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**A HEURISTIC APPROACH FOR MODELING THE SURFACE HISTORIES OF CRATONS USING APATITE
FISSION-TRACK “SUPER SAMPLES”**

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A heuristic approach for modeling the surface histories of cratons using apatite fission-track “super samples”

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Abstract

Understanding the long-term erosion and burial history of cratons is often challenging due to the incompleteness of the geologic record. Low-temperature thermochronology has been used to provide constraints on these histories and apatite fission-track dating has long been one of the preferred methods. In terms of analytical protocol the convention has been to measure ~ 100 confined track lengths and to produce ~ 20 single-grain ages. These data are then inverted for thermal history along with sparse constraints and other assumptions pertaining to the regional geologic evolution. However, imposing constraints will influence the form of the inferred thermal histories. In some cases this step may limit impartial assessment of the unknown history in terms of what features are required by the data and those that the data are consistent with (or at least do not contradict). Here we present a study involving apatite fission-track data collected from central Canadian Shield basement rocks with more dated age grains and $\sim 3\text{--}7\times$ the number of track-length measurements when compared to a conventional analysis. We refer to these data as “super samples” (AFTSS) and show such data can improve resolution of complex histories involving episodic reheating and partial annealing. Importantly for the data we discuss, AFTSS can also be used to independently infer past geologic conditions without the enforcement of many *a priori* constraints during modeling—such as the approximate times of past basement exposure. Modeling in this way is guided by a heuristic philosophy regarding the use of thermal history constraints. This allows us to examine the ability of the model to independently infer geologically plausible time-temperature paths from the fission-track data alone. Inversions of these data establish that

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the currently exposed basement near the Hudson Bay Basin was buried in the middle Paleozoic and late Mesozoic, in agreement with the preserved regional rock record and adding further evidence to suggest that the basin is an erosional remnant. The AFTSS data alone imply two reheating events and indirectly require periods at cooler (near-surface) conditions in the latest Neoproterozoic to early Paleozoic and in the Jurassic to early Cretaceous—the timing of which are consistent with known Hudson Platform unconformities. We recommend that cratonic basement rocks that may have experienced episodic burial reheating (~ 60 to $< 100^\circ\text{C}$) and partial annealing over hundreds of millions of years should have a minimum of 250–300 track lengths collected to provide adequate time-temperature information for thermal history modeling.

Keywords: apatite fission track, cratons, thermochronology, Bayesian modeling, Canadian Shield, burial history

1. Introduction

Cratons or shields are the ancient nuclei of continents that are considered to have been tectonically stable since the Archean-Paleoproterozoic. These regions are typically characterized by low topographic relief and Precambrian igneous and metamorphic basement exposed at the surface. Many shields are devoid of sedimentary cover—making reconstruction of their post-orogenic geological history difficult. For example, most of the Canadian interior is comprised of Precambrian basement sporadically covered only by thin early Paleozoic or middle-late Mesozoic sedimentary strata (e.g., Sloss, 1963; Telford and Long, 1986; Norris, 1993; Pinet et al., 2013; Burgess, 2019)—leaving much of the Phanerozoic geological history an open question. To address the potential to recover this missing record, apatite fission-track (AFT) thermochronology has been one of the primary tools used to constrain the potentially complex burial and erosion histories of cratons (Kohn and Gleadow, 2019, for review).

The AFT thermochronometer provides time and temperature information from the damage features or ‘tracks’ produced by the energetic fission of ^{238}U within the apatite crystal lattice (e.g., Fleischer and Price, 1963). The number of spontaneous tracks per unit area is related to the amount of U in the grain and thus can provide an estimate of the time (i.e., apparent age) over which tracks have accumulated and been preserved in the crystal. Fission tracks form continuously over time with an initial etched length of ~ 16 – $17\ \mu\text{m}$, and fade or anneal when subjected to higher temperature, resulting in a nearly equivalent reduction in track density (per area) across the etched grain surface (e.g., Gleadow and Duddy, 1981). Observations of borehole samples showed that with increasing depth, mean track length is reduced with increasing temperature (Gleadow et al., 1986; Fig. 1). As a consequence, annealing decreases the ‘age’ of the sample as each track is shortened to a degree reflecting the maximum temperature experienced during its history before being totally annealed at

22 approximately 110–120°C (Gleadow and Duddy, 1981; Green et al., 1986; Gleadow et al., 1986). Laboratory
23 experiments have also demonstrated that resistance to thermal annealing is influenced by apatite composition,
24 primarily Cl and various elemental substitutions such as Fe, OH, Mg, Na, Mn, and Sr that enhance track
25 retentivity compared to common fluorapatite (Green et al., 1985; Carlson et al., 1999; Barbarand et al.,
26 2003). Apatite composition is measured directly by electron microprobe or laser ablation inductively coupled
27 plasma mass spectrometry (LA-ICPMS)—although it is commonly estimated indirectly by proxy with the
28 D_{par} parameter (track etch-pit diameter; e.g., Donelick et al., 2005). Grain chemistry provides a means for
29 approximating the track annealing kinetics, which are a critical requirement for thermal history modeling.
30 (e.g., Laslett et al., 1987; Ketcham et al., 1999; Donelick et al., 2005; Ketcham, 2019).

31 The temperature range of the AFT partial annealing zone (PAZ; $\sim 120\text{--}60^\circ\text{C}$) varies as a function of the
32 annealing kinetics and the rock cooling rate (Gleadow and Duddy, 1981; Green et al., 1986; Gleadow et al.,
33 1986; Duddy et al., 1988). The length of a given fission track will reflect to a large degree the maximum
34 temperature that track experienced, whereas the distribution of track lengths provides key information on
35 the structure of the thermal history. The ages can inform us about the overall duration of, and sometimes
36 timing of events in, the overall thermal history. Figure 1 conceptually demonstrates this using a forward
37 model for a hypothetical host rock that experienced four different simplified thermal histories, including: (1)
38 rapid cooling followed by quiescence; (2) linear, slow cooling at a typical ‘cratonic rate’ of $\sim 0.2^\circ\text{C}/\text{My}$; (3)
39 slow cooling to the surface, followed by reheating to 65°C and cooling out of the PAZ; and (4) same style
40 as history 3 except reheating to 85°C within the PAZ. Each of these histories produce characteristic track
41 length distributions (Fig. 1B–E) that are diagnostic of the type of history the AFT sample experienced. The
42 histories in Figure 1A yield either, a unimodal (normal) distribution of long track lengths of $\sim 15\ \mu\text{m}$ for
43 the rapid cooling scenario; a unimodal negative skew distribution for slow cooling with a mean length of
44 $\sim 14\ \mu\text{m}$; a unimodal broad or flattened distribution with a similar mean length as the slow cooling case;
45 and a bimodal distribution for the 85°C reheating example. The progression from Figure 1B–E generally
46 shows that track length distributions become broader and shorter with increased magnitude and duration of
47 heating (e.g., Gleadow et al., 1986). From these simple models, we can see that track lengths are essential for
48 understanding thermal history.

49 2. Motivation

50 For cratonic studies, many rock samples are often collected across a broad area and these samples then
51 undergo standard mineral separation and AFT analysis. The AFT data are then modelled within a framework
52 of geologic constraints (or geologic assumptions/interpretations) for the given study area. However, when

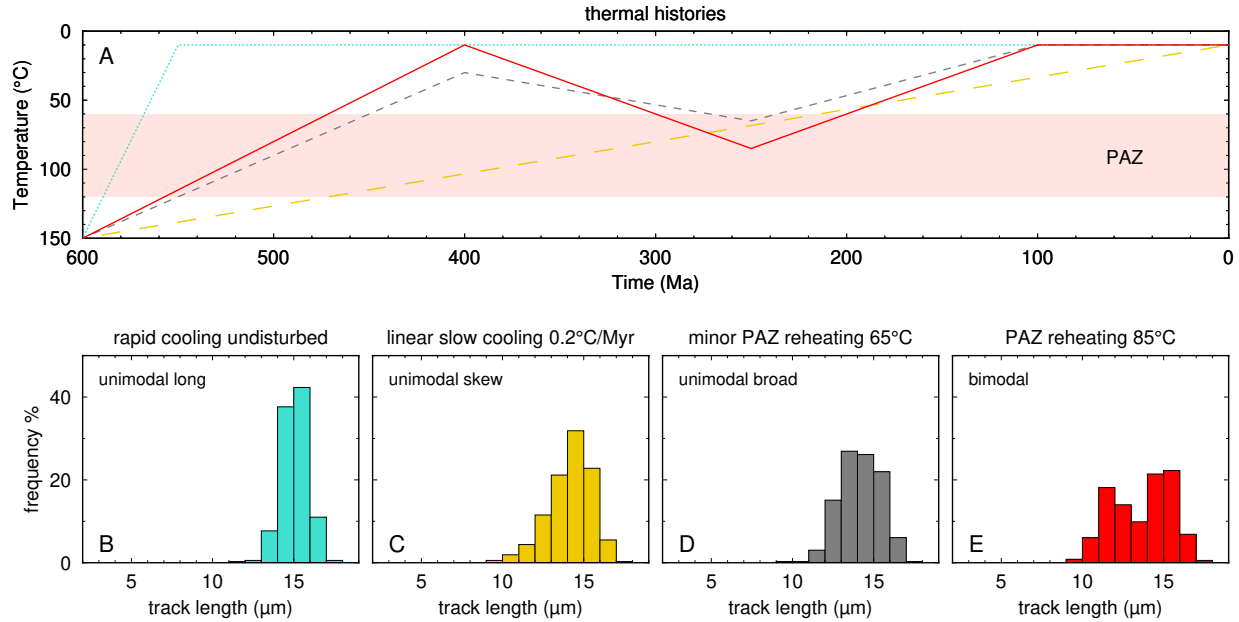


Figure 1: (A) Hypothetical thermal history scenarios and the corresponding c-axis projected track length distributions produced from each $t-T$ path. Rapid cooling (blue dotted line), slow cooling (yellow long dash line), minor PAZ reheating (gray short dash line), and greater PAZ reheating (red solid line). (B) unimodal long track lengths corresponding to rapid cooling and subsequent stasis. (C) unimodal right skew track length distribution typical of simple, slow cooling. (D) unimodal track length distribution that has been shortened and broadened due to reheating to 65°C. (E) bimodal track length distribution due to a history involving greater reheating to 85°C.

53 trying to reconstruct the time-temperature ($t-T$) histories from these data, the lack of physical geologic
 54 constraints to inform modeling is problematic (McDannell and Flowers, 2020; McDannell and Issler, 2021).
 55 This is commonly addressed by utilizing whatever geologic information we do have—however, unless samples
 56 are taken directly from well-constrained locations (e.g., near basement unconformities), there is typically
 57 some degree of regional extrapolation of, or uncertainty in, assumptions about past geologic conditions. In
 58 some situations these regional inferences may be warranted, whereas in others they may not, and it is difficult
 59 to know which is the case before carrying out modeling. The issue then relates to our ability to resolve more
 60 complex thermal histories in the absence of firm geological constraints.

61 One option to constrain low-temperature histories ($< 150^{\circ}\text{C}$) is to better exploit the information contained
 62 in the horizontal confined track-length distributions provided by the AFT method, as track lengths are
 63 sensitive indicators of thermal history style (Crowley, 1985; Gleadow et al., 1986; Duddy et al., 1988; Green
 64 et al., 1989). The convention has been for analysts to count the number of spontaneous tracks (N_s) from up to
 65 20 grains for age determination and measure a minimum of ~ 50 – 100 track lengths to obtain a representative
 66 distribution for use in $t-T$ modeling (e.g., Rahn and Seward, 2000; Donelick et al., 2005). While the optimal
 67 number of data to collect is dependent upon the geological problem, 100 tracks is generally considered
 68 sufficient for statistical reasons and analytical economy (Donelick et al., 2005). For instance, if a volcanic
 69 rock is rapidly cooled at or near the surface and is characterized by a long ($> 14 \mu\text{m}$), narrow track-length

70 distribution (e.g., Gleadow et al., 1986; and our Fig. 1), then 100 track lengths is more than enough data for
71 characterizing the thermal history. The implicit assumption is that at some finite number of tracks, there are
72 diminishing returns regarding the information contained in, and retrievable from, AFT data—which is in
73 principle dependent upon the complexity of the thermal history and the amount of annealing endured by
74 a sample. In the particular case of cratons, histories are complex and often involve slow cooling rates on
75 the order of a few °C/My (or less) and relatively minor, episodic heating (~60–90°C) into the PAZ due to
76 burial—thus presenting a challenge for modeling, especially if geologic constraints are lacking.

77 Here we discuss AFT “super samples” (AFTSS), which are defined as samples where a far greater number
78 of confined track lengths are measured (~300–700) compared to conventional AFT methods. AFTSS have
79 increased resolving power for deciphering complex thermal histories involving partial annealing and multiple
80 reheating events—and can be used to independently deduce past geologic conditions (without the enforcement
81 of many *a priori* constraints during modeling). Modeling is therefore guided by a heuristic or empirical
82 philosophy regarding ‘constraint’ placement. While indisputable geologic information should be used if
83 available, it is often not available in cratonic settings. Therefore, we minimize the implementation of
84 constraints (as time-temperature boxes) that force the model to take a predefined path, allowing us to
85 instead examine the ability of the model to independently infer geologically plausible t – T paths from the
86 thermochronologic data alone. Simulations were performed in the Bayesian QTQt software (Gallagher, 2012)
87 to illustrate the benefits of this approach. AFTSS analysis opens up the possibility of enhancing thermal
88 history recovery by maintaining established AFT methodologies but simply increasing the number of track
89 lengths collected for use during t – T inversion.

90 3. Time-temperature modeling approach

91 Forward and inverse modeling was carried out within a Bayesian modeling framework using the QTQt
92 v. 5.8.0 software (Gallagher, 2012). For the inversion, QTQt implements a reversible jump Markov Chain
93 Monte Carlo (MCMC) algorithm that utilizes various prior information (defining the range of allowable values
94 for parameters such as time and temperature, heating-cooling rate, kinetic parameter variability, i.e., track
95 annealing kinetics, and more specific geological-type constraints such as the depositional age of sedimentary
96 rocks or timing of unconformities). These parameters are randomly sampled and perturbed as individual
97 forward models are iteratively constructed many times, yielding an ensemble of accepted t – T solutions
98 that reproduce the observed data. The criterion for proposed model acceptance in MCMC is based on the
99 combined prior-likelihood-proposal ratio, and simple thermal histories with fewer t – T points are generally
100 preferred over more complex ones if the fit between the predicted and observed data is similar—hence the

101 data determine the level of history complexity (Gallagher, 2012). This general approach is also beneficial for
102 assessing the resolving power of low-temperature thermochronometric data with or without user-specified
103 constraints (McDannell and Issler, 2021).

104 QTQt model runs were setup with the same general prior for the thermal history: 300 ± 300 Ma and 75
105 $\pm 75^\circ\text{C}$ ($70 \pm 70^\circ\text{C}$ for real data; see below) and a modern surface temperature of $10 \pm 10^\circ\text{C}$ (maximum
106 allowed heating/cooling rate of $3^\circ\text{C}/\text{My}$)¹. The annealing model of Ketchum et al. (1999) was used with
107 the r_{mr0} kinetic parameter and track length c-axis projection. The apatite composition was specified as
108 common fluorapatite with a r_{mr0} value of 0.84 (or 0.0 eCl) for synthetic data. Apatite composition was
109 allowed to vary within uncertainty for the real AFT data discussed below and the initial track length was
110 calculated based on composition. Models were run for a total of 500,000 iterations, with an initial burn-in
111 of 100,000 iterations. The 400,000 MCMC post burn-in iterations were used to approximate the posterior
112 probability distribution of model parameters. We also incorporated a recently introduced option in QTQt to
113 reject a more complex proposed model (or accept a simpler proposed model explicitly if the data fit does
114 not change). This is achieved by monitoring the likelihood during proposed addition or removal of a t - T
115 point—if a point is added (i.e., increasing t - T path complexity) and the likelihood remains the same, then
116 the proposal model is rejected, whereas the opposite occurs for the removal of a point. This option inherently
117 reduces t - T uncertainty and penalizes complexity more heavily than the general algorithm presented in
118 Gallagher (2012), providing a lower bound on the complexity required to best explain the observations. It
119 should be noted that the final population of accepted thermal history models is of course conditional on this
120 assumption and as such should be considered as a conditional posterior distribution.

121 4. How many track lengths do we need to resolve complex histories?

122 4.1. Synthetic resolution tests

123 We consider how the number of confined track lengths affects our ability to reconstruct the thermal
124 history. We initially examined whether a typical AFT analysis with 100 ± 50 track lengths contains enough
125 information for cratonic thermal history reconstruction without imposing numerous model assumptions. We
126 may then ask how many tracks are necessary for adequate t - T resolution? While these questions are specific
127 to the examples discussed here, the requirement of a representative number of track lengths is axiomatic to
128 *any* AFT thermal history reconstruction and may generally apply to other regions that experienced similar
129 protracted histories involving episodic reheating and partial track annealing from sedimentary burial. We first

¹These limits were imposed to prevent extreme temperature fluctuations and t - T paths that are unlikely for this geologic setting. The allowance of higher rates during tests did not change the form of the model thermal histories.

130 use synthetic AFT data to explore a simple case and so avoid the problems inherent to natural samples with
 131 unknown histories. We use a thermal history in which the maximum reheating temperature is relatively low
 132 but still high enough to cause some annealing of the tracks present at that time. The aim is to demonstrate
 133 the sensitivity of the length distribution (and the number of tracks defining it) to subtle reheating events and
 134 the our ability to recover the thermal history with different amounts of track-length data.

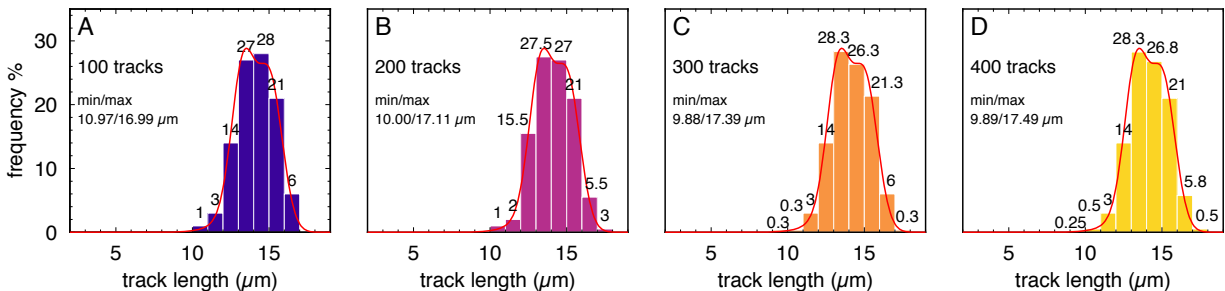


Figure 2: Track length distributions derived from forward modeling dashed gray t - T path in Figure 1 (i.e., broad unimodal with heating to 65°C). Red curve is the true predicted distribution. The number of tracks that define the predicted distribution were randomly drawn and increased from 100 to 400 and are shown as histograms with 1 μm bins. (A) 100 tracks. (B) 200 tracks. (C) 300 tracks. (D) 400 tracks. True distributions in B–D were normalized to panel A. Values above histogram bars are the percent of total tracks in each bin (rounded 0.1%) that define the distribution.

135 The reheating history shown in Figure 1A (dashed gray path) was forward modelled to produce synthetic
 136 AFT data (Fig. 2). The AFT age data were held constant, whereas the number of track lengths sampled
 137 from the predicted length distribution was progressively increased from 100 to 400. Increasing the number of
 138 tracks represented in the histograms improves characterization of subtle features of the predicted distribution,
 139 namely the tails and the ‘shoulder’ at 14–15 μm (Fig. 2). We are demonstrating that with a greater number
 140 of tracks, we more accurately represent the ‘true’ length distribution (Fig. 2). These synthetic samples were
 141 then inverted in an attempt to recover the true history used to generate the track data (Fig. 3). While these
 142 results are conditional on rejecting more complex models—100 measured track lengths are not enough data to
 143 fully resolve the t - T path. These models illustrate that > 200 track lengths are required to properly capture
 144 the details of the thermal history in a case involving minor thermal annealing. Inverse models with a greater
 145 number of tracks improved the resolution of the early cooling episode, which is to be expected since more
 146 tracks experienced this cooling event—however, as more tracks are utilized, the reheating event is better
 147 resolved by a larger proportion of the accepted model paths (Fig. 3). A general point learned from this
 148 demonstration is that if the thermal history is complex, then we will likely require more track lengths to
 149 properly define the (similarly complex) distribution for modeling. We examined these concepts further using
 150 real AFT data from the Canadian Shield.

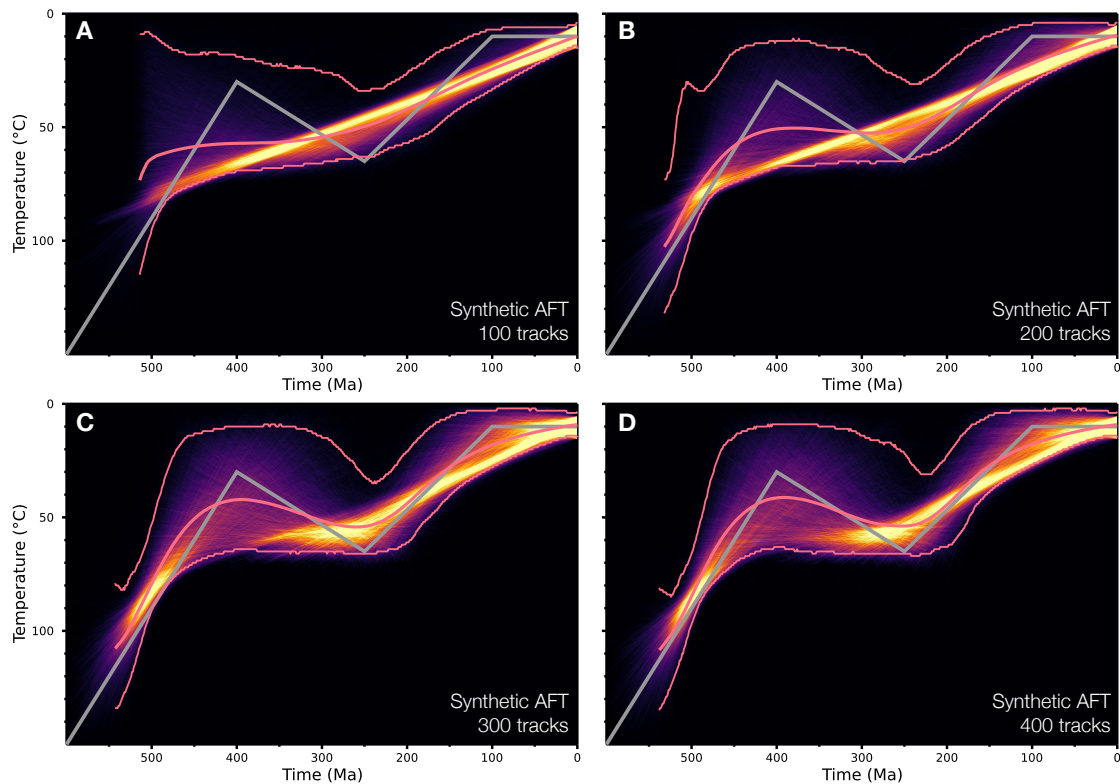


Figure 3: Inverse QTQt models using synthetic AFT data derived from the dashed gray t - T path in Fig. 1A (lengths in Fig. 1D). Results are shown as heat maps of t - T path density, where brighter colors are higher relative posterior probability. The difference between each model going from A to D is the increased number of tracks that define the true predicted distribution. (A) results for 100 tracks; (B) results for 200 tracks; (C) results for 300 tracks; (D) results for 400 tracks. The gray path is the true history and the pink lines are the QTQt Expected model with 95% credible interval. The latter model is the average of the marginal distribution and is shown as a summary of all accepted post burn-in solutions and does not represent an individual history sampled during the inversion. Figure S1 in the *SI* shows forward models of the same t - T path for a typical endmember fluorapatite where the thermal peak is progressively increased from 65°C (shown here) to 115°C in 10°C increments. This demonstrates how the AFT central age and track-length distribution evolve with increased heating into the PAZ until the sample is thermally reset near ~110°C.

151 4.2. Case study: Hearne Domain and Trans-Hudson Orogen, Canadian Shield

152 Two crystalline basement samples were collected from the central Canadian Shield that have some reliable,
 153 yet limited geologic information (described below) to support thermal history modeling. The Hearne Domain
 154 lies in the Churchill Province of the shield (Fig. 4) and is primarily comprised of Neoproterozoic granitoids,
 155 greenstones, metasedimentary and volcanic rocks, and Paleoproterozoic granites that flank the *c.* 1900–1800
 156 Ga Trans-Hudson Orogen (THO) basement to the south (Hoffman, 1989; Fig. 4) and the Paleozoic-Mesozoic
 157 Hudson Bay sedimentary basin to the east (e.g., Pinet et al., 2013). This area is considered to have generally
 158 been tectonically stable since *c.* 1650 Ma (Rainbird et al., 2007) following the Trans-Hudson orogeny. The
 159 Hearne sample (97-10-365) is from the exposed granodiorite basement within the Seal River Fold Belt. This
 160 location is at the erosional edge of the Hudson Bay Precambrian unconformity at the mouth of the Seal River
 161 in northeastern Manitoba. The THO sample was collected from a foliated biotite tonalite from Stephens
 162 Lake, ~28 km from the Paleozoic unconformity in Manitoba. Regional geologic context for the Phanerozoic,
 163 with respect to the sample locations, is as follows:

- 164 • The preserved onshore basal Paleozoic section of the Hudson Bay Basin is the upper Ordovician Portage
165 Chute Formation (*c.* 450 Ma) of the Bad Cache Rapids Group (e.g., Lavoie et al., 2019, for summary).
- 166 • The Moose River Basin (~ 700 – 1000 km to the SE; Fig. 4) contains Upper Ordovician through Upper
167 Devonian strata with a major unconformity overlain by erosional remnants of minor Middle Jurassic
168 and unconformable (Albian and Aptian?) Cretaceous rocks (Norris, 1977; Telford and Long, 1986;
169 Norris, 1993; Pinet et al., 2013).
- 170 • The *c.* 180–170 Ma hypabyssal facies kimberlites in the Attawapiskat vicinity of the Moose River Basin
171 were erupted subaerially through basement and Paleozoic cover (Sage, 2000, for review).
- 172 • The Williston Basin lies to the southwest of our samples (Fig. 4) and contains thick basin fill of > 4 km
173 due to deposition during most of the Phanerozoic (Burrus et al., 1996), beginning with the platform
174 onlap of the Sauk sequence (Sloss, 1963; Burgess, 2019).
- 175 • The INCO-Winisk #49204 borehole (~ 500 – 700 km to the SE; Fig. 4) contains palynological evidence
176 of Aptian-Turonian sediment recycling and sediments preserved at ~ 70 m depth of Miocene age (*c.*
177 23–5 Ma) unconformably overlying the Paleozoic section (Galloway et al., 2012).

178 This information suggests that Precambrian basement was exposed by 450 Ma. An interval of regional
179 subaerial exposure during the Early-Middle Jurassic was possible, followed by deposition during the Cretaceous
180 and exhumation by approximately Miocene. There is also the question of whether this part of the currently
181 exposed shield basement was buried during deposition of the Hudson Bay sequence. We present our new
182 analytical results, which are then modelled to assess whether our AFTSS data can yield thermal histories
183 that are independently consistent with the accepted regional geological evolution.

184 5. Apatite fission track and electron microprobe methods and results

185 Apatite grains were double-dated (AFT and U–Pb) by the LA-ICPMS method (Chew and Donelick,
186 2012; Cogné et al., 2020). The modified ζ -calibration approach was utilized with the Durango and McClure
187 Mountain age standards for FT and U–Pb data acquisition. The AFT pooled age obtained in analytical
188 sessions for Durango was 31.4 ± 1.6 Ma (2σ) and 256 ± 14 Ma for McClure Mtn. apatite. The weighted
189 mean U–Pb age of McClure Mtn. apatite was 525 ± 27 Ma (2σ). All ages are in agreement with accepted
190 previously published values (see Chew and Donelick, 2012). All analytical methods are the same as those
191 discussed in McDannell et al. (2019a) and McDannell et al. (2019b).

192 Single guided laser-ablation spots were chosen within minimized grain counting areas to avoid potential U
193 zonation and all analytical results are shown in Table 1 and Table 2. The high N_s track densities make U

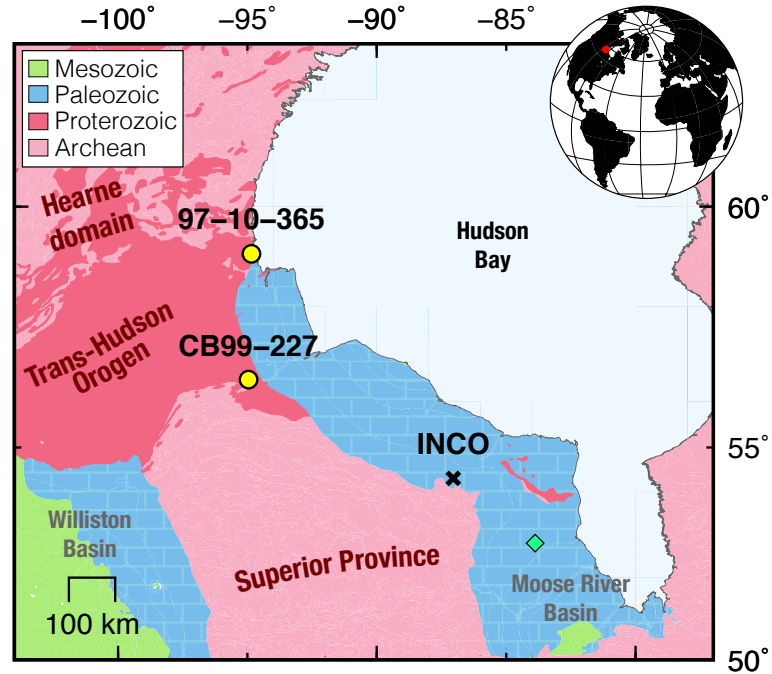


Figure 4: Simplified geologic map of the central Canadian Shield near Hudson Bay, modified from Wheeler et al. (1997). AFT sample locations are yellow points. Trans-Hudson Orogen (THO; c. 1.9–1.8 Ga) rocks are within the solid dark red area of the map. The Hudson Bay Basin Paleozoic section outcrops (blue) along the THO and W. Superior Province. Green diamond is location of the Attawapiskat kimberlite field. INCO is the borehole discussed in Galloway et al. (2012); refer to the text for discussion.

194 zoning on the etched grain surface easily detectable, and neither example showed evidence for strong zoning.
 195 One procedural difference for the data discussed here is that the AFT samples were split into two aliquots,
 196 and thus different grain mounts. The first aliquot was analysed using the typical, faster LA-ICPMS operation
 197 where track lengths are measured on all grains from which an age was measured and also other (undated)
 198 grains. Whereas, the second aliquots had track lengths measured *only* from grains that had ages measured.
 199 The latter approach is more time consuming, since all lengths within a count area are measured to avoid
 200 measurement bias—in this case resulting in a large number of collected track lengths due to the high N_s
 201 tracks present. The N_s counts alone for our two samples totalled nearly 26,800 and the number of measured
 202 track lengths was 1,365—for comparison, this is $\sim 10\text{--}100\times$ the amount of track/count data acquired with
 203 respect to a conventional AFT analysis.

204 Electron probe microanalysis (EPMA) was carried out using a single-spot per grain on the AFT mounts
 205 at Washington State University for the elements: Ca, P, F, Cl, Na, Mg, Mn, Fe, Sr, Y, La, Ce, S, and OH
 206 estimated by difference. The second AFT aliquots included Si and had two EPMA spots analysed, one near
 207 the LA pit, and the other located in a different area of the grain to assess potential compositional heterogeneity.
 208 Complete EPMA data are provided in the Supplementary Information (*SI*), and are summarized in Table
 209 1 and Table 2. Elemental analyses with wt% oxide totals are $98.8 \pm 1.8\%$ for 225 analyses (including

OH estimation) and suggest near endmember F-apatite for both samples with insignificant variation in composition. The few grains with low totals $< 97\%$ are flagged in the supplemental dataset and should be used with caution for any petrogenetic interpretation. The elemental data are combined into a single value, r_{mr0} , for approximating the annealing kinetics of the AFT data during inverse modeling. The r_{mr0} values were calculated using the Carlson et al. (1999) equation and apatite stoichiometric calculations for EPMA data from Ketcham (2015) and were converted to ‘effective Cl’ values (see McDannell and Issler, 2021 and Issler et al., 2021 for discussion). Effective Cl of 0.0 apfu is indicative of endmember fluorapatite and negative eCl indicates an extrapolation of the Carlson et al. (1999) r_{mr0} -Cl relation for r_{mr0} values > 0.84 .

The AFT central age for sample 97-10-365 is 512 ± 18 Ma (1σ , $n = 63$, age dispersion = 26%, $P(\chi^2) = 0.0$) and the central age for sample CB99-227 is 486 ± 22 Ma (1σ , $n = 50$, age dispersion = 30%, $P(\chi^2) = 0.0$). Sample 97-10-365 has an overall conventional mean track length of 12.01 ± 1.75 μm and c-axis projected mean length of 13.63 ± 1.02 μm ($n = 709$), whereas sample CB99-227 has a conventional mean track length of 11.81 ± 1.67 μm and c-axis projected mean length of 13.53 ± 0.94 μm ($n = 656$). The samples overlap in central age and mean track length at 1σ , which could qualitatively indicate a similar or shared thermal history given their proximity to one another. In spite of χ^2 failures for both samples, there is no clear indication of multiple kinetic age populations due to compositional variation. The samples exhibit high age scatter and a weak negative trend between single-grain age and uranium (i.e., $^{238}\text{U}/^{43}\text{Ca}$ ratio), apparently indicative of ‘radiation-enhanced annealing’ (REA) encountered in AFT data from Precambrian rocks (Hendriks and Redfield, 2006; McDannell et al., 2019a). While recent laboratory experiments confirm REA is a real phenomenon, it is evidently not a concern for apatite (Li et al., 2021). Outstanding questions relate to how and if time plays a role in this process with respect to radiation damage and fission-track accumulation for ancient apatites, or if over long timescales, accumulated alpha-radiation damage lowers thermal annealing resistance (Ketcham, 2019; McDannell et al., 2019a). Here the data were interpreted as overdispersed single populations. High dispersion is likely attributable to a continuous distribution of ages rather than the typically assumed discrete age components (Vermeesch, 2019)—which may be at least partially due to the protracted slow cooling (and differential annealing) these samples experienced, the greater number of analyses relative to conventional AFT of ≤ 20 age grains, and higher relative LA-ICPMS age precision (Ketcham et al., 2018; Vermeesch, 2019; McDannell, 2020).

6. Canadian Shield time-temperature inversions

We examined the ability of the AFTSS data to resolve the shield thermal history and QTQt model results are shown in Figure 5 as heat maps of t - T path density, where brighter colors are higher relative posterior

Table 2: Apatite fission-track data for sample CB99-227, Trans-Hudson Orogen.

N_s	Area (Ω_i) (cm^2)	$^{238}\text{U}/^{43}\text{Ca}$	1σ	$P_i\Omega_i$	$\sigma P_i^2\Omega_i^2$	AFT age † (Ma)	1σ (Ma)	D_{par} (μm)	F* (apfu)	Cl* (apfu)	OH* (apfu)	r_{mr0} 1999	eCl (A) (apfu)	eCl (B) (apfu)	U-Pb ‡ age (Ma)	2σ (Ma)	aliquot grain
461	5.82E-05	1.33E-01	2.97E-03	7.77E-06	2.98E-14	473	26	2.09	1.65	0.01	0.34	0.848	-0.022	-	1526	208	a1-1
175	3.88E-05	4.07E-02	2.14E-03	1.58E-06	6.88E-15	856	80	1.91	1.55	0.01	0.44	0.838	0.008	-	1471	319	a1-2
367	5.82E-05	8.80E-02	1.97E-03	5.12E-06	1.32E-14	567	34	2.16	-	-	-	-	-	-	1581	221	a1-3
131	2.91E-05	7.94E-02	1.85E-03	2.31E-06	2.91E-15	452	42	2.16	1.69	0.01	0.30	0.848	-0.025	-	1559	152	a1-4
257	9.71E-05	3.00E-02	6.97E-04	2.91E-06	4.57E-15	692	48	2.16	1.61	0.01	0.38	0.843	-0.009	-	1621	293	a1-5
241	5.82E-05	6.46E-02	1.74E-03	3.76E-06	1.02E-14	509	37	2.20	1.53	0.01	0.46	0.841	-0.001	-	1572	213	a1-6
72	3.88E-05	2.42E-02	5.89E-04	9.38E-07	5.23E-16	606	74	2.12	1.53	0.01	0.46	0.837	0.011	-	1605	301	a1-7
211	4.85E-05	3.83E-02	8.69E-04	1.86E-06	1.78E-15	878	65	1.59	1.74	0.01	0.25	0.851	-0.033	-	1541	219	a1-8
103	4.85E-05	2.99E-02	7.08E-04	1.45E-06	1.18E-15	562	58	2.10	1.50	0.01	0.49	0.835	0.016	-	1582	323	a1-9
197	5.82E-05	3.77E-02	9.32E-04	2.20E-06	2.95E-15	703	54	2.25	1.67	0.02	0.31	0.838	0.007	-	1528	281	a1-10
71	3.88E-05	1.98E-02	7.41E-04	7.70E-07	8.27E-16	721	91	1.80	1.59	0.01	0.39	0.837	0.011	-	1433	566	a1-11
438	5.82E-05	9.98E-02	3.01E-03	5.81E-06	3.08E-14	595	35	1.89	1.59	0.01	0.39	0.833	0.022	-	1516	261	a1-12
153	4.37E-05	5.64E-02	1.22E-03	2.46E-06	2.83E-15	494	42	2.22	1.64	0.01	0.35	0.846	-0.019	-	1596	219	a1-13
334	6.21E-05	5.62E-02	1.37E-03	3.49E-06	7.22E-15	746	46	2.07	1.73	0.01	0.26	0.851	-0.034	-	1541	234	a1-14
343	7.77E-05	3.51E-02	1.24E-03	2.73E-06	9.29E-15	965	64	2.22	1.64	0.01	0.35	0.847	-0.021	-	1485	374	a1-15
615	5.82E-05	2.29E-01	4.70E-03	1.34E-05	7.51E-14	370	18	1.64	1.53	0.01	0.47	0.836	0.013	0.026	1722	285	a2-1
714	5.82E-05	2.18E-01	4.38E-03	1.27E-05	6.51E-14	449	21	1.70	1.43	0.01	0.56	0.834	0.018	0.025	1661	219	a2-2
103	3.98E-05	3.87E-02	6.06E-03	1.54E-06	5.82E-14	530	99	2.16	1.60	0.01	0.39	0.837	0.010	-	-	-	a2-3
218	9.71E-05	8.79E-02	3.06E-03	8.53E-06	8.80E-14	208	16	1.74	1.45	0.01	0.54	0.837	0.010	0.036	-	-	a2-4
114	4.37E-05	4.08E-02	1.90E-03	1.78E-06	6.91E-15	509	54	1.43	1.59	0.01	0.41	0.835	0.015	-0.023	-	-	a2-5
118	9.71E-05	2.15E-02	1.73E-03	2.09E-06	2.82E-14	452	56	1.54	1.51	0.01	0.48	0.839	0.003	0.013	-	-	a2-6
138	5.82E-05	4.77E-02	9.40E-04	2.78E-06	3.00E-15	399	35	1.63	1.60	0.01	0.40	0.835	0.017	-0.021	1626	478	a2-7
80	4.37E-05	3.91E-02	8.71E-03	1.71E-06	1.45E-13	376	94	1.41	-	-	-	-	-	-	-	-	a2-8
145	4.85E-05	2.88E-02	7.38E-04	1.40E-06	1.28E-15	806	71	1.49	1.55	0.00	0.45	0.842	-0.006	0.001	1631	607	a2-9
384	2.91E-05	3.37E-01	6.10E-03	9.81E-06	3.15E-14	316	18	1.68	1.57	0.01	0.42	0.837	0.009	0.025	1593	195	a2-10
472	4.85E-05	1.95E-01	3.91E-03	9.47E-06	3.61E-14	400	21	1.79	1.45	0.01	0.55	0.832	0.024	0.016	1635	232	a2-11
294	6.79E-05	5.78E-02	1.41E-03	3.92E-06	9.20E-15	592	39	2.16	1.52	0.02	0.46	0.833	0.020	0.028	1624	426	a2-12
440	4.85E-05	1.67E-01	3.35E-03	8.11E-06	2.65E-14	434	24	1.89	1.52	0.02	0.46	0.833	0.022	0.017	1615	289	a2-13
128	4.85E-05	4.35E-02	1.25E-03	2.11E-06	3.67E-15	483	46	1.89	1.69	0.01	0.30	0.849	-0.026	0.010	1560	421	a2-14
324	9.71E-05	5.34E-02	1.42E-03	5.19E-06	1.89E-14	497	32	1.87	1.68	0.01	0.31	0.848	-0.022	0.017	1547	661	a2-15
119	4.85E-05	3.60E-02	1.23E-03	1.75E-06	3.57E-15	541	54	1.64	-	-	-	-	-	-	1548	535	a2-16
404	4.85E-05	1.25E-01	3.01E-03	6.05E-06	2.14E-14	530	31	1.71	1.49	0.01	0.50	0.841	-0.001	-0.022	1473	324	a2-17
195	5.82E-05	6.32E-02	1.57E-03	3.68E-06	8.35E-15	424	33	1.71	1.61	0.01	0.38	0.837	0.011	-0.003	1641	418	a2-18
234	4.85E-05	6.93E-02	2.43E-03	3.37E-06	1.39E-14	551	42	1.72	1.51	0.02	0.48	0.831	0.028	0.018	-	-	a2-19
242	5.82E-05	7.26E-02	2.72E-03	4.23E-06	2.50E-14	457	35	1.65	1.52	0.01	0.46	0.836	0.012	-0.013	-	-	a2-20
203	2.91E-05	1.50E-01	7.94E-03	4.37E-06	5.35E-14	373	33	1.77	1.52	0.01	0.47	0.834	0.018	0.008	-	-	a2-21
140	3.88E-05	5.66E-02	2.68E-03	2.20E-06	1.08E-14	507	50	1.60	1.57	0.01	0.43	0.837	0.011	0.006	-	-	a2-22
555	5.82E-05	1.55E-01	4.73E-03	9.05E-06	7.59E-14	488	27	2.03	1.58	0.01	0.42	0.845	-0.016	0.003	-	-	a2-23
129	4.85E-05	4.29E-02	1.45E-03	2.08E-06	4.96E-15	493	47	1.56	1.60	0.01	0.39	0.839	0.005	-0.001	-	-	a2-24
84	4.85E-05	1.98E-02	1.35E-03	9.59E-07	4.30E-15	687	89	1.72	1.57	0.01	0.42	0.838	0.008	0.045	-	-	a2-25
300	4.85E-05	1.70E-01	3.69E-03	8.23E-06	3.21E-14	295	19	1.77	1.56	0.01	0.43	0.843	-0.009	0.009	-	-	a2-26
316	4.85E-05	9.24E-02	2.09E-03	4.49E-06	1.03E-14	558	35	1.73	1.46	0.01	0.53	0.839	0.004	-0.001	1637	292	a2-27
222	5.82E-05	1.02E-01	2.14E-03	5.95E-06	1.56E-14	301	22	1.47	1.72	0.00	0.28	0.840	0.000	-0.029	-	-	a2-28
238	2.91E-05	2.18E-01	4.37E-03	6.34E-06	1.62E-14	303	21	2.11	1.58	0.01	0.42	0.842	-0.004	0.038	1665	221	a2-29
63	3.88E-05	3.33E-02	1.76E-03	1.29E-06	4.69E-15	391	54	1.43	1.71	0.01	0.28	0.843	-0.009	-0.041	-	-	a2-30
195	4.85E-05	8.53E-02	2.19E-03	4.14E-06	1.13E-14	378	29	2.17	1.47	0.01	0.52	0.835	0.015	-0.013	1736	430	a2-31
248	4.85E-05	7.39E-02	1.99E-03	3.59E-06	9.34E-15	548	39	1.51	1.47	0.01	0.52	0.836	0.011	0.001	1546	396	a2-32
290	5.82E-05	1.22E-01	3.49E-03	7.09E-06	4.14E-14	330	22	1.72	1.62	0.02	0.36	0.840	-0.001	0.007	1504	250	a2-33
98	2.91E-05	6.77E-02	2.12E-03	1.97E-06	3.80E-15	399	43	1.66	1.95	0.01	0.04	0.856	-0.048	0.030	1614	279	a2-34
328	3.88E-05	2.15E-01	5.78E-03	8.34E-06	5.04E-14	317	20	1.92	1.51	0.01	0.48	0.839	0.003	-0.001	1753	304	a2-35
12444	2.63E-03			2.19E-04	1.14E-12	486	22	1.83	1.58	0.01	0.41	0.838	0.001	0.007	1585	46	

N_s = spontaneous track count; Ω_i = track count area; P_i = down-pit weighted $^{238}\text{U}/^{43}\text{Ca}$ ratio

† AFT single-grain ages are calculated using the LA-ICPMS (ζ -calibration) method with modified $\zeta = 8.2727$, standard error (ζ) = 0.1407 and ^{238}U total decay constant of $1.55125 \times 10^{-10} \text{ yr}^{-1}$. Bottom table row (bold) displays the analysis sums, AFT central age $\pm 1\sigma$ error, and the mean values for the tabulated elements/kinetic parameters.

*Average values reported for F, Cl, OH, D_{par} , and effective Cl (eCl) in bottom row, median value shown for r_{mr0} ; Individual grain D_{par} values are the mean of 4 measurements. Aliquot 2 had two EPMA probe spots, one near the AFT laser ablation pit and another elsewhere on the grain to assess compositional heterogeneity. Only elemental data for spot A are reported here for aliquot 2. Average wt % oxide total for aliquot 2 replicates is $99.6 \pm 1.2\%$; median = 99.7% ($n = 65$).

‡ Individual U-Pb dates are common Pb-corrected isotopic sums. Summary U-Pb date of 1585 ± 46 Ma in the table is the simple weighted mean of individual dates (2σ , $n = 35/35$, MSWD = 0.22, $P(\chi^2) = 1$). The weighted mean $^{207}\text{Pb}/^{206}\text{Pb}$ date calculated in IsoplotR (Vermeesch, 2018) using $^{238}\text{U}/^{206}\text{Pb}$ and $^{207}\text{Pb}/^{206}\text{Pb}$ isotopic ratios is 1603 ± 72 Ma (2σ , $n = 35/35$, MSWD = 0.13, $P(\chi^2) = 1$).

241 probability. The ‘unconstrained’ model does not include t - T constraints. The geologic information being
242 evaluated includes two distinct times in the past that we can reasonably assume basement was at near-surface
243 conditions (15 ± 15 °C) based on the regional geologic information discussed in Section 4.2. This information
244 was subsequently added to the model as constraint boxes, namely at: (i) 450 ± 10 Ma and (ii) 175 ± 25 Ma².

245 We refrain here from showing the individual maximum likelihood, maximum posterior, maximum mode,
246 or expected model paths (Gallagher, 2012), so as not to draw undue attention to a single t - T path since
247 they are single models or a representative summary for a broader range of solutions (i.e., mode or expected
248 model). Those models can be found in the *SI* or refer to the data repository for QTQt output (McDannell,
249 2022). We focus on the entire stationary distribution of paths, particularly the ‘unconstrained’ model without
250 t - T constraint boxes shown in Figure 5A and D. These examples reflect the ability of the AFTSS data to
251 solely resolve both the thermal history and the necessary minimum level of complexity to adequately explain
252 the data. Note that this does not mean that the true thermal history may not be more complex. Rather,
253 any additional complexity (that does not compromise fitting the data) is not actually required by the data
254 and so needs to be justified independently. The distributions for AFT age and mean track length for the
255 accepted (post burn-in) models are essentially the same for every model for each sample (*SI*, Fig. S2). The
256 fits to the observed track length distributions are also shown in the *SI* (Fig. S3). We note that the AFT
257 age is reproduced at the margin of acceptability at the -2σ level for all examples, whereas the mean track
258 length is well determined. This remained true throughout model trials with a larger general t - T prior and
259 the addition of constraint boxes at high temperatures. We conclude that the high number of track length
260 measurements dominate the (log) likelihood values and thus exert more influence on the inversion results.

261 7. Discussion

262 7.1. Burial and erosion history interpretations

263 For both samples, nearly identical Phanerozoic thermal histories are recovered without enforcing geologic
264 constraints—yet both models independently corroborate the known cratonic geology by requiring two reheating
265 events. Given the imposition of simple models, the time-temperature paths also indirectly need periods
266 at low temperatures in the mid Mesozoic to produce a heating event. Thus, the thermal histories suggest
267 similar, albeit poorly resolved surface conditions in the late Precambrian to early Paleozoic (Fig. 5). The low
268 temperatures are required to form a population of tracks that are then shortened by reheating to produce the
269 observed lengths—without this, a certain component of lengths cannot be generated that are needed to fit

²Placement of a Miocene surface constraint at 14 ± 9 Ma did not significantly change the results when compared to the ‘unconstrained’ or ‘Ordovician/Jurassic box’ models, and was therefore excluded for simplicity. The AFT data independently allow cooling to near-surface temperatures by Miocene time.

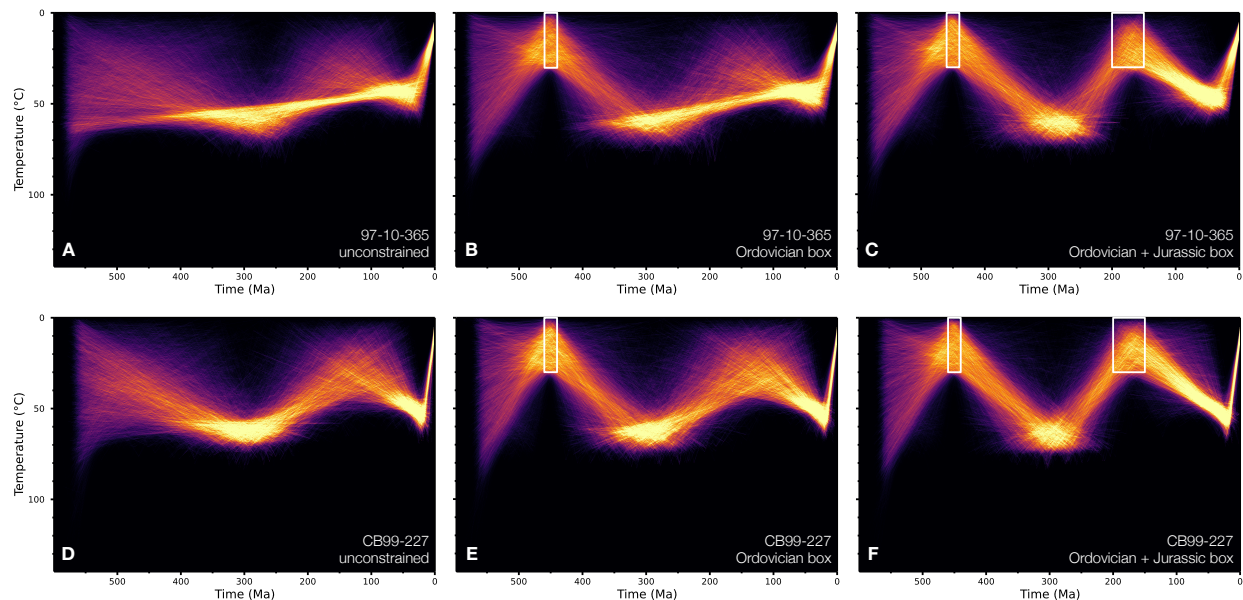


Figure 5: QTQt time-temperature simulations shown as path density heat maps resolved to a pixel size of 1 My and 1 °C. Relative probability is proportional to path density, where brighter colors (or higher saturation) indicate more thermal histories pass through that region. More complex t - T paths were rejected in QTQt for equivalent likelihood. (A–C) models results for sample 97-10-365. (D–F) model results for sample CB99-227. Geologic constraint boxes (white) represent Ordovician and Jurassic unconformities discussed in Section 4.2. A notable result is that the general features of the two-peak thermal history are visible in the unconstrained models. The high-quality track length data resolved the heating events and the t - T solutions independently support the regional geologic information. The ‘unconstrained’ model in panel A clearly illustrates the penalization of more complex histories due to more simple, ‘linear’ paths being accepted or retained preferentially between the two thermal peaks. All QTQt models are available in McDannell (2022).

270 the observations. It may be that time or duration at higher temperatures become increasingly important over
 271 long timescales, which we can similarly observe in Figure 3 where maximum temperatures are slightly lower
 272 than the true peak and a subset of paths remain nearly isothermal, therefore producing similar amounts of
 273 annealing as the true history with high maximum temperatures for a geologically instantaneous duration.
 274 The AFTSS models best resolve a broad thermal peak between approximately latest Devonian to Triassic
 275 (*c.* 360 to 240 Ma) for both samples that is consistent for all simulations (Fig. 5; albeit more defined
 276 in panels C and F). The timing of maximum temperature is poorly constrained due to the low degree of
 277 thermal annealing within the PAZ for these apatites and also partially reflects the trade-off between t - T
 278 path inflections (i.e., uncertainty on the times at hotter vs. cooler temperatures; Fig. 5A–B, D–E) and the
 279 allowable heating-cooling rates imposed on the solutions. Step-wise addition of the Ordovician and Jurassic
 280 constraint boxes (Fig. 5B–C and E–F) refine the overall history results and the requirement of two heating
 281 events by the AFTSS data suggest maximum (burial) heating to ~ 70 – 75°C occurred at *c.* 300 Ma. The
 282 timing of maximum temperature at 300 Ma is provocative because it lends support for the deposition of
 283 Pennsylvanian strata on the Hudson platform, which was controversially posed by Tillement et al. (1976).
 284 The Michigan and Williston basins also contain a few hundred meters of Pennsylvanian and Jurassic strata
 285 (e.g., Burrus et al., 1996; Burgess, 2019), perhaps suggesting a regionally common history for interior North

286 America. The final cooling event in the model takes place in the Oligocene-Miocene. The White River Group
287 (< 38 Ma) provides geological support for this as it records the last burial event during the Paleogene in the
288 Williston Basin, which was followed by Miocene erosion (Burrus et al., 1996). These model thermal histories
289 are significant because they further establish that burial extended across the currently exposed basement of
290 the Canadian Shield, that the Hudson Bay sedimentary succession is an erosional remnant (Pinet et al., 2013;
291 McDannell et al., 2021), and the Hudson Bay and Williston basins were probably intermittently connected.

292 In summary, model results indicate $\sim 2\text{--}3$ km of Paleozoic burial followed by erosion until the Jurassic
293 (assuming a 10°C surface temperature and $20\text{--}30^\circ\text{C}/\text{km}$ paleo-geothermal gradient). The Mesozoic-Cenozoic
294 history is characterized by inferred $\sim 1.5\text{--}2.5$ km of burial during the Cretaceous to Oligocene-Miocene, and
295 subsequent erosion (with climatic cooling?) until present day. While speculative, the timing of late cooling
296 approximately aligns with climate change and the growth of the Antarctic ice sheet, including ephemeral
297 northern hemisphere Oligocene-Miocene continental glaciation (Tripathi and Darby, 2018, and refs. therein).

298 *7.2. Modeling fission-track length distributions*

299 The inferred complexity of a thermal history is related to the number of track lengths (Fig. 3). Our
300 simulations clearly show that our AFTSS data have enough lengths to independently require two thermal
301 events (i.e., without requiring $t\text{--}T$ boxes) during the Phanerozoic for the exposed Precambrian basement of
302 the central Canadian Shield—but adding the constraints improves the resolution on the timing of maximum
303 temperatures. However, it seems clear that 100 measured tracks for a single kinetic AFT population are not
304 enough to resolve complicated deep-time thermal histories without applying interpretation-based constraints
305 (e.g., McDannell et al., 2021; McDannell and Issler, 2021). To further explore this with the real data, we
306 took the entire length dataset for each AFT example and randomly downsampled it using a simple Monte
307 Carlo method, retaining $\sim 10\%$, $\sim 20\%$, and $\sim 50\%$ of the original length distributions, while maintaining
308 a stable mean length within uncertainty (Fig. 6). This was done to determine how well we resolve the
309 two thermal peaks in the full model $t\text{--}T$ history from Figure 5A and D with a reduced number of length
310 measurements. This essentially simulates what a real AFT analysis would be like if fewer measurements were
311 collected. Each resampled distribution was modelled in QTQt, while keeping the AFT age information fixed
312 to assess how resampling of the total number of track lengths affected the model resolution. The results (Fig.
313 7) indicate that there is an inadequate amount of track length data in a typical AFT analysis (100 lengths)
314 to fully or independently resolve a complex cratonic thermal history involving minor annealing in response
315 to temperatures equivalent to the lower temperature end of the PAZ. A notable feature of the 97-10-365
316 models is that the timing of the last cooling event is poorly resolved (Fig. 7A) and is shifted ‘younger’ but
317 becomes better defined with the progressive inclusion of more track length data (Fig. 7B–C). The track

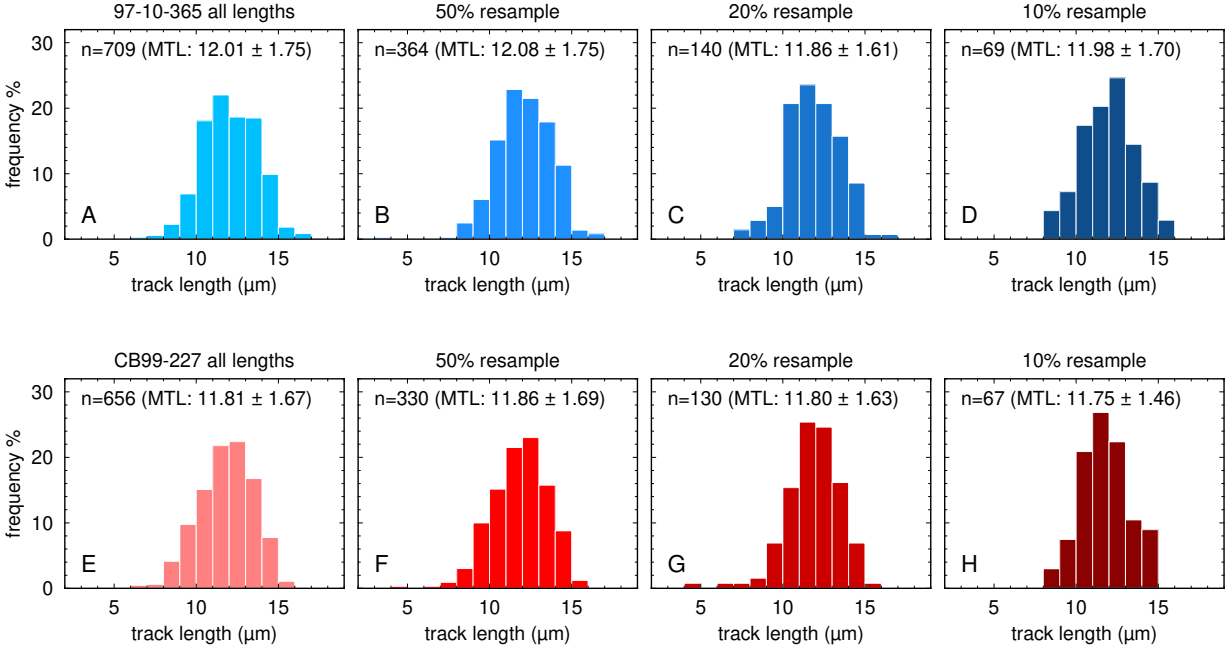


Figure 6: Conventional (i.e., unprojected) track length distributions for the AFTSS as histograms with 1 μm bins. Track lengths are displayed as they were originally measured but were modelled using c -axis angles (see below). (A) all 709 track lengths combined from both sample aliquots of 97-10-365 with a conventional mean track length of $12.01 \pm 1.75 \mu\text{m}$ and c -axis projected mean length of $13.63 \pm 1.02 \mu\text{m}$. (B) random 50% downsampling or resampling of the total lengths in panel A. (C) random 20% resampling of the total lengths in panel A. (D) random 10% resampling of the total lengths in panel A. Sample CB99-227 (E–H) is the same as panels A–D with a conventional mean track length of $11.81 \pm 1.67 \mu\text{m}$ and c -axis projected mean length of $13.53 \pm 0.94 \mu\text{m}$. All distributions in panels B–D and F–H are similar in form to the ones in A and E, respectively. MTL = mean track length.

318 resampling exercise (Fig. 6) implies that more short/intermediate lengths and overall broadening of the track
 319 distribution are required (absent in the low n models) to better resolve the timing of recent cooling. This
 320 pattern broadly aligns with the results in Figure 2. The timing of cooling to surface conditions agrees with
 321 the occurrence of Miocene strata in the INCO borehole (Galloway et al., 2012; Fig. 4). In this particular
 322 instance, we have geologic information to empirically validate our model, whereas in more frontier regions
 323 where less Phanerozoic strata are known or preserved, a t - T model such as this may be more difficult to
 324 justify or be considered an artifact. To that end, AFTSS data may be extremely valuable for inferring and
 325 resolving the timing of unrecognized or poorly recorded geologic events on cratons.

326 The results of our modeling emphasize that amount of track length data is possibly too low in many
 327 cratonic t - T modeling applications and that inadequate characterization of length distributions may affect
 328 our ability to recover thermal history information. While this is not conceptually novel—what constitutes a
 329 robust track length dataset and if those data can independently support geologic observations has gone mostly
 330 unrecognized. While the mean track length is often a useful summary statistic, it is the width and shape of
 331 the track length distribution that are critical for modeling (Crowley, 1985; Gleadow et al., 1986). The main
 332 body of the distribution needs to be well defined with many tracks, but the tails of the true distribution also
 333 need to be well represented. Namely, any shorter lengths that provide key temperature information must

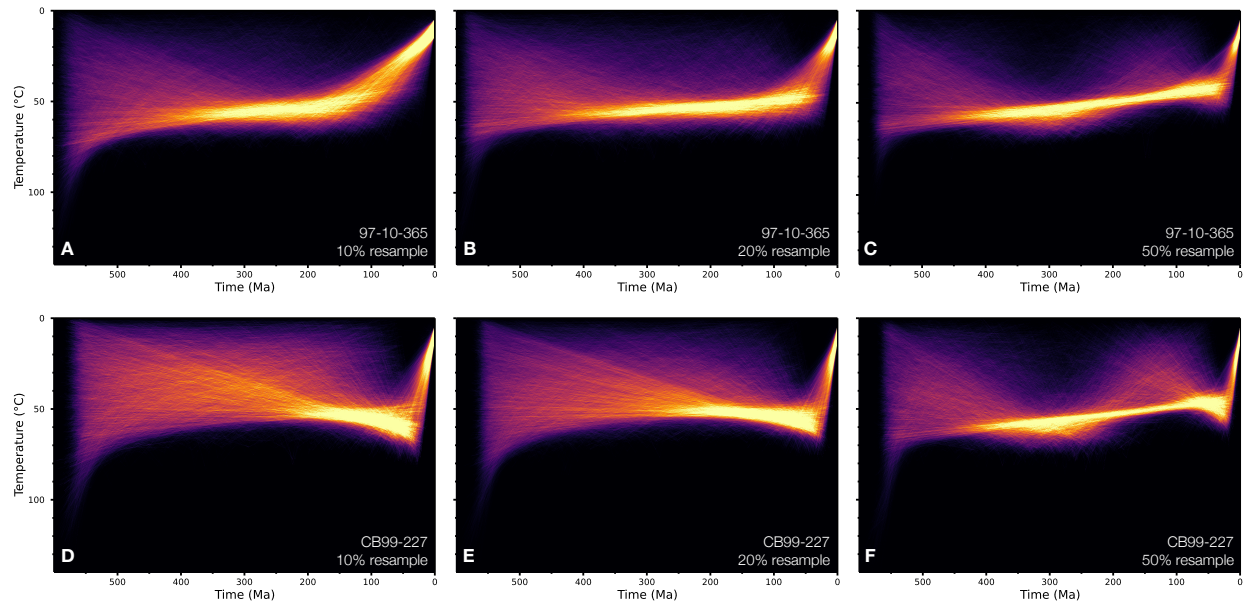


Figure 7: QTQt time-temperature simulations shown as path density heat maps. All other figure attributes and model run conditions are the same as Figure 5. (A–C) models results for 69, 140, and 364 randomly resampled track lengths for sample 97-10-365. (D–F) model results for 67, 130, and 330 randomly resampled track lengths for sample CB99-227. The two-peak history is not resolved until > 250–300 tracks are utilized during modeling. Models for 30% and 40% track resampling not shown for simplicity.

334 be included, which will typically require more measurements because they have a lower probability both
 335 of being observed and measured accurately (Laslett et al., 1982). C-axis angle projection of track lengths
 336 also plays a role in improving resolution by reducing length dispersion due to track orientation (Donelick
 337 et al., 1999), yielding a better defined length distribution (Ketcham et al., 2018; Ketcham, 2019)—thereby
 338 taking advantage of the extra information contained in the annealing dependence on track orientation. If the
 339 distribution shape is well characterized then the thermal model can deconvolve the mixed length components
 340 generated by the different heating-cooling cycles.

341 In detail, many different thermal histories can satisfy a given track length distribution. However, even if
 342 the distribution looks similar between an example with many tracks and fewer tracks, the possibility to resolve
 343 multiple heating-cooling events in a history is reduced in the latter case. A good example of this is apparent
 344 in the downsampling results shown in Figure 6. Here the increased number of tracks tends to broaden the
 345 overall distribution, implying (or requiring) greater history complexity—which is then verified in the Figure
 346 7 inversion results. The same limitations can apply to different forms of thermal histories as reflected for
 347 the example shown in Figure 1. The real slow-cooling history may be misinterpreted as rapid and/or recent
 348 cooling if the skewed distribution (Fig. 1C) were undersampled such that shorter lengths were not measured.
 349 The same generally applies to the broad distribution (Fig. 1D) if there are not enough intermediate (~ 12 – 13
 350 μm) and/or long (~ 15 – 16 μm) c-axis projected lengths collated to distinguish between a narrow or wide
 351 unimodal track population. In addition, the synthetic AFT inversions (Fig. 3) suggest to us that exploratory

352 forward modeling potentially offers a means to practically estimate the number of track lengths required for
353 a robust AFT analysis if a ‘schematic’ burial history can be surmised from the regional geology or other data.
354 However, it should be noted that if old cratonic AFT samples are thermally reset ($> 120^{\circ}\text{C}$; depending upon
355 apatite composition) at any time during the Phanerozoic—then the additional t - T information normally
356 provided by an AFTSS analysis will diminish in relation to the timing of the resetting event (i.e., a thermal
357 pulse late in the history will tend to erase or at least reduce the information provided by additional lengths).
358 The examples and model results presented here demonstrate that a *minimum* of ~ 250 – 300 confined length
359 measurements are required for robust thermal history recovery for single-age population samples in cratonic
360 regions where rocks experienced modest thermal annealing over the past 500–600 million years.

361 8. Conclusions

362 Studies of cratons have shown that they are typically characterized by long duration and episodic thermal
363 histories involving low to moderate degrees of thermal annealing from sedimentary burial. Apatite fission-track
364 dating has traditionally been a preferred method for constraining aspects of these complex burial and erosion
365 events. However, due to the absence of physical geologic constraints, detailed thermal history reconstruction
366 is often difficult. This issue leads to a thermal history modeling approach that incorporates interpretive
367 assumptions about the geologic history that may be invalid or at least difficult to validate independently.
368 New apatite fission-track data were presented from the central Canadian Shield that included many more
369 confined track-length measurements than a typical fission-track analysis. Inversions of these data yield results
370 that are consistent with the regional shield geology without requiring the imposition of t - T ‘constraint boxes’.
371 Subsequently, consideration of known geologic constraints with either forward or inverse modeling approaches
372 allows an assessment of the impact of constraints relative to the unconstrained thermal histories. While the
373 appropriate number of tracks lengths to collect is a function of the thermal history, our results demonstrate
374 that the conventional approach of measuring around 100 track lengths may be inadequate for long duration
375 (500–1000 My) thermal history scenarios involving a higher level of history complexity and/or episodic minor
376 annealing. Ultimately, each problem is unique and analyses should be tailored to optimize the amount of
377 information available for modeling since a standardized approach may not yield sufficient data to clearly
378 resolve significant thermal events. We suggest that 250–300 confined track lengths (with c-axis angles) may
379 be considered an effective minimum—suitable for thermal history inversion in cratonic settings for rocks that
380 contain a single kinetic population and have experienced low-to-moderate thermal annealing. This simple
381 change in analytical protocol may improve thermal history recovery and lend more credence to geologic
382 interpretations in slowly cooled continental interiors.

383 9. Author Contributions

384 CRediT author statement. **K. McDannell:** Conceptualization, Investigation, Methodology, Formal
385 analysis, Visualization, Funding acquisition, Writing - original draft; **P. O'Sullivan:** Formal analysis,
386 Methodology, Resources; **K. Gallagher:** Conceptualization, Validation, Writing - Review & Editing; **S.**
387 **Boroughs:** Formal analysis, Methodology, Resources

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394 11. Data Availability

395 Fission track data, electron microprobe data, and QTQt models are available from the Open Science
396 Framework (OSF) repository: <https://osf.io/73u8j/>

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