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**Effect of Pressure and Stress cycles on fluid flow in hydraulically-fractured, low-
porosity, anisotropic sandstone**

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Abstract

Hydraulic fracture in deep rock masses is used across a variety of disciplines, from
unconventional oil and gas to geothermal exploration. The overall efficiency of this process
requires not only knowledge of the fracture mechanics of the rocks, but also how the newly
generated fractures influence macro-scale pore connectivity. We here use cylindrical samples
of Crab Orchard sandstone (90mm length and 36mm diameter), drilled with a central conduit
of 9.6mm diameter, to simulate hydraulic fracture. Results show that the anisotropy (mm-scale
cross-bedding orientation) affects breakdown pressure, and subsequent fluid flow. In

25 experiments with samples cored parallel to bedding, breakdown pressures of 11.3MPa,
26 27.7MPa and 40.5MPa are recorded at initial confining pressures at injection of 5MPa, 11MPa
27 and 16MPa respectively. An increase in confining pressure (from 5 MPa to 26 MPa) after the
28 initial fracture event results in a flow rate decrease from 1.67 mL/min to 0.043 mL/min. For
29 samples cored perpendicular to bedding, breakdown pressure of 15.4MPa, 27.4MPa and
30 34.2MPa were recorded at initial confining pressure at injection of 5MPa, 11MPa and 16MPa
31 respectively. As confining pressure increases from 5 MPa to 26 MPa, flow rate through the
32 newly generated fracture decreases from 0.043 mL/min to 0.0073 mL/min. We note that fluid
33 flow recovers during a confining pressure “re-set” and that the ability of flow to recover is
34 strongly dependent on sample anisotropy and initial confining pressure at injection.

35

36 **Keywords:** flow rate; confining pressure; tensile fracturing; acoustic emissions; anisotropy;
37 tight sandstone;

38

39 **List of symbols**

P_b	Breakdown pressure	k_w	Wall permeability
S_h	Minor horizontal stress	k_{wc}	Critical wall permeability
S_H	Major horizontal stress		
σ_T	Tensile strength		
P_0	Pore pressure		
α	Biot poroelastic coefficient		
ν	Poisson’s ratio		
σ_{ax}	Axial pressure		

40

41 **Declarations**

42 **Conflict of Interest**

43 The authors declare no conflict of interest.

44

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51

52 **Author Contributions**

53 Peter Ibemesi wrote the manuscript and performed the experiments. Philip Benson designed
54 the experiments, and supervised data curation and analysis.

55

56 **Introduction**

57 Hydraulic fracturing is an important natural phenomenon in the earth subsurface, exhibited
58 across a range of processes including magma intrusion (Rubin 1993; Tuffen and Dingwell,
59 2005) and mineral emplacement (Richards, 2003). In the engineered environment, hydraulic
60 fracturing has been used in the petroleum industry since the mid-1950's (Tueffel, 1981) to
61 enhance oil and gas production from tight reservoirs (characterized by low permeability, often
62 in the microDary range of $10\text{-}100\text{'s} \times 10^{-18} \text{ m}^2$). To date, hydraulic fracture has become a
63 common, albeit controversial, practice to improve oil and gas recovery (Gillard et al., 2010;
64 Kennedy et al., 2012; Wang et al., 2014). These new technologies have led some nations (for
65 example the USA) to become significant producers of natural gas (Wang et al., 2014) as

66 previously low permeable formations were fractured. However, the process is not without
67 controversy, and additionally has been developed over years in a somewhat ‘ad-hoc’ or trial-
68 and-error manner. This has resulted in varying degrees of overall success due to the
69 complexities of reservoirs that contain significant structural, sedimentological and mechanical
70 heterogeneities. Together, these features alter the relationship between the tensile fracture
71 mechanics needed to generate new fractures for fluid movement, as balanced against the
72 fundamental rock physical properties and local stress field (Martin and Chandler 1993; Sone,
73 2013; Gehne & Benson 2017; 2019).

74

75 The objective of hydraulic fracture is to increase the rock permeability through induced fracture
76 in the rock mass. This is usually achieved by pumping a pore fluid (with or without additional
77 propping agents to keep new fractures mechanically open) into a wellbore at a sufficiently high
78 pressure to fracture the surrounding rock mass in tension. This requires a sufficiently high fluid
79 flow rate to overcome the background permeability and radial fluid flow, which is a function
80 of the permeability of the unfractured rock mass (Fazio et al., 2020). If the fluid injection is
81 higher than the natural fluid dispersion rate, pressure builds up inside the borehole which leads
82 to fracture, including reopening and further propagation of existing fractures when the *in-situ*
83 tensile rock strength is exceeded. The resultant hydraulic fracture extends until the formation
84 loss is greater than the pumping rate (Reinicke et al., 2010).

85

86 Different approaches have been applied to study the pressure (P_b) at which the rock first yields
87 (fractures), known as the breakdown pressure. The simple linear elastic approach considers a
88 defect-free, impermeable and non-porous rock matrix around the borehole (Hubbert and Willis,
89 1972; Jaeger et al., 2009) via

90
$$P_b = 3S_h - S_H + \sigma_T \quad [\text{Eq. 1}]$$

91 where σ_T is the tensile strength (an inherent property of the rock), and S_h and S_H are the
 92 minimum and maximum horizontal stresses respectively.

93

94 However, the above approach represents an ‘end-member’ case as no rock is truly
 95 impermeable: all rocks contain pores and fractures, and when saturated with pore fluid exerting
 96 a fluid pressure P_0 , [Eq. 1] above is modified to:

97

98
$$P_b = 3S_h - S_H + \sigma_T - P_0 \quad [\text{Eq. 2}]$$

99

100 The expression above [Eq. 2] may be further modified by adding poroelastic effects which
 101 account for the rock being both porous and permeable (e.g. Haimson and Fairhurst, 1969;
 102 Jaeger et al., 2009):

103

104
$$P_b = \frac{3S_h - S_H + \sigma_T}{2 - \alpha \frac{1 - 2\nu}{1 - \nu}} - P_0 \quad [\text{Eq. 3}]$$

105

106 where (α) is the Biot poroelastic coefficient and ν is the Poisson’s ratio.

107

108 A final, minor, modification considers the role of rock matrix permeability in hydraulic
 109 fracturing. In Fazio et al., 2020, [Eq. 3] is assumed to be only valid under conditions whereby
 110 the bulk rock permeability (k_w) at the interface between the injection fluids and the wall is
 111 below a critical permeability (k_{wc}). Adding these boundary conditions yields:

112

113
$$P_b = \frac{3S_h - S_H + \sigma_T}{2 - \alpha \frac{1 - 2\nu}{1 - \nu}} - P_0 \quad \text{for } k_w < k_{wc} \quad [\text{Eq. 4}]$$

114

115 An accurate characterisation of the fluid flow through the bulk rock mass is key to understanding
 116 reservoir properties (Tan et al., 2018). However, measuring permeability remains challenging
 117 due to its sensitivity to heterogeneity. This is further complicated by the strong anisotropy
 118 found in typical formations used for unconventional hydrocarbons (such as mudrock, shale and
 119 crossbedded/tight sandstone). Nonetheless, numerous studies using wellbore tools and core
 120 plugs have attempted to link the fracture process to permeability enhancement via numerical
 121 models (Ma et al., 2016). To calibrate these models and in-situ data, laboratory measurements
 122 of flow through fractures under controlled conditions have used images of the post-test fracture
 123 aperture (e.g. Stanchits, 2014) or morphology of the post-test shear fracture planes (Kranz et
 124 al., 1979; Bernier et al., 2004; Gillard et al., 2010, Zhang 2015), as a function of flow rate or
 125 permeability. Collectively, these experiments have provided useful data on fracture behavior,
 126 but have tended to focus on mudrocks (shale) over other rock types.

127

128 Here we report a new laboratory study designed to measure the fluid-flow rate through tensile
 129 fractures in a tight anisotropic sandstone (Crab Orchard), with respect to anisotropy. Fractures
 130 are freshly generated in the tensile mode using water, via the method of Gehne and Benson
 131 (2019) before fluid-flow data are taken, up to simulated reservoir conditions to 2.5km. Fracture
 132 aperture data are then imaged post-test using X-ray Computed Tomography (CT) to analyze
 133 the final fracture aperture to measured flow rate. Our laboratory set-up is designed to eliminate
 134 the possibility of altering the fracture properties when extracting the fractured sample as flow
 135 rate data is taken immediately after fracture, and so allows better comparison between the fluid-
 136 driven tensile fracture processes (and the associated flow enhancement), to reservoir

137 conditions. Finally, we link these fracture mechanics and fluid flow through the fracture to the
138 accompanying Acoustic Emission (AE, the laboratory proxy to tectonic seismicity) as an
139 additional guide to the timing and development of fracture properties with respect to the mm-
140 scale crossbedding.

141

142 **Experimental methods**

143 **Sample Material and preparation**

144 Crab Orchard sandstone (COS) has a relatively low permeability and porosity for a sandstone
145 of approximately 10^{-18} m² and 5% respectively (Benson et al., 2003). The rock, from the
146 Cumberland Plateau, Tennessee (USA), is a fine grained cross bedded fluvial sandstone, with
147 sub-hedral to sub-rounded grains of about 0.25mm size. It consists predominantly of quartz
148 (>80%) with little feldspar and lithic fragments cemented by sericitic clay (Benson et al., 2006).
149 This material exhibits a high anisotropy (up to 20% P-wave velocity anisotropy and up to 100%
150 permeability anisotropy), and has a tensile strength calculated through the Brazilian Disc
151 (Ulusay, 2014) of 9.8 MPa perpendicular to bedding and 8.6 MPa parallel to bedding.

152

153 Cylindrical samples of 36mm diameter and approximately 90 mm in length were cored from
154 blocks with a long axis either parallel (defined as the x-orientation) or normal (z-orientation)
155 to the visible bedding plane (figure 1). Samples were then water-saturated by immersing under
156 water using a vacuum pump to extract void space air for a minimum of 24 hours (for ‘saturated’
157 hydraulic fracture experiments). Each core sample had a central axially-drilled conduit of
158 10.5mm diameter through the length of the sample, generating a ‘thick-walled’ cylinder (figure
159 1A) arrangement that can be accommodated into a standard triaxial apparatus. The samples are
160 inserted into a 3D printed liner (figure 1C) that is, in turn, is encapsulated in a rubber jacked

161 (figure 1B). This allows water from generated tensile fractures to be received, regardless of
162 their radial orientation, by a water outlet port (Gehne and Benson, 2019).

163

164 The sample setup is completed by fitting two steel waterguides (figure 1D) into the central
165 conduit. These waterguides direct pressurized fluid into a sealed section of the drilled conduit
166 (using O-rings), allowing fluid to apply a uniform pressure to the inner surface of the sealed
167 section, leading to tensile fracture in the central section from which water flow is received via
168 the outlet port, measured using a volurometer.

169

170

FIGURE 1

171

172 **Hydraulic fracture procedure and protocol**

173 Sample assemblies were mounted within a conventional servo-controlled triaxial machine
174 capable of confining pressures up to 100 MPa (Figure 2). Four 100 MPa servo-controlled
175 pumps provide: (i), axial pressure through a piston-mounted pressure intensifier to provide a
176 maximum of 680 MPa axial stress, (ii), confining pressure up to 100 MPa. Both these pumps
177 use heat transfer oil (Julabo Thermal HS) as pressurizing medium. Two pore pumps
178 independently provide fluid pressure to (iii), the bottom of the sample (via the lower water-
179 guide) and (iv), receive water through the generated tensile fracture and exiting via the fluid
180 outlet. Pumps (iii) and (iv) are set to maintain a set pressure gradient and thus establish steady
181 fluid flow through the freshly generated tensile fracture. The final flow rate value is only taken
182 when the flow between the two pumps have achieved a steady, but equal and opposite rate to
183 signify no leaks in the system and to allow transients to settle (approximately 2 minutes).

184

185 Mechanical data (stress, strain, fluid pressures) is recorded at both a ‘low’ recording rate of 1
186 sample/second and high sampling rates (10k samples/s), for axial strain and fluid injection
187 pressure only, to record fast changing transients (Gehne et al., 2019). In addition, a suite of 11
188 acoustic emission sensors, fitted to ports in the engineered rubber jacket (Fig. 1B), received
189 Acoustic Emission (AE) data to monitor fracture speed and progress. The AE signals are first
190 amplified by 60 dB and then received on an ASC “Richter” AE recorder at 10 MHz. For
191 accurate seismo-mechanical data synchronisation during the dynamic tensile fracture, the fluid
192 injection pressure output is split across both mechanical and a single channel of the AE data
193 acquisition systems through an amplified circuit as described by Gehne (2018). This allows
194 data synchronization with an accuracy of ± 0.01 ms.

195

196 FIGURE 2

197

198 The experimental procedure spans three stages (Figure 3). Firstly, hydrostatic pressure is
199 established by increasing the confining pressure and the axial pressure concomitantly to attain
200 the target pressure, and a pre-fracture measurement of fluid flow is taken by setting a
201 differential pressure of 2 MPa between central conduit and the fluid outlet port. Secondly, pore
202 fluid injection was activated at a constant flow rate of 5mL/min resulting in an increasing
203 conduit pressure, until failure (hydraulic fracture) occurred (Figure 3). Evidence of fracture
204 development includes a sharp decrease in injection (pore) pressure, accompanied by a swarm
205 of AE. Thirdly, after tensile failure, a fluid pressure gradient (differential fluid pressure of 2
206 MPa) was re-established between the conduit pressure and the fluid outlet port to initiate a
207 steady state flow through the freshly generated tensile fracture(s). The volume of the two

208 pressure pumps were monitored independently; steady state flow is reached when the volume
209 change with time is equal and opposite for the two pumps, averaged across a 4-minute time
210 period and after an initial 2 minutes elapsed to allow transient effects to decay away. This
211 procedure was repeated as a function of confining pressure increase (and decrease) to
212 investigate the effect of confining pressure and pressure hysteresis on flow rate.

213

214

FIGURE 3

215

216

217 **Results**

218 Six experiments were conducted on COS at initial confining pressures (before injection) of 5
219 MPa, 11 MPa, and 16 MPa. At each pressure, a pair of samples were cored with long axis either
220 parallel or perpendicular to bedding. As detailed above, for each sample an initial fluid flow is
221 measured by setting a differential pore pressure (difference between conduit and outlet
222 pressure) and measuring at the upstream and downstream reservoir (Fig. 3). These initial flow
223 rate data are tabulated in Table 1.

224

225

TABLE 1

226

227 *Hydraulic fracture*

228 The hydraulic fracture stage of the experiment is initiated by injecting water into the sample at
229 a fixed flow rate of 5mL/min. Data from sample COSx-1 (5 MPa initial confining pressure,
230 core axis parallel to bedding) is shown in figure 4. As fluid was injected, a concomitant increase
231 in injection pressure is recorded. This continues until an experiment time of approximately
232 1276s where tensile fracture is recorded at an injection pressure (or breakdown pressure, P_b) of

233 11.29 MPa, accompanied by a swarm of AE which increases steadily from 1260s, reaching a
234 peak of 225 counts/s. After fracture, the injection pressure rapidly decreases to 2 MPa, and
235 cumulative AE reaches a steady value.

236

237 FIGURE 4

238

239 At 5 MPa confining pressure but with the sample axis perpendicular to bedding (sample COSz-
240 1), we see the injection pressure building until a breakdown pressure of 15.4 MPa (figure 5),
241 some 4 MPa higher than sample COSx-1. Again, after the hydro-fracture event injection
242 pressure decreases rapidly to approximately 2 MPa (figure 5). Relatively few AE events (and
243 rather sparsely distributed in time) were recorded during the time of fluid injection (2344s to
244 2366s), however a swarm of activity was recorded at the moment of fracture. The cumulative
245 AE counts increases rapidly at this point up to a peak of 4×10^4 counts at 2367s.

246

247 FIGURE 5

248

249 At 11 MPa and parallel to bedding (experiment COSx-2), breakdown occurs at an injection
250 pressure of 27.7 MPa (figure 6). Compared to COSx1, the injection fluid pressure dropped
251 abruptly to approximately 5 MPa and it is again accompanied with a swarm of AE at 2364s
252 (figure 6). The cumulative AE steadily increases from 4598s to 2×10^2 counts after
253 approximately 4630s, followed by a significant and rapid final increase at the moment of
254 fracture at 4634s and a peak of 10^5 counts.

255

256

FIGURE 6

257

258 Mechanical data for sample COSz-2 (11 MPa and perpendicular to bedding) is shown in figure
259 7. Data exhibits a similar trend in injection pressure as previously seen for sample COSz-1,
260 with a sharp decrease as tensile fracture is generated accompanied by a peak in AE events.
261 However, a breakdown in injection pressure of 27.3 MPa is recorded in COSz-2, which
262 decreases rapidly to approximately 6 MPa, again accompanied by a swarm of AE events which
263 decrease in counts over time until approximately 3540s. However, the trend of AE leading up
264 to failure is different, with no build-up in AE prior to the prominent swarm of activity failure
265 time, resulting in a large cumulative AE count of 1.2×10^6 counts at 3531s (sample failure).

266

267

FIGURE 7

268

269 At 16 MPa and parallel to bedding (experiment COSx-3), breakdown occurs at an injection
270 pressure of 40.4 MPa which decreases rapidly to approximately 15 MPa after fracture, again
271 accompanied with a swarm of AE (figure 8). Abundant AEs were recorded from approximately
272 4955s, rapidly increasing at the moment of breakdown pressure when compared with samples
273 COSx-1 and COSx-2 (fig.8). Cumulative AE count increases at 4956s to a peak of 7×10^5 at
274 4981s.

275

276

FIGURE 8

277

278 Finally, for sample COSz-3 (16 MPa and parallel to bedding), tensile fracture was recorded at
279 injection pressure of 33.9 MPa accompanied once again by a swarm of AE (figure 9). Notably,
280 the conduit pressure decreased slowly after fracture, only reaching 15.25 MPa after 30s had
281 elapsed. Similarly to previous experiments, abundant AEs were recorded with an increase in
282 cumulative AE count first registered at 6919s, but this time with a second significant increase
283 at 6940s to a peak of 2×10^4 counts (figure 9).

284

285 FIGURE 9

286

287 *Post-Fracture fluid flow*

288 With the tensile (radial) fracture established across samples at three different initial confining
289 pressures, and across two different orientations with respect to anisotropy, a set of fluid flow
290 measurements are made. Fluid flow is measured in cycles of increasing confining pressure,
291 followed by a 're-set' to the original confining pressure, followed by a second cycle of
292 increasing confining pressure. Figure 10 shows data from COSx-1 and COSz-1 (5 MPa initial
293 conditions). Here, an increase in confining pressure (from 5 MPa to 26 MPa) for COSx-1
294 results in flow rate decreasing from 1.67 mL/min to 0.043 mL/min respectively. During the re-
295 set of confining pressure from 26 MPa to 5 MPa, flow rate recovered only marginally,
296 increasing from 0.043 mL/min to 0.134 mL/min. The second cycle of confining pressure
297 increase gives a further reduction of flow rate from 0.134 mL/min to 0.028 mL/min, lower than
298 the minimum of the first cycle. Sample COSz-1 shows a decreasing flow rate from 0.6 mL/min
299 at 5 MPa confining pressure to 0.027 mL/min at 26 MPa confining pressure. During the 're-
300 set' of confining pressure from 26 MPa, flow rate recovered from 0.027 mL/min to 0.099

301 mL/min. The second cycle of confining pressure increase resulted to a further reduction in flow
302 rate from 0.099 mL/min to 0.014 mL/min.

303

304 **FIGURE 10**

305

306 For sample COSx-2 (11 MPa initial conditions), a general decreasing trend in flow rate was
307 measured for a confining pressure increase from 11 MPa to 31 MPa (Figure 11). In the first
308 cycle, the flow rate decreases from 0.043 mL/min to 0.0073 mL/min respectively. The
309 confining pressure re-set resulted in a flow rate recovery from 0.0073 mL/min to 0.014
310 mL/min. The second cycle of confining pressure increase generates a reduction in flow rate
311 from 0.014 mL/min to 0.0067 mL/min. Conversely, for COSz-2, the flow rate decreases from
312 0.0375 mL/min to 0.0042 mL/min at between 11 and 31 MPa confining pressure respectively.
313 Pressure is again re-set, resulting in a flow rate recovery from 0.0042 mL/min to 0.0105
314 mL/min. The second cycle of confining pressure increase gives a further reduction of flow rate
315 from 0.0105 mL/min to 0.0013 mL/min.

316

317 **FIGURE 11**

318

319 For sample COSx-3 (16 MPa initial conditions), flow rate decreases from 0.27 mL/min to 0.05
320 mL/min from 16 MPa to 31MPa respectively (figure 12). Confining pressure re-set results in a
321 marginal flow rate recovery from 0.05 mL/min to 0.09 mL/min. The second cycle of confining
322 pressure increase then results in a further decrease in the flow rate from 0.09 mL/min to 0.029
323 mL/min. Conversely, for sample COSz-3 (figure 12) flow decreases from 0.09 mL/min at 16
324 MPa confining pressure to 0.017 mL/min at 31 MPa. Confining pressure is again 're-set' from

325 31 MPa to 16 MPa resulting in almost no recovery (0.017 to 0.018 mL/min) followed by a final
326 confining pressure increase which resulted to a further decrease in the flow rate from 0.018
327 mL/min to 0.011 mL/min.

328

329

FIGURE 12

330

331 **Discussion**

332 Hydraulic fracturing has been established as a key process in both a natural environment (e.g.
333 magma intrusion, and mineralization) as well as the engineered geo-environment, most
334 frequently to develop hydraulic fractures in unconventional reservoirs (Guo et al., 2013; Gehne
335 and Benson, 2017; Tan et al., 2018; Gehne and Benson, 2019). The ultimate aim of these
336 methods is to generate conduits for fluid flow through tensile fracture and damage zone.
337 However, whilst there have been a large number of studies investigating the fluid flow and
338 permeability properties of highly anisotropic rocks such as shale (e.g.; Walsh, 1981; Benson et
339 al., 2005; Gehne & Benson, 2017), and studies investigating the fracture mechanics (e.g.
340 Hubbert and Willis, 1972; Zoback et al., 1977; Teufel and Clark, 1981; Rubin et al., 1993;
341 Reinicke et al., 2010), there are fewer that have combined these two elements into a single
342 experimental procedure (e.g. Fredd et al., 2001; Guo et al., 2013; Zhang et al., 2015). There
343 are also few studies investigating low porosity or ‘tight’ sandstone, compared to (say) shale.
344 This is important as the hydraulic properties of low porosity rocks is significantly modified by
345 both pressure and the presence of larger macro-fracture (Nara et al., 2011), and are often highly
346 anisotropic due to small scale crossbedding, such as in COS (e.g. Gehne and Benson, 2019).

347

348 Here, we have focused on hydraulic fracture in tight sandstone with fluid flow measurement
349 directly after this stage in order to assess fluid flow as a function of anisotropy across cycles of
350 confining pressure. This coupled process is particularly important when considering cyclical
351 extraction of fluids that, in turn, changes the effective pressure, such as in the charge/re-charge
352 cycles of geothermal extraction or unconventional hydrocarbon extraction. In our experiments,
353 we find an interplay between the inherent anisotropy of the fracturing materials, with samples
354 cored with long axis perpendicular having a higher breakdown pressure than those parallel to
355 bedding. In all cases, and irrespective of bedding, the cycles of effective pressure have a largely
356 irreversible effect on fluid flow, and with a larger proportionate decrease than in rocks without
357 a fracture network (Gehne and Benson, 2017). This is consistent with past studies, including
358 from large sample volumes (Guo et al., 2013; Tan et al., 2018). Hence, a better understanding
359 of micro-scale fracture is likely to be helpful in optimizing larger scale hydraulic fracture
360 design if the effects of both anisotropy and burial pressure (as a proxy for burial depth) may be
361 incorporated.

362

363

FIGURE 13

364

365

FIGURE 14

366

367 *Effect of Anisotropy*

368 Results from the mechanical data, backed up by AE data, show that bedding plane orientation
369 has a pronounced effect on the strength and energy release during tensile fracture. However,
370 these effects are more pronounced at low confining pressure (5 MPa) where we measure a

371 breakdown pressure of 11 MPa (parallel) and 15 MPa (perpendicular) (Fig. 4 & 5) and (Fig.
372 5). However, this effect rapidly decreases with increasing confining pressure. In every case,
373 breakdown is accompanied by a significant swarm in AE output, and for 5 MPa and 11 MPa
374 confining pressures, with higher cumulative AE counts in experiments conducted
375 perpendicular to bedding compared to parallel to bedding, suggesting these orientations release
376 more energy. However, this pattern is not seen in the data from 16 MPa (Fig. 8 and Fig. 9)
377 suggesting a higher tensile strength in rocks when the tensile stress is normal to bedding due
378 to a more complex fracture morphology, where the tensile fracture must cut through the rock
379 bedding planes (Gehne and Benson, 2019; Hu et al., 2017).

380 In addition to the cumulative AE counts, more pre-facture acoustic events are recorded in data
381 at 5 MPa (Fig 4 and Fig. 5) and in data parallel to bedding at 11 MPa (Fig. 6). We attribute this
382 effect to the lower effective pressure in these experiments promoting earlier fracture nucleation
383 compared to data from experiment perpendicular to bedding (Fig. 7) compared to the data from
384 the highest confining pressure of 16 MPa (Fig. 8 and 9) that suppress early hydrofracture
385 events. This is supported by fact that no AE data is recorded before 4955s and 6918s (Fig. 8
386 and 9 respectively).

387 Anisotropy provides the major influence on fluid flow, with samples cored parallel to the
388 bedding orientation recording a high fluid flow rate at a given confining pressure when
389 compared to the experiments with sample cored perpendicular to the bedding orientation. Our
390 data reveal an initial fluid flow anisotropy (the ratio of flow in samples fractured perpendicular
391 to parallel to bedding) of 0.4 at 5 MPa, 0.9 at 11 MPa, and 0.3 at 16 MPa, illustrating a very
392 low fluid flow anisotropy even at high effective pressures. This general result is consistent with
393 that obtained by Gehne and Benson (2017), which shows that fluid flow is significantly
394 influenced by bedding plane orientation. However, the fluid flow anisotropy as measured on
395 our tensile fracture samples is generally lower than the equivalent permeability anisotropy

396 measured in unfractured samples (Benson et al., 2005; Gehne, and Benson 2017) particularly
397 at high effective pressures. Our data compares to fluid flow (permeability) anisotropy of 16.5-
398 25% as reported for unfractured Crab Orchard sandstone at 5-30 MPa confining pressure
399 (Gehne and Benson, 2017).

400 To better understand the complexities of heterogeneity and fluid flow, we have collected X-
401 Ray Computed Tomography (XCT) data on each sample post-test (Figure 13). These images
402 were then segmented in Avizio to extract an approximate tensile fracture tortuosity with
403 bedding plane orientation (Fig. 14). Using this, we note that samples cored parallel to bedding
404 exhibit a slightly lower fracture thickness of about 35 microns (COSx-1; Fig. 14A), while
405 samples cored perpendicular to bedding have fracture thickness of about 45 microns (COSz-1;
406 Fig. 14B). However, we also note that the fluid flow data, both pre- and -post fracture, is likely
407 to follow a largely radial pathway, whereas the comparison to Gehne and Benson (2017) is to
408 a linear Darcy flow along the cylindrical sample. Hence, we present fluid flow in this study
409 rather than permeability. Also, our data suggests that the fracture geometry is influenced by the
410 bedding orientation (anisotropy) during injection. Whereas a single fracture tends to develop
411 in samples cored parallel and perpendicular to bedding at a low confining pressure (5MPa), at
412 elevated confining pressure (11MPa and 16MPa), two fractures tend to be formed (Figure 13).

413

414 *Effect of Confining Pressure*

415 The increase of initial confining pressure from 5 MPa, through 11 MPa, and to 16 MPa has the
416 overall effect of increasing the breakdown pressure respectively to 10, 27, and 40 MPa for
417 samples parallel to bedding, and to 15, 26, and 35 MPa perpendicular to bedding. This is
418 consistent with the findings of Jaeger et al. (2009) and Haimson and Fairhurst (1969) who
419 postulated that an increase in confining pressure increases the horizontal stresses and hence a

420 resultant increase in breakdown pressure as expressed in equation(s) 1-4. A key output when
421 considering fluid flow through newly generated tensile fracture is the pressure history on
422 fracture properties (a key control on the bulk fluid flow).

423 Previous data focusing on cyclical fluid flow on solid samples of COS have reported a
424 reduction of permeability in subsequent cycles of between approximately 66% to 70% (Gehne
425 & Benson, 2017). For fluid flow through a tensile fracture, as shown here, the equivalent
426 decrease per fluid flow cycles ranges from 92% (COSx-3) to 68% (COSx-2) to 95% (COSx-
427 1). This suggests that the addition of the tensile fracture increases the compliance of the rock,
428 and therefore makes the application of confining pressure more sensitive when measured in
429 terms fluid flow. Similar effects were also reported by Nara et al. (2011).

430 We also find that the hysteresis in fluid flow is more sensitive to the overall specimen
431 anisotropy (i.e. whether fluid flow is parallel to perpendicular to bedding) rather than the XCT-
432 measured fracture thickness. At each initial pressure, post fracture flow rate is lower in the z-
433 orientation samples (Fig. 1) compared to x-orientation despite larger fracture aperture (Fig. 14).
434 This suggests that these larger average apertures are generally more tortuous, resulting in a
435 lower flow rate, which is consistent with fracture in the z-orientation, or so-called divider
436 orientation, where the tensile fracture crosses multiple layers of bedding (Gehne et al., 2020).

437 As the elevated confining pressure is released and restored to its initial state at injection, the
438 fluid flow does tend to recover, but not to its initial value at injection. This phenomenon is
439 known as flow hysteresis and has been widely studied and reported (e.g. Gehne and Benson
440 2017). It is also likely that rocks with significant clay and fine crossbedding, such as this tight
441 sandstone, results in tensile fractures of low compliance, and therefore causing them to fail to
442 reopen during subsequent pressure cycles. This would also be manifested as an irreversible

443 decrease in the fracture aperture and therefore lower permeability (Walsh, 1981; Vinciguerra
444 et al., 2014).

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446

447 **Conclusions**

448 In this study we have investigated the influence of confining pressure and anisotropy on fluid
449 flow through tensile fracture under simulated in-situ pressures relevant to hydraulic fracture in
450 a low porosity (tight) sandstone (Crab Orchard). We find that a general increase trend in
451 breakdown pressure and cumulative acoustic emission when confining pressure increases,
452 which leads to an irreversible decrease in fluid flow through the tensile fracture when confining
453 pressure is cycled. In addition, breakdown pressure is higher in experiments with samples cored
454 parallel to bedding at a lower confining pressure (5MPa), this effect decreases at higher
455 confining pressure (11MPa and 16MPa) at injection. We conclude that anisotropy is a
456 significant contributing factor to both the fluid flow hysteresis effect and breakdown stress,
457 with the tortuosity a key factor rather than fracture aperture alone in describing fluid flow rate
458 through the fracture.

459

460 In general, the fluid flow is higher in experiments with samples cored parallel to bedding and
461 additionally has weaker recoverability when confining pressure is 're-set'. We observed two
462 stages of flow rate reduction during in the two cycles of confining pressure. The first cycle of
463 confining pressure is identified by a rapid decrease in flow rate (e.g. 97% for COSx-1 and 95%
464 for COSz-1) while the second cycle is characterized by a slow decrease in flow rate (e.g. 79%
465 for COSx-1 and 86% for COSz-1). We conclude that it is likely that a combination of
466 mechanisms operate, and must be considered in determining the overall permeability of tight

467 sandstone to regional stresses during burial and upliftment (expressed as confining pressure
468 cycles and ‘re-set’). This is not limited to tight sandstone but also a low permeability
469 anisotropic rock material such as shale and mudstone. Finally, we suggest that the open fracture
470 compliance is also important, particularly with regards to cyclical pressure and stress, which is
471 further complicated for rocks such as Crab Orchard that have significant clay content.

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Sample	Length (mm)	Diameter (mm)	Orientation	Pc (MPa)	Pre HF flow rate (mL/min)	Post HF flowrate (mL/mL)	Pb (MPa)
COSx_1	92.34	36.11	Parallel	5	0.036	1.67	11.29
COSz_1	92.15	36.10	Perpendicular	5	0.012	0.6	15.41
COSx_2	94.54	36.10	Parallel	11	0.012	0.043	27.70
COSz_2	90.71	36.12	Perpendicular	11	0.018	0.037	27.30
COSx_3	90.87	36.10	Parallel	16	0.024	0.127	40.47
COSz_3	90.24	36.10	Perpendicular	16	0.006	0.09	34.24

589

590 Table 1: Summary of experimental conditions and sample orientations / dimensions, Pc is confining pressure,
591 Pb is breakdown pressure (the fluid pressure at the moment of tensile fracture), Pre HF (Hydraulic fracture) flow
592 rate and Post HF (Hydraulic fracture) flow rate

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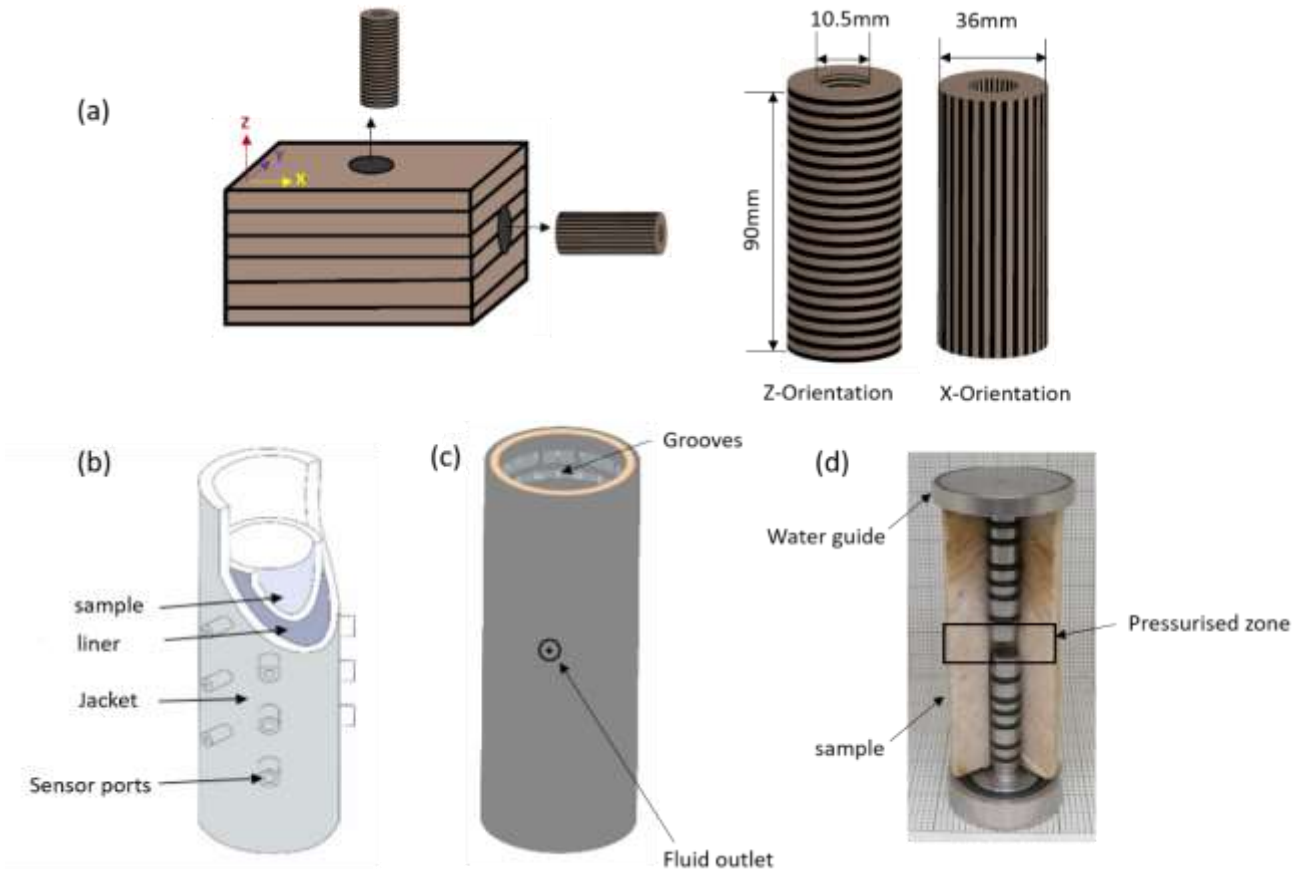
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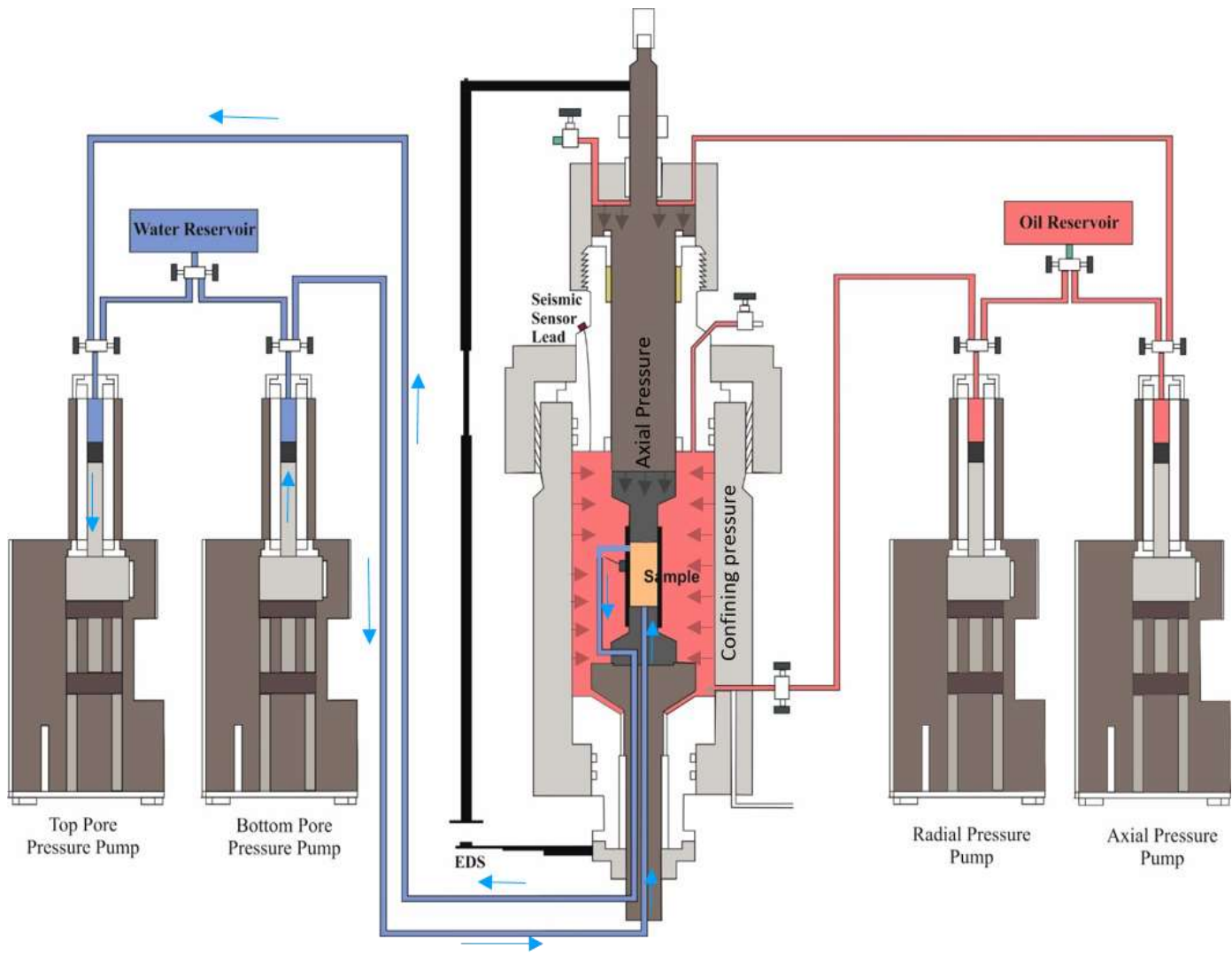
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Fig. 1 (a): Sample cored in Z and X orientations with respect to the visible mm-scale crossbedded sandstone. (b): Sample assembled in the liner and rubber jacket. (c): 3D printed water transport liner. (d): Cross section of sample with water guide showing the pressurized zone (modified after Gehne and Benson, 2019)

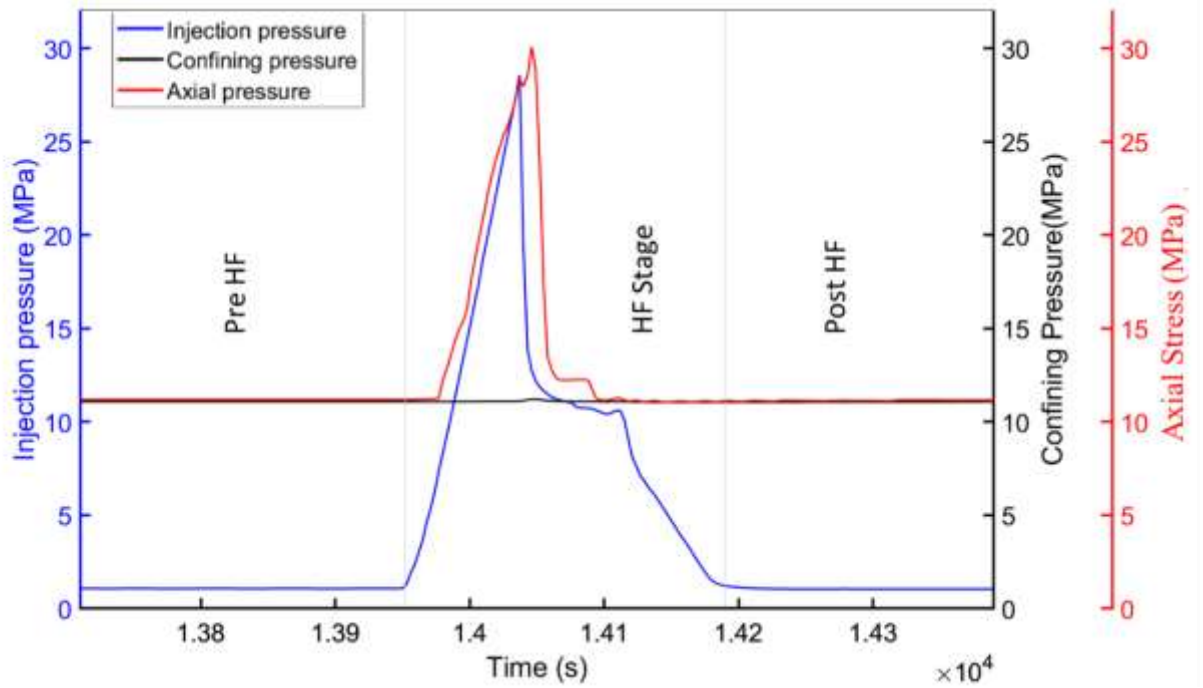


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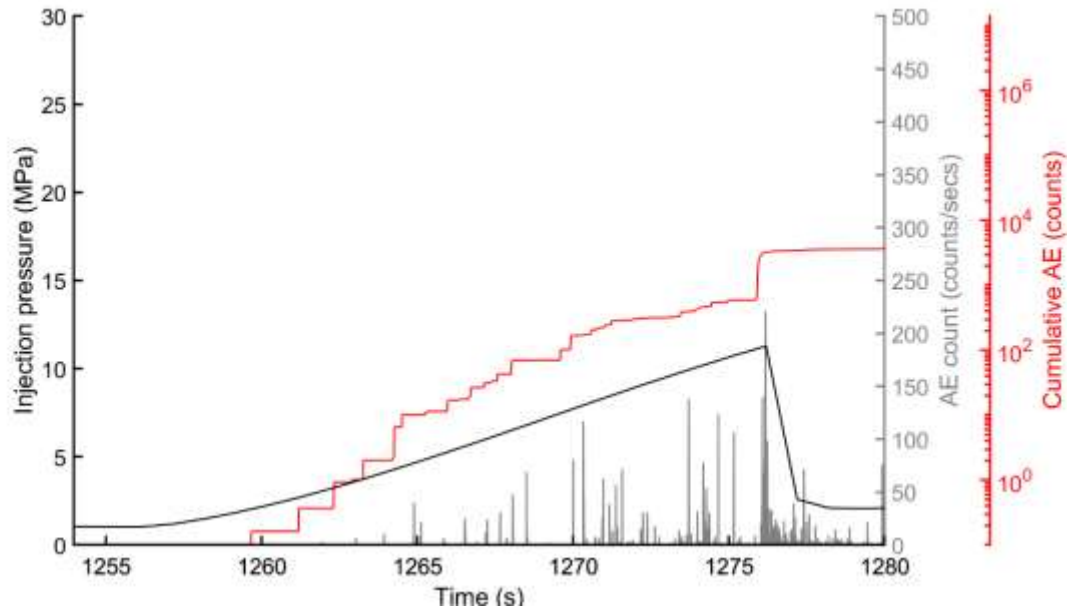
Fig. 2 Schematic of the triaxial apparatus and pump systems

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Fig 3 Overview plot of a typical experiment with injection pressure (blue), confining pressure (black) and axial stress (red) with time, showing the 3 experiment stages: (i) Pre-hydraulic fracture (pre HF) flow (after hydrostatic conditions are established); (ii) The hydraulic fracturing stage (HF): axial stress (σ_{ax}) is increased simultaneously with the injection (pore) pressure increase to maintain approximate hydrostatic conditions during fluid injection; (iii) Post hydraulic fracture (Post HF) flow (with hydrostatic conditions re-established)



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633 **Fig. 4** Mechanical properties and AE in COS during injection at 5MPa initial conditions. Injection pressure
 634 (grey continuous line) cumulative AEs (red line) and hit count (grey bar) for sample COSx-1 (parallel to
 635 bedding)

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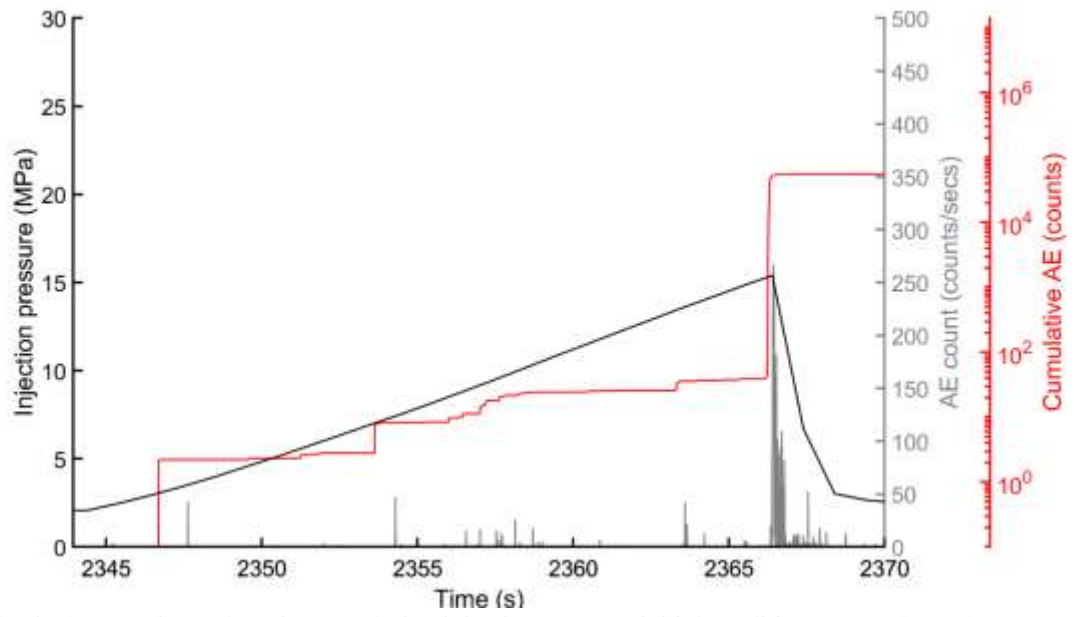
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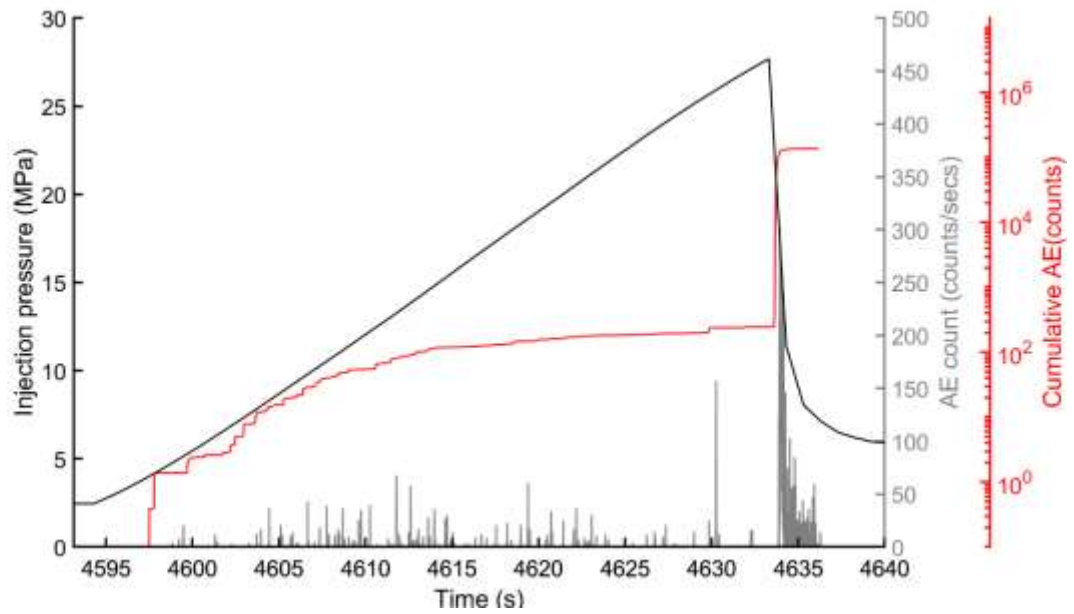
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Fig. 5 Mechanical properties and AE in COS during injection at 5MPa initial conditions. Data shown here are the injection pressure (black continuous line), cumulative AEs (red line) and hit count (grey bar) for sample COSz-1 (perpendicular to bedding)



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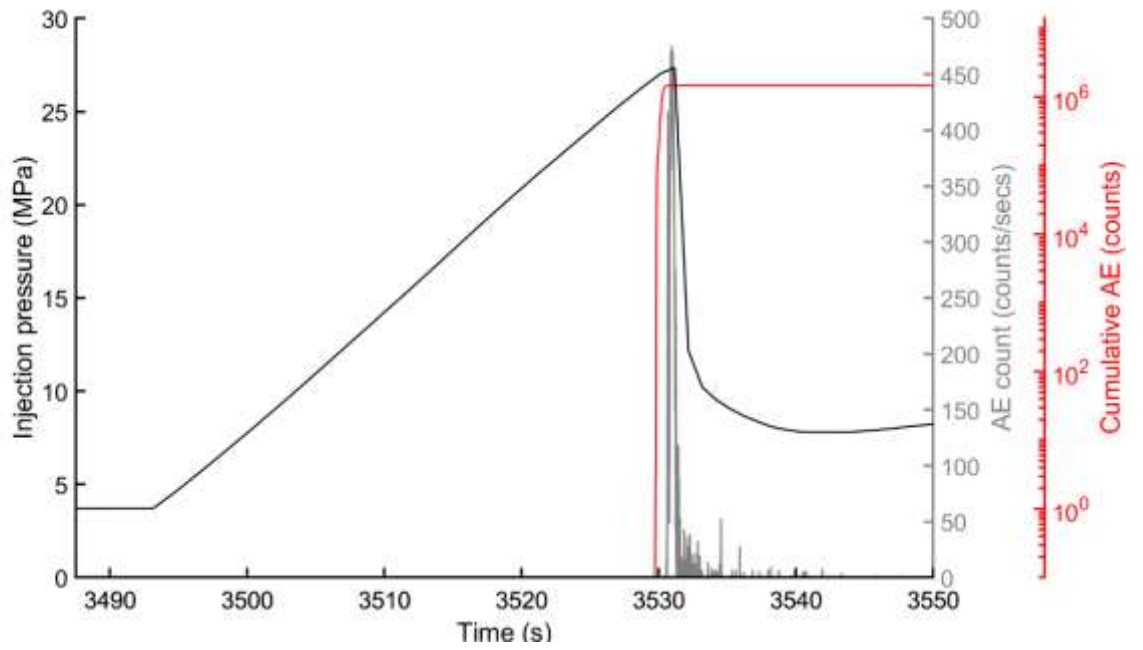
Fig. 6 Mechanical properties and AE in COS during injection at 11MPa initial conditions. Data shown here are the injection pressure (black continuous line), cumulative AEs (red line) and hit count (grey bar) for sample COSx-2(parallel to bedding)

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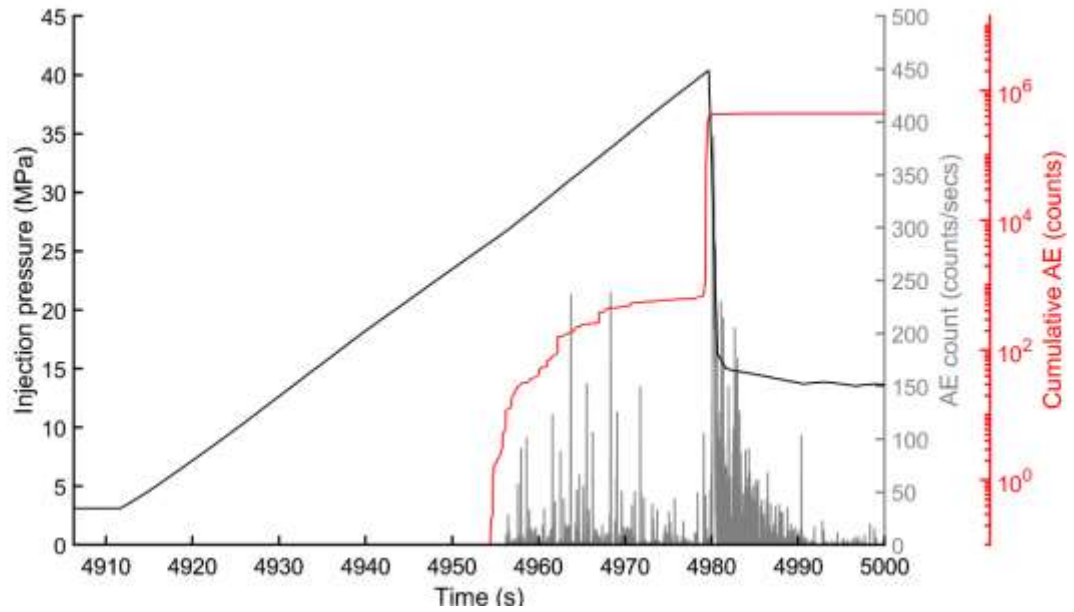
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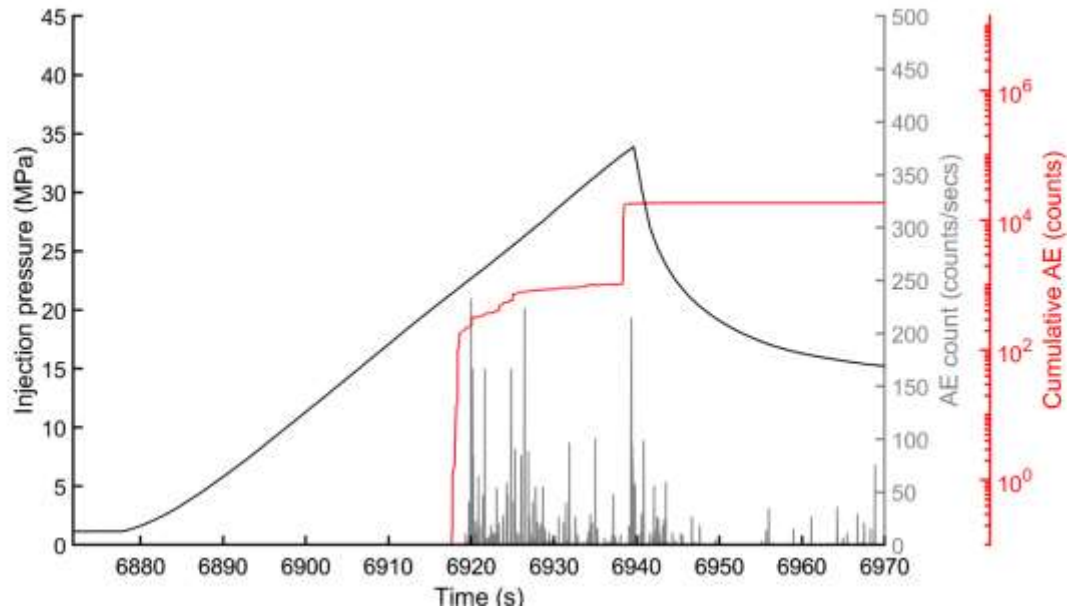
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Fig.7 Mechanical properties and AE in sample COSz-2 during injection at 11MPa initial conditions. Injection pressure (black continuous line), injected volume (blue line), cumulative AEs (red line) and hit count (grey bar)



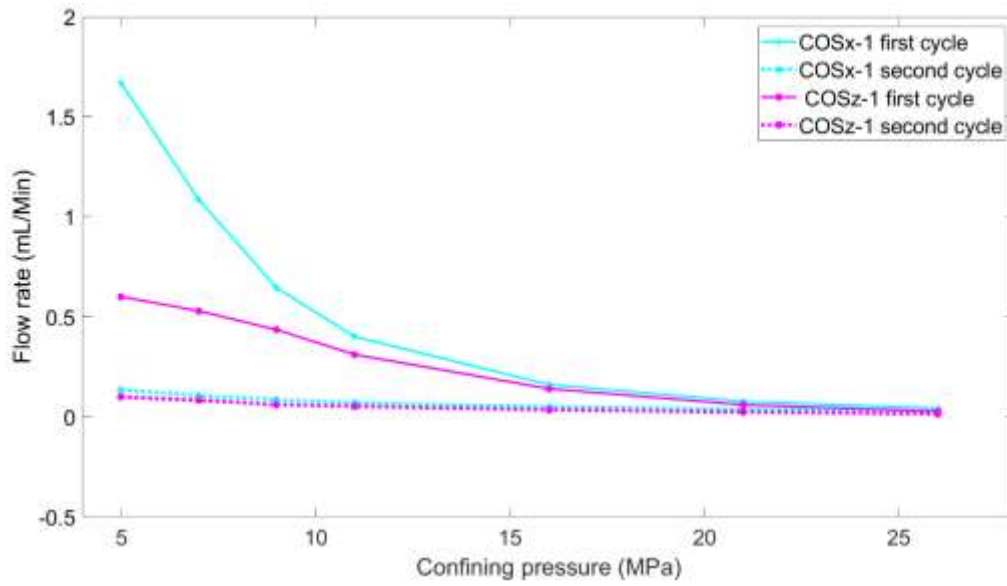
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Fig. 8 mechanical property behavior and AE in COS during injection at 16MPa initial conditions. Injection pressure (black continuous line), injected volume (blue line), cumulative AEs (red line) and hit count (grey bar) for sample COSx-3



731 **Fig. 9** mechanical property behavior and AE in COS during injection at 16MPa initial conditions. Injection
 732 pressure (black continuous line), injected volume (blue line), cumulative AEs (red line) and hit count (grey bar)
 733 for sample COSz-3
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 746 **Fig. 10** Average flow rate for first cycle (continuous cyan line) and average flow rate for second cycle
 747 (discontinuous cyan line) for COSx-1 and average flow rate for first cycle (continuous pink line) and average
 748 flow rate for second cycle (discontinuous pink line) for COSz-1 are calculated at each steady state condition for
 749 every confining pressure step, plotted as a confining pressure

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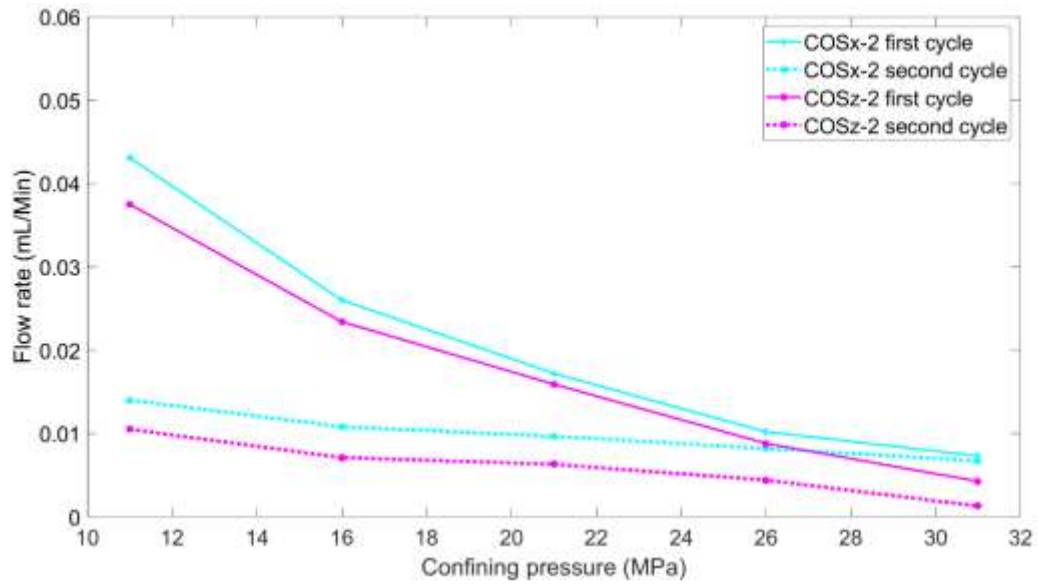
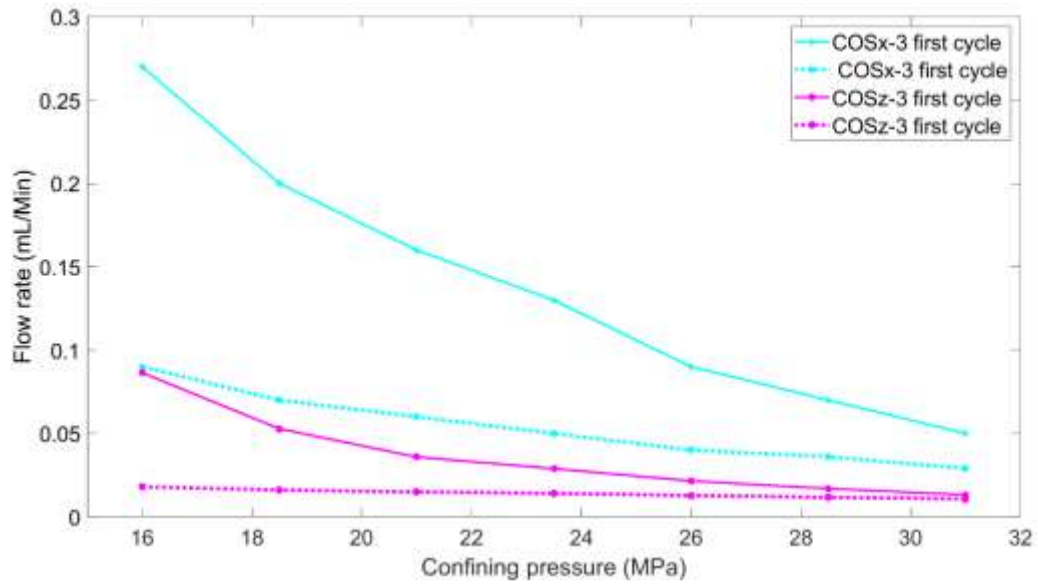


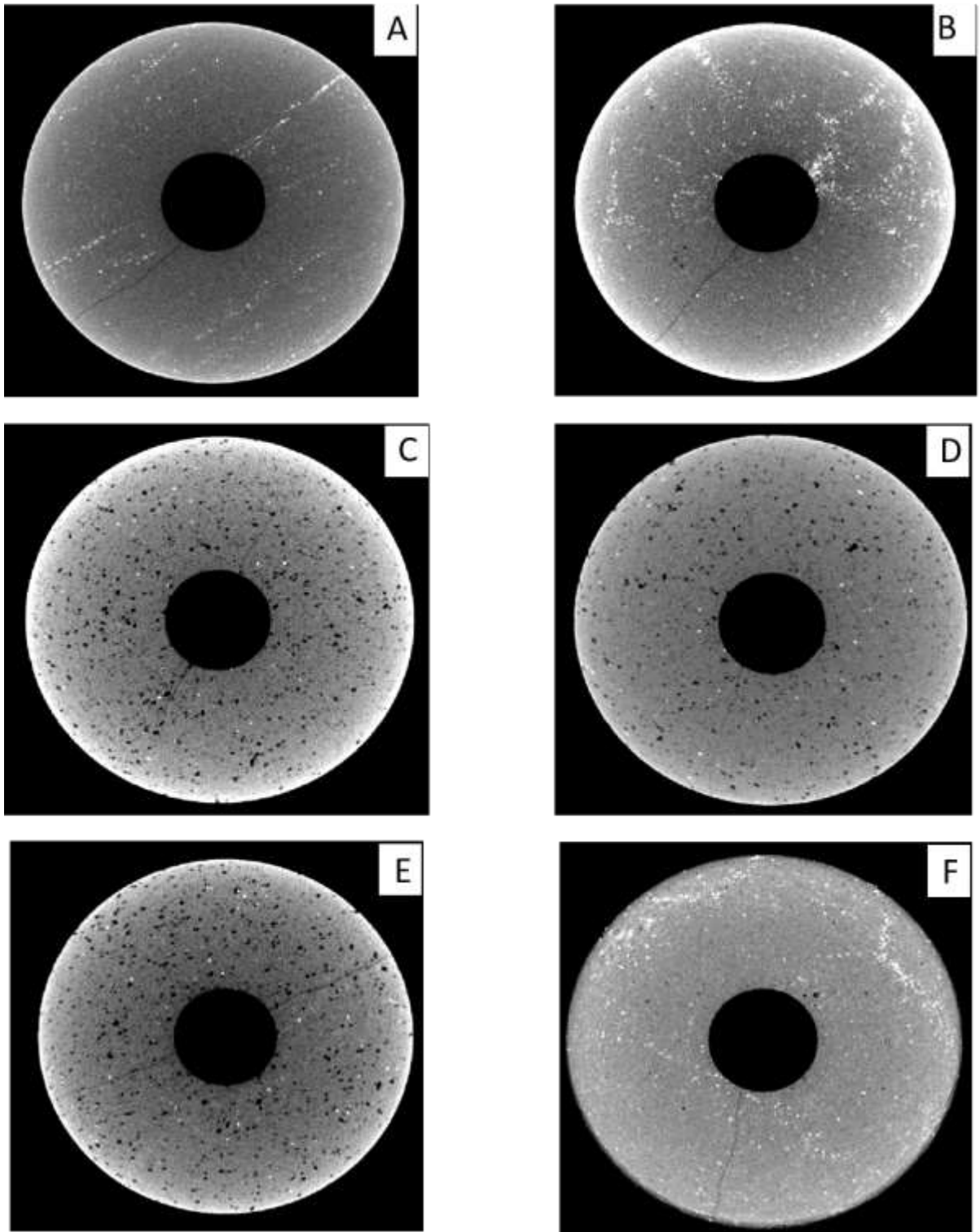
Fig. 11 Average flow rate for first cycle (continuous cyan line) and average flow rate for second cycle (discontinuous cyan line) for COSx-2 and average flow rate for first cycle (continuous pink line) and average flow rate for second cycle (discontinuous pink line) for COSz-2 are calculated at each steady state condition for every confining pressure step, plotted as a confining pressure

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775 **Fig. 12** Average flow rate for first cycle (continuous cyan line) and average flow rate for second cycle
 776 (discontinuous cyan line) for COSx-3 and average flow rate for first cycle (continuous pink line) and average
 777 flow rate for second cycle (discontinuous pink line) for COSz-3 are calculated at each steady state condition for
 778 every confining pressure step, plotted as a confining pressure
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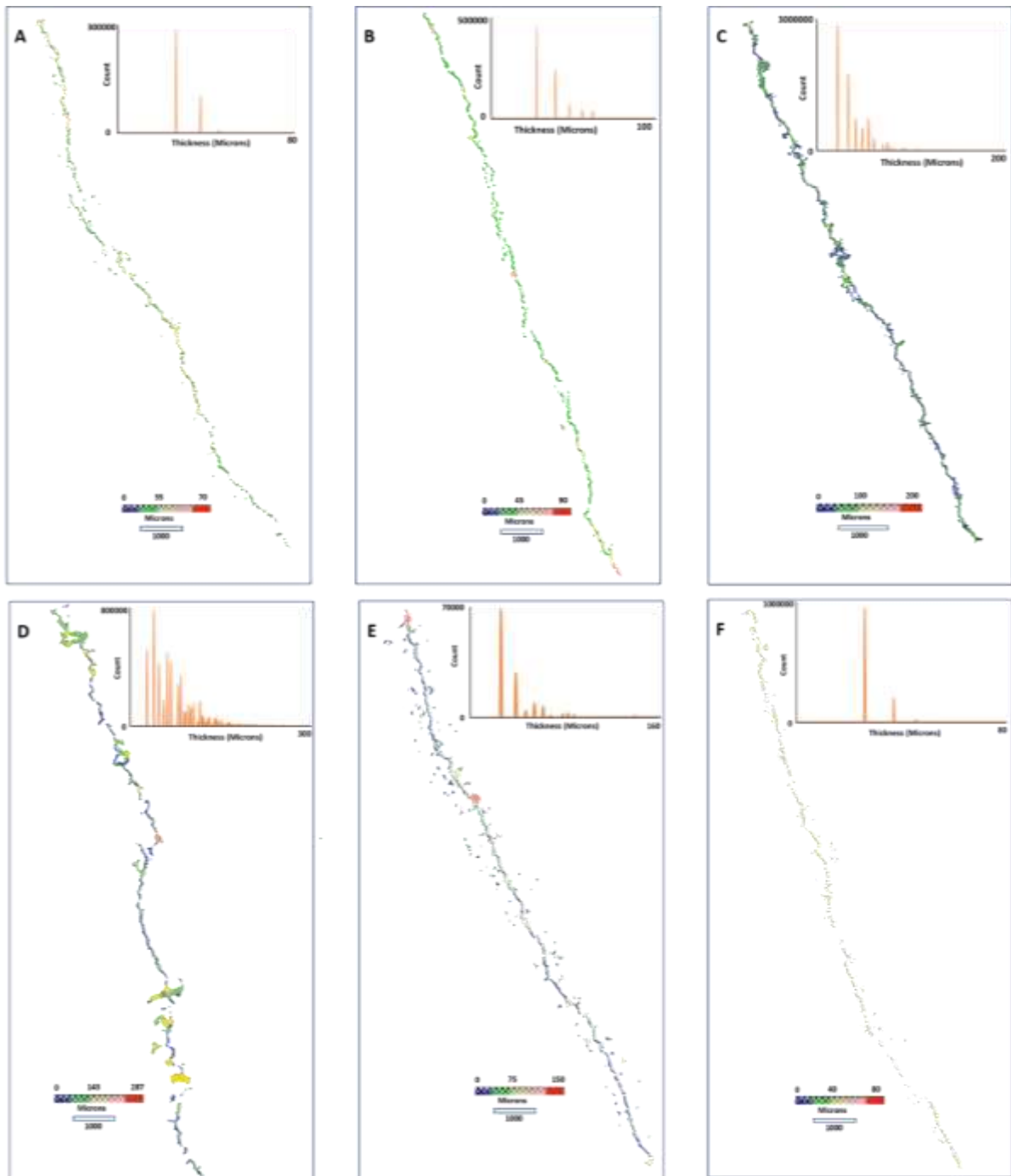
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Fig. 13 X-ray Computed Tomography showing tensile fracture: (A) fracture pattern in COSx_1 (B) fracture geometry in COSz_1 (C) fracture pattern in COSx_2 (D) tensile fracture development in COSz_2 (E) tensile fracture pattern in COSx_3 (F) fracture geometry in COSz_3. In all cases a prominent fracture is seen orientated lower-left to top-right, and favoring two fractures in samples cored in the 'x' direction (panels A, C, E) and one in samples cored in the 'z' direction (panels B, D, F)

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 789 **Fig. 14** Analysis of the tensile fracture showing thickness and pore connectivity; The insert is a histogram
 790 distribution of the thickness for both fracture and pore space: (A) fracture thickness in COSx-1, average 35 μm
 791 (B) fracture geometry in COSz-1, average 45 μm (C) fracture thickness distribution in COSx-2, average 100 μm
 792 (D) tensile fracture analysis for COSz-2, average 145 μm (E) tensile fracture thickness in COSx-3, average 75
 793 μm (F) fracture geometry in COSz-3, average 40 μm

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