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Sedimentological data-driven bottom friction parameter estimation in modelling Bristol Channel tidal dynamics

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Abstract Accurately representing the bottom friction effect is a significant challenge in numerical tidal models. Bottom friction effects are commonly defined via parameter estimation techniques. However, the bottom friction coefficient (BFC) can be related to the roughness of the sea bed. Therefore, sedimentological data can be beneficial in estimating BFCs. Taking the Bristol Channel and Severn Estuary as a case study, we perform a number of BFC parameter estimation experiments, utilising sedimentological data in a variety of ways. Model performance is explored through the results of each parameter estimation experiment, including applications to tidal range and tidal stream resource assessment. We find that theoretically derived sediment-based BFCs are in most cases detrimental to model performance. However, good performance is obtained by retaining the spatial information provided by the sedimentological data in the formulation of the parameter estimation experiment; the spatially varying BFC can be represented as a piecewise-constant field following the spatial distribution of the observed sediment types. By solving the resulting low-dimensional parameter estimation problem, we obtain good model performance as measured against tide gauge data. This approach appears well suited to modelling tidal range energy resource, which is of particular interest in the case study region. However, the applicability of this approach for tidal stream resource assessment is limited, since modelled tidal currents exhibit a strong localised response to the BFC; the use of piecewise-constant (and therefore discontinuous) BFCs is found to be detrimental to model performance for tidal currents.

Keywords Bottom friction · Manning coefficient · Calibration · Parameter estimation · Sedimentological data

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1 Introduction

Numerical modelling of tides in coastal and estuarine regions has applications in a wide variety of areas. An application of particular interest is marine renewable energy, with tidal modelling central to resource assessment for both tidal range [1,37,32] and tidal stream based energy projects [50,53,55]. With other applications of tidal models including sediment and pollutant transport [39,28], fisheries and ecosystems [34,57] and hazards such as storm surge [12,23,54], accurate numerical modelling of tides is highly valuable.

However, such models are subject to a variety of uncertainty sources. Modelling errors arise from assumptions and simplifications in the governing equations, as well as discretisation errors, limitations in model resolution, and imperfect model inputs. One particular source of uncertainty, which is commonly addressed within the literature using parameter estimation methods, is the bottom friction coefficient (BFC). Friction between the ocean and the sea floor arises due to a boundary layer at the sea bed, and form drag due to bathymetry fluctuations. The process is not explicitly resolved in numerical models, and is instead treated as a parameterised process, via any of several formulations [60]. The value of the BFC therefore cannot be directly measured in the field, but can under certain assumptions be related to the roughness of the sea floor surface [46]. However, in addition to spatial variation due to bottom roughness, bottom friction parameters can also vary temporally (e.g. due to morphological changes [9] or seasonal changes in hydrological conditions [24]), as well as with mesh resolution, and a number of other physical or numerical variables [13]. For these reasons, bottom friction parameters are commonly treated via model calibration methods, where their value is determined by minimising the misfit between model outputs and observations, typically using data from tide gauges, acoustic Doppler current profilers (ADCPs) or satellite altimetry.

Approaches to model calibration within the literature vary widely in their complexity. Excluding studies dedicated to parameter estimation, the most common approach is to apply a spatially uniform BFC. In contrast, the highest-complexity approach is to allow the BFC to vary freely over the whole domain, and in this case it is common to supplement the observation data with a form of regularisation, to avoid the problem of over-fitting [35]. Intermediate complexity in the friction coefficient can be achieved via several approaches. [22] divide their model domain into regions of similar influence on the model-observation misfit using an adjoint gradient-based method, also taking into account the physical properties of the system. Another more common approach is the so-called independent points scheme, where the friction coefficient field is specified by interpolation between a selected set of ‘independent points’ [60,8]. The locations of these points can be distributed uniformly or according to physical features such as the bathymetry gradient [30]. Similarly, [48] divide their model domain by bathymetry contours in order to select a low-dimensional parameter space for their spatially varying BFC, while [36] propose the use of land use data to inform the BFC.

Alternatively, sedimentological data can be used for the purpose of constraining the spatial variation of the BFC, due to the underlying physical relationship between sediment type and the roughness of the sea bed, and hence the value of the friction coefficient. [33] directly apply Manning coefficients derived from sedimentological data within a model of the Irish Sea, supplemented by a localised BFC enhancement around a region of interest which they tune for optimal model performance. Similarly, [17] utilise sedimentological data to derive a spatially varying quadratic drag parameter for a tidal stream power application off the coast of Brittany, and subsequently perform a sensitivity analysis with respect to the roughness length assigned to one of the sediment types.

49 Within this study, we explore the use of sedimentological data within a BFC parameter
 50 estimation problem. We perform a number of parameter estimation experiments, utilising
 51 such data in different ways. By comparing model performance using the results of each
 52 parameter estimation experiment, the objective is to arrive at recommendations regarding
 53 the use of sedimentological data in informing bottom friction parameters.

54 A description of the case study region, numerical model and data sources can be found
 55 in section 2. Section 3 presents the Bayesian inference parameter estimation method used,
 56 which is based on M2 and S2 harmonic amplitude and phase data at 15 tide gauges within
 57 the model domain. Calibration and validation results can be found in sections 4 and 5, re-
 58 spectively. In section 6, we apply the calibrated model to the estimation of tidal range energy
 59 resource. The case study is primarily motivated by tidal range energy, and hence the main
 60 focus is on model comparisons with tide gauge data. However, in section 7 we explore
 61 model performance using tidal current observations from an ADCP, as a step towards appli-
 62 cation of the calibrated model to tidal stream resource assessment. Finally, a discussion and
 63 conclusions can be found in sections 8 and 9, respectively.

64 2 Description of model and data

65 2.1 Model study region

66 The model study region consists of the Bristol Channel and Severn Estuary, situated to the
 67 south-west of the UK, as shown in Fig. 1. A macrotidal inlet offering significant tidal range
 68 energy resource [2], the Bristol Channel is also of interest for tidal stream energy [50].
 69 Accurate tidal models of the region are also relevant to flood risk studies (e.g. [31]) due to
 70 its susceptibility to storm surge [40,58]. A number of flooding events have occurred in the
 71 area in recent years, for example in the Somerset Levels [45], and future flood risk is linked
 72 to climate change [41]. The region is also to be used as a case study for a calibration and
 73 validation phase of the forthcoming SWOT mission [38].

74 The tidal dynamics in the region are dominated by the M2 and S2 constituents, whose
 75 average amplitudes within the Bristol Channel are around 3.5 m and 1.2 m, respectively.
 76 Within this work we also utilise observations of the N2 and M4 constituents, whose ampli-
 77 tudes are around 0.6 and 0.2 m, respectively.

78 2.2 The Thetis numerical model

79 Within this work we use *Thetis*, an unstructured-mesh finite element coastal ocean model
 80 [26] which utilises the *Firedrake* finite element code generation framework [42]. We employ
 81 *Thetis* in its two-dimensional configuration (as in [51]), which solves the nonlinear shallow
 82 water equations given by

$$\frac{\partial \eta}{\partial t} + \nabla \cdot (H \mathbf{u}) = 0, \quad (1a)$$

$$\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} + \mathbf{F}_C + g \nabla \eta = -\frac{\tau_b}{\rho H} + \nabla \cdot (\nu (\nabla \mathbf{u} + \nabla \mathbf{u}^T)), \quad (1b)$$

84 where η is the free surface elevation, $H = \eta + h$ is the total water depth, h is the bathymetry,
 85 \mathbf{u} is the two-dimensional depth-averaged velocity, \mathbf{F}_C is the Coriolis force, g is the acceler-
 86 ation due to gravity, ρ is the water density (which is taken as a constant), τ_b is the bottom

87 stress due to friction between the ocean and sea bed, and ν is the eddy viscosity (which we
 88 assign a constant value of $1 \text{ m}^2 \text{ s}^{-1}$). We parameterise the bottom friction τ_b via a Manning's
 89 n formulation

$$\frac{\tau_b}{\rho} = \frac{gn^2}{H^{3/2}} |\mathbf{u}| \mathbf{u}, \quad (2)$$

90 where n is the Manning coefficient (units $\text{sm}^{-1/3}$). For the purposes of model calibration
 91 within this work, n depends on the sediment type found on the ocean bed (see section 2.3).

92 Since the Bristol Channel and Severn Estuary contain significant intertidal regions, we
 93 include wetting and drying within Thetis using the scheme of [25], which we summarise
 94 here. Under this scheme, a modification is applied dynamically to the bathymetry in order
 95 to avoid negative water depth. The modified bathymetry is given by

$$\tilde{h} = h + f(H), \quad (3)$$

96 such that the modified water depth is similarly given by

$$\tilde{H} = H + f(H). \quad (4)$$

97 The implementation of this scheme simply requires this modified depth \tilde{H} to be substituted
 98 for H in the governing equations (1). The function $f(H)$ is chosen such that the modified
 99 water depth \tilde{H} is always positive. Following [25], we use

$$f(H) = \frac{1}{2} \left(\sqrt{H^2 + \alpha^2} - H \right), \quad (5)$$

100 where α is a wetting-drying parameter which controls the transition from wet to dry regions,
 101 and is user defined. In general, smaller values of α result in more accurate results, but
 102 there exists a minimum stable value which is related to the mesh element size. In all Thetis
 103 simulations presented herein, α is taken to be 1 m; this value was found through preliminary
 104 experiments (not shown) to be close to the minimum stable value for the selected mesh.

105 Mesh generation was performed using the Python package *qmesh* [5], which interfaces
 106 the mesh generator *Gmsh* [14]. The mesh, shown in Fig. 1, adopts a UTM30 coordinate
 107 projection, and uses a variable mesh element size from 250 m in the inner Bristol Chan-
 108 nel, to 8 km in open regions, resulting in a total of 42,862 triangular elements. Coastline
 109 data for mesh generation is from the Global Self-consistent, Hierarchical, High-resolution
 110 Geography Database (GSHHG) [56]. Thetis is run using a $\text{P}_1^{\text{DG}}\text{-P}_1^{\text{DG}}$ discretisation, with a
 111 Crank-Nicolson timestepping scheme with a timestep $\Delta t = 100\text{s}$. The bathymetry is from 6
 112 arcsecond resolution data available from Digimap [10], and is shown in Fig. 2.

113 Tidal dynamics are introduced through a Dirichlet boundary condition for the surface
 114 elevation η at the ocean boundary, extracted from the *TPXO* database [11]. The location
 115 of the ocean boundary of the model domain was selected to be in reasonably deep water,
 116 to minimise the influence of errors in this tidal boundary forcing data. The tidal dynamics
 117 within the Bristol Channel are dominated by the M2 and S2 constituents (with amplitudes
 118 in excess of 1 m), with some contribution from the N2, K2 and M4 constituents (amplitudes
 119 in the 10s of cm), and no other constituents above 10 cm amplitude. Due to their similar
 120 frequencies and the constraints of the Rayleigh criterion, the K2 and S2 constituents require
 121 long periods of observation/simulation to be resolved, and we therefore neglect the K2 con-
 122 stituent. The M2, S2, N2 and M4 constituents are therefore the focus of model-observation
 123 comparisons we perform within this study, and thus we use the same four constituents to
 124 force the model at its boundaries. The shallow-water M4 constituent is mostly generated
 125 within the model domain and has small amplitude on the boundaries, but is nevertheless
 126 included in the boundary forcing. Model runs span a 5-day spinup period, followed by two
 127 full spring-neap cycles (approximately one month).

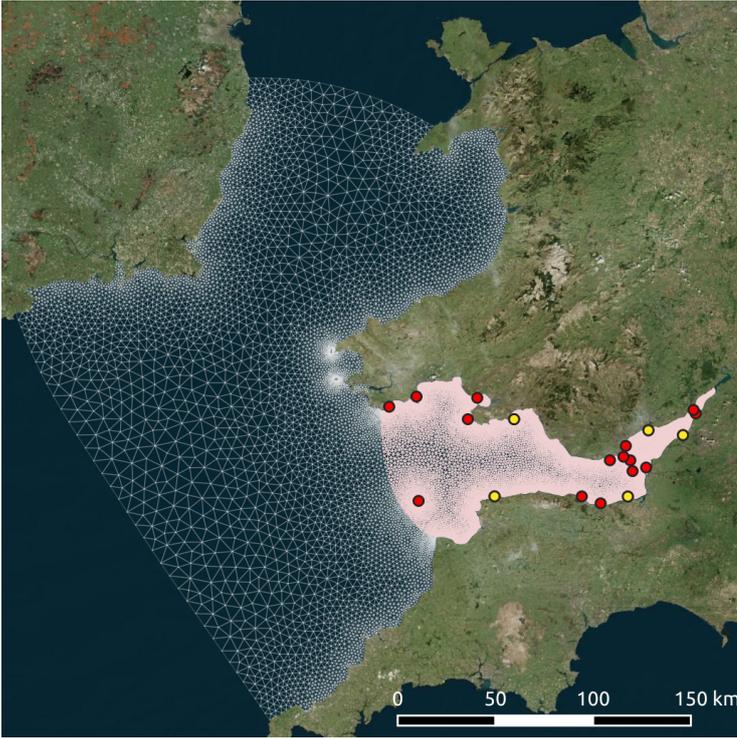


Fig. 1: Mesh used for all simulations within this paper. Red circles: locations where harmonic analysis data are available. M2 and S2 harmonic data at these locations are used within this work for model calibration, and N2 and M4 data for validation. Yellow circles: BODC tide gauge locations, where timeseries data is available. M2 and S2 data derived from these timeseries are used within this work for validation. The coloured region of the mesh indicates where a spatially variable friction coefficient is applied.

128 2.3 Parameterising the Manning coefficient

129 We employ a parameter estimation method in order to calibrate the model with respect to
 130 the spatially varying Manning coefficient, n . In order to constrain the parameter's spatial
 131 variation, we use sediment maps within the model domain. In an approach similar to [33],
 132 we use data from the British Geological Survey [7], which indicates the type of sediment
 133 found at each point in the domain. The distribution of sediment types is shown in Fig. 3, and
 134 summarised in Table 1.

135 The Manning coefficient can in principle be determined directly from the sediment type
 136 found at a given location, via a lookup table for the median sediment grain size for the
 137 corresponding sediment type. Denoting the median grain size d_{50} (in m), the corresponding
 138 theoretical Manning coefficient is given by

$$n(d_{50}) = 0.04 \sqrt[6]{2.5 d_{50}} \quad (6)$$

139 [46]. This results in the set of Manning coefficients detailed in Table 1, which are consistent
 140 with standard sediment-based values from other sources (e.g. [4]). Throughout this paper, we

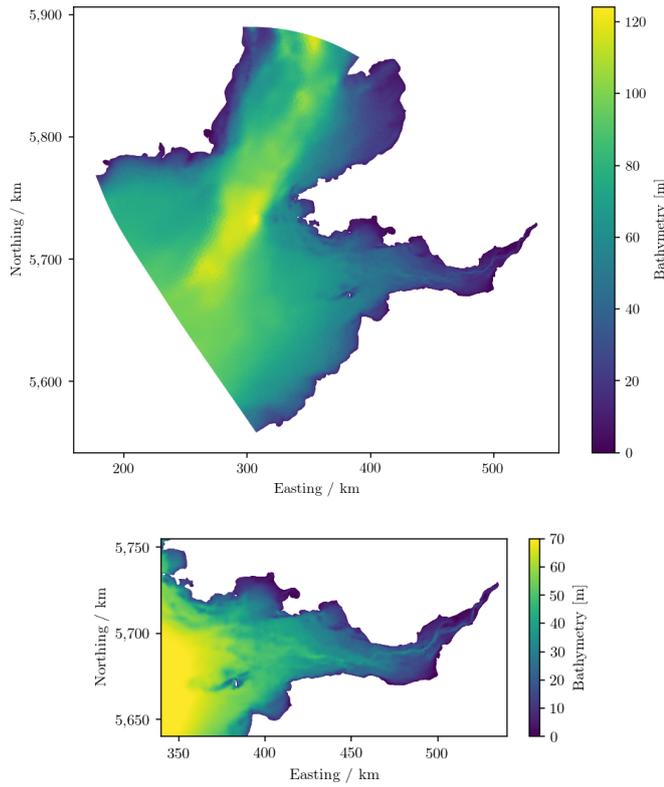


Fig. 2: Top: Bathymetry over the full model domain. Bottom: Bathymetry within the Bristol Channel and Severn Estuary. Coordinates are in the UTM30 projection.

141 refer to the set of Manning coefficients computed via Eq. (6) as the ‘standard’ or ‘theoretical’
 142 sediment-based parameters.

143 However, there is uncertainty inherent in the direct application of Manning coefficients
 144 computed as above. The bed friction term in the model governing equations must ideally ac-
 145 count for unresolved bathymetry and bedforms, which are not accounted for within equation
 146 (6). Additionally, due to numerical dissipation, it may be the case that the optimal friction
 147 coefficients within a numerical model are smaller than those corresponding to the true prop-
 148 erties of the sea bed [13]. Therefore, even when sediment data is available (as is the case
 149 here), it is common within the numerical modelling literature to perform model calibration
 150 with respect to the bottom friction coefficient. Nevertheless, the availability of sediment data
 151 can be used to constrain the spatial variation of the bottom friction parameter, in order to
 152 reduce the dimension of the parameter space for parameter estimation.

153 Within this work, we perform several parameter estimation experiments labelled A, B,
 154 C1 and C2 and described below. In each case, the Manning coefficient in the outer region of
 155 the model domain, indicated by the white region of the mesh in Fig. 1, is held constant at
 156 $n = 0.025 \text{ s m}^{-1/3}$. Since model-observation comparisons are made only within the Bristol
 157 Channel, the value for n within this outer region was found to have only a very weak influ-
 158 ence on the model performance metrics, and a value of $n = 0.025 \text{ s m}^{-1/3}$ was found through

159 preliminary experiments (not shown) to produce adequate results. The value for n inside the
160 Bristol Channel (coloured region in Fig. 1) is described below for each experiment:

161 **Experiment A: Estimation of a spatially uniform Manning coefficient.**

162 The simplest approach is to discard the sediment data entirely, and estimate only a spa-
163 tially uniform Manning coefficient (i.e. a single value), n_0 . This is a commonly taken
164 approach within the literature, especially where more advanced model calibration is not
165 directly the focus of the work.

166 **Experiment B: Estimation of a scaling factor for the standard sediment-based Manning
167 coefficients.**

168 An alternative is to scale the Manning coefficients given by Eq. (6) by a spatially uniform
169 factor γ , such that

$$n(d_{50}) = 0.04 \gamma \sqrt[6]{2.5 d_{50}}. \quad (7)$$

170 The parameter estimation problem is to determine the optimal value for γ . The moti-
171 vation for this approach is that the sediment-based Manning coefficient is likely to
172 overestimate the required bottom friction, due to the presence of numerical dissipation,
173 but that the relative values of the Manning coefficients based on the sediment data may
174 still be appropriate. This approach results in the same number of degrees of freedom
175 (one) in the parameter estimation problem as experiment A, but incorporates *a priori*
176 knowledge about the physical process of bottom friction.

177 **Experiment C: Direct estimation of a small number of Manning coefficients correspond-
178 ing to groups of sediment classes.**

179 The third approach we take within this work is to estimate three Manning coefficients
180 (n_1, n_2, n_3), each corresponding to a group of sediment types. We choose to group the
181 sediment types into approximately equal area (see Table 1), such that n_1 corresponds to
182 sediment types 1–4, n_2 to types 5–8, and n_3 to types 9–13. This grouping is shown in Fig.
183 4. While we could have used the sediment data to divide the domain into more than three
184 subdomains, this would result in large variation in subdomain area, with parameters
185 corresponding to small domain areas unlikely to be well constrained by the observations.
186 We further subdivide this experiment into two. In **experiment C1**, we use uniform priors
187 for each parameter within the Bayesian inference parameter estimation algorithm we
188 employ. In **experiment C2**, we use the standard sediment-derived Manning coefficients
189 to construct Gaussian prior distributions for each parameter.

190 Alongside the results of each of the above parameter estimation experiments, we also
191 present results based on a uniform Manning coefficient of $0.025 \text{ s m}^{-1/3}$ throughout the
192 model domain. This value is somewhat arbitrary, but falls within the commonly used range
193 of uniform Manning coefficients within the literature. Results using this uniform BFC rep-
194 resent a useful benchmark against which to compare the performance resulting from each of
195 the above parameter estimation experiments.

196 2.4 Observation data

197 We use data from two sources for the purposes of model calibration and validation, as indi-
198 cated in Fig. 1:

- 199 (i) 15 locations at which tidal harmonic data is available (National Oceanography Cen-
200 tre, personal communication 2018), which are shown as red circles in Fig. 1. We use

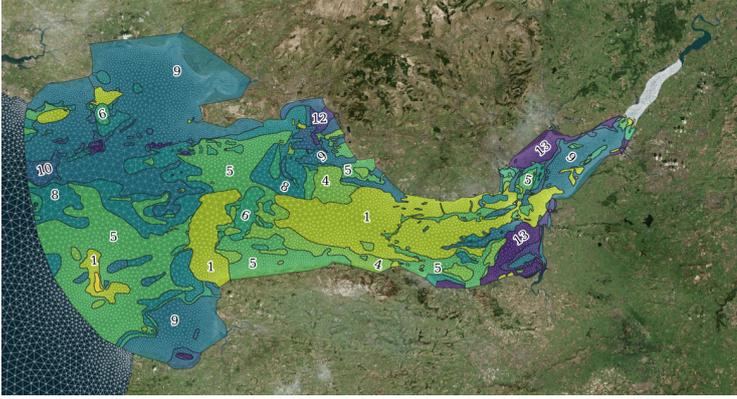


Fig. 3: Spatial distribution of sediment types within the Bristol Channel, from the British Geological Survey [7]. See also Table 1.

Table 1: Sediment types defined by the British Geological Survey [7], sorted by roughness length. Theoretical values for the Manning coefficient n are calculated from Eq. (6). See Fig. 3 for the spatial distribution of the sediment types. Based on [33].

Sediment ID	Sediment name	Area of Bristol Channel [km ²]	Theoretical n [s m ^{-1/3}]
1	Bedrock	1090	0.049
2	Boulder	0	0.041
3	Cobble	0	0.033
4	Very coarse gravel	334	0.0275
5	Coarse gravel	1465	0.0245
6	Medium gravel	227	0.022
7	Fine gravel	34	0.020
8	Very coarse sand	831	0.018
9	Coarse sand	1775	0.016
10	Medium sand	192	0.014
11	Fine sand	1	0.0125
12	Very fine sand	87	0.011
13	Silt, clay, mud	190	0.0095

201 the M2 and S2 harmonic amplitudes and phases at these locations for the model cal-
 202 ibration. N2 and M4 data at these locations are used for model validation. The tidal
 203 harmonics at each observation location were computed from tide gauge records be-
 204 tween one month and one year in length, between 1960 and 1980.

205 (ii) Five tide gauges where quality controlled timeseries surface elevation data are avail-
 206 able from the British Oceanographic Data Centre (BODC). These locations are shown
 207 in Fig. 1 by yellow circles. The tidal constituent data we use at these locations is from
 208 a harmonic analysis of observations spanning a 10 year period from 1997. We use M2
 209 and S2 amplitude and phase observations at these locations for further validation of
 210 the calibrated models.

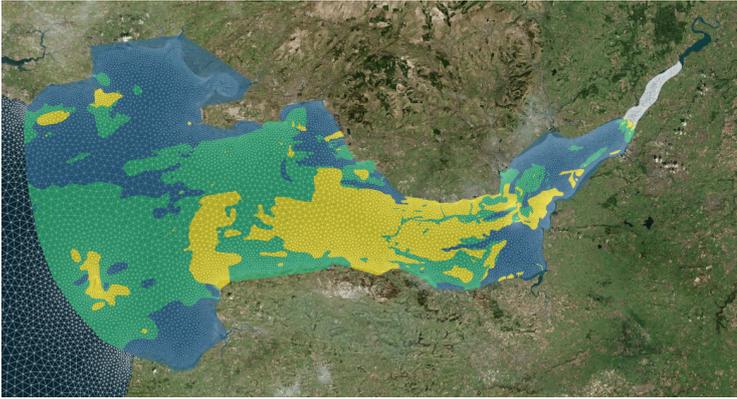


Fig. 4: Grouping of sediment classes for the purposes of parameter estimation experiments C1 and C2. Yellow corresponds to parameter n_1 , green n_2 and blue n_3 . In any regions where sediment data is unavailable, the default Manning coefficient of $n = 0.025 \text{ s m}^{-1/3}$ is applied.

211 3 Parameter estimation method

212 There exist a large number of algorithms within the literature for estimating unknown bottom
 213 friction parameters. In the simple one-dimensional case (i.e. using a spatially uniform BFC),
 214 it is common to employ a simple grid search. This involves simply running the numerical
 215 model with a small number of different BFC values, and selecting the value which min-
 216 imises a given measure of model-observation misfit. However, this approach scales poorly
 217 with the number of parameters to be estimated. The high-complexity approach (estimating
 218 an independent BFC value at every mesh node) typically requires numerical adjoint models,
 219 which constitute an efficient technique for evaluating gradients of model outputs (typically a
 220 functional representing the model-observation misfit) with respect to the control parameters,
 221 thus facilitating the use of gradient-based optimisation methods for performing model cali-
 222 bration [35]. The use of intermediate-complexity BFC parameterisations is compatible with
 223 a number of approaches, with adjoint [60] or other gradient-based methods [47], Kalman fil-
 224 ters [36, 43] and Markov Chain Monte Carlo (MCMC) methods [18, 48] all employed within
 225 the literature.

226 Within this work, we take a Bayesian inference approach via an MCMC algorithm. We
 227 utilise a Gaussian process emulator as an efficient surrogate for the full numerical model.
 228 This is necessary because the MCMC algorithm requires large numbers of model runs (typ-
 229 ically $\mathcal{O}(10^6)$), which is not feasible with the full numerical model. While our numerical
 230 model does have an adjoint model available, the size of the parameter estimation problems
 231 we solve within this work are relatively small and do not warrant adjoint methods. Kalman
 232 filter approaches typically require some tuning of algorithm parameters for optimal perfor-
 233 mance [43]. The MCMC approach however is fairly straightforward and well suited to the
 234 size of the problem considered here. Its results are simple to interpret, and also yield a direct
 235 estimate of the uncertainty in the estimated parameters.

236 The following exposition of the Bayesian inference algorithm proceeds for parameter
 237 estimation experiment C, since this is the most general case (estimating the greatest number

of parameters). The application of the method to experiments A and B requires only minor adaptation.

3.1 Bayesian inference

Within this work, the observation data we use for calibration consists of M2 and S2 harmonic amplitudes and phases at 15 tide gauge locations (as indicated by the red circles in Fig. 1).

We denote these four observations types by $j = 1, 2, 3, 4$, corresponding to M2 amplitude, S2 amplitude, M2 phase and S2 phase, respectively. The observation data is thus represented by four vectors \mathbf{y}_j , each of length $N = 15$. For compactness, we denote the full set of observations Y , a matrix with shape $(4 \times N)$, whose rows are given by the vectors \mathbf{y}_j . The corresponding model outputs for observation type j are denoted $\mathbf{f}_j(\mathbf{n})$. Bayes' theorem gives

$$\Pi(\mathbf{n}|Y) \propto L(Y|\mathbf{n}) \prod_{i=1}^3 q_i(n_i), \quad (8)$$

where Π is the posterior distribution of the parameters $\mathbf{n} = (n_1, n_2, n_3)$ given the observed data Y , L is the likelihood of observing the outputs Y given the parameters \mathbf{n} , and q_i is the prior distribution for each of the parameters n_i .

The likelihood L is estimated from the numerical model. For observation type j , we assume that the model-observation discrepancies, which are the components of the vector $\mathbf{y}_j - \mathbf{f}_j(\mathbf{n})$, are independent and identically distributed variables with zero mean and variance σ_j^2 . The likelihood $L(Y|\mathbf{n})$ is then given by

$$L(Y|\mathbf{n}) = \prod_{j=1}^4 \left[(2\pi\sigma_j^2)^{-N/2} \exp\left(-\frac{1}{2} \frac{|\mathbf{y}_j - \mathbf{f}_j(\mathbf{n})|^2}{\sigma_j^2}\right) \right]. \quad (9)$$

Since the σ_j^2 values are unknown *a priori*, they are treated as hyperparameters, i.e. they are included as additional parameters to be inferred by the inversion algorithm. We denote the full vector of unknowns $\theta = (n_1, n_2, n_3, \log \sigma_1^2, \log \sigma_2^2, \log \sigma_3^2, \log \sigma_4^2)$, and the full posterior distribution is therefore given by

$$\Pi(\theta|Y) \propto \prod_{j=1}^4 \left[(2\pi\sigma_j^2)^{-N/2} \exp\left(-\frac{1}{2} \frac{|\mathbf{y}_j - \mathbf{f}_j(\mathbf{n})|^2}{\sigma_j^2}\right) \right] \prod_{i=1}^3 q_i(n_i) \prod_{j=1}^4 q_j(\log \sigma_j^2), \quad (10)$$

where $q_j(\log \sigma_j^2)$ is the prior distribution of $\log \sigma_j^2$.

3.1.1 Priors

For parameter estimation experiments A, B and C1, we use uniform priors for the corresponding control parameters. This is equivalent to setting $q_i(n_i) = 1$ in Eq. (10) (the normalisation is not important). For parameter estimation experiment C2, we use the 'standard' sediment-based Manning coefficients of Table 1 to construct Gaussian priors for each of the Manning coefficients. That is, the priors are given by

$$q_i(n_i) = \frac{1}{s_i\sqrt{2\pi}} \exp\left(-\frac{1}{2} \frac{(n_i - \mu_i)^2}{s_i^2}\right), \quad (11)$$

Table 2: Mean (μ) and standard deviation (s) for the Manning coefficient priors in experiment C2.

Manning coefficient	$\mu_i / \text{sm}^{-1/3}$	$s_i / \text{sm}^{-1/3}$
n_1	0.0395	0.0135
n_2	0.0215	0.0045
n_3	0.013	0.004

267 where μ_i and s_i are the mean and standard deviation of the prior distributions, whose values
 268 are summarised in Table 2.

269 For the unknown variances σ_j^2 , the only prior constraint is that they must be positive.
 270 For all parameter estimation experiments within this study, we follow the approach of [48]
 271 and assume Jeffreys priors [44], such that

$$q_j(\log \sigma_j^2) = \frac{1}{\sigma_j^2}. \quad (12)$$

272 3.2 Markov Chain Monte Carlo algorithm

273 A technique for sampling the posterior distribution given by Eq. (10) is the Markov Chain
 274 Monte Carlo (MCMC) method, which has the advantage that the constant of proportionality
 275 in the equation need not be determined. We use an implementation of the Random Walk
 276 Metropolis Hastings MCMC algorithm [21], which is given by Algorithm 1. The algorithm
 277 requires the selection of an appropriate proposal distribution covariance matrix, Σ_{step} , gov-
 278 erning the size of the random steps within the parameter space. We set

$$\Sigma_{\text{step}} = \text{diag}(0.001^2, 0.001^2, 0.001^2, 0.1^2, 0.1^2, 0.1^2, 0.1^2) \quad (13)$$

279 so that the random steps in each of the Manning coefficients have zero mean and a standard
 280 deviation of $0.001 \text{ sm}^{-1/3}$, and the random steps in each value of $\log \sigma_j^2$ have zero mean and
 281 a standard deviation of 0.1. These step sizes were found to give satisfactory results, without
 282 the need for an adaptive MCMC algorithm.

283 In the results presented here, we take $M = 10^6$ samples, discarding the first 2×10^5 as
 284 a burn-in period, and the resulting chain of values $n^{[k]}$ generated by the MCMC algorithm
 285 constitute samples from the posterior distribution. The mean of these samples is taken as the
 286 best estimate of the parameter values.

Algorithm 1: Random Walk Metropolis Hastings algorithm

Initial guess for parameters $\theta = \theta^{[0]}$;

for $k = 1 : M$ **do**

1. Draw proposed set of parameters θ^* from multivariate normal proposal distribution:

$$\theta^* \sim \mathcal{N}(\theta^{[k-1]}, \Sigma_{\text{step}})$$

2. Compute posterior $\Pi(\theta^* | \{\mathbf{y}_j\})$ using Eq. (10)

3. Calculate $p_{\text{accept}} = \min\left(1, \frac{\Pi(\theta^* | \{\mathbf{y}_j\})}{\Pi(\theta^{[k-1]} | \{\mathbf{y}_j\})}\right)$

4. Generate $u \sim U(0, 1)$ and set $\theta^{[k]} = \theta^*$ if $p_{\text{accept}} > u$. Otherwise, set $\theta^{[k]} = \theta^{[k-1]}$.

end

287 3.3 Gaussian process emulation

288 We employ a Gaussian process emulator (GPE) as a computationally inexpensive surrogate
 289 for the full numerical model. For parameter estimation experiment C, this GPE is trained
 290 using 40 model runs with Manning coefficient samples drawn from uniform prior distri-
 291 butions in the range $[0.01, 0.05]$, using Latin Hypercube Sampling to evenly sample the
 292 three-dimensional parameter space. Experiment A is a simplified version of experiment C,
 293 and can therefore utilise the same GPE. For experiment B, where the objective is to esti-
 294 mate the scaling parameter γ (see Eq. (7)), the GPE is trained using 10 samples for γ drawn
 295 uniformly between 0.55 and 1.0, inclusive. Values for γ smaller than 0.55 resulted in model
 296 instabilities due to the very low friction coefficients in some regions. Once trained, the GPE
 297 is substituted for $\mathbf{f}(\mathbf{n})$ within the MCMC algorithm described above. Within this study, we
 298 use the Python package GPy [15] for the construction of GPEs.

299 The use of a GPE in place of the full Thetis model introduces additional uncertainty.
 300 However, this uncertainty can be directly estimated by the GPE. The GPE-introduced co-
 301 variances were typically around 10^{-6} m^2 for emulated amplitudes, and $2 \times 10^{-3 \circ 2}$ for em-
 302 ulated phases. Since the model-observation variances (σ_j^2 in the above description of the
 303 Bayesian inference) were typically around 25 cm^2 for amplitudes, and $6.25^{\circ 2}$ for phases,
 304 the additional uncertainty introduced by the GPEs is small, and can be neglected.

305 4 Calibration results

306 4.1 Optimal parameters

307 The optimal Manning coefficient fields for each parameter estimation experiment are shown
 308 in Fig. 7. Note that in all cases, the value of the Manning coefficient outside the Bristol
 309 Channel takes a fixed value of $n = 0.025 \text{ sm}^{-1/3}$, as described in section 2.3. We make
 310 further comments on the results from each experiment below.

311 Experiment A: **uniform parameter inside Bristol Channel**

312 The optimal uniform parameter within the Channel (and its uncertainty) is given by $n_0 =$
 313 0.0274 ± 0.0003 . This value lies within the range of commonly used uniform parameter
 314 values in the literature.

315 Experiment B: **scaling of ‘standard’ sediment-based parameters**

316 The MCMC algorithm returns a scaling parameter $\gamma = 0.813 \pm 0.013$. This is consis-
 317 tent with the expectation that the ‘standard’ sediment-based parameters are too strongly
 318 dissipative, due to the presence of numerical dissipation.

319 Experiment C1: **three-dimensional parameter space, uniform priors**

320 The values for each Manning coefficient returned by the MCMC algorithm are $n_1 =$
 321 0.032 ± 0.002 , $n_2 = 0.021 \pm 0.007$, $n_3 = 0.025 \pm 0.003$. The marginal posterior distri-
 322 butions for each parameter are shown in Fig. 5. Each marginal distribution is obtained
 323 by integrating the full posterior distribution over two of the parameters, leaving the
 324 marginal PDF for each parameter individually. The relative magnitudes of the Manning
 325 coefficients returned by this experiment are unexpected; given the sediment types corre-
 326 sponding to each parameter, we would expect $n_1 > n_2 > n_3$. We note that the posterior
 327 distribution for n_2 is very broad. The parameter estimation results are therefore not nec-
 328 essarily inconsistent with this expectation, but the means of the distributions do not fall
 329 in the expected order.

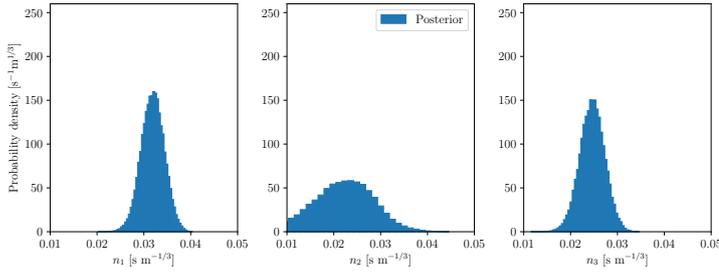


Fig. 5: Marginal posterior distributions for each parameter n_i , from experiment C1.

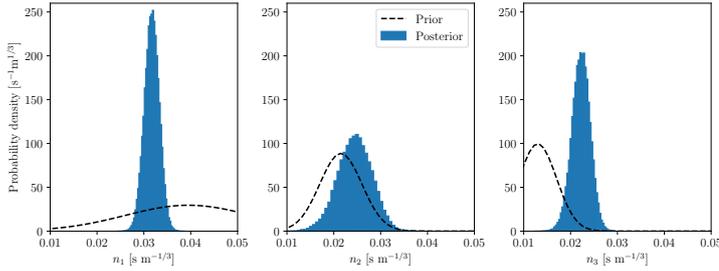


Fig. 6: Marginal posterior distributions for each parameter n_i , from experiment C2. Dotted lines indicate the prior distributions for each parameter.

330 Experiment C2: **three-dimensional parameter space, Gaussian priors**

331 The values for each Manning coefficient returned by the MCMC algorithm are $n_1 =$
 332 0.0317 ± 0.0016 , $n_2 = 0.024 \pm 0.004$, $n_3 = 0.0222 \pm 0.0019$. The marginal posterior
 333 distributions for each parameter are shown in Fig. 6, along with the prior distributions.
 334 The prior distribution for n_1 is very broad, with the observation data able to achieve a
 335 far tighter constraint. For all three parameters, the posterior distributions are narrower
 336 than for experiment C1, due to the additional constraints provided by the priors. Note
 337 also that the influence of the priors is sufficient for the parameters to fall in the expected
 338 order ($n_1 > n_2 > n_3$), in contrast to experiment C1.

339 4.2 Performance against calibration dataset

340 In this section, we summarise the performance of the model with the Manning coefficient
 341 field resulting from each parameter estimation experiment, as measured against the calibra-
 342 tion dataset (locations indicated by red circles in Fig. 1). Results presented here are based
 343 on runs of the full numerical model (not the GPE). The M2 and S2 amplitude and phase
 344 RMSEs achieved with each coefficient field are summarised in Table 3.

345 As described in section 2.3, the uniform BFC of $0.025 \text{ s m}^{-1/3}$ is used as a benchmark,
 346 with which we can compare model performance using the other BFC fields. The ‘standard’
 347 sediment-based parameters perform very poorly, with significantly greater RMSEs than the

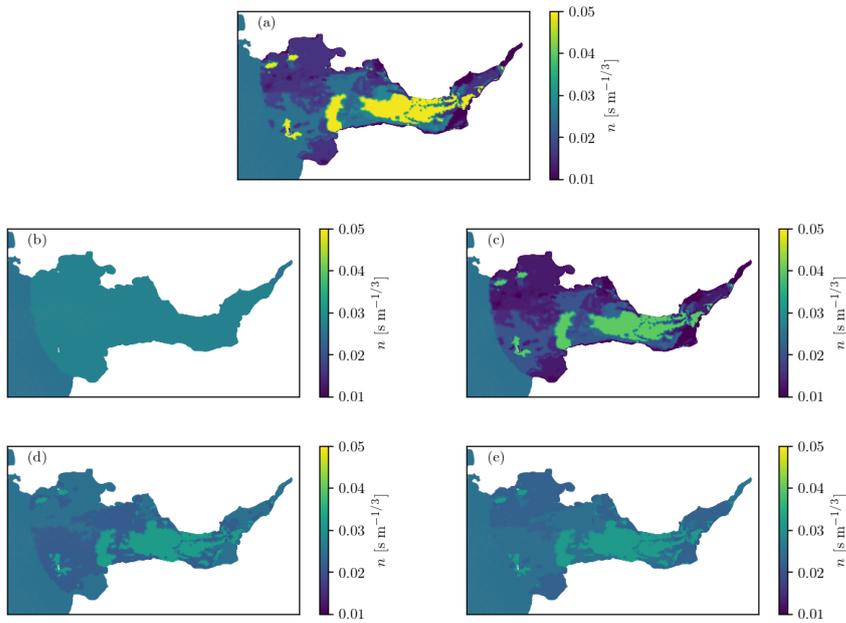


Fig. 7: Manning coefficient fields used for model validation. (a) Standard sediment-based parameters. (b) Result of experiment A. (c) Result of experiment B. (d) Result of experiment C1. (e) Result of experiment C2.

348 benchmark run. Experiment A (optimal uniform BFC) performs well, and achieves the over-
 349 all lowest amplitude and phase RMSEs for the S2 constituent, while the greatest improve-
 350 ment over the benchmark run is for the M2 amplitude. Experiment B does not perform as
 351 well as experiment A, suggesting that the direct use of sediment-derived coefficients (even
 352 when scaled) is detrimental to model performance. Experiments C1 and C2 both perform
 353 well. Experiment C1 performs best overall, since its RMSEs are all within 0.1 cm or 0.1° of
 354 the lowest achieved in all cases. This is to be expected, since experiment C1 uses the great-
 355 est number of degrees of freedom in representing the Manning coefficient, with the fewest
 356 additional constraints (whereas experiment C2 includes Gaussian priors for the unknown
 357 parameters).

358 Fig. 8 compares the modelled and observed M2 and S2 amplitudes and phases for both
 359 the ‘standard’ and experiment C1 cases. These results demonstrate the excessive dissipation
 360 due to the ‘standard’ friction coefficients, resulting in underestimated amplitudes. Figure 9
 361 indicates the spatial distribution of the M2 amplitude errors within the Bristol Channel using
 362 the ‘standard’ parameters, and shows the increasing magnitude of the model errors further
 363 into the channel, where the amplitude increases due to resonance. The result of experiment
 364 C1 exhibits significantly reduced scatter, corresponding to the reduced RMSEs summarised
 365 in Table 3.

Table 3: Root mean squared errors (RMSEs) of the modelled M2 and S2 amplitudes (α) and phases (ϕ), for each Manning coefficient field, aggregated across the calibration tide gauges (red circles in Fig. 1). Figures in bold indicate the best performance.

Manning coefficient field	RMSE			
	M2 α [cm]	M2 ϕ [°]	S2 α [cm]	S2 ϕ [°]
'Standard' sediment-based parameters	22.6	8.6	15.2	9.2
Experiment A	4.9	2.6	6.1	3.0
Experiment B	9.9	3.8	7.3	5.0
Experiment C1	3.4	2.5	6.1	3.1
Experiment C2	3.3	2.7	6.3	3.3
Uniform $n = 0.025 \text{ s m}^{-1/3}$	11.4	2.9	6.3	5.1

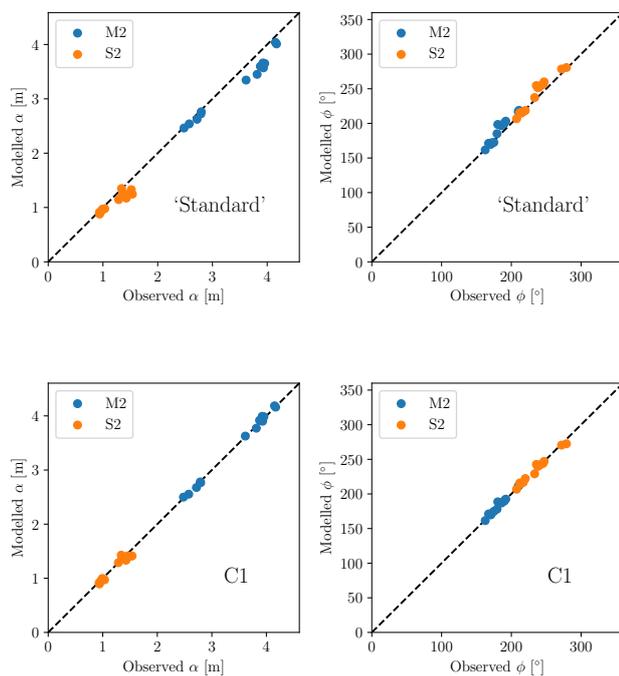


Fig. 8: Scatter plots of modelled M2 and S2 amplitude and phase, against observed values. Top: using 'standard' sediment-based parameters. Bottom: using result from experiment C1. The 'standard' parameters systematically underestimate the observed amplitudes.

366 5 Validation of calibrated models

367 Section 4.2 summarised model performance against the set of data which was used directly
 368 within the model calibration. In this section we make additional model-observation com-
 369 parisons in order to validate the calibrated models resulting from each parameter estimation
 370 experiment.

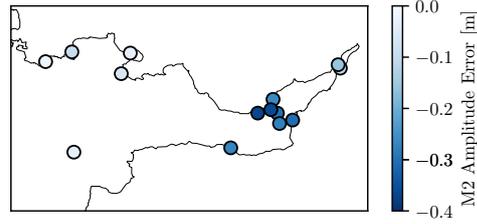


Fig. 9: Map of M2 amplitude model errors, using the ‘standard’ parameters. The errors increase in magnitude further into the channel.

371 5.1 Validation using additional harmonic constituents

372 The parameter estimation algorithm used only the M2 and S2 amplitude and phase data at
 373 the locations indicated by red circles in Fig. 1. As described in section 2.2, the N2 and M4
 374 constituents have amplitudes in the 10s of cm within the model domain. These constituents
 375 are included in the model boundary condition, and can be resolved by harmonic analysis
 376 based on the one-month model runs. We can therefore make additional comparisons between
 377 the modelled and observed amplitudes and phases for these two constituents. These RMSEs
 378 are summarised in Table 4.

379 The ‘standard’ sediment-based friction field produces the smallest N2 amplitude RMSE,
 380 in contrast with its poor performance on all other error metrics. The benchmark run (with
 381 uniform $n = 0.025 \text{ s m}^{-1/3}$) produces the smallest N2 phase errors. Experiment B produces
 382 the smallest RMSEs for the M4 amplitude, while experiment C2 produces the smallest M4
 383 phase RMSE. As was the case for the error metrics against the calibration data, experi-
 384 ments C1 and C2 produce similar RMSEs. Overall, the N2 and M4 validation metrics do
 385 not strongly favour a particular parameter estimation experiment, and the N2 amplitude in
 386 particular appears difficult to model accurately.

Table 4: Root mean squared errors of the modelled N2 and M4 amplitudes and phases, for each Manning coefficient field, aggregated across the calibration tide gauges (red circles in Fig. 1). Figures in bold indicate the best performance.

Manning coefficient field	RMSE			
	N2 α [cm]	N2 ϕ [°]	M4 α [cm]	M4 ϕ [°]
‘Standard’ sediment-based parameters	12.2	13.0	6.7	20.8
Experiment A	12.4	6.5	6.6	17.9
Experiment B	13.4	6.0	5.4	20.7
Experiment C1	12.6	6.1	5.8	17.9
Experiment C2	12.5	6.2	5.7	17.5
Uniform $n = 0.025 \text{ s m}^{-1/3}$	13.2	4.9	6.0	19.0

387 5.2 Validation using additional tide gauge locations

388 In this section we compare model outputs with data from the five BODC tide gauge locations
 389 (indicated by yellow circles in Fig. 1). Data at these locations were not used in the parameter
 390 estimation experiments.

391 The M2 and S2 amplitude and phase RMSEs aggregated across these five tide gauges are
 392 summarised in Table 5 for each BFC field. We find that experiment C1 produces the smallest
 393 values for all four RMSEs. Experiments A and C2 also perform well. Experiment B produces
 394 a relatively high M2 amplitude RMSE, but is still an improvement on the benchmark $n =$
 395 $0.025 \text{ s m}^{-1/3}$ run. Model performance for the N2 and M4 constituents at these validation
 396 tide gauges follows a similar pattern to the performance at the calibration gauges, and is
 397 therefore not shown.

Table 5: Root mean squared errors of the modelled M2 and S2 amplitudes and phases, for each Manning coefficient field, aggregated across the validation tide gauges (yellow circles in Fig. 1). Figures in bold indicate the best performance.

Manning coefficient field	RMSE			
	M2 α [cm]	M2 ϕ [°]	S2 α [cm]	S2 ϕ [°]
‘Standard’ sediment-based parameters	26.2	7.9	13.6	7.9
Experiment A	3.3	1.7	1.9	1.2
Experiment B	6.2	1.8	2.7	1.8
Experiment C1	2.6	1.4	1.7	0.7
Experiment C2	3.5	1.6	2.1	0.7
Uniform $n = 0.025 \text{ s m}^{-1/3}$	8.0	1.8	3.7	3.8

398 These results suggest that over-fitting has not been an issue in any of the parameter
 399 estimation experiments. The N2 and M4 error metrics do not strongly favour any particular
 400 BFC configuration, while the M2 and S2 error metrics at new locations show improvements
 401 which are consistent with the corresponding error metrics against the calibration data.

402 Due to the similarity in the results of experiments C1 and C2, throughout the remainder
 403 of this paper we limit our analysis to the ‘standard’ sediment-based parameters, and the
 404 results from parameter estimation experiments A, B and C1.

405 6 Implications for tidal range energy

406 In this section, we consider the mean modelled tidal range energy, and its sensitivity to the
 407 bottom friction parameterisation. At a given location, the mean tidal range energy density
 408 (or potential energy density, PED) is computed as

$$\text{PED} = \frac{1}{M} \sum_{i=1}^M \frac{1}{2} \rho g (HW_i - LW_i)^2, \quad (14)$$

409 where the sum is over $M = 28$ semidiurnal tidal periods spanning a single complete spring-
 410 neap cycle, ρ is the density of water, and HW_i and LW_i are the high and low water surface
 411 elevations from each semidiurnal cycle i , respectively. The result has units of J m^{-2} per tidal
 412 cycle.

413 We compute the mean tidal range energy density at each of the tide gauge locations
 414 shown in Fig. 1, using both the model (with various friction parameters) and observations.
 415 This energy density is computed from surface elevation timeseries reconstructed from the
 416 M2 and S2 harmonic constituents, since these constituents dominate the tidal dynamics
 417 in the region and are well captured by the model. A comparison between these modelled
 418 and observed values is presented in Fig. 10. The ‘standard’ sediment parameters result in
 419 a severe underestimate of the tidal range energy density, while the other parameter sets all
 420 perform reasonably well. As shown in Table 6, experiment C1 produces the smallest tidal
 421 range energy density RMSE; this is to be expected, since it also performs best in terms of
 422 M2 and S2 amplitude and phase RMSEs.

423 Fig. 11 shows the modelled mean tidal range energy density, computed over the entire
 424 Bristol Channel, using the BFC field from experiment C1. Fig. 12 shows the difference
 425 between the modelled mean tidal range energy density for each other BFC field, and the
 426 result from BFC field C1 (we use the model result from experiment C1 as a central value for
 427 these different plots since it has the lowest RMSE with respect to the available observations).
 428 The results are consistent with those of Fig. 10, and the spatial patterns can be explained by
 429 the BFC distributions shown in Fig. 7. Fig. 12(a) again demonstrates the under-estimation
 430 of the available tidal range energy when using the ‘standard’ sediment-based parameters.
 431 Fig. 12(b) shows that the uniform parameter tends to overestimate the tidal range energy
 432 density compared with parameters C1, particularly in the central part of the channel. This
 433 central region largely coincides with the presence of bedrock, i.e. where the BFC within
 434 experiment A is smaller than within C1, leading to the observed difference. This pattern
 435 is largely reversed in Fig. 12(c), corresponding to the difference between experiments B
 436 and C1; experiment B produces larger values for the BFC in the central rocky region than
 437 experiment C1, and therefore produces smaller modelled sea surface elevations. Towards
 438 the east end of the model domain (further upstream), the relative values of the BFCs are
 439 reversed, leading to a change in sign in the tidal range energy difference plots. Overall,
 440 these results reveal that the BFC has a somewhat localised effect on the modelled tidal
 441 range energy density, although the long tidal wavelength means that the differences in tidal
 442 range energy are much smoother than the differences between the BFC fields themselves
 443 (which are piecewise-constant and discontinuous).

Table 6: Root mean squared errors (RMSEs) of the modelled mean tidal range energy densities, compared with observations at the tide gauge locations.

Manning coefficient field	RMSE / kJ m^{-2}
‘Standard’ parameters	44.3
Experiment A	10.4
Experiment B	16.5
Experiment C1	8.8

444 7 Modelling tidal currents

445 In this section we perform further model validation using available tidal current observa-
 446 tions, and discuss the application of the calibrated model to tidal stream resource assessment.
 447 Freely available ADCP data is relatively scarce within the study region, but here we make
 448 comparisons with ADCP data collected at Minehead (shown as a purple diamond in Fig.

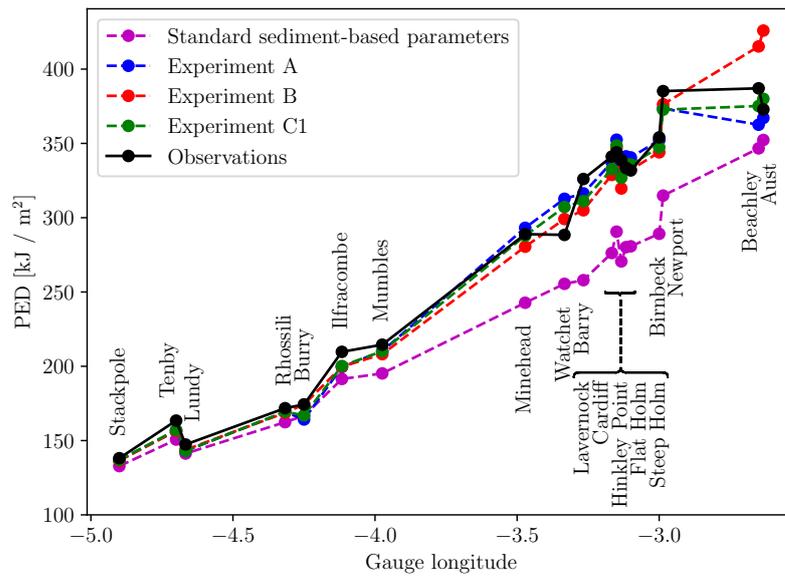


Fig. 10: Comparison of modelled and observed mean tidal range energy density over a spring-neap cycle. The names of each tide gauge location are indicated.

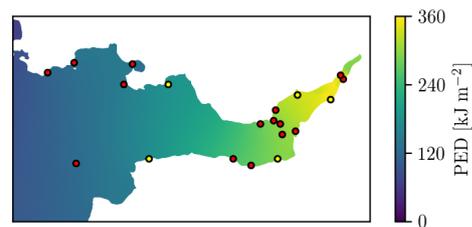


Fig. 11: Mean tidal range energy density per tidal cycle, computed over the entire Bristol Channel, using friction field C1 (spatially varying calibrated parameter). This field results in the smallest RMSEs vs observed tidal range energy density, and is therefore the best estimate of the tidal range energy resource across the Bristol Channel.

449 14), on 30th July and 1st August 2001 [49,29]. The ADCP measured velocity at 6 depths,
450 and has been depth-averaged for numerical model comparisons.

451 Fig. 13 compares modelled and observed current speeds at the ADCP deployment loca-
452 tion, for the four model BFC configurations. In all cases, the model overestimates the current
453 speeds. One surprising result is that the ‘standard’ sediment parameters, which previous re-
454 sults suggest overestimate the bottom friction, produce the greatest modelled velocity mag-
455 nitudes at the ADCP location. This can be explained by inspecting the friction coefficient
456 distributions of Fig. 7. The sediment types within the region are shown in Fig. 14, with the
457 ADCP location indicated. The large region of high friction coefficient in the centre of the

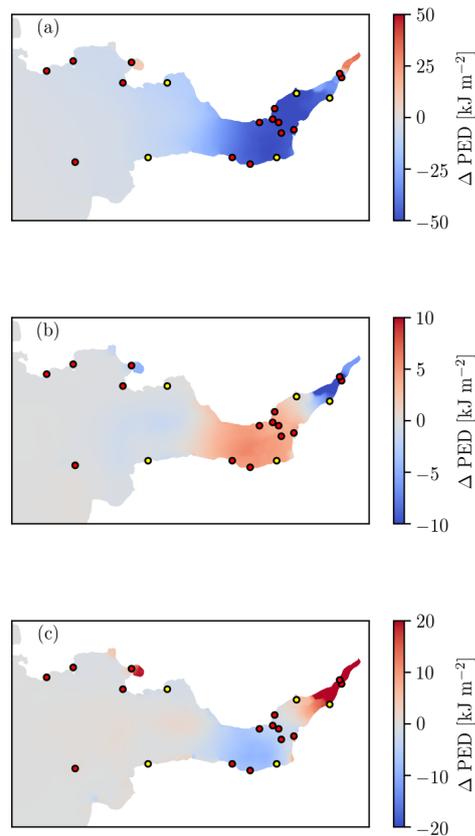


Fig. 12: Difference between modelled tidal range energy density (a) with ‘standard’ parameters and parameters from experiment C1; (b) with parameters from experiments A and C1; (c) with parameters from experiments B and C1. Note the different colorbar ranges in each figure. We again observe that the ‘standard’ sediment-based parameters underestimate the energy density compared with the calibrated parameters, by an increasing amount further into the Channel. In contrast, the uniform coefficient produces higher energy densities in the central bedrock region of the channel, since it does not impose higher friction here.

458 channel (corresponding to bedrock, sediment ID 1) acts to block the flow, driving higher
 459 currents along the southern edge of the model domain, where the sediments are finer and
 460 the BFC therefore smaller. This blockage effect depends on the relative friction coefficients
 461 between the bedrock region and the southern lower-friction area. Since the ADCP is situ-
 462 ated within this lower friction region, the modelled velocities here are amplified by higher
 463 values for the bedrock friction coefficient. This explains why both the ‘standard’ sediment-
 464 based friction parameters, and the result of experiment B, produce the highest velocities at
 465 the ADCP location. For the parameters resulting from experiment C1, the BFC values are
 466 less extreme, and the blockage effect is therefore somewhat reduced. The parameters from
 467 experiment A, corresponding to a uniform BFC within the Bristol Channel, result in the best

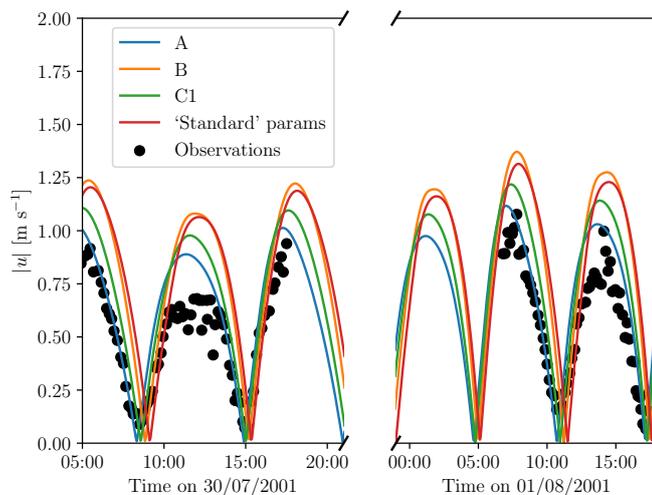


Fig. 13: Comparison between models with various friction parameters, and depth-averaged current speed data at Minehead ADCP, from [29].

468 performance at the ADCP location, because the uniform BFC removes the blockage effect
 469 altogether.

470 This is further demonstrated by Figs. 15 and 16. Fig. 15 shows the mean modelled ki-
 471 netic power density (KPD) across the model domain, using the C1 parameters, and exhibits
 472 small-scale variability in the tidal stream resource, due mostly to bathymetric and coastline
 473 features. Similar to Fig. 12 for mean tidal range energy, Fig. 16 shows the differences be-
 474 tween the modelled mean tidal stream power density for each BFC field, compared with the
 475 result from BFC field C1. There is high spatial correlation between these differences and the
 476 differences in the BFC fields (see Fig. 7), revealing a strongly localised effect of the BFC
 477 on the modelled tidal stream resource. In particular, Fig. 16b shows the difference in mod-
 478 elled mean tidal stream power density between parameters A (uniform BFC) and C1, and
 479 demonstrates the blockage effect described above, with the uniform BFC producing lower
 480 velocities in regions of finer sediment at the southern edge of the model domain.

481 Overall, the results of this section demonstrate the increased complexity of tidal currents
 482 compared with tidal elevations, with both the bathymetry and BFC having a strong localised
 483 effect on model velocities. We therefore conclude that calibration for tidal stream resource
 484 assessment requires further work. Tidal current observations spanning a broader spatial re-
 485 gion are essential, and since currents are typically influenced by localised features that may
 486 well be underestimated in the interpolation of the bathymetry data to the unstructured mesh,
 487 the use of higher resolution in both the model mesh and the bathymetry may be required.

488 8 Discussion

489 This study has compared various uses of sedimentological data within BFC parameter esti-
 490 mation, using the Bristol Channel and Severn Estuary as a case study region. We have

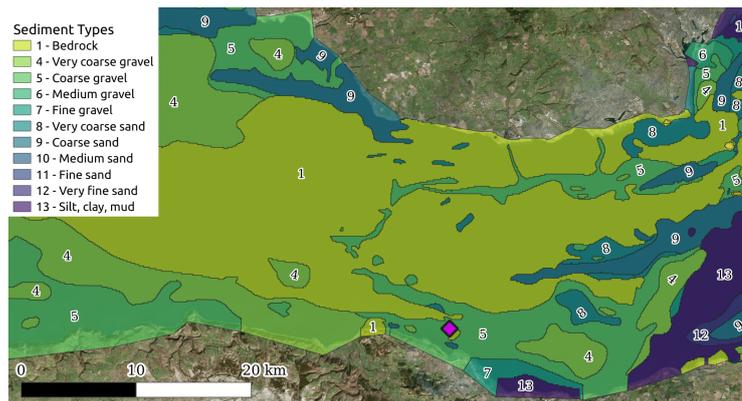


Fig. 14: Sediment zones, zoomed in to the central part of the channel. The purple diamond indicates the ADCP location, which lies within a region of relatively fine sediment.

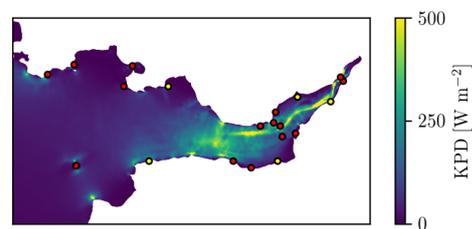


Fig. 15: Mean tidal stream power density, computed over the entire Bristol Channel, using friction parameters from experiment C1.

491 performed a number of parameter estimation experiments, utilising the sedimentological
 492 data in different ways. These calibration experiments can be considered to be zero-, one-
 493 and three-dimensional parameter estimation problems.

494 The use of ‘standard’ sediment-derived BFC parameters can be considered zero-dimensional,
 495 since this approach does not involve the use of any tide gauge data to infer any model pa-
 496 rameters. Instead, theoretical values for the BFC were applied directly to the numerical
 497 model, based on the median grain size of the sediment found at each point within the model
 498 domain. This resulted in excessive friction parameters, leading to underestimation of tidal
 499 amplitudes. This is consistent with the presence of numerical diffusion within the model in
 500 addition to the bottom friction term within the governing equations; the optimal model BFCs
 501 are smaller than would be expected from the physics of the bottom friction effect [13].

502 Parameter estimation experiments A and B are both one-dimensional problems, but they
 503 take differing approaches. In experiment A, a spatially uniform BFC was inferred, whereas
 504 in experiment B we took the sediment-derived BFC as a starting point, scaling the BFC by a
 505 uniform factor which was determined via the parameter estimation algorithm. Between these
 506 experiments, the uniform BFC (experiment A) produced better model performance, as mea-
 507 sured against both the calibration and validation tide gauge data, than experiment B. This
 508 implies that scaling by a constant factor is not sufficient to compensate for the shortcom-

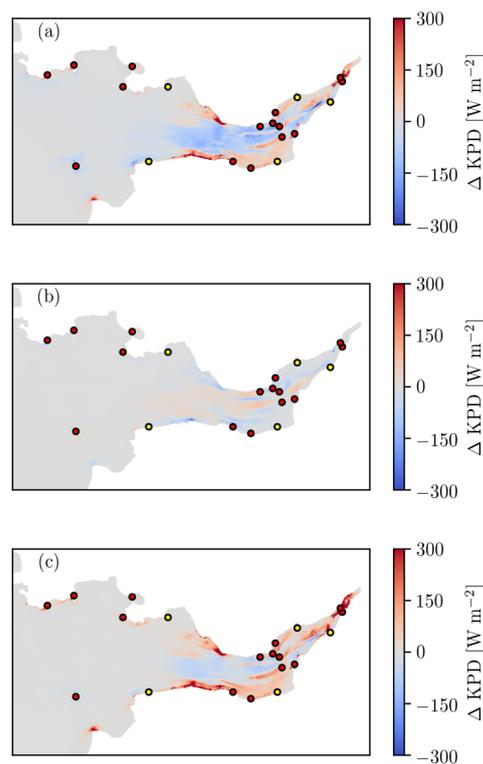


Fig. 16: (a) Difference in modelled mean tidal stream power density between ‘standard’ parameters and parameters C1. (b) Difference for parameters A and C1. (c): Difference for parameters B and C1. Similarly to the tidal range energy density, the tidal stream power density is mostly underestimated by the ‘standard’ sediment-based parameters compared with the calibrated parameters, with a particularly strong local effect in the region of bedrock in the channel centre. However, due to the blockage effect of increased friction in the centre of the channel, the kinetic energy increases at the southern edge, where the friction coefficient is smaller.

509 ings of the theoretical sediment-derived parameters, and therefore in modelling applications
 510 where there is insufficient data for estimating more than one parameter, or such calibration is
 511 considered unnecessary, the commonly-taken approach of a uniform BFC is most suitable.
 512 There may exist some function of the theoretical sediment-derived BFC (more complex than
 513 simple scaling as performed here) which can produce better model performance than a uni-
 514 form BFC, but this would amount to the estimation of more than one parameter. The model
 515 performance with the optimal uniform BFC meets the recommended accuracy criteria of
 516 [59], and we therefore conclude that the estimation of a spatially uniform BFC is sufficient
 517 for many practical purposes. This may particularly be the case when using a calibration al-
 518 gorithm whose computational cost increases with the number of parameters to be estimated
 519 (such as the algorithm we use in this study), and given that reducing model errors under
 520 one metric may be liable to increase errors under another metric (such as is observed in this

521 study, where the spatially varying BFCs, calibrated using tidal elevation data alone, perform
522 worse in terms of tidal currents).

523 In experiments C1 and C2, the sedimentological data was used to divide the Channel
524 into three subdomains, corresponding to groups of sediment types, and a Bayesian inference
525 algorithm employed to estimate the optimal BFC corresponding to each sediment group.
526 Experiments C1 and C2 differed in their choice of prior within the Bayesian inference; ex-
527 periment C1 used a uniform prior, whereas experiment C2 used Gaussian priors based on the
528 theoretical sediment-derived BFC values. Due to the increased dimension of the parameter
529 space for experiments C, their performance against both the calibration and validation tide
530 gauge data was better than experiments A and B. Overall, experiment C1 produced slightly
531 better performance than experiment C2; this is further evidence that the theoretical BFC
532 values derived from the sediment data are spurious in the context of numerical model BFCs,
533 which may be due to the presence of other modelling errors. Nevertheless, the sediment
534 data provides a physically motivated decomposition of the model domain for constraining
535 the spatial variation of the friction parameter, for applications where there is sufficient ob-
536 servation data to calibrate the model with more than one degree of freedom.

537 This study did not investigate the use of BFC parameterisations with more than three de-
538 grees of freedom. Doing so could result in greater model performance, but could encounter
539 overfitting issues, and is ultimately limited by the available observation data. Furthermore,
540 since calibration implicitly compensates for a broad variety of modelling errors, calibration
541 with respect to a greater number of degrees of freedom will arguably become increasingly
542 disconnected from the underlying physics of the bottom friction effect, thus making the sed-
543 imentological data less useful in constraining the spatial variation of the BFC. The results
544 of this study suggest that, for small-dimensional parameter estimation problems, the use of
545 sediment data for subdividing the model domain constitutes a practical approach.

546 However, we acknowledge that even for the low-dimensional parameter spaces we con-
547 sidered here, the calibration problem will be affected by the presence of a variety of sources
548 of error [16,52]. These sources include assumptions made within the governing equations
549 (e.g. the choice between two- and three-dimensional models, barotropic vs baroclinic mod-
550 els, etc), discretisation errors, mesh resolution [20], unresolved bathymetry (e.g. sandbars
551 [27]), other imperfect model inputs, and other unresolved or parameterised processes. How-
552 ever, reductions in each of these uncertainties typically incur additional computational cost,
553 and/or require a greater volume of observation/survey data. The modelling approach and
554 assumptions we have taken in this work are typical of many tidal range energy studies (in-
555 cluding several utilising the same Thetis numerical model [3, 19, 32, 6]), and we have sought
556 to make the most of the available data. This study has also neglected temporal dependence
557 of the BFC, e.g. within the spring-neap cycle, and has assumed calm conditions with no
558 wind or atmospheric pressure forcing, or the propagation of storm surges from outside the
559 model domain. On longer time scales, differences in the timing of observations may also
560 be significant. For example, the sedimentological data used within this study was collected
561 between 1977 and 1993, with the tide gauge observations also spanning multiple decades,
562 whereas the bathymetry is likely to change on time scales of years to decades due to both
563 anthropogenic and natural causes. Any calibrated BFC field is always specific to the model
564 configuration with which it was derived, and model calibration should always be interpreted
565 within the context of these other sources of model error. However, the use of spatially-
566 dependent BFC is common within the literature (including within this model domain [33]).
567 This study has attempted to make the most of limited data, demonstrating that sedimento-
568 logical data can be an effective basis for constraining spatially varying BFCs.

569 Within this work, we utilised M2 and S2 harmonic constituent data for model calibra-
570 tion. We acknowledge that the model-observation errors for these constituents are already
571 small prior to calibration with a spatially varying BFC, given the broader context of the other
572 modelling errors discussed above. However, this work has demonstrated that small changes
573 in the BFC can correspond to changes in the tidal resonance, which is critical for the tidal
574 dynamics and hence the tidal renewable energy resource. N2 and M4 data were withheld
575 from the calibration, for the purposes of model validation. It is likely that incorporating all
576 available data within the parameter estimation process would be beneficial, and may facil-
577 itate the estimation of a greater number of unknown parameters. We also note that the use
578 of N2 data for validation was inconclusive in terms of differentiating model performance
579 with each BFC field. Since the calibrated BFC fields will in part be compensating for im-
580 perfect model boundary conditions, the failure of M2- and S2-based calibration to improve
581 the modelled N2 constituent may suggest the presence of errors in the boundary condition.
582 It is certainly likely that calibration with respect to the boundary condition could produce
583 additional improvements in model performance, but further investigation of this aspect is
584 left to future work.

585 The results of section 6 reveal a somewhat localised effect of the BFC on the tidal range
586 energy resource. This highlights the need for observations in regions of interest, although
587 this is mitigated by the relatively smooth variation of tidal sea surface elevations. However,
588 in an application to modelling tidal stream resource, the highly spatially variable nature of
589 currents, which are affected by local coastline and bathymetry features, exacerbates this
590 issue. Reliable tidal stream resource assessment therefore requires higher-density observa-
591 tions in regions of interest. The results of this study also suggest that the use of sediment
592 types to parameterise the spatial variation of the friction parameter may not be appropriate
593 when tidal currents are of interest. This is because the tidal currents are affected on small
594 spatial scales by rapid changes in the BFC. We have also observed the BFC exerting a non-
595 local effect on the tidal currents, where the use of high values for the BFC in the centre
596 of the Channel drive higher currents along the southern edge of the Channel, where the
597 BFC is lower. This blockage effect results in the counter-intuitive result that the ‘standard’
598 sediment-based BFC field, which results in underestimated sea surface heights, actually pro-
599 duces the highest current speeds at an ADCP situated near the southern edge of the Channel.
600 Model calibration for tidal currents may require an alternative approach to BFC parameter-
601 isation which avoids sharp changes in the coefficient, e.g. via smoothing of the BFC field,
602 or avoiding piecewise-constant BFC fields entirely. This aspect requires further work, and
603 more extensive tidal current data.

604 **9 Conclusions**

605 This study has utilised sedimentological data within a numerical model of the Bristol Chan-
606 nel and Severn Estuary, in order to calibrate the model against available tide gauge data. The
607 direct use of theoretical Manning coefficient values corresponding to the median grain size
608 for each sediment type results in severe underestimates of the sea surface height, and con-
609 sequently the tidal range energy resource. This can be improved by the reduction of these
610 theoretical BFCs by scaling with a uniform factor, with the factor determined via a Bayesian
611 inference algorithm. However, the resulting model performance can be further improved by
612 the use of a well-selected spatially uniform BFC, confirming that when the data or com-
613 putational resources permit the solution of only a one-dimensional parameter estimation
614 problem, the spatially uniform BFC approach remains the best option.

615 However, the results have demonstrated that the sedimentological data can be used to
616 produce a piecewise-constant BFC according to three groups of sediment types. The solu-
617 tion of the resulting three-dimensional parameter estimation problem results in significant
618 improvements in model performance over the uniform-BFC case, as measured against both
619 the calibration and validation tide gauge data.

620 The application of the numerical model to tidal range resource assessment reveals a
621 somewhat localised sensitivity to the BFC, highlighting the need for observation data in
622 regions of interest. Due to the smaller-scale spatial variation in tidal currents, this issue is
623 greater for tidal stream resource assessment, and we have also identified a non-local effect
624 where excessive BFC values in the centre of the channel drive spuriously high currents
625 in other regions. This smaller-scale variation may also mean that the use of a piecewise-
626 constant BFC (such as the one used here based on dividing the domain by sediment types)
627 is incompatible with calibration for tidal currents, but further exploration of this issue is left
628 to future work, and will require a larger volume of ADCP data.

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635 **Conflict of interest**

636 The authors have no conflicts of interest to declare that are relevant to the content of this
637 article.

638 **Data availability statement**

639 The datasets generated during and/or analysed during the current study are available from
640 the corresponding author on reasonable request.

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