rassta: Raster-Based Spatial Stratification Algorithms

by Bryan A. Fuentes, Minerva J. Dorantes, and John R. Tipton

Abstract Spatial stratification of landscapes allows for the development of efficient sampling surveys, the inclusion of domain knowledge in data-driven modeling frameworks, and the production of information relating the spatial variability of response phenomena to that of landscape processes. This work presents the **rassta** package as a collection of algorithms dedicated to the spatial stratification of landscapes, the calculation of landscape correspondence metrics across geographic space, and the application of these metrics for spatial sampling and modeling of environmental phenomena. The theoretical background of **rassta** is presented through references to several studies which have benefited from landscape stratification routines. The functionality of **rassta** is presented through code examples which are complemented with the geographic visualization of their outputs.

Introduction

The application of robust, quantitative approaches for the spatial modeling of environmental phenomena has increased in the past few decades mainly due to an increase in computational power, advances in statistical modeling, and the availability of geospatial layers of environmental information (Scull et al., 2003; Elith and Leathwick, 2009). Most of these approaches aim at building explicit quantitative relationships between environmental controls and response phenomena through statistical learning. Examples of these approaches include digital soil mapping (DSM) (McBratney et al., 2003), species distribution modeling (SDM) (Guisan and Zimmermann, 2000), land use/land cover classification (Ham et al., 2005), and forest fire modeling (Chuvieco et al., 2010). Despite the extensively documented success of these approaches, there are still some challenges that limit their application. For instance, poor statistical performance is often reported in studies where input data is too limited to accurately represent control-response relationships (Araújo and Guisan, 2006). Moreover, model parsimony and interpretation of results can be compromised when using 'black-box' algorithms (Arrouays et al., 2020). Similarly, including a priori knowledge about natural processes in purely statistical approaches can be challenging to achieve (Heuvelink and Webster, 2001).

Several studies have suggested embedding spatial stratification routines within approaches such as DSM, SDM, land use/cover mapping, forest fire modeling, and others to overcome the challenges limiting their application. In such studies, the spatial stratification of landscapes creates units with reduced spatial variability of environmental phenomena as compared to the overall variability across a landscape. The use of these units allows the researcher to (a) obtain balanced representations of control-response relationships (Guisan and Zimmermann, 2000; West et al., 2016); (b) include expert knowledge of physical processes for improving modeling with limited data (Zhu et al., 2008); (c) improve the performance of parameterization of mechanistic models (Park and Van De Giesen, 2004; Baldwin et al., 2017); and, (d) facilitate the interpretation of environmental conditions and their influence on the spatiotemporal variability of processes of interest (Rodrigues et al., 2019).

In general, landscape stratification routines follow fundamental ecological concepts that explain the hierarchical and multi-scale nature of relationships between environmental phenomena across space (Allen and Starr, 1982). Therefore, landscape stratification methods have been applied in many studies that use geospatial information for environmental modeling, such as those previously cited. However, few packages exist in the R environment with functions strictly aimed at landscape stratification routines using geospatial data. Although one could implement custom stratification algorithms using multiple all-purpose geospatial analysis packages such as terra (Hijmans, 2021) and sf (Pebesma, 2018), the ease of use, reproducibility, and replicability of analysis is often enhanced when algorithms are implemented as part of a dedicated package. The motif package (Nowosad, 2021) is the only example the authors could find of a package that is fully dedicated to landscape stratification in R using geospatial data. Although the methods offered by motif are effective for large-scale studies (Jasiewicz et al., 2015; Nowosad, 2021), their application is currently limited to rasters of categorical data. Thus, motif is not practical for the modeling of spatially continuous environmental phenomena, which is often a goal of landscape stratification routines.

This work presents the **rassta** package as a collection of algorithms for the spatial stratification of landscapes, sampling, and modeling of environmental phenomena. The **rassta** package is not intended as a drop-in replacement for statistically-robust environmental modeling approaches. Rather, it is intended to serve as a generalized framework to derive geospatial information that can be used to improve inference with these statistical approaches.

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Conceptual overview and functionality

The algorithms in the **rassta** package assist in the analysis of environmental information related to the spatial variability of natural phenomena across landscapes. These functions focus on integrating standard geospatial techniques and quantitative analysis in a generalized framework for landscape stratification, sampling, and modeling. All of the functions in the **rassta** package take geospatial data in raster format as input. In the context of geographic information systems (GIS), the raster format can be considered a graphical representation of a matrix that is organized in rows and columns, and which may be stacked in multiple layers (e.g., multi-band satellite imagery). Each cell (pixel) in the raster contains a value representing a spatially-varying phenomenon, such as elevation or precipitation. A few functions in **rassta** also produce geospatial data in vector format. Vector data represents geometric entities in the form of points, lines, and polygons. The **rassta** package uses the highly efficient **terra** package as the backbone for handling raster and vector data. Most of the geospatial data manipulation with **terra** is performed in C++ and is based on two main R data types (classes): SpatRaster and SpatVector. Note that **terra** imports the **Rcpp** package (Eddelbuettel and François, 2011) since **terra** uses C++ (including external pointers) to manipulate these classes.

Most of the functions implemented in **rassta** are interrelated in the sense that the outputs from some functions can be used as the inputs for others. This functional interrelation allows for a generalized framework to conduct spatial stratification, sampling, and modeling in a single package following a project-oriented approach. In general, the functions of **rassta** can be grouped into five categories: (a) landscape stratification; (b) landscape correspondence metrics; (c) stratified sampling; (d) spatial modeling; and (e) miscellaneous (Figure 1). Each category and its corresponding functions (except for miscellaneous) are theoretically founded on several studies focused on understanding spatially-varying natural phenomena across landscapes. In the next sections, the rationale behind each category and its functions is described. This description is complemented with references to corresponding scientific literature and includes code examples showing the application of each function with extensive use of plotting functions (for visualization purposes only). Most of the plotting functions are derived from the **terra** package using the SpatRaster and SpatVector classes. [Note: To reduce the extension of code examples, all the map and graph plotting functions were consolidated in the function figure()].

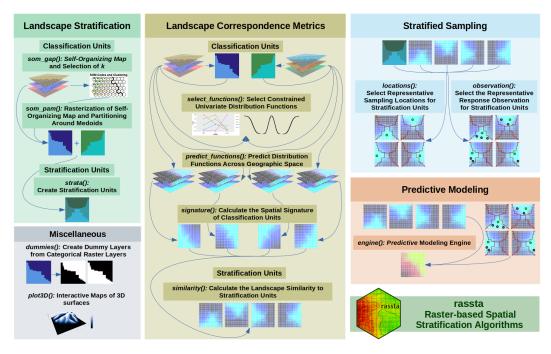


Figure 1: Functions of the rassta package. Connectors relate the inputs and outputs of the functions. The functions can be grouped in five categories: landscape stratification, landscape correspondence metrics, stratified sampling, predictive modeling, and miscellaneous.

Landscape stratification

Several studies have suggested the need to account for the hierarchical and multi-scale nature of landscape processes. Allen and Starr (1982) suggested that landscape processes can be explained through hierarchical multivariate structures given their multiple spatial and temporal scales. Based on

Dokuchaeiv's theory of soil formation (Glinka, 1927) and the soil-landscape paradigm (Hudson, 1992), McSweeney et al. (1994) proposed a nested model of soil-landscape processes at the physiographic, geomorphometric, and within-soil domains. Flügel (1995) suggested that the regionalization of hydrology-related processes should consider the multi-scale landscape heterogeneity in terms of soil, topography, geology, climate, and vegetation. These ideas have led these and other authors to formulate frameworks for the creation of spatial entities that stratify the landscape. The general purpose of these entities has been to define spatially-explicit domains that represent distinctive landscape processes and/or interactions (McSweeney et al., 1994). Accordingly, spatial stratification using rassta focuses on the creation of such domains (hereafter referred to as units).

The landscape stratification process with rassta follows a hierarchical approach similar to Austin and Heyligers (1989), who individually classified gradients of precipitation and elevation into intervals that were intersected with geologic classes for sampling purposes. Similarly, in rassta, a set of first-level units is created separately for each landscape factor under analysis. Then, multiple sets of first-level units are integrated into a single set of second-level units. The first-level units, called classification units, can be created outside of rassta via multicriteria analysis, statistical learning, or other methods. Moreover, the classification units can be formally defined through classification schemes, such as those based on taxonomic keys. The second-level units, called stratification units, result from the spatial intersection of multiple sets of classification units. Note that both classification and stratification units represent a spatial stratification for a given landscape. Figure 2 shows an example of a simple landscape stratification process based on two landscape factors, each with three raster layers representing continuous variables.

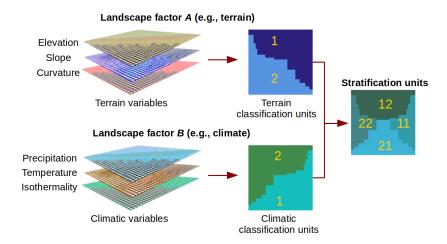


Figure 2: Schematic of a landscape stratification process. Raster layers of variables related to landscape factors are the inputs. The outputs are raster layers representing classification and stratification units.

There are three important aspects of the stratification approach used within **rassta** that must be considered. (a) One can simply create stratification units by incorporating variables from multiple landscape factors in a single classification process. However, the interpretation of results is often compromised when using a large number of variables in "all-in-the-bag" statistically driven classification schemes. (b) Multiple sets of classification units can belong to a single landscape factor, and each set can be created from variables at a distinct spatial scale. Presumably, this can account for the multi-scale nature of landscape factors in the stratification process. (c) A landscape factor can be represented by a single categorical variable, as in the case of geologic units or soil parent material. In this case, the landscape factor/variable is already in the form of classification units. Figure 3 shows a landscape stratification scenario like that addressed in (b) and (c).

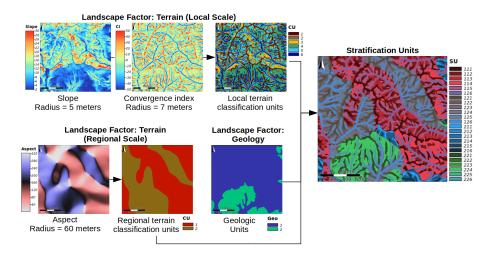


Figure 3: Schematic of a multi-scale landscape stratification process including a categorical variable. The stratification is based on two landscape factors: terrain and geology. Terrain is represented by raster layers of variables at two different spatial scales. Geology is represented by a single categorical raster layer.

Classification Units

A set of *n* classification units represents *n* distinct landscape configurations related to a single landscape factor. Note that the term *landscape configuration* is used here as a generic term for a particular pattern in the spatial variability of one or multiple variables belonging to a landscape factor. Currently, **rassta** allows the creation of classification units via unsupervised learning thanks to its functions som_gap() and som_pam(). The function som_gap() performs dimension reduction based on the self-organizing map (SOM) proposed by Kohonen (1990). The R package **kohonen** (Wehrens and Kruisselbrink, 2018) is called internally by som_gap() to produce the SOM. The function som_gap() also performs cluster analysis on the SOM codes based on the partitioning around medoids (PAM) (Kaufman and Rousseeuw, 1990), with estimation of the optimum number of clusters (*k*) through the gap statistic (Tibshirani et al., 2001). It is important to mention that the output SOM object returned by som_gap() can be used as input for any other clustering algorithm (e.g., hierarchical, spectral, etc.) or statistical analysis outside of **rassta**.

The code below shows how $som_gap()$ reduces the feature space and selects k clusters from four terrain variables. Note that the processing time of $som_gap()$ is significant (around 162 seconds on a 4-cores Intel processor at 3.2 GHz for the following example). The processing time increases as the number of cells/layers in the argument var.rast increases, and/or as the argument var.rast increases.

```
# Load the rassta and terra packages
library(rassta)
library(terra)
# Note that terra imports Rcpp, but if Rcpp is not automatically loaded then:
library(Rcpp)
# Get the data required to run the examples from rassta's installation folder
wasoil <- system.file("exdat/wasoil.zip", package = "rassta")</pre>
# Copy data to current working directory and extract files
file.copy(from = wasoil, to = getwd())
unzip("wasoil.zip")
# Set seed
set.seed(963)
# Multi-layer SpatRaster with 4 terrain variables
terr.var <- rast(c("height.tif", "midslope.tif", "slope.tif", "wetness.tif"))</pre>
# Scale variables to mean = 0 and standard deviation = 1
terr.varscale <- scale(terr.var)</pre>
# Dimensionality reduction and estimation of optimum k (max k to evaluate: 12)
terr.som <- som_gap(terr.varscale, xdim = 10, ydim = 10, K.max = 12)</pre>
# Plot results
figure(4, d = list(terr.var, terr.som))
```

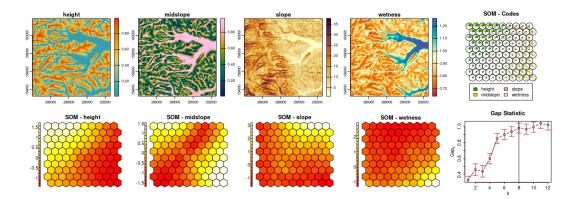


Figure 4: Dimension reduction and selection of k. The top row shows four terrain variables and the self-organizing map. The bottom row shows the reduced feature space and the Gap statistic to guide the selection of k.

The function som_pam() creates raster versions from the outputs of som_gap(). The code below shows how som_pam() creates raster versions of the SOM grid and PAM clustering computed in the previous example.

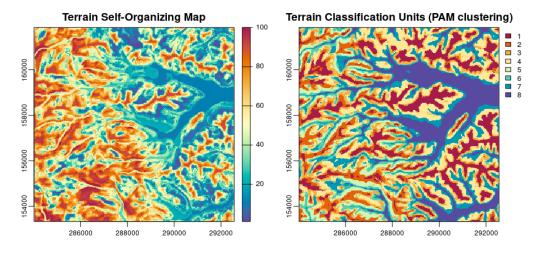


Figure 5: SOM grid and PAM clustering. Rasterized versions of the terrain SOM grid (left) and the terrain PAM clustering (right) are produced. The resulting clusters represent the classification units for the terrain landscape factor.

Note that the approach for creating classification units should not be limited to that offered by som_gap() and som_pam(). There are many other approaches outside of rassta that can be followed, such as supervised classification based on statistical learning, or GIS-based multicriteria analysis. The best approach may depend on the research question(s) being addressed. Therefore, the selection of the proper approach and the optional use of other R packages and/or GIS software is left to the user. Also, note that classification units created outside of rassta are completely compatible with rassta objects and methods if the units are represented through the SpatRaster class from terra.

Stratification Units

A set of *n* stratification units represents *n* distinct landscape configurations related to multiple landscape factors. Note that the term *landscape configuration* is used here as a generic term for a particular pattern in the spatial variability of multiple variables belonging to multiple landscape factors, or

to the same factor represented at multiple spatial scales. The function strata() allows the spatial intersection of multiple sets of classification units into a single set of stratification units. This function also assigns a unique numeric code to each stratification unit. The numeric code makes it possible to trace back each classification unit composing a given stratification unit. The code below shows the construction of stratification units with strata() using classification units from three landscape factors (climate, soil parent material, and terrain).

```
# Multi-layer SpatRaster with 3 sets of classification units
all.cu <- rast(c("climate.tif", "material.tif", "terrain.tif"))
# Stratification units
su <- strata(cu.rast = all.cu)
# Plot results
figure(6, d = list(su, all.cu))</pre>
```

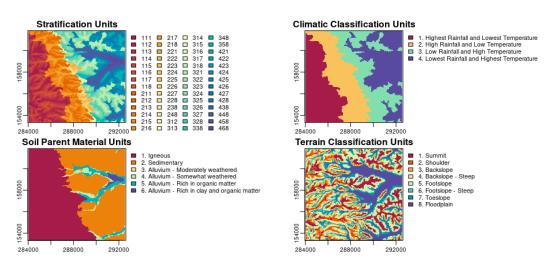


Figure 6: Stratification and classification units. A set of classification units is produced for soil parent material, terrain, and climate. The spatial intersection of these sets results in the stratification units for the landscape.

Metrics of landscape correspondence

There are two metrics of landscape correspondence that can be calculated with **rassta**: (a) the spatial signature of classification units, and (b) the landscape similarity to stratification units. These metrics quantify the relative correspondence between any location across geographic space and landscape configurations represented by classification and stratification units. Several studies have applied similar concepts related to continuous correspondence between landscape configurations for the modeling of spatially-varying phenomena. Early examples include studies using multivariate distance metrics in the feature space for SDM (Carpenter et al., 1993) and studies applying the fuzzy set theory (Zadeh, 1965) for multicriteria evaluation (Burrough, 1989), DSM (Zhu and Band, 1994) and landform classification (MacMillan et al., 2000).

Spatial signature of classification units

The spatial patterns of the degree of correspondence between any landscape configuration and the configuration represented by a given classification unit are defined as the *spatial signature*. The spatial signature is represented by a raster layer of continuous values that results from the cell-wise aggregation of empirical distribution functions mapped over geographic space. Each distribution function corresponds to one variable and relates the classification unit to "typical" values of the variable within the classification unit. The concept of spatial signature is based on the work of Pike and Rozema (1975) and Pike (1988). These authors used the term *geometric signature* to describe a set of sample statistics (e.g., mean, standard deviation) of terrain variables (e.g., slope, curvature) used to distinguish "geomorphically disparate landscapes" (Pike, 1988).

The spatial signature in **rassta** replaces the geometric signature's measurements of central tendency and dispersion statistics with statistical distribution functions generated across geographic space. The statistical distribution functions used in **rassta** are: (a) the probability density function (PDF) based on the kernel density estimation, (b) the empirical cumulative distribution function (ECDF), and (c) an

inverted version of the ECDF (iECDF). Note that the spatial signature concept is somewhat similar to the virtual ecological niche (Hirzel et al., 2001) and the multivariate environmental similarity surface (Elith et al., 2010), which are implemented in R through the packages virtualspecies (Leroy et al., 2016) and dismo (Hijmans et al., 2020), respectively. Figure 7 and Figure 8 show an illustration and a pseudocode of the process to calculate the spatial signature of a classification unit, respectively. Note that the function FUNSIG() in the pseudocode is just a placeholder to encompass the three functions from rassta that are required to calculate spatial signatures. These functions are select_functions(), predict_functions(), and signature(), each will be further discussed next.

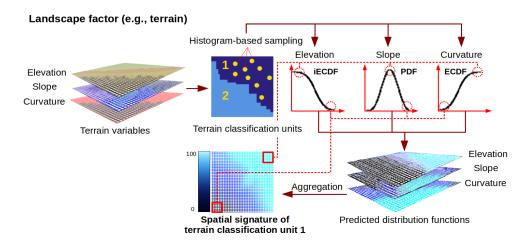


Figure 7: Schematic of the calculation process for spatial signatures. A set of classification units is produced using three variables. A distribution function is calculated for each variable within classification unit 1, and then predicted across geographic space. The predicted functions for unit 1 are aggregated, which results in the spatial signature of that unit.

```
Select and predict distribution functions, then calculate spatial signature
Require:
                    multi-layer SpatRaster with n layers (i.e., variables)
     V_{v1,...,vn}
                    single-layer SpatRaster representing n classification units
     C_{c1,\ldots,cn},
 1: function FUNSIG(V_{v1,...,vn}, C_{c1,...,cn})
 2:
         for each v in V_{v1,...,vn} do
              S_{c1,...,cn} \leftarrow \text{SUMMARY}(v, C_{c1,...,cn})
                                                                                        \triangleright within-unit statistic (e.g., mean) of v
 3:
 4:
              for each c in C_{c1,...,cn} do
 5:
                   v_c \leftarrow \text{EXTRACT}(v, c)
                                                                                           \triangleright Extract observations of v within c
                  if S_c = MAX(S_{c1,...,cn}) or S_c = MIN(S_{c1,...,cn}) then
                                                                                                       \triangleright S_c: statistic of v within c
 6:
                       f \leftarrow ECDF

ightharpoonup select distribution function for v_c
 7:
                       v_{cs} \leftarrow \text{QUANTILES}(v_c)

ightharpoonup sample from v_c to reduce processing time
 8.
 9:
                       c_f \leftarrow f(v_{cs})
                                                                                        \triangleright calculate distribution function of v_{cs}
                       if S_c = MIN(S_{c1,...,cn}) then
10:
                        c_f \leftarrow \text{INVERT}(c_f)
11:
12:
                       end if
13:
                   else
14:
                       v_{cs} \leftarrow \text{CentralPoints}(\ \textit{histogram}(v_c)\ )
15:
16:
                       c_f \leftarrow f(v_{cs})
                   end if
17:
                   c_{loess} \leftarrow \text{LOESS}(y \sim x); \ y = c_f, \ x = v_{cs}

ightharpoonup fit loess regression
18:
19:
                  cv_{predfun} \leftarrow PREDICT(c_{loess}, v)
                                                                         \triangleright predict the distribution function of v_{cs} across v
20:
              end for
         end for
21:
22:
         for each c in C do
23:
              c_{predfun} \leftarrow cv1_{predfun}, ..., cvn_{predfun}  \triangleright Predicted distribution functions for c (one per each v)
                                                                                                \triangleright calculate Spatial signature of c
24:
              c_{sig} \leftarrow \text{AGGREGATE}(c_{predfun})
         end for
26: end function
```

Figure 8: Pseudocode of the calculation process for spatial signatures. The calculation process involves the selection, prediction, and aggregation of distribution functions. The spatial signature is calculated for each classification unit in a set.

An important assumption is made when using the PDF, ECDF, and iECDF to characterize the typical values of a given variable within a given classification unit. The position of a value within the distribution function is an indicator of how typical the value is in terms of the variable's distribution within the classification unit. For instance, values closer to, or at the peak of the PDF are assumed to be the most typical values of the variable within the classification unit. Contrarily, values at the tails of the PDF are the less typical. Although one could simply use the PDF as a generalized function to denote typical values, this function assigns the same weight to values at the tails of the distribution regardless of the tail's location (left or right). In some cases, a priori knowledge can dictate that typical values of a variable within a given classification unit are those approaching $+\infty$, or those approaching $-\infty$. The use of the ECDF and the iECDF is intended for those cases. More specifically, if a classification unit is known to be associated with a variable's extreme values toward $+\infty$, then the ECDF can be used to represent this association. Conversely, if the classification unit is associated with those variable's extreme values toward $-\infty$, then the iECDF can be used.

The function select_functions() allows the user to select the statistical distribution function used to represent the typical values for a given variable within a specific classification unit. Both automatic and interactive selection modes are supported, with the latter based on a **shiny** app (Chang et al., 2021). The automatic selection of distribution functions is based on within-unit statistics, also referred to as *zonal statistics* in the GIS literature, and it follows the criteria described next:

- PDF = when the mean (or median) of the variable's values within the classification unit is neither the maximum nor the minimum of all the mean (or median) values across all the units.
- ECDF = when the mean (or median) of the variable's values within the classification unit is the
 maximum of all the mean (or median) values across all the units.
- iECDF = when the mean (or median) of the variable's values within the classification unit is the minimum of all the mean (or median) values across all the units.

The code below shows the automatic selection of statistical distribution functions for four climatic classification units and two variables with select_functions().

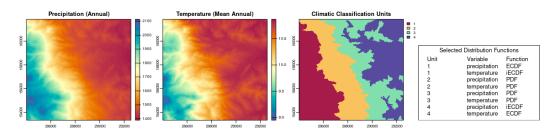


Figure 9: Selection of distribution functions. A set of four climatic classification units are produced using two variables: precipitation and temperature. A distribution function is selected for each variable within each classification unit.

The selected distribution functions can be used to generate predictions of distribution function values over geographic space with the function $predict_functions()$ as shown in the code below. The predictions are generated by fitting a locally estimated scatterplot smoothing (LOESS) regression with the within-unit distribution function's values (y) and the within-unit variable's values (x). The fitted LOESS and the raster layer of the variable are then used to predict new distribution function values across geographic space.

```
# Multi-layer SpatRaster of climatic variables and classification units
clim.all <- c(clim.var, clim.cu)
# Ouput table from select_functions()</pre>
```

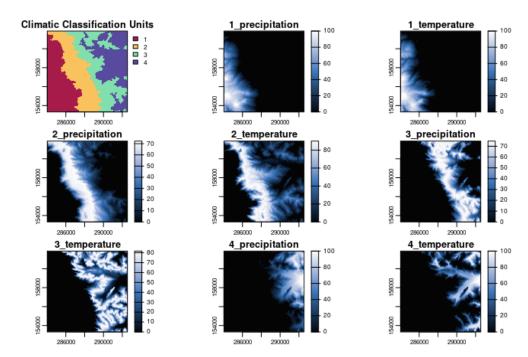


Figure 10: Prediction of distribution functions. A selected distribution function for each variable is predicted across geographic space. The predicted distribution function relates the landscape to a classification unit with regard to a variable.

The function signature() calculates the spatial signature of a given classification unit by aggregating all of the predicted distribution functions associated with the unit. The code below shows the calculation of spatial signatures with signature(). Note that the arguments inprex and outname allow the user to identify the raster layers representing the predicted distribution functions associated with each classification unit in a set, and to assign a unique name to each resulting raster layer of spatial signature, respectively.

Figure 11: Calculation of spatial signatures. The set of predicted distribution functions associated with a climatic classification unit are aggregated. The aggregation process results in the spatial signature of that unit.

Landscape similarity to stratification units

The spatial patterns of the degree of correspondence between any landscape configuration and the landscape configuration represented by a given stratification unit are defined as the *landscape similarity*. The landscape similarity is represented by a raster layer of continuous values, which results from the cell-wise aggregation of the spatial signatures of multiple classification units. This aggregation is possible because any given stratification unit is the result of the spatial intersection of multiple classification units, commonly one per landscape factor or factor scale (see Figure 2 and 3). Moreover, each classification unit has one spatial signature associated with it. Therefore, any given stratification unit will be associated with multiple spatial signatures, which can be cell-wise aggregated to calculate the landscape similarity. Figure 12 shows an example of the calculation process for a layer of landscape similarity to stratification unit.

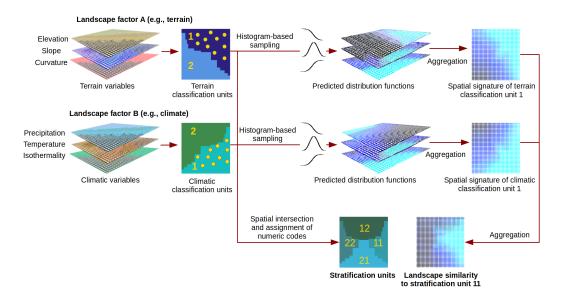


Figure 12: Schematic of the calculation process for landscape similarities. Each stratification unit has two or more classification units associated with it. Moreover, each classification unit has a spatial signature associated with it. Aggregating the spatial signatures of the classification units associated with a stratification unit results in the landscape similarity to that stratification unit.

The function similarity() calculates the landscape similarity layer for each stratification units in a given set (with the set being represented by a single-layer SpatRaster object), as shown in the following example. The argument su.code indicates the name of the landscape factors/factor scales used to create the stratification units, and the digit position (start, end) of the classification units' ID in the stratification unit's numeric code.

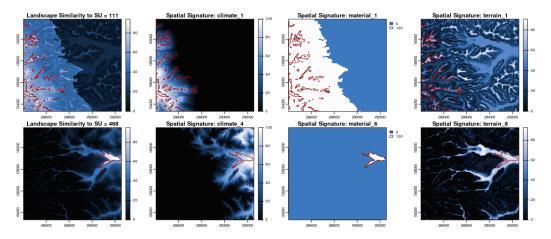


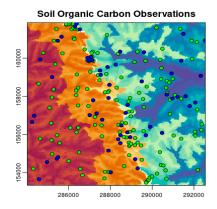
Figure 13: Metrics of landscape correspondence. Landscape similarity (extreme left) and spatial signatures associated with stratification units 111 (top row) and 468 (bottom row). The red polygons indicate the boundaries of the units.

Stratified non-probability sampling

Stratified sampling is an efficient technique for achieving an adequate representation of environmental variability, reducing cost of field work, and improving modeling with limited observations (Austin and Heyligers, 1989; Wessels et al., 1998; Guisan and Zimmermann, 2000; Zhu et al., 2008; West et al., 2016). Accordingly, sampling with rassta to select observations/sampling locations is performed in a stratified fashion using stratification units. Additionally, the raster layers of landscape similarity to stratification units can be included in the sampling process. Including the landscape similarity layers results in a non-probability sample. For each stratification unit, the sampling process selects the observation(s)/sampling location(s) at the raster cell where the highest landscape similarity value occurs, resulting in a stratified, non-probability sample that is biased towards maximizing the representativeness of landscape configurations. This idea of biased, stratified sampling is based on the work of Gillison (1983); Gillison and Brewer (1985), Austin and Heyligers (1989), and Zhu et al. (2008). These authors have suggested that bias related to landscape configurations is relevant for the maximization of environmental representativeness, detection of maximum diversity, and representation of non-stochastic control-response relationships.

The function observation() performs the automatic selection of the representative response observation for each stratification unit in a given set. Given a stratification unit, the unit's representative response observation is that whose value best reflects the influence that the unit's landscape configuration exerts on the response. This function requires a set of observations/samples already collected for a set of stratification units. Currently, observation() selects observations based on the following methods: (a) *mls*: select the observation at the raster cell with the maximum landscape similarity value; (b) *mrv*: select the observation whose response value is the median of all the values; and (c) *random*: select an observation at random. Note that the latter represents a case of stratified random sampling.

The code below shows the selection of representative soil organic carbon (SOC) observations based on the maximum landscape similarity method. Note that the arguments su.rast and ls.rast require the stratification units and landscape similarity layers previously created with strata() and similarity(), respectively.



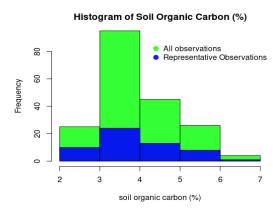
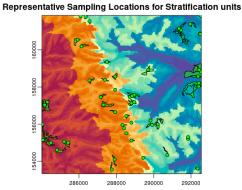


Figure 14: Selection of representative observations. Green points in the map represent the complete set of observations. Blue points represent the representative observation for each stratification unit.

The function locations() performs the automatic selection of the representative sampling location(s) for each stratification unit in a given set, where the representative sampling location is the raster cell where the highest landscape similarity value occurs. Currently, locations() implements two selection methods: (a) *buffer*: select sampling locations within areas with landscape similarity values above a certain threshold; and (b) *absolute*: select sampling locations with the highest landscape similarity values. The code below shows the use of locations() based on the buffer method.

```
# Representative sampling location and its buffer area for each stratification unit
su.samp <- locations(ls.rast = su.ls$landsim, su.rast = su, method = "buffer")
# Plot results
figure(14, d = list(su.samp, su))</pre>
```



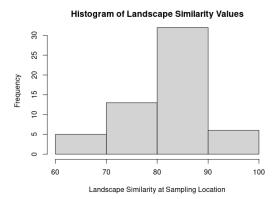


Figure 15: Selection of representative sampling locations. Green points in the map represent the sampling location for each stratification unit. Green polygons represent the buffer area for each sampling location.

Predictive modeling

Predictive modeling with **rassta** is based on the assumption that each stratification unit represents a distinct landscape configuration and that this configuration influences a natural phenomenon in a distinctive manner. It is assumed that the influence that a stratification unit's landscape configuration has on response phenomena at a specific location (i.e, raster cell) is proportional to the unit's landscape similarity value at that raster cell. Therefore, given a stratification unit x, the corresponding raster layer of landscape similarity ls, the response y, and a raster cell c, the greater the value of ls at c, the more similar y at c will be to the typical y for x. The typical (i.e., representative) value of a response phenomenon for a given stratification unit can be defined in several ways. For instance, if a response phenomenon was sampled/measured multiple times within a given stratification unit, the typical response value could be that from the sample/measurement at the raster cell with the highest landscape similarity value (see observation()).

Several studies have used landscape similarity layers to model the spatial variability of natural phenomena. These studies argue that the use of similarity layers is appropriate in cases when (a)

available observations for modeling are limited (Zhu et al., 2008); (b) initial spatial distribution patterns are needed for survey design (Carpenter et al., 1993); (c) expert-driven selection of informative variables is possible (Knick and Dyer, 1997); (d) *a priori* knowledge of response-control relationships in the form of conceptual models is available (Zhu et al., 2010; Schmidt et al., 2005); and (e) discriminating between (ecologically) positive and negative deviations from reference environments is required (Watrous et al., 2006). Accordingly, engine() allows the modeling of environmental phenomena with a number of training observations as few as the number of landscape similarity layers [cases (a) and (b)]; training observations and landscape similarity layers as outcomes of expert-driven landscape stratification [cases (c) and (d)]; and landscape similarity layers derived from spatial signatures that discriminate between the tails of distribution functions [case (e)].

Modeling with **rassta** is performed using the function <code>engine()</code>. For continuous responses, <code>engine()</code> performs a weighted average involving representative response values and landscape similarity layers. For a raster cell c, the modeled response value is equal to the weighted average of the representative values for those stratification units with the highest landscape similarity values at c. The stratification units with the highest landscape similarity values at c can be considered as the <code>nearest neighbors</code> (in feature space) of the landscape configuration at c. These nearest neighbors are called <code>winning stratification units</code>, and the weight of their corresponding representative value is proportional to the winning unit's landscape similarity value at c. For categorical responses, the modal response value of the winning stratification units replaces the weighted average. Figure 16 shows an example of the modeling process for continuous responses with <code>rassta</code>.

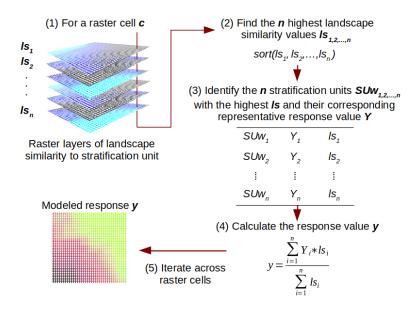


Figure 16: Schematic of the modeling process with rassta. The modeling process is performed in a cellwise fashion. The inputs required are the raster layers of landscape similarity and the representative observations for each stratification unit.

Note that the weighted average for modeling phenomena across geographic space has been widely applied in GIS-based multicriteria decision analysis (GIS-MCDA). In GIS-MCDA, attributes (i.e., variables) in the form of raster layers are weighted according to expert criteria. The weighted variables are then combined through (cell-wise) overlay operators such as multiplication, addition and (ordered) averaging. The resulting value at each cell represents the relative suitability for a certain condition/decision (Malczewski, 2006). The function engine() generalizes the weighted overlay process of GIS-MCDA by allowing the use of sampled/measured data of a response phenomenon in conjunction with the landscape similarity layers acting as weighted variables. This generalization allows the modeling of real-valued phenomena in continuous or categorical form. The modeling approach of engine() is almost the same as that proposed by Zhu (1997) to model landscape attributes across geographic space. The difference between engine() and the approach of Zhu (1997) is that engine() allows the selection of the number of landscape similarity layers for the weighted average calculation. Presumably, restricting the number of layers will reduce the shortening ('shrinking') effect that weighted averaging has on the range of modeled continuous response values (Nolan et al., 2019).

The code below demonstrates the use of engine() for the predictive modeling of soil organic carbon. Note that the representative response values (argument su.repobs) are those previously selected with observation(), and that the layers of landscape similarity (argument ls.rast) are those

previously created with similarity().

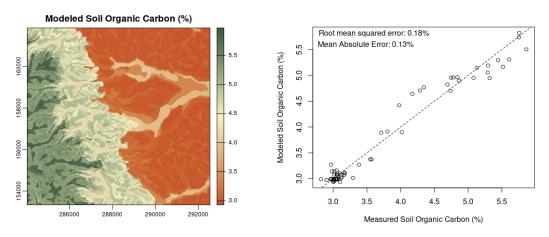


Figure 17: Modeled SOC (percent). The map shows the modeled SOC values across the landscape. The plot shows a simple statistical evaluation of the modeled values based on 62 independent observations.

Miscellaneous

The spatial signature only applies to classification units created from continuous variables. Thus, spatial signatures cannot be calculated for classification units that represent categorical variables, such as land use/land cover. In such cases, a one-hot encoding can be applied to produce binary layers for the units. These layers are considered the spatial signatures of the classification units. The code below shows the creation of binary layers for soil parent material units with dummies().

```
# Multi-layer SpatRaster of soil parent material units
mat.cu <- rast("material.tif")
# Binary layers for each soil parent material unit
mat.sig <- dummies(mat.cu, preval = 100, absval = 0)
# Plot results
figure(17, d = mat.sig)</pre>
```

Figure 18: Construction of binary layers. Binary layers act as the spatial signatures for categorical variables. In this example, soil parent material acts as both landscape factor and classification units.

The function plot3D() produces interactive maps showing the 3-dimensional (XYZ) variability in raster layers representing continuous variables. The XYZ reference positions are obtained from a user-supplied elevation layer. For large raster layers (large spatial coverage and/or high spatial resolution), this function allows the option to decrease resolution and subset the data. The code below shows how plot3D() creates a 3D map for SOC, as modeled with engine().

```
# Single-layer SpatRaster of terrain elevation
elev <- rast("elevation.tif")
# 3D map
plot3D(c(elev, soc), z = 1, ex = 0.2, pals = "Fall", rev = TRUE)</pre>
```

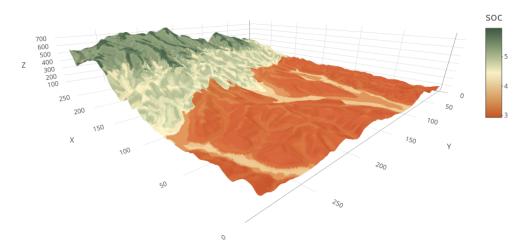


Figure 19: 3D map of SOC (percent). The Z dimension is obtained from a reference terrain model. Visit the online article to access the interactive version of the map.

Future versioning and summary

This work presented the **rassta** package for spatial stratification, sampling, and modeling of environmental phenomena within the R environment. Future versioning of the **rassta** package will focus on developing new approaches for spatial stratification. Stratification based on spatial intersection may not be feasible to implement in highly complex landscapes because these landscapes may require many (sets of) classification units to accurately represent the spatial variability of landscape factors, leading to over-stratification, and thus, greater demand for samples/observations to conduct predictive modeling based on landscape similarity. One plausible solution is the application of the stratification methods presented by Jasiewicz et al. (2015), Jasiewicz et al. (2018), Nowosad (2021), and Nowosad and Stepinski (2021). However, these methods have been purposely designed for studies with continental/global applications. Therefore, these methods should be adapted for **rassta** to tailor their application at local scales to allow for more precise representations of natural phenomena and their spatial variability. Another focus of versioning can be new functions to visualize the variability of response phenomena relative to the hierarchical structure represented by the stratification units. Lastly, future versioning of **rassta** should also consider the user's experiences to ensure its general applicability.

The core ideas implemented in the **rassta** package include the multi-scale, hierarchical landscape stratification based on spatial intersection, the application of non-parametric distribution estimators to define the typical landscape configuration of stratification units, and the use of spatially explicit landscape correspondence metrics for non-probability sampling and predictive modeling. Some of these ideas have previously been implemented in R through a few packages dedicated to the analysis of geospatial data. Nevertheless, **rassta** offers a unified, generalized framework to conduct multiple landscape stratification routines through a dedicated set of algorithms. Moreover, spatially-explicit information created with **rassta**, like stratification units, landscape similarity layers, and representative observations, can be embedded into statistically robust modeling approaches to optimize the analysis of environmental phenomena.

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