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# 8 De-risking the energy transition by quantifying the uncertainties in fault stability

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13

## 14 Abstract

15 The operations needed to decarbonise our energy systems increasingly involve faulted rocks in the  
16 subsurface. To manage the technical challenges presented by these rocks and the justifiable public concern  
17 over induced seismicity, we need to assess the risks. Widely used measures for fault stability, including slip  
18 and dilation tendency and fracture susceptibility, can be combined with Response Surface Methodology from  
19 engineering and Monte Carlo simulations to produce statistically viable ensembles for the analysis of  
20 probability. In this paper, we describe the implementation of this approach using custom-built open source  
21 Python code (*pfs* – probability of fault slip). The technique is then illustrated using two synthetic datasets and  
22 two case studies drawn from active or potential sites for geothermal energy in the UK, and discussed in the  
23 light of induced seismicity focal mechanisms. The analysis of probability highlights key gaps in our knowledge  
24 of the stress field, fluid pressures and rock properties. Scope exists to develop, integrate and exploit citizen  
25 science projects to generate more and better data, and simultaneously include the public in the necessary  
26 discussions about hazard and risk.

27

## 28 Introduction

### 29 *Rationale & Objectives*

30 Faults in the crust slip in response to changes in stress or pore fluid pressure, and the source of these changes  
31 can be either natural or anthropogenic. Estimating the likelihood of slip on a particular fault for a given  
32 change in loading is critical for the industrial operations of the energy transition, especially geothermal  
33 energy and carbon sequestration and storage (CCS). The target formations of these operations are nearly  
34 always faulted and fractured to some degree, and experience from waste-water injection in the USA shows  
35 how even small changes in pore fluid pressure can trigger frequent seismic slip on these faults, with  
36 significant and widespread impact on society (e.g., Elsworth et al., 2016; Hincks et al., 2018; Hennings et al.,  
37 2019).

38 Stephenson et al. (2019) have shown how quantitative analysis of the subsurface is one of the key  
39 contributions that geoscientists can make to decarbonising energy production to meet national and  
40 international targets (e.g., CCC, 2019; IPCC, 2018). This includes the systematic geomechanical  
41 characterisation of rock formations, better understanding of fluid flow in fractured rocks, and the need for  
42 pilot projects to explore the scaling of behaviours from the laboratory to the field. Perhaps the most  
43 important aspect is to understand the public attitudes to subsurface decarbonisation technology  
44 (Stephenson et al., 2019; Roberts et al., 2021). Several recent studies have addressed the uncertainties in  
45 subsurface structural analysis of faulted rocks (Bond, 2015; Alcalde et al., 2017; Miocic et al., 2019). In this  
46 paper, we extend this work to specifically include fault stability, and argue that in order to simultaneously  
47 address public concerns and assess the viability of different schemes, we need a more rigorous approach to  
48 risking subsurface decarbonisation activities, especially where these involve changes in load on faulted rocks.

49 Useful measures of fault stability include slip and dilation tendency ( $T_s$  and  $T_d$  respectively) and fracture  
50 susceptibility ( $S_f$ , the change in fluid pressure to push effective stress to failure). These measures are defined  
51 as functions of the *in situ* stress, the orientation of the fault plane and, in the case of  $S_f$ , rock properties. It is  
52 widely recognised that the inputs for the prediction of stability are always uncertain, and to varying degrees:  
53 e.g., the vertical stress component of the *in situ* stress tensor can often be quite well constrained (to within

54 5%) from density log data, whereas the maximum horizontal stress is generally much harder to quantify. To  
55 improve and focus our predictions of fault stability in the subsurface, we need to accept and incorporate  
56 these uncertainties into our calculations. In this paper, we describe and explore a statistical approach to fault  
57 stability calculations, and then apply these methods to examples in geothermal energy, in both low- and  
58 high-enthalpy settings.

59 The specific aims of this paper are to:

- 60 1. describe and explain the Response Surface Methodology, and show how it can be applied to the  
61 probabilistic estimation of fault stability using a range of different measures;
- 62 2. explore how the main variables – in situ stress, fault orientation and rock properties – relate to the different  
63 measures of fault stability ( $T_s$ ,  $T_d$  and  $S_f$ ) using synthetic (i.e., artificial) data;
- 64 3. use case studies of active and proposed geothermal projects with publicly available data to illustrate the  
65 method, and then highlight the relationships between our known but uncertain input data and the predicted  
66 risk of fault slip.

### 67 *Importance & Previous work*

68 Small changes in stress or fluid pressure (e.g., a few MPa) from human activities can have significant  
69 consequences for fault stability. For example, waste-water injection from hydraulic fracturing (“fracking”)  
70 operations has led to dramatic increases in seismicity in Oklahoma since 2009 (Hincks et al., 2018) and in  
71 Texas since 2008 (Hennings et al., 2019; Hicks et al., 2021). The precise mechanical cause(s) of this seismicity  
72 is the subject of some debate, and could be due to either ‘direct’ pore fluid pressure transfer to basement-  
73 hosted faults leading to a reduction in effective stress, or ‘indirect’ poroelastic effects at a distance (Elsworth  
74 et al., 2016; Goebel et al., 2019). The concept of critically stressed faults in the crust (Townend & Zoback,  
75 2000), where relatively high permeability serves to maintain near-hydrostatic pore pressures, is consistent  
76 with the idea that only minor perturbations in loading can have dramatic consequences, even in areas of  
77 apparently low seismicity and, implicitly, low background tectonic loading.

78 In densely populated areas such as the UK, public support for, and confidence in, subsurface operations are  
79 key. Hydraulic fracturing operations for shale gas in Lancashire (UK) were stopped after earthquakes were  
80 triggered by fluid injection (Clarke et al., 2019). Triggered felt seismicity has already been reported at the  
81 United Downs deep geothermal pilot in Cornwall (Holmgren & Werner, 2021). Note that, in both of these  
82 cases, fracturing and/or fault slip are intrinsic to the success of the operation as they are needed to enhance  
83 fluid flow, and therefore earthquakes are inevitable. In detail, microseismicity (i.e.,  $M < 2$ ) is inevitable, but it  
84 is important to understand whether felt (i.e.  $M > 2$ ) seismicity can be forecast ahead of time. Furthermore,  
85 many sites for energy transition projects in the UK are located in (beneath) areas of extreme poverty and  
86 social deprivation, both rural (e.g., Cornwall, South Wales) and urban (e.g., Greater Manchester, Glasgow),  
87 and therefore the risks from these projects fall disproportionately on the less well off (Nolan, 2016;  
88 McLennan et al., 2019). To begin to address these complex issues, we need to quantify which faults are more  
89 or less likely to slip in response to induced changes in loading. One approach is to analyse data during  
90 subsurface operations and attempt to manage the consequences (e.g., Verdon & Budge, 2018). An  
91 alternative approach, and the one taken in this paper, is to look at the bigger picture before operations  
92 commence and reduce risk from the outset.

93 Various measures have been proposed to quantify the propensity or tendency of a given fault to slip (or  
94 open) in a known stress field. The following methods are based around an assumption of Mohr-Coulomb  
95 (brittle-plastic) failure which has been shown to capture the key aspects of faulting in the upper crust. Slip  
96 tendency ( $T_s$ ) was introduced by Morris et al. (1996) and is the simplest measure of fault stability, defined as:

$$97 \quad T_s = \tau / \sigma_n \quad (1)$$

98 where  $\tau$  is the shear stress and  $\sigma_n$  is the normal stress acting on the fault plane. These stress components in  
99 turn depend on the principal stresses and the orientation of the fault plane (see Lisle & Srivastava, 2004 for  
100 details). In the absence of cohesion, if the slip tendency on a fault equals or exceeds the coefficient of sliding  
101 friction, then the fault can be deemed “unstable”. This dimensionless index embodies the key mechanical

102 principle underlying Mohr-Coulomb shear failure: as the shear (“sliding”) stress acting on a fault plane rises  
 103 in relation to the normal (or “clamping”) stress, the fault approaches failure and will slip. Dilation tendency  
 104 ( $T_d$ ) has been defined to describe the propensity for a fault to open, or dilate, in a given stress regime:

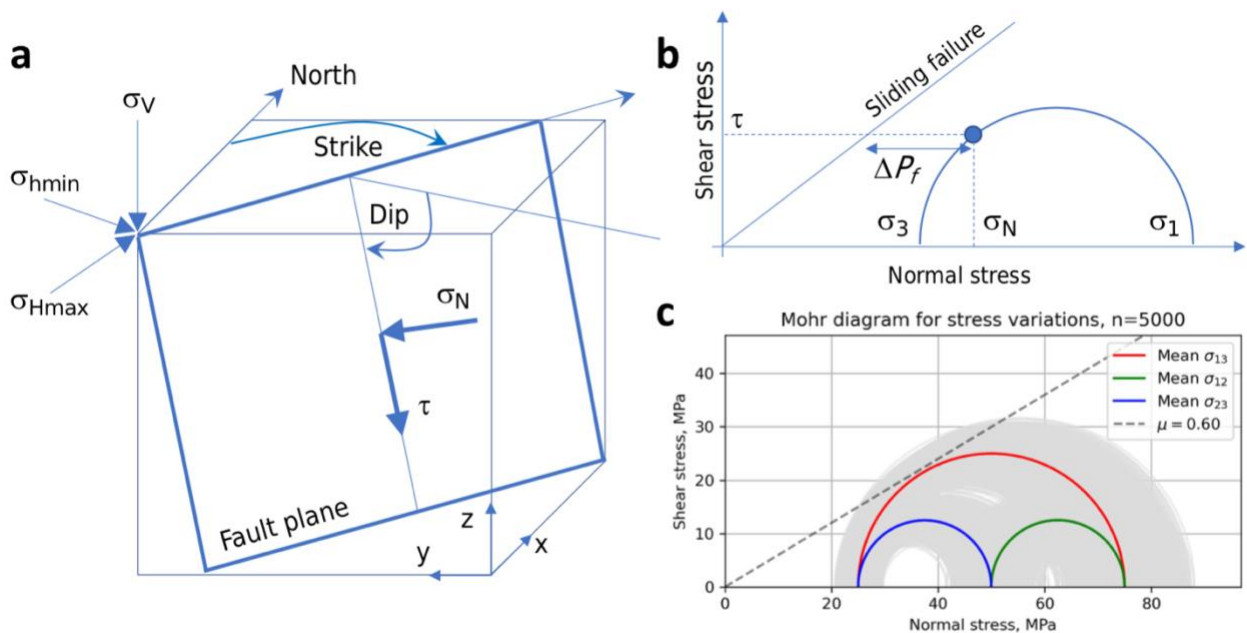
$$105 \quad T_d = (\sigma_1 - \sigma_n) / (\sigma_1 - \sigma_3) \quad (2)$$

106 where  $\sigma_1$  and  $\sigma_3$  are the principal stresses of the *in situ* stress tensor (Ferrill et al., 1999).

107 Most rocks in the upper crust are porous and permeable to some degree, and fault rocks are no exception,  
 108 so these rocks are generally fluid saturated. This implies that we should include pore fluid pressure and the  
 109 concept of effective stress in our assessment of fault stability. Fracture susceptibility ( $S_f$ ) is the change in pore  
 110 fluid pressure needed to push a stressed fault to failure (Streit & Hillis, 2004) and is defined by:

$$111 \quad S_f = \Delta P_f = (\sigma_n - P_f) - (\tau - C_0) / \mu \quad (3)$$

112 where  $P_f$  is the pore fluid pressure at the fault,  $C_0$  is the cohesive strength (or cohesion), and  $\mu$  is the  
 113 coefficient of sliding friction (see Figure 1b).



114  
 115 **Figure 1. a.** Schematic block diagram of a fault plane showing the terminology used in this paper. Also shown  
 116 are the cartesian and geographic reference frames and the Andersonian principal stresses. **b.** Mohr diagram  
 117 for a given state of stress (blue semi-circle) with normal ( $\sigma_n$ ) and shear stresses ( $\tau$ ) marked for a selected fault  
 118 plane orientation (blue dot). Failure envelope for frictional sliding (cohesion=0) also shown as straight blue  
 119 line. **c.** Mohr diagram depicting one of the key issues tackled in this paper: given uncertainty in the input  
 120 stress values (grey Mohr circles for the variation around the average principal stresses in red, blue and green),  
 121 what is the probability of failure? i.e., what percentage of all these stress states will intersect the failure  
 122 envelope?

123 Previous applications of these three measures of fault stability –  $T_s$ ,  $T_d$  and  $S_f$  – cover the full spectrum of rock  
 124 types and stress fields, from basins to basement and from extensional, contractional and wrench tectonic  
 125 settings. Applications within the domain of the energy transition include examples from geothermal energy  
 126 (both shallow and deep) and CCS. The original definition of fracture susceptibility by Streit & Hillis (2004) was  
 127 concerned with safe injection limits for CO<sub>2</sub> in potential reservoirs in Australia. Moeck et al. (2009) used slip  
 128 tendency to quantify the relative stability of different fault sets in different horizons in a geothermal reservoir  
 129 in the North German Basin, and Barcelona et al. (2019) used a similar method for Copahue geothermal  
 130 reservoir in Argentina. For CCS, Williams et al., (2016, 2018) have used slip tendency analyses of faults in  
 131 potential sandstone reservoirs on the UK continental shelf, including the North Sea and East Irish Sea basins.  
 132 The links between subsurface fluid flow, seismicity, and fault stability have recently been explored by Das &

133 Mallik (2020) for the Koyna earthquakes in India, and by Wang et al. (2020) for strike-slip faults in the Tarim  
 134 Basin of China.

135 Probabilistic approaches to fault stability have been adopted by various workers. In risking CO<sub>2</sub> storage for  
 136 an oil reservoir in the Williston basin, Ayash et al. (2009) used a features, events and processes (FEP)  
 137 approach to constrain the likelihood of occurrence of fault slip (based on slip tendency) and the severity of  
 138 the consequences, with their product defined as the risk. Rohmer & Bouc (2010) used RSM to assess cap rock  
 139 integrity for tensile or shear failure above deep aquifers in the Paris basin targeted for the storage of CO<sub>2</sub>.  
 140 Coupled RSM and Monte Carlo approaches to fault stability have been used by Chiaramonte et al. (2008) and  
 141 Walsh & Zoback (2016), following their initial application in the field of wellbore stability by Moos et al.  
 142 (2003). This Fault Slip Potential (FSP) method developed by Stanford (e.g., Chiaramonte et al., 2008 & Walsh  
 143 & Zoback, 2016) calculates the response surface for fracture susceptibility, with the in situ stress tensor  
 144 calculated by inversion of abundant seismicity data (focal mechanisms), and then uses a Monte Carlo  
 145 simulation to generate cumulative distribution functions (CDFs) of conditional probability of slip defined with  
 146 reference to an arbitrary pore pressure perturbation ( $\Delta P_f = 2$  MPa, in the case of Walsh & Zoback, 2016).  
 147 Note that FSP assumes cohesionless faults ( $C_0=0$ ) and hydrostatic pore fluid pressure, and that *conditional*  
 148 probability in this sense refers to the fact that we do not know where any particular fault is with respect to  
 149 the seismic cycle.

#### 150 *Conventions and layout for this paper*

151 In the sections below, we describe the underlying equations for measuring fault stability and then show how  
 152 we can use Response Surface Methodology (RSM) from engineering to explore the consequences of  
 153 uncertainties in the input variables. After assessing the quality of the solutions obtained from RSM, we then  
 154 apply a brute force Monte Carlo (MC) approach to generate cumulative distribution functions (CDFs) of the  
 155 different measures ( $T_s$ ,  $T_d$  and  $S_f$ ). The case studies use published, publicly available data to constrain the  
 156 input variable distributions and then a combined RSM/MC approach is used to explore the uncertainty in  
 157 fault stability in different settings.

158 In this paper, compressive stress is reckoned positive, with  $\sigma_1$  as the maximum compressive principal stress  
 159 and  $\sigma_3$  as the minimum principal stress. Stress states and fault regimes are assumed to be Andersonian, with  
 160 one principal stress vertical, although the underlying model and code could be changed to incorporate non-  
 161 Andersonian stress states with the addition of extra variables for the stress tensor orientation (Walsh &  
 162 Zoback, 2016). The likelihood of slip on a fault is assessed in the framework of Mohr-Coulomb failure, with  
 163 or without cohesion (Jaeger et al., 2009). Fault orientations are quantified as strike and dip, following the  
 164 right-hand rule: with your right hand flat on the fault plane and fingers pointing down dip, the right thumb  
 165 points in the direction (azimuth) of strike. The relationship between the geographical and cartesian reference  
 166 frames follows a North-East-Down convention. Figure 1 depicts the key terms and elements used in the  
 167 analysis, and Table 1 contains a list of terms and symbols used with units where appropriate.

Quantity	Symbol	Units
Maximum compressive stress	$\sigma_1$	MPa
Intermediate compressive stress	$\sigma_2$	MPa
Minimum compressive stress	$\sigma_3$	MPa
Vertical stress	$\sigma_v$	MPa
Maximum horizontal stress	$\sigma_{Hmax}$	MPa
Minimum horizontal stress	$\sigma_{Hmin}$	MPa
Azimuth of max. horizontal stress	$sHaz$	°
Pore fluid pressure	$P_f$	MPa
Coefficient of friction	$\mu$	dimensionless
Cohesive strength (or cohesion)	$C_0$	MPa
Slip tendency	$T_s$	dimensionless
Dilation tendency	$T_d$	dimensionless
Fracture susceptibility	$S_f$	MPa
Fault strike	$\varphi$	°

Fault dip	$\delta$	°
Shear stress on a fault plane	$\tau$	MPa
Normal stress on a fault plane	$\sigma_n$	MPa

168

169 **Table 1.** List of terms and symbols used in this paper, with units where appropriate.

170

171 **Statistical analysis of geomechanical fault stability**

172 *Introduction to Response Surface Methodology (RSM)*

173 RSM is widely used in engineering and industry along with a Design of Experiments approach, and often  
 174 employed to optimise a specific process of interest – e.g., to maximise the yield of a reaction given the input  
 175 variables of pressure, temperature, reactant mass etc. RSM is a large and growing field and is best considered  
 176 as a toolbox of different methods with a common mathematical basis. The governing equations for RSM were  
 177 derived by Box & Wilson (1951). The core idea is that a response  $y$  can be represented by a polynomial  
 178 function of a number ( $q$ ) of input variables  $x_1 - x_q$ :

179 
$$y = f(x_1, x_2, \dots, x_q) \quad (4)$$

180 Each of the  $q$  input variables can be represented by either a discrete set of measurements made in the  
 181 laboratory (or field) or drawn from appropriate statistical distributions (normal/Gaussian, skewed normal,  
 182 Von Mises etc.). The simplest polynomial function that relates  $y$  and  $x$  is a linear one:

183 
$$y_i = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2} + \dots + \beta_q x_{iq} + \epsilon_i \quad (5)$$

184 
$$y_i = \beta_0 + \sum_{j=1}^q \beta_j x_{ij} + \epsilon_i \quad (6)$$

185 where  $\beta_q$  are the coefficients (to be determined),  $y_i$  is the set of observations of the response ( $i = 1, 2, \dots, N$ ),  
 186 and  $x_{ij}$  are the input variables ( $j = 1, 2, \dots, q$ ).  $\epsilon$  is the experimental error, and the number of ‘observations’  $N$   
 187  $> q$ , the number of input variables. This is therefore a multiple regression model linking the response  $y$  to  
 188 more than one (i.e., multiple) independent variables,  $x$ .

189 A more complex polynomial relationship is the quadratic form:

190 
$$y = \beta_0 + \sum_{j=1}^q \beta_j x_j + \sum_{j=1}^q \beta_{jj} x_j^2 + \sum_{i < j}^q \beta_{ij} x_i x_j + \epsilon \quad (7)$$

191 This 2<sup>nd</sup> order multiple regression model contains all the terms of the linear (1<sup>st</sup> order) model, but also extra  
 192 terms for the squares and cross-products of the input variables (second and third terms on the RHS of  
 193 equation 7).

194 To define a response surface, either linear or quadratic, we need to calculate the values of the  $\beta_q$  coefficients.  
 195 We can rewrite the key equations in matrix form:

196 
$$\mathbf{y} = \mathbf{X}\boldsymbol{\beta} + \boldsymbol{\epsilon} \quad (8)$$

197 where  $\mathbf{y}$  is an ( $N \times 1$ ) vector of observations (or calculations),  $\mathbf{X}$  is an ( $N \times k$ ) matrix of input variable values ( $k$   
 198  $= q + 1$ ), and  $\boldsymbol{\beta}$  is a ( $k \times 1$ ) vector of regression coefficients. We solve this system of equations using the  
 199 standard linear algebra technique of least squares regression (Myers et al., 2016):

200 
$$\hat{\boldsymbol{\beta}} = (\mathbf{X}'\mathbf{X})^{-1}\mathbf{X}'\mathbf{y} \quad (9)$$

201 The response surface (linear or quadratic) is then defined by

202 
$$\hat{y} = \mathbf{X}\hat{\boldsymbol{\beta}} \quad (10)$$

203 The values used in  $\mathbf{X}$  are chosen to efficiently span the parameter space. A typical sampling design for  $\mathbf{X}$  is  
 204 called the  $3^q$  model with 3 values of each variable, usually the minimum, mean (or mode) and maximum. For  
 205 slip tendency,  $q = 6$  and this means we use  $3^q = 3^6 = 729$  data points to calculate the response surface. In

206 practice, coded variables are used in  $\mathbf{X}$  where the absolute values for the minimum, mean and maximum of  
 207 each variable are scaled to  $-1$ ,  $0$  and  $+1$  respectively, and then scaled back when the response surface is used  
 208 in the Monte Carlo simulation (Myers et al., 2016).

209 The response surface – i.e., the set of  $\beta$  coefficients – is defined using a limited number of sample points,  
 210 depending on the chosen sample design ( $3^q$  in the examples used in this paper; other variants exist – see  
 211 Myers et al., 2016 for details). To explore the possible variations of a response more fully, we use a Monte  
 212 Carlo (MC) approach of pre-defined size ( $N_{MC} = 5,000$  in the examples in this paper). The MC simulation uses  
 213 the response surface calculated from the design points to calculate the responses for  $N_{MC}$  combinations of  
 214 input variables drawn from their distributions. This produces a statistically viable ensemble of response  
 215 values from which we can infer the probability of the response with respect to a chosen threshold.

216 With respect to fault stability, we can use RSM to produce a parameterised relationship – the response  
 217 surface in  $q$  dimensions – between a stability measure of interest and the  $q$  input variables. In the case of slip  
 218 tendency  $T_s$ , we can rewrite the components of equation 1 in terms of the measurable input quantities as  
 219 follows:

$$220 \quad \tau = \sqrt{(\sigma_1 - \sigma_2)^2 l^2 m^2 + (\sigma_2 - \sigma_3)^2 m^2 n^2 + (\sigma_3 - \sigma_1)^2 l^2 n^2} \quad (11)$$

$$221 \quad \sigma_n = \sigma_1 l^2 + \sigma_2 m^2 + \sigma_3 n^2 \quad (12)$$

222 where  $l$ ,  $m$  and  $n$  are the direction cosines of the normal (pole) to the fault plane given by

$$223 \quad l = \sin \delta \sin \phi \quad (13a)$$

$$224 \quad m = -\sin \delta \cos \phi \quad (13b)$$

$$225 \quad n = \cos \delta \quad (13c)$$

226 where  $\phi$  is the fault strike and  $\delta$  is the fault dip, in a North-East-Down reference frame (Allmendinger et al.,  
 227 2012).

228 All terms on the right-hand sides of equations 11-13 are uncertain to some degree, therefore estimating the  
 229 uncertainty of  $T_s$ , and as importantly, the *key controls on the uncertainty of  $T_s$* , in terms of these input  
 230 variables, is non-trivial. This difficulty in estimating and visualising possible variations in our estimates of  $T_s$   
 231 is exacerbated by the recognition that each of the input variables may be distributed differently: some  
 232 quantities (e.g., the principal stresses) may follow normal (Gaussian) statistics, whereas others (e.g., strike,  
 233 dip, sHmax azimuth) will follow Von Mises distributions. In the case of fracture susceptibility ( $S_f$ , equation 3),  
 234 it is even more complicated with the addition of three further input variables for friction, cohesion and pore  
 235 fluid pressure. Measurements or calculations of coefficients of friction and cohesive strength often display  
 236 asymmetric or skewed distributions (skewed high or low), and this adds further complexity to the task of  
 237 estimating and constraining fault stability from the data at hand.

### 238 *Worked Example 1: Slip tendency from synthetic input data*

239 The calculations presented in this paper were all performed with the custom pfs (**p**robability of **f**ault **s**lip)  
 240 package, written by the first author (DH) in Python 3, and freely available on GitHub (see Code Availability,  
 241 below).

242 The first example calculates a response surface for slip tendency ( $T_s$ ) from  $q=6$  input variables: the  
 243 magnitudes of the three principal stresses of the *in situ* stress tensor ( $\sigma_1$ ,  $\sigma_2$ ,  $\sigma_3$ ) assumed Andersonian with  
 244 one principal stress vertical, the azimuth of the maximum horizontal stress (*sHaz*), and the strike and dip of  
 245 the fault plane. This response surface is then used in a Monte Carlo simulation ( $N_{MC} = 5,000$ ) to generate a  
 246 CDF of  $T_s$  values for the fault. The specific Python code to run this example in the pfs package is wrapped in  
 247 a Jupyter notebook available on GitHub (WorkedExample1.ipynb).

248 The first task is to define the distributions of the input variables. In pfs, examples are shown for normal,  
 249 skewed normal and Von Mises (circular normal) distributions, but other statistical distributions are allowed.  
 250 Table 2 and Figure 2 describe the ranges and moments of these distributions for each input variable. For this

251 example, the normally distributed principal stresses are defined with a variation (standard deviation) of 5%  
 252 of their central (mean) value, and the Von Mises distributions of the azimuthal variables (sHaz, strike and dip)  
 253 all have  $\kappa = 200$  to model their dispersion about their mean. The fault of interest strikes  $060^\circ$  and dips  $60^\circ$  to  
 254 the south (right hand rule). The key questions to be addressed by this example are:

- 255 1. given these uncertainties in the input stresses and orientation data, how does the estimation of  $T_s$   
 256 vary? What is the range and the mode?
- 257 2. which variables exert the greatest (and least) control on the predicted variation in  $T_s$ ?

258 We first build a response surface using a  $3^q$  design, i.e., 3 data points for each variable – minimum, mean and  
 259 maximum – and for  $T_s$ ,  $q = 6$ . This means we calculate the response surface from  $3^6 = 729$  data points. We  
 260 compare a calculated linear response surface with a quadratic response surface, using a normal probability  
 261 plot of residuals (Figure 3). These residuals are the differences between the values of  $T_s$  derived from the  
 262 observations (taken from the input distributions shown in Table 2 (upper) and Figure 2), and the calculated  
 263 values of  $T_s$  using the  $\beta$  coefficients derived by least squares regression i.e., the response surface. The  
 264 adjusted  $R^2$  value for the quadratic 2<sup>nd</sup> order model is significantly better than that for a linear 1<sup>st</sup> order model,  
 265 and we use quadratic models throughout the rest of this paper. More detailed inspection of the quality of fit  
 266 between the response surface and the observations is possible, including analysis of variance, main effects  
 267 plots and the use of t-statistics for each input variable to quantify their significance to the definition of the  $\beta$   
 268 coefficients (Myers et al., 2016). In practice, visualising sections of the response surface for individual  
 269 variables is generally sufficient (see below; Moos et al., 2003; Walsh & Zoback, 2016).

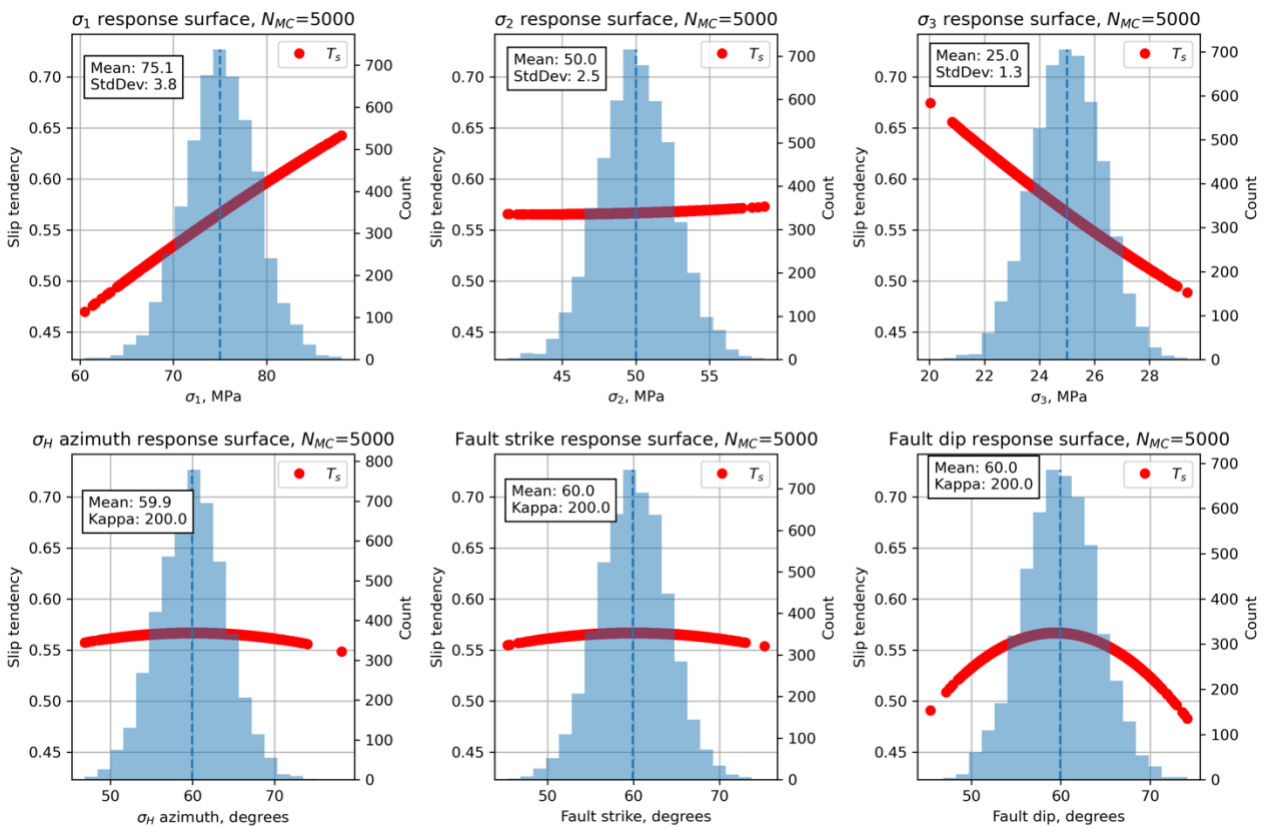
Variable	Mean	Standard deviation ( $\kappa$ for Von Mises)	Units	Distribution	Comments
<b>Worked Example 1 – Synthetic <math>T_s</math> – modelled depth=3 km</b>					
$\sigma_v$ , vertical stress	75.0	3.75 (5% of mean)	MPa	Normal	Lithostatic for depth of 3 km, assuming average rock density of $2500 \text{ kg m}^{-3}$
$\sigma_H$ , max. horizontal stress	50.0	2.5 (5% of mean)	MPa	Normal	Andersonian normal faulting regime
$\sigma_h$ , min. horizontal stress	25.0	1.25 (5% of mean)	MPa	Normal	
Azimuth of $\sigma_{Hmax}$	060	$\kappa=200$	$^\circ$	Von Mises (circular Normal)	
Fault strike	060	$\kappa=200$	$^\circ$	Von Mises (circular Normal)	
Fault dip	60.0	$\kappa=200$	$^\circ$	Von Mises (circular Normal), truncated at 0 and 90	
<b>Worked Example 2 – Synthetic <math>S_f</math> – modelled depth=3 km</b>					
$\sigma_v$ , vertical stress	75.0	7.5 (10% of mean)	MPa	Normal	Lithostatic for depth of 3 km, assuming average rock density of $2500 \text{ kg m}^{-3}$
$\sigma_H$ , max. horizontal stress	55.0	5.5 (10% of mean)	MPa	Normal	
$\sigma_h$ , min. horizontal stress	35.0	3.5 (10% of mean)	MPa	Normal	



$P_f$ , pore fluid pressure	30.0	3.0 (10% of mean)	MPa	Normal	Hydrostatic for depth of 3 km, assuming fluid density=1000 kg m <sup>-3</sup>
Azimuth of $\sigma_{Hmax}$	060	$\kappa=200$	°	Von Mises (circular Normal)	
Fault strike	060	$\kappa=200$	°	Von Mises (circular Normal)	
Fault dip	60.0	$\kappa=200$	°	Von Mises (circular Normal), truncated at 0 and 90	
Friction, $\mu$	0.6	0.12 (20% of mean)	n/a	Skewed normal	$\alpha = -3$ i.e., skewed low
Cohesion, $C_0$	20.0	2.0 (10% of mean)	MPa	Skewed normal	$\alpha = +3$ i.e., skewed high

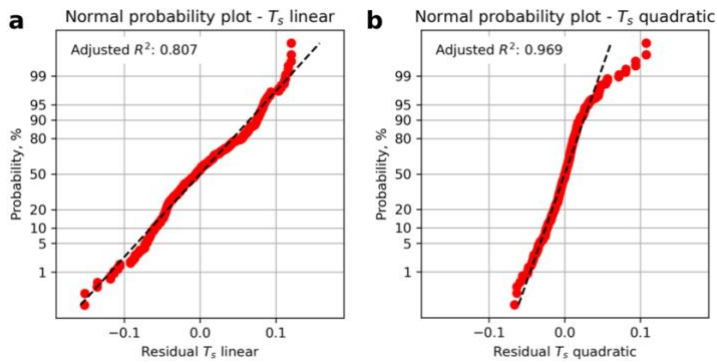
270

271 **Table 2.** Table of input variable distributions for the synthetic models in Worked Examples 1 and 2.



272

273 **Figure 2.** Histograms of input variables used to calculate slip tendency  $T_s$  for the synthetic distributions shown  
274 in Table 2.



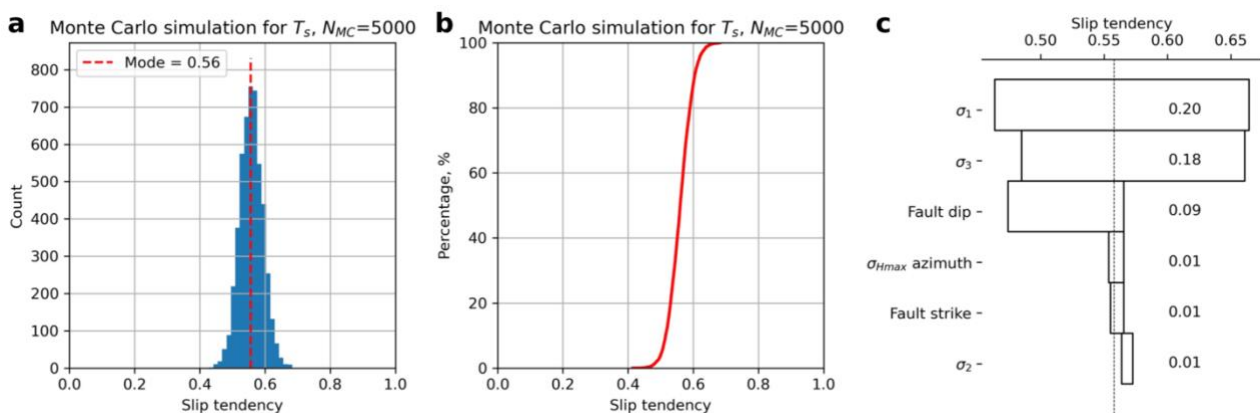
275

276 **Figure 3.** Residual plots for linear and quadratic response surfaces for slip tendency using synthetic data. The  
 277 quadratic fit has a higher value of the adjusted  $R^2$  parameter and is therefore deemed better in this case.

278 Having generated the quadratic response surface for  $T_s$  for these input distributions, we can now use it to  
 279 perform a Monte Carlo (MC) simulation with the aim of generating a statistically viable ensemble from which  
 280 we can infer the probability of  $T_s$  exceeding a critical value of sliding friction. The results from the MC analysis  
 281 of  $T_s$  are shown in Figure 4. The histogram of all values of  $T_s$  shows a symmetrical and rather narrow  
 282 distribution with a modal value of about 0.56 (Figure 4a). The CDF of all values of  $T_s$  also shows this narrow  
 283 and symmetrical distribution (Figure 4b).

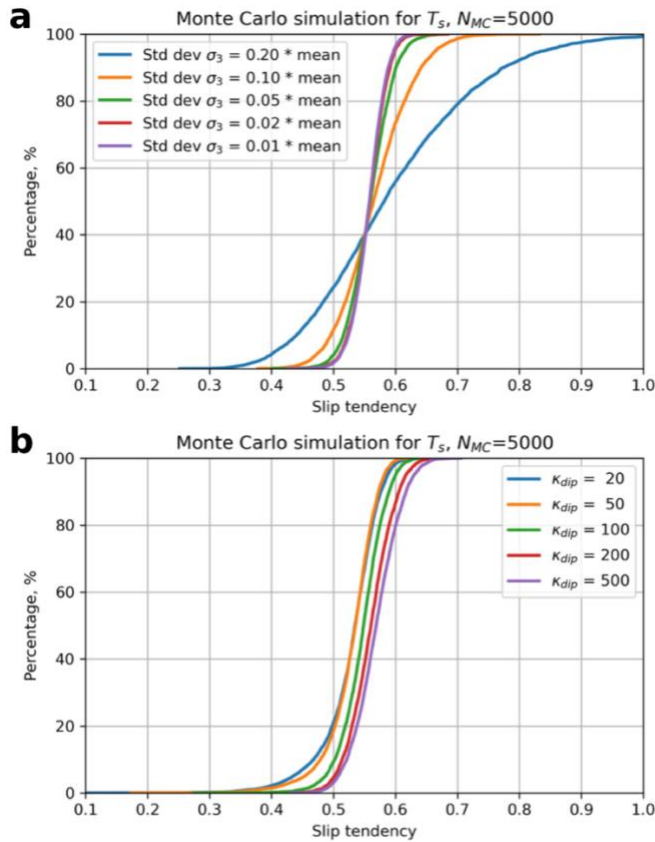
284 A response surface of more than two variables is not easy to visualise. One approach is to take sections  
 285 through the surface at specific values of all but one variable and graph that. The red lines shown in Figure 2  
 286 depict the response surface for that variable with all other variables held at their mean values. Thus the red  
 287 line in Figure 2a shows the variation in  $T_s$  as  $\sigma_1$  varies with all other variables ( $\sigma_2$ ,  $\sigma_3$ ,  $sHaz$ ,  $\varphi$  and  $\delta$ ) held at  
 288 their mean values. There is a clear positive correlation of increasing  $T_s$  with increasing  $\sigma_1$ , as expected from  
 289 the definition of  $T_s$  and its underlying dependence on differential stress ( $=\sigma_1 - \sigma_3$ ); the clear negative  
 290 correlation of  $T_s$  with  $\sigma_3$  shown in Figure 2c confirms this. Many of the response surface sections shown in  
 291 Figure 2 are quasi-linear, but some are not: in particular, the dependencies of  $T_s$  on  $sHaz$ , strike and dip are  
 292 all non-linear, and this further justifies the selection of a 2<sup>nd</sup> order quadratic response surface model.

293 A useful way to visualise the results from the response surface calculated by the MC simulation is the tornado  
 294 plot shown in Figure 4c. Here the ranges of  $T_s$  for each input variable (shown as red lines over the histograms  
 295 in Figure 2) are plotted to show the relative sensitivity of  $T_s$  to each variable. Variables are ranked from the  
 296 largest range at the top to the lowest range at the bottom. Again, the core dependence of  $T_s$  on differential  
 297 stress ( $=\sigma_1 - \sigma_3$ ) is apparent, with  $\sigma_1$  and  $\sigma_3$  ranked highest in the plot. Interestingly, fault dip is ranked the  
 298 next highest in terms of sensitivity and this reflects the geometry of this particular example. The Andersonian  
 299 stress regime is for normal faulting, with  $\sigma_1$  vertical.  $\sigma_2$  is oriented parallel to fault strike ( $sHaz = strike = 060$ ),  
 300 and the fault dips at 60. This fault is therefore ideally oriented for slip in this stress field. Small changes to dip  
 301 will influence the ratio of  $\tau$  to  $\sigma_n$ , and therefore  $T_s$ .



302

303 **Figure 4.** Output from Monte Carlo simulation ( $N_{MC}=5,000$ ) of slip tendency calculated using a quadratic  
 304 response surface from synthetic input data. **a.** Histogram of calculated slip tendency values, in this case  
 305 showing a quasi-normal distribution with a mode of  $\sim 0.55$ . **b.** Cumulative distribution function (CDF) of  
 306 calculated slip tendency values, showing the range in values from  $\sim 0.4$  to  $\sim 0.7$ . **c.** Tornado plot showing  
 307 relative sensitivity to the input variables. The vertical dashed line shows the modal (most frequent) value of  
 308  $T_s$  from the MC ensemble.



309 **Figure 5.** Output from Monte Carlo sensitivity tests for slip tendency,  $T_s$ . **a.** Effect of variation in standard  
 310 deviation of the least principal stress,  $\sigma_3$ . **b.** Effect of variation in dispersion ( $\kappa$  parameter of the Von Mises  
 311 distribution) of fault dip.  
 312

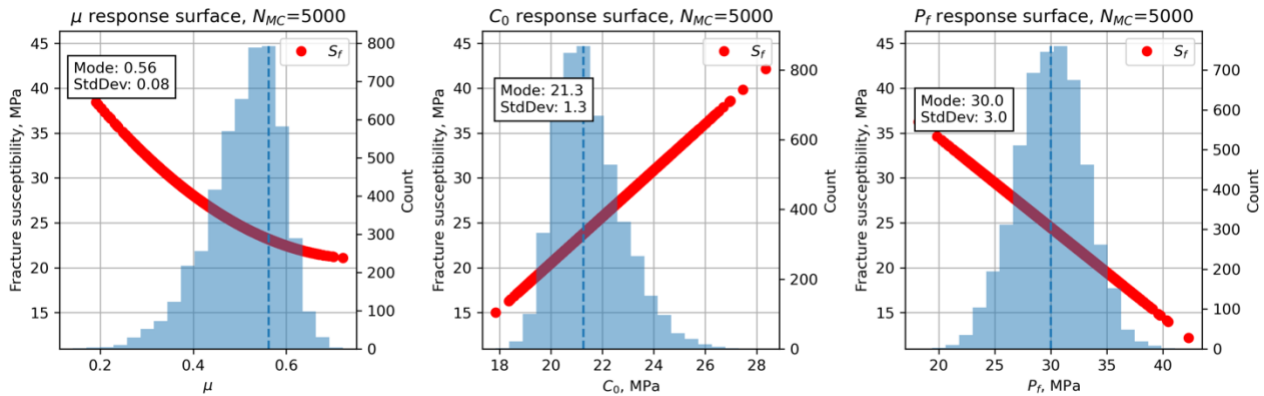
313 We can use a Monte Carlo approach to explore these sensitivities in more detail. Given the shape of the  
 314 response surface sections shown in Figure 2 and the ranking of variables in Figure 4c, we can quantify how  
 315 more or less variation in the inputs will affect the predicted  $T_s$ . Figure 5 shows the results of this sensitivity  
 316 analysis for  $\sigma_3$  and fault dip. The most significant effect on the CDF of  $T_s$  is produced by increasing the  
 317 variation in  $\sigma_3$  to 20% of the mean. This level of uncertainty for the minimum stress is not unreasonable in  
 318 real-world scenarios (see Case Studies below). Increased uncertainty in  $\sigma_3$  at this level leads to a  $\sim 20\%$  chance  
 319 of  $T_s$  being in excess of 0.7 ( $p = 0.8$  for  $T_s \leq 0.7$  from Figure 5a). Increased uncertainty in fault dip is achieved  
 320 by varying the dispersion parameter  $\kappa$  of the Von Mises distribution (lower values of  $\kappa =$  more dispersed).  
 321 Very disperse distributions of fault dip with  $\kappa = 20$  only change  $T_s$  by  $< 0.1$ .

### 322 *Worked Example 2: synthetic Sf*

323 We can explore variations in predicted fracture susceptibility using the same principles as for slip tendency,  
 324 but adjusted by incorporating three new variables as required by equation 3 – pore fluid pressure, friction  
 325 coefficient and cohesion (code in GitHub: WorkedExample2.ipynb). The number of variables  $q$  is now 9, and  
 326 therefore the design space used to compute the response surface is  $3^q = 3^9 = 19,683$  data points. In practice  
 327 this means a slower run-time, but still only takes a few minutes on a modern processor.

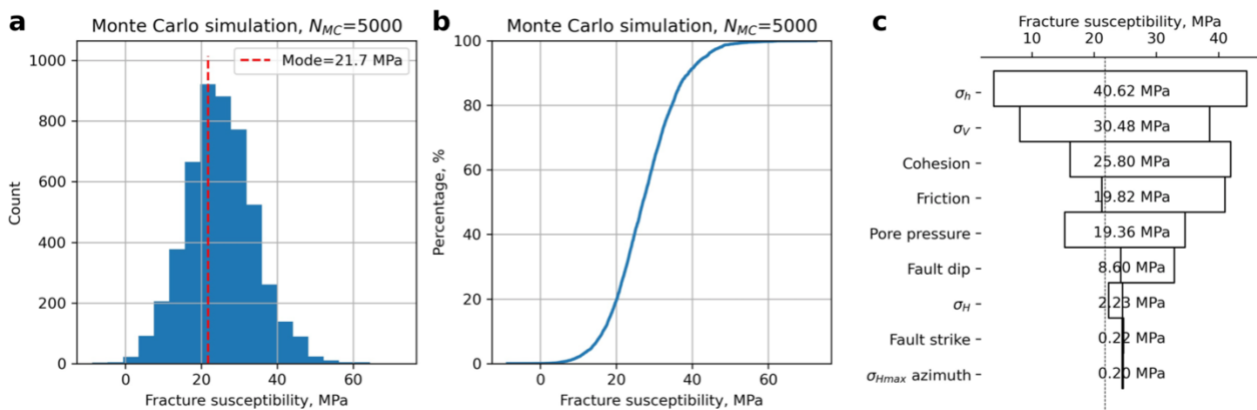
328 For this example, we use the same stress tensor as for the  $T_s$  example, with  $\sigma_1$  as the maximum principal  
 329 stress and vertical, i.e., an Andersonian normal fault regime for a depth of approximately 3 km. We constrain

330 the *in situ* pore pressure with a symmetrical normal distribution with a mean value of 30 MPa, which is  
 331 approximately hydrostatic for a depth of 3 km, and with a variation of 10% of this mean. Friction is  
 332 constrained by a skewed normal distribution with a mode of 0.56 and  $\alpha = -3$ , i.e., skewed towards lower  
 333 values. This shape of distribution for friction coefficients is consistent with previous studies (e.g., Moos et al.,  
 334 2003; Walsh & Zoback, 2016) but is open to question (see Discussion). Similarly for cohesion, we use a skewed  
 335 normal distribution with a mode of 21 MPa and  $\alpha = +3$ , i.e., skewed towards higher values again consistent  
 336 with previous work. These input variable distributions are documented in Table 2 (lower) and shown in the  
 337 histograms of Figure 6.



338

339 **Figure 6.** Histograms of the input variables, in addition to those shown in Figure 2, used to calculate fracture  
 340 susceptibility for the synthetic distributions shown in Table 2. Note the skewed (asymmetric) distributions  
 341 for  $\mu$  and  $C_0$ .

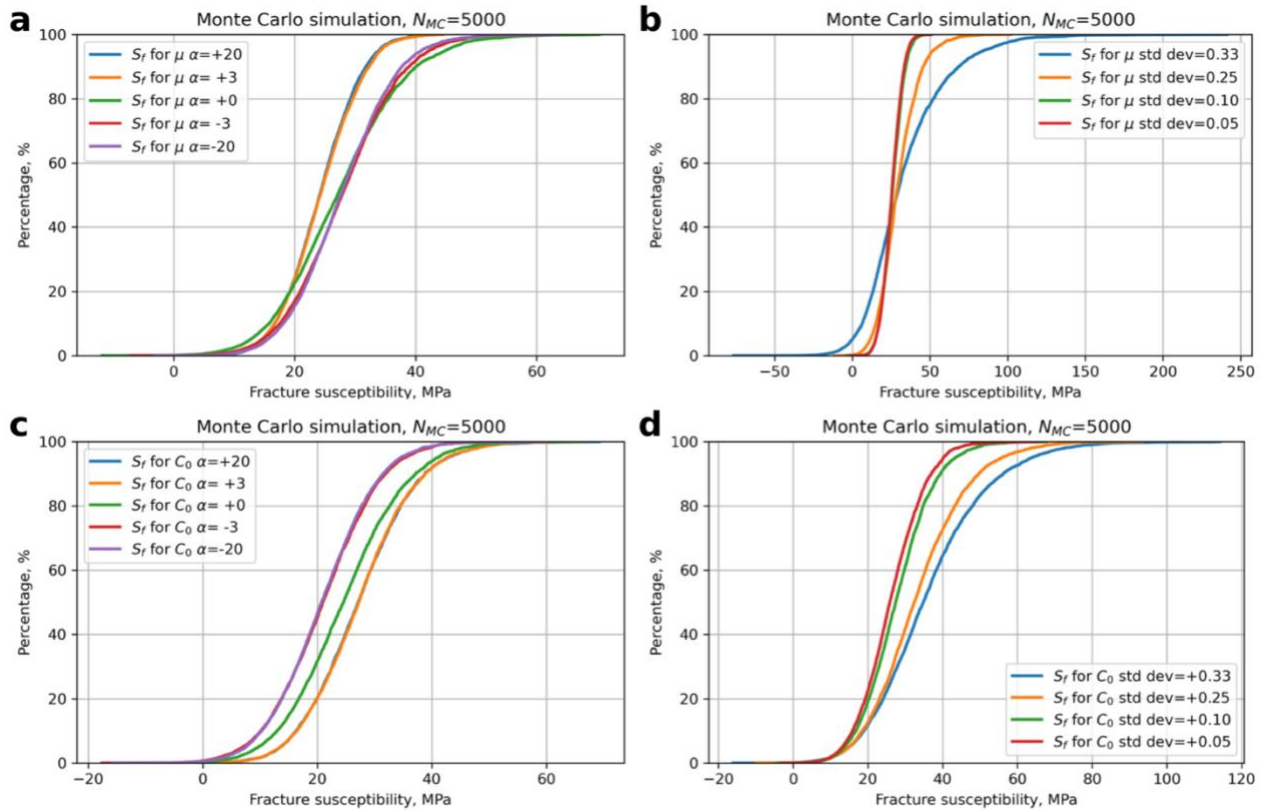


342

343 **Figure 7.** Output from Monte Carlo simulation ( $N_{MC}=5,000$ ) of fracture susceptibility calculated using a  
 344 quadratic response surface from synthetic input data. **a.** Histogram of calculated fracture susceptibility,  
 345 showing a quasi-normal distribution with a mode of 21.7 MPa. **b.** Cumulative distribution function (CDF) of  
 346 calculated fracture susceptibility, showing the range in values from just less than 0 to about 60 MPa. **c.**  
 347 Tornado plot of relative sensitivities of the input variables used to calculate fracture susceptibility.

348 We calculate a quadratic response surface and use a Monte Carlo simulation ( $N_{MC} = 5,000$ ) to generate the  
 349 ensemble summarised in Figure 7. The mode of the distribution of  $S_f$  is 21.7 MPa meaning that, on average,  
 350 an increase in pore fluid pressure of about 22 MPa above the average *in situ* value of 30 MPa is needed to  
 351 push the effective stress state to Mohr-Coulomb failure. The histogram in Figure 7a is approximately  
 352 symmetrical, perhaps with a slight skewness to higher values, and this is reflected in the CDF shown in Figure  
 353 7b. The distribution is overwhelmingly positive, meaning that this fault is almost unconditionally stable for  
 354 any change in pore fluid pressure, *at these conditions*. The response surface sections for  $\mu$ ,  $C_0$  and  $P_f$  shown  
 355 in Figure 6 (red lines) all show a strong influence on the fracture susceptibility, and these are confirmed in  
 356 the tornado plot of Figure 7c. Pore fluid pressure exhibits a negative correlation with  $S_f$  (Figure 6c) which is  
 357 consistent with the general principle of effective stress: i.e., if the original *in situ* pore pressure is already

358 high, it only takes a small perturbation (small  $\Delta P_f = S_f$ ) to promote sliding failure. The response to changes in  
 359  $\mu$  and  $C_0$  is more interesting (Figure 6a and b). For this magnitude of cohesion, the effect of cohesion on  $S_f$  is  
 360 greater than that of  $\mu$  ( $C_0$  ranks higher than  $\mu$  in the tornado plot, Figure 7c), and the dependence of  $S_f$  on  $\mu$   
 361 is negative. However, this relationship is not general as will be shown in the Case Study for the Porthtowan  
 362 Fault Zone (see below).



363

364 **Figure 8.** Sensitivity of fracture susceptibility to variations in  $\mu$  and  $C_0$ . Note the changes in scale along the x-  
 365 axis between the plots.

366 The relative asymmetries of the skewed normal distributions for  $\mu$  and  $C_0$  have already been noted. Given  
 367 their significant effect on  $S_f$  (high ranking in the tornado plot, Figure 7c), it is useful to explore how the  
 368 *skewness* of these distributions might influence  $S_f$ . Figure 8 shows the results of repeated Monte Carlo  
 369 sensitivity tests for  $\mu$  (Figure 8a, b) and  $C_0$  (Figure 8c, d). For friction, a positive skewness to higher values ( $\alpha$   
 370  $> 0$ ) would tend to reduce  $S_f$  – i.e., faults would be less stable. For cohesion, the opposite is true – a negative  
 371 skewness ( $\alpha < 0$ ) would make faults less stable to changes in  $P_f$ . These asymmetries are opposite to the ones  
 372 used in the main Worked Example 2 and used by other workers (see Discussion). Widening the distributions  
 373 for  $\mu$  or  $C_0$  by increasing their standard deviations (and retaining the original  $\alpha$  values) tends to broaden the  
 374 distribution of predicted  $S_f$  with asymmetry to higher (i.e., more stable) values.

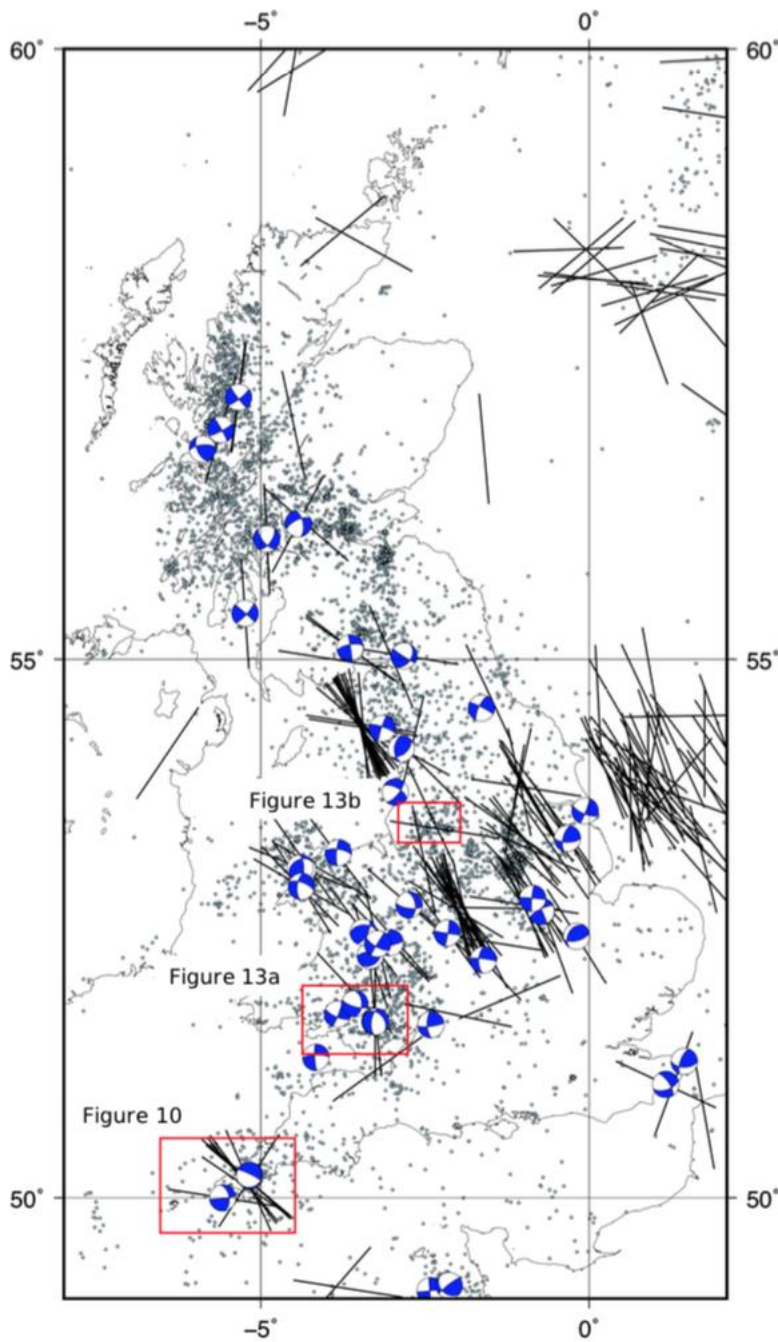
375

### 376 Case Studies

377 The case studies have been chosen to illustrate how a combined RSM/MC approach can be used to estimate  
 378 the probability of slip on one or more faults, and to show that even with relatively good – i.e., complete –  
 379 input data, these predictions highlight that industrial operations remain significantly hazardous, with a  
 380 greater than 1 in 3 chance of slip on many faults across different settings. Selected specific aspects of the  
 381 modelling and the visualisation of results are emphasised in each case study. Figure 9 shows a map of the UK  
 382 with the case study areas marked, together with the locations of instrumentally-recorded earthquakes and  
 383 their focal mechanisms (Baptie, 2010). Also shown are data from the World Stress Map database of 2016  
 384 (Heidbach et al., 2018) indicating the orientation of the maximum horizontal stress. A basic observation from  
 385 this map is the level of complexity and heterogeneity in the present day seismotectonics of the UK, reflecting



386 the variation in the subsurface geology. However, there is a broad prevalence of NW-SE trending  $\sigma_{Hmax}$   
387 directions and strike-slip earthquake mechanisms.

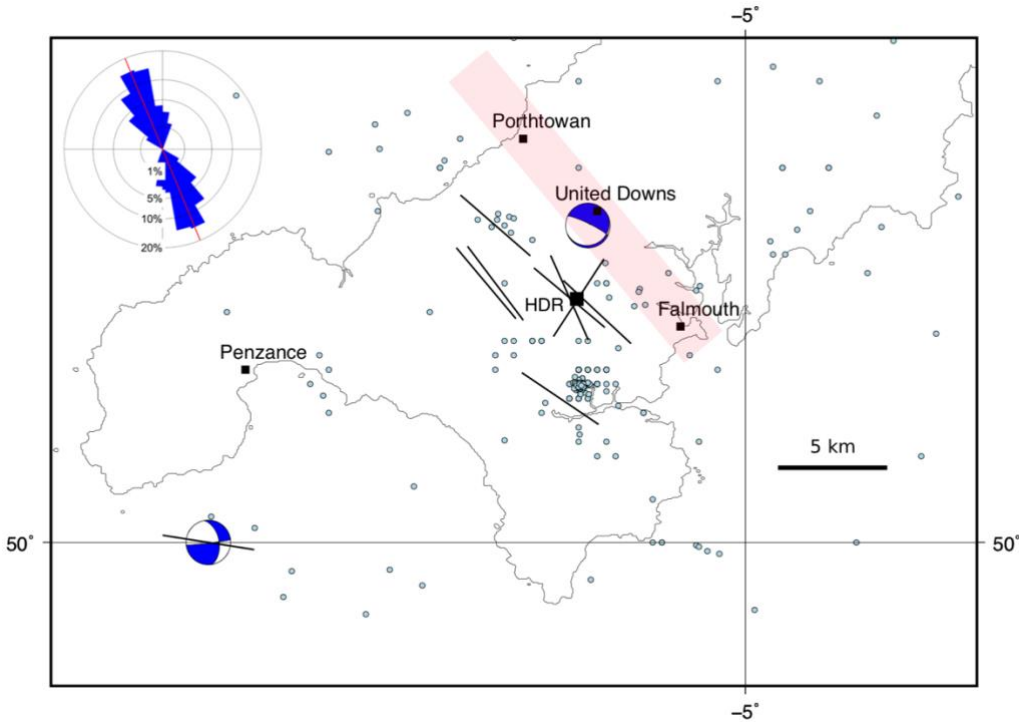


388  
389 **Figure 9.** Map of most of the UK showing the locations of the selected case studies. Also shown: epicentres  
390 of seismicity (light blue dots; BGS catalogue – Musson, 1996), focal mechanisms (blue and white; Baptie,  
391 2010), and orientations of the maximum horizontal stress (black lines; World Stress Map data – Heidbach et  
392 al., 2018).

393 *1. Porthtowan Fault Zone in Cornwall, UK*

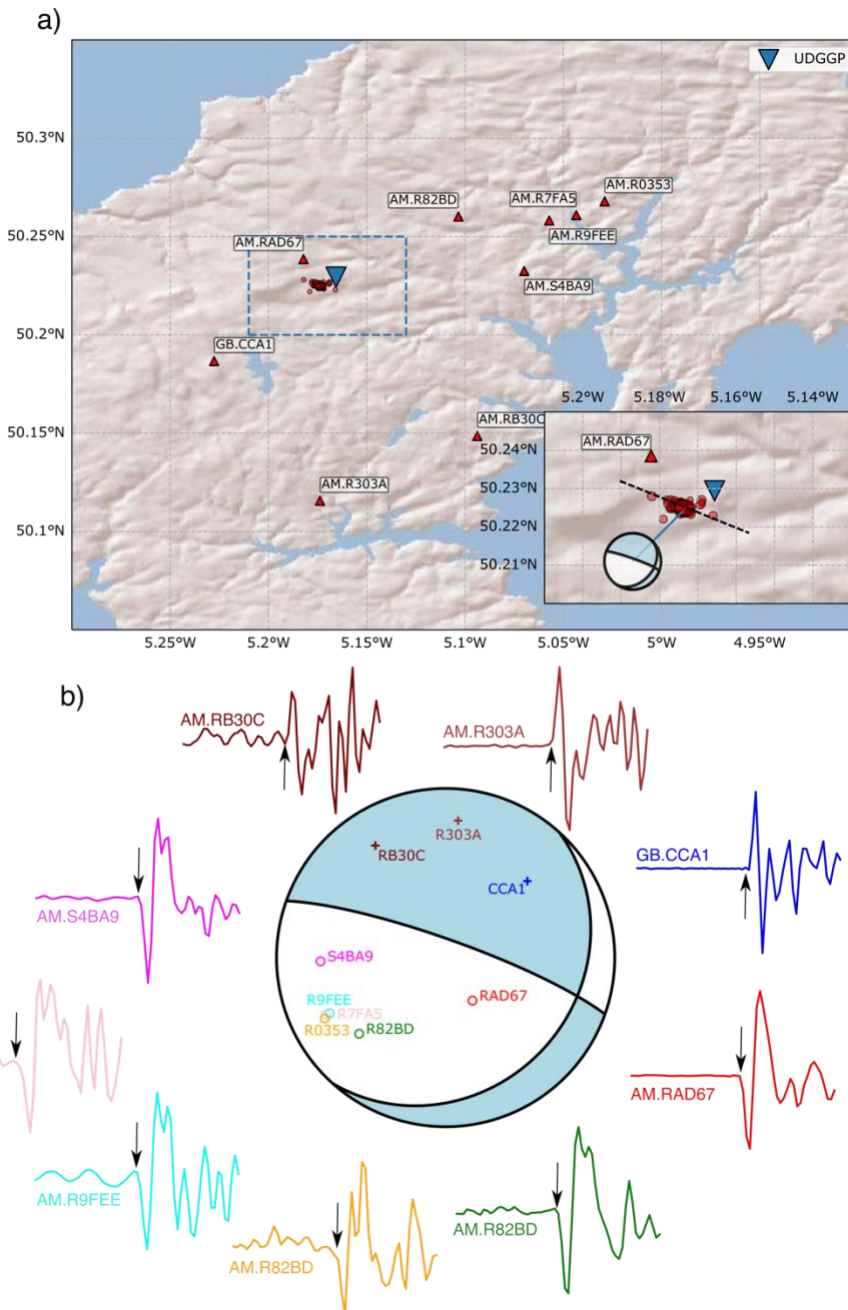
394 The Porthtowan Fault Zone (PFZ) cuts the Carnmenellis granite in Cornwall in southwest England (Figure 10).  
395 This granite is a target for deep high-enthalpy geothermal energy due to its high radiogenic heat production  
396 (Beamish & Busby, 2016). Following the Hot Dry Rock (HDR) project in the 1980s (Pine & Batchelor, 1984;  
397 Batchelor & Pine, 1986), the United Downs pilot project has drilled two boreholes (UD-1, UD-2) to intersect  
398 the fault zone at depths of about 5,275 m and 2,393 metres, respectively, making UD-1 the deepest onshore  
399 borehole in the UK. The pilot project relies on shear-enhanced stimulation of pre-existing fractures (joints,

400 partially filled veins and faults) to drive fluid flow from the shallow injector (UD-2) to the deeper producer  
 401 (UD-1). Temperatures at the base of UD-1 have been predicted at about 200°C (Ledingham et al., 2019).  
 402 Shearing and downward flow of injected fluid was observed in boreholes as part of the earlier HDR project  
 403 and tracked with measured microseismicity (Pine & Batchelor, 1984; Green et al., 1988; Li et al., 2018).



404  
 405 **Figure 10.** Map of South West England showing: selected population centres, the United Downs deep  
 406 geothermal pilot project and the former Hot Dry Rock project (black squares); epicentres of seismicity (light  
 407 blue dots; BGS catalogue – Musson, 1996); focal mechanisms (blue and white; Baptie, 2010); and orientations  
 408 of the maximum horizontal stress (black lines; World Stress Map data – Heidbach et al., 2018). Approximate  
 409 trend and extent of the Porthtowan Fault Zone shown in pale red. Inset shows an equal area rose diagram  
 410 with strikes of fault segments in the Porthtowan Fault Zone measured on BGS Falmouth sheet 352 ( $N=140$ ;  
 411 circular mean strike= $158^\circ$ , circular standard deviation= $27^\circ$ ).

412 Figure 10 shows a map of SW England overlain with seismicity data from the BGS (Musson, 1996). The PFZ is  
 413 poorly exposed inland, and runs NNW-SSE from Porthtowan on the north Cornish coast to Falmouth on the  
 414 south coast (see inset rose diagram for strikes of constituent faults taken from the BGS Falmouth sheet 352).  
 415 Overall, the fault zone is believed to dip steeply to the east at around  $80^\circ$ , but note that there is considerable  
 416 variation in strike and dip of individual fault and fracture planes within the fault zone (Fellgett & Haslam,  
 417 2021). The azimuth of the maximum horizontal stress is broadly NW-SE, with one exception trending NE-SW.

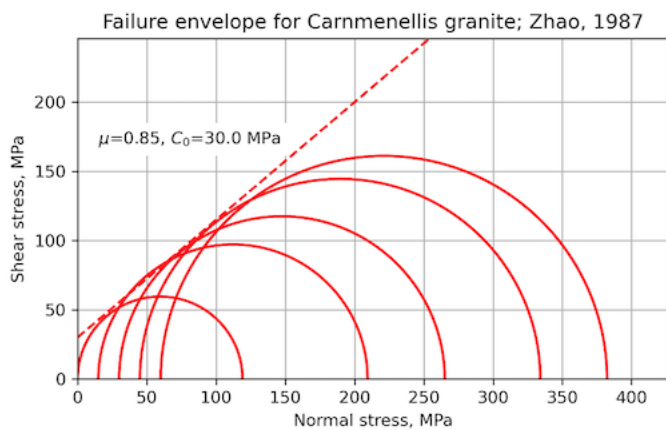
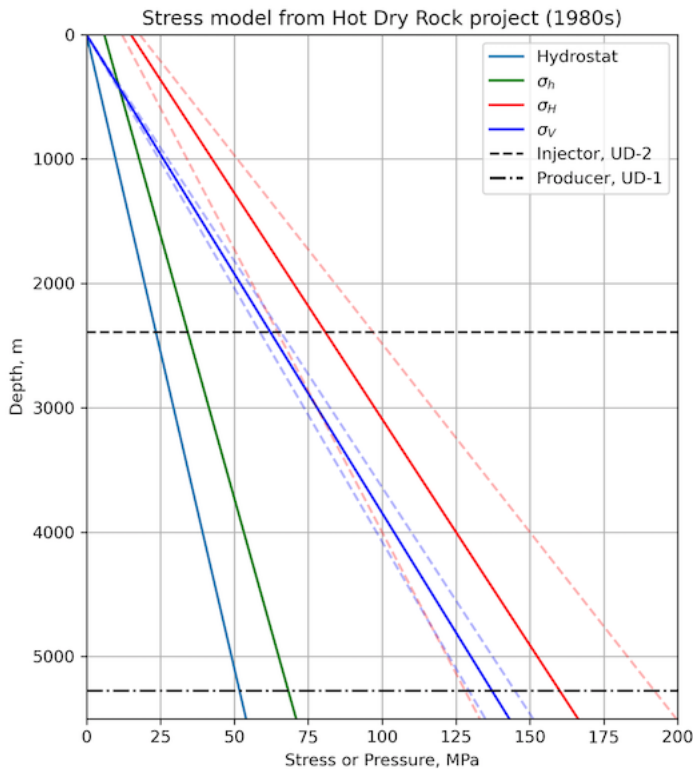


418

419 **Figure 11. a.** Red triangles show Raspberry Shake (network code: AM) and BGS (network code: GB) seismic  
 420 stations in Cornwall, with station names labelled. Seismicity during geothermal operations is indicated by red  
 421 circles. The inset shows a close-up of the area demarcated by the blue dashed line in the main map. The black  
 422 dashed line in the inset shows the broad WNW-ESE alignment in seismicity. **b.** Computed focal mechanism  
 423 for the 2020-09-30 11:44:01  $M_L$  1.6 induced earthquake. First-motions are plotted on the focal sphere with  
 424 “+” indicating positive polarity, and “o” for negative polarities. P-wave first-motions are plotted starting and  
 425 ending 0.3 seconds before and after the picked arrival, respectively, and are coloured in the same way as the  
 426 points on the focal sphere.

427





428

429 **Figure 12.** Constraints on input variables for the Porthtowan Fault Zone modelling. **a.** Stress-depth plot based  
 430 on data and equations from the Hot Dry Rock project in the Carnmenellis granite (Batchelor & Pine, 1986).  
 431 Also shown are the depths of the two wells in the pilot project at United Downs. **b.** Mohr diagram showing  
 432 data from laboratory mechanical tests of Zhao (1987) for brittle failure of Carnmenellis granite at 200°C.  
 433 Estimated Mohr-Coulomb failure envelope (dashed red line) is defined by  $\mu=0.85$ ,  $C_0=30$  MPa.

434 Detailed geomechanical analyses were performed in the Carnmenellis granite in the 1980s as part of the HDR  
 435 project, and these provide useful constraints on the variation of stress and fluid pressure with depth (Figure  
 436 12a; Batchelor & Pine, 1986). From these data, a strike-slip regime is most likely with  $\sigma_1 = \sigma_{Hmax}$  and  $\sigma_2 = \sigma_V$ ,  
 437 but note the uncertainties (based on quoted values in Batchelor & Pine, 1986): from around the depth of the  
 438 injector well at United Downs and deeper, a normal fault regime is also consistent with the data, i.e.,  $\sigma_1 = \sigma_V$   
 439 and  $\sigma_2 = \sigma_{Hmax}$ . Note that the earlier HDR project did not target a specific fault zone in the granite.

440 The thermo-mechanical properties of the Carnmenellis granite have been studied by Zhao (1987). Figure 12b  
 441 shows a Mohr diagram of data taken from Table 2.3 of Zhao (1987) for laboratory brittle failure tests  
 442 conducted at 200°C (the approximate temperature of the injector well at United Downs). From these data,  
 443 we have estimated a linear Mohr-Coulomb failure envelope defined by a friction coefficient of 0.85 and a

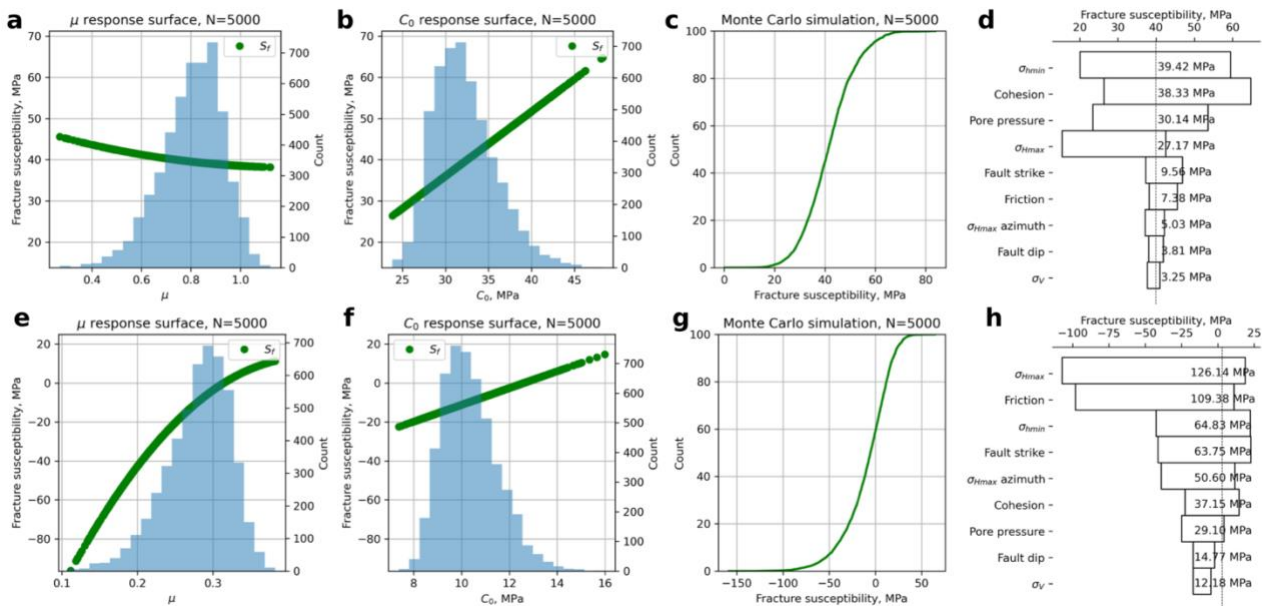
444 cohesive strength of 30 MPa. Cuttings from the boreholes at United Downs have been used to measure  
 445 friction coefficients of rocks within the PFZ, and values ranging between  $\mu=0.28-0.6$  were recorded (Sanchez  
 446 et al., 2020).

447 We present model results for fracture susceptibility in the PFZ as the plan at United Downs (and elsewhere  
 448 in the future) is to inject fluid into the fault zone in order to generate shear-enhanced permeability on pre-  
 449 existing fractures. Table 3 lists the input variable distributions used in the “base case” model for hydrostatic  
 450 pore fluid pressure in the fault zone and mechanical properties taken from laboratory tests of intact  
 451 Carnmenellis granite (Figure 12b). The modelled depth is chosen as 4 km, in between the depths of the UD-  
 452 1 and UD-2 wells.

Variable	Mean	Standard deviation ( $\kappa$ for Von Mises)	Units	Distribution	Comments
$\sigma_v$ , vertical stress	105.0	5.25 (5% of mean)	MPa	Normal	Lithostatic for depth of 4 km, assuming average rock density of 2650 kg m <sup>-3</sup> Batchelor & Pine, 1986
$\sigma_H$ , max. horizontal stress	125.0	25.0 (20% of mean)	MPa	Normal	Batchelor & Pine, 1986
$\sigma_h$ , min. horizontal stress	53.0	5.3 (10% of mean)	MPa	Normal	Batchelor & Pine, 1986
$P_f$ , pore fluid pressure	40.0	4.0 (10% of mean)	MPa	Normal	Hydrostatic for depth of 4 km, assuming average fluid density of 1000 kg m <sup>-3</sup>
Azimuth of $\sigma_{Hmax}$	140	$\kappa=200$	°	Von Mises (circular Normal)	Batchelor & Pine, 1986
Fault strike	340	$\kappa=150$	°	As mapped	Digitised from BGS map
Fault dip	80.0	$\kappa=1000$	°	Von Mises (circular Normal), truncated at 0 and 90	
Friction, $\mu$	0.85	0.17 (20% of mean)	n/a	Skewed normal	$\alpha = -3$ i.e., skewed low
Cohesion, $C_0$	30.0	6.0 (20% of mean)	MPa	Skewed normal	$\alpha = +3$ i.e., skewed high

453

454 **Table 3.** Distributions of input variables used in the base case model of fracture susceptibility in the  
 455 Porthtowan Fault Zone.



456

457 **Figure 13.** Outputs from the Monte Carlo simulation of fracture susceptibility in the Porthtowan Fault Zone.  
 458 **a-d.** The response surface for the base case, with friction and cohesion estimated from the laboratory failure  
 459 tests of Zhao (1987), predicts positive fracture susceptibility i.e., a stable fault zone. The tornado plot (**d**)  
 460 shows that for relatively high values of cohesion (mode of  $C_0=30$  MPa in this case), the sensitivity to variations  
 461 in friction is slight. **e-h.** In contrast, the response surface for the ‘weak fault’ case, with reduced values of  
 462 friction and cohesion (mode of  $\mu=0.3$ , mode of  $C_0=10$  MPa), predicts fault zone instability i.e., overwhelmingly  
 463 negative values of  $S_f$ . The effect of friction on these predictions is now very strong, as shown in the shape of  
 464 the response surface for  $\mu$  (**e**) and in the ranking within the tornado plot (**h**).

465 The results from the Monte Carlo simulation of  $S_f$  for the PFZ are shown in Figure 13. For the base case, with  
 466 hydrostatic pore fluid pressure and a ‘strong fault’ (mode of  $\mu=0.85$ , mode of  $C_0=30$  MPa), the fault appears  
 467 unconditionally stable for the modelled *in situ* stress variations. The CDF shows almost exclusively positive  
 468 values of  $S_f$  up to about 60 MPa. Note that, for the input stress variations listed in Table 3, 22% of the MC  
 469 simulations produced an Andersonian normal fault regime ( $\sigma_1 = \sigma_v$ ), rather than a strike-slip ( $\sigma_2 = \sigma_v$ ) regime.

470 232 microseismic events with hypocentre depths of 4-5 km were detected by the BGS during geothermal  
 471 testing operations in 2021-2022 ([http://www.earthquakes.bgs.ac.uk/data/data\\_archive.html](http://www.earthquakes.bgs.ac.uk/data/data_archive.html); last accessed  
 472 23 July 2021). The largest earthquake induced by geothermal operations during this period occurred on 2020-  
 473 09-30 11:44:01, and had a local magnitude of  $M_L$  1.6, and was felt by residents in the area. This event was  
 474 well-recorded on a network of single-component Raspberry Shake stations (e.g. Holmgren & Werner, 2021)  
 475 and a single station of the BGS permanent monitoring network (Figure 11a). These stations offer excellent  
 476 azimuthal coverage of the geothermal seismicity, with the closest station lying only 2 km away (AM.RAD67).  
 477 Since no focal mechanisms have yet been documented for these induced earthquakes, we used recorded P-  
 478 wave first motions to compute a focal mechanism of the  $M_L$  1.6 event using the method of Hardebeck &  
 479 Shearer (2002). Take-off angles were computed using a 1D seismic velocity model for the Cornwall area  
 480 (<http://earthwise.bgs.ac.uk/index.php/OR/18/015> Table 4: Depth/crustal velocity models used in eart  
 481 [hquake locations](http://earthwise.bgs.ac.uk/index.php/OR/18/015); last accessed 23 July 2021). The best-fitting focal mechanism (Figure 11b) indicates either  
 482 normal faulting on a WNW-ESE steeply-dipping plane or strike-slip faulting on a shallow-dipping plane NE-  
 483 SW striking plane. Single event relocated epicentres reported by the BGS, which use arrivals from a local  
 484 dedicated microseismic monitoring array, show a NW-SE trend (Figure 11a), consistent with normal faulting  
 485 on a steeply east-dipping, WNW-ESE striking plane during this earthquake. Negative P-wave polarities were  
 486 recorded at AM.RAD67 for all  $M > 0$  events, indicating that the same fault plane was reactivated during many  
 487 of the induced events. The inferred fault plane is sub-parallel to the interpreted strike of the Porthtowan  
 488 Fault Zone that is targeted by the geothermal testing. This observed normal faulting mechanism is consistent  
 489 with our MC simulations (more than 1 in 5 of the predicted stress states were for normal faulting).

490

491 The response surface (green lines on Figure 13a-b) and the tornado plot of relative sensitivities of the input  
492 variables (Figure 13d) shows a positive dependence of  $S_f$  on the cohesion, and that variations in friction are  
493 relatively unimportant. If we reduce the strength of the modelled fault zone, by changing the input  
494 distributions of  $\mu$  and  $C_0$  to lower values – but with the same shape and skewness – the situation changes.  
495 The predicted fracture susceptibility is now much more strongly correlated with variations in friction, and  
496 less so with variations in cohesion. This can be explained by looking at the underlying formula for  $S_f$  (equation  
497 3), in particular the 2<sup>nd</sup> term on the RHS. If  $C_0 > \tau$  then the numerator of this term can be negative, producing  
498 a net positive term. However, if  $C_0 < \tau$  and  $\mu$  is small then this term is larger and negative. The important  
499 point is that the probability distribution of  $S_f$  (compare Figure 13c and 13g) is controlled by the *relative*  
500 magnitudes of  $\mu$  and  $C_0$ . In a weak fault zone, with low  $\mu$  and low  $C_0$ , the predictions are very sensitive to the  
501 value of friction. In a strong fault, the effect of  $\mu$  is less important. Thus, we need to know more about the  
502 relationship between  $\mu$  and  $C_0$  in fault rocks (see Discussion).

## 503 2. Coalfields in South Wales and Greater Manchester, UK

504 Scope exists to extract low enthalpy geothermal heat from disused coalmines in the UK (Farr et al., 2016),  
505 using either open- or closed-loop technology. Possible sites include the South Wales and Greater Manchester  
506 coalfields, where folded and faulted Coal Measures of Westphalian (upper Carboniferous) age have been  
507 mined for centuries, up until the 1980s. Initial plans for shallow mine geothermal schemes include *passive*  
508 dewatering which may not change the loading on faults by much. However, *active* dewatering schemes can  
509 promote ingress of deeper ground water (Farr et al., 2021), and as this fluid flow must be driven by gradients  
510 in fluid pressure, this could in turn lead to the instability of faults at greater depth. The models below are for  
511 a depth of 2 km.

512 The locations and orientations of faults have been taken from published BGS maps. For the South Wales  
513 coalfield (Figure 14a), we used the BGS Hydrogeology map of S Wales to map the traces of faults in the Coal  
514 Measures (Westphalian), and BGS 1:50k solid geology sheets over the same area to collect data on fault dips.  
515 For the Greater Manchester coalfield (Figure 14b), we used the BGS 1:50k solid geology sheets for Wigan,  
516 Manchester and Glossop. Faults were traced onto scanned images of the maps in a graphics package (Affinity  
517 Designer on an Apple iPad using an Apple Pencil). These fault trace maps were saved in Scalable Vector  
518 Graphics (.SVG) format, after deleting the original scanned image layer of the geological map. The saved .SVG  
519 files were read into FracPaQ (Healy et al., 2017) to quantify their orientation distributions (inset rose plots in  
520 Figure 14a and b). The fault trace maps were then overlain on maps containing historical seismicity and  
521 available focal mechanisms (from the public BGS catalogue; Musson, 1996) and the orientations of  $\sigma_{Hmax}$   
522 taken from the World Stress Map project (Heidbach et al., 2018).

523 In the South Wales coalfield 3,408 fault segments were traced, and the dominant trend is clearly NNW/SSE,  
524 but with important (and long) fault zones running ENE-WSW, such as the Neath and Swansea Valley  
525 Disturbances (Figure 14a). From cross sections, we measured 142 fault dips to help constrain the distribution  
526 of friction coefficients in these rocks (Figure 15b-c; see below), corrected for vertical exaggeration on the  
527 section line where necessary. Focal mechanisms in this area ( $n=4$ ) suggest that NNW/SSE and N/S faults are  
528 active in the current stress regime. Historical seismicity is widely, if unevenly, distributed with no obvious  
529 direct correlation to the surface mapped fault traces. For example, there are areas of intense surface faulting  
530 but no recorded historical seismicity, and vice versa – areas with abundant historical events but few mapped  
531 faults.

532 Around Greater Manchester 3,453 faults were traced, and the dominant trend is NW/SE, but E/W faults are  
533 also present (Figure 14b). From cross sections, we measured 89 faults to help constrain the distribution of  
534 friction coefficients in these rocks (Figure 15d-e; see below). Historical seismicity is again widely, if unevenly,  
535 distributed with few obvious direct correlations to the surface mapped fault traces. However, there was an  
536 earthquake swarm in 2002-2003 which comprised more than 100 events, with a maximum local magnitude  
537 of 3.9. Calculated focal depths were 1 – 3 km, although these have large uncertainties (Walker et al., 2003).  
538 The World Stress Map database has the orientation of  $\sigma_{Hmax}$  trending WNW/ESE in this area (Figure 12b),  
539 based on the focal mechanisms for local events in the 2002-2003 swarm (this is distinct from the regional

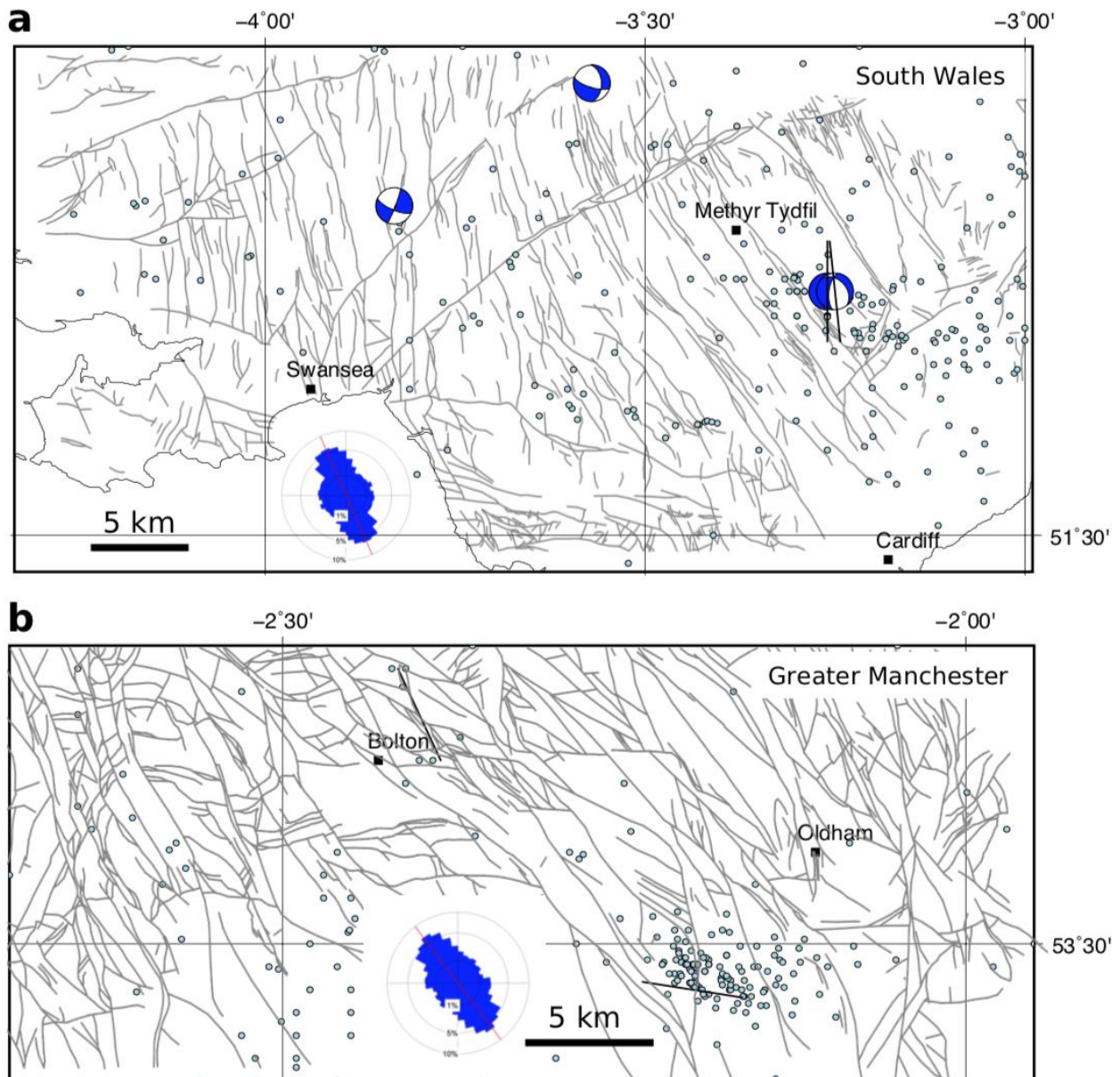
540 trend of  $\sigma_{Hmax}$  which is more NW/SW e.g., Williams et al., 2016). These observations suggest that faults  
541 oriented more nearly E/W are more likely to slip in the current stress regime.

542 There are no published geomechanical analyses for the variation of stress with depth for either of these two  
543 areas. To constrain the depth dependence of stress, we have used larger scale syntheses of stress for onshore  
544 UK produced by the BGS (e.g., Kingdon et al., 2016; Fellgett et al., 2018). The stress-depth plot in Figure 15a  
545 has been constructed using the data shown in Fellgett et al. (2018), and shows that, in general, a strike-slip  
546 fault regime with  $\sigma_1 = \sigma_{Hmax}$  is most likely. However, given the known uncertainties in these data, a normal  
547 fault regime ( $\sigma_1 = \sigma_v$ ) cannot be ruled out, especially at depth. Note that the stress-depth data shown in  
548 Fellgett et al. (2018) and used in Figure 15a are compiled from different areas, and remain untested for the  
549 specific areas shown in this paper. The azimuth of  $\sigma_{Hmax}$  is known to vary across the UK ranging from ~130 to  
550 ~170 (Baptie et al., 2010; Becker & Davenport, 2001).

551 Despite the economic and historical significance of the Coal Measures, there are no published datasets of  
552 laboratory measured friction or cohesion for either intact rocks or their faulted equivalents (although data  
553 may exist in proprietary company records). Data for specific units of interest does exist, e.g., for the  
554 Oughtibridge Ganister, a seat earth in the Coal Measures (Rutter & Hadizadeh, 1991); and the Pennant  
555 Sandstone, a rare marine sandstone unit (Cuss et al., 2003; Hackston & Rutter, 2016), but a systematic  
556 analysis of the volumetrically dominant sandstone, siltstone and mudstone formations is notably absent.  
557 Instead, we use the measured dips of faults in the Coal Measures as a proxy for the coefficient of sliding  
558 friction, using the relationship

559 
$$\mu = 1/\tan(\pi - 2\beta) \quad \text{equation 14}$$

560 where  $\beta$  is the angle between the fault plane and  $\sigma_1$  at failure (Jaeger et al., 2009; Carvell et al., 2014). Such  
561 a calculation assumes Mohr-Coulomb failure and that the current dip of the fault is reasonably close to the  
562 dip at failure in the post-Westphalian deformation of the coalfields. For measured fault dips  $< 45^\circ$ , we assume  
563 that  $\sigma_1$  was horizontal (Andersonian thrust/reverse fault regime) and for fault dips  $\geq 45^\circ$  we assume  $\sigma_1$  was  
564 vertical (Andersonian normal fault regime). In practice, some of these faults probably originated as strike-slip  
565 faults (i.e., with a sub-vertical dip and  $\sigma_2$  vertical), and some of their dips have almost certainly been modified  
566 by compaction since their formation. However, this method of estimating the likely range of friction  
567 coefficients from measured dips remains simple to apply and useful to first order, in the absence of better  
568 data. From the dip data, the calculated friction coefficients vary between 0.0 and 6.0 for South Wales, and  
569 between 0.35 and 2.0 for Greater Manchester (Figures 15c and e, respectively).

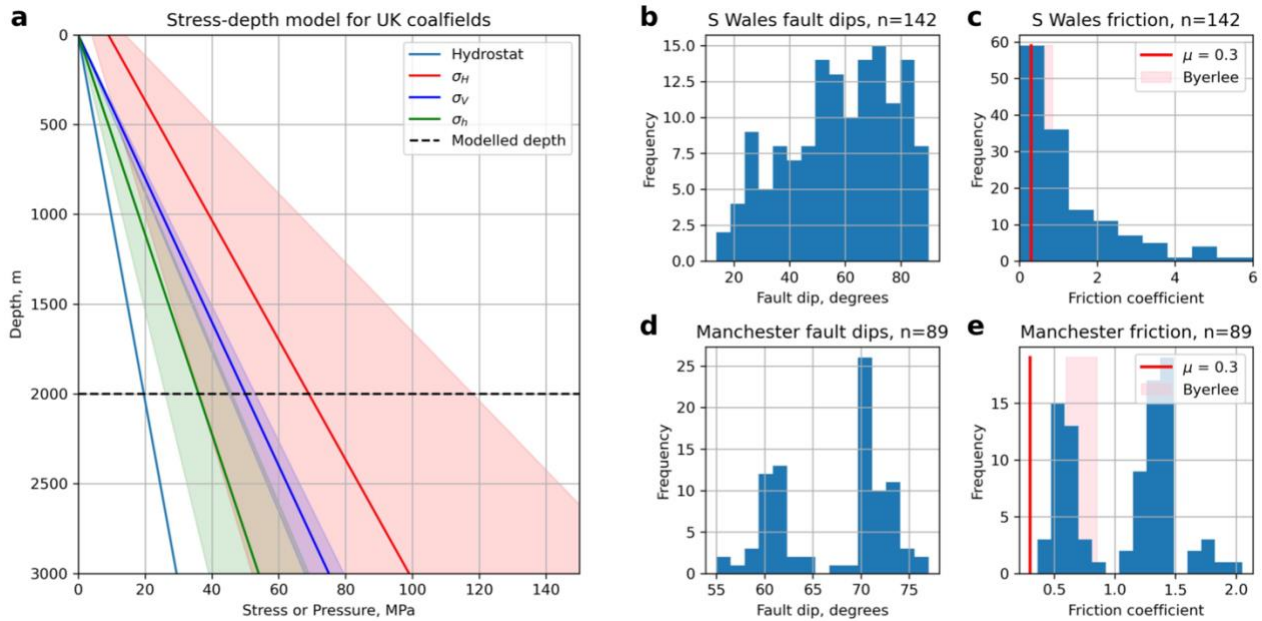


570

571 **Figure 14.** Maps of selected UK coalfields (suggested sites of shallow mine geothermal energy) showing:  
 572 selected population centres (black squares); epicentres of seismicity (light blue dots; BGS catalogue –  
 573 Musson, 1996); focal mechanisms (blue and white; Baptie, 2010); and orientations of the maximum  
 574 horizontal stress (black lines; World Stress Map data – Heidbach et al., 2018). Inset equal area rose diagrams  
 575 show orientations of mapped faults. **a.** South Wales area. Faults in the Coal Measures taken from the BGS  
 576 Hydrogeological Map of South Wales (1:125k) ( $n=3,408$ ), with a circular mean strike= $156^\circ$  and a circular  
 577 standard deviation= $65^\circ$ . **b.** Greater Manchester area. Faults in the Coal Measures taken from the BGS 1:50k  
 578 sheets Wigan, Manchester and Glossop ( $n=3,453$ ), with a circular mean strike= $143^\circ$  and a circular standard  
 579 deviation= $64^\circ$ .

580 Based on the values of sliding friction calculated from measured fault dips across both coalfields a threshold  
 581 stability value of  $\mu=0.3$  is taken as a reasonable lower bound for faulted rock. This is the value used to  
 582 compare with predicted slip tendencies calculated for each fault. For  $T_s > 0.3$ , the fault is deemed unstable,  
 583 for  $T_s \leq 0.3$  it is stable.





584

585 **Figure 15.** Constraints on input variables for the coalfield modelling of slip tendency. **a.** Stress-depth plot  
 586 based on data from onshore UK (after Fellgett et al., 2018). Also shown is the modelled depth of 2 km. **b-e.**  
 587 Histograms of fault dips measured cross-sections on published BGS 1:50k maps of South Wales and Greater  
 588 Manchester, and calculated values of friction coefficients derived from these dips assuming Mohr-Coulomb  
 589 failure. Byerlee friction ( $\mu=0.6-0.85$ ) shown as shaded pink box. Modelled critical values of friction ( $\mu=0.3$ )  
 590 shown by red lines.

591

Variable	Mean	Standard deviation ( $\kappa$ for Von Mises)	Units	Distribution	Comments
<b>South Wales coalfield <math>T_s</math> model, depth=2 km</b>					
$\sigma_v$ , vertical stress	50.0	3.75 (5% of mean)	MPa	Normal	Lithostatic for depth of 2 km, assuming average rock density of 2500 kg m <sup>-3</sup>
$\sigma_H$ , max. horizontal stress	70.0	14.0 (20% of mean)	MPa	Normal	After Fellgett et al., 2018
$\sigma_h$ , min. horizontal stress	35.0	3.5 (10% of mean)	MPa	Normal	After Fellgett et al., 2018
Azimuth of $\sigma_{Hmax}$	160	$\kappa=200$	°	Von Mises (circular Normal)	After Fellgett et al., 2018; Baptie, 2010; WSM, 2016
Fault strike	-	-	°	As mapped	Digitised from BGS Hydrogeology sheet
Fault dip	n/a	$\kappa=25$	°	Von Mises (circular Normal), truncated at 0 and 90	Fitted to data taken from cross-sections on BGS 1:50k sheets 229-231, 247-249, 263, 263
<b>Greater Manchester coalfield <math>T_s</math> model, depth=2 km</b>					
$\sigma_v$ , vertical stress	50.0	7.5 (5% of mean)	MPa	Normal	Lithostatic for depth of 2 km, assuming average rock density of 2500 kg m <sup>-3</sup>

$\sigma_H$ , max. horizontal stress	70.0	14.0 (20% of mean)	MPa	Normal	After Fellgett et al., 2018
$\sigma_h$ , min. horizontal stress	35.0	3.5 (10% of mean)	MPa	Normal	After Fellgett et al., 2018
Azimuth of $\sigma_{Hmax}$	145	$\kappa=200$	°	Von Mises (circular Normal)	After Fellgett et al., 2018; Baptie, 2010; WSM, 2016
Fault strike	-	-	°	As mapped	Digitised from BGS 1:50k sheets 84-86
Fault dip	60.0	$\kappa=200$	°	Von Mises (circular Normal), truncated at 0 and 90	Fitted to data taken from cross sections on BGS 1:50k sheets 84-86

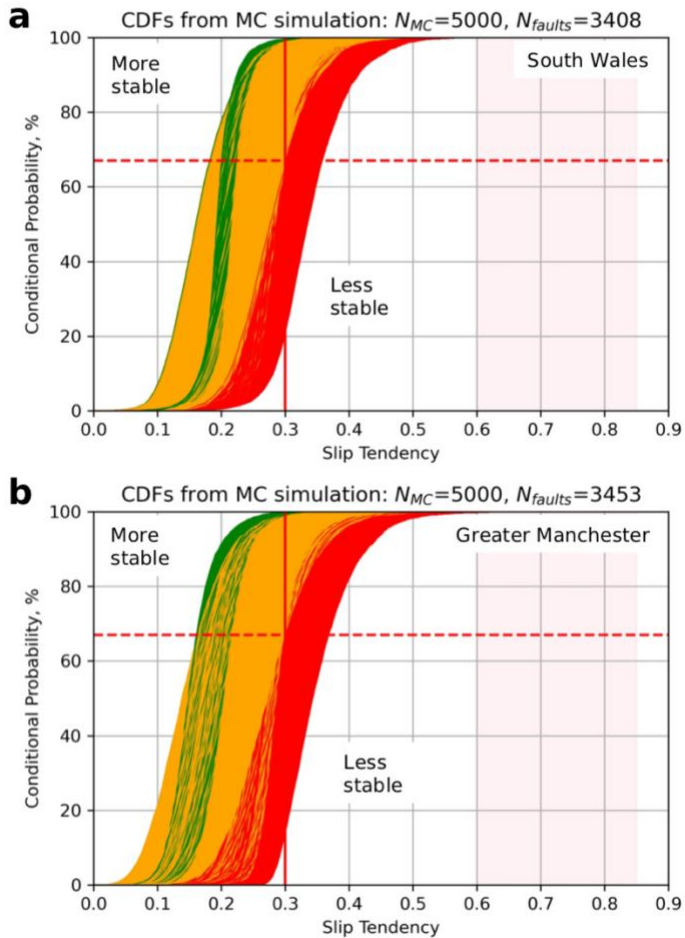
592

593 **Table 4.** Distributions of input variables used to model slip tendency in the coalfields of South Wales and  
594 Greater Manchester.

595 Predictions of conditional probability for fault slip have been calculated for all faults in both coalfields using  
596 slip tendency as the chosen measure: in the absence of detailed pore fluid pressure constraints or estimates  
597 of cohesive strength, it is hard to justify modelling the fracture susceptibility. Slip tendency provides a first  
598 order estimate of fault stability. A quadratic response surface was constructed for each coalfield using the  
599 full range of measured fault strikes and dips, and the input variable distributions listed in Table 4 and  
600 constrained by the data in Figure 15. Monte Carlo simulations ( $N_{MC}=5,000$ ) were run for each mapped fault  
601 segment with the other input variables drawn from their respective distributions. Note that the principal  
602 stresses used were the same for both coalfields, for a depth of 2 km (see Table 4), but the azimuth of  $sH_{max}$   
603 was varied to reflect the regional differences reported by other authors (Becker & Davenport, 2001; Baptie,  
604 2010), and the recorded focal mechanisms.

605 Output CDFs for all faults in both coalfields are shown in Figure 16. For South Wales ( $N=3,408$  faults),  
606 approximately 46% of faults are predicted to have a 1 in 3 chance of being unstable (i.e.,  $T_s > 0.3$ , shown in  
607 red), and 42% of faults are predicted to have a 1 in 10 chance of being unstable (shown in amber). For Greater  
608 Manchester ( $N=3,453$  faults), approximately 46% of faults are predicted to have a 1 in 3 chance of being  
609 unstable (i.e.,  $T_s > 0.3$ , shown in red), and 54% of faults are predicted to have a 1 in 10 chance of being  
610 unstable (shown in amber).



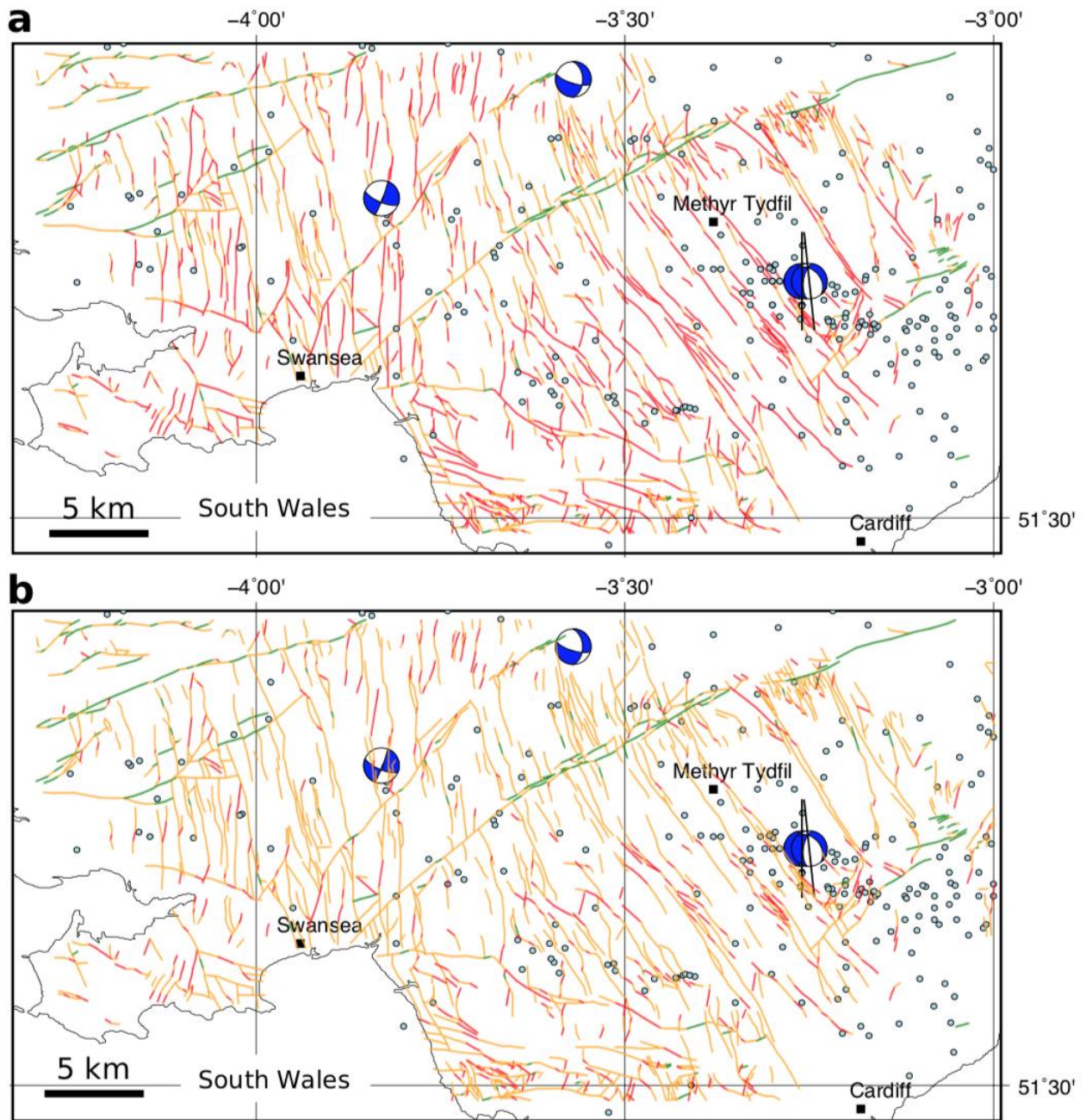


611

612 **Figure 16.** Output from the Monte Carlo modelling of slip tendency in UK coalfields. For slip tendency, more  
 613 stable faults skew towards the left (low  $T_s$ ), less stable faults skew to the right (high  $T_s$ ). **a.** CDFs of predicted  
 614 slip tendency for each mapped fault in South Wales. **b.** CDFs of predicted slip tendency for each mapped fault  
 615 in Greater Manchester. Colour coding of CDFs – red: >33% chance of exceeding threshold friction ( $\mu=0.3$ ,  
 616 vertical red line), amber: >1% and <33% chance, green: < 1% chance. Range of Byerlee friction shown by pink  
 617 shading.

618 The results from the RSM/MC modelling shown in the CDFs are replicated in map view in Figures 17 and 18.  
 619 Each fault segment is colour coded using the same heuristic applied in the CDF: red faults have a conditional  
 620 probability of at least 33% of their slip tendency exceeding the chosen threshold value of fault rock friction  
 621 ( $\mu=0.3$ ), amber (orange) faults have a 1-33% chance, and green faults have a less than 1% chance of being  
 622 unstable.

623 For South Wales, the general pattern of the predictions is consistent with the recorded focal mechanisms  
 624 (Figure 17a). The most likely fault segments to slip (coloured red) are those oriented either NNW/SSE or N/S,  
 625 corresponding with one of the nodal planes in each of the focal mechanisms. Faults trending ENE/WSW, such  
 626 as the Neath Disturbance, are predicted to have low probability of slip in the modelled stress regime (green).  
 627 Note that the Swansea Valley Disturbance trends ENE/WSW as a fault zone, but the constituent fault  
 628 segments are variously oriented including elements that trend NE/SW, and these are marked in red (high  
 629 probability of slip). Blenkinsop et al. (1986) noted that this fault zone may in fact have a shallow dip at depth,  
 630 which is not covered by the dip distribution used in our modelling, so further work is required here. The  
 631 location with the most recorded events lies to the SE of Merthyr Tydfil, and this corresponds to an area with  
 632 many mapped faults trending NW/SE marked with a high probability of slip, and consistent with two of the  
 633 focal mechanisms.



634

635 **Figure 17.** Output from the Monte Carlo modelling of slip tendency in South Wales coalfield. **a.** Colour-coded  
 636 fault map showing conditional probability of slip for each mapped fault. This map shows the unweighted  
 637 values, as shown on the CDFs in Figure 14a. **b.** Colour-coded fault map showing conditional *weighted*  
 638 probability of slip for each mapped fault. The weighted probability is calculated by multiplying the probability  
 639 from the CDF in Figure 14a by the normalised fault smoothness, ranging from 1.0 for a perfectly straight (i.e.,  
 640 smooth) fault, and tending to 0.0 for a rough fault. Colour coding of CDFs – red: >33% chance of exceeding  
 641 threshold friction ( $\mu=0.3$ ), amber: >1% and <33% chance, green: < 1% chance.

642

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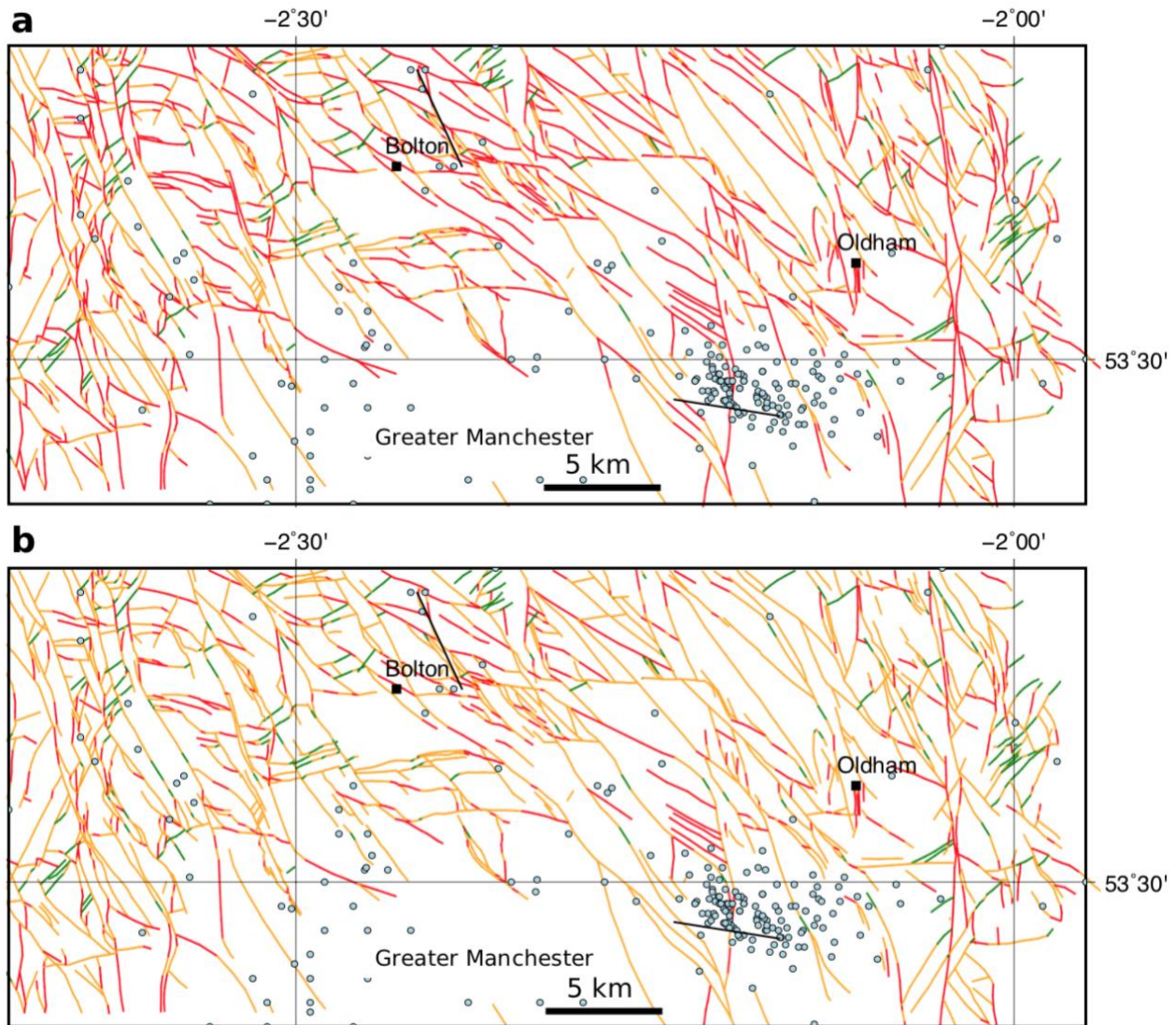
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645

646



647 For Greater Manchester (Figure 18a), the simulation suggests that many faults are likely to slip in the  
648 modelled stress regime, even though the recorded seismicity is generally sparse. The exception is the area  
649 of the 2002-2003 swarm near Manchester city centre. Here the recorded events coincide with mapped  
650 surface faults trending WNW/ESE and predicted as likely to slip (red).



651  
652 **Figure 18.** Output from the Monte Carlo modelling of slip tendency in Greater Manchester coalfield. **a.**  
653 Colour-coded fault map showing conditional probability of slip for each mapped fault. This map shows the  
654 unweighted values, as shown on the CDFs in Figure 14b. **b.** Colour-coded fault map showing conditional  
655 *weighted* probability of slip for each mapped fault. The weighted probability is calculated by multiplying the  
656 probability from the CDF in Figure 14b by the normalised fault smoothness, ranging from 1.0 for a perfectly  
657 straight (i.e., smooth) fault, and tending to 0.0 for a rough fault. Colour coding of CDFs – red: >33% chance  
658 of exceeding threshold friction ( $\mu=0.3$ ), amber: >1% and <33% chance, green: < 1% chance.

659  
660 **Discussion**

661 *Stress, pressure, and temperature*

662 The simulations described in this paper all critically depend on our knowledge of the *in situ* stress tensor. We  
663 can constrain some of the components of this tensor better than others. The vertical stress ( $\sigma_v$ ) is usually the  
664 best constrained, a reflection of its derivation from the borehole density logs sampled at sub-metre  
665 resolution. Our estimates of the horizontal stresses,  $\sigma_{Hmax}$  and  $\sigma_{Hmin}$ , remain poorly constrained. Even in cases

666 with relatively good data, e.g., from borehole leak-off tests (LOTs) and formation integrity tests (FITs), the  
667 “data density” for these stress components is generally sparse (compared to  $\sigma_v$ ), and we are stuck with  
668 significant uncertainties. And these uncertainties matter, as shown by this study and previous work (e.g.,  
669 Chiaramonte et al., 2008; Walsh & Zoback, 2016). The fundamental dependence of shear failure on  
670 differential stress inherent in the Mohr-Coulomb failure criterion is reflected in the high ranking of stress  
671 tensor components in the tornado plots shown in this study. Also, larger uncertainties in stress components  
672 mean that the Andersonian regime may flip from the default “average” assumption to another orientation:  
673 e.g., an apparently strike-slip regime may in fact include a significant proportion of normal fault possibilities  
674 (>20% in the case of the Porthtowan Fault Zone shown here). One way to improve our knowledge of the  
675 stress tensor, and especially the azimuth of  $\sigma_{Hmax}$  would be to exploit richer catalogues of seismicity to  
676 produce more focal mechanisms for natural or induced events. Most countries would benefit from better –  
677 i.e., more widespread and higher resolution – continuous seismic monitoring. While this may be expensive  
678 with top of the range broadband equipment, citizen science devices, such as the Raspberry Shake, offer a  
679 low cost and viable alternative (Cochran, 2018; Anthony et al., 2019; Hicks et al., 2021; Holmgren & Werner,  
680 2021). Our study shows how Raspberry Shake data are effective for computing focal mechanisms. Analysis  
681 of more events would allow stress inversions to be performed on the data measured by these devices,  
682 especially when they are combined in *ad hoc* arrays to improve signal to noise ratios.

683 Pore fluid pressures at depth are also poorly known, even for a country like the UK with a long tradition of  
684 geological (and geophysical) science and rich history of mining and drilling into the crust. Most importantly,  
685 our knowledge of measured *in situ* pore fluid pressures in and around fault zones is generally poor.  
686 Theoretical predictions and model simulations abound, but direct measurements of this key parameter are  
687 almost non-existent. We need to know the actual limits of pore fluid pressures in fault zones, and their likely  
688 spatial and temporal variation over a fault plane throughout the seismic cycle. The situation is complicated  
689 by the finer scale structure of fault zones. Fault zones in low porosity and/or crystalline rocks (such as granite)  
690 can be divided into one or more narrow cores defined by fine grained fault rocks (gouges, cataclasites)  
691 surrounded by wider damage zones of more or less fractured rock. Permeability may be low in and across  
692 the core(s) and higher in the damage zones (Caine et al., 1996; Faulkner et al., 2010). In high porosity and/or  
693 granular rocks (such as sandstone), fault zones may be simpler, with a fine grained fault rocks along narrow  
694 fault planes forming an effective fluid seal (Wibberley et al., 2008) These differences in the physical  
695 characteristics of the fault zones have consequences for the distribution of dynamic pore fluid pressures,  
696 which remain poorly known in detail.

697 The work described in this paper has ignored the effects of temperature. However, thermoelastic stress may  
698 be more important than poroelastic stress by a factor of 10 (Jacquey et al., 2015). In short, colder injected  
699 water may increase the chance of slip on a given fault. In the UK, our knowledge of the subsurface  
700 temperature field is increasing (Beamish & Busby, 2016; Farr et al., 2021), but we need more data, and again,  
701 especially from faulted rocks.

## 702 *Faults*

703 An implicit assumption in all of the modelling performed in this paper (and many others) is that we know  
704 something about the fault which may slip: i.e., we can only quantify risk on known faults. There will, in  
705 general, be many more unmapped faults in the subsurface, and these may be the ones most likely to slip due  
706 to a change in loading (of either *in situ* stress or fluid pressure). This is apparent in the maps for the coalfields  
707 shown in this paper in terms of the relative lack of correspondence between the surface mapped fault traces  
708 and the locations of recorded earthquakes. Some of this “mismatch” could be explained by the dip of the  
709 faults measured at the surface, but not all. Moreover, there are areas of apparently intense surface faulting  
710 and no recorded seismicity, and vice versa (recorded seismicity but no mapped surface faults). Some advance  
711 could be made to address this problem with the recognition that each recorded seismic event documents a  
712 fault plane, assuming that a double couple focal mechanism implies fault slip rather than dilation from dyke  
713 emplacement or other mechanisms. And therefore the 3D position of each focal mechanism points to at least  
714 part of a subsurface fault. The challenge then lies in mapping these seismic event fault planes into a viable  
715 fault network. Better data (i.e., higher spatial resolution and extending to smaller event magnitudes) from

716 more dense arrays of seismometers would help with this task, as for the refinement of stress estimates noted  
717 above.

### 718 *Rock properties*

719 The importance of good data on rock properties has been emphasised above, in the Worked Example for  
720 fracture susceptibility and in the case study for the Porthtowan Fault Zone. In general, we need more and  
721 better data on coefficients of friction and cohesive strength, especially for the target formations of  
722 decarbonisation operations. Moreover, we need data for the intact *and* faulted rocks. We also need better  
723 constrained correlations among rock properties. A widely used method in oil and gas is to derive estimates  
724 of friction coefficient and UCS from wireline log datasets measuring porosity, slowness (velocity) or elasticity  
725 e.g., Chang et al., 2006. However, as noted by these authors, the correlations are strictly valid only for the  
726 specific formations tested in the laboratory, and even then, the uncertainties remain large. A further issue is  
727 the tendency to average wireline log derived estimates over a depth interval, when for most sections of crust  
728 this is the direction in which rock properties are expected to vary most rapidly. The Porthtowan Fault Zone  
729 example above highlighted another issue: the relative impact of cohesion and friction on the predicted  
730 stability depends on the magnitude of the cohesion in relation to the shear stress on the fault. For low  
731 cohesion values, the constraints on friction become much more important. We need systematic  
732 investigations of frictional behaviour at low cohesive strength. We need detailed systematic correlations  
733 among rock properties, especially for faulted crystalline basement rocks.

734 Collecting more laboratory data is no panacea, evidenced by the well-aired concerns over how we up-scale  
735 rock properties and behaviours from mm- and cm-sized samples to whole fault zones. But calibrations and  
736 correlations from careful, systematic laboratory data remain the cornerstone of estimating the key *in situ*  
737 values. An interesting new focus would be to explore the nature of the skewness in mechanical property  
738 datasets: why should friction coefficients skew low, and cohesive strength skew high?

739 The utility of the Mohr-Coulomb criterion used in this paper is largely down to its mathematical simplicity,  
740 i.e., linearity and only two parameters (friction and cohesion). Other criteria are perfectly viable and could  
741 easily be added to the pfs Python code, but some other failure criteria lack a clear mapping between their  
742 parameters and the mechanics of sliding on rock surfaces.

### 743 *Applicability of $T_s$ , $T_d$ and $S_f$ for quantifying risk*

744 A valid question is to ask whether any of these widely used measures of fault stability are, in fact, useful in  
745 practical terms at the scale of faults on maps. All three measures focus on the simplified mechanics of slip on  
746 a specific fault plane, with a fixed orientation and with specific rock properties. But seismic hazard is not  
747 isolated at the level of single fault planes. Faults occur in patterns or networks, more or less linked together.  
748 Geometrical factors may be more important than the specifics of either the *in situ* stress or the rock  
749 properties, at the scale of observation. The observational record shows that bigger fault zones are the sites  
750 of bigger earthquakes, and they are also the locus of most displacement in a given network. Conversely,  
751 smaller faults host smaller seismic events, and accrue less overall displacement (Walsh et al., 2001). To begin  
752 to address this issue, we can weight the conditional probabilities of slip for a specific fault segment by a  
753 dimensionless normalised factor derived from the total length of the fault: e.g.,  $w_{size} = l_s / l_t$  where  $l_s$  is fault  
754 segment length and  $l_t$  is fault trace length. An alternative, but related idea, is that of the relationship between  
755 fault smoothness (or inversely, roughness) and fault maturity, and therefore seismic hazard (Wesnousky et  
756 al., 1988). The most seismically active faults are not only, or necessarily, the largest ones in their network,  
757 but tend to be the smoothest or most connected, reflecting the coalescence of fault segments through time  
758 and the removal of asperities through repeated slip events (Stirling et al., 1996). Therefore, we can weight  
759 the conditional probabilities of slip by a dimensionless factor of smoothness:  $w_{smooth} = l_{straight} / \sum(l_s)$ , where  
760  $l_{straight}$  is the straight line length between fault end points, which is 1.0 for a perfectly smooth fault with all  
761 segments parallel and connected, and tends to 0.0 for rough, complex fault traces. Examples of the effect of  
762 these smoothness weightings applied to the conditional probabilities are shown in Figures 17b and 18b for  
763 the UK coalfield faults. The net effect is to reduce the number of most risky faults (shown in red) by about  
764 half. These approaches are the subject of further work and testing.

765

## 766 Summary

767 In this paper, we have described and explained the Response Surface Methodology and shown how it can be  
768 combined with a Monte Carlo approach to generate probabilistic estimates of fault stability using published  
769 measures of slip tendency, dilation tendency and fracture susceptibility. Simulations show that a quadratic  
770 response surface always generates a better fit to the input variables in comparison to a linear surface, at the  
771 cost of larger matrices (more computer memory) and longer run times. Worked examples to calculate  $T_s$  and  
772  $S_f$  with synthetic input distributions show how the quadratic response surfaces vary for each input parameter.  
773 For slip and dilation tendency, the primary dependence is (as expected) on the maximum differential stress,  
774 and therefore the maximum and minimum principal stresses of the *in situ* stress tensor, with a lesser  
775 dependence on the fault orientation. For fracture susceptibility, the situation is more complex: if cohesion is  
776 relatively high,  $S_f$  is mainly dependent on the *in situ* stresses and cohesion. But if cohesion is low – quite likely  
777 in fault zones – then the dependence of  $S_f$  on friction is much more significant. This is a key finding: the  
778 relative sensitivity of the input variables on the response surface varies with the absolute value of the  
779 variables.

780 Sensitivity tests were used to assess how the shapes of different input distributions affect the predictions of  
781 fault stability. Varying the spread of symmetric (normal, Gaussian) distributions of input variables has a  
782 significant effect on the predictions, and this mirrors the reality of uncertainties in, for example, the principal  
783 stresses in a standard geomechanical analysis. As noted above, the vertical stress is often well constrained  
784 and has a lower relative standard deviation (say, 5% of the mean) than either the maximum or minimum  
785 horizontal stresses (typically 15-20% of their mean value). The shape and spread of skewed (asymmetric)  
786 distributions of rock properties (friction and cohesion) is also important. The direction of skewness is  
787 described by the sign of the parameter  $\alpha$  for the skewed normal distributions used in this paper to model  
788 variations in rock properties. Friction is modelled with a negative skewness towards lower values, whereas  
789 cohesion is modelled with positive skewness towards higher values, but systematic laboratory data are  
790 needed to verify these assumptions. This will require a statistically significant number of repeat tests for each  
791 property on quasi-identical samples of the same rock.

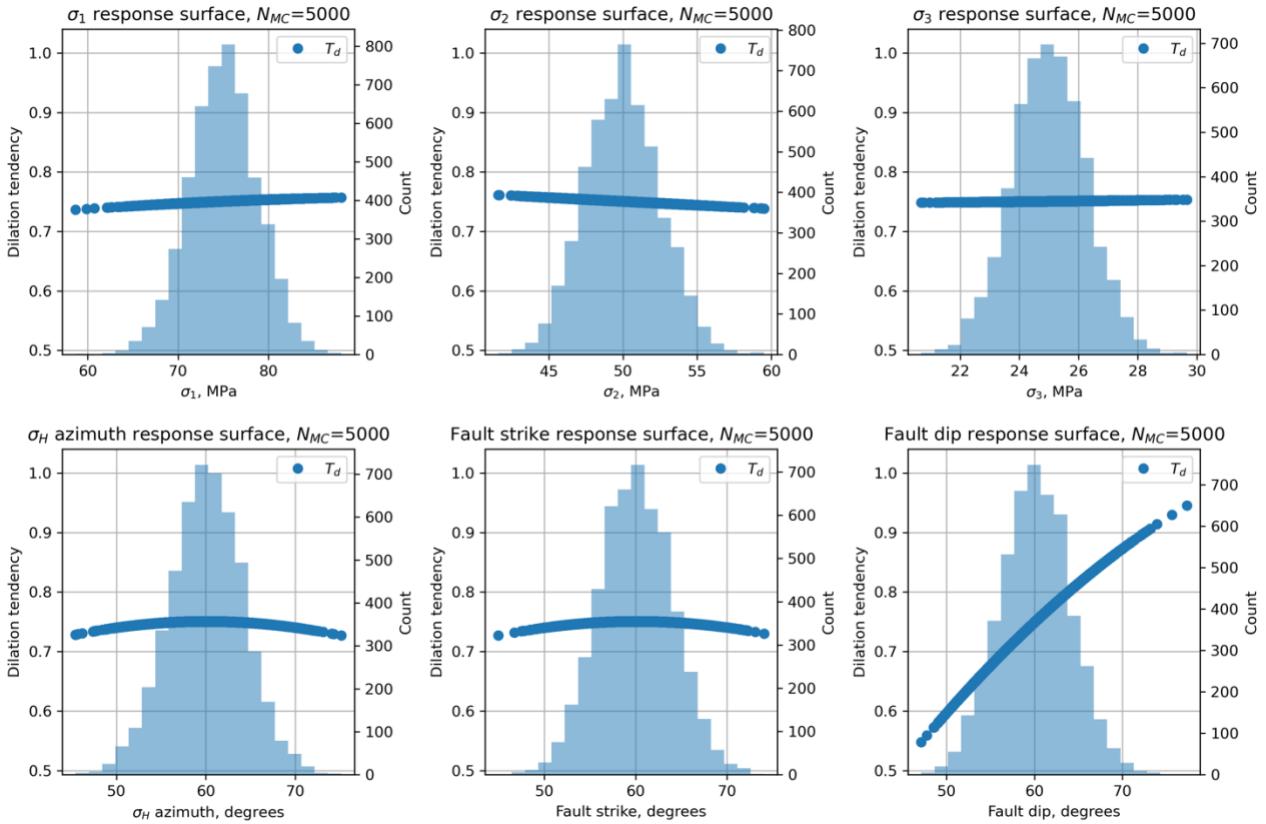
792 Case studies of three different locations demonstrated how a probabilistic approach can provide a useful  
793 assessment of fault stability, including which of the input variables are the most important for a given  
794 combination of *in situ* stress, fault plane orientation and rock properties. This then enables greater focus on  
795 improving the estimates of the key variables, and the relationships between them. For the Porthtowan Fault  
796 Zone in Cornwall, the modelling in this paper shows that we need more data for, and a better understanding  
797 of the relationship between, coefficients of friction and cohesive strength, especially at low values of friction  
798 (i.e., less than the Byerlee range of 0.6-0.85) to be expected in fault zones. For the coalfields in South Wales  
799 and Greater Manchester, model outputs show how predictions of fault stability can be weighted by a simple  
800 index of fault smoothness to begin to allow for the effects of geometrical weakening within the fault system  
801 as whole, rather than focusing on each individual fault plane taken in isolation.

802 It's obvious that uncertainty in the input parameters must translate into uncertainty in the output  
803 predictions. By combining a Response Surface Methodology with a Monte Carlo approach to the  
804 quantification of fault stability, we can explore, understand, and quantify how differing degrees of  
805 uncertainty among the input parameters feed through to uncertainty in the predicted stability measure.  
806 Response surfaces and tornado plots can help to identify which parameters are the most important in a  
807 particular analysis. Given our current state of knowledge of stress, fault orientations and fault rock  
808 properties, probabilistic estimates and iterative modelling are useful approaches to begin to de-risk the  
809 energy transition. Free, open source software to perform these analyses, such as the Python package pfs,  
810 can help to encourage their wider adoption and further refinement ("given enough eyeballs, all bugs are  
811 shallow"; Raymond, 2001). The deployment of abundant and relatively low-cost citizen science seismometers  
812 (e.g., Raspberry Shakes) could synergise two critical issues: the wider involvement of the public into open  
813 science debates about risk and the simultaneous collection of better data to constrain the local stress field.  
814 The energy transition and decarbonisation are urgent and essential tasks: we will only be successful if we  
815 manage to balance public perceptions of risk with the technical challenges inherent to the exploitation of  
816 faulted rock.



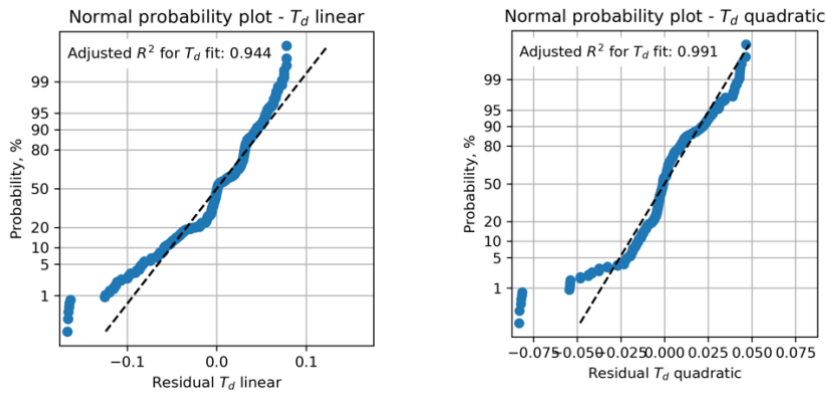
818 **Appendix A – Dilation tendency plots**

819 For completeness, we include the analysis of dilation tendency ( $T_d$ ) for the same synthetic input dataset used  
 820 to calculate slip tendency ( $T_s$ ) – i.e., input variable distributions taken from Table 2.



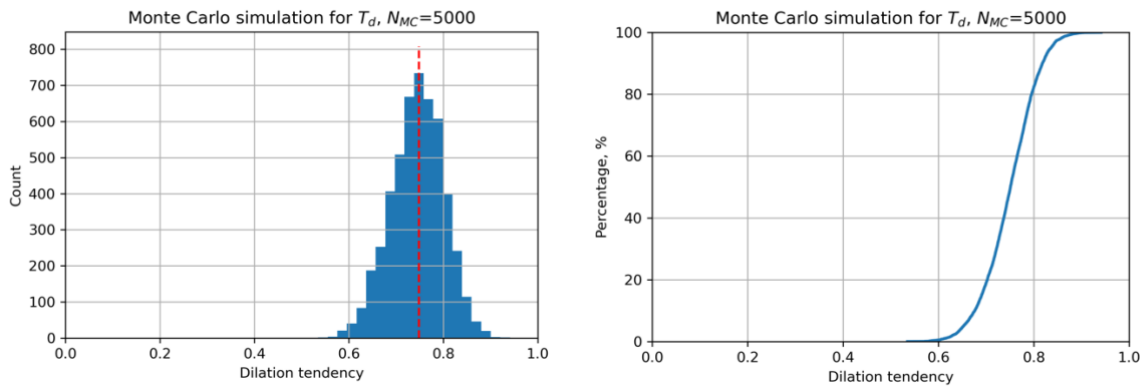
821

822 **Figure A1.** Histograms of input variables used to calculate dilation tendency  $T_d$  for the synthetic distributions  
 823 shown in Table 2.



824 **Figure A2.** Residual plots for linear and quadratic response surfaces for dilation tendency using synthetic  
 825 data. The quadratic fit has a higher value of the adjusted  $R^2$  parameter and is therefore deemed better in this  
 826 case.





827

828 **Figure A3.** Output from Monte Carlo simulation ( $N_{MC}=5,000$ ) of dilation tendency calculated using a quadratic  
 829 response surface from synthetic input data. **a.** Histogram of calculated dilation tendency values, in this case  
 830 showing a quasi-normal distribution with a mode of  $\sim 0.75$ . **b.** Cumulative distribution function (CDF) of  
 831 calculated dilation tendency values, showing the range in values from  $\sim 0.5$  to  $\sim 0.9$ .

832

### 833 Code availability

834 <https://github.com/DaveHealy-github/pfs>

835

### 836 Data availability

837

### 838 Author contribution

839 DH – 80%, SH – 20%. DH originated the study, wrote the code, ran the models. SH contributed seismology  
 840 data and expertise, and contributed to the writing of the text.

841

### 842 Competing interests

843 The authors declare that they have no conflicts of interest.

844

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 849 oil industry wireline log data for quantifying geomechanical models. GMT (Wessel et al., 2013) was used for  
 850 the maps. SciPy (Virtanen et al., 2021), Numpy (Harris et al., 2020), and matplotlib (Hunter, 2007) were used  
 851 for the Python pfs code and Allmendinger et al. (2012) for various geomechanical and geometrical algorithms.

852

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