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Sub-kilometre scale distribution of snow depth on Arctic sea ice from Soviet drifting stations

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Abstract:	The sub-kilometre scale distribution of snow depth on Arctic sea ice impacts atmosphere-ice fluxes of heat and light, and is of importance for satellite estimates of sea ice thickness from both radar and lidar altimeters. While information about the mean of this distribution is increasingly available from modelling and remote sensing, the full distribution cannot yet be resolved. We analyse 33539 snow depth measurements from 499 transects taken at Soviet drifting stations between 1955 and 1991 and derive a simple statistical distribution for snow depth over multi-year ice as a function of only the mean snow depth. We then evaluate this snow depth distribution against snow depth transects that span first-year ice to multiyear ice from the MOSAiC, SHEBA and AMSR-Ice field campaigns. Because the distribution can be generated using only the mean snow depth, it can be used in the downscaling of several existing snow depth products for use in flux modelling and altimetry studies.

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Sub-kilometre scale distribution of snow depth on Arctic sea ice from Soviet drifting stations

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ABSTRACT.

The sub-kilometre scale distribution of snow depth on Arctic sea ice impacts atmosphere-ice fluxes of heat and light, and is of importance for satellite estimates of sea ice thickness from both radar and lidar altimeters. While information about the mean of this distribution is increasingly available from modelling and remote sensing, the full distribution cannot yet be resolved. We analyse 33539 snow depth measurements from 499 transects taken at Soviet drifting stations between 1955 and 1991 and derive a simple statistical distribution for snow depth over multi-year ice as a function of only the mean snow depth. We then evaluate this snow depth distribution against snow depth transects that span first-year ice to multiyear ice from the MOSAiC, SHEBA and AMSR-Ice field campaigns. Because the distribution can be generated

using only the mean snow depth, it can be used in the downscaling of several existing snow depth products for use in flux modelling and altimetry studies.

INTRODUCTION

The snow cover of Arctic sea ice insulates the underlying ice from solar radiation in the summer and cold temperatures in the winter. In addition, snow impacts the propagation of laser and radar pulses from satellite altimeters, affecting the timing of their return. This importance has driven the development of a range of modelling and remote sensing approaches to accurately characterise the snow cover (see Zhou and others, 2021, for intercomparison of several products). Satellite remote sensing approaches (e.g. Rostosky and others, 2018; Lawrence and others, 2018) are generally limited by their low (multi-kilometre) spatial resolution, which has the effect of averaging out kilometre and sub-kilometre scale variability. Modelling approaches (e.g. Petty and others, 2018; Liston and others, 2020; Stroeve and others, 2020a) have similar limitations, with grid resolutions not falling below tens of kilometres. This in part reflects the coarse spatial resolution of standard atmospheric reanalysis and sea ice drift products.

This lower-bound on spatial resolution is a significant barrier to scientific progress, as the effects of snow on fluxes and sea ice thickness retrievals cannot be characterised solely by the mean snow depth in a grid-cell of a traditional data product (Iacozza and Barber, 1999), so a *sub-grid* scale snow depth distribution must be employed (e.g. Petty and others, 2020; Glissenaar and others, 2021). For instance, the amount of light incident on the ice surface in a multi-kilometre grid cell is sensitive to the fractional coverage of snow which is *optically thin* ($<\sim$15 cm for dry snow; Warren, 2019). This area cannot be straightforwardly gleaned from modelling or satellite observations of the mean snow depth in the grid cell (Stroeve and others, 2021).

In the example above, the area of optically thin snow within a larger area of level ice with given mean thickness will be primarily dicated by wind redistribution (Moon and others, 2019). Snow is dynamically transported through wind suspension and saltation, and is eroded and deposited heterogeneously around ice topography such as ridges and hummocks (Sturm and others, 2002; Chung and others, 2011). Furthermore, turbulence-induced features such as sastrugi introduce depth variability even on level ice (Eicken and others, 1994; Massom and others, 1997). The probability of snow transport and redistribution is dependent on its bulk and microstructural properties such as density and bond-radius (Filhol and Sturm, 2015). The

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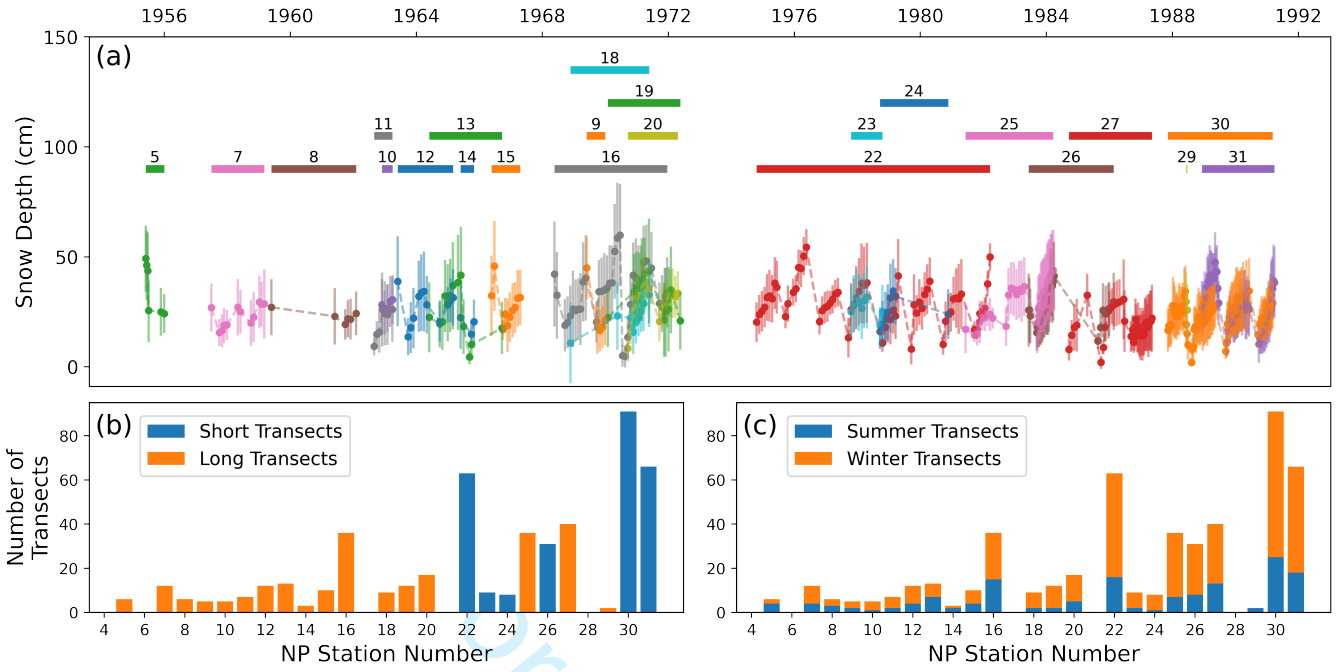

Fig. 1. (a) Operational periods of the NP stations contributing in this study. Bars at top indicate the time period between the first and last snow depth transect of the station. Solid circles indicate mean snow depth of transects, with vertical bars indicating one standard deviation in snow depth (b) The number of transects measured by each station, broken down by transect length (500m vs. 1000m). (c) Number of transects measured by each station broken down by summer (May-Sep) and winter (Oct-Apr).

combination of these factors makes deterministic modelling of snow redistribution a major challenge when the local ice topography is not known to a high level of detail (e.g. Liston and others, 2018), which is generally the case on sea ice. In this paper we derive a statistical model for the snow depth distribution based on the large number of snow depth measurements taken at Soviet drifting stations.

Snow transects from Soviet drifting stations

We analyse the results of snow depth transects performed at Soviet North Pole (NP) drifting stations between 1955 and 1991. These were crewed stations that drifted year-round in the Arctic Ocean while measuring a range of atmospheric, oceanographic and cryospheric parameters on what was generally multi-year sea ice. In particular we examine 33539 snow depth measurements from 499 transects from NP stations 5 - 31. Snow transects did not begin until NP 5, and the NP program was halted in 1991. While it was restarted in 2003, these data are not publicly available.

Snow depths were measured every 10 m along a line of either 500 or 1000 m long when snow depth was

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at least 5 cm and more than 50% of the surrounding area was snow covered. 166 transects were 500 m long and 333 were around 1000 m long, with transects prior to 1974 generally being of the 500 m type. The direction of the line was chosen randomly but did deviate where hummocks were present, and was at least 500 m from the station at its closest point. We note that this deviation around hummocks may introduce a bias in the snow depth measurements to sample more level ice with thinner snow. Where successive transects were taken at the same station, each was offset by 3 m from the previous line.

RESULTS

We now present a method for transforming an estimate of mean snow depth (from remote sensing or modelling) into a distribution of snow depths. We first characterise the linear relationship between the standard deviation of snow depths measured along a transect and the mean of that transect (Fig. 2a). When a linear regression is performed (and forced through the origin), the root-mean-square of the residuals is 3.20 cm, meaning that the standard deviation of the transect depths can be predicted with this standard-error where the mean is known. For every 10 cm increase in the mean snow depth, we find the standard deviation of the snow depths to increase by 4.17 cm.

$$\sigma_D = 0.417 \times \overline{D} \tag{1}$$

Where σ_D is the standard deviation of snow depth in a transect, and $\overline{D}$ the mean depth of the transect. We then convert all NP station snow depth measurements into depth-anomalies from their respective transect means (by subtracting the transect-mean value from each). We further transform these anomalies (measured in centimetres) into relative anomalies from the mean by dividing them by the standard deviation of their respective transects. When the distribution of these relative anomalies from the mean are plotted and normalised, a probability distribution is formed (Fig. 2b). To this distribution we fit a skewed-normal curve.

Our skewed normal distribution function is defined following O'Hagan and Leonard (1976) and Azzalini and Capitanio (1999) such that:

$$f(\sigma_D) = \frac{2}{\omega}\phi\left(\frac{\sigma_D - \xi}{\omega}\right)\Phi\left(a\frac{\sigma_D - \xi}{\omega}\right) \tag{2}$$

where:

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$$\phi(x) = \frac{1}{\sqrt{2\pi}} e^{-\frac{x^2}{2}} \quad \text{and} \quad \Phi(x) = \frac{1}{2}\left(1 + \text{erf}(\frac{x}{\sqrt{2}})\right) \tag{3}$$

with a being the skewness parameter, ξ being a location parameter, ω being a scaling parameter, and erf being the error function. We find the values of the three parameters to be $a = 2.54$, ξ = -1.11, $\omega = 1.50$. We also find that the skew-normal curve provides a marginally better fit to the data than a log-normal curve, reducing the root mean squared error by 8.5%.

We repeat this process for the winter and summer seasons individually (October-April, May-September). While the scaling of standard deviation with mean depth is slightly steeper in Summer (Fig. 2c), the shape of the summer probability distribution is not significantly different (Fig. 2d). This difference in the scaling is relatively small compared to the uncertainty and residuals in the regression, and as such we opt for a singular analysis, considering all transects from all months.

The above method allows the standard deviation of the snow depth to be estimated from the mean snow depth (Fig. 2a). When both of these quantities are known, the snow depth distribution may be calculated using the skewed normal curve shown in Fig. 2b.

For instance, if the mean snow depth is assumed to be 0.5 metres, then the standard deviation of the snow depth distribution is estimated using Eq. 1 such that $\sigma_D = 0.209 \pm 0.032$. Multiplying the x axis of Fig. 2b by this factor, it can be inferred (for example) that the probability of randomly sampled snow of less than 30 cm is 17%, the chance of sampling snow thicker than 1 metre deep is 1.8%.

For calculations of light flux through thin snow, it may be found that for snow of a mean thickness of 0.5 m, the probability of snow being of less than 15 cm is around 2%. The same probability for snow of 0.25 m is around 17%.

When applied in this way, the method described above functions as a statistical *model* for the snow depth distribution, and we use this term interchangably with 'method' when evaluating its performance in the next section.

Negative Snow Depths

The use of a skewed normal distribution (or any normal distribution) results in a small fraction of negative snow depths. We find that the total fraction is relatively constant at 0.1% in the 0 - 50 cm range of mean snow depths. Above this range, it transitions to a linear decline with increasing mean snow depth, dropping below 0.075% for snow depths larger than 200 cm.

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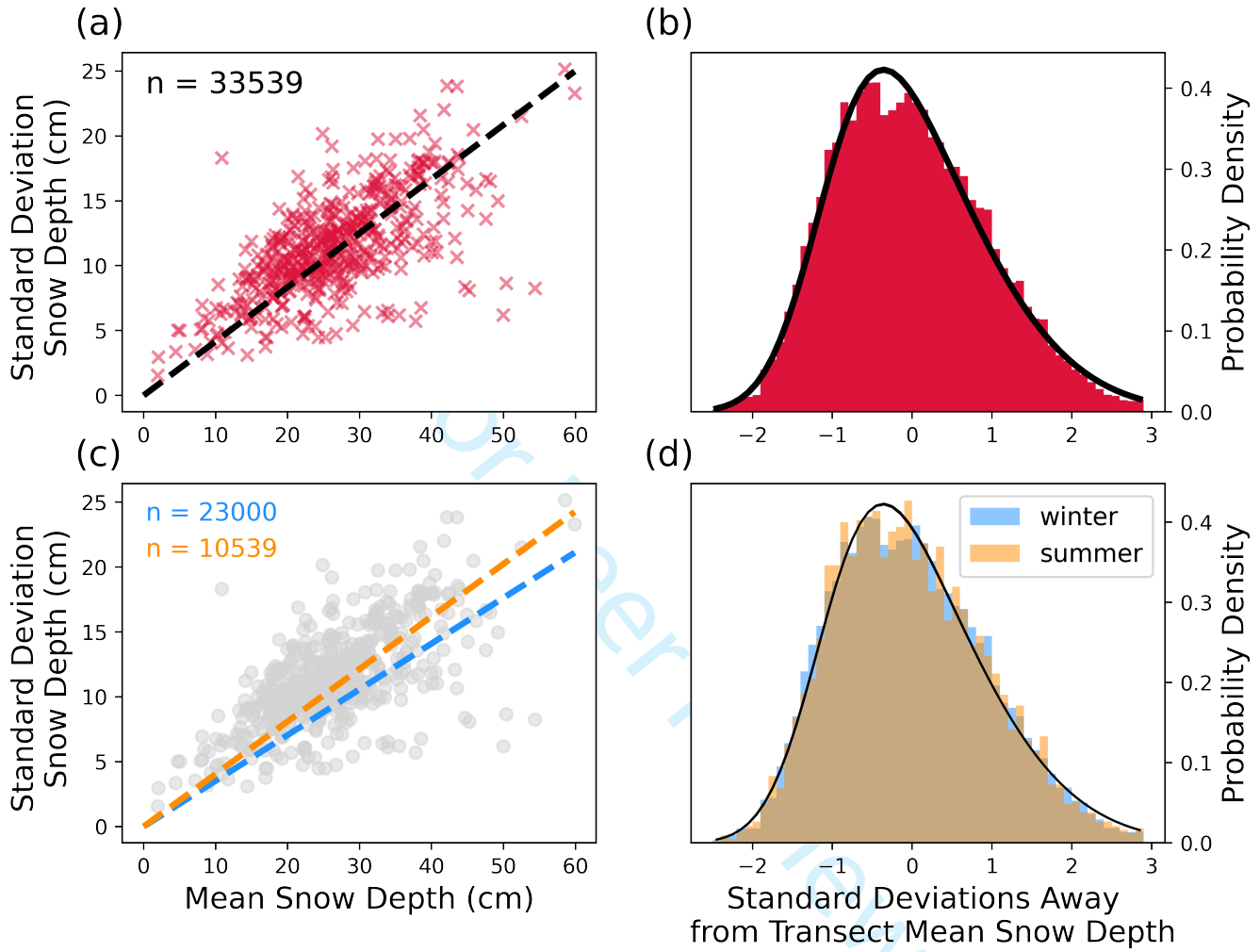

Fig. 2. **(a)** Relationship between a transect's mean snow depth and the standard deviation. The slope of the regression (forced through the origin) is 0.41, the root-mean-squared-residual is 3.20 cm, and the Pearson correlation coefficient (r value) is 0.66 **(b)** The probability density of a snow depth being measured such that it is a given number of standard deviations from the mean of the transect. The empirical distribution is given in red from drifting station data and a skewed-normal curve is fitted in black. **(c)** Same as a, but with individual regressions for winter and summer transects. **(d)** same as b, but with individual probability density distributions for winter and summer transects. The two seasonal skew-normal fits (black) are visually indistinguishable.

Because the fraction of negative snow depths does not exceed 0.1%, we treat it as negligible in the analysis that follows. However, if this distribution were implemented in a snow-conserving model it would be necessary to modify the low-tail of the distribution. This could be done by merging the distribution with an exponential curve at low values, or by truncating it at zero and redistributing the coverage so that the area under the probability distribution is unity. In the redistribution case, it would be possible to either scale the whole curve by a small amount, or instead preferentially add the 'lost' coverage to the low-end of the distribution. We stress however that the effect of this would be extremely small (and not noticeable in the analysis of this paper), and so is only necessary for applications where snow must be precisely conserved.

DISCUSSION

Cross-validation

We now evaluate the consistency of our snow depth distribution method with a leave-one-out-cross-validation (LOOCV) approach (Stone, 1978). To do this we select a single transect and recalculate the skewed-normal curve using the remaining 498 transects. We then assess the goodness-of-fit of the curve against the selected transect. This is performed iteratively for each transect such that 499 goodness-of-fit statistics are generated. We calculate the goodness-of-fit using the root-mean-square error (RMSE) for the fitted probability distribution and that of the transect, using ten equal-width depth bins that span from 0 cm to the maximum depth measured.

This cross-validation exercise allows for the estimation of model skill as a function of different variables, such as the transect's length, its mean depth and the month in which it was performed (Fig. 3a - c). We also investigate whether the snow depth distribution of a transect can be better predicted with the model presented here (the 'NP model') when its corresponding station has contributed many other transects to the distribution (Fig. 3d).

We first show that the NP model's skill is very similar when applied to both long and short NP transects (Fig. 3a). The mean RMSE for long and short transects is 0.053 and 0.057 cm respectively (a difference of 7%). This similarity is to be expected, with the difference likely reflecting the more incomplete sampling of the local snow depth distribution by a shorter transect. We also show that the skill of the NP distribution is relatively independent of the depth of the transect. The skill of the method is maximal for snow distributions with means in the range of 20 - 40 cm. Transects where the model exhibited lowest

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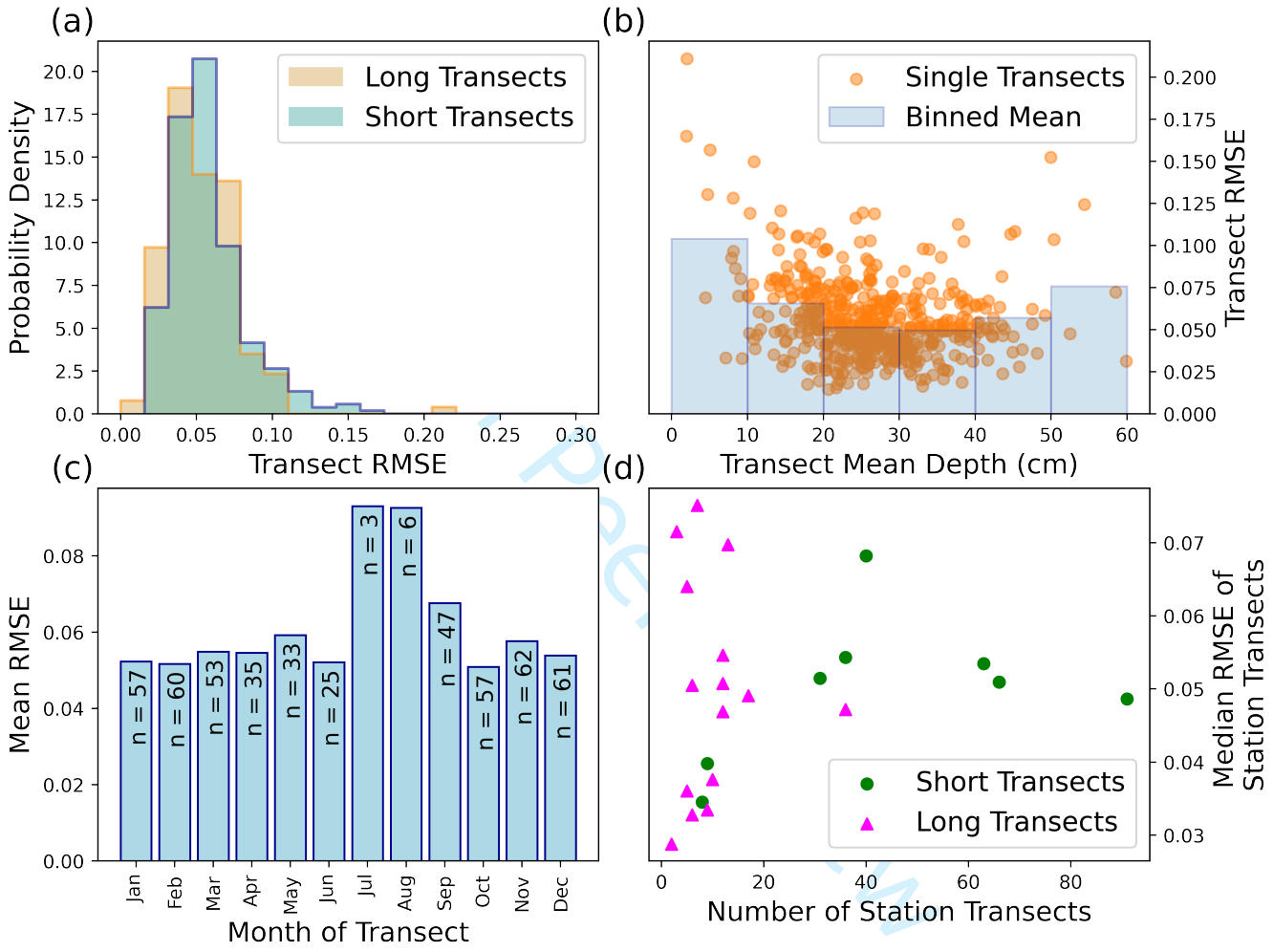

Fig. 3. (a) Histograms of the RMSE for long transects (1km) and short transects (500m) separately. (b) RMSE of the NP distribution against observed transects shown as a function of transect mean depth. (c) NP distribution RMSE as a function of month. 'n' indicates the number of transects contributing to the model from that month (d) Mean RMSE of all transects at a given station, shown as a function of the number of transects at that station. RMSE values are unitless as they represent the error in a probability distribution.

skill had very shallow depths (<10 cm). In this category the model's skill is halved relative to the 20 - 40 cm range. This mean-depth dependent skill reflects the relative representation of transects that contribute to the NP model: the model performs best when predicting transects similar to those on which it was 'trained' (Fig. 2a).

The model's skill is relatively insensitive to the month of the year with the exception of July and August (Fig. 3c). In these two summer months its skill is diminished with the RMSE being on average 67% higher in these two months by comparison to the average of the other months. Again, this is ostensibly a reflection of the low contributions of these months to the total number of transects: July and August contribute three and six transects to the NP model respectively, whereas the other months on average each contribute 49 transects. Low skill in these months is also likely a reflection of the snow depths being lowest, which is also associated with low skill (see Fig. 3b). We also point out that in summer a bias is introduced in the form of a 'surface scattering layer' (e.g. Polashenski and others, 2012), which forms at the snow-ice interface and can be penetrated by a probe despite being formed of ice rather than snow.

We finally address the potential lack of independence between successive transects at the same station. Our LOOCV approach assumes that by not training the model with the transect being validated against, the validation transect is independent. But the potential exists that information about the validation transect enters the model through previous and subsequent transects at the same station that are included. If successive transects are strongly related, we would expect stations that contribute more transects to the model to have their transects perform better in the LOOCV exercise. We apply the non-parametric Spearman's Rank test for correlation and find no statistically significant ($p < 5\%$) between the number of transects contributed by a station to the model and the mean or median RMSE of its transects in the LOOCV exercise (Fig. 3d). This supports the premise that LOOCV is an appropriate tool with which to evaluate the skill of the NP model.

Evaluation against MOSAiC Measurements

We compare our regression and fitted curve (Fig. 2a, b) against the snow surveys taken on the MOSAiC expedition using a magnaprobe (Figs 4, 5). To do this we select snow suveys of the "Northern Transect" (Stroeve and others, 2020a), which predominantly consisted of second-year ice.

We first note that the NP-based regression of snow depth-standard-deviation against mean depth results in an underestimation of the standard deviation of snow depths from MOSAiC (Fig. 4a). The effect of this

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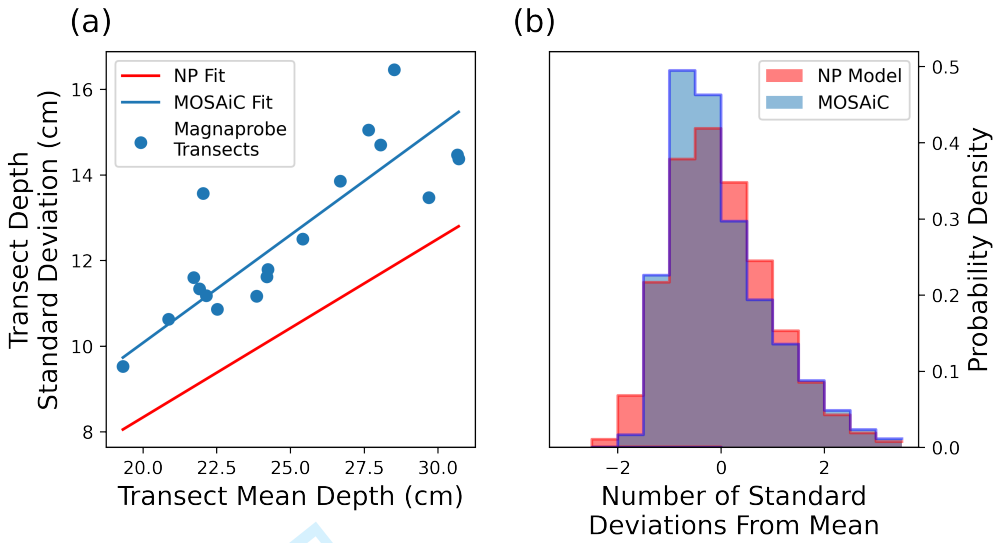

Fig. 4. (a) Snow depth variability for a given mean depth was larger on the MOSAiC transects than on average for the NP stations. Regression for NP station data shown in red, MOSAiC transects in blue. (b) Because the depth variability is lower in the NP model, the probability distribution in standard deviation space is wider (as the standard deviations themselves are smaller).

is that the width of the modelled depth distribution is too high in standard-deviation space (Fig. 4b). This can be understood because if the size of a standard deviation is smaller, then individual measurements end up being a higher number of smaller standard deviations away from the transect mean.

Despite this bias, the NP model generally provides a good fit to the individual MOSAiC transects (Fig. 5). We find that the skewness parameter of the NP model ($a = 2.54$) is smaller than when a skew-normal fit is applied to the MOSAiC transects ($a = 6.4$). This results in the modal depth bin often being overestimated by the NP model (Fig. 5). A corrolary to this underestimation of skewness by the NP model is that that where the modal bin is overestimated by the model, the probability (or fractional coverage) of the depth bin is underestimated. This can be seen (for example) in the panel of Fig. 5 corresponding to January 30$^{\text{th}}$. The skewness parameter of data in this panel is 13.7, higher than that of the NP model. This results in the model's modal depth bin being one too high (20 - 25 cm vs 15 - 20 cm), and the probability of the modal bin being 3.5% too low.

The fractional coverage of shallow snow is a key parameter for light and heat flux modelling, so is now given specific consideration. We find the NP model underestimates the coverage of thin snow (<10 cm) in early winter (end of October - mid December) with respect to MOSAiC observations. The observed coverage is 6.1%, and the NP model produces a coverage of 4.3%. After mid December the model begins

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to overestimate the thin snow coverage. On average it was observed to be 1.5%, and modelled to be 2.1%, an overestimate by 0.6 percentage points.

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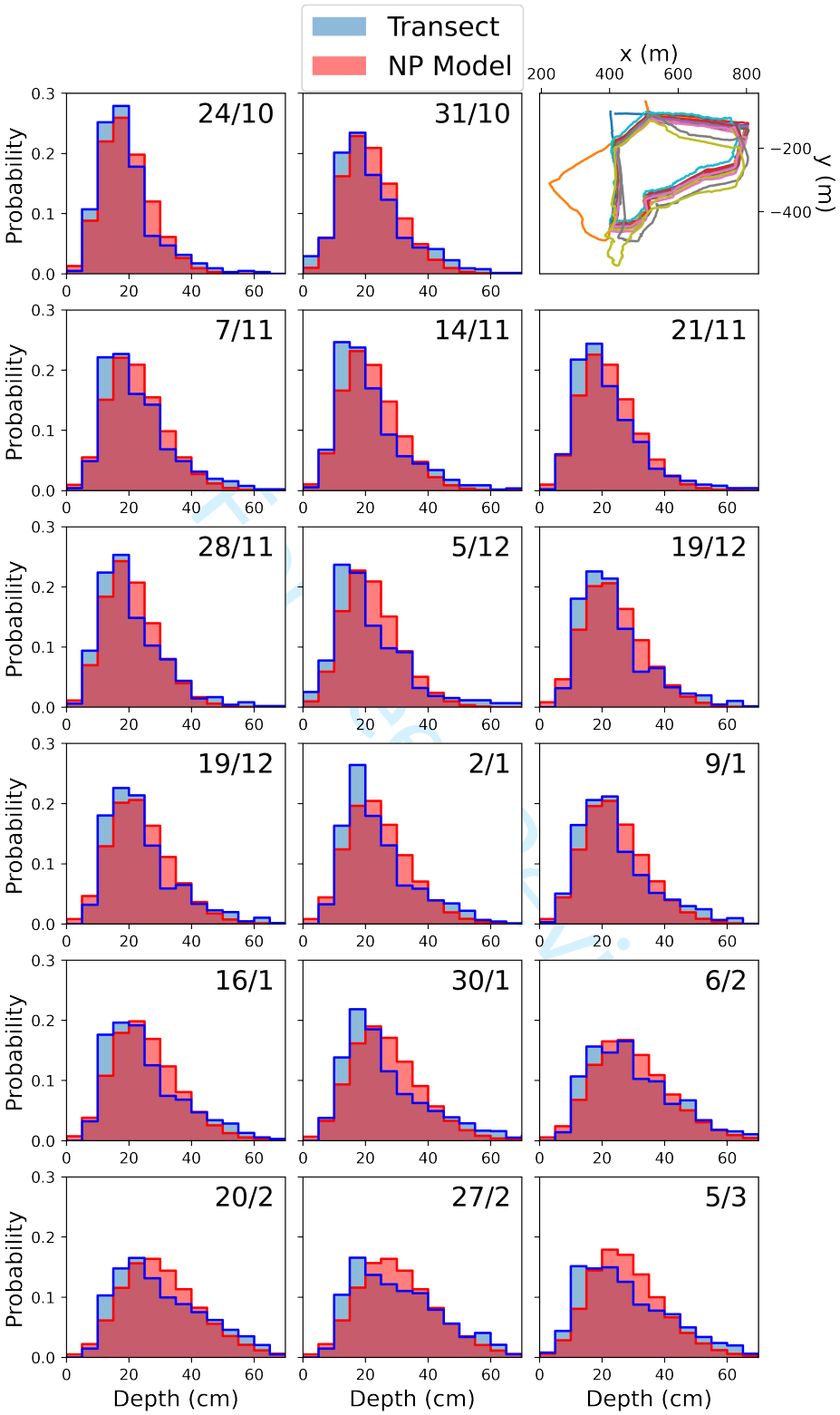

Fig. 5. Winter evolution of the snow depth distribution on the MOSAiC Northern Transect (blue histograms, 5 cm bins). The modelled depth distribution described in this paper shown in red. Top right: plots of the fourteen transects contributing to the MOSAiC evaluation exercise.

Evaluation against SHEBA Measurements

We now evaluate our method using snow depth transect data from the Surface Heat Budget of the Arctic (SHEBA) expedition (Sturm and others, 2002). Snow transects were taken over a variety of ice types during the SHEBA expedition, and here we opt to compare our method to transects taken in the 'Atlanta' and 'Tuk' areas which were dominated by multi-year ice. These areas were described using ice-class codes, and were indicated as 2-3 and 4 respectively. Class 2 indicates 'Refrozen melt ponds', 3 'Hummocky', and 4 'Deformed' (Sturm and others, 2002). Snow depths were initially measured with a marked ski-pole, with a prototype magnaprobe being used later. While the NP-model provides a good fit to the Atlanta transects, it is less appropriate for Tuk transects (where the RMSE is on average doubled compared to Atlanta).

Atlanta Transects

We find the ratio between the transect standard deviation and the transect mean to be very similar between the SHEBA and NP transects (Fig. 6a). Removing transects from the high-melting month of July from the SHEBA data marginally improves this agreement, but not greatly relative to the uncertainty in the regressions. We note that no transects were taken in the Atlanta region in August.

Unlike the standard deviation to mean depth ratio, the agreement of the snow depth distribution is clearly improved by removing July transects from the SHEBA distribution (Fig. 6b). We attribute this to strong alteration of the snow depth distribution by melt ponds in this month, which developed at the site in the second half of June (Webster and others, 2015). Outside of this period the snow depth distribution is primarily dictated by wind redistribution, but within the period it is dictated by small-scale snow surface topography and resulting melt pond distribution.

The poor performance of our model in July and its association with intense snow melting is shown in Fig. (6c). After strong melting (decreasing snow depth) in June, the snow depth distribution begins to diverge from the NP model during the transition from June to July, and increases throughout July.

Tuk Transects

The NP model performs considerably less well when applied to Tuk transects (Fig. 7). Unlike Atlanta, the standard deviation of snow depth on Tuk transects is significantly underestimated by the NP regression. Furthermore, the skew-parameter of the NP model ($a = 2.54$) is less than half that of a skew-normal curve fitted to the Tuk transects ($a = 6.27$).

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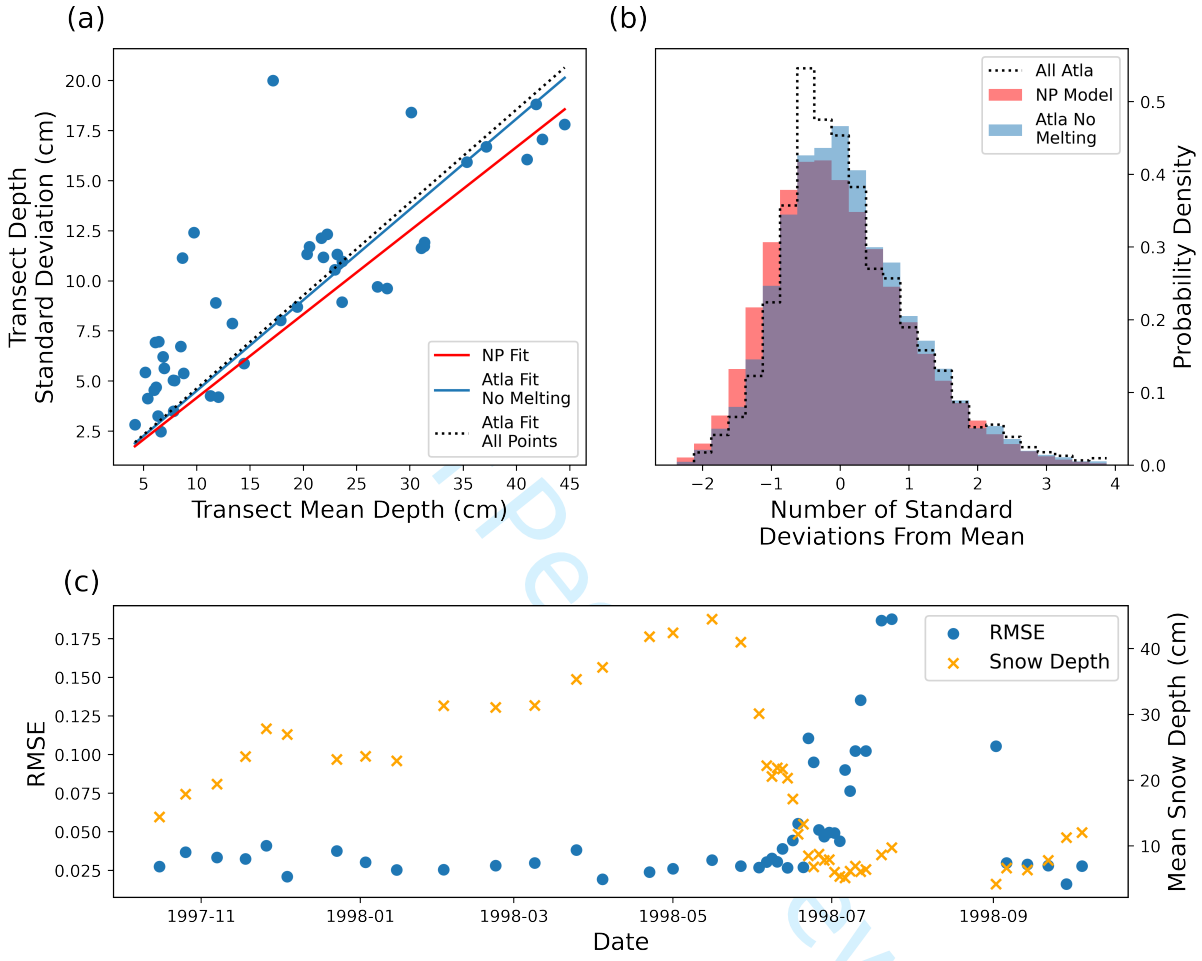

Fig. 6. (a) Releationship between the mean snow depth and standard deviation of the snow depth on SHEBA 'Atlanta' transects (blue scatter). Linear regressions through the points are shown both including and excluding datapoints from July and August (blue solid and black dotted lines respectively). Linear regression from all NP transects shown by red line. (b) The snow depth distribution on the SHEBA 'Atlanta' transect excluding July and August (blue) and from NP stations (red). The SHEBA fit from all transects including July and August shown by black dotted line. (c) Time evolution of the error in this paper's method (blue scatter). RMSE is higher during July and August than in other months, which coincides with melted snow (depth in orange scatter).

It is striking that the mismatch in the skewness parameter for the Tuk transects is slightly smaller than the MOSAiC transects, but the model-observations mismatch is much larger. Furthermore it is notable that although the skewness of the Tuk transects is larger than the NP model, the NP model still does a good job of predicting the modal depth bin. We would expect the modal bin to be too deep where the skewness is underestimated (see Fig. 5). These features are explained by the fact that a skew-normal curve cannot be easily fitted to the Tuk transects in standard deviation space (Fig. 8).

To illustrate, we display the transect data alongside the best possible skew-normal fit (not involving the NP data) to the data. The agreement is good for the Atlanta and MOSAiC data sets, but noticeably less good for the Tuk data (Fig. 8). This indicates that unlike the MOSAiC northern transects and the SHEBA Atlanta transects, the SHEBA Tuk transects do not display a skew-normal distribution of snow depths.

We attribute the deviation of the Tuk data from the skew-normal distribution to the highly deformed nature of the ice relative to that seen at Atlanta and the MOSAiC northern transects, and at most of the NP stations. Firstly we point out that over strongly deformed ice the wind dynamics may cause snow to be distributed differently. Secondly we raise the fact that NP transects deviated around highly deformed ice such as that dominating the Tuk transects. There is a related sampling bias for the MOSAiC Northern transect, because the transect layout was chosen such that a snowmobile could drive around it.

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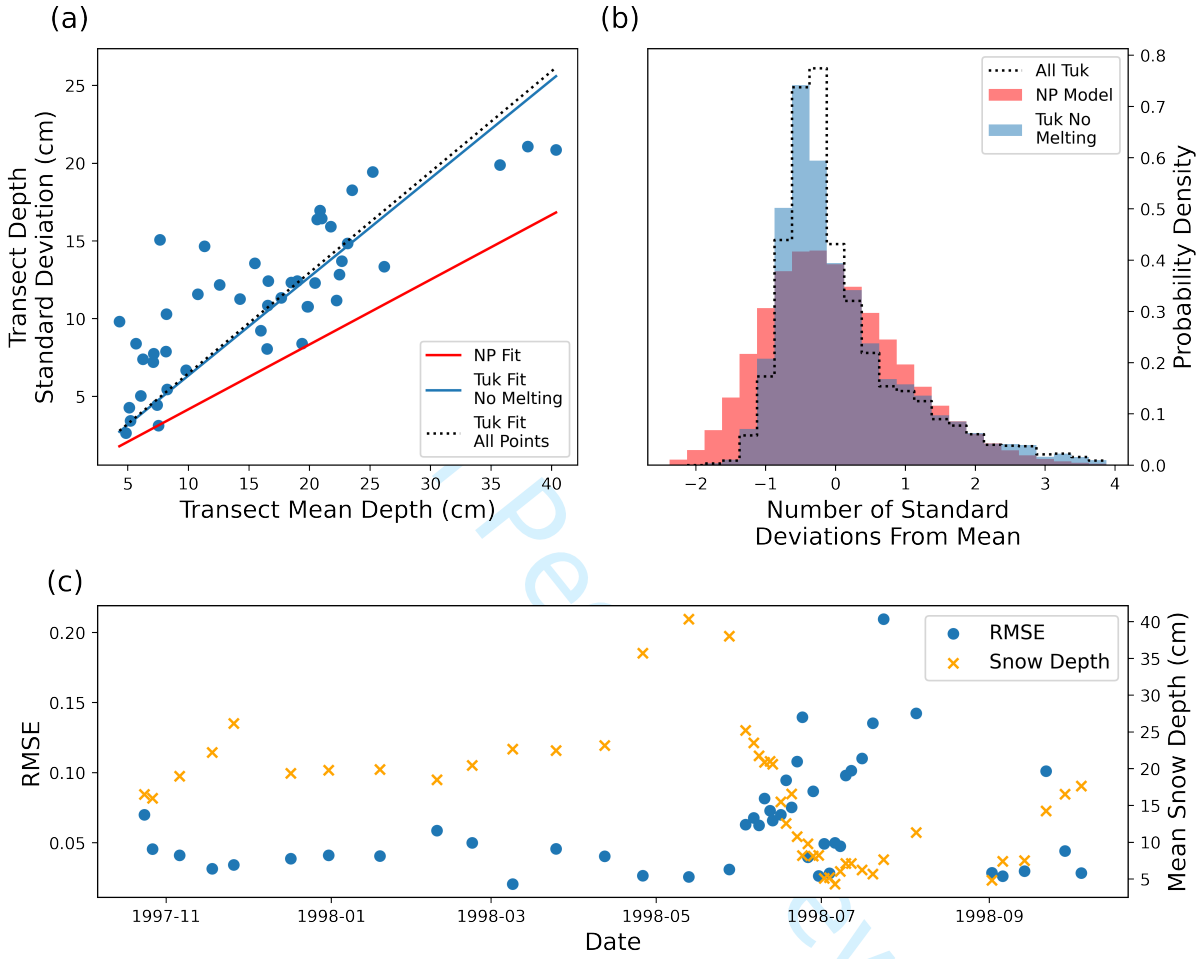

Fig. 7. (a) Releationship between the mean snow depth and standard deviation of the snow depth on SHEBA 'Tuk' transects (blue scatter). Linear regressions through the points are shown both including and excluding datapoints from July and August (blue solid and black dotted lines respectively). Linear regression from all NP transects shown by red line. (b) The snow depth distribution on the SHEBA 'Tuk' transect excluding July and August (blue) and from NP stations (red). The SHEBA fit from all transects including July and August shown by black dotted line. (c) Time evolution of the error in this paper's method (blue scatter). RMSE is significantly higher during July and August than in other months, which coincides with melted snow (depth in orange scatter).

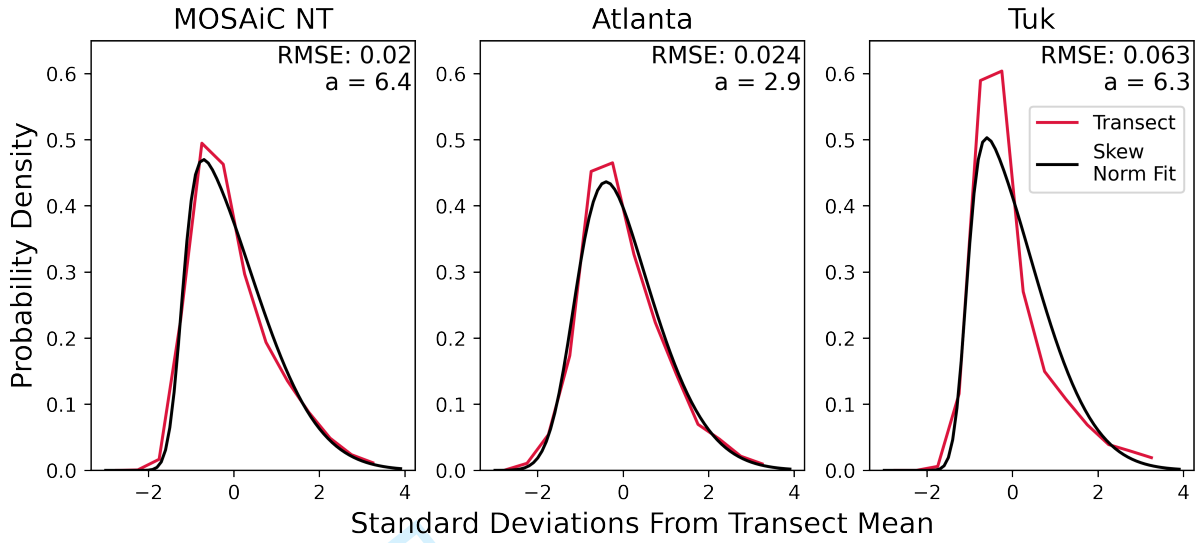

Fig. 8. Distribution of relative depth anomalies for the three evaluation data sets used in this paper (red). Distributions were generated with a bin width of 0.5 standard deviations. Skew-normal distributions are fitted to each and show variable agreement (black).

Potential for Application to First Year Ice

No multi-station data similar to the NP transects exist for first year ice (FYI). This is in part because first year ice cannot be drifted on for long before experiencing a melt season, but also because FYI is thinner and more liable to break up, making crewed research installations difficult to establish. Because of these difficulties, it is natural to wonder whether the NP snow depth distribution can be applied to FYI and with what uncertainty. To investigate this we apply the NP model to FYI snow depth transects taken on the AMSR-Ice03, AMSR-Ice06 (Sturm and others, 2006) and MOSAiC field campaigns (Krumpen and others, 2020). Several of these transects were performed in Elson Lagoon (EL in Fig. 9), which consists of level ice. This contrasts with the more deformed ice on the nearby Beaufort sea measured during AMSR-Ice03 (BS in Fig. 9). During AMSR-Ice06 a smooth-ice section in the Chukchi Sea was also surveyed (CS in Fig. 9). Finally, during the MOSAiC expedition, successive transects were taken on a refrozen lead (nicknamed the 'runway', described in Stroeve and others (2020b)), which provides some information about the thin-snow regime on FYI (Fig. 9 g, h & i). For the eight transects described above we calculate the RMSE of the NP model when applied based on the mean value, calculated with 5 cm bins. We also fit a skew-normal curve to the transect data and investigate the skewness-parameter (a) to shed light on the mismatch between the NP model and the observations.

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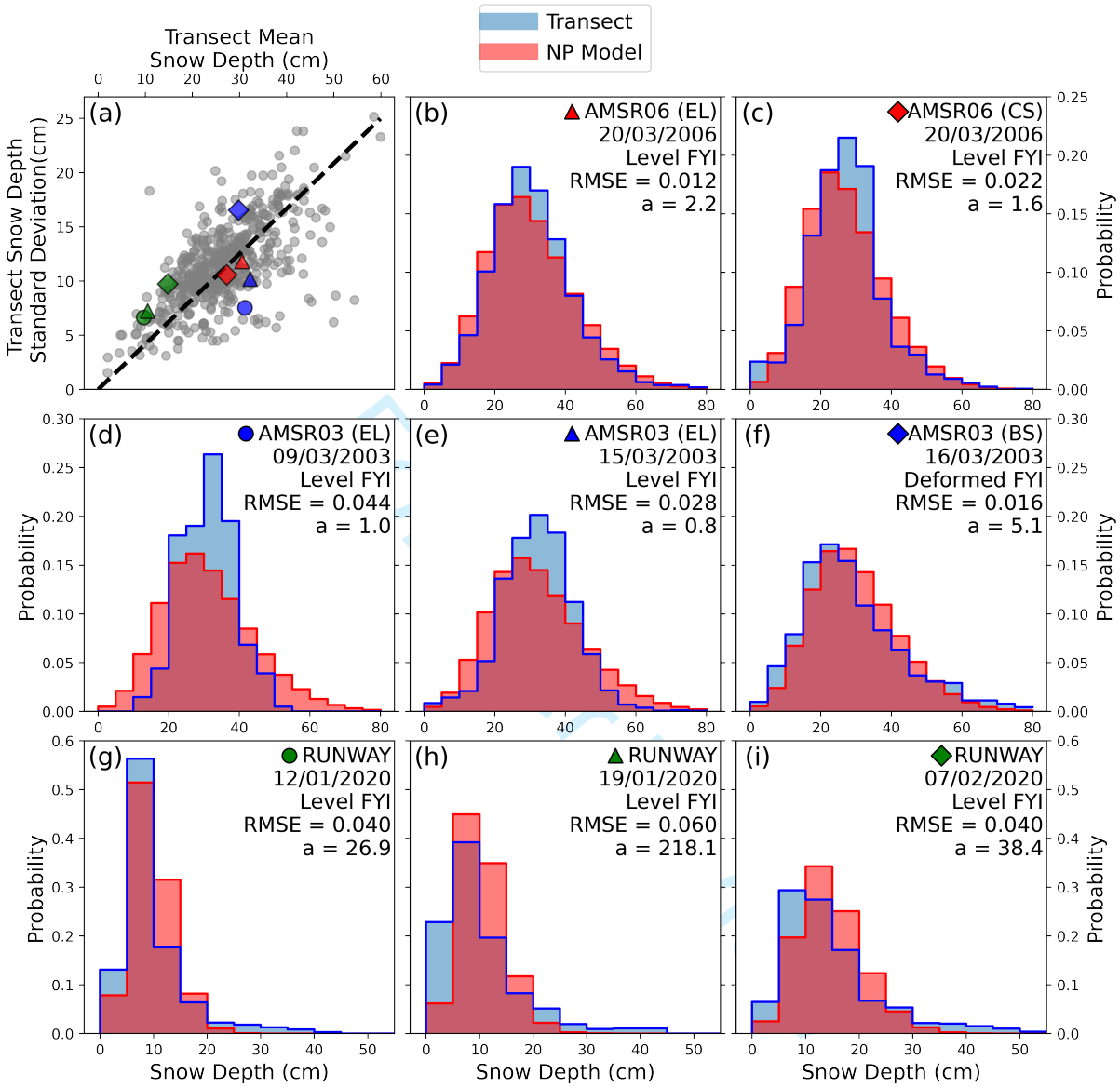

Fig. 9. Comparison of the NP model with data from first year ice transects taken during the AMSR-Ice 03, AMSR-Ice 06, and MOSAiC field campaigns. Panel (a) shows ratio of snow depth-standard-deviation to transect mean depths for the FYI transects (large markers) as well as for the NP transects (gray dots). All other panels show the snow depth distribution produced by the NP model (red) against the transects (blue), with 5 cm wide depth bins for comparative purposes. Panels represent (in order b-i) Elson Lagoon (EL) and level ice on the Chukchi Sea (b & c), two transects on Elson Lagoon one week apart (d & e), a transect on FYI of the Beaufort sea near Elson Lagoon (f). Bottom row (g - i) displays snow transects taken on a refrozen lead during the MOSAiC expedition.

We first observe that all eight FYI transects have ratios of depth-standard-deviation to mean depth roughly consistent with that observed in the NP stations (Fig. 9a), particularly those from AMSR-Ice06. We also note that the skewness parameter of the AMSR-Ice06 data ($a = 1.6$ & 2.2) is close to the skewness parameter of the NP-model ($a = 2.54$). These characteristics lead to the NP model performing better on the AMSR-Ice06 data than the AMSR-Ice03 data. The AMSR-Ice06 survey on Elson Lagoon has the lowest RMSE of all eight FYI transects (0.012) when compared to the NP model - this is related to it having the most closely matching skewness parameter to the NP model.

While all three AMSR-Ice03 transects have very similar mean snow depths to each other (~30 cm), we find that the ratio of depth-standard-deviation to mean snow depth is lower than for the NP station transects for the Elson Lagoon transects, but higher for the Beaufort Sea (Fig. 9a). That is to say, the snow over the deformed first year ice in the Beaufort Sea exhibited considerably more variability than that over the smooth ice in Elson Lagoon during AMSR-Ice03. In addition to being more variable, the Beaufort Sea transect showed a much higher skewness parameter ($a = 5.14$) than those on Elson Lagoon ($a = 1.02$ & 0.844). Because a skewness parameter of 1 represents a symmetrical distribution, it follows that the transect on the 15$^{\text{th}}$ March on Elson Lagoon was skewed the *other* way to that typical of the other surveys studied in this paper. The transect over deformed ice exhibits the lowest RMSE value of the AMSR-Ice03 transects by some margin.

We attribute the low-skewness (symmetry) of the 2003 Elson Lagoon data to a lack of ice topography around which to build up a 'long tail' of drifted, thick snow. Conversely, the highly deformed ice of the Beaufort Sea produces a noticeable long tail of thick snow, such that the probability of finding snow deeper than 55 cm is underestimated by the NP model (Fig. 9f). However it is striking that the AMSR-Ice06 transects at Elson Lagoon are more weakly governed by this: while the skewness parameters are still lower than for the NP transects, there is a smaller difference.

We now turn to the thin snow cover of the three MOSAiC 'runway' transects (Fig. 9 g, h & i). We first point out that a skew-normal curve cannot be easily fitted to these data (not shown; similar to the situation with the SHEBA 'Tuk' transects above). This indicates that the NP model will not be a good fit, even before it is applied. Because of this feature, the skewness-parameter values listed in the panels of Fig. 9 should not be understood to properly capture the underlying transect data. When the NP model is applied and compared, it exhibits a high RMSE relative to the other FYI transects. As well as being related to the poor approximation with a skew-normal curve, this performance is also linked to the

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three 'runway' transects having the highest error in depth-standard-deviation to mean depth ratio (Fig. 9a) by comparison to the NP transects. One key physical difference between the runway transects and the other FYI surveys is the low average snow depth. However other contextual differences exist: for example the transects were performed in a colder region (near the pole), and at a colder time of year (January/February). This may result in a more weakly bonded snowpack at the time of measurement, susceptible to more wind-redistribution and resulting in a higher depth-standard-deviation to mean-depth ratio (by comparison to the AMSR-Ice transects).

Because of the differences in the age of the snow (and the ice topography over level ice), there is no a priori reason that the NP-model for the snow depth distribution derived in this paper should be applicable to FYI, and indeed our model works relatively poorly when simulating the 'symmetrical' snow depth distributions at Elson Lagoon in 2003, and the thin snow on the MOSAiC runway.

However in the instance where the ice was deformed (Fig. 9f) the model performs relatively well. Perhaps counterintuitively given the 2003 results, the NP model also performed well in 2006 over both level ice transects. The RMSE of the NP Model when applied to the Beaufort Sea transect was 0.016, which is in fact lower than the corresponding values for the MOSAiC Northern Transects (Fig. 5), which ranged from 0.019 - 0.031. By this metric the performance of the model over FYI in 2006 was also better (0.012) and comparable (0.022).

In summary, we have shown that the NP model is capable of performing well over deformed FYI, and even over level ice in the case of 2006 (where 'well' is defined with reference to its performance over MYI at MOSAiC). But despite this capability, it also clearly performs poorly in the case of thin snow (MOSAiC runway, where we observed that the measurements could not be well-represented by any skew-normal distribution), and also in the case of highly symmetrical (low-skew) snow distributions over FYI (Elson Lagoon in 2003).

Application to point-measurements of snow depth

There are several drifting, autonomous platforms in existence that record the snow depth at a single point, such as snow buoys and ice mass balance buoys (Nicolaus and others, 2021). If the buoy is deployed at random, it is most likely to sample the modal snow depth. In reality these instruments are often not deployed at random, and a conscious choice is made to sample what is perceived to be the modal depth. However for applications such as laser and radar altimetry retrievals of sea ice thickness, the mean snow

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depth is the quantity required for characterising the floe's hydrostatic equilibrium (e.g. Mallett and others, 2021). We now present a simple method of relating these point measurements to the mean snow depth of the surrounding area.

If the mean snow depth ($\overline{D}$) is related linearly to the standard deviation (σ_D, Fig. 2a, Eq. 1) by a constant K, and we observe the modal snow depth to be X standard deviations below the mean (Fig. 2b), then we can relate the modal depth to the mean depth as follows:

$$\sigma_D = K\overline{D} \quad \& \quad \overline{D} = D_{mode} + X\sigma_D \tag{4}$$

$$\overline{D} = \frac{D_{mode}}{(1 - XK)} \tag{5}$$

Using the NP data from Fig. (2) we now calculate that $X = 0.35$. The value of K was found earlier (Eq. 1) to be 0.417. We therefore calculate that the mean snow depth is 17% larger than the modal depth. Where singular drifting instruments are assumed to retrieve the modal snow depth in their environment, we recommend this correction for estimation of the mean.

Length Scales

The NP station transects were performed over distances of 500 - 1000 m, and this characterises the length scale on which our distribution is relevant. If the same transects were theoretically performed over just a few centimetres, the ratio of the standard deviation in snow depth to the mean snow depth (Fig. 2a) would be lower, and the distribution about the mean would likely be different. The distribution would be sensitive to the small-scale roughness of the snow surface, rather than larger scale features like sastrugi and snow drifts around ice topography. If the transects were performed (again, theoretically) over thousands of kilometres then the snow distribution would again be different, and more representative of synoptic variability in snowfall and ice type. As such we stress that we have characterised the distribution of snow depth at the *sub-kilometre* length scale (on the order of hundreds of metres).

We also conduct an analysis to ensure that our results are robust to the spatial sampling interval of the transects, which was 10 m for the NP stations. We investigate whether Fig. 2 and the resulting NP model would be different if the transects had five or ten times the spacing. We find that artificially increasing the spacing of measurements by only considering one in every five or ten measurements (sampling at 50

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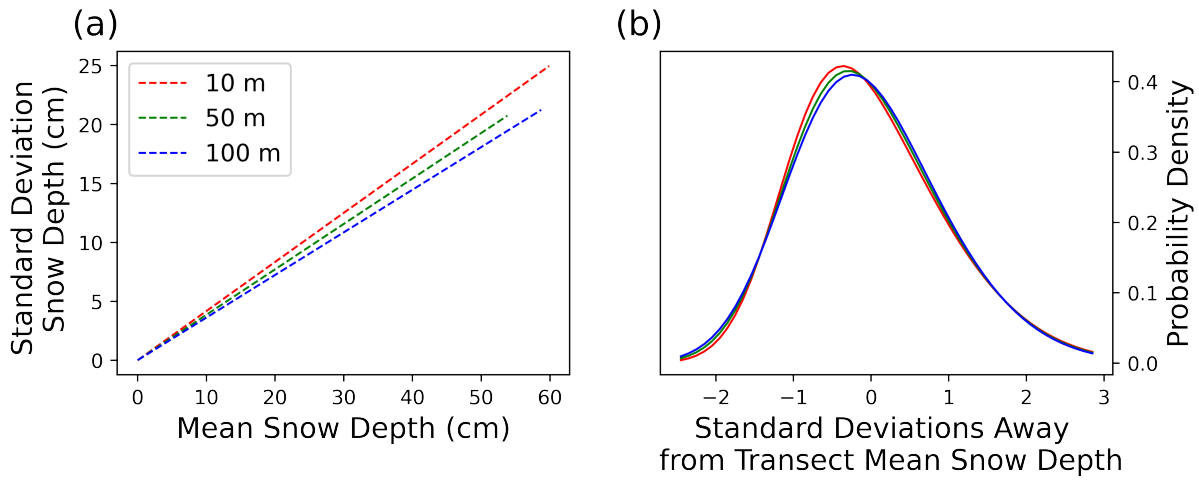

Fig. 10. Impact of undersampling the transect by taking every fifth and tenth measurement on (a) the ratio of transect standard deviation to transect mean snow depth (b) the probability density distribution in standard deviation space.

and 100 m respectively) has a small impact on the ratio of the standard deviation to the mean, and the parameters of the skew-normal curve of best fit (Fig. 10). When comparing a 10 m sampling interval to a 100 m sampling interval, the standard deviation to mean depth ratio decreases from 0.416 to 0.361, and the skewness parameter to decrease from 2.54 to 1.84. Extrapolating from this trend, magnaprobe samples used in the validation data sets which have a sampling interval of 1 m may therefore have a high-skew and high $\sigma_D : \overline{D}$ bias relative to transects from NP stations.

Relevance in a changing Arctic Ocean and other limitations

The potential for application of the NP-model to first year ice was discussed above, and it was found that while the NP model was capable of performing well over FYI, it performed poorly when simulating the distribution of thin snow, and overestimated the skew in some cases. Here we point out that the Arctic Ocean is becoming increasingly dominated by first year ice, so arguably the relevance of this MYI-trained model is in slow decline.

There may also be spatial limitations on applicability. The NP drifting stations generally operated in the Central Arctic Ocean rather than in the marginal regions such as the Kara, Beaufort and Barents Seas (Warren and others, 1999). However these areas are generally dominated by first year ice, so this geographic constraint is less strict that the ice-type one described above.

The average age of multi-year ice is in decline, with the coverage of ice aged five years or more shrinking

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from 28% to 1.9% between 1984 and 2018 (Stroeve and Notz, 2018). The mean thickness of sea ice is also in decline (Kwok, 2018). Because we produce our statistical model using drifting station data from 1955 - 1991, it likely reflects snow conditions on ice older and thicker than that which currently exists in the Arctic. We note however that our method does still display good skill with respect to the MOSAiC transects, which were generally performed on ice that had only experienced one melt season.

SUMMARY

In this paper we have developed a generic snow depth distribution for multi-year ice that can be fully characterised by the mean snow depth. This allows it to be superimposed onto estimates of mean snow depth from satellites and models for the purposes of flux modelling and altimetry studies.

We performed a cross-validation exercise and found the model's skill to be highest in winter, and lowest during the summer months of intense melt and sparse measurements. We then evaluated the distribution against snow depth transects from the MOSAiC, SHEBA and AMSR-Ice field campaigns. We found that the model generally overestimated the variability in snow depths for the MOSAiC campaign, but the fit parameters were otherwise broadly appropriate. On the smoother multiyear ice of the SHEBA campaign the model performed well, but the model performed poorly on transects executed over highly deformed ice. We found that this was related to the fact that the snow depth distribution in this area was not well approximated by the skewed normal distribution used in the NP model. We then applied the distribution to eight transects conducted over first year ice, and found that while the NP-model was capable of performing well (over deformed FYI and in two cases over level ice), it performed poorly when simulating thin snow on a refrozen lead in the Central Arctic, and also when simulating a highly symmetrical snow distribution over level ice.

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Code and Data Availability

All code and data required to reproduce this analysis can be downloaded from github/robbiemallett/sub_km.

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