, recurring patterns  
143 (Plapp & Mitchell, 1960; Stacey & Bowen, 1988; Garcia & Parker, 1993; Altinakar *et al.*, 1996; Kneller  
144 *et al.*, 1999; Kneller & Buckee, 2000; Best *et al.*, 2001; Xu *et al.*, 2002; Gray *et al.*, 2005; Straub *et al.*,  
145 2008; Islam & Imran, 2010; Sequeiros *et al.*, 2010a; Xu, 2011; Eggenhuisen & McCaffrey, 2012;  
146 Sequeiros, 2012; Cartigny *et al.*, 2013; Cooper, 2013; Pittaluga & Imran, 2014; Azpiroz-Zabala *et al.*,  
147 2017a; Sequeiros *et al.*, 2018). This robustness of the shape of the velocity profile results from the  
148 simple essential structure of turbidity currents: the bottom boundary is assumed to be a turbulent,  
149 wall-bound, shear layer; and the upper boundary is a turbulent mixing layer between the turbidity  
150 current and the ambient fluid. The velocity model developed here is therefore formed by the

151 addition of two velocity functions: the logarithmic law of the wall, and a plane-mixing-layer velocity  
 152 function. Different approaches have been proposed for the effective superposition of these functions  
 153 (Altinakar *et al.*, 1996; Kneller *et al.*, 1999).

154 We follow the approach of Kneller *et al.* (1999;) instead of Altinakar *et al.* (1996), by assuming a  
 155 logarithmic velocity profile from the bed to the flow depth, and applying a mixing layer structure  
 156 throughout the water column (Fig. 2). We deviate slightly from Kneller *et al.* (1999) who use the  
 157 “interface” between sediment laden and clear water as the flow depth. This interface can be  
 158 qualitatively observed instantaneously in turbidity currents, e.g. in pictures of experiments, but due  
 159 to the multitude of turbulent mixing structures passing any one location over time it cannot be  
 160 quantitatively defined in a time-averaged structure of a turbidity current, where the velocity and  
 161 concentration asymptotically approach 0 with height (Garcia & Parker, 1989; Islam & Imran, 2010;  
 162 Sequeiros *et al.*, 2010b; de Leeuw *et al.*, 2018a). Instead, we follow Hermidas *et al.* (2018) by defining  
 163 the elevation  $z=H$  as the center of mixing layer and top of the logarithmic profile (Fig. 2). This  
 164 measure of flow depth is equated to levee height in our approach (Fig. 1B). This definition is a key  
 165 aspect of the modelling strategy, and will be further justified below.

166 The velocity  $u$  [m/s] as a function of elevation above the bed  $z$  [m] is then:

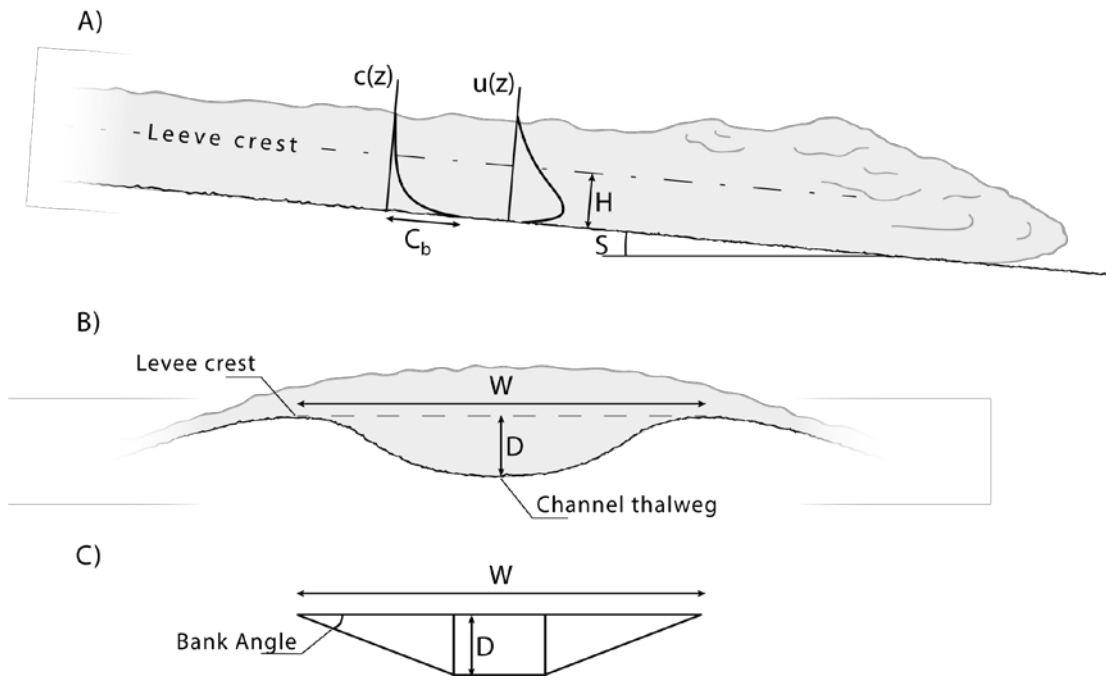
$$167 \quad u(z) = u_{\log}(z) - u_{PML}(z) \quad (1)$$

168 The logarithmic velocity function is:

$$169 \quad u_{\log}(z) = \frac{u^*}{\kappa} \ln \left( \frac{z}{z_0} \right) \Bigg|_{z_0 \leq z \leq H} \quad (2)$$

$$u_{\log}(z) = \frac{u^*}{\kappa} \ln \left( \frac{H}{z_0} \right) \Bigg|_{z \geq H}$$

170 Where  $u^*$  is the shear velocity [m/s],  $\kappa$  is von Karman’s constant [0.4],  $z$  is the bed-perpendicular  
 171 coordinate, and  $z_0$  is the elevation at which the turbulent velocity profile intersects 0 m/s (Van Rijn,  
 172 2011).

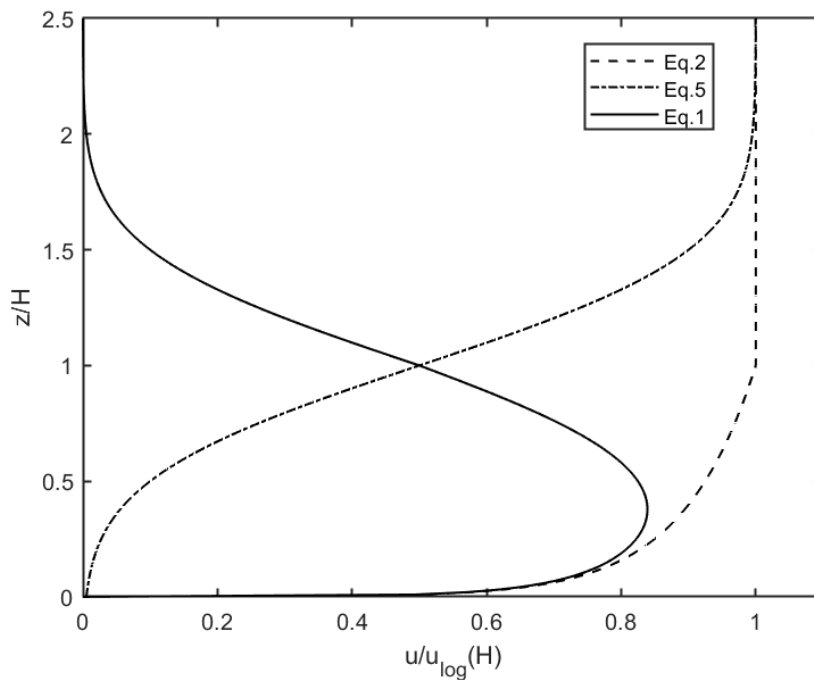


173

174 **Fig. 1:** A) Schematic representation of the structure of a turbidity current, simplified from Altinakar et

175 al. (1996). B) Schematic of the relation between channel cross-section and the modelled turbidity

176 current. C) Trapezoidal cross-section of the model channel.



177

178 **Fig. 2:** The analytical formulation for the velocity profile of turbidity currents (Eq. 1; solid line), as

179 obtained by subtracting the PML term (Eq. 5; dash-dotted line) from the logarithmic velocity (Eq. 2;

180 dashed line). Following Kneller et al. (1999) in lieu of Altinakar et al. (1996).



181 The non-dimensional velocity distributions of plane mixing layers collapses into a universal function  
182 with the form (Champagne *et al.*, 1976; Pope, 2000):

$$183 \quad f(\xi) = 1/2 \operatorname{erf}\left(\frac{\xi}{\sigma\sqrt{2}}\right) \quad (3)$$

184 Where  $\sigma$  has been analytically determined to be  $\sim 0.39$  (Pope, 2000), and  $\xi$  is a non-dimensional  
185 coordinate perpendicular to the bed:

$$186 \quad \xi = (z - z_{50}) / (z_{10} - z_{90}) \quad (4)$$

187 The subscripts denote the elevations of the velocity percentiles, e.g.  $z_{50}$  is the z-coordinate where the  
188 velocity is equal to 50% of the maximum velocity ( $u_{\log}(H)$ ). The range between  $z_{10}$  and  $z_{90}$  is  
189 approximated closely by  $H$  (Pope, 2000).

190 The scaled velocity function  $f(\xi)$  relates to the dimensional plane-mixing-layer velocity function as:

$$191 \quad u_{PML}(\xi) = u_{\log}(H) [f(\xi) + 1/2] \quad (5)$$

192 Note that the plane mixing layer is scaled with the logarithmic velocity, not with the velocity  
193 maximum of the turbidity current (Kneller *et al.*, 1999). The maximum velocity, as well as the  
194 elevation of the maximum velocity of the turbidity current thus arise from the modelling, and are not  
195 constrained *a priori*. Equation 5 mathematically extends below the bed where it asymptotically  
196 approaches 0. The residual velocity of Eq. 5 at  $z=0$  is 0.1% of  $u_{\log}(H)$ , which is deemed insignificant for  
197 the purpose of modelling the sediment budget of submarine channel systems.

198

### 199 *Concentration Profile*

200 The shape of the concentration profile of many experiments is a rather similar, slightly concave  
201 exponential function (Garcia, 1994; Choux *et al.*, 2005; Islam & Imran, 2010; Sequeiros *et al.*, 2010a;  
202 Tilston *et al.*, 2015; de Leeuw *et al.*, 2018a). The concentration function is here expressed in the  
203 simplest form of an exponential decay function:

$$204 \quad c(z) = C_b e^{-kz} \quad (6)$$

205 Where  $c(z)$  is the sediment concentration at elevation  $z$  [m],  $C_b$  is the sediment concentration at the  
206 base of the flow [-], and  $k$  is a decay constant [1/m].

207

### 208 *Closure Relations Between Variables*

209 **Sediment Bypass Closure** --- Submarine channels are effective bypass conduits for sediment  
210 into deep basins (Stevenson *et al.*, 2015b; Kneller *et al.*, 2016) that remain open conduits for most of  
211 their lifespan (Hubbard *et al.*, 2014), such that the sediment mass eventually deposited in the  
212 channel-fill deposits at a given cross section represents only a minute portion of the sediment mass  
213 transported through that cross section (Paola & Martin, 2012; Stevenson *et al.*, 2015a; de Leeuw *et*  
214 *al.*, 2018b). A bypass condition is therefore used here to reconstruct the characteristic sediment flux  
215 going through a channel. The bypass condition is here based on the suspension capacity parameter  $\Gamma$   
216 of Eggenhuisen *et al.* (2017), which balances the gravitational, buoyancy and turbulent forces acting  
217 on the suspended load. It includes universal turbulent flow scales and material properties of the  
218 fluid and particles only. The condition  $\Gamma < 1$  coincides with the complete consumption of bed-  
219 generated turbulence by sediment suspension, as observed in direct numerical simulations (Cantero  
220 *et al.*, 2009, 2011, 2012). This over-saturated sediment condition is thought to lead to rapid  
221 deposition. The condition  $\Gamma = 1$  can be used to relate the sediment concentration at the base of a  
222 bypassing turbidity current  $C_b$  to flow conditions and material properties of water and sediment  
223 (Eggenhuisen *et al.*, 2017):

$$224 \quad C_b = \frac{u_*^3}{140\nu g R} \quad (7)$$

225 Where  $\nu$  [m<sup>2</sup>/s] is the kinematic viscosity of water,  $g$  [m/s<sup>2</sup>] is the acceleration by gravity, and  $R$  [-] is  
226 the submerged relative density of quartz in water (1.65).

227 **Parameterization of the Logarithmic Velocity Profile** --- Shear velocity and  $z_0$  are the two  
228 parameters that are needed to resolve the logarithmic velocity function (Eq. 2).

229 The shear velocity is estimated from the shear stress at the base of the flow due the excess weight of  
 230 suspended sediment:

$$231 \quad u^* = \sqrt{H_r \bar{C} g R S} \quad (8)$$

232 Where  $H_r$  is the hydraulic radius [m], which is calculated as the cross-sectional area divided by the  
 233 frictional perimeter. The interface with the ambient fluid is included into the frictional perimeter  
 234 here.  $\bar{C}$  is the input depth-averaged sediment concentration [-], which is evaluated between the bed  
 235 and  $z=H$  (see *Boundary Conditions, below*).  $S$  is the tangent of the slope [-].

236 Different empiric relations have been suggested for  $z_0$  (Garcia, 2008; van Rijn, 2011). In the version  
 237 used here, a distinction is made between mobile and non-mobile beds, based on the ratio between  
 238 the bed shear stress ( $\tau_b$ ) and the critical bed shear stress ( $\tau_c$ ) for initiation of transport of the bed  
 239 material (“transport stage” *sensu* van Rijn, 2011):

$$240 \quad \begin{aligned} z_0 &= \frac{k_s}{30} + \frac{\nu}{9u^*} \Big|_{\tau_b < \tau_c} \\ z_0 &= \frac{k_s}{30} + \delta_b \Big|_{\tau_b \geq \tau_c} \end{aligned} \quad (9)$$

241 Where  $k_s$  is the Nikuradse equivalent sand roughness [m], and  $\delta_b$  is the thickness of the bedload  
 242 layer [m]. The Nikuradse equivalent sand roughness can be estimated from the grainsize of the  
 243 coarsest sediment particles on the bed ( $d_{90}$ ; 90<sup>th</sup> percentile of the grainsize distribution; van Rijn,  
 244 2011):

$$245 \quad \begin{aligned} k_s &\approx 3d_{90} \text{ (sand)} \\ k_s &\approx d_{90} \text{ (gravel)} \end{aligned} \quad (10)$$

246 The thickness of the bedload layer is estimated as (Garcia, 2008):

$$247 \quad \delta_b = \frac{0.015d_{50}[\tau_b/\tau_c]}{1+0.2[\tau_b/\tau_c]}$$

248 Where  $d_{50}$  is the median grainsize of the bed material [m]. Form roughness effects related to  
 249 irregular shapes of the bed (e.g. bedforms) are not incorporated in Eq. 9.

250

251

### *Boundary Conditions*

252 The structure of equations 1-10 has been chosen such that they can now be solved when boundary  
253 condition values are set for flow thickness  $H$ , depth averaged sediment concentration  $\bar{C}$ , slope  $S$ ,  
254 and characteristic bed-grainsize, which are all variables that deep marine geologists can estimate and  
255 debate. The probabilistic nature of the SBE will allow the users to rapidly test their ideas on the  
256 confidence bounds of these parameters. It is thus not necessary to know exactly how thick  
257 characteristic turbidity currents in a system of interest are, nor what their average concentration  
258 was. Rather, the model can be used to test the implications of perspectives on these parameters,  
259 perspectives that all deep marine geologists have, for predictions of sediment fluxes and budgets.  
260 This includes the perspective that it is wholly unknown what the scales of characteristic turbidity  
261 currents in a system are, as will be illustrated in the discussion. This probabilistic functionality is  
262 realized by requiring the user to define a range between likely minimum and maximum values for  
263 each of the boundary conditions. These ranges are uniformly sampled by the SBE with a user-defined  
264 number of steps in between the minimum and maximum values. Equations 1-10 are solved for all  
265 combinations of each of the boundary condition values. This can lead to thousands or tens of  
266 thousands turbidity currents being simulated.

267

268 **Flow Thickness Correlates to Channel Depth** --- Turbidity current thickness is often assumed  
269 to be closely related to the depth of the channel in modelling approaches (Salles *et al.*, 2009; Abd El-  
270 Gawad *et al.*, 2012; Arfaie *et al.*, 2014; Basani *et al.*, 2014; Hamilton *et al.*, 2017; Jobe *et al.*, 2017;  
271 Kane *et al.*, 2017). Such bank-full discharge assumptions are bread-and-butter in fluvial  
272 paleohydrology, but much less straightforward in channelized turbidity currents, which may extend  
273 above the channel. This key assumption of the model will therefore be addressed in depth.  
274 Firstly, the simple argument of scale is supported by the validity of laboratory modelling of  
275 channelized turbidity current morphodynamics (de Leeuw *et al.*, 2016), which demonstrates that  
276 laboratory-sized flows that are orders of magnitude smaller than real world flows self-generate

277 channels at similar dimensions to the flows: small turbidity currents build small channels and large  
278 turbidity currents build large channels.

279 Furthermore, our morphodynamic understanding of levee-building includes a self-regulatory  
280 mechanism, whereby the levees aggrade by deposition from the dilute top of the flow, causing the  
281 levee-building to halt when the channel relief reaches a similar scale as the flow thickness (Straub &  
282 Mohrig, 2008; Shumaker et al., 2018)). Indeed, the variability of flow thickness with respect to  
283 channel dimensions has been argued to be small by Straub et al. (2008) who argue that the channel  
284 form and flow scale will always be tuned to each other. The robustness of this self-regulatory  
285 mechanism is reflected in the successful application of the geomorphological concept of hydraulic  
286 geometry (Leopold & Maddock, 1953) to submarine channels by Konsoer et al. (2013), who  
287 established that a correlative power-law relation between turbidity current discharge and submarine  
288 channel dimensions does exist.

289 Investigating the process of channelized flow in more detail, Mohrig and Buttle (2007) established  
290 experimentally that channels serve as effective conduits for turbidity currents that are 1.3 times  
291 thicker than the channel-form is deep. The along-axis flow velocities are an order of magnitude  
292 higher than the cross-channel overspill velocity in such confined flows. The ratio of along-axis to  
293 cross-channel velocity rapidly decreases for partially confined flows that are thicker than 1.3 times  
294 the channel depth (Mohrig & Buttle, 2007), indicating that those flows are poorly confined by the  
295 channel and rapidly spread out over the overbank area. Mohrig and Buttle (2007) use a  
296 conventional definition of flow thickness as the distance between the bed and an interface between  
297 ambient fluid and the turbidity current ( $H_{MB}$ ). This interface is not defined in a time-averaged velocity  
298 profile, and falls somewhere in the top half of the mixing layer. The proposal of Hermidas et al.  
299 (2018) to define the center of the mixing layer as the flow depth (Fig. 2) is less ambiguous and more  
300 straightforward: the simple condition of  $H=D$  (Fig. 1a&b) is roughly equal to the regime-boundary for  
301 fully channelized flows as defined by Mohrig and Buttle (2007), because  $H_{MB}=1.3*D$ , and  $H=D$  here.  
302

303 Finally, the bypass condition based on the suspension capacity parameter of Eggenhuisen et al.  
304 (2017) also contains a mechanism that causes channel dimensions to be attracted to a bypass state  
305 for the characteristic turbidity currents in the system. If the concentration at the base of the flow  
306 exceeds the saturation concentration, this will lead to the immediate deposition of excess sediment  
307 on the bed, until  $\Gamma = 1$ . This will partially fill the channel form, decreasing levee height to re-  
308 equilibrate channel dimensions with smaller characteristic turbidity currents. If the concentration  
309 falls below the saturation concentration, there is excess suspension capacity that will lead to  
310 entrainment of sediment from the channel floor. This will increase the depth and cross-sectional area  
311 of the channel to re-equilibrate with the size of larger characteristic turbidity currents.

312 In conclusion, a diverse suite of concepts suggests that channel size and thickness of characteristic  
313 turbidity currents are related to each other, and this justifies the equation of channel depth and flow  
314 thickness ( $H=D$ ) in the first order prediction of flow structures from channel dimensions.

315

316 **Concentration: the Density of the Turbidity Current** --- Robust first order predictability of  
317 concentration magnitude through wholly process-based equations in this simplified model  
318 framework is not yet feasible. The choice is therefore made here to make the average concentration  
319 a user-defined boundary condition, rather than set it through some empiric parameters behind the  
320 scenes of the SBE. This approach at least makes the concentration uncertainty clearly defined by the  
321 user at the front end of the model. The question now arises what typical concentrations are of  
322 turbidity currents.

323 The only reliable measurements of depth-averaged concentrations of real-world turbidity currents  
324 were published by Azpiroz-Zabala et al. (2017) and Simmons et al. (2020). They recorded very low  
325 concentrations of 0.017-0.023 % in 48-77m thick turbidity currents travelling down the Congo  
326 Canyon with a velocity of under 1 m/s. These conditions are likely to represent the slower end of the  
327 spectrum of turbidity currents in the Congo Canyon, though other measurement attempts of faster  
328 events have so far resulted in equipment failures (Khripounoff et al., 2003). Reliable average

329 concentration measurements are not available for such faster natural turbidity currents in other  
330 systems either. Due to the near-complete lack of accurate concentration measurements in natural  
331 flows (Wang et al., 2020), various authors have tried to estimate average concentrations by  
332 combining other variables with equations. Konsoer et al. (2013) combine friction factor estimates  
333 with estimations of bank full conditions that are much like the perspective set out in the previous  
334 section. This leads them to estimate a sediment concentration range of 0.2-0.6% for a selection of  
335 channels exposed on the modern sea floor. Zeng et al. (1991) also applied friction factors to estimate  
336 sediment concentration during a turbidity current that occurred in May 1986 in the submarine  
337 channel in Bute Inlet (Canada). This turbidity current travelled at 3.6 m/s, resulting in a sediment  
338 concentration estimate of 0.5-0.7% (Zeng et al., 1991). These depth-averaged concentration values  
339 seem to be more representative for a broader range of active and ancient turbidity current systems  
340 than the very dilute concentrations reported by Azpiroz-Zabala et al. (2017) for the Congo Canyon.  
341 Indeed, a compilation by Sequeiros (2012) of concentration estimations from literature leads the  
342 author to suggest that 0.45% is a typical average concentration at field scale, consistent with both  
343 the range suggested by Konsoer et al. (2013), and the estimate of Zeng et al. (1991). Finally, the  
344 Grand Banks 1929 turbidity current was the single largest turbidity current event known to have  
345 occurred in modern times, and its size, velocity, and sediment concentration have historically been  
346 thought of as the upper limits of what is possible in oceans on Earth (Kuenen, 1952). The sediment  
347 concentration was estimated to be 1.1-2.9% (Plapp and Mitchell, 1966), an estimate that has recently  
348 been adjusted to 2.7-5.4% (Stevenson et al., 2018; see below). This upper concentration limit is  
349 consistent with the review by Sequeiros (2012), who suggests that the average sediment  
350 concentration of a turbidity current rarely exceeds 5%.

351 Based on these sources, we suggest the following broad subdivisions for the average input  
352 concentration in SBE simulations: very dilute [0.05-0.2%]; dilute [0.2-0.6%]; intermediate [0.6-2%];  
353 high [2-5%], with the dilute range advisable as a default. Interestingly, Reginald Daly arrived at likely

354 sediment concentrations of 0.3-0.6% in his rather brilliant 1936 paper, solely by applying deductive  
355 and partially intuitive reasoning (Daly, 1936).

356 The user defined depth-averaged concentration allows evaluation of the following integral in the  
357 model workflow:

$$358 \quad \overline{CH} = \int_0^{\infty} C_b e^{-kz} dz \quad (11)$$

359 Evaluation of the integral results in an expression of the decay constant  $k$ :

$$360 \quad k = \frac{C_b}{C} \frac{1}{H} \quad (12)$$

361 The decay constant thus depends on flow thickness, and the ratio of near-bed concentration to  
362 average concentration. This ratio often appears in modelling studies of turbidity currents (Parker *et al.*,  
363 1986; Halsey *et al.*, 2017). It is the simplest measure for the degree of density stratification in the  
364 turbidity current. It approaches 2 in many experiments (Parker *et al.*, 1987), while higher numbers  
365 have been proposed, and recently confirmed, for natural scale flows (Azpiz-Zabala *et al.*, 2017 &  
366 Simmons *et al.*, 2020). Note that the concentration profile as described by Eq. 6 asymptotically  
367 approaches 0 at an indefinite elevation above the channel floor; some of the sediment declared in  
368 the two boundary conditions  $\overline{CH}$  is thus actually suspended above the bank-full elevation in the  
369 exponential concentration profile. The chosen structure of Eq. 11 therefore creates a small  
370 discrepancy between the average concentration between the channel floor and the bank full depth,  
371 and the average of Eq. 6 between these two levels. A similar effect occurs in the more common  
372 integral approach of Ellison and Turner (1959). We accept this minor discrepancy and claim that its  
373 effects will be negligible in highly stratified natural currents (see for example Fig. 3b).

374 **Slope of the System** --- The slope of a channel is well defined in medium-low resolution  
375 oceanographic datasets. In subsurface systems, the slope can be estimated from seismic datasets  
376 (Shumaker *et al.*, 2017; Beelen *et al.*, 2019). If data does not allow the slope to be measured directly  
377 for a system, slope estimates can also be based on analogues from modern oceanography (Covault *et al.*,  
378 2011; Prather *et al.*, 2016) or stratigraphic panels of outcrop systems (Johannessen & Steel, 2005;



379 Hubbard *et al.*, 2010; Daniels *et al.*, 2018). Compaction of clinofolds adds an extra source of  
380 uncertainty (Beelen *et al.*, 2019) that can be taken into account when setting the confidence bounds  
381 of the slope values. Helland-Hansen *et al.* (2016) qualitatively grouped system styles with different  
382 steepness (Helland-Hansen *et al.*, 2016), and quantifications of the slope steepness have also  
383 recently been reviewed (Patruno *et al.*, 2015; Patruno & Helland-Hansen, 2018). Based on these  
384 sources, users of the SBE could use the following classes if no slope data is available for their system  
385 of interest: Gentle: 0.5-1°; Intermediate: 1-2.5°; Steep: 2.5-6°; Very Steep 6-12°. The very-steep class  
386 appears to be relevant only for steep submarine canyon systems, such as the Var Canyon (Mulder *et al.*  
387 *et al.*, 1998), the canyons in the Ebro and North Catalan margins (Amblas *et al.*, 2006; Lastras *et al.*,  
388 2011), or some canyons on the North American Pacific Margin (Lee *et al.*, 2002).

389 **Bed Roughness** --- The size of the coarsest sediment particles making up the bed determines  
390 the bed roughness, which provides a boundary condition needed to solve Eqs. 10, 9, and 2. The user  
391 is therefore required to supply an estimation of the coarse fraction of the sediment particles present  
392 on the channel thalweg. This data can be obtained from grain-size analysis of core-samples obtained  
393 from the channel under investigation. It can also be taken from samples within other parts of the  
394 system when the channel body itself has not been cored, though this approach could lead to under-  
395 estimation of the grain size in the channel thalweg. No grain-size samples may be available in  
396 exploration settings. Geologists will then generally be able to set likely values (250  $\mu\text{m}$ ; coarse sand;  
397 small pebbles; etc.) based on their understanding of the basin setting and the source area of the  
398 sediment (Reading & Richards, 1994; Richards *et al.*, 1998).

399

#### 400 **THE SEDIMENT FLUX [ $\text{M}^3/\text{S}$ ] AND BUDGET [ $\text{KM}^3$ ] MODULES**

401 The equations, closures, and boundary conditions discussed above suffice to solve the first order  
402 velocity and concentration structure of the multitude of characteristic turbidity currents in channels.  
403 The aim of this work, however, is to use the model for calculations of sediment flux and sediment  
404 budget. The SBE executes each of these calculations for all of the turbidity currents resulting from

405 the probabilistic sampling of the flow boundary conditions. In turn, the boundary conditions needed  
406 to complete these modelling steps are also supplied as ranges between likely minimum and  
407 maximum values by the user. These ranges are uniformly sampled in a user-defined number of steps  
408 during the execution of an SBE simulation.

409

#### 410 *From Flow Structure to Sediment Flux*

411 The sediment flux per unit width by the characteristic turbidity current can be determined by  
412 multiplying the concentration at each elevation with the corresponding velocity and integrating from  
413 the bed to an elevation some distance above the channel (Plapp & Mitchell, 1960):

$$414 \quad Flux_{1D} = \int_0^{\infty} c(z)u(z)dz \quad (12)$$

415 The vertical coordinate is discretized in the SBE with steps of size  $\Delta z$ , such that this expression can be  
416 evaluated as the dot product of the concentration and velocity profiles multiplied by the vertical step  
417 size:

$$418 \quad Flux_{1D} = c(z) \bullet u(z) \Delta z \quad (13)$$

419 The units of this sediment flux per unit width are  $m^2/s$ . The channel cross-section is here simplified to  
420 a trapezoidal shape, consisting of a flat channel-thalweg section in the middle, and two channel  
421 margins on either side (Fig. 1c). The lateral channel-bank angle is user defined, but will be set to 10  
422 degrees throughout this paper for simplicity. The estimation of the total sediment flux through the  
423 channel cross section follows an established procedure in fluvial processes and engineering (Chang,  
424 1988): For each section in the trapezoidal cross section, we calculate a hydraulic radius, shear  
425 velocity, and velocity and concentration profiles. The resulting flux of Eq. 13 is multiplied by the  
426 section-width, and the section-fluxes are added to obtain the total sediment flux through the channel  
427 cross-section [ $m^3/s$ ]. The section-method can be used to calculate fluxes through more sophisticated  
428 cross-sectional channel shapes, for instance by calculating turbidity current structures that represent  
429 more (e.g. 10) lateral channel sections within a single channel cross section. This is not pursued here,

430 because this is deemed to only give second order improvements in predicting the sediment flux at  
431 the cost of an order of magnitude increase in amount of turbidity current structures that need to be  
432 calculated. The added demand on the specificity of boundary condition constraints, in this case the  
433 channel cross-sectional shape, is also contrary to the philosophy of the SBE.

434

435 *From Sediment Flux to Sediment Budget*

436 The sediment supply to deep-water sedimentary systems is punctuated on the time scales of events  
437 and geological cycles (Romans *et al.*, 2016). The geological sediment budget need to be calculated by  
438 multiplying sediment flux of the characteristic turbidity currents with the typical duration of a typical  
439 flow event, its frequency, and the (geologic) time-scale of the system's activity.

440

441 **Turbidity Current Duration** --- Turbidity currents have commonly been estimated to last  
442 minutes to hours (Piper *et al.*, 1988, [minimum 2 hours]; Allen, 1991, [20-52 minutes]; Baas *et al.*,  
443 2000, [16-19 minutes]; Jobe *et al.*, 2012, [3-176 minutes]; Jobe *et al.*, 2017, [minimum 6-12 minutes];  
444 Stevenson *et al.*, 2018, [4-8 hours]). Measurements of turbidity currents indicate that flows last  
445 minutes on proximal delta slopes (Hughes Clark, 2016). The majority of monitored flows in upper  
446 canyons, however, last between 1-10 hours (see Talling *et al.*, 2013 for a review). Measurements in  
447 the Congo Canyon, which is the only of the major passive-margin deep water systems that is  
448 presently active, show that flows last up to 10 days 170 km away from the canyon head at water  
449 depths of 2000 m (Cooper, 2013; Azpiroz-zabala *et al.*, 2017). This longer flow duration in a major  
450 canyon system is consistent with the estimation for the Pleistocene Amazon flows by Pirmez and  
451 Imran (2003). They estimated that flows lasted several days in the Pleistocene phase of activity of the  
452 Amazon fan. These measurements and estimations are in line with the suggestion by Azpiroz-Zabala  
453 *et al.* (2017) that turbidity current duration is a function of distance from the source area of the flows  
454 and the stretching of flows as they transit down the system. The transit time of a flow towards a  
455 location in the basin allows the flow to stretch due to different velocities in different parts of the

456 flow. Flows therefore last longer further away from the source, and similarly they last longer in the  
457 distal sections of larger systems. Even the very long turbidity currents measured in the Congo Canyon  
458 can be explained in this way without invoking a sustained source mechanism (Azpiroz-Zabala et al.,  
459 2017). The timescale of duration of turbidity currents at a location can thus be estimated by dividing  
460 the distance to the source area by a characteristic stretching-velocity scale of the currents. The  
461 estimation of the stretching velocity scale might require an iterative procedure where the SBE is  
462 initially used to reconstruct velocity profiles, which are subsequently used to evaluate the turbidity  
463 current duration boundary condition for sediment budget estimations. An alternative workflow in  
464 ancient and subsurface cases, where uncertainties are inherently large, might be to set broad ranges  
465 of turbidity current durations based on the geological setting: minutes to 1 hour for delta slopes;  
466 hours to 10 hours for canyons in the upper continental slope and slope channels in smaller basins  
467 with steep slopes; 10 hours to a few days for larger canyons in the lower continental slope; and a few  
468 days to a week for distal parts of large (~1000 km long) submarine fans.

469

470 **Recurrence Time** --- Recurrence times of turbidity currents are increasingly well constrained  
471 in literature (Piper & Deptuck, 1997; Pirmez & Imran, 2003; Xu, 2011; Talling *et al.*, 2013; Clare *et al.*,  
472 2014, 2016; Stevens *et al.*, 2014; Azpiroz-Zabala *et al.*, 2017; Allin *et al.*, 2018; Jobe *et al.*, 2018;  
473 Stacey *et al.*, 2019). Much direct monitoring evidence points to a few to many tens of turbidity  
474 currents being generated each year at the top of the slope in active systems. This activity can be  
475 bundled seasonally in summer in response to meltwater hydrographs (Clare *et al.*, 2016; Hizzett *et*  
476 *al.*, 2018), or winter in response to storm activity (Xu *et al.*, 2004; Pope *et al.*, 2017). These very short  
477 recurrence times rapidly increase down-slope (Stevens *et al.*, 2014; Stacey *et al.*, 2019), because  
478 many turbidity currents dissipate within the slope system (Heerema *et al.*, 2020), which is thus a  
479 staging area for sediment that is only occasionally exported all the way to the basin floor by large,  
480 fan-building turbidity currents (Jobe *et al.*, 2018). Recurrence time of turbidity currents thus depends  
481 highly on the position in the system of interest, the mechanism that ignites these flows, and the size

482 of the shelf itself. Consequently, flow frequency can vary from weekly to monthly or seasonal event  
483 in low storage capacity (short) shelves, to decadal, centennial, or even millennial -scale recurrence  
484 intervals in high storage capacity (broad) shelves, especially if these flows are triggered through  
485 geologic factors like the Grand Banks earthquake rather than fluvial flooding as per the Congo  
486 system. In summary, if upper slope sedimentation is of most interest, the shorter recurrence times  
487 are advised as input. If sediment export to submarine fans at the base of slope is of interest,  
488 recurrence times of decades to centuries can be appropriate (see Jobe et al., 2018, for compilations  
489 of recurrence times in dated Quaternary fan systems), though evidence suggests that turbidity  
490 currents travel down major channel-levee systems, such as the Amazon, annually during periods of  
491 glacioeustatic lowstands of sea level (Piper & Deptuck, 1997; Pirmez & Imran, 2003). The largest  
492 millennial recurrence times seem to be restricted to systems where turbidity currents are triggered  
493 by rare seismic events (Clare *et al.*, 2014).

494 If recurrence times for ancient examples are considered too uncertain to set as an input condition, an  
495 alternative strategy is to enforce an event count, based on stratigraphic evidence, by the  
496 combination of recurrence time and duration of system activity.

497

498 **Allocyclic System Activity** --- The duration and recurrence time of turbidity currents are both  
499 aspects of the short timescale punctuation of submarine channel activity. Punctuation of activity also  
500 exists on longer timescales. This long timescale punctuation of activity generally relates to external,  
501 or allogenic, forcing that causes periodic attachment and detachment from the feeder systems of the  
502 submarine depositional system (e.g. shelf-edge deltas; litoral cells; or estuaries).

503 Classic sequence stratigraphy incorporates the best-known concept for external forcing of  
504 punctuated deep water activity (e.g. Posamentier and Vail, 1988). It describes how deep-water  
505 systems are mostly sediment-starved during periods of relative sea-level highstand, when basin  
506 margins are generally flooded and the sediment budget that is brought to the basin margin by rivers  
507 is mostly deposited in coastal plain and deltaic environments on the shelf. Deltas prograde to the

508 shelf edge during subsequent periods of relative sea-level lowstand. The shelf-edge deltas are  
509 positioned at the top of the slope leading into the deep basin, such that sediment accumulated in  
510 these deltas can easily be mobilized to trigger turbidity currents (Daly, 1936). This concept has been  
511 validated on various deep-water systems around the world, especially for the Pleistocene era  
512 (Anderson, 2000; Sylvester, 2012). In lowstand-dominated systems, the deep-water system activity  
513 duration should therefore be set by the user to the phase within the dominant geological cycle  
514 during which shelf-edge deltas are present. The precise timing of this phase has been determined for  
515 the Eastern Gulf of Mexico (Pirmez et al., 2012) and the Niger Delta slope (Jobe et al., 2015). Pirmez  
516 et al. (2012) document that sedimentation in the Brazos-Trinity system in the Gulf of Mexico took  
517 place mostly in the 9 kyr period from 24-15 ka, around the maximum sea-level lowstand in the latest  
518 Late Glacial Maximum. In the case of the Niger Delta system, Jobe et al. (2015) documented how one  
519 of the prominent channel conduits was abandoned during the sea level rise at the end of the second-  
520 last glacial, at 130 ka. Sandy turbidity current activity resumed at 50 ka, concurrent with the sea level  
521 fall in Marine Isotope Stage 3. The activity lasted through the glacial sea level lowstand until the  
522 channel system was abandoned again in two steps from 19-15 ka. The system activity thus lasted  
523 ~30-35 kyr within a ~100 kyr glacioeustatic cycle. The SBE should primarily be used to determine the  
524 sediment budget for these active phases of sediment delivery in deep marine systems.

525 The human mind is naturally prone to project situations that it knows best as the norm onto the  
526 unknown. For geologists this leads to a Pleistocene-projection bias, a pitfall that entails regarding the  
527 present-day ice-house setting as the norm for the geological past. Many deep-water depositional  
528 systems of interest were active in Jurassic, Cretaceous, or Paleogene times, when fluctuations of  
529 relative sea-level are generally believed to have been less prominent as a forcing of sediment supply  
530 to deep-water depositional systems (Blum and Hattier-Womack, 2009). In such systems climate is  
531 operating through mechanisms other than glacio-eustasy, for instance by forcing sediment  
532 production and transport cycles on the continents (Carvajal and Steel, 2006; Zhang et al., 2019).  
533 Interestingly, the time scale of climatic forcing of sediment supply to deep marine basins appears to

534 be of order 10-100 kyr, which is similar to glacio-eustatic lowstand re-occurrence times (Carvajal and  
535 Steel, 2006; Crabaugh and Steel, 2004; Grundvåg et al., 2014; Burgess and Hovius, 1998; Blum &  
536 Hattier-Womack, 2009). In such cases the system activity parameter of the SBE should be set to the  
537 length of time within the climatic cycle that characterizes the phase of maximum regression of deltas  
538 to the basin margin.

539 The considerations above are tailored to low-gradient systems on non-glaciated, tectonically passive  
540 margins. Geologists must be willing to depart from this established standard model that has been  
541 tailored to such a specific basin-setting when the context suggests to do so. For instance, it has been  
542 shown that the effect of sea-level fluctuations on deep water sediment delivery can be  
543 fundamentally different in steep, tectonically active systems characterized by a narrow shelf (Covault  
544 *et al.*, 2007). Covault et al. (2007) documented how sediment derived from part of Southern  
545 California is predominantly delivered to submarine fans during sea level highstand, when the  
546 Oceanside littoral cell is at its peak activity and generates a high supply of sediment to the La Jolla  
547 Canyon head. The Congo Canyon system is another example that does not follow the sea-level  
548 lowstand paradigm (Khripounoff *et al.*, 2003; Azpiroz-Zabala *et al.*, 2017) due to the direct  
549 connection that exists between the Congo Canyon head and the Congo Estuary. These examples  
550 illustrate that general rules of allocyclic activity must be released if particular aspects of the basin  
551 configuration invalidate them.

552

### 553 **SBE-RESULT STRUCTURE AND SENSITIVITY ANALYSIS**

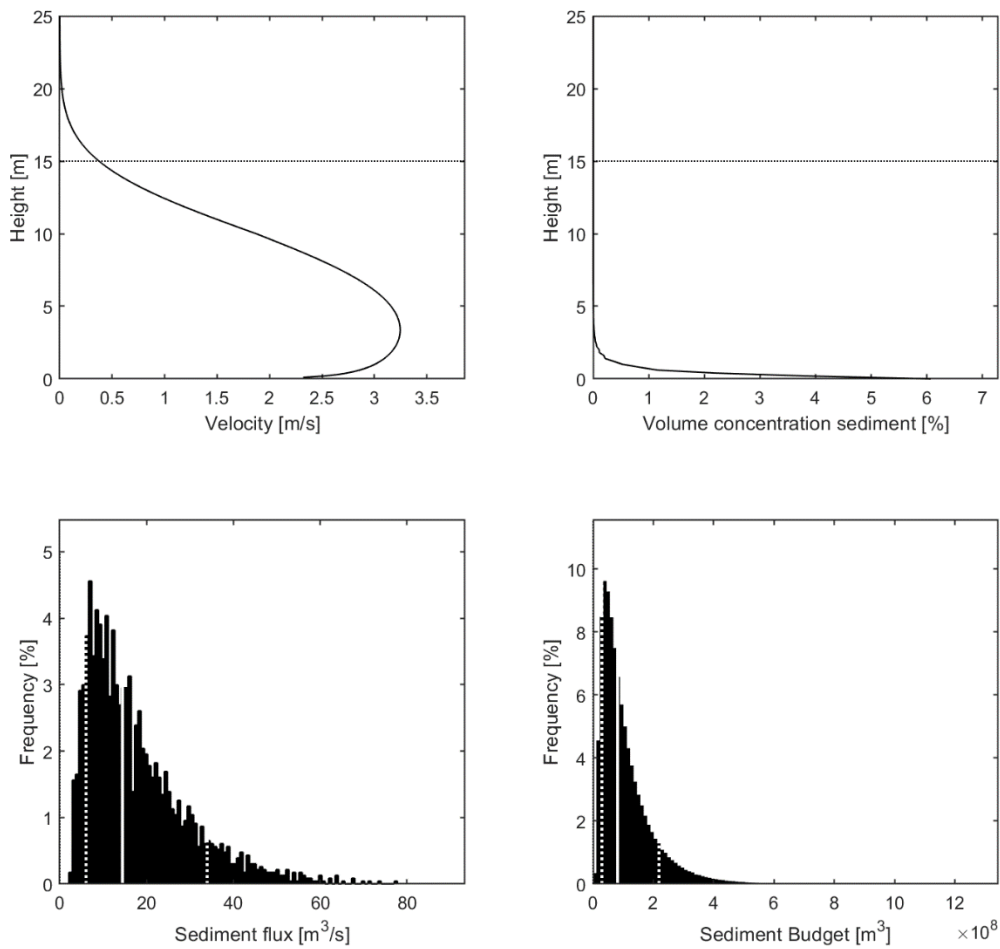
554 The structure of the default SBE results is illustrated with a simulation of a hypothetical system  
555 characterized by dilute turbidity currents ( $C=0.2-0.6\%$ ), down intermediate slopes of  $1-2.5^\circ$ , through  
556 channels with dimensions of width and depth spanning 200-400 m and 10-20 m respectively. The  
557 median grainsize of the channel bed is  $150\ \mu\text{m}$ , and the coarse sediment ( $d_{90}$ ) is  $350\ \mu\text{m}$ . Currents last  
558 a few hours (2-4), and deliver sediment to the base of slope once every 10-20 years during a  
559 maximum regression that lasts 5-10 kyr (see Table 1 for an overview of conditions). Figure 3 displays

560 the default results of the SBE run with these input conditions. The velocity and concentration profiles  
561 of all simulated turbidity currents are stored by the SBE, but for simplicity only the profiles of a single  
562 simulated turbidity current are displayed as an example (Fig. 3a&b). This example simulation is  
563 picked from the characteristic turbidity currents whose maximum velocity is closest to the mean of  
564 all simulated maximum velocities. This procedure means that the displayed example profiles do not  
565 necessarily result from the mean boundary conditions. They may reflect, for instance, thicker or  
566 thinner flows that combined with changes in the other boundary conditions result in a maximum  
567 velocity that lies close to the mean of maximum velocities in all simulations.

568 The turbidity currents in this hypothetical system have a maximum velocity of  $\sim 3$  m/s, are highly  
569 stratified with a maximum concentration near the bed of  $\sim 6\%$ , transport  $\sim 15$  m<sup>3</sup> of sediment every  
570 second, which amounts to  $\sim 0.1$  km<sup>3</sup> of sediment per cycle (Fig. RefCase). These results will not be  
571 analyzed in detail, but serve as the reference to a) explore the sensitivity of the simulation results to  
572 uncertainty of the input conditions, and b) the response of the results to changing input conditions.

573





574

575 **Fig. 3:** SBE default results for the base case simulation [Table 1]. A&B) Velocity and concentration  
 576 profiles of a characteristic turbidity current in the base case system. Horizontal dotted line indicates  
 577 the mean input channel depth for reference. Note that the displayed example was thinner than the  
 578 mean thickness. C) Histogram of sediment flux ( $m^3/s$ ) through a characteristic channel cross section.  
 579 D) Histogram of sediment budget of the system over a full cycle of activity. Vertical white line  
 580 indicates the  $p_{50}$  of predicted sediment budgets, white dotted lines indicate  $p_{10}$  and  $p_{90}$ .

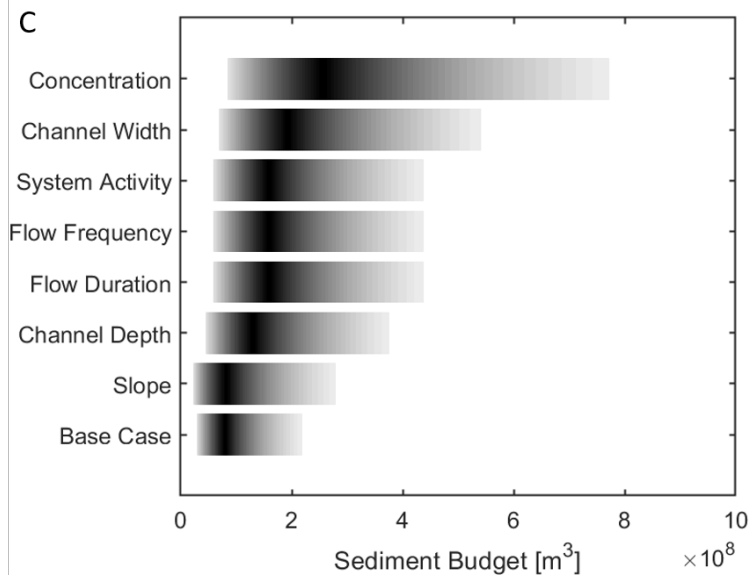
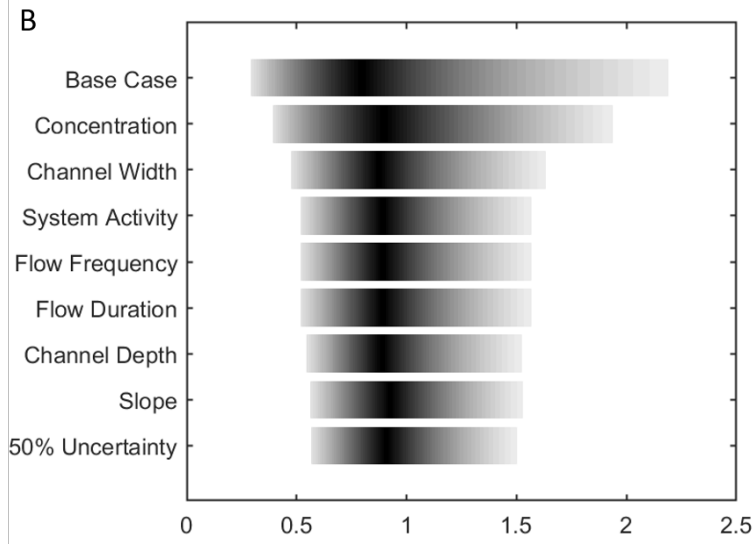
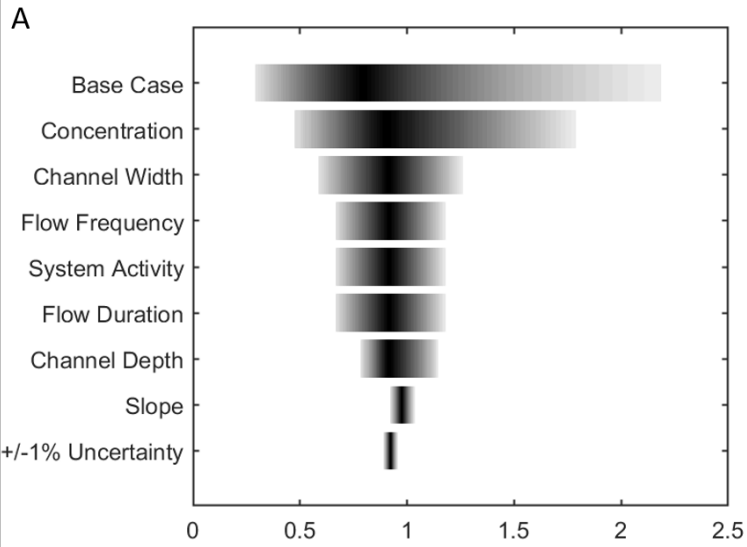
581

582 The sensitivity of the SBE to changes in input conditions is tested by reducing the uncertainty of all  
 583 input variables, apart from one, to +/-1% of the mean of the base case input range. The simulation is  
 584 repeated with the uncertainty of a single different variable reinstated each time. The sediment  
 585 budgets of all the simulations are displayed in order of descending spread of the predicted sediment

586 budgets (Fig. 4), in a so-called tornado diagram (Holbrook & Wanas 2014; Lin & Battacharya 2017).  
587 These diagrams reflect the sensitivity of the model output to the uncertainty of the variables used as  
588 input conditions. The average input sediment concentration comes out as the variable with most  
589 impact on the simulation results (Fig. 4a); most of the spread of the base case is maintained when all  
590 variables apart from the sediment concentration are set to range +/-1% around the mean of the base  
591 case input. Channel width also has a relatively large impact on the spread of the sediment budget  
592 results, but is a distant second to the sediment concentration parameter. The three temporal  
593 parameters in the SBE (flow duration, frequency and system activity) show an identical and moderate  
594 influence on the spread of the sediment budget. Channel depth, interestingly has a smaller impact on  
595 the total uncertainty. The insensitivity to uncertainty in slope of the system is striking: the spread of  
596 predicted sediment budgets is reduced to a narrow range while the slope is still varied from 1° to 2.5°  
597 (Fig. 4a). There is thus very little benefit to be gained from increasing the confidence levels of slope  
598 estimates. This is a somewhat unexpected result due to the importance generally attributed to slope  
599 in the literature (Kneller, 2003; Stevenson *et al.*, 2015; Pohl *et al.*, 2020).

600 Achieving uncertainty levels of +/-1% is unrealistic in natural turbidity current systems. Another  
601 tornado diagram is therefore produced for which uncertainties in all variables apart from one have  
602 been reduced by 50% (Fig. 4b). This diagram confirms the sensitivity ranking of variables that was  
603 found in Fig. 4a. It also shows that the spread in sediment budgets in most simulations is rather equal  
604 to that of the simulation where uncertainty in all variables has been reduced by 50% (Fig. 4b). This  
605 result indicates that it is acceptable for relatively high uncertainty to remain in one or two of the  
606 intermediate-sensitivity input parameters. There is little benefit in spending much effort on reducing  
607 that uncertainty of a single variable, because the spread in sediment budgets will remain similar even  
608 if it's uncertainty is reduced by 50%. The exception to this is the input sediment concentration: even  
609 if all other variables are set to a 50% reduction of uncertainty, the spread of results does not  
610 decrease much (Fig. 4b), which again points to the importance of uncertainty about sediment  
611 concentration in turbidity currents.

612 As a final exercise in this section, the base case is repeated with the input range doubled for one  
613 variable at a time. The duration, frequency, and system activity all have a linear relation with the  
614 sediment budget, and doubling these variables results in doubling of the simulated sediment budgets  
615 (Fig. 4c). Channel width and sediment concentration both have a nonlinear effect. The concentration  
616 again has the largest impact with the predicted sediment budgets quadrupling as a result of the  
617 doubled input range. Channel depth has a subdued effect, and doubling of the slope range from 1-  
618 2.5° to 2-5°, a dramatic increase in slope within the band-width of natural slope angles, merely has  
619 the effect of increasing the spread of predicted sediment budgets somewhat.  
620



622 **Fig. 4:** Tornado diagrams of sensitivity analyses of the SBE results. Base case conditions are given in  
623 Table 1. A) Uncertainty in all variables apart from 1 is reduced to +/-1% of the mean input of the base  
624 case. Uncertainty of all variables was reduced in the “+/-1% Uncertainty” scenario. B) Uncertainty of  
625 all variables apart from one was reduced to 50% of the uncertainty in the base case. Uncertainty of all  
626 variables was reduced in the “50% Uncertainty” scenario. C) Input range of a single variable was  
627 doubled compared to the base case. The gray scales changes from black for  $p_{50}$  to light gray for  $p_{10}$   
628 and  $p_{90}$ .

629

630

#### VALIDATION OF THE MODEL

631 We validate the SBE app here with examples of the smallest and largest scale turbidity currents on  
632 earth for which detailed data is available: laboratory turbidity currents and the 1929 Grand Banks  
633 turbidity current.

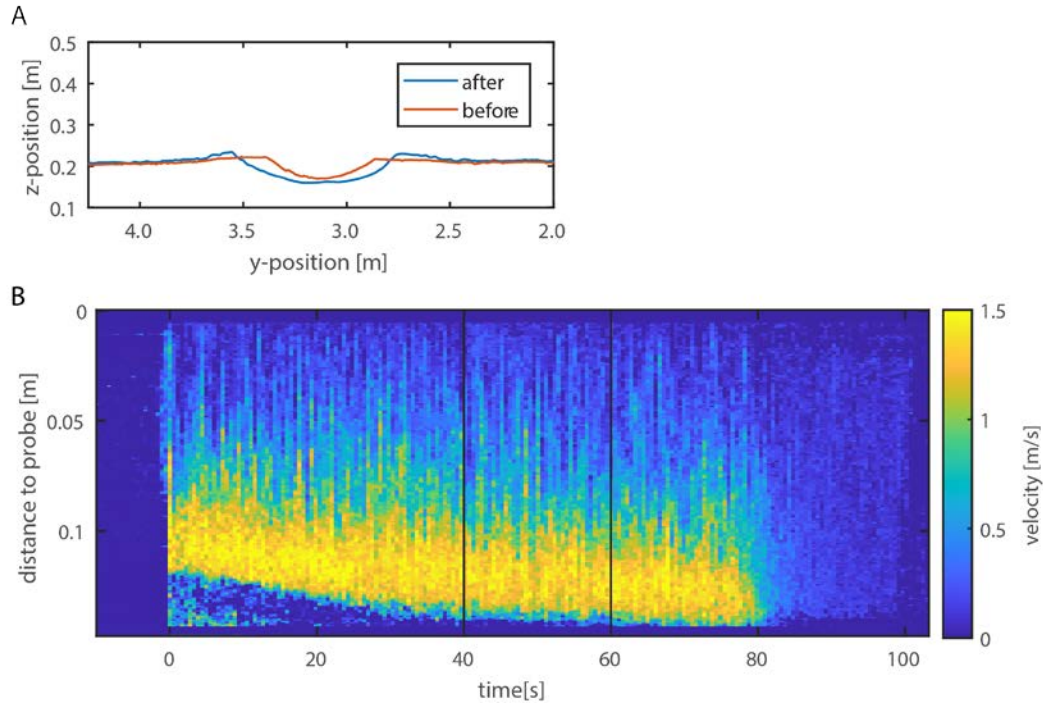
634

635

#### *Laboratory Turbidity Currents*

636 **Boundary Conditions** --- The model is tested on Run 3 of de Leeuw et al. (2018b). This  
637 experiment was selected because it displayed the least amount of in-channel and levee deposition of  
638 all the experiments reported in that paper. It was therefore most representative of a bypassing  
639 channel, indicative of the flow-channel size equilibrium discussed in section 2.3, above. In fact, the  
640 size of the pre-formed channel resulted in a phase of initial channel deepening and widening (Fig.  
641 5a), which indicates that the channel dimensions were smaller than the dimensions in equilibrium  
642 with the characteristic turbidity current initiated by de Leeuw et al. (2018b). The velocimetry data  
643 shows that channel deepening took place in the initial 40 seconds of the experiment, after which the  
644 channel thalweg stays at a constant elevation throughout the final 40 seconds of the experiment (Fig.  
645 5b). This is interpreted here to indicate that the initial erosive channel enlargement led to an  
646 equilibrium between the turbidity current and the channel dimensions. The channel dimensions used  
647 as input for the SBE are there for obtained from the digital elevation model of the topography

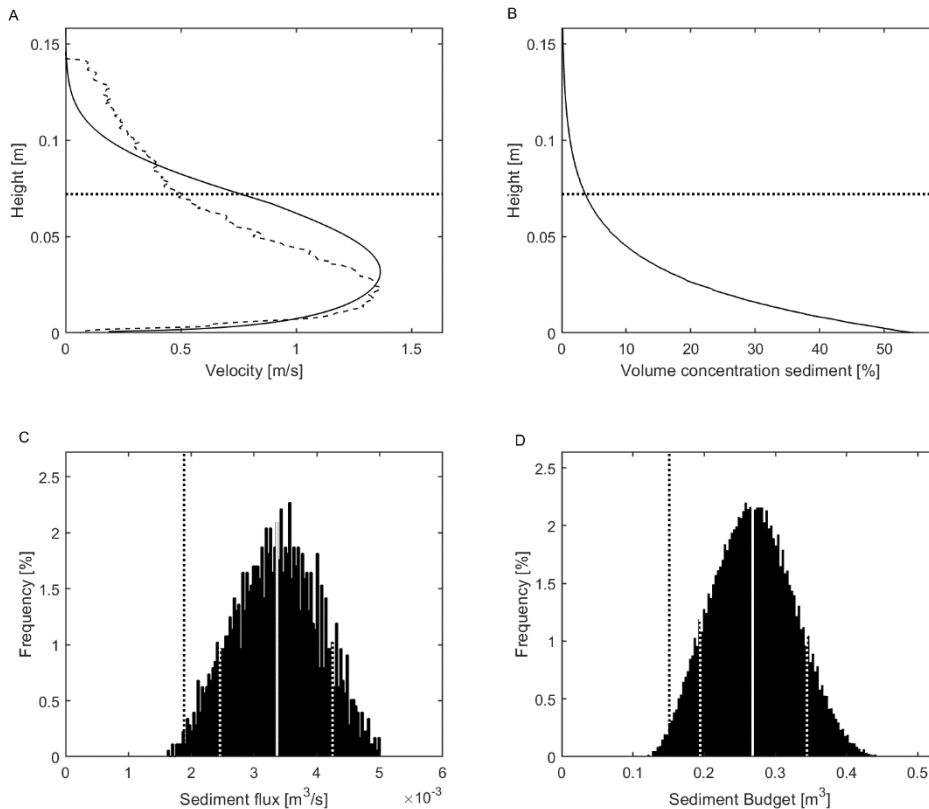
648 measured after the experiment. The full list of input conditions for the SBE are displayed in Table 1.  
649 The uncertainty ranges for the input conditions have been determined by applying an error margin of  
650 +/-10% to the best guess values, which is appropriate for controlled sedimentology experiments.



651 **Fig. 5:** A) Channel cross-sections measured before and after Run 3 of de Leeuw et al. (2018b). B)  
652 Velocity of the experimental turbidity current measured at the channel thalweg measured with an  
653 Ultrasonic Velocimetry Profiler (UVP). The distance from the high-velocity core of the turbidity current  
654 to the UVP probe increases during the first 40 seconds of the experiment, which indicates erosion of  
655 the channel thalweg. Vertical black lines indicate the 20 s averaging window used for validation of the  
656 SBE velocity profile.  
657  
658

659           **Results** --- The predicted velocity profiles match the UVP measurements quite closely (Fig.  
660 6a). The velocity maximum is predicted precisely (1.36 m/s). The elevation of the velocity maximum  
661 is predicted at a higher position in the SBE compared to the experimental measurements (3.2 cm vs.  
662 2.4 cm). Also, the velocity in the mixing layer was more asymmetrical in the experiment compared to  
663 the SBE velocity profile. The predicted concentration profile has elevated concentrations near the  
664 base and decreased concentrations towards the top compared to the average input concentration  
665 (Fig. 6b). The predicted basal sediment concentration reaches the maximum granular concentration  
666 due to the high bed shear stress. The actual experimental sediment budget does fall within the range  
667 of predicted values (Fig. 6c&d), albeit at the very low end of the distribution, around the first  
668 percentile value ( $p_{01}$ ). The  $p_{50}$  values of predicted flux and budget are 80% overestimated by the SBE  
669 compared to the actual experiment.

670



671

672 **Fig. 6:** Results for the SBE simulation of Run 3 of de Leeuw et al. (2018). A) Velocity profile resulting  
673 from the SBE (solid line); measured velocity profile (dashed line). Horizontal dotted line indicates  
674 channel confinement depth. B) Concentration profile resulting from the SBE. C) Simulated range of  
675 sediment flux. Black dotted line indicates sediment flux of the experiment ( $1.9 \cdot 10^{-3} \text{ m}^3/\text{s}$ ). White  
676 vertical line indicates the median of the reconstructed sediment fluxes ( $3.4 \cdot 10^{-3} \text{ m}^3/\text{s}$ ); dotted lines  
677 indicate 10<sup>th</sup> and 90<sup>th</sup> percentiles of reconstructions. D) Reconstructed sediment budget. Black dotted  
678 line indicates the amount of sediment supplied to the mixing tank in preparation of Run 3 of de Leeuw  
679 et al. (2018b;  $0.15 \text{ m}^3$ ). White vertical line indicates the median of the reconstructed sediment  
680 budgets ( $0.27 \text{ m}^3$ ); white dotted lines indicate 10<sup>th</sup> and 90<sup>th</sup> percentiles of simulated budgets.

681

682 **Evaluation** --- Estimations of the error margins of UVP measurements do not exist, but the  
683 prediction of the maximum velocity can clearly be qualified to be within the margin of this error. The  
684 elevation of the velocity maximum and the inability to capture the asymmetry of the mixing layer are  
685 here classed as mismatches of secondary importance. These discrepancies could point to the 2<sup>nd</sup>  
686 order importance of the density profile, which is assumed to be negligible in both the law of the wall  
687 (Eq. 2) and the plane mixing layer structure (Eq. 3) applied in the SBE. Improvements of the velocity  
688 profile function is not pursued here because even though this output is informative and interesting, it  
689 is merely a necessary step to obtain the key sediment flux output of the SBE.

690 The actual experimental sediment budget equals the 1<sup>st</sup> percentile value of the distribution of  
691 predictions, and the  $p_{50}$  of the predictions overestimates the sediment budget by 80%, which is  
692 within the factor of 2, the expected level of accuracy of any sediment transport flux estimations  
693 obtained from comparatively simple and tightly controlled open-channel flows (Chang, 1988). The  
694 very high predicted basal sediment concentrations are likely a major contribution to the  
695 overestimation of the sediment budget. The concentration profile was not measured by de Leeuw et  
696 al. (2018b), but concentrations obtained by siphoning similar turbidity currents in another set-up  
697 suggest that basal sediment concentrations reach ~30% (e.g. Pohl et al., 2020), not the 50+%



698 predicted by the SBE. Another major contributor could be the eroded sediment added to the  
699 turbidity current in excess of the budget supplied from the mixing tank, which is estimated to have  
700 supplied ~60 liters of sediment (an average of 3 cm erosion over a 0.8 m wide 4 m long channel  
701 section). Addition of this eroded sediment to the experimental sediment budget would raise it to ~0.21  
702 m<sup>3</sup>, just above the p<sub>10</sub> value of the simulated population. Furthermore, scrutiny of the logbook of the  
703 experimental procedure of the experiment that was simulated here also revealed that the volume of  
704 water supplied to the mixing tank could have been as much as 0.928 m<sup>3</sup>, and that 28 kg of sediment  
705 has been recorded to remain in the pump & pipe system that supplies the mixture to the Eurotank.  
706 While the sediment in the pipes lowers the experimental sediment budget slightly, in combination  
707 with the elevated water volume it implies that the actual experimental sediment concentration could  
708 have been as low as 15% instead of the intended 17%. The sensitivity analysis (Fig. 4c) suggests that  
709 this lower actual concentration would have a marked effect to decrease the SBE-predicted sediment  
710 budgets.

711 A number of improvements to the prediction could be pursued by tailoring the SBE more closely to  
712 the laboratory experiments. However, all such improvements would necessarily entail using more  
713 intricate boundary conditions, and go against the idea of the SBE as a robust tool to be used across a  
714 range of scales when information about the system is sparse. Furthermore, it is not very satisfying or  
715 useful to optimize a model for predictions at laboratory scale before investigating how it performs  
716 for real world cases. Fitting the SBE more closely to laboratory experiments will therefore not be  
717 pursued here. Instead we will investigate the validity of the SBE across scales by turning our attention  
718 to the largest turbidity current for which measurements are available: the 1929 Grand Banks  
719 turbidity current.

	Base Case	Eurotank Experiment	1929 Grand Banks Event
Channel Width [m]	200-400	0.82 +/-10%	23000 +/-10%
Channel Depth [m]	10-20	0.072 +/-10%	201 +/-10%
System Slope [°]	1-2.5	11 +/-10%	0.45 +/-10%
Thalweg grainsize (d <sub>50</sub> ; d <sub>90</sub> ) [*10 <sup>-6</sup> m]	150; 350	131,223	1250; 5000
Sediment Concentration [%]	0.2-0.6	17 +/-10%	Ref. 2.7-5.4 High 5.4 +/-10% Low 2.7 +/-10%
Current Duration [h]	2-4	80/3600 +/-10%	4-8
Current Frequency [-/yr]	0.05-0.1	1	1
System Activity [kyr]	5-10	0.001	0.001

720 **Table 1** Input parameters for the SBE simulations of a hypothetical base case, EuroSEDS experiments,  
721 and the 1929 Grand Banks turbidity current.

722

723 *Validation against the 1929 Grand Banks turbidity current*

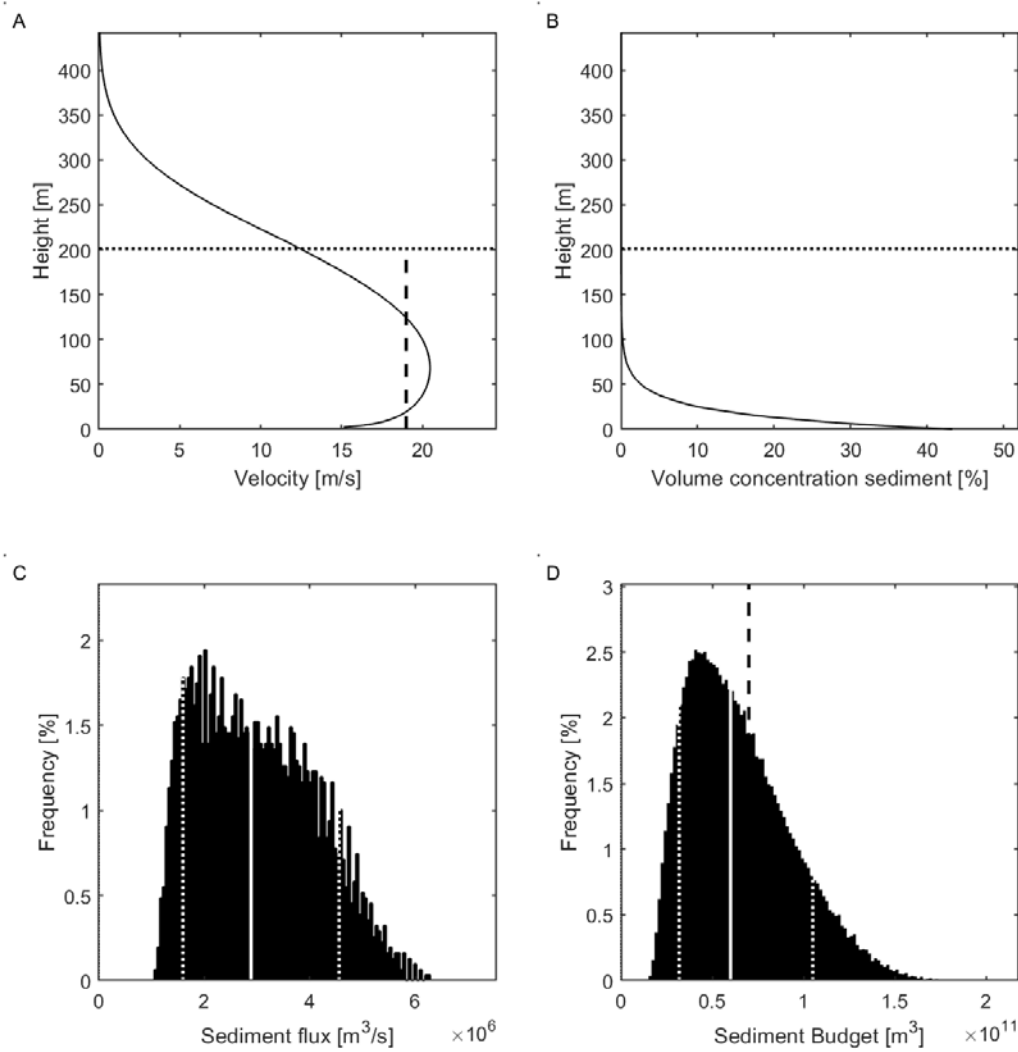
724 **Boundary Conditions** --- The 1929 Grand Banks turbidity current is the largest scale event, in  
725 terms of volume of sediment transported, for which data on bathymetry, flow velocity, flow  
726 thickness, and flow composition is available (Heezen & Ewing, 1952; Piper & Aksu, 1987; Piper *et al.*,  
727 1988; Hughes Clark *et al.*, 1990; Krastel *et al.*, 2016; Stevenson *et al.*, 2018). It has long been used as  
728 a testing ground for models of turbidity current dynamics (Kuenen, 1952; Plapp & Mitchell, 1960;  
729 Stevenson *et al.*, 2018). Insights from the 2015 RV Maria S. Merian cruise (Cruise No. MSM47; Krastel  
730 *et al.*, 2016; Stevenson *et al.*, 2018) are used here to constrain the SBE. The aim of this exercise is to  
731 validate the velocity and concentration results of the SBE and establish how the range of sediment  
732 budget estimates from the SBE relates to the estimated volume of 175-185 km<sup>3</sup> of the deposit that  
733 was formed on the Atlantic abyssal plane during this event (Piper & Aksu, 1987; Piper *et al.*, 1988).

734 The boundary conditions for the simulation of the Grand Banks turbidity current are set using a  
735 combination of parameters measured in the field and reconstructed flow properties such as  
736 sediment concentration (from Stevenson et al., 2018). Channel bathymetry at Transect 2 across the  
737 Eastern Valley provides constraints on flow thickness (201 m), channel width (23,000 m) and slope  
738 (0.45°). Cable breaks across this part of the slope measured the flow speed to be 19.1 m/s (Heezen &  
739 Ewing, 1952). From these data the depth-averaged sediment concentration of the flow was  
740 reconstructed between 2.7-5.4 % by volume (Stevenson *et al.*, 2018). Given these input conditions  
741 (Table 1), the SBE model outputs include a prediction of the overall sediment budget of the flow. This  
742 parameter is constrained by deposits mapped out in the field, whereby approximately 70 km<sup>3</sup> of  
743 sediment passed through Transect 2 of the Eastern Valley (Stevenson *et al.*, 2018). The rest of the  
744 175-185 km<sup>3</sup> deposit on the abyssal plane was transported along other flow-pathways on the Grand  
745 Banks continental slope.

746

747 **Results** --- First, we present model outputs using input conditions from Transect 2 (Table 1)  
748 with sediment concentrations of 2.7-5.4 % (reconstructed by Stevenson et al., 2018). The SBE model  
749 shows remarkable agreement with the observed and reconstructed properties of the 1929 Grand  
750 Banks deposit and flow (Fig. 7). The velocity profile of a representative simulated flow shows a  
751 velocity maximum being slightly higher than 20 m/s, which is consistent with the velocity of 19 m/s  
752 deduced from the timing of cable breaks (Fig. 7a). The concentration profile indicates a highly  
753 stratified dense basal flow with high concentrations (>10%) up to ~25m from the bed, overlain by a  
754 low-density cloud (Fig. 7b).

755 The predicted sediment flux through the channel at Transect 2 was  $\sim 3 \times 10^6$  m<sup>3</sup>/s ( $p_{50}$ ; Fig. 7c), an  
756 order of magnitude more than the water discharge of the Amazon, which is largest river on Earth by  
757 discharge. This flux is combined with an estimated 4-8 hour flow duration (Stevenson *et al.*, 2018).  
758 The model then predicts a  $p_{50}$  of deposit volume of 60 km<sup>3</sup> with a  $p_{10}$ - $p_{90}$  range between ~30 and  
759 ~100 km<sup>3</sup> (Fig. 7d).



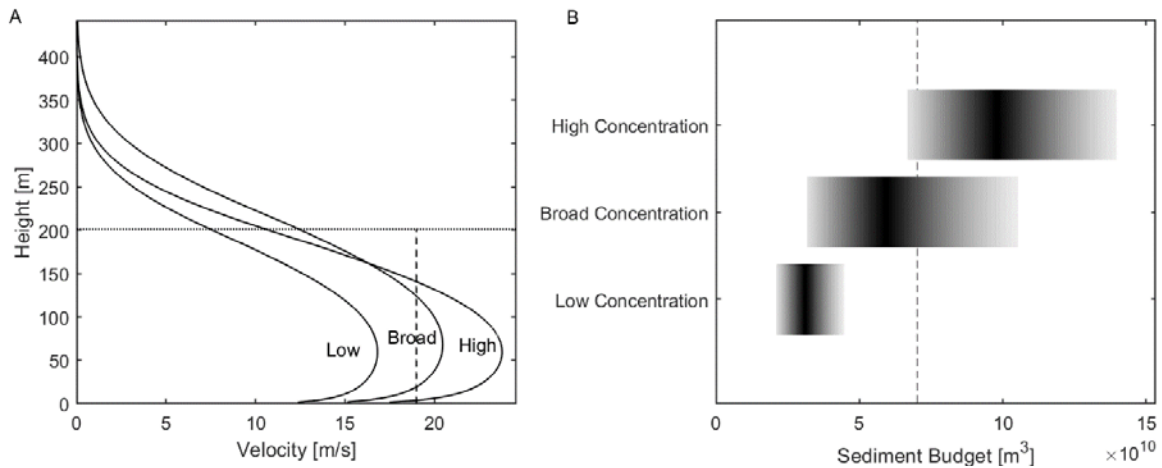
760

761 **Fig. 7:** SBE results of the Grand Banks 1929 turbidity current reconstruction. A&B) Representative  
 762 velocity and concentration profiles. Horizontal dotted line indicates flow thickness from Stevenson et  
 763 al. (2018). Vertical dashed line indicates velocity based on the timing of cable breaks (Heezen &  
 764 Ewing, 1952). C) Sediment flux. Vertical white line indicates the  $p_{50}$  of predicted sediment flux, white  
 765 dotted lines indicate  $p_{10}$  and  $p_{90}$ . D) Simulated sediment budget of the flow through Transect 2.  
 766 Vertical white line indicates the  $p_{50}$  of predicted sediment budgets, white dotted lines indicate  $p_{10}$  and  
 767  $p_{90}$ . Vertical black dashed line indicates estimated sediment budget of the Eastern Valley (70 km<sup>3</sup>).

768

769           **Evaluation** --- The input sediment concentration used had a broad range from 2.7-5.4%, and  
770 it was shown in the general sensitivity analysis that this can impact the SBE results to a great extent  
771 (Fig. 4). To explore the validity of these results we first present a sensitivity analysis on the sediment  
772 concentration parameter. Simulations were repeated with all parameters except the concentration  
773 kept the same; the concentration range was adjusted to the lower end and upper end of the  
774 estimates by Stevenson et al. (2018), each with a +/-10% uncertainty (Table 1). Low sediment  
775 concentrations of 2.7% result in flow velocities of ~15m/s (Fig. 8). In contrast, using a high sediment  
776 concentration condition of 4.9-5.9% results in flow velocities of ~23 m/s. The low and high end of  
777 Stevenson et al.'s (2018) concentration reconstructions thus result in under- and over-estimation of  
778 the Grand Banks velocity respectively. A concentration value midway between 2.7 and 5.4% (~4 %)   
779 produces flow velocities very similar to the values measured in the field (Fig. 7b). At the same time  
780 this result validates the velocity function of the SBE and the sediment concentration reconstruction  
781 by Stevenson et al. (2018). It is worthwhile emphasizing that the sediment concentration range was  
782 estimated by Stevenson et al. (2018) based on Chézy friction equations. This Chézy calculation output  
783 is used as an input constraint in the SBE simulation. The success of the present analysis should  
784 therefore not be seen as an independent validation against measurements only. Rather, the SBE is a  
785 corroboration of Chézy approaches (Middleton, 1966; Zeng *et al.*, 1991; Konsoer *et al.*, 2013;  
786 Stevenson *et al.*, 2018; Simmons *et al.*, 2020), while modelling the effects of the mixing layer through  
787 a technique rooted in fluid mechanics (Pope, 2000) rather than empirical coefficients. Stevenson et  
788 al. (2018) also estimated flow duration by dividing the sediment budget transported through the  
789 Eastern Valley by average velocity and concentration. This yields an estimated flow duration of 4-8  
790 hours. This flow duration was used in the SBE Grand Banks simulation (Table 1). The range of  
791 calculated sediment budgets is centered around the 70 km<sup>3</sup> observed in the field. Though this result  
792 seems remarkable it adds little to the validation of the velocity and concentration scales because the  
793 SBE procedure is simply the inverse of the duration calculations performed by Stevenson et al.  
794 (2018). It does illustrate, however, how the SBE quantifies the effects of remaining geologic

795 uncertainties explicitly by reconstructing a histogram of likely sediment budgets, with a  $p_{10}$ - $p_{90}$  range  
 796 of 30-100 km<sup>3</sup>, centered on the remarkable volume of 70 km<sup>3</sup> sediment transported through Transect  
 797 2 of the Eastern Valley during the Grand Banks event (Piper et al., 1988; Stvenson et al., 2018).  
 798



799 **Fig. 8:** A) Examples of characteristic velocity profiles obtained for low concentration estimate (slow  
 800 flow), broad concentration estimates (intermediate flow), and high concentration estimates (fast  
 801 flow). Vertical dashed line indicates cable break velocity. B) Simulated sediment budget ranges for  
 802 the three concentration ranges (see Table 1). Gray scale changes from black at  $p_{50}$  to light gray at  
 803  $p_{10}$  and  $p_{90}$ . Vertical dashed line indicates observed 70 km<sup>3</sup> sediment budget.  
 804

805  
 806 *Validation discussion: The smallest and the largest.*

807 Heezen and Ewing (1952), and Kuenen (1952) perceived the recording of the 1929 Grand Banks event  
 808 by cable breaks as a turbidity current experiment at the largest scale possible on Earth. The Eurotank  
 809 experiments represent the smallest scale at which turbidity currents can be studied with natural  
 810 sediments, a fluid with the viscosity of water at room temperature, and with a gravitational  
 811 acceleration of 1\*g. The SBE performs within standard acceptable accuracy of sediment flux  
 812 predictors in these validations in isolation. It is remarkable that the SBE achieves this level of success  
 813 at the smallest and largest scales possible on planet Earth, which are separated by 12 orders of  
 814 magnitude, without any changes in parameterizations or the equations themselves. There is  
 815 apparently no application on Earth that is outside the range of scales for the SBE, and no need to

816 apply it outside the range for which it is established. This robustness of the SBE encourages us to  
817 seek applications of the SBE in cases where it is predictive without the possibility of validation.

818

### 819 **APPLICATION OF THE SBE TO AN ANCIENT CHANNEL DEPOSIT IN OUTCROP**

820 The slope channels of the Cretaceous Tres Pasos Formation (Chile) have been extensively studied in  
821 the past decade (e.g. Hubbard et al., 2010; Macauley and Hubbard, 2013; Hubbard et al., 2014;  
822 Pemberton et al., 2016; Reimchen et al., 2016; Daniels et al., 2018; Hubbard et al., 2020) and provide  
823 an excellent testing ground for the application of the SBE to an ancient deep-water depositional  
824 system. The challenge of applying the SBE to ancient systems is making the distinction between the  
825 dimensions of channel fill deposits and the dimensions of the conduit that define their sediment  
826 fluxes. Channel fill sandstones are commonly compound deposits formed by multiple turbidity  
827 currents during alternating phases of erosion and deposition. Thus channel dimensions associated  
828 with a single turbidity current are uncorrelated to those of the channel fills. Hubbard et al (2014;  
829 2020) recognized this discrepancy and argued for using inter-channel erosion surfaces to make the  
830 distinction between sediment conduit dimensions (“storey” deposit) versus those of the composite  
831 channel element. The analysis below will investigate the significance of this interpretation for the  
832 projected sediment budget associated with the lifespan of a channel element. Additionally, an  
833 erroneous attribution of channel complex dimensions, which are commonly observed in seismic data  
834 (Samuel et al., 2003; Macauley & Hubbard, 2013), to the characteristic turbidity current scale will be  
835 investigated.

836

#### 837 *Boundary Conditions*

838 **Channel form dimensions** --- Channel form dimensions are estimated for the “M2” channel  
839 element, which is the focus of the recent paper by Hubbard et al. (2020). Three sets of dimensions  
840 are used as input conditions (Table Tres Pasos Scale): a) intra-channel element surfaces delineating  
841 channel storey deposits have vertical and horizontal scales of 2.5-6.5 m and ~200 m,

842 respectively (Hubbard et al., 2020); b) the primary channel surface delineating the M2 channel  
843 element deposit has a vertical scale of 17 m, and is 400 m wide (Hubbard et al., 202X); and c) channel  
844 elements are commonly grouped in channel complexes that are typically 800-1000 m wide, and 30-  
845 60 m thick (Macauley and Hubbard, 2013).

846

847 **System Slope** --- The M2 channel is part of the Figueroa clinothem (*sensu* Hubbard et al.,  
848 2010), which has an estimated paleorelief of ~1000 m. Daniels et al. (2018) estimated the paleo-slope  
849 at this position in the Figueroa clinothem at 0.7-0.9°.

850

851 **Grainsize** --- The axial channel-fill deposits of the Tres Pasos Formation slope channels are  
852 dominated by amalgamated, thick bedded, fine to medium-grained sandstones. Grainsize  
853 measurements on thin section images yielded a  $D_{50}$  of 200  $\mu\text{m}$  (de Leeuw, 2017). The  $D_{90}$  was  
854 measured as 400  $\mu\text{m}$ .

855

856 **Turbidity current duration** --- Tres Pasos Formation contains relatively small, slope channels  
857 with a length of 10s of km, and the flow duration is therefore set to 3-6 hours.

858

859 **Turbidity currents frequency and system activity** --- Hubbard et al. (2020) recognized  
860 evidence for approximately 500 turbidity current events in the terrace deposits on the margin of the  
861 M2 channel. For the purpose of the parameterization of the SBE input conditions, this event count is  
862 transformed into paired values of decadal recurrence times and 5kyr system activity.



	Scenario Storey	Scenario Element	Scenario Complex
Channel Width [m]	200+/-10%	400+/-10%	800-1000
Channel Depth [m]	2.5-6.5	17+/-10%	30-60
System Slope [°]	0.7-0.9	0.7-0.9	0.7-0.9
Thalweg grainsize (d <sub>50</sub> ; d <sub>90</sub> ) [µm]	200;400	200;400	200;400
Sediment Concentration [%]	0.2-0.6	0.2-0.6	0.2-0.6
Current Duration [h]	3-6	3-6	3-6
Current Frequency [-/yr]	0.1	0.1	0.1
System Activity [kyr]	5	5	5

863 **Table 2:** *Input conditions used to simulate characteristic turbidity currents at the storey, element, and*  
864 *complex scales in the Tres Pasos Formation.*

865

866

### *Results*

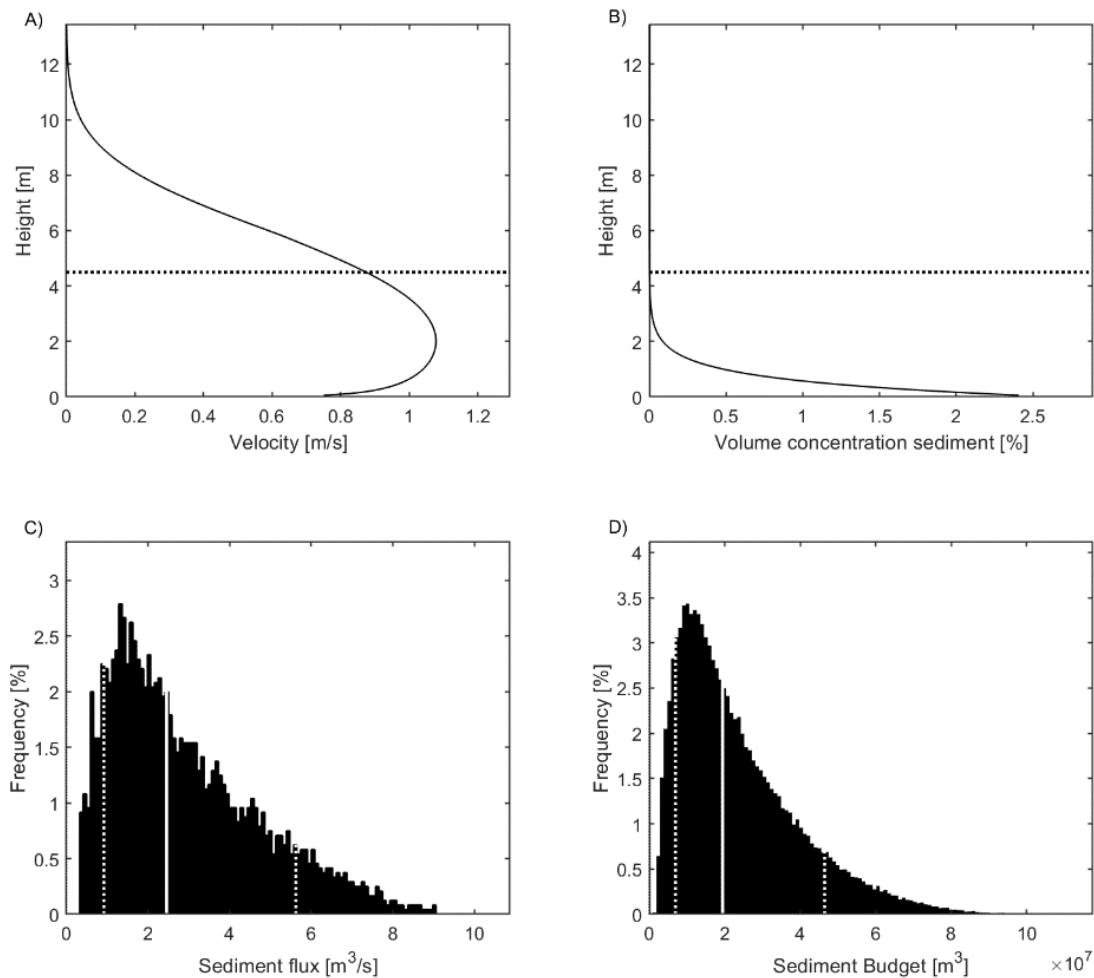
867 From the constraints of the field data, the SBE model predicts turbidity current structure and the  
868 sediment flux and budget for the different stratigraphic scales of channel organization. We here  
869 follow the interpretation by Hubbard et al. (2014; 2020) that the intra-element surfaces that  
870 delineate channel storeys are correlated to the scale of the characteristic turbidity currents that  
871 formed the compound channel-element deposit. The structure of these characteristic turbidity  
872 currents at the channel-storey scale is therefore discussed in most detail before addressing the  
873 implications of using channel-element and channel-complex scales in estimating the systems  
874 sediment flux/budget.

875

876           **Turbidity Current Structure** --- Turbidity currents are simulated to flow at a maximum  
877 velocity of just over 1 m/s (Fig. 9a). The velocity maximum of the single simulation presented in this  
878 figure is located approximately 2 m above the bed, roughly half of the mean channel-storey surface  
879 elevation. The velocity decreases until it approximates 0 m/s at 10-12 m above the channel floor.  
880 The sediment concentration profile displays strong stratification, with most sediment suspended  
881 near the base of the flow (Fig. 9b). The basal sediment concentration of the example simulation is 2.5  
882 % by volume, yet at the elevation of the maximum velocity (2 m), the sediment concentration has  
883 decreased to less than 0.1 % by volume. The mean of the basal sediment concentrations for all 2401  
884 simulated characteristic turbidity currents is 3.0 % by volume, roughly 10 times the depth-averaged  
885 sediment concentration used as input condition (0.2-0.6 % vol.).

886

887           **Sediment flux and budget** --- The simulated sediment fluxes through the channel cross  
888 section are 0.9-2.5-5.8 m<sup>3</sup>/s (p<sub>10</sub>-p<sub>50</sub>-p<sub>90</sub>; Fig. 9c). This amounts to a sediment budget of 6.6\*10<sup>6</sup>-  
889 2.0\*10<sup>7</sup>-4.5\*10<sup>7</sup> m<sup>3</sup> (p<sub>10</sub>-p<sub>50</sub>-p<sub>90</sub>) over the full evolution of the 500 turbidity currents that formed the  
890 channel-element deposit (Fig. 9d).

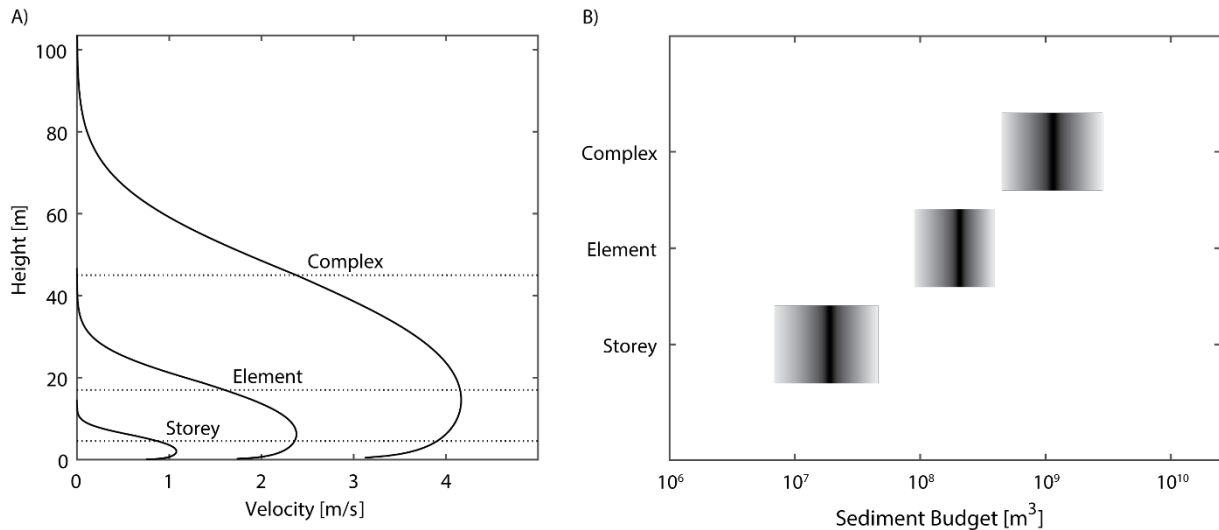


891  
 892 **Fig. 9:** SBE-results for characteristic turbidity currents related to storey-dimensions in Tres Pasos  
 893 Formation slope channels. A) Velocity profile of one typical simulation, dotted line indicates mean  
 894 storey-surface depth. B) Sediment concentration profile of one typical simulation. C) Histogram of  
 895 calculated sediment fluxes through the channel cross-section per second. Vertical white line indicates  
 896 the  $p_{50}$  of predicted sediment flux, white dotted lines indicate  $p_{10}$  and  $p_{90}$ . D) Histogram of cumulative  
 897 sediment budget of 500 characteristic turbidity currents. Vertical white line indicates the  $p_{50}$  of  
 898 predicted sediment budgets, white dotted lines indicate  $p_{10}$  and  $p_{90}$ .

899  
 900 **Storey – element – complex** --- The larger dimensions of the composite channel-element and  
 901 channel-complex scales lead, if associated with characteristic turbidity currents, to much larger flows  
 902 and sediment budgets (Fig. 10). The simulated flow velocities increase to 2.5 and 4 m/s, respectively  
 903 (Fig. 10a). This combines with the much thicker column of suspended sediment to accumulate

904 sediment budgets that are in the order of  $10^8 \text{ m}^3$  for the element-dimension simulations and  $10^9 \text{ m}^3$   
905 ( $1 \text{ km}^3$ ) for the complex-dimensions simulations. Rather than the  $10^7 \text{ m}^3$  simulated when storey  
906 dimensions are used to simulate the characteristic turbidity currents (Fig. 10b).

907



908

909 **Fig. 10:** A) Example characteristic turbidity currents resulting from storey dimensions, element  
910 dimensions, and complex dimensions.

911

912

### Evaluation

913

**Highly stratified turbidity current structure** --- The majority of the sediment in the

914

characteristic turbidity currents simulated for the Tres Pasos Formation M2 channel is suspended

915

near the base of the flow. The remainder of what would typically be viewed as “the turbidity current”

916

(say from 2-12 m above the bed), is relatively devoid of sediment. This result corroborates recently

917

emerging measurements and perspectives on the concentration structure of turbidity currents.

918

Measurements of sediment concentration with Acoustic Doppler Current Profilers (ADCPs) indicate

919

that sediment concentrations in the bulk of the recorded flows are indeed very low (~0.02 %;

920

Azpiroz-Zabala et al., 2017; Simmons et al., 2020). ADCPs have generally been deployed above

921

submarine channels and canyons, to monitor turbidity currents downwards, which gives interference

922

and resolution problems near the bed. These measurement difficulties mean that the 2 m thick part

923 with elevated sediment concentrations depicted in Fig. 9b would typically be poorly resolved at most  
924 in ADCP data (Simmons et al., 2020). This would obscure the fact that the turbidity current is a very  
925 dilute cloud that is driven mainly by a dense basal layer (Cartigny et al., 2013; Paull et al., 2018;  
926 Simmons et al., 2020).

927 It is interesting to discuss here how stratification of concentration profiles is included in depth-  
928 averaged modelling workflows of turbidity currents, an approach that is more complicated than the  
929 simplified approach of the SBE. Parker (1982) proposed a simple measure for stratification in depth-  
930 averaged modelling of turbidity currents: the ratio between the near-bed sediment concentration  
931 and the depth-averaged sediment concentration,  $r_o$ , a notation that has mostly been followed by the  
932 many papers following the depth-averaged approach to modelling turbidity currents (for recent  
933 examples see Halsey et al., 2017; Bolla Pittaluga et al., 2018; Traer et al., 2018). On its first  
934 appearance,  $r_o$  was evaluated as a function of grain size with the Rouse equation for suspended  
935 sediment concentration (Parker, 1982). The Rouse equation was not derived for turbidity currents,  
936 but for open channel flow (Rouse, 1938). Even though it has been shown to be a reasonable  
937 approximation for fine grained suspended sand, and in general for the sediment suspended in the  
938 lower part of the flow, it mispredicts suspension of mud, especially in the upper part of the flow,  
939 because it neglects mixing with the ambient water in the mixing layer (Eggenhuisen et al., 2019).  
940 Parker et al. (1986) dropped reliance on the Rouse equation and instead advised a value of  $r_o=1.6$ ,  
941 while Garcia (1994) advised  $r_o=2.0$ , both based on a compilation of concentration profiles obtained  
942 from weakly-stratified, small-scale laboratory experiments. These low values for  $r_o$  are used in  
943 modelling studies to this date (Traer *et al.*, 2012; Halsey *et al.*, 2017; Bolla Pittaluga *et al.*, 2018).  
944 Dorrell et al. (2014) attempted to validate depth-averaged simulations with unstratified “top-hat”  
945 concentration profiles (with  $r_o=1$ ) and weakly-stratified profiles against measurements of gravity  
946 currents in the Black Sea. The unsatisfactory results of their validation led Dorrell et al. (2014) to  
947 hypothesize that field-scale flows have larger degrees of stratification that are poorly represented by  
948 the stratification observed in small scale experiments. Recent acoustic measurements of sediment

949 concentrations in the Congo Canyon indicate that  $r_o$  was  $\sim 10$  in the turbidity currents reported by  
950 Azpiroz-Zabala et al. (2017) and Simmons et al. (2020). The SBE results presented here are consistent  
951 with this elevated stratification in field-scale turbidity currents compared to laboratory turbidity  
952 currents, with  $r_o \sim 10$  for the Tres Pasos simulations, and  $r_o \sim 11$  for the Grand Banks simulation (Figs.  
953 Experiment, Tres Pasos, Grand Banks).

954

955 **Sediment flux and budget of the M2 channel element** --- The simulated sediment flux  
956 through the M2 channel (Fig. 9) is comparable to the sediment flux of the turbidity currents in the  
957 Congo Canyon reported by Azpiroz-Zabala et al. (2017). The total sediment budget of the M2 channel  
958 element is comparable to the “X-channel” on the Niger slope ( $1.7\text{-}5.2 \times 10^7 \text{ m}^3$ ; Jobe et al., 2018),  
959 though this was delivered to the lobe by a smaller number (20-50) of turbidity currents with a  
960 centennial recurrence time, rather than the 500 events of the M2 channel. The M2 sediment budget  
961 is smaller than the volumes of other Quarternary fans evaluated in Jobe et al. (2018), which are  
962 typically order  $10^9 \text{ km}^3$  with event counts varying from 10-700. This comparison shows that the  
963 reconstructed sediment flux and budget for the M2 channel are within the bandwidth of values  
964 measured in other systems, though on the lower part of this bandwidth. This is consistent with the  
965 suggestion by Jobe et al (2018) that smaller volumes are associated with intraslope and base-of-slope  
966 channels. A consideration of stratigraphic hierarchy could also explain the modest sediment budget  
967 predicted for the M2 channel element. Though it is not entirely clear whether lobe elements (Prélat  
968 *et al.*, 2009) can be correlated one-to-one with a single, coeval channel element (Cullis *et al.*, 2018), it  
969 is interesting to observe that the predicted sediment budget for the M2 channel compares very well  
970 with the volume estimates of lobe elements compiled by Prélat et al. (2010). This point will be  
971 considered further in the section below.

972

973 **Storey – Element – Complex – Fan** --- Constraining the SBE with different hierarchical scales  
974 leads to disparate distributions of predicted sediment budgets (Fig. 10). The  $p_{10}\text{-}p_{90}$  ranges of the 3

975 sets of simulations do not overlap. Each step upward in dimensions of the assumed  
976 contemporaneous channel form results in roughly an order of magnitude increase in predicted  
977 sediment budget. Hubbard et al. (2014; 2020) have argued extensively for the association between  
978 intra-channel element surfaces and formative turbidity current processes based on facies analyses.  
979 The larger channel-fill deposits recognized in single channel elements are formed by a compound  
980 evolution of erosion and deposition, akin to “the fluvial valleys that never were” of Strong and Paola  
981 (2008; Hubbard et al., 2020). Association of channel element thickness with formative turbidity  
982 current flows would lead to much thicker (17 m vs 2.5-6.5 m) and faster flow (~2.5 m/s vs. ~1 m/s),  
983 which combines to yield an order of magnitude larger sediment budget over the 500 turbidity  
984 currents constituting the lifespan of the M2 element. Multiple channel elements are commonly  
985 stacked consistently into channel complexes (e.g. McHargue et al., 2011; Macauley and Hubbard,  
986 2013). In our preferred interpretation, the sediment budget for channel complexes is obtained by  
987 multiplying the budget based on intra-channel surfaces (channel storey dimensions) by the typical  
988 count of elements in a complex. Macauley and Hubbard (2013) mapped 18 channel elements in the  
989 three channel complexes that form the lower half of the Figueroa clinotherm. This suggests a typical  
990 sediment budget during one channel complex evolution of  $\sim 1 \times 10^8 \text{ m}^3$  ( $p_{50}$ ), much less than the  
991 volumes predicted if the complexes themselves were erroneously associated with formative turbidity  
992 currents ( $p_{50} = 1.2 \times 10^9 \text{ m}^3$ ). This illustrates the consequences of erroneously relating channel fill or  
993 complex dimensions to the sizes of their formative flows. It also emphasizes that careful  
994 interpretation of stratigraphy matters a great deal for accurate estimation of primary aspects of the  
995 system, such as the order of magnitude of sand transported down-dip. This is particularly important  
996 in large-scale subsurface datasets that can lack resolution to map individual elements.  
997 Extrapolation of the sediment budget to the entire sand-rich package of the Figueroa clinotherm at  
998 the Laguna Figueroa localities (Macauley and Hubbard, 2013; Hubbard et al., 2014; Pemberton et al.,  
999 2016; Hubbard et al., 2020) yields a total SBE-derived turbidity-current sediment budget of order 1  
1000  $\text{km}^3$ . This volume would have been deposited during an unconstrained subsidiary phase within an  $\sim 2$

1001 Myr stratigraphic interval duration (Daniels et al., 2018). The depositional body formed at this largest  
1002 timescale could appropriately be called a fan. This SBE volume estimate is an entry into the suite of  
1003 source-to-sink metric correlations available from literature (Somme *et al.*, 2009b; a). A 1 km<sup>3</sup> volume  
1004 for the Figueroa clinothem fan could correlate to a fan length of 20-150 km, and a fan area of order  
1005 1000 km<sup>2</sup> (Somme *et al.*, 2009b).

1006

1007

## GENERAL DISCUSSION

1008

1009

### *An Extra Tool in the Source-to-Sink Toolshed*

1010 Estimations of sediment budgets in submarine depositional systems is interesting in its own right, but  
1011 can also form an inroad into a broader understanding of the setting of the system in a source-to-sink  
1012 analysis (Jobe et al., 2018). An important aspect of source-to-sink analyses is that metrics obtained  
1013 for different segments can be correlated to each other because regional plate tectonic and climatic  
1014 conditions ensure regulate consistency within a system (Somme *et al.*, 2009b; a; Walsh *et al.*, 2016).  
1015 By predicting metrics of basin-floor lobes from base-of-slope channel metrics the SBE intrinsically  
1016 correlates between the deep-marine segments of the chain of sediment transport. Furthermore, the  
1017 reconstructed fan volume, length, and area can be used to estimate a correlated slope length  
1018 (Somme *et al.*, 2009a; 2009b). The estimated slope length for the Tres Pasos Formation example  
1019 analysed above would be kilometers to tens of kilometers, which is consistent the stratigraphic  
1020 reconstructions of Daniels et al. (2018). Dimensions of the shelf-staging area (Somme et al., 2009a)  
1021 can be evaluated against the depositional style of coeval shelf-top delta deposits of the Dorotea  
1022 Formation (Romans *et al.*, 2011; Daniels *et al.*, 2018). And correlated long-term deposition rates of  
1023 order 10<sup>6</sup> t/yr (Somme *et al.*, 2009a) can be used to evaluate the nature of river catchment areas that  
1024 supplied sediment from the Andes into the retro-arc foreland basin (Romans *et al.*, 2011).  
1025 Sediment budget estimations are a rapidly evolving topic in sedimentary system science. It has been  
1026 developed for the sediment budget coming from continental catchment areas over decadal



1027 timescales in the BQART model (Syvitsky & Milliman, 2007; Somme *et al.*, 2011; Helland-hansen *et*  
1028 *al.*, 2016), and for the geological sediment budget in fluvial systems using the fulcrum approach  
1029 (Holbrook & Wanas, 2014; Bhattacharya *et al.*, 2016; Lin & Bhattacharya, 2017; Sharma *et al.*, 2017).  
1030 The fulcrum method perceives a fluvial channel cross section as the pivot between the sediment load  
1031 received from the up-stream domain and transmitted to a downstream domain. It analyzes the  
1032 relation between local channel-fill deposit architecture and this expected sediment throughput. The  
1033 SBE has a nearly identical philosophy to the fulcrum approach, but applied to submarine channel-  
1034 cross sections. Indeed, the relation between channel deposit architecture and the formative turbidity  
1035 current processes that were once active is critical in determining the sediment budgets (see section  
1036 6.3, above). Estimations with as many different tools as possible are combined in an ideal source-to-  
1037 sink study. Where possible, triple assessments with BQART on catchment area budget, the fulcrum  
1038 approach for the fluvial segment, and the SBE for the deep-marine segments will result in a  
1039 consistency check that can confirm the source-to-sink understanding of a system. In this sense, the  
1040 SBE should be regarded as a tool in the growing toolshed of source-to-sink studies.

1041

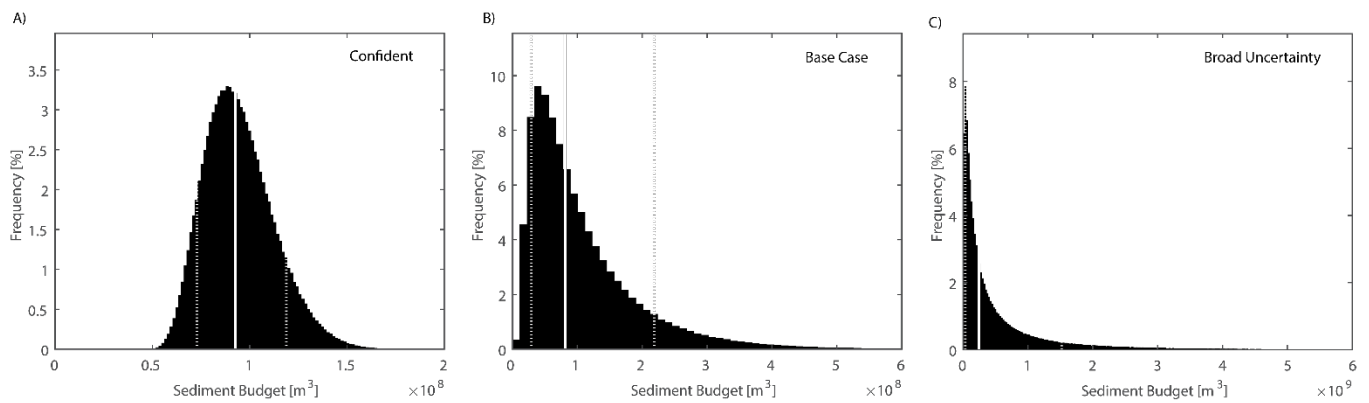
#### 1042 *Model functionality and complexity*

1043 **Functionality** --- The EuroSEDS-SBE is an example of simplified modelling where much of the  
1044 hydraulic complexity is hidden from the intended users (marine and sedimentary geologists) because  
1045 it could lie outside their immediate area of expertise. The simplicity of the tool presented here allows  
1046 computation of  $10^4$  turbidity currents within seconds on a standard desktop computer. This makes  
1047 the tool suited to consider multitudes of scenarios, resulting in the probability distribution function  
1048 of sediment fluxes into the deep oceans. Also, its computational efficiency lends itself to running  
1049 multiple simulations to test different geological perspectives, and the overall sensitivity of the  
1050 system. The benefit of such a rapid interaction is that the geologist gains immediate insight into the  
1051 consequence of different geological models for the probability distribution of predicted sediment  
1052 budgets. There is no overstating of the importance of sensible geological interpretations of the

1053 stratigraphic observations of a system. The Tres Pasos Formation evaluation shows that  
1054 interpretations of stratigraphic hierarchy are a primary control the scale of sediment budget  
1055 estimations. An even more fundamental point is made here by comparing budget histograms of  
1056 simulations with different uncertainty bounds (Table 3). The middle scenario represents the base  
1057 case used earlier to evaluate the basic structure of the SBE results and perform a sensitivity analysis.  
1058 The minimum and maximum bounds of ranges of input conditions were set to differ by a factor of 2-3  
1059 in that scenario. This resulted in a log-normal distribution of estimated sediment budgets (Figs. 3d &  
1060 11b). An over-confident geologist may ascertain uncertainty bounds of +/-10 %, which is normally  
1061 only possible under controlled laboratory conditions or in modern systems with high-fidelity  
1062 monitoring. This over-confidence leads to sediment budget predictions that approaches a normal  
1063 distribution, closely centered around the  $p_{50}$  (Fig. 11a). Finally, a scenario with broad uncertainty (a  
1064 factor 5 difference between minimum and maximum input conditions) results in an exponential  
1065 distribution with the highest probability being that the sediment budget is small, but very large  
1066 values also considered a possibility (Fig. 11c). These results demonstrate that the degree of  
1067 geological uncertainty is directly linked to the shape of the Probability Density Function (PDF) of the  
1068 system's sediment-budget estimations. It is worth noting that the shape of these PDFs are not  
1069 discrete, but transition into each other with growing levels of uncertainty. This implies that the  
1070 distributions are in fact all realizations of a single family of PDFs such as the binomial function or  
1071 Poisson function, which are two and one-parameter functions respectively. The premise is then that  
1072 it should be possible to parameterize the distribution of sediment budgets directly from the  
1073 boundary conditions, without the need of the Monte Carlo realizations of the SBE. This mathematical  
1074 exercise is not pursued herein.

1075 As an ultimate test of geological uncertainty, a simulation was run with input parameters set to  
1076 minimum and maximum values that cover most of the submarine literature. The resulting predictions  
1077 of sediment budgets were, perhaps unsurprisingly, that any amount of sediment might have gone  
1078 through these channels, yet that the most likely amount converges to nothing. Process-based

1079 prediction of sediment budget is thus not possible in absence of geological constraints on the model.  
 1080 This insight justifies continued efforts by the sedimentological community to try to understand the  
 1081 expression of turbidity current processes in the stratigraphic record. It also underscores the need for  
 1082 modelers and stratigraphers to engage in integrated projects. This should motivate the research  
 1083 community to strive for integrated studies with research teams involving both experts in stratigraphy  
 1084 and sediment transport processes.



1085

1086 **Fig. 11:** Sediment budget histograms for scenarios with decreasing confidence of interpretation.

1087 Vertical white line indicates the  $p_{50}$  of predicted sediment budgets, white dotted lines indicate  $p_{10}$  and

1088  $p_{90}$ . A) Confident levels of uncertainty with  $\pm 10\%$  ranges around a mean estimates of input

1089 conditions. B) The base case scenario with factor 2-3 differences between minimum and maximum

1090 inputs. C) Broad uncertainty with a factor 5 difference between minimum and maximum inputs.

	Scenario Confident	Scenario Base Case	Scenario Broad Uncertainty
Channel Width [m]	300 +/-10%	200-400	100-500
Channel Depth [m]	15 +/-10%	10-20	6-30
System Slope [°]	1.75 +/-10%	1-2.5	0.5-2.5
Thalweg grainsize (d <sub>50</sub> ; d <sub>90</sub> ) [µm]	150; 350	150; 350	150; 350
Sediment Concentration [%]	0.4 +/-10%	0.2-0.6	0.2-1.0
Current Duration [h]	3 +/-10%	2-4	2-10
Current Frequency [- /yr]	0.075 +/-10%	0.05-0.1	0.03-0.15
System Activity [kyr]	7.5 +/-10%	5-10	2-10

1091 **Table 3:** *The input conditions used to illustrate the effect of scenario confidence on predicted downdip*  
1092 *sediment volumes.*

1093

1094 **Complexity** --- While the SBE results are consistent with known cases at the largest and  
1095 smallest scales, the simulated flow structures in fact differ for the different scales (Fig. 6 vs. 7 & 9).  
1096 Specifically, the real world flows are more stratified at their base, meaning that the near-bed  
1097 gradients in suspended sediment concentration are larger in nature than in small scale laboratory  
1098 experiments. Another striking feature is that the SBE captures the similarity of scale in flow velocity  
1099 between real world (Tres Pasos) and experimental flows (order 1 m/s), despite the 2 orders of  
1100 magnitude difference in flow thickness. The fact that the SBE produces varying turbidity current  
1101 structures at varying scales is a sign that while it is a simple model, it is still complex enough to yield  
1102 results that cannot be foreseen and that fulfill the essential requirement of any model: we can learn  
1103 something new about the process from the model results.

1104 Empirical relations obtained by fitting small-scale experimental data cannot readily be extrapolated  
1105 to full field scale, because there is always the concern of extrapolating beyond the parameter space  
1106 for which the relation was originally obtained. Understanding of the physical processes, however, can  
1107 be based on small scale experiments, because the equations that describe the physical process can  
1108 yield different predictions at different scales. This is illustrated by the ability of the SBE to simulate  
1109 strongly stratified, high- $r_o$  turbidity currents at field scale while many of the ideas were justified from  
1110 scientific studies of small scale experiments with poorly stratified flows. It further demonstrates that  
1111 the aim of an experimental study in sedimentology can, and should be to learn more about nature,  
1112 not to learn more about the laboratory. We suggest that researchers modelling turbidity currents at  
1113 the full natural scale consider highly stratified flows with  $r_o \sim 10$ , in future work, rather than the  
1114 customary weakly stratified values of 1.6-2.0. Better still, since the input conditions of the SBE are a  
1115 limited subset of the boundary conditions required for depth-averaged modelling of turbidity  
1116 currents, such models could *a priori* query the SBE to obtain an estimate for  $r_o$ . These considerations  
1117 are an illustration of how more simple models can be used to direct more complex models to more  
1118 relevant segments of their parameter space, and how model integration between simple and more  
1119 complex models can improve the relevance of simulations performed.

1120 More complex modelling workflows exist for turbidity-current research that addresses questions  
1121 beyond bulk sediment budgets. It is tempting to select one of these more complex approaches in the  
1122 pursuit of higher-fidelity results. However, a potential pitfall is that more intricate model systems are  
1123 in practice associated with more parameters and variables and will therefore require the user to set  
1124 more intricate and precise boundary conditions, i.e. to be more knowledgeable about the system *a*  
1125 *priori*. This is a problem especially in ancient systems, where parameters such as bathymetry can  
1126 have a controlling effect on modelled turbidity currents, yet are essentially unresolved at the  
1127 resolution needed for high-fidelity simulations (Aas *et al.*, 2010). The model presented in this paper  
1128 has purposefully been designed with many simplifications, so that it can serve as the first, quick,

1129 check of a system's range of parameters, either as the final stage in sediment budget estimation  
1130 workflows, or ahead of more concerted modelling efforts with higher-fidelity modelling approaches.  
1131 The benefits of the simplified modeling approach of the SBE that have been emphasized in this  
1132 discussion do not preclude meaningful future extensions of the model. One desirable extension could  
1133 be to include physics-based modelling of the concentration profile, the shape of which is now  
1134 included with a crude exponential equation; another is the incorporation of grain-size distributions  
1135 within the concentration profiles. Another useful added complexity could be distinction between  
1136 flow structure and sediment flux in short duration, dense, thin, fast, frontal cells and extended (in  
1137 time), dilute, quasi-steady phases that have recently been described in monitoring studies (Azpiroz-  
1138 Zabala et al., 2017; Simmons et al., 2020; Wang et al., 2020). These different phases of events could  
1139 have different roles in the sediment fluxes along deep-marine systems, while the initial version of the  
1140 SBE presented here assumes a single, steady flow structure during the entire event duration. Such  
1141 extensions of the SBE, however, should not come at the expense of the core virtues of the SBE as  
1142 called for by Somme and Martinsen (2017): a simple, quantitative model, which reflects natural  
1143 variability and can be applied to ancient systems.

1144

1145

## CONCLUSIONS

1146 We presented the Sediment Budget Estimator, a simplified, robust model that links the flow  
1147 structure of turbidity currents to observable submarine channel characteristics. The SBE uses this  
1148 structure for stochastic first order predictions of sediment fluxes and budgets in channelized  
1149 turbidity current systems. The model has been structured such that all necessary input conditions  
1150 can be obtained from geological or oceanographic observations or published analogue datasets.  
1151 A sensitivity analysis reveals that fundamental uncertainty about the sediment concentration of  
1152 turbidity currents has the largest impact on variability of the results. Channel width also has a  
1153 marked effect. Aspects of timing of turbidity currents (recurrence time, duration of individual flows,  
1154 and duration of the geological activity of the system) all have linear influences on uncertainty.

1155 Channel depth is less influential and the slope of the system has a surprisingly modest effect on the  
1156 results.

1157 The SBE is successfully validated against small scale laboratory experiments and the 1929 Grand  
1158 Banks turbidity current, with sediment budgets that differ by 12 orders of magnitude.

1159 Application of the model to slope-channel deposits of the Cretaceous Tres Pasos Formation  
1160 demonstrates the potential for paleo sediment-budget estimations. Intra channel-deposit surfaces  
1161 with a vertical amplitude of 2.5-6.5 m are associated with formative turbidity currents. Alternative,  
1162 less likely, associations between formative currents and channel element or channel complex scales  
1163 yield budget estimates that are 1 or 2 orders of magnitude too large, respectively. The estimates of  
1164 sediment budget for the lifespan of a single channel element offer an inroad into estimation of lobe  
1165 element, lobe, and fan volumes. These can in turn be correlated to metrics of the slope, shelf, and  
1166 catchment segments of the source-to-sink system. In such a comprehensive source to sink analysis  
1167 the SBE can be applied in tandem with existing sediment budget estimators for catchment areas and  
1168 fluvial systems, such as BQART and the Fulcrum approach for fluvial paleohydrology. As such, the SBE  
1169 represents a new tool in the growing toolshed of source-to-sink studies of sedimentary systems.

1170 Application of the SBE to submarine channels and their deposits in modern sea-floor settings,  
1171 geological outcrops of ancient systems, and subsurface datasets will enable first order flux and  
1172 budget predictions and reconstructions of sediment and other phases.

1173

#### 1174 **SUPPORTING MATERIAL**

1175 The Matlab scripts that constitute the Eurotank Studies of Experimental Deepwater Sedimentology  
1176 Sediment Budget Estimator (EuroSEDS-SBE) will be made available as supplementary material to this  
1177 paper on publication.

1178

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1185 of the SBE. Their collective success in using the SBE to constrain sediment budgets in diverse deep-

1186 water systems has provided the necessary motivation to carry this manuscript to completion.

1187

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