Complex evolution of the 2016 Kaikoura earthquake

2 revealed by teleseismic body waves

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32 Abstract

The 2016 Kaikoura earthquake, New Zealand, ruptured more than a dozen faults, making itdifficult to prescribe a model fault for analysing the event by inversion. To model this

earthquake from teleseismic records, we used a potency density tensor inversion, which projects 35 multiple fault slips onto a single model fault plane, reducing the non-uniqueness due to the 36 uncertainty in selecting the faults' orientations. The resulting distribution of potency-rate 37 density tensors is consistent with observed surface ruptures. In its initial stage, the rupture 38 propagated northeastward primarily at shallow depths, and the rupture propagated 39 40 northeastward at deep depths beneath a gap in reported surface ruptures. The main rupture phase started in the northeastern part of the Kekerengu fault after 50 s and propagated bilaterally to 41 42 the northeast and southwest. The non-double-couple component grew to a large fraction of the source elements as the rupture went through the junction of the Jordan Thrust and the Papatea 43 fault, which suggests that the rupture branched into both faults as it back-propagated toward the 44 45 southwest. The potency density tensor inversion sheds new light on the irregular evolution of this earthquake, which produced a fault rupture pattern of unprecedented complexity. Our 46 source model should provide new insights into source process of the 2016 Kaikoura earthquake 47 48 (e.g., back-rupture propagation), which should prompt research to determine a more realistic model with segmented faults using near-field data. 49

50 Keywords

51 Earthquake dynamics, Waveform inversion, Body waves, Earthquake source observation

52

53 **1 Introduction**

54 On 13 November 2016, the Kaikoura earthquake struck in the South Island of New Zealand near the boundary between the Pacific and Australia plates (Fig. 1a). Field studies 55 reported that the earthquake produced a complex set of surface ruptures of more than 12 faults 56 (Hamling et al. 2017, Stirling et al. 2017, Litchfield et al. 2018). The rupture area, extending a 57 58 total length of ~ 165 km, can be divided into south and north sections separated by a gap of about 30 km with no mapped surface ruptures between the northeast end of the Conway-59 60 Charwell fault and the southwest end of the Manakau fault (Litchfield et al. 2018) (Fig. 1b). 61 The south section involved the Humps fault and the Conway-Charwell fault with mixed dextral and reverse faulting (Litchfield et al. 2018) (Fig. 1b). The north section displayed a linear set 62 63 of surface ruptures with mixed vertical and dextral displacements on the Manakau fault, the 64 Upper Kowhai fault, the Jordan Thrust, the Kekerengu fault, and the Needles fault (Litchfield et al. 2018). In addition, surface rupture with mixed sinistral and reverse offsets occurred on the 65 66 west-dipping Papatea fault, which extends southward nearly orthogonal to the linear rupture set near the junction of the Kekerengu fault and the Jordan Thrust (Litchfield et al. 2018) (Fig. 1b). 67 Aftershocks were distributed throughout the zone of surface ruptures (Lanza et al. 2019) (Fig. 68

69 lb).

70	The Global Centroid Moment Tensor (GCMT) solution for the mainshock
71	(Dziewonski et al. 1981, Ekström et al. 2012) indicates oblique reverse faulting (Fig. 1). A
72	multiple-point-source inversion using the records of long-range seismographs (teleseismic
73	waveforms) detects four subevents, consisting of three oblique strike-slip subevents and one
74	thrust subevent (Duputel and Rivera 2017), indicating that the earthquake ruptured multiple
75	faults with different faulting mechanisms. Finite-fault inversions using seismic data alone (Bai
76	et al. 2017, Hollingsworth et al. 2017, Zhang et al. 2017, Zheng et al. 2018) or using both
77	seismic and geodetic data (Cesca et al. 2017, Holden et al. 2017, Wang et al. 2018b) commonly
78	find the initial rupture episode during the first ~60 s, followed by the main rupture episode, and
79	discuss the rupture propagated toward northeast from the epicenter in both episodes. Notably,
80	the field surveys identify large co-seismic deformation with sinistral and reverse offsets at the
81	Papatea fault (Clark et al. 2017, Hamling et al. 2017, Stirling et al. 2017, Litchfield et al. 2018).
82	However, finite-fault inversions using only teleseismic body waves, which can estimate the
83	overall rupture propagation process during an earthquake, has not identified sub-events with
84	focal mechanism corresponding to that Papatea fault rupture (Bai et al. 2017, Hollingsworth et
85	al. 2017, Zhang et al. 2017).

Finite-fault inversions in previous studies estimated the rupture process under the 86 87 assumption that the rupture unilaterally propagates northeastward (Bai et al. 2017, Cesca et al. 2017, Holden et al. 2017, Hollingsworth et al. 2017, Zhang et al. 2017, Wang et al. 2018b, 88 Zheng et al. 2018). Such the strong constraints on the unilateral rupture scenario may not always 89 90 be appropriate for the earthquake modeling in a complex fault zone, which sometimes involves 91 the irregularity in rupture manner, including the back-rupture propagation as a part of its bilateral propagation that is initiated as a secondary rupture episode (e.g., Yamashita et al. 2022a, 92 93 Yagi et al. 2023). The assumption of unilateral northeastward rupture propagation may make the interpretation of the inversion results more difficult. Indeed, it is difficult to explain how a 94 right-lateral strike-slip rupture propagating in a northeast direction along the Jordan Thrust 95 could have triggered a reverse fault rupture on the Papatea fault, situated in the extensional 96 97 quadrant. Therefore, there should still be a room to investigate whether the source inversion only allowing for the unilateral rupture scenario should be a valid approach or not to adequately 98 99 explain the rupture evolution along the unprecedentedly complex fault network.

100 As the 2016 Kaikoura earthquake includes multiple faults and complex fault 101 geometries, finite-fault inversion assuming one or a few simplified model fault planes may 102 produce erroneous inversion results due to modelling errors caused by the inappropriate

103	assumed fault geometries (Shimizu et al. 2020). Thus, it is desirable to estimate the rupture
104	process of the 2016 Kaikoura earthquake with a method, onto a model plane, like a potency
105	density tensor inversion (PDTI) (Shimizu et al. 2020), instead of a method requiring assumption
106	of fault geometries. The PDTI incorporates the uncertainty of the Green's function in the data
107	covariance matrix (Yagi and Fukahata 2011) and introduces the Akaike's Bayesian Information
108	Criterion (ABIC) (e.g., Akaike 1980, Yabuki and Matsu'ura 1992, Sato et al. 2022), making it
109	possible to perform stable inversion analyses using seismic source model with a high degree of
110	freedom in the rupture direction (e.g., Hicks et al. 2020, Yamashita et al. 2022a, Yagi et al.
111	2023).

In this study, we applied the PDTI to teleseismic P-waveforms of the 2016 Kaikoura 112 113 earthquake to simultaneously estimate the rupture propagation and the focal mechanism 114 variation. It revealed a source process consisting of an initial and a main rupture episode. The initial rupture propagates northeast from the hypocenter and breaks shallow and deep parts of 115 the source area; deep rupture occurs where there is no surface rupture reported. Then the main 116 117 rupture begins at the northeast end of the Kekerengu fault and propagates bilaterally to the northeast and southwest. An estimated fault geometry that incorporates variation in the focal 118 119 mechanism is consistent with surface ruptures reported from the New Zealand Active Faults

Database (Langridge et al. 2016), and back-rupture propagation during the main rupture that
branched out and propagated into the Jordan Thrust and the Papatea fault.

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123 2 Methods, data, and modelling

124 The PDTI of teleseismic P-waveforms has been developed to mitigate the effect of the 125 modelling error due to the inaccurate model fault geometries (Shimizu et al. 2020). Teleseismic P-waveforms are sensitive to perturbations in the focal mechanism but insensitive to errors in 126 127 the source location, which is confirmed by both the synthetic tests and real applications (e.g., Shimizu et al., 2020; Tadapansawut et al., 2022; Yamashita et al., 2022b). Therefore, it should 128 be critical to incorporate the focal mechanism change during the rupture propagation when 129 130 building a seismic source model to robustly estimate the rupture process (Shimizu et al. 2020). 131 In the PDTI, which is adopted in this study, fault slip along a model plane is described by a superposition of five basis double-couple components (Kikuchi and Kanamori 1991), then the 132 133 rupture evolution (including perturbations in the focal mechanism) is estimated as a spatio-134 temporal distribution of the potency-rate density tensor (Ampuero and Dahlen 2005). Thus, the seismic waveform u_i observed at a station j is given by 135

136
$$u_j(t) = \sum_{q=1}^5 \int_S (G_{qj}(t,\xi) + \delta G_{qj}(t,\xi)) * \dot{D}_q(t,\xi) d\xi + e_{bj}(t),$$

137 where G_{qj} is the Green's function of the *q*th basis double-couple moment tensor, δG_{qj} is the 138 modelling error on G_{qj} (Yagi and Fukahata 2011), \dot{D}_q is the potency-rate density function for 139 the *q*th component of the basis double-couple moment tensor, e_{bj} is a background and 140 instrumental Gausian noise, ξ represents a position on the assumed model plane (*S*), and * 141 denotes the convolution operator in the time domain.

Because this inversion allows any type of faulting mechanism on the assumed model 142 plane, information about the fault geometry can be extracted from the observed data (Shimizu 143 et al. 2020). To stably invert such a high degree-of-freedom seismic source model, the PDTI 144 145 introduces the error term of the Green's function into the data covariance matrix (Yagi and 146 Fukahata 2011), then evaluates the relative weights of information from observed data and prior constraints using Akaike's Bayesian Information Criterion (ABIC) (Akaike 1980, Yabuki and 147 Matsu'ura 1992, Sato et al. 2022). This inversion formulation reduces the effect of modelling 148 149 errors caused by uncertainties in fault geometry and Green's function and allows stable 150 estimates of the seismic source process even when the predefined model plane deviates from 151 the true fault plane (Shimizu et al. 2020). The PDTI has been effectively applied to earthquakes 152 for which it is difficult to assume a reasonable fault model (Okuwaki et al. 2020, 2021, Tadapansawut et al. 2021, Yamashita et al. 2021, 2022a, Okuwaki and Fan 2022). This PDTI is 153

154	thus suitable for analyzing the 2016 Kaikoura earthquake, with its complex distribution of
155	surface ruptures, in enabling us to project multiple fault ruptures onto a single assumed model
156	plane (Okuwaki et al. 2021, Yamashita et al. 2022a).
157	For the PDTI, we used the teleseismic P-waveforms (vertical component) from 48
158	stations at epicentral distances of 30°-100° downloaded from the Data Management Center of
159	the Incorporated Research Institutions for Seismology (IRIS-DMC) (Fig. 2a). We converted the
160	waveform data to velocity waveforms at a sampling interval of 0.8 s. We calculated Green's
161	functions at a sampling interval of 0.1 s by the method of Kikuchi and Kanamori (Kikuchi and
162	Kanamori 1991). We used CRUST2.0 (Bassin et al. 2000) as a 1-D structure model around the
163	source (see Supplementary Table S1), and set the value of t*, which controls the inelastic
164	attenuation of P-waves, to 1 s. We aligned the P-wave first motion manually to correct the
165	travel-time deviations due to 3-D earth structure (e.g., Fan and Shearer, 2015). The effect of
166	uncertainty of underground structure was mitigated by introducing the error term of the Green's
167	function into the data covariance matrix (Yagi and Fukahata 2011).
168	Because the high-frequency component of the teleseismic body waveforms is
169	effectively suppressed owing to the natural low-pass filtering caused by inelastic attenuation,

170 given a sufficiently short resampling interval, the waveforms are little affected by aliasing (see

171 Supplementary Fig. S1). Conversely, applying a low-pass filter that includes an anti-aliasing 172 filter increases the off-diagonal component of the data covariance matrix (Yagi and Fukahata 2011), making it difficult to stably invert the data covariance matrix. We exploited this natural 173 filtering to obtain a more stable analysis by not using a low-pass filter on the waveforms or 174 Green's functions. As a result, we were able to estimate a solution that reproduced the features 175 176 of the observed waveform without distortion by low-pass filtering (Fig. 2b, Supplementary Fig. 177 S2). We adopted a hypocenter location at 172.95°E, 42.62°S, and 15 km depth (Lanza et al. 178 2019). We established a 200 km × 35 km vertical model plane striking NE-SW (230°) to 179 180 represent surface ruptures (Langridge et al. 2016, Hamling et al. 2017, Stirling et al. 2017,

Litchfield et al. 2018) and aftershock activity (Lanza et al. 2019) (Fig. 1b). We set a maximum rupture velocity of 2.6 km/s to allow for the northeastward migration of the high-frequency source at about 2.0 km/s indicated by P-waveform back-projection (Xu et al. 2018). The slip on the model plane was expanded by linear B-spline functions in space with an interval of 10 km and 5 km in the strike and dip directions, respectively, and by linear B-spline functions in time with an interval of 0.8 s with a maximum duration of 60 s for each source element, which is long enough to detect possible re-rupture and/or back rupture propagation (Holden et al. 2017,

- 188 Hicks et al. 2020). The total duration of the event was set to 95 s. The ABIC can prevent
 189 overfitting, even using large number of model parameters (Sato et al. 2022).
- 190 We applied a time-adaptive smoothing constraint that adjusts the smoothing strength
- 191 in inverse proportion to the changing amplitude of the potency-rate function (Yamashita et al.
- 192 2022b). This constraint can mitigate the problem of oversmoothing during the main rupture,
- 193 which obscures the results (Yamashita et al. 2022b).
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195 3 Results

196 We estimated the distribution of potency-rate density tensors on the assumed vertical model plane, then time-integrated them at each source element to yield the spatial distribution 197 198 of potency density tensors shown in Fig. 2c. This figure shows an area of high potency density 199 centered around 110 km northeast of the epicenter on the shallow part of the model plane. The dominant focal mechanism (with relatively large potency density) differs along the length of 200 the fault plane, being oblique reverse slip for 50-120 km and strike-slip for 130-150 km 201 northeast of the epicenter (Fig. 2c). The total seismic moment is 1.1×10^{21} Nm. The moment-202 rate function, obtained by calculating the seismic moment-rate of the best-fitted double-couple 203 source at each sampling time, shows that the moment rate is around 1.0×10^{19} Nm/s until 55 s 204

205

from the origin time and then increases rapidly, reaching 6.0×10^{19} Nm/s at 66 s (Fig. 2d).

206	Figure 3 shows selected snapshots of the potency-rate density tensors on a cross section
207	of the model fault plane; see Supplementary Figure S3 for the full set of snapshots. Figure 4 is
208	a map view of the strike angles of the nodal planes of these tensors along the top of the model
209	plane. During the first 10 s from the origin time, a strike-slip rupture striking about 25°
210	clockwise from the model plane propagated to the northeast of the epicenter (Figs. 3a, 4).
211	Hereafter, we refer to the origin time as 0s. The rupture then propagated further northeastward
212	on the shallow part of the model plane, changing to an oblique reverse focal mechanism. This
213	shallow rupture stagnated at about 40 km northeast of the epicenter after 20 s; however, a deeper
214	rupture continued on the model plane during 20–30 s, reaching 70 km northeast of the epicenter.
215	An isolated reverse rupture occurred at 25–30 s near the ground surface around the epicenter.
216	During 30-45 s, an oblique reverse rupture appeared near the ground surface about 70 km
217	northeast of the epicenter and propagated northeast; during 45-50 s, the rupture propagation
218	pattern was obscure (see Supplementary Fig. S3a).

219	After 50 s, the main rupture emerged near the ground surface about 110 km northeast of
220	the epicenter and propagated bilaterally to the northeast and southwest (Figs. 3, S4). During
221	50-55 s, the dominant focal mechanisms were mixed reverse and strike-slip with the right-

222	lateral nodal plane oriented about 40° clockwise from the model plane (Figs. 3a, 4). The
223	northeastward rupture, a strike-slip rupture striking about 10° counterclockwise from the model
224	plane, propagated through the shallow part of the model plane and reached the edge of the
225	model plane at about 68 s (Figs. 3b, 4). The southwestward rupture reached about 70 km
226	northeast of the epicenter by 70 s (Fig. 3b). During 60-64 s, it was dominantly strike-slip near
227	the ground surface and reverse in the deep part of the model plane (Fig. 3b). The reverse slip
228	component increased with time after 64 s. The rupture gradually weakened after 70 s and ceased
229	at 95 s. The inverted solution well explains the teleseismic P-waveforms (Fig. 2b,
230	Supplementary Fig. S2).

231

232 **4 Reproducibility and sensitivity tests**

We performed a numerical experiment to test the stability and reproducibility of our potency-rate density tensor distribution. Using the obtained source model as an input model, we generated synthetic waveforms for the 48 stations used in the analysis by convoluting the obtained solution with the Green's function used in the analysis for real waveforms plus an error for the Green's function, and then adding background noise (Shimizu et al. 2020) (see Supplementary Fig. S5). The resulting synthetic waveforms were inverted with the same

settings used with the real waveforms.

We performed a structure sensitivity test using the 1-D structure model CRUST1.0 (Laske et al. 2013) for the source region instead of CRUST2.0 (Bassin et al. 2000) (see Supplementary Table S2). We estimated the rupture evolution using the same observed dataset and the same inversion settings as for our preferred modelling.

We also performed another sensitivity test projecting rupture process onto the 244 245 horizontal model plane. We established a 200 km × 70 km horizontal model plane striking NE-SW (230°) to represent surface ruptures (Langridge et al. 2016, Hamling et al. 2017, Stirling et 246 247 al. 2017, Litchfield et al. 2018) and aftershock activity (Lanza et al. 2019) (see Supplementary Fig. S8). The slip on the model plane was expanded by bilinear B-spline functions in space with 248 249 an interval of 10 km. The hypocentral depth was 10 km, where rupture mainly detected in the 250 analysis using vertical model plane (Figs. 2 and 3). We used the same observed dataset and the same inversion settings as for our preferred modelling using the vertical plane. 251

Both the reproducibility and structure sensitivity tests successfully reproduced the features in our preferred model: these included the initial strike-slip rupture during the first 10 s, the northeast-propagating oblique reverse rupture at varying depths during 10–30 s and reappearing near the ground surface about 70 km northeast of the epicenter, and the main bilateral

rupture starting about 110 km northeast of the epicenter around 50 s with a strike-slip rupture
propagating northeast and an oblique-slip rupture propagating southwest (see Supplementary
Figs. S6, S7). Although the sensitivity test using the horizontal model plane does not have depth
resolution, the aforementioned lateral variation of rupture evolution was also detected (see
Supplementary Fig. S8).

261

262 **5 Discussion**

Our result shows that the rupture process of the 2016 Kaikoura earthquake can be divided into initial and main rupture episodes: the initial rupture propagated northeastward; the main rupture propagated bilaterally from 110 km northeast of the epicenter, involving backward rupture propagation toward the epicenter. The total moment tensor shows oblique reverse faulting, which is consistent with the GCMT solution (Fig. 1). In the following, we will discuss how those rupture episodes relate to the observed surface ruptures, to unravel the unprecedentedly complex rupture process of the 2016 Kaikoura earthquake.

As the initial strike-slip rupture propagated northeast during the first 10 s (Fig. 3a), the right-lateral nodal planes of the potency-rate density tensors matched the strike of the Humps fault (Langridge et al. 2016) (Fig. 4). An oblique reverse rupture then propagated northeast

through the shallow part of the model plane. After 20 s, the shallow rupture stagnated about 40 273 274 km northeast of the epicenter while the oblique reverse rupture continued to propagate deeper on the model plane (Fig. 3a). The location where the shallow rupture stagnated corresponds to 275 the gap in surface ruptures between the Conway-Charwell and Manakau faults (Langridge et al. 276 2016) (Figs. 1, 3a), and the deep oblique reverse slip has also been identified by the finite-fault 277 inversion of geodetic data (Hamling et al. 2017). During 30-35 s, oblique reverse rupture 278 appeared near the ground surface about 70 km northeast of the epicenter, corresponding to the 279 280 southwest end of the Manakau fault (Langridge et al. 2016), and then propagated near the ground surface until 45 s (Fig. 3a). Our results show that the initial rupture shifted deeper around 281 the area of no surface rupture during 20-30 s. However, because slips on multiple fault planes 282 283 are projected onto the single model plane in our inversion, it is difficult to determine whether 284 these ruptures were connected at depth. It is controversial how the plate interface contributed to moment release in the 2016 Kaikoura earthquake (e.g., Lanza et al., 2019). Although the deep 285 286 rupture during 20-30 s appeared at about 25 km depth, the resolved dip angles (~40°) are steeper than those of the hypothesised plate interface (e.g., Williams et al., 2013). 287

After 50 s, the main rupture appeared in the northeast part of the Kekerengu fault (Langridge et al. 2016) and then propagated bilaterally until about 70 s, such that one end of

the rupture appeared to propagate backward toward the epicenter (Fig. 3). Because we cannot 290 291 trace the rupture migration during 45–50 s, it is difficult to determine how the initial rupture migrated to the main rupture. The potency-rate density tensors obtained at 50-55 s indicate both 292 strike-slip and reverse faulting, and the strikes of their right-lateral nodal planes are consistent 293 with that of the northeastern Kekerengu fault (Langridge et al. 2016) (Fig. 4). For the 294 295 northeastward strike-slip rupture, the strikes of the right-lateral nodal planes match the 296 orientation of the Needles fault (Langridge et al. 2016) (Fig. 4), and the dominance of strike-297 slip faulting in the shallow part of the model plane (Fig. 3b) is consistent with other studies (Bai et al. 2017, Cesca et al. 2017, Hollingsworth et al. 2017, Wang et al. 2018a, 2018b, Zheng et al. 298 299 2018, Xu et al. 2018, Mouslopoulou et al. 2019). For the backward rupture, the potency-rate 300 density tensors near the ground surface show a transition from oblique strike-slip to oblique reverse faulting 80-110 km northeast of the epicenter (Fig. 3b), and the strikes of the right-301 302 lateral or northwest-dipping nodal planes match those of the central Kekerengu fault and the 303 Jordan Thrust (Langridge et al. 2016) (Fig. 4).

The potency-rate density tensors around the Jordan Thrust and Papatea fault contain large non-double-couple components, reaching an 80% maximum from 60 to 66 s, that then rapidly decrease to less than 20% after 66 s (Fig. 5). Our reproducibility tests also captured the

time variation of this component (see Supplementary Figs. S6, S7). The size of the non-double-307 308 couple component from 60 to 66 s suggests that slips occurred on multiple faults with different orientations; this is consistent with reverse faulting with sinistral strike-slip reported on the 309 Papatea fault (Hamling et al. 2017, Stirling et al. 2017, Litchfield et al. 2018, Wang et al. 2018b, 310 311 Xu et al. 2018), which is nearly perpendicular to the other surface ruptures (see Supplementary 312 Fig. S9). Our result suggests that the backward rupture on the Kekerengu fault not only 313 propagated into the Jordan Thrust, but also branched out and propagated into the Papatea fault. 314 Given the right-lateral strike-slip rupture propagates in a southwest direction along the Kekerengu fault, the Papatea fault is situated in the compressional quadrant; this suggests that 315 the southwestward rupture along the Kekerengu fault can better explain a trigger of the reverse 316 317 faulting rupture along the Papatea fault than the northeastward rupture along the Jordan Thrust, which should require the Papatea fault to be located in the extensional quadrant. Although we 318 319 find it reasonable to explain the Papatea rupture by our series of bilateral ruptures, more detailed 320 analyses and simulations incorporating the detailed geometries of those faults will be required 321 to testify which of the scenarios is more favorable for the Papatea rupture. Near the southwest 322 end of that rupture, the strikes of the right-lateral or northwest-dipping nodal planes were about 10° clockwise from the model plane, which is consistent with the strikes of the Upper Kowhai 323 324 and Manakau faults (Langridge et al. 2016) (Fig. 4). So far, an earthquake source modelling has

often been relying on a restricted degree of freedom, which has been considered as a 325 326 requirement for a plausible solution. However, the modelling employing fewer degrees of freedom might be easy to drop information that are recorded in the observed data and critical 327 to interpret the source process (e.g., Shimizu et al., 2020), albeit the solution derived from those 328 modelling apparently looks not bad. One of the advantages of employing a model with a high 329 330 degree of freedom (e.g., this study) is that a solution is less susceptible to the modellers' preconceptions. By estimating the potency tensor density distribution including the non-double-331 332 couple component, we found that the backward rupture branched out and propagated on the Papatea fault, which, to our best knowledge, has not been reported in previous attempts of the 333 teleseismic body waves analyses. 334

Our analysis suggests the following scenario for the main rupture: it propagated bilaterally from the northeast part of the Kekerengu fault, the northeastward rupture propagating along the Needles fault and the southwestward rupture propagating along the Kekerengu fault, Jordan Thrust, Papatea, Upper Kowhai, and Manakau faults. We interpret the simultaneous rupture events in the area around the Needles fault and the Jordan Thrust noted in previous studies (Bai et al. 2017, Cesca et al. 2017, Hollingsworth et al. 2017) as bilateral rupture propagation. In addition, the back-projection image (Xu et al. 2018) shows that the seismic

wave radiation point moves toward the epicenter from around the south edge of the Papateafault during 50–70 s, a finding consistent with backward rupture propagation.

344	In the region of the backward rupture, multiple faults may have ruptured during the
345	initial rupture phase, because the aftershock region extends perpendicular to the model plane
346	and the focal mechanisms varied during the initial rupture (Fig. 6). Because our model fault
347	plane may include projections of multiple independent ruptures, we cannot determine which
348	faults participated in the initial rupture. Therefore, we cannot say whether the backward rupture
349	was a re-rupture (Holden et al. 2017) or a rupture on a different fault, as in the 2010 El Mayor-
350	Cucapah earthquake (Yamashita et al. 2022a).

Back-propagating ruptures in seismic events are not so rare; they have been reported 351 in the 2010 El Mayor-Cucapah earthquake (Yamashita et al. 2022a), the 2011 Tohoku-oki 352 353 earthquake (Ide et al. 2011), the 2014 Iquique earthquake (Yagi et al. 2014), the 2016 Romanche 354 transform-fault earthquake (Hicks et al. 2020), and the 2018 Peru earthquake (Hu et al. 2021). With the exception of the 2011 Tohoku-oki earthquake, where the backward rupture followed 355 an overshooting rupture near the free surface (Ide et al. 2011), these earthquakes have in 356 common an initial weak rupture which triggers a main rupture, at a point distant from the 357 hypocenter, that involves a back-propagating rupture. It appears that the 2016 Kaikoura 358

arthquake is another example of this kind of event.

360	Our modelling approach requires few assumptions of modelling, that is, we solve for
361	multiplicity of fault configuration and diverse rupture geometries on the flat single model fault.
362	This is still prone to non-uniqueness in the Kaikoura rupture, primarily due to the limited spatial
363	resolution of tele-seismic records, but the rupture directions and timing, involving back-rupture
364	propagation resolved in our model, in turn, can be useful for further inverse and/or forward
365	modelling using near-field datasets, which contribute to converge to a realistic source model of
366	the Kaikoura earthquake.

367

368 6 Conclusions

We obtained the source process of the 2016 Kaikoura earthquake by a potency density tensor inversion from teleseismic P-waveform data, a method for which we did not need to strictly define the fault geometry and rupture directions. We found a complex episode including an initial unilateral and a delayed main bilateral rupture, and the variations of the focal mechanisms are consistent with the reported surface ruptures. The initial rupture propagated northeastward at deep depths, when it passed through a gap in reported surface ruptures. The main rupture involved the southwestward back-rupture propagation, and it branched out and

376	propagated into the Jordan Thrust and Papatea fault from the Kekerengu fault. Our result
377	suggests that tele-seismic waveform data can resolve such a complex rupture process (e.g., the
378	bilateral rupture, including rupture bifurcation to the Papatea fault), and the potency density
379	tensor inversion approach of projecting slips on multiple faults onto a single model plane, as
380	opposed to an approach of prescribing fault planes, is useful for analyzing earthquakes with
381	complex fault geometries.

382

383 Abbreviations

384 GCMT: Global Centroid Moment Tensor; PDTI: Potency density tensor inversion

385

386 **Declarations**

387 Availability of data and material

388 All seismic downloaded through the IRIS Wilber data were 3 system (https://ds.iris.edu/wilber3/) or IRIS Web Services (https://service.iris.edu/), including the 389 390 following seismic networks: (1) BDSN (https://doi.org/10.7932/BDSN), (2) SCSN (https://doi.org/10.7914/SN/CI), (3) GEOSCOPE (https://doi.org/10.18715/GEOSCOPE.G), 391 392 (4) GEOFON (https://doi.org/10.14470/TR560404), (5) the Global Telemetered Seismograph

- 393 Network (<u>https://doi.org/10.7914/SN/GT</u>), (6) the Hong Kong Seismograph Network, (7) the
- 394 New China Digital Seismograph Network (<u>https://doi.org/10.7914/SN/IC</u>), (8) the IRIS/IDA
- 395 Seismic Network (<u>https://doi.org/10.7914/SN/II</u>), and (9) the Global Seismograph Network
- 396 (https://doi.org/10.7914/SN/IU). The CRUST1.0 and CRUST2.0 structural velocity models are
- 397 available from <u>https://igppweb.ucsd.edu/~gabi/crust1.html</u> and
- 398 <u>https://igppweb.ucsd.edu/~gabi/crust2.html</u>, respectively.
- 399

400 **Competing interests**

401 The authors declare no competing interests. Correspondence and requests for materials should

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403

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407

408 Authors' contributions

409 K.O. and Y.Y. designed this study, compiled the data, and performed the analyses. All authors

410	interpreted the research results. K.O. prepared figures and wrote the manuscript, which was
411	revised by Y.Y., S.Y., R.O., S.H., and Y.F. All authors approved the manuscript. All authors
412	agreed both to be personally accountable for their own contributions and to ensure that
413	questions related to the accuracy or integrity of any part of the work were appropriately
414	investigated and resolved and their resolution documented in the literature.

415

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609 **Figure legends**

Figure 1. **a** Tectonic setting of the study region. The dashed lines represent the plate boundary (Bird 2003). The arrow denotes the plate motion of the Pacific plate relative to the fixed Australia plate in NUVEL 1A (DeMets et al. 1994). The star marks the mainshock epicenter (Lanza et al. 2019). **b** Seismotectonic summary of the study region of the 2016 Kaikoura earthquake. The left and right beachball show the obtained total moment tensor and the Global Centroid Moment Tensor (Dziewonski et al. 1981, Ekström et al. 2012) solution for the

- mainshock, respectively. Black dots represent aftershocks during the week after the mainshock
 (Lanza et al. 2019). Grey, orange, blue, and green lines indicate surface ruptures of the
 2016 Kaikoura earthquake from the New Zealand Active Faults Database (Langridge et al.
 2016). The black line represents the assumed model plane. Background contours display
 topography/bathymetry (Mitchell et al. 2012). HmF–Humps fault zone, CCF–Conway-
- 622 Charwell fault, MF–Manakau fault, UKF–Upper Kowhai fault, JT–Jordan Thrust, PF–Papatea
- 623 fault, KF–Kekerengu fault, NF–Needles fault.



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626 Figure 2. Summary of inversion results. a Azimuthal equidistant projection of the station distribution used in the inversion. The star denotes the epicenter (Lanza et al. 2019). Triangles 627 628 denote station locations; the waveforms for the four stations indicated with red triangles are shown in **b**. The circles represent epicentral distances of 30° and 100°. **b** Observed (upper black 629 630 trace) and synthetic (lower red trace) waveforms at the stations marked in red in a. Station codes and maximum amplitudes are shown at the top. c Potency density tensors on the assumed model 631 632 plane. The map view in the top panel shows the top row of tensors on the assumed model plane, represented by the black line, and grey lines indicate surface ruptures (Langridge et al. 633

2016). The profile in the bottom panel shows the tensors on the assumed model plane. Note that
the beachballs in the map are shown as a lower-hemisphere projection in the map and as a crosssection view from the southeast side in the bottom panel. Beachballs in the bottom panel are
colored based on a Frohlich diagram (Frohlich 2001), in which blue is reverse faulting (T),
green is strike-slip faulting (SS), red is normal faulting (N), and grey is other. The star denotes
the hypocenter (Lanza et al. 2019). d Moment-rate function.



Figure 3. Selected snapshots of potency-rate density tensors **a** before 55 s and **b** after 60 s. Beachballs are shown in cross-section view from the southeast side of the assumed model plane. The background color is scaled with the maximum potency-rate density during 0–55 s for **a** and 60–74 s for **b**; note that the scales differ for the two plots. The star denotes the

- 646 hypocenter (Lanza et al. 2019). Black bars are the locations of the surface faults (Langridge et
- 647 al. 2016) projected onto the model plane.



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Figure 4. Map views showing selected snapshots of strikes of the potency-rate density tensors (cross marks) in the top row of the model plane. Right-lateral or northwest-dipping nodal planes of tensors with relatively large potency-rate density are emphasized. Note that the color scale changes after 55 s.





656 Figure 5. Map views showing selected snapshots of potency-rate density tensors (lower

hemisphere projections) between 60 and 70 s in the top row of the model plane 80–100 km

658 northeast of the epicenter. The color of the beachball symbols represents the potency-rate

density. Above each symbol is shown the ratio of the non-double-couple component.



661

662 Figure 6. Map views showing selected snapshots of potency-rate density tensors (lower

hemisphere projections) between 32 and 42 s in the top row of the entire model plane.

Black dots represent aftershocks during the week after the mainshock (Lanza et al. 2019).

665 Grey, orange, blue, and green lines indicate surface faults (Langridge et al. 2016).