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2	Diapycnal motion, diffusion, and stretching of tracers in the ocean
3	Henri F. Drake, ^{a,b} Xiaozhou Ruan, ^c Raffaele Ferrari, ^c
4	^a Princeton University / Geophysical Fluid Dynamics Laboratory
5	^b Previously, MIT–WHOI Joint Program in Oceanography/Applied Ocean Science &
6	Engineering, Cambridge and Woods Hole, Massachusetts.
7	^c Massachusetts Institute of Technology, Department of Earth, Atmospheric, and Planetary
8	Sciences

⁹ Corresponding author: Henri F. Drake, henrifdrake@gmail.com

ABSTRACT: Small-scale mixing drives the diabatic upwelling that closes the abyssal ocean 10 overturning circulation. Measurements of in-situ turbulence reveal that mixing is bottom-enhanced 11 over rough topography, implying downwelling in the interior and stronger upwelling in a sloping 12 bottom boundary layer. However, in-situ mixing estimates are indirect and the inferred vertical 13 velocities have not yet been confirmed. Purposeful releases of inert tracers, and their subsequent 14 spreading, have been used to independently infer turbulent diffusivities; however, these Tracer 15 Release Experiments (TREs) provide estimates in excess of in-situ ones. In an attempt to reconcile 16 these differences, Ruan and Ferrari (2021) derived exact buoyancy moment diagnostics, which 17 we here apply to quasi-realistic simulations. We show in a numerical simulation that tracer-18 averaged diapycnal motion is directly driven by the tracer-averaged buoyancy velocity, a convolution 19 of the asymmetric upwelling/downwelling dipole. Diapycnal spreading, however, involves both 20 the expected contribution from the tracer-averaged in-situ diffusion and an additional non-linear 21 diapycnal stretching term. These diapycnal stretching effects, caused by correlations between 22 buoyancy and the buoyancy velocity, can either enhance or reduce tracer spreading. Diapycnal 23 stretching in the stratified interior is compensated by diapycnal contraction near the bottom; for 24 simulations of the Brazil Basin Tracer Release Experiment these nearly cancel by coincidence. 25 By contrast, a numerical tracer released near the bottom experiences leading-order stretching that 26 varies in time. These results suggest mixing estimates from TREs are not unambiguous, especially 27 near topography, and that more attention should be paid towards the evolution of tracers' first 28 moments. 29

30 1. Introduction

The lower limb of the ocean's meridional overturning circulation traces the diabatic life cycle of 31 abyssal bottom waters (Talley 2013), which store vast quantities of climatically-active tracers like 32 heat and carbon. Bottom waters are formed at the surface of the Southern Ocean by atmospheric 33 cooling and brine rejection and are consumed in the deep ocean by buoyancy-flux convergence 34 due to small-scale mixing and geothermal heating (Abernathey et al. 2016; de Lavergne et al. 35 2016b). Since mixing processes are too small to be resolved by large-scale ocean models, the rate 36 at which tracers are mixed across density surfaces- the diapycnal diffusivity- enters as a key free 37 parameter in ocean and climate models (Bryan and Lewis 1979; Simmons et al. 2004; de Lavergne 38 et al. 2020). While early models of the abyssal circulation assume this mixing to be spatially 39 uniform (Munk 1966; Stommel and Arons 1959), subsequent in-situ observations reveal a complex 40 geography of mixing processes (e.g. Polzin et al. 1997; Waterhouse et al. 2014). A robust pattern 41 that emerges from these in-situ mixing observations is the bottom-enhancement of mixing over 42 rough topography, consistent with theoretical arguments that this mixing is predominantly caused 43 by breaking internal waves radiating from flow over topography (Munk and Wunsch 1998; Polzin 44 2009; Nikurashin and Ferrari 2009; Nikurashin and Legg 2011; MacKinnon et al. 2017; Whalen 45 et al. 2020). 46

The observed bottom-enhancement of deep mixing demands a revision of classic abyssal circu-47 lation theory: in the stratified interior, bottom-enhanced mixing above rough topography results in 48 a layer of buoyancy flux divergence-the downwelling Stratified Mixing Layer (SML)-and a thin 49 layer of even larger buoyancy flux convergence at the insulating¹ seafloor—the upwelling Bottom 50 Boundary Layer (BBL). These ideas were first introduced as the regional scale in the Brazil Basin 51 (Polzin et al. 1997; Ledwell et al. 2000; St. Laurent et al. 2001; Huang and Jin 2002) and then 52 generalized to the global context by (Ferrari et al. 2016; McDougall and Ferrari 2017; Callies 53 and Ferrari 2018). The global diabatic overturning circulation is the small residual of substantial 54 downwelling in the SML and even larger upwelling in the BBL (Ferrari et al. 2016; Drake et al. 55 2020). While the existence of these upwelling/downwelling flows is virtually guaranteed by the 56 combination of a bottom-enhanced turbulent buoyancy flux and an insulating boundary condi-57 tion along a sloping seafloor, their structure, magnitudes, and underlying dynamics remain poorly 58

¹Geothermal heat flux into the BBL acts to amplify upwelling, but is thought to be secondary to mixing globally (de Lavergne et al. 2016a) and is negligible in the Brazil Basin subregion considered here (Thurnherr et al. 2020).

understood (Callies 2018; Drake et al. 2020; Polzin and McDougall 2022). Since diapycnal (or 59 vertical) velocities and fluxes are challenging to measure directly due to the ocean's small aspect 60 ratio, indirect methods must be used to infer the flow, such as volume or buoyancy budgets (e.g. 61 St. Laurent et al. 2001; Lele et al. 2021). Watermass transformation analysis is a commonly-used 62 framework which combines volume and buoyancy budgets to express diapycnal transport across a 63 buoyancy surface in terms of the average turbulent buoyancy flux along the surface, which can be 64 inferred from indirect observations (Walin 1982; Marshall et al. 1999; de Lavergne et al. 2016b; 65 Ferrari et al. 2016; Spingys et al. 2021). 66

There are several observational methods for estimating in-situ turbulent buoyancy fluxes and 67 their corresponding diffusivities (listed roughly in order of decreasing accuracy and generality; 68 Gregg et al. 2018): 1) velocity variance microstructure based on an approximate turbulent kinetic 69 energy budget (Osborn 1980), 2) temperature variance microstructure based on an approximate 70 temperature variance budget (Osborn and Cox 1972), 3) scaling analysis based on the Thorpe 71 scale of density overturns (Thorpe and Deacon 1977; Dillon 1982), and 4) shear/strain variance 72 finestructure based on idealized spectral models of internal wave dynamics (e.g. Garrett and Munk 73 1972, 1975; Henyey et al. 1986; Gregg 1989; Polzin et al. 1995; Gregg et al. 2003; Kunze et al. 74 2006). All of these methods are indirect and require some degree of approximation to convert 75 the measured quantity into a diffusivity. Furthermore, they provide only localized snapshots of 76 spatially and temporally intermittent mixing events and thus may provide biased estimates of the 77 mean diffusivity (Whalen 2021), which is often the goal of parameterization. 78

Tracer (or Dye²) Release Experiments (TREs; Watson et al. 1988) are considered by many 79 to provide the gold standard of mixing rate estimates. In TREs, an assumed inert chemical 80 tracer is deliberately injected into the ocean and its distribution is surveyed by ship-board rosette 81 sampling over timescales of months to years. The evolution of the tracer is then inverted (using 82 approximate advection-diffusion models) to yield estimates of the mean diffusivity and velocity, 83 which can be compared to independent in-situ turbulence measurements. Localized TREs are 84 experimental analogues of mathematicians' Green's function approach and are easier to interpret 85 than thermodynamic or biogeochemical tracers with less well known initial or boundary conditions 86 and more complicated dynamics and mixing histories (e.g. Hogg et al. 1982; Lumpkin and Speer 87

²Fluorescent dye can be used for timescales of hours to days and can be sampled as much higher resolution with in-situ fluoremeters (e.g. Ledwell et al. 2004), or—for near-surface releases—remote sensing instruments (Sundermeyer et al. 2007).

⁸⁸ 2007; Trossman et al. 2020). However, the results of the TRE inversion process still depend upon
 ⁸⁹ the assumptions made to infer the diffusivity from simple advection-diffusion forward models.

Watson et al. (1988) pitch TREs in the ocean as an "unambiguous measure of the diapycnal 90 mixing rate" since tracers average over the spatial and temporal variability that challenges the 91 interpretation of in-situ mixing estimates; for example, Watson et al. (1988) hypothesize that the 92 sparse sampling of log-normally distributed (or worse, log-skew-normal) mixing events by in-situ 93 microstructure measurements risks under-estimating mean mixing rates (see also Baker and Gibson 94 1987; Cael and Mashayek 2021). Superficially, observations from two deep-ocean TREs seem to 95 corroborate this hypothesis: tracer-based estimates of mixing rates are ubiquitously 1.5-10 times 96 larger than co-located in-situ microstructure measurements (Ledwell et al. 2000; Watson et al. 97 2013; Mashayek et al. 2017). While there are ad-hoc and site-specific explanations for each of 98 these discrepancies, there is no consensus on how best to compare tracer-based and microstructure-99 based estimates (Gregg et al. 2018), nor what to make of the fact that tracer-based estimates seem 100 to always exceed microstructure-based estimates. 101

Recent advances in the numerical modelling and theory of TREs provide some guidance for 102 interpreting tracer-based estimates of mixing and comparing them to microstructure-based esti-103 mates. For example, Mashayek et al. (2017) use a realistic regional simulation to argue that the 104 mixing inferred from the DIMES TRE (Watson et al. 2013) was an order-of-magnitude larger than 105 the in-situ diffusivity estimated from microstructure because the average diapycnal spreading of 106 the tracer was dominated by a small fraction the tracer distribution that resided in regions of strong 107 mixing near rough topography. Ruan and Ferrari (2021) derive exact evolution equations for the 108 first and second tracer-weighted buoyancy moments (see Section 2a), which confirm Mashayek 109 et al. (2017)'s speculation that the tracer's diapycnal variance grows like the tracer-weighted in-situ 110 diffusivity. Ruan and Ferrari (2021) also identify a second "diapycnal stretching" term through 111 which the bottom-enhancement of the buoyancy velocity in the SML further accelerates the diapy-112 cnal spreading of the tracer. Holmes et al. (2019) use a similar approach but include the effects 113 of a sloping bottom boundary, and find that the diapycnal stretching in the SML is somewhat 114 compensated for by a diapycnal contraction (or "boundary suppression") effect due to upwelling of 115 relatively dense tracer in the BBL. However, since both of these analyses use extremely idealized 116 models, it remains unclear to what extent diapycnal stretching affects tracers in realistic conditions. 117

Previous studies have speculated about the qualitative impacts of these stretching effects (Ledwell
and Hickey 1995; Ledwell et al. 2000; Waterman et al. 2013), but did not quantify these impacts
or the degree to which stretching effects are even included in their inverse models.

In this paper, we apply the buoyancy moments method in a quasi-realistic TRE simulation. We 121 use tracer-weighted buoyancy moments diagnosed from the simulation to reinterpret the diapycnal 122 downwelling and spreading observed in the Brazil Basin TRE (BBTRE; Ledwell et al. 2000 and 123 St. Laurent et al. 2001) in the context of an emerging paradigm of bottom mixing layer control 124 of the global abyssal circulation (Ferrari et al. 2016; McDougall and Ferrari 2017). We also 125 provide guidance for the interpretation of past (e.g. Ledwell and Hickey 1995; Ledwell et al. 2004; 126 Holtermann et al. 2012; Ledwell et al. 2016; Mackay et al. 2018; Visbeck et al. 2020) and future 127 TREs that encounter topography. 128

129 **2.** Theory

¹³⁰ We briefly review Ruan and Ferrari (2021)'s recently proposed framework for comparing tracer-¹³¹ based and microstructure-based mixing estimates, based on exact evolution equations for tracer ¹³² moments in buoyancy space. The derivation begins with the conservation equations for tracer ¹³³ concentration *c* and buoyancy *b*,

$$\frac{\partial c}{\partial t} + \mathbf{u} \cdot \nabla c = \nabla \cdot (\kappa \nabla c) \tag{1}$$

$$\frac{\partial b}{\partial t} + \mathbf{u} \cdot \nabla b = \nabla \cdot (\kappa \nabla b), \qquad (2)$$

where **u** is the velocity vector, $\nabla = \left(\frac{\partial}{\partial x}, \frac{\partial}{\partial y}, \frac{\partial}{\partial z}\right)$ is the gradient operator, and κ is an isotropic 134 turbulent diffusivity (assumed to be the same for all tracers). Buoyancy, tracer concentrations, 135 and velocity have been filtered on spatial and temporal scales larger than those associated with 136 small-scale turbulence, and the filtered scalar fluxes are parameterized as an enhanced diffusive flux 137 $\mathbf{F}_{\phi} = -\kappa \nabla \phi$, where the effective turbulent diffusivity is much larger than the molecular diffusivity. 138 For simplicity of exposition, we here approximate density as a linear function of temperature; thus, 139 density ρ , buoyancy b, and temperature T are all proportional and will be used interchangeably 140 throughout: $b \equiv -g \frac{\rho}{\rho_0} \approx g \alpha T$, where ρ_0 is a reference density and α is the thermal contraction 141

¹⁴² coefficient. (Salinity can be easily included as long as it is assumed to also be linearly proportional
 ¹⁴³ to density.)

a. Exact tracer-weighted buoyancy-moment models

In his classic paper, Taylor (1922) demonstrates that the growth rate of half the second moment of a 1D tracer distribution in physical space is exactly equal to its diffusivity. Ruan and Ferrari (2021) generalize this theory to the case of variable diffusivity in a stably stratified fluid by considering moments in buoyancy space. By cross-multiplying the passive tracer (1) and buoyancy (2) equations and integrating over a volume V containing the tracer (or bounded by insulating and impermeable boundaries), they derive straightforward and exact evolution equations for the first and second tracer-weighted buoyancy moments,

$$w_{\text{tracer}} \equiv \frac{\partial_t \overline{T}}{|\nabla T|} = \frac{2\overline{\omega}}{|\nabla T|} \quad \text{and}$$
 (3)

152

$$\underbrace{\frac{1}{2} \frac{\partial_t \overline{\left(T - \overline{T}\right)^2}}{|\nabla T|^2}}_{\substack{\kappa_{\text{tracer}} \\ \text{(spreading)}}} = \underbrace{\frac{\overline{\kappa} |\nabla T|^2}{|\nabla T|^2}}_{\substack{\kappa_{\text{Taylor}} \\ \text{(diffusion)}}} + \underbrace{2 \frac{\overline{\omega' T'}}{|\nabla T|^2}}_{\substack{\kappa_{\omega} \\ \text{(stretching)}}},$$
(4)

respectively, where overlines denote the tracer-weighted average, $\overline{\star} \equiv \frac{\int_{V} \star c \, dV}{\int_{V} c \, dV}$; primes denote variations from the tracer average, $\star' \equiv \star - \overline{\star}$; and $\omega \equiv \nabla \cdot (\kappa \nabla T)$ is the in-situ buoyancy velocity, which is the magnitude of the diapycnal velocity through buoyancy space (e.g. Marshall et al. 1999). We have taken an additional step of converting to physical velocity and diffusivity units by normalizing by the appropriate tracer-weighted powers of the buoyancy gradient.

¹⁶⁵ b. Interpreting the tracer-weighted buoyancy moments

¹⁶⁶ Consider the extreme example of a tracer distribution $c_{i,j}$ consisting of two infinitesimal patches ¹⁶⁷ at locations \mathbf{x}_i and \mathbf{x}_j and with equal mass,

$$c_{i,j}(\mathbf{x}) = \delta(\mathbf{x}_i) + \delta(\mathbf{x}_j), \tag{5}$$



FIG. 1. Examples of diapycnal stretching and contraction of bi-modal tracer distributions (eq. 5) in physical space (a) and in (ω ,*T*) space (b). a) The three tracer distributions $c_{1,3}$, $c_{1,2}$, and $c_{3,2}$ experience diapycnal spreading or contraction effects due to temperature and buoyancy velocity differences. Gray lines show the equally-spaced temperature surfaces corresponding to the three tracer patches. Arrows represent the magnitude of the buoyancy velocity ω and are oriented normal to temperature surfaces. b) PDF of contributions to $c_{3,2}$'s net diapycnal stretching effects both tracer patches. Olive lines mark the average buoyancy velocity and temperature of the tracer.

where $\delta(\mathbf{x})$ is the Delta function. The evolution of the first moment (3) is simply given by the twice the average buoyancy velocity of the two patches,

$$\partial_t T = 2\overline{\omega} = \omega_i + \omega_j,\tag{6}$$

where we use the shorthand $\phi_k \equiv \phi(\mathbf{x}_k)$. The evolution of the centered second moment (4), is given by

$$\frac{1}{2}\partial_t \overline{\left(T - \overline{T}\right)^2} = \overline{\kappa |\nabla T|^2} + \frac{1}{2}\Delta\omega\Delta T,\tag{7}$$

where $\Delta \omega \equiv \omega_j - \omega_i$ and $\Delta T \equiv T_j - T_i$ are buoyancy velocity and temperature differences between the two patches, respectively. While the first moment tendency is simply given by the average of the two patches' tendencies, the centered second moment tendency includes an additional non-linear interaction term. If the warmer patch upwells faster than the colder patch ($\Delta \omega \Delta T > 0$), this term drives diapycnal stretching (e.g. $c_{1,3}$ and $c_{3,2}$ in Figure 1); conversely, $\Delta\omega\Delta T < 0$ corresponds to diapycnal contraction (e.g. $c_{1,2}$ in Figure 1).

A corollary of (7) is the fact that estimates of the in-situ diffusivity are most reliable when the 178 injected tracer distribution is compact in buoyancy space (i.e. $\Delta T \approx 0$), supporting the practice 179 of localized TREs. Even for an initially compact tracer injection with $\Delta\omega\Delta T \simeq 0$, diapycnal 180 stretching effects may become significant over time as ΔT increases due to diapycnal diffusion; on 181 the other hand, while isopycnal stirring does not increase ΔT (by definition), it can increase $\Delta \omega$ by 182 distributing tracer into regions with varying buoyancy velocities. While the former effect is likely 183 to be well represented in 1D advection-diffusion models used to interpret TRE data, the latter is 184 not. 185

3. Numerical methods overview: simulated Tracer Release Experiments

We configure the MITgcm to simulate mixing-driven flow in the BBTRE region (Figure 2a). 195 Inspired by sloping bottom boundary layer theory (reviewed by Garrett et al. 1993), the system is 196 solved in a coordinate frame aligned with the mean MAR slope, as described in detail in a submitted 197 companion manuscript (Drake et al. 2022) and summarized in Appendix A. The simulation is forced 198 only by bottom-enhanced turbulent mixing, which controls diabatic tracer upwelling and spreading 199 and is thought to provide much of the available potential energy that drives sub-inertial abyssal 200 flows. Sub-grid scale turbulent fluxes of a filtered tracer ϕ are parameterized as down-gradient 201 turbulent diffusion, $\mathbf{F}_{\phi} \approx -\kappa \nabla \phi$, whose magnitude is controlled by a turbulent diffusivity κ that 202 increases exponentially towards the seafloor (Figure 2b), 203

$$\kappa(x, y, z) = \kappa(z; d) = \kappa_{BG} + \kappa_{BOT} \exp\left(\frac{z-d}{h}\right),$$

and is fit to the mean height-above-bottom microstructure profile in the region according to Callies (2018), with $\kappa_{BOT} = 1.8 \times 10^{-3} \text{ m}^2/\text{s}$, $\kappa_{BG} = 5.2 \times 10^{-5} \text{ m}^2/\text{s}$, and h = 230 m.

After spinning up the flow to a quasi-equilibrium state at t = 5000 days, we release three Gaussian blobs of tracer,

$$c_n(x, y, z, t = 0) = c_0 \exp\left\{-\left(\frac{(x - x_0)^2}{\sigma_x^2} + \frac{(y - y_0)^2}{\sigma_y^2} + \frac{(z - z_n)^2}{\sigma_z^2}\right)\right\},\tag{8}$$



FIG. 2. Numerical model configuration: domain geometry, prescribed forcing, and key features. a) Rectangular 187 domain (solid lines) centered along the BBTRE canyon thalweg (dashed line) and interpolated onto locally-188 tangent cartesian coordinates (\hat{x}, \hat{y}) . b) Prescribed bottom-enhanced mixing (colors) along the canyon thalweg 189 (grey shading). Dashed black lines show the domain limits in the slope-native coordinate frame (x, z). The 190 transparent grey line shows the average height of the canyon crests, which rise 500 m to 1000 m above the thalweg 191 (its deepest section). White dots/contours show the locations of the simulated tracer releases. The location of 192 the prominent Dynamics of the Mid-Ocean Ridge Experiment (DoMORE- see Clément et al. 2017) sill is shown 193 for reference. 194

with horizontal widths of $\sigma_x = \sigma_y = 10$ km, a thickness $\sigma_z = 100$ m, and horizontal release coordinates (x_0, y_0) corresponding to the location where the tracer was released in the BBTRE $(18.3 \,^{\circ}\text{W}, 21.7 \,^{\circ}\text{S})$ (Figure 2). The tracers are released at three different heights z_n corresponding to distinct dynamically interesting regimes: far above the topography, $z_{\text{BBTRE}} - d(x_0, y_0) = 1050$ m above the seafloor (actual BBTRE release location; hereafter the BBTRE tracer); roughly at the height of the canyon crests, $z_{\text{Crest}} - d(x_0, y_0) = 600$ m (Crest); and within the thick BBL of the canyon trough, $z_{\text{Bottom}} - d(x_0, y_0) = 150$ m (Bottom). We follow the evolution of these released tracers until $t_f = 440$ days after release, roughly corresponding to the first survey in the BBTRE at 14 months.

4. Results

²¹⁸ a. Temporal evolution of the released tracer distributions

Within the first few eddy turnover timescales, the released tracer blobs are stirred into a web of filaments along isopycnals by submesoscale eddies (e.g. Figure 3). While the BBTRE and Crest tracers are released well above the canyon thalweg (its deepest section; Figure 2a), vigorous along-ridge mean flow (Figure 4) and isopycnal stirring by submesoscale eddies spread them to shallower regions (Figure 5).

The tracers are diffused diapycnally by the prescribed bottom-enhanced turbulent mixing (e.g. 230 Figure 5b,d). For the BBTRE tracer, which mostly remains well above the bottom, its distribution 231 in temperature space remains reasonably Gaussian (Figure 5d), reminiscent of diffusion with a 232 constant diffusivity and in the absence of boundaries; for the Crest and Bottom tracers, however, the 233 tracer distributions depart significantly from Gaussianity (Figure 5h,l), suggesting the importance 234 of variations in the diffusivity or boundary effects. Most notably, the Bottom tracer develops a bi-235 modal distribution in temperature space as some of the tracer spills over the minor sill at x = 120 km 236 and crosses the T = 0.7 °C surface (Figure 5j, 1). By the end of the experiment at 440 days, most 237 of the Bottom tracer has spilled over the sill and its bi-modal distribution collapses onto a single, 238 warmer, peak. While only the Bottom tracer exhibits a tracer-weighted diapycnal motion that is 239 discernible by visually inspecting the tracer distributions in temperature space, the BBTRE and 240 Crest tracers do exhibit slow mean diapycnal downwelling and upwelling, respectively. 241

²⁴² b. Diapycnal interior downwelling and boundary upwelling driven by bottom-enhanced mixing

As described in Section 2a, the mean diapycnal motion of the tracer is directly driven by the tracer-weighted buoyancy velocity $\overline{\omega} \equiv \overline{\nabla \cdot (\kappa \nabla T)}$ (eq. 3). In the SML, well above the seafloor, the bottom-enhancement of the diffusivity κ dominates the buoyancy velocity, resulting in diapycnal downwelling, $\omega < 0$. Closer to the seafloor, the temperature flux must vanish to satisfy the insulating bottom boundary condition, resulting in vigorous diapycnal upwelling, $\omega > 0$, in the BBL.



FIG. 3. Instantaneous snapshots of the BBTRE tracer mass, vertically-integrated over the $\{1.0 \text{ °C}, 1.1 \text{ °C}\}$ temperature layer, and normalized by the maximum initial tracer mass. The grey shading represents two major topographic obstacles, where the temperature layer in-crops.

The BBTRE tracer, which is released in the SML, exhibits diapycnal downwelling throughout the experiment (Figure 6c), consistent with the above phenomenology. The magnitude of downwelling, however, is modulated by a 45-day damped oscillation due to along-ridge advection by a mean-flow



FIG. 4. (a) Cross-canyon meridional velocity 1300 m above the mean slope, i.e. at the release height of BBTRE tracer. The black contour shows the initial extent of the tracers, which is released in an anomalously northward flow. (b) Same as a), but averaged across the whole domain.

of speed $U \approx 15 \text{ mm/s}$ (Figure 4a) across a periodic domain of width $L_y = 60 \text{ km}$, such that the tracer aliases the roughly sinusoidal trough-crest topography on a timescale of $\tau = L_y/U \approx 45 \text{ days}$. This modulation is damped over time as the tracer spreads isopycnally and spans a region wider than the typical trough-crest separation (Figure 5a).

In the first 100 days, interpreting the mean diapycnal sinking of the BBTRE tracer is straightforward: the entire tracer distribution experiences a negative buoyancy velocity and so the tracer sinks diapycnally (Figure 6c), i.e. $\overline{\omega} \approx \overline{\omega_{<0}}$, where we define:

$$\overline{\omega_{<0}} \equiv \frac{\int_{\mathcal{V}_{\omega<0}} \omega \, c \, \mathrm{d}V}{\int_{\mathcal{V}} c \, \mathrm{d}V} \tag{9}$$

as the strictly downwelling buoyancy velocity. While this strictly downwelling contribution to the tracer-weighted buoyancy velocity increases slightly over the remainder of the experiment as the tracer sinks towards larger diffusivities, sufficient tracer is entrained into the BBL that a strictly upwelling contribution $\overline{\omega}_{>0}$ (similarly defined) grows at an even faster rate, such that the net diapycnal sinking of the tracer weakens over the last few hundred days of the experiment (Figure 6c).

At the other extreme, the Bottom tracer is released entirely in the BBL and thus upwells vigorously upon release, with $\overline{\omega} \approx \overline{\omega_{>0}}$ (Figure 6g). As some of the tracer eventually spreads into the SML above and the strictly negative contribution $\overline{\omega_{<0}}$ grows, the net upwelling of the tracer weakens over time³.

³The Bottom tracer is released near the bottom of a weakly stratified depression along the canyon thalweg, and its average stratification increases dramatically over the first 200 days (Figure 6a,b). Thus, the early diapycnal upwelling and spreading is enhanced when converting to physical space because the buoyancy surfaces are on average much further apart than they are later on (see normalization in equations 3 and 4).



FIG. 5. Temporal evolution of the tracer distributions in Cartesian, height-above-bottom, and temperature 243 coordinates for the BBTRE (a-d; blues), Crest (e-h; purples), and Bottom releases (i-l; reds). (a,e,i) Slope-normal 244 column-integrated tracer concentrations and (b,f,j) cross-canyon-integrated tracer concentrations, normalized by 245 their maximum value (logarithmic scale). Grey contours in (a,e,f) show two representative isobaths of ocean 246 depth $\hat{d}(\hat{x}, \hat{y})$. Black lines in (b,f,j) show equally-spaced cross-canyon-averaged temperature surfaces. Tracer 247 distributions in (c,g,k) height-above-bottom and (d,h,l) temperature coordinates, normalized by their maximum 248 initial values (linear scale). Olive contours show the 10% contour for the initial tracer distribution; olive dashed 249 and arrows show the temporal evolution of the tracer's center of mass (first moments). 250

²⁹⁰ The Crest release is perhaps the most interesting: at first, the Crest tracer is in the SML far above ²⁹¹ the canyon thalweg and thus downwells similarly to the BBTRE tracer; after roughly $\tau = 46$ days, ²⁹² however, enough of the Crest tracer is advected into the BBLs along the rim of the canyon and the ²⁹³ surrounding hills that the strictly upwelling component wins out and the tracer begins upwelling ²⁹⁴ in the net (Figure 6e). Over the last few hundred days of the experiment, the weak net upwelling of ²⁹⁵ the tracer is the small residual of a substantial compensation between strictly upwelling and strictly ²⁹⁶ downwelling contributions.

³⁰³ By plotting the evolution of the temperature moment tendency as a function of the tracer-weighted ³⁰⁴ height-above-bottom, we gain a qualitative sense of the height-above-bottom structure of the in-situ ³⁰⁵ buoyancy velocity (Figure 7a). As the three tracers' centers of mass drift over time, their average ³⁰⁶ buoyancy velocities trace out a diapycnal downwelling that increases rapidly towards the bottom in ³⁰⁷ the SML (Figure 7a, blue). Below about 300 m, however, this downwelling gives way to upwelling ³⁰⁸ (Figure 7a, purple) which intensifies the closer the tracer is to the bottom (Figure 7a, red).

In practice, however, *instantaneous* measurement of the tracer-weighted temperature (or temperature variance) tendency is infeasible. Instead, practical methods are akin to estimating the time-average of the right hand-side of eq. 3 (or eq. 4) from finite differencing of the tracer-weighted volume-averaged temperature (or temperature variance)

$$\frac{1}{t_1 - t_0} \int_{t_0}^{t_1} \partial_t \overline{T} \, \mathrm{dt} = \frac{\overline{T}(t_1) - \overline{T}(t_0)}{t_1 - t_0} = \frac{1}{t_1 - t_0} \int_{t_0}^{t_1} 2\overline{\omega} \, \mathrm{dt}$$
(10)

between observational surveys at t_0 and t_1 , typically representing two separate cruises separated by multiple months⁴ (Watson et al. 2013; Ledwell et al. 2000). Alternatively, a linear fit through multiple surveys of $\overline{T}(t)$ can be interpreted as an estimate of *twice* the time-mean tracer-weighted buoyancy velocity. Ledwell et al. (1998) follow this general approach but incorrectly omit the factor of two, which would have brought their tracer-based mixing estimates more in-line with St. Laurent and Schmitt's (1999) in-situ mixing estimates).

Taking t_0 at release and $t_1 = 14$ months, as in BBTRE, the changes in the tracers' first moments still reveal the structure of abyssal mixing layer transformations, albeit at very low resolution: slow

⁴With this method, the number of distinct time-mean buoyancy velocity estimates produced by all pairs of the *n* surveys of $\overline{T}(t_n)$ is $\binom{n}{2} =$

 $[\]frac{n!}{2(n-2)!} = \frac{n(n-1)}{2} \propto n^2$, potentially providing insight into the temporal variability of mixing rates on various timescales. However, most past studies typically only consider either the *n* pairs that include the release as one endpoint (e.g. Watson et al.'s 2013 estimates of the second moments) or the *n* pairs of consecutive surveys (e.g. Ledwell et al.'s 1998's estimates of second moments).

sinking in the SML, rapid upwelling in the BBL, and slow upwelling in between the two (Figure 7a, stars). These promising results suggest that equation (10) offers a novel practical method for estimating buoyancy velocities from TREs based on Ruan and Ferrari (2021)'s tracer-weighted buoyancy moment equations, with the caveat that we have assumed perfect spatial information at instantaneous surveys at both t_0 and t_1 .

³³³ Watermass transformations provide a helpful reference for contextualizing the magnitude and ³³⁴ vertical structure of tracer-weighted velocities. In Appendix B, we convert the height-above-bottom ³³⁵ (or η) structure of watermass transformations into an effective vertical velocity versus η -profile ³³⁶ (see Appendix B),

$$\overline{W}^{T}(\eta) \equiv \frac{\sin\theta}{L_{y}} \frac{\partial}{\partial \eta} \overline{\mathcal{E}}^{T}(\eta).$$
(11)

This metric reveals that vigorous upwelling of $O(4 \times 10^{-5} \text{ m/s})$ is on average confined to the 40 mthick BBL, largely compensated by downwelling an order of magnitude weaker and broader in the SML above (Figure 8b-d, grey lines). This would superficially seem to be inconsistent with the tracer diagnostics, which exhibit weaker BBL upwelling that extends an order of magnitude higher above the bottom.

The key to reconciling the two diagnostics is that the tracer distributions, while initially compact, rapidly spread in η -space (Figure 5c,g,k). To demonstrate the effect of this spreading on the tracer diagnostics, we convolve the vertical velocity versus η -profile (11) with smoothing tracer kernels of different shapes and widths (Figure 8a),

$$\overline{W}(\eta) \approx \int_{-\infty}^{\infty} \mathcal{K}(\eta - \eta') \overline{W}^{T}(\eta') \, \mathrm{d}\eta'.$$
(12)

Tracer kernels with widths less than the thickness of the BBL accurately reproduce its η -structure, 346 while thicker kernels begin smearing the BBL and SML together, reducing both of their magnitudes 347 and elevating the apparent interface between them (Figure 8b,c,d). This smearing effect is partic-348 ularly dramatic for exponential kernels with thick tails, which reasonably approximates the shapes 349 of the Crest and Bottom tracers for most of the experiment (Figure 5g,k). Indeed, convolving the 350 vertical velocity η -profile with exponential kernels of the same approximate width of these tracers 351 reasonably reproduces the tracer-diagnosed η -structure of the buoyancy velocity (Figure 8d). By 352 contrast, the buoyancy velocity experienced by the BBTRE tracer is not as severely convoluted 353

³⁵⁴ (Figure 8b-d) because it neither spreads as rapidly nor does it feel much of the compensating BBL
 ³⁵⁵ upwelling (Figure 5c).

³⁵⁶ c. Bottom-enhanced diapycnal tracer spreading

Over the course of the experiment, all three tracers spread across isopycnals on average. As 357 anticipated from the prescribed bottom-enhanced diffusivity profile: the closer a tracer is released 358 to the bottom, the faster it spreads (Figure 7a; stars). However, this time-mean view obscures 359 surprisingly large temporal variability (Figure 6f,h). This tendency is particularly dramatic for 360 the Bottom tracer, which experiences extremely rapid diapycnal spreading in the first 150 days 361 but, by day 350, stops spreading entirely and even begins temporarily *contracting* in buoyancy 362 space (Figure 6h)! The interpretation of diapycnal tracer spreading is more subtle than that of 363 the mean diapycnal motion of the tracer, since two separate terms contribute to spreading: the 364 tracer-weighted effective diffusivity κ_{Taylor} and diapycnal stretching κ_{ω} (eq. 4). The contribution 365 from the tracer-weighted effective diffusivity is familiar from Taylor (1922)'s classic derivation, 366 and is reasonably well approximated by the tracer-weighted in-situ diffusivity $\overline{\kappa}$ since correlations 367 between the diffusivity and the squared temperature gradients are relatively small (Figure 6d,f,h), 368

$$\kappa_{\text{Taylor}} \equiv \frac{\overline{\kappa |\nabla T|^2}}{|\nabla T|^2} \approx \overline{\kappa}.$$
(13)

This contribution to diapycnal spreading from the tracer-weighted diffusivity remains roughly constant in time, aside from an initial transient as the tracer spreads towards shallower topographic features (Figures 7b). In contrast, the diapycnal stretching effect drives the substantial temporal variability in the diapycnal spreading experienced by the tracers (Figure 6d,f). Depending on the instantaneous distribution of the tracer, this term can vary substantially both in magnitude and sign, either amplifying the tracer-weighted diffusivity by up to 100% or off-setting it entirely (Figure 7b,c; at 40 and 400 days, respectively).

³⁷⁶ *d.* Disentangling diapycnal stretching and contraction effects

³⁷⁷ Motivated by the bi-modal example in Section b, we decompose the diapycnal stretching term ³⁷⁸ κ_{ω} by binning its contributions in (ω, T) space (Figure 9, as in Figure 1b), i.e. by decomposing the volume integral into a sum over sub-volumes:

$$\frac{\kappa_{\omega}}{\kappa_{\text{Taylor}}} = \sum_{i,j} \int_{\mathcal{V}_{\{\omega_i\} \cap \{T_j\}}} \frac{2\omega' T' c}{\mathcal{M} \overline{|\nabla T|^2}} \, dV, \tag{14}$$

where $\mathcal{M} \equiv \int_{\mathcal{V}} c \, dV$ is the total tracer mass and the intersection of subsets $\{\omega_i\}$ and $\{T_j\}$ correspond 380 to distinct sub-volumes $\mathcal{V}_{\{\omega_i\},\{T_i\}}$ of the tracer distribution, defined by their (ω, T) characteristics. 381 Figure 9 shows heatmaps of the contributions from relatively narrow (ω', T') bins as well as the 382 summed contributions from each of the quadrants delineated by the respective signs of ω' and T'. 383 In (14) and throughout this section, we normalize by the total effective diapycnal diffusion κ_{Taylor} 384 to quantify the relative importance of the unconventional stretching effects compared to the more 385 conventional diapycnal diffusion; for example, $\kappa_{\omega}/\kappa_{\text{Taylor}} = 100\%$ implies stretching doubles the 386 diffusive spreading rate while $\kappa_{\omega}/\kappa_{\text{Taylor}} = -100\%$ implies net stretching is sufficiently negative 387 (i.e. contraction) to exactly offset the diffusive spreading. 388

We begin by exploring why the BBTRE tracer experiences very little net diapycnal stretching, 389 in contrast to the idealized SML simulation of Ruan and Ferrari (2021). At day 100 (Figure 9a), 390 for example, the tracer is diapychally stretched ($\overline{\omega'T'} > 0$) by an additional 23% κ_{Taylor} (hereafter 391 dropping the κ_{Taylor} for convenience) as relatively cold tracer relatively downwells ($T' < 0, \omega' < 0$) 392 and relatively warm tracer relatively upwells (T' > 0, $\omega' > 0$). This stretching of 23% is so far 393 consistent with Ruan and Ferrari (2021)'s idealized result of 18% additional stretching. However, 394 a very small amount of cold tracer has made it close enough to the seafloor to be entrained in the 395 BBL, where it upwells vigorously and results in a contraction effect of -9% which, supplemented 396 by an additional -2% contraction from warm downwelling tracer, results in a reduction of the net 397 diapycnal stretching to only 23% - 11% = 12%. By day 440, this patch of tracer is pulled further 398 towards the bottom and its stretching effect grows to 69%, but is offset by an even larger diapycnal 399 contraction of -76% in the BBL (Figure 9b); combined, these diapycnal stretching effects have 400 a negligible effect of reducing diapycnal spreading by only -6%, in contrast to the continued 401 strengthening of stretching effects⁵ predicted by Ruan and Ferrari (2021). 402

At the other extreme, we aim to understand how the Bottom tracer undergoes first a large net diapycnal stretching effect and then an even larger net diapycnal contraction effect. Over the

⁵Ruan and Ferrari (2021) acknowledge stretching may eventually be limited by boundary suppression (as in Holmes et al. 2019), but do not elaborate on its relative timing or magnitude.

first 100 days, most of the tracer upwells in the BBL and warms (Figure 6g). Some of the 415 warmest tracer remains in the BBL, where its upwelling drives a substantial diapycnal stretching 416 of 91% (Figure 9c). However, part of this warm branch of the tracer is entrained into the SML, 417 where its downwelling drives a largely compensating diapychal contraction effect of -80%. The 418 relatively cold patch of tracer that is left behind contributes a stretching of 41% - 15% = 26%, 419 dominated by its relatively slow upwelling ($\omega > 0$ but $\omega' < 0$), bringing the net diapycnal stretching 420 to 91% - 80% + 26% = 37%. By day 440, however, both modes of the tracer distribution (Figure 421 51) drive large diapycnal contraction effects: -98% due to cold upwelling upstream of the sill and 422 -101% due to warm downwelling downstream of the sill (Figures 5j,1 9d). Diapycnal stretching 423 of 93% from the other quadrants offset about half of this diapycnal stretching effect, but the 424 net diapycnal contraction of -106% still overwhelms the spreading due to the in-situ diffusivity, 425 causing the Bottom tracer to temporarily contract in buoyancy space—countering conventional 426 intuition about the average effects of down-gradient diapycnal diffusion. 427

5. Discussion and Conclusion

By applying Ruan and Ferrari (2021)'s buoyancy-moment diagnostics to our quasi-realistic 431 regional simulation of mixing-driven abyssal flows (described in detail in a submitted companion 432 manuscript, Drake et al. 2022), we confirm the qualitative results of Holmes et al. (2019)'s 433 idealized analysis of the BBTRE release in the SML: over time, boundary suppression in the 434 BBL almost exactly compensates for vertical stretching in the SML, such that the net diapycnal 435 spreading of the BBTRE tracer coincidentally provides a reasonably accurate ($\pm 20\%$) estimate 436 of the tracer-weighted in-situ diffusivity (Figure 6d). These simulation results are supported by 437 a recent re-analysis of the BBTRE observations, which reveal a similarly negligible diapycnal 438 stretching effect of $< 5\%\kappa_{Taylor}$ (Figure 6d; Ledwell, personal communication). Quantitatively, 439 however, the diapycnal spreading we simulate for the BBTRE tracer is smaller than the observed 440 spreading by a factor of 2 (Figures 6d, 11), suggesting either the microstructure measurements 441 we use to tune the prescribed diffusivity profile are biased low or our simulation is missing other 442 unknown tracer dispersion processes. This is consistent with Ledwell (in prep)'s inversion of a 443 1D advection-diffusion model, which produced optimal diffusivities about twice as large as the 444 microstructure's sample-mean. Our results are also consistent with the conclusion of the submitted 445

⁴⁴⁶ companion manuscript (Drake et al. 2022), which shows that biases in the simulated flows and ⁴⁴⁷ stratification of the BBTRE fracture zone canyon also suggest the imposed microstructure mixing ⁴⁴⁸ rates may be biased low by a factor of roughly 2. These BBTRE-specific results are consistent ⁴⁴⁹ with the broader observational literature, which unanimously finds that mixing rates estimated ⁴⁵⁰ from TREs are larger than those suggested by co-located microstructure measurements (Ruan and ⁴⁵¹ Ferrari 2021).

In contrast to the BBTRE release, we find that for near-bottom tracers diapycnal stretch-456 ing/contraction effects can be of either sign (depending on the tracer distribution) and of com-457 parable magnitude to the tracer-weighted in-situ diffusivity, $|\kappa_{\omega}| \sim \kappa_{\text{Taylor}} \simeq \overline{\kappa}$ (Figure 6h). Our 458 simulations demonstrate that three-dimensional eddies and topographic effects have a leading or-459 der effect on diapycnal tracer spreading, as tracer distributions are chaotically transported in and 460 out of regions of vigorous mixing. Unsurprisingly, diapycnal stretching and contraction effects are 461 much stronger—and more variable—in our three dimensional flows over rough topography than 462 the already substantial effects reported by Holmes et al. (2019) for two-dimensional tracer trans-463 port under one-dimensional boundary layer dynamics with parameterized isopycnal eddy stirring. 464 For our Bottom tracer release, for example, diapycnal stretching amplifies diapycnal spreading by 465 $O(100\%\kappa_{\text{Taylor}})$ in the first few dozen days of the simulation but suppresses diapycnal spreading 466 by $O(-100\%\kappa_{\text{Taylor}})$ for the last few dozen days (Figures 6h; 7c). 467

Given that rough topography generally implies strong bottom-enhanced diapycnal mixing (Polzin 468 et al. 1997; Waterhouse et al. 2014), which is in turn thought to incite bottom mixed layer eddies 469 (Callies 2018; Wenegrat et al. 2018; Ruan and Callies 2020), significant diapycnal stretching and 470 contraction effects are to be expected near sloping rough topography in the abyss, such as along 471 the global mid-ocean ridge system (Ledwell et al. 2000; Thurnherr et al. 2005, 2020) and within 472 continental slope canyons (Nazarian et al. 2021; Hamann et al. 2021; Alberty et al. 2017). In these 473 regions, unlike for interior ocean releases such as BBTRE, tracer-based estimates of mixing rates 474 must take into account the three-dimensional history of the tracer distribution's evolution. 475

It has long been appreciated that the interpretation of tracer spreading near topography requires greater care because of enhanced boundary mixing and hypsometric effects (e.g. Ledwell and Hickey 1995). Attempts to modify the conventional 1D model to include these boundary effects are varied: by separating the tracer distribution into "boundary" and "interior" regions (Ledwell and Hickey 1995; Ledwell et al. 2016), by allowing vertical structure in the diffusivity profile (Ledwell
et al. 2000), or by extending the 1D model to a 2D (Watson et al. 2013) or 3D (Mackay et al.
2018) model to account for lateral transport into and out of regions of strong mixing. However,
the ad-hoc derivations of these models render them difficult to interpret and compare, suggesting
a complementary role for the more exact buoyancy-moment approach (Ruan and Ferrari 2021).

Mesoscale/submesoscale-resolving regional simulations of TREs are now feasible thanks to 485 exponential increases in computational power (Tulloch et al. 2014; Mashayek et al. 2017; Ogden et 486 al., in prep; this study) and have been used *a posteriori* to help interpret observations and explain 487 differences between mixing rates inferred from TREs and microstructure profiles. However, such 488 simulations have not yet been used to evaluate (or improve upon) operational methods for comparing 489 tracer and microstructure observations, such as by using a "perfect model" framework in which 490 simulated tracer observations are inverted in an attempt to recover the prescribed "true" diffusivity 491 field. Similarly, a priori or real-time numerical simulations could be used to inform future TRE 492 sampling strategies (current best practice is to roughly estimate horizontal transport from real-time 493 velocity estimates from ADCPs or altimetry; Messias and Ledwell, personal communication). To 494 our knowledge, this has not yet been done, with the notable exception of the *Bottom Boundary* 495 Layer Turbulence and Abyssal Recipes team (BLTTRE; NSF Award #1756251), who are using 496 TRE simulations to inform the experiment's planning and sampling strategies. 497

While our results suggest that estimates of in-situ diffusivity profiles from observations of a 498 tracer's second buoyancy moment may be corrupted by complicated diapycnal stretching processes 499 (Figure 7c; consistent with Holmes et al. 2019), they also suggest that the *first* buoyancy moment 500 provides a more robust and straight-forward estimate of the tracer-weighted in-situ turbulent buoy-501 ancy flux convergence (or buoyancy velocity ω ; Figure 7a). However, if the width of the tracer 502 distribution is longer than the scale of flow variations, or if the tails are sufficiently thick, even the 503 first moment diagnostics can be a misleading combination of upwelling and downwelling flows 504 (Figure 8). Nevertheless, as long as a sizable fraction (here $\gg \overline{W}_{SML}^T / \overline{W}_{BBL}^T \approx 10\%$; Figure 8) of 505 the tracer remains in the BBL, the change in the first tracer-weighted buoyancy-moment is likely 506 to provide at least a reasonable lower-bound estimate of the average in-situ buoyancy velocity in 507 the BBL (Section 2b). This is a promising result in light of the ongoing BLTTRE, which aims to 508 provide the first in-situ estimates of BBL upwelling. Short-term surveys, when the tracer distribu-509

tion is still relatively compact (e.g. from a dye release experiment)—may be interpreted as lower 510 bound estimates of BBL upwelling—while long-term surveys—when the tracer roughly equally 511 occupies the BBL and SML-may be interpreted as estimates of net upwelling. Combined, these 512 two estimates could constrain the strength of the amplification factor, the ratio of strictly upwelling 513 transport in the BBL to net upwelling, which is predicted by theory to be much larger than 1 (Ferrari 514 et al. 2016; McDougall and Ferrari 2017; Callies 2018; Holmes and McDougall 2020). In com-515 bination with previous observations of tracer-weighted diapycnal sinking in the SML above rough 516 topography (Ledwell et al. 2000), observations of vigorous tracer-weighted diapycnal upwelling in 517 the BBL would be compelling direct evidence for the emerging paradigm of bottom mixing layer 518 control of the abyssal meridional overturning circulation (Ferrari et al. 2016; de Lavergne et al. 519 2016a; Callies 2018; Callies and Ferrari 2018; Drake et al. 2020; submitted companion manuscript, 520 Drake et al. 2022). 521



FIG. 6. Decomposition of the first and second tracer-weighted temperature moment tendencies, i.e. the rates 272 of diapycnal motion and spreading, in terms of their driving mixing processes. The realistic BBTRE release is 273 shown in blue, the Crest release in purple, and the Bottom release in red. (a-b) show the temporal evolution of the 274 tracer-weighted stratification and stratification squared, with the background stratification $\Lambda \equiv \frac{dT_b}{d\hat{z}}$ for reference 275 (see Appendix A). (c-h) show the temporal evolution of the first and second moment tendencies (opaque solid 276 lines) which are visually indistinguishable from the sum of the contributing mixing processes (transparent solid 277 lines; demonstrating that spurious numerical mixing is negligible), as described by the left- and right-hand-sides 278 of equations (3), $\partial_t \overline{T} = 2\overline{\omega}$, and (4), $\frac{1}{2}\partial_t \overline{(T - \overline{T})^2} = \overline{\kappa |\nabla T|^2} + 2\overline{\omega' T'}$, respectively. Orange lines in (c,d) show the 279 time-averaged BBTRE moment tendencies estimated from observations, where the κ used in the right-hand-side 280 terms is a height-above-bottom profile estimated from an inverse model (Ledwell et al. 1998, revised by Ledwell, 281 in prep). (c,e,g) Dashed and dotted lines show the contributions from strictly upwelling and strictly downwelling 282 regions, respectively. (d,f,h) Dashed lines show the contribution from tracer-weighted in-situ diffusion κ_{Taylor} 283 (approximately equal to the tracer-weighted in-situ diffusivity $\overline{\kappa}$; dash-dotted lines) and dotted lines show the 284 contribution from diapycnal stretching κ_{ω} . 285



FIG. 7. (a) Height-above-bottom-averaged tracer-weighted buoyancy velocity, normalized by the buoyancy gradient to yield an effective vertical velocity (colors). (b,c) As in (a), but for the tracer-weighted in-situ diffusivity $\bar{\kappa}$ and tracer diffusivity κ_{Tracer} . Dots show trajectories (colors darken over time) in terms of the magnitude of moment tendency terms and the tracer-weighted height-above-bottom ($\bar{\text{hab}}(t)$). Stars in (a,c) show the time-averaged moments, as they would be estimated from a TRE survey 440 days after release (assuming perfect spatial coverage).



FIG. 8. Understanding the height-above-bottom structure of tracer transport by convolving the average velocity profile with idealized tracer kernels. (a) Three idealized shapes of tracer kernels, shown with a characteristic width of 200 m meters and centered 150 m above the bottom. (b-d) Grey lines show the height-above-bottom averaged effective vertical velocity, estimated using watermass transformation analysis (eq. 11). Colored lines show the result of convolving this profile with idealized kernels (eq. 12) of different shapes (columns) and widths (colors). Black dots in (d) reproduce the snapshots of tracer-weighted buoyancy velocities shown in Figure 7a, for comparison.



FIG. 9. Percentage contributions to the normalized net diapycnal stretching effect $\kappa_{\omega}/\kappa_{\text{Taylor}}$ from each (ω, T) 403 bin, as a percentage, for the BBTRE (top) and Bottom (bottom) tracers at 100 days (left) and 440 days (right). 404 The plotted quantity is the summand in eq. 14, which are integrated such that the contributions from each bin 405 (log-spaced in ω) can be visually and quantitatively compared. Numbers in the four corners of each panel show 406 the summed contributions from each of the four quadrants delineated by the respective signs of $\omega' \equiv \omega - \overline{\omega}$ and 407 $T' \equiv T - \overline{T}$. The $\omega' = 0$ and T' = 0 lines in olive delineate the four quadrants. For reference, grey contours 408 show the effective diapycnal stretching diffusivity, $\kappa_{\omega} \equiv 2 \frac{\overline{\omega'T'}}{|\nabla T|^2}$, that corresponds to each (ω, T) bin. Sub-409 titles decompose the net diapycnal stretching effect into strictly stretching ($\omega'T' > 0$) and strictly contracting 410 components ($\omega'T' < 0$). PDFs of tracer mass show that a large portion of the tracers' mass does not contribute 411 significantly to these stretching effects (Figure 10). 412



FIG. 10. Probability density function of tracer mass, as a percent contribution of each bin to the total tracer mass. Grey contours and olive lines as in Figure 9.



FIG. 11. Simulated and observed tracer distributions in density space at 14 months. We fit a Gaussian distribution $\propto \exp\left\{\frac{-(\sigma_4 - \sigma_{4,0})^2}{2\tilde{\kappa}t}\right\}$ to the observations by eye (dashed orange). The simulated distribution is reasonably well fit by a Gaussian distribution corresponding to a diffusivity reduced by a factor of 2 (dashed blue), consistent with the results of the buoyancy moments method (Figure 6c,d).

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⁵²⁸ Data availability statement. The source code for the MITgcm simulations and all of the Python ⁵²⁹ code necessary to produce the figures will be publicly available at github.com/hdrake/ ⁵³⁰ sim-bbtre upon acceptance (or earlier by requesting the corresponding author). Our analysis ⁵³¹ of labeled data arrays is greatly simplified by the xarray package in Python (Hoyer and Hamman ⁵³² 2017).

533

APPENDIX A

534

A slope-native MITgcm configuration of mixing layer flows in the Brazil Basin

We use a hydrostatic formulation of the MIT General Circulation Model (MITgcm; Marshall 535 et al. 1997) to simulate mixing-driven flows in the BBTRE canyon and the transient evolution of 536 three localized tracer releases. Regional bathymetry is extracted from the Global Bathymetry and 537 Topography at 15 Arc Sec dataset (SRTM15+; Tozer et al. 2019) and interpolated onto a locally-538 tangent Cartesian grid $(\hat{x}, \hat{y}, \hat{z})$ aligned with the BBTRE canyon, where \hat{x} denotes the along-canyon 539 (or cross-ridge) dimension, \hat{y} denotes the cross-canyon (or along-ridge) dimension, and $\hat{d}(\hat{x}, \hat{y})$ is 540 the seafloor depth (Figure 2a). The domain includes both the BBTRE tracer release location and 541 ample room for up-canyon advection of the tracer, which is anticipated based on both the BBTRE 542 observations (Ledwell et al. 2000) and bottom boundary layer theory (Holmes et al. 2019). 543

Inspired by 1D boundary layer theory and the idealized 3D simulations of Callies (2018), we configure a slope-native implementation of the MITgcm (only summarized here; details in Drake et al., in prep). First, we separate a quiescent ($\mathbf{u}_b \equiv \mathbf{0}$) background with uniform stratification $\Lambda \equiv \frac{dT_b}{d\hat{z}} = 9 \times 10^{-4} \,^{\circ}\text{C/m}$ from the solution and solve only for the perturbations $T_p \equiv T - T_b$ and $\mathbf{u}_p \equiv \mathbf{u} - \mathbf{u}_b$ about this background state, which requires adding the appropriate tendency terms to the perturbation temperature and momentum equations, respectively. Second, we transform the MITgcm into the coordinates of the mean slope, with slope angle $\theta = 1.26 \times 10^{-3}$ (Figure 2b), allowing us to apply periodic boundary conditions to the perturbations in the (x, y) plane of the mean slope. The de-trended seafloor depth is given by $d(x, y) \equiv \hat{d}(\hat{x}, \hat{y}) - \hat{x} \tan \theta$. Mean crossslope upwelling and downwelling across the periodic **x** boundary provide infinite sources of dense and light waters, respectively, allowing equilibration of the solution without requiring an explicit restoring force to balance the homogenizing tendency of turbulent mixing (Garrett 1991).

A submitted companion paper (Drake et al. 2022) explores the mixing-driven circulations that 556 arise in this simulation in detail. Bottom-enhanced mixing spins up a broad diapycnal sinking 557 in the well-stratified interior and a vigorous diabatic upwelling in the bottom boundary layer. 558 Despite a modest restratifying effect by this mean overturning circulation, the solution develops a 559 substantial horizontal temperature gradient which stores available potential energy. This available 560 potential energy fuels instabilities, which grow to finite amplitude and are characterized by a 561 Rossby number of $R_o \approx 1$, i.e. are submesoscale in nature (see e.g. McWilliams 2016). One 562 effect of these eddies is to restratify the bottom 20m or so, bringing the simulated stratification 563 more in line with observations than 1D boundary layer dynamics would suggest (Callies 2018; 564 Ruan and Callies 2020). A hierarchy of progressively simplified versions of the simulation are 565 used as mechanism denial experiments to show the importance of different dynamical processes 566 in controlling the near-bottom stratification, which in turn controls the magnitude of near-bottom 567 diapycnal upwelling. 568

In our slope-native configuration, one should imagine infinitely many copies of TREs, each 569 separated by a horizontal distance $L_x = 480 \text{ km}$ (domain length) and vertical height $L_x \tan \theta \approx$ 570 1000 m (corresponding to a background temperature difference $\Delta T \approx \frac{dT_b}{d\hat{z}} L_x \sin \theta = 0.52 \,^{\circ}\text{C}$). A 571 limitation of this configuration is that by 1000 days enough of the tracer crosses the periodic 572 boundaries that the copies of the tracers begin significantly interfering with each other and the 573 temperature moment calculations become meaningless, which is why we truncate the simulations 574 after the timing of the first BBTRE survey (14 months \approx 440 days). For all of the analysis presented 575 here, we re-center our periodic domain on the center of mass of a single copy of the tracer cloud 576 before adding the background state (i.e. the constantly stratified background temperature field T_b) 577 back in and then we crop the infinite domain to ignore other copies of the tracer (similar to the 578 approach used to compute watermass transformations in Appendix B). 579

APPENDIX B

Eulerian and tracer-weighted watermass transformations

⁵⁸² A natural framework for understanding the drivers of diapycnal transport is watermass trans-⁵⁸³ formation analysis (Walin 1982; Marshall et al. 1999), which reframes the buoyancy budget in ⁵⁸⁴ buoyancy space by integrating along buoyancy surfaces (or over buoyancy classes). Following ⁵⁸⁵ Ferrari et al. (2016), the diapycnal transport $\mathcal{E}(T,t)$ across a buoyancy surface $\mathcal{A}(T)$ is given by

$$\mathcal{E}(T,t) \equiv \iint_{\mathcal{A}(T)} \mathbf{e} \cdot \mathbf{n} \, \mathrm{d}A = \partial_T \int_{\mathcal{V}(\tilde{T} < T)} \omega \, \mathrm{d}V,\tag{B1}$$

⁵⁸⁶ where $\mathbf{e} \equiv \left(\mathbf{u} \cdot \mathbf{n} - \frac{T_t}{|\nabla T|}\right) \mathbf{n}$ is the diapycnal velocity and $\mathcal{V}(\tilde{T} < T)$ is the volume enclosing any water ⁵⁸⁷ denser than *T*. Since our simulations have not fully equilibrated in the SML, diapycnal transports ⁵⁸⁸ include two components: flow across a buoyancy surface and the movement of the buoyancy ⁵⁸⁹ surfaces themselves. In the present context, it is useful to distinguish contributions to the diapycnal ⁵⁹⁰ transport from a strictly upwelling BBL component, where the integral is only evaluated over the ⁵⁹¹ strictly upwelling volume $\mathcal{V}(\tilde{T} < T; \omega > 0)$, and a strictly downwelling SML component, similarly ⁵⁹² defined (see Figure B1).

In practice, meaningful evaluation of this integral in the slope-native configuration requires 593 stitching together $H/(L_x \tan \theta) \approx O(5)$ periodic copies of the domain (where H is the height of 594 the domain) before adding in the background buoyancy field B, so that each isopycnal can be 595 followed all the way from its incrop at the seafloor to the interior far-field where mixing is weak 596 (Figure B1). Further, because our simulation is periodic in the cross-slope direction (and thus in 597 mean buoyancy), the resulting watermass transformations are periodic over a buoyancy interval 598 $\Delta T = \Lambda L_x \tan \theta \approx 0.52 \,^{\circ}$ C. Temporal variability of watermass transformations is small relative to 599 the other variations we focus on, so all results hereafter refer to their time-mean. 600

⁶⁰⁸ Averaging over a buoyancy layer of thickness ΔT yields a single representative value of the net ⁶⁰⁹ watermass transformation,

$$\overline{\mathcal{E}}^{T} \equiv \frac{1}{\Delta T} \int_{T}^{T+\Delta T} \mathcal{E}(\tilde{T}) \, \mathrm{d}\tilde{T} = \int_{\mathcal{V}(T < \tilde{T} < T+\Delta T)} \frac{\omega}{\Delta T} \, \mathrm{d}V. \tag{B2}$$

581



FIG. B1. Turbulent buoyancy (temperature) flux convergence along the trough of the BBTRE canyon. Vertical olive lines show along-canyon boundaries of the simulation domain; the solution is doubly periodic in buoyancy perturbations, but discontinuous in the total buoyancy in the along-canyon direction due to a constant background mean slope and stratification. For the small mean slopes considered here, computing watermass transformations thus requires reconstructing the full extent of buoyancy surfaces by stitching together multiple copies of the domain, each translated by a multiple of the domain extent L_x and by a background temperature jump $\Delta T =$ $\Delta \Delta z \approx 0.52 \text{ °C}$ (where $\Delta z = L_x \tan \theta$ is the layer thickness).

This equation is also reminiscent of that for the evolution of the first tracer-weighted buoyancy moment (3), with the whole domain being weighted equally as opposed to being weighted by the tracer concentration.

The detailed height-above-bottom (η , for short) structure of upwelling and downwelling watermass transformations are also of interest, since these are more directly comparable with measurements from vertical profilers, 1D BBL theory, and the diapycnal transport of localized tracers. Building upon Holmes and McDougall (2020), we define the height-above-bottom cumulative watermass transformation as:

$$\overline{\mathcal{E}}^{T}(\eta) = \int_{\mathcal{V}(T_0 < \tilde{T} < T_0 + \Delta T; \, \tilde{\eta} < \eta)} \frac{\omega}{\Delta T} \, \mathrm{d}V. \tag{B3}$$

⁶¹⁸ We aim to convert these watermass transformations into effective vertical velocities, for more ⁶¹⁹ direct comparison with the tracer diagnostics. Loosely, taking the slope-normal (or η) derivative provides the up-slope upwelling flux (in m^2/s) at a given height-above-bottom:

$$\frac{\partial}{\partial \eta} \overline{\mathcal{E}}^{T}(\eta) = \frac{\partial}{\partial \eta} \int_{\mathcal{V}(T_{0} < \tilde{T} < T_{0} + \Delta T; \, \tilde{\eta} < \eta)} \frac{\omega}{\Delta T} \, \mathrm{d}V. \tag{B4}$$

⁶²¹ Multiplying by $\sin \theta$ approximately converts this to a vertical flux, and dividing by the width L_y ⁶²² of the domain finishes the conversion to the effective velocity (11). Profiles of $\overline{W}^T(\eta)$ are shown in ⁶²³ Figure 8 and, after convolution with idealized height-above-bottom tracer distributions, compare ⁶²⁴ favorably with the diagnosed vertical structure of tracer upwelling.

625 References

Abernathey, R. P., I. Cerovecki, P. R. Holland, E. Newsom, M. Mazloff, and L. D. Talley, 2016:

⁶²⁷ Water-mass transformation by sea ice in the upper branch of the Southern Ocean overturning.

⁶²⁸ *Nature Geoscience*, **9** (**8**), 596–601, https://doi.org/10.1038/ngeo2749, URL http://www.nature.

com/articles/ngeo2749, publisher: Nature Publishing Group.

Alberty, M. S., S. Billheimer, M. M. Hamann, C. Y. Ou, V. Tamsitt, A. J. Lucas, and
 M. H. Alford, 2017: A reflecting, steepening, and breaking internal tide in a submarine
 canyon. *Journal of Geophysical Research: Oceans*, **122** (**8**), 6872–6882, https://doi.org/
 10.1002/2016JC012583, URL https://onlinelibrary.wiley.com/doi/abs/10.1002/2016JC012583,
 _eprint: https://onlinelibrary.wiley.com/doi/pdf/10.1002/2016JC012583.

Baker, M. A., and C. H. Gibson, 1987: Sampling Turbulence in the Stratified Ocean:
Statistical Consequences of Strong Intermittency. *Journal of Physical Oceanography*, **17** (10), 1817–1836, https://doi.org/10.1175/1520-0485(1987)017<1817:STITSO>2.0.CO;
URL https://journals.ametsoc.org/view/journals/phoc/17/10/1520-0485_1987_017_1817_
stitso_2_0_co_2.xml, publisher: American Meteorological Society Section: Journal of Physical

640 Oceanography.

- Bryan, K., and L. J. Lewis, 1979: A water mass model of the world ocean. *Journal of Geophysical Research*, 84 (C5), 2503–2517, https://doi.org/10.1029/JC084iC05p02503, iSBN: 0148-0227.
- Cael, B., and A. Mashayek, 2021: Log-Skew-Normality of Ocean Turbulence. *Physical Review Letters*, **126 (22)**, 224 502, https://doi.org/10.1103/PhysRevLett.126.224502, URL https://link.

aps.org/doi/10.1103/PhysRevLett.126.224502, publisher: American Physical Society. 645

Callies, J., 2018: Restratification of Abyssal Mixing Layers by Submesoscale Baroclinic 646 Eddies. Journal of Physical Oceanography, JPO-D-18-0082.1, https://doi.org/10.1175/ 647 JPO-D-18-0082.1, URL http://journals.ametsoc.org/doi/10.1175/JPO-D-18-0082.1. 648

- Callies, J., and R. Ferrari, 2018: Dynamics of an Abyssal Circulation Driven by Bottom-Intensified 649
- Mixing on Slopes. Journal of Physical Oceanography, 48 (6), 1257–1282, https://doi.org/ 650
- 10.1175/JPO-D-17-0125.1, URL http://journals.ametsoc.org/doi/10.1175/JPO-D-17-0125.1. 651

Clément, L., A. M. Thurnherr, and L. C. St. Laurent, 2017: Turbulent Mixing in a Deep 652 Fracture Zone on the Mid-Atlantic Ridge. Journal of Physical Oceanography, 47 (8), 1873– 653 1896, https://doi.org/10.1175/JPO-D-16-0264.1, URL http://journals.ametsoc.org/doi/10.1175/ 654 JPO-D-16-0264.1.

655

- de Lavergne, C., G. Madec, J. Le Sommer, A. J. G. Nurser, and A. C. Naveira Garabato, 656 2016a: The Impact of a Variable Mixing Efficiency on the Abyssal Overturning. *Journal* 657 of Physical Oceanography, 46 (2), 663-681, https://doi.org/10.1175/JPO-D-14-0259.1, URL 658 http://journals.ametsoc.org/doi/10.1175/JPO-D-14-0259.1. 659
- de Lavergne, C., G. Madec, J. Le Sommer, A. J. G. Nurser, and A. C. Naveira Garabato, 660 2016b: On the Consumption of Antarctic Bottom Water in the Abyssal Ocean. Journal 661 of Physical Oceanography, 46 (2), 635–661, https://doi.org/10.1175/JPO-D-14-0201.1, URL 662 http://journals.ametsoc.org/doi/10.1175/JPO-D-14-0201.1. 663
- С., and Coauthors, 2020: A Parameterization of Local Rede Lavergne, and 664 Journal of Advances in Modeling Earth Systems, (5), mote Tidal Mixing. 12 665 e2020MS002065, https://doi.org/https://doi.org/10.1029/2020MS002065, URL 666 https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2020MS002065, _eprint: 667 https://agupubs.onlinelibrary.wiley.com/doi/pdf/10.1029/2020MS002065. 668
- Dillon. T. M., 1982: Vertical overturns: А comparison of Thorpe and Ozmi-669 Journal 87 (C12), dov length scales. of Geophysical Research: Oceans. 670 9601-9613, https://doi.org/https://doi.org/10.1029/JC087iC12p09601, URL https: 671

34

⁶⁷² //agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/JC087iC12p09601, __eprint:

https://agupubs.onlinelibrary.wiley.com/doi/pdf/10.1029/JC087iC12p09601.

Drake. H. F., R. Ferrari, and J. Callies, 2020: Abyssal Circulation Driven 674 Near-Boundary Water Mass Transformations and Interior by Mixing: Stratifi-675 50 (8), Journal of Physical Oceanography, 2203-2226, https://doi.org/ cation. 676 10.1175/JPO-D-19-0313.1, URL https://journals.ametsoc.org/jpo/article/50/8/2203/348530/ 677 Abyssal-Circulation-Driven-by-Near-Boundary-Mixing, publisher: American Meteorological 678 Society. 679

Drake, H. F., X. Ruan, R. Ferrari, A. M. Thurnherr, K. Ogden, and J. Callies, 2022: Dynamics
 of eddying abyssal mixing layers over rough topography. URL https://eartharxiv.org/repository/
 view/3000/, publisher: EarthArXiv.

Ferrari, R., A. Mashayek, T. J. McDougall, M. Nikurashin, and J.-M. Campin, 2016: Turning Ocean
 Mixing Upside Down. *Journal of Physical Oceanography*, 46 (7), 2239–2261, https://doi.org/
 10.1175/JPO-D-15-0244.1, URL http://journals.ametsoc.org/doi/10.1175/JPO-D-15-0244.1.

Garrett, C., 1991: Marginal mixing theories. *Atmosphere-Ocean*, **29** (2), 313–339,
 https://doi.org/10.1080/07055900.1991.9649407, URL http://www.tandfonline.com/doi/abs/10.
 1080/07055900.1991.9649407.

Garrett, C., P. MacCready, and P. Rhines, 1993: Boundary Mixing and Arrested Ekman Layers: Rotating Stratified Flow Near a Sloping Boundary. *Annual Review of Fluid Mechan- ics*, 25 (1), 291–323, https://doi.org/10.1146/annurev.fl.25.010193.001451, URL http://www.
annualreviews.org/doi/10.1146/annurev.fl.25.010193.001451, publisher: Annual Reviews 4139
El Camino Way, P.O. Box 10139, Palo Alto, CA 94303-0139, USA.

Garrett, C., and W. Munk, 1972: Space-Time scales of internal waves. *Geo- physical Fluid Dynamics*, **3** (**3**), 225–264, https://doi.org/10.1080/03091927208236082,
 URL https://doi.org/10.1080/03091927208236082, publisher: Taylor & Francis _eprint:
 https://doi.org/10.1080/03091927208236082.

C.. 1975: Space-time Garrett. and W. Munk. scales of internal waves: 698 of Geophysical (1896 - 1977),А progress report. Journal Research 699

 700
 80
 (3),
 291–297,
 https://doi.org/10.1029/JC080i003p00291,
 URL
 https:

 701
 //agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/JC080i003p00291,
 __eprint:

 702
 https://agupubs.onlinelibrary.wiley.com/doi/pdf/10.1029/JC080i003p00291.
 __eprint:

E. D'Asaro, J. Riley, and E. Kunze, 2018: Gregg, М., Mixing Efficiency in 703 Ocean. Annual Review of Marine Science, 10 (1), 443-473, https://doi.org/ the 704 10.1146/annurev-marine-121916-063643, URL http://www.annualreviews.org/doi/10.1146/ 705 annurev-marine-121916-063643. 706

Gregg, M. C., 1989: Scaling turbulent dissipation in the thermocline. *Journal of Geophysical Research*, 94 (C7), 9686, https://doi.org/10.1029/JC094iC07p09686, URL http://doi.wiley.com/
 10.1029/JC094iC07p09686.

Gregg, M. C., T. B. Sanford, and D. P. Winkel, 2003: Reduced mixing from the breaking of internal
waves in equatorial waters. *Nature*, 422 (6931), 513–515, https://doi.org/10.1038/nature01507,
URL https://www.nature.com/articles/nature01507, number: 6931 Publisher: Nature Publishing
Group.

Hamann, M. M., M. H. Alford, A. J. Lucas, A. F. Waterhouse, and G. Voet, 2021: Turbulence Driven by Reflected Internal Tides in a Supercritical Submarine Canyon. *Journal of Physical Oceanography*, **51** (2), 591–609, https://doi.org/10.1175/JPO-D-20-0123.1, URL
https://journals.ametsoc.org/view/journals/phoc/51/2/jpo-d-20-0123.1.xml, publisher: American Meteorological Society Section: Journal of Physical Oceanography.

- J. and S. M. Flatté, 1986: F. S., Wright, Energy and action flow Henyey, 719 through the internal wave approach. Journal of Geophysical field: An eikonal 720 91 (C7), 8487–8495, https://doi.org/10.1029/JC091iC07p08487, *Research:* Oceans. 721 https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/JC091iC07p08487, eprint: URL 722 https://agupubs.onlinelibrary.wiley.com/doi/pdf/10.1029/JC091iC07p08487. 723
- Hogg, N., P. Biscaye, W. Gardner, and W. Jr, 1982: On the Transport and Modification of Antarctic
 Bottom Water in the Vema Channel. *J. Mar. Res.*, 40, 231–263.
- Holmes, R. M., C. de Lavergne, and T. J. McDougall, 2019: Tracer Transport within Abyssal
 Mixing Layers. *Journal of Physical Oceanography*, 49 (10), 2669–2695, https://doi.org/10.

⁷²⁸ 1175/JPO-D-19-0006.1, URL https://journals.ametsoc.org/doi/full/10.1175/JPO-D-19-0006.1,
 ⁷²⁹ publisher: American Meteorological Society.

Holmes, R. M., and T. J. McDougall, 2020: Diapycnal Transport near a Sloping Bottom
Boundary. *Journal of Physical Oceanography*, **50** (11), 3253–3266, https://doi.org/10.1175/
JPO-D-20-0066.1, URL https://journals.ametsoc.org/view/journals/phoc/50/11/jpoD200066.
xml, publisher: American Meteorological Society Section: Journal of Physical Oceanography.

- Holtermann. P. L., L. Umlauf. T. Tanhua, O. Schmale. G. Rehder, and J. J. 735 Waniek. 2012: The Baltic Sea Tracer Release Experiment: 1. Mixing rates. 736 Journal of Geophysical Research: Oceans, 117 (C1), https://doi.org/10.1029/ 737 2011JC007439, URL https://onlinelibrary.wiley.com/doi/abs/10.1029/2011JC007439, _eprint: 738 https://onlinelibrary.wiley.com/doi/pdf/10.1029/2011JC007439. 739
- Hoyer, S., and J. Hamman, 2017: xarray: N-D labeled arrays and datasets in Python. *Journal of Open Research Software*, 5 (1), https://doi.org/10.5334/jors.148, URL http://doi.org/10.5334/
 jors.148.
- Huang, R. X., and X. Jin, 2002: Deep Circulation in the South Atlantic Induced by Bottom Intensified Mixing over the Midocean Ridge*. *Journal of Physical Oceanography*, 32 (4),
 1150–1164, https://doi.org/10.1175/1520-0485(2002)032<1150:DCITSA>2.0.CO;2.

Kunze, E., E. Firing, J. M. Hummon, T. K. Chereskin, and A. M. Thurnherr, 2006: Global
Abyssal Mixing Inferred from Lowered ADCP Shear and CTD Strain Profiles. *Journal of Physical Oceanography*, **36 (8)**, 1553–1576, https://doi.org/10.1175/JPO2926.1, URL https:
//journals.ametsoc.org/view/journals/phoc/36/8/jpo2926.1.xml, publisher: American Meteorological Society Section: Journal of Physical Oceanography.

Ledwell, J. R., T. F. Duda, M. A. Sundermeyer, and H. E. Seim, 2004: Mix-751 ing in a coastal environment: 1. A view from dye dispersion. Journal of 752 Geophysical Research: 109 (C10), https://doi.org/https://doi.org/10.1029/ Oceans. 753 2003JC002194, URL https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2003JC002194, 754 eprint: https://agupubs.onlinelibrary.wiley.com/doi/pdf/10.1029/2003JC002194. 755

37

Ledwell, J. R., R. He, Z. Xue, S. F. DiMarco, L. J. Spencer, and P. Chapman, 2016: Dispersion of a tracer in the deep Gulf of Mexico. *Journal of Geo- physical Research: Oceans*, **121** (2), 1110–1132, https://doi.org/https://doi.org/10.1002/
2015JC011405, URL https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1002/2015JC011405,
_eprint: https://agupubs.onlinelibrary.wiley.com/doi/pdf/10.1002/2015JC011405.

Ledwell, J. R., and B. M. Hickey, 1995: Evidence for enhanced boundary mix-761 ing in the Santa Monica Basin. Journal of Geophysical Research: Oceans, 762 100 (C10), 20665-20679. https://doi.org/https://doi.org/10.1029/94JC01182, 763 URL https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/94JC01182, _eprint: 764 https://agupubs.onlinelibrary.wiley.com/doi/pdf/10.1029/94JC01182. 765

Ledwell, J. R., E. T. Montgomery, K. L. Polzin, L. C. St. Laurent, R. W. Schmitt, and J. M.
 Toole, 2000: Evidence for enhanced mixing over rough topography in the abyssal ocean. *Nature*,
 403 (6766), 179–182, https://doi.org/10.1038/35003164, URL http://www.nature.com/articles/
 35003164, publisher: Nature Publishing Group.

Ledwell, J. R., A. J. Watson, and C. S. Law, 1998: Mixing of a tracer in the pycnocline. *Journal of Geophysical Research: Oceans*, **103** (C10), 21 499–21 529, https://doi.org/https://doi.org/10.
1029/98JC01738, URL https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/98JC01738,
__eprint: https://agupubs.onlinelibrary.wiley.com/doi/pdf/10.1029/98JC01738.

 Lele, R., and Coauthors, 2021: Abyssal Heat Budget in the Southwest Pacific Basin. *Journal* of *Physical Oceanography*, **51** (**11**), 3317–3333, https://doi.org/10.1175/JPO-D-21-0045.1,
 URL https://journals.ametsoc.org/view/journals/phoc/51/11/JPO-D-21-0045.1.xml, publisher:
 American Meteorological Society Section: Journal of Physical Oceanography.

Lumpkin, R., and K. Speer, 2007: Global Ocean Meridional Overturning. *Journal of Physical Oceanography*, **37** (10), 2550–2562, https://doi.org/10.1175/JPO3130.1, URL http://dx.doi.org/
 10.1175/JPO3130.1, iSBN: 0022-3670.

Mackay, N., J. R. Ledwell, M.-J. Messias, A. C. N. Garabato, J. A. Brearley, A. J. S.
 Meijers, D. C. Jones, and A. J. Watson, 2018: Diapycnal Mixing in the Southern
 Ocean Diagnosed Using the DIMES Tracer and Realistic Velocity Fields. *Journal of Geo- physical Research: Oceans*, **123** (4), 2615–2634, https://doi.org/https://doi.org/10.1002/

- ⁷⁸⁵ 2017JC013536, URL https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1002/2017JC013536,
 ⁷⁸⁶ _eprint: https://agupubs.onlinelibrary.wiley.com/doi/pdf/10.1002/2017JC013536.
- MacKinnon, J. A., and Coauthors, 2017: Climate Process Team on Internal Wave–Driven Ocean
 Mixing. *Bulletin of the American Meteorological Society*, 98 (11), 2429–2454, https://doi.org/10.
- ⁷⁸⁹ 1175/BAMS-D-16-0030.1, URL http://journals.ametsoc.org/doi/10.1175/BAMS-D-16-0030.1.
- Marshall, J., C. Hill, L. Perelman, and A. Adcroft, 1997: Hydrostatic, quasi-hydrostatic, and non hydrostatic ocean modeling. *Journal of Geophysical Research*, **102** (C3), 5733, https://doi.org/
 10.1029/96JC02776, iSBN: 2156-2202.
- Marshall, J., D. Jamous, and J. Nilsson, 1999: Reconciling thermodynamic and dynamic methods
 of computation of water-mass transformation rates. *Deep-Sea Research Part I: Oceanographic Research Papers*, 46 (4), 545–572, https://doi.org/10.1016/S0967-0637(98)00082-X, iSBN:
- ⁷⁹⁶ 0967-0637.
- ⁷⁹⁷ Mashayek, A., R. Ferrari, S. Merrifield, J. R. Ledwell, L. St Laurent, and A. N. Garabato,
 ⁷⁹⁸ 2017: Topographic enhancement of vertical turbulent mixing in the Southern Ocean. *Nature* ⁷⁹⁹ *Communications*, 8, 14197, https://doi.org/10.1038/ncomms14197, URL http://www.nature.
 ⁸⁰⁰ com/doifinder/10.1038/ncomms14197, publisher: Nature Publishing Group.
- McDougall, T. J., and R. Ferrari, 2017: Abyssal Upwelling and Downwelling Driven by Near Boundary Mixing. *Journal of Physical Oceanography*, **47** (2), 261–283, https://doi.org/10.
 1175/JPO-D-16-0082.1, URL https://journals.ametsoc.org/doi/full/10.1175/JPO-D-16-0082.1,
 publisher: American Meteorological Society.
- McWilliams, J. C., 2016: Submesoscale currents in the ocean. *Proceedings of the Royal Society A: Mathematical, Physical and Engineering Sciences*, **472** (**2189**), 20160117, https://doi.org/
- 10.1098/rspa.2016.0117, URL https://royalsocietypublishing.org/doi/10.1098/rspa.2016.0117,
 publisher: Royal Society.
- Munk, W. H., 1966: Abyssal recipes. *Deep Sea Research and Oceanographic Abstracts*,
 13 (4), 707–730, https://doi.org/10.1016/0011-7471(66)90602-4, arXiv: cs/9605103 ISBN:
 1600117471.

Munk, W. H., and C. Wunsch, 1998: Abyssal Recipes II: energetics of tidal and wind mixing. *Deep-Sea Research Part I: Oceanographic Research Papers*, **45**, 1978–2010.

Nazarian, R. Н., С. M. Burns, S. Legg, M. C. Buijsman, H. Kaur, and 814 On the Magnitude of Canyon-Induced Mixing. B. K. Arbic, 2021: Journal of 815 Oceans, 126 (11), e2021JC017671, https://doi.org/10.1029/ Geophysical Research: 816 2021JC017671, URL https://onlinelibrary.wiley.com/doi/abs/10.1029/2021JC017671, _eprint: 817 https://onlinelibrary.wiley.com/doi/pdf/10.1029/2021JC017671. 818

Nikurashin, M., and R. Ferrari, 2009: Radiation and Dissipation of Internal Waves Gener ated by Geostrophic Motions Impinging on Small-Scale Topography: Theory. *Journal of Physical Oceanography*, **40** (5), 1055–1074, https://doi.org/10.1175/2009JPO4199.1, URL
 https://journals.ametsoc.org/doi/full/10.1175/2009JPO4199.1.

Nikurashin, M., and S. Legg, 2011: A Mechanism for Local Dissipation of Internal Tides Generated
 at Rough Topography. *Journal of Physical Oceanography*, 41 (2), 378–395, https://doi.org/
 10.1175/2010JPO4522.1, URL http://journals.ametsoc.org/doi/abs/10.1175/2010JPO4522.1.

Osborn, T. R., 1980: Estimates of the Local Rate of Vertical Diffusion from Dissipation
 Measurements. *Journal of Physical Oceanography*, **10** (1), 83–89, https://doi.org/10.1175/
 1520-0485(1980)010<0083:EOTLRO>2.0.CO;2, URL http://journals.ametsoc.org/doi/abs/10.
 1175/1520-0485%281980%29010%3C0083%3AEOTLRO%3E2.0.CO%3B2.

Osborn, T. R., and C. S. Cox, 1972: Oceanic fine structure. *Geophysical Fluid Dynamics*, 3 (1),
 321–345, https://doi.org/10.1080/03091927208236085, URL http://www.tandfonline.com/doi/
 abs/10.1080/03091927208236085.

Polzin, K., J. Toole, J. R. Ledwell, and R. Schmitt, 1997: Spatial Variability of Turbulent Mix ing in the Spatial Variability Abyssal Ocean. *Science*, **276** (**5309**), 93–96, https://doi.org/10.
 1126/science.276.5309.93, URL http://www.sciencemag.org/cgi/content/abstract/276/5309/93,
 iSBN: 0036-8075.

⁸³⁷ Polzin, K. L., 2009: An abyssal recipe. *Ocean Modelling*, **30** (4), 298–309, https://doi.org/10.
 ⁸³⁸ 1016/j.ocemod.2009.07.006.

40

Polzin, K. L., and T. J. McDougall, 2022: Chapter 7 - Mixing at the ocean's bottom boundary.
 Ocean Mixing, M. Meredith, and A. Naveira Garabato, Eds., Elsevier, 145–180, https://doi.org/
 10.1016/B978-0-12-821512-8.00014-1, URL https://www.sciencedirect.com/science/article/
 pii/B9780128215128000141.

Polzin, K. L., J. M. Toole, R. W. Schmitt, K. L. Polzin, J. M. Toole, and R. W. Schmitt, 1995:
 Finescale Parameterizations of Turbulent Dissipation. *Journal of Physical Oceanography*, 25 (3),
 306–328, https://doi.org/10.1175/1520-0485(1995)025<0306:FPOTD>2.0.CO;2.

Ruan, X., and J. Callies, 2020: Mixing-Driven Mean Flows and Submesoscale Eddies over
Mid-Ocean Ridge Flanks and Fracture Zone Canyons. *Journal of Physical Oceanography*,
50 (1), 175–195, https://doi.org/10.1175/JPO-D-19-0174.1, URL https://journals.ametsoc.org/
view/journals/phoc/50/1/jpo-d-19-0174.1.xml, publisher: American Meteorological Society
Section: Journal of Physical Oceanography.

⁸⁵¹ Ruan, X., and R. Ferrari, 2021: Diagnosing Diapycnal Mixing from Passive Tracers. *Journal* of Physical Oceanography, **51** (**3**), 757–767, https://doi.org/10.1175/JPO-D-20-0194.1, URL
 ⁸⁵³ https://journals.ametsoc.org/view/journals/phoc/51/3/JPO-D-20-0194.1.xml, publisher: Amer ⁸⁵⁴ ican Meteorological Society Section: Journal of Physical Oceanography.

Simmons, H. L., S. R. Jayne, L. C. St. Laurent, and A. J. Weaver, 2004: Tidally driven mixing
in a numerical model of the ocean general circulation. *Ocean Modelling*, 6 (3-4), 245–263,
https://doi.org/10.1016/S1463-5003(03)00011-8, iSBN: 1463-5003.

Spingys, C. P., A. C. N. Garabato, S. Legg, K. L. Polzin, E. P. Abrahamsen, C. E. Buckingham, A. Forryan, and E. E. Frajka-Williams, 2021: Mixing and Transformation in a
Deep Western Boundary Current: A Case Study. *Journal of Physical Oceanography*, **51** (4),
1205–1222, https://doi.org/10.1175/JPO-D-20-0132.1, URL https://journals.ametsoc.org/view/
journals/phoc/aop/JPO-D-20-0132.1/JPO-D-20-0132.1.xml, publisher: American Meteorological Society Section: Journal of Physical Oceanography.

St. Laurent, L., and R. W. Schmitt, 1999: The Contribution of Salt Fingers to Vertical
 Mixing in the North Atlantic Tracer Release Experiment. *Journal of Physical Oceanog- raphy*, **29** (7), 1404–1424, https://doi.org/10.1175/1520-0485(1999)029<1404:TCOSFT>

41

- 2.0.CO;2, URL https://journals.ametsoc.org/view/journals/phoc/29/7/1520-0485_1999_029_
- 1404_tcosft_2.0.co_2.xml, publisher: American Meteorological Society Section: Journal of
 Physical Oceanography.
- St. Laurent, L. C., J. M. Toole, and R. W. Schmitt, 2001: Buoyancy Forcing by Turbulence above

Rough Topography in the Abyssal Brazil Basin*. *Journal of Physical Oceanography*, **31** (12),

⁸⁷² 3476–3495, https://doi.org/10.1175/1520-0485(2001)031<3476:BFBTAR>2.0.CO;2.

Stommel, H., and A. B. Arons, 1959: On the abyssal circulation of the world ocean —
II. An idealized model of the circulation pattern and amplitude in oceanic basins. *Deep Sea Research (1953)*, 6, 217–233, https://doi.org/10.1016/0146-6313(59)90075-9, URL http:

⁸⁷⁶ //www.sciencedirect.com/science/article/pii/0146631359900759.

Sundermeyer, M. A., E. A. Terray, J. R. Ledwell, A. G. Cunningham, P. E. LaRocque, J. Banic,

and W. J. Lillycrop, 2007: Three-Dimensional Mapping of Fluorescent Dye Using a Scanning,

⁸⁷⁹ Depth-Resolving Airborne Lidar. *Journal of Atmospheric and Oceanic Technology*, **24**(**6**), 1050–

1065, https://doi.org/10.1175/JTECH2027.1, URL https://journals.ametsoc.org/view/journals/

atot/24/6/jtech2027_1.xml, publisher: American Meteorological Society Section: Journal of Atmospheric and Oceanic Technology.

Transpierre and Oceanie Teennoregy.

Talley, L. D., 2013: Closure of the Global Overturning Circulation Through the Indian, Pacific, and

Southern Oceans: Schematics and Transports. *Oceanography*, **26** (1), 80–97, https://doi.org/10.

5670/oceanog.2013.07, URL http://apps.webofknowledge.com/full_record.do?product=UA&

search_mode=GeneralSearch&qid=14&SID=W1jPgx8kkS6brME6NvD&page=1&doc=1,

arXiv: 1011.1669v3 ISBN: 1042-8275.

Taylor, G. I., 1922: Diffusion by Continuous Movements. *Proceedings of the London Mathe- matical Society*, s2-20 (1), 196–212, https://doi.org/https://doi.org/10.1112/plms/s2-20.1.196,
 URL https://londmathsoc.onlinelibrary.wiley.com/doi/abs/10.1112/plms/s2-20.1.196, _eprint:

https://londmathsoc.onlinelibrary.wiley.com/doi/pdf/10.1112/plms/s2-20.1.196.

⁸⁹² Thorpe, S. A., and G. E. R. Deacon, 1977: Turbulence and mixing in a Scottish Loch.

Philosophical Transactions of the Royal Society of London. Series A, Mathematical and

Physical Sciences, 286 (1334), 125–181, https://doi.org/10.1098/rsta.1977.0112, URL https:

//royalsocietypublishing.org/doi/10.1098/rsta.1977.0112, publisher: Royal Society.

Thurnherr, A. M., L. Clément, L. S. Laurent, R. Ferrari, and T. Ijichi, 2020: Transformation
and Upwelling of Bottom Water in Fracture Zone Valleys. *Journal of Physical Oceanogra- phy*, **50** (3), 715–726, https://doi.org/10.1175/JPO-D-19-0021.1, URL https://journals.ametsoc.
org/view/journals/phoc/50/3/jpo-d-19-0021.1.xml, publisher: American Meteorological Soci-

ety Section: Journal of Physical Oceanography.

⁹⁰¹ Thurnherr, A. M., and Coauthors, 2005: Mixing Associated with Sills in a Canyon on the Midocean

Ridge Flank*. Journal of Physical Oceanography, **35** (8), 1370–1381, https://doi.org/10.1175/

JPO2773.1, URL http://journals.ametsoc.org/doi/abs/10.1175/JPO2773.1.

Tozer, B., D. T. Sandwell, W. H. F. Smith, C. Olson, J. R. Beale, and P. Wes-904 2019: Global Bathymetry and Topography at 15 Arc Sec: SRTM15+. Earth sel. 905 1847-1864, Space Science, 6 (10),https://doi.org/10.1029/2019EA000658, and 906 URL https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2019EA000658, _eprint: 907 https://agupubs.onlinelibrary.wiley.com/doi/pdf/10.1029/2019EA000658. 908

Trossman, D., and Coauthors, 2020: Tracer and observationally-derived constraints on horizontal
 and diapycnal diffusivities in ocean models. URL http://www.essoar.org/doi/10.1002/essoar.
 10502123.4, archive Location: world Publisher: Earth and Space Science Open Archive Section:
 Oceanography, https://doi.org/10.1002/essoar.10502123.4.

Tulloch, R., and Coauthors, 2014: Direct Estimate of Lateral Eddy Diffusivity Upstream of
 Drake Passage. *Journal of Physical Oceanography*, 44 (10), 2593–2616, https://doi.org/10.1175/
 JPO-D-13-0120.1, URL https://journals.ametsoc.org/view/journals/phoc/44/10/jpo-d-13-0120.
 1.xml, publisher: American Meteorological Society Section: Journal of Physical Oceanography.

⁹¹⁷ Visbeck, M., M. Dengler, T. S. Tanhua, and M. Freund, 2020: Mixing and Upwelling Dy ⁹¹⁸ namics along the Continental Slope off Peru inferred from Tracer Release, Hydrographic and
 ⁹¹⁹ Microstructure Measurements. AGU, URL https://agu.confex.com/agu/osm20/meetingapp.cgi/
 ⁹²⁰ Paper/651229.

Walin, G., 1982: On the relation between sea-surface heat flow and thermal circulation in the
 ocean. *Tellus*, **34** (2), 187–195, https://doi.org/10.3402/tellusa.v34i2.10801, URL https://doi.
 org/10.3402/tellusa.v34i2.10801.

Waterhouse, A. F., and Coauthors, 2014: Global Patterns of Diapycnal Mixing from Measure ments of the Turbulent Dissipation Rate. *Journal of Physical Oceanography*, 44 (7), 1854–
 1872, https://doi.org/10.1175/JPO-D-13-0104.1, URL http://journals.ametsoc.org/doi/abs/10.
 1175/JPO-D-13-0104.1, iSBN: 0022-3670.

Waterman, S., A. C. N. Garabato, and K. L. Polzin, 2013: Internal Waves and Turbulence in the Antarctic Circumpolar Current. *Journal of Physical Oceanography*, 43 (2), 259–282, https://doi.org/10.1175/JPO-D-11-0194.1, URL https://journals.ametsoc.org/view/journals/phoc/43/2/jpo-d-11-0194.1.xml, publisher: American Meteorological Society Section: Journal of Physical Oceanography.

Watson, A. J., J. R. Ledwell, M.-J. Messias, B. A. King, N. Mackay, M. P. Meredith, B. Mills,
 and A. C. Naveira Garabato, 2013: Rapid cross-density ocean mixing at mid-depths in the
 Drake Passage measured by tracer release. *Nature*, **501** (**7467**), 408–411, https://doi.org/10.1038/
 nature12432, URL http://www.nature.com/articles/nature12432, publisher: Nature Publishing
 Group.

Watson, A. J., J. R. Ledwell, D. J. Webb, and C. Wunsch, 1988: Purposefully Released Tracers
 [and Discussion]. *Philosophical Transactions of the Royal Society of London. Series A, Mathe- matical and Physical Sciences*, **325** (1583), 189–200, URL https://www.jstor.org/stable/38109,
 publisher: The Royal Society.

Wenegrat, J. O., J. Callies, and L. N. Thomas, 2018: Submesoscale Baroclinic Instability in the
 Bottom Boundary Layer. *Journal of Physical Oceanography*, JPO–D–17–0264.1, https://doi.org/
 10.1175/JPO-D-17-0264.1, URL http://journals.ametsoc.org/doi/10.1175/JPO-D-17-0264.1.

Whalen, C. B., 2021: Best Practices for Comparing Ocean Turbulence Measurements across
Spatiotemporal Scales. *Journal of Atmospheric and Oceanic Technology*, 38 (4), 837–841,
https://doi.org/10.1175/JTECH-D-20-0175.1, URL https://journals.ametsoc.org/view/journals/
atot/38/4/JTECH-D-20-0175.1.xml, publisher: American Meteorological Society Section:
Journal of Atmospheric and Oceanic Technology.

⁹⁵⁰ Whalen, C. B., C. de Lavergne, A. C. Naveira Garabato, J. M. Klymak, J. A. MacKinnon, ⁹⁵¹ and K. L. Sheen, 2020: Internal wave-driven mixing: governing processes and consequences

- for climate. Nature Reviews Earth & Environment, 1 (11), 606–621, https://doi.org/10.1038/
- s43017-020-0097-z, URL https://www.nature.com/articles/s43017-020-0097-z, number: 11
- ⁹⁵⁴ Publisher: Nature Publishing Group.