Deep-water cycling and the Magmatic History of the Earth

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This is a preprint of the manuscript currently in review at Science Advances. Subsequent versions of this manuscript may contain different content. Should you have any questions or feedback, please feel free to contact any of the authors.

⁸ Abstract

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Earth is a magmatically active planet. Magmatism connects Earth's interior to its atmosphere, hy-9 drosphere, and biosphere through cycling of volatiles, greenhouse gasses, and nutrients [18]. Earth's 10 magmatic history is intertwined with its thermal and tectonic evolution. How magmatism has evolved 11 and been maintained in the face of planetary cooling remains an open question. We address this question 12 using data-constrained deep-water cycling and thermal history models. We track magmatic potential 13 using a homologous temperature: the ratio of upper mantle to melting temperatures. After an initial 14 decline, homologous temperature is buffered at a nearly constant value from roughly 2.5-2.0 Ga to the 15 present day. Melt buffering reflects two factors: 1) The dependence of melting temperature on water 16 content [21], and 2) The dependence of mantle viscosity on temperature and water content [15, 31, 27]. 17 The latter allows solid Earth evolution to self-regulate via feedbacks that keep mantle viscosity at a near 18 constant value. Self-regulation occurs even though the mantle remains far from thermal equilibrium, 19 consistent with heat flow data. The added feedback from water-dependent melting allows magmatism 20 to be co-buffered over geological time. This indicates that coupled thermal and water cycling feedbacks 21 have maintained melting on Earth and associated volcanic/magmatic activity. Magmatic self-regulation 22 affects not only the lifetime of geological activity on Earth but also, to the degree that planetary life 23 connects to volcanic activity, the maintenance of conditions favorable for life. 24

25 Teaser

The cycling of water between Earth's surface and interior maintains volcanic activity and buffers longterm thermal and tectonic evolution.

28 Introduction

It has long been noted that the temperature of Earth's shallow mantle is remarkably close to the melting 29 temperature of rock [39]. That proximity (Figure 1a) is critical to Earth's current volcanic activity. It 30 could be a coincidence, in which case our planet's magmatic/volcanic activity will decline as it continues 31 to cool. More likely, it could reflect some form of feedback(s) that allow the Earth's cooling and magmatic 32 potential to be co-buffered. Magmatic/volcanic regulation over geologic time has not generally been 33 considered. However, data constraints on melt fraction from continental arcs indicate that it is a viable 34 hypothesis (Figure 1b). The melting data from Brenhin Keller and Schoene [2] are consistent with the 35 the idea that Earth experienced a decline in magmatic potential since early in its history, leveling off 36 to quasi-steady state around 2.0 to 2.5 billion years ago. A quasi-steady state evolution in the face 37 of continued planetary cooling requires some form of regulating feedback(s). This connects magmatic 38 history to another long standing issue: Is Earth's evolution self-regulated? 39



Figure 1: (a)The position of the Earths mean oceanic geotherm (red) relative to the dry (green) and wet solidus (light blue) and liquidus (dark blue) of the upper mantle. The geotherm is calculated following the procedure in the Methods and assuming a present day heat flow of 35 TW and potential temperature of 1350 o C. The melting curves represent the dry solidus [14] and wet solidus [21] assuming 2.5 OMs in the mantle - roughly the median value found in our analysis (Figure 2c). (b) Melt fraction from continental arcs over geologic history. [2, 22]

⁴⁰ A class of planetary cooling models do allow for thermal self-regulation [40, 8, 34]. A feedback ⁴¹ between temperature and planetary cooling rate, facilitated by the temperature-dependence of mantle ⁴² viscosity, allows the internal temperature of Earth to track the decay of radiogenic heat sources. This ⁴³ maintains the ratio of heat generation to heat loss, termed the Urey ratio (Ur), near unity. However, ⁴⁴ this regulation mechanism is not connected to magmatic evolution [39]. More problematic, such models ⁴⁵ cannot account for updated constraints on Earth's cooling history [4, 24]. In particular, data constraints ⁴⁶ place Ur between 0.2 and 0.5 [19], i.e., heat loss and heat generation appear to be far from equilibrium.

Self-regulation relates to the characteristic reactance time of the solid planet [25, 38]. Reactance time 47 characterizes system response to deviations from a secular trend. The secular trend is associated with 48 the time scale over which the driving energy source for mantle convection changes due to radiogenic 49 decay. Cooling histories that allow for thermal self-regulation have short reactance times relative to the 50 decay time. Short thermal reactance times cannot lead to low Ur values, as they damp large deviations 51 from thermal equilibrium. This, in turn, has been used to argue that mantle convection is not self-52 regulated, which has implications not only for understanding our own planet's evolution, but also for 53 comparative planetology [25]. Although this argument is robust for thermal self-regulation, it does not 54 rule out self-regulation altogether. 55

The ability of a planet to self-regulate depends on a relationship between the vigor of mantle convection, as characterized by the mantle Rayleigh number (Ra), and convective heat flux (Nu). That relationship is given by

$$Nu \sim Ra^{\beta}$$
 (1)

59 where

$$Ra = \frac{\rho g \alpha \Delta T Z^3}{\kappa \eta} \tag{2}$$

and ρ is density, α is thermal expansivity, q is the acceleration due to gravity, ΔT is the superadiabatic 60 driving temperature, Z is the thickness of the convecting layer, κ is the thermal diffusivity and η is the 61 mantle viscosity. Models that allow for thermal self-regulation invoke a strong relationship between Nu62 and Ra [40]. That is, β values near the high-end limit of 1/3 [34]. Physically, this means that mantle 63 viscosity is the dominant resistance to tectonic plate overturn. Conceptually, the regulating feedback 64 works as follows: If fluctuations cause heat flux to become low relative to internal heat generation then 65 the mantle will heat up, viscosity will decrease, and heat flux will increase (due to increased tectonic 66 plate overturn associated with lower viscous resistance). The feedback operates on a short time scale 67 relative to secular radiogenic heat source decay. As a result, interior cooling evolves along a series of 68 quasi-equilibrium steps [8]. This is equivalent to Ur remaining near unity. Models with $\beta \leq 0$ can 69 match Ur constraints as they have long reactance times that allow the Earth to remain far from thermal 70

equilibrium [4, 24, 25]. Low or negative β indicates that the dominant resistance to plate motion does not come from mantle viscosity, but instead from the strength of plates and/or plate margins. This connects self-regulation to the balance of plate tectonic forces. That balance is not agreed upon and it is critical to developing a dynamic theory of plate tectonics [6].

Although classic thermal histories focused on thermal-regulation, the critical assumption at their core 75 is viscosity-regulation. That is, changes in viscosity dominate changes in the Earth's Rayleigh number 76 and, over time scales shorter than secular decay times, viscosity, and by association the Rayleigh number, 77 can be approximated as remaining constant. This is a critical assumption in using $Nu \sim Ra^{\beta}$ scaling 78 relationships to begin with, as they are based on theory, experiments, and/or numerical simulations carried out under constant Ra values [32]. If viscosity depends only on temperature, then a lack of 80 thermal-regulation rules out self-regulation. If that is not the case then self-regulation remains viable. 81 The dependence of mantle viscosity on water opens this possibility [28, 27]. It also allows for potential 82 co-regulation of mantle melting, as water content affects the melting temperature of rock [21]. 83

The first generation of thermal history models that considered the role of water predicted Ur values 84 greater than one [17] or comparable to classic models [29]. The former enforced a net loss of water from 85 the Earth's interior. The latter assumed that Ur should be 0.8 and, as such, calibrated free parameters 86 to keep mantle water content nearly constant. Crowley et al. [7] elegantly showed that a larger range of 87 behavior is possible if the system allows for imbalances in mantle dewatering (D) and rewatering (R). 88 Mantle dewatering occurs at mid-ocean ridges. The rate of mantle water loss depends on the relative 89 positioning of the solidus and geotherm. Mantle rewatering occurs at subduction zones, where descending 90 slabs carry some of their bound water into the mantle. How much water the slab can carry scales with 91 its thickness, which will increase as the mantle cools. If mantle viscosity depends on temperature (T)92 and mantle water content (χ) , then the time rate of change of mantle viscosity can be written as 93

$$\frac{d\eta}{dt} = \frac{\partial\eta}{\partial T}\frac{dT}{dt} + \frac{\partial\eta}{\partial\chi}\frac{d\chi}{dt}.$$
(3)

94 Conservation of energy leads to

$$\frac{dT}{dt} = \frac{1}{\rho C_p V} (H - Q_s) \tag{4}$$

where C_p is specific heat, V is mantle volume, H is mantle heat production, and Q_s is surface heat flow.

96 Conservation of mantle water content leads to

$$\frac{d\chi}{dt} = \frac{1}{\rho V} (R - D). \tag{5}$$

⁹⁷ Following the assumption that viscosity remains statistically steady, relative to the time scale over which

⁹⁸ significant changes occur in internal heat generation, leads to an estimate for the Urey ratio given by

$$Ur \approx 1 - \frac{\eta_{\chi}}{\eta_T} \frac{C_p}{Q_s} (R - D), \tag{6}$$

⁹⁹ where $\eta_{\chi} = \frac{\partial \eta}{\partial \chi}$ and $\eta_T = \frac{\partial \eta}{\partial T}$. If *R* exceeds *D*, then the Earth can be out of thermal equilibrium and low ¹⁰⁰ values of *Ur* are viable without requiring a weak, or negative, relationship between surface heat loss and ¹⁰¹ *Ra*. The analysis of Crowley et al. [7] is significant in motivating our work, as it re-opens the possibility ¹⁰² of planetary self-regulation. It did not, however, show that the Earth followed a self-regulated path, ¹⁰³ nor did it address magmatic evolution. In what follows we will do so using data-constrained thermal ¹⁰⁴ evolution models that allow for water cycling.

105 **Results**

Thermal history models have multiple free parameters and initial conditions. This can require millions 106 of model paths to map parameter space, with the vast majority of paths falling outside of observational 107 constraints [38, 36]. The problem can be bridled via data assimilation. Here we develop and employ 108 a novel data assimilation method applied to coupled thermal history and deep-water cycling models. 109 The method directly builds in data constrained thermal history trajectories over geologic time (a full 110 overview can be found in the Methods). The trajectories are constrained to match, within uncertainty, 111 petrological data [13, 5, 11]. Figure 2a shows the subset of trajectories (> 250) that met a goodness of 112 fit criteria (see Methods). The method also assimilates constraints on the present day Urey ratio. We 113 varied the Ur between 0.2 and 0.5 [19]. Variable β values are allowed for to test models with different 114 resisting forces to tectonic plate motions. For each thermal trajectory we randomly sampled one-hundred 115 different combinations of Ur and β within the assigned bounds and inverted for mantle water content. 116 This involved converting a forward model of coupled thermal and water history [37] into an inverse 117 model. Present day surface water content was constrained to be one ocean mass equivalent (OM) and 118 present day mantle viscosity was required to fall between 10^{19} and 10^{22} Pa s. With these constraints, 119 the evolution of mantle and surface water content was determined throughout Earth's history. This 120 procedure produced 10,000 mantle water evolution paths. 121

Figure 2b shows the relative density of successful $Ur - \beta$ space. Successful models preferentially gathered towards the lower Ur bound of Jaupart et al. [19]. Successful trajectories also required approximately $\beta \ge 0.2$. Figure 2c shows mantle water evolution. Model and data uncertainties demand that outputs be calculated, and plotted, as probability distributions, versus a single preferred path. The median of the distribution is depicted as a thick, black line. The darker region encompassing the median



Figure 2: Thermal trajectories consistent with Earth data (a) used for obtaining inversion results (b-d). (b) successful $Ur - \beta$ parameter space colored by relative point density with higher values meaning the density of points is larger. (c) Distribution of mantle water content and (d) mantle viscosity shown as distributions about their median value. The dark gray highlights values falling between the upper and lower quartiles and the lighter gray constraining the maximal and minimal limits.

is bounded by the upper and lower quartiles. The lighter regions extend from these quartiles to one 127 and half times the interquartile range. The distribution shows that successful models experienced an 128 early period of net mantle dewatering followed by net rewatering. The change occurred between two 129 and three billion years ago. The timing aligns with the findings of Parai and Mukhopadhyay [33] and 130 Seales and Lenardic [37]. Dong et al. [9] suggested a net rewatering over Earth's history by estimating 131 the mantle water capacitance. This, however, defines an upper limit within some uncertainty. We know 132 of no physical reasoning demanding that the mantle remain at this limit, and the majority of our results 133 fall within or below their uncertainties. Figure 2d shows the evolution of mantle viscosity from successful 134 models. In the absence of water, an expectation would be a monotonically increasing viscosity due to 135 mantle cooling. However, successful models show an increase in mantle viscosity for roughly the first half 136

of Earth's history followed by a milder decline. The rollover coincides with the change from net mantle
dewatering to rewatering. Physically, this corresponds to a switch from hot and dry subduction to cold
and wet subduction that cycles larger volumes of water into the mantle.



Figure 3: Measure of mantle self-regulation and co-regulation of mantle melting. (a) Inversion results showing *Ra* falling within a relatively narrow range throughout Earth's history. (b) Inversion results showing recent regulation of Earth's Homologous temperature. (c) Inversion results showing melt zone thickness. (d) Inversion results for melt fraction showing a decay following by a level off near present day. Each of the figures show results as distributions about their median value. The darker color highlights values falling between the upper and lower quartiles and the lighter color constraining the maximal and minimal limits.

The mild change of viscosity shown in Figure 2d leads to a similar trend for the mantle Rayleigh number, a measure of convective vigor. Figure 3a plots model Ra evolution. The mild change in Ra, in the face of a significant decline of internal radiogenic heating, is indicative of a self-regulated mantle evolution. In the absence of deep-water cycling, mantle cooling would lead to a a decrease in Ra. A flat, and potentially increasing, Ra trend is consistent with observationally based inferences from passive margins that plate speeds have not been decreasing over geologic time and could, within data uncertainty, even be increasing [1]. It is also consistent with the conjecture, based on observational
constraints on water transport beneath Japan arcs, that deep-water cycling could stabilize and prolong
mantle convection and the associated geological activity of the Earth [16].

Another measure of self-regulation, beyond Ra, is the homologous temperature (T_H) . We define T_H as the ratio of two depth-dependent profiles: the mantle geotherm and the wet solidus. Figure 1a shows these profiles in black and blue, respectively. As the two profiles change with depth, we define T_H at the maximum distance between the two curves (see Methods). In Figure 1a this point occurs at the change in slope of the geotherm, which is the base of the thermal lithosphere. The greater the thermal distance between the solidus and geotherm, the greater the value of T_H . When T_H drops below unity, melting ceases.

Figure 3b shows how T_H evolves for successful models. The decrease over the first few billion years 156 coincides with net mantle dewatering (Figure 2c). Decreasing T_H is associated with melt zone thinning 157 (Figure 3c). The change from net mantle dewatering to rewatering changes the behavior of T_H . The 158 flattening of the slope around 2 Ga in Figure 3b indicates that the thermal distance between the solidus 159 and geotherm remains nearly constant. Melt zone thickness also remains constant within ± 10 km (Figure 160 3c). This indicates that melt fraction can remain relatively constant over the same time period. Figure 161 3d shows that we indeed find a higher melt fraction early in Earth's history followed by a self-regulated 162 period towards present. The onset of self-regulation is consistent with geochemical constraints on a switch 163 from net mantle dewatering to rewatering [33]. It has been argued that this timing is also coincident 164 with a change from dominantly mafic to felsic continental composition, which led to a rise of atmospheric 165 oxygen [26, 10]. This, in turn, is consistent with the onset of cold and wet subduction, which leads to 166 melt regulation, also driving a switch toward the formation of felsic volcanism. 167

One might assume that an initial drop in T_H over the first 2 billion years of evolution would be 168 due to rapid initial mantle cooling [2, 22]. However data constraints show that over this time, mantle 169 cooling is mild, if at all, and accelerates subsequently (Figure 2a). This may run counter to intuition, 170 but it is critical to Earth's present-day Urey ratio. A low Ur indicates that, at present, mantle heat 171 flow is high relative to internal heat generation (i.e., the mantle is far from thermal equilibrium). This 172 requires a period of relatively low mantle heat flow in the Earth's past to retain heat such that it is then 173 available to supply elevated present day heat flow. Our successful models allow for this, while at the same 174 time maintaining a strong relationship between Ra and convective heat flux via a switch from mantle 175 dewatering, and associated mild cooling, to net mantle rewatering and an associated increased cooling 176 rate. Over the accelerated cooling phase, thermal and water cycling feedbacks lead to a self-regulation 177 of mantle melt potential as expressed by T_H (Figure 3b). 178

The trends of Figure 3 cannot extend indefinitely as interior cooling will eventually lead to T_H 179 dropping below unity. Exactly when this occurs depends on the future path of mantle temperature and 180 water content. Given that the solidus depends on water content, the self-regulation mechanisms mapped 181 by our models can delay melt shutdown relative to a dry planet or a planet that does not allow for 182 two way water cycling. In principal, we could extend our models forward in time. The results would, 183 however, be deceptive as we would be taking a data assimilation method outside of data constraints. This 184 leads to increasing uncertainty the further a projection is taken outside of the data [23]. The constraints 185 our models give on current conditions (e.g., mantle temperature, water content, Ur, β) could be used 186 as initial conditions and parameter constraints on forward models that are subject to a full uncertainty 187 quantification [38, 36] to provide probability densities for the timing of melt shut down. That type of 188 analysis would also need to consider the potential of cooling induced shifts in tectonic modes from plate 189 tectonics to a single plate planet. That goes beyond the intent and scope of this paper (i.e., to investigate 190 the hypothesis that mantle melting was self-regulated over the Earth's evolution to the present day). 191



Figure 4: An example of how fluctuations within Earth's mantle convection and plate tectonic system can affect the mantle potential temperature (a), water content (b) and homologous temperature (c).

Results thus far have shown the evolution of mean trends, together with uncertainties. Self-regulation 192 does not, however, require that planetary variables remain on slowly varying mean paths. Fluctuations 193 can occur but negative feedbacks tend to bring the system back toward a mean trend. The Earth's 194 thermal-tectonic system allows for fluctuations due to, for example, the chaotic nature of mantle con-195 vection, changes in plate-dimensions, and the amalgamation/dispersal of super-continents. These fluc-196 tuations can lead to variations in deep-water cycling [20]. Fluctuations could also occur as a result 197 of variations in the time scale of mixing water into the mantle [3]. Our methodology can deal with 198 these possibilities. An example can demonstrate the effects of including fluctuations into our analysis by 199 comparing smooth to fluctuating thermal paths (Figure 4a). The particular form of fluctuations is an 200 example only. Figures 4b and 4c show how thermal fluctuations effect water cycling and melt potential, 201 respectively. The system maintains a self-regulated evolution but it does so in a statistical sense. This 202

is consistent with the data of Keller and Schoene [22], which show fluctuations in melt fraction about a slowly varying mean trend over the last 2 billion years (Figure 1b). In principal, one could build in direct data constraints on, for example, fluctuations in mantle potential temperature [41] and/or mean plate subduction age [20]. That goes beyond our scope of demonstrating that self-regulation is robust in the face of thermal-tectonic fluctuations.

208 Discussion

Data-constrained models of Earth's thermal history indicate that coupled deep-water and thermal cycles 209 can lead to a self-regulated mode of mantle convection with an associated self-regulation of the Earth's 210 magmatic potential. In the more than five decades since the advent of a mobilist, plate-tectonic view 211 of Earth dynamics, the notion that the solid-Earth's strong dependence of viscosity upon temperature 212 should buffer variations in mantle internal temperature against the decay of secular radiogenic heat 213 sources has dominated much work on thermal evolution of the mantle. Recently, that possibility has 214 been questioned based on the recognition that the low value of the present-day Urey ratio is inconsistent 215 with thermal self-regulation. However, when we incorporate the effects of mantle volatile concentration 216 on melting, and hence viscosity, we find a broad and plausible range of models that are compatible with a 217 more general form of self-regulation. Models that operate in that mode of self-regulation are compatible 218 with constraints on the internal temperature, volatile content, viscosity, and magmatic history of the 219 Earth, as well as with low values for Ur. They also imply that the dominant resistance to the motion 220 of tectonic plates comes from mantle viscosity. Within uncertainty, the strength of plates and/or plate 221 margins can play a non-trivial, if not dominant, role (Figure 2b). Critically, successful models imply a 222 balance of resisting forces that is consistent with more detailed models of subduction zone dynamics [12]. 223

Fundamentally, partial melting in Earth's upper mantle (asthenosphere), due to the presence of 224 volatiles, mode locks the mantle toward higher (nearer wet solidus) interior temperatures, and hence 225 higher heat flow and lower Ur, relative to a planet that might otherwise have interior temperatures 226 that more closely track the secular decrease in internal heat sources. This conclusion is likely to have 227 important implications for Earth's plate tectonic style of mantle convection, in that partial melting in the 228 asthenosphere profoundly influences the existence and behavior of plates and plate motions - indeed sound 229 arguments can be made that the long-term persistence of plate tectonics on Earth requires the persistence 230 of a partially-molten uppermost mantle, which in turn is necessary in order for the melt-related self-231 regulation mechanism we have explored to be effective. We further suggest that exploration of both 232 constraints for and models of mantle dewatering and rewatering (related primarily to volatile processing 233 at ridges and subduction zones) should shed further light on mantle evolution and self-regulation. 234

²³⁵ Materials and Methods

²³⁶ Assimilating data into parameterized thermal history models

The average mantle temperature changes with time (\dot{T}_m) according to the balance of heat produced within (H) and lost from (Q) the mantle:

$$\rho V c_p \dot{T}_m = H - Q \tag{7}$$

where V and c_p are the volume and heat capacity of the mantle, respectively [35]. The amount of heat produced by the decay of radiogenic elements within the mantle scales as

$$H = Vh_i exp(-\lambda t) \tag{8}$$

where h_i is the initial heat generation rate, λ is the decay constant, and t is time. The total amount of heat lost by convective cooling is

$$Q = Aq_m \tag{9}$$

where A is the surface area of the convecting mantle and q_m the convective heat flux. Non-dimensional heat flux (Nu) scales with the Rayleigh number (Ra), a measure of convective vigor, according to

$$Nu = \frac{q_m}{q_{cond}} = \left(\frac{Ra}{Ra_c}\right)^{\beta} \tag{10}$$

where q_{cond} is the amount of heat lost were it transferred solely by conduction through the entire layer, *Ra_c* is the critical Rayleigh number and β is a scaling exponent. The parameter β varies between models that make different assumptions as to the dominant forces resisting tectonic plate motion (see Seales and Lenardic [36] for a fuller discussion of what different β values mean for mantle convection). Fourier's law states that

$$q_{cond} = k \frac{\Delta T}{Z} \tag{11}$$

where k is the thermal conductivity of the mantle, Z is the depth of the convecting layer, and ΔT is the temperature difference driving convection. The latter is the difference between the surface temperature (T_s) and the average mantle temperature. Combining Equations 10 and 11 and rearranging, the convective heat flux is

$$q_m = k \frac{\Delta T}{Z} \left(\frac{Ra}{Ra_c}\right)^{\beta} \tag{12}$$

 $_{254}$ where Ra is

$$Ra = \frac{\rho g \alpha \Delta T Z^3}{\kappa \eta} \tag{13}$$

and α is the mantle thermal expansivity, κ is the mantle thermal diffusivity and η is the mantle viscosity. Viscosity depends on temperature and water content according to

$$\eta = \eta_o A_{cre}^{-1} [exp(c_0 + c_1 ln\chi_m + c_2 ln^2 \chi_m + c_3 ln^3 \chi_m)]^{-r} exp\left(\frac{E}{RT_m}\right)$$
(14)

where η_o is a scaling constant, c_1 , c_2 and c_3 are empirically determined constants [27], r is the water fugacity exponent, A_{cre} is a material constant, E is the activation energy for creep and R is the universal gas constant. In Equation 14, χ_m has units $H/10^6$ SI.

²⁶⁰ Combining Equations 7 to 13, we find that the change in mantle temperature evolves according to

$$\dot{T}_m = \frac{1}{\rho c_p} \left[\sum_{i=1}^n h_i exp\left(-\lambda_i t\right) - \frac{A}{V} \frac{k\Delta T}{D} \left(\frac{\rho g \alpha \Delta T D^3}{R a_c \kappa \eta}\right)^{\beta} \right]$$
(15)

Rearranging to isolate mantle viscosity, Equation 15 becomes

$$\eta = \frac{Ra_c\kappa}{\rho g\alpha\Delta TD^3} \left[\frac{V}{A} \frac{D}{k\Delta T} \left(\sum_{i=1}^n h_i exp\left(-\lambda_i t\right) - \rho c_p \dot{T}_m \right) \right]^{-\frac{1}{\beta}}$$
(16)

Equations 14 and 16 have η isolated. As such, we can use these equations to estimate χ_m . We use 262 Herzberg et al. [13] and Condie et al. [5] as constraints on T_m . Viable thermal paths based on those T_m 263 constraints (Section) provide constraints on the time derivative of mantle temperature (\dot{T}_m) . The Urey 264 ratio, defined as Ur = H/Q, serves as a data constraint. Given a present day estimate of Q, we can 265 calculate present day H. Substituting this value of H into Equation 8, we can rearrange and solve for 266 h_i , which will determine the rate of radiogenic heating for that model. Given the parameters in Table 1 267 and the constraints laid out here, χ_m remains the only unknown in Equations 14 and 16. We initially 268 estimate the mantle water content and then iteratively adjust this value until Equations 14 and 16 are 269 within some tolerance (ϵ) of each other. We verified the inversion results against the outputs of forward 270 models. The global maximum inversion error remained less than one percent and the average inversion 271 error remained below 0.01 percent over the modelled time domain. 272

²⁷³ Constructing Thermal Trajectories

The method detailed above requires a thermal trajectory as input. One can imagine many trajecto-274 ries satisfying the uncertainties in estimated mantle potential temperature (Figure 2a). As such, we 275 constructed a number of data constrained thermal trajectories, each of which passed through strategic 276 control points (P_i) defined by the coordinates (t_i, T_i) , with time t_i in billions of years before present and 277 mantle potential temperature T_i in ^oC. The control points P_o and P_f define the initial and present day 278 temperatures, respectively. We required each thermal trajectory pass through at least one intermediate 279 control point P_{m1} , which coincides with the rollover in the Herzberg et al. [13] and the change in slope of 280 Condie et al. [5]. Table 1 lists the uncertainties we considered for each control point. We drew random 281 samples from uniform distributions defined by these bounds. These samples served as the starting point 282 of our thermal trajectory. If the sampling resulted in $T_{m1} > T_o$, we defined the thermal trajectory using 283 the quadratic 284

$$T(t) = \alpha_1 t^2 + \alpha_2 t + \alpha_3. \tag{17}$$

We determined the constants α_i by using the control points P_o , P_{m1} and P_f to form a system of three equations with three unknowns. If sampling resulted in $T_{m1} < T_o$, we defined the thermal trajectory using the cubic

$$T(t) = \alpha_1 t^3 + \alpha_2 t^2 + \alpha_3 t + \alpha_4.$$
(18)

Solving for α_i required a system of equations based on four control points. To account for this, we introduced P_{m2} such that $t_{m2} = t_{m1} - \tau_{mt}$ and $T_{m2} = T_{m2} - \tau_{mT}$. Here τ_{mt} and τ_{mT} represent offset times and temperatures. These allow for flattening of the thermal trajectory after an initial temperature decline, which can occur when water and thermal cycles effect mantle viscosity [37].

We required that each thermal trajectory fit the data of Herzberg et al. [13] and Condie et al. [5] within some measure of goodness. We used a reduced chi-squared statistic, the chi-square (χ^2) per degree of freedom (ν) . We adopt χ^2 as traditionally defined:

$$\chi^{2} = \sum_{t} \frac{\left[D(t) - M(t)\right]^{2}}{\sigma(t)}.$$
(19)

This cumulatively measures the error $(\sigma(t))$ normalized difference between the data (D(t)) and modeled thermal trajectory (M(t)). For measuring the goodness of fit we included all data points from both data sets. This gave us a total of 38 data points (N_d) . The definition for degrees of freedom is: $\nu = N_d - N_\alpha + N_P$ given the number of parameters (N_α) and control points (N_P) . We only kept thermal trajectories that had $\chi^2/\nu <= 1$. Using this method, we found a median accepted value of 0.98. As this is nearly unity, so the thermal paths approximate the data error variance without over-fitting. To mimic a fluctuating mantle temperature, we constructed fluctuations (T_f) that followed the form of an exponentially damped sine wave, which is of the form

$$T_f(t) = A_f e^{-\lambda_f t} \sin\left(\frac{2\pi}{P_f}t\right)$$
(20)

where A_f is the amplitude of the sine wave, λ_f is the decay constant, P_f is the period and t is time, in 303 billion of years. We set A_f to one percent of the initial mantle potential temperature, λ_f to 0.22 Gyr^{-1} 304 and P_f to 1 Gyr. We then superimposed T_f on top of a path defined as above. We still enforced the 305 condition that $\chi^2/\nu \ll 1$. We do no pretend to know what path fluctuations follow. They likely follow 306 something much more complicated than presented here. However, we believe that the qualitative form of 307 our findings will hold. An exact description of the fluctuations is beyond the scope of this paper. How to 308 account for them in forward modeling was covered by Seales et al. [38]. Regardless, choosing any other 309 path would find the same qualitative conclusions presented herein. 310

311 Homologous Temperature

Our analysis relied on the geotherm consisting of two elements: a shallow conductive profile through the mantle lithosphere and a convective profile beneath it. For a given value of T_p and χ_{H_2O} , we can calculate q_m according to Equation 12. We can rearrange Fourier's Law to give the conductive profile according to

$$T_{cond}(z) = \frac{q_m}{k_m} z + T_s.$$
⁽²¹⁾

The convective profile is the mantle adiabat. We used a linearized version of Mckenzie and Bickle [30] above to convert from T_m to T_p . We can also use this adiabat to construct the convective element of the geotherm according to

$$T_{conv}(z) = T_m \left[1 - \frac{g\alpha}{c_p} \left(\frac{R_p - R_c}{2} - z \right) \right]$$
(22)

³¹⁹ The conductive and convective profiles intersect at the base of the lithosphere (H_L) :

$$H_L = \left[T_m - T_s - \frac{T_m g\alpha}{2c_p} \left(R_p - R_c\right)\right] \left(\frac{q_m}{k_m} - \frac{T_m g\alpha}{c_p}\right)^{-1}$$
(23)

In our analysis we compared the geotherm to the solidus. We used the dry solidus of Hirschmann [14]. We accounted for water suppressing the dry solidus using the parameterization of Katz et al. [21]:

$$T_{sol}(z) = A_1 + A_2 * \rho g z + A_3 (\rho g z)^2 - \Delta T + 273$$
(24)

$$\Delta T(\chi_{H_2O}) = K \chi^{\gamma}_{H_2O} \tag{25}$$

where the temperature is given in Kelvin and A_1 , A_2 , A_3 , K and γ are calibration constants.

Generally a homologous temperature is defined as the ratio of actual temperature to melting temperature. We follow this convention and define the homologous temperature (T_H) as the ratio of the geotherm temperature to the solidus temperature. Both temperatures vary with depth, so we chose the depth that maximized the thermal distance between them - the base of the lithosphere:

$$T_H = \frac{T_{cond} \left(H_L\right)}{T_{sol} \left(H_L\right)} \tag{26}$$

We can insert Z_L into Equation 21 to get the actual temperature and into Equation 24 to obtain the melting temperature.

330 Calculating Melt Zone Thickness

Melt zone thickness (H_M) is defined as the vertical difference between the two points where the geotherm and solidus intersect. The shallower point defines the top of the melt zone (H_T) . Equating Equations 21 and 21 and gathering like therms gives the quadratic

$$A_T z^2 + B_T z + C_T = 0 (27)$$

$$A_T = A_3 \left(\rho g\right)^2 \tag{28}$$

$$B_T = A_2 \rho g - \frac{q_m}{k_m} \tag{29}$$

$$C_T = A_1 - K_{H_2O}^{\gamma} + 273 - T_s \tag{30}$$

This quadratic has two roots, one above the surface (unphysical) and one at depth. The one at depth defines (H_T) and is given by

$$H_T = \frac{-B_T - \sqrt{B_T^2 - 4A_T C_T}}{2A_T}$$
(31)

We found the base of the melt zone (H_B) by equating the convective profile (Equation 21) with the solidus (Equation 24). Grouping like terms and gathering gives the quadratic

$$A_B z^2 + B_B z + C_B = 0 (32)$$

$$A_B = A_3 \left(\rho g\right)^2 \tag{33}$$

$$B_B = A_2 \rho g - \frac{g\alpha}{c_p} T_m \tag{34}$$

$$C_B = A_1 - K_{H_2O}^{\gamma} + 273 - T_m \left[1 - \frac{g\alpha}{c_p} \left(\frac{R_p - R_c}{2} \right) \right]$$
(35)

This quadratic has two roots. The physical root is the shallower of the two. The deeper is an artifact of the chosen solidus structure rather than anything physical. We define the base of the melt zone (H_B) , then, as

$$H_B = \frac{-B_B + \sqrt{B_B^2 - 4A_B C_B}}{2A_B}$$
(36)

Data constrain the solidus to a depth of 300 km. We set this as a hard maximum limit for H_B .

337 Calculating Melt Fraction

The distance between the the solidus and geotherm determines the amount of melt produced. The distance between the solidus and geotherm varies between the top and bottom of the melt zone. As such, we calculate the melt fraction (ϕ) at each depth according to

$$\phi = \frac{T(z) - T_{sol}(z)}{T_{liq}(z) - T_{sol}(z)}$$
(37)

assuming that the melt fraction increases linearly between the solidus and liquidus (T_{liq}) . We integrate Equation 37 over the entire melt zone and normalize by melt zone thickness to obtain an estimate of average melt fraction $(\bar{\phi})$.

Parameter	Description	Value	Unit
ρ	Mantle density	3000	kg/m^3
c_p	Mantle heat capacity	1400	J/(kg K)
k	Mantle thermal conductivity	4.2	$\dot{W}/(m K)$
α	Mantle thermal expansivity	$3x10^{-5}$	K^{-1}
κ	Mantle thermal diffusivity	10^{-6}	m^2/s
λ	Radiogenic decay constant	$3.4x10^{-10}$	yr^{-1}
Q_i	Present day mantle heat flow	$35x10^{12}$	W
Ur	Present day Urey ratio	0.2 - 0.5	-
β	Convective scaling exponent	0.15 - 0.33	-
Ra_c	Critical Rayleigh number	1100	-
T_s	Surface Temperature	300	Κ
g	Acceleration due to gravity	9.8	m/s^2
R_p	Radius of Earth's surface	6371000	m
$\hat{R_c}$	Radius of Earth's core	3471000	m
Z	Thickness of convecting layer	2900000	m
η_o	Viscosity constant	$1.7x10^{17}$	Pa s
A_{cre}	Material constant	90	$MPa^{-r/s}$
C_0	Empirically determined viscosity constant	-7.98	-
C_1	Empirically determined viscosity constant	4.35	-
C_2	Empirically determined viscosity constant	-0.57	-
C_3	Empirically determined viscosity constant	0.03	-
\mathbf{E}	Creep activation energy	$4.8x10^{5}$	$\rm J/mol$
\mathbf{R}	Universal gas constant	8.314	J/mol
r	Water fugacity exponent	1.2	-
T_o	Starting mantle temperature	1400-1800	^{o}C
T_{f}	Present day mantle temperature	1300-1400	^{o}C
T_{m1}	Rollover temperature	1450 - 1650	^{o}C
$ au_{mT}$	Rollover temperature	-5-25	^{o}C
t_o	Initial model time	0	Gyr
t_f	Final model time	4.5	Gyr
t_{m1}	Intermediate model time	1.25 - 2.5	Gyr
$ au_{mt}$	Intermediate model time	0.75 - 0.25	Gyr
A_f	Temperature fluctuation amplitude	1%	^{o}C
λ_f	Temperature fluctuation decay constant	1/4.5	$\rm Gyr^{-1}$
P_f	Temperature fluctuation frequency	1	$\rm Gyr^{-1}$
A_1	Anhydrous solidus calibration constant	1085.7	^{o}C
A_2	Anhydrous solidus calibration constant	132.9	^{o}C GPa ⁻¹
A_3	Anhydrous solidus calibration constant	-5.1	^{o}C GPa $^{-2}$
Κ	Hydrous solidus calibration constant	43	$^{o}C \text{ wt}\%^{-\gamma}$
γ	Hydrous solidus scaling exponent	0.75	-
ϵ	χ convergence tolerance	10^{-8}	$H/10^6$ Si
OM	Present day ocean mass equivalent	$1.39x10^{2}1$	$_{\rm kg}$

Table 1: Model parameters and values

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