

1     **An adaptive auto-reduction solver for speeding up integration of chemical**  
2     **kinetics in atmospheric chemistry models: implementation and evaluation in**  
3             **the Kinetic Pre-Processor (KPP) version 3.0.0**

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14  
15    **Key Points:**

- 16       • An updated version 3.0.0 of the Kinetic Pre-Processor (KPP) integrator of chemical kinetics for  
17       atmospheric models has been developed.
- 18       • KPP 3.0.0 features an adaptive solver option for reducing chemical mechanisms locally and on the  
19       fly where full complexity is not needed.
- 20       • The adaptive solver implemented in the global GEOS-Chem model shows a 32% speedup with  
21       errors less than 1% for key tropospheric species.

22 **Abstract**

23 Kinetic integration of large and stiff chemical mechanisms is a computational bottleneck in models of  
24 atmospheric chemistry. It requires implicit solution of the coupled system of kinetic differential equations  
25 with time-consuming construction and inversion of the Jacobian matrix. We present here a new version of  
26 the Kinetic Pre-Processor (KPP 3.0.0) for fast integration of chemical kinetics featuring a range of  
27 improvements over previous versions in performance, diagnostics, versatility, and community openness.  
28 KPP 3.0.0 includes a new adaptive auto-reduction solver to decrease the size of any mechanism locally and  
29 on the fly under conditions where full complexity is not needed, by partitioning species as “fast” or “slow”  
30 based on their local production and loss rates. Previous implementations of this adaptive solver suffered  
31 from excessive overhead in the repeated construction of the local Jacobian matrix or were hard-wired to  
32 specific mechanisms. Here we retain the general applicability of the method to any mechanism and avoid  
33 overhead by using pre-computed Jacobian matrix terms for the full mechanism and cropping the matrix  
34 locally to remove the slow species with no change in memory allocation. We apply this adaptive solver  
35 within KPP 3.0.0 to the GEOS-Chem global 3-D model of atmospheric chemistry and demonstrate a 32%  
36 reduction in solver time while maintaining a mean error lower than 1% for key species in the troposphere.

37

38 **Plain Language Summary**

39 Calculating chemical evolution in global atmospheric chemistry models is computationally expensive  
40 because the chemical mechanisms typically include hundreds of species to account for all conditions from  
41 urban to remote. However, the full chemical complexity is not needed under most conditions. Here we have  
42 developed an adaptive auto-reduction chemical solver that reduces any mechanism on the fly depending on  
43 local conditions and without significant computational overhead. We apply this adaptive solver as an option  
44 in a new version 3.0.0 of the Kinetic Pre-Processor (KPP) chemical solver software package that also  
45 includes a number of updates relative to previous versions. The adaptive solver achieves a 32% reduction  
46 in solver time in a global model simulation while incurring less than 1% average errors for key species.

47 **1 Introduction**

48 Modeling atmospheric chemistry is a grand computational challenge. Current global 3-D models of oxidant-  
49 aerosol chemistry use chemical mechanisms that may involve hundreds of coupled chemical species with  
50 lifetimes ranging from less than a second to many years. Chemical evolution in such a mechanism is  
51 computed by solving a large, stiff system of coupled non-linear ordinary differential equations (ODEs)  
52 expressing the chemical kinetics of individual species. Implicit solvers are required to accommodate the  
53 coexistence of short and long time constants but are computationally expensive because of the need for  
54 repeated construction and inversion of the Jacobian matrix (Brasseur & Jacob, 2017). Chemical integration  
55 often dominates the overall computational cost of global 3-D atmospheric chemistry model simulations,  
56 even in massively parallel environments or using graphics processing units (GPUs) (Alvanos &  
57 Christoudias, 2017; Eastham et al., 2018; Zhuang et al., 2020; Dawson et al., 2022).

58  
59 Considerable research has gone into devising algorithms to speed up chemistry solvers. A common strategy  
60 is to split the mechanism species by time scales in order to decrease the stiffness of the system (Young &  
61 Boris, 1977; Gong & Cho, 1993; Djouad & Sportisse, 2002), but this tends to be mechanism-specific and  
62 is difficult to apply in global models because of the wide range of conditions that may be experienced.  
63 Wholesale reduction of the mechanism, such as in the Super-Fast mechanism used in some climate models  
64 (Brown-Steiner et al., 2018), may lead to large errors (Kelp et al., 2022) and incorrect chemical responses  
65 to perturbations. Machine learning methods can in principle speed up chemical integration by orders of  
66 magnitude but have met with little success because of the large dimensionality of the problem resulting in  
67 error growth (Keller & Evans, 2019; Kelp et al., 2020, 2022).

68  
69 A promising approach for global models is to recognize that the full complexity of the mechanism is not  
70 needed everywhere. For example, reactions involving volatile organic compounds (VOCs) and their short-  
71 lived products typically account for much of the complexity but may be unimportant outside of continental  
72 boundary layers where they are emitted. Jacobson (1995) thus applied separate mechanisms in a global  
73 model for the urban boundary layer, the global troposphere, and the stratosphere. However, this approach  
74 can result in errors and inefficiencies by not accounting for the interactions at chemical boundaries between  
75 domains (Rastigejev et al., 2007) and not allowing for a continuum of chemical regimes from source regions  
76 to the remote atmosphere. Santillana et al. (2010) developed an adaptive mechanism reduction method in  
77 which the size of the mechanism is adjusted at each grid cell and time step, classifying species as fast  
78 (coupled) or slow (uncoupled) on the basis of their total production and loss rates. However, the overhead  
79 involved in local definition of the reduced mechanism offset the computational gains. Sander et al. (2019)

80 and Shen et al. (2020, 2022) improved the method by pre-compiling a limited ensemble of chemical sub-  
81 mechanisms. Sub-mechanisms were selected based on local conditions at each timestep, thus avoiding the  
82 overhead required to define sub-mechanisms. Shen et al. achieved a 30%-50% reduction in computational  
83 cost compared to the full parent mechanism in a global simulation of the troposphere and stratosphere, but  
84 the selection of sub-mechanisms had to be customized to the parent mechanism.

85  
86 Here we develop a mechanism-agnostic, ready-to-use method for adaptive auto-reduction of any chemical  
87 mechanism and implement it as an option in a new version 3.0.0 of the Kinetic PreProcessor (KPP). KPP,  
88 originally developed by Damian et al. (2002) and Sandu and Sander (2006), is a software tool that  
89 automatically generates code to efficiently integrate chemical mechanisms. KPP takes in a set of human-  
90 readable input files describing the mechanism species and reactions and generates Fortran 90, C, or  
91 MATLAB code solving the corresponding system of ODEs using one of a suite of integration methods.  
92 KPP is used to generate the chemistry solver source code in several atmospheric chemistry models including  
93 MECCA within MESSy (Sander et al., 2019; Jöckel et al., 2010), WRF-Chem (Grell et al., 2005; Fast et  
94 al., 2006), the forward and adjoint GEOS-Chem models (Henze et al., 2007), and the adjoint for the CMAQ  
95 model (Hakami et al., 2007; Zhao et al., 2020). Our new version KPP 3.0.0 incorporates several  
96 performance and diagnostic updates over the previous version KPP 2.1 (Sandu & Sander, 2006), in addition  
97 to the adaptive solver option presented below.

## 98 **2 Adaptive solver for chemical kinetics**

99 Atmospheric chemistry models alternate chemical integration and transport calculations through operator  
100 splitting (Brasseur & Jacob, 2017). The chemistry solver is called for a time interval of length  $\Delta t$ , referred  
101 to as the external time step, and returns a vector of updated concentrations  $\mathbf{C}$  at the end of that time step to  
102 be operated on by transport. The kinetic integration of the mechanism by the chemistry solver is done over  
103 internal time steps  $\delta t \leq \Delta t$  to reach the desired accuracy.

104  
105 The chemistry solver integrates a system of  $N$  coupled nonlinear first-order ODEs of the form

$$106 \quad \frac{dC_i}{dt} = P_i(\mathbf{C}) - L_i(\mathbf{C}) \quad (i = 1, 2, \dots, N) \quad (1)$$

107 where  $N$  is the number of coupled species in the mechanism,  $\mathbf{C}$  is the vector of species concentrations of  
108 dimension  $N$ , and  $P_i(\mathbf{C})$  and  $L_i(\mathbf{C})$  are the production and loss rates of species  $i$  that depend on the  
109 concentrations of other species in the mechanism through the reaction rate expressions.

110

111 The external time step in a global model is typically  $\sim 10^3$  s, but many species in the mechanism have  
 112 lifetimes  $\sim 1$  s or shorter. An explicit solver would require internal time steps shorter than the lifetime of the  
 113 shortest-lived species in order to achieve stability, but this is not computationally practical. An implicit  
 114 solver is required. The simplest such solver is the first-order backward Euler method, which approximates  
 115 the solution to (1) over the internal time step  $\delta t$  with

$$116 \quad \mathbf{C}(t + \delta t) = \mathbf{C}(t) + \mathbf{s}(\mathbf{C}(t + \delta t))\delta t \quad (2)$$

117 where we define the net source term  $\mathbf{s} = \mathbf{P} - \mathbf{L}$  as a vector of functions ( $P_i - L_i$ ). Solving (2) for the  
 118 unknown quantity  $\mathbf{C}(t + \delta t)$  using the Newton-Raphson method requires the repeated construction and  
 119 inversion of the  $N \times N$  Jacobian matrix  $\mathbf{J}$ :

$$120 \quad \mathbf{J} = \frac{\partial \mathbf{s}}{\partial \mathbf{C}} \quad (3)$$

121 The construction and inversion of this Jacobian matrix is computationally expensive. Higher-order solvers  
 122 generally used in atmospheric chemistry models, such as Rosenbrock (Rosenbrock, 1963; Hairer & Wanner,  
 123 1991; Sandu et al., 1997) or Gear (Jacobson & Turco, 1994), similarly require the repeated construction  
 124 and inversion of the Jacobian over internal time steps. The Jacobian is typically  $\sim 90\%$  sparse allowing for  
 125 efficient sparse-matrix inversion methods (Sandu et al., 1997), so that the overall cost of construction and  
 126 inverting the Jacobian scales as  $\sim N$  rather than a higher power.

127  
 128 A way to reduce the dimensionality  $N$  of the problem is to split the mechanism into “fast” species for which  
 129 the coupled implicit solution is necessary and “slow” species that may be solved independently over the  
 130 external time step using a fast explicit method. Young and Boris (1977) and Gong and Cho (2003) separate  
 131 species into fast and slow based on their lifetimes compared with the integration time step. However, the  
 132 separation results in non-conservation of mass because the reaction rates are not computed consistently.  
 133 This may not be of consequence in a regional model (as used in those applications) where the domain is  
 134 ventilated by the boundary conditions, so that errors do not accumulate, but it is more problematic in a  
 135 global model. Santillana et al. (2010) separated instead “fast” and “slow” species on the basis of their  
 136 production and loss rates, with the slow species having sufficiently low rates that their influences on other  
 137 species would be negligible and the non-conservation of mass would be inconsequential. This is more  
 138 relevant for global models where concentrations and rates of VOCs become very small outside of their  
 139 source regions. Shen et al. (2020, 2022) used the same approach to partition species between fast and slow.

140  
 141 Here we also follow the partitioning method of Santillana et al. (2010). At the beginning of each external  
 142 time step we calculate  $\mathbf{P}$  and  $\mathbf{L}$  and classify species  $i$  as fast if  $\max(P_i, L_i) > \delta$  and as slow otherwise,  
 143 where  $\delta$  is a user-selected partitioning threshold. Fast species are assigned to the coupled implicit solver as

144 a subset (sub-mechanism) of the full mechanism, while the evolution of slow species over the external time  
 145 step is calculated using an explicit first-order approximation with first-order loss rate constant  $k_i(t_0) =$   
 146  $L_i(t_0)/C_i(t_0)$ :

$$147 \quad C_i(t_0 + \Delta t) = \frac{P_i(t_0)}{k_i(t_0)} + \left( C_i(t_0) - \frac{P_i(t_0)}{k_i(t_0)} \right) e^{-k_i(t_0)\Delta t} \quad (4)$$

148 In the Santillana et al. (2010) implementation, the Jacobian had to be reconstructed locally at every external  
 149 time step for the identified subset of fast species and that incurred large overhead, canceling the benefit of  
 150 the method. Here we avoid the overhead by taking advantage of the pre-computed Jacobian matrix terms  
 151 for the full mechanism in the KPP solver to simply remove rows and columns corresponding to the slow  
 152 species. This is explained in Section 3.2 and is the key new development to make the method  
 153 computationally practical.

154  
 155 The partitioning threshold  $\delta$  is set prior to integration and is tuned to balance performance and accuracy.  
 156 Previous work (Santillana et al., 2010; Shen et al, 2020, 2022) considered that in a typical tropospheric  
 157 chemistry mechanism, much of the coupling is associated directly or indirectly with cycling of the hydroxyl  
 158 radical (OH). OH has a daytime concentration of  $\sim 10^6$  molecules  $\text{cm}^{-3}$  and a lifetime  $\sim 1$  s, so its production  
 159 and loss rates are  $\sim 10^6$  molecules  $\text{cm}^{-3} \text{ s}^{-1}$ . A species with production and loss rates that are several orders  
 160 of magnitude smaller would not be expected to contribute significantly to the coupling. They found  
 161  $\delta \sim 10^2 - 10^3$  molecules  $\text{cm}^{-3} \text{ s}^{-1}$  to be adequate after testing for performance and accuracy.

162  
 163 Here we include the option to dynamically define  $\delta$  instead of specifying a uniform value over the domain,  
 164 to account for rates varying with local conditions. This is done by identifying a target species which is  
 165 considered central to the mechanism and scaling its production and loss rates to define a local partitioning  
 166 threshold:

$$167 \quad \delta = \alpha_{\text{target}} \max(P_{\text{target}}, L_{\text{target}}) \quad (5)$$

168 where  $P_{\text{target}}$  and  $L_{\text{target}}$  are the local production and loss rates of the target species, and  $\alpha_{\text{target}} \ll 1$  is  
 169 a user-selected coefficient that depends on the target species but is otherwise fixed for the model domain.  
 170 For example, a model may use OH as target species for daytime and  $\text{NO}_2$  for nighttime. When using OH as  
 171 a target species and with  $\max(P_{\text{OH}}, L_{\text{OH}}) \sim 10^6$  molecules  $\text{cm}^{-3} \text{ s}^{-1}$ , a value  $\alpha_{\text{OH}} \sim 10^{-4} - 10^{-3}$  would  
 172 correspond to the criteria for  $\delta$  used by Santillana et al. (2010). But  $\max(P_{\text{OH}}, L_{\text{OH}})$  can in fact vary over  
 173 orders of magnitude depending on pressure, UV flux, and other factors, and our local specification of  $\delta$   
 174 accounts for this variability.

175

176 We also include two new options in the algorithm. First is to force individual species to remain in the  
177 coupled implicit solver even if  $\max(P_i, L_i) \ll \delta$ . As we will see, this may be helpful for inorganic halogen  
178 species that cycle between radical and non-radical forms across sunrise/sunset. Second is to include an  
179 ‘append’ functionality in the algorithm so that a species initially diagnosed as slow at the beginning of the  
180 external time step can be transferred into the coupled implicit solver if it becomes fast over the course of  
181 the integration. This increases accuracy with minimum overhead.

## 182 **3 Kinetic Pre-Processor (KPP) version 3.0.0**

### 183 **3.1 KPP 3.0.0 overview**

184 The Kinetic Pre-Processor (KPP, Damian et al., 2002; Sandu & Sander, 2006) generates code for solving  
185 the chemical kinetics for a given chemical mechanism defined by a list of species, reactions, and rate  
186 constants. It is designed for speed by exploiting sparse matrix algebra and pre-computation of terms. We  
187 have made several improvements to KPP relative to the previous version 2.1 (Sandu & Sander, 2006),  
188 including the adaptive solver option. We present these improvements as KPP version 3.0.0, available for  
189 download from <https://github.com/KineticPreProcessor/KPP/> (DOI: 10.5281/zenodo.6828026) with  
190 detailed documentation at <https://kpp.readthedocs.io>.

191  
192 KPP takes in as input one or more text files, with an example shown in Figure 1. The input is not necessarily  
193 in one single file, and may be split into multiple files for readability. The files describe the chemical  
194 mechanism, the choice of the numerical solver (e.g., Rosenbrock), target language (e.g., Fortran 90, C, or  
195 MATLAB), floating point type (single- or double-precision), production and loss diagnostics for selected  
196 chemical families (optional), and whether to use the adaptive solver option (optional). Some inputs are not  
197 part of the KPP code generation and are instead left for users to adjust at runtime, including convergence  
198 criteria (absolute and relative tolerance), numerical order (e.g., order of the Rosenbrock solver), and  
199 adaptive solver options, in order to enable the user to experiment with different thresholds for performance  
200 and accuracy.

```

#INTEGRATOR   rosenbrock_autoreduce
#LANGUAGE     Fortran90
#MINVERSION   3.0.0
#AUTOREDUCE   on
#FAMILIES
POx : O3 + NO2 + HNO3;
LOx : O3 + NO2 + HNO3;

#DEFVAR
O3   = IGNORE;
NO   = IGNORE;
...

#EQUATIONS
O3 + hv = 2OH + O2 : PHOTOL(1);
NO + O3 = NO2 + O2 : ARR(1.8d-12, -1370.0);
CO + OH = CO2 + H2O : 2.4d-13;
H2 + NO = OH + NO2 : ARR(3.7d-12, 240.0);
NO2 + hv = NO + O3 : PHOTOL(2);
H2O2 + hv = 2OH : PHOTOL(3);
CH4 + OH = CO + H2O : ARR(3.1d-12, -187.0);
...

```

**KPP Options**  
Integrator, target language, and other code generation options

**Production and Loss Families (Optional)**

**Definition of species**  
"IGNORE" if mass balance checks are not required  
Otherwise specify stoichiometric composition

**List of reactions**  
Reactants = Products : Rate constant  
Fortran 90 expressions are supported in rate constants

201  
202 **Figure 1. Example KPP input file.** The KPP input file includes options for code generation, adaptive auto-  
203 reduction, diagnostics for production and loss rates of chemical families, and a list of species and reactions.  
204 Reaction rate constants can be specified as expressions in the target language (in this case Fortran 90), here  
205 showing calls to functions calculating photolysis and Arrhenius rate expressions.

206  
207 Based on the specifications in the KPP input file(s), KPP creates files in the target language containing a  
208 description of the system of ODEs (number of species, reactions, and a numbered list of species) code to  
209 calculate the time derivatives, Jacobian matrix, and solution by back-substitution, along with a copy of the  
210 numerical solver (such as Rosenbrock) and supporting routines for sparse linear algebra. This set of files  
211 can be either run standalone as a box model or can be included in a 3-D model to update concentrations  
212 locally over external time steps.

213  
214 Auto-reduction of the mechanism with the adaptive solver described in Section 2 is an option in KPP 3.0.0  
215 using the Fortran 90 language, enabled in the configuration file by #AUTOREDUCE on and specifying the  
216 corresponding integrator (e.g., #INTEGRATOR rosenbrock\_autoreduce). This sets up the  
217 capability for the user to reduce the mechanism locally through specification of the partitioning threshold  
218  $\delta$  between fast and slow species, listing any species for which this partitioning should not be applied. These  
219 specifications are done at runtime for flexibility. Even when the auto-reduction solver is used, mechanism  
220 auto-reduction can be disabled at runtime, defaulting to the behavior of the original integrator. A test case  
221 box model for auto-reduction is included as part of KPP 3.0.0 documentation.

222



223 In addition to the option for adaptive mechanism auto-reduction, several additional features and  
224 improvements were added to KPP 3.0.0. These include:

225

226 **a. Redeployment of KPP source code, continuous integration, and documentation for community**  
227 **development.** KPP 3.0.0 source code has been redeployed on GitHub for community development.  
228 The GitHub repository incorporates continuous integration (CI) tests which automatically compile the  
229 KPP source code to build and run combinations of sample chemistry mechanisms and integrators into  
230 box models at every code revision. This helps to ensure that new features and updates added to KPP do  
231 not break existing functionality. The documentation has also been relocated to  
232 <https://kpp.readthedocs.io> where it is automatically built with each code revision on GitHub.

233

234 **b. Diagnostic improvements.** Diagnostic features have been added to KPP 3.0.0:

- 235 • **Production and loss rates for chemical families.** KPP 3.0.0 allows for the definition of families of  
236 chemical species for computing production and loss for that family, ignoring interconversion  
237 reactions within the family. Families are defined in the #FAMILIES section of the KPP input file.
- 238 • **Stoichiometric numbers.** The stoichiometric numbers of all reactions in the mechanism are now  
239 available in the CalcStoichNum subroutine in the KPP-generated code. This feature is used to  
240 calculate the importance of chemical species in a mechanism for the skeletal mechanism reduction  
241 in Sander et al., 2019.
- 242 • **Individual reaction rates and time derivatives.** The reaction rates and time derivatives are now  
243 available as optional outputs from the KPP-generated code.

244

245 **c. Addition of new solvers.** Several solvers have been added as options for integrating chemical kinetics  
246 including VODE (Brown et al., 1989), SDIRK (Hairer & Wanner, 1991), 3-stage Runge-Kutta, and  
247 forward and backward Euler methods.

248

249 **d. Addition of new rate law functions.** Rate law functions for three-body reactions using the formulas  
250 proposed by JPL (<https://jpldataeval.jpl.nasa.gov>) and IUPAC (<https://iupac.aeris-data.fr/>) have been  
251 added to the built-in rate laws in KPP 3.0.0. Rate law functions are not limited to those built in KPP  
252 and can be added by including extra source code files in the KPP input.

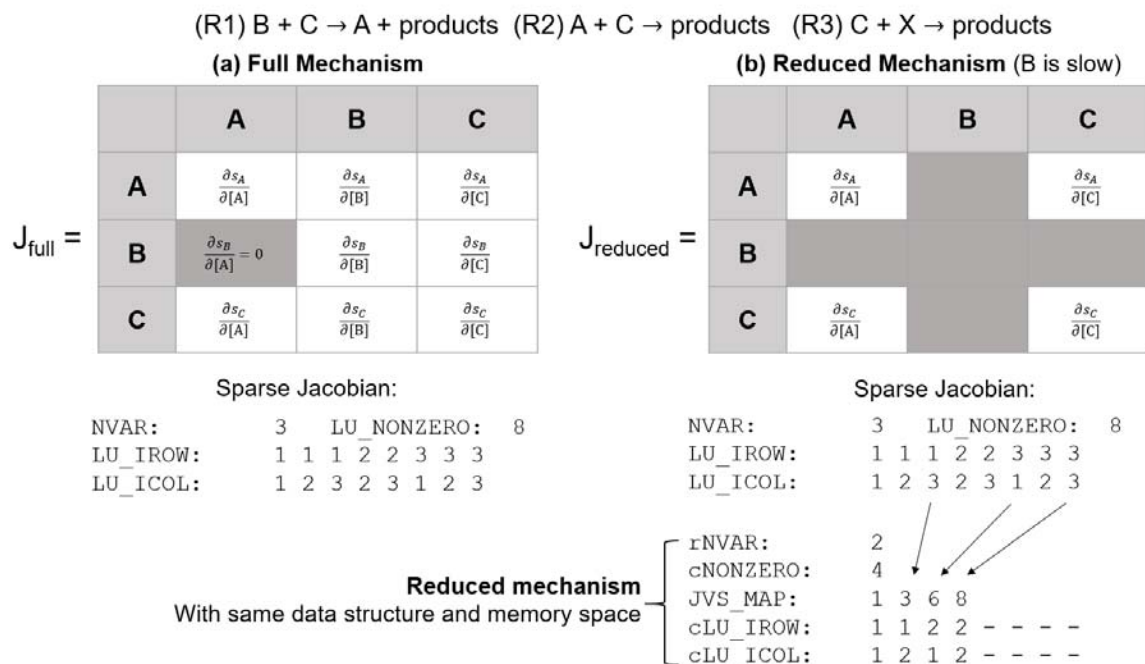
253

254 **e. Miscellaneous performance improvements in Fortran 90.** KPP 3.0.0 optimizes for Fortran 90  
255 performance by applying several guidelines in coding, particularly in reaction rate calculations that are  
256 computed repeatedly in loops:

- 257
- 258 • **Unifying number precision.** Previous inputs to KPP used both single- and double-precision  
259 numbers. KPP input files and code now do not mix number precision to avoid conversion, which  
260 loses precision and costs computational time.
  - 261 • **Switch to control update of reaction rate constants.** Previously, KPP called subroutines to update  
262 reaction rate constants at every internal time step, but this is computationally expensive and may  
263 not be needed in most model applications, because the variables affecting rate constants are not  
264 updated between internal time steps in these models. An optional switch has been added so rate  
265 constants can be updated only at the beginning of the external time step.
  - 266 • **Optimized rate law functions.** Rate law functions have been split to avoid computation of  
267 unnecessary terms. For example, previously a single function with Arrhenius temperature  
268 dependence was used for all reactions:  $ARR_{abc}(A, B, C) = A * \exp(B/T) * (300/T)^C$ . However,  
269 certain reactions may have  $B = 0$  or  $C = 0$ , but in this case the expressions  $300/T$  or  $\exp(0)$  are  
270 still computed, leading to the waste of CPU cycles. Separate rate functions where coefficients lead  
271 to constants, such as  $ARR_{ab}(A, B) = A * \exp(B/T)$  have been added to skip computations that  
272 can be pre-evaluated to constants, leading to a 44% performance improvement of reaction rate  
273 computations in a full-chemistry GEOS-Chem model run.
  - 274 • **Avoiding conditionals and optional arguments.** Conditional clauses such as IF, ELSE, and  
275 SELECT CASE, and testing for optional arguments add significant computational cost if called  
276 thousands of times. If a conditional clause or optional argument is present in a frequently called  
277 subroutine, the subroutine is split into different functions for each case.
  - 278 • **Thread safety for generated code.** The code generated is now thread safe, so that calls for  
279 updating rate constants and running the integrator can be placed in an OpenMP parallel loop for  
280 parallelization.
  - 281 • **Improved expressions for vector and array functions.** Several functions for basic vector and  
282 array operations originally used reference BLAS (Basic Linear Algebra Subprograms)  
283 implementations. These have been replaced with Fortran 90 expressions to allow for compilers to  
284 better optimize the code.
- 285 **f. Miscellaneous code improvements in KPP.** The C source code of KPP has been improved so that no  
286 compiler warnings are generated. A more consistent memory allocation helps to avoid buffer overflow  
287 problems. The KPP language is now parsed by `bison` instead of `yacc`.

288 **3.2 Adaptive solver implementation in KPP 3.0.0**

289 We implemented the adaptive solver as an option within KPP’s Fortran 90 version of the Rosenbrock solver  
 290 using sparse matrix algebra. KPP is computationally efficient because the functions to compute the time  
 291 derivatives for each species and the Jacobian matrix (expressed in terms of reaction rates and species  
 292 concentrations), along with all sparse matrix algebra routines, are pre-generated and use fixed indices to  
 293 access species vectors and matrices. This means that the problem size and memory space is fixed at compile  
 294 time, avoiding expensive memory allocation operations. However, this also yields a fixed problem structure  
 295 that is difficult to manipulate. One major source of overhead in locally defined sub-mechanisms as in  
 296 Santillana et al. (2010) is associated with repeatedly re-allocating and de-allocating memory to  
 297 accommodate changing problem sizes for each sub-mechanism (Shen et al., 2020). Our adaptive solver  
 298 implementation in KPP 3.0.0 uses a mapping operation to project the full mechanism into sub-mechanisms,  
 299 thus reusing the same memory space to avoid expensive resizing operations.



300  
 301 **Figure 2. Mechanism auto-reduction in KPP.** Panel (a) shows the data structure of the sparse Jacobian  
 302 data within KPP for a sample 3-species mechanism. If species B is diagnosed as slow, then the  
 303 corresponding rows and columns of the Jacobian are no longer calculated (panel (b)), and the indices  
 304 pointing to the sparse Jacobian data (LU\_IROW, LU\_ICOL) are adjusted to remove the slow species  
 305 (cLU\_IROW, cLU\_ICOL) through a mapping array (JVS\_MAP) while preserving the sparse matrix in  
 306 row-compressed form. The result is a reduced mechanism with the same data structure as the original one,  
 307 but with smaller dimensions.

309 Figure 2(a) shows the sparse Jacobian data as stored within KPP. In this example mechanism, there are 3  
310 species (NVAR) and 8 non-zero entries in the Jacobian (LU\_NONZERO) of the full mechanism. The row and  
311 column indices of these 8 non-zero entries in Jacobian matrix are correspondingly specified in LU\_IROW,  
312 LU\_ICOL in row-compressed form. At the beginning of every external time step, the production and loss  
313 rates of each species are calculated and compared to the partitioning threshold to separate species into fast  
314 and slow. Figure 2(b) shows an example where species B is slow. The entries in the Jacobian corresponding  
315 to B no longer need to be computed, and a mapping operation is performed: JVS\_MAP corresponds to the  
316 non-zero Jacobian matrix entries still present in the sub-mechanism consisting of fast species. The smaller  
317 sub-mechanism can now be described by 2 species (rNVAR) and 4 non-zero entries in the reduced Jacobian  
318 (cNONZERO) with indices described by cLU\_IROW and cLU\_ICOL. The data structure of the smaller sub-  
319 mechanism is identical to the full mechanism, and the same routines are used to solve it, without the need  
320 to generate extra code, or resizing memory.

321  
322 The mechanism auto-reduction is performed once at the beginning of every external time step. The set of  
323 fast and slow species are established according to the runtime options for the partitioning threshold  $\delta$  and  
324 the list of species to be excluded from partitioning and kept in the fast subset under all conditions  
325 (keepSpcActive). Based on the list of species in the fast set, the mapping (JVS\_MAP) from the full  
326 mechanism to the fast sub-mechanism is created. Because KPP generates hard-coded source code to  
327 compute each term of the Jacobian matrix and back-substitution for computational efficiency, two logical  
328 control vectors, DO\_JVS and DO\_SLV, are created to skip computation of terms corresponding to slow  
329 species as these are no longer necessary.

330  
331 The separation between fast and slow species is controlled by the initial conditions at the beginning of the  
332 external time step, but an optional “append” function is added to account for an initially slow species  
333 becoming fast over the course of the internal time steps. This function appends new species to the fast sub-  
334 mechanism and adjusts the logical control vectors if these species are initially partitioned as slow but their  
335 production or loss rate exceed the partitioning threshold over the course of the internal time stepping.  
336 Diagnosing this has little overhead, because the production and loss rates of all species are already  
337 computed at every internal time step.

338  
339 We used a box model integration of the GEOS-Chem chemical mechanism (described below) to analyze  
340 the overhead of the adaptive solver implemented within KPP. By forcing the adaptive solver routines to run  
341 with a threshold of 0, we determined that the KPP overhead added by the auto-reduction is 10-16%,  
342 depending on the initial condition provided to the box model. The main source of overhead is the copying

343 of data between the full and reduced sub-mechanism (Figure 2), where the worst-case scenario is when all  
344 species are partitioned as fast and all species' data need to be copied between the full to the "reduced" data  
345 structures. Profiling tests show that other steps such as the partitioning of species between fast and slow, or  
346 the first-order approximation for slow species, contribute negligible overhead.

#### 347 **4 Adaptive mechanism auto-reduction in the GEOS-Chem model using KPP version 3.0.0**

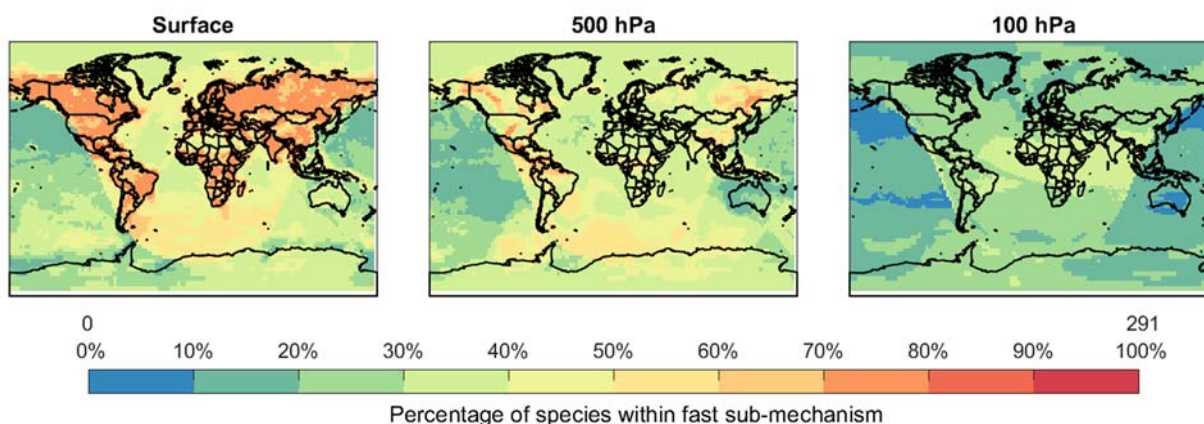
348 We demonstrate the adaptive solver capability in KPP version 3.0.0 with the GEOS-Chem global 3-D  
349 atmospheric chemistry model version 13.4.0 (Bey et al., 2001; <https://doi.org/10.5281/zenodo.6511970>).  
350 The chemical mechanism includes comprehensive oxidant-aerosol chemistry in the troposphere and the  
351 stratosphere with 291 chemical species and 913 reactions. Recent updates to the mechanism include Cl-Br-  
352 I tropospheric halogen chemistry (Wang et al., 2021), isoprene chemistry (Bates & Jacob, 2019), aromatic  
353 chemistry (Bates et al., 2021), hydroxymethanesulfonate cloud chemistry (Moch et al., 2020), and NO<sub>y</sub>  
354 cloud and aerosol chemistry (Holmes et al., 2019). Heterogeneous sulfur chemistry that was previously  
355 simulated with a separate module was brought into KPP in version 13.4.0 with the addition of new rate  
356 functions.

357  
358 GEOS-Chem has been structured to interact with the KPP-generated solver code through the FlexChem  
359 interface which prepares data for the solver code, executes the code, and retrieves concentrations at the end  
360 of the time step. FlexChem allows GEOS-Chem to use modules outside of KPP for computing reaction  
361 rates, for example interfacing with Fast-JX for photolysis rates (Bian & Prather, 2002; Mao et al., 2010).  
362 FlexChem also includes a derived type object, `State_Het`, which passes state variables from GEOS-  
363 Chem model for calculating heterogeneous chemistry reaction rates including cloud liquid water content,  
364 aerosol size distribution, pH, and/or alkalinity. This derived type object holds common intermediate  
365 quantities necessary for heterogeneous reaction rate computations, such as aerosol area, avoiding repeated  
366 computation and memory use. FlexChem also allows GEOS-Chem users to modify the chemical  
367 mechanism input into KPP without modifying the GEOS-Chem source code.

368  
369 We evaluate the accuracy and computational performance of the adaptive solver in KPP version 3.0.0 using  
370 global GEOS-Chem simulations at 2°×2.5° resolution with 72 vertical levels extending up to 0.1 hPa. The  
371 model is driven by the Modern-Era Retrospective analysis for Research and Applications, Version 2  
372 (MERRA-2) meteorological fields from the NASA Global Modeling and Assimilation Office (GMAO).  
373 The external time step for the chemistry solver is 20 minutes. All simulations are conducted on the same  
374 single-node hardware with 24 Intel Cascade Lake physical cores (Intel(R) Xeon(TM) Platinum 8268 CPUs

375 with a base clock speed of 2.90GHz, no hyper-threading logical cores), 100 GB of RAM, and a high-  
 376 performance Lustre parallel file system. The model was compiled using Intel(R) Fortran Compiler (ifort)  
 377 version 2021.2.0.

378  
 379 We select as the standard configuration of the adaptive solver within the GEOS-Chem model a dynamically  
 380 defined threshold with OH as target species during daytime, and NO<sub>2</sub> during nighttime, with coefficients  
 381  $\alpha_{OH} = 5 \times 10^{-5}$  and  $\alpha_{NO_2} = 1 \times 10^{-4}$ . We do not force any species to remain in the implicit KPP solver  
 382 as fast and we do not use the append functionality. We find that we achieve a net 32% reduction in  
 383 integration time in this standard configuration.



384  
 385 **Figure 3. Percentage of GEOS-Chem species retained in the fast sub-mechanism when using the**  
 386 **adaptive solver.** The full GEOS-Chem mechanism has 291 species to describe tropospheric and  
 387 stratospheric oxidant-aerosol chemistry. Only a fraction of species is retained as fast in the KPP solver,  
 388 while the other slow species are solved individually using equation (4). Results are shown for a snapshot in  
 389 time on July 1, 2014, 12:00 UTC at different altitudes. The adaptive solver uses a dynamically defined  
 390 threshold (equation (5)) with target species OH in daytime ( $\alpha_{OH} = 5 \times 10^{-5}$ ) and NO<sub>2</sub> at night ( $\alpha_{NO_2} =$   
 391  $1 \times 10^{-4}$ ).

392  
 393 Figure 3 shows the percentage of species retained in the fast sub-mechanism using the adaptive solver's  
 394 standard configuration. Over 60% are retained in surface air over land, reflecting VOC sources, whereas  
 395 only 10-50% are needed over the ocean. The fraction of retained species decreases with altitude, and fewer  
 396 than 40% are needed in the stratosphere where VOC chemistry is mainly limited to methane. Fewer species  
 397 are needed at night than in daytime. These results are consistent with Shen et al. (2020).  
 398

399 We evaluate the accuracy of the adaptive solver (AS) relative to the full mechanism solver over the global  
 400 GEOS-Chem domain using the relative root mean squared (RRMS) error metric. For each species  $i$ , the  
 401 RRMS error is:

$$402 \quad RRMS_i = \sqrt{\frac{1}{N_i} \sum_{j=1}^{N_i} \left( \frac{C_{i,j,\text{full}} - C_{i,j,\text{AS}}}{C_{i,j,\text{full}}} \right)^2} \quad (6)$$

403 where  $C_{i,j,\text{full}}$ ,  $C_{i,j,\text{AS}}$  are the concentrations of species  $i$  in grid box  $j$  for simulations without and with the  
 404 adaptive solver. The RRMS is computed over the ensemble  $N_i$  of ordered grid boxes that account for 99%  
 405 of the total mass of species  $i$  in the boundary layer (surface to PBL height from MERRA2), free troposphere  
 406 (boundary layer height to tropopause), and stratosphere, respectively, and where  $C_{i,j,\text{full}}$  is greater than 10  
 407 molecules  $\text{cm}^{-3}$ .

408  
 409 Figure 4(a) shows the mean errors at the end of a 1-year simulation for species in different chemical  
 410 categories (Table S1) and Figure 4(b)-(d) shows the time evolution of errors over the 1-year simulation for  
 411 all species in the standard configuration of the adaptive solver within the GEOS-Chem model. The mean  
 412 error for most categories is below 1% within the boundary layer and the free troposphere. There is no error  
 413 growth in the troposphere but there is some in the stratosphere. Figure 5 shows the geographical distribution  
 414 of errors for ozone, OH, and  $\text{NO}_2$  at the surface and 500 hPa for the end of the 1-year simulation. Errors are  
 415 generally lower than 1% except for OH at high latitudes and  $\text{NO}_2$  over the Southern Ocean, where errors  
 416 are up to 3% for OH and 6~10% for  $\text{NO}_2$ . Errors over land for these species are minimal.

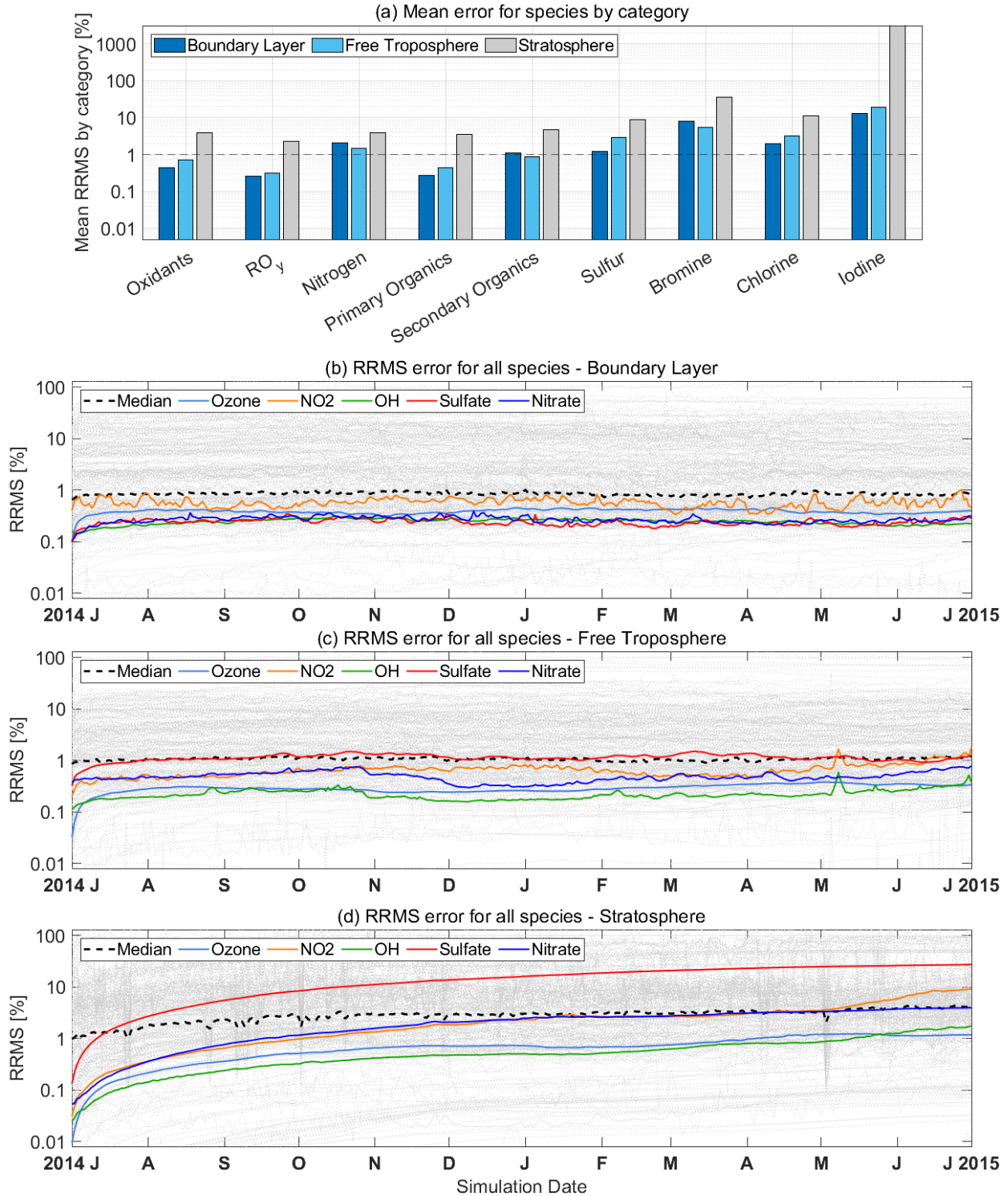
417  
 418 The largest errors in Figure 4 are found for inorganic halogen radicals and their reservoirs. Halogens cycle  
 419 through species with lifetimes spanning several orders of magnitude, and include several highly reactive  
 420 photochemical forms. As a result, partitioning between fast and slow species at sunrise/sunset leads to large  
 421 errors and mass balance issues associated with the use of the first-order approximation (equation (4)).  
 422 Halogen errors are compounded due to their cycling through gas and aerosol phases. These problems were  
 423 previously identified by Shen et al. (2020, 2022). Halogen errors compounded with long residence times  
 424 are the cause of the slow error growth for other species in the stratosphere. The impact is much less in the  
 425 troposphere.

426  
 427 Our results in Figure 4 indicate that halogen species should be kept in the implicit solver as fast species if  
 428 the primary interest of the simulation is the stratosphere. Keeping the halogen radicals and their reservoir  
 429 species as fast prevent large errors for halogen species in the stratosphere, in addition to avoiding error  
 430 growth and spikes in errors as shown in Figure 4(d). Similarly, atomic oxygen (O) and  $\text{HO}_2$  radicals are the

431 cause of high sulfate errors in the stratosphere (exceeding 10% above 85 hPa), and may be kept as fast to  
432 reduce this error. The performance improvement of the adaptive mechanism is then 23%, as compared to  
433 32% in the standard configuration. Such ad hoc adjustments to the fast/slow species partitioning would be  
434 mechanism-specific and can be experimented with by users but we find in GEOS-Chem that they are not  
435 needed for standard applications focusing on oxidant-aerosol tropospheric chemistry.

436  
437 We find in this application that the append functionality (allowing species to switch from slow to fast over  
438 internal time steps) does not provide significant error reduction, in particular for the halogen species, and  
439 degrades the performance improvement of the adaptive mechanism to 24% instead of 32%. We retain it as  
440 an option in the adaptive solver code as it may be helpful for longer external time steps (here 20 minutes)  
441 or other chemical mechanisms.

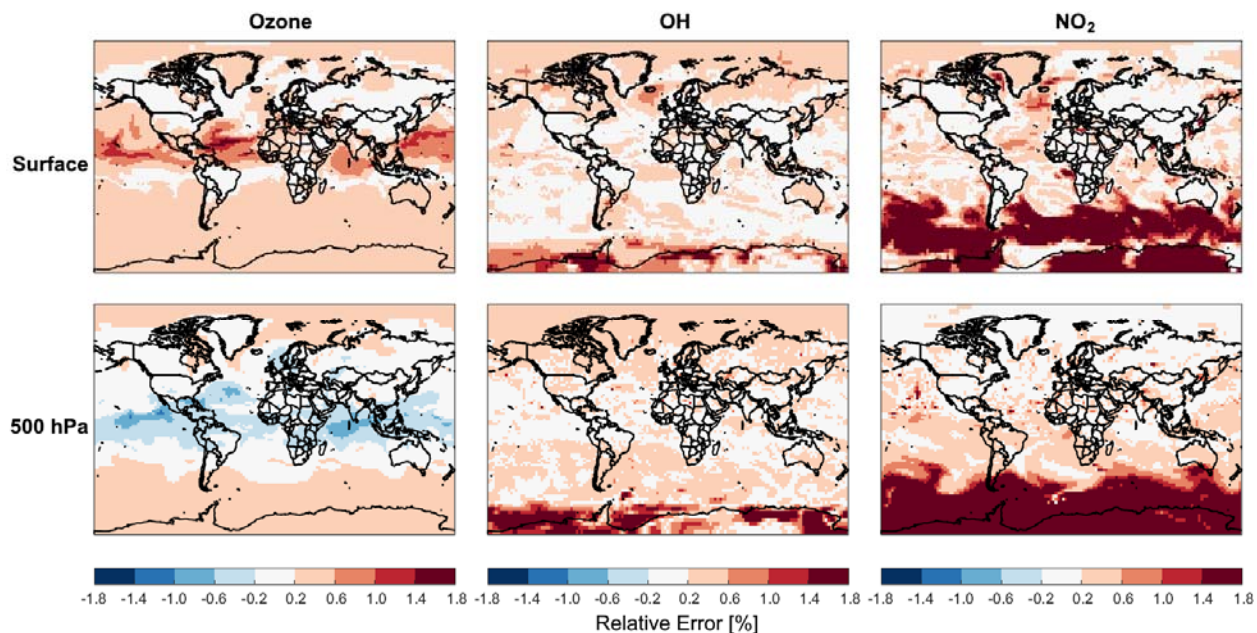




442

443 **Figure 4. Accuracy of the adaptive solver in a 1-year GEOS-Chem simulation.** Panel (a) shows the  
 444 mean RRMS errors for species in different categories at the end of the 1-year simulation starting on July 1,  
 445 2014. The categories are as defined in the standard GEOS-Chem benchmarking output diagnostics (Table

446 S1). Panels (b)-(d) show the time evolution of RRMS errors for all species in the boundary layer, free  
 447 troposphere, and stratosphere, respectively, with colored lines for species of particular interest.  
 448 The adaptive solver uses a dynamically defined threshold (equation (5)) with target species OH in daytime  
 449 ( $\alpha_{\text{OH}} = 5 \times 10^{-5}$ ) and NO<sub>2</sub> at night ( $\alpha_{\text{NO}_2} = 1 \times 10^{-4}$ ), and does not force any species below that  
 450 threshold to remain as fast.



451  
 452 **Figure 5. Accuracy of the adaptive solver for ozone, OH, and NO<sub>2</sub> global distributions.** The Figure  
 453 shows the errors relative to the full solver for the daily mean concentrations on July 1, 2015, the last day of  
 454 the 1-year simulation. The relative error can be up to  $\pm 3\%$  at high latitudes for OH and up to  $\pm 10\%$  over  
 455 the Southern Ocean for surface NO<sub>2</sub>.

## 456 5 Conclusions

457 We presented an updated version of the Kinetic Pre-Processor (KPP 3.0.0) to integrate stiff chemical  
 458 mechanism kinetics. KPP was originally designed for flexibility and speed. KPP 3.0.0 features several  
 459 improvements for performance, diagnostics, choice of solvers, and code openness. It includes an adaptive  
 460 solver capability for mechanism auto-reduction where and when the full mechanism is not needed.

461  
 462 The adaptive solver performs auto-reduction of the chemical mechanism locally and on-the-fly at runtime,  
 463 by comparing the local production and loss rates of each species with a partitioning threshold ( $\delta$ ). Species  
 464 with production and loss rates higher than the threshold are considered fast and are solved as a coupled sub-  
 465 mechanism within KPP, while other species are considered slow and solved individually by an explicit

466 method. Previous application of this adaptive solver method suffered from large overhead due to the need  
467 for local reconstruction of the reduced Jacobian matrix and the associated memory allocation and  
468 deallocation. We solved this problem here by using pre-computed Jacobian terms for the full mechanism  
469 with a mapping operation to crop rows and columns corresponding to the slow species without changing  
470 the memory allocation.

471  
472 KPP 3.0.0 features additional improvements for performance, diagnostics, versatility, and openness.  
473 Improved performance includes more efficient calculation of reaction rates from the KPP rate functions  
474 and thread safety for parallelization. New diagnostics include individual reaction rates, production and loss  
475 rates for chemical families, and stoichiometric numbers. Improved versatility includes expanded choice of  
476 chemical solvers. KPP 3.0 is now hosted on GitHub (<https://github.com/KineticPreProcessor/KPP>) to  
477 enable community access, development, and testing.

478  
479 We evaluated the adaptive solver implemented in KPP 3.0.0 in a 1-year simulation with the global 3-D  
480 GEOS-Chem atmospheric chemistry model including 291 species in the full mechanism for oxidant-aerosol  
481 chemistry in the troposphere and stratosphere. Results show that a 32% performance improvement in the  
482 solver can be achieved with a target error of 1% for key species in the troposphere. Errors in the stratosphere  
483 can be larger, driven by halogen chemistry. Lower errors especially in halogen species can be achieved by  
484 keeping these species within the fast sub-mechanism but reduces the performance improvement to 23% and  
485 is mainly beneficial in the stratosphere. Our standard configuration of KPP and the adaptive solver within  
486 the GEOS-Chem model is mechanism-independent and can be readily applied to other models using KPP.

487  
488 The release of KPP 3.0.0 introduces improvements in development infrastructure, diagnostics, and  
489 performance, particularly in Fortran 90 applications. However, one of the strengths of the KPP software is  
490 the capability to generate code for different programming languages. Development directions for future  
491 versions include (1) adding support for modern languages such as Python and Julia; (2) refactoring of the  
492 generated code to avoid global data structures for easier parallelization; (3) streamlining inputs and outputs  
493 of all integrators for consistency; (4) supporting the adaptive solver option in other integrators and  
494 programming languages; and (5) Improve interaction and compatibility with the Master Chemical  
495 Mechanism (<http://mcm.york.ac.uk>). These improvements will allow KPP to better serve the community  
496 as a versatile tool for solving chemical kinetics.

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500 Modeling and Analysis Program (ACMAP).

501

502 **Open Research**

503 ***Data Availability Statement***

504 *Model Code Availability:* Source code for KPP 3.0.0 is available at

505 <https://github.com/KineticPreProcessor/KPP> (<https://doi.org/10.5281/zenodo.6828026>). The adaptive

506 solver box model is available at <https://github.com/KineticPreProcessor/KPP-AR-boxmodel/>

507 (<https://doi.org/10.5281/zenodo.6791657>). The adaptive solver implementation within the GEOS-Chem

508 atmospheric chemistry model used in this work is available at [https://github.com/jimmielin/geos-](https://github.com/jimmielin/geos-chem/tree/staging/autoreducekpp)

509 [chem/tree/staging/autoreducekpp](https://github.com/jimmielin/geos-chem/tree/staging/autoreducekpp) (<https://doi.org/10.5281/zenodo.6791655>).

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