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## The effect of a weak asthenospheric layer on surface kinematics, subduction dynamics and slab morphology in the lower mantle

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#### Abstract 15

On Earth, the velocity at which subducting plates are consumed at their trenches (termed 16 'subduction rate' herein) is typically 3 times higher than trench migration velocities. The 17 subduction rate is also 5 times higher than estimated lower mantle slab sinking rates. Us-18 ing simple kinematic analyses, we show that if this present-day "kinematic state" operated 19 into the past, the subducting lithosphere should have accumulated and folded beneath 20 near-stationary trenches. These predictions are consistent with seismic tomography, which 21 images localized and widened lower-mantle slab piles. They are, however, at odds with 22 most dynamic-subduction models, which predict rapid trench retreat and inclined slabs 23 in the mantle transition zone. We test the hypothesis that a weak asthenospheric layer 24 (WAL), between the lithosphere-asthenosphere boundary and 220 km depth, compatible 25 with geophysical constraints, can remedy the discrepancies between numerical models and 26 observations. The WAL lubricates the base of the lithosphere, increases the subduction 27 rate while reducing trench retreat. As a consequence, simulations featuring a WAL pre-28 dict slab accumulation at the mantle transition zone, and thicker, folded slabs in the 29 lower mantle. A WAL viscosity only 2-5 times lower than that of the adjacent mantle is 30 sufficient to shift subduction regimes towards a mode of vertical slab sinking and folding 31 beneath near-stationary trenches, across a wide range of model parameters, producing 32 surface and slab velocities close to those observed at the present-day. These findings 33 provide support for the existence of a weak asthenosphere beneath Earth's lithosphere, 34 complementing independent evidence from various geophysical data. 35

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#### <sup>36</sup> 1 Introduction

The negative buoyancy of subducting plates is the primary driving force sustaining sub-37 duction and surface plate motions Forsyth & Uveda (1975). Subduction zones are the 38 sites of tectonically-forced horizontal deformation Uyeda & Kanamori (1979); Lallemand 39 et al. (2005) and dynamic vertical motions Davies (1981); Gurnis (1993). Crust and litho-40 sphere subducting beyond the mantle transition zone add chemical heterogeneities to the 41 lower mantle, which are stirred and homogenised by mantle convection Zindler & Hart 42 (1986); Jones et al. (2016), or persist to the core-mantle-boundary, as suggested by mod-43 ern tomographic models (e.g. Hosseini et al., 2020). Understanding the deep dynamics of 44 subducting slabs is thus key for addressing the geodynamical and geochemical evolution 45 of our planet. 46

Observed plate kinematics provide insights into the dynamics of the subduction system 47 Forsyth & Uyeda (1975); Jarrard (1986); Lallemand et al. (2005); Heuret & Lallemand 48 (2005); Sdrolias & Müller (2006); Doglioni et al. (2007); Funiciello et al. (2008); Schellart 49 (2008b); Becker & Faccenna (2009); Goes et al. (2011). Subduction kinematics (see Fig. 50 1) involve the velocities of the subducting plate  $v_{sp}$  ("SP velocity" for short); the velocity 51 of the overriding plate  $v_{op}$  ("OP velocity"); and the velocity of the trench  $v_t$ , which is 52 equal to OP velocity if the overriding plate does not undergo (back-arc) deformation. 53 Note that  $v_{sp}$  and  $v_t$  are defined with opposite signs: the natural (positive) direction of 54 trench migration is "retreat" towards the SP. These velocities are given in some absolute 55 reference frame, which is taken as the stable lower mantle herein Becker & Faccenna 56 (2009).57

We also use a relative velocity, the subduction rate  $v_s$ . This is the velocity of the 58 subducting plate relative to the trench (i. e., the rate at which the subducting plate is 59 consumed by the migrating trench). It has been repeatedly shown that typical values of 60  $v_s$  on Earth are higher than 3-4 cm/yr Forsyth & Uyeda (1975); Jarrard (1986), while 61 absolute trench motions are usually between -2 and 2 cm/yr Heuret & Lallemand (2005); 62 Funiciello et al. (2008); Schellart (2008b). Other studies have pointed out that the mag-63 nitude of the (absolute) SP velocity  $v_{sp}$  is generally two to three times higher than that 64 of the (absolute)  $v_t$  Becker & Faccenna (2009); Goes et al. (2011); Carluccio et al. (2019). 65 Hence plates are consumed at much faster rates than their trenches move laterally. 66

Analogue and numerical models of subduction dynamics without external forcing 67 (hereafter simply referred to as models of subduction dynamics) have shed light on 68 the internal force balance of subduction systems and the resulting kinematics. They 69 have illuminated various subduction regimes and slab morphologies in the upper man-70 tle (e. g. Guillou-Frottier et al., 1995; Schellart, 2008a; Di Giuseppe et al., 2008; Ribe, 71 2010; Stegman et al., 2010). Recent studies that included an overriding plate with finite 72 strength, concluded that the slab pull force associated with the negative buoyancy of a 73 subducting plate (SP) favored slab rollback and migration of the trench towards the 74 subducting plate (i. e., trench retreat), unless the SP was weak and/or the overriding plate 75 (OP) was strong Garel et al. (2014); Sharples et al. (2014); Holt et al. (2015); Hertgen 76 et al. (2020). It has been pointed out that such analogue and numerical models of sub-77 duction dynamics tend to produce surface kinematics that are at odds with some of the 78 first-order observations outlined above Goes et al. (2011); Carluccio et al. (2019). These 79 subduction models generally produce trench retreat velocities that exceed present-day 80 observations, especially once the subducting slab reaches the bottom of the upper mantle, 81 which was sometimes treated as a rigid barrier Funiciello et al. (2004); Schellart (2005); 82



Figure 1: a) Sketch illustrating the various kinematics that can be inferred within a subduction system. Positive values denote absolute trenchward motion for both the subducting plate (p) and the overriding plate  $(v_{op})$ . Absolute trench velocity  $(v_t)$  is considered positive towards the subducting plate. We define relative to a fixed lower-mantle reference frame, in order to compare to absolute motions in nature, which can be quantified in empirical, approximate mantle reference frames, such as the fixed-hotspot frame. Subduction velocity  $(v_s)$  is a relative velocity, the rate at which the subducting plate is consumed at the trench  $(v_s = v_{sp} + v_t)$ .

Capitanio et al. (2007); Goes et al. (2011). More modest trench motions over a relatively 83 wide range of parameters have only been produced by 2-D models that consider both the 84 penetration of the subducting slab into the lower mantle and complex rheologies Garel 85 et al. (2014); Holt et al. (2015); Li et al. (2019). Even then, slower trench motion is only 86 achieved at the cost of decreasing the SP velocity to values of less than 2 cm/yr once the 87 slab interacts with the viscosity increase around 660-km depth (hereafter referred to as 88 "first slab-660 interaction") (e.g. Garel et al., 2014; Suchoy et al., 2021). Hence, in most 89 subduction dynamics models, more than half of the subduction rate  $v_{sp}$  is accounted for 90 by trench motion  $v_t$ , which contradicts present-day observations of plate kinematics. 91

Independent constraints on subduction dynamics come from seismic tomographic im-92 ages of slab morphologies at and below the mantle transition zone. A few slabs under 93 present-day subduction zones in the Western Pacific appear to stagnate above the 660-km 94 discontinuity Karason & Van Der Hilst (2000); Amaru (2007); Li et al. (2008); Fukao & 95 Obayashi (2013) - for instance, under Japan Fukao et al. (1992) and under Izu-Bonin Wu 96 et al. (2016), at least under its northernmost part Zhang et al. (2019). But many other 97 slabs have breached the 660-km discontinuity and are sinking into the lower mantle Goes 98 et al. (2017). Transition-zone and lower-mantle slabs are imaged more robustly and con-99 sistently than slabs in the upper(most) mantle. The opposite would be expected if slabs 100 retained a constant thickness across depths. Hence the deeper slab must be thicker Ribe 101 et al. (2007); Loiselet et al. (2010), which is well-documented under the Americas Karason 102 & Van Der Hilst (2000); Ren et al. (2007); Sigloch & Mihalynuk (2013); Mohammadzaheri 103 et al. (2021), but also globally Van der Voo et al. (1999); Shephard et al. (2017); Van der 104 Meer et al. (2018); Hosseini et al. (2020). Under the particularly well-instrumented Cas-105 cadia subduction zone of North America, tomography can resolve a shallow slab of single 106 lithospheric thickness, and also confidently show that the slab is multiply thickened from 107 the transition zone downward Sigloch et al. (2008). 108

Thickened slabs in the lower mantle have been attributed to slab buckling and folding through the mantle transition zone Guillou-Frottier et al. (1995); Ribe et al. (2007); Běhounková & Čížková (2008); Lee & King (2011); Cerpa et al. (2014); Billen & Arredondo (2018), with possible slab detachment Čížková et al. (2012). Slab folds have not yet been resolved by tomography, so the exact widening mechanism remains speculative from the observational side.

In order to produce slab folding and realistic lower-mantle slab morphologies, numer-115 ical subduction models often require a fixed overriding plate, i.e. zero trench velocity  $v_t$ . 116 Even then, the models predict sub-vertical slab folding only for rather extreme values 117 of model parameters, e. g. a very young subducting plate Garel et al. (2014); Strak & 118 Schellart (2021), and/or if special model setups are considered such as those involving two 119 nearby subduction zones Cížková & Bina (2015); Lyu et al. (2019). Thus the observations 120 of pervasively thickened lower-mantle slabs are generally not predicted in current models 121 of subduction dynamics. The models may lack a first-order mechanism that generates 122 thick lower-mantle slabs. 123

To summarize, there are at least two discrepancies between existing models of subduction dynamics and first-order observations. First, current models generally produce trench retreat velocities  $v_t$  in excess of those observed at present-day subduction zones, alongside SP velocities  $v_{sp}$  and subduction rates  $v_s$  that are too slow after first slab-660 interaction. Second, models seldom reproduce the tomographically observed, multiply thickened geometries that prevail in the transition zone and lower mantle.

This study considers how a weak asthenospheric layer (WAL) beneath the plate can 130 resolve these discrepancies. The presence of a WAL on Earth has been proposed to explain 131 a large range of geophysical observations, including postglacial rebound and gravity data 132 (e.g. Paulson & Richards, 2009), shear-wave tomography Kawakatsu et al. (2009); Barruol 133 et al. (2019), seismic attenuation Debayle et al. (2020), seismic anisotropy Debayle & 134 Ricard (2013); Becker (2017) and electrical conductivity tomography Naif et al. (2013). 135 The viscosity reduction could originate from a plume-fed asthenosphere Phipps Morgan 136 et al. (1995), from the depth-dependency of dislocation creep flow laws Raterron et al. 137 (2011), from crystal-preferred orientation Meyers & Kohlstedt (2021), or from the presence 138 of melt pockets Cooper & Kohlstedt (1986); Chantel et al. (2016), which may remain 139 trapped due to low melt fractions Holtzman (2016) or low density contrast Sakamaki 140 et al. (2013). 141

The presence of a WAL is predicted to affect large-scale dynamics of the underlying, 142 convecting mantle Lenardic et al. (2006), and to favor 'plate-like' rather than 'stagnant-lid' 143 regimes Höink et al. (2012). Since the sub-lithospheric mantle resists a plate's trenchward 144 motion, the inclusion of a WAL in models of subduction dynamics yields faster subduction 145 velocities  $v_{sp}$ , as shown by Carluccio et al. (2019) and Suchoy et al. (2021). The latter 146 authors also showed that increased  $v_{sp}$  was coeval with reduced trench retreat  $v_t$ , although 147 they did not detail the implications for lower mantle slab morphologies. We hypothesize 148 that increasing subduction rates while reducing trench motion results in the accumulation 149 of slab material in a near-vertical column beneath the (quasi stationary) trench, and that 150 the slab must widen (through folding) around the depths where it slows down to lower-151 mantle sinking rates, given that slab input  $v_s$  remains high. Thus, a WAL could resolve 152 both first-order discrepancies regarding plate velocities and slab morphologies. 153

We carry out a systematic numerical analyses of how a WAL impacts the dynamics of thermo-mechanical subduction models featuring an overriding plate. Section 2 provides a first-order quantification of slab widening behavior in modern subduction zones, using plate kinematic data. Section 3 describes the model setup. Section 4 presents our
modeling results, and Section 5 discusses their implications for subduction systems on
Earth.

# Quantifying slab folding from plate motions and slab sinking rates

#### <sup>162</sup> 2.1 Conceptual assessment

We start by demonstrating how slab folding can be assessed theoretically as a geomet-163 rical/kinematic phenomenon, involving slab accumulation in the mantle transition zone. 164 This analysis is inspired by subduction models where (unlike our own model) velocities 165 are applied to one or both plates, and which can predict slab morphology as a function 166 of these imposed surface kinematics Christensen (1996); Heuret et al. (2007); Arcay et al. 167 (2008); Gibert et al. (2012); Cerpa et al. (2015); Guillaume et al. (2018); Cerpa et al. 168 (2018). Among these, Gibert et al. (2012), anchored the subducting slab to a rigid 660-169 km discontinuity, which aims to simulate the effect of a strong viscosity jump at 660 km, 170 as inferred from e.g. geodetic constraints Mitrovica & Forte (2004). Gibert et al. (2012) 171 showed that if the subduction rate  $v_s = v_{sp} + v_t$  exceeds the trench velocity  $v_t$ , continued 172 subduction results in slab folding at the base of the upper mantle. Essentially, the slab 173 has to fold because trench retreat does not create enough lateral accommodation space 174 to permit all incoming slab to lie down flat on the '660'. Here we extend their analysis to 175 the more general case where the subducting slab sinks into the lower mantle. 176

Let  $v_s \times \Delta t$  be the length of subducted material consumed at the trench over some 177 duration  $\Delta t$ . The lateral displacement of the trench over the same duration is  $v_t \times \Delta t$ . The 178 displacement of the deepest portions of the subducting slab (simplified as the displacement 179 of the slap tip) within the upper mantle is approximated as  $v_{\rm tip} \times \Delta t$ , where  $v_{\rm tip}$  is the 180 absolute velocity of the deepest point of the slab. Slab folding can thus be understood 181 as a simple geometrical constraint. When the length of subducted material is larger than 182 the lateral displacement of the trench plus the displacement of the slab tip, the excess 183 length (slab accumulation) is expected to be accommodated by folding. Put in another 184 form, slab accumulation and folding occurs when: 185

consumption rate of subducted material > trench displacement + slab tip motion in the mantle

Alternatively, we can define a kinematic ratio  $K_r$  which predicts whether the subducting slab undergoes folding as:

$$K_r = \frac{v_s}{|v_t| + \sqrt{(v_{\rm tip}^x)^2 + (v_{\rm tip}^z)^2}}$$
(1)

where we have decomposed the velocity of the deepest point of the slab into its horizontal and vertical components.

When  $K_r \simeq 1$ , the free space created by trench retreat and slab sinking can accommodate all newly incoming lithosphere, which does not have to compress (fold). Hence the slab's apparent thickness remains similar in the upper and lower mantle (Fig. 2). A kinematic ratio  $K_r$  higher than 1 implies a surplus of slab material that cannot be accommodated by trench retreat and slab sinking into the lower mantle, and instead has to be accommodated by slab folding. At  $K_r > 1$ , the higher the value of  $K_r$ , the greater the frequency of slab folds (or alternatively, the wider the amplitude of the folds). Also at  $K_r > 1$ , the apparent thickness of the folded slab in the lower mantle is predicted to be multiples of the lithospheric thickness observed in the uppermost mantle.



Figure 2: Schematic theoretical diagram depicting various subduction regimes of subducting slabs, well after they have penetrated in to the lower mantle (LM). UM: upper mantle. Dashed line marks the viscosity interface between UM and LM, which we speculatively equate with the seismic '660 km' discontinuity.

The ratio of trench velocity to slab-sinking velocity  $(v_t/v_{tip}^z)$  controls, to first order, the average slab dip. This is true for both the unfolded  $(K_r \leq 1)$  and folded  $(K_r > 1)$  cases. Note that we use only the vertical component of the slab-tip velocity as it is thought to be much higher than the horizontal component (see also below section 2.2).

Hence the parameter space along the dimensions of  $K_r$  and  $v_t/v_{tip}^z$  spans a variety of 203 candidate slab morphologies and subduction regimes, as depicted in (Fig. 2). For negative 204 trench motion (trench advance), the subducting slab leans forward, so that the deepest 205 slab portions lie beneath the subducting plate at increasing distances from the trench 206 (leftmost regimes in Fig. 2). For quasi-null trench motions, the subducting slab sinks 207 vertically, with all slab portions remaining below the trench. For relatively high, positive 208 trench motions (trench "retreat"), the subducting slab leans backwards (" slab rollback"), 209 with deeper slab beneath the overriding plate. It has been proposed that high trench-210 retreat rates promote the complete stagnation of slab atop the 660-km discontinuity Torii 211 & Yoshioka (2007); Goes et al. (2017), so that high values of  $v_t/v_{tip}^z$  may lead to the end-212 member subduction regime where the slab flattens and folds on the 660-km discontinuity 213 (rightmost regimes in Fig. 2). 214

#### <sup>215</sup> 2.2 Estimating slab folding at present-day

In order to gauge the prevalence of slab folding in nature, we seek to calculate an observational estimate of  $K_r$  in active subduction zones, using Equation 1. Hence we need estimates of subduction rate  $v_s$ , absolute trench velocity  $v_t$ , and slab sinking velocity  $v_{tip}$ .

For estimating  $v_s$  and  $v_t$ , we use an updated version of the SUBMAP database Lalle-219 mand et al. (2005), which defines 249 transects of active subduction zones. Subduction 220 rates are retrieved from the relative plate motions of the MORVEL56-NNR model (based 221 on a circuit of 56 tectonic plates Argus et al. (2011) as explained in the Supporting In-222 formation Text S1). Each SUBMAP subduction transect is assigned to a subducting 223 plate and an overriding plate of the MORVEL56-NNR plate circuit. For transects that 224 cross significant arc and back-arc deformation, MORVEL56-NNR permits the definition 225 of an "arc block" and assessment of trench motion relative to that of a rigid overrid-226 ing plate, enhancing the accuracy of the derived subduction rate. For a few subduction 227 zones, the MORVEL56-plate circuit does not account for active arc and back-arc de-228 formation even though such a deformation has been well-established in the literature 229 (Southernmost-Central Andes, Izu-Bonin, Calabria). For these transects, we complement 230 MORVEL56-NNR with published regional studies (see Supporting Information). 231

To define the absolute motion of the plates and trenches, we need to consider an 232 absolute plate motion model within an absolute reference frame, comparable to the fixed 233 reference frame of our numerical models. In this paper we calculate and compare the value 234 of  $K_r$  in three recent absolute plate motion models, constructed in different manners: 235 the "SA" ("spreading-alignement") model Becker et al. (2015), the "TM25" model Wang 236 et al. (2018), and the "GMHRF-1Ma" model by Doubrovine et al. (2012). The SA model 237 minimizes the angular misfit between spreading-ridge orientations and plate velocities. 238 This plate motion was found to give a good fit to azimuthal seismic anisotropy, a proxy 239 for the shear induced by the relative motion between the tectonic plates and the upper 240 mantle. The TM25 model is based on 25 hotspot tracks under the assumption of fixed 241 hotspots relative to the deep mantle. The GMHRF-1Ma model is based on a global fit of 242 hotspot tracks since the Late Cretaceous, accounting for modest relative motions between 243 the hotspots' mantle plumes, computed by numerical models of whole mantle convection. 244 We extract the trench-normal component of the plates and trench velocities for com-245 parison with our 2-D models. In what follows, the absolute and relative velocities at each 246 transect are those of their trench-normal components. 247

The observed subduction rates are non-negative with a median value of 5.3 cm/yr and a 248 long tail up to almost 12 cm/yr (Fig. 3a). In all three reference frames (Fig. 3b-d), absolute 249 trench velocity  $v_t$  scatters around slightly positive values with a median values of 0.71 to 250 0.79 cm/yr. This tendency towards slow trench retreat may or may not be significantly 251 different from zero motion (stationary trench), given the large formal standard deviations 252 of almost 3 cm/yr but also the non-Gaussian, heavy tails of the histogram. In any case, 253 two thirds of the subduction transects have trench velocities between -1 and 1 cm/yr254 in the three absolute plate motion frames. Hence typical present-day trench motion is 255 roughly five times smaller than typical subduction velocities. 256

Estimating  $K_r$  also requires an observational estimate of slab sinking rates in the lower 257 mantle. Since slabs are not directly dateable, they have been correlated to the geology 258 of accretionary orogens, which hold the surface record of subduction. The subduction of 259 lithosphere is accompanied by the formation of a volcanic arc at the surface, which often 260 survives and is dateable. Such slab-arc correlations have inferred time-averaged sinking 261 rates of 1.0-1.5 cm/yr for slabs that have penetrated the lower mantle Van Der Meer et al. 262 (2010); Sigloch & Mihalynuk (2013); Domeier et al. (2016); Van der Meer et al. (2018); 263 Mohammadzaheri et al. (2021). 264

Using 1 cm/yr as the slab sinking velocity estimate, 70–80% of subduction transects exhibit values of  $K_r > 1$  in all three absolute reference frames (Fig. 4 and Fig. S1). Only



Figure 3: a) Histogram of the trench-normal component of subduction rate  $v_s$  in presentday subduction zones. b Histogram of the trench-normal component of trench velocity (retreat)  $v_t$ , in the spreading-alignment reference frame Becker et al. (2015). c) Histogram as in b) but for T25M reference frame Wang et al. (2018). d) Like b), but for GMHRF-1Ma frame Doubrovine et al. (2012).

a few subduction transects consistently display  $K_r < 1$  in all reference frames, mostly at the edges of longer arcs: the southernmost Andes (Patagonian transects), the northern edge of the Lesser Antilles (e.g. Puerto Rico Trench), or the edges of the South Sandwich SZ.

The present-day prevalence of  $K_r > 1$  is relatively insensitive to the assumed slab sinking velocity. Even when considering  $v_{tip} = 1.5$  cm/yr, at the high end of the reasonable estimate range ?see e.g.>[]butterworth2014geological,domeier2016global), 63% of transects remain above  $K_r > 1$  in the spreading-aligned absolute plate motion model, and 72% of transects in the two other reference frames.

Figure 4a plots the global inventory of slabs (between 600-1800 km depth), from which 276 the sinking rates were derived. Importantly, most areas are slab free. Existing slabs 277 cluster in two vast, linear belts: one under the Alpine-Eurasian-Himalayan-southwest 278 Pacific orogens; the second under the Americas and into Siberia. From the geologic record 279 and quantitative plate reconstructions, these are the known, absolute locations of major 280 orogenies over the past 200 million years, hence the known paleo-trench locations. The 281 observation that slabs are still located only beneath these independently inferred paleo-282 trench regions means that slabs sank rather vertically. The vast slab-free mantle areas are 283 known not to have hosted trenches over the past 200 m.y. This implies that paleo-trenches 284 have remained quite stationary over a time period during which the areal equivalent of 285 all ocean basins was subducted once or twice over Coltice et al. (2012). Thus trenches 286 had the opportunity to migrate across the globe but did not, which indicates sustained 287 K > 1 (slab folding regime) over geologic time. 288

Finally, slab dimensions directly point towards folding. In figure 4a, the Eurasian and American slab belts are 15,000-20,000 km long; individual slab segments are 1,000-3,000 km long (i.e., arc length) and 400-700 km wide. The latter is a multiple of lithospheric thickness, and suggests slab folds of this amplitude.



Figure 4: a) Map shows estimates of the kinematic ratio  $K_r$  (reddish color scale) for all subduction transects of the SUBMAP database Heuret & Lallemand (2005). The regime of inferred slab folding ( $K_r > 1$ ) prevails in most subduction zones. The absolute plate motion model is GMHRF-1Ma, which yields intermediate  $K_r$  values compared to the also-investigated spreading-alignment and TM25 models (plotted in the supplementary information). Also shown in blue shades is the global inventory of subducted slabs in the lower mantle (600-1800 km depth). More precisely, these are contours of seismically fast P-velocity anomalies exceeding dvp/vp>0.35% in global model DETOX-P2 Hosseini et al. (2020). b) Histogram of  $K_r$  values in the spreading-alignment reference frame. c) Histogram of  $K_r$  values in the TM25 reference frame. d) Histogram of  $K_r$  values in the GMHRF-1Ma reference frame.

Thus three separate lines of observational reasoning suggest that most present and past subduction zones feature(d) a surplus of subducted material not accommodated by lateral trench migration and slab sinking, so that instead slab folding is required. As discussed, common models of subduction dynamics (hereafter referred to as standard models) seldom reproduce this regime. Next we investigate whether adding a WAL to a standard model can shift its regimes from non-folding to folding over a wide range of model parameters.

### 300 3 Modeling approach

We use 2-D thermo-mechanical models of subduction dynamics. The governing equations 301 are those suitable for multi-material, incompressible viscous flow, under the Boussinesq 302 approximation, which are solved using the finite-element, control-volume, unstructured 303 adaptive mesh Fluidity computational modelling framework, which has been carefully 304 validated for simulations of this nature Davies et al. (2011); Kramer et al. (2012); Le Voci 305 et al. (2014); Kramer et al. (2021). Our model setup and material properties are similar 306 to Garel et al. (2014), albeit that in some cases we extend the models by incorporating a 307 sub-lithospheric weak asthonospheric layer (WAL), similar to that in Suchoy et al. (2021). 308 Below we summarize our modeling approach. 309



#### 310 3.1 Model Setup

Figure 5: Model setup and boundary conditions. In the standard models the viscosity of the WAL is equal to that of ambient mantle ( $\alpha = 1$ ), i.e., no weak asthenospheric layer (WAL) is present. We implement a viscosity contrast  $\Delta \eta$  of 30 at 660-km depth, the boundary between upper and lower mantle. The initial curved geometry of the subducting plate is prescribed using a bending radius of 250 km, including the weak layer.

The model predicts the evolution of an isolated subduction zone comprising both a subducting plate (SP) and an overriding plate (OP), with no external forces or velocities applied to the system. The model domain is a Cartesian box that is 8000-km wide and 2900-km in height (i.e. the whole mantle depth). Mechanical boundary conditions on the sides and base of the domain are free-slip, with a free-surface at the top. We use no-flux thermal boundary conditions on the sides and impose constant temperatures of 0°C and 1300°C at the surface and at the bottom boundaries, respectively.

The initial temperature field is given by a half-space cooling model where the age of the plates vary linearly from the 0 at the ridges to  $(A_{SP})$  for the subducting plate and to  $(A_{OP})$  for the overriding plate. Models begin with a curved subducting slab to initiate subduction (see inset Fig. 5). Below the plates, the initial mantle temperature is equal to that of the bottom boundary.

We consider a composite visco-plastic rheology that accounts for four deformation mechanisms: linear diffusion creep, and non-linear dislocation creep, Peierls creep and <sup>325</sup> pseudo-brittle yielding. The effective viscosity is:

$$\frac{1}{\eta_{eff}} = \left(\frac{1}{\eta_{diff}} + \frac{1}{\eta_{disl}} + \frac{1}{\eta_P} + \frac{1}{\eta_Y}\right)$$
(2)

<sup>326</sup> which is bounded at lower and upper limits.

The diffusion  $(\eta_{\text{diff}})$ , dislocation  $(\eta_{\text{disl}})$  and Peierls  $(\eta_{\text{P}})$  viscosities follow the generic form:

$$\eta_{\text{diff}|\text{disl}|\text{P}} = A^{\frac{1}{n}} \exp\left(\frac{E + PV}{nRT_r}\right) \dot{\epsilon}_{II}^{\frac{1-n}{n}} \tag{3}$$

where A is a prefactor, n is the stress exponent, E and V are the activation energy and volume, respectively. P is the lithostatic pressure, R the gas constant, and  $\dot{\epsilon}_{II}$  the second invariant of the strain-rate tensor.  $T_r$  is the sum of model temperature and an adiabatic temperature gradient of 0.5 °C/km and of 0.3 °C/km in the upper and lower mantle, respectively. The pseudo-brittle yielding viscosity follows a yield-stress law

$$\eta_Y = \frac{\tau_Y}{2\epsilon_{II}}\tag{4}$$

where the yield strength  $\tau_Y = \min(\tau_0 + f_c P, \tau_Y^{\max})$ , with  $\tau_0$  the surface yield strength,  $f_c$ the friction coefficient, P the lithostatic pressure, and  $\tau_Y^{\max}$  the maximum yield strength. The weak layer is 8-km thick, with a friction coefficient 10 times lower than the mantle material, and a maximum prescribed viscosity of  $10^{20}$  Pa s. All rheological parameters are as in Table 1 of Garel et al. (2014) and we use a consistent solution strategy.

#### 339 3.2 Treatment of WAL

The depth extent of a potential WAL is not well constrained. Some studies, which consider 340 it to be a layer of partial melt, suggest that it is only 10-20 km thick Schmerr (2012); 341 Sakamaki et al. (2013); Stern et al. (2015), whereas others advocate for a layer extending 342 from the lithosphere-asthenosphere boundary up to 200-300 km depth (thus a thickness of 343 approximately 100-200 km) Kawakatsu et al. (2009); Paulson & Richards (2009); French 344 et al. (2013); Becker (2017); Barruol et al. (2019); Debayle et al. (2020). Here, we simulate 345 the presence of the WAL by imposing a viscosity reduction between the 1100 °C isotherm 346 (a proxy for the LAB) and a depth of 220 km, similarly to Suchoy et al. (2021). Note 347 that models tested with a WAL extending up to 300 km depth showed little differences 348 with the results reported below. We define the effective viscosity within the WAL as: 349

$$\eta_{\rm WAL} = \alpha \eta_{\rm eff} \tag{5}$$

where  $0 < \alpha \leq 1.0$  is a reduction-viscosity factor.

The viscosity reduction of a WAL, and its origin, is also debated. For example, partial 351 melt can lead to a 20-fold or larger viscosity reduction Holtzman (2016), but strongly 352 depends on melt fraction, creep regime, grain size and wetting angle Kohlstedt & Zim-353 merman (1996). Milder viscosity reduction (< 5-fold) are expected from crystal-preferred 354 orientation considerations Meyers & Kohlstedt (2021). We choose here to explore values 355 of  $\alpha$  in [0.2; 0.5; 1.0] (respectively, a viscosity reduction of 5-, 2-, or zero-fold – see below 356 Section 4.1). Note that larger viscosity reductions ( $\alpha$  of 0.01-0.1) have usually been used 357 in global mantle flow models reproducing sub-plate seismic anisotropy Conrad & Behn 358 (2010); Becker (2017). However, values of  $\alpha$  lower than 0.1 in our set-up led to unre-359 alistically large asthenospheric flow velocities (>50 cm/yr) and to thermal instabilities 360 potentially associated to small-scale convection (further discussion in Section 5.3.1). 361

#### <sup>362</sup> 4 Model results

We first perform a set of simulations without a WAL ( $\alpha = 1$ ), that we hereafter refer to as standard cases. Next, we explore sets of simulations with different degrees of weakening in the WAL (i.e. various values of  $\alpha$ ), that we refer to as WAL cases. For each case, we define a reference simulation (with plate ages  $A_{sp} = 40$  My and  $A_{op} = 20$  My). We subsequently run simulations that span a range of initial ages to cover a wide range of strength and buoyancy for both plates, while being representative of all regions of the subduction regime diagram presented in Garel et al. (2014).

#### 370 4.1 Standard cases - no WAL

#### 371 4.1.1 Reference simulation $[A_{sp} = 40 \text{ My}; A_{op} = 20 \text{ My}]$



Figure 6: Reference standard model, featuring  $A_{sp} = 40$  and  $A_{op} = 20$  My. (a-f) Temporal snapshots of the evolution of the temperature field, from 4 to 62 My. g) Kinematics of plates, slab, and trench.  $v_{sp}$  in dark blue, positive to the right.  $v_{op}$  in green, positive to the left.  $v_t$  in light blue, positive to the left.  $v_{tip}$  in dark red is the magnitude of slab tip velocity in. Vertical dashed lines mark snapshots times of (a-f). h) Temporal evolution of Kinematic ratio  $K_r$ , a proxy for the slab's propensity to fold (definition in the text). Horizontal black line denotes the boundary between the folding ( $K_r > 1$ ) versus non-folding (K < 1) regime.

Figure 6 displays the temporal evolution of the reference simulation for the standard cases ( $\alpha = 1$ ). During the first stage of free-sinking through the upper mantle (Fig. 6a), the subducting plate accelerates as slab pull increases with increasing slab length, reaching

a peak velocity of  $\sim 13$  cm/yr with trench retreat/OP velocity peaking at  $\sim 4$  cm/yr 375 (Fig. 6g). Since trench velocity is very similar to OP velocity, indicating little back-arc 376 deformation, we will only describe the evolution in terms of trench velocity. As soon as 377 the slab tip encounters the high-viscosity lower mantle at  $t \simeq 5$  My, the plate velocities 378 decrease to between 1 and 3 cm/yr. This slab-660 interaction is followed by two subsequent 379 episodes of slab folding. First, the slab bends with an OP-wards concavity between  $\sim 6$ 380 and  $\sim 14 \text{ My}$  (Fig. 6b-c), with an increase in SP velocity (up to 3 cm/yr) and low trench 381 velocity of approximately 1 cm/yr. Then, a transient stage of slab rollback, associated 382 with a slight increase in the trench velocities up to 1.5 cm/yr, lasts for approximately 383 5 My (Fig. 6c) and lowers slab dip in the upper mantle. The second folding episode 384 occurs between  $\sim 25$  and  $\sim 40$  My: the deeper, folded portion of the slab flattens above 385 the lower mantle while the shallow slab continues to roll back (Fig. 6d), increasing slab 386 pull ( $v_{sp}$  up to ~ 2.5 cm/yr). Another transient stage of trench retreat without buckling 387 follows (Fig. 6e), with trench velocity (1.8 cm/yr) greater than the SP velocity (1 cm/yr). 388 From 50 My, a third slab-folding episode occurs, but with a smaller amplitude due to the 389 obliquity of slab relative to the viscosity jump (Fig. 6f), and a smaller increase in  $v_{sp}$ . 390 Overall, through time, all velocities decrease and tend towards 1 cm/yr, comparable to 391 the sinking velocity of the deepest part of the slab within the lower mantle. Slab sinking 392 rates in the lower mantle therefore strongly modulate, and perhaps even limit, surface 393 kinematics. 394

The kinematic ratio,  $K_r$ , given in Equation 1 provides an alternative quantitative 395 diagnostic. During the free-sinking stage, the slab-tip velocity reaches a peak value of 396 20 cm/yr, higher than the peak SP velocity  $v_{sp}$  (13 cm/yr). As a consequence, the kine-397 matic ratio  $K_r \leq 1$  (Fig. 6g). After the slab has interacted with the 660-km discontinuity 398  $K_r$  display oscillations. These oscillation follow those observed for  $v_{sp}$  and  $v_t$ , when one 399 of the two increases while the other decreases. Folding episodes occur when  $K_r > 1$ , 400 while slab-retreating stages occurs for lower  $K_r \simeq 1$ . Through time, the amplitude of  $K_r$ 401 oscillations decrease, reflecting the decrease in folding as the slab inclines and the impact 402 angle with the 660-km viscosity discontinuity decreases. 403

#### 404 4.1.2 Slab morphologies and kinematic ratios across all standard cases

We run a series of no-WAL simulations with various initial plate ages (20-100 for the overriding plate; 10-100 for the subducting plate). Since we focus on the long-term evolution of these systems (i.e. well after the first stage of slab-free sinking through the upper mantle), Figure 7a only displays their state at t = 80 My.

Several studies have focused on the interaction and passage of slabs through the mantle 409 transition and the resulting slab morphologies Torii & Yoshioka (2007): Billen (2010): Lee 410 & King (2011); Cížková & Bina (2013); Billen & Arredondo (2018), sometimes character-411 izing a range of so-called subduction regimes Garel et al. (2014); Agrusta et al. (2017); 412 Li et al. (2019); Briaud et al. (2020). Here we focus on two features after initial slab-660 413 interaction: trench motion and the amount of slab folding. Thus we define three regimes: 414 strong trench retreat without slab folding (SR), strong trench retreat with slab folding 415 (SRwF), and a weak trench retreat with slab folding (WRwF) (7a). The strong-retreat 416 modes are those for which the total displacement of the trench during the simulation 417 amounts to an average rate higher than 1 cm/yr, and weak-retreat modes when it is 418 le1cm/yr. Following, Garel et al. (2014), the results of simulations are reported as func-419 tions of initial SP and OP ages, with the former controlling slab buoyancy and resistance 420 to bending, and the latter controlling the OP bending resistance opposing trench retreat. 421

<sup>422</sup> Note that due to our focus on the long-term trench motion and the tendency and nature
<sup>423</sup> of slab folding, the subduction regimes outlined herein differ from those used in Garel
<sup>424</sup> et al. (2014).

The SR regime in the simulations of the standard case occurs for both relatively old SPs and relatively old OPs. The regime WRwF occurs only for very young SPs. The regime that lies in between, SRwF, occurs over the widest parameter space. In simulations with relatively young OPs, only the SRwF is observed. For extremely young cases ( $A_{SP} = A_{OP} = 20$  Myr), subduction is rapidly terminated through slab detachment, because the low slab pull cannot initially overcome the resisting forces.

Figure 7b displays the evolution of  $K_r$  for four selected standard simulations. These simulations display peak  $K_r$  of 1.5-2.2, shortly after the first slab-660 interaction (time range 5 to 20 Myr). Simulations  $[A_{sp}=40 \text{ My}; A_{op}=20 \text{ My}]$  (ref. simulation - SRwF) and  $[A_{sp}=40 \text{ My}; A_{op}=65 \text{ My}]$  (SRwF) display oscillations of  $K_r$  associated with slab folding. Simulations  $[A_{sp}=65 \text{ My}]$  (SRwF) display oscillations of  $K_r$  associated with slab folding. K<sub>r</sub> ~ 1 at all times after initial slab-660 interaction. At later times, the value of  $K_r$  tends to 1, associated a decrease of both  $v_{sp}$  and  $v_s$  (see Figure S6 of Supp. Inf.).

#### $_{438}$ 4.2 WAL cases

We next perform simulations with a WAL, that is simulations where we impose values of the weakening factor  $\alpha < 1$  in the sub-lithospheric mantle.

#### 441 4.2.1 Reference WAL simulation with $\alpha = 0.5$ ( $A_{sp}=40$ My and $A_{op}=20$ My)

In the reference WAL simulation (Fig. 8), the first slab-660 interaction occurs at  $\sim 1.5$ 442 My, earlier than in the comparable standard simulation ( $\simeq 4$  My). The first slab buckling 443 episode occurs shortly after at 2-10 My (Fig. 8a-b), with subducting plate and trench 444 velocities of 5.5 cm/yr and 1 cm/yr, respectively. A second folding episode takes place 445 after 10 My (Fig. 8c-d) during which the SP velocity increases from 1.8 to 3.8 cm/yr446 between t = 14 My and t = 22 My and that of the trench decreases from 1.8 to 0.8 cm/yr. 447 The next folding episode (between t = 35 My and t = 55 My, Fig. 8e) is associated with 448 a stationary trench, while the SP velocity stabilizes at  $\sim 2.5$  cm/yr. A third fold forms 449 after t = 55 My (Fig. 8f) which produces a peak subducting-plate velocity of 4.8 cm/yr. 450 The opposite evolution of trench and SP velocity, associated with  $K_r$  oscillation, is 451 even more apparent that in the reference simulation of the standard case. After the first 452 slab-660 interaction, the slab tip velocity remains nearly constant at around 1 cm/yr, 453 independent of slab folding and oscillation of surface velocities. 454

#### 455 4.2.2 Mantle drag forces on the subducting plate

<sup>456</sup> Differences in the evolution of reference simulations can be explained by a reduction of <sup>457</sup> mantle drag at the base of the subducting plate. We calculate a drag force as the integral <sup>458</sup> of the tangential stress along the 1100°C isotherm (in N m<sup>-1</sup>). Figure 9 displays the <sup>459</sup> temporal evolution of this diagnostic for the reference simulations (i. e, with and without <sup>460</sup> a WAL).

Prior to initial slab-660 interaction, both models show sub-lithospheric mantle moving
towards the trench but with velocities reduced relative to overlying lithosphere (Couetteflow type). Shear stresses beneath the subducting plate are positive and mostly negative
beneath the overriding plate. Shear stresses along the base of the subducting plate remains



Figure 7: a) Snapshots of the final state (after model run times of 80 My) of all standard models superimposed on a regime diagram. The three regimes are: strong trench retreat without slab folding (SR, purple), strong trench retreat with slab folding (SRwF, dark blue), and weak trench retreat with slab folding (WRwF, light blue). The boundaries between regimes are approximate. b) Kinematic ratio  $K_r$  as a function of the time since the initiation of subduction, for four of the standard models shown in (a). The subduction regimes associated with the evolution of those models is indicated by labels. Over time, all four models tend towards no-folding ( $K_r \approx 1$ ).

positive after initial slab-660 interaction (Fig. 9c,e), and the drag force remains negative.
Overall, we observe that the absolute value of the drag force beneath the subducting plate
decreases with time as a consequence of the reduction in the length of that plate with
time.

The two simulations display similar oscillatory trends that reflect slab folding behavior. However, as expected, the absolute drag is lower in the simulation featuring a WAL,



Figure 8: Reference simulation  $[A_{sp}=40 \text{ My}; A_{op}=20\text{My}]$  of the WAL case with a two-fold viscosity reduction ( $\alpha = 0.5$ ). Panels and plotting styles as in Fig. 6. Panel (h) displays the evolution of  $K_r$  for this reference WAL case (solid blue) and also for the reference standard case of Fig. 6 (dashed blue).

explaining the higher SP velocities observed in this case (Fig. 8g) relative to the comparable no-WAL case (Fig. 6g). The faster subducting plate may hamper trench retreat with faster trench-wards asthenospheric flow opposing slab rollback Alsaif et al. (2020). Slab sinking, and hence a faster subducting plate, may also be enhanced through dislocation creep decreasing the viscosity of adjacent asthenosphere, further facilitating slab descent Garel et al. (2020). All these effects favor the higher  $K_r$  observed in the reference WAL case compared to the reference standard case.

#### 478 4.2.3 Subducting slab morphologies and kinematic ratios in the WAL case

As with the standard cases, we run a series of WAL simulations with  $\alpha = 0.5$  spanning 479 plate ages that range from 20-100 My. Figure 10a displays their final state at 80 My, 480 together with the inferred regime diagram. Consistent with the standard cases, WAL 481 cases exhibit three regimes (SR, SRwF, and WRwF), but regime boundaries are shifted 482 towards higher plate ages. In particular, the WAL simulations  $[A_{sp}=65 \text{ My}-A_{op}=65 \text{ My}]$ 483 and  $[A_{sp}=65 \text{ My}-A_{op}=100 \text{ My}]$  now lie more clearly in the SRwF regime while their 484 standard equivalents belong to the SR regime. Moreover, the WAL simulations with 485  $A_{sp} = 40$  My lie within, or very close to, the WRwF regime, whereas for standard cases, 486 only those with  $A_{sp} \geq 20$  My are within this regime. 487

Figure 10b displays the kinematic ratio  $K_r$  of selected WAL simulations. As in the standard cases, the ratios  $K_r$  before and during the first slab-660 interaction is generally



Figure 9: Viscous mantle resistance acting below the subducting plate in the reference standard model versus in the reference WAL model. (a,c,e) Snapshots of the shear stress field (background colour) the reference standard model at times 4 My, 44 My, and 62 My. (b,d,f) Same snapshots for the reference WAL model. Red line traces the LAB isotherm of 1100°C (pink) used to calculate the drag below the subducting plate. Positive shear stresses imply that the tangential component of the stress vector - calculated along the quasi-horizontal LAB isotherm of the subducting plate - is toward the left. g) Evolution of the mantle drag force below the subducting plate for the reference standard model (dashed red) and the reference WAL model (solid red). Negative values denote a force toward the left. The total mantle drag force onto the subducting plate is negative in accordance with the stress vector. Three vertical dashed lines indicate the times of the snapshopts (a-f). The drag force beneath the overriding plate is less straightforward to analyze, see Supporting Information section S4.

higher than 1. Some peak values of  $K_r$  reached in the WAL simulations are even greater (> 490 2) than the highest values observed in the standard simulations (7b). Most importantly, 491 two of these simulations  $[A_{sp} = 40 \text{ My}; A_{op} = 20 \text{ My}]$  (ref. simulation for the WAL case) 492 and  $[A_{sp} = 65 \text{ My}; A_{op} = 65 \text{ My}]$  display  $K_r > 2$  even after the first slab-660 interaction: 493 the presence of a weak layer favors the excess accumulation of subducted material in the 494 mantle relative to the accommodation by motion of both the trench and slab tip, resulting 495 in substantial slab folding. The simulation  $[A_{sp}=100 \text{ My}; A_{op}=65 \text{ My}]$  shows values of  $K_r$ 496 close to 1 at all times after initial slab-660 interaction, consistent with the standard case, 497 lying in the SR regime. WAL simulation  $[A_{sp}=65 \text{ My}; A_{op}=65 \text{ My}]$  exhibits intermediate 498 behavior, with oscillations of  $K_r$  up to 1.5, while its standard equivalent show values close 499 to 1. This is because the former clearly lies in the SRwF regime while its equivalent 500 standard case lies near the transition from the SRwF to the SR regime. 501



Figure 10: a) Regime diagram of WAL models with two-fold viscosity reduction ( $\alpha = 0.5$ ). Panels and plotting styles as in Fig. 7.

#### 502 4.2.4 WAL cases with $\alpha = 0.2$

We finally run a series of simulations for a WAL with  $\alpha = 0.2$  (Fig. 11a). The most 503 striking difference, relative to all previous cases examined, is that the SR regime no longer 504 appears within the range of plate ages investigated: slab folding behavior is consistently 505 observed, throughout the investigated parameter space. Moreover, the boundary between 506 the WRwF and SRwF regimes shifts to values of subducting plate ages higher than 65 507 My and for overriding plate ages higher than 20 My. Hence, strong retreat ( $v_t > 1 \text{ cm/yr}$ ) 508 now only occurs for heavy and stiff plates, with the WRwF regimes becoming dominant. 509 In particular, when the overriding plate is relatively weak  $(A_{op} \simeq 20 \text{ My})$  vertical slab 510 folding piles in the lower mantle are ubiquitous. Cases also exhibit higher  $K_r$  values 511 (1.5-4) well after the first slab-600 interaction (Fig. 11b). 512

<sup>513</sup> Finally, it is worth noting that in the majority of the above simulations with a WAL

and  $\alpha = 0.2$ , thermal instabilities form within the weak layer at the base of the plates. 514 These transient instabilities, which take the form of drips of cold lithosphere generated 515 beneath both overriding and subducting plates, develop as the lithosphere thickens in 516 response to conductive cooling. The drips are then advected by lateral mantle flow and 517 mix with underlying mantle. We note that they only occur when the asthenospheric 518 viscosity reaches values close to or below  $\sim 10^{19}$  Pa s, as advocated by previous studies 519 van Hunen et al. (2003); Ballmer et al. (2011); Le Voci et al. (2014); Davies et al. (2016). 520 Further analyses of these features will be the focus of a future study. 521



Figure 11: Regime diagram of WAL models with a five-fold viscosity reduction ( $\alpha = 0.2$ ). Panels and plotting styles as in Fig. 7. The models remain in the weak retreat and folding regime over the entire run time, unless they feature very old plate ages.

#### 522 5 Discussion

#### 523 5.1 Surface velocities and kinematic ratios

On Earth, subduction rates are typically 3 to 5 times higher than absolute trench velocities, and 5 times higher than estimated slab sinking velocities (see Section 2). This yields kinematic ratio  $K_r$  estimates above 1 for most subduction zones, creating a scenario that favours a slab thickening/folding regime (see section 2.2).

Simulations without a WAL produce surface kinematics at odds with these obser-528 vational constraints because once the slab has interacted with the transition zone, the 529 subducting plate  $v_{sp}$  slows down to approach slab sinking rates of 1 cm/yr. The addition 530 of a WAL renders the simulations more compatible with observational constraints, in that 531  $v_{sp}$  up to 5 cm/yr are maintained long after initial slab-660 interaction (Fig. S4-S5 in Supp 532 Info), and trench velocities  $v_t$  are attenuated to typically lower than 1 cm/yr. Our models 533 with WAL thus reproduce the rapid subduction rate, near-stationary trenches, and slow 534 slab-sinking rates observed on Earth. WAL simulations have higher  $K_r$  values than the 535 standard models, as summarized by Figure 12. The time-averaged kinematic ratio  $K_r$ 536 (after initial slab-660 interaction, i.e., averaged between 20-80 My) ranges from 1.0–1.3 537 in the standard models (Fig. 12a, except for the youngest SP plate ages). In contrast,  $K_r$ 538 ranges between 1.0–3.1 in WAL simulations with two-fold weakening ( $\alpha = 0.5$ , Fig. 12b), 539 and between 1.0–2.9 for five-fold weakening ( $\alpha = 0.2$ , Fig. 12c).  $K_r$  is generally higher 540 in WAL simulations with  $\alpha = 0.2$  (although the maximum value of  $K_r = 3.1$  occurs for 541  $\alpha = 0.5$  and the youngest plate ages). 542

WAL simulations also show higher peak values of (non-averaged)  $K_r$ , before and after first slab 660-interaction. In the standard models,  $K_r$  mostly ranges between 1–2 (see Fig. 7 and Supp Info Fig. S6a), whereas the WAL simulations exhibit peak  $K_r$  values above 2 and up to 6-7 (Figs. 10 and Fig. 11 – see also Figs. S6b,c in Supp. Info.). Hence only the models with a weak layer produce kinematic ratios  $K_r$  that are comparable to those estimated for subduction zones in nature (Fig. 4).

Behr & Becker (2018) have suggested the lubrication effect of a weak sedimentary layer 549 above the subducting plate as an alternative mechanism for increasing  $v_{sp}$  in models of 550 subduction dynamics ?see also>[]duarte2013three. They showed that  $v_{sp}$  could increase by 551 one to two orders of magnitude if sediments reduced viscous resistance at the interface by a 552 comparable amount. However, recent models have shown that a weaker plate interface also 553 favors an increase in trench retreat  $v_t$  Pusok et al. (PREPRINT); Behr et al. (2022). We 554 investigated this by running a simulation without a WAL but featuring a plate interface 555 layer with a two-fold reduction in maximum viscosity (see Fig. S8). Relative to our 556 comparable standard case, both  $v_{sp}$  and  $v_t$  increased slightly, resulting in a negligible 557 difference to  $K_r$ . This suggests that a weaker plate interface would not allow us to 558 reconcile model predictions with the available observational constraints on  $K_r$ , further 559 supporting an important role for a WAL. 560

#### <sup>561</sup> 5.2 Slab morphologies

The presence of a WAL strongly impacts the subduction regimes and lower mantle slab morphologies, as encapsulated by the proxy of  $K_r$ . Simulations without a WAL produce low-to-moderate values of  $K_r$ , and moderate-to-high trench retreat rates. Without a WAL, strong-retreat regimes are thus dominant across the parameter space examined, and only models with the youngest, weakest overriding plate (20 My) exhibit some slab-folding



Figure 12: Summary of modeling runs and regime diagrams. Time-averaged kinematic ratio  $\bar{K}_r$  after the first slab-600 interaction, plotted in the two-dimensional space of SP and OP plate ages (unit Myr). for (a) standard non-WAL models; (b) WAL models with  $\alpha = 0.5$ ; (c) WAL models with  $\alpha = 0.2$ .  $\bar{K}_r$  is represented by black dots with sizes proportional to  $\bar{K}_r$  values, which are also printed. Background colors denote folding regimes as in previous figures. The time-averaging window for obtaining  $\bar{K}_r$  is [20-80] My.

behaviour. However, even for a WAL with a moderate viscosity decrease ( $\alpha = 0.2$ ), the 567 (non-folding) SR regime disappears and the SRwF regime only occurs in simulations with 568 relatively stiff and buoyant plates  $(A_{sp} > 80 \text{ My}, A_{sp} > 40 \text{ My})$ . Hence, Slabs folding and 569 vertically piling in the lower mantle, beneath near-stationary trenches, become the pre-570 vailing morphologies of the WAL simulations (light blue shading in Fig. 12). These results 571 demonstrate, for the first time, that models of subduction dynamics (without external 572 forcing) are able to produce lower-mantle slab morphologies observed by tomography, 573 while also honouring the plate and trench velocities measured at the surface. 574

We note that the amplitude of lower-mantle slab folds in our simulations is consistent 575 with theoretical predictions based on a thin-sheet mathematical formulation. Ribe (2003) 576 and Ribe et al. (2007) used these formulations to derive a scaling law for the amplitude 577 of folds of a vertically descending, viscous sheet that buckles as it encounters resistance 578 at a sharp viscosity jump, or a rigid barrier. The predicted fold amplitude is half the 579 fall height, which would be half the thickness of the upper mantle in the context of 580 subduction: approximately 330 km. Our simulations with more pronounced vertical slab 581 folding produce 300 to 500-km wide folds in the lower mantle, that are consistent with 582 this theory. We note that the presence of a WAL enhances the frequency of folding in 583 the models but leaves their width reasonably unchanged. The modeled fold amplitudes 584 of 300-500 km are moderately smaller than the 400-700 km wide "slab walls" imaged by 585 seismic tomography (e. g. Sigloch & Mihalynuk, 2013). It remains to be investigated 586 whether this difference is due to shortcomings of the physical approximations used in our 587 dynamic models, or due to tomographic blur. 588

From models of subduction dynamics, it has been suggested that sustained, quasiperiodic slab folding, over tens of millions of years after initial slab-660 interaction, can occur only if the mineralogical phase transition around 410 and 660 km were included in the models Běhounková & Čížková (2008); Čížková & Bina (2013); Agrusta et al. (2017); Briaud et al. (2020), and/or if the subducting slab was quite weak, e.g., made of young

seafloor Garel et al. (2014); Agrusta et al. (2017); Strak & Schellart (2021). While we 594 acknowledge that these factors may further enhance slab folding, we stress that our sim-595 ulations with a WAL did not require the phase transitions in order to produce sustained 596 slab folding. The Clapeyron slopes of the phase transitions remain under discussion ?see 597 e.g.>[and references therein]agrusta2017subducting, so their relative role in slab folding 598 remains to be clarified. In a similar vein, the inclusion of a WAL yielded slab folding 599 of relatively thick and stiff subducting plates (Fig.12). No additional slab-weakening 600 mechanism or slab-buoyancy variation was required. We note that it has also been sug-601 gested that vertical piles of lower-mantle slabs could only be produced in the context of 602 a fixed overriding plate Lee & King (2011); Běhounková & Cížková (2008); Cížková & 603 Bina (2013); Billen & Arredondo (2018). Here we have demonstrated that vertical slab 604 folding slab can also occur in simulations with a WAL, in which trench retreat remains 605 self-consistently limited (Fig. 8). 606

### 607 Conclusion

Previous numerical and analogue models of subduction dynamics tend to produce surface 608 kinematics and lower-mantle slab morphologies that do not match first-order observa-609 tional constraints. We have shown that including a weak asthenospheric layer below the 610 lithosphere into numerical models of subduction dynamics eliminates these mismatches. 611 The lubricating effect of the asthenosphere produces a velocity increase of the subducting 612 plate and a reduction of trench retreat, yielding predicted velocities that closely match 613 those recorded on Earth. These velocity changes are sustained long after the subducting 614 slab has penetrated into the lower mantle. The surplus of rapidly subducting lithosphere 615 is accommodated by folding, rather than by accelerating trench retreat or slab sinking. 616 This leads to an apparent horizontal widening of the slab in the lower mantle, as is ob-617 served by seismic tomography. Substantial near-vertical slab piles accumulate over time 618 because trench motion is limited. We find that a viscosity reduction below the plate by 619 a factor of only 2 to 5 is sufficient to completely shift the dynamics in these models – 620 from non-folding with slow subduction and substantial trench retreat, to regimes of mul-621 tiply folded, wall-like slab piles under near-stationary trenches. The latter then dominate 622 across a wide parameter space of subducting and overriding plate ages. Our results pro-623 vide strong independent support for the presence of a weak asthenospheric layer beneath 624 Earth's lithosphere. 625

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