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1 **Advecting Superspecies: Efficiently Modeling**
2 **Transport of Organic Aerosol with a Mass-Conserving**
3 **Dimensionality Reduction Method**

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12 **Key Points:**

- 13 • We develop a machine learning method to find a reduced-dimension set of
14 superspecies representing tracers in a chemical transport model
15 • This method is designed to be physically consistent, preserving information on
16 phase and conserving mass to numerical precision
17 • Advecting the superspecies reduces computation time to 56-66% of the
18 original advection computation time

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19 **Abstract**

20 The chemical transport model LOTOS-EUROS uses a volatility basis set (VBS)
21 approach to represent the formation of secondary organic aerosol (SOA) in the
22 atmosphere. Inclusion of the VBS approximately doubles the dimensionality of
23 LOTOS-EUROS and slows computation of the advection operator by a factor of
24 two. This complexity limits SOA representation in operational forecasts. We develop
25 a mass-conserving machine learning (ML) method based on matrix factorization to
26 find latent patterns in the VBS tracers that correspond to a lower-dimension set of
27 superspecies. Tracers are reversibly compressed to superspecies before transport, and
28 the superspecies are subsequently decompressed to tracers for process-based SOA
29 modeling. This physically interpretable ML method conserves the total
30 concentration and phase of the tracers throughout the process. The superspecies
31 approach is implemented in LOTOS-EUROS and found to accelerate the advection
32 operator by a factor of 1.5 to 1.8. Concentrations remain numerically stable over
33 model simulation times of two weeks, including simulations at higher spatial
34 resolutions than the ML models were trained on. Results from this case study show
35 that this method can be used to enable detailed, process-based secondary organic
36 aerosol representation in air quality operational forecasts in a computationally
37 efficient manner. Beyond this case study, the physically consistent ML approach
38 developed in this work enforces conservation laws that are essential to other Earth
39 system modeling applications, and generalizes to other processes where
40 computational benefit can be gained from a two-way mapping between detailed
41 process variables and their representation in a reduced-dimensional space.

42 **Plain Language Summary**

43 The chemical composition of the atmosphere is a complex system involving
44 many physical processes. Computer models can be used to improve our
45 understanding of how these processes interact, as well as simulate hypothetical
46 scenarios to support scientifically-informed climate and air quality policies. However,
47 complicated models with many variables can take a lot of time to run. The
48 LOTOS-EUROS model spends a lot of time and energy on computer simulations of
49 the transport of chemical species, like particulate matter, by wind. Our method
50 combines artificial intelligence with scientific fundamentals to reduce the number of
51 variables: we model representative combinations of chemical species that are
52 transported all at once, rather than transport each species individually. This leads
53 to faster and cheaper simulations without loss of scientific detail or internal
54 consistency.

55 1 Introduction

56 Vast amounts of computational resources are required to model phenomena in
57 the earth sciences. This includes complex models of atmospheric composition that
58 couple a large number of properties and processes (Brasseur & Jacob, 2017).
59 Machine learning (ML) approaches are an emerging technique for decreasing the
60 computational burden of earth system models with more efficient ML
61 parameterizations, but have documented challenges such as unstable error growth
62 and physical inconsistency which can happen when predicted recurrently (Kelp et
63 al., 2018) or when interacting with other processes in the context of larger models
64 (Rasp et al., 2018; Brenowitz & Bretherton, 2019). One approach towards ML
65 models that can stably interact with other model processes is online training:
66 parameter optimization of ML surrogates while running the entire model (Rasp,
67 2020; Kelp et al., 2022).

68 Other recent efforts have aimed to constrain ML approaches using scientific
69 knowledge to ensure physically consistent results. One strategy for physically
70 consistent ML models reposes the learning targets: rather than estimate important
71 properties or their tendencies, instead estimate fluxes between the properties. The
72 fluxes can then be related to tendencies in a way that balances mass, energy, or
73 atoms (Sturm & Wexler, 2020; Yuval, O’Gorman, & Hill, 2021; Sturm & Wexler,
74 2022). Custom neural network architectures can also obey conservation laws by
75 incorporating hard constraints (e.g. flux balances) in their hidden layers (Beucler et
76 al., 2021; Sturm & Wexler, 2022): this can also improve the physical interpretability
77 of the inner working of neural networks. Acknowledgement of the importance of
78 physically consistent ML tools in the earth sciences (Keller & Evans, 2019; Yuval,
79 Pritchard, et al., 2021) has informed the mass-conserving machine learning
80 parameterization in this paper.

81 Within the field of atmospheric chemistry modeling, Kelp et al. (2020) have
82 made progress towards a stable ML neural network emulating a box model of
83 chemistry and aerosol microphysics processes, through training parameters on the
84 accuracy of multiple future timesteps after predicting in a lower-dimensional latent
85 space. Kelp et al. (2020) pose a future research direction: how the low-dimensional
86 representation of chemical species might interact with other processes, such as
87 advection, in a larger 3-dimensional model.

88 The current work develops and explores a physically consistent machine
89 learning method that compresses the high dimensional set of organic aerosol (OA)
90 tracers to reduce the computational cost of advection in the LOTOS-EUROS
91 chemical transport model (CTM) (Manders et al., 2017). We use unsupervised
92 machine learning approaches to find manifold dimensions, or characteristic regimes,
93 of organic aerosol tracers. The characteristic regimes are used to form
94 lower-dimensional combinations of OA tracers, interpreted as superspecies, which
95 require fewer transport calculations. These superspecies are mapped back to the full
96 OA tracer space after the advection operator. Additional constraints are applied
97 when compressing to and decompressing from the reduced-dimension space, to
98 conserve mass to machine precision. We compare the linear and additive method of
99 non-negative matrix factorization to a nonlinear and more complex neural network
100 autoencoder, and make a model selection after evaluating several configurations
101 based on reconstruction accuracy and physical consistency.

102 Organic aerosol forms an important contribution to particulate matter
103 (Jimenez et al., 2009). OA can be emitted to the atmosphere as semi-volatile
104 primary organic aerosol (POA) through various direct sources, including vehicle
105 exhaust, wildfire smoke, and residential wood combustion. OA can also be formed in
106 the atmosphere as secondary organic aerosol (SOA) through gas-phase reactions of

107 volatile organic compounds (VOCs), which tend to form less volatile products: semi
108 and intermediate volatility organic compounds (siVOCs) that can partition
109 appreciably to the particle phase. Both anthropogenic sources, like industrial
110 activity, and biogenic sources, such as forests, emit VOC precursors to SOA.
111 Another source of SOA is the partial evaporation of POA to siVOCs, which in turn
112 react and partition to form SOA (Robinson et al., 2007). This SOA from evaporated
113 and aged POA is often chemically distinct from POA, showing a higher degree of
114 oxidation (Jimenez et al., 2009), and can be tracked separately in models. SOA can
115 form a significant fraction of the total OA concentration (de Gouw et al., 2005;
116 Heald et al., 2005).

117 Due to the large number of distinct organic species in the atmosphere, organic
118 aerosols are rarely speciated in models, but often lumped together into volatility
119 bins according to the magnitude of their saturation vapor pressures (Donahue et al.,
120 2006). This modeling approach is called the volatility basis set (VBS) and accounts
121 for the tendency of compounds to become less volatile as they are oxidized. The
122 partitioning between gas and particle phase in each volatility bin is governed by its
123 corresponding saturation vapor pressure and the total OA concentration. A 2D-VBS
124 extension has also been developed that includes oxygen to carbon ratio along
125 another dimension (Jimenez et al., 2009; Donahue et al., 2011), which can account
126 for fragmentation of larger compounds and estimation of hygroscopicity (Jimenez et
127 al., 2009). However, the 1D-VBS approach is most commonly applied in chemical
128 transport models, including separate basis sets for different classes of OA precursors
129 (Bergström et al., 2012; Hayes et al., 2015; Janssen et al., 2017; Jiang et al., 2019)
130 Use of multiple VBS classes enables distinct properties per class and can give insight
131 into different aerosol systems contributing to total OA. However, increased
132 complexity and dimensionality adds a computational burden to CTM calculations.
133 This limits the inclusion of detailed, process-based OA modeling in chemical
134 transport models like LOTOS-EUROS v2.2.1 (Manders-Groot et al., 2021), which
135 uses 4 VBS classes based on the configuration from Bergström et al. (2012). The
136 VBS module in LOTOS-EUROS v2.2.1 is not used by default, and when included,
137 significantly increases wall time of simulations. The inclusion of VBS tracers adds
138 computation time to other operators in the model relatively more than OA-specific
139 calculations themselves.

140 Most notably, the high dimensionality caused by the VBS tracers adds a
141 computational burden to the advection operator in LOTOS-EUROS v2.2.1, which is
142 based off of Walcek (2000). Model timing experiments in Sturm (2021) found that
143 wall time for the advection operator can double when using the VBS module.
144 Advection is a bulk process and does not perform OA-specific calculations. This
145 motivates a reduced-order approach: rather than advecting each tracer separately,
146 instead advect a smaller set of superspecies formed from combinations of the VBS
147 tracers. We leverage the large amount of model output for the VBS tracers, and
148 develop a mass-conserving, data-driven machine learning approach to find latent
149 patterns in the VBS tracers that allow for a more parsimonious representation of OA
150 in transport processes. Though demonstrated for compression of OA and related
151 compounds during transport, the methods developed in this work generalize to other
152 Earth system applications, enabling use of high-dimensional process models whose
153 variables can be reversibly compressed to a physically consistent reduced-dimension
154 representation for use in other processes.

2 Materials and Methods

2.1 VBS approach in LOTOS-EUROS

The chemical transport model LOTOS-EUROS v2.2.1 uses a VBS scheme based off of the approach in Bergström et al. (2012) that has 4 distinct VBS classes: POA, SOA from siVOCs that are chemically aged after evaporating from semi-volatile POA emissions, (abbreviated as siSOA), and SOA from anthropogenic and biogenic gaseous VOCs abbreviated as aSOA and bSOA respectively.

Figure 1 provides an overview of the 58 tracers specific to the VBS module. Primary organic material (POM) emissions are modeled using a 9-bin VBS approach: the logarithmically distributed bins represent semi-volatile organics with effective saturation concentrations ranging from 10^{-2} to $10^5 \mu\text{g m}^{-3}$ at 298 K. The reported mass of primary emissions is distributed over the lower 4 volatility bins. As in previous work (Shrivastava et al., 2008), an additional 1.5 times this mass is distributed over the highest 5 volatility bins to represent non-reported intermediate volatility organic compounds (IVOCs). Only a fraction of the total mass remains in the particle phase: the fraction that evaporates is assumed to be semi-volatile VOCs (SVOCs), with effective saturation concentrations on the order of $1 < C^* < 10^3 \mu\text{g m}^{-3}$ or IVOC, with saturation concentrations on the order of $10^3 < C^* < 10^6 \mu\text{g m}^{-3}$, defined at 298 K. The S/IVOCs undergo oxidation by the hydroxyl radical OH and enter the distinct siSOA VBS class. As material moves from the POA VBS to the siSOA VBS, it also moves to lower volatility bins, as shown in Figure 1. The total siSOA is represented by an 8-bin VBS using effective saturation concentrations from 10^{-2} to $10^3 \mu\text{g m}^{-3}$ (defined at 298 K). Each bin uses two tracers, one aerosol and one gas, to represent the partitioning: this results in 18 tracers for the POA VBS class and 16 tracers for the siSOA VBS class.

Formation of SOA from anthropogenic VOCs is represented with a 6-bin VBS class, defined using effective saturation concentrations of 10^{-2} to $10^3 \mu\text{g m}^{-3}$ at 298 K. This results in 12 tracers (6 in the gas phase and 6 in the particle phase). VOCs such as aromatics, alkenes and alkanes are classified in LOTOS-EUROS as anthropogenic precursors of secondary organic aerosols and upon oxidation are distributed over the 4 highest volatility bins as done by Tsimpidi et al. (2010), linearly interpolating between a low-NOx and high-NOx case as originally suggested by Lane et al. (2008).

An analogous 6-bin VBS class is used to model SOA formation from the biogenic VOCs in LOTOS-EUROS: monoterpene and isoprene. Yields from biogenic gaseous precursors are distributed over the 4 highest volatility bins according to Tsimpidi et al. (2010), with yields calculated by a branching ratio continuously dependent on NOx (Lane et al., 2008). Unlike the anthropogenic VBS class, ageing between bins is turned off for the biogenic VBS in LOTOS-EUROS v2.2.001, as in prior work (Murphy & Pandis, 2009; Tsimpidi et al., 2010, 2014; Matsui, 2017). This is informed by the low sensitivity of biogenic SOA concentration to oxidative ageing (Ng et al., 2006; Donahue et al., 2012), thought to arise from fragmentation effects that balance out functionalization effects on volatility (Murphy et al., 2012). For this reason, material never enters the 2 lowest volatility bins in LOTOS-EUROS v2.2.1, rendering the 4 corresponding tracers effectively inert. However, in LOTOS-EUROS v2.2.1 with the VBS module on, these 4 tracers are still dealt with by the model, contributing to the computational burden on processes such as advection.

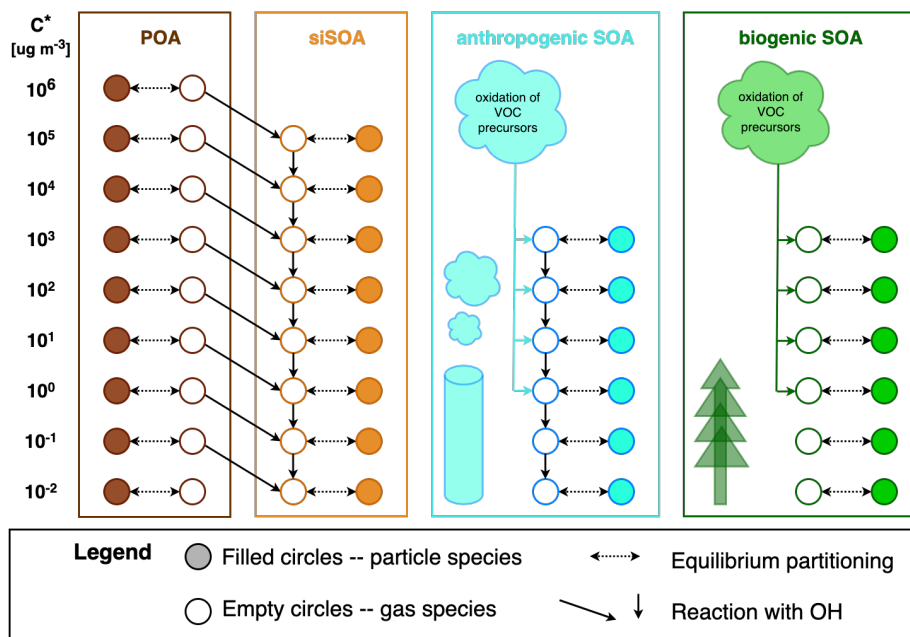


Figure 1. Schematic representation of the VBS approach in LOTOS-EUROS v2.2.1, including the 4 VBS classes with 58 tracers, and their thermodynamic and chemical relationships. This diagram was inspired by the schematic in Shrivastava et al. (2008).

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2.2 Tracer compression methods

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A method for tracer compression for transport in the GEOS-Chem global CTM is given by Liao et al. (2007), where various oxidation products are lumped together by phase and class, and assumed to behave similarly in transport. The relative compositions are stored separately and used to distribute the lumped tracers back to individual products after transport. Another approach for OA tracers given by Matsui (2017) compresses VBS tracers in a global aerosol model from 106 to 26 (a compression factor of approximately 4) by using fewer volatility bins. This effectively lowers the bin resolution and combines material across a wider range of saturation vapor pressures. Analogously, Matsui (2017) converts between high-resolution and low-resolution bins in a sectional aerosol model for use in processes not directly related to aerosols. An example of tracer compression for advection in a 2D-VBS is given by Zhao et al. (2020) who sum tracers along the O:C axis, resulting in a 1D-VBS for decreased dimensionality in advection.

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One compression technique for advection of 1D-VBS tracers could be developed based on partitioning, where the compressed tracers themselves contain all the information needed to decompress to the VBS tracer space without losing resolution. The total concentration for each volatility bin could be advected, as well as total OA concentration, reducing the 58 phase-specific tracers to 29 combined phase tracers, and an additional tracer to keep track of total organic aerosol concentration. After advection, total OA along with the saturation vapor

224 concentration determines the partitioning between phase in each volatility bin. This
 225 compression is not "lossy", meaning no information is lost on compression itself.
 226 However, such a strategy yields a compression factor of only approximately 2, about
 227 halving the number of tracers. We seek a compression technique that can reduce the
 228 number of tracers further, which may be lossy but leverages a large amount of
 229 representative model output, using machine learning algorithms optimized to
 230 accurately reconstruct VBS distributions.

231 **2.3 Model Configuration**

232 To find latent patterns for a reduced order representation of the 58 VBS
 233 tracers, we use LOTOS-EUROS version 2.2.1 (Manders-Groot et al., 2021; Manders
 234 et al., 2017) with the optional VBS module. The model was used in its default
 235 configuration using 5 levels, the first one being a 25 m surface layer, the second layer
 236 reaching the top of the mixing layer, and the other three layers being reservoir layers
 237 up to 5 km altitude. The horizontal domain covers 15°W to 35°E and 35-70°N on a
 238 lonxlat grid of 0.5x0.25°. This grid is termed the 'MACC' grid, referring to the grid
 239 used in the project 'Monitoring Atmospheric Composition and Change, a
 240 predecessor of the current CAMS (Copernicus Atmospheric Monitoring Service).
 241 Meteorology is taken from ECMWF IFS 12-hour operational forecasts, using hourly
 242 surface values and 3-hour 3-D fields interpolated to hourly values. For gas-phase
 243 chemistry, a condensed and slightly modified version of CBM-IV is used (Gery et al.,
 244 1989). Wet deposition includes in-cloud and below-cloud scavenging as described in
 245 Seinfeld and Pandis (2006), deposition of gases is calculated using DEPAC (Zanten
 246 et al., 2010), and deposition of particles follows Zhang (2001). The model includes
 247 tree-specific biogenic isoprene and terpene emissions as described in Beltman et al
 248 (2013) using a high-resolution tree-species database (Köble & Seufert, 2001) that are
 249 combined with land cover data from CORINE2000 (EEA, 2005). Anthropogenic
 250 emissions are CAMS emissions for 2015 (CAMS-regional air pollutants as delivered
 251 in 2018) with a bottom-up estimation for residential wood combustion emissions,
 252 providing the best estimate of organic carbon emissions (Denier van der Gon et al.,
 253 2015). Wildfire emissions are taken from the MACC global fire assimilation system
 254 (Kaiser et al., 2012). Initial and boundary conditions for most species were taken
 255 from CAMS-near real-time, for organic matter no boundary conditions were used.

256 Short simulations of 14 days in the last two weeks of February and July 2018
 257 were used with 5 days of spin-up, the subsequent 5 days for training and the last 4
 258 days for evaluation. Evaluation of the simulations with observations is outside the
 259 scope of the present paper, as the model is regularly evaluated in model validation
 260 reports, as well as CAMS ensemble and model evaluations.

261 **2.4 Linear Approach**

262 A linear approach could be used to project the tracer space into a lower
 263 dimensional subspace allowing linear combinations of the tracers to be passed to the
 264 advection operator. Principal component analysis is a common linear projection
 265 method but is mean-centered and can lead to negative values, which are less readily
 266 interpretable as concentrations. Non-negative matrix factorization (NMF), also
 267 called positive matrix factorization, is an unsupervised machine learning algorithm
 268 chosen in applications where values must remain non-negative, for example pixel
 269 values in image compression (Lee & Seung, 1999) or concentrations in the physical
 270 sciences (Paatero & Tapper, 1994). Given a matrix of non-negative data $\mathbf{V} \in \mathbb{R}^{m \times n}$
 271 with m dimensions and n data points, the NMF algorithm returns two non-negative
 272 approximate factors of \mathbf{V} according to an objective function

$$\underset{\mathbf{W}, \mathbf{H}}{\operatorname{argmin}} \|\mathbf{V} - \mathbf{WH}\| \quad \text{s.t.} \quad \mathbf{W}, \mathbf{H} \geq 0 \quad (1)$$

where $\mathbf{W} \in \mathbb{R}_{\geq 0}^{m \times r}$ is a mapping from the m dimensional space to a lower dimensional latent space with r features, and $\mathbf{H} \in \mathbb{R}_{\geq 0}^{r \times n}$ is the latent space representation of each data point. The inequality is interpreted as an element-wise constraint. We use the Frobenius norm in the objective function, which is the default NMF norm in the scikit-learn Python package (Pedregosa et al., 2011).

The NMF algorithm operates on a data matrix, handling batches of observations all at once. For our application, compression of current concentrations of VBS tracers $\vec{v} \in \mathbb{R}^m$ to a lower dimensional space needs to happen with each new time step. For the purpose of speeding computations, it might be counterproductive to perform the NMF algorithm online in every time step. If \mathbf{W} is optimized using equation 1 on sufficiently representative training data, it can be used to decompress a set of superspecies $\vec{h} \in \mathbb{R}^r$ to a decompressed set of tracers $\vec{v}_{dec} \in \mathbb{R}^m$ to approximate \vec{v} . However, we still need to obtain the superspecies vector \vec{h} . Given a sufficiently representative \mathbf{W} , we can use its Moore-Penrose pseudoinverse $\mathbf{W}^+ \in \mathbb{R}^{r \times m}$ to compress a new set of tracers \vec{v} to a corresponding set of new superspecies \vec{h} . \mathbf{W}^+ may have negative elements for $r > 1$ (more than one superspecies, or degree of freedom), theoretically yielding negative superspecies values or decompressed tracer values. This potential limitation is quantified in section 3.2. Instead of a Moore-Penrose pseudoinverse, a positive-valued compression matrix $\mathbf{B} \in \mathbb{R}_{\geq 0}^{r \times m}$ can be obtained by similar non-negative matrix factorization methods, using the objective function:

$$\underset{\mathbf{B}}{\operatorname{argmin}} \|\mathbf{H} - \mathbf{BV}\|_F^2 \quad \text{s.t.} \quad \mathbf{B} \geq 0 \quad (2)$$

The full approach to obtain non-negative compression and decompression matrices then becomes

- 296 1. Given tracer data \mathbf{V} , find \mathbf{H} , \mathbf{W} such that $\mathbf{V} - \mathbf{WH}$ is minimized.
- 297 2. Given tracer data \mathbf{V} , and using \mathbf{H} from the previous step, find \mathbf{B} such that
- 298 $\mathbf{H} - \mathbf{BV}$ is minimized.
- 299 3. Use \mathbf{B} to compress subsequent observations of VBS tracers \vec{v} to a
- 300 non-negative vector of superspecies \vec{h} , and \mathbf{W} to decompress \vec{h} to the original
- 301 tracer space \vec{v}_{dec} .

The compression and decompression matrices \mathbf{B} and \mathbf{W} are optimized for each VBS class, to avoid mixing different classes of OA that have different properties (e.g. molar mass). An important hyperparameter of this approach is r , the size of the latent space (number of superspecies). This can be chosen by constructing an elbow plot of error metrics with varying r , while also considering compression factor.

307 2.5 Nonlinear Approach

We investigate whether a more complicated model than the pair of non-negative matrices is appropriate for compressing VBS tracers. Given the recent success of artificial neural networks (NNs) in emulating models of atmospheric phenomena (Beucler et al., 2021; Kelp et al., 2020), we construct a neural network autoencoder that can reversibly compress the VBS tracers to a latent space. Neural networks are connected networks of artificial neurons: each neuron calculates a linear combination of its input, adds a bias scalar, and feeds this result to a (usually non-linear) activation function (Marsland, 2014). Neurons performing this operation

316 on the same input in parallel are designated as a layer within the neural network.
 317 Neural networks can have multiple such layers: vector output from neuron layers
 318 that are not final output of the NN are called hidden layers. A neural network
 319 autoencoder attempts to replicate the identity function via compression, where
 320 hidden layers compress the input to the NN to a smaller latent space of size r . For
 321 our application, the activation function chosen for each neuron is a rectified linear
 322 unit that outputs the maximum of its input and zero. This choice of activation
 323 function constrains output of both the hidden layer and the NN output to their
 324 respective positive half-spaces. In other words, like the non-negative
 325 compression/decompression matrices in section 2.4, this activation function ensures
 326 concentrations will not go below zero.

327 While matrix multiplication to a lower-dimensional space is also part of the
 328 linear approach in section 2.4, the neural network adds complexity in its parameter
 329 space via multiple layers with weight parameters, as well as bias and activation
 330 functions between layers of neurons. This model should be chosen if it significantly
 331 outperforms the linear method using the same size r . As the NNs are compared
 332 directly to the linear method, one NN per VBS class is chosen.

333 Training a neural network involves optimizing the coefficients of the linear
 334 combination and bias scalar for each perceptron through local minimization
 335 methods, often gradient descent. To prevent overfitting of the NNs, dropout layers
 336 are used to temporarily remove some neurons during training, and training of NNs is
 337 stopped if predictions are not improved on a set of validation data after a certain
 338 number of passes through the training data. The neural network models are
 339 constructed and trained using the Keras library (Chollet et al., 2015) using a
 340 Tensorflow backend (Abadi et al., 2016).

341 2.6 Physically Consistent Models: Conserving Mass and Phase

342 Sections 2.4 and 2.5 developed methods to ensure non-negativity of both the
 343 compressed superspecies and decompressed tracers. This section refines the linear
 344 method to encode other physical information: concentration and phase.

345 An advantage of the linear method is that the direction of the decompressed
 346 tracer space is invariant to scaling of the superspecies space. In other words, the
 347 concentration of superspecies can be adjusted without changing the relative
 348 volatility distribution of the decompressed tracers. We can use a scaling factor after
 349 compression to ensure that the total concentration of superspecies is equal to the
 350 total concentration of the tracers for each VBS class. Similarly, after decompression,
 351 we can ensure that the total concentration of decompressed tracers is equal to the
 352 total concentrations of superspecies. This ensures that compression and
 353 decomposition neither add nor remove mass. The scaling factor s_{com} after using \mathbf{B}
 354 to compress tracers \vec{v} to the superspecies vector \vec{h} is

$$s_{com} = \frac{\sum_{i=1}^m v_i}{\sum_{j=1}^r h_j} \quad (3)$$

355 After decompression to \vec{v}_{dec} using \mathbf{W} , the decompressed tracers can be scaled
 356 using a factor s_{dec} , where

$$s_{dec} = \frac{\sum_{j=1}^r h_j}{\sum_{i=1}^m v_{dec,i}} \quad (4)$$

357 Despite conserving total concentration of all tracers, the concentration of total
 358 organic aerosol (TOA) may not be conserved due to errors in the mass distribution
 359 over volatility bins after decompression. A variation of this method to conserve TOA
 360 instead of total concentration, as well as an alternative way to conserve total
 361 concentration only using \mathbf{W} from NMF, is explored in Sturm (2021). However, the
 362 compromise of conserving TOA versus total concentration is avoidable by adding
 363 another cross section: creating compression and decompression matrices \mathbf{B} and \mathbf{W}
 364 for each phase as well as VBS class, e.g. one transformation for all biogenic gaseous
 365 VBS tracers and a separate transformation for all biogenic particle tracers.

366 2.7 Implementing the ML Parameterization into a CTM

367 We select the most promising method (section 3.3) based on accuracy,
 368 compression factor, and physical consistency. This method is then built into a
 369 version of LOTOS-EUROS v2.2.1, extended to include the ML superspecies
 370 parameterization. Additional tracers for superspecies are added to the model and
 371 adopt the characteristics of their respective tracers. Subroutines were added to the
 372 VBS module to load the ML parameterizations, as well as perform the compression
 373 and decompression operations. These subroutines are then called in the driver
 374 program:

- 375 1. The initialization subroutine loads offline-optimized ML parameterizations
 376 before the time loop starts.
- 377 2. Within the time loop, directly before the call to the advection operator, the
 378 compression subroutine is called to map VBS tracers to superspecies
 379 concentrations, overwriting the current superspecies values. The advection
 380 operator is resolved using superspecies instead of the VBS tracers, which are
 381 skipped.
- 382 3. Within the time loop, directly after the call to the advection operator, the
 383 decompression routine is called to transform superspecies into VBS tracers,
 384 overwriting previous VBS tracer values which were not included in advection
 385 calculations.

386 3 Results: Model Development and Selection

387 3.1 Compression Factor and Accuracy

388 To obtain a sense of error obtained by a maximum compression factor and the
 389 simplest model, we use NMF with a single superspecies ($r = 1$) per VBS class to
 390 obtain a decompression matrix (in this case a vector) \mathbf{W} and calculate its
 391 pseudoinverse \mathbf{W}^+ to be used for compression. This compression strategy is
 392 evaluated on reconstruction accuracy of test model output of the entire domain and
 393 time period, using average bias and root mean square error (RMSE). While bias is
 394 an indicator of the total material that is introduced or removed artificially by
 395 compression, RMSE is an absolute metric that indicates how accurately the
 396 reconstructed VBS tracers reproduce the volatility distribution. Table 1 shows both
 397 reconstruction error metrics for the tracer set of each class, as well as the
 398 reconstruction bias and RMSE's of total organic aerosol concentration (TOA) and
 399 total organic material (TOM) from summing across VBS classes. The mean

400 concentrations for each VBS class, as well as TOA and TOM, are included for
 401 comparison.

Table 1. Test reconstruction error metrics using the NMF/Pseudoinverse approach with 1 superspecies per VBS class.

	Mean [$\mu\text{g m}^{-3}$]	RMSE [$\mu\text{g m}^{-3}$]	Bias [$\mu\text{g m}^{-3}$]
aVOC	0.0043	0.0021	-3.9×10^{-6}
bVOC	0.0262	0.0061	2.9×10^{-4}
POA	0.0558	0.0441	-0.0021
siSOA	0.0153	0.0205	6.4×10^{-5}
TOA	0.386	0.266	0.094
TOM	1.61	0.0978	-0.0328

402 Moreover, by the use of a single superspecies ($r = 1$) the tracers pass through a
 403 linear transformation of rank 1: the concentration distribution over the volatility bins
 404 will always have the same shape, with gridcells and different time steps differing only
 405 in magnitude, as scaled by h . This means any spatiotemporal variability of the
 406 distribution shape will be lost after passing through a single-dimensional
 407 superspecies space. More complexity is needed to capture variation in volatility
 408 distribution. This motivates larger matrices that have more degrees of freedom r ,
 409 which comes at the cost of compression factor: the inevitable trade-off between
 410 accuracy and computational speed is a canonical problem in atmospheric chemistry
 411 modeling. Figure 2 visualizes the effect of compression extent on accuracy, using
 412 \mathbf{W}^+ to convert to superspecies and \mathbf{W} to map back to tracers. Reconstruction
 413 accuracy is reported for the set of tracers in each class (both particle and gas) as
 414 well as TOA (total organic aerosol, calculated by summing the concentrations of
 415 particle tracers across classes).

416 Figure 2 shows RMSE monotonically decreasing with increasing number of
 417 superspecies, with diminishing returns after 3 superspecies. More superspecies to
 418 advect will increase the computational burden of the advection operator in
 419 LOTOS-EUROS without a substantial improvement in RMSE or bias. In light of
 420 the desire to maximize compression factor, the two elbow plots indicate that 3
 421 superspecies strikes a good balance between dimension reduction and accuracy.
 422 Using 3 superspecies per class ranges from a compression factor of 4 (the aVOC and
 423 bVOC basis sets) to 6 (the POA basis set) with a significant improvement in
 424 accuracy from 2 superspecies and minimal improvement in accuracy when using 4
 425 or more superspecies.

426 Improved accuracy with number of superspecies comes from the increased
 427 degrees of freedom, as each subsequent column of \mathbf{W} adds another basis direction.
 428 Each column of \mathbf{W} , when normalized, can also be interpreted as a superspecies of
 429 unit concentration, and its elements corresponding to composition of VBS tracers.
 430 Each superspecies can also be interpreted as a different regime of organic aerosol,
 431 found through a data-driven method. Multiple superspecies can be combined in
 432 different amounts, corresponding to their concentrations, to form other distributions.

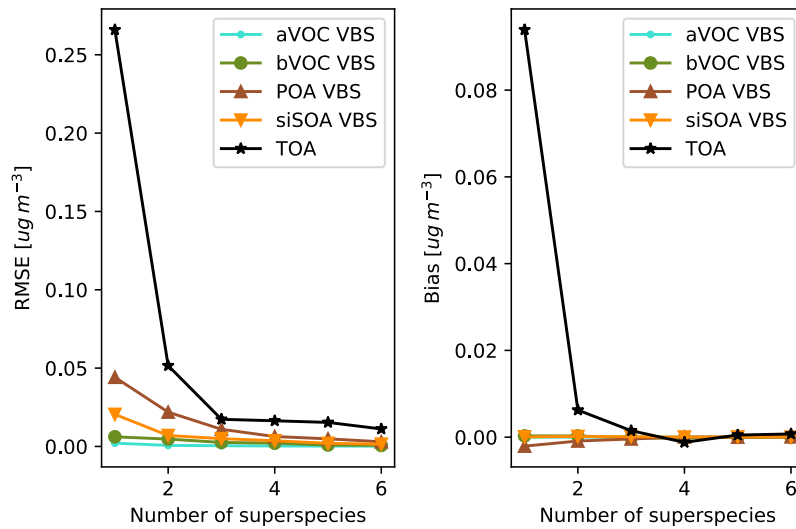


Figure 2. Relationship between the number of superspecies and the RMSE and bias for the 4 VBS classes, as well as TOA. There are diminishing returns in accuracy after 3 superspecies per VBS class.

3.2 Physical Consistency of Results

3.2.1 Motivating Non-negative Constraints

Section 2.4 raised the theoretical possibility of obtaining negative concentrations when using the pseudoinverse \mathbf{W}^+ to compress tracers into superspecies. Negative elements in \mathbf{W}^+ can lead to negative superspecies. Negative superspecies concentrations are not directly a problem, as the current advection scheme in LOTOS-EUROS v2.2.1 is based on that of Walcek (2000), which is able to handle negative tracer values. However, using the non-negative \mathbf{W} to decompress negative superspecies concentrations back to the tracer space can lead to negative tracer values. Here, we quantify this limitation in practice using 3 superspecies.

Negative concentrations that are extremely small in magnitude can be approximated as zero. This tolerance can of course be set to a threshold, for example $-1 \times 10^{-8} \mu\text{g m}^{-3}$. However, using the test data of the POA VBS as an example, there are over 4.7 million cases in the test data where a POA VBS tracer is below $-1 \times 10^{-8} \mu\text{g m}^{-3}$, which is more than 19% of the 24 million values in the test data for the POA VBS.

One could choose a more relative, less arbitrary tolerance: for instance, all concentrations that are more negative than the magnitude of the corresponding bias for each VBS. These "significantly negative" concentrations would be negative even after an additive bias correction. For the POA VBS, there were 855,083 such concentrations, about 3.5% of the total test data. Using this relative tolerance, other VBS classes showed even larger proportions of "significantly negative" concentrations: 4.2%, 5.6%, and 7.0% respectively for the siSOA, aSOA, and bSOA VBS classes (for the anthropogenic VBS and siSOA VBS, which had positive biases, the tolerance was chosen to be the negative magnitude of the corresponding bias).

458 Using the pseudoinverse \mathbf{W}^+ for compressing VBS tracers can result in a
 459 number of significantly negative values when using 3 superspecies per VBS class,
 460 which motivates the development of non-negative compression strategies. For each
 461 VBS class, we find a positive compression matrix \mathbf{B} to replace \mathbf{W}^+ , according to the
 462 objective function and constraints in equation 2.

463 We compare this matrix factorization approach with a neural network
 464 autoencoder approach for each VBS class. We construct and train a 5-layer neural
 465 network autoencoder with rectified linear unit activation functions in the
 466 superspecies and output layers to ensure non-negativity of both superspecies and
 467 decompressed VBS tracers. In other hidden layers, a sigmoidal activation function,
 468 hyperbolic tangent, is used. In training, a dropout rate of 0.1 is used for every layer
 469 except for the superspecies layer. Figure 3.2.1 shows the general layer and node
 470 architecture of both anthropogenic and biogenic NN autoencoders: the autoencoders
 471 for the POA and siSOA VBS classes vary only in the dimensionality of their input
 472 and output layers (18 and 16 values, as opposed to 12). For the autoencoder of each
 473 VBS class, the center superspecies layer is chosen to have 3 values: the value of this
 474 hyperparameter is chosen for comparison to the linear matrix factorization approach.
 475 Both the matrix factorization and autoencoder approaches are evaluated on how well
 476 they reconstruct the tracers after decompression.

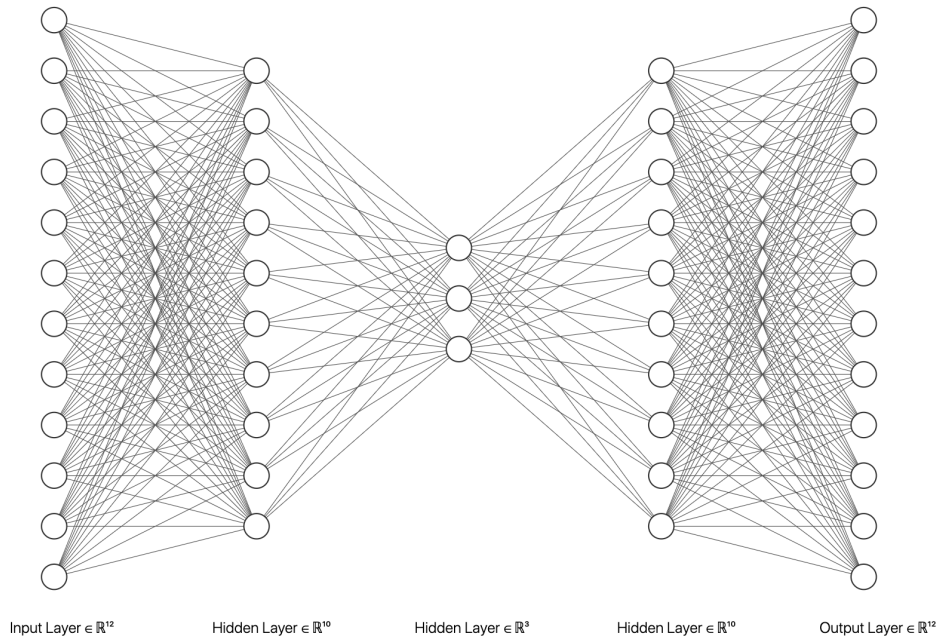


Figure 3. Neural network autoencoder architecture for the anthropogenic and biogenic VBS classes, compressing 12 tracers to 3 superspecies and back again. The central layer of 3 superspecies uses a ReLu activation function, as well as the output layer, to ensure semi-positivity. The autoencoders for the other VBS classes have analogous architectures, differing only in the size of input and output layers: 18 nodes for POA and 16 nodes for siSOA. This figure was generated using the tool from LeNail (2020).

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3.2.2 Conserving Mass and Phase

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Section 2.6 proposed a method for conserving total concentration of the VBS tracers in both the superspecies representation and in subsequent reconstruction to decompressed tracers. Applying this method to the cross-sections of VBS class and phase (particle or gas) ensures that the superspecies transformation does not add or remove mass artificially in the gas and particle phases of every class: this necessitates conservation of total gas concentration, total aerosol concentration, and concentration of total organic material (TOM). Phase-specific superspecies are composed of entirely gas or entirely aerosol tracers, conserving information on phase while in the latent space representation.

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Phase-specific superspecies require adding another cross-section, halving the number of tracers to be compressed and decompressed by each pair of \mathbf{B} and \mathbf{W} , respectively. For this reason, continuing to use 3 superspecies for each phase within each VBS class would reduce the compression factor to slightly over 2.4, not much better than compression factor of around 2 when using the non-lossy partitioning approach. However, using only 1 superspecies per phase per class would fix each corresponding set of tracers to a single shape upon reconstruction, analogously to the discussion in section 3.1. To ensure that this method captures spatiotemporal variability of volatility distributions, while maintaining a decent compression factor, we choose to use 2 superspecies per phase per VBS class. This design choice results in a compression factor of approximately 3.6. Its accuracy is compared to the other strategies in the model selection process in section 3.3.

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Figure 4 demonstrates the mass-conserving properties of this approach using representative examples of the primary organic aerosol VBS distribution at two different atmospheric monitoring sites: the Cabauw Experimental Site for Atmospheric Research in the Netherlands, and Mace Head Atmospheric Research Station in Ireland. Mace Head is as a more pristine and remote station (O'Dowd et al., 2014). The legend in Figure 4 shows that POA concentration at Cabauw is two orders of magnitude higher than that at Mace Head, $4.984 \mu\text{g m}^{-3}$ compared to $0.032 \mu\text{g m}^{-3}$.

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Figure 4 compares the primary VBS distribution to the reconstructed primary VBS distributions after mapping to phase-specific superspecies and back again using two sites: Cabauw and Mace Head, as representative examples. Comparing the legends of (a) with (c), it can be seen that total POA concentration, as well as total concentration of tracers in the gas phase, is conserved to machine precision after passing through compression. The same holds for the total concentrations at Mace Head, (b) and (d), at orders of magnitude more dilute. With phase information and concentration conserved, the only source of error caused by compression to superspecies is in the shape of the distribution. This reconstruction error is more apparent at Mace Head in Figure 4 (b) and (d).

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3.3 Model Selection

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In this section, we compare the four approaches described thus far, and make a judgment about the most promising strategy, evaluated on reconstruction accuracy and physical consistency. The selected approach will be implemented in LOTOS-EUROS v2.2.1 to accelerate the advection operator.

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1. NMF/Pseudoinverse linear approach: NMF to find an optimal decompression matrix \mathbf{W} , and use its pseudoinverse (with negative elements) \mathbf{W}^+ as a compression matrix using 3 superspecies per VBS class

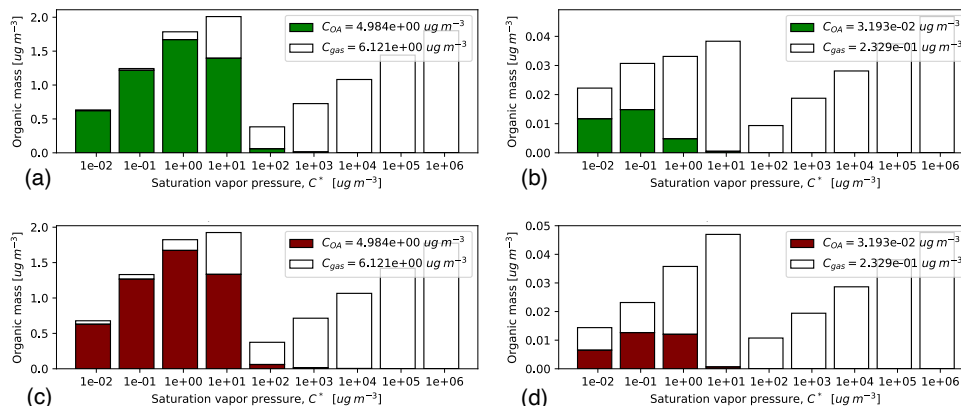


Figure 4. Comparison of the volatility basis set distribution for POA near two sites: Cabauw and Mace Head at a snapshot in time on February 26, 2018. The top row in green shows the distributions as modeled by LOTOS-EUROS at Cabauw (a) and (b) Mace Head. The bottom row in maroon shows the distributions at Cabauw (c) and Mace Head (d) after the non-negative compression/decompression using phase-specific superspecies. Total concentrations are conserved when comparing the legends of the modeled distributions to the reconstructed distributions.

- 525 2. Non-negative linear compression: NMF to find an optimal decomposition
 526 matrix \mathbf{W} , as well as a non-negative compression matrix \mathbf{B} using 3
 527 superspecies per VBS class
 528 3. Non-negative neural network autoencoder: Create a more complicated neural
 529 network with ReLU activation functions in the superspecies and output layers,
 530 using 3 superspecies per VBS class
 531 4. Mass-conserving, non-negative linear compression with phase specific
 532 superspecies: Create \mathbf{W} , as well as a non-negative compression matrix \mathbf{B}
 533 using 2 superspecies per phase per VBS class

534 Tables 2 and 3 show RMSE and Bias of the tracers for each VBS class for the
 535 4 approaches, as well as total organic aerosol (TOA) and total organic material
 536 (TOM) concentrations.

Table 2. Evaluation RMSE of selected approaches. All values reported in $\mu\text{g m}^{-3}$.

-	Approach 1	Approach 2	Approach 3	Approach 4
aVOC VBS	4.4×10^{-4}	0.0010	0.0021	0.0011
bVOC VBS	0.0026	0.0078	0.0181	0.0042
POA	0.0109	0.0285	0.0306	0.0142
siSOA	0.0050	0.0086	0.0094	0.0057
TOA	0.0173	0.133	0.101	6.9×10^{-13}
TOM	0.0547	0.240	0.328	1.0×10^{-12}

537 Using non-negative \mathbf{B} and \mathbf{W} to linearly combine tracers into three
 538 superspecies shows lower RMSE values than the NN autoencoder in Approach 3,

Table 3. Evaluation bias of selected approaches. All values reported in $\mu\text{g m}^{-3}$.

	Approach 1	Approach 2	Approach 3	Approach 4
aVOC VBS	2.6×10^{-5}	1.2×10^{-4}	-3.9×10^{-4}	2.8×10^{-20}
bVOC VBS	-1.6×10^{-4}	3.8×10^{-4}	-0.0051	-1.6×10^{-16}
POA	-4.2×10^{-4}	0.0050	-0.0075	-8.8×10^{-18}
siSOA	-9.9×10^{-5}	7.7×10^{-4}	-0.0022	1.2×10^{-19}
TOA	0.0015	0.0657	-0.0346	-1.3×10^{-15}
TOM	-0.00763	0.108	-0.237	-2.1×10^{-15}

539 with the exception of TOA concentration. This indicates that a linear approach is
540 probably suitable for VBS tracer compression. Using the pseudoinverse \mathbf{W}^+ for
541 compression resulted in much lower RMSE for all the VBS classes, but has the
542 critical weakness of producing a significant amount of negative concentrations for
543 superspecies and subsequently reconstructed tracers as explored in Section 3.2.1.
544 Though the phase-specific superspecies approach does not have as low of RMSE for
545 each VBS class as the pseudoinverse approach, it outperforms the other two
546 non-negative approaches. Moreover, it conserves absolute metrics on compression,
547 ensuring that material will stay in each class and each phase, and no material will be
548 added or removed by compression: for this reason, all biases are negligible to
549 machine precision. Preserving information on phase during compression to
550 superspecies has another advantage. This approach can be used in other processes
551 such as dry deposition, which handles particle and gas tracers separately and is a
552 computationally expensive operator in LOTOS-EUROS. Because the phase-specific
553 superspecies method (Approach 4) is physically consistent while quite accurate in
554 reconstruction error, and is readily extended to other phase-specific processes, it is
555 chosen for implementation in LOTOS-EUROS v2.2.1.

556 4 Results: Superspecies Implementation in LOTOS-EUROS

557 The phase-specific, matrix factorization superspecies method (Approach 4)
558 chosen in section 3.3 was implemented in LOTOS-EUROS v2.2.1 as described in
559 section 2.7. This section explores the accuracy and speedup of replacing VBS tracers
560 with ML superspecies in advection, as well as the generalizability of the superspecies
561 to different seasonal conditions and spatial resolutions.

562 After offline training on data from February 20th through 24th, 2018, the
563 selected superspecies parameterization was implemented into LOTOS-EUROS, and
564 used in the advection operator for a run from February 15th through 28th. This is
565 compared with a control run advecting VBS tracers as a baseline to directly assess
566 the error from advecting superspecies. With the ML parameterization implemented
567 in LOTOS-EUROS, small errors caused by advecting superspecies change
568 subsequent VBS tracer concentrations such that the period of February 20th
569 through 24th differs from the training dataset. In that time period, however,
570 meteorological conditions and other processes independent of the VBS and
571 superspecies parameterization are identical to that of the offline training dataset.
572 For the sake of comparison, the superspecies run and control run are evaluated on
573 February 25th through 28th, even though the superspecies run has the chance to
574 accumulate error and diverge from the control run from the beginning of the
575 simulation on February 15th.

576 Advecting ML superspecies reproduces the spatial patterns of average TOA
577 across the entire domain. Figure 5 shows average TOA of the control run and the

578 superspecies run, from February 25th through February 28th. This test time period
 579 is well into the model run, 10 days after the begin of the simulation. During this
 580 time period and over the entire domain, average bias of TOA of the superspecies run
 581 compared to the control run is small and slightly negative, $-0.0095 \mu\text{g m}^{-3}$. Small
 582 average bias is not in itself indicative of low error, as positive and negative bias
 583 cancellations throughout the domain and time period are possible. RMSE, an
 584 absolute metric, was larger at $0.217 \mu\text{g m}^{-3}$. However, the general spatial patterns
 585 of total OA across the entire domain are preserved when advecting superspecies.

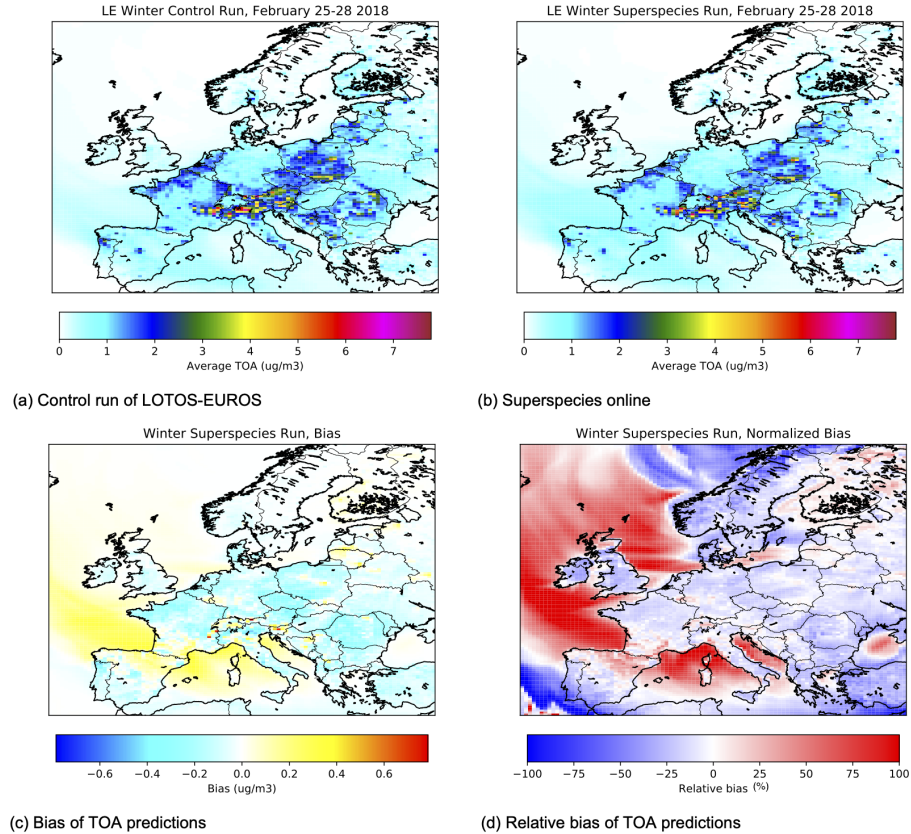


Figure 5. Average TOA for February 25th through 28th 2018, during a 2 week simulation from February 15th through 28th using superspecies matrices optimized offline on winter conditions from February 20th through 24th.

586 4.1 Seasonal Superspecies

587 Advecting superspecies was shown to reproduce the spatial patterns of OA in a
 588 winter test period from February 25th through 28th. This test period occurred
 589 directly after the training test period February 20 through 24th, and has relatively
 590 similar conditions to what the superspecies transformation matrices were optimized
 591 for.

592 A run in summer from July 20th through August 1st was chosen to assess the
 593 robustness of the winter-optimized superspecies. Summer conditions differ from
 594 winter conditions in Europe for several reasons. One, biogenic precursor gases make
 595 up a larger contribution to formation of secondary organic aerosol in the summer,
 596 partially due to emissions from forests. Two, average temperatures are higher,
 597 affecting the partitioning of the VBS by changing the volatility basis set values C^* .
 598 The different conditions lead to different modeled compositions of total organic
 599 aerosol (TOA). Table 4 compares the modeled average composition of OA for
 600 February 25th through 28th to that for July 29th through August 1st.

Table 4. Average TOA composition for the LOTOS-EUROS runs for February and July.

OA Type	February	July
aSOA	0.8%	9.5%
bSOA	4.5%	34.8%
POA	61.2%	12.5%
siSOA	33.5%	43.2%

601 Though siSOA is on average the largest component of TOA in the run from
 602 July 29th through August 1st this is not the full picture, and underscores the
 603 importance of bSOA under some conditions. The maximum concentration of surface
 604 siSOA over the entire domain over the entire period from July 29th through August
 605 1st was $15.0 \mu\text{g m}^{-3}$, and 99th percentile $1.3 \mu\text{g m}^{-3}$ compared to the maximum
 606 bSOA concentration of $100.3 \mu\text{g m}^{-3}$ and 99th percentile $9.4 \mu\text{g m}^{-3}$. This indicates
 607 that although siSOA may dominate in background conditions and when TOA is low,
 608 bSOA is the dominant component of TOA in other conditions.

609 4.1.1 Domain-wide assessment

610 Figure 6 shows average surface TOA, as predicted by the control run (a), the
 611 run with superspecies advected (b), and the bias and relative bias of the
 612 superspecies run with regards to the control, (c) and (d) respectively. The spatial
 613 patterns of TOA are visually different from the winter conditions in Figure 5.
 614 Primary organic emissions corresponding to POA are often the largest contributor to
 615 winter TOA, and for this time period TOA is most concentrated in the Po Valley,
 616 Czechia, and Poland. The winter superspecies run is able to recreate these large
 617 regions of high TOA, as well as other smaller but distinct pockets of TOA, such as
 618 Madrid (the most populous city in Spain) and northwest Portugal, a region with a
 619 lot of industrial activity. In contrast, summer TOA is concentrated around southern
 620 Germany, Switzerland, Austria, and Slovenia. Many places in this region are
 621 forested, and contribute to TOA via emission of biogenic precursors of bSOA. The
 622 superspecies run shown in (b) is able to capture these spatial patterns, but with a
 623 strong bias. For this reason, other regions with high biogenic emissions become
 624 visually apparent in (b), such as southern Sweden, Finland Proper, and
 625 northwestern Russia, which are all heavily forested and which is taken into account
 626 in LOTOS-EUROS via land use maps and tree-species emissions. (Manders et al.,
 627 2017).

628 The superspecies, optimized on winter conditions and tested on a 2 week run
 629 in July, show a large positive bias over the areas with high average TOA, especially
 630 heavily forested regions. RMSE for TOA over the whole domain and time period is
 631 $2.12 \mu\text{g m}^{-3}$, with an average bias of $0.321 \mu\text{g m}^{-3}$. RMSE of the tracers from the
 632 biogenic VBS for all times and gridcells is $0.66 \mu\text{g m}^{-3}$, an order of magnitude

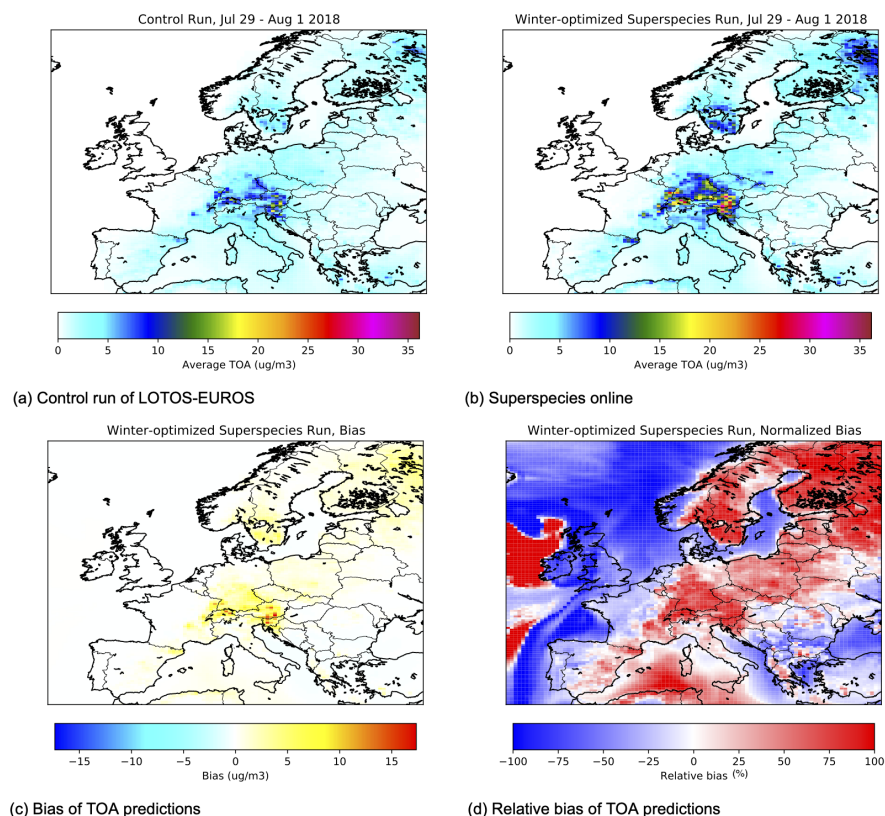


Figure 6. Average TOA for July 29th through August 1st 2018, during a 2 week simulation from July 19th through August 1st using superspecies matrices optimized offline on winter conditions from February 20th through 24th.

633 higher than tracers from the other VBS classes: the class of tracers with the next
 634 highest RMSE value is the siSOA VBS class, at $0.062 \mu\text{g m}^{-3}$. The average bSOA
 635 bias (bias of total biogenic aerosol neglecting gaseous tracers) is $0.068 \mu\text{g m}^{-3}$, three
 636 orders of magnitude smaller than the maximum bSOA bias of $82.9 \mu\text{g m}^{-3}$.
 637 Overestimation of bSOA in the superspecies run under some conditions is likely due
 638 to errors in decompression, artificially shifting mass to lower volatility bins.
 639 However, the large positive bias in parts of the domain indicate that this tendency
 640 to overestimate bSOA only happens in certain conditions: namely, forested regions.
 641 The following section analyzes one gridcell in a forested region, and finds additional
 642 temporal patterns where bSOA is significantly overestimated, leading to
 643 overestimation of TOA.

644 4.1.2 Case Study: Summer Night in a Forest

645 We choose a single gridcell over a forested area to take a closer look at the
 646 superspecies tendency to lead to high bSOA. We study the LOTOS-EUROS gridcell
 647 containing the Schönbuch Natural Reserve in southwest Germany, which is 156
 648 square kilometers and 85% forested. Figure 7a shows the temporal variation of TOA

649 in the Schönbuch from July 29th through August 1st. This overestimation
 650 systematically occurs at night, with the night of July 30th to July 31st a
 651 particularly high TOA event showing the highest bias.

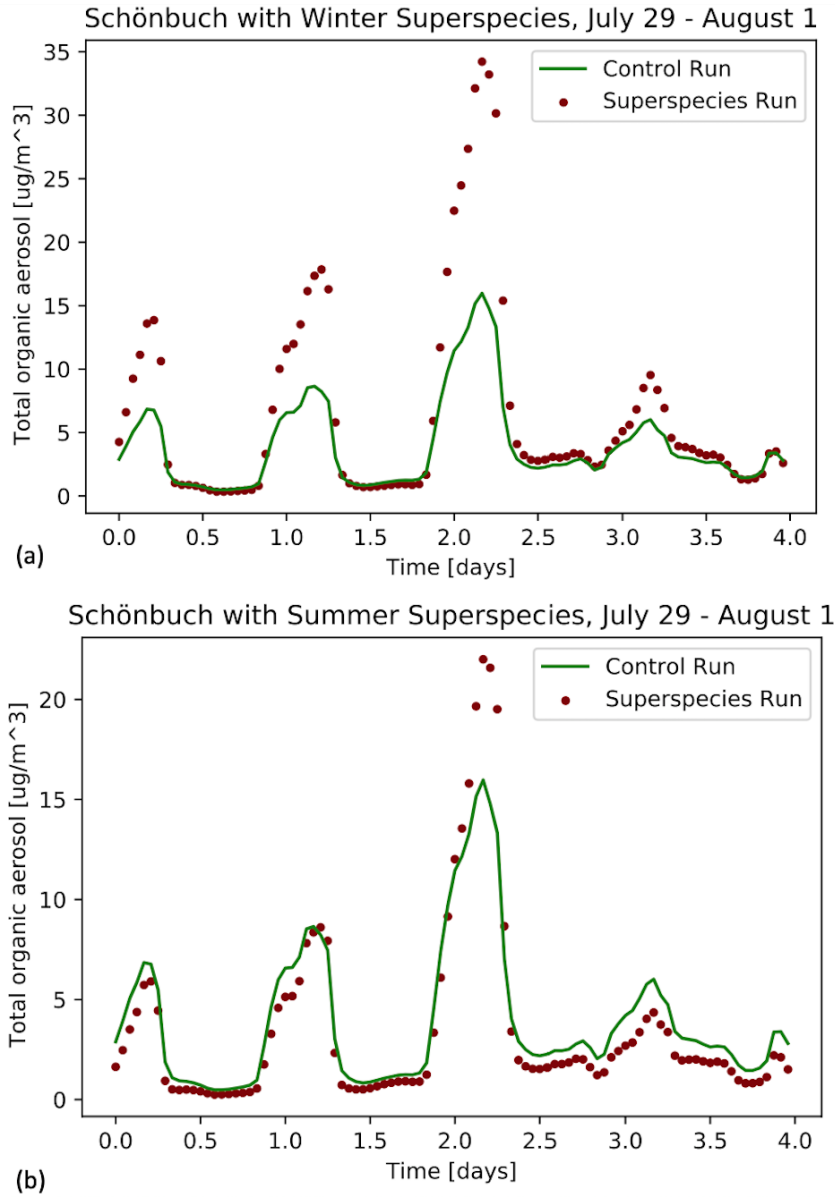


Figure 7. Temporal variation of TOA over Schönbuch from July 29th through August 1st using (a) winter-optimized superspecies and (b) summer-optimized species. The maroon points of TOA as predicted with when advecting superspecies are compared to the green line of TOA as modeled by the LE control run used as a baseline.

652 Examining Figure 7a, the peak overestimation occurs on 05:00 July 31st and
 653 overestimates total bSOA with a factor between 2 and 2.5 times that of the control
 654 run. The superspecies run has a bSOA concentration of $32.9 \mu\text{g m}^{-3}$, which
 655 comprises 99% of total OA concentration for that gridcell and time. The control run
 656 concentration of bSOA is $14.1 \mu\text{g m}^{-3}$, about 95% of TOA for that simulation. By
 657 09:00 July 31st, both runs return to a total bSOA concentration of less than 3.5
 658 $\mu\text{g m}^{-3}$. This night episode of high bSOA contains the largest overpredictions for
 659 that particular gridcell in the whole time period. However, it is illustrative of a
 660 failure mode of the winter-optimized superspecies to capture the total concentration
 661 of bSOA, and ultimately TOA due to the importance of bSOA contributions in this
 662 example. The spatial patterns and temporal patterns of the superspecies run
 663 compared to the control run show that the superspecies are limited in their ability
 664 to model conditions over forested areas on summer nights.

665 Given that winter-optimized superspecies showed limitations in capturing high
 666 bSOA events over forested areas at night, we investigate whether superspecies
 667 optimized on summer conditions and implemented online reproduce high bSOA
 668 conditions with more accuracy. The phase and mass conserving method selected in
 669 Section 3 is applied to model output from July 23rd through 28th, 2018, to obtain a
 670 superspecies parameterization optimized on summer conditions. The loss of accuracy
 671 is evaluated for the subsequent 4 days, from July 29th to August 1st, 2018.

672 The superspecies approach optimized on summer conditions shows a much
 673 lower bias than the winter-optimized superspecies. The temporal behavior of
 674 summer-optimized superspecies from July 29th through August 1st is shown in
 675 Figure 7b. Comparing Figure 7a to 7b, it can be seen that the spatiotemporal
 676 pattern of bSOA bias is fixed by using summer-optimized superspecies, which do not
 677 show the same nightly overestimation pattern of winter-optimized superspecies.
 678 Total bSOA is even slightly underestimated in the day when using
 679 summer-optimized superspecies.

680 Averaged over the entire domain and time period of July 29th through August
 681 1st, the summer-optimized superspecies display a slightly negative average bias for
 682 bSOA of $-0.023 \mu\text{g m}^{-3}$. Small pockets of TOA overestimation (within $10 \mu\text{g m}^{-3}$)
 683 still occur in the same regions as the winter-optimized superspecies: over highly
 684 forested areas. Quantitatively, the superspecies optimized on summer conditions
 685 result in more accurate runs in the summer. The RMSE over the whole domain of
 686 time-averaged TOA was $0.98 \mu\text{g m}^{-3}$ when using summer-optimized superspecies,
 687 less than half of the RMSE of $2.12 \mu\text{g m}^{-3}$ when using winter-optimized
 688 superspecies. RMSE of the tracers from the biogenic VBS (both gas and particle
 689 phases) for all times and gridcells is reduced by a factor of 2, at $0.32 \mu\text{g m}^{-3}$
 690 compared to $0.66 \mu\text{g m}^{-3}$.

691 The limitation of winter-optimized superspecies and the subsequent
 692 improvement in accuracy when using summer-optimized superspecies indicates that
 693 this method might be best applied to different seasons: creating seasonal-specific
 694 superspecies might result in higher accuracy. However, in superspecies trained on
 695 either conditions, the biogenic VBS tracers in the summer show significantly higher
 696 error than the tracers of the other VBS classes, with the siSOA VBS class having
 697 the next highest RMSE value at $0.050 \mu\text{g m}^{-3}$.

698 **4.2 Towards Operational Forecasting on Higher-Resolution Domains**

699 LOTOS-EUROS is one model in the ensemble used in the Copernicus
 700 Atmospheric Modeling Service (CAM5) operational forecasts, which requires all
 701 models to include secondary organic aerosol (SOA) representation by 2022. The
 702 domain used in CAM5 operational forecasts has a higher resolution and wider

703 domain than the domain used by MACC: 0.1° by 0.1° for 420 by 700 gridcells
 704 compared to the 0.50° by 0.25° used in the MACC domain, and extending past
 705 Moscow, Russia. The change of resolution and domain increases the number of
 706 gridcells by a factor of 20. One result of this is many more gridcells and many more
 707 computations. Another result is that the operator splitting timestep Δt needs to
 708 decrease in order to satisfy the Courant-Friedrichs-Lewy criterion as the gridcell
 709 distance is smaller. With a smaller operator splitting timestep, the call to the
 710 advection operator occurs more times per simulated hour. With every call to the
 711 advection operator, compression of tracers into superspecies and decompression of
 712 superspecies back into tracers also occurs.

713 We investigate how the superspecies approach, optimized on model output
 714 from February 20th through 24th on the coarse-resolution MACC domain,
 715 generalizes to a 2 week run on the extended high-resolution CAMS domain. Figure 8
 716 shows the time-averaged TOA concentration across the entire CAMS domain for the
 717 test period of February 25th-28th, 2018, chosen for ease of comparison with the
 718 winter run on the MACC domain.

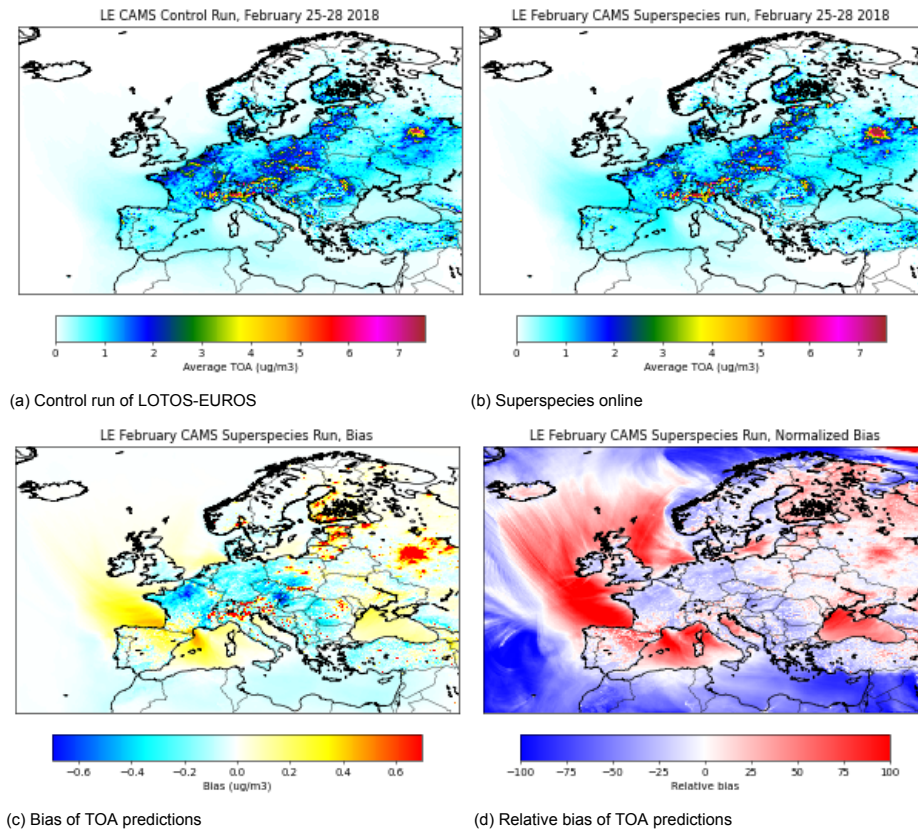


Figure 8. Time averaged TOA for the period of February 25th through 28th on the high-resolution domain used in CAMS operational forecasting, from control and superspecies runs, as well as bias and relative bias. The superspecies were optimized on model output from a simulation using the coarse-resolution MACC domain.

719 The superspecies run has a positive bias for TOA of $0.019 \mu\text{g m}^{-3}$, with visible
 720 overestimation in the area near Moscow, Russia, which is not in the MACC grid
 721 used to optimize the compression/decompression matrices.

722 The colorbar limits of Figure 8 (a), (b), and (c) were adjusted for visual
 723 comparison with Figure 5. For this reason, colors at the upper or lower limits should
 724 be interpreted as greater or equal to the limit. Though the maximum gridcell
 725 concentration of time-averaged TOA from both the superspecies run and the control
 726 run was $28.2 \mu\text{g m}^{-3}$, 99.85% of the gridcells had a time-averaged TOA under 7.6
 727 $\mu\text{g m}^{-3}$, which was chosen as the upper limit of the colorbar. This means that only
 728 0.15% of the gridcells in Figures 8a and 8b exceed the limit shown in the colorbar.
 729 Neglecting the highest 0.15% of average TOA, the spatial patterns of the CAMS
 730 control run in Figure 8a are visually very similar to those of the that the CAMS
 731 superspecies run in Figure 8b. Both show spatial patterns similar to the simulations
 732 performed on the MACC grid for the same time period. The same approach is done
 733 for the bias shown in Figure 8c, with very few gridcells in the CAMS simulation
 734 exceeding the maximum error of time-averaged TOA on the MACC grid. The
 735 maximum absolute error of time-averaged TOA between the superspecies run and
 736 the control run was $8.9 \mu\text{g m}^{-3}$, but 99.2% of all gridcells had an absolute error of
 737 less than $0.70 \mu\text{g m}^{-3}$. Less than 1% of the gridcells in Figure 8c exceed the
 738 colorbar limit.

739 The largest bias for TOA over all cells and the entire test time period (not
 740 time averaged) was $89 \mu\text{g m}^{-3}$, corresponding to a gridcell in northwestern Spain,
 741 near Ponferrada. This gridcell also showed the highest time-averaged TOA
 742 concentration of $32.0 \mu\text{g m}^{-3}$ for the superspecies run, compared to $19.4 \mu\text{g m}^{-3}$ for
 743 the control run.

744 At the highest positive bias of $89 \mu\text{g m}^{-3}$, TOA concentration as modeled by
 745 the superspecies run is $206.4 \mu\text{g m}^{-3}$ while the control run predicts a TOA
 746 concentration of $117.4 \mu\text{g m}^{-3}$. TOA during this event is composed almost wholly of
 747 primary material: the superspecies run models a POA concentration of 205.9
 748 $\mu\text{g m}^{-3}$ (99.78% of TOA concentration) while the control run POA concentration is
 749 $117.1 \mu\text{g m}^{-3}$ (99.75 %). Rather than error compounding and leading to divergence
 750 from the control run, the superspecies run restabilizes without error accumulation
 751 for the rest of the simulation: TOA concentration in the superspecies run converges
 752 to that of to the control run. This indicates that other processes in LOTOS-EUROS
 753 can correct temporary overestimation arising from the superspecies parameterization
 754 as the simulation progresses.

755 4.3 Speed Improvement

756 The advection operator has an outer for-loop over all tracers that are
 757 transported. Using superspecies instead of VBS tracers reduces the overall amount
 758 of variables in the outer for-loop. With the superspecies selected in Section 3, 16
 759 superspecies (two gas and two particle superspecies for each of the four VBS classes)
 760 are advected rather than the 58 VBS tracers.

761 The MACC run on the small domain was run sequentially on one node. Wall
 762 time for the advection operator when advecting superspecies rather than VBS
 763 tracers was 6790 seconds, 56% of the time of (1.8 times faster than) the 12073
 764 seconds to advect all tracers in the control run.

765 The high resolution required for CAMS operational forecasts increases the
 766 computational intensity of the simulations. The CAMS runs for both the control
 767 and superspecies runs were performed using domain decomposition over 24
 768 computing nodes with each node computing a subdomain of 175 by 70 gridcells.

769 Using the VBS on the CAMS domain, advection wall time more than doubled from
 770 34959 seconds to 74762 seconds. With superspecies advected instead of VBS tracers,
 771 wall time for the advection operator was then reduced to 49473 seconds. Advecting
 772 superspecies on the CAMS domain took about 66% of the time that advecting all
 773 the VBS tracers took, a speedup of approximately 1.5.

774 The timing results suggest that advection wall time depends linearly on
 775 number of tracers, which is expected behavior given the structure of the advection
 776 operator: an outer for-loop over all tracers. VBS inclusion approximately doubles
 777 the tracers and therefore should be expected to double the computation time of the
 778 advection operator. The set of 16 superspecies is slightly more than a quarter the
 779 size of the 58 VBS tracers. The VBS tracers are slightly more than half of the 104
 780 advected tracers (some of the other 64 tracers, like radicals, are not advected), so
 781 the theoretical estimate of timing is 59% of the original timing when using 16
 782 superspecies instead of 58 VBS tracers.

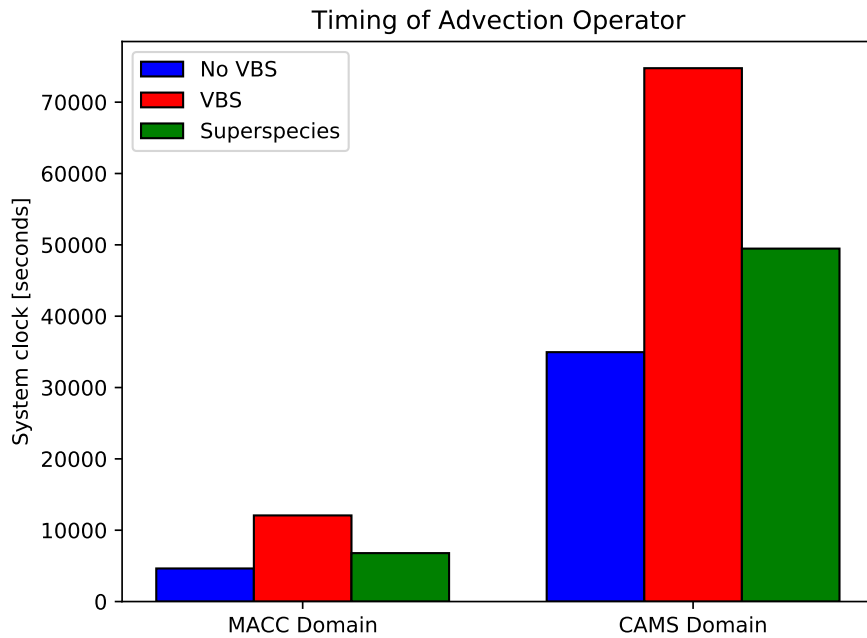


Figure 9. Use of the 58 VBS tracers approximately doubles the wall time spent on advection calculations. Advecting superspecies takes 56% and 66% of the time compared to advecting VBS tracers on the MACC and CAMS domains, respectively.

5 Conclusions

The high-dimensional modeling of organic aerosol processes via four VBS classes is computationally expensive in LOTOS-EUROS v2.2.1, slowing the advection operator down by a factor of 2. We developed unsupervised machine learning (ML) methods to reduce the dimension of VBS tracers to a set of superspecies and reduce the computational burden on the advection operator. These methods were refined to ensure physical consistency, including semi-positive constraints, mass conservation, and information on phase. Multiple approaches were compared in Section 3 and a linear approach based on non-negative matrix factorization was judged to be the most appropriate after being evaluated on reconstruction accuracy and physical consistency. This approach creates 16 phase-specific, class-specific superspecies (a compression factor of 3.6) while preserving phase and conserving total concentration to machine precision. Section 4 explores the results of implementing the ML superspecies in LOTOS-EUROS v2.2.1. The ML parameterization ran stably without runaway error for a model simulation of 2 weeks. Higher bias of total OA concentration was shown when the superspecies, optimized to reconstruct winter OA patterns, were used in a 2 week run in the summer. During the summer run, the bias showed a clear spatiotemporal pattern, with biogenic SOA overestimated over forests at night. The ML approach was retrained on model output from summer conditions and implemented in LOTOS-EUROS v2.2.1 to reduce high bias. The results of this case study indicate that the superspecies might work best when optimized for season-specific conditions.

We found that the ML superspecies trained on the coarse-resolution MACC domain performed well when used on the fine-resolution domain used in CAMS operational forecasts for a period of 2 weeks. In an analysis period of 4 days performed at the end of the 2 week CAMS run, over 99% of all gridcells showed an absolute bias of time-averaged TOA within the maximum error of the MACC grid. Evaluating a gridcell that exceeded the maximum average error, we found that high overestimation of total OA concentration occurred at a high OA event, and converged back to the baseline simulation as time progressed rather than displaying continued error growth.

Advecting superspecies reduced the wall time spent on the advection operator: advecting superspecies took 56% to 66% of the time that it took to advect VBS tracers. Timing experiments indicate a linear dependence of wall time on number of tracers to advect, an expected relation from the structure of the advection operator, which uses a for-loop over all advected tracers. With linear dependence demonstrated, the design choice of compression factor (number of superspecies) can already give an estimate of theoretical speedup.

The use of physically consistent machine learning to find superspecies allows for inclusion of organic aerosol processes without doubling the computational burden on the advection operator. Preserving information on phase of the superspecies allows for their future use in phase-specific processes such as dry deposition, which can be computationally intensive in LOTOS-EUROS. Though demonstrated on organic aerosol species in a regional CTM as a case study, this approach readily generalizes to other tracers, processes, and models. As physical consistency and computational efficiency are widely desired aspects of numerical modeling in the physical sciences, this approach could be adapted for use in comprehensive earth system models with the purpose of providing forecasts of global atmospheric composition, for example GEOS-CF (Keller et al., 2021). More generally, this method contributes additional physical consistency to a widely used linear dimensionality reduction technique (non-negative matrix factorization) that can be used to reversibly map between high and low detail in earth system models.

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840 The exact version of LOTOS-EUROS used in this work including the superspecies
841 extension, as well as all Python code used for analysis of model output and figure
842 generation, is available at <https://doi.org/10.5281/zenodo.6601166>.

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