

# 1 **Progressive weakening within the overriding plate during dual inward dipping subduction**

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## 6 Highlights:

- 7 1. Investigate dynamic internally driven dual inward dipping subduction models
- 8 2. Viscosity evolves as a function of multiple physical parameters
- 9 3. Self-consistently forms a fixed boundary condition and strong convective mantle flow
- 10 4. Strain rate weakening plays a dominant role in initiating viscosity reduction

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## 12 **Abstract**

13 Dual inward dipping subduction often produces complex deformation patterns in the overriding  
14 plate. However, the geodynamic process of how dual inward dipping subduction relates to this  
15 deformation is still poorly understood. Here we apply a composite viscosity, dependent on multiple  
16 parameters, e.g., temperature, pressure, strain rate etc., in 2-D thermo-mechanical numerical  
17 modelling to investigate how dual inward dipping subduction modifies the rheological structure of  
18 the overriding plate. Three variables are investigated to understand what controls the maximum  
19 degree of weakening. We find that the initial length and thickness of the overriding plate are  
20 negatively correlated with the magnitude of viscosity reduction. While the initial thickness of the  
21 subducting plate positively relates to the magnitude of viscosity reduction. The progressive  
22 weakening can result in a variety of stretching states ranging from 1) little or no lithosphere thinning  
23 and extension, to 2) limited thermal lithosphere thinning, and 3) localised rifting followed by  
24 spreading extension. Compared with single sided subduction, dual inward dipping subduction  
25 further reduces the magnitude of viscosity of the overriding plate. It does this by creating a dynamic  
26 fixed boundary condition for the overriding plate and forming a stronger upwelling mantle flow  
27 underlying the overriding plate. Three types of feedback weakening cycles are recognised, among  
28 which the strain rate weakening mechanism plays the dominant role in lowering the viscosity of the  
29 overriding plate throughout the simulation. Strain rate weakening is also a precondition for initiating  
30 thermal weakening, strain localisation and lithosphere thinning.

31 **Keywords:** dual inward dipping subduction; composite viscosity; feedback weakening; numerical  
32 modelling.

## 33 **1. Introduction**

34 Subduction can pose a fundamental tectonic overprint on the overriding plate by generating a  
35 volcanic arc (Perfit et al., 1980; Straub et al., 2020), back-arc basin (Uyeda, 1981), orogeny  
36 (Faccenna et al., 2021), or even continental breakup (Dal Zilio et al., 2018). Most subduction zones  
37 involve only one subducting slab. Here we consider multiple subducting slabs, in particular dual  
38 inward dipping subduction. Dual inward dipping subduction, or bi-vergent subduction occurs when  
39 the overriding plate is decoupled with two subducting slabs dipping towards each other. It is one of  
40 the four most commonly described subduction zones with multiple slabs, i.e., inward-dipping, same-  
41 dip, outward-dipping and oppositely dipping adjacent subduction zones (Holt et al., 2017; Király et  
42 al., 2021).

43 Dual inward dipping subduction zones are often found in areas which exhibit complex geodynamic  
44 processes in their geological history. Seismic tomography shows that dual inward dipping  
45 subduction exists at the Caribbean plate between the Cocos slab and Lesser-Antilles subduction  
46 zone (Van Benthem et al., 2013), the Philippine islands between the Philippine trench and Manila  
47 trench (Wang and He, 2020), and South-East Asia between the Philippine and the Sumatra  
48 subduction (Hall and Spakman, 2015; Huang et al., 2015; Maruyama et al., 2007). In combination  
49 with seismic tomography, plate reconstructions have made it more evident that dual inward dipping  
50 subduction could have existed in some regions in the past (Faccenna et al., 2010; Hall and  
51 Spakman, 2015) constrained by suture zone petrology demonstrating oceanic floor closure. A good  
52 example is the North China Craton. Suture zone studies reveal that multiple inward dipping  
53 subduction may have surrounded the North China Craton from Early Paleozoic to Tertiary (Santosh,

54 2010; Windley et al., 2010). Despite these improved observations and evidence, dual inward  
55 dipping subduction is still poorly understood in terms of how it differs from single sided subduction  
56 in deforming or weakening the overriding plate.

57 Numerical investigations have been conducted to understand the dynamics of dual inward dipping  
58 subduction. Research shows that the initial slab dip of the subducting plate affects the upper mantle  
59 dynamic pressure between the convergent slabs and stress state within the overriding plate (Holt  
60 et al., 2017). Varying the distance between the trenches, convergence rate, and asymmetry of  
61 subducting plates can alter the topography of the overriding plate (Dasgupta and Mandal, 2018).  
62 The thickness of the plates and the lithosphere to asthenosphere viscosity ratio are all tested to  
63 investigate their effect on the slab geometry and the magnitude of mantle upwelling flow underlying  
64 the overriding plate (Lyu et al., 2019). These pioneering investigations show that dual inward  
65 dipping subduction can generate a variety of upper mantle flow patterns which regulate the stress  
66 state and topography of the overriding plate. However, these models all applied a simplified  
67 constant rheology for both plates and convective mantle flow, i.e., the viscosity is neither  
68 temperature, pressure nor stress-dependent. Mineral rheology experiments indicate that viscosity  
69 varies as a function of multiple parameters, e.g., temperature, pressure, stress, strain rate etc.  
70 (Bürgmann and Dresen, 2008; Burov, 2011; Hirth and Kohlstedt, 2003; Karato, 2010; Lynch and  
71 Morgan, 1987). Previous models with simplified rheology were unable to quantitatively calculate  
72 the softening effect due to slab rollback and/or induced mantle wedge flow. Also, the simplified  
73 rheology does not allow the lithosphere to weaken and produce new plate boundaries.

74 In this research, a series of 2-D thermo-mechanical and self-consistently driven models are run to

75 investigate what role dual inward dipping subduction plays in altering the rheology within the  
 76 overriding plate and identifying the underlying driving mechanism. The composite rheology law  
 77 enables the viscosity to self-consistently evolve as a function of multiple varying variables including  
 78 temperature, strain rate, stress and pressure.

## 79 **2. Methods**

80 We ran the thermally-driven dual inward dipping subduction models using the code Fluidity (Davies  
 81 et al., 2011; Kramer et al., 2012), a finite-element control-volume computational modelling  
 82 framework, with an adaptive mesh that is set up to capture evolving changes with a maximum  
 83 resolution of 0.4 km in this research.

### 84 **2.1 Governing equations and rheology setup**

85 Under the Boussinesq approximation (McKenzie et al., 1974), the equations governing thermally  
 86 driven subduction process are derived from conservation of mass, momentum, and energy, for an  
 87 incompressible Stokes flow

$$\partial_i u_i = 0, \quad (1)$$

$$\partial_i \sigma_{ij} = -\Delta \rho g_j, \quad (2)$$

$$\frac{\partial T}{\partial t} + u_i \partial_i T = \kappa \partial_i^2 T, \quad (3)$$

88 in which  $u$ ,  $g$ ,  $\sigma$ ,  $T$ ,  $\kappa$  are the velocity, gravity, stress, temperature, and thermal diffusivity,

89 respectively (Table 1). In particular, the full stress tensor  $\sigma_{ij}$  consists of deviatoric and lithostatic  
 90 components via

$$\sigma_{ij} = \tau_{ij} - p\delta_{ij}, \quad (4)$$

91 where  $\tau_{ij}$  represents the deviatoric stress tensor,  $p$  the dynamic pressure, and  $\delta_{ij}$  the Kronecker  
 92 delta function.

93 Table 1. Key parameters used in this research.

| Quantity                        | Symbol      | Units               | Value  |
|---------------------------------|-------------|---------------------|--|
| Gravity                         | $g$         | $m s^{-2}$          | 9.8  |
| Gas constant                    | $R$         | $J K^{-1} mol^{-1}$ | 8.3145   |
| Mantle geothermal gradient      | $G$         | $K km^{-1}$         | 0.5 (UM)<br>0.3 (LM)                                     |
| Thermal expansivity coefficient | $\alpha$    | $K^{-1}$            | $3 \times 10^{-5}$                                       |
| Thermal diffusivity             | $\kappa$    | $m^2 s^{-1}$        | $10^{-6}$  |
| Reference density               | $\rho_s$    | $kg m^{-3}$         | 3300   |
| Cold, surface temperature       | $T_s$       | $K$                 | 273  |
| Hot, mantle temperature         | $T_m$       | $K$                 | 1573   |
| Maximum viscosity               | $\mu_{max}$ | $Pa \cdot s$        | $10^{25}$  |
| Minimum viscosity               | $\mu_{min}$ | $Pa \cdot s$        | $10^{18}$  |
| <b>Diffusion Creep</b>          |             |                     |  |
| Activation energy               | $E$         | $kJ mol^{-1}$       | 300 (UM)<br>200 (LM)                                     |
| Activation volume               | $V$         | $cm^3 mol^{-1}$     | 4 (UM)<br>1.5 (LM)                                       |
| Prefactor                       | $A$         | $Pa^{-n} s^{-1}$    | $3.0 \times 10^{-11}$ (UM)<br>$6.0 \times 10^{-17}$ (LM) |
|                                 | $n$         |                     | 1  |
| <b>Dislocation Creep (UM)</b>   |             |                     |  |
| Activation energy               | $E$         | $kJ mol^{-1}$       | 540  |
| Activation volume               | $V$         | $cm^3 mol^{-1}$     | 12   |
| Prefactor                       | $A$         | $Pa^{-n} s^{-1}$    | $5.0 \times 10^{-16}$                                    |
|                                 | $n$         |                     | 3.5  |
| <b>Peierls Creep (UM)</b>       |             |                     |  |
| Activation energy               | $E$         | $kJ mol^{-1}$       | 540  |
| Activation volume               | $V$         | $cm^3 mol^{-1}$     | 10   |
| Prefactor                       | $A$         | $Pa^{-n} s^{-1}$    | $10^{-150}$  |
|                                 | $n$         |                     | 20   |

**Yield Strength Law**

|                        |                |            |                   |
|------------------------|----------------|------------|-------------------|
| Surface yield strength | $\tau_0$       | <i>MPa</i> | 2                 |
| Friction coefficient   | $f_c$          |            | 0.2               |
|                        | $f_{c,weak}$   |            | 0.02 (weak layer) |
| Maximum yield strength | $\tau_{y,max}$ | <i>MPa</i> | 10,000            |

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94 The deviatoric stress tensor and strain rate tensor  $\dot{\epsilon}_{ij}$  are related according to

$$\tau_{ij} = 2\mu\dot{\epsilon}_{ij} = \mu(\partial_j u_i + \partial_i u_j), \quad (5)$$

95 with  $\mu$  the viscosity. The density difference due to temperature is defined as

$$\Delta\rho = -\alpha\rho_s(T - T_s), \quad (6)$$

96 where  $\alpha$  is the coefficient of thermal expansion,  $\rho_s$  is the reference density at the surface  
 97 temperature  $T_s$  (Table 1).

98 The key rheology difference of the model setup with previous dual inward dipping subduction  
 99 models (Dasgupta and Mandal, 2018; Holt et al., 2017; Lyu et al., 2019) is that the magnitude of  
 100 viscosity throughout the model can self-consistently vary with time as the model evolves. The  
 101 governing rheological laws are identical throughout the model domain, though the rheology  
 102 parameters we use differ to match different deformation mechanisms observed at different depths  
 103 in the Earth. In detail, a uniform composite viscosity is used to take account of four deformation  
 104 mechanisms under different temperature-pressure conditions: diffusion creep, dislocation creep,  
 105 Peierls mechanism, and yielding (Garel et al., 2014). The effective composite viscosity in the  
 106 computational domain is given by

$$\mu = \left( \frac{1}{\mu_{diff}} + \frac{1}{\mu_{disl}} + \frac{1}{\mu_P} + \frac{1}{\mu_y} \right)^{-1}, \quad (7)$$

107 where  $\mu_{diff}$ ,  $\mu_{disl}$ ,  $\mu_y$  define the creep viscosity following

$$\mu_{diff/disl/P} = A^{-\frac{1}{n}} \exp\left(\frac{E + PV}{nRT_r}\right) \dot{\epsilon}_{II}^{\frac{1-n}{n}}, \quad (8)$$

108 in which  $A$  is a prefactor,  $n$  the stress component,  $E$  the activation energy,  $P$  the lithostatic  
 109 pressure,  $V$  the activation volume,  $R$  the gas constant,  $T_r$  the temperature obtained by adding  
 110 an adiabatic gradient of 0.5 K/km in the upper mantle and 0.3 K/km in the lower mantle to the  
 111 Boussinesq solution (Fowler, 2005),  $\dot{\epsilon}_{II}$  the second invariant of the strain rate tensor. Note that in  
 112 the lower mantle only diffusion creep applies and the lower mantle is 30 times more viscous than  
 113 the upper mantle. While the fourth deformation mechanism, yielding, is defined by a brittle-failure  
 114 type yield-stress law as

$$\mu_y = \frac{\tau_y}{2\dot{\epsilon}_{II}}, \quad (9)$$

115 with  $\mu_y$  the yielding viscosity and  $\tau_y$  the yield strength.  $\tau_y$  is determined by

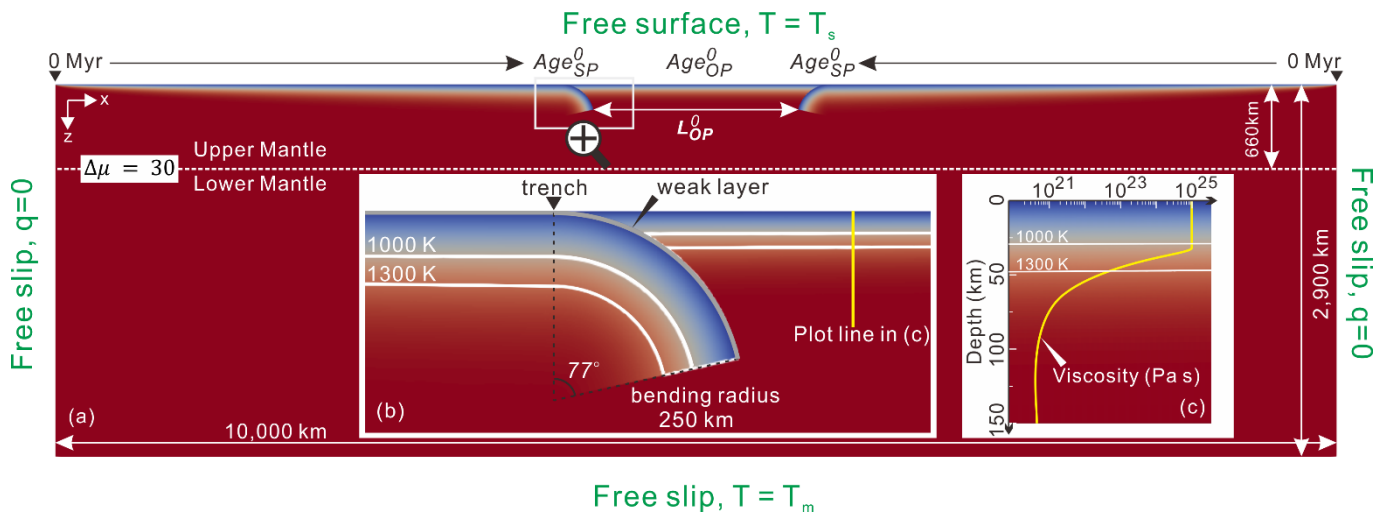
$$\tau_y = \min(\tau_0 + f_c P, \tau_{y,max}), \quad (10)$$

116 with  $\tau_0$  the surface yield strength,  $f_c$  the friction coefficient,  $P$  the lithostatic pressure, and  $\tau_{y,max}$   
 117 the maximum yield strength (Table 1).

## 118 **2.2 Model setup**



119 The computational domain is 10,000 km by 2,900 km, with x (width) coordinates and z (depth)  
 120 coordinates extending from the surface to the bottom of the lower mantle (Figure 1). Such a wide  
 121 domain reduces the influence of side and bottom boundary conditions (Chertova et al., 2012). The  
 122 thermal boundary conditions at the surface and bottom are defined by two isothermal values:  $T =$   
 123  $T_s$  and  $T = T_m$  for surface and base of lower mantle respectively, while the sidewalls are insulating.  
 124 As for velocity boundary conditions, a free-surface is applied at the top boundary to enable trench  
 125 mobility, while the other boundaries are free-slip.



126  
 127 Figure 1. Dual inward dipping model geometry and initial setup illustrated with the initial temperature field as the background. (a)  
 128 The whole computational domain.  $Age_{SP}^0$  and  $Age_{OP}^0$  represent the initial ages of subducting plate and overriding plate at trench.  
 129 The viscosity jump ( $\Delta\mu$ ) between upper and lower mantle at 660 km transition zone is set up with a fixed value of 30. To be noted,  
 130  $L_{OP}^0$  represents the distance between the leading tip edges of the slabs initially penetrating into the upper mantle.  $L_{OP}^0$  roughly  
 131 equals the length of the overriding plate with constant thickness, excluding the overriding plate above the interface with the bending  
 132 slab. (b) Enlarged area of the trench zone where the bending slab meets the flat overriding plate. The 1100 K and 1300 K isotherms  
 133 are marked in white contours. (c) Vertical profile of viscosity against depth within the overriding plate. The plot line is 400 km away  
 134 from the initial trench.

135 To simplify the complexity of the model, a laterally symmetric dual inward dipping subduction is  
 136 applied, i.e., the model is strictly symmetric along the vertical middle line of the domain (5000 km  
 137 away from the side boundaries) in all aspects, e.g., the geometry and rheology properties.  $Age_{SP}^0$   
 138 and  $Age_{OP}^0$  represent the initial ages of subducting plate and overriding plate at the trench, where

139 the two plates meet at the surface. Laterally on the surface, the age of the subducting plates  
 140 increases linearly with their distance away from the mid-ocean ridge on either side. While vertically,  
 141 the age of the plate at surface defines the initial thermal structure through a half-space cooling  
 142 model (Turcotte and Schubert, 2014),

$$T(x, z) = T_s + (T_m - T_s) \operatorname{erf} \left( \frac{z}{2\sqrt{\kappa A \operatorname{age}^0(x)}} \right), \quad (11)$$

143 with  $x$  the distance away from the mid-ocean ridge,  $\operatorname{erf}$  the error function,  $z$  the depth,  $\kappa$  the  
 144 thermal diffusivity. All parameters are listed in Table 1. The whole overriding plate is set up with a  
 145 constant age. Thus, the thermal structure within the overriding plate is laterally homogeneous. The  
 146 bottom of thermal lithosphere is defined as the isotherm of 1300 K, where the temperature gradient  
 147 starts to drop quickly (Garel and Thoraval, 2021). The initial thickness of the subducting plate ( $H_{SP}^0$ )  
 148 and overriding plate ( $H_{OP}^0$ ) can be calculated using

$$H_{Plate}^0 = \operatorname{erfinv}((T_{1300K} - T_s)/(T_m - T_s)) * 2 * \sqrt{\kappa * \operatorname{Age}_{Plate}^0(x)}, \quad (12)$$

149 where  $H_{Plate}^0$  is the initial thickness of the plate thermal lithosphere and  $\operatorname{erfinv}$  is the inverse error  
 150 function.

151 The free surface boundary condition together with the mid-ocean ridge setup allows the subducting  
 152 slabs, and overriding plate and therefore the trench to move freely as subduction evolves. To initiate  
 153 self-driven subduction without implementing external forces, the subducting plate is set up with a  
 154 bend into the mantle and an 8 km thick low-viscosity decoupling layer on the top. This weak layer  
 155 has the same rheology as the rest of the domain, other than its maximum viscosity is  $10^{20}$  Pa s,

and its friction coefficient is 0.02 (i.e. an order of magnitude lower). The initial bending radius is 250 km and the slab bends over 77 degrees from the trench (Figure 1).

### 2.3 Model variables

Three variables are investigated here: the initial length of the overriding plate ( $L_{OP}^0$ ), the initial thickness of the subducting plate ( $H_{SP}^0$ ) and overriding plate ( $H_{OP}^0$ ) (Table 2). These are parameters also varied in previous research and therefore will allow easier comparison.  $H_{SP}^0$  and  $H_{OP}^0$  are dependent on plate age and calculated using Equation (12). The magnitude of  $L_{OP}^0$  that has been tested in previous models ranging from 500 km to 4000 km (Dasgupta and Mandal, 2018; Holt et al., 2017; Lyu et al., 2019), and the result shows that  $L_{OP}^0$  greater than 2500 km has little impact on the result (Lyu et al., 2019). Here  $L_{OP}^0$  is tested in the range from 500 km to 1600 km. The values of  $H_{SP}^0$  and  $H_{OP}^0$  that has been tested before ranges from 75-125 km and 75-150 km separately and those models suggest that  $H_{SP}^0$  is more important in deciding the magnitude of upwelling mantle flow than  $H_{OP}^0$  (Lyu et al., 2019). So the range of  $H_{SP}^0$  is extended to 94-141 km while the range of  $H_{OP}^0$  is narrowed down to 67-100 km.

Table 2. List of model setup.

| Model name                  | $L_{OP}^0$ (km) | $H_{SP}^0$ (km) | $H_{OP}^0$ (km) | $Age_{SP}^0$ (Ma) | $Age_{OP}^0$ (Ma) |
|-----------------------------|-----------------|-----------------|-----------------|-------------------|-------------------|
| $H_{SP}^0 = 94 \text{ km}$  | 500             | 94              | 67              | 90                | 45                |
| $H_{SP}^0 = 100 \text{ km}$ | 500             | 100             | 67              | 100               | 45                |
| $H_{SP}^0 = 111 \text{ km}$ | 500             | 111             | 67              | 125               | 45                |
| $H_{SP}^0 = 122 \text{ km}$ | 500             | 122             | 67              | 150               | 45                |
| $H_{SP}^0 = 141 \text{ km}$ | 500             | 141             | 67              | 200               | 45                |
| $H_{OP}^0 = 67 \text{ km}$  | 500             | 141             | 67              | 200               | 45                |
| $H_{OP}^0 = 70 \text{ km}$  | 500             | 141             | 70              | 200               | 50                |
| $H_{OP}^0 = 74 \text{ km}$  | 500             | 141             | 74              | 200               | 55                |
| $H_{OP}^0 = 77 \text{ km}$  | 500             | 141             | 77              | 200               | 60                |
| $H_{OP}^0 = 100 \text{ km}$ | 500             | 141             | 100             | 200               | 100               |
| $L_{OP}^0 = 500 \text{ km}$ | 500             | 141             | 67              | 200               | 45                |

|                              |      |     |    |     |    |
|------------------------------|------|-----|----|-----|----|
| $L_{OP}^0 = 600 \text{ km}$  | 600  | 141 | 67 | 200 | 45 |
| $L_{OP}^0 = 700 \text{ km}$  | 700  | 141 | 67 | 200 | 45 |
| $L_{OP}^0 = 800 \text{ km}$  | 800  | 141 | 67 | 200 | 45 |
| $L_{OP}^0 = 1000 \text{ km}$ | 1000 | 141 | 67 | 200 | 45 |
| $L_{OP}^0 = 1200 \text{ km}$ | 1200 | 141 | 67 | 200 | 45 |
| $L_{OP}^0 = 1600 \text{ km}$ | 1600 | 141 | 67 | 200 | 45 |

Models are named with the variable tested, e.g.,  $H_{SP}^0 = 94 \text{ km}$  and  $H_{SP}^0 = 122 \text{ km}$  corresponds to the initial subducting plate thickness of 94 km and 122 km separately, while the initial overriding plate length and thickness in both models remain the same as 500 km and 67 km.

## 3. Results

### 3.1 Varying viscosity in an evolving model: an example

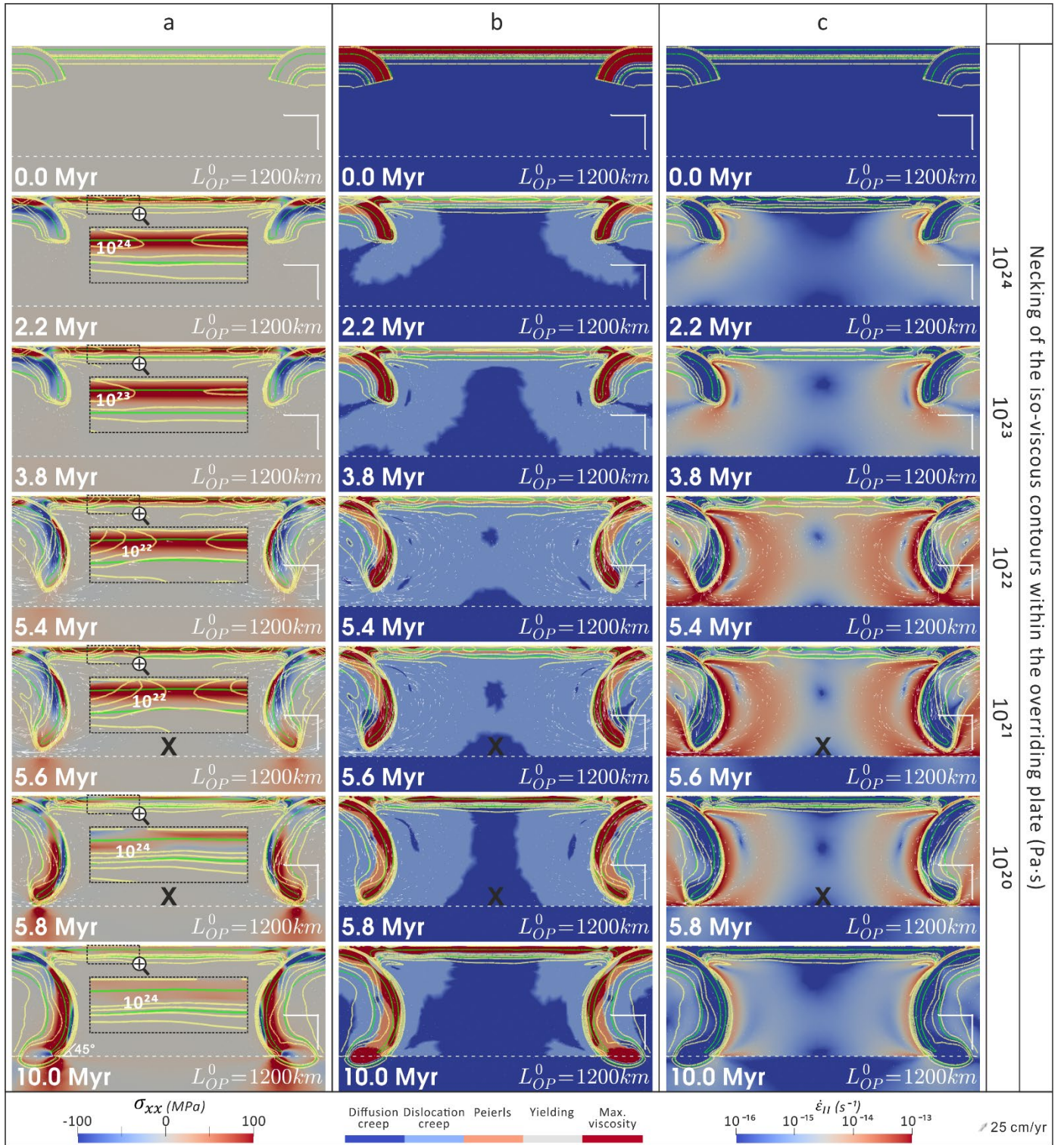
The thermal-mechanical model setup of this research enables self-consistent subduction. Similar to the self-consistent single subduction numerical and analogue models, subduction starts with a non-steady state phase where negative buoyancy pulls the slab to sink into the deeper mantle (e.g., Capitanio et al., 2010; Gerya et al., 2008; Schellart and Moresi, 2013). Following this short period of adjustment, the slab interacts with the lower mantle and steady state subduction ensues. We next describe in detail the dynamic evolution of dual inward dipping subduction for the model ' $L_{OP}^0 = 1200 \text{ km}$ '.

#### 3.1.1 Non-steady state subduction

During the non-steady state subduction, symmetric subduction develops about the midline of the overriding plate (~5000km away from the side boundaries). As more slab is pulled into the mantle, the negative buoyancy grows gradually. It takes ~5.8 Myr before the slab starts to interact with the lower mantle (Figure 2).

188 Convective mantle wedge flow is generated as the subducting slab bends and sinks in the upper  
189 mantle. The size of the convective cell grows with time and forms a crescent shape as wide as  
190 ~500 km before the slab reaches the depth of lower mantle. The convective cell is composed of a  
191 narrow downwelling flow coupling close to the sinking slab and a wide upwelling flow further away.  
192 The upwelling flow fades gradually as its distance away from the subducting slab increases. In the  
193 model ' $L_{OP}^0 = 1200 \text{ km}$ ', the two sets of wedge flow have little interaction and can be considered as  
194 two separate units. This is because the length of the overriding plate is 1200 km, which is greater  
195 than two times the width (~500 km) of a convection cell.

196 The overriding plate exhibits a widespread extensional stress field as a result of continuous  
197 subduction and the induced convective mantle wedge flows. Only a limited area close to the  
198 interface with the bending slabs develops compression (Figure 2, a). The widespread extensional  
199 stress field implies that the overriding plate has an overall stretching tendency. Within the overriding  
200 plate, the governing deformation mechanism is spatially layered (Figure 2, b). At depths shallower  
201 than 30 km within the overriding plate, yielding (brittle or plastic) deformation dominates. Underlying  
202 the yielding layer lies ~10 km thick Peierls creep layer. While for depths from ~40 km to the bottom  
203 of the thermal lithosphere deformation is dominated by dislocation creep. High strain rate areas are  
204 observed within and underneath the overriding plate (Figure 2, c). The thermal thickness of the  
205 overriding plate, defined by the 1300 K isotherm contour, does not change much throughout the  
206 simulation.



207  
 208 Figure 2. The Simulation screenshots of model ' $L_{OP}^0 = 1200 \text{ km}$ '. (a) Horizontal stress component where positive value represents  
 209 stretching and negative value denotes compression. (b) The dominant deformation mechanism. (c) Magnitude of second invariant  
 210 of strain rate. The progressive weakening process within the overriding plate is demonstrated by the necking of the iso-viscous  
 211 contours. The 5 groups of yellow contours encompassing the plates in each screenshot are iso-viscous contours of  
 212  $10^{24}, 10^{23}, 10^{22}, 10^{21}, 10^{20} \text{ Pa}\cdot\text{s}$  from outward to inward. Screenshot with a bold 'X' underlying the overriding plate means there is  
 213 no necking developing in that timestep for the iso-viscous contour whose value is noted on the right-hand side, e.g.,  $10^{21} \text{ Pa}\cdot\text{s}$ .  
 214 The two sets of green solid lines are 700 K and 1300 K isotherm contours to image the geometry of the plate. The transition zone  
 215 at the depth of 660 km is marked by the horizontal white dashed line. The white right-angle scale bar lying above the right end of  
 216 the transition zone represents 200 km in both directions. The bottom left corner caption shows the elapsed simulation time and  
 217 bottom right corner is the name of the model.

218 The non-Newtonian rheology laws applied define viscosity as a function of multiple variables, e.g.,  
219 temperature, pressure, stress, strain rate etc. As subduction initiates, it creates rheology  
220 heterogeneities within what initially was a laterally homogeneous overriding plate, allowing part of  
221 it to become weaker than other parts. To visualize the variation in lithosphere viscosity, several  
222 levels of iso-viscous contours are plotted, e.g.,  $10^{24}, 10^{23}, 10^{22}, 10^{21} Pa \cdot s$  (Figure 2). Here, the  
223 overriding plate weakening level is defined as the maximum order of viscosity magnitude drop. That  
224 is, weakening level 'I', 'II', 'III', 'IV' represents that the iso-viscous contour  $10^{24}, 10^{23}, 10^{22}, 10^{21} Pa \cdot$   
225  $s$  is necked within the overriding plate respectively. It shows that the homogeneous overriding plate  
226 is gradually segmented into three strong cores connected with two low viscosity necking regions.  
227 Strain deformation is likely to localize upon these two necking areas and continuously lower the  
228 magnitude of viscosity therein. The minimum viscosity achieved in the overriding plate for model  
229 ' $L_{OP}^0 = 1200 km$ ' is  $10^{21} \sim 10^{22} Pa \cdot s$  (weakening level 'III'). The distance between these two  
230 necking regions is  $\sim 620 km$  (Figure 2, a, 3.8Myr). These necking regions match well with the high  
231 strain rate areas developed in the overriding plate. The initial result suggests that high strain rate  
232 may play an important role in softening the overriding plate during dual inward dipping subduction.

### 233 **3.1.2 Steady state subduction**

234 The steady state subduction process initiates after a short period of transition once slabs start to  
235 interact with the lower mantle. Due to the viscosity increase as the sinking slab enters the lower  
236 mantle at 660 km depth, it slows down, and the induced mantle wedge flow gets much weaker.  
237 After this, the model enters a steady state subduction process where mobility becomes slow and  
238 constant, and deformation reduces. Meanwhile, the necking of the iso-viscous contours is reversed

239 by a cooling and healing process within the overriding plate (Figure 2). At the end of the 10 Myr  
240 simulation, the dip between the top of bending slab and the transition zone is  $\sim 45^\circ$  and the total  
241 trench retreat is  $\sim 100$  km.

### 242 **3.2 Length of the overriding plate**

243 The first series of models investigate decreasing the initial length of the overriding plate ( $L_{OP}^0$ ) from  
244 1600 km to 500 km, while keeping the initial thickness of the subducting and overriding plate as  
245 141 km and 67 km separately. As  $L_{OP}^0$  decreases, the two symmetric subducting slabs become  
246 closer. The two separate convective mantle wedge flows start to combine with each other and form  
247 a stronger joint upwelling flow underneath the overriding plate (Figure 3). Consequently, as  $L_{OP}^0$  is  
248 reduced, the two separate necking areas within the overriding plate get closer and merge into a  
249 single one in the end. Also as  $L_{OP}^0$  is reduced it takes less time to lower each level of viscosity  
250 within the overriding plate during the non-steady state subduction. Besides, the progressive  
251 weakening process can go further and neck the  $10^{21}$  Pa s iso-viscous contour (weakening level  
252 'IV') when  $L_{OP}^0$  reaches  $\leq 800$  km, initiating significant lithosphere thinning and even rifting or  
253 spreading extension within the overriding plate (Figure 3, b-c). The significant extension usually  
254 lasts less than 1 Myr before it gradually stops after the slab reaches the depth of the lower mantle,  
255 but it causes substantial changes to the dual inward dipping subduction system. For example,  
256 significant slab rollback starts to develop, creating a flattening slab geometry in the upper mantle  
257 and steepening dip angle ( $45^\circ$  to  $75^\circ$ , Figure 3) at the transition zone depth by the end of the 10  
258 Myr simulation.

259 It is noted that the continuous thinning of the thermal lithosphere only initiates when the iso-viscous



260 contour of  $10^{21} \text{ Pa} \cdot \text{s}$  starts to neck. This implies a potential coupling of the thermal lithosphere  
261 and the rheology boundary layer (usually defined as the depth of  $10^{21} \text{ Pa} \cdot \text{s}$ ) in the model. All  
262 models necking  $10^{21} \text{ Pa} \cdot \text{s}$  will continue to neck lower magnitudes of viscosity, e.g.,  
263  $10^{20}, 10^{19} \text{ Pa} \cdot \text{s}$ . Simultaneously, the upwelling hot mantle flow can then ascend to fill the thinning  
264 region and create a new plate boundary (rifting extension) or even new sea floor (spreading  
265 extension) after it ascends to the surface. Thus, the ability to neck  $10^{21} \text{ Pa} \cdot \text{s}$  (or not) can be used  
266 as a key diagnostic to predict whether a new spreading ridge (new plate boundary) develops within  
267 the overriding plate (or just limited thinning).

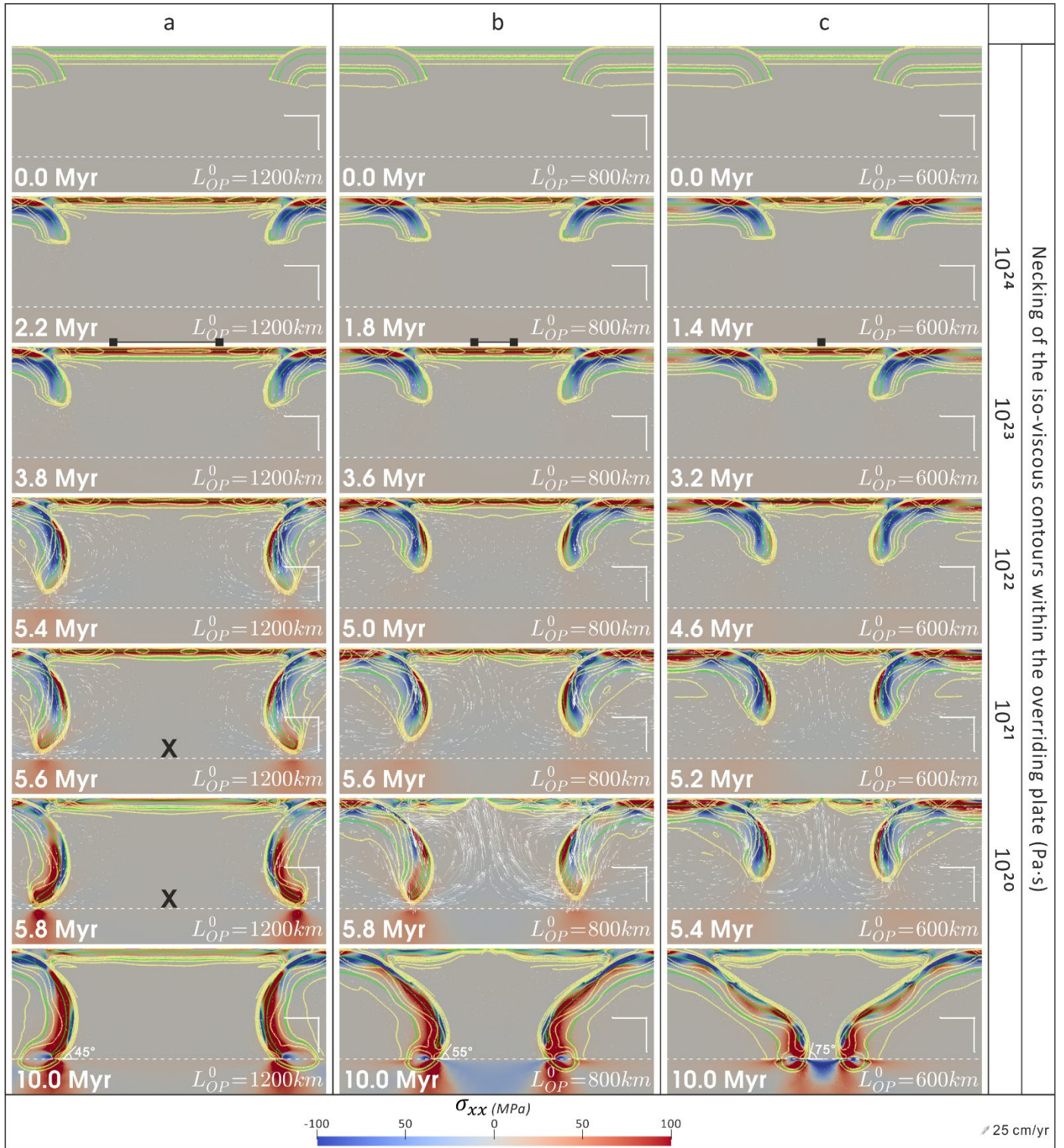
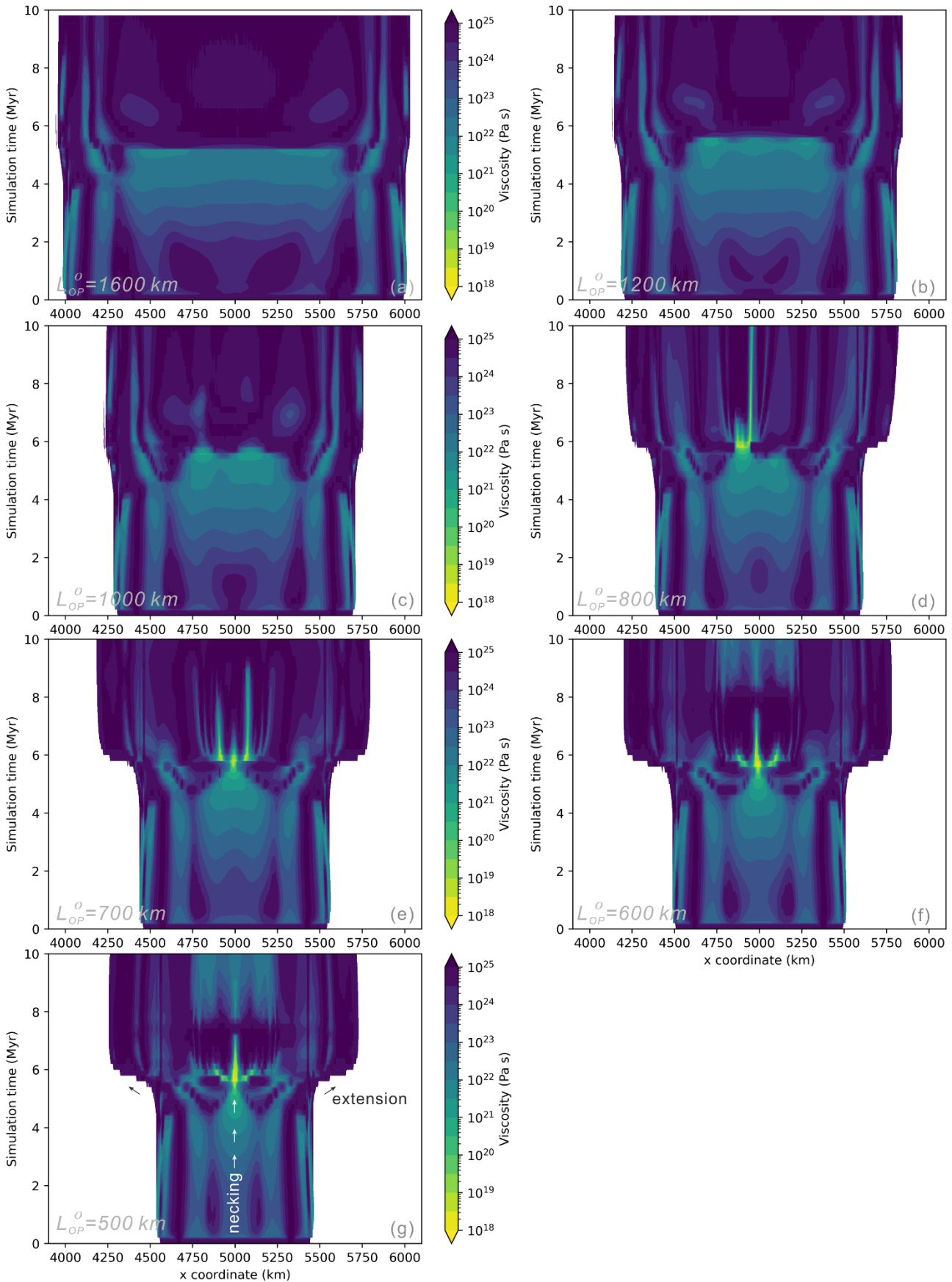


Figure 3. Progressive weakening of the overriding plate during dual inward dipping subduction with decreasing length of the overriding plate, (a) model ' $L_{OP}^0 = 1200$  km', (b) model ' $L_{OP}^0 = 800$  km', (c) model ' $L_{OP}^0 = 600$  km'. The location of necked regions in the overriding plate are marked with black squares. A detailed explanation of the contours and symbols could be found in the caption of Figure 2.

To take a closer look at the extension behaviour within the overriding plate, we plot the evolving magnitude of viscosity at 5km depth (Figure 4). The filled region in the figure represents the overriding plate, therefore its widening represents extension within the overriding plate. As the initial

276 length of the overriding plate ( $L_{OP}^0$ ) decreases from 1600 km to 500 km, the total extension in the  
277 10 Myr simulations increases from ~100 km (Figure 4, a-c) to 400~600 km (Figure 4, d-g). In detail,  
278 it is noted that extensional behaviour only become observable after the iso-viscous contour of  
279  $10^{23} Pa \cdot s$  is necked, i.e., after weakening level 'II' is achieved. Extension combining with  
280 lithospheric thinning only becomes significant when the iso-viscous contour  $10^{21} Pa \cdot s$  is necked,  
281 i.e., when weakening level 'IV' is achieved. The highest weakening level achieved within the  
282 overriding plate increases from 'II' ( $L_{OP}^0 = 1600 km$ ) to 'III' ( $L_{OP}^0 = 1000 km$ ) and on to 'IV' ( $L_{OP}^0 \leq$   
283  $800 km$ ). During the spreading extension period, a highly centralised spreading centre (Figure 4,  
284 d,f-g) is observed in the middle of the overriding plate (Figure 4, d,f-g), while multiple spreading  
285 centres are observed to accommodate the extension in model ' $L_{OP}^0 = 700 km$ ' (Figure 4, e).

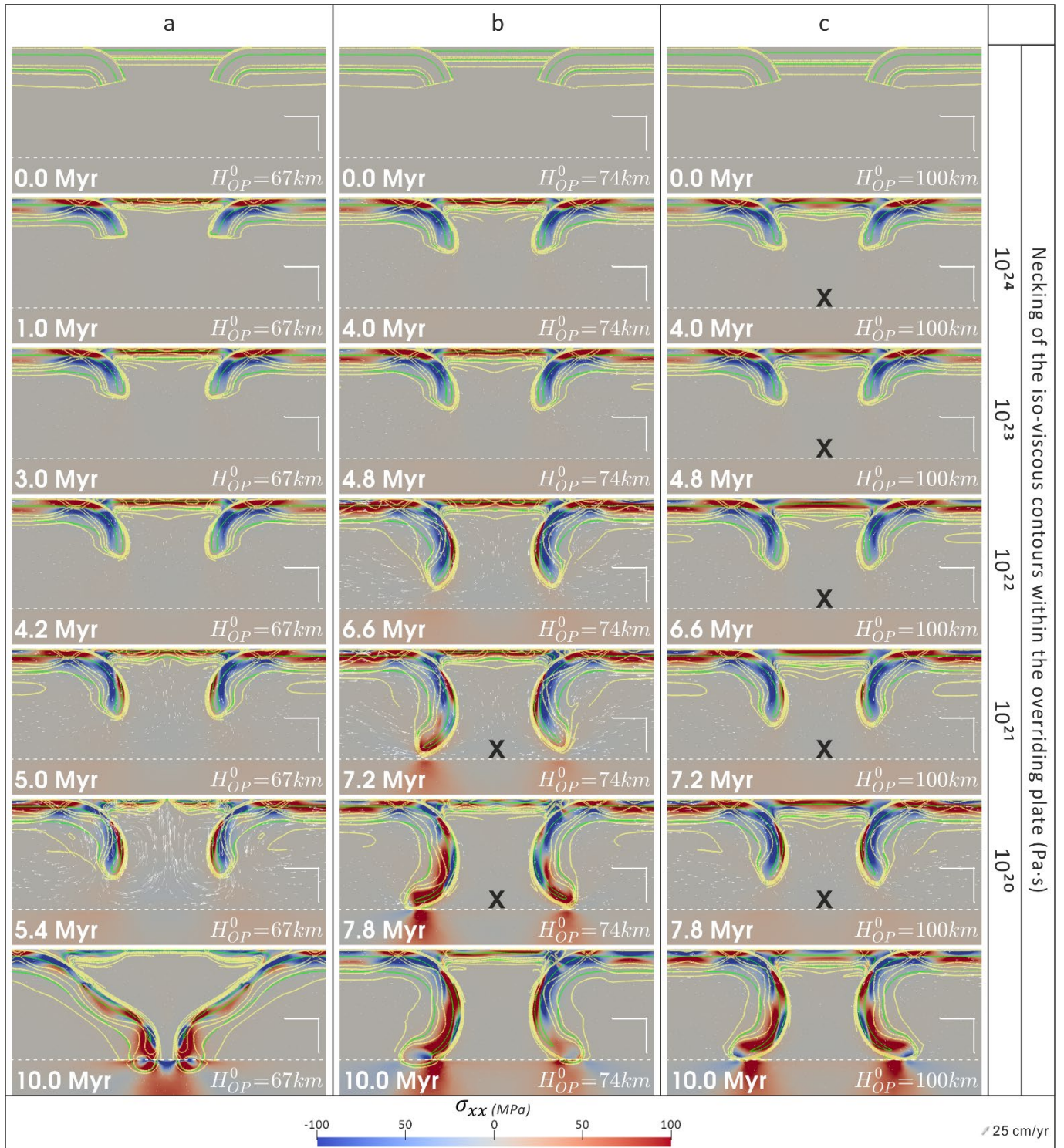


286  
 287 Figure 4. Temporal evolution of viscosity magnitude along the depth of 5 km within the overriding plate for models with different  
 288 length of the overriding plate. (a) Model ' $L_{OP}^0 = 1600 \text{ km}$ '. (b) Model ' $L_{OP}^0 = 1200 \text{ km}$ '. (c) Model ' $L_{OP}^0 = 1000 \text{ km}$ '. (d) Model ' $L_{OP}^0 =$   
 289  $800 \text{ km}$ '. (e) Model ' $L_{OP}^0 = 700 \text{ km}$ '. (f) Model ' $L_{OP}^0 = 600 \text{ km}$ '. (g) Model ' $L_{OP}^0 = 500 \text{ km}$ '. All models have the same setup of  $H_{SP}^0$   
 290 ( $141 \text{ km}$ ) and  $H_{OP}^0$  ( $67 \text{ km}$ ). The edge of the filled contour in the lateral direction represents the interface between the overriding  
 291 plate and subducting plate. The white arrows display the necking process of the overriding plate.

292 Apart from the necking regions that may develop into rifting extension within the overriding plate,  
293 there are some secondary necking regions developed close to the trench (Figure 4). The maximum  
294 weakening level is 'II' in these secondary necking regions and the viscosity reduction stops after  
295 ~4 Myr into the simulation. The lateral distance away from the nearest trench of these secondary  
296 necking regions are equal, showing little correlation with the varying  $L_{OP}^0$ .

### 297 **3.3 Thickness of the overriding plate**

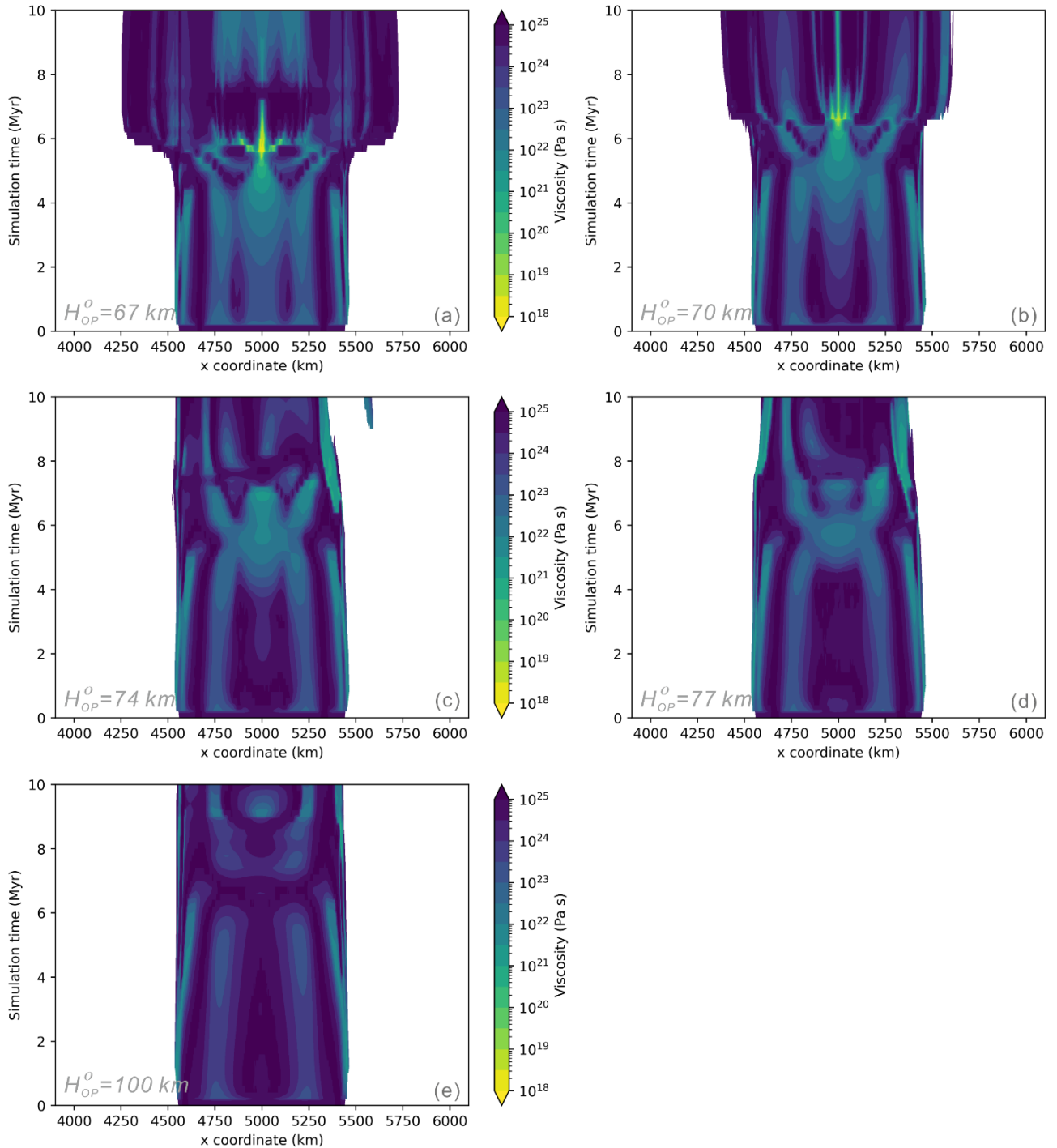
298 The second series of models increase the initial thermal thickness (defined by the 1300 K contour)  
299 of the overriding plate ( $H_{OP}^0$ ) from 67 km to 100 km (Figure 5), while keeping the subducting plate's  
300 thickness ( $H_{SP}^0$ ) and the length of the overriding plate ( $L_{OP}^0$ ) constant (Table 2). As  $H_{OP}^0$  increases,  
301 the maximum weakening level developed within the overriding plate drops from 'IV' ( $H_{OP}^0 = 67$  km)  
302 to 'III' ( $H_{OP}^0 = 74$  km) and less than 'I' ( $H_{OP}^0 = 100$  km). The time it takes to lower each order of  
303 viscosity magnitude increases, indicating a slower progressive weakening.



304  
 305 Figure 5. Progressive weakening, illustrated by visualising the stress  $\sigma_{xx}$ , of the overriding plate during dual inward dipping  
 306 subduction with increasing thickness of the overriding plate, (a) model ' $H_{OP}^0 = 67 \text{ km}$ ', (b) model ' $H_{OP}^0 = 74 \text{ km}$ ' and (c) model ' $H_{OP}^0 =$   
 307  $100 \text{ km}$ '. A detailed explanation of the contours and symbols could be found in the caption of Figure 2.

308 Besides, the total extension decreases from  $\sim 600 \text{ km}$  ( $H_{OP}^0 = 67 \text{ km}$ , Figure 6, a) to  $\sim 350 \text{ km}$  ( $H_{OP}^0 =$   
 309  $70 \text{ km}$ , Figure 6, b) and ultimately to  $\sim 0 \text{ km}$  ( $H_{OP}^0 = 100 \text{ km}$ , Figure 6, c-e). The maximum viscosity  
 310 reduction in both the primary and secondary necking regions decreases as  $H_{OP}^0$  increases, while

311 the lateral distance away from the trench of necking regions are equal, showing no correlation with  
 312  $H_{OP}^0$ .



313  
 314 Figure 6. Temporal evolution of viscosity along a horizontal line at the depth of 5km in the overriding plate. (a) Model ' $H_{OP}^0 = 67 \text{ km}$ '.  
 315 (b) Model ' $H_{OP}^0 = 70 \text{ km}$ '. (c) Model ' $H_{OP}^0 = 74 \text{ km}$ '. (d) Model ' $H_{OP}^0 = 77 \text{ km}$ '. (e) Model ' $H_{OP}^0 = 100 \text{ km}$ '. All models have the same  
 316  $H_{SP}^0$  (141 km) and  $L_{OP}^0$  (500 km). The edge of the contour filling in the lateral direction represents the interface between the  
 317 overriding plate and subducting plate.

318 To investigate the details of the progressive weakening in the necking region, 6 diagnostics are  
 319 evaluated along the vertical slice in the middle of the overriding plate. This is where the necking  
 320 belt develops in models with  $L_{OP}^0$  of 500 km. The diagnostics are integrated along the vertical slice  
 321 and then divided by the thickness of the plate (Equation (13)),

$$\bar{D} = \frac{1}{H_{OP}} \int_0^{H_{OP}} D \, dy, \quad (13)$$

322 in which  $D$  represent the diagnostic. The averaged results include magnitude of viscosity ( $\bar{\mu}$ ),  
 323 second invariant of strain rate ( $\bar{\dot{\epsilon}}_{II}$ ), lithosphere thickness ( $\bar{d}_{OP}$ ), horizontal stretching stress  
 324 component ( $\bar{\sigma}_{xx}$ ), vertical velocity component ( $\bar{v}_y$ ), and temperature ( $\bar{T}$ ).

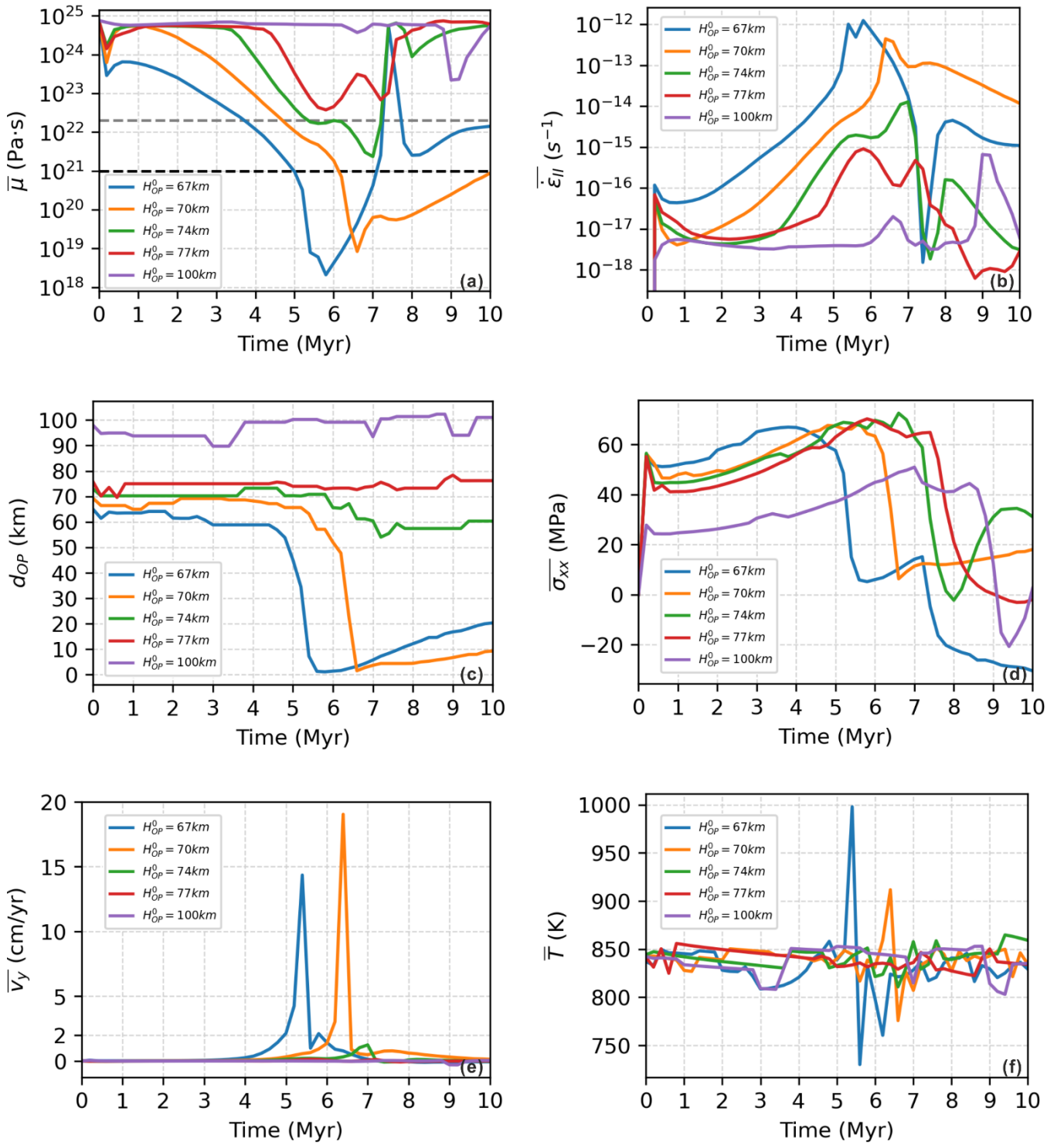
325 Take the model ' $H_{OP}^0 = 67 \text{ km}$ ' for example (blue line), the evolution of the 6 diagnostics during dual  
 326 inward dipping subduction is analysed (Figure 7). There is linear increase of  $\bar{\dot{\epsilon}}_{II}$  and  $\bar{\sigma}_{xx}$ , and linear  
 327 decrease of  $\bar{\mu}$  during the simulation between 1 Myr to 4 Myr. While  $\bar{d}_{OP}$ ,  $\bar{T}$  and  $\bar{v}_y$  remains nearly  
 328 constant. From 4 Myr to 5 Myr,  $\bar{\dot{\epsilon}}_{II}$  and  $\bar{\mu}$  keep a similar linear trend as before. But  $\bar{\sigma}_{xx}$  stops  
 329 increasing and starts to decrease gently.  $\bar{v}_y$  starts to increase and  $\bar{d}_{OP}$  starts to decrease, while  
 330  $\bar{T}$  experiences little change. During the rifting and spreading extension between 5 Myr to 6 Myr, all  
 331 diagnostics are varying more rapidly, with  $\bar{\mu}$ ,  $\bar{d}_{OP}$  and  $\bar{\sigma}_{xx}$  dropping and  $\bar{\dot{\epsilon}}_{II}$ ,  $\bar{v}_y$  and  $\bar{T}$  climbing  
 332 steeply. Afterwards, the model enters the steady state subduction stage, and the weakening  
 333 process is replaced by a healing process where  $\bar{\mu}$  and  $\bar{d}_{OP}$  both increase while  $\bar{\dot{\epsilon}}_{II}$  and  $\bar{v}_y$   
 334 decrease gradually.

335 As the thickness of the overriding plate increases from 67 km to 100 km, the magnitude of viscosity  
 336 drop in the necking area decreases. In detail, the plotting shows that if  $\bar{\mu}$  in the necking area of the



337 overriding plate is above  $\sim 2 \times 10^{22} Pa \cdot s$  (Figure 7, a, grey dashed line), there is no lithospheric  
338 thinning in the necking region (Figure 7, c, purple and red lines). In the timesteps when  $\bar{\mu}$  is in the  
339 range of  $10^{21} \sim 2 \times 10^{22} Pa \cdot s$ , thinning starts to build up, but it's not weak enough to have rifting  
340 extension (Figure 7, c, green line). Only when the  $\bar{\mu}$  drops below  $10^{21} Pa \cdot s$  does significant  
341 thinning develop within the overriding plate (Figure 7, c, blue and orange lines). The results of  $\bar{\mu}$   
342 confirms that the iso-viscous contour  $10^{21} Pa \cdot s$  can be used to predict if rifting or spreading  
343 extension develops during the dual inward dipping subduction. It also reveals a more precise  
344 maximum viscosity below which the thinning of lithosphere develops.

345 The average temperature ( $\bar{T}$ ) of the thermal lithosphere is  $\sim 850$  K for all models. In models where  
346 iso-viscous contour of  $10^{21} Pa \cdot s$  is necked, there are some thermal fluctuations as high as  $\sim 150$   
347 K. In detail, the transient heating up only takes place during the rifting extension process of the  
348 overriding plate, and  $\bar{T}$  returns to  $\sim 850$  K gradually during the spreading extension when new  
349 oceanic floor cools down quickly.



350

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Figure 7. Temporal evolution of averaged diagnostics along the vertical slice in the middle of the overriding plate, (a) viscosity ( $\bar{\mu}$ ), (b) second invariant of strain rate ( $\bar{\epsilon}_{II}$ ), (c) lithosphere thickness ( $d_{OP}$ ), (d) horizontal stretching stress component ( $\bar{\sigma}_{xx}$ ), (e) vertical velocity component ( $\bar{v}_y$ ), and (f) temperature ( $\bar{T}$ ). Positive value of  $\bar{v}_y$  represent upward motion. We note the noisier  $\bar{T}$  is a result of temperature also controlling the thickness of integration.

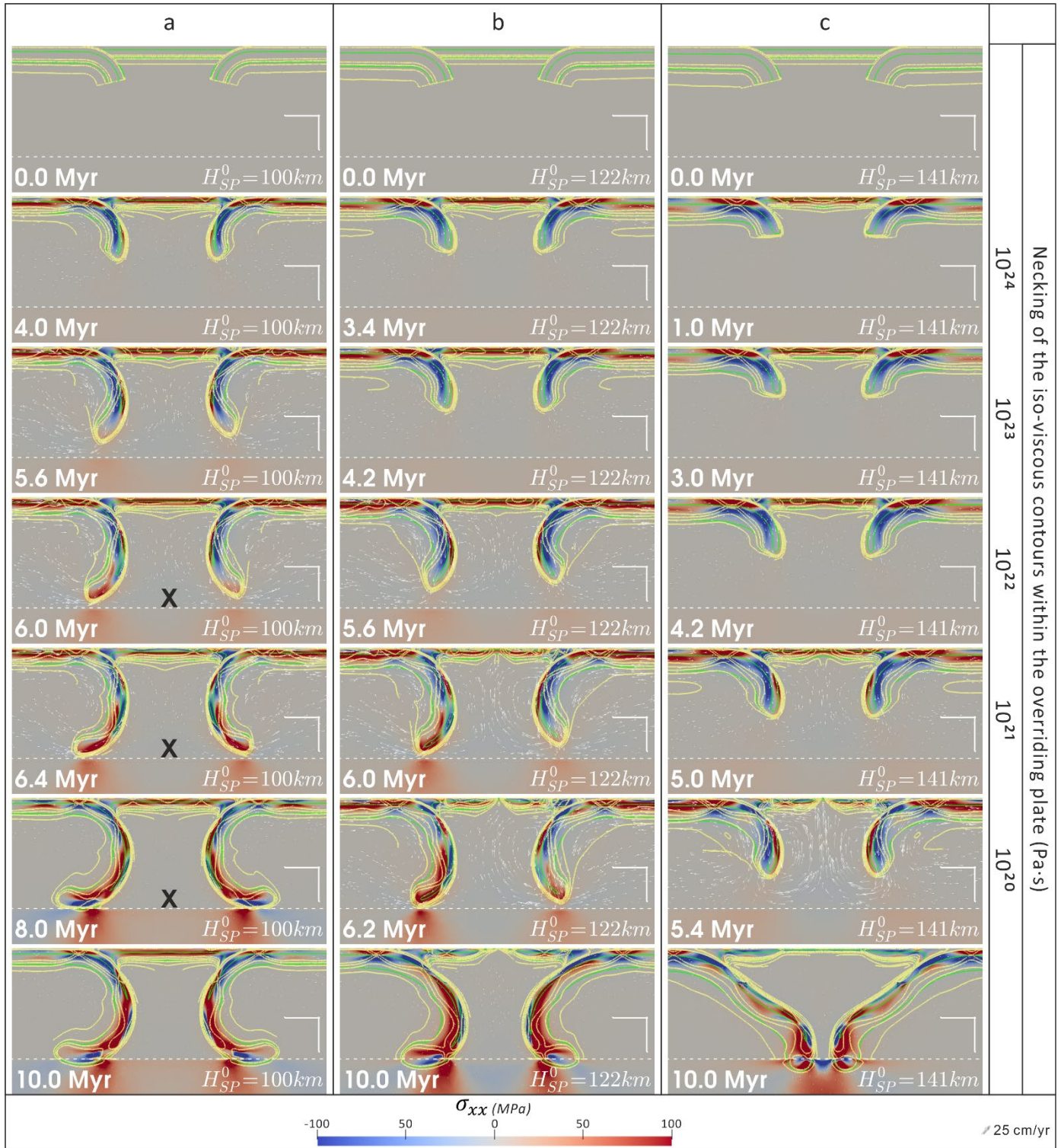
355

### 3.4 Thickness of the subducting plate

356

The third series of models investigate increasing the initial thermal thickness (again as defined by

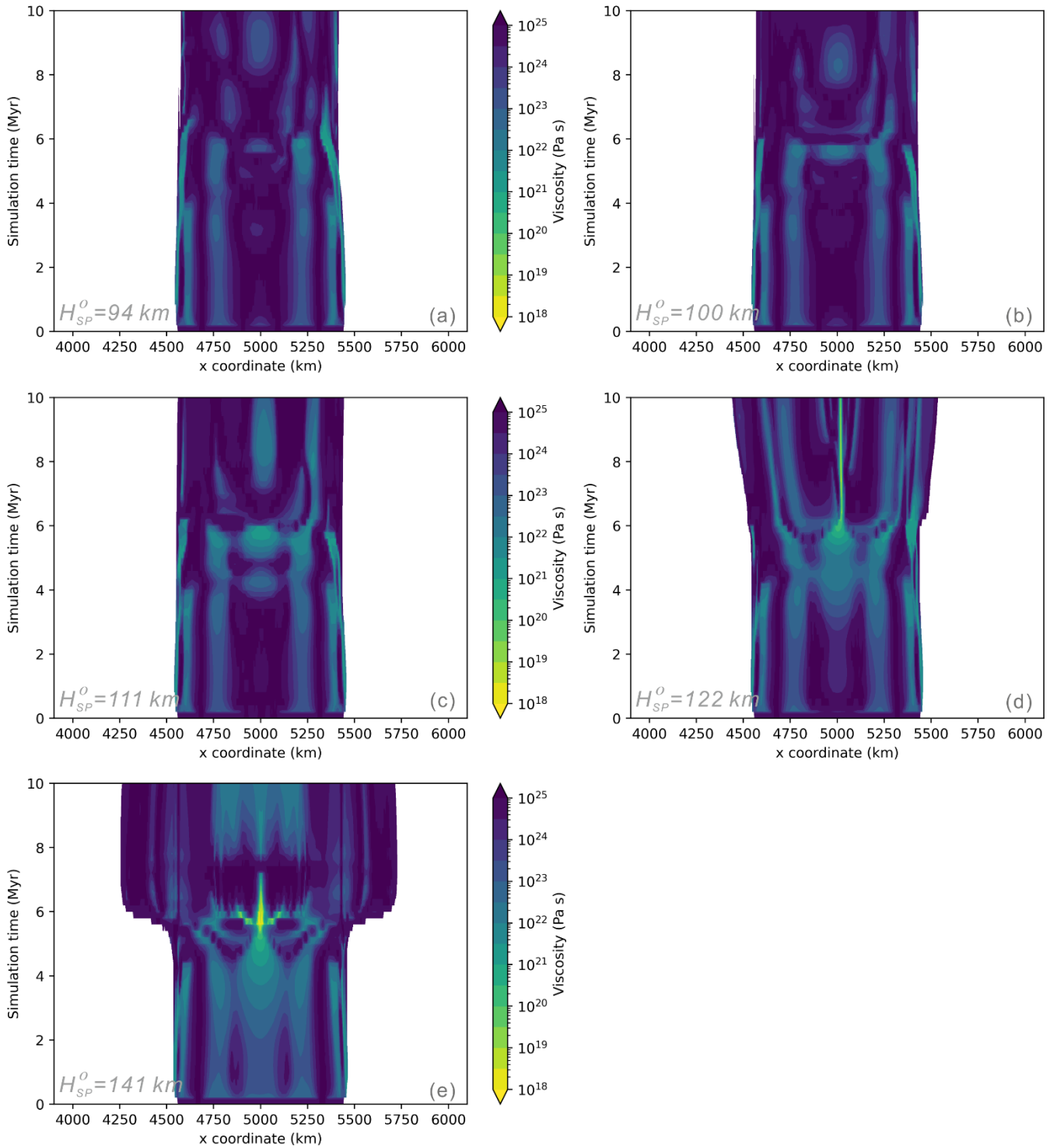
357 the 1300 K contour) of the subducting plate ( $H_{SP}^0$ ) from 94 km to 141 km (Figure 8), while keeping  
358 the subducting plate's thickness ( $H_{OP}^0$ ) and the length of the overriding plate ( $L_{OP}^0$ ) constant. As  $H_{SP}^0$   
359 increases, the maximum weakening level developed within the overriding plate drops from 'I' ( $H_{SP}^0 =$   
360 94 km) to 'III' ( $H_{SP}^0 = 122$  km) and 'IV' ( $H_{SP}^0 = 141$  km). The time it takes to lower each order of  
361 viscosity magnitude decreases, indicating a faster progressive weakening.



362  
 363 Figure 8. Progressive weakening of the overriding plate during dual inward dipping subduction with increasing age of the subducting  
 364 plate. (a) Model ' $H_{SP}^0 = 100 \text{ km}$ '. (b) Model ' $H_{SP}^0 = 122 \text{ km}$ '. (c) Model ' $H_{SP}^0 = 141 \text{ km}$ '. A detailed explanation of the contours and  
 365 symbols could be found in the caption of Figure 2.

366 Besides, the total extension increases from  $\sim 0 \text{ km}$  ( $H_{SP}^0 \leq 111 \text{ km}$ , Figure 9, a-c) to  $\sim 200 \text{ km}$  ( $H_{SP}^0 =$   
 367  $122 \text{ km}$ , Figure 9, d) and ultimately to  $\sim 600 \text{ km}$  ( $H_{SP}^0 = 141 \text{ km}$ , Figure 9, e). The maximum viscosity  
 368 reduction in both the primary and secondary necking regions increases as  $H_{SP}^0$  increases, while

369 the lateral distance away from the trench of necking regions are equal, showing little correlation  
 370 with  $H_{SP}^0$ .



371  
 372 Figure 9. Temporal evolution of viscosity along a horizontal line at the depth of 5 km in the overriding plate. (a) Model ' $H_{SP}^0 = 94$  km'.  
 373 (b) Model ' $H_{SP}^0 = 100$  km'. (c) Model ' $H_{SP}^0 = 111$  km'. (d) Model ' $H_{SP}^0 = 122$  km'. (e) Model ' $H_{SP}^0 = 141$  km'. Both models have the  
 374 same  $H_{OP}^0$  (67 km) and  $L_{OP}^0$  (500 km). The edge of the contour filling in the lateral direction represents the interface between the  
 375 overriding plate and subducting plate.

376 **3.5 Regime of stretching state**

377 A variety of deformation patterns and stretching state within the overriding plate have been  
 378 observed when varying  $L_{OP}^0$ ,  $H_{OP}^0$  and  $H_{SP}^0$ . Several diagnostics are reported together to quantify  
 379 the deformation developed within the overriding plate during the 10 Myr simulation (Table 3). The  
 380 detail of each diagnostic is described as follows.

381 Table 3. Summary of diagnostics for all models. For further description of the diagnostics please see the main text.

| Model name                   | weakeni<br>ng level | $t_{\text{rift}}$<br>(Myr) | $t_{660}$<br>(Myr) | $\bar{v}_{\text{sink}}$<br>(cm/yr) | $l_{n2n}$<br>(km) | $l_{n2t}$<br>(km) | total<br>strain  |
|------------------------------|---------------------|----------------------------|--------------------|------------------------------------|-------------------|-------------------|------------------|
| $H_{SP}^0 = 94 \text{ km}$   | I                   | -                          | 6.6                | 7.0                                | 0                 | 341               | 1%               |
| $H_{SP}^0 = 100 \text{ km}$  | III                 | -                          | 6.4                | 7.2                                | 0                 | 341               | 2%               |
| $H_{SP}^0 = 111 \text{ km}$  | III                 | -                          | 6.4                | 7.2                                | 0                 | 341               | 21%              |
| $H_{SP}^0 = 122 \text{ km}$  | IV                  | 6.2                        | 6.4                | 7.2                                | 0                 | 341               | 110%             |
| $H_{SP}^0 = 141 \text{ km}$  | IV                  | 5.4                        | 6.0                | 7.7                                | 0                 | 341               | 2800%            |
| $H_{OP}^0 = 67 \text{ km}$   | IV                  | 5.4                        | 6.0                | 7.7                                | 0                 | 341               | 2800%            |
| $H_{OP}^0 = 70 \text{ km}$   | IV                  | 6.4                        | 6.6                | 7.0                                | 0                 | 341               | 1300%            |
| $H_{OP}^0 = 74 \text{ km}$   | III                 | -                          | 7.2                | 6.4                                | 0                 | 341               | 30%              |
| $H_{OP}^0 = 77 \text{ km}$   | II                  | -                          | 7.6                | 6.1                                | 0                 | 341               | 4%               |
| $H_{OP}^0 = 100 \text{ km}$  | I                   | -                          | 8.8                | 5.2                                | 0                 | 341               | 1%               |
| $L_{OP}^0 = 500 \text{ km}$  | IV                  | 5.4                        | 6.0                | 7.7                                | 0                 | 341               | 2800%            |
| $L_{OP}^0 = 600 \text{ km}$  | IV                  | 5.4                        | 6.0                | 7.7                                | 0                 | 384               | 690%             |
| $L_{OP}^0 = 700 \text{ km}$  | IV                  | 5.6                        | 6.0                | 7.7                                | 130               | 371               | 630%             |
| $L_{OP}^0 = 800 \text{ km}$  | IV                  | 5.8                        | 6.0                | 7.7                                | 231               | 364               | 14% <sup>a</sup> |
| $L_{OP}^0 = 1000 \text{ km}$ | III                 | -                          | 6.0                | 7.9                                | 282               | 369               | 15%              |
| $L_{OP}^0 = 1200 \text{ km}$ | III                 | -                          | 5.8                | 7.9                                | 621               | 370               | 11%              |
| $L_{OP}^0 = 1600 \text{ km}$ | II                  | -                          | 5.4                | 8.5                                | 937               | 411               | 4%               |

382 <sup>a</sup> The total strain listed here is calculated along the middle vertical slice (5000 km away from side boundaries). For models  $L_{OP}^0 \geq$   
 383 800 km, the necking zones are away from this middle vertical slice. So, the total strain could be underestimated for these models.  
 384 Considering that only model ' $L_{OP}^0 = 800 \text{ km}$ ' achieved weakening level 'IV', the corrected total strain along its necking zone is ~600%.  
 385 While the underestimation for other models is moderate and will not change the conclusion of this research.

386 As introduced in section 3.1.1, weakening levels 'I', 'II', 'III', 'IV' are determined by the minimum  
 387 viscosity contour which is necked in the overriding plate during subduction. The higher the  
 388 weakening level, the stronger the localised rheology modification observed within the overriding  
 389 plate. All three groups of dual inward dipping subduction models manage to yield a variety of

390 weakening levels in the overriding plate (Figure 10, a-c).

391  $t_{\text{rift}}$  indicates the timestep when the overriding plate develops rifting extension (weakening level  
 392 'IV'), and a void value means that model fails to generate rifting extension within the overriding  
 393 plate. It shows that only models achieving weakening level 'IV' develop rifting extension.  $t_{\text{rift}}$   
 394 increases with thicker or longer overriding plate, and decreases with thicker subducting plate.

395  $t_{660}$  equals how much time the subducting plate (defined by its 1300 K isotherm) takes to sink to  
 396 the depth of 660km. It is most sensitive to the variation of  $H_{OP}^0$ , while varying  $L_{OP}^0$  and  $H_{SP}^0$   
 397 generates less than ~1 Myr difference of  $t_{660}$  compared with a ~3 Myr difference when modifying  
 398  $H_{OP}^0$ .  $\bar{v}_{\text{sink}}$  equals 460 km (the vertical distance from the initial slab tip depth to the depth of 660  
 399 km) divided by  $t_{660}$ .  $\bar{v}_{\text{sink}}$  ranges from 5.2 to 8.5 cm/yr and the magnitude does not correlate with  
 400 the weakening level or  $t_{\text{rift}}$ , i.e., high sinking rate does not necessarily lead to higher weakening  
 401 level or faster rifting extension.

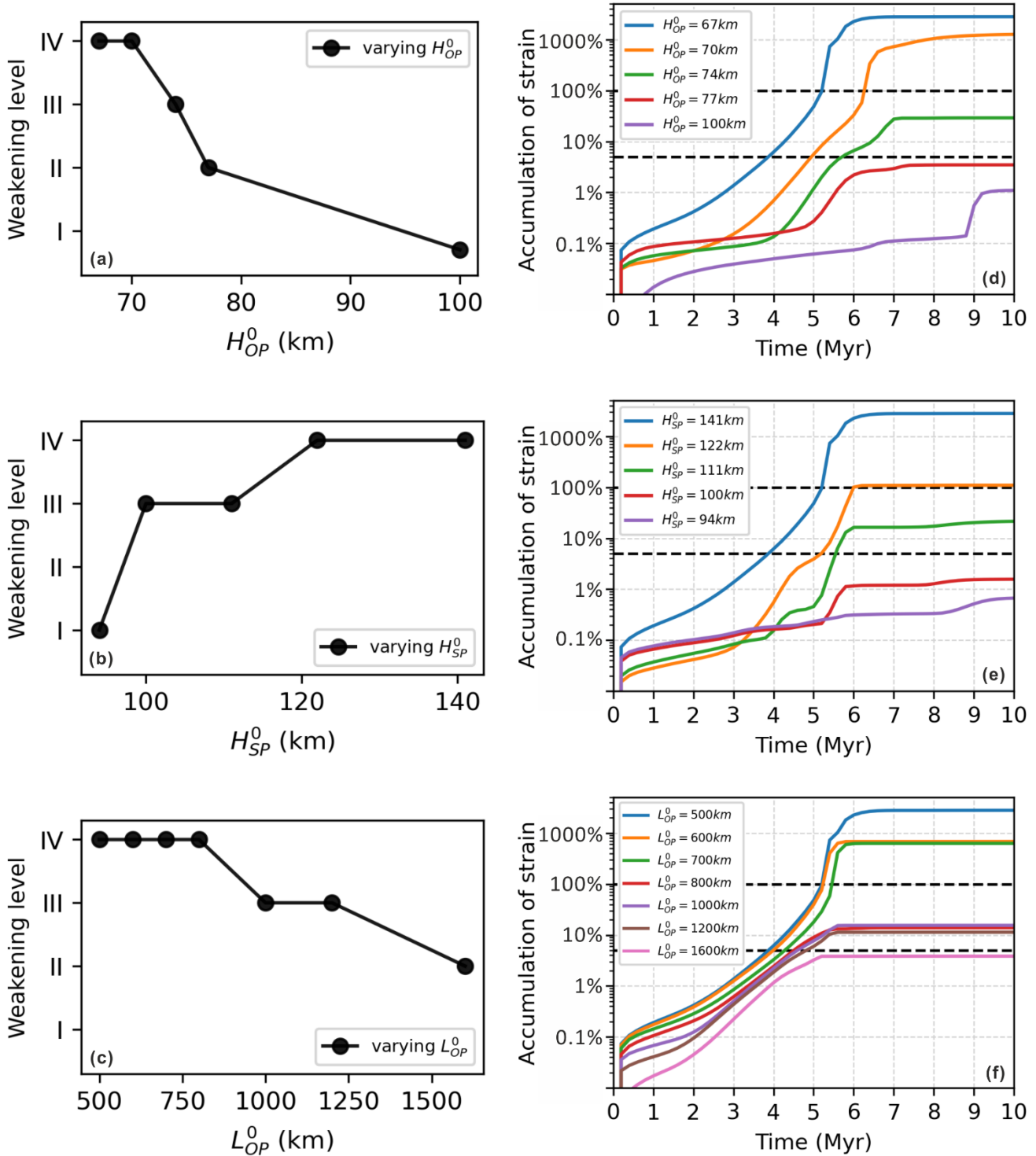
402  $l_{n2n}$  is the horizontal distance between necking centres which may develop rifting extension during  
 403 dual inward dipping subduction, i.e., secondary necking regions are excluded. The value of  $l_{n2n}$  is  
 404 0 km if there is only one necking centre within the overriding plate.  $l_{n2n}$  starts to increase with  $L_{OP}^0$   
 405 when  $L_{OP}^0$  is greater than ~700 km.  $l_{n2n}$  in Table 3 is recorded at the timestep of 4.4 Myr. It should  
 406 be noted that,  $l_{n2n}$  may vary with time and the difference is at most ~250 km (Figure 4).

407  $l_{n2t}$  marks the lateral distance from the centre of the necking area to its nearest trench at the 4.4  
 408 Myr timestep. For all simulations,  $l_{n2t}$  is in a narrow range of ~340-410 km and the variation is  
 409 likely to originate from the fact that  $l_{n2t}$  is also time dependent. Since the average sinking rate is

410 different for these models, different models may behave differently at the same timestep.

411 Total strain is calculated by integrating the average strain rate ( $\overline{\dot{\epsilon}_{II}}$  based on Equation (13)) with  
412 time throughout the 10 Myr simulation. All three groups of models generate a variety of total strain  
413 at the end of the simulation (Figure 10, d-f). For all models that develop rifting extension, the total  
414 strain is greater than 100%. Total strain in the range of 5% to 100% is observed from limited thinning  
415 up to significant extension. For models where the total strain is less than 5%, the weakening  
416 deformation is hardly observable in the overriding plate.





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Figure 10. Key diagnostics used to characterise the rheology modification within the overriding plate. (a-c) Weakening level developed within the overriding plate. (d-f) Accumulation of strain in the middle of the overriding plate (5000 km away from the side boundaries).

421  
422  
423

By combing all the qualitative and quantitative diagnostics presented in these results, we classify three stretching states: 1) little or no lithosphere thinning and extension, discriminated by low weakening level up to level 'II', little total strain up to 5% and almost no thermal lithosphere thinning

424 in the necking area; 2) limited lithosphere thinning and extension, identified by medium weakening  
425 level up to level 'III', medium total strain up to 30%, and limited thermal lithosphere thinning, e.g.,  
426 ~15 km thinning for model ' $H_{OP}^0 = 74 \text{ km}$ ' (Figure 7, c); 3) rifting and spreading extension,  
427 characterised by high weakening level up to level 'IV', high total strain over 100%, and total thinning  
428 of the thermal lithosphere during rifting extension.

## 429 **4. Discussion**

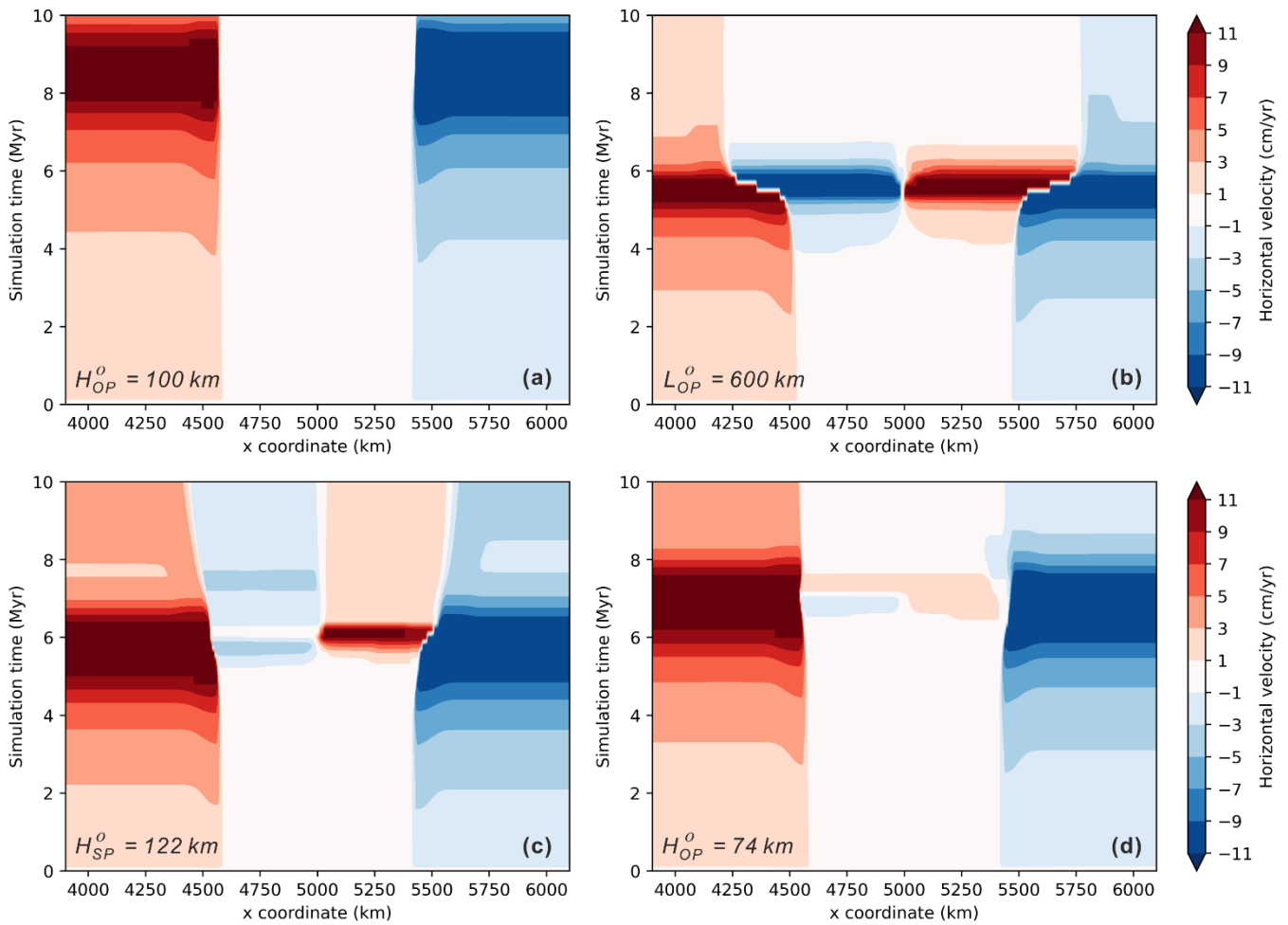
430 The results show that the non-steady state subduction provides a time window to develop  
431 progressive weakening within a uniform overriding plate. With appropriate conditions, tested in this  
432 research, e.g., thick enough  $H_{SP}^0$ , thin enough  $H_{OP}^0$ , short enough  $L_{OP}^0$ , different levels of stretching  
433 state, ranging from no thinning nor extension to rifting and spreading extension, can develop within  
434 the homogeneous overriding plate. The role that dual inward dipping subduction plays during the  
435 progressive weakening and the origin of the softening process are worth discussion.

### 436 **4.1 The role dual inward dipping subduction plays**

#### 437 ***4.1.1 Creating fixed trailing boundary condition for the overriding plate***

438 Due to the symmetric model setup, subducting plates on both sides are prone to advance or retreat  
439 simultaneously. This creates roughly equal and symmetric competing force from both ends of the  
440 middle plate during subduction. As a result, the mobility of the overriding plate is inhibited, and in  
441 comparing to single-sided subduction, it would be as if the velocity boundary condition on the  
442 overriding plate was fixed (Figure 11, a-c). This helps cultivating an ever-increasing stretching

443 stress field and forming localised necking weak zones within the middle plate during non-steady  
 444 state subduction. This is unlike the single sided subduction cases, where the mobile overriding  
 445 plate can move as a whole to slow down the build up of deviatoric stress within the plate. Thus, the  
 446 lack of mobility of the overriding plate plays a key role in the weakening process during subduction.



447  
 448 Figure 11. Temporal evolution of horizontal velocity along a lateral slice, x coordinate from 3900km to 6100 km, at the depth of 20  
 449 km from the surface. (a) model ' $H_{OP}^0 = 100 \text{ km}$ ', (b) model ' $L_{OP}^0 = 600 \text{ km}$ ', (c) model ' $H_{SP}^0 = 122 \text{ km}$ ', (d) model ' $H_{OP}^0 = 74 \text{ km}$ '. The  
 450 contour filling represents the variation of horizontal component of velocity vector throughout the 10 Myr simulation. Positive value  
 451 means right-ward motion and negative value is left-ward motion. The white area represents that the plate is nearly stagnant. And  
 452 the edge of the white area marks the interface between the subducting plate and overriding plate or rifting and spreading centre  
 453 within the overriding plate.

454 The fixed boundary condition environment is likely to be favoured as long as on both sides the slab  
 455 has symmetric trench motion tendencies. Once one side is prone to advance, or move slower than

456 the other, then the fixed boundary condition effect is likely to weaken and the magnitude of the  
457 velocity of the overriding plate can increase from ~0 cm/yr to 1-3 cm/yr (Figure 11, d). But still, the  
458 overriding plate is not as mobile as a free mobile boundary condition in single subduction models,  
459 where the overriding plate can move as fast as 5 cm/yr as a whole during the non-steady state  
460 subduction (e.g., Chen et al., 2016).

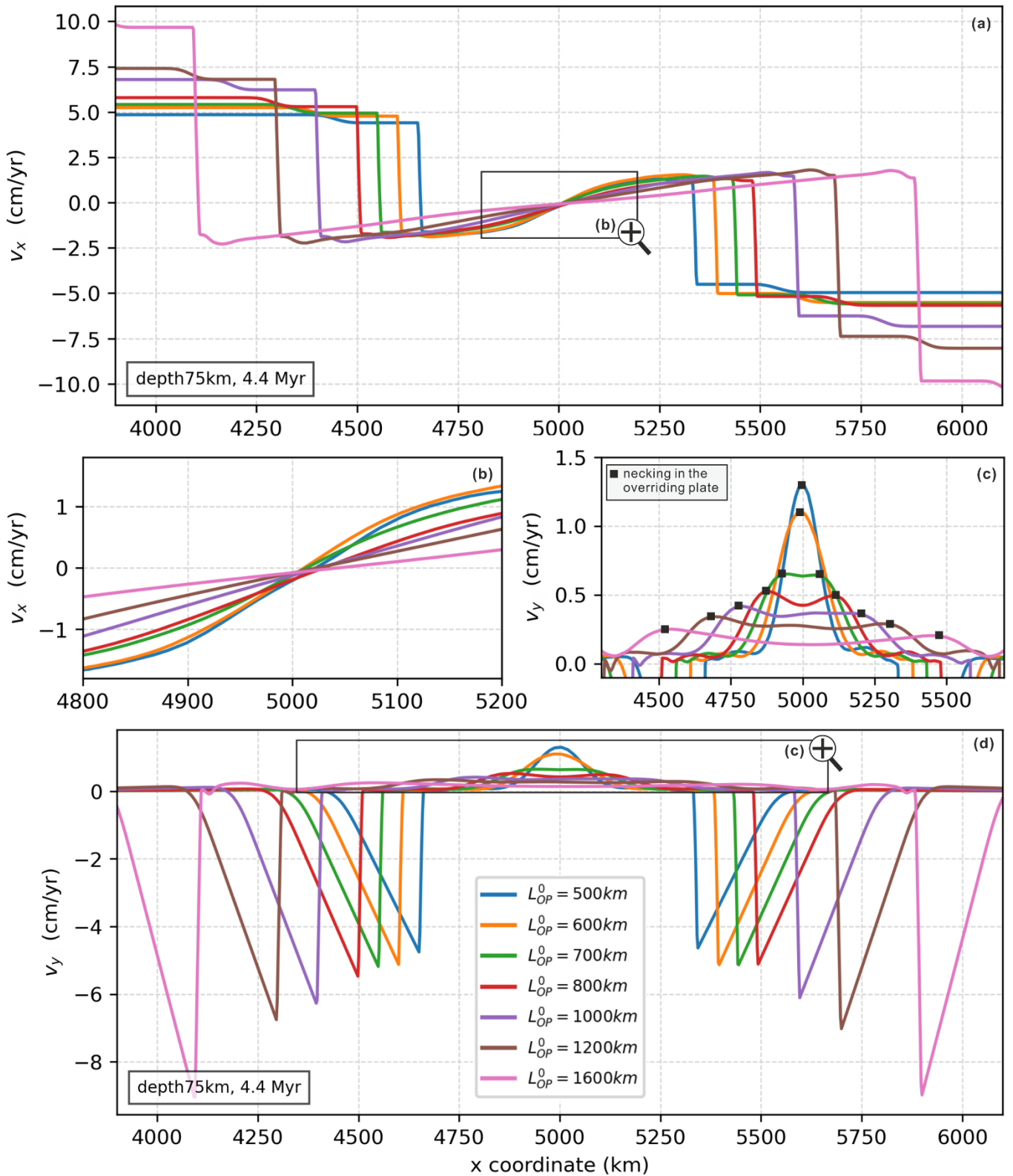
461 In previous subduction models, a fixed boundary condition is achieved on the overriding plate by  
462 extending the overriding plate to the side boundary and applying a fixed velocity to the plate. It is  
463 suggested that such a boundary condition is responsible for the increased degree of deformation  
464 in the overriding plate compared with mobile plates (Chen et al., 2016; Erdős et al., 2021; Yang et  
465 al., 2019). A comparable effect is achieved by bringing in another subducting plate at the other end  
466 of the overriding plate. The fixed boundary condition effect is also observed in previous dual inward  
467 dipping subduction models (Dasgupta and Mandal, 2018; Holt et al., 2017; Lyu et al., 2019), but its  
468 role in affecting the weakening of the overriding plate was not addressed since the viscosity was  
469 only composition-dependent and did not change with evolving stress or temperature.

#### 470 **4.1.2 Stronger poloidal return flow**

471 Our results show that varying the size of the overriding plate can affect the degree of extension  
472 within the overriding plate. Previous research shows that subduction can induce poloidal mantle  
473 return flow, which has been suggested to account for extensional deformation within the overriding  
474 plate, e.g., back-arc extension, supercontinent breakup (Chen et al., 2016; Dal Zilio et al., 2018;  
475 Erdős et al., 2021; Sleep and Toksöz, 1971). Previous research also implies that, a) increasing the  
476 thickness of the subducting plate ( $H_{SP}^0$ ) can increase the net negative buoyancy thus leading to a

477 stronger poloidal flow (Garel et al., 2014); b) lowering the thickness of the overriding plate ( $H_{OP}^0$ )  
478 can not only increase the net negative buoyancy by increasing the hanging slab area in the upper  
479 mantle, but also reduces the dissipation during subduction along the interface between two plates  
480 (Erdős et al., 2021). These two mechanisms also come into play for dual inward dipping subduction  
481 models.

482 In addition, dual inward dipping subduction models can yield a third way to strengthen the return  
483 flow. This is by combining the two separate poloidal convection flows, one from each subducting  
484 plate, as the length of the overriding plate ( $L_{OP}^0$ ) shortens (Figure 3). This is shown for example by  
485 the velocity variation in both the horizontal ( $v_x$ ) and vertical ( $v_y$ ) direction at the depth of 75 km  
486 (Figure 12). For all dual inward dipping subduction models, the magnitude of  $v_x$  decreases  
487 gradually from  $\sim 2.5$  cm/yr in the mantle wedge corner to 0 cm/yr underlying the middle part ( $\sim 5000$   
488 km away from side boundaries) of the overriding plate (Figure 12, a). As  $L_{OP}^0$  changes, models with  
489 shorter overriding plate have greater  $v_x$  gradient along the lateral slice (Figure 12, b). The  
490 maximum magnitude of  $v_y$  increases from  $\sim 0.25$  cm/yr to  $\sim 1.3$  cm/yr, implying a faster upwelling  
491 flow, as the length of the overriding plate ( $L_{OP}^0$ ) shortens (Figure 12, c-d). It is also noted that the  
492 necking area developed within the overriding plate (e.g., Figure 3) lies right above the maximum  
493 upwelling component of the return flow (Figure 12, c). The observation indicates a spatial  
494 correlation between the stronger poloidal return flow and the progressive weakening in the  
495 overriding plate.



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Figure 12. Velocity variation along a slice at the depth of 75 km, which is  $\sim 8$  km below the 1300 K isotherm of the overriding plate, after 4.4 Myr simulation. (a, d) Horizontal and vertical component of velocity along the slice. (b) and (c) are zoom-in of (a) and (d) under the middle part of the overriding plate ( $5000 \pm 200$  km and  $5000 \pm 650$  km away from the side boundaries respectively). Positive value means rightward or upward motion, and negative value represents leftward or downward motion. In (c), the horizontal coordinate of the necked region in the overriding plate is plotted as black square to visualize its spatial correlation with upwelling component of mantle wedge flow. All plots share the same legend listed in (d).

503 Previous research on subduction induced continental breakup implies that spreading extension  
504 develops above where the upwelling mantle flow diverges, flow which creates the highest shear  
505 stress gradient at the bottom of the overriding plate (Dal Zilio et al., 2018). This does not fully agree  
506 with our simulation results with varying  $L_{OP}^0$ . The divergent return flow is defined as the place where  
507  $v_x$  changes direction. It always lies under the middle part (~5000 km away from the side boundaries)  
508 of the overriding plate for all models (Figure 12, a). However, the weakening area does not always  
509 develop in the middle of the overriding plate, e.g., when  $L_{OP}^0 \geq 800$  km. Instead, it correlates better  
510 in space with the highest upwelling mantle flow velocity (Figure 12, c). The lateral distance from the  
511 highest upwelling component to the nearest trench is measured (Figure 12, d), and it is noted that  
512 the distance remains relatively constant at ~370 km for all models at 4.4 Myr. This suggests that  
513 the wavelength of the slab induced mantle wedge flow is not related with varying  $L_{OP}^0$ .

514 An interesting observation is that the subducting slab's sinking velocity increases ( $t_{660}$  decreases)  
515 with longer  $L_{OP}^0$  (Table 3), while the poloidal mantle flow gets weaker and the maximum weakening  
516 level in the overriding plate decreases. From the perspective of energy conservation, all the  
517 dynamic processes, e.g., plate motion, mantle convection, internal deformation etc., originates from  
518 the potential energy of the subducting slabs. This implies that more of the potential energy transfers  
519 into kinetic energy of the subducting plates instead of being consumed as dissipation energy in the  
520 overriding plates, as  $L_{OP}^0$  increases.

## 521 **4.2 Overriding plate weakening mechanism**

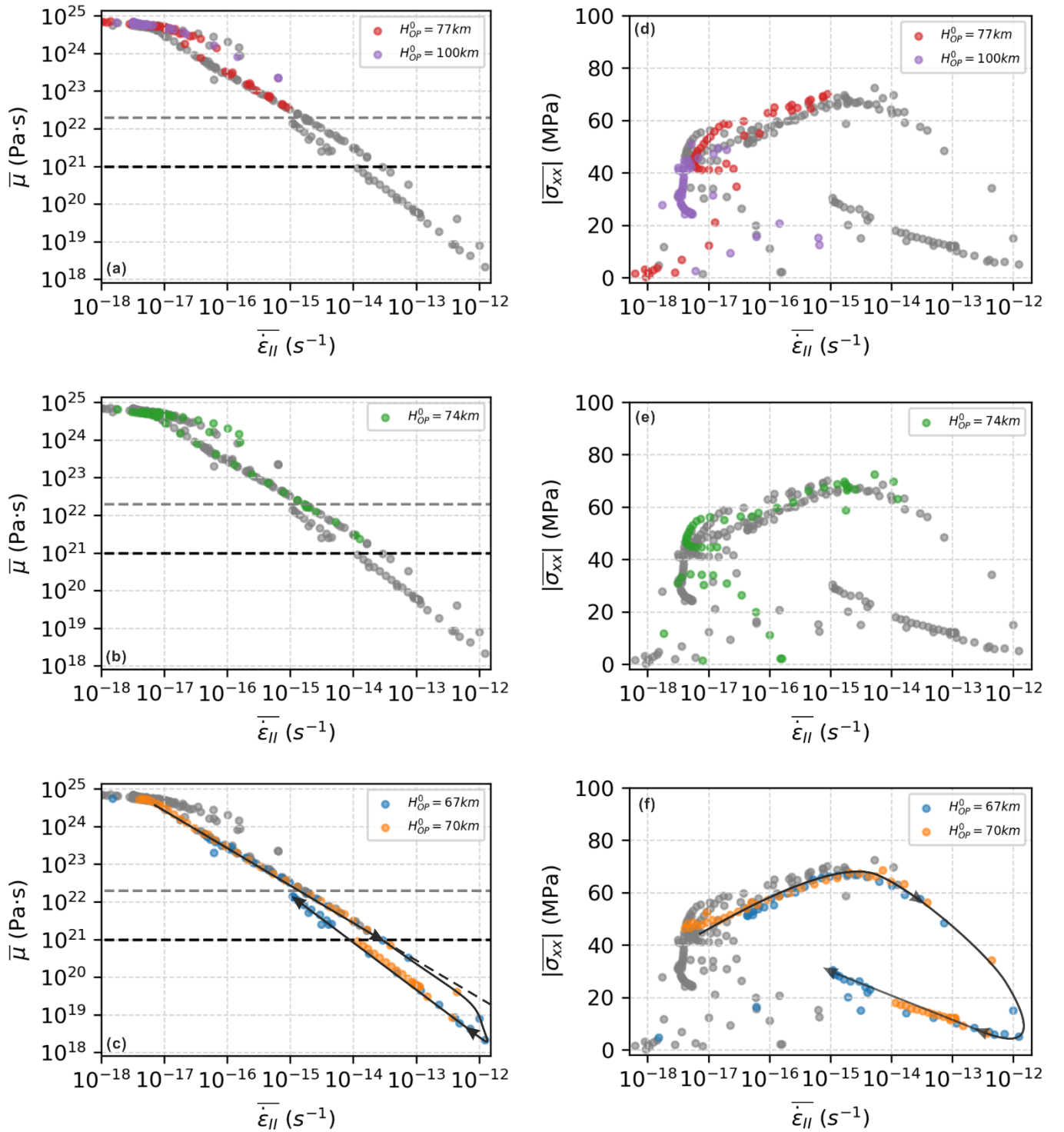
522 To understand the viscosity weakening mechanism in the necking area, the dependency of viscosity  
523 on the three variables, strain rate, temperature and pressure are examined. Averaged variables are

524 calculated based on Equation (13) along the middle slice (~5000 km away from side boundaries)  
525 of the thermal lithosphere, where the necking weak zone develops. Each dependency investigation  
526 is divided into three subplots based on the regime of stretching state developed within the overriding  
527 plate. They are 1) little or no thinning and extension; 2) limited thinning and extension; 3) rifting and  
528 spreading extension.

#### 529 **4.2.1 Strain rate weakening**

530 The scatter plot of viscosity dependency upon strain rate in the necking area (Figure 13, a-b) shows  
531 that when the magnitude of average viscosity ( $\bar{\mu}$ ) is higher than  $10^{21} \text{ Pa} \cdot \text{s}$  (weakening level < 'IV'),  
532  $\bar{\mu}$  decreases linearly with increasing  $\bar{\dot{\epsilon}}_{II}$ . For models which develop significant lithospheric thinning  
533 and extension within the overriding plate (Figure 13, c), i.e., weakening level 'IV' and  $\bar{\mu} \leq 10^{21} \text{ Pa} \cdot$   
534  $\text{s}$ ,  $\bar{\mu}$  starts to decrease faster with increasing  $\bar{\dot{\epsilon}}_{II}$  than the former linear relationship. After the  
535 subducting slab reaches the lower mantle,  $\bar{\mu}$  starts to increase linearly again with the decreasing  
536  $\bar{\dot{\epsilon}}_{II}$ , indicating a hardening process after the progressive weakening. For models which do not neck  
537 the iso-viscous contour of  $10^{21} \text{ Pa} \cdot \text{s}$  (e.g.,  $H_{OP} \geq 74 \text{ km}$ ), the path of hardening process is nearly  
538 reversely parallel to its initial weakening trace (Figure 13, a-b).





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Figure 13. Scatter plot throughout the 10 Myr simulation of model series with varying thickness of the overriding plate. (a-c)  $\bar{\mu}$  versus  $\bar{\dot{\epsilon}}_{II}$ , (d-f)  $|\bar{\sigma}_{xx}|$  versus  $\bar{\dot{\epsilon}}_{II}$ . Variables in (a-f) are calculated based on Equation (13). The solid trajectory lines with arrow in (c) and (f) indicate the evolution orientation of the scatter points with time. Models in the same series of simulation but with different overriding plate stretching state are plotted in grey dots as comparison.

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Then when  $\bar{\dot{\epsilon}}_{II}$  is lower than  $\sim 10^{-14} \text{ s}^{-1}$ , the horizontal component of stress ( $\bar{\sigma}_{xx}$ ) varies linearly

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with  $\bar{\dot{\epsilon}}_{II}$ , indicating a highly viscous flow behavior within the overriding plate (Figure 13, d). But at

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larger strain rate (weakening level 'IV'), the viscosity decreases so rapidly with increasing strain

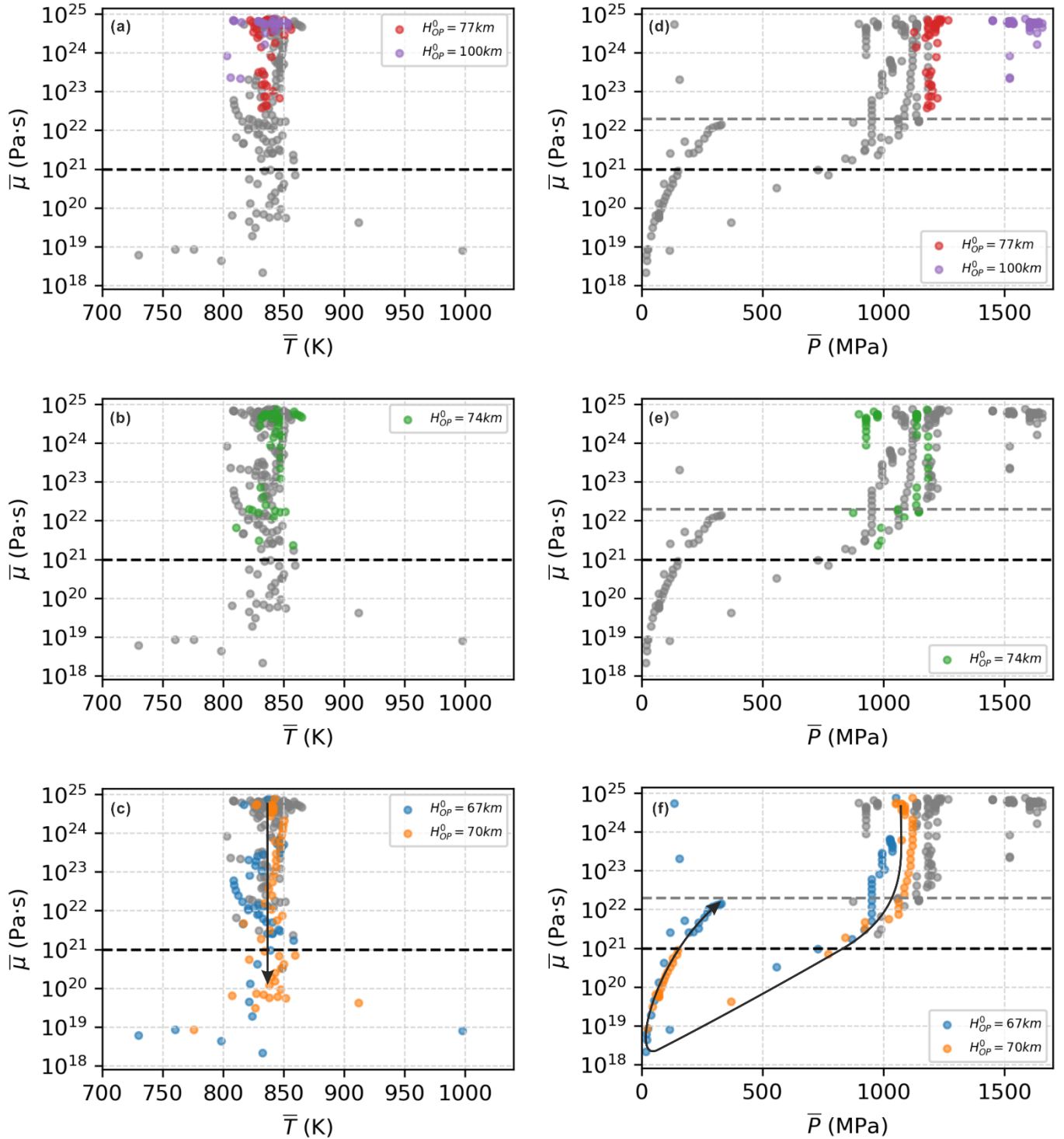
547 rate that the stress, the very resistance to flow, decreases as well. The negative correlation between  
548 stress and strain rate suggests a decreasing plate strength which is proportional to  $\bar{\mu} \times H_{OP}$  in the  
549 case of uniaxial stretching (Ribe, 2001). Such negative correlation has also been observed in a  
550 velocity-weakening rheology when strain rate exceeds a certain level (Bercovici et al., 2015), and  
551 in a crystal softening experiment (Poirier, 1985). The continuous plate strength reduction during  
552 dual inward dipping subduction also suggests that high strain rate may relate to the formation of  
553 new plate boundaries (Gueydan et al., 2014).

554 In this research, strain rate can affect the viscosity component related to yielding, Peierls and  
555 dislocation creep deformation (Equation (8), (9)). Thus, all three deformation mechanisms  
556 contribute to the softening process in the overriding plate. Considering that the sensitivity to strain  
557 rate decreases from yielding, to Peierls and dislocation creep respectively, their contribution to the  
558 viscosity drop may decrease accordingly. However, the evolution of the iso-viscous contour shows  
559 that the viscosity drop initiates from the surface (yielding) and the bottom of the plate (dislocation  
560 creep). Then the viscosity contour necks in the middle depth of the plate where Peierls creep  
561 dominates (Figure 2, b). This suggests that yielding and dislocation are more important for initiating  
562 plate softening than Peierls creep.

#### 563 **4.2.2 Thermal weakening and lithosphere thinning**

564 The scatter plot of viscosity dependency upon the average temperature ( $\bar{T}$ ) and pressure ( $\bar{P}$ ) show  
565 that  $\bar{T}$  and  $\bar{P}$  have no correlation with viscosity drop when  $\bar{\mu} \geq \sim 2 \times 10^{22} Pa \cdot s$  (Figure 14, a, d).  
566 We note that  $\bar{P}$  is a good indicator of lithosphere thickness. The thickness of thermal lithosphere  
567 starts to reduce as  $\bar{\mu}$  keeps dropping to  $\sim 10^{21} Pa \cdot s$ .  $\bar{T}$  still shows little correlation with  $\bar{\mu}$ , while

568  $\bar{P}$  becomes proportional to  $\bar{\mu}$  (Figure 14, b, e). As  $\bar{\mu}$  continues decreasing and rifting extension  
 569 starts to develop,  $\bar{T}$  shows a fluctuated and nonlinear correlation with  $\bar{\mu}$ , while  $\bar{P}$  stays in a  
 570 positive linear relationship (Figure 14, c, f).



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Figure 14. Scatter plot throughout the 10 Myr simulation of model series with varying thickness of the overriding plate. (a-c)  $\bar{\mu}$  versus  $\bar{T}$ , (d-f)  $\bar{\mu}$  versus  $\bar{P}$  (mainly a measure of plate thickness). Variables in (a-f) are calculated based on Equation (13). Models in the same series of simulations but with different stretching states are plotted in grey dots for comparison.

575 Temperature increase, according to the rheology setup (Equation (8)), can lower the viscosity of  
576 Peierls, dislocation and diffusion creep. Temperature increase and lithosphere thinning can both  
577 contribute to weakening the overriding plate, but they may only play a role when the overriding  
578 plate is weakened to a certain level. For example, they may contribute to the additional viscosity  
579 drop seen in the non-linear relationship between  $\overline{\dot{\epsilon}_{II}}$  and  $\bar{\mu}$  (Figure 13, c).

580 In general, three feedback weakening loops are recognised during the dual inward dipping  
581 subduction. Among them, the strain rate weakening mechanism plays a dominant role in lowering  
582 the viscosity of the overriding plate throughout the simulation, and it is a precondition to develop  
583 thermal weakening and lithosphere thinning, which strengthens the feedback weakening loop. The  
584 dominant role of strain rate weakening over thermal weakening is also reported in the interaction  
585 between upwelling plumes and overlying lithosphere (Burov and Guillou-Frottier, 2005). That is to  
586 say, the rheology and buoyancy parameters will be more important than the heat conduction  
587 parameters in producing different levels of rheology weakening within the overlying plate.

### 588 **4.3 Limitations**

589 The major contribution of this work is incorporating a composite rheology which depends on multiple  
590 parameters, e.g., temperature, pressure and strain rate. However, previous research indicates that  
591 viscosity can also be affected by hydrous fluids, partial melting, and grain size of minerals in  
592 subduction zones (Bercovici et al., 2015; Braun et al., 1999; England and Katz, 2010; Montési and  
593 Hirth, 2003). In particular, grain size reduction is likely to take place when strain builds up (Gueydan  
594 et al., 2014). Taking these parameters into consideration is likely to strengthen the feedback  
595 weakening process within the overriding plate during dual inward dipping subduction.

596 Subduction can generate convective mantle flow that includes both poloidal and toroidal  
597 components. The 2D models tested here neglect the effects of toroidal flow and the third dimension.  
598 This could amplify the magnitude of poloidal flow and its weakening effect applied within the  
599 overriding plate. Considering that poloidal component dominates over toroidal component during  
600 non-steady state subduction (Funiciello et al., 2004), and it is the poloidal cell that provides the  
601 relevant traction driving the deformation within the overriding plate (Király et al., 2017; Schellart  
602 and Moresi, 2013), the lack of toroidal flow would only have limited impact on the progressive  
603 weakening presented.

604 In this research, to obtain the designed wide range of plate thicknesses (67 km to 141 km), the half-  
605 space cooling model is used instead of the plate model. Plate thickness in plate model flattens  
606 when the plate age is greater than ~80 Ma, thus it is not ideal for investigating the effect of thick  
607 plates investigated here. We note that there is still great uncertainty in terms of how oceanic  
608 lithosphere thickness evolves with ocean floor's age. Half-space cooling model was initially  
609 proposed to explain the age dependency of bathymetry and heat flow observed. However, this  
610 model does not fit these observations as well when the age of the oceanic plate is over 80 Ma. The  
611 plate model fits the flattening bathymetry and heat flow in older oceanic plates, but at the cost of  
612 applying an artificial temperature boundary condition at the bottom of lithosphere (Parsons and  
613 Sclater, 1977; Stein and Stein, 1992). Some question the existence of flattening seafloor  
614 bathymetry with age. There is research that indicates that excluding "anomalous oceanic crust",  
615 such as sea mountains and hotspots, from the bathymetry dataset can reduce the flattening  
616 behaviour and make a half-space cooling model fit well with plates over 80 Ma (Korenaga et al.,  
617 2021; Korenaga and Korenaga, 2008). Another hypothesis suggests that half-space cooling model

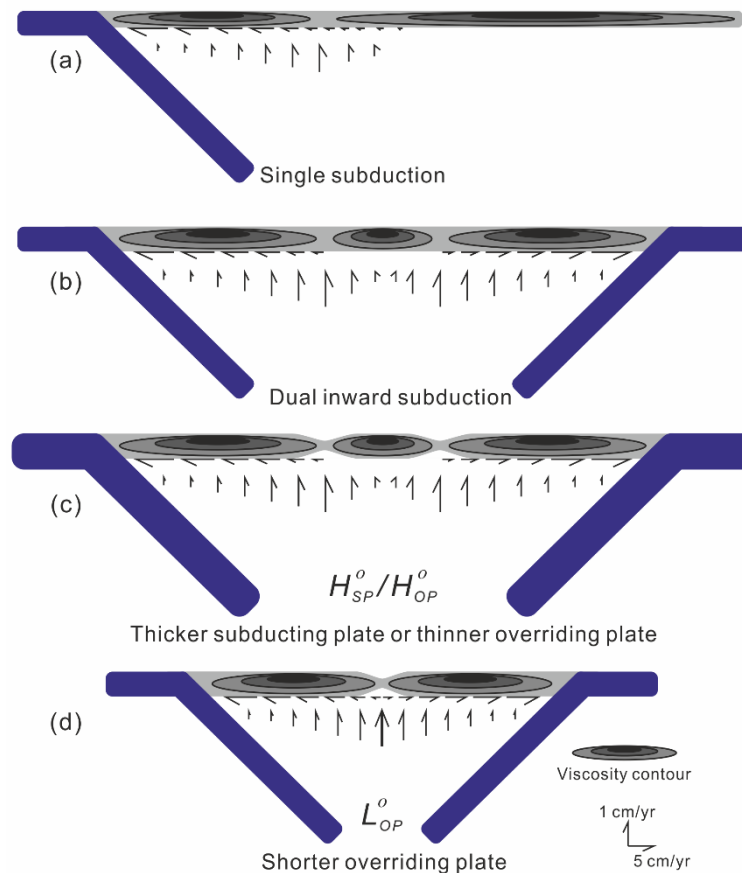
618 fits well with bathymetry along mantle flow lines instead of age trajectories in the Pacific (Adam and  
619 Vidal, 2010). The uncertainty regarding how oceanic lithosphere thickness evolves with ocean floor  
620 age, and the 2D nature of the models, requires the results of this study to be interpreted carefully  
621 before applying to Earth.

622 Bearing all the limits in mind, we cautiously compare our model predictions with observations in the  
623 North China Craton (NCC). Based on suture zone studies, the NCC may have experienced dual  
624 inward dipping subduction (Santosh, 2010; Windley et al., 2010). The Paleo-Asian Ocean subducts  
625 from the north of the craton, while to the southeast lies the subducting Pacific Plate. Surface wave  
626 tomography implies that the thickness of the overriding plate ( $H_{OP}^0$ ), i.e., the NCC, decreases from  
627 ~150 km in the western block to ~70 km in the eastern block (Huang et al., 2009). The distance  
628 between the trenches of two subducting plates ( $L_{OP}^0$ ) narrows beneath the eastern block. According  
629 to this work, we might suggest that the eastern block would suffer more weakening. This is  
630 consistent with the observation that rifting extension and magmatism intrusion, equivalent to  
631 weakening level 'IV', only develops in the eastern block, e.g., Bohai Bay Basin. So for now we only  
632 speculate that a dual subduction driven weakening process might have played a role in modifying  
633 the rheology and resulting in a variety of deformation patterns within the eastern block of the NCC,  
634 though to fully understand this would require further investigation utilising more advanced models,  
635 beyond the limits of this work.

#### 636 **4.4 Synoptic summary**

637 The thermo-mechanical modelling here provides a generic understanding of the progressive  
638 weakening developed within a varying rheology overriding plate during dual inward dipping

639 subduction. To summarize, dual inward dipping subduction holds a stronger tendency to weaken  
 640 the overriding plate compared with single sided subduction. This is achieved by creating a fixed  
 641 trailing boundary condition for the overriding plate and generating a stronger poloidal return flow  
 642 underlying the overriding plate (Figure 15). The stronger poloidal mantle flow is exhibited as a  
 643 higher horizontal velocity gradient and higher maximum magnitude of upwelling component  
 644 underlying the overriding plate. It can also initiate higher degree of viscosity reduction, strain  
 645 localisation and lithosphere thinning or even spreading extension within the overriding plate.  
 646 Besides, a dual inward dipping subduction system with thinner and shorter overriding plate, and  
 647 thicker subducting plate is likely to induce higher degree of viscosity reduction within the overriding  
 648 plate (Figure 15, b-d).



649  
 650 Figure 15. Synoptic comparison of different model setup's role in affecting the necking behaviour developed within the overriding  
 651 plate. (a) Single sided subduction (e.g., Garel et al., 2014). (b) Dual inward dipping subduction. (c) Thickness of the subducting plate  
 652 or overriding plate ( $H_{SP}^o, H_{OP}^o$ ). (d) Length of the overriding plate ( $L_{OP}^o$ ).

## 5. Conclusion

These 2-D thermo-mechanical numerical models demonstrate that dual inward dipping subduction can generate progressive weakening by lowering viscosity within the overriding plate on a ~10 Myr time scale. Three variables are investigated to understand what controls the maximum degree of weakening. It shows that the initial length ( $L_{OP}^0$ ) and thickness ( $H_{OP}^0$ ) of the overriding plate are negatively correlated with the maximum degree of weakening. While the initial thickness of the subducting plate ( $H_{SP}^0$ ) positively relates to the maximum weakening level. The progressive weakening can result in a variety of irreversible stretching states ranging from 1) little or no lithosphere thinning and extension, to 2) limited thermal lithosphere thinning, and 3) localised rifting followed by spreading extension.

Comparing with single sided subduction, dual inward dipping subduction shows that it can reduce the magnitude of viscosity to a lower level within the overriding plate. Two aspects are analysed. On the one hand, a dual inward dipping subduction set-up effectively creates a dynamic fixed boundary condition for the middle (overriding) plate. This inhibits the mobility of the plate and helps promote localised strain deformation to accommodate the slab rollback tendency on both sides. On the other hand, when the initial length of the overriding plate is short enough ( $L_{OP}^0 \leq 800 \text{ km}$ ), dual inward dipping subduction can form a united upwelling mantle flow which interacts with the bottom of overriding plate and generates a stronger viscosity perturbation within it than single sided subduction models. As a result, dual inward dipping subduction can induce higher degrees of extension in the overriding plate compared with single sided subduction.

To understand the viscosity weakening mechanism in the necking area of the overriding plate, the



674 dependency of viscosity on strain rate, temperature and pressure are evaluated separately. Three  
675 positive feedback weakening cycles are recognised, among which the strain rate weakening  
676 mechanism plays the dominant role in lowering the viscosity of the overriding plate throughout the  
677 simulation. Strain rate weakening is a precondition to initiate thermal weakening and lithosphere  
678 thinning, both of which only reinforce the feedback weakening loop during the rifting extension  
679 period.

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