

This is a pre-copyedited, author-produced PDF of an article accepted for publication in *Geophys. J. Int.* following peer review. The version of record “Takemura, S., Yabe, S., & Emoto, K., “Modelling high-frequency seismograms at ocean bottom seismometer: effects of heterogeneous structures on source parameter estimation for small offshore earthquakes and shallow low-frequency tremors” is available online at <http://dx.doi.org/10.1093/gji/ggaa404>.
https://academic.oup.com/journals/pages/self_archiving_policy_p

1 **Modelling high-frequency seismograms at ocean bottom seismometers:**
2 **effects of heterogeneous structures on source parameter estimation for**
3 **small offshore earthquakes and shallow low-frequency tremors**

4
5 **Authors**

6 **Shunsuke TAKEMURA^{1*}, Suguru YABE², Kentaro EMOTO³**

7 ¹Earthquake Research Institute, the University of Tokyo, 1-1-1 Yayoi, Bunkyo-ku,
8 Tokyo 113-0032, Japan

9 ²Geological Survey of Japan, National Institute of Advanced Industrial Science and
10 Technology, Tsukuba Central 7, 1-1-1 Higashi, Tsukuba, Ibaraki 305-8567, Japan

11 ³Geophysics, Graduate School of Science, Tohoku University, 6-3, Aramaki-aza-
12 aoba, Aoba-ku, Sendai 980-8578, Japan

13
14 **Running Title**

15 Modelling HF seismograms at OBSs

16 **Corresponding Author**

17 Shunsuke Takemura

18 E-mail: shunsuke@eri.u-tokyo.ac.jp

19 Phone: +81 3-5841-5689

20

21 **Summary**

22 The source characteristics of offshore seismic events, especially regular (or fast) and slow
23 earthquakes, can provide key information on their source physics and frictional conditions at
24 the plate boundary. Due to strong three-dimensional heterogeneities in offshore regions, such
25 as those relating to seawater, accretionary prism, and small-scale velocity heterogeneity,
26 conventional methods using a one-dimensional Earth model may misestimate source
27 parameters such as the duration and radiation energy. Estimations could become severe
28 inaccuracies for small offshore seismic events because high-frequency (> 1 Hz) seismograms,
29 which are strongly affected by three-dimensional heterogeneities, are only available for
30 analysis because of their signal-to-noise ratio. To investigate the effects of offshore
31 heterogeneities on source parameter estimation for small seismic events, we analysed both
32 observed and simulated high-frequency seismograms southeast off the Kii Peninsula, Japan,
33 in the Nankai subduction zone. Numerical simulations of seismic wave propagation using a
34 three-dimensional velocity structure model clarified the effects of each heterogeneity.
35 Comparisons between observations and model simulations demonstrated that the thick low-
36 velocity accretionary prism has significant effects on high-frequency seismic wave
37 propagation. Especially for shallow low-frequency tremors occurring at depths just below the
38 accretionary prism toe, seismogram durations are significantly broader than an assumed
39 source duration, even for stations with epicentral distances of approximately 10 km. Spindle-
40 shape seismogram envelopes were observed even at such close stations. Our results suggest
41 that incorporating three-dimensional heterogeneities is necessary for practical estimation of
42 source parameters for small offshore events.

43 **Keywords:**

44 Computational seismology, earthquake ground motions, earthquake source observations,
45 seismicity and tectonics, wave propagation, wave scattering and diffraction

46

47 **1. Introduction**

48 To understand the physics and characteristics of earthquake sources, seismologists analyse
49 observed seismograms around the world. Following the correction of the frequency responses
50 of seismometers and local site effects at each station, the observed seismograms provide
51 information on the source rupture complexity and heterogeneous structures along each
52 propagation path. For centroid moment tensor (CMT) inversion for teleseismic events or
53 local crustal earthquakes using low-frequency (< 0.1 Hz) seismograms, path effects are
54 typically evaluated by assuming a simple one-dimensional (1D) Earth model (e.g., Ekström et
55 al., 2012; Kanamori & Rivera, 2008; Nakano et al., 2008) because low-frequency seismic
56 waves are usually considered insensitive to structural heterogeneities. Given the recent
57 developments in computer resources and three-dimensional (3D) subsurface structure models,
58 CMT inversions using 3D velocity models have been practically conducted for not only
59 crustal, but also offshore earthquakes (e.g., Hejrani et al. 2017; Takemura, Okuwaki, et al.
60 2020; Wang & Zhan 2020). The 3D heterogeneities in the offshore regions, such as seawater,
61 accretionary prism, and small-scale velocity heterogeneity, are developed just beneath the
62 epicentre regions of offshore subduction zone earthquakes. Thus, the 3D CMT method better
63 constrains earthquake source characteristics compared to the 1D method, especially for
64 offshore earthquakes.

65 Moment tensor inversion is only applicable to moderate-to-large earthquakes because of
66 the signal-to-noise ratios of coherent low-frequency seismic signals. Thus, small events, such
67 as microearthquakes or tectonic and volcanic tremors, are usually evaluated via methods
68 based on the amplitudes or energies of high-frequency (> 1 Hz) seismic waves (e.g., Fletcher
69 & McGarr, 2011; Gusev & Pavlov, 1991; Maeda & Obara, 2009; Nakahara, 2008; Poiata et
70 al., 2018; Sawazaki & Enescu, 2014; Staudenmaier et al., 2016). The precise evaluation of
71 small events is important for not only understanding source physics (e.g., Ellsworth & Bulut,
72 2018; Gomberg et al., 2016; Hawthorne et al., 2019; Ide et al., 2003; Supino et al., 2020;
73 Thomas et al., 2016; Uchide & Ide, 2010), but also for monitoring crustal and volcanic
74 activities (e.g., Battaglia & Aki, 2003; Kato et al., 2012; Kumagai et al., 2013; Kurokawa et
75 al., 2016; Peng & Zhao, 2009; Yabe & Ide, 2014). The characteristics of high-frequency
76 seismic waves, and related small-scale structural properties in onshore regions, have been
77 widely investigated by numerical, theoretical, and observational approaches (e.g., Carcolé &
78 Sato 2010; Chaput et al. 2015; Margerin 2005; Morioka et al. 2017; Saito et al. 2002;
79 Takahashi et al. 2009; Takemura et al. 2016, 2017; Wegler et al. 2006). Consequently, the

80 estimated location and energy for onshore small seismic events are generally robust even
81 with 1D conventional methods.

82 Due to long distances between onshore stations and offshore seismic sources, the source
83 parameters of small offshore seismic events cannot be precisely determined from onshore
84 seismic stations. Thus, temporal observations of ocean bottom seismometers (OBSs) have
85 been extensively carried out. Around the Japanese Islands, permanent OBS networks of
86 DONET and S-net (National Research Institute for Earth Science and Disaster Resilience,
87 2019c, 2019a) have been recently deployed. Several studies have used temporal OBS data or
88 such permanent networks to estimate the source characteristics of small earthquakes and
89 shallow low-frequency tremors (LFTs) (e.g., Nakano et al., 2015, 2019; Nishikawa et al.,
90 2019; Tamaribuchi et al., 2019; Tanaka et al., 2019; Yabe et al., 2019). Offshore 3D
91 heterogeneities, seawater, and bathymetry significantly affect seismic wave propagation even
92 for low-frequency ground motions (e.g., Gomberg 2018; Guo et al. 2016; Nakamura et al.
93 2015; Shapiro et al. 1998, Takemura, Kubo, et al. 2019; Volk et al. 2017), complicated
94 seismic waves such as T phase, Scholte, acoustic-coupled, and ocean-mode Rayleigh waves,
95 as has been observed in previous studies (e.g., Haney & Tsai, 2017; Muyzert, 2007; Noguchi
96 et al., 2016; Obara & Maeda, 2009; Okal, 2008; Takeo et al., 2014; Tonegawa, Fukao,
97 Takahashi, et al., 2015). However, despite such complexities, 1D velocity structure models
98 have been widely used in seismic source analyses, where incorrect estimations of source
99 parameters may have been provided, especially for the duration and source energy.

100 Figure 1 shows examples of NS-component filtered velocity seismograms of onshore F-
101 net and offshore DONET stations (National Research Institute for Earth Science and Disaster
102 Resilience, 2019b, 2019a). The sensor orientations of X and Y at the DONET station
103 (M.KMD14) were rotated to North (NS) and East (EW) by using estimations of sensor
104 orientations of Nakano et al. (2012). The estimated event sizes of regular earthquakes in
105 Figure 1 were similar. The event size of a shallow LFT, estimated by using an accompanied
106 shallow very low-frequency earthquake (VLFE), was also similar. However, the observed
107 waveforms of these events were very different. Although an F-net seismogram of an onshore
108 regular earthquake showed a short-duration pulse-like *S*-wave envelope, a DONET
109 seismogram of an offshore regular earthquake was broadened as result of the multiple wave
110 packets. The seismogram of a shallow LFT was more complex, in which a spindle-shaped
111 seismogram envelope was detected. In order to understand the differences in source processes
112 among these seismic events, it is necessary to evaluate the effects of seismic wave

113 propagation through 3D strong heterogeneities in offshore regions, including the seawater,
114 low-velocity accretionary prism, and small-scale velocity heterogeneity.

115 In this study, to investigate the effects of offshore heterogeneities on high-frequency
116 seismic waves and source parameter estimations, we analysed simulated and observed high-
117 frequency seismograms at offshore seismic stations. Using a realistic 3D offshore
118 heterogeneous model, we conducted 3D numerical simulations of seismic wave propagation
119 via open-source finite-difference method (FDM) software (OpenSWPC; Maeda et al., 2017).
120 Simulated seismograms enable analysis of the effects of each heterogeneity on offshore high-
121 frequency seismograms. By combining various structural model simulations and observed
122 seismograms, we can evaluate the effects of the seawater, accretionary prism, and small-scale
123 velocity heterogeneity on high-frequency seismograms at offshore stations. We also estimated
124 a source time function (STF) of a shallow LFT via the conventional method, and conducted a
125 numerical simulation of seismic wave propagation by using the estimated STF. By comparing
126 simulated and observed seismogram envelope shapes, we also discuss reliable settings for
127 source parameter estimations of offshore small seismic events via conventional methods.

128

129 **2. Data and methods**

130 The target region, southeast off the Kii Peninsula, southwest Japan (Figures 1 and 2a), has
131 repeatedly experienced large megathrust earthquakes (e.g., Ando, 1975). To understand stress
132 and frictional conditions of the megathrust zone along the Nankai Trough, regular and slow
133 earthquakes around this region have been monitored by DONET stations (locations
134 represented by diamond symbols in Figures 1 and 2a), operated jointly by the Japan Agency
135 for Marine-Earth Science and Technology (JAMSTEC) and the National Research Institute
136 for Earth Science and Disaster Resilience (NIED). Various small seismic phenomena,
137 including small interplate and intraplate regular earthquakes and shallow slow earthquakes,
138 have been observed by broadband seismometers installed at each DONET station. Interplate
139 earthquake activity is quite low, except for activity of the 2016 southeast off Kii Peninsula
140 earthquake (Nakano, Hyodo, et al., 2018; Wallace et al., 2016), but shallow slow earthquakes
141 are often observed (e.g., Annoura et al., 2017; Araki et al., 2017; Nakano, Hori, et al., 2018;
142 Toh et al., 2018). Precise source parameter estimation of such small phenomena is an
143 important issue for understanding earthquake source physics and seismic activity in the
144 Nankai subduction zone.

145 The effects of offshore heterogeneities on seismic wave propagation were investigated by

146 using both simulated seismograms and three-component broadband velocity seismograms of
147 DONET stations. Simulated seismograms were evaluated at the same locations as the
148 observational stations and virtual seafloor seismic stations, which were uniformly distributed
149 at a horizontal interval of 0.05° in the model region. We used a parallel staggered-grid FDM
150 code of OpenSWPC software (Maeda et al., 2017) to simulate seismic wave propagation of a
151 shallow LFT and small regular earthquakes in the 3D viscoelastic medium. We employed the
152 Cartesian coordinate system of Aki & Richards (2002), where x , y , and z are taken as north,
153 east, and down, respectively. To avoid artificial reflections from model boundaries, perfectly
154 matched layer boundary conditions (e.g., Zhang & Shen, 2010) were assumed at each model
155 boundary.

156 The 3D velocity structure model developed by Koketsu *et al.* (2012) was used as the
157 model beneath the bedrock. This model has been widely used for various applications across
158 Japan (e.g., Furumura & Kennett 2018; Iwaki et al. 2018; Petukhin et al. 2016; Takemura et
159 al. 2017, 2020). The ETOPO1 model (Amante & Eakins, 2009) was used as the topographic
160 model in simulations. The 1D S -wave velocity structures beneath the DONET stations
161 (Tonegawa et al., 2017) were used to model a 3D velocity structure within the accretionary
162 prism. We converted the depth-varying velocity structure model of Tonegawa *et al.* (2017) to
163 a 5-layer model beneath each DONET station. Extrapolation and interpolation of depths of
164 the bottom of each layer via the ‘*Surface*’ gridding algorithm of Generic Mapping Tools
165 (Wessel et al., 2013) were applied to construct the 3D layered accretionary prism model
166 (Figure S1). Details of the model construction are described in the Supporting Material (Text
167 S1, Figures S1-S4). The P - and S -wave velocities, density (V_P , V_S , and ρ), and attenuations
168 (Q_P and Q_S) for each layer are listed in Table 1. The minimum V_S of 0.5 km/s was assumed in
169 the solid column. The 3D simulation model for shallow LFT and small earthquakes covered
170 an area of $120 \times 82.5 \times 45 \text{ km}^3$ (delineated by the dashed-blue rectangle in Figure 2a), which
171 was discretised by a grid interval of 0.015 km. Cross-sections of the constructed layered
172 structure model are illustrated in Figures 2b and 2c. This model is the reference model.
173 Simulations of high-frequency seismic wave propagation were conducted using calculation
174 resources of the Earth Simulator at JAMSTEC. Each simulation required 24 TB of computer
175 memory and a wall-clock time of 6.3 h by parallel computing using 1,280 nodes (5,120 cores)
176 of the Earth Simulator to evaluate a seismic wave propagation of 60 s.

177 According to the observed seismic activity in this region, many intraslab earthquakes
178 occurred at depths of 10–15 km and 20–30 km (e.g., Nakano et al., 2015; Sakai et al., 2005;

179 Takemura et al., 2020). Interplate earthquakes (~10 km), related with the 2016 southeast off
180 Kii Peninsula earthquake, and shallow (< 7 km) slow earthquakes were also observed. Thus,
181 we investigated the effects of 3D heterogeneities on seismic wave propagations from those
182 three different hypocentres in our simulations (Table 2). Simulation results for earthquakes at
183 different depths allowed us to investigate depth-dependent structural responses. Events A, B,
184 and C occurred on 16 April 2016, 19 April 2016, and 4 December 2014, respectively.
185 Because source parameters for events A–C were not precisely estimated, we assumed double-
186 couple point sources of CMT solutions for the nearest shallow VLFE or moderate size
187 earthquakes (Takemura et al. 2019, 2020). Although source durations of LFTs estimated in
188 previous studies ranged from 10 to 30 s (e.g., Gomberg et al., 2016; Nakano et al., 2019;
189 Yabe et al., 2019), the present source models all employed a simple triangle function duration
190 of 0.2 s, which roughly corresponds to a duration of earthquakes with magnitudes of 3.

191 Before the analysis of simulated envelopes, we calculated the Fourier amplitude spectrums
192 for both observed and simulated DONET (M.KMB07) seismograms for the 50 s time window
193 that began at the origin time (Figure 3). The multi-radix fast Fourier transformation algorithm
194 (Takahashi, 2013) was employed. Amplification due to the accretionary prism commonly
195 appeared in low-frequency (0.1–0.2 Hz) components for a shallow LFT. Noise levels of
196 observed seismograms around frequencies of 0.1–0.5 Hz were high due to secondary
197 microseism (e.g., Nishida, 2017). The spectrum of a shallow LFT (red line) showed a weaker
198 high frequency (> 2 Hz) component compared with regular earthquakes. However, spectrums
199 of simulated seismograms showed similar levels for the high frequency (> 2 Hz) range.
200 According to the comparison of Fourier spectrums, we note that a 0.1 s triangle function is
201 unrealistic, especially for a shallow LFT case. However, simulation results of such an
202 unrealistic and short duration STF provide opportunities for investigating the effects of
203 structural heterogeneities on high-frequency seismic wave propagation in offshore regions. In
204 other words, the effects of structural heterogeneities are important for source parameter
205 estimation.

206

207 **3. Simulation results**

208 Figure 4 shows snapshots of the simulated *P*- and *S*-wave propagations of a shallow LFT.
209 The *P*- and *S*-wavefields were evaluated by calculating the divergence and rotation,
210 respectively, of the simulated velocity wavefield of a shallow LFT source. The *P* and *S*
211 waves, which radiated from a shallow LFT on the plate boundary, showed complex

212 propagation through heterogeneous structures and repeating scattering and reflection from
213 each layer boundary. The intensities of *P* and *S* waves at depths below the bedrock were very
214 weak, but large seismic energies were trapped within the low-velocity accretionary prism.
215 The *P* waves were also trapped within the seawater layer as ocean acoustic waves. According
216 to these simulated *P* and *S* wavefields, long-duration complicated simulated seismograms can
217 be expected.

218 The root-mean-square (RMS) envelopes for the shallow LFT simulation are shown in
219 Figure 5a. After synthesizing three-component MS envelopes for the frequencies of 1–5 Hz,
220 the RMS envelopes were evaluated by taking the mean square for the sum of the three-
221 component MS envelopes. The RMS envelope was smoothed by taking the 1 s moving
222 average. Because the FDM can evaluate the seismic wave propagation for frequencies less
223 than 5 Hz due to our simulation settings, we investigated simulated seismograms for the 1–5
224 Hz frequency band, which is lower than the typical dominant frequencies of LFTs (2–8 Hz).
225 After calculating the vector sum of three-component envelopes, a moving average with a time
226 window of 1 s was applied. Each trace was normalized by each maximum amplitude. The
227 envelopes at stations around the epicentre (< 10 km) clearly showed a short-duration *S*-wave
228 pulse and weak later phases. However, as distance increased, RMS envelopes broadened
229 rapidly. At distances greater than 30 km, the onsets of *S* waves were not clear and RMS
230 envelopes were characterized by spindle shapes with durations of 20–30 s. These *S*-wave
231 durations were significantly longer than the assumed source pulse (0.2 s). This broadening
232 and delayed peak of simulated seismogram envelopes was much larger than for seismic
233 waves propagating through the typical lithosphere (e.g., Saito et al., 2005; Takahashi et al.,
234 2007; Tripathi et al., 2010).

235 On the other hand, the simulated RMS envelopes for regular earthquakes were composed
236 of pulse-like *S* waves and multiple distinct later packets (Figures 5b and 5c). Multiple later
237 packets may be developed by the seawater layer, accretionary prism, or subducting oceanic
238 plate. The simulation of the deepest source (event C; Figure 5c) showed simpler RMS
239 envelopes. Simulations of all events were conducted by using the same source time function
240 (0.2 s triangle function), but the simulated envelopes for event A were very different from
241 those for events B and C. Significant differences were found in simulated RMS envelopes
242 between events A and B, despite similar source mechanisms, both of which were low-angle
243 thrust faulting on the plate boundary. Thus, we considered that differences in simulated RMS
244 envelopes between a shallow LFT and regular earthquakes could be caused by shallower

245 heterogeneous structures.

246 Figure 6 shows observed RMS envelopes of a shallow LFT on 16 April 2016, an interplate
247 earthquake on 19 April 2016, and an intraplate earthquake on 4 December 2014. Because we
248 did not know the precise source parameters of these small events and incorporated the effects
249 of site amplification at each station, we compared the shapes of seismogram envelopes
250 between simulations (Figure 5) and observations (Figure 6). Similar characteristics of
251 simulated RMS envelopes were found in observations. Although the durations of observed
252 RMS envelopes for a shallow LFT were longer than the simulation with a 0.2 s triangle
253 function (Figure 5 a), the observed RMS envelopes also broadened with increasing distance
254 (Figure 6a). Pulse-like wave packets of *S* waves and later phases appeared in observed RMS
255 envelopes for regular earthquakes (Figures 6b and 6c). To quantify the similarity between
256 observed and simulated envelopes, we calculated cross-correlation coefficients (CCs)
257 between both envelopes. In calculations of CCs, we allowed time shifts within ± 3 s because
258 we did not know the precise source parameters for observed seismograms. Figure 7 shows
259 spatial variations of cross-correlation coefficients for Events A–C. Due to sensor conditions,
260 we discarded DONET E-node (northwest four stations) in the comparison for Event C. We
261 confirmed high (> 0.7) correlation coefficients except for Event A. The cause of CCs for
262 Event A can be explained by an assumed STF. The comparison of simulation with a complex
263 STF is discussed in the later section. The CCs of RMS envelopes between simulations and
264 observations suggest that our local 3D model reliably characterizes seismic wave propagation
265 southeast off the Kii Peninsula, Japan.

266 Figure 8 shows the spatial variations of maximum RMS amplitudes and envelope half-
267 value widths derived from ground motion simulation for a shallow LFT. The envelope half-
268 value width is the period for which the amplitude is greater than half of the maximum
269 amplitude (Figure 8a) and has been used to represent the event duration of LFTs (e.g., Ide,
270 2010; Yabe et al., 2019). We used simulated RMS envelopes at both DONET and virtual
271 seismic stations for detailed evaluations of spatial variations in amplitude and duration. The
272 simulated amplitude distribution did not show a simple two-lobe pattern, which was expected
273 from the assumed source mechanism. Generally, the high-frequency maximum amplitude
274 distribution is distorted from the expected source radiation pattern by seismic wave scattering
275 and diffraction due to small-scale subsurface heterogeneities (e.g., Imperatori & Mai 2013;
276 Morioka et al. 2017; Takemura et al. 2009, 2016). Because we did not introduce a small-scale
277 velocity heterogeneity into the reference model in this simulation, we confirmed that the

278 shallower heterogeneities, such as seawater and the thick low-velocity accretionary prism,
279 also distorted the maximum amplitude distribution. Thus, the assumption of isotropic
280 radiation for energy estimations of small offshore seismic events in many studies could be
281 suitable (e.g., Tamaribuchi et al., 2019; Yabe et al., 2019). Because our simulations did not
282 include site amplifications caused by structures with $V_S < 0.5$ km/s, the observed maximum
283 amplitude distribution could be more complicated because of site amplification factors at
284 DONET stations for high-frequency seismic waves (e.g., Kubo et al., 2018; Yabe et al.,
285 2019).

286 Figures 8c and 8d show spatial variations and distance-change properties of half-duration
287 widths from the simulation results for a shallow LFT source. We also plotted the theoretical
288 values of t_q via the method of Sato & Emoto (2018) as a typical envelope broadening for
289 onshore earthquakes. Parameter t_q is defined as the time between S -wave onset and the time
290 when the RMS envelope decays to half the maximum amplitude. This t_q value only reflect the
291 effect of envelope broadening due to small-scale velocity heterogeneity. Typical t_q values in
292 onshore regions gradually increase from 2 to 10 s at distances of 20–200 km (e.g., Tripathi et
293 al., 2010). Although the half-value widths exhibited heterogeneous distribution and were
294 widely scattered, these values increased with increasing distance and were of much longer
295 duration than values of t_q (red lines). These longer and distance-dependent S -wave durations
296 could be caused by shallower heterogeneous structures, such as seawater and the accretionary
297 prism. Thus, to reliably estimate source duration, the effects of elongation due to shallower
298 structures should be incorporated.

299 On the other hand, the half-value widths for a simulated interplate earthquake did not
300 show clear distance-dependent properties (Figure 9). Some stations showed distinct reflection
301 phases from the sea surface or bedrock (Figures 5b, 6b, and 9b). Similar features appeared in
302 cases of an intraslab earthquake (Figure S5). Weak distance-dependent features were
303 confirmed in half-value widths for later portions. Step-like elongation of half-value widths
304 could be explained by multiple reflections from sea surface and bedrock boundary. Source
305 durations of interplate earthquakes could be overestimated if such multiple reflections are
306 counted as the durations of S waves. Conversely, by excluding such reflection phases and site
307 amplifications from the analysis, the source parameters of offshore regular earthquakes,
308 which occurred at sufficient depths below the accretionary prism, could be robustly
309 estimated.

310

311 **4. Effects of heterogeneous structures on source parameter estimation for small seismic** 312 **events**

313 **4.1. Effects of heterogeneous structures on offshore seismograms**

314 We demonstrated that high-frequency seismic waves show complicated propagation in
315 offshore regions due to the influence of 3D heterogeneous structures. Our model in previous
316 3D simulations contains seawater, low-velocity accretionary prism, crust, and the subducting
317 Philippine Sea plate. According to the snapshots of the simulated wavefield and differences in
318 simulated envelopes due to source locations, shallower heterogeneities could strongly affect
319 high-frequency seismic wave propagation. Shallower heterogeneities affect the maximum
320 amplitude distribution and envelope broadening of high-frequency seismic waves. At
321 frequencies greater than 1 Hz, characteristics of seismic wave propagation were usually
322 affected not only by deterministic layered structures but also small-scale velocity
323 heterogeneities along the propagation path (summarized in Ch. 2 of Sato et al., 2012). In this
324 sub-section, we discuss the effects of a small-scale velocity heterogeneity, seawater, and low-
325 velocity accretionary prism on high-frequency seismic wave propagation through offshore
326 regions.

327 Small-scale velocity heterogeneities were modelled by using stochastic random velocity
328 fluctuations characterized by an exponential autocorrelation function (ACF). The parameters
329 of small-scale velocity heterogeneity (correlation length and RMS value) within the slab
330 mantle and others were derived from Furumura & Kennett (2005) and Takemura et al. (2017),
331 respectively (see Table 3). We assumed the small-scale velocity heterogeneity within the
332 accretionary prism as the same as that within the crust. Similar small-scale heterogeneity
333 models were previously used for waveform modelling in the Kanto sedimentary basin
334 (Takemura & Yoshimoto 2014).

335 We employed the following four heterogeneous models to evaluate the effects of each
336 heterogeneity on offshore seismograms: model with a small-scale velocity heterogeneity;
337 model without a seawater layer; model without an accretionary prism; and model without a
338 seawater layer and accretionary prism. The model with a small-scale velocity heterogeneity
339 was constructed by superposing small-scale velocity heterogeneities (in Table 3) on the
340 reference model. In the model without the seawater layer, the physical parameters within the
341 seawater layer were replaced with those within the air column, and the seafloor was treated as
342 the free surface. In the model without the low-velocity accretionary prism, physical
343 parameters were replaced with those of the upper crust (Table 1). All models included

344 bathymetry, but we do not discuss its effects because previous studies have reported limited
345 effects of topographic scattering on body wave propagation (e.g., Imperatori & Mai, 2015;
346 Takemura et al., 2015).

347 Figure 8 shows the simulated RMS envelopes at DONET stations using the four different
348 heterogeneous models. To visualize the effects of heterogeneities, RMS envelopes of the
349 reference model were also plotted by grey lines. Although maximum amplitudes and later
350 phases were slightly changed by introducing small-scale velocity heterogeneities, these
351 effects were not significant (Figure 10a). This tendency remained unchanged when using
352 stronger models or those with different random seeds (Figure S6). The durations of RMS
353 envelopes also showed slight differences between models with/without small-scale velocity
354 heterogeneities (Figure S7). In typical crustal earthquakes, the effects of small-scale velocity
355 heterogeneity appear as amplitude fluctuations of high-frequency seismic waves even for
356 stations at shorter distances (e.g., Yoshimoto et al., 2015). Numerical simulations by Iwaki et
357 al. (2018) showed that crustal small-scale heterogeneity has limited effects on ground
358 motions for frequencies lower than 1 Hz in the Kanto sedimentary basin. Our large-scale
359 simulations demonstrate that the effects of the sedimentary layers (accretionary prism) on
360 high-frequency seismic waves are stronger than those of small-scale velocity heterogeneities.

361 In the model without seawater, the seafloor was treated as the free surface, and
362 consequently, RMS amplitudes were amplified (Figure 10b). The low-velocity accretionary
363 prism has dominant effects on high-frequency seismic waves in this region. The model
364 without the accretionary prism exhibited simple pulse-like RMS envelopes, which were very
365 similar to the typical envelopes of onshore small earthquakes (Figure 10c). Pulse-like *S*
366 waves and multiple small pulses after *S* waves were found in simulated RMS envelopes. The
367 differences between the RMS envelopes of the reference model and the model without the
368 accretionary prism indicate that elongations of *S* waves at offshore stations were mostly
369 caused by the low-velocity accretionary prism.

370 Multiple later packets after *S* waves were weak but also present in the RMS envelopes of
371 the model without both seawater and an accretionary prism (Figure 10d). These phases could
372 be interpreted as reflections from the subducting Philippine Sea slab. It was difficult to find
373 the phases reflected from the subducting Philippine Sea slab in the RMS envelopes of the
374 model that included the accretionary prism, as the elongation and amplification effects of the
375 accretionary prism masked reflections from the Philippine Sea plate. Tonegawa et al. (2015)
376 also reported that reflections from the bedrock (bottom of oceanic sediments) are also

377 dominant in ambient noise wavefields, and it can be difficult to identify reflections from the
378 boundaries at depths below the bedrock.

379 According to the above results, we conclude that the low-velocity accretionary prism is the
380 dominant influence on high-frequency seismic wave propagation through the offshore region,
381 whereas other heterogeneities, such as seawater and small-scale velocity heterogeneities,
382 have minor effects. Similar tendencies were also found in simulations of interplate and
383 intraslab earthquakes (Figures S8 and S9). The low-velocity accretionary prism is also
384 important for low-frequency surface wave propagation (e.g., Takemura, Kubo, et al. 2019;
385 Volk et al. 2017). Strong amplification or waveguide effects for both low- and high-frequency
386 seismic waves due to the accretionary prism were also reported in the Cascadia, Mexico, and
387 Hikurangi subduction zones (e.g., Gomberg, 2018; Kaneko et al., 2019; Shapiro et al., 2000).
388 To achieve reliable modelling of broadband seismic wave propagation through offshore
389 regions, and precise source-parameter estimations for offshore seismic events, a detailed
390 model of the low-velocity accretionary prism should be considered.

391

392 **4.2. Source parameter estimation for a shallow LFT via the conventional method**

393 For small events, especially LFTs, the durations, source energies, or band-limited
394 moments have been estimated by using stacked coherent RMS envelopes or average values
395 for the used stations after correction of site amplification and attenuations (e.g., Annoura et
396 al., 2016; Ghosh et al., 2009; Kao et al., 2010; Maeda & Obara, 2009; Yabe et al., 2019; Yabe
397 & Ide, 2014). However, our simulations demonstrated that elongation of RMS envelopes for
398 a shallow LFT, due to the low-velocity accretionary prism, occurs even for stations as close
399 as 10 km from the epicentre (Figures 5a and 8). Thus, incorrect estimation of source
400 parameters via the conventional method can be expected. In this sub-section, we conducted
401 an FDM simulation of seismic wave propagation and compared it with observed RMS
402 envelopes to investigate the validity and limitations of STFs estimation by the conventional
403 method.

404 We used observed DONET seismograms for a shallow LFT that occurred at 11:18 on 24
405 October 2015 (JST), located at 136.91°E, 33.35°N. For deep slow earthquakes, the
406 proportionality between seismic energy rate functions estimated from high-frequency
407 seismograms and seismic moment rate functions estimated from low-frequency seismograms
408 has been confirmed (Ide et al., 2008). Yabe et al. (2019) showed that the same proportionality
409 holds true for shallow slow earthquakes. Therefore, seismic energy rate functions estimated

410 from high-frequency seismograms can be converted into STFs by dividing them by the value
411 of scaled energy. The seismic energy rate function of the event observed at each station is
412 conventionally calculated from squared seismograms at each station after correction of site
413 and attenuation effects within time windows of half-value width measured for the stacked
414 RMS envelope. Seismograms were excluded from the analysis if the cross-correlation
415 coefficient with the same event envelopes at any other stations did not exceed 0.6. This
416 procedure removed stations lacking tremor signals. Modelling for direct-*S* wave energies
417 using the uniform background velocity structure ($V_S = 3.5$ km/s and $\rho = 2700$ kg/m³) and
418 distance-dependent attenuation model (Figure 3 of Yabe et al., 2019) was employed. The
419 seismic energy rate functions were converted into STFs by assuming a scaled energy value of
420 3.0×10^{-9} (Ide & Maury, 2018; Ide & Yabe, 2014; Yabe et al., 2019). The STF of the event
421 was calculated by stacking STFs at each station after applying a 10 s low-pass filter.

422 Figure 11 shows the STFs of a shallow LFT that occurred on 24 October 2015. The
423 conventional method typically provided STFs represented by blue dashed or red lines, which
424 were estimated by using stacking seismic energy rate functions of B-node stations and B- and
425 C-node stations, respectively. The moment releases of these STFs continued 50–60 s from the
426 origin and peaks of moment rate appeared at around 25 s. The STF described by the solid-
427 blue line was constructed by using the seismic energy rate function at M.KMB06 only, which
428 was located just above the shallow LFT hypocentre. This STF was completely different from
429 the others. The peak of this STF appeared within 3.2 s of the origin, and the moment release
430 continued 30–40 s from the origin. By using these STFs, we synthesized seismograms of the
431 shallow LFT. Hypocentre depth was fixed on the plate boundary, and the focal mechanism
432 was the same as in previous simulations of event A (Table 2). After FDM simulations, we
433 convolved the estimated STFs to simulated envelopes. To achieve suitable STF convolutions,
434 we assumed a simple 0.1 s triangle function, which was sufficiently shorter than the STFs in
435 Figure 11. After FDM simulations, we convolved the estimated STFs to simulated envelopes.

436 Figure 12 compares 1–5 Hz RMS envelopes between simulations and observations. In this
437 comparison, the amplitudes of each trace were normalized by each maximum amplitude
438 because the precise seismic moment and site amplification factors from the $V_S = 0.5$ km/s
439 layer were not well known. The analysis focused on differences in envelope shapes between
440 simulations and observations. To quantify fitness of envelope shapes, we also calculated CCs
441 between observed and simulate envelopes (blue numbers in each trace). The simulation
442 results with the STF from M.KMB06 reproduced the observed envelope shapes and durations

443 at all stations. Almost all of the simulated envelopes had CCs larger than 0.7. This STF also
444 reproduced the seismograms observed for a shallow VLFE (Yabe et al., 2019), which
445 occurred in the same time window as the target shallow LFT but appeared for frequencies of
446 0.03–0.05 Hz.

447 The simulations with the other STFs were much longer than the observations. Two of the
448 simulated STFs also showed delayed peak amplitudes compared to the observations. The
449 epicentral distances of B-node stations except for M.KMB06 ranged from 10 to 16 km. The
450 simulation with a simple STF (Figures 5a and 8) demonstrated that the durations of *S* waves
451 increased rapidly with increasing distance, and values reached to 5–15 s at stations located at
452 distances of 10–15 km. Thus, STFs from stacked seismic energy rate functions via the
453 conventional method were delayed and overestimated. The simulation with a simple STF of
454 duration 0.2 s (see Figure 5a) shows that the RMS envelopes at very close (< 10 km) stations
455 are characterized by a pulse-like *S* wave packet, and consequently, seismic energy rate
456 functions at close stations could preserve source information. Thus, the shapes and durations
457 of observed RMS envelopes were only well reproduced in the STF estimated from the nearest
458 station (~1.4 km, M.KMB06).

459 Our numerical tests in this sub-section revealed that STFs from stations very close to the
460 source reproduced the observed seismogram envelopes of the target shallow LFT. In other
461 words, the effects of offshore heterogeneities were limited at stations with epicentral
462 distances less than 10 km, even for shallower (~5 km) seismic events (see Figure 5), and,
463 consequently, the source parameter information could be preserved. At stations with
464 epicentral distances greater than approximately 10 km, RMS envelopes were strongly
465 elongated due to the effects of the accretionary prism (Figure 5a). At stations with epicentral
466 distances greater than approximately 10 km, durations of the RMS envelope were controlled
467 by the heterogeneous structure of the accretionary prism along the propagation path. Thus,
468 STFs calculated by using such stations via the conventional method (e.g., Yabe et al., 2019)
469 were overestimated and could not reproduce the observed RMS envelopes. When the
470 conventional method is applied to OBS data, seismograms should be selected from stations
471 located closer than approximately 10 km. If stations further than 10 km from the source are
472 used, the effects of 3D offshore heterogeneities should be included in the method of source
473 parameter estimation.

474

475 **5. Conclusions**

476 We investigated the effects of offshore heterogeneities, such as a small-scale velocity
477 heterogeneity, seawater, and the accretionary prism, on high-frequency seismic propagation
478 southeast off the Kii Peninsula, southwest Japan. Our simulations demonstrated that the low-
479 velocity accretionary prism affects the shapes of seismogram envelopes. A thick low-velocity
480 accretionary prism is also developed in the Cascadia, Mexico, and Hikurangi subduction
481 zones, and this affects not only low-frequency surface waves, but also high-frequency seismic
482 waves. The effects of the accretionary prism are significant for shallow-depth events along
483 the plate boundary, which correspond to shallow LFTs along the Nankai Trough, as these
484 sources are typically located just beneath the accretionary prism toe at depths of 5–8 km near
485 the trench axis. On the other hand, seismogram envelopes for sufficiently deep-depth events,
486 which correspond to interplate and intraslab regular earthquakes along the Nankai Trough,
487 comprise multiple pulse-like wave packets that consist of direct-*S* waves and multiple
488 reflections from the bedrock.

489 The seismogram envelopes of a source at shallow LFT depths (5–7 km) were broadened
490 due to the low-velocity accretionary prism, even when assuming a simple STF. The durations
491 of RMS envelopes exceeded 10 s, even at stations located at distances greater than 10 km.
492 Multiple reflected phases found in seismograms of regular earthquakes also can affect half-
493 value widths. Such elongation of envelopes will cause incorrect estimations of event
494 durations. Event durations are important for discussing the scaling law of regular and slow
495 earthquakes. After removing such reflection phases and site amplification from the analysis,
496 the source parameters of offshore regular earthquakes, which occurred at sufficient depths
497 below the accretionary prism, could be reliably estimated.

498 At stations very close (< 10 km) to the source, pulse-like *S* wave envelopes, reflecting an
499 assumed STF, were preserved for shallow (5–30 km) small seismic events. If stations at
500 distances greater than 10 km are used, the STF could be overestimated in terms of the
501 duration and peak time of the moment rate. By estimating the STF by using only the nearest
502 stations, the FDM simulations reproduced the shapes and durations of observed RMS
503 envelopes. Thus, conventional approaches might work well by using stations at distances less
504 than 10 km.

505 High-frequency seismogram envelopes are useful for both studies of structural property
506 (e.g., Carcolé & Sato, 2010; Przybilla et al., 2009; Saito et al., 2005; Takemura et al., 2015)
507 and source parameter estimations (e.g., Battaglia & Aki, 2003; Gusev & Pavlov, 1991; Ide et
508 al., 2008; Yabe et al., 2019). Envelope based source inversions have been conducted by using

509 theoretical Green's function envelopes (e.g., Nakahara, 2013; Petukhin et al., 2004; Sawazaki
510 & Enescu, 2014). Theoretical envelopes can be easily evaluated, but 3D heterogeneous
511 structures cannot be incorporated. Combined use of the Green's functions of numerical
512 simulations in a 3D local model and site amplifications due to lower ($V_S < 0.5$ km/s) velocity
513 sediments at each station can potentially enable reliable source parameter estimations even
514 for small offshore events. Green's functions within the local layered model are also useful for
515 estimations of small-scale heterogeneities within oceanic sediments, which may reflect
516 physical properties or clack distributions of the accretionary prism. Such challenging work
517 remains for future studies.

518

519 **Acknowledgements**

520 F-net and DONET waveform data are available via the NIED website
521 (<https://doi.org/10.17598/NIED.0005>, <https://doi.org/10.17598/NIED.0008>). Bathymetric
522 depth data were obtained from ETOPO1 (Amante & Eakins, 2009). OpenSWPC software
523 (Maeda et al., 2017) and the 3D model of Koketsu et al. (2012) were obtained from
524 <https://doi.org/10.5281/zenodo.3712650> and
525 https://www.jishin.go.jp/evaluation/seismic_hazard_map/lpshm/12_choshuki_dat/,
526 respectively. Generic Mapping Tools (GMT; Wessel et al., 2013) and Seismic Analysis Code
527 (SAC; Helffrich *et al.* 2013) were used to produce the figures and in signal processing,
528 respectively. The multi-radix FFT package (ffte; Takahashi, 2013) is available at
529 <http://www.ffte.jp/>. The catalogues of slow earthquakes (Nakano, Hori, *et al.* 2018, Takemura
530 *et al.* 2019) were downloaded from the Slow Earthquake Database website (Kano et al.,
531 2018; <http://www-solid.eps.s.u-tokyo.ac.jp/~sloweql/>). The CMT results of the 2016 southeast
532 off Kii Peninsula earthquake, Japan, and an intraslab earthquake used in regular earthquake
533 simulations are available from <https://doi.org/10.5281/zenodo.3523583>. We also used the
534 unified hypocentre catalogue of the Japan Meteorological Agency
535 (<https://www.data.jma.go.jp/svd/eqev/data/bulletin/index.html>). The FDM simulations of
536 seismic wave propagation were conducted by using the Earth Simulator of JAMSTEC. This
537 study was supported by the Japan Society for the Promotion of Science (JSPS) KAKENHI
538 Grant Numbers 17K14382, 18K13639 in the Grant-in-aid for Young Scientists and Grant
539 Number 19H04626 in the Scientific Research under Innovative Areas 'Science of Slow
540 Earthquakes'. We would like to thank Editage (www.editage.com) for English language
541 editing. We also thank three anonymous reviewers and Editor Prof. J. Virieux for carefully
542 reviewing the study and providing constructive comments, which have helped to improve the
543 manuscript.

544

545 **Tables**

546 **Table 1.** Physical parameters of each layer in the 3D velocity structure model. The
 547 parameters were obtained from the Japan Integrated Velocity Structure Model (JIVSM)
 548 (Koketsu et al., 2012). The air and seawater layers were treated as being the same,
 549 following Maeda *et al.* (2017).

	V_P [km/s]	V_S [km/s]	ρ [kg/m ³]	Q_P	Q_S
Air	0.0	0.0	0.001	10^{10}	10^{10}
Seawater	1.5	0.0	1.04	10^6	10^6
Sedimentary layer 1	1.8	0.5	1.95	170	100
Sedimentary layer 2	2.2	0.8	2.07	272	160
Sedimentary layer 3	2.4	1.0	2.15	340	200
Sedimentary layer 4	3.0	1.5	2.25	510	300
Sedimentary layer 5	3.5	2.0	2.35	680	400
Basement	5.5	3.2	2.65	680	400
Upper crust	5.8	3.4	2.70	680	400
Lower crust	6.4	3.8	2.80	680	400
Upper mantle	7.5	4.5	3.20	850	500
Philippine Sea plate					
Oceanic crust layer 2	5.0	2.9	2.40	340	200
Oceanic crust layer 3	6.8	4.0	2.90	510	300
Oceanic mantle	8.0	4.7	3.20	850	500

550

551

552 **Table 2.** Source parameters used in FDM simulations. A shallow LFT and intraslab
 553 earthquakes were referred from the nearest shallow VLFE and intraslab earthquakes of
 554 CMT solutions in our previous studies (Takemura, Okuwaki, *et al.* 2019, Takemura *et al.*
 555 2019). Double-couple point sources were assumed. The value of T_0 represents the STF
 556 duration.

	Type	Lon. [E°]	Lat. [°N]	Depth [km]	Strike [°]	Dip [°]	Rake [°]	M_w	T_0 [s]
A	LFT	136.90	33.20	6.20	255.0	7.0	116.0	3	0.2
B	Interplate earthquake	136.34	33.40	11.15	243.3	10.1	114.4	3	0.2
C	Intraslab earthquake	137.11	33.28	28.7	264.3	37.9	37.9	3	0.2

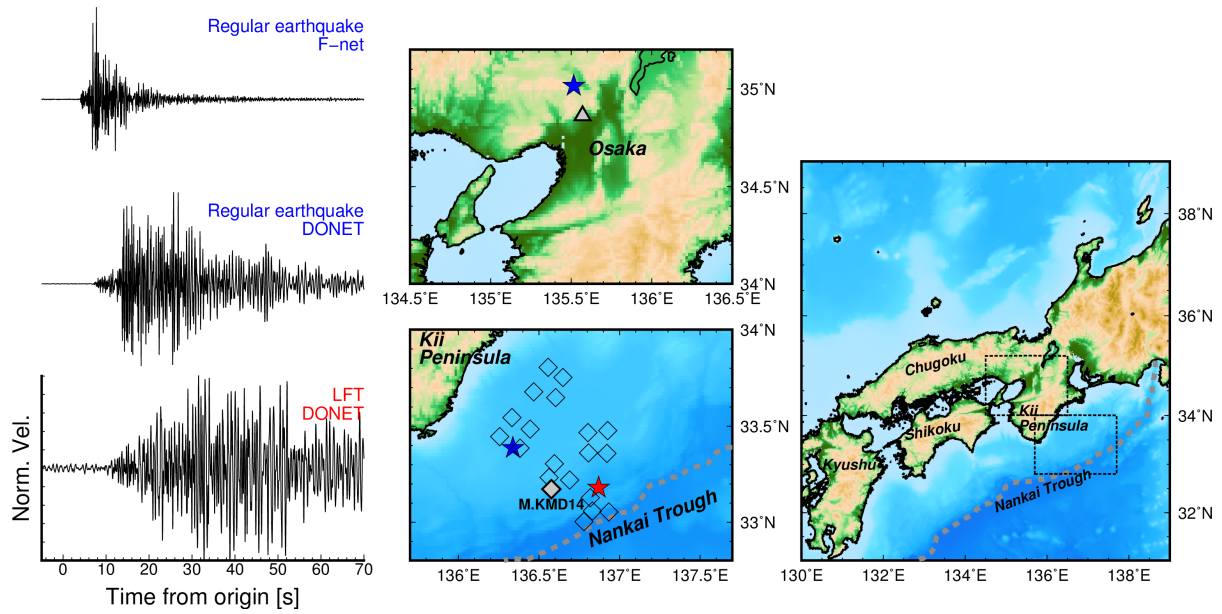
557
 558 **Table 3.** Parameters of small-scale velocity heterogeneities in each layer. The models of the
 559 crust and oceanic crust were assumed to be the same as the model of crustal
 560 heterogeneity (Takemura *et al.* 2017). The model of the oceanic mantle was derived from
 561 Furumura & Kennett (2005).

Layer	ACF-type	Correlation length a	RMS value ε
Air and seawater	-	-	-
Accretionary prism	Exponential	Isotropic: 1 km	0.03
Crust	Exponential	Isotropic: 1 km	0.03
Mantle	-	-	-
Oceanic crust	Exponential	Isotropic: 1 km	0.03
Oceanic mantle	Exponential	Horizontal: 10 km Vertical: 0.5 km	0.03

562

563

564 **Figures**

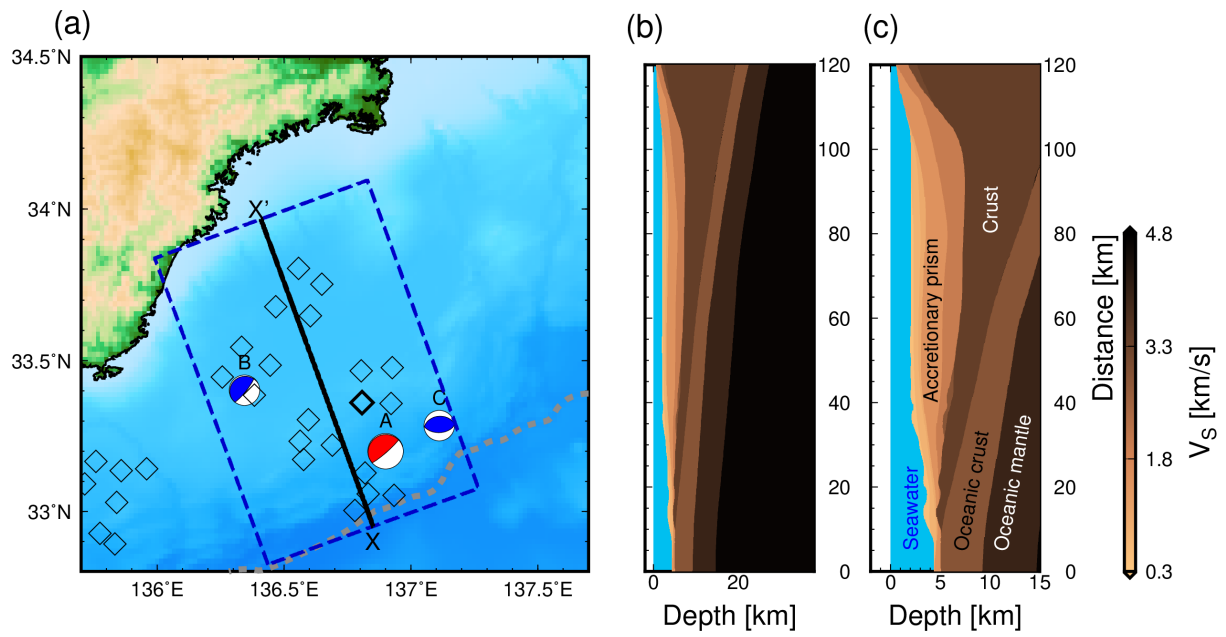


565

566 **Figure 1.** Examples of observed NS-component seismograms for a crustal earthquake, an
 567 offshore interplate earthquake, and a shallow LFT. Crustal and offshore interplate
 568 earthquakes occurred on 24 January 2015 and 1 April 2016, respectively. A shallow LFT
 569 occurred on 3 April 2016. The magnitudes of these events were approximately 3, and
 570 epicentral distances were also similar. The blue stars and red star in enlarged maps are
 571 the epicentres of regular earthquakes and the shallow LFT, respectively. The triangle and
 572 diamond symbols show the locations of the F-net and DONET stations, respectively.

573

574



575

576

577

578

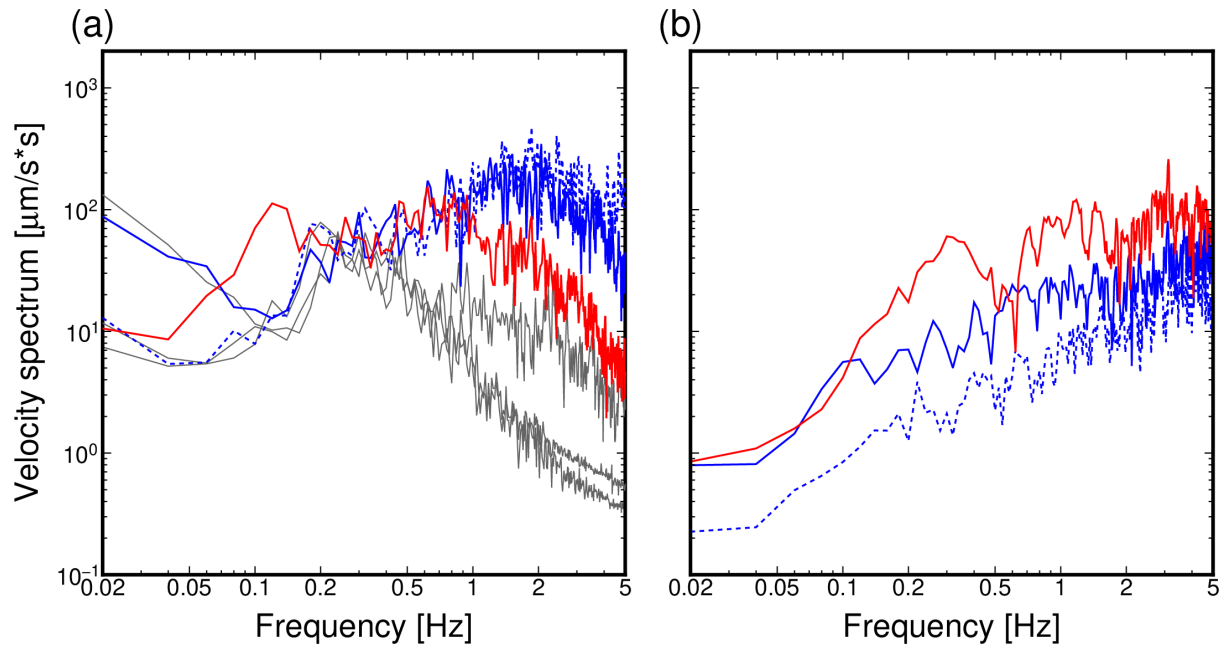
579

580

581

582

Figure 2. (a) Map of the simulation region, and cross-sections of the (b) S -wave velocity model along the X—X' profile and (c) S -wave velocity model at shallower (< 15 km) depths. The red and blue focal mechanisms are source models of a shallow LFT and regular earthquakes, respectively. Details of physical parameters in each layer are listed in Table 1.

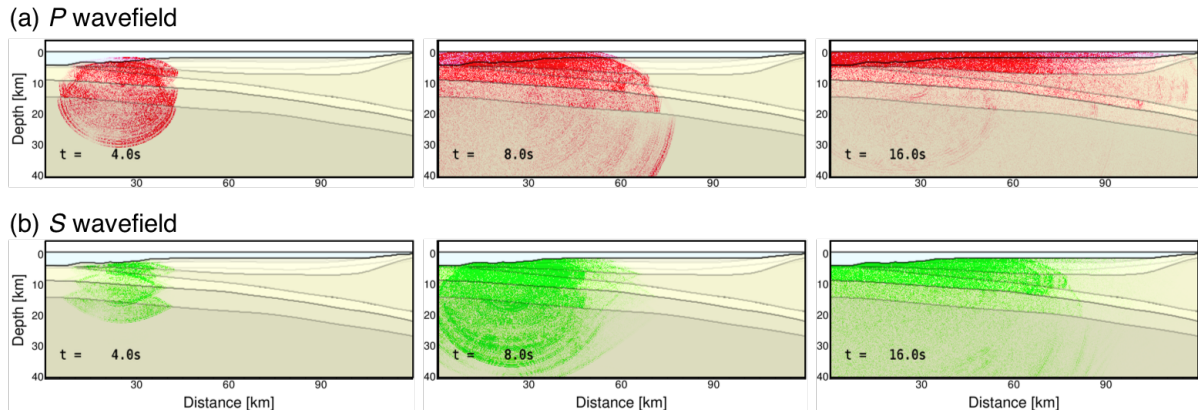


583

584 **Figure 3.** Fourier spectrums of (a) observed and (b) simulated seismograms at M.KMB07.

585 The location of M.KMB07 is shown in Figure 2 (bold diamond). The red, blue solid,
 586 blue dashed, and grey lines in (a) are spectrums of a shallow LFT on 16 April 2016, an
 587 interplate earthquake on 19 April 2016, an intraplate earthquake on 4 December 2014,
 588 and noise parts, respectively. The red, blue, and blue dashed lines in (b) are spectrums of
 589 simulated seismograms for Events A–C. The time window for the event signal is from
 590 the origin time to the lapse time of 50 s.

591



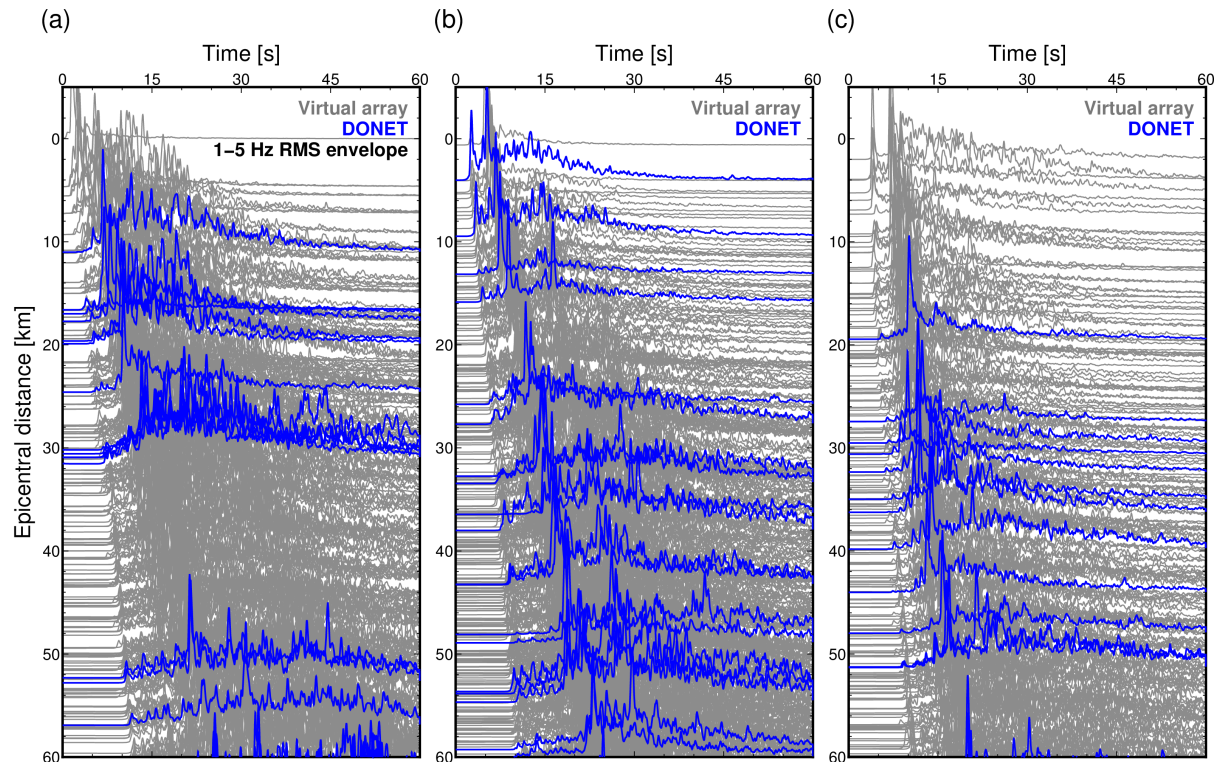
592

593

Figure 4. Simulated snapshots of (a) *P* and (b) *S* wavefields along profile X—X' for the shallow LFT simulation (red focal sphere in Figure 2).

594

595



596

597

Figure 5. Simulated RMS envelopes for frequencies of 1–5 Hz from simulations of the (a) shallow LFT, (b) interplate earthquake, and (c) intraslab earthquake. Source parameters and locations are shown in Table 2 and Figure 2a. The RMS envelopes at DONET and virtual stations are represented by blue and grey lines, respectively.

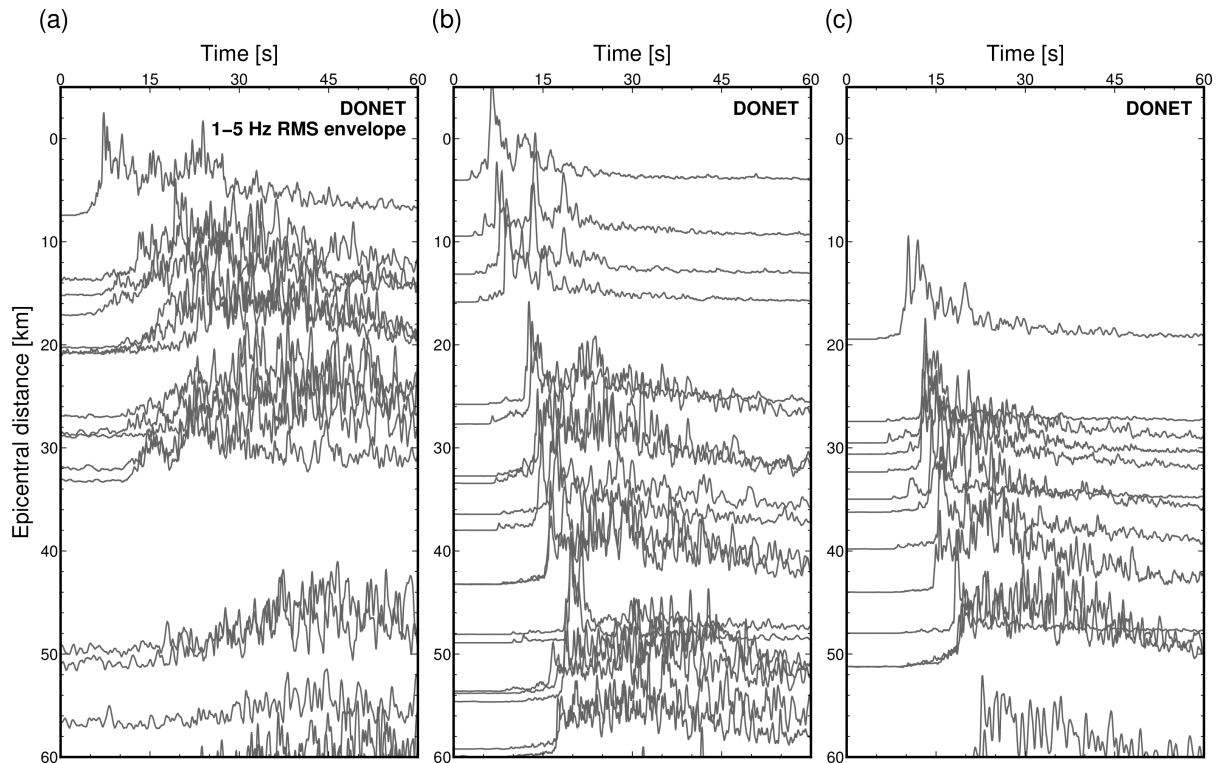
598

599

600

601

602



603

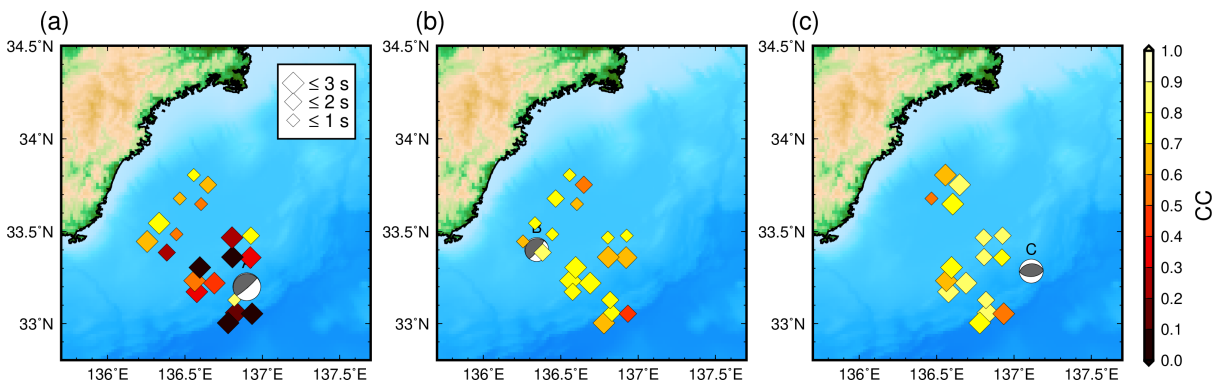
604

605

606

607

Figure 6. Observed RMS envelopes for frequencies of 1–5 Hz at DONET stations. The RMS envelopes for (a) a shallow LFT on 16 April 2016, (b) an interplate earthquake on 19 April 2016, and (c) an intraplate earthquake on 4 December 2014.



608

609

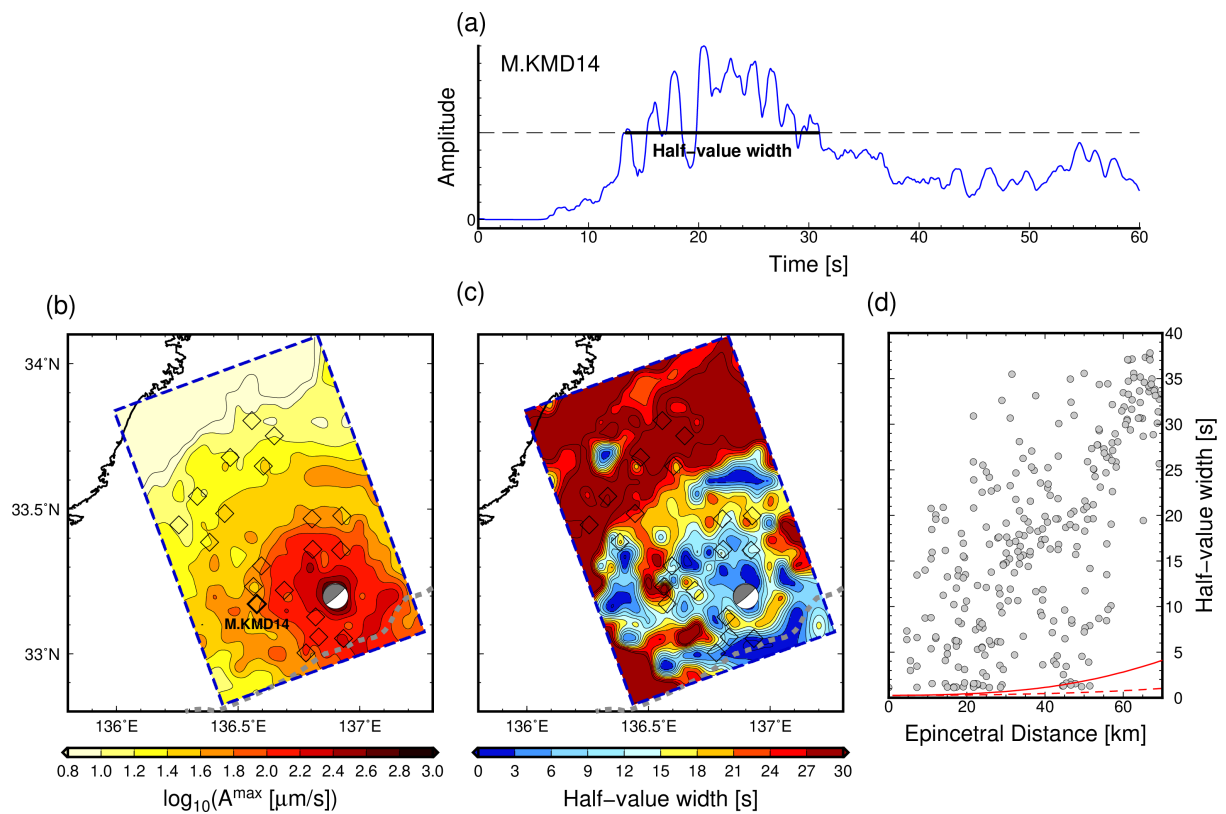
610

611

612

613

Figure 7. Spatial variations of cross-correlation coefficients between observed and synthesized envelopes for (a) Event A, (b) Event B, and (c) Event C. The sizes of symbols represent the absolute values of time shifts, which provide maximum correlation coefficients at each station.



614

615 **Figure 8.** Spatial variations of maximum RMS amplitudes and half-value widths of simulated

616 RMS envelopes for a shallow LFT: (a) an example of half-value width estimations, (b)

617 maximum RMS amplitude distribution, (c) half-value width distribution, and (d) half-

618 value widths as a function of the epicentral distance. The example in (b) is an RMS

619 envelope at M.MRD14 (location shown in (a)). The red dashed and solid lines in (d) are

620 values of t_q via the method of Sato & Emoto (2018). Here, t_q is defined as the time

621 between S -wave onset and the time when the RMS envelope decays to half the maximum

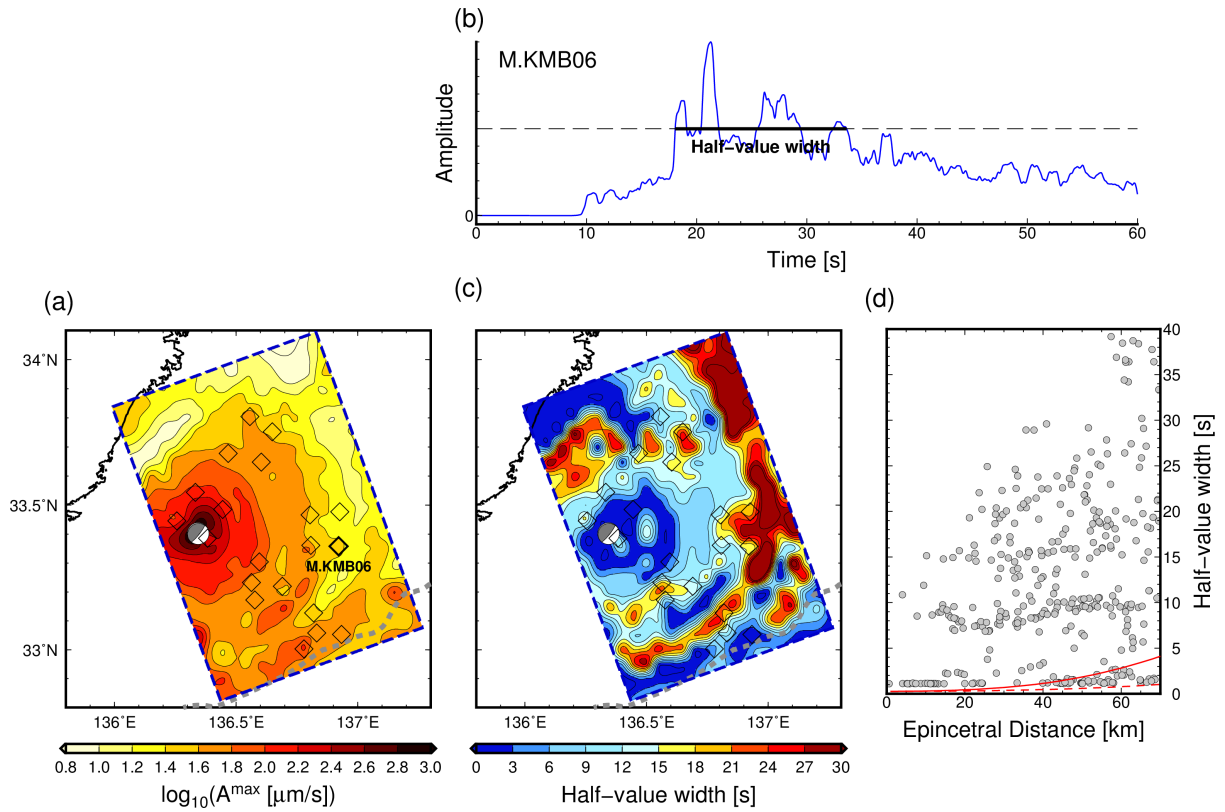
622 amplitude. The assumed small-scale random velocity heterogeneity models for dashed

623 and solid lines are characterized by an exponential-type autocorrelation function with

624 correlation length of 1 km and RMS values of 0.03 and 0.05, respectively. The central

625 frequency in theoretical synthetics is 4 Hz.

626



627

628

629

630

631

632

633

634

635

636

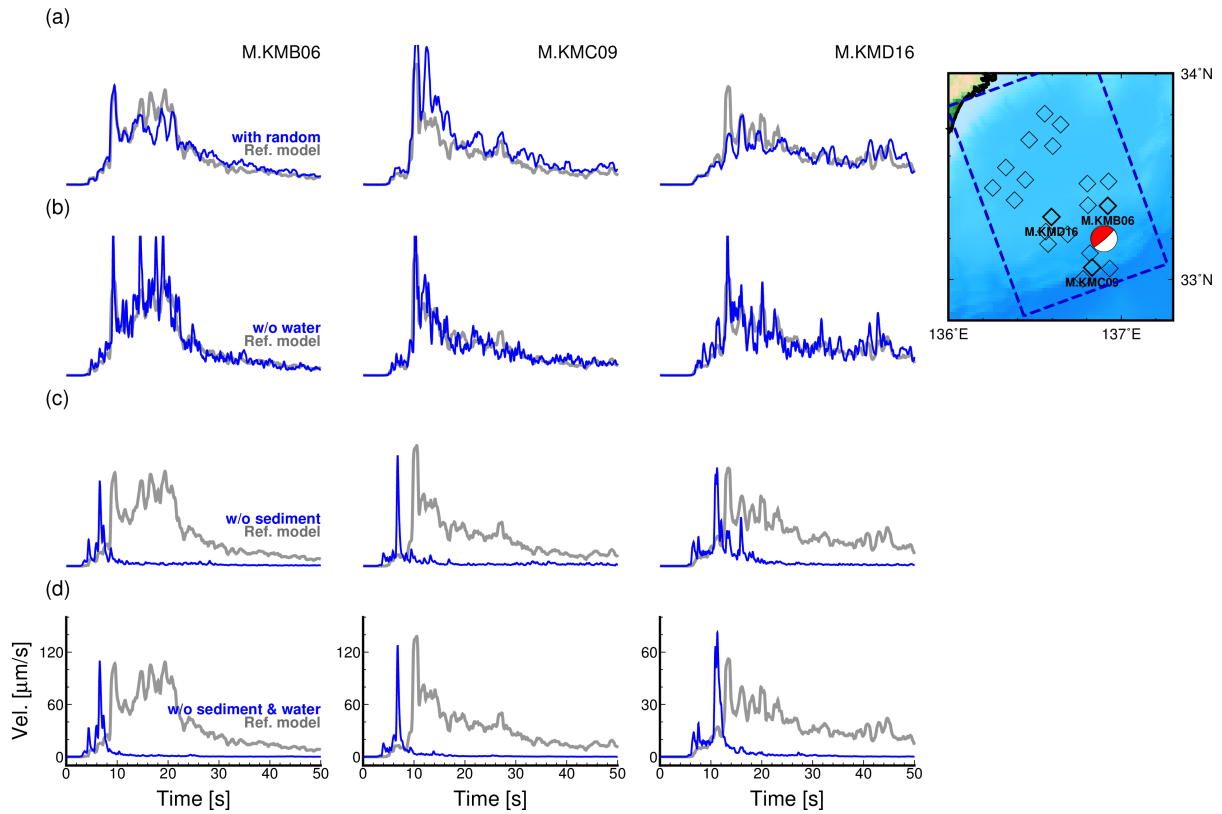
637

638

639

640

Figure 9. Spatial variations of maximum RMS amplitudes and half-value widths of simulated RMS envelopes for an interplate earthquake: (a) an example of half-value width estimations, (b) maximum RMS amplitude distribution, (c) half-value width distribution, and (d) half-value widths as a function of epicentral distance. The example in (b) is an RMS envelope at M.MRB06 (location shown in (a)). The red dashed and solid lines in (d) are values of t_q via the method of Sato & Emoto (2018). Here, t_q is defined as the time between S -wave onset and the time when the RMS envelope decays to half the maximum amplitude. The assumed small-scale random velocity heterogeneity models for dashed and solid lines are characterized by an exponential-type autocorrelation function with correlation length of 1 km and RMS values of 0.03 and 0.05, respectively. The central frequency in theoretical synthetics is 4 Hz.



641

642

643

644

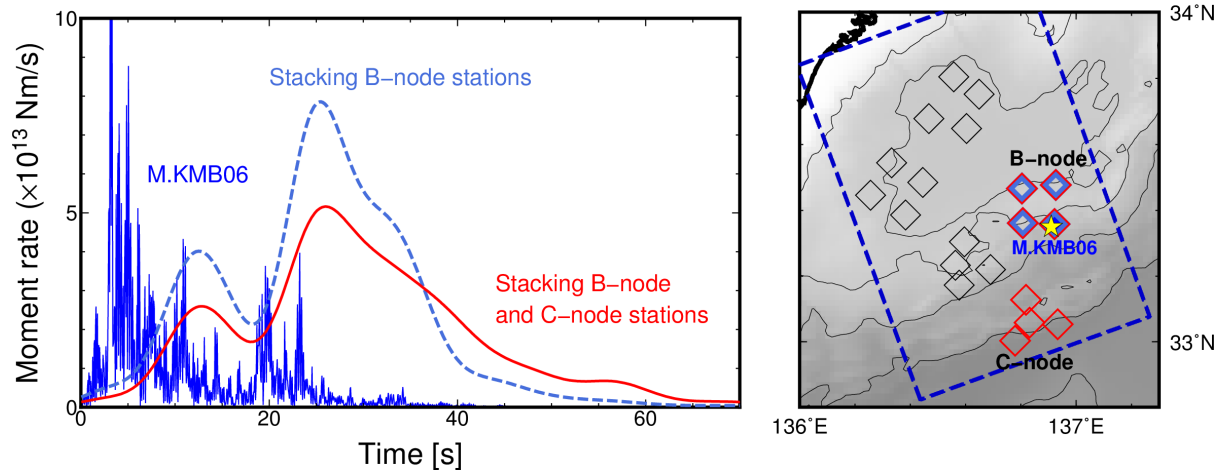
645

646

647

648

Figure 10. Simulation results for various heterogeneous models of a shallow LFT. The blue lines are RMS envelopes derived from models (a) with small-scale random velocity heterogeneities, (b) without seawater, (c) without oceanic sediments (accretionary prism), and (d) without oceanic sediments and seawater. Grey lines are the simulation results with the reference model.



649

650

651

652

653

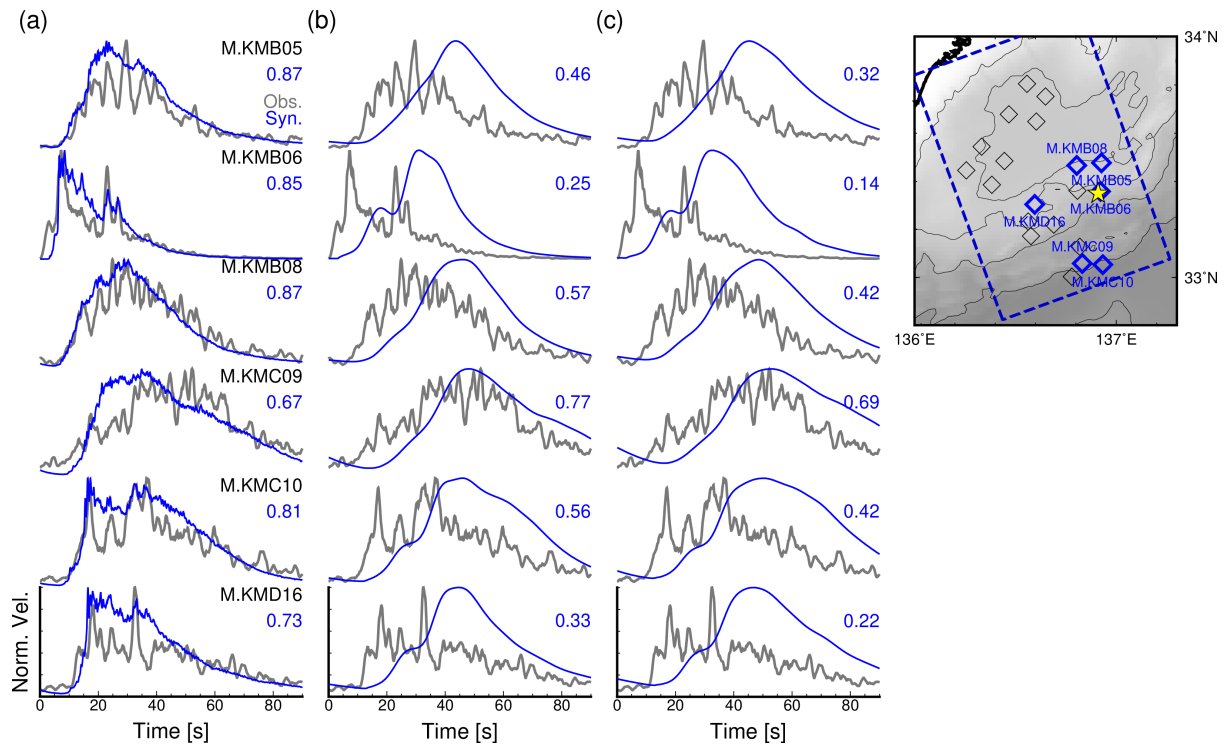
654

655

656

657

Figure 11. Source time functions (STFs) estimated from observed RMS envelopes of a shallow LFT at 11:18 on 24 October 2015 (JST). The blue dashed, blue, and red lines are source time functions estimated from the RMS envelope of M.KMB06, envelopes of B-node stations, and envelopes of B- and C-node stations, respectively. The yellow star on the map is the epicentre. The epicentral distance of M.KMB06 was 1.4 km. The stations represented by coloured symbols were used in the STF estimation for corresponding coloured lines.



658

659

660

661

662

663

664

665

666

667

668

Figure 12. Comparison between simulated RMS envelopes with observations. The RMS envelopes were synthesized from simulation results of source time functions estimated by using (a) M.KMB06, (b) B-node stations, and (c) B- and C-node stations. Because the precise seismic moment for the target shallow LFT and site amplification factors were not well known, the amplitudes of each trace were normalized by each maximum amplitude. The numbers written by blue characters are cross-correlation coefficients between observed and synthesized envelopes at each station. The upper-right panel shows the stations used (blue diamonds) and the epicentre location (yellow star).

669 **References**

- 670 Aki, K., & Richards, P. (2002). *Quantitative Seismology* (2nd ed.). University Science Books.
671 Retrieved from https://www.ldeo.columbia.edu/~richards/Aki_Richards.html
- 672 Amante, C., & Eakins, B. W. (2009). ETOPO1 1 arc-minute global relief model: Procedures,
673 data sources and analysis. NOAA Technical Memorandum NESDIS NGDC-24. *NOAA*
674 *Technical Memorandum NESDIS NGDC-24. National Geophysical Data Center, NOAA,*
675 (March), 19. <https://doi.org/10.7289/V5C8276M>
- 676 Ando, M. (1975). Source mechanisms and tectonic significance of historical earthquakes
677 along the Nankai trough, Japan. *Tectonophysics*, 27(2), 119–140.
678 [https://doi.org/10.1016/0040-1951\(75\)90102-X](https://doi.org/10.1016/0040-1951(75)90102-X)
- 679 Annoura, S., Obara, K., & Maeda, T. (2016). Total energy of deep low-frequency tremor in
680 the Nankai subduction zone, southwest Japan. *Geophysical Research Letters*, 43(6),
681 2562–2567. <https://doi.org/10.1002/2016GL067780>
- 682 Annoura, S., Hashimoto, T., Kamaya, N., & Katsumata, A. (2017). Shallow episodic tremor
683 near the Nankai Trough axis off southeast Mie prefecture, Japan. *Geophysical Research*
684 *Letters*, 44(8), 3564–3571. <https://doi.org/10.1002/2017GL073006>
- 685 Araki, E., Saffer, D. M., Kopf, A. J., Wallace, L. M., Kimura, T., Machida, Y., et al. (2017).
686 Recurring and triggered slow-slip events near the trench at the Nankai Trough
687 subduction megathrust. *Science*, 356(6343), 1157–1160.
688 <https://doi.org/10.1126/science.aan3120>
- 689 Battaglia, J., & Aki, K. (2003). Location of seismic events and eruptive fissures on the Piton
690 de la Fournaise volcano using seismic amplitudes. *Journal of Geophysical Research*,
691 108(B8), 2364. <https://doi.org/10.1029/2002JB002193>
- 692 Carcolé, E., & Sato, H. (2010). Spatial distribution of scattering loss and intrinsic absorption
693 of short-period S waves in the lithosphere of Japan on the basis of the Multiple Lapse
694 Time Window Analysis of Hi-net data. *Geophysical Journal International*, 180(1), 268–
695 290. <https://doi.org/10.1111/j.1365-246X.2009.04394.x>
- 696 Chaput, J., Campillo, M., Aster, R. C., Roux, P., Kyle, P. R., Knox, H., & Czoski, P. (2015).
697 Multiple scattering from icequakes at Erebus volcano, Antarctica: Implications for
698 imaging at glaciated volcanoes. *Journal of Geophysical Research: Solid Earth*, 120(2),
699 1129–1141. <https://doi.org/10.1002/2014JB011278>
- 700 Ekström, G., Nettles, M., & Dziewoński, A. M. (2012). The global CMT project 2004-2010:
701 Centroid-moment tensors for 13,017 earthquakes. *Physics of the Earth and Planetary*
702 *Interiors*, 200–201, 1–9. <https://doi.org/10.1016/j.pepi.2012.04.002>
- 703 Ellsworth, W. L., & Bulut, F. (2018). Nucleation of the 1999 Izmit earthquake by a triggered
704 cascade of foreshocks. *Nature Geoscience*, 11(7), 531–535.
705 <https://doi.org/10.1038/s41561-018-0145-1>
- 706 Fletcher, J. B., & McGarr, A. (2011). Moments, magnitudes, and radiated energies of non-

707 volcanic tremor near Cholame, CA, from ground motion spectra at UPSAR.
708 *Geophysical Research Letters*, 38(16), n/a-n/a. <https://doi.org/10.1029/2011GL048636>

709 Furumura, T., & Kennett, B. L. N. (2005). Subduction zone guided waves and the
710 heterogeneity structure of the subducted plate: Intensity anomalies in northern Japan.
711 *Journal of Geophysical Research*, 110(B10), B10302.
712 <https://doi.org/10.1029/2004JB003486>

713 Furumura, Takashi, & Kennett, B. L. N. (2018). Regional Distance PL Phase in the Crustal
714 Waveguide-An Analog to the Teleseismic W Phase in the Upper-Mantle Waveguide.
715 *Journal of Geophysical Research: Solid Earth*, 123(5), 4007–4024.
716 <https://doi.org/10.1029/2018JB015717>

717 Ghosh, A., Vidale, J. E., Sweet, J. R., Creager, K. C., & Wech, A. G. (2009). Tremor patches
718 in Cascadia revealed by seismic array analysis. *Geophysical Research Letters*, 36(17),
719 L17316. <https://doi.org/10.1029/2009GL039080>

720 Gomberg, J. (2018). Cascadia Onshore-Offshore Site Response, Submarine Sediment
721 Mobilization, and Earthquake Recurrence. *Journal of Geophysical Research: Solid*
722 *Earth*, 123(2), 1381–1404. <https://doi.org/10.1002/2017JB014985>

723 Gomberg, J., Wech, A., Creager, K., Obara, K., & Agnew, D. (2016). Reconsidering
724 earthquake scaling. *Geophysical Research Letters*, 43(12), 6243–6251.
725 <https://doi.org/10.1002/2016GL069967>

726 Gusev, A. A., & Pavlov, V. M. (1991). Deconvolution of squared velocity waveform as
727 applied to the study of a noncoherent short-period radiator in the earthquake source.
728 *Pure and Applied Geophysics*, 136(2–3), 235–244. <https://doi.org/10.1007/BF00876375>

729 Haney, M. M., & Tsai, V. C. (2017). Perturbational and nonperturbational inversion of
730 Rayleigh-wave velocities. *GEOPHYSICS*, 82(3), F15–F28.
731 <https://doi.org/10.1190/geo2016-0397.1>

732 Hawthorne, J. C., Thomas, A. M., & Ampuero, J.-P. (2019). The rupture extent of low
733 frequency earthquakes near Parkfield, CA. *Geophysical Journal International*, 216(1),
734 621–639. <https://doi.org/10.1093/gji/ggy429>

735 Hejrani, B., Tkalčić, H., & Fichtner, A. (2017). Centroid moment tensor catalogue using a 3-
736 D continental scale Earth model: Application to earthquakes in Papua New Guinea and
737 the Solomon Islands. *Journal of Geophysical Research: Solid Earth*, 122(7), 5517–5543.
738 <https://doi.org/10.1002/2017JB014230>

739 Helffrich, G., Wookey, J., & Bastow, I. (2013). *The Seismic Analysis Code*. Cambridge:
740 Cambridge University Press. <https://doi.org/10.1017/CBO9781139547260>

741 Ide, S. (2010). Striations, duration, migration and tidal response in deep tremor. *Nature*,
742 466(7304), 356–359. <https://doi.org/10.1038/nature09251>

743 Ide, S., & Maury, J. (2018). Seismic Moment, Seismic Energy, and Source Duration of Slow
744 Earthquakes: Application of Brownian slow earthquake model to three major subduction

745 zones. *Geophysical Research Letters*, 45(7), 3059–3067.
746 <https://doi.org/10.1002/2018GL077461>

747 Ide, S., & Yabe, S. (2014). Universality of slow earthquakes in the very low frequency band.
748 *Geophysical Research Letters*, 41(8), 2786–2793.
749 <https://doi.org/10.1002/2014GL059712>

750 Ide, S., Beroza, G. C., Prejean, S. G., & Ellsworth, W. L. (2003). Apparent break in
751 earthquake scaling due to path and site effects on deep borehole recordings. *Journal of*
752 *Geophysical Research: Solid Earth*, 108(B5). <https://doi.org/10.1029/2001JB001617>

753 Ide, S., Imanishi, K., Yoshida, Y., Beroza, G. C., & Shelly, D. R. (2008). Bridging the gap
754 between seismically and geodetically detected slow earthquakes. *Geophysical Research*
755 *Letters*, 35(10), 2–7. <https://doi.org/10.1029/2008GL034014>

756 Imperatori, W., & Mai, P. M. (2013). Broad-band near-field ground motion simulations in 3-
757 dimensional scattering media. *Geophysical Journal International*, 192(2), 725–744.
758 <https://doi.org/10.1093/gji/ggs041>

759 Imperatori, W., & Mai, P. M. (2015). The role of topography and lateral velocity
760 heterogeneities on near-source scattering and ground-motion variability. *Geophysical*
761 *Journal International*, 202(3), 2163–2181. <https://doi.org/10.1093/gji/ggv281>

762 Iwaki, A., Maeda, T., Morikawa, N., Takemura, S., & Fujiwara, H. (2018). Effects of random
763 3D upper crustal heterogeneity on long-period (≥ 1 s) ground-motion simulations. *Earth,*
764 *Planets and Space*, 70(1), 156. <https://doi.org/10.1186/s40623-018-0930-5>

765 Kanamori, H., & Rivera, L. (2008). Source inversion of W phase: Speeding up seismic
766 tsunami warning. *Geophysical Journal International*, 175(1), 222–238.
767 <https://doi.org/10.1111/j.1365-246X.2008.03887.x>

768 Kaneko, Y., Ito, Y., Chow, B., Wallace, L. M., Tape, C., Grapenthin, R., et al. (2019). Ultra-
769 long Duration of Seismic Ground Motion Arising From a Thick, Low-Velocity
770 Sedimentary Wedge. *Journal of Geophysical Research: Solid Earth*, 124(10), 10347–
771 10359. <https://doi.org/10.1029/2019JB017795>

772 Kano, M., Aso, N., Matsuzawa, T., Ide, S., Annoura, S., Arai, R., et al. (2018). Development
773 of a Slow Earthquake Database. *Seismological Research Letters*, 89(4), 1566–1575.
774 <https://doi.org/10.1785/0220180021>

775 Kao, H., Wang, K., Dragert, H., Kao, J. Y., & Rogers, G. (2010). Estimating seismic moment
776 magnitude (M_w) of tremor bursts in northern Cascadia: Implications for the “seismic
777 efficiency” of episodic tremor and slip. *Geophysical Research Letters*, 37(19), n/a-n/a.
778 <https://doi.org/10.1029/2010GL044927>

779 Kato, A., Obara, K., Igarashi, T., Tsuruoka, H., Nakagawa, S., & Hirata, N. (2012).
780 Propagation of slow slip leading up to the 2011 Mw9.0 Tohoku-Oki earthquake.
781 *Science*, 335(6069), 705–708. <https://doi.org/10.1126/science.1215141>

782 Koketsu, K., Miyake, H., & Suzuki, H. (2012). Japan Integrated Velocity Structure Model

783 Version 1. *Proceedings of the 15th World Conference on Earthquake Engineering*, 1–4.
784 Retrieved from http://www.iitk.ac.in/nicee/wcee/article/WCEE2012_1773.pdf
785 Kubo, H., Nakamura, T., Suzuki, W., Kimura, T., Kunugi, T., Takahashi, N., & Aoi, S.
786 (2018). Site Amplification Characteristics at Nankai Seafloor Observation Network,
787 DONET1, Japan, Evaluated Using Spectral Inversion. *Bulletin of the Seismological*
788 *Society of America*, XX(Xx), 1–9. <https://doi.org/10.1785/0120170254>
789 Kumagai, H., Lacson, R., Maeda, Y., Figueroa, M. S., Yamashina, T., Ruiz, M., et al. (2013).
790 Source amplitudes of volcano-seismic signals determined by the amplitude source
791 location method as a quantitative measure of event size. *Journal of Volcanology and*
792 *Geothermal Research*, 257, 57–71. <https://doi.org/10.1016/j.jvolgeores.2013.03.002>
793 Kurokawa, A., Takeo, M., & Kurita, K. (2016). Two types of volcanic tremor changed with
794 eruption style during 1986 Izu-Oshima eruption. *Journal of Geophysical Research:*
795 *Solid Earth*, 121(4), 2727–2736. <https://doi.org/10.1002/2015JB012500>
796 Maeda, T., & Obara, K. (2009). Spatiotemporal distribution of seismic energy radiation from
797 low-frequency tremor in western Shikoku, Japan. *Journal of Geophysical Research:*
798 *Solid Earth*, 114(10). <https://doi.org/10.1029/2008JB006043>
799 Maeda, T., Takemura, S., & Furumura, T. (2017). OpenSWPC: an open-source integrated
800 parallel simulation code for modeling seismic wave propagation in 3D heterogeneous
801 viscoelastic media. *Earth, Planets and Space*, 69(1), 102.
802 <https://doi.org/10.1186/s40623-017-0687-2>
803 Margerin, L. (2005). Introduction to radiative transfer of seismic waves. *Geophysical*
804 *Monograph Series*, 157(January 2005), 229–252. <https://doi.org/10.1029/157GM14>
805 Morioka, H., Kumagai, H., & Maeda, T. (2017). Theoretical basis of the amplitude source
806 location method for volcano-seismic signals. *Journal of Geophysical Research: Solid*
807 *Earth*, 122(8), 6538–6551. <https://doi.org/10.1002/2017JB013997>
808 Muzyert, E. (2007). Seabed property estimation from ambient-noise recordings: Part I —
809 Compliance and Scholte wave phase-velocity measurements. *GEOPHYSICS*, 72(2),
810 U21–U26. <https://doi.org/10.1190/1.2435587>
811 Nakahara, H. (2008). Chapter 15 Seismogram Envelope Inversion for High-Frequency
812 Seismic Energy Radiation from Moderate-to-Large Earthquakes. In *Advances in*
813 *Geophysics* (Vol. 50, pp. 401–426). [https://doi.org/10.1016/S0065-2687\(08\)00015-0](https://doi.org/10.1016/S0065-2687(08)00015-0)
814 Nakahara, H. (2013). Envelope inversion analysis for high-frequency seismic energy
815 radiation from the 2011 Mw 9.0 Off the Pacific Coast of Tohoku earthquake. *Bulletin of*
816 *the Seismological Society of America*, 103(2 B), 1348–1359.
817 <https://doi.org/10.1785/0120120155>
818 Nakamura, T., Takenaka, H., Okamoto, T., Ohori, M., & Tsuboi, S. (2015). Long-period
819 ocean-bottom motions in the source areas of large subduction earthquakes. *Scientific*
820 *Reports*, 5, 1–2. <https://doi.org/10.1038/srep16648>

- 821 Nakano, M., Kumagai, H., & Inoue, H. (2008). Waveform inversion in the frequency domain
822 for the simultaneous determination of earthquake source mechanism and moment
823 function. *Geophysical Journal International*, 173(3), 1000–1011.
824 <https://doi.org/10.1111/j.1365-246X.2008.03783.x>
- 825 Nakano, M., Tonegawa, T., & Kaneda, Y. (2012). Orientations of DONET seismometers
826 estimated from seismic waveforms. *JAMSTEC Report of Research and Development*,
827 15(0), 77–89. <https://doi.org/10.5918/jamstecr.15.77>
- 828 Nakano, M., Nakamura, T., & Kaneda, Y. (2015). Hypocenters in the Nankai trough
829 determined by using data from both ocean-bottom and land seismic networks and a 3D
830 velocity structure model: Implications for seismotectonic activity. *Bulletin of the*
831 *Seismological Society of America*, 105(3), 1594–1605.
832 <https://doi.org/10.1785/0120140309>
- 833 Nakano, M., Hori, T., Araki, E., Kodaira, S., & Ide, S. (2018). Shallow very-low-frequency
834 earthquakes accompany slow slip events in the Nankai subduction zone. *Nature*
835 *Communications*, 9(1), 984. <https://doi.org/10.1038/s41467-018-03431-5>
- 836 Nakano, M., Hyodo, M., Nakanishi, A., Yamashita, M., Hori, T., Kamiya, S., et al. (2018).
837 The 2016 Mw 5.9 earthquake off the southeastern coast of Mie Prefecture as an
838 indicator of preparatory processes of the next Nankai Trough megathrust earthquake.
839 *Progress in Earth and Planetary Science*, 5(1), 30. [https://doi.org/10.1186/s40645-018-](https://doi.org/10.1186/s40645-018-0188-3)
840 [0188-3](https://doi.org/10.1186/s40645-018-0188-3)
- 841 Nakano, M., Yabe, S., Sugioka, H., Shinohara, M., & Ide, S. (2019). Event Size Distribution
842 of Shallow Tectonic Tremor in the Nankai Trough. *Geophysical Research Letters*,
843 46(11), 5828–5836. <https://doi.org/10.1029/2019GL083029>
- 844 National Research Institute for Earth Science and Disaster Resilience. (2019a). NIED
845 DONET. <https://doi.org/10.17598/NIED.0008>
- 846 National Research Institute for Earth Science and Disaster Resilience. (2019b). NIED F-net.
847 <https://doi.org/10.17598/NIED.0005>
- 848 National Research Institute for Earth Science and Disaster Resilience. (2019c). NIED S-net.
849 <https://doi.org/10.17598/NIED.0007>
- 850 Nishida, K. (2017). Ambient seismic wave field. *Proceedings of the Japan Academy, Series*
851 *B*, 93(7), 423–448. <https://doi.org/10.2183/pjab.93.026>
- 852 Nishikawa, T., Matsuzawa, T., Ohta, K., Uchida, N., Nishimura, T., & Ide, S. (2019). The
853 slow earthquake spectrum in the Japan Trench illuminated by the S-net seafloor
854 observatories. *Science*, 365(August), 808–813. <https://doi.org/10.1126/science.aax5618>
- 855 Noguchi, S., Maeda, T., & Furumura, T. (2016). Ocean-influenced Rayleigh waves from
856 outer-rise earthquakes and their effects on durations of long-period ground motion.
857 *Geophysical Journal International*, 205(2), 1099–1107.
858 <https://doi.org/10.1093/gji/ggw074>

859 Obara, K., & Maeda, T. (2009). Reverse propagation of T waves from the Emperor seamount
860 chain. *Geophysical Research Letters*, 36(8), 1–5. <https://doi.org/10.1029/2009GL037454>

861 Okal, E. A. (2008). The generation of T waves by earthquakes (pp. 1–65).
862 [https://doi.org/10.1016/S0065-2687\(07\)49001-X](https://doi.org/10.1016/S0065-2687(07)49001-X)

863 Peng, Z., & Zhao, P. (2009). Migration of early aftershocks following the 2004 Parkfield
864 earthquake. *Nature Geoscience*, 2(12), 877–881. <https://doi.org/10.1038/ngeo697>

865 Petukhin, A., Miyakoshi, K., Tsurugi, M., Kawase, H., & Kamae, K. (2016). Visualization of
866 Green ' s function anomalies for megathrust source in Nankai Trough by reciprocity
867 method. *Earth, Planets and Space*. <https://doi.org/10.1186/s40623-016-0385-5>

868 Petukhin, A. G., Nakahara, H., & Gusev, A. A. (2004). Inversion of the high-frequency
869 source radiation of M6 . 8 Avachinsky Gulf , Kamchatka , earthquake using empirical
870 and theoretical envelope Green functions, (1998), 921–925.

871 Poiata, N., Vilotte, J.-P., Bernard, P., Satriano, C., & Obara, K. (2018). Imaging different
872 components of a tectonic tremor sequence in southwestern Japan using an automatic
873 statistical detection and location method. *Geophysical Journal International*, (February).
874 <https://doi.org/10.1093/gji/ggy070/4898035>

875 Przybilla, J., Wegler, U., & Korn, M. (2009). Estimation of crustal scattering parameters with
876 elastic radiative transfer theory. *Geophysical Journal International*, 178(2), 1105–1111.
877 <https://doi.org/10.1111/j.1365-246X.2009.04204.x>

878 Saito, T., Sato, H., & Ohtake, M. (2002). Envelope broadening of spherically outgoing waves
879 in three-dimensional random media having power law spectra. *Journal of Geophysical*
880 *Research*, 107(B5), 2089. <https://doi.org/10.1029/2001JB000264>

881 Saito, T., Sato, H., Ohtake, M., & Obara, K. (2005). Unified explanation of envelope
882 broadening and maximum-amplitude decay high-frequency seismograms based on the
883 envelope simulation using the Markov approximation: Forearc side of the volcanic front
884 in northeastern Honshu, Japan. *Journal of Geophysical Research B: Solid Earth*, 110(1),
885 1–18. <https://doi.org/10.1029/2004JB003225>

886 Sakai, S., Yamada, T., Shinohara, M., Hagiwara, H., Kanazawa, T., Obana, K., et al. (2005).
887 Urgent aftershock observation of the 2004 off the Kii Peninsula earthquake using ocean
888 bottom seismometers. *Earth Planets and Space*, 57, 363–368.
889 <https://doi.org/10.1186/BF03352577>

890 Sato, H., & Emoto, K. (2018). Synthesis of a Scalar Wavelet Intensity Propagating Through
891 von Kármán-type Random Media: Radiative Transfer Theory Using the Born and Phase-
892 Screen Approximations. *Geophysical Journal International*, 909–923.
893 <https://doi.org/10.1093/gji/ggy319>

894 Sato, H., Fehler, M. C., & Maeda, T. (2012). Seismic Wave Propagation and Scattering in the
895 Heterogeneous Earth : Second Edition. In *Seismic Wave Propagation and Scattering in*
896 *the Heterogeneous Earth : Second Edition*. Berlin, Heidelberg: Springer Berlin

897 Heidelberg. https://doi.org/10.1007/978-3-642-23029-5_2

898 Sawazaki, K., & Enescu, B. (2014). Imaging the high-frequency energy radiation process of a
 899 main shock and its early aftershock sequence: The case of the 2008 Iwate-Miyagi
 900 Nairiku earthquake, Japan. *Journal of Geophysical Research: Solid Earth*, *119*(6),
 901 4729–4746. <https://doi.org/10.1002/2013JB010539>

902 Shapiro, N. M., Campillo, M., Singh, S. K., & Pacheco, J. (1998). Seismic channel waves in
 903 the accretionary prism of the Middle America Trench. *Geophysical Research Letters*,
 904 *25*(1), 101–104. <https://doi.org/10.1029/97GL03492>

905 Shapiro, N. M., Olsen, K. B., & Singh, S. K. (2000). Wave-guide effects in subduction zones:
 906 Evidence from three-dimensional modeling. *Geophysical Research Letters*, *27*(3), 433–
 907 436. <https://doi.org/10.1029/1999GL010982>

908 Staudenmaier, N., Edwards, B., Tormann, T., Zechar, J. D., & Wiemer, S. (2016). Spatial
 909 distribution and energy release of nonvolcanic tremor at Parkfield, California. *Journal of*
 910 *Geophysical Research: Solid Earth*, *121*(12), 8833–8854.
 911 <https://doi.org/10.1002/2016JB013283>

912 Supino, M., Poiata, N., Festa, G., Vilotte, J. P., Satriano, C., & Obara, K. (2020). Self-
 913 similarity of low-frequency earthquakes. *Scientific Reports*, *10*(1), 1–9.
 914 <https://doi.org/10.1038/s41598-020-63584-6>

915 Takahashi, D. (2013). Implementation of Parallel 1-D FFT on GPU Clusters. In *2013 IEEE*
 916 *16th International Conference on Computational Science and Engineering* (pp. 174–
 917 180). IEEE. <https://doi.org/10.1109/CSE.2013.36>

918 Takahashi, T., Sato, H., Nishimura, T., & Obara, K. (2007). Strong inhomogeneity beneath
 919 quaternary volcanoes revealed from the peak delay analysis of S-wave seismograms of
 920 microearthquakes in northeastern Japan. *Geophysical Journal International*, *168*(1), 90–
 921 99. <https://doi.org/10.1111/j.1365-246X.2006.03197.x>

922 Takahashi, T., Sato, H., Nishimura, T., & Obara, K. (2009). Tomographic inversion of the
 923 peak delay times to reveal random velocity fluctuations in the lithosphere: Method and
 924 application to northeastern Japan. *Geophysical Journal International*, *178*(3), 1437–
 925 1455. <https://doi.org/10.1111/j.1365-246X.2009.04227.x>

926 Takemura, S., & Yoshimoto, K. (2014). Strong seismic wave scattering in the low-velocity
 927 anomaly associated with subduction of oceanic plate. *Geophysical Journal*
 928 *International*, *197*(2), 1016–1032. <https://doi.org/10.1093/gji/ggu031>

929 Takemura, S., Furumura, T., & Saito, T. (2009). Distortion of the apparent S -wave radiation
 930 pattern in the high-frequency wavefield: Tottori-Ken Seibu, Japan, earthquake of 2000.
 931 *Geophysical Journal International*, *178*(2), 950–961. <https://doi.org/10.1111/j.1365-246X.2009.04210.x>

932

933 Takemura, S., Furumura, T., & Maeda, T. (2015). Scattering of high-frequency seismic
 934 waves caused by irregular surface topography and small-scale velocity inhomogeneity.

- 935 *Geophysical Journal International*, 201(1), 459–474. <https://doi.org/10.1093/gji/ggv038>
- 936 Takemura, S., Kobayashi, M., & Yoshimoto, K. (2016). Prediction of maximum P- and S-
937 wave amplitude distributions incorporating frequency- and distance-dependent
938 characteristics of the observed apparent radiation patterns. *Earth, Planets and Space*,
939 68(1), 166. <https://doi.org/10.1186/s40623-016-0544-8>
- 940 Takemura, S., Kobayashi, M., & Yoshimoto, K. (2017). High-frequency seismic wave
941 propagation within the heterogeneous crust: effects of seismic scattering and intrinsic
942 attenuation on ground motion modelling. *Geophysical Journal International*, 210(3),
943 1806–1822. <https://doi.org/10.1093/gji/ggx269>
- 944 Takemura, S., Kubo, H., Tonegawa, T., Saito, T., & Shiomi, K. (2019). Modeling of Long-
945 Period Ground Motions in the Nankai Subduction Zone: Model Simulation Using the
946 Accretionary Prism Derived from Oceanfloor Local S-Wave Velocity Structures. *Pure
947 and Applied Geophysics*, 176(2), 627–647. <https://doi.org/10.1007/s00024-018-2013-8>
- 948 Takemura, S., Yoshimoto, K., & Tonegawa, T. (2015). Scattering of trapped P and S waves
949 in the hydrated subducting crust of the Philippine Sea plate at shallow depths beneath
950 the Kanto region, Japan. *Geophysical Journal International*, 203(3), 2261–2276.
951 <https://doi.org/10.1093/gji/ggv423>
- 952 Takemura, S., Shiomi, K., Kimura, T., & Saito, T. (2016). Systematic difference between
953 first-motion and waveform-inversion solutions for shallow offshore earthquakes due to a
954 low-angle dipping slab. *Earth, Planets and Space*, 68(1), 149.
955 <https://doi.org/10.1186/s40623-016-0527-9>
- 956 Takemura, S., Matsuzawa, T., Noda, A., Tonegawa, T., Asano, Y., Kimura, T., & Shiomi, K.
957 (2019). Structural Characteristics of the Nankai Trough Shallow Plate Boundary
958 Inferred From Shallow Very Low Frequency Earthquakes. *Geophysical Research
959 Letters*, 46(8), 4192–4201. <https://doi.org/10.1029/2019GL082448>
- 960 Takemura, S., Okuwaki, R., Kubota, T., Shiomi, K., Kimura, T., & Noda, A. (2020). Centroid
961 moment tensor inversions of offshore earthquakes using a three-dimensional velocity
962 structure model: slip distributions on the plate boundary along the Nankai Trough.
963 *Geophysical Journal International*, 222(2), 1109–1125.
964 <https://doi.org/10.1093/gji/ggaa238>
- 965 Takeo, A., Forsyth, D. W., Weeraratne, D. S., & Nishida, K. (2014). Estimation of azimuthal
966 anisotropy in the NW Pacific from seismic ambient noise in seafloor records.
967 *Geophysical Journal International*, 199(1), 11–22. <https://doi.org/10.1093/gji/ggu240>
- 968 Tamaribuchi, K., Kobayashi, A., Nishimiya, T., Hirose, F., & Annoura, S. (2019).
969 Characteristics of shallow low-frequency earthquakes off the Kii Peninsula, Japan, in
970 2004 revealed by ocean bottom seismometers. *Geophysical Research Letters*,
971 2019GL085158. <https://doi.org/10.1029/2019GL085158>
- 972 Tanaka, S., Matsuzawa, T., & Asano, Y. (2019). Shallow Low-Frequency Tremor in the

973 Northern Japan Trench Subduction Zone. *Geophysical Research Letters*, 46(10), 5217–
974 5224. <https://doi.org/10.1029/2019GL082817>

975 Thomas, A. M., Beroza, G. C., & Shelly, D. R. (2016). Constraints on the source parameters
976 of low-frequency earthquakes on the San Andreas Fault. *Geophysical Research Letters*,
977 43(4), 1464–1471. <https://doi.org/10.1002/2015GL067173>

978 Toh, A., Obana, K., & Araki, E. (2018). Distribution of very low frequency earthquakes in
979 the Nankai accretionary prism influenced by a subducting-ridge. *Earth and Planetary
980 Science Letters*, 482(March 2011), 342–356. <https://doi.org/10.1016/j.epsl.2017.10.062>

981 Tonegawa, T., Fukao, Y., Takahashi, T., Obana, K., Kodaira, S., & Kaneda, Y. (2015).
982 Ambient seafloor noise excited by earthquakes in the Nankai subduction zone. *Nature
983 Communications*, 6, 1–7. <https://doi.org/10.1038/ncomms7132>

984 Tonegawa, T., Fukao, Y., Fujie, G., Takemura, S., Takahashi, T., & Kodaira, S. (2015).
985 Geographical distribution of shear wave anisotropy within marine sediments in the
986 northwestern Pacific. *Progress in Earth and Planetary Science*, 2(1), 27.
987 <https://doi.org/10.1186/s40645-015-0057-2>

988 Tonegawa, T., Araki, E., Kimura, T., Nakamura, T., Nakano, M., & Suzuki, K. (2017).
989 Sporadic low-velocity volumes spatially correlate with shallow very low frequency
990 earthquake clusters. *Nature Communications*, 8(1), 2048.
991 <https://doi.org/10.1038/s41467-017-02276-8>

992 Tripathi, J. N., Sato, H., & Yamamoto, M. (2010). Envelope broadening characteristics of
993 crustal earthquakes in northeastern Honshu, Japan. *Geophysical Journal International*,
994 182(2), 988–1000. <https://doi.org/10.1111/j.1365-246X.2010.04657.x>

995 Uchide, T., & Ide, S. (2010). Scaling of earthquake rupture growth in the Parkfield area: Self-
996 similar growth and suppression by the finite seismogenic layer. *Journal of Geophysical
997 Research: Solid Earth*, 115(11), 1–15. <https://doi.org/10.1029/2009JB007122>

998 Volk, O., Shani-kadmiel, S., Gvirtzman, Z., & Tsesarsky, M. (2017). 3D Effects of
999 Sedimentary Wedges and Subsurface Canyons : Ground-Motion Amplification in the
1000 Israeli Coastal Plain, 107(3). <https://doi.org/10.1785/0120160349>

1001 Wallace, L. M., Araki, E., Saffer, D., Wang, X., Roesner, A., Kopf, A., et al. (2016). Near-
1002 field observations of an offshore M w 6.0 earthquake from an integrated seafloor and
1003 subseafloor monitoring network at the Nankai Trough, southwest Japan. *Journal of
1004 Geophysical Research: Solid Earth*, 121(11), 8338–8351.
1005 <https://doi.org/10.1002/2016JB013417>

1006 Wang, X., & Zhan, Z. (2020). Moving from 1-D to 3-D velocity model: automated
1007 waveform-based earthquake moment tensor inversion in the Los Angeles region.
1008 *Geophysical Journal International*, 220(1), 218–234. <https://doi.org/10.1093/gji/ggz435>

1009 Wegler, U., Korn, M., & Przybilla, J. (2006). Modeling Full Seismogram Envelopes Using
1010 Radiative Transfer Theory with Born Scattering Coefficients. *Pure and Applied*

1011 *Geophysics*, 163(2–3), 503–531. <https://doi.org/10.1007/s00024-005-0027-5>

1012 Wessel, P., Smith, W. H. F., Scharroo, R., Luis, J., & Wobbe, F. (2013). Generic mapping
1013 tools: Improved version released. *Eos*, 94(45), 409–410.
1014 <https://doi.org/10.1002/2013EO450001>

1015 Yabe, S., & Ide, S. (2014). Spatial distribution of seismic energy rate of tectonic tremors in
1016 subduction zones. *Journal of Geophysical Research: Solid Earth*, 119(11), 8171–8185.
1017 <https://doi.org/10.1002/2014JB011383>

1018 Yabe, S., Tonegawa, T., & Nakano, M. (2019). Scaled Energy Estimation for Shallow Slow
1019 Earthquakes. *Journal of Geophysical Research: Solid Earth*, 124(2), 1507–1519.
1020 <https://doi.org/10.1029/2018JB016815>

1021 Yoshimoto, K., Takemura, S., & Kobayashi, M. (2015). Application of scattering theory to P-
1022 wave amplitude fluctuations in the crust. *Earth, Planets and Space*, 67(1), 199.
1023 <https://doi.org/10.1186/s40623-015-0366-0>

1024 Zhang, W., & Shen, Y. (2010). Unsplit complex frequency-shifted PML implementation
1025 using auxiliary differential equations for seismic wave modeling. *GEOPHYSICS*, 75(4),
1026 T141–T154. <https://doi.org/10.1190/1.3463431>

1027

1 **Supporting information:**

2 **Modelling high-frequency seismograms at ocean bottom seismometers:**
3 **effects of heterogeneous structures on source parameter estimation of small**
4 **offshore earthquakes and shallow low-frequency tremors**

5
6 **Authors**

7 **Shunsuke TAKEMURA^{1*}, Suguru YABE², Kentaro EMOTO³**

8 **¹Earthquake Research Institute, the University of Tokyo, 1-1-1 Yayoi, Bunkyo-ku,**
9 **Tokyo, 113-0032, Japan**

10 **²Geological Survey of Japan, National Institute of Advanced Industrial Science and**
11 **Technology, Tsukuba Central 7, 1-1-1 Higashi, Tsukuba, Ibaraki, 305-8567, Japan**

12 **³Geophysics, Graduate School of Science, Tohoku University, 6-3, Aramaki-aza-**
13 **aoba, Aoba-ku, Sendai, 980-8578, Japan**

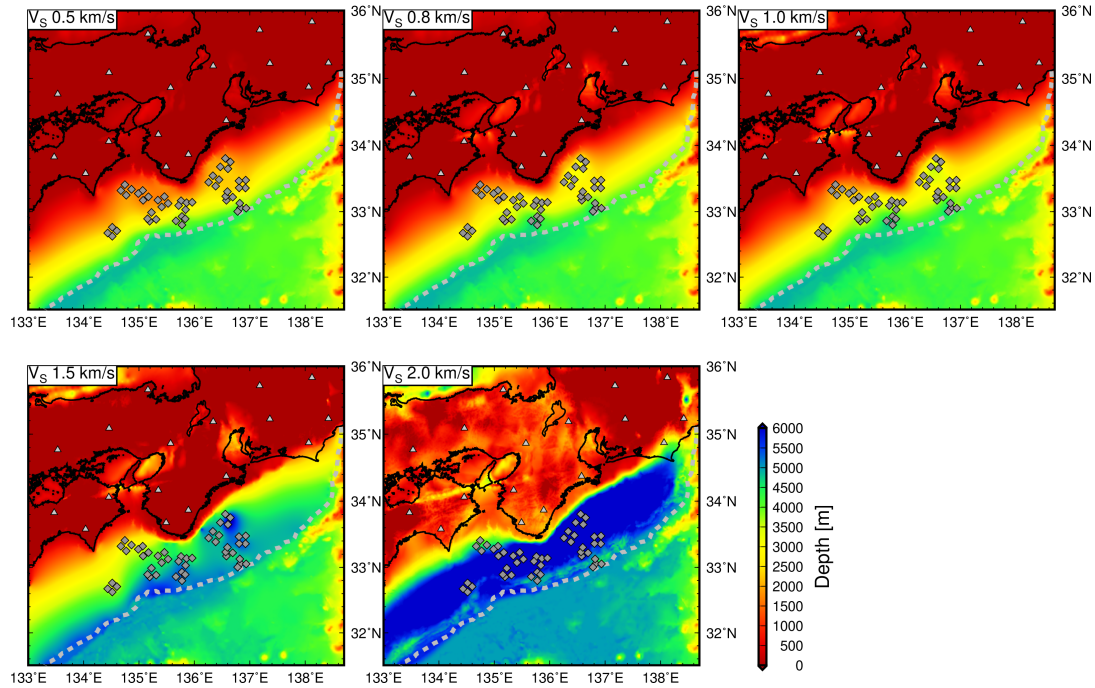
14
15 **Text S1**

16 The 3D model used in the simulations was basically constructed from the Japan Integrated
17 Velocity Structure Model (JIVSM) (Koketsu et al., 2012; Table 1 and Figure S1b). Because the
18 accretionary prism of the JIVSM is modelled by a $V_S = 1$ km/s constant layer and is too simple
19 for realistic ground motion simulation, we introduced estimations of 1D S -wave velocity
20 structures beneath DONET stations by Tonegawa *et al.* (2017). We converted the depth-varying
21 velocity structure model of Tonegawa *et al.* (2017) to a 5-layer model beneath each DONET
22 station. The physical parameters of each layer are listed in Table 1 of the main text. Thicknesses
23 of each layer were determined by fitting the depth-average S -wave velocities derived by
24 Tonegawa *et al.* (2017). For example, if the depth-average V_S of Tonegawa *et al.* (2017) become
25 the V_S of layer 1 at a certain depth, this depth is considered as the bottom of layer 1. After
26 obtaining the bottom depths of layers 1–4 beneath DONET stations, the bottom depths of each
27 station were interpolated and extrapolated via the ‘*Surface*’ gridding algorithm in Generic
28 Mapping Tools software (GMT; Wessel *et al.* 2013). Interpolation and extrapolation were only
29 applied within the region of the accretionary prism (Figure S1). In other words, the JIVSM
30 onshore and outer-rise sedimentary structures, and structures beneath bedrock, were fixed.

31 This construction method was basically the same as in Takemura, Kubo, *et al.* (2019).
32 However, in the present model, a layered structure was employed rather than a depth velocity-
33 gradient function. The simulation results of both the smooth-gradient and layered models were

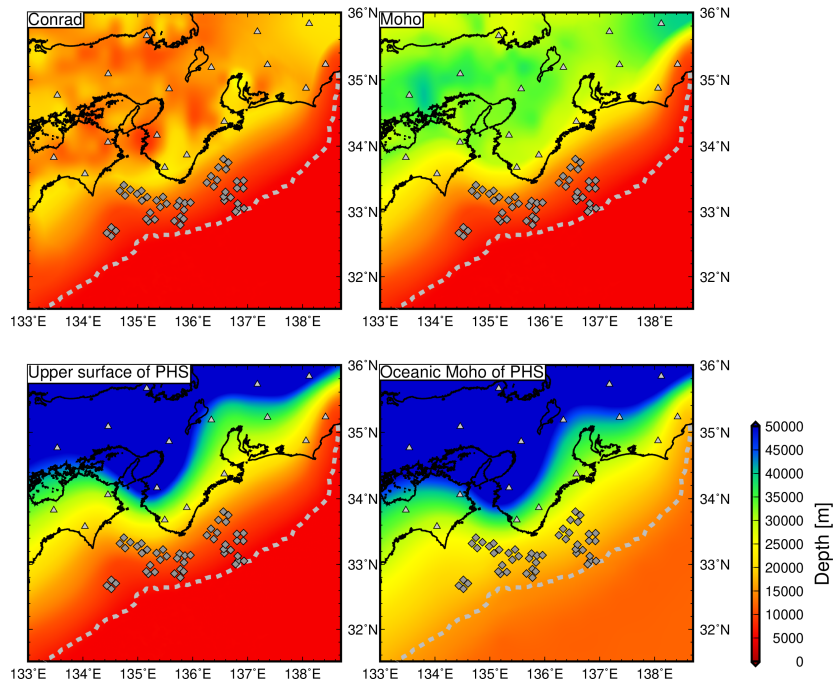
34 almost the same (Figures S2–S4).

35



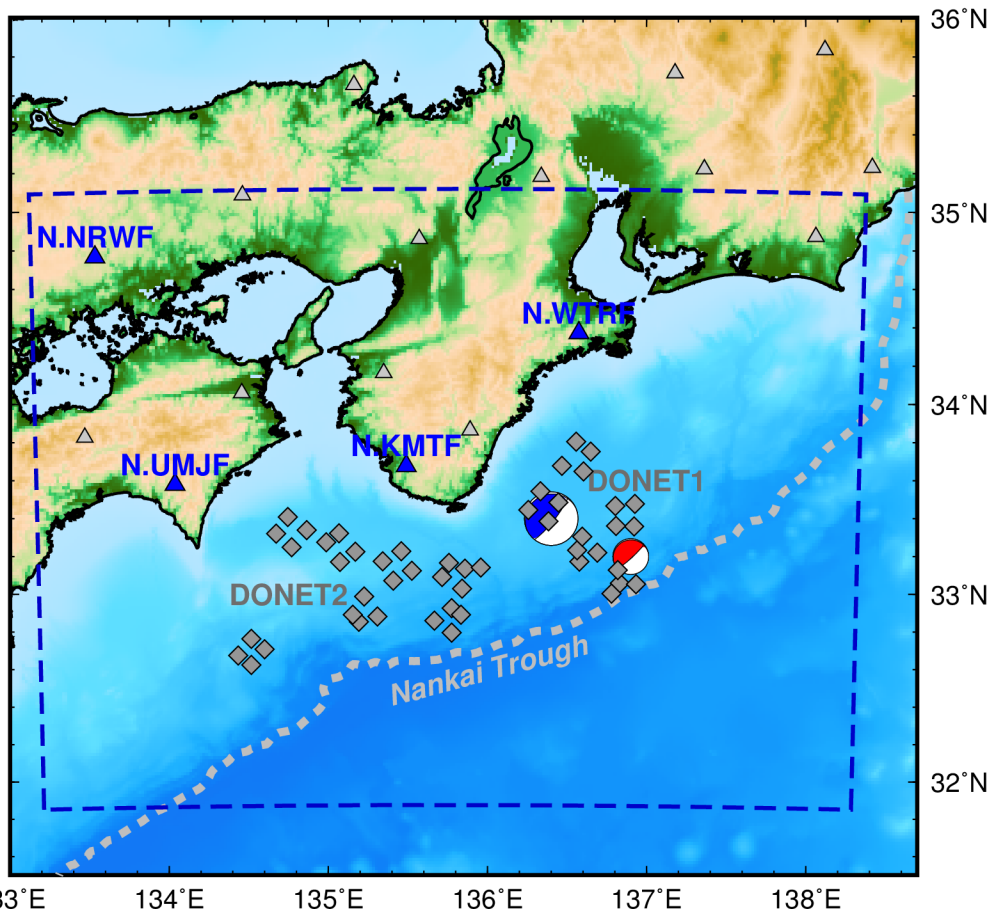
36

37 **Figure S1a.** The 3D layered structure of the accretionary prism. Background colours represent
38 depths of the bottom of each layer (see Table 1). The bottom of layer with V_S of 2.0 km/s
39 is corresponding to the bedrock depths of the JIVSM (Koketsu et al., 2012).



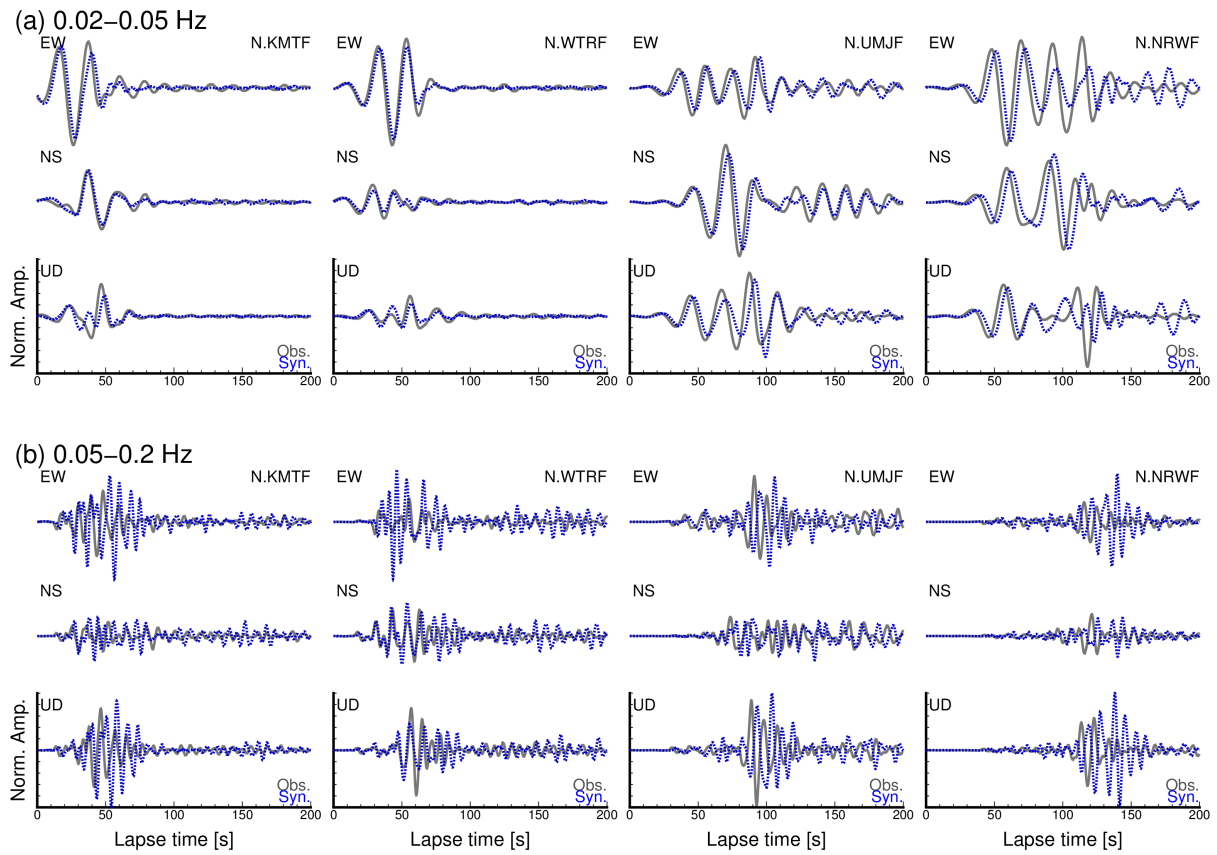
40

41 **Figure S1b.** Spatial variations of depths for Conrad, Moho, upper surface and oceanic Moho
42 of the Philippine Sea plate in the assumed model, JIVSM (Koketsu et al., 2012).



43 133°E 134°E 135°E 136°E 137°E 138°E
 44 **Figure S2.** Map for validation of simulations. The dashed-blue rectangle represents the
 45 horizontal coverage of the calculation region, which was discretised at intervals of 0.2
 46 km in horizontal directions and 0.1 km in the vertical direction. Simulations were
 47 conducted using the computer system at the Earthquake and Volcano Information Center,
 48 Earthquake Research Institute, University of Tokyo. The blue and red focal spheres are
 49 CMT solutions of the 2016 M_w 5.9 earthquake southeast off Kii Peninsula, Japan
 50 (Takemura et al., 2020), and a shallow very low-frequency earthquake on 10 April 2016
 51 (Takemura et al., 2018, 2019), respectively. The triangles and diamonds represent F-net
 52 and DONET stations, respectively.

53
 54



55

56

Figure S3. Simulation of the 2016 M_w 5.9 earthquake southeast off Kii Peninsula, Japan

57

(Shunsuke Takemura et al., 2020): (a) 0.02–0.05 Hz, (b) 0.05–0.2 Hz. Seismic wave

58

propagation in our model was evaluated via OpenSWPC software (Maeda et al., 2017).

59

The simulation model covered the area within the blue rectangle shown in Figure S1,

60

which was discretised by grid intervals of 0.2 km in horizontal directions and 0.1 km in

61

the vertical direction. Observed and synthetic seismograms at F-net stations are

62

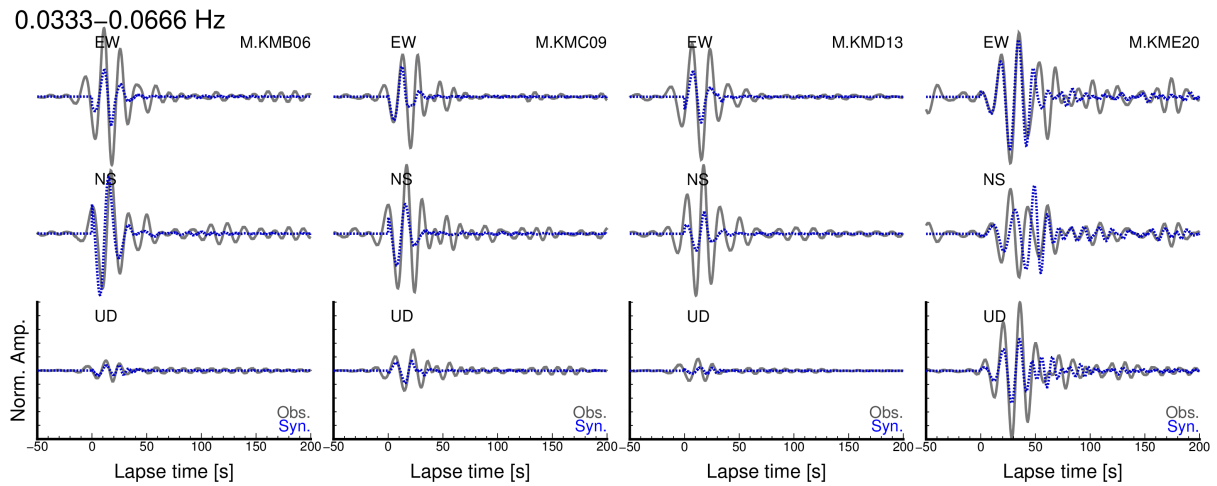
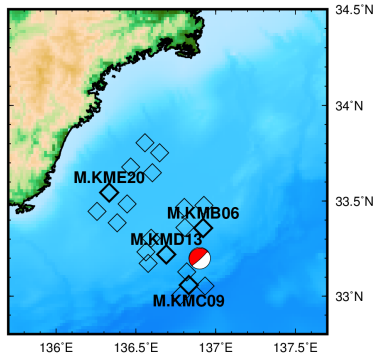
represented by grey and blue dotted lines, respectively. Amplitudes at each station were

63

normalized by the maximum amplitude of six-component filtered seismograms.

64

65

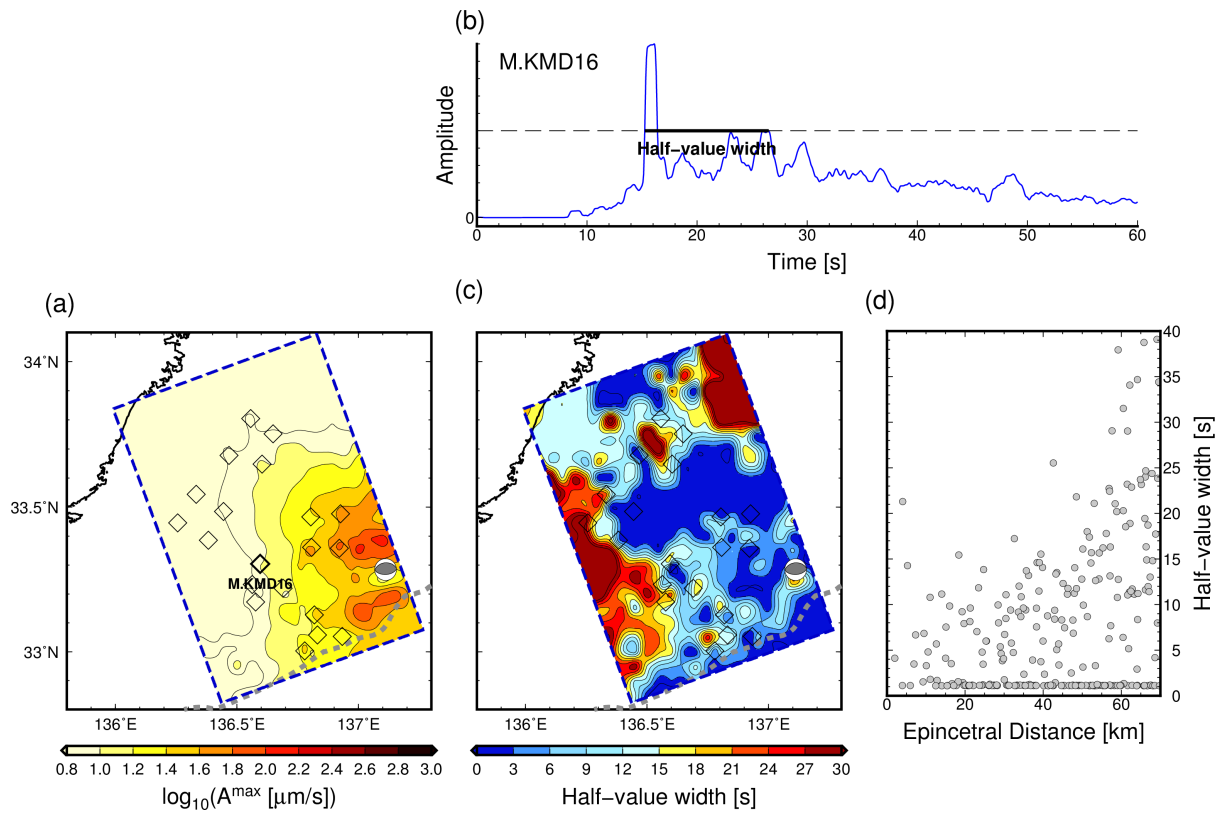


66

67 **Figure S4.** Simulation result of a shallow very low-frequency earthquake on 10 April 2016
 68 (S. Takemura et al., 2018; Shunsuke Takemura et al., 2019). Observed and synthetic
 69 seismograms at DONET stations are represented by grey and blue dotted lines,
 70 respectively. Amplitudes at each station were normalized by the maximum amplitude of
 71 six-component filtered seismograms. Locations of stations and the source are shown in
 72 the upper-left panel. The simulation model and settings are similar to those in Figure S2.

73

74



75

76

Figure S5. Spatial variations of maximum RMS amplitudes and half-value widths of

77

simulated RMS envelopes for an intraslab earthquake: (a) Maximum RMS amplitude

78

distribution, (b) example half-value width estimations, (c) half-value width distribution,

79

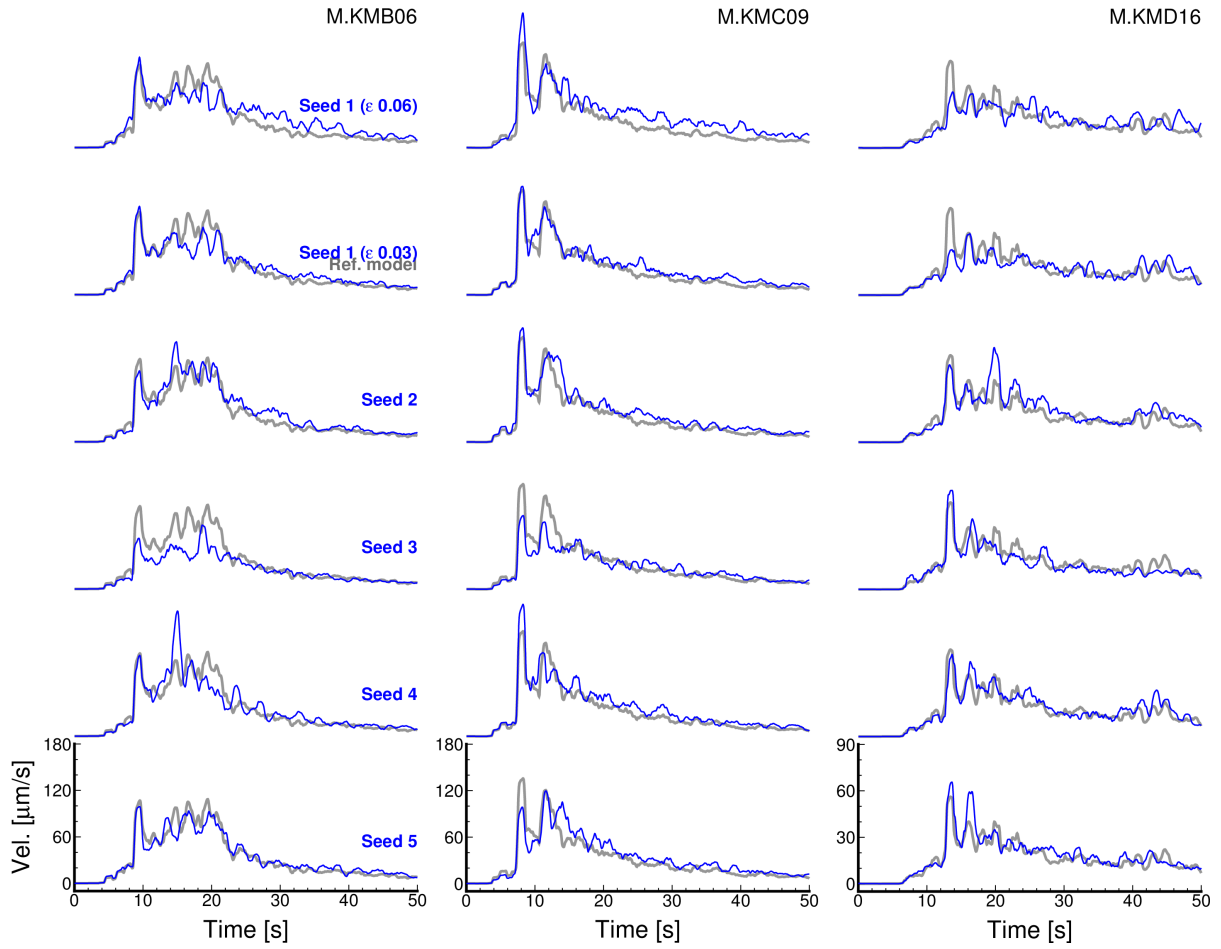
and (d) half-value widths as a function of epicentral distance. An example in (b) is an

80

RMS envelope at M.MRD16 (location shown in (a)).

81

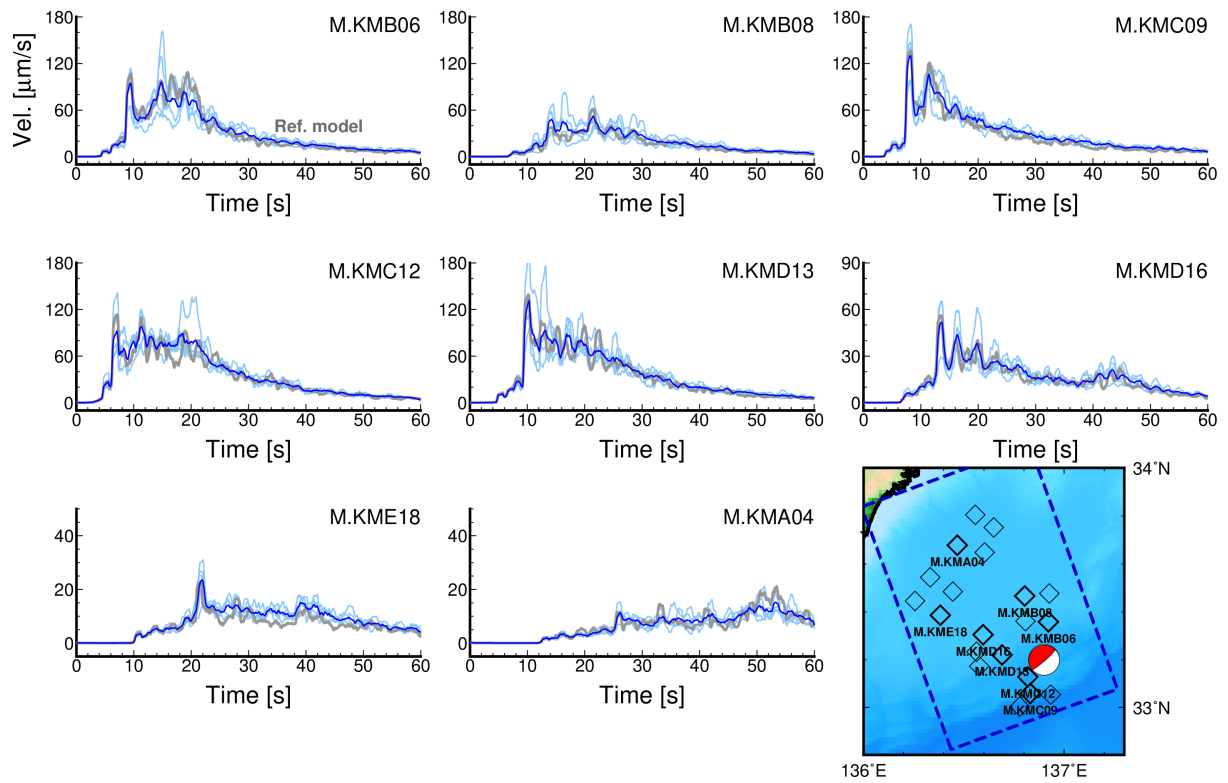
82



83

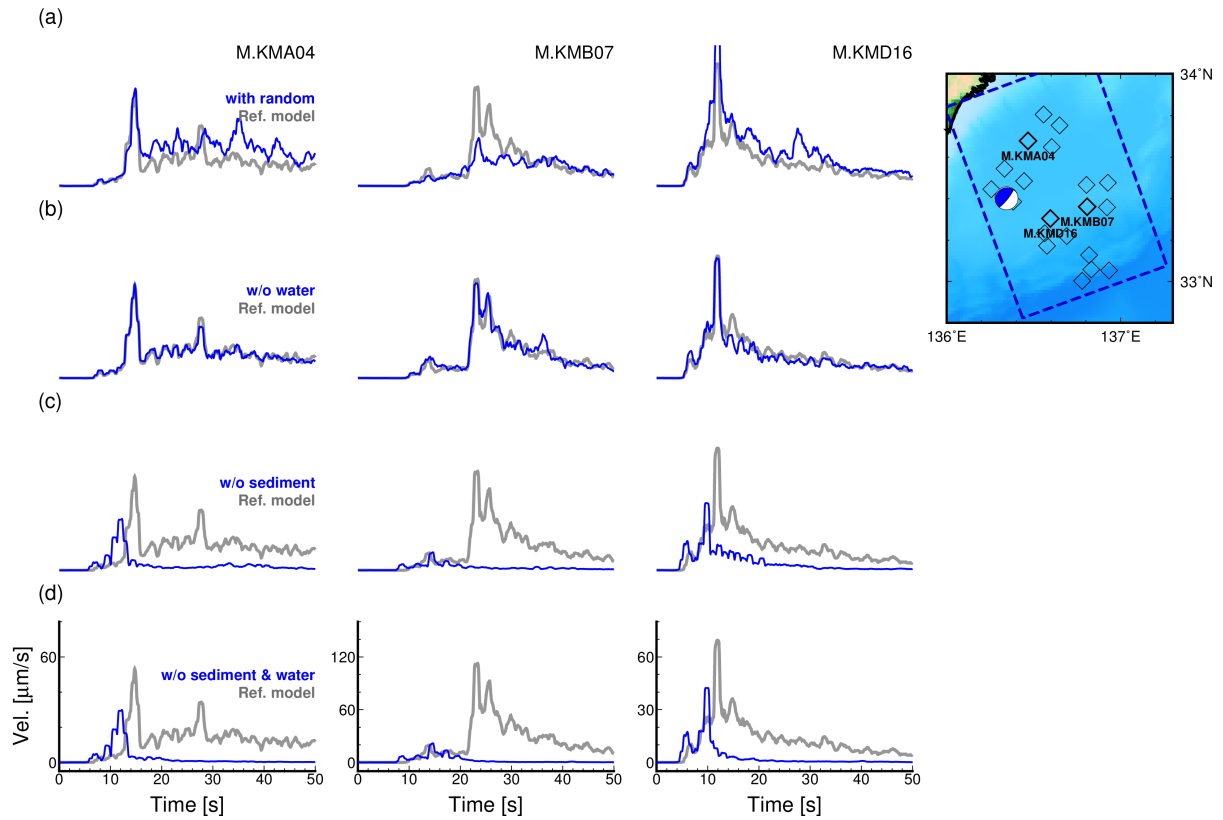
84 **Figure S6.** Comparisons of simulated RMS envelopes with different small-scale random
 85 velocity heterogeneity models. The PSDF type is an exponential type, and the parameters
 86 for small-scale random velocity heterogeneity models within the crust and accretionary
 87 prism are correlation length of $a = 1$ km and RMS values of $\varepsilon = 0.03, 0.06$. The models
 88 with $a = 1$ km and $\varepsilon = 0.03$ were conducted using different random seeds (numbered 1–
 89 5). Details of small-scale velocity heterogeneity models are described in Table 3.
 90 Locations of DONET stations are shown in Figure 8.

91



92
 93
 94
 95
 96
 97
 98
 99

Figure S7. Comparisons between simulated envelopes with/without small-scale velocity heterogeneities. Grey lines are envelopes from the reference model (without small-scale velocity heterogeneities). Blue and light blue lines are stacked and individual envelopes in the model with small-scale velocity heterogeneities. Details of small-scale velocity heterogeneity models are described in Table 3.



100

101 **Figure S8.** Simulation results of various heterogeneous models for an interplate earthquake.

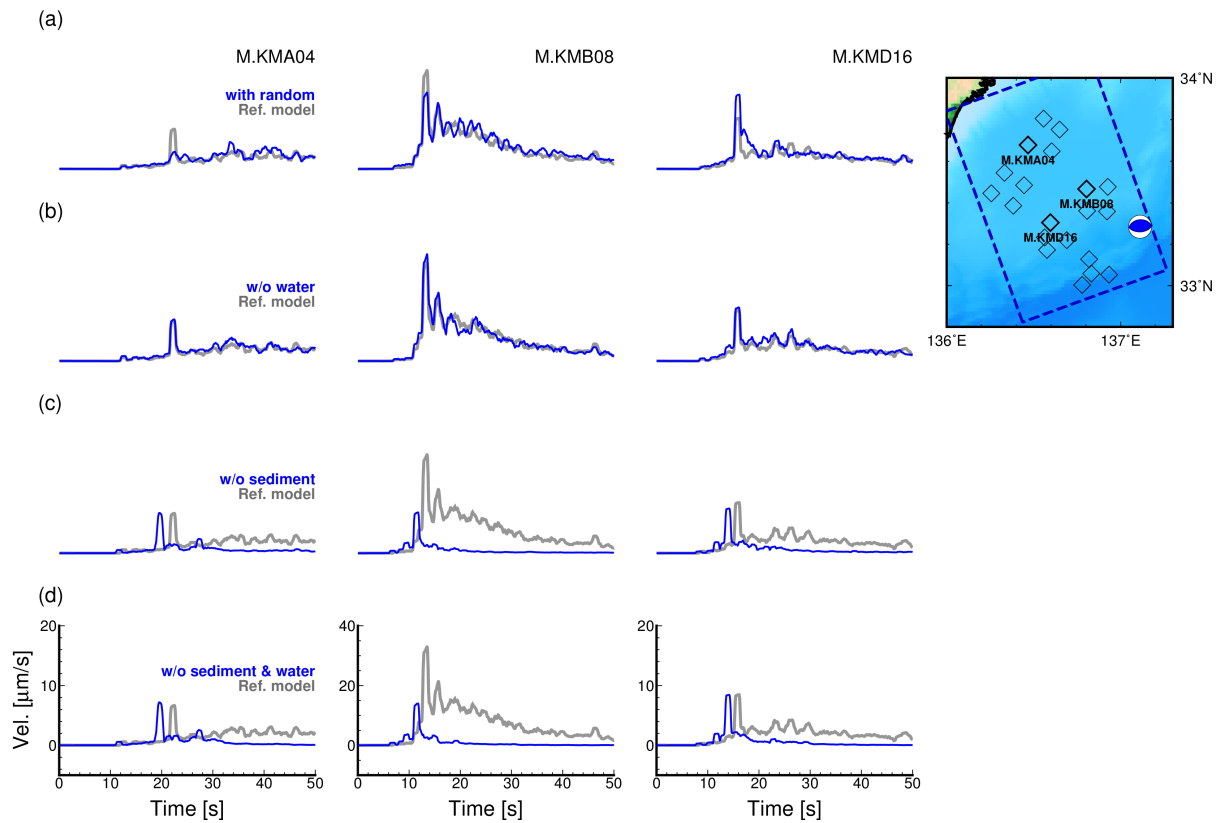
102 The blue lines are RMS envelopes derived from models: (a) with small-scale random

103 velocity heterogeneities, (b) without seawater, (c) without oceanic sediments

104 (accretionary prism), and (d) without oceanic sediments and seawater. Grey lines are the

105 simulation results with the reference model.

106



107

108 **Figure S9.** Simulation results of various heterogeneous models for an intraslab earthquake.

109 The blue lines are RMS envelopes derived from models: (a) with small-scale random

110 velocity heterogeneities, (b) without seawater, (c) without oceanic sediments

111 (accretionary prism), and (d) without oceanic sediments and seawater. Grey lines are the

112 simulation results with the reference model.

113

114 **References**

- 115 Koketsu, K., Miyake, H., & Suzuki, H. (2012). Japan Integrated Velocity Structure Model
116 Version 1. *Proceedings of the 15th World Conference on Earthquake Engineering*, 1–4.
117 Retrieved from http://www.iitk.ac.in/nicee/wcee/article/WCEE2012_1773.pdf
- 118 Maeda, T., Takemura, S., & Furumura, T. (2017). OpenSWPC: an open-source integrated
119 parallel simulation code for modeling seismic wave propagation in 3D heterogeneous
120 viscoelastic media. *Earth, Planets and Space*, 69(1), 102.
121 <https://doi.org/10.1186/s40623-017-0687-2>
- 122 Takemura, S., Matsuzawa, T., Kimura, T., Tonegawa, T., & Shiomi, K. (2018). Centroid
123 Moment Tensor Inversion of Shallow Very Low Frequency Earthquakes Off the Kii
124 Peninsula, Japan, Using a Three-Dimensional Velocity Structure Model. *Geophysical
125 Research Letters*, 45(13), 6450–6458. <https://doi.org/10.1029/2018GL078455>
- 126 Takemura, S., Kubo, H., Tonegawa, T., Saito, T., & Shiomi, K. (2019). Modeling of Long-
127 Period Ground Motions in the Nankai Subduction Zone: Model Simulation Using the
128 Accretionary Prism Derived from Oceanfloor Local S-Wave Velocity Structures. *Pure
129 and Applied Geophysics*, 176(2), 627–647. <https://doi.org/10.1007/s00024-018-2013-8>
- 130 Takemura, S., Matsuzawa, T., Noda, A., Tonegawa, T., Asano, Y., Kimura, T., & Shiomi, K.
131 (2019). Structural Characteristics of the Nankai Trough Shallow Plate Boundary
132 Inferred From Shallow Very Low Frequency Earthquakes. *Geophysical Research
133 Letters*, 46(8), 4192–4201. <https://doi.org/10.1029/2019GL082448>
- 134 Takemura, S., Okuwaki, R., Kubota, T., Shiomi, K., Kimura, T., & Noda, A. (2020). Centroid
135 moment tensor inversions of offshore earthquakes using a three-dimensional velocity
136 structure model: slip distributions on the plate boundary along the Nankai Trough.
137 *Geophysical Journal International*, 222(2), 1109–1125.
138 <https://doi.org/10.1093/gji/ggaa238>
- 139 Tonegawa, T., Araki, E., Kimura, T., Nakamura, T., Nakano, M., & Suzuki, K. (2017).
140 Sporadic low-velocity volumes spatially correlate with shallow very low frequency
141 earthquake clusters. *Nature Communications*, 8(1), 2048.
142 <https://doi.org/10.1038/s41467-017-02276-8>
- 143