

Stress-based forecasting of induced seismicity with instantaneous earthquake failure functions: Applications to the Groningen Gas Reservoir.

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Abstract

In this study we use the Groningen gas field to test a new method to assess stress changes due to gas extraction and forecast induced seismicity. We take advantage of the detailed knowledge of the reservoir geometry and production history, and of the availability of surface subsidence measurements and high quality seismicity data. The subsurface is represented as a homogeneous isotropic linear poroelastic half-space subject to stress changes in three-dimensional space due to reservoir compaction and pore pressure variations. The reservoir is represented with cuboidal strain volumes. Stress changes within and outside the reservoir are calculated using a convolution with semi-analytical Green functions. The uniaxial compressibility of the reservoir is spatially variable and constrained with surface subsidence data. We calculate stress changes since the onset of gas production. Coulomb stress changes are maximum near the top and bottom of the reservoir where the reservoir is offset by faults. To assess earthquake probability, we use the standard Mohr-Coulomb failure criterion assuming instantaneous nucleation and a non-critical initial stress. The distribution of initial strength excess, the difference between the initial Coulomb stress and the critical Coulomb stress at failure, is treated as a stochastic variable and estimated

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from the observations and the modelled stress changes. The exponential rise of seismicity nearly 30 years after the onset of production, provides constraints on the distribution of initial strength. The lag and exponential onset of seismicity are well reproduced assuming either a generalized Pareto distribution, which can represent the tail of any distribution, or a Gaussian distribution, to describe both the tail and body of the distribution. The Gaussian distribution allows to test if the induced seismicity at Groningen has transitioned to the steady-state where seismicity rate is proportional to the stressing rate. We find no evidence that the system has reached such a steady-state regime. The modeling framework is computationally efficient making it possible to test the sensitivity to modeling assumptions regarding the estimation of stress changes. The forecast is found robust to uncertainties about the ability of the model to represent accurately the physical processes. It does not require in particular a priori knowledge of the location and orientation of the faults that can be activated. The method presented here is in principle applicable to induced seismicity in any setting provided deformation and seismicity data are available to calibrate the model.

Keywords: Induced Seismicity, Probabilistic Forecasting, Reservoir Deformation

1 Introduction

The Groningen gas field, situated in the north-east of the Netherlands (Figure 1), has been in production since 1963. Prior to gas extraction, no historical earthquakes had been reported in the area (Dost et al., 2017). Starting in the 1990s small magnitude earthquakes have been detected, with some of these shallow events causing non-structural damage and public concern (Figure 1; Dost et al., 2017). As a result, it was decided to reduce production from 2014 on (van der Molen et al., 2019). The concern caused by induced seismicity at Groningen has prompted large efforts to monitor the seismicity and surface deformation induced by the reservoir compaction and to develop quantitative

11 models of the seismicity response to the reservoir operations (e.g. Bourne and
12 Oates, 2017; Bourne et al., 2018; Dempsey and Suckale, 2017; Dost et al., 2017,
13 2020; Richter et al., 2020).

14 In this study we take advantage of this rich dataset to explore different mod-
15 eling strategies to forecast induced seismicity. We follow the well established
16 paradigm that seismicity is driven by Coulomb stress changes (King et al., 1994),
17 a view already adopted in previous studies of induced seismicity at Groningen
18 (Bourne and Oates, 2017; Bourne et al., 2018; Dempsey and Suckale, 2017;
19 Richter et al., 2020). We test different strategies to assess stress changes, taking
20 advantage of a refined model of reservoir compaction constrained from produc-
21 tion data and from surface deformation measurements (Smith et al., 2019). We
22 additionally assume that the lag of seismicity is due to the fact that faults
23 in this stable tectonic area were not critically stressed initially (Bourne and
24 Oates, 2017; Bourne et al., 2018). Assuming the standard Mohr-Coulomb fail-
25 ure model, an earthquake nucleates when the Coulomb stress on a fault reaches
26 a critical value that represent the fault strength. In this context the seismicity
27 evolution depends on the shape of the function representing the distribution of
28 excess strength, the difference between the initial stress and the critical stress
29 at failure. We test whether the time evolution of seismicity reflects only the tail
30 of that distribution, as assumed in the extreme threshold failure model (Bourne
31 and Oates, 2017; Bourne et al., 2018) which explains well the initial exponential
32 rise of seismicity, or whether it shows a transition to the steady-state regime
33 where seismicity should be proportional to stress rate. Dempsey and Suckale
34 (2017) were able to forecast satisfactorily the time-evolution of seismicity as-
35 suming such a steady-state regime but didn't model how it was established.

36 Here, we treat earthquake nucleation as instantaneous. The nucleation process
37 is in fact not instantaneous and this feature, which can be accounted for us-
38 ing the rate-and-state friction formalism (Dieterich, 1994), could explain the
39 seismicity lag (Candela et al., 2019). We assess the effect of non-instantaneous
40 earthquake nucleation in another study (Heimisson et al., 2021). The forecasting
41 performance can be further improved with a more sophisticated representa-

42 tion of earthquake nucleation, but the assumption of an instantaneous failure
43 is an appropriate approximation to forecast seismicity at the annual to multi-
44 annual time-scale considered here.

45

46 **2. Stress changes due to pore pressure variations and reservoir com-** 47 **paction**

48 *2.1. Principle of our approach and comparison with previous approaches*

49 To estimate the probability of fault failure, we need to model the stress re-
50 distribution due to the reservoir compaction and pore pressure variations within
51 and outside the reservoir with account for poroelastic effects (Wang, 2018). The
52 geometry of the reservoir is well known from various geophysical investigations
53 (seismic reflection and seismic refraction), borehole core samples and logging
54 data. The reservoir lies at a depth varying between 2.6 and 3.2km, with a
55 thickness increasing northeastward from about 100m to 300m. Numerous faults
56 are offsetting the reservoir (Figure 1) with throws exceeding the reservoir thick-
57 ness at places. Pressure depletion lead to compaction of the reservoir, shear
58 stress build up on these faults and deformation of the surrounding medium.

59 Various approaches have been used in past studies to calculate the resulting
60 stress redistribution. Some have adopted a simplified model to enable fore-
61 casting seismicity at the scale of the entire reservoir as we do in this study.
62 Dempsey and Suckale (2017) proposed a forecasting scheme which accounts for
63 the effect of the local pore pressure change on poroelastic stress changes. They
64 ignore reservoir heterogeneities and assume that the earthquakes occur within
65 the reservoir. These model assumptions are questionable. The distribution of
66 hypocenter depth, which were determined with an uncertainty of 500m taking
67 into account heterogeneities of seismic velocities (Smith et al., 2020), suggests
68 that earthquake nucleate within the reservoir (28%) or in the overburden (60%),
69 with the mode of the distribution peaking at the depth of the reservoir caprock.
70 In addition, the earthquakes should tend to occur in zones of stress concentration

71 induced by spatial variations of the the reservoir properties. Bourne et al. (2018)
72 developed a semi-analytical reservoir depth integrated model which is also lim-
73 ited to the estimate of stress changes within the reservoir itself, but account for
74 stress concentration at the faults offsetting the reservoir. The faults character-
75 istics are not represented in any detail though, and the reservoir compressibility
76 is assumed uniform. Some other studies have used approaches that allow for
77 a more detailed representation of stress concentration at the faults offsetting
78 the reservoir and for the assessment of stress changes within and outside the
79 reservoir. In particular, Jansen et al. (2019) used a two-dimensional closed-form
80 analytical expressions to investigate stress redistribution and the possibility of
81 reactivating faults with any geometry. Other authors have carried out similar
82 investigations using two-dimensional finite-element simulations (Mulders, 2003;
83 Rutqvist et al., 2016; Buijze et al., 2017, 2019). It provided important insight
84 on the mechanics of fault reactivation, but the methods used in these studies to
85 estimate stress redistribution can't be easily included in a seismicity forecasting
86 scheme at the large scale of the reservoir due to the need to consider 3-D effects
87 and the computational cost. Finally, some authors have adopted a simplified
88 representation of the deforming reservoir as a series of point sources of strain
89 (van Wees et al., 2019; Candela et al., 2019). This approach is efficient as the
90 Green Functions are analytical. It allows to calculate stress changes in the 3-D
91 volume and can feed a seismicity forecasting scheme easily. It however suffers
92 from the fact that it is very sensitive to the number and distribution of point
93 sources representing the reservoir and to the distribution of the receiver points
94 where stress changes are evaluated. This issue is inherent to the point source
95 representation due to the stress singularity at the source location.

96 We also use a Green function approach but adopt a strain volume formulation
97 (Kuvshinov, 2008) rather than a point source formulation. The deforming reser-
98 voir is represented as a series of cuboidal volumes which are deforming proe-
99 lastically. We adopted a cuboidal elementary volumes as it is an efficient way
100 to represent, to the first order, spatial variations of the reservoir geometry, due
101 in particular to the faults offsetting the reservoir. These faults are represented

102 as vertical faults but the method could be expanded to account for any fault
103 dip angles using more general polyhedral elementary volumes. The displace-
104 ment and stress Green’s functions for polyhedral volumes are semi-analytical
105 and therefore easy to compute (Kuvshinov, 2008). This approach has the addi-
106 tional benefit that the method makes it easy to compute the stress changes for
107 any production scenario by the convolution of the Green’s functions with the
108 evolving pressure field. This is an appreciable feature for earthquake forecast-
109 ing, eventually applicable in real-time. A difference between our approach and
110 that of Candela et al. (2019), in addition to the strain volume instead of the
111 point formulation, is that we assume that earthquakes can occur on unmapped
112 faults. We therefore don’t restrict the stress calculations to the set of known
113 faults. The advantage is that our approach doesn’t require any prior knowledge
114 of the faults that could be reactivated.

115 *2.2. Implementation of the strain-volume model*

116 We use the pressure depletion model developed by the operator, MoReS
117 (Nederlandse Aardolie Maatschappij, 2013), which was generated from history
118 matching using the production rates, pressure gauge measurements, flow gauge
119 measurements, and tracer timing measurements.

120 Surface subsidence over the gas field has been well documented with differ-
121 ent geodetic and remote sensing techniques including optical levelling, persistent
122 scatterer interferometric synthetic aperture radar (PS-InSAR) and continuous
123 GPS (cGPS). Smith et al. (2019) combined all these data to describe the evolu-
124 tion of surface subsidence and the related reservoir compaction from the start
125 of gas production until 2017. They additionally used the pressure depletion
126 model of Nederlandse Aardolie Maatschappij (2013) to determine the spatially
127 variable compressibility of the reservoir. Since the lateral extent of the reservoir
128 ($\sim 40 \times 40\text{km}$) is much greater than the reservoir thickness (100 – 300m), the
129 reservoir pressure depletion at any map point can be related to the reservoir

130 compaction by:

$$C = hC_m\Delta P \quad (1)$$

131 where C is the compaction of the reservoir, C_m the uniaxial compressibility, ΔP
132 the pressure depletion and h the reservoir thickness. The uniaxial compressibil-
133 ity was determined based on the pressure depletion from MoReS, the reservoir
134 thickness, and the reservoir compaction (Smith et al., 2019). Kuvshinov (2008)
135 determined the semi-analytical Green functions relating compaction of a cuboid
136 to surface subsidence by integration of the nucleus of strain solution (Geertsma,
137 1973) over the cuboid volume assumed to be isotropic and homogeneous. Dyskin
138 et al. (2020) recently questioned the validity of Geerstma’s solution based on
139 the fact that the subsidence is always smaller than the reservoir compaction
140 by a factor $2(1 - \nu)$ even if the reservoir is assumed of large horizontal extent
141 compared to its depth. This paradox is discussed by Kuvshinov (2007) who
142 demonstrates that this factor is due to the uplift of the reservoir bottom. The
143 Green function of Dyskin et al. (2020) for a nuclei of strain may however have a
144 merit in the case of a very stiff underburden compared to the reservoir and could
145 be used as a alternative to Geerstma’s solution which assumes a homogeneous
146 elastic half space.mKuvshinov (2008)’s formulation depends on the relative po-
147 sition of the vertices defining each cuboid (i) relative to the observation point,
148 $\vec{x} = (x, y, z)$,

$$\bar{x}_{(i)} = x_{(i)} - x, \quad (2)$$

$$\bar{y}_{(i)} = y_{(i)} - y, \quad (3)$$

$$\zeta^\pm = z_{(i)} \mp z, \quad (4)$$

149 where $x_{(i)}$, $y_{(i)}$ and $z_{(i)}$ are the location for each vertex. The displacement,
150 $U = (U_x, U_y, U_z)$, at an observation point at the free surface, $Z = 0$, due to a

151 given cuboid is determined from the summation over all its vertices with

$$U_x = \frac{\alpha C_m \Delta P}{4\pi} \sum_{\text{vertices}} (-1)^{i-1} [f(\bar{y}, \zeta_-, \bar{x}, R_-) + (3 - 4\nu) f(\bar{y}, \zeta_+, \bar{x}, R_+) + 2 \cdot z \ln(|R_+ \bar{y}|)], \quad (5)$$

$$U_y = \frac{\alpha C_m \Delta P}{4\pi} \sum_{\text{vertices}} (-1)^{i-1} [f(\bar{x}, \zeta_-, \bar{y}, R_-) + (3 - 4\nu) f(\bar{x}, \zeta_+, \bar{y}, R_+) + 2z \cdot \ln(|R_+ + \bar{x}|)], \quad (6)$$

$$U_z = -\frac{\alpha C_m \Delta P}{4\pi} \sum_{\text{vertices}} (-1)^{i-1} [f(\bar{x}, \bar{y}, \zeta_-, R_-) + (3 - 4\nu) f(\bar{x}, \bar{y}, \zeta_+, R_+) - 2z \cdot \text{atan}\left(\frac{\zeta_+ R_+}{\bar{x} \bar{y}}\right)], \quad (7)$$

where $R^\pm = \sqrt{\bar{x}^2 + \bar{y}^2 + (\zeta^\pm)^2}$ and

$$f(x, y, Z, R) = Z \cdot \text{atan}\left(\frac{xy}{ZR}\right) - x \ln(|R + y|) - y \ln(|R + x|). \quad (8)$$

152 Following Smith et al. (2019) we represent the reservoir with cuboids of 500m ×
 153 500m horizontal dimension. The depth and height of each cuboid is set to the
 154 average depth and thickness of the reservoir over this 500 × 500m area.

155 Smith et al. (2019) found that the uniaxial compressibility is pressure in-
 156 variant and determine spatial variations of compressibility with a resolution
 157 approximately 3km. Smaller-scale spatial variations of compaction, and hence
 158 of compressibility, cannot be derived from surface deformation due to the depth
 159 of the reservoir. As such the uniaxial compressibility model can be considered
 160 as a smoothed representation of the reservoir compressibility. Downstream ap-
 161 plications of this model for stress calculations, Coulomb stress and earthquake
 162 forecasting should be smoothed to the same 3km resolution.

163

164 Given that earthquake might nucleate within the reservoir, possibly in the
 165 underburden, or more probably in the overburden (Smith et al., 2020), the stress
 166 changes are evaluated both within, and outside the reservoir. We assume no
 167 pore pressure depletion outside the reservoir.

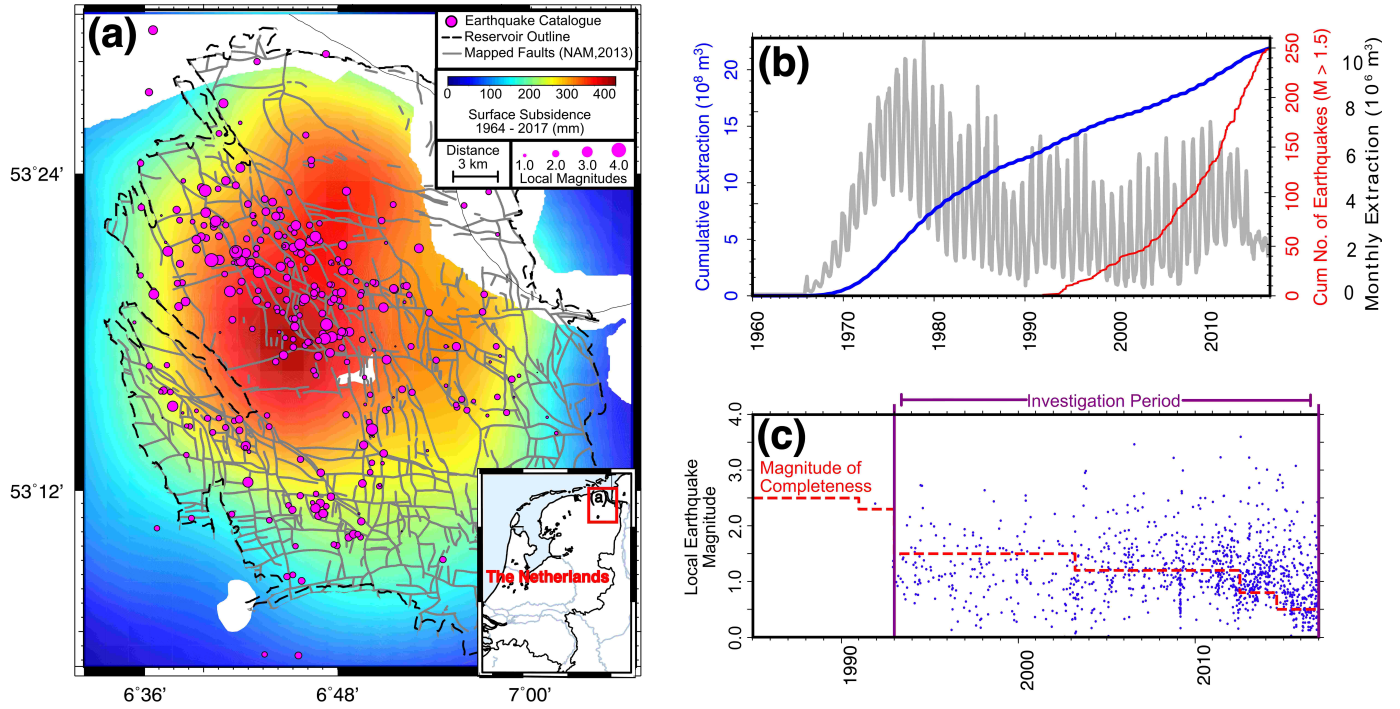


Figure 1: Relationships between surface subsidence, seismicity and cumulative extraction. (a) Surface subsidence and seismicity (pink circles with size proportional to magnitude) from 1964 to 2017 (Smith et al., 2019). The maximum magnitude over the period is $M_L = 3.6$. The black dashed line shows the extent of the gas reservoir. (b) Cumulated extracted gas volume, monthly extracted volumes, and cumulative number of earthquakes as a function of time. (c) Earthquake magnitude from 1985 to 2017. Red dashed line show magnitude of completeness. Purple lines show the time period under investigation in this article.

168 The stress changes are calculated with Kuvshinov (2008) solution with the
 169 convention that normal stress is positive in compression,

$$\sigma_{xx} = \frac{\alpha C_m G \Delta P}{2\pi} \sum_{\text{vertices}} (-1)^{i-1} \left[-\text{atan} \left(\frac{\bar{x} R_-}{\bar{y} \zeta_-} \right) - (3 - 4\nu) \text{atan} \left(\frac{\bar{x} R_+}{\bar{y} \zeta_+} \right) \right. \\ \left. + 4\nu \cdot \text{atan} \left(\frac{\zeta_+ R_+}{\bar{x} \bar{y}} \right) - \frac{2\bar{x} \bar{y} z}{R_+ (\bar{x}^2 + \zeta_+^2)} \right], \quad (9)$$

$$\sigma_{yy} = \frac{\alpha C_m G \Delta P}{2\pi} \sum_{\text{vertices}} (-1)^{i-1} \left[-\text{atan} \left(\frac{\bar{y} R_-}{\bar{x} \zeta_-} \right) - (3 - 4\nu) \text{atan} \left(\frac{\bar{y} R_+}{\bar{x} \zeta_+} \right) \right. \\ \left. + 4\nu \cdot \text{atan} \left(\frac{\zeta_+ R_+}{\bar{x} \bar{y}} \right) - \frac{2\bar{x} \bar{y} z}{R_+ (\bar{y}^2 + \zeta_+^2)} \right], \quad (10)$$

$$\sigma_{zz} = -\frac{\alpha C_m G \Delta P}{2\pi} \sum_{\text{vertices}} (-1)^{i-1} \left[-\text{atan} \left(\frac{\zeta_- R_-}{\bar{x} \bar{y}} \right) + \text{atan} \left(\frac{\zeta_+ R_+}{\bar{x} \bar{y}} \right) \right. \\ \left. - \frac{2\bar{x} \bar{y} z}{R_+} \left(\frac{1}{\bar{x}^2 + \zeta_+^2} + \frac{1}{\bar{y}^2 + \zeta_+^2} \right) \right], \quad (11)$$

$$\sigma_{xy} = -\frac{\alpha C_m G \Delta P}{2\pi} \sum_{\text{vertices}} (-1)^{i-1} \left[\ln (|R_- + \zeta_-|) \right. \\ \left. + (3 - 4\nu) \ln (|R_+ + \zeta_+|) - \frac{2z}{R_+} \right], \quad (12)$$

$$\sigma_{xz} = \frac{\alpha C_m G \Delta P}{2\pi} \sum_{\text{vertices}} (-1)^{i-1} \left[\ln \left(\left| \frac{R_- + \bar{y}}{R_+ + \bar{y}} \right| \right) \right. \\ \left. - \frac{2z \bar{y} \zeta_+}{R_+ (\bar{x}^2 + \zeta_+^2)} \right], \quad (13)$$

$$\sigma_{yz} = -\frac{\alpha C_m G \Delta P}{2\pi} \sum_{\text{vertices}} (-1)^{i-1} \left[\ln \left(\left| \frac{R_- + \bar{x}}{R_+ + \bar{x}} \right| \right) \right. \\ \left. - \frac{2z \bar{x} \zeta_+}{R_+ (\bar{y}^2 + \zeta_+^2)} \right]. \quad (14)$$

170 All model parameters are listed in Table 1. The Biot coefficient is in par-
 171 ticular set to $\alpha = 1.0$. Due to poroelasticity, the pressure depletion leads to
 172 a decrease of the horizontal stress. For a reservoir of large horizontal extent
 173 compared to its depth this effect is characterized by the stress path coefficient

<i>Parameter</i>	<i>Value</i>
Biot's Coefficient Alpha	1.0
Coefficient of Friction	0.66
Poisson Ratio	0.25
Shear Modulus	6GPa

Table 1: Parameters used in the calculation of stress changes induced by pressure changes in the reservoir using the strain volume formulation

174 $A = \frac{\Delta\sigma_h}{\Delta P} = \alpha \frac{1-2\nu}{1-\nu}$. Because the vertical stress is determined by the overbur-
175 den, it remains constant during gas extraction if the mass of the extracted gas
176 is neglected. It results that the stress path is an important parameters which
177 determines stress changes in the reservoir (Hettema et al., 2000). Given the
178 value of the Poisson coefficient, $\nu = 0.25$, the stress path coefficient correspond-
179 ing to our model parameters is $A = 0.66$. For comparison, field measurements
180 have indicated $A = 0.4 \pm 0.2$ and laboratory measurements have yielded values
181 between 0.7 and 0.8 (Hettema et al., 2000; Hol et al., 2018). The displacement
182 and stress fields for a single cuboid is shown in Supplementary Figure A1. The
183 cross-section is taken along the y-axis in the centre of the cuboid. Note the
184 stress localization at the edges of the cuboid. The free surface has little effect
185 in he case of a single cuboid due to its small size compared to the reservoir depth.

186
187 The point of failure of an intact rock or of reactivation of an existing fault
188 is commonly assessed using the Mohr-Coulomb failure criterion (Handin, 1969).
189 A number of studies have also demonstrated that this criterion can be used
190 effectively to assess earthquake triggering by stress changes (e.g. King et al.,
191 1994). According to this criterion failure occurs when the shear-stress τ exceeds
192 the shear-strength of the material τ_f , which depends on the effective normal
193 stress, $\sigma'_n = \sigma_n - \Delta P$, according to

$$\tau_f = \mu(\sigma_n - P) + C_0, \quad (15)$$

194 where τ_f is shear-stress, σ_n is the normal-stress (positive in compression), P is
 195 the pore pressure, μ is the internal friction and C_0 is the cohesive strength. If
 196 the material is not at failure the strength excess is $\tau_f - \tau$. Pressure changes
 197 play an important role in preventing or promoting fault failure. Assuming the
 198 total stresses do not change, a greater pore pressure acts to lower the effective
 199 normal stress and promotes failure. By contrast, a pressure decrease should
 200 inhibit failure. It is customary to assess jointly the effect of stress changes and
 201 pore pressure changes using the Coulomb stress change defined as

$$\Delta C = \Delta\tau + \mu(\Delta P - \Delta\sigma_n), \quad (16)$$

202 where ΔC is the change in Coulomb stress, $\Delta\tau$ is the shear stress change, μ is
 203 the internal friction, $\Delta\sigma_n$ is the change in normal stress, and ΔP is the change
 204 in pore pressure.

205

206 A cross-section of the displacement and stress calculated with our represen-
 207 tation of the reservoir as a series of cuboids is shown in Figure 2. The figure
 208 also shows the ‘maximum Coulomb stress change’, defined as the maximum
 209 Coulomb stress change for all possible faults orientation, and a ‘fault Coulomb
 210 stress change’ defined as the Coulomb stress change on faults with a fixed orien-
 211 tation. The rose diagram of faults orientation (Figure A2) shows two dominant
 212 modes corresponding to strikes of N270°E and N350°E. Dip angles are steep
 213 typically around 85° (Nederlandse Aardolie Maatschappij, 2013). We consider
 214 one or the other fault orientation. The choice of any fixed orientation result
 215 in fact in only a rescaling of the Coulomb stress changes. The Coulomb stress
 216 changes are largest at the top or bottom of the reservoir in the vicinity of the
 217 most prominent reservoir discontinuities. The stress concentrations at the edges
 218 of the cuboids interfere destructively where there are no offsets between adja-
 219 cent cuboids.

220 A striking feature of our model is that the Coulomb stress change is mostly nega-
 221 tive within the reservoir. Within the reservoir, the pore pressure the poroelastic

222 effect can outweigh the pressure decrease and this effect has been considered to
 223 be major cause for the seismicity at Groningen. In fact, considering a 1-D reser-
 224 voir model and the dependence on the effective normal stress $\sigma'_n = \sigma_n - \Delta P$,
 225 the Coulomb stress can increase for a decrease of the pore pressure only if the
 226 Biot-coefficient, $A = \alpha \frac{1-2\nu}{1-\nu}$, exceeds a critical values which depends on the on
 227 the internal friction angle ϕ and Poisson coefficient ν ,

$$\alpha_c = \frac{1 - \nu}{1 - 2\nu} \frac{2\sin\phi}{1 + \sin\phi}. \quad (17)$$

228 With the standard parameters we have chosen (Table 1), $\alpha_c = 1.07$ so that
 229 the poroelastic effect in the reservoir cannot in principle exceeds the effect the
 230 pressure drop since the Biot coefficient cannot exceed 1. A combination of a
 231 small Poisson coefficient, a large Biot coefficient and low internal friction is
 232 needed. This happens with the parameters used by Buijze et al. (2019) who
 233 assumed a Poisson coefficient of 0.15, a friction of 0.6 and Biot coefficient 1.0.
 234 The critical value of the Biot coefficient is 0.83 in that case. We verified this by
 235 calculating the stress changes at the center of a reservoir of large spatial extent
 236 (see supplementary Figure A6).

237
 238 The calculation using the cuboid approach is very efficient. For example, it
 239 takes 60s to calculate the cross-section presented in Figure 2 on a standard
 240 desktop computer with the code supplied in the Google Colab notebook. This
 241 section is composed of 8174 receiver points at 15m spacing in X and Z dimen-
 242 sions, computed from the convolution with the 8174 cuboids.

243

244 *2.3. Comparison with other models of stress changes*

245 We compare our results with the stress change calculations presented by
 246 Candela et al. (2019) and to those obtained with the Elastic Thin-Sheet (ETS)
 247 approximation of Bourne and Oates (2017).

248 Candela et al. (2019) calculated the maximum Coulomb stress changes on
 249 faults offsetting the reservoir using the 3-D model MACRIS (van Wees et al.,

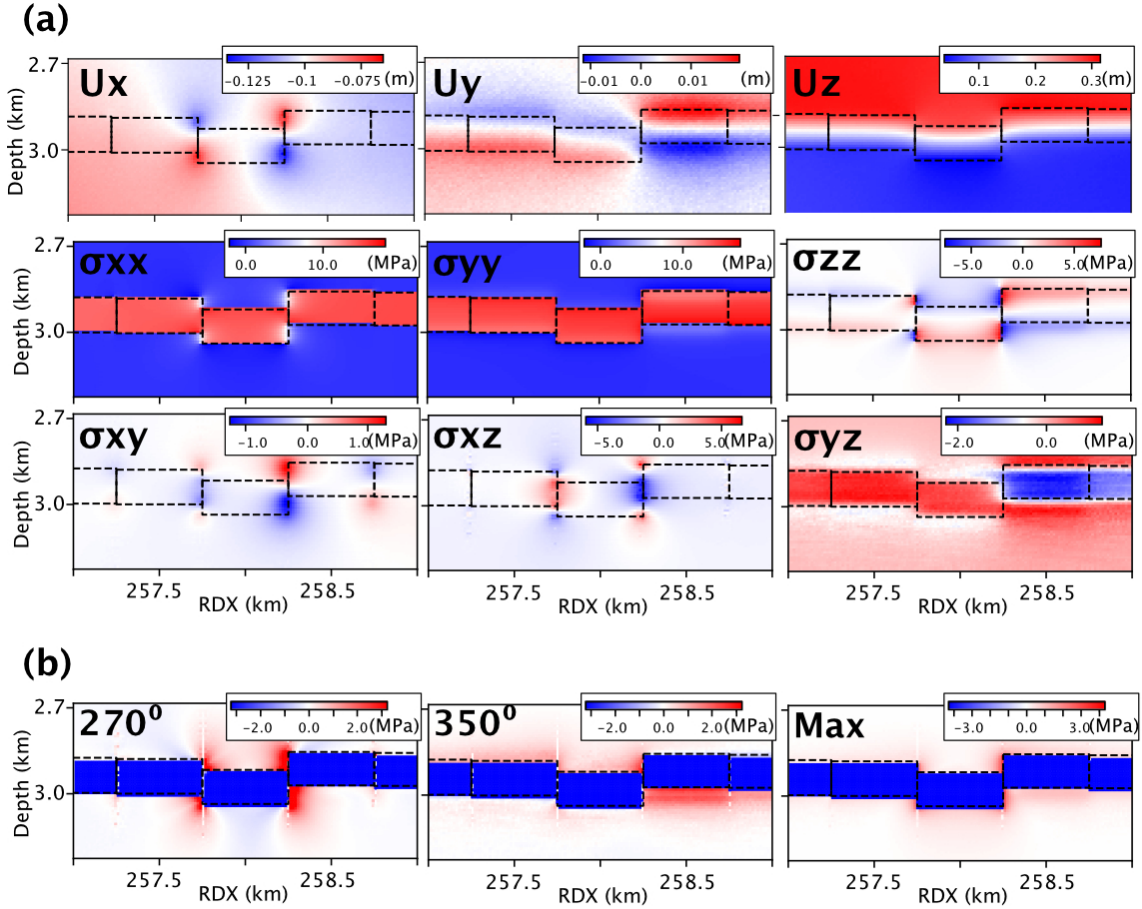


Figure 2: (a) Displacement (U in m), and stress tensor components (σ in MPa) along a vertical cross-section through a series of cuboids representing the simplified geometry of the depleting reservoir (black dashed lines). (b) Maximum Coulomb stress and fault Coulomb stress (MPa) calculated for a fault orientation corresponding to the regional average strike directions (270° and 350°), and dip (85°) angles.

250 2019). Their calculation shows an overall pattern and amplitudes of stress
251 changes similar to the stress changes calculated with our model near the edges
252 of the cuboids (Figure 3). Note that our calculation cannot be made exactly at
253 the the edges within the reservoir because the mathematical singularity. The
254 values are therefore very sensitive to the choice of the exact point of sampling.
255 Similarly the output from MACRIS is very sensitive to the exact location of
256 the point sources with respect to the faults. The comparison between the two
257 models can therefore only be qualitative. Sampling our model near the cuboid
258 edges exaggerates the fractional area of high stress change because the peak
259 value is assigned to the entire sampling cell. If the calculation is made in the
260 caprock above the reservoir, the stress changes are very sensitive to the distance
261 from the top of the reservoir if sampled above the edges of the cuboids. The
262 stress change calculated at the grid points above the centers of the cuboids are
263 more stable, although much smaller (Figure 3) but probably more representative
264 of the stress change with the sampling cell.

265 In the ETS formulation, the vertical averaged strain of a reservoir with
266 spatially varying thickness $h(x, y)$ is expressed a function of the vertical strain,
267 ε_{zz} and reservoir depth, z_0 according to,

$$\varepsilon_{xz}^- = -\frac{\varepsilon_{zz}}{2} \frac{\partial z_0}{\partial x} + \frac{h}{4} \frac{\partial \varepsilon_{zz}}{\partial x}, \quad (18)$$

$$\varepsilon_{yz}^- = -\frac{\varepsilon_{zz}}{2} \frac{\partial z_0}{\partial y} + \frac{h}{4} \frac{\partial \varepsilon_{zz}}{\partial y}, \quad (19)$$

$$\varepsilon_{zz}^- = \varepsilon_{zz}. \quad (20)$$

268 In the ETS formulation the distribution of earthquakes in time and space is
269 derived from the deformation of the reservoir due to uniaxial compaction and
270 to the associated vertical shear strain resulting from the spatial variations of
271 the reservoir elevation and thickness. It accounts for the effect of poroelasticity
272 and for shear at the faults offsetting the reservoir. The earthquakes are assumed
273 to occur only within the reservoir. For consistency with the study of Bourne

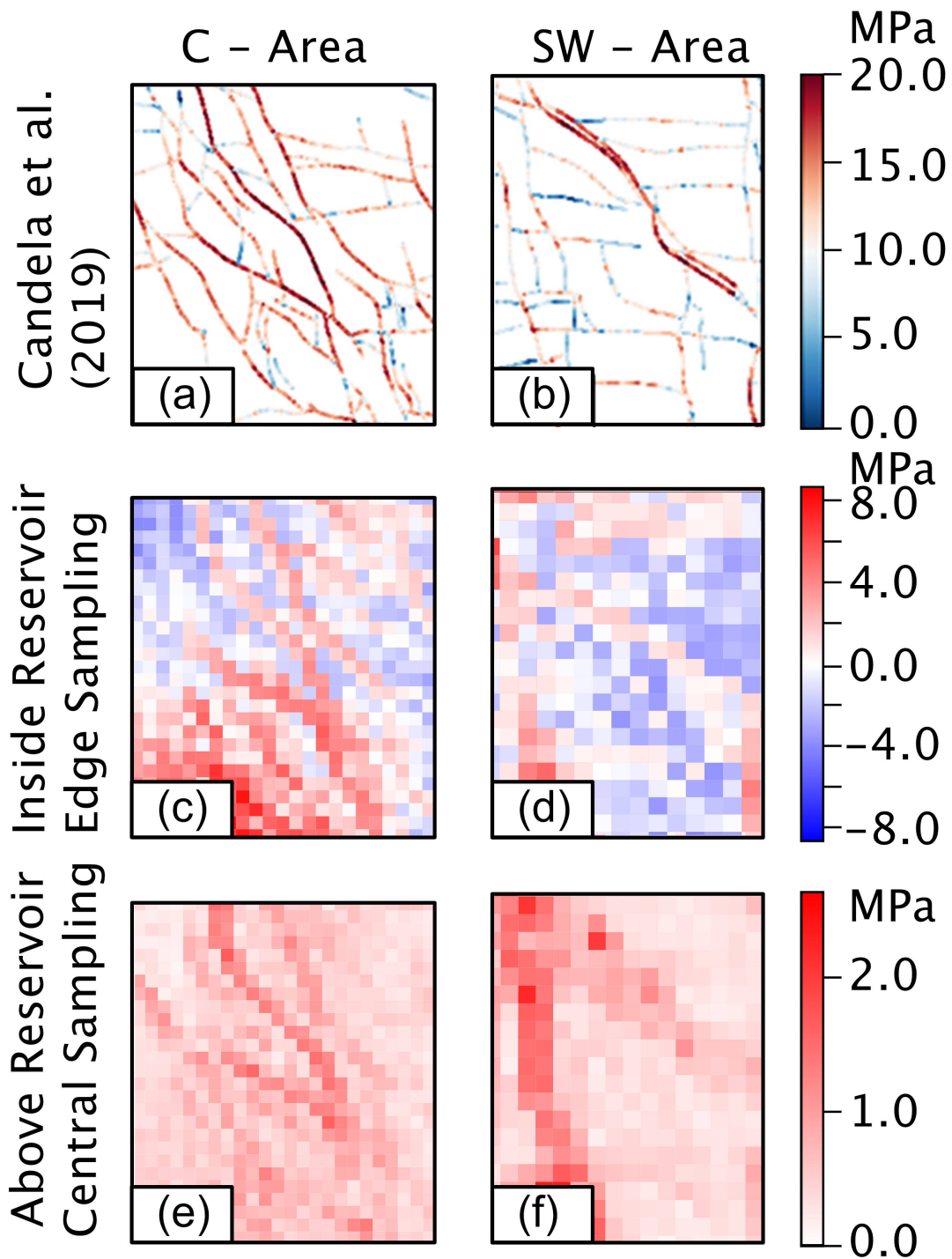


Figure 3: Coulomb stress changes between 1965 and 2016 for two regions in South-West (a) and Central (b) part of the reservoir from Candela et al. (2019). The plots shows the maximum Coulomb stress change on the known faults in these areas. Maximum Coulomb stress change calculated with our model in the reservoir near the cuboid edges (c,d), 10 m away in the E and N direction from the north east corner of each cuboid, or in the caprock (e,f), 5m above the top of the reservoir and above the centers of the cuboids.

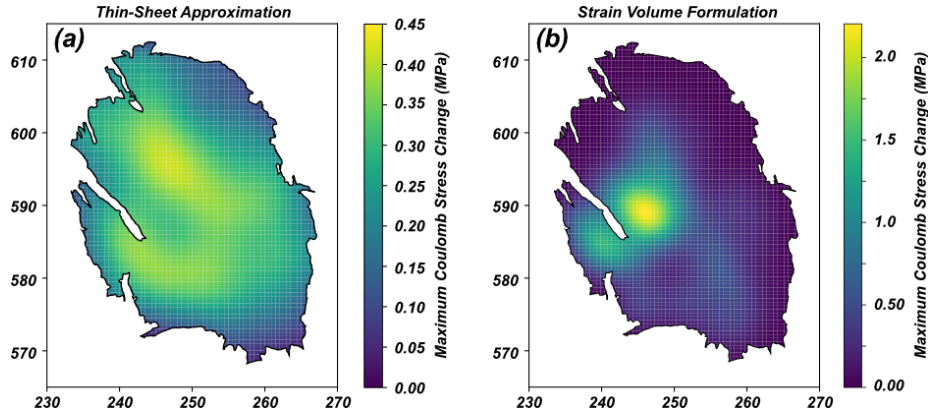


Figure 4: Comparison of the Thin-Sheet Bourne and Oates (2017) and Strain-Volume maximum Coulomb stress change for the period of 1965-2017. (a) Thin-sheet maximum Coulomb stress change with black outline representing the reservoir outline at depth (b) Strain volume maximum Coulomb stress change calculated within the reservoir at the North-East of the cell blocks, smoothed to 3.2km resolution

274 and Oates (2017), the calculation is made with a Poisson Coefficient $\nu = 0.2$, a
 275 friction angle $\phi = 0.5$ and a Biot coefficient = 1. In that case, failure is promoted
 276 both by the shear induced by the reservoir geometry and by the poroelastic
 277 increase of differential stress. In their implementation Bourne and Oates (2017)
 278 applied a spatial smoothing and filter out faults with offset exceeding some given
 279 fraction of the reservoir thickness offset. The two parameters, optimized to
 280 best fit the seismicity data using a Markov-Chain Monte Carlo procedure, were
 281 determined as 3.2km and 0.43 respectively. Thresholding faults with large offset
 282 relative to the reservoir thickness is justified by the presence of salt above the
 283 anhydrite caprock. Faults with large offset presumably juxtapose the reservoir
 284 against the salt and could be considered aseismic. The pattern of stress Coulomb
 285 changes within the reservoir, sampled near the cuboid edges and smoothed with
 286 the same Gaussian kernel is similar to that obtained with the ETS (Figure 4).

287 2.4. Stress sampling scheme

288 Keeping in mind that the objective is to feed a seismicity forecast, different
 289 sampling strategies of the stress changes might be adopted. A natural choice

290 would be to sample the stress field at the location where changes are max-
291 imum and assuming faults with orientation yielding the maximum Coulomb
292 stress change (Figure 5a) or with a fixed orientation corresponding to one or
293 the other dominant mapped fault orientations (Figure 5b and 5c). These sam-
294 pling schemes give a disproportionate influence of the very localized areas of
295 faster stress buildup where the reservoir is offset by small faults, as is the case
296 in the southern part of the reservoir, and the stress values are very sensitive to
297 the details of the meshing. In fact, the seismicity does not match particularly
298 well the known faults offsetting the reservoir (Figure 1). A large fraction of
299 the earthquakes thus probably occur on secondary faults that were not mapped
300 and in areas of stress concentration not represented in our reservoir model. We
301 take this as an indication that the reservoir model, although quite detailed,
302 does not account for all the complexity of the reservoir geometry and for the
303 heterogeneities of compressibility responsible for stress build up during reservoir
304 compaction. We however tested these possible sampling schemes as described
305 below and in supplementary figures, and chose as our reference stress model
306 the solution obtained from the more robust scheme by sampling at the cuboid
307 centers (Figure 5d). None of these sampling schemes is completely satisfying to
308 yield a realistic estimate of the stress changes at the exact location of where the
309 earthquakes are induced, but we show below and in supplement that using any
310 of them doesn't impact much the seismicity forecast, essentially because of the
311 model calibration step. In addition, to avoid a seismicity forecast too tightly
312 tied to the particular set of faults represented in the reservoir model, we apply a
313 smoothing to the stress field using a Gaussian kernel with 3.2km standard devi-
314 ation. This particular value was chosen for consistency with Bourne and Oates
315 (2017) and the resolution of spatial heterogeneities of compressibility. This is
316 an ad hoc way to account for stress concentrations due to secondary faults or
317 to small scale variations of compressibility not represented in our model. This
318 procedure predicts a spatial distribution of earthquakes in better qualitative
319 agreement with the observations than the other sampling schemes that we have
320 tested, including in particular those shown in supplement.

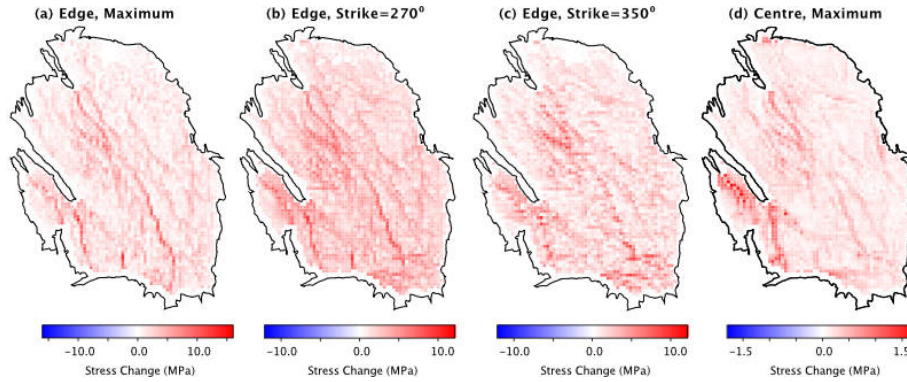


Figure 5: Coulomb stress changes in the caprock, calculated 5m above the reservoir top, between 1965 and 2017. (a) Maximum Coulomb stress change sampled 10m within from the North-East of the cuboid edges. (b) Coulomb stress changes on N270°E striking faults sampled 10m within from the top-right of the cuboid edges. (c) Coulomb stress changes on N350°E striking faults sampled 10m within from the top-right of the cuboid edges. (d) Maximum Coulomb stress change sampled at the center of the cuboids.

321

322 We also tested different schemes regarding the depth of the sampling points.
 323 Figure 6 shows the stress changes at grid points coinciding in map view with
 324 the centers of the cuboids, and at various elevations relative to the reservoir. It
 325 illustrates how the maximum Coulomb stress change attenuates away from the
 326 zone of stress concentration where the reservoir is offset by faults both in map
 327 view and with depth.

328 We assume that the pore pressure in the domains above and below the
 329 reservoir is not connected to the fluid pressure in the reservoir. Figure 6 shows
 330 similar patterns of Coulomb stress increase above and below the reservoir. The
 331 amplitude of the Coulomb stress change decreases above the reservoir and the
 332 spatial distribution evolves slightly, with a Coulomb stress change high in the
 333 south-west of the reservoir shifted to the north-east at shallower depth. The
 334 variations are small within the top 50m of the reservoir where the distribution
 335 of hypocentral depths is peaking (Figure 6). The time-evolution of the maximum
 336 Coulomb stress 5m above the reservoir is shown in Supplementary Figure A4.

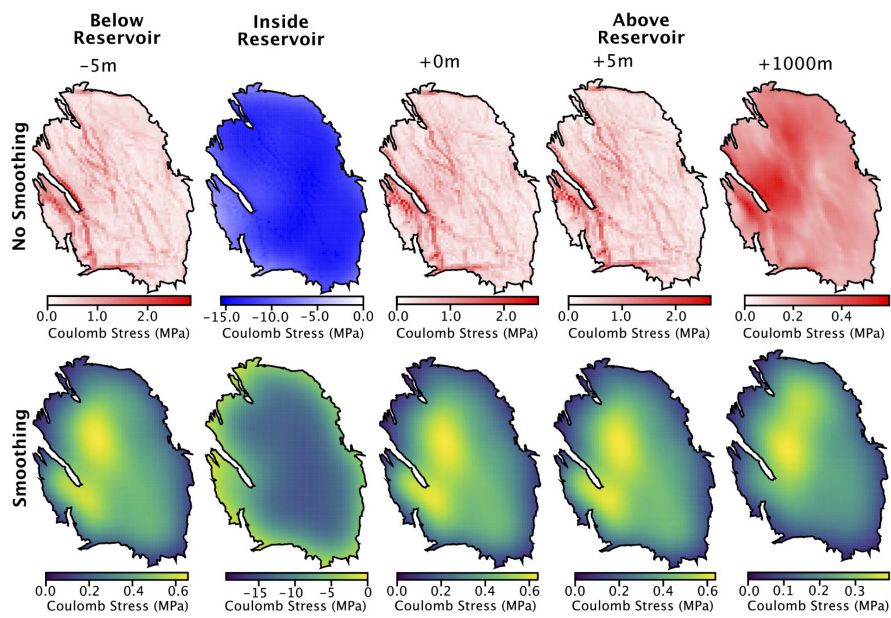


Figure 6: Maximum Coulomb stress changes from 1965 to 2017 at various elevations relative to the reservoir. (a)-(e) represent the maximum Coulomb stress for the unsmoothed. (f)-(j) maximum Coulomb stress models smoothed to a length scale consistent with uniaxial compressibility (3.2km).

337 Given the similar patterns of stress changes at the various depths, we choose
338 to tie the seismicity to a single reference elevation above the reservoir. This 2-D
339 assumption allows to reduce the computation cost that would be needed for a
340 full 3-D calculation. Given that the depth distribution of hypocenters peaks
341 right above the top of the reservoir, we estimate seismicity rate based on the
342 maximum Coulomb stress change computed 5m above the top of the reservoir
343 with the strain-volume model (Figure 4b; with forecasting potential at different
344 depths and different Coulomb models discussed further in Section 3).

345 We compare the maximum Coulomb stress change from 1965 to 2017 for the
346 ETS formulation and the maximum Coulomb stress change calculated with our
347 model at 5m above the reservoir (Figure 4). Although the two stress calculation
348 methods significantly differ, the spatial pattern and the amplitudes of Coulomb
349 stress changes are relatively similar.

350

351 **3. Relating stress changes and seismicity**

352 Stress-based earthquake forecasting requires some scheme to relate induced
353 seismicity to stress changes. Previous Earthquake forecasting studies focused on
354 Groningen have assumed instantaneous failure and a non-critical initial stress
355 (Bourne and Oates, 2017; Bourne et al., 2018; Dempsey and Suckale, 2017),
356 or non-instantaneous failure based on rate-and-state friction (Candela et al.,
357 2019; Richter et al., 2020). In this study we aim at simulating the evolution
358 of seismicity at the annual to multi-annual timescale. In a related study we
359 show that the finite duration of earthquake nucleation doesn't matter at these
360 time scales (Heimisson et al., 2021). We therefore assume here instantaneous
361 failure. Below we test the possibility that the seismicity is consistent the near-
362 exponential rise of seismicity rate due to the tail of the distribution, represented
363 by a generalized Pareto distribution by Bourne et al. (2018), or has transitioned
364 to the steady regime assumed by Dempsey and Suckale (2017).

365 We use the stress changes calculated from our model and the observed seis-

366 micity to estimate the initial strength excess, defined as the Coulomb stress
367 change needed to bring a fault patch to failure. An earthquake indeed indicates
368 a Coulomb stress change due to gas production equal to the initial strength ex-
369 cess before production started. This calculation requires some knowledge of the
370 fault orientation, which is known only for a very limited number of earthquakes
371 for which focal mechanisms could be calculated (Smith et al., 2020). There-
372 fore, we make the calculation for the fault orientation that yields the maximum
373 Coulomb stress change or the regional fault orientation. Because stress changes
374 are calculated at a reference elevation, samples at the center of the cuboids and
375 smoothed, this distribution does not rigorously represent the strength excess,
376 but can be considered a proxy for it, which we use to estimate of probability of
377 inducing an earthquake at a given stress change. In fact, we can only estimate
378 the part of the initial strength distribution that is revealed by seismicity. The
379 forecast requires a parametric representation of the part of the distribution that
380 has not yet been brought to failure. The shape of that distribution depends
381 in principle on the orientation of the faults and the heterogeneities of the ef-
382 fective stress tensor. For a homogenous tri-axial stress regime and standard
383 Mohr-Coulomb failure criterion, the strength excess can be calculated assuming
384 some distribution of fault orientations. If the activated faults have all the same
385 orientation either because they correspond to a pre-existing tectonic fabric, or
386 are optimally oriented with respect to the stress field, the distributions should
387 be close to a Dirac distribution. In that case all earthquakes would happened
388 at approximately the same Coulomb stress change. Our calculation shows a
389 relatively wide spread of values. The spread of this distribution can result from
390 the heterogeneities of initial effective stress, cohesion, friction, fault orientation,
391 hypocentral depths and from the uncertainties in the stress change calculation.
392 We therefore consider the strength excess as a stochastic variable. This ap-
393 proach is similar to the Extreme threshold Model of Bourne and Oates (2017)
394 which assumes that the seismicity only reflects the tail of the failure probability
395 function (failure of the faults with the smallest strength excess). According to
396 the extreme value theory the tail of the distribution can be represented by a gen-

397 eralised Pareto distribution (Figure 7) so that the failure probability function
 398 becomes

$$P_f = \exp(\theta_1 + \theta_2 \Delta C), \quad (21)$$

399 where $\theta_1 = \frac{C_t}{\bar{\sigma}}$ and $\theta_2 = \frac{1}{\bar{\sigma}}$ relate to the mean C_t , and standard-deviation $\bar{\sigma}$ of
 400 the initial strength excess distribution.

401 However, it is possible that the seismicity may have transitioned to a more
 402 steady regime in which case the representation of only the tail of the distribution
 403 might be inadequate. For each fault the distribution of strength excess depends
 404 on the probability distributions describing its orientation, stress and strength.
 405 Heterogeneities of stress resulting from variations of elastic properties of litho-
 406 logical origin can result in a Gaussian distribution of Coulomb stress changes
 407 (Langenbruch and Shapiro, 2014). The other factors of strength excess variabil-
 408 ity might be assumed, like the geometric effect due to the faults orientation, to
 409 be unimodal as well. If we assume that the initial Coulomb stress values on dif-
 410 ferent fault patches are independent and identically distributed random values,
 411 then, by virtue of the central limit theorem, we may assume a Gaussian distri-
 412 bution of initial strength excess, as is expected in the case where the only source
 413 of strength excess is due to heterogeneities of elastic properties (Langenbruch
 414 and Shapiro, 2014). In that case the probability of failure of a fault at a location
 415 with a maximum Coulomb stress changes ΔC is derived from integration of the
 416 Gaussian function yielding

$$P_f = \frac{1}{2} \left(1 + \operatorname{erf} \left(\frac{\Delta C - \theta_1}{\theta_2 \sqrt{2}} \right) \right), \quad (22)$$

417 where θ_1, θ_2 represent the mean and standard deviation of the Gaussian distri-
 418 bution, representing the fault strength distribution. This formulation is shown
 419 by the blue line in Figure 7b, with the initial Gaussian represented by the dashed
 420 blue line. As the Coulomb stress increases, the first earthquakes will occur on
 421 the faults with the lowest strength excess and so will provide information on
 422 the tail of the initial strength excess distribution. In that regime the extreme

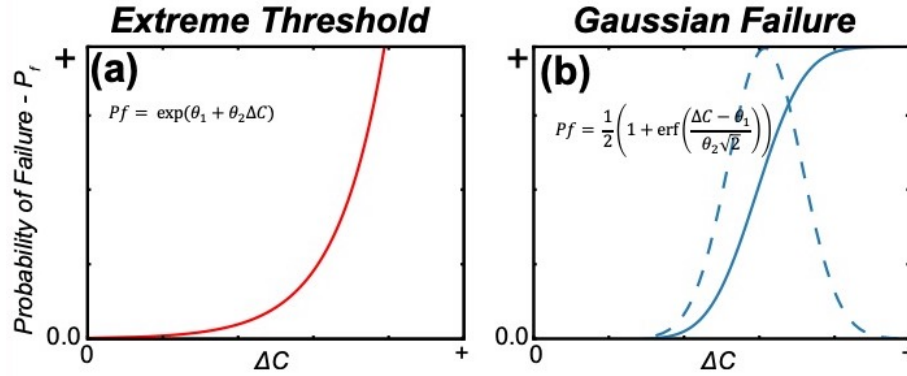


Figure 7: Probabilistic failure functions for the Extreme-Threshold (a) or Gaussian Failure (b) models. The blue dashed line represents the Gaussian distribution and the solid dashed line the cumulative distribution function.

423 value theory implies an exponential rise of seismicity for a constant stress rate
 424 (Bourne and Oates, 2017). As the stress increases to a value of the order of the
 425 mean initial strength excess (θ_1) the seismicity rate will gradually evolve to a
 426 regime where the seismicity rate will be proportional to the stress rate. If the
 427 faults that have already ruptured are allowed to re-rupture and if the Coulomb
 428 stress has increased to a value significantly larger than the typical stress drop
 429 during an earthquake, the distribution of strength excess will become uniform
 430 (constant between 0 and the co-seismic stress drop); the seismicity rate would
 431 then remain proportional to the stress rate. This is the steady regime expected
 432 an active tectonic setting for instantaneous nucleation (Ader et al., 2014). One
 433 important question for seismic hazard assessment at Groningen is whether the
 434 system has moved out of the initial exponential rise of seismicity. To address
 435 this question, we compare the performance of the Gaussian model describes
 436 above, which allows for this transition, and of the Extreme threshold Model of
 437 Bourne and Oates (2017) which assumes that the seismicity only reflects the
 438 tail of the failure probability function.

Failure Function	θ_1 Bounds	θ_2 Bounds	θ_3 Bounds
Extreme Threshold	0.0 – 15.0 MPa	0.0 – 30.0 MPa ⁻¹	0.0 – 2.0
Gaussian Failure	0.01 – 0.75 MPa	0.01 – 0.75 MPa	–2.0 – 15

Table 2: Failure function uniform priors for Extreme Threshold and Gaussian Failure functions.

439 4. Estimation of model parameters

440 Here we determine the best fitting failure function parameters relating the
441 modelled Coulomb stress change with the observed regional seismicity. We use
442 the catalogue of Dost et al. (2017) which reports earthquake locations since
443 1990, with a completeness of $M_{LN} > 1.5$ since 1993. We separate the observed
444 earthquakes into yearly bins, denoted as R_y^o , where subscript y indicates the
445 year and superscript o stands for “observed”. We select a training period $y \in$
446 $[y_s : y_e]$, where y_s represents the start year of training and y_e is the end year
447 bin. The start year is selected as $y_s = 1990$, where the magnitude of detection
448 is consistently above $M_{LN} = 1.5$ (Dost et al., 2017). The end year is set at
449 2012 and 2012 – 2017 is used for validation. The bounds of the uniform prior
450 for the parameter optimisation for the Extreme Threshold and Gaussian failure
451 functions are given in Table 2.

452 Predicted earthquake rates are formulated using a non-homogeneous Poisson
453 point process with the intensity function represented by:

$$\Lambda = \theta_3 \frac{\partial P_f}{\partial t} \quad (23)$$

454 where λ represents an earthquake productivity per given volume and $\frac{\partial P_f}{\partial t}$ the
455 partial differential of the probability function changing in time. This formulation
456 contains three unknowns, θ_1 , θ_2 and θ_3 , which are assumed spatially uniform.

457 Following Heimissson et al. (2021), we quantify misfit using a Gaussian log-
458 likelihood function. The Poisson Loglikelihood Ogata (1998) is more commonly
459 used. One issue is that it requires a declustered catalog to remove aftershocks.
460 Heimissson Heimissson (2019) shows that Dieterich’s model is actually valid even

461 in presence of inter-event triggering so that it is actually better not to remove af-
 462 tershocks and that, in that case, a Gaussian Loglikelihood is more adequate. The
 463 catalog of Groningen doesn't include much aftershocks apparently, so whether
 464 one likelihood or the other is chosen makes no significant difference. The misfit
 465 function writes,

$$\log(p(m|R^o)) = -\frac{1}{2} \sum_{i=1990}^{i=2016} \left(R_i^o - \int_{\Sigma} R(m, i, x, y) dx dy \right)^2, \quad (24)$$

466 where $R(m, i)$ is the model predicted rate density in year i , where m is the
 467 vector of model parameters. R_i^o is the observed rate in year i . Integration in
 468 Easting, x , and Northing y , is carried over the area Σ . because of the predicted
 469 seismicity rate can be equal to zero ($R = 0$). During the training we sample
 470 the PDF (Equation 24) using an Metropolis-Hastings sampler. After sufficient
 471 number of samples, hindcasts are obtained by selecting 1000 random samples of
 472 $m = m_1, m_2, \dots$ at random and computing $R^p(m, t)$ for $t > y_e + 1$.

473

474 5. Results and Discussion

475 In this section we discuss how the observed seismicity compares to model
 476 predictions in time and space based on the stress change calculated with strain-
 477 volume formulation for the Gaussian and Extreme-Threshold failure functions.
 478 We consider predictions based on our reference stress model where the Maxi-
 479 mum Coulomb stress changes calculated with the strain-volume formulation at
 480 the cuboid centers and smoothed spatially. To simplify the forecast and reduce
 481 the computational cost, we relate the seismicity to stress changes calculated 5m
 482 above the reservoir top. We also show forecast based on stress changes calcu-
 483 lated with the Elastic-Thin-Sheet model and on a variations from our reference
 484 model. We show in particular that the forecast is insensitive to the choice of a
 485 particular reference depth (Supplementary Figures A4 and A5). We also con-
 486 sider the forecast obtained if no smoothing is applied to the stress field, if stress
 487 changes are sampled at the edges of the cuboids where they are maximum, or

488 if the forecast is based on the Coulomb stress changes on faults with a fixed a
489 orientation set to one or the other of the two dominant orientations observed at
490 Groningen (Supplementary Figures A6, A7 and A8).

491

492 *5.1. Failure Functions and temporal evolution of seismicity*

493 The observed time-evolution of seismicity is compared to the prediction for
494 the Gaussian and Extreme-Threshold models, using our reference stress model,
495 in Figures 8a and 8c respectively. The differences between the earthquake rates
496 derived from the extreme-threshold and Gaussian failure model are insignificant
497 over the training period. However, we note that the Gaussian model predicts
498 a longer seismicity lag with the onset of seismicity occurring three years af-
499 ter that of the extreme-threshold (Figure 8a and 8b). We verified that given
500 the magnitude-frequency distribution of earthquakes is well described by the
501 Gutenberg-Richter law for a b-value of 1 (Bourne and Oates, 2020), both mod-
502 els are consistent with the fact that no seismicity was reported before 1990 when
503 only earthquakes with magnitude larger than about 2.5 could be detected.

504

505 Investigating the temporal forecast across all the model with have tested by
506 varying the sampling location of the stress field and using either the maximum
507 Coulomb stress change or the Coulomb stress change calculated for the average
508 fault orientation, we find little variation in the training logp value. All models
509 perform similarly and also yield similar forecast over the validation period. The
510 validation log-p is however best for the forecast based on the Coulomb stress
511 change calculated 5m above the reservoir (Supplementary Figures A8 and A9).

512 Figure 9 shows the distribution of Coulomb stress changes calculated at the
513 earthquake location for comparison with the failure functions obtained from our
514 inversion. The comparison shows that even with the Gaussian model the seis-
515 micity data constrain mostly the tail of the distribution. Some of the acceptable
516 Gaussian models show a roll-over that would suggest the beginning of the tran-
517 sition to a more steady regime. In any case, the two model parametrizations

518 yield relatively similar failure function in the domain constrained by the obser-
519 vations. These distributions depend on the input stress field and so the actual
520 values of the stresses would be rescaled if another stress field is chosen as an in-
521 put. A key point is that the introduction of a stress threshold provides a sound
522 way to explain the lag of the seismicity response to the gas extraction. Another
523 key point is that the stochastic distribution of this threshold can explain well
524 the initially exponential rise of seismicity as initially suggested by Bourne et al.
525 (2018). An alternative representation, presented in Heimisson et al. (2021), is
526 to assume a population of faults below steady-state with nucleation governed
527 by rate and state friction. In that case, a single stress threshold is introduced,
528 which estimated to 0.17MPa with a 95% of 0.07 – 0.18MPa using the same
529 reference stress model as in this study. For comparison, we get a threshold
530 distribution peaking at 0.32MPa with a standard deviation of 0.07MPa. The
531 two notions are however not equivalent as the threshold associated to the rate-
532 and-state model of nucleation determines the stress needed for a fault patch to
533 evolve toward rupture, while our Gaussian failure model assumes instantaneous
534 nucleation. The distribution of the initial state variable determines the time
535 distribution of earthquakes in the rate and state model.

536 *5.2. Spatial distribution of seismicity*

537 We compare here the spatial distribution of earthquake probability predicted
538 by our models to the observed seismicity. We test the strain-volume and thin-
539 sheet stress redistribution models, and the extreme-threshold and Gaussian fail-
540 ure models, leading to four predictions. Figure 10 shows the observed and pre-
541 dicted seismicity for various models in addition to our reference model. All these
542 model were calibrated against the observations. We show only the prediction
543 from the best-fitting set of parameters.

544 The Gaussian and extreme-threshold failure models predicts similar spatial
545 distribution of earthquake probability, whether the strain-volume or thin-sheet
546 formulations is chosen to calculate stress redistribution. Slight differences are
547 visible though. For the thin-sheet formulation the Gaussian failure function

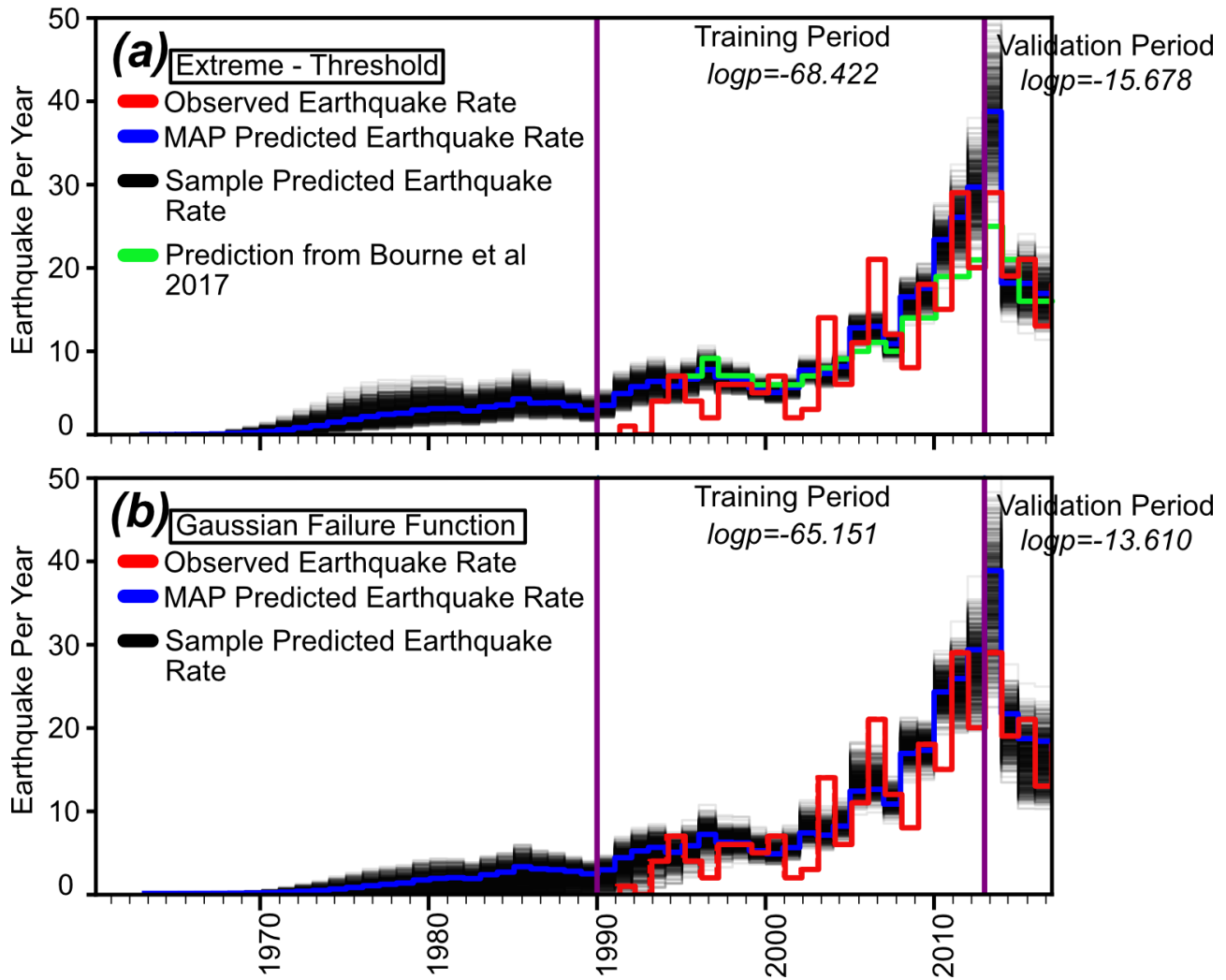


Figure 8: Comparisons of the observed seismicity rate with predicted rates calculated with the extreme-threshold (a) and Gaussian (b) failure models using the strain-volume formulation. Blue lines represent the maximum a posteriori (MAP) estimate of earthquake rate. Grey shading represents the probability distribution. Red solid line represents the observed seismicity catalogue used for training. The green line in panel (a) represents the best fitting prediction based on the thin-sheet approximation and extreme threshold model (Bourne and Oates, 2017).

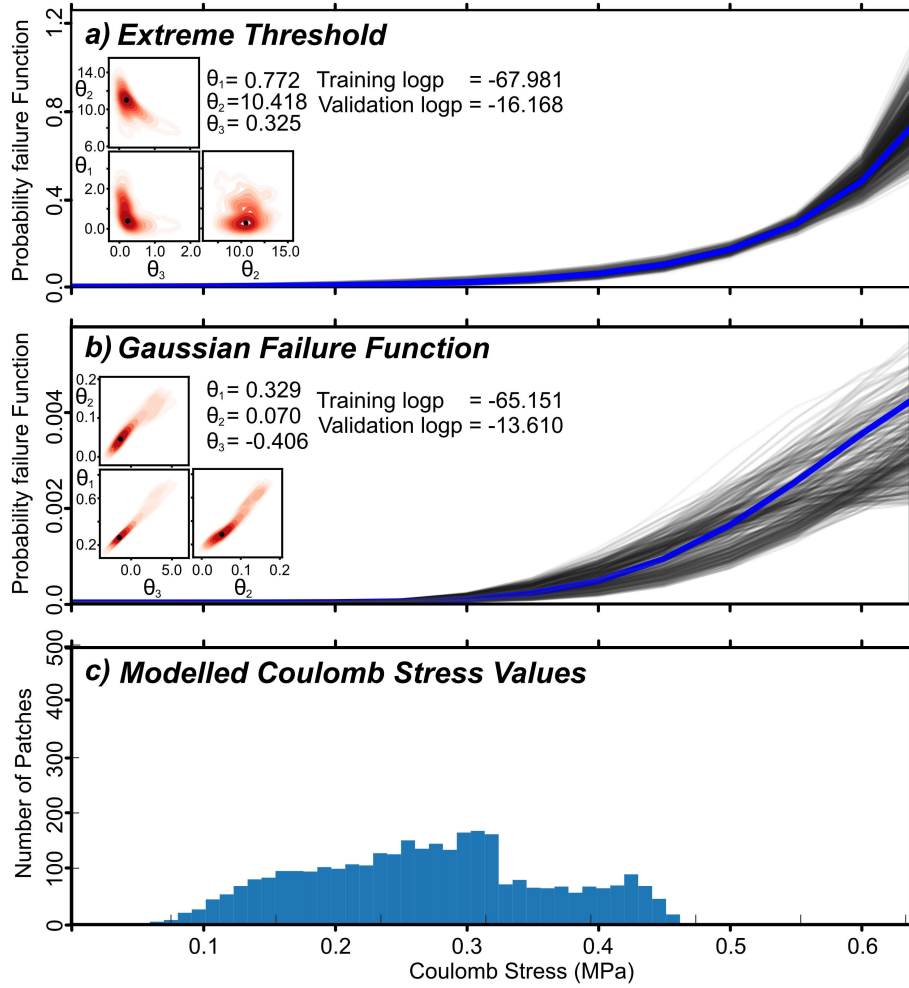


Figure 9: Optimised probability failure functions for the extreme-threshold and Gaussian failure functions. Blue lines represent the maximum a priori estimate of synthetic earthquake rate. Black lines represent samples from the probability distribution with colour dependent on the probability. (a) Extreme threshold failure function. (b) Gaussian failure function. (c) Histogram of the modelled Coulomb stress values across the reservoir from the strain-volume formulation.

548 yields higher probability of failure in the north-west of the reservoir region com-
549 pared to the extreme-threshold failure criterion. When the the input stress field
550 is not smoothed and sampled either at the cuboid centers or at the cuboid edges
551 where stress changes are maximum, the forecast in time is good (Figure A7),
552 although with p-values not as good as what can obtained with the smoothed
553 stress field. They however make distinct predictions regarding the spatial dis-
554 tribution of earthquakes (Figure A7). They predict a very heterogenous spatial
555 distributions that don't match well the observed seismicity (Figure 10). Because
556 of the small catalog, we didn't carry out statistical tests, but we don't think
557 would be appropriate to use such models for hazard assessment because there
558 is no indication that the spatial heterogeneities predicted by those models are
559 valid.

560

561 It should be noted that the best-fitting model parameters are significantly
562 different depending on the choice of the input stress field and reference elevation.
563 The Coulomb stress changes at the location of the EQs are probably underes-
564 timated in our reference model. This bias is compensated by the calibration of
565 the model parameters against the observed seismicity. The procedure has merit
566 for the purpose of probabilistic seismicity forecasting but the model parameters
567 are biased.

568 *5.3. Are earthquake nucleating in the caprock, reservoir or underburden?*

569 The model accounts for stress redistribution withing and outside the reser-
570 voir with account for stress localization at the faults offsetting the reservoir.
571 The importance of accounting for this process has been demonstrated in a num-
572 ber of previous studies (Mulders, 2003; Rutqvist et al., 2016; Buijze et al., 2017,
573 2019; Jansen et al., 2019). In agreement with these studies, we find that the
574 stress changes are maximum at the top or bottom of the reservoir in the vicin-
575 ity of discontinuities created by faults offsetting the reservoir due to faulting.
576 The model is consistent with the observation that seismicity hypocenters tend
577 to concentrate in the caprock. The seismic ruptures don't need to be confined

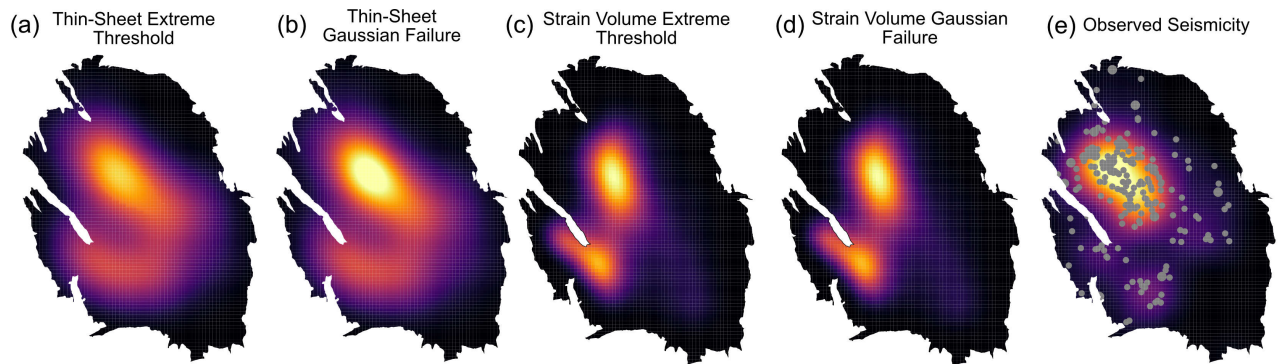


Figure 10: Spatial distribution of earthquake probability for various models compared to observed seismicity. (a) Observed seismicity during the 1993 – 2012 training period (white dots), with shading showing the normalized density of earthquakes obtained by convolution with a Gaussian kernel with a 3.2 km standard deviation. (b) Model prediction using the reference stress model (maximum Coulomb stress change sampled at cuboid centers, 5m above the top of the reservoir smoothed with a Gaussian kernel of 3.2 km standard deviation) and the Gaussian failure function.(c) Same as (a) using the extreme threshold failure function. (d) Model prediction using the Elastic-Thin-sheet formulation and extreme threshold failure model. (e) Elastic-Thin-sheet stress formulation using Gaussian failure function.(f) Same as (a) using the unsmoothed version of the reference model. (g) Model prediction using maximum Coulomb stress change sampled at the cuboid centers with no-smoothing and the Gaussian failure function (h) Same as (e) for Coulomb stress change on N270E striking faults

578 to the caprock though, are they can expand both into the reservoir or into the
579 overburden.

580 This view contrast with a number of previous studies (Dempsey and Suckale,
581 2017; Bourne and Oates, 2017; Richter et al., 2020) which have assumed that
582 earthquakes were triggered within the reservoir due to poroelasticity. The seis-
583 micity data don't exclude that the earthquakes might nucleate within the reser-
584 voir. In that regard, it should be noted that our reference model predicts no
585 Coulomb stress increase in the reservoir due to the choice of standard mechan-
586 ical properties (Poisson coefficient of 0.25, Friction of 0.66, and Biot coefficient
587 1.0). Our model can however predict an increase of Coulomb stress in the reser-
588 voir for still realistic model parameters ($\alpha > \alpha_c = \frac{1-\nu}{1-2\nu} \frac{2\sin\phi}{1+\sin\phi}$). This condition
589 is not strict however as it ignores the effect of the finite extent of the reservoir
590 and spatial variation of its geometry. Most importantly we find that, once the
591 model parameters are calibrated to fit the observations, the forecast is nearly
592 identical whether the earthquakes are assumed to nucleate within or outside the
593 reservoir.

594 The seismicity data make it improbable that earthquakes below the reservoir.
595 Our model doesn't provide any explanation for this observation as it predicts a
596 similar stress concentration in the overburden and underburden. Stress changes
597 are actually slightly smaller in the underburden because of the asymmetry in-
598 duced by the free surface. One possible explanation would be that the fluid
599 pressure in the underburden is more connected to the reservoir than in the
600 caprock, which has obviously been an effective seal over geological time. This
601 explanation is plausible because the Carboniferous shale-Slitstone formation in
602 the underburden is actually the source of the gas that has accumulated in the
603 Slochteren reservoir sandstone. In that case the Coulomb stress might have
604 actually dropped in the underburden leading to fault stabilization. Another
605 possibility is that faults in the underburden had a larger initial strength excess
606 due to the larger lithostatic pressure (as in Buijze et al. (2019)), or to stress
607 relaxation associated with ductile flow of the shale. Finally, it is possible also
608 that the shale and siltstone below the reservoir are less seismogenic than the an-

609 hydrite caprock. Laboratory measurements show no evidence that earthquake
610 cannot nucleate in the underburden, although they point to a larger strength
611 drop in the caprock that would be more favorable to earthquake nucleation there
612 (Hunfeld et al., 2021) .

613 **6. Conclusions**

614 This manuscript presents a framework for stress-based earthquake forecast-
615 ing of induced seismicity which should in principle be applicable in any setting
616 where earthquake are induced by deformation of a reservoir whether due to ex-
617 traction or injection. The framework requires some knowledge of the reservoir
618 geometry and compressibility on one hand, and of the pore pressure evolution on
619 the other hand. By representing the reservoir as a series of poroelastic cuboids,
620 the stress redistribution within and outside the reservoir can be calculated with
621 proper account for stress localization at the faults offsetting the reservoir and
622 poroelastic effects. The stress changes are calculated using semi-analytical Green
623 functions. This procedure is computationally very efficient and can therefore be
624 applied to compute stress changes at the scale of the entire reservoir over sev-
625 eral decades with a sub-kilometric spatial sampling rate and a yearly temporal
626 resolution. We use our method to calculate stress changes due to the reservoir
627 compaction to feed an earthquake forecasting scheme. Our scheme is similar
628 to but expands on the extreme threshold model of Bourne and Oates (2017);
629 Bourne et al. (2018) by allowing in principle to represent the transition from the
630 initial exponential rise of seismicity to the steady state regime where the seis-
631 micity rate should be proportional to the stress rate. We find that the Gaussian
632 failure function, which we introduce to that effect, has in fact an only slightly
633 lower validation loss than the extreme-threshold function. We find no evidence
634 that the seismicity at Groningen has actually transitioned to the steady-state
635 regime. Assuming a steady state regime therefore probably lead to an underes-
636 timation of the hazard level.
637 We find that the forecasting performance is similar if the stress calculation is

638 based on the elastic thin sheet approximation (Bourne and Oates, 2017) or on
639 the strain-volume method presented here. It is also independent of the chosen
640 vertical distance from the top of the reservoir used to extract the stress changes.
641 This is due to the fact that, in all these cases, the seismicity forecast is driven
642 by the spatial distribution of the discontinuities of the reservoir and the time
643 evolution by the pressure depletion history. The forecasting procedure seems
644 therefore relatively robust to the uncertainties on the modeling assumptions.
645 However, it is likely the forecast performance is satisfying because the seismic-
646 ity has been relatively stationary. If seismicity had shifted to the underburden
647 for example, it is probable that the forecasting performance of the algorithm
648 would drop and that the model parameters would need to be reevaluated. In
649 any case, one should be cautious about the interpretation of the model param-
650 eters and about the implications of a satisfying forecast. For example, the stress
651 threshold needed to initiate seismicity in our model depends on the chosen ele-
652 vation above the reservoir where the stresses are calculated and on the scheme
653 used to sample stress changes or evaluate earthquake probabilities. A satisfying
654 forecast doesn't mean that the particular choices made in the stress calculation
655 or the failure functions are correct. As an example a forecast based on the
656 assumption that the earthquakes initiate in the reservoir can be found satisfy-
657 ing, although the assumption might be incorrect. Similarly, the assumption of
658 a steady regime might seem acceptable to forecast seismicity over a short pe-
659 riod of time but the linear extrapolation that the assumption implies could be
660 incorrect and the model parameters (the ratio between the stress rate and the
661 seismicity rate) would be dependent on the period used to calibrate the model
662 and would have little physical significance.

663 The procedures presented in this article is computationally effective and could
664 be implemented into a traffic-light system during reservoir operations. It would
665 also easily allow for data assimilation (re-evaluation of the model parameters as
666 seismicity observations are collected).

667 In this work we have assumed that earthquakes nucleate instantaneously at a
668 critical stress. We do not account for the finite duration of the nucleation process

669 which can be described using the rate-and-state friction formalism and which
670 has been used in some previous studies and could partly explain the seismicity
671 lag at Groningen (Candela et al., 2019; Richter et al., 2020). These studies use
672 the Dieterich (1994) model, that the earthquake population is at state of steady
673 earthquake production before it is perturbed. This hypothesis therefore ignores
674 that the system may have been initially in a relaxed state due to the low level of
675 tectonic loading in the Groningen context. Some modification of the formalism,
676 presented in Heimisson et al. (2021), is needed to account for a possible initial
677 strength excess. Although we didn't presented any such simulations here, the
678 code supplied in the Google Colab notebook include the possibility of running
679 forecast with the threshold rate-and-state model (Heimisson et al., 2021).

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686 (<http://www.knmi.nl/>). Strain Volume simulations can be found at the inter-
687 active Google Colab notebook [https://colab.research.google.com/drive/
688 1GDKMHD02obj4bT8ezvCxFumHz3CSE3Ns?usp=sharing](https://colab.research.google.com/drive/1GDKMHD02obj4bT8ezvCxFumHz3CSE3Ns?usp=sharing).

689 **Contributions**

690 J.D.Smith: Model method conceptualization, software development and
691 manuscript writing. E.R.Heimisson: Software development and manuscript
692 writing. S.J.Bourne: Supervision, Model method conceptualization, software
693 development. JP.Avouac: Supervision, Model method conceptualization and
694 manuscript writing.

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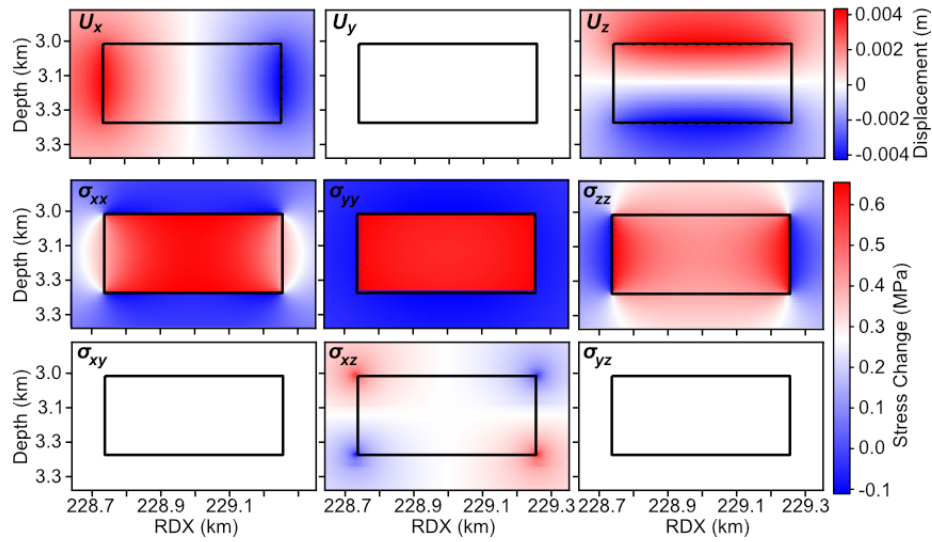


Figure A1: Displacement and stress changes induced by a single cuboid. The position and width of the cuboid is [228.5 km RDX, 574.5 km RDX, 3.018 km Depth] and [500 m, 500 m, 216 m]. The pressure depletion and uniaxial compressibility is 3.3 MPa and 1.816×10^{-11}

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810 Figure A5

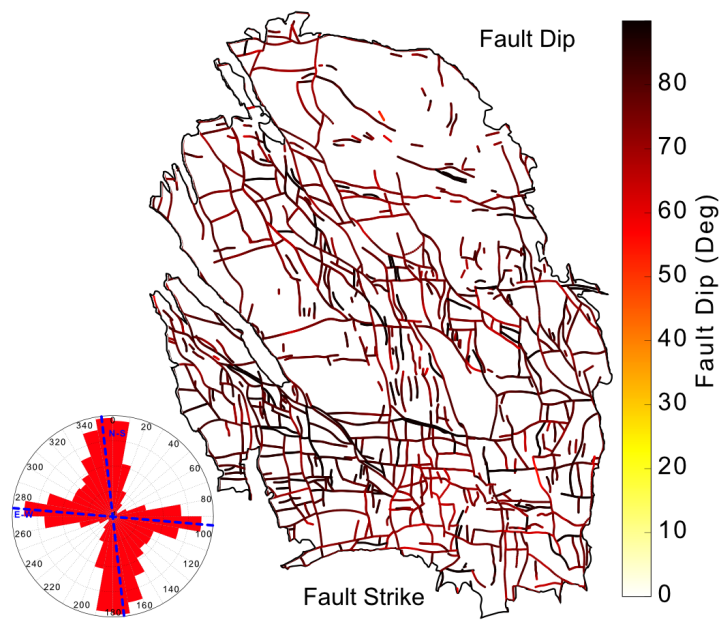


Figure A2: Map of faults offsetting the reservoir, color-coded with estimated dip angle (right). Rose diagram in inset shows the distribution of fault strike. Information on faults taken from Nederlandse Aardolie Maatschappij (2013).

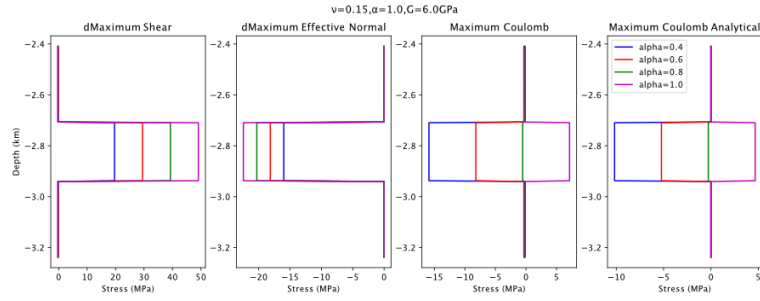


Figure A3: Stress changes calculated at the center of a reservoir of large spacial extent (a cuboid of 230m thickness and $38.5\text{km} \times 38.5\text{km}$ extent) at 2.94km depth, submitted to a pressure drop of 19.5MPa. The same values of the Poisson and friction coefficients ($\nu = 0.15$, $\mu = 0.66$) are used as in the nominal simulations shown in the main text, but the Biot coefficient is varied. In that case the maximum Coulomb stress is positive if the Biot coefficient exceeds a critical value. For a reservoir of infinite extent the critical value is $\alpha_c = 0.84$ (Equation 17). The ratio of the Coulomb stress change to the pore pressure change is $\frac{\Delta C}{\Delta P} = 2(1 - \frac{\alpha}{\alpha_c})\sin\phi$, where ϕ is the friction angle ($\tan\phi = \mu$). This analytical prediction is shown for comparison with the model output in the right panel.

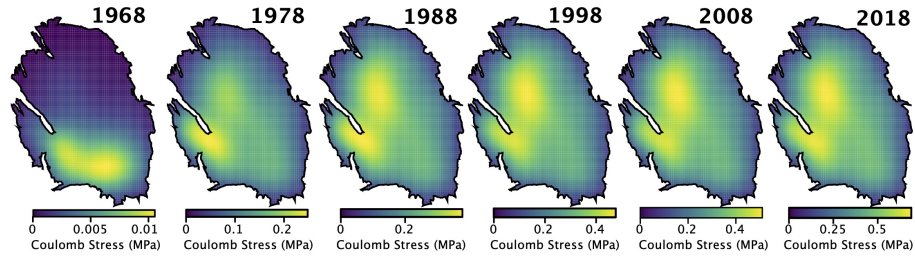


Figure A4: Time evolution of maximum Coulomb stress change calculated 5m above the top of the reservoir and smoothed with a Gaussian kernel with 3.2km standard deviation.

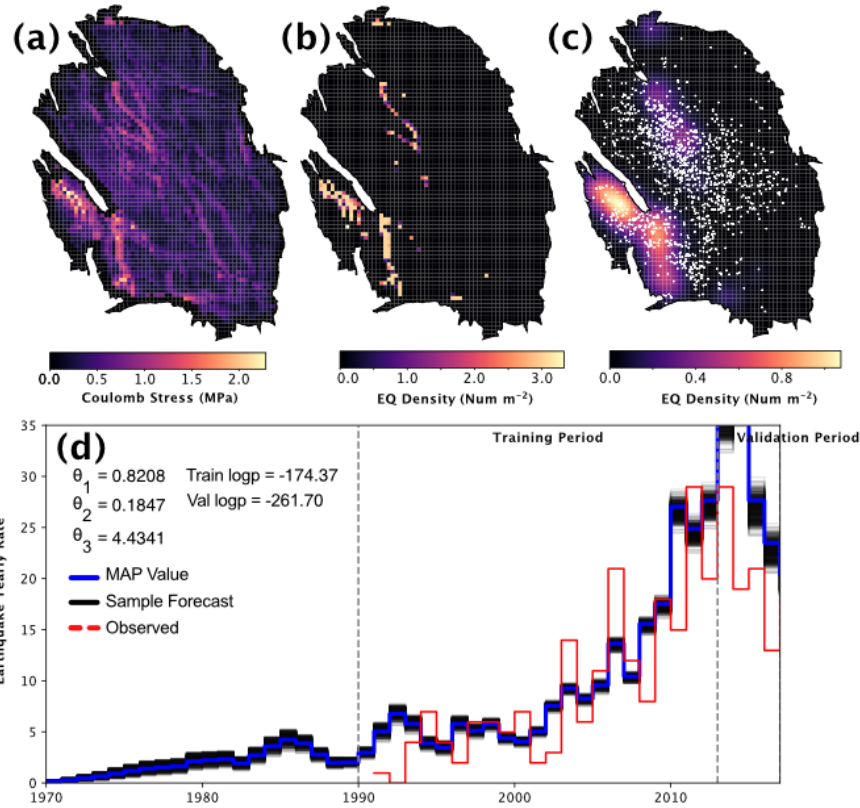


Figure A5: Temporal and spatial variations of seismicity rate predicted based on the maximum Coulomb stress changes on $N270\text{ deg }E$ striking and 80 deg dipping faults calculated 5 m above the reservoir at the midpoint of the cuboid edges. No smoothing was applied. (a) Map of Coulomb stress change. (b) Spatial distribution of forecast seismicity. (c) Observed seismicity (white dots) and predicted spatial distribution of seismicity rate smoothed using a Gaussian filter with 3km standard deviation. (d) Comparison of predicted and observed temporal variation of seismicity rate. The best fitting model parameters and the loglikelihood p-values for the training and validation periods are listed in panel d.

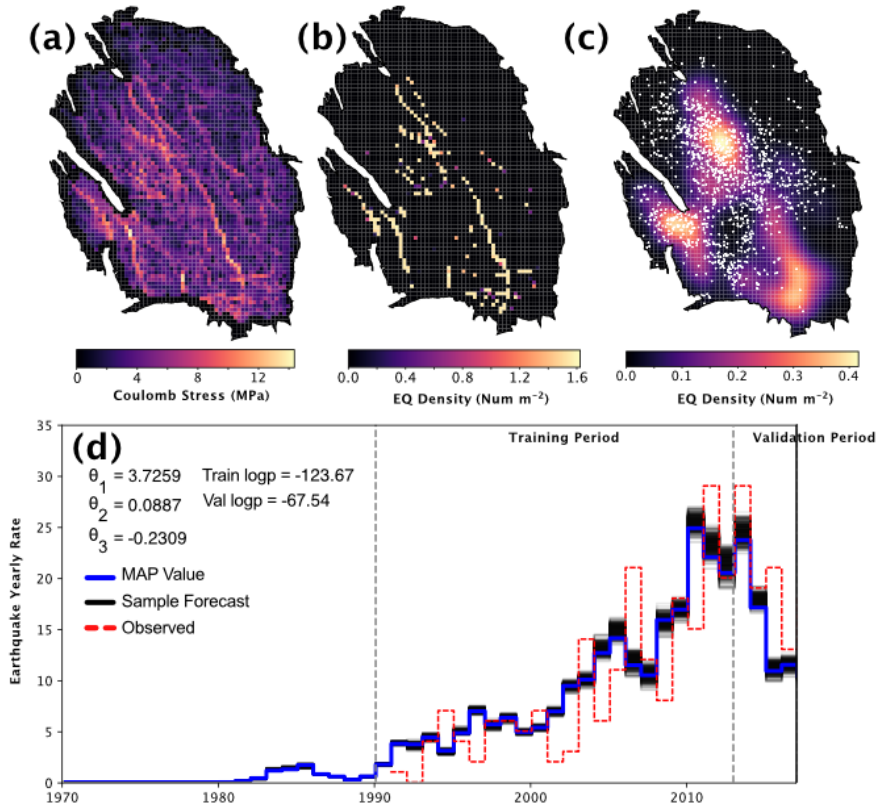


Figure A6: Temporal and spatial variations of seismicity rate predicted based on the Coulomb stress changes on $N270$ deg E striking and 80 deg dipping faults calculated 5 m above the reservoir 10 m within the North-East corner of the cell. (a) Map of Coulomb stress change with no smoothing. (b) Spatial distribution of forecast seismicity based on panel a. (c) Observed seismicity (white dots) and predicted spatial distribution of seismicity rate smoothed using a Gaussian filter with 3 km standard deviation. (d) Comparison of predicted and observed temporal variation of seismicity rate. The best fitting model parameters and the loglikelihood p-values for the training and validation periods are listed in panel d.

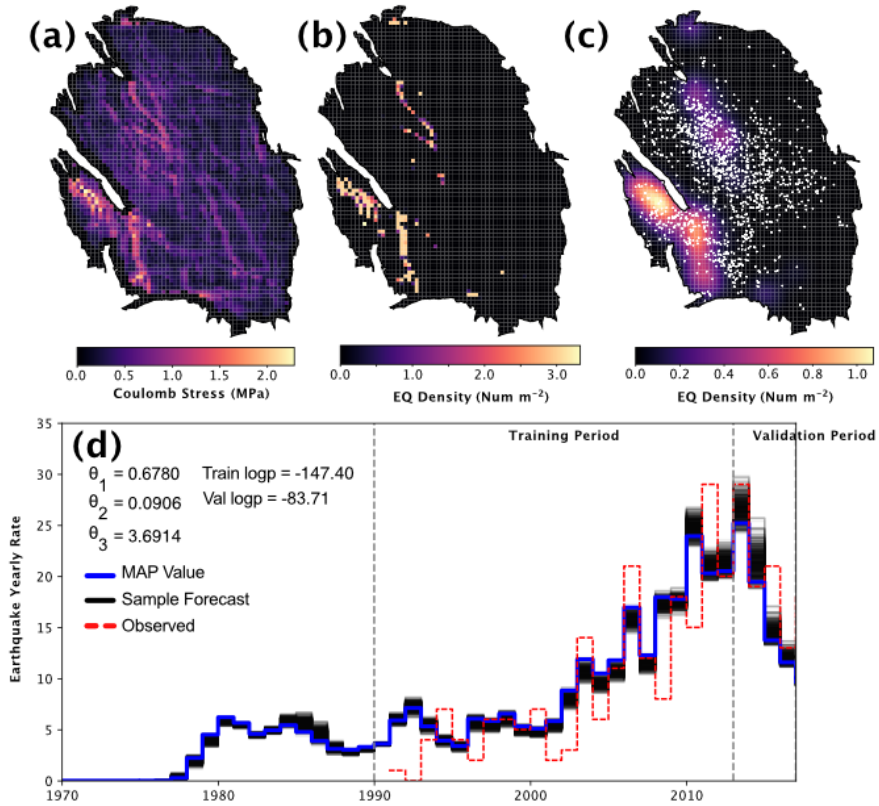


Figure A7: Temporal and spatial variations of seismicity rate predicted based on the Coulomb stress changes on $N350$ deg E striking and 80 deg dipping faults calculated at an elevation of 5 m above the reservoir at the cuboid centers. (a) Map of Coulomb stress change with no smoothing. (b) Spatial distribution of forecast seismicity based on panel a. (c) Observed seismicity (white dots) and predicted spatial distribution of seismicity rate smoothed using a Gaussian filter with 3km standard deviation. (d) Comparison of predicted and observed temporal variation of seismicity rate. The best fitting model parameters and the loglikelihood p-values for the training and validation periods are listed in panel d.

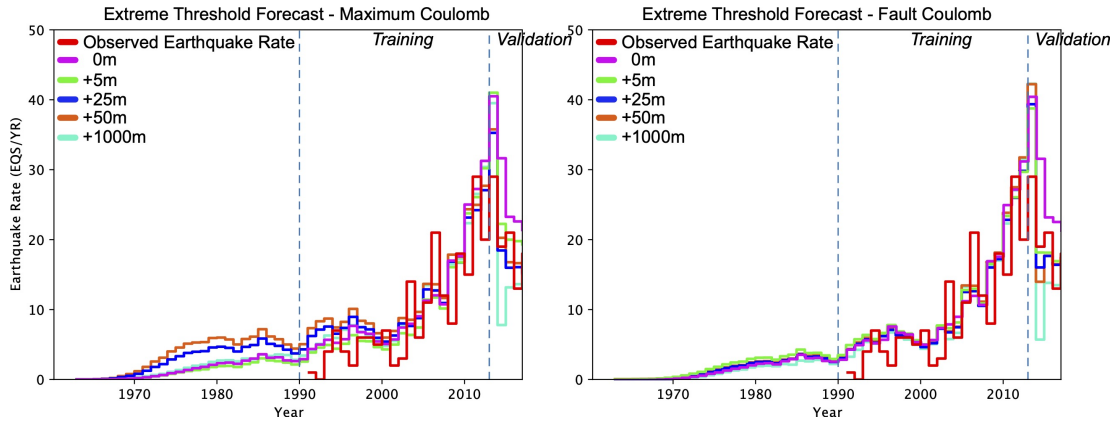


Figure A8: Predicted earthquake rates at different depths for the Extreme Threshold failure criterion and based on the smoothed distribution stress changes calculated at the cuboid centers. Left panel: maximum Coulomb stress change. Right panel: Coulomb stress change on $N350$ deg E striking and 80 deg dipping faults.

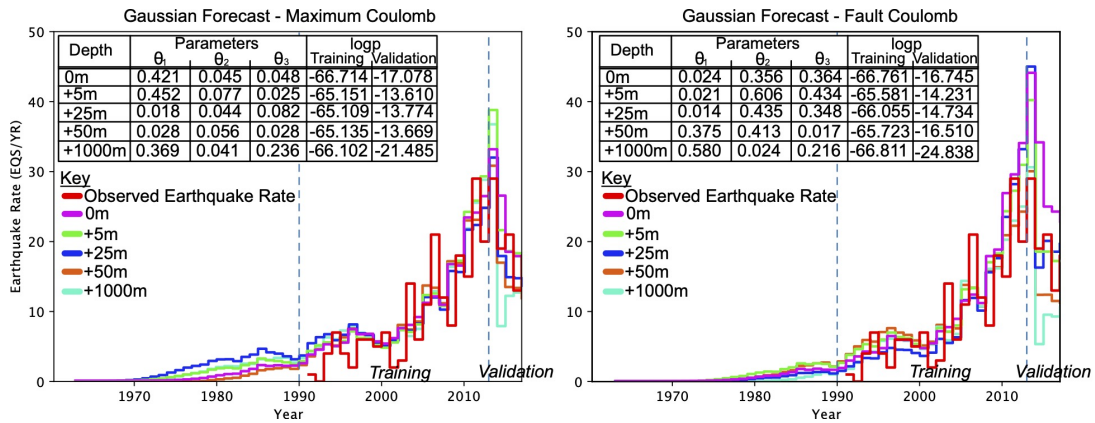


Figure A9: Predicted earthquake rates at different depths for the the Gaussian failure criterion and based on the smoothed distribution stress changes calculated at the cuboid centers. Left panel: maximum Coulomb stress change. Right panel: Coulomb stress change on $N350$ deg E striking and 80 deg dipping faults.