STEEP: a remotely-sensed energy balance model for evapotranspiration estimation in seasonally dry tropical forests

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Highlights

- STEEP is a RS-based SEB model from a one-source bulk transfer equation for SDTF.
- STEEP includes improved representations of phenology and soil moisture for SDTF.
- STEEP is tested against eddy covariance data from the largest SDTF in South America.
- STEEP exhibits satisfactory metrics and outperforms SEBAL, MOD16, and PMLv2.

Abstract

Improvement of evapotranspiration (ET) estimates using remote sensing (RS) products based on multispectral and thermal sensors has been a breakthrough in hydrological research. In large-scale applications, methods that use the approach of RS-based surface energy balance (SEB) models often rely on oversimplifications. The use of these models for Seasonally Dry Tropical Forests (SDTF) has been challenging due to incompatibilities between the assumptions underlying those models and the specificities of this environment, such as the highly contrasting phenological phases or ET being mainly controlled by soil–water availability. We developed a RS-based SEB model from
a one-source bulk transfer equation, called Seasonal Tropical Ecosystem Energy Partitioning (STEEP). Our model uses the plant area index to represent the woody structure of the plants in calculating the moment roughness length. We included the parameter $kB^{-1}$ and its correction using RS soil moisture in the calculation of the aerodynamic resistance for heat transfer. Besides, $\lambda ET$ caused by remaining water availability in endmembers pixels was quantified using the Priestley-Taylor equation. We implemented the algorithm on Google Earth Engine, using freely available data. To evaluate our model, we used eddy covariance data from four sites in the Caatinga, the largest SDTF in South America, in the Brazilian semiarid region. Our results show that STEEP increased the accuracy of ET estimates without requiring any additional climatological information. This improvement is more pronounced during the dry season, which, in general, ET for these SDTF is overestimated by traditional SEB models, such as the Surface Energy Balance Algorithms for Land (SEBAL). The STEEP model had similar or superior behavior and performance statistics relative to global ET products (MOD16 and PMLv2). This work contributes to an improved understanding of the drivers and modulators of the energy and water balances at local and regional scales in SDTF.

Keywords: Sensible heat flux, Aerodynamic resistance for heat transfer, Surface energy balance, Caatinga, Google Earth Engine

1. Introduction

Quantifying evapotranspiration (ET) is one of the largest research challenges in hydrology because ET is driven by a complex combination of atmospheric, vegetation, edaphic, and terrain characteristics (Wang et al., 2016; Bhattarai et al., 2017). The traditional techniques to quantify ET, e.g. Bowen ratio or eddy covariance system (EC), are limited to areas up to ~10 km² (Allen et al., 2011; Anapalli et al., 2016; Mcshane et al., 2017; Mallick et al., 2018; Chu et al., 2021). Over the past decades, models based on satellite remote sensing (RS) data have been increasingly developed and applied to estimate ET for multiple temporal and spatial scales (Anderson et al., 2011; Chen and Liu, 2020). RS-based surface energy balance (SEB) models estimate ET in terms of energy per unit area (e.g. W/m²), i.e. by latent heat flux, $\lambda ET$, where $\lambda$ is the latent heat of vaporization of water (Shuttleworth, 2012; Barraza et al., 2017; Trebs et al., 2021). SEB models obtain $\lambda ET$ by subtracting the soil heat ($G$) and sensible heat ($H$) fluxes from the net radiation ($R_n$). Estimates of $R_n$
obtained with RS data have been improving, and this flux can nowadays be estimated with acceptable precision (Allen et al., 2011; Ferreira et al., 2020). The G:R, ratio can be predicted with reasonable accuracy through the use of empirical relationships with soil, vegetation, and temperature characteristics (Bastiaanssen, 1995; Murray and Verhoef, 2007; Allen et al., 2011; Danelichen et al., 2014). Challenges in estimating λET as a residual of the energy balance are mostly associated with the uncertainties in H (Gokmen et al., 2012; Paul et al., 2014; Mohan et al., 2020a, Mohan et al., 2020b; Costa-Filho et al., 2021). The bulk heat transfer calculation that is used to compute H involves variables related to the temperature gradient and to the aerodynamic resistance for heat transfer (rah). If any of these variables are poorly estimated, the performance of SEB models will be reduced (Verhoef et al., 1997a, b; Su et al., 2001; Gokmen et al., 2012; Costa-Filho et al., 2021; Liu et al., 2021; Trebs et al., 2021).

The difference between the aerodynamic surface temperature and air temperature (dT) drives H. However, the lack of techniques to measure the aerodynamic surface temperature required strategies to use the radiometric land surface temperature (LST) as an alternative. Bastiaanssen et al. (1998), when creating the Surface Energy Balance Algorithms for Land (SEBAL), proposed that dT can be estimated with a linear relationship on LST. This requires identifying areas with contrasting extreme conditions in terms of cover and humidity, e.g., dry bare and well-watered soil surfaces, commonly known as hot/dry and cold/wet endmembers, respectively. The sensible heat transfer equation in conjunction with the surface energy balance in hot/dry and cold/wet endmembers allows one to obtain the coefficients of the linear relationship between dT and LST. Bastiaanssen et al. (1998) proposed the selection of endmembers by assuming that H in the cold/wet endmember and λET in the hot/dry endmember are zero. However, these assumptions are not necessarily valid (Singh and Irmak, 2011; Singh et al., 2012). The cold/wet endmember refers to an area with a well-irrigated crop surface having ground fully covered by vegetation, so it can be assumed that a non-negligible amount of sensible heat can still be generated by such a surface. Similarly, for the hot/dry endmember, an area dominated by bare soil, there may be a λET resulting from antecedent rainfall events, hereafter referred to as remaining λET. Some studies have quantified H and λET in hot/dry and cold/wet endmembers (Trezza, 2006; Allen et al., 2007; Singh and Irmak, 2011); they have shown that this quantification produces a better approximation of daily ET.
Based on the Monin-Obukhov similarity theory, $rah$ is defined as a function of the momentum

\[ (z_0m) \] and heat \( (z_0h) \) roughness lengths. Theoretically, the sum of the zero plane displacement

\[ (d_0) \] together with \( z_0h \) defines the level of the effective source of sensible heat (Thom, 1972;

Chehbouni et al., 1996; Gokmen et al., 2012) and, therefore, \( z_0h \) constitutes one of the most crucial

parameters for the accurate calculation of \( H \) (Verhoef et al., 1997a; Su et al., 2001). However, as

\( z_0h \) cannot be measured directly, it is commonly calculated via the dimensionless parameter \( kB^{-1} \)

formulated to express the excess resistance of heat transfer compared to momentum transfer (Owen

and Thomson, 1963). In RS-based SEB models, oversimplifications are present in the calculation of

$rah$, e.g. different land use types are represented by the same values for \( z_0h \) (Bastiaanssen et al.,

2005; Allen et al., 2007) and \( kB^{-1} \) (Bastiaanssen et al., 1998), or the values for the aerodynamic

parameters are kept constant in time and space. However, these parameters should not be

considered constant, nor set to zero, because this can lead to large inaccuracies in the estimates of

\( H \) (Verhoef et al., 1997a) and, consequently, of \( \lambda ET \) (Liu et al., 2007; Paul et al., 2014; Liu et al.,

2021). Studies have shown that \( kB^{-1} \) typically ranges from 1 to 12, depending on the dominant

surface coverage (Kustas et al., 1989a; Troufleau et al., 1997; Verhoef et al., 1997a; Lhomme et al.,

2000; Su et al., 2001). Studies confirm that if appropriate values of \( kB^{-1} \) are used, \( H \) can be accurately

estimated using LST via the bulk transfer method (Stewart et al., 1994; Su et al., 2001; Jia et al.,

2003; Paul et al., 2013).

Another problem with RS-based SEB models is that these methods are imprecise when

applied to non-agricultural environments, such as forests, deserts, sparse savannahs or rangelands,

and riparian systems, because of the heterogeneous nature of the vegetation, terrain, soils, and

water availability in these environments. This causes the flux estimates obtained with the SEB

methods, and the underlying aerodynamic parameters, to be highly variable (Allen et al., 2011;

Gokmen et al., 2012; Barraza et al., 2017; Chen and Liu, 2020; Costa-Filho et al., 2021). This is

especially true in Seasonally Dry Tropical Forests (SDTF) regions, where there is a large spatio-
temporal variation in vegetation density, in vegetation structural parameters such as canopy height,
crown shape and branching, and water availability. SDTF are an important tropical biome and one

of the most threatened ecoregions of the world (Moro et al., 2015; Pennington et al., 2018). SDTF

are broadly defined as forest formations in tropical regions characterised by marked seasonality in
rainfall distribution, resulting in a prolonged dry season that usually lasts five or six months (Pennington et al., 2009; Paloschi et al., 2020). The most extensive contiguous areas of SDTF are in the neotropics, comprising more than 60% of the remaining global stands of this vegetation (Miles et al., 2006; Queiroz et al., 2017). The physiognomies exhibited by SDTF are heterogeneous, with vegetation ranging from tall forests with closed canopies to scrublands rich in succulents and thorn-bearing plants (Moro et al., 2015; Paloschi et al., 2020). SDTF foliage patterns are adapted to the intense climate and water seasonality, which is highly dependent on interannual climate variability (Alberton et al., 2017; Medeiros et al., 2022). The vegetation drops most leaves during the dry season, and the first rainfall events trigger a rapid leaf growth in the wet season (Alberton et al., 2017; Paloschi et al., 2020; Medeiros et al., 2022). SDTF are being rapidly degraded (12% between 1980 and 2000), highlighting an urgent priority for their conservation (Moro et al., 2015; Maia et al., 2020). The risks faced by SDTF mainly stem from anthropogenic disturbance effects, which range from local habitat loss to global climate change, leading to biodiversity loss and reductions in biomass (Allen et al., 2017; Maia et al., 2020).

Application of SEB models to estimate evapotranspiration over SDTF has been challenging due to the incompatibility between the existing assumptions of the models and the specificities of these forests. Precipitation seasonality is the primary phenological regulator of SDTF (Moro et al., 2016; Campos et al., 2019; Paloschi et al., 2020), and land-cover patterns show distinct intra- and inter-annual spectral responses (Cunha et al., 2020; Andrade et al., 2021; Medeiros et al., 2022). Therefore, biophysical remotely-sensed variables, such as Normalized Difference Vegetation Index (NDVI) and surface albedo, which are usually used to select the endmembers, exhibit high spatial and temporal variability in SDTF, which causes ET estimates from the SEB models to lack fidelity (Silva et al., 2019). Selection of suitable roughness parameters such as $z_0m$, $d_0$, and $kB^{-1}$ is important for the correct quantification of the energy balance in SDTF. However, these parameters are more challenging to obtain in SDTF than for evergreen forests, as in addition to vegetation height, other characteristics such as plant density, above-ground plant structure and the strong seasonality of phenology (Alberton et al., 2017; Miranda et al., 2020; Paloschi et al., 2020) have a considerable effect on the turbulent transfer in these forests. Another key issue is how to verify the results of SEB methods due to the scarcity, in many regions, of terrestrial observations and the uneven
spatiotemporal distribution of monitoring data. SEB models may not satisfactorily represent ET in regions with sparse vegetation and high climatic seasonality, such as SDTF (Senkondo et al., 2019; Laipelt et al., 2021; Melo et al., 2021). The main reason is that these methods have generally been evaluated and/or parameterized using sites located in other ecosystems and climates in North America, Europe, Australia, East Asia, and in agricultural regions that have characteristics quite distinct from SDTF (Melo et al., 2021). Therefore, a better quantification of ET, especially in regions with high climatic seasonality, will help to design better water management policies that will be able to deal with the effects of climate variability, land use/cover and climate changes (Lima et al., 2021).

We hypothesise that a SEB model that improves or considers estimates of $r_{ah}$ via $z_0m$ and $kB^{-1}$ will improve $H$ and ET for STDF. To test this assumption, we introduce a novel calibration-free SEB model based upon a one-source bulk transfer equation, herein referred to as Seasonal Tropical Ecosystem Energy Partitioning (STEEP). The STEEP model aims to improve $H$ and ET estimates for STDF by incorporating the woody structure of plants through the Plant Area Index (PAI), and soil moisture obtained by remote sensing to help represent the seasonality of the aerodynamic and surface variables that drive the energy fluxes. To obtain the coefficients of the linear relationship between $dT$ and LST its coefficients, we computed $H$ by the surface energy balance, and the remaining $\lambda ET$ through the principle of the Priestley-Taylor equation in the hot/dry and cold/wet endmembers. STEEP is designed to take advantage of the extensive free database available on the Google Earth Engine (GEE) cloud computing environment. STEEP is herein evaluated at the field scale against four flux towers in the Caatinga, the largest continuous SDTF in the Americas. Additionally, the model was compared with SEBAL and two consolidated global ET products: MOD16 (Mu et al., 2011; Running et al., 2017) and PMLv2 (Zhang et al., 2019).

2. Methodology

2.1 Study areas and respective data

The study concerns the Brazilian Caatinga, located between the Equator and the Tropic of Capricorn (about 3 and 18° south), in the Brazilian semiarid region. It covers an area of about 850,000 km² (Silva et al., 2017a; Andrade et al., 2021; Brazil MMA, 2021). The climate in the Caatinga is characterized by high air temperatures (around 26–30° C) and high potential
evapotranspiration (1,500–2,000 mm/year) coupled with low annual rainfall (300–800 mm/year, normally concentrated in 3–6 months) with high intra- and inter-annual variability in space and time, and a long dry season which sometimes lasts up to 11 months in some areas of Caatinga (Moro et al., 2016; Miranda et al., 2018; Paloschi et al., 2020). The Caatinga vegetation has at least thirteen physiognomies ranging from woods to sparse thorny shrubs, morphologically adapted to resist water stress and high air temperatures (Araújo et al., 2009; Silva et al., 2017a; Marques et al., 2020; Miranda et al., 2020), and it has been identified as one of the most biodiverse SDTF regions globally (Pennington et al., 2006; Santos et al., 2014; Koch et al., 2017). Still, the Caatinga and other SDTF are among the least studied ecoregions compared to tropical forests and savannas (Santos et al., 2012; Koch et al., 2017; Tomasella et al., 2018; Borges et al., 2020). Only 1% of the Brazilian Caatinga area is legally protected (Koch et al., 2017).

We used data from four sites located in the Caatinga (Fig. 1 and Table 1). The surrounding areas of each of our study sites — which exceeds these EC towers footprints — are homogeneously covered by Caatinga vegetation (Fig. S1). Located on crystalline terrain (Fig. 1a), these Caatinga sites have soils with highly variable properties, ranging from fertile (those with a clayey texture) to poor (those soils that are sandier). However, most soils of the SDTF are typically shallow and stony (i.e. Entisols, Alfisols, and Ultisols; WRB, 2006), retaining water only for a short period between rainfall events and after the rainy season (Moro et al., 2015; Queiroz et al., 2017). The wet and (dry) seasons from the sites Petrolina (PTN) are concentrated in Jan–Apr (May–Dec; Souza et al., 2015); Serra Negra do Norte (SNN) in Jan–May (June–Dec; Marques et al., 2020); Serra Talhada (SET) in Nov–Apr (May–Oct; Silva et al., 2017b) and Campina Grande (CGR) in Mar–July (Aug–Feb; Oliveira et al., 2021). The climate of the four observation sites is semi-arid, type BSh (Fig. 1b) according to the Köppen climate classification (Alvares et al., 2013).

Eddy covariance data, covering several periods from 2011 to 2020 (Fig. 1c), were used to evaluate the modelled ET and $H$. The four sites were instrumented with five flux towers equipped with three-dimensional ultrasonic anemometers (CSAT3, Campbell Scientific Inc., Logan, UT, USA in all the sites except CGR 2020) and open-path infrared gas analysers (LI-7500, LI-COR Inc., Lincoln, NE, USA, in the PTN site, or EC150, Campbell Scientific Inc., Logan, UT, USA, in the SET, SNN, and CGR 2014 sites). In the more recent experiment (CGR 2020), the flux tower was equipped
with an IRGASON (Campbell Scientific Inc., Logan, UT, USA) that integrates the two sensors in just one instrument. ET data for the PTN, SNN, and SET sites have been previously described; they underwent standard procedures to ensure their quality and were published by Melo et al. (2021). Observations at the CGR site were collected through two micrometeorological towers, located in a dense Caatinga area within the Brazilian National Institute of Semiarid (INSA) experimental area, a 300 ha forest reserve with different stages of regeneration. The first tower (height of 7 m) was active between the years of 2014 and 2017, as described in Oliveira et al. (2021). The second tower (height of 15 m) is part of the Caatinga Observatory (OCA) and includes an EC system that has been collecting data since 2020. The OCA is a laboratory maintained by the Federal University of Campina Grande and INSA. H data for the PTN, SNN and CGR sites have been obtained from the respective principal investigators, while data for the SET site have been obtained from the AmeriFlux network (Antonino, 2019). For the retrieval of λET and H, LoggerNet software (Campbell Scientific, Inc., Logan, UT, USA) was used in order to transform 10 Hz raw data into 30 min binaries. Afterwards, EdiRe software (Campbell Scientific Inc., Logan, UT, USA) was used to process the high-frequency data, averaging every 30 min. The data from the EC flow towers in CGR have previously gone through standard procedures to ensure their quality. Detailed information on data processing, quality control, and post-processing can be found in Campos et al. (2019) and Cabral et al. (2020). The raw data from the CGR flux tower were processed by Easy-flux data processing software (Campbell Scientific Inc., Logan, UT, USA). In addition, data for any day with rainfall greater than 0.5 mm were removed. The daily ET was calculated using the daily average λET.
Table 1. List of EC-equipped flux tower observation sites in the study area.

<table>
<thead>
<tr>
<th>Sites</th>
<th>State of Brazil</th>
<th>Mean annual of rainfall (mm)¹</th>
<th>Site average elevation (m)</th>
<th>Main tree species</th>
<th>Location (Lon;Lat)</th>
<th>Data availability</th>
<th>Wet / Dry Seasons</th>
<th>Main reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Campina Grande (CGR)</td>
<td>Paraíba</td>
<td>777</td>
<td>490</td>
<td>Croton blanchetianus, Mimosa ophthalmoncentra, Poincianella pyramidalis, Allophylus quercifolius, Mimosa sp.²</td>
<td>-35.9763; -7.2805</td>
<td>Jan–Dec 2020</td>
<td>Mar-July / Aug-Feb</td>
<td>This study</td>
</tr>
</tbody>
</table>
¹ Rainfall Data Sources: Brazilian National Institute of Meteorology (INMET) and Pernambuco State Agency for Water and Climate (APAC).

² Barbosa et al. (2020).
Fig. 1. Location of flux tower observation sites in Caatinga. a) Geographical overview of the Caatinga (Moro et al., 2015), b) Köppen’s climate classification map: Tropical zone with dry summer (As), Tropical zone with dry winter (Aw), Dry zone semi-arid low latitude and altitude (Bsh), Humid subtropical zone without dry season and with hot summer (Cfa), Humid subtropical zone with dry winter and hot summer (Cwa), Humid subtropical zone with dry winter and temperate summer (Cwb), Humid subtropical zone with dry winter and short and cool summer (Cwc), Humid subtropical zone with dry summer and hot (Csa), according to Alvares et al. (2013) and c) Data availability on the observation sites after procedures to ensure their quality.

2.2 The Seasonal Tropical Ecosystem Energy Partitioning (STEEP) model

SEB models have been applied in many parts of the world (Mohan et al., 2020a). The one-source SEB models that are most commonly found in the literature are SEBAL (Bastiaanssen et al., 1998), Surface Energy Balance System (SEBS; Su, 2002), Mapping EvapoTranspiration at high Resolution with Internal Calibration (METRIC; Allen et al., 2007), and Operational Simplified Surface Energy Balance (SSEBop; Senay et al., 2013). As in other SEB models, STEEP performs the energy balance at the time of satellite overpass (instantaneous) to obtain λET as the surface energy balance residual. The computation of \( R_n \) and \( G \), necessary to get \( \lambda ET \), followed the procedures described in Ferreira et al. (2020) and Bastiaanssen et al. (2002), respectively, but with input data from the
Moderate-Resolution Imaging Spectroradiometer (MODIS) sensor. $H$ was calculated following the methods described in Table 2: using $rah$ and $dT$, both traditionally applied in SEB models, but also focusing on peculiarities of SDTF that have never been considered in other SEB models. In this proposed version, $rah$ was described according to Verhoef et al. (1997a) and Paul et al. (2013), which requires, among other parameters/variables, the momentum roughness length ($z0m$), the zero plane displacement height ($d0$), the dimensionless parameter $kB^{-1}$, and the atmospheric stability corrections (Paulson, 1970). $z0m$ is influenced by a range of plant structural properties, e.g. vegetation height, breadth and vegetation drag coefficients, and spacing (or density). $z0m$ is commonly computed as a function of Leaf Area Index (LAI; Verhoef et al., 1997b; Liu et al., 2021). However, most SDTF plants spend a substantial part of the year without leaves; under these conditions, $z0m$ should be derived from information on dimensions of trunks, stems, and branches. Since LAI is only related to leaf cover quantity and variability, it cannot represent the woody plant structure without leaves (Miranda et al., 2020). Therefore, the Plant Area Index (PAI), which is the total above-ground plant area, i.e. leaves and woody structures, was used to represent plant structures in the computation of $z0m$ and $d0$.

To incorporate the conditions of water variability in the forest system in the calculation of sensible heat we applied the procedure described in Gokmen et al. (2012) that corrects the $kB^{-1}$ equation presented in Su et al. (2001), incorporating soil moisture obtained by remote sensing. The canopy conductance profiles are the link between soil moisture and sensible/latent heat flux. The source of sensible/latent heat moves vertically throughout the canopy as a function of plant water stress (Gokmen et al., 2012; Bonan et al., 2021), which affects heat roughness length, and, therefore, $kB^{-1}$ and $rah$. Thus, when there is a reduction in soil moisture, there is also a reduction in the value of $rah$ and, consequently, an increase of $H$ and a decrease in $\lambda ET$. Furthermore, to calculate $dT$, we used the linear relationship on LST, using the assumption of extreme contrast in terms of cover and soil wetness (hot/dry and cold/wet endmembers) to determine the linear relationship coefficients. However, in the hot/dry and cold/wet endmembers pixels, $H$ was computed by the surface energy balance (Allen et al., 2007), and the remaining $\lambda ET$ was incorporated through the Priestley-Taylor (1972) equation and plant physiological constraints following the approach in Singh and Irmak (2011) and French et al. (2015). PAI and soil moisture time series used in our study can be seen in Fig. S2.
The references for the methods and equations adopted to formulate the STEEP model can be found in Table 2 and Appendix A, respectively. For illustration purposes, Table 2 also shows the references for the methods for one of the most widely used RS SEB models, the SEBAL model.

Table 2. References for the methods used in the STEEP and SEBAL models to obtain the sensible heat flux.

<table>
<thead>
<tr>
<th>Variable/Parameter</th>
<th>STEEP</th>
<th>SEBAL</th>
</tr>
</thead>
<tbody>
<tr>
<td>Aerodynamic resistance for heat transfer (r_{ah})</td>
<td>Verhoef et al., 1997a; Paul et al., 2013</td>
<td>Bastiaanssen et al., 2002; Laipelt et al., 2021</td>
</tr>
<tr>
<td>Roughness length for momentum transfer (z_{0m})</td>
<td>Verhoef et al., 1997b; Paul et al., 2013, replacing LAI with PAI</td>
<td>Bastiaanssen et al., 2002; Laipelt et al., 2021</td>
</tr>
<tr>
<td>Zero plane displacement height (d_{0})</td>
<td>Verhoef et al., 1997b; Paul et al., 2013</td>
<td>-</td>
</tr>
<tr>
<td>Plant Area Index (PAI)</td>
<td>Miranda et al., 2020</td>
<td>-</td>
</tr>
<tr>
<td>Parameter $k_B^{-1}$</td>
<td>Su et al., 2001</td>
<td>uses $z_0h$ with constant value (0.1); Bastiaanssen et al., 2002</td>
</tr>
<tr>
<td>Correction of soil moisture by remote sensing in $k_B^{-1}$</td>
<td>Gokmen et al., 2012</td>
<td>-</td>
</tr>
<tr>
<td>Calculation of the $H$ and the remaining $\lambda ET$ in endmembers pixels</td>
<td>Allen et al., 2007; Singh and Irmak, 2011; French et al., 2015</td>
<td>Calculation of the $H$ in the hot/dry endmember only; Bastiaanssen et al., 2002</td>
</tr>
</tbody>
</table>

2.3 Algorithm implementation and processing

We implemented STEEP on the Google Earth Engine (GEE) cloud computing environment (Gorelick et al., 2017) using the Python API (version 3.6). Statistical analyses to evaluate the performance of the models were also conducted in Python and implemented in the Jupyter programming environment. The Python package geemap (Wu, 2020) enabled the integration of Python with the GEE environment, and the hydrostats package (Roberts et al., 2018) was used for the statistical evaluation of the performance of the models.

We designed the application of the model to take advantage of the data available on GEE (Table 3). The remote sensing datasets were derived from MODIS sensor products, the Shuttle Radar Topography Mission (SRTM; Farr et al., 2007), and the Global Forest Canopy Height product provided vegetation height (Potapov et al., 2021). The climate data necessary to run the model, i.e. wind speed, air temperature, relative humidity, shortwave radiation, and net thermal radiation at the surface, were sourced from the ERA5-Land reanalysis product (Muñoz Sabater, 2019). For data
regarding soil moisture, we used the Global Land Data Assimilation System (GLDAS) product (Rodell et al., 2004). CHIRPS precipitation product (Funk et al., 2015) was used to estimate the daily rainfall amount at the sites evaluated.

Table 3. Description of the datasets available on the GEE platform used in the research.

<table>
<thead>
<tr>
<th>Product</th>
<th>GEE ID</th>
<th>Bands/variables</th>
<th>Time coverage</th>
<th>Spatial resolution</th>
<th>Temporal resolution</th>
</tr>
</thead>
<tbody>
<tr>
<td>MCD43A4.006</td>
<td>MODIS/006/MCD43A4</td>
<td>B1–B7</td>
<td>Feb 2000–present</td>
<td>0.5 km</td>
<td>1 day</td>
</tr>
<tr>
<td>MOD09GA.006</td>
<td>MODIS/006/MOD09GA</td>
<td>SolarZenith</td>
<td>Feb 2000–present</td>
<td>1 km</td>
<td>1 day</td>
</tr>
<tr>
<td>MOD11A1.006</td>
<td>MODIS/006/MOD11A1</td>
<td>LST_Day_1km; Emis_31, Emis_32</td>
<td>Mar 2000–present</td>
<td>1 km</td>
<td>1 day</td>
</tr>
<tr>
<td>SRTM</td>
<td>USGS/SRT MGL1_003</td>
<td>Elevation</td>
<td>Feb 2000</td>
<td>0.03 km</td>
<td>-</td>
</tr>
<tr>
<td>ERA5-Land</td>
<td>ECMWF/ERA5_LAND/HOURLY</td>
<td>dewpoint_temperature_2m, temperature_2m, u_component_of_wind_10, v_component_of_wind_10m, surface_net_solar_radiation_hourly, surface_net_thermal_radiation_hourly</td>
<td>Jan 1981–present</td>
<td>0.1°</td>
<td>1 h</td>
</tr>
<tr>
<td>GLDAS</td>
<td>NASA/GLDAS S/V021/NOAH/G025/T3H</td>
<td>SoilMoi0_10cm_inst</td>
<td>Jan 2000–present</td>
<td>0.25°</td>
<td>3 h</td>
</tr>
<tr>
<td>Global Forest Canopy Height, 2019</td>
<td>users/potapo vpeter/GEDI_V2</td>
<td>-</td>
<td>Apr 2019</td>
<td>0.03 km</td>
<td>-</td>
</tr>
<tr>
<td>CHIRPS</td>
<td>UCSB-CHG/CHIRPS/DAILY</td>
<td>Precipitation</td>
<td>Jan 1981–present</td>
<td>0.05°</td>
<td>1 day</td>
</tr>
<tr>
<td>MOD16A2.006</td>
<td>MODIS/006/MOD16A2</td>
<td>ET</td>
<td>Jan 2001–present</td>
<td>0.5 km</td>
<td>8 days</td>
</tr>
<tr>
<td>PML_V2</td>
<td>projects/pml _evapotranspiration/PML/OUTPUT/PML_V2_8day_yv016</td>
<td>Es, Ec, Ei</td>
<td>Feb 2000–present</td>
<td>0.5 km</td>
<td>8 days</td>
</tr>
</tbody>
</table>

The presence of clouds or instrumental malfunctioning of orbital sensors can cause gaps in data. To reduce the loss of information due to missing data, we chose to use the MODIS MCD43A4
reflectance product. By combining reflectance data from MODIS sensors aboard the AQUA and TERRA satellites and modelling the anisotropic scattering characteristics using sixteen-day quality observations, the MCD43A4 product represents the daily dynamics of the Earth’s surface without missing data (Schaaf and Wang, 2015). Daily surface reflectance data from the MCD43A4 product were used to obtain the surface albedo and vegetation indices (NDVI and PAI) needed to run STEEP. Thus, the surface albedo data and the vegetation indices show a low percentage of missing data.

To compose the LST time series, we used data from MOD11A1, and to fill its missing data, a filter with the average value for a monthly window was applied. This procedure is similar to the method proposed by Zhao et al. (2005) and it is also used by the MOD16 algorithm to generate the continuous global ET (Mu et al., 2011).

Following the approach in comparable studies, STEEP algorithm processing was conducted with automatic selection of endmembers pixels (Bhattarai et al., 2017; Silva et al., 2019; Laipelt et al., 2021). Like Silva et al. (2019), we used the biophysical variables NDVI, surface albedo and LST to automate selection of the endmembers, but we applied different criteria. For the hot/dry endmember selection, the first step consisted of selecting those pixels whose surface albedo values are between the 50 and 75% quantiles, and with NDVI values greater than 0.1 and less than the 15% quantile. After this first selection, a refinement is applied by selecting only those pixels from this first set that have LST values between the 85 and 97% quantiles. Using the set of pixels that met these criteria, the median values of $R_n$, G, LST and $rah$ were calculated to establish a single value for each variable and describe the characteristics of the hot pixel. We applied a similar procedure to select the cold/wet endmember but with different limits (Table 4). The procedure for finding endmembers was conducted daily. To execute the model and conduct the selection of endmembers, we used an area of interest (AOI), also known as domain size. AOI was defined as a square area with 1000-km sides within the Caatinga domain and centred on the tower coordinates of each site. Cheng et al. (2021), for example, applied the SEBAL using MODIS data in China and used an AOI of 1200-km x 1200-km.

<table>
<thead>
<tr>
<th>Endmembers</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
</tr>
</tbody>
</table>

Table 4. Methodology used for the selection of endmembers pixels.
<table>
<thead>
<tr>
<th>Step 1</th>
<th>Hot/dry pixel</th>
<th>Cold/wet pixel</th>
</tr>
</thead>
<tbody>
<tr>
<td>Q50% &lt; surface albedo &lt; Q75% and 0.10 &lt; NDVI &lt; Q15%</td>
<td>Q25% &lt; surface albedo &lt; Q50% and NDVI &gt; Q97%</td>
<td></td>
</tr>
<tr>
<td>Step 2</td>
<td>Of the pixels of the 1st Step, select pixels with Q85% &lt; LST &lt; Q97%</td>
<td>Of the pixels of the 1st Step, select pixels with LST &lt; Q20%</td>
</tr>
<tr>
<td>Step 3</td>
<td>Of the set of pixels that met the previous steps, the median values of $R_n$, $G$, LST and $r_{ah}$ were calculated to establish a single value for each variable and describe the characteristics of endmembers</td>
<td></td>
</tr>
</tbody>
</table>

Q = quantile.

2.4 Analysis of the algorithms’ performance

We used SEBAL as a reference RS SEB model for comparison with STEEP. SEBAL is one of the most applied SEB models since the algorithm uses a minimal number of in situ measurements compared to similar models, e.g. METRIC and SSEBop, and is considered a suitable choice for evapotranspiration estimates over cropped areas and in the context of water resource management (Kayser et al., 2022). Applications with SEBAL have been conducted in the Caatinga as in the studies of Teixeira et al. (2009), Santos et al. (2020), Costa et al. (2021), and Lima et al. (2021). Implementations of the SEBAL algorithm are popular on several computing platforms, e.g. GRASS-Python (Lima et al., 2021); Google Earth Engine (Laipelt et al., 2021); Python (Mhawej et al., 2020), following the formulations described in Bastiaanssen et al. (1998) and Bastiaanssen et al. (2002). The SEBAL version implemented in this work followed those presented by Bastiaanssen et al. (2002), Costa et al. (2021) and Laipelt et al. (2021). The remote sensing datasets and endmembers pixels selection for SEBAL were the same as described in STEEP.

ET and $H$ estimates from STEEP and SEBAL were evaluated against the eddy covariance measurements of the corresponding tower. Here, the modelled values were extracted for the pixel representing the EC tower for each observation site. The footprint fetches for PTN, SET, SNN is less than 500 m (Silva et al., 2017b; Campos et al., 2019; Santos, et al., 2020). We assume a similar footprint for CGR due to its similarity in terms of wind characteristics and terrain slope compared to the other sites. Moreover, the surrounding areas of each of our study sites (Fig. S1) — which exceeds these EC towers footprints — are homogeneously covered by Caatinga vegetation. We evaluated daily ET values, and instantaneous hourly $H$ values more specifically with the modelled/measured $H$
value at 11:00 am local time (GMT-3), considering this is the closest time to the satellite’s overpass.

Additionally, the STEEP model was compared with two consolidated global ET products available on GEE: MODIS Global Terrestrial Evapotranspiration A2 version 6 (MOD16; Mu et al., 2011; Running et al., 2017) and Penman-Monteith-Leuning model version 2 global evaporation (PMLv2; Zhang et al., 2019); both products have a pixel resolution of 500 m (Table 3). The algorithm used in MOD16 is based on the Penman-Monteith equation and driven by MODIS remote sensing data with Modern-Era Retrospective analysis for Research and Applications (MERRA; Mu et al., 2011). In MOD16 ET is the sum of soil evaporation (Es), canopy transpiration (Tc) and wet-canopy evaporation (Ec) and is provided as eight-day cumulative values. More details about MOD16 can be found in Mu et al. (2011) and Running et al. (2017). The global PMLv2 product involves a biophysical model based on the Penman-Monteith-Leuning equation which also uses MODIS remote sensing data, but with meteorological reanalysis data from GLDAS as model inputs. As in MOD16, ET in PMLv2 is also the sum of Es, Tc and Ec but is provided as eight-day average values. To make MOD16 and PMLv2 values compatible, ET of PMLv2 was multiplied by eight. Details about PMLv2 can be found in Gan et al. (2018) and Zhang et al. (2019). We accumulated the daily ET measured at the observation sites, i.e. derived from EC data, and ET modelled with STEEP for the same eight-day time periods to make them compatible with the temporal resolution of the MOD16 and PMLv2 datasets. The average of the measured daily values over each eight-day time period (even if there were missing values within this period) was multiplied by eight to calculate the observed 8-day ET.

To match the time steps of STEEP and MOD16/PMLv2 ET values, the 8-day average of the evaporative fraction (EF) was multiplied by the daily net radiation over those 8 days, assuming that EF can be considered constant in each of these periods. Then the ET was summed over the 8-day interval. Finally, we also compared the modelled ET (by STEEP and the two global products) with the observed ET, only in the 8-day periods when no field-observed data was missing. However, with this criterion the number of observations dropped dramatically.

The STEEP and SEBAL models and global ET products were evaluated with five performance metrics (Table 5). A combination of performance metrics is often used to assess the overall performance of models because a single metric provides only a projection of a certain aspect of the error characteristics (Chai and Draxler, 2014). Root mean square error (RMSE) is commonly used...
to express the accuracy of the results with the advantage that it presents error values in the same units of the variable analysed; optimal values are close to zero (Hallak and Pereira Filho, 2011). Coefficient of determination ($R^2$) represents the quality of the linear trend between observed and simulated data and ranges from 0 to 1; high values indicate better model performance. Nash–Sutcliffe efficiency ($NSE$) indicates the accuracy of the model output compared to the average of the referred data ($NSE = 1$ is the optimal value; Nash and Sutcliffe, 1970). Concordance correlation coefficient ($\rho_c$) is a measure that evaluates how well bivariate data falls on the 1:1 line. $\rho_c$ measures both precision and accuracy. It ranges from -1 to +1 similar to Pearson’s correlation coefficient, with perfect agreement at +1 (Lin, 1989; Liao and Lewis, 2000; Akoglu, 2018). Percentage bias ($PBIAS$) measures the average relative difference between observed and estimated values, with an optimal value of 0 (Gupta et al., 1999). Additionally, we evaluate STEEP’s model structure by extracting model’s performance metrics after excluding it from its main implementations individually (Table 2) and by two-by-two combinations of $z0m, rah$ and $r\lambda ET$. We run the control version of the SEB model, i.e. SEBAL in our case, while incorporating one or two improvements in the model and keeping the remaining parts of the algorithm the same as the reference SEB model.

Table 5. Performance metrics used to evaluate ET and $H$ in this study.

<table>
<thead>
<tr>
<th>Performance metric</th>
<th>Equation</th>
<th>Range (Perfect value)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Root mean square error ($RMSE$)</td>
<td>$RMSE = \sqrt{\frac{\sum_{i=1}^{N}(M_i - O_i)^2}{N}}$</td>
<td>[0, $+\infty$] [0)</td>
</tr>
<tr>
<td>Coefficient of determination ($R^2$)</td>
<td>$R^2 = \frac{\left[\sum_{i=1}^{N}(O_i - \bar{O})(M_i - \bar{M})\right]^2}{\sum_{i=1}^{N}(O_i - \bar{O})^2 \cdot \sum_{i=1}^{N}(M_i - \bar{M})^2}$</td>
<td>[0, 1] (1)</td>
</tr>
<tr>
<td>Nash–Sutcliffe efficiency ($NSE$)</td>
<td>$NSE = 1 - \frac{\sum_{i=1}^{N}(M_i - O_i)^2}{\sum_{i=1}^{N}(O_i - \bar{O})^2}$</td>
<td>[-\infty, 1] (1)</td>
</tr>
<tr>
<td>Concordance correlation coefficient ($\rho_c$)</td>
<td>$\rho_c = \frac{2\sum_{i=1}^{N}(O_i - \bar{O})(M_i - \bar{M})}{\sum_{i=1}^{N}(O_i - \bar{O})^2 + \sum_{i=1}^{N}(M_i - \bar{M})^2 + (N - 1)(\bar{O} - \bar{M})^2}$</td>
<td>[-1, 1] (1)</td>
</tr>
<tr>
<td>Percentage bias ($PBIAS$)</td>
<td>$PBIAS = \frac{\sum_{i=1}^{N}(M_i - O_i) \cdot 100}{\sum_{i=1}^{N}O_i}$</td>
<td>[-\infty, +\infty] [0)</td>
</tr>
</tbody>
</table>

where: $N$ sample size; $O$ observed value; $M$ modelled value; $\bar{O}$ observed mean; $\bar{M}$ modelled mean.

3. Results and discussion

3.1 Comparison of STEEP and SEBAL models results with observed (EC) values
The performance statistics of daily ET by STEEP and SEBAL in wet and dry seasons for the evaluated sites are shown in Fig. 2. In general, STEEP exhibited a better performance than SEBAL. Although the better statistical metrics of STEEP were in the dry season, in the wet season, they were also superior compared to SEBAL. Specifically, in the dry season, STEEP exhibited a RMSE between 0.6 and 1.06 mm/day, while SEBAL this was between 1.06 and 2.24 mm/day. The maximum value of $R^2$ in STEEP was 0.62 (sites PTN and SNN), whereas SEBAL achieved only 0.33. The NSE metric was the worst among the five analysed in SEBAL: values lower than -7.5 occurred in three of the five sites. Although in STEEP, PTN and SNN sites NSE had values higher than 0 (0.55 and 0.25, respectively) the other sites also had negative values, reaching up to -2.5. In terms of $\rho_c$, values ranged from 0.09 to 0.77 in STEEP and from -0.04 to 0.41 in SEBAL. It is also possible to see the reduction that STEEP has brought to ET modelling in terms of PBIAS when compared to SEBAL.

Globally, without discriminating between wet and dry seasons, STEEP exhibited better statistical performance than SEBAL at all the evaluated sites (Fig. 3). While STEEP exhibited a RMSE between 0.75 and 0.94 mm/day, the RMSE for SEBAL was between 1.08 and 1.75 mm/day. In terms of $R^2$, the values were between 0.24 to 0.69 for STEEP, and were below 0.2 for SEBAL for all sites except in SNN (0.55). Similarly, NSE and $\rho_c$ values were higher for STEEP compared to SEBAL. For STEEP, all sites had NSE and $\rho_c$ values above -0.42 and 0.41, respectively, whereas all sites except SNN had values below these limits for SEBAL. Both models overestimated ET ($PBIAS > 0$), with the exception of the STEEP estimates for the PTN site. The highest overestimation by the STEEP model was less than 60%, whereas in SEBAL it was greater than 140%.
SEBAL metrics concerning the modelled ET were similar to those found in other studies. Laipelt et al. (2021) found $R^2$ ranging from 0.18 to 0.87 when applying SEBAL and comparing it with data from ten EC towers located in different Brazilian biomes (Amazon, Cerrado, Pantanal, and Pampa). Cheng et al. (2021) obtained $R^2$ of 0.53–0.77 and RMSE of 0.89–1.02 mm/day when comparing estimates from SEBAL and EC towers on different land covers in China. Costa et al. (2021), when applying SEBAL in the Caatinga, found $R^2$ and NSE values of 0.57 and 0.36, respectively. Santos et al. (2020) modelled ET with SEBAL at the SNN site for the 2014–2016 period and obtained $R^2$ and RMSE values of 0.28 and 1.43 mm/day, respectively. For this site, we obtained $R^2$ and RMSE of 0.55 and 1.08 mm/day, respectively, for the year 2014 using SEBAL.

STEEP exhibited a greater seasonal accuracy compared to SEBAL (Fig. 3), as evidenced by the goodness-of-fit between simulated and observed values expressed by the NSE indicator. STEEP estimates followed the same temporal evolution as the observed values. STEEP satisfactorily captured both minimum and maximum ET values, including after rainfall events, this is particularly evident in Fig. 3a, where the two observed ET peaks in late 2011 — between DOY 300 and 360 — in the PTN site were captured nicely by STEEP. This improved performance can be explained because soil moisture is incorporated in the STEEP algorithm. In semi-arid regions and particularly in the SDTF, besides the availability of energy, evapotranspiration is highly dependent on the soil–water availability (Lima et al., 2012; Carvalho et al., 2018; Mutti et al., 2019; Paloschi et al., 2020). In rainy months, low daily ET rates are often observed due to the reduced levels of incoming radiation caused by high cloud cover (Mutti et al., 2019; Paloschi et al., 2020). Towards the end of the wet period, when the available energy increases, the daily ET values also increase as a result of the high soil water availability from previous precipitation events (Allen et al., 2011; Marques et al., 2020). In the transition period from the rainy to the dry season, the leaves do not fall immediately (see Table 1, main tree species). Instead, leaf-shedding depends on the environmental conditions in each location, including the rainy season duration, and species composition (Lima and Rodal, 2010; Lima et al., 2012; Miranda et al., 2020; Paloschi et al., 2020; Queiroz et al., 2020; Medeiros et al., 2022). The remaining water available in the soil or previously accumulated in plant tissues is sufficient for the Caatinga vegetation to maintain its leaves, for short periods, at levels similar to the rainy season (Barbosa et al., 2006; Mutti et al., 2019). However, in the dry season, when soil moisture reaches its
lowest levels, the Caatinga vegetation enters a state of dormancy that is accompanied by leaf drop and a drastic reduction of photosynthetic activity (and hence of transpiration) as a strategy to cope with the lack of available soil moisture (Dombroski et al., 2011; Paloschi et al., 2020). This resilience mechanism is typical of xerophytic and/or deciduous species such as those found in the Caatinga (Lima et al., 2012; Mutti et al., 2019; Paloschi et al., 2020), and explains the low rates of ET in the dry season. In contrast, in SEBAL, which does not consider water availability, it was observed that the daily ET followed the course of the daily net radiation throughout the year, especially in the dry period of each of the experimental sites. This is in agreement with the results of Kayser et al. (2022), who pointed out that estimates with SEBAL can be seasonally accurate in locations where the main driver of ET is the available energy. Our results highlight that SEB models such as SEBAL, which are formulated to be mainly dependent on energy availability and do not consider soil and plant water availability, may not satisfactorily represent ET in semi-arid vegetation such as that found in the SDTF (Gokmen et al., 2012; Paul et al., 2014; Melo et al., 2021).
Fig. 3. Observed and modelled daily evapotranspiration (ET, mm/day) for the different experimental sites: a) and b) PTN 2011, c) and d) SNN 2014, e) and f) SET 2015, g) and h) CGR 2014, i) and j) CGR 2020. The black lines represent observed ET; the red crosses and points are STEEP and SEBAL estimates, respectively; the blue bars represent CHIRPS daily rainfall; the gray region represents daily net radiation from ERA5-land.

The core of the STEEP and SEBAL algorithms is based on finding $\lambda ET$ as the residual of the energy balance; however, they differ with regards to the approach used to calculate $H$. In the STEEP model, the seasonal variation of $H$ fitted the observed values of the instantaneous measurements at 11:00 am (local time) better than SEBAL, for all the sites (Fig. 4). Our results show that an improvement in $H$ leads to a correspondent in ET estimates. This is contrary to the findings of Faivre et al. (2017), who used the same formulation for $kB^{-1}$ applied in our study, but included four different methods to compute $z0m$. While STEEP estimates of $H$ exhibited $\rho_c$ values over 0.5 for three of the five sites, SEBAL $H$ estimates exhibited $\rho_c$ values below 0.5 for all sites. When wet and dry seasons data are analysed separately (Fig. 5), the same trend is observed in the results: in general, the STEEP model presents better statistical metrics than SEBAL.
Fig. 4. Observed and modelled instantaneous sensible heat flux ($H$, at 11:00 am, W/m²) for the different experimental sites: a), b) and c) PTN 2011, d), e) and f) SNN 2014, g), h) and i) SET
25

2015, j), k) and l) CGR 2014, m), n) and o) CGR 2020. The blue line represents the observed values; the red crosses and grey points correspond to the STEEP and SEBAL estimates, respectively. The black line is the 1:1 line.

Fig. 5. Results of the performance statistics of instantaneous sensible heat flux ($H$, at 11:00 am, W/m²) in wet and dry seasons, for the evaluated sites.

Evaluation of the STEEP and SEBAL daily ET and instantaneous $H$ for all experimental sites (Fig. 6) indicates that both models lack a high performance for $H$ estimates, although the use of STEEP resulted in better statistical measures than when SEBAL was employed (Fig. 6b). This substantiates previous findings (Gokmen et al., 2012; Paul et al., 2014; Trebs et al., 2021), that have shown the tendency of underestimation (overestimation) of $H$ (ET) at water-limited sites. It can be seen that the overestimation of $H$ by the STEEP model, compared to SEBAL, produced modelled ET values that were closer to the EC measurements (see Fig. 3 and 4). We ascribe the poor performance of $H$ in the models relative to observed data to the continuous $H$ oscillations throughout the day (Campos et al., 2019; Lima et al., 2021). As we compare an instantaneous $H$ estimate (STEEP or SEBAL) to the 30-min $H$ average measurement (EC), it is expected that modelled $H$ performs worse than daily ET for the same site and period. Furthermore, for sites with fewer observations of $H$ (SET 2015 and CGR 2020), especially in the dry season, the metrics showed that STEEP did not perform as well, for each season, as other sites with more data available. Still, these limited data were sufficient to show that STEEP outperformed SEBAL in estimating $H$. 
Fig. 6. Evaluation of observed and modelled: (a) daily evapotranspiration (ET, mm/day) and b) instantaneous sensible heat flux ($H$, at 11:00 am, W/m$^2$) for all experimental sites. STEEP (red crosses) and SEBAL (black points). The black line is the 1:1 line; the cyan (black) dashed line is the fitted linear regression between observed and STEEP (SEBAL) model values.

We attribute the better performance of STEEP over SEBAL for the Brazilian Caatinga to at least three reasons, shown in order of impact of model implementation on its performance (Fig. 7 and Table S1). First, by quantifying the remaining $\lambda ET$ in the endmembers pixels through the Priestley-Taylor equation, a more reliable estimate of $H$ in the endmembers pixels can be obtained, as was also evidenced by Singh and Irmak (2011). This process is critical for the subsequent numerical calculation of $H$ in SEB models that use $dT$, as its accuracy is closely related to quantifying the energy balance at the hot and cold endmembers (Trezza, 2006; Allen et al., 2007; Singh and Irmak, 2011; Singh et al., 2012). Secondly, roughness characteristics near the surface where the heat fluxes originate are parameterised by $z_0m$, which depends on several factors, such as wind direction, height and type of the vegetation cover (Kustas et al., 1989b). Estimation of $z_0m$ only with an exponential relationship, as a function of vegetation indices, may be an oversimplification (Kustas et al., 1989a; Paul et al., 2013). In our study, $z_0m$ and $d0$ are calculated with the equations and coefficients proposed in Raupach (1994) and Verhoef et al. (1997b), and using PAI because this
index better represents the intra-annual phenological changes in the Caatinga (Miranda et al., 2020). This procedure considers the characteristics of SDTF, such as seasonality of phenology and vegetation height, that considerably affect the quantification of turbulent transfer (Liu et al., 2021).

Third, our study uses the equation described in Verhoef et al. (1997a) and Paul et al. (2013) to estimate $r_{ah}$, which considers the differences between heat and momentum transfer, unlike the original equation employed in other SEB models e.g. SEBAL or METRIC that only considers $z_{0m}$ and sets $z_{0h} = 0.1$ when computing this resistance. Furthermore, we account for the $k_{B^{-1}}$ parameter that varies in space and time and incorporates the soil moisture content obtained by RS (Su et al., 2001; Gokmen et al., 2012). ET estimation is best represented with a spatially varying $k_{B^{-1}}$ values, as pointed out by the studies of Gokmen et al. (2012) and Paul et al. (2014). Long et al. (2011) report that the introduction of these fixed values ($z_{0h}$ or $k_{B^{-1}}$) has a significant impact on the magnitudes of the estimates of $H$. Furthermore, Mallick et al. (2018) and Trebs et al. (2021) indicate that the parameterization of $r_{ah}$ can influence the estimation of ET, especially in SEB models that are largely dependent on $r_{ah}$. Our results show that including just one or two of the refinements had only partial performance gains (Fig. 7 and Table S1). In contrast, all the proposed STEEP improvements when implemented together resulted in the best performance metrics for all sites.

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**Fig. 7.** Change of the concordance correlation coefficient ($\rho_c$) by the exclusion/modification of one or two parameters/variables implemented in the STEEP model, in the wet and dry seasons: scale factor soil moisture correction (SF), the parameter $k_{B^{-1}}$, the aerodynamic resistance for heat transfer ($r_{ah}$), PAI replace with LAI (determined by two different methods), the roughness length for momentum transport ($z_{0m}$) and the residual latent heat flux in the end members pixels ($r_{\lambda ET}$).

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3.2 Comparison of STEEP model estimates with global evapotranspiration products

The comparison of ET estimates by STEEP, MOD16 and PMLv2 with the observed values at the different sites (Fig. 8) reveals that the ET estimates by STEEP and global products adequately followed the seasonality of the values, with a better fit for STEEP and MOD16. In general, the evaluation at the different sites shows that the $RMSE$ of STEEP was not higher than 6.45 mm/8 days, while the ET products' maximum $RMSE$ was close to 15 mm/8 days. It is noted that the lowest $RMSE$ value found (4.11 mm/8 days) was for MOD16 at the SET site. Regarding $R^2$ values, 80% of the evaluations with STEEP were equal to or greater than 0.50. For MOD16, 60% of the $R^2$ values were equal to or greater than 0.70, while for PMLv2, no site had $R^2$ values that exceeded 0.55. The best $NSE$ value produced by STEEP was 0.77, while with MOD16, it was 0.70, both at the SNN site, while PMLv2 did not exceed 0.39 (PTN site). Regarding $\rho_c$, the percentages of ET evaluations that obtained values equal to or greater than 0.70 were 60% for STEEP and MOD16, and only 20% for PMLv2 (site PTN). The overestimations ($PBIAS$) with STEEP were not higher than 50%, and not higher than 95% with MOD16. For PMLv2 the overestimations did not exceed 80%, except for the SET site that obtained a $PBIAS$ approx. 160%. We highlight the good performance of MOD16 for the SET, SNN, and especially the PTN sites, with very good performance metrics and seasonal behaviour, capturing ET values in dry periods very well. The evaluation results of STEEP, MOD16 and PMLv2 for all observation sites combined are shown in Fig. 9. Noteworthy is the better performance of STEEP over MOD16 and PMLv2, with $RMSE$ of $< 6$ mm/8 days, $R^2$ and $NSE$ greater than or close to 0.60, $\rho_c$ of $> 0.75$ and an average overestimation $< 12%$. Analysis with the dataset considering only the 8-day time periods without missing field-observed data, i.e. periods with valid ET measurements during eight consecutive days (Fig. S3) did not change the results overall, confirming STEEP’s dominance compared to the two standard products evaluated.
Fig. 8. Temporal evolution of ET from STEEP, MOD16 and PMLv2 for the different observation sites, and their individual performance statistics. a), b) and c) PTN 2011; d), e) and f) SNN 2014; g) h) and i) SET 2015; j), k) and l) CGR 2014; m), n) and o) CGR 2020. Black lines correspond to observed ET while data points refer to estimates by the STEEP model (red crosses), MOD16 (blue diamonds) and PMLv2 (green squares) products.

Fig. 9. Evaluation of evapotranspiration (ET, mm/8 days) observed and modelled with STEEP (red crosses), MOD16 (blue diamonds) and PMLv2 (green squares) for all experimental sites. The black line is the 1:1 line; dashed lines are the fitted linear regressions of observed versus modelled values by the STEEP model (red), MOD16 (blue) and PMLv2 (green) products. \( N = 138 \) is the total number of eight-day periods with at least one day of EC data measured in at least one of the five experimental sites of Caatinga where all the ET models (STEEP, MOD16 and PMLv2) outputs were available.
The explanation of the differences between STEEP and the MOD16 and PMLv2 products is two-fold. Firstly, the way ET is obtained differs between STEEP and the other products. While STEEP and other SEB single-source models estimate ET as a combined single process, i.e. soil evaporation and transpiration estimates are provided as a lumped sum (Sahnoun et al., 2021), and interception loss is not taken into account, MOD16 and PMLv2 discriminate the ET components, i.e. soil evaporation, transpiration, and wet canopy evaporation (Mu et al., 2011; Zhang et al., 2019). With this in mind it is remarkable that STEEP performs better than the other, widely used, multiple-source ET products. Secondly, the input data sets and their uses are different. The driving meteorological data for STEEP are from ERA5-Land, while in MOD16, they are from MERRA and in PMLv2 are provided by GLDAS (Mu et al., 2011; Zhang et al., 2019). In addition, the meteorological elements used are different among the ET products. MOD16 requires air temperature, atmospheric pressure, relative humidity, and downward shortwave radiation. In addition to these elements, PMLv2 also requires precipitation, downward longwave radiation, and wind speed (Mu et al., 2011; Zhang et al., 2019; Yin et al., 2020; Chen et al., 2022). Although both ET products use the same land cover data (MOD12Q1), only MOD16 integrates it into its algorithm. In MOD16, the land cover type defines biome delimitation for the characterization of leaf stomatal conductance, vapour pressure deficit (VPD) and other related factors, while PMLv2 only uses land cover to construct a mask of the land area (Chen et al., 2022). The sources and use of LAI in these two products are also different. LAI is used to increase leaf conductance in MOD16, while it is used to divide the total available energy into canopy uptake and soil uptake in PMLv2 (Mu et al., 2011; Zhang et al., 2019; Chen et al., 2022). Although MOD16 uses EC data from 46 distributed sites for validation (Mu et al., 2011) and PMLv2 uses EC data from 95 distributed sites and ten plant functional types for calibration (Zhang et al., 2019; Yin et al., 2020), none of the products had observation sites in SDTF.

The uncertainties associated with field measurements of ET can also influence the evaluation of the model products. It is generally accepted that EC flux towers provide reliable local, i.e. for areas of relatively limited spatial extensions, ca. 10 km², ET measurements (Mu et al., 2011; Chu et al., 2021; Salazar-Martínez et al., 2022). However, generally flux tower data have a lack of energy balance closure, that is the difference between net radiation and ground heat flux is sometimes greater than the sum of the turbulent latent and sensible heat fluxes, an error that can be in the of
10–30% range (Wilson et al., 2002; Foken, 2008; Allen et al., 2011). This gap can result from instrument errors, weather and surface conditions, e.g. those that result in advection, and gap-filling methods (Mu et al., 2011). In addition, the complex and heterogeneous canopy structure, the stochastic nature of turbulence (Hollinger and Richardson, 2005) and adverse weather conditions, e.g. rainy and stormy days, tower sensors recording abnormal values, can affect ET measurements obtained by EC systems (Ramoelo et al., 2014).

3.3 Sources of error and further research for STEEP

In its current configuration, STEEP has some limitations that should be noted. Meteorological reanalysis provides only large-scale averages and can misrepresent local meteorological conditions; hence, it suffers from biases, especially over heterogeneous surfaces (Rasp et al., 2018). However, despite moderate accuracy and biases at regional scales, ground-based assimilation and reanalysis data have become important sources of meteorological inputs for ET estimates (Mu et al., 2011; Zhang et al., 2019; Allam et al., 2021; Senay et al., 2022). Laipelt et al. (2020) and Kayser et al. (2022) showed that global reanalysis data when used as meteorological inputs had modest effects only on the accuracy of SEBAL for estimating ET. In our study, ERA5-Land exhibited relatively high and satisfactory agreement with micrometeorological data measured at each site (Fig. S4). Also, although gap-filling was used in the present study to improve the availability of LST data, this procedure should be used with caution. In addition, care should be taken when using the MCD43A4 reflectance product, because in its composition there is also gap-filling. For example, on some cloudy days, the estimates of vegetation indices, surface albedo, and LST may have introduced inaccuracies in the STEEP (and in SEBAL) model calculation process due to these gap-filling methods. Regarding the selection of endmembers pixels, although the temporal evolution of the selected pixels in this study seems plausible, their representativeness of the actual conditions may be debatable, especially considering the considerable extent of the AOI. The computational capacity and the effectiveness of GEE for running SEB models should be commended. Although other studies have demonstrated GEE's strength (Laipelt et al., 2021; Jaafar et al., 2022; Senay et al., 2022), this platform has some limitations when it comes to the number of iterations, e.g. a convergence threshold cannot be set to stop the within-loop iterations of \(H\) calculations; instead a fixed number of
iterations needs to be defined. Still, the availability of the several necessary datasets within one platform greatly facilitates the run of STEEP and other SEB models.

One of the main focuses of this study is to provide a one-source model capable of representing ET in environments that are mainly governed by soil–water availability, such as those represented by SDTF, in a parsimonious way. Based on our findings we deem this main aim to be achieved due to the relative simplicity of the STEEP model and its low data demand. The improved performance of STEEP was the result of improvement of existing and physically meaningful parameters ($z_{0m}$ and $k_B^{-1}$), rather than by introducing additional empirical parameters, thereby satisfying the principle of equifinality (see Beven and Freer, 2001). To explore further the potential and accuracy of STEEP, more research is needed to analyse the impact that the improved $H$ approach has on ET of different land covers at longer time scales. Despite the promising overall results, additional efforts are required on modelling $H$ in SDTF regions. Although we have shown that STEEP outperforms other models in simulating either $H$ or ET, we acknowledge that there is still room for model improvement. Given that the STEEP model was formulated to be a calibration-free model, it may be possible to improve $H$ estimates by, for example, optimising coefficients associated to soil moisture (see Eq A.12) and applying dynamic values to $\alpha_p$ (see Eq A.25) varying seasonally. Another potential improvement for instantaneous $H$ estimates can be achieved by accounting for biomass heat storage (BHS; Swenson et al., 2019) in STEEP. Meier et al. (2019) have shown that considering BHS can enable land surface models to capture the diurnal asymmetry of the temperature impact on energy fluxes and, consequently, provide improved sub-hourly $H$. Improving the quantification of regional ET via RS-based SEB models has a great potential to provide a more accurate estimate of the energy and water fluxes in SDTF regions, and will contribute to a better understanding of the water cycle, its uses, and the interrelationships with ecosystem functioning.

4. Conclusions

Our work developed a calibration-free model (STEEP) with an improved approach for estimating the latent and sensible heat fluxes by remote sensing for SDTF. In summary, the main conclusions are:

- The estimates of $H$ by STEEP allowed ET estimates to be closer to the observed field values than those obtained by SEBAL. Based on all the performance metrics used to
analyse the models, STEEP was superior to SEBAL. STEEP showed $RMSE$ less than 1mm/day, $R^2$ between 0.24 and 0.69, $NSE$ between -0.17 and 0.65, $\rho_c$ between 0.41 and 0.80 and $PBIAS$ between -17% to 54%. Also noteworthy is how well STEEP captured the seasonal course of observed ET.

- Compared with ET data from the global MOD16 and PMLv2 products, the STEEP model simulated a similar but generally superior seasonal evolution and its performance metrics were also better. Considering all observation sites simultaneously, at the eight-day scale, STEEP showed superior performance with $RMSE$ less than 6 mm/8 days, $R^2$ and $NSE$ equal to or greater than 0.60, $\rho_c$ greater than 0.75, and an overestimation of $< 12\%$.

Thus, we conclude that STEEP, a one-source model that incorporated the seasonality of the aerodynamic and surface variables, was well-heeled in representing ET in environments that are mainly governed by soil–water availability. All the same, there is a need to evaluate the newly developed STEEP model performance for different land covers, climate, and for longer time series than those considered during the modelling process in this study.

Acknowledgements

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Data Availability Statement

ET data for the PTN, SNN, and SET sites were published by Melo et al. (2021), and are available at https://doi.org/10.5281/zenodo.5549321. ET data for the CGR site; H data for the PTN, SNN, CGR sites, and the code used for the formulation of the STEEP model presented in this study can be accessed at https://doi.org/10.5281/zenodo.7109043 and https://github.com/ulissesaalencar/ET_SDTF, respectively. H data for the SET site is publicly available for download at https://ameriflux.lbl.gov/.

Supplementary material

Table S1. Performance statistics by the exclusion/modification of one or two parameters/variables implemented in the STEEP model, in the wet and dry seasons: scale factor soil moisture correction (SF), the parameter kB⁻¹, the aerodynamic resistance for heat transfer (rah), PAI replace with LAI (determined by two different methods), the roughness length for momentum transport (z0m), the residual latent heat flux in the end members pixels (rλET), and of the SEBAL model.
### Performance statistics

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*PTN (N = 239; 2011)*

*SNN (N = 267; 2014)*

*SET (N = 283; 2015)*
<p>| (-) SF | 1.04 | 0.61 | 0.11 | 0.02 | -0.25 | -0.99 | 0.28 | 0.14 | 36.58 | 38.26 |
| (-) kB-1 | 1.13 | 0.58 | 0.06 | 0.07 | -0.49 | -0.86 | 0.21 | 0.23 | 36.71 | 40.83 |
| (-) rah | 1.06 | 0.56 | 0.04 | 0 | -0.43 | -1.03 | 0.18 | 0.03 | 21.82 | 39.71 |
| LAI* | 1.3 | 0.68 | 0.03 | 0.09 | -0.98 | -1.51 | 0.12 | 0.2 | -62.3 | -75.32 |
| LAI** | 1.15 | 0.6 | 0.04 | 0.05 | -0.53 | -0.97 | 0.19 | 0.21 | -6.83 | -29.78 |
| (-) z0m | 1.09 | 0.75 | 0.1 | 0 | -0.36 | -2.74 | 0.26 | -0.02 | 42.62 | 80.96 |
| (-) rλET | 2.11 | 1.37 | 0.15 | 0.04 | -4.18 | -9.27 | 0.15 | 0.06 | 151.66 | 190.07 |
| (-) z0m &amp; rah | 1.06 | 0.58 | 0.05 | 0 | -0.3 | -1.24 | 0.21 | 0.02 | 21.6 | 51.96 |
| (-) rah &amp; rλET | 1.99 | 1.37 | 0.11 | 0.01 | -3.99 | -9.27 | 0.13 | 0.04 | 143.27 | 183.22 |
| (-) z0m &amp; rλET | 1.66 | 1.16 | 0.07 | 0.01 | -2.47 | -6.31 | 0.14 | 0.04 | 104.32 | 134.34 |
| SEBAL | 1.83 | 1.28 | 0.1 | 0 | -3.21 | -7.93 | 0.14 | 0.03 | 128 | 161.89 |
| STEEP | 0.8 | 0.72 | 0.35 | 0.51 | -0.35 | -0.8 | 0.55 | 0.58 | 5.85 | 25.16 |
| (-) SF | 0.7 | 0.67 | 0.36 | 0.52 | -0.02 | -0.53 | 0.59 | 0.6 | 6.57 | 30.14 |
| (-) kB-1 | 0.78 | 0.8 | 0.25 | 0.44 | -0.28 | -1.18 | 0.47 | 0.51 | 15.04 | 38.9 |
| (-) rah | 0.71 | 0.78 | 0.28 | 0.46 | -0.06 | -1.07 | 0.51 | 0.48 | -8.54 | 54.63 |
| LAI* | 0.76 | 0.83 | 0.49 | 0.61 | -0.23 | -1.35 | 0.64 | 0.51 | -7.64 | -62.39 |
| LAI** | 0.75 | 0.68 | 0.46 | 0.58 | -0.18 | -0.57 | 0.63 | 0.63 | -9.25 | -26.31 |
| (-) z0m | 0.71 | 0.83 | 0.28 | 0.35 | -0.05 | -1.35 | 0.51 | 0.38 | -11.12 | 62.72 |
| (-) rλET | 1.15 | 2.32 | 0.09 | 0.07 | -1.77 | -17.48 | 0.19 | 0.04 | 46.68 | 217.84 |
| (-) z0m &amp; rah | 0.69 | 0.84 | 0.24 | 0.44 | -0.01 | -1.43 | 0.48 | 0.39 | 3.9 | 68.9 |
| (-) rah &amp; rλET | 1.14 | 2.44 | 0.05 | 0.03 | -1.72 | -19.4 | 0.15 | 0.02 | 43.77 | 229.58 |
| (-) z0m &amp; rλET | 0.85 | 1.97 | 0.11 | 0.04 | -0.51 | -12.27 | 0.33 | 0.04 | 9.18 | 175.39 |
| SEBAL | 0.97 | 2.24 | 0.07 | 0.03 | -0.97 | -14.7 | 0.21 | 0.03 | 28.63 | 208.13 |
| STEEP | 0.61 | 1.06 | 0.39 | 0.02 | 0.29 | -2.98 | 0.62 | 0.09 | -1.19 | 101.37 |
| (-) SF | 0.82 | 1.03 | 0.3 | 0 | -0.29 | -2.76 | 0.52 | 0.02 | -6.52 | 106.36 |
| (-) kB-1 | 0.83 | 1.26 | 0.29 | 0 | -0.3 | -4.63 | 0.51 | -0.03 | -5.31 | 135.98 |
| (-) rah | 1.11 | 1.13 | 0.25 | 0 | -1.2 | -3.55 | 0.42 | -0.02 | -15.37 | 133.29 |
| LAI* | 0.85 | 1.02 | 0.29 | 0.01 | -0.38 | -0.99 | -3.06 | 0.4 | -4.71 | 31.63 |
| LAI** | 0.67 | 0.76 | 0.36 | 0.07 | 0.14 | -1.03 | 0.59 | 0.26 | -3.58 | 2.87 |</p>
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$z0m = \text{roughness length for momentum transfer}$; $rah = \text{aerodynamic resistance for heat transfer}$; $r\lambda ET = \text{remaining } \lambda ET \text{ in the endmembers pixels}$.
Fig. S1. Location of the flux towers sites and MOD16 and PMLv2 pixel boundaries. True colour composite (bands 4, 3, and 2) of Harmonized Sentinel-2 MSI acquired via Google Earth Engine. Scene acquired of PTN (12/06/2021); SNN and SET (25/05/2021); CGR (29/07/2021).
Fig. S2. PAI and soil moisture time series for the different observation sites.
Fig. S3. Evaluation of evapotranspiration (ET, mm/8 days) observed and modelled with STEEP (red crosses), MOD16 (blue diamonds) and PMLv2 (green squares) for all experimental sites considering only the 55 periods where the field-observed data had eight consecutive days. The black line is the 1:1 line; dashed lines are the fitted linear regressions of observed or modelled values by the STEEP model (red), MOD16 (blue) and PMLv2 (green) products.
Fig. S4. Comparison between ERA5-Land reanalysis dataset and local observational meteorological measurements from the flux tower at the closest time from the satellite overpass. Micrometeorological sensors installed at the flux towers are up to 16 m in distance from the land surface, and ERA5-Land variables have different reference elevation (e.g. 2 m for air temperature and 10 m to wind speed).
Appendix A – Equations adopted to formulate the STEEP model

Latent heat flux ($\lambda ET$) was modeled using Eq. (A.1):

$$\lambda ET = R_n - G - H$$  \hspace{1cm} (A.1)

where $R_n$ is net radiation, $G$ is soil heat flux, and $H$ is sensible heat flux. All variables are expressed in energy units (e.g., W/m$^2$).

Net radiation ($R_n$) was modeled based on the radiation budget indicated by Allen et al. (2007) and Ferreira et al. (2020) by Eq. (A.2):

$$R_n = R_{S\downarrow} \times (1 - \alpha) + \varepsilon_S \times R_{L\downarrow} - R_{L\uparrow}$$  \hspace{1cm} (A.2)

where $R_{S\downarrow}$ is incident shortwave radiation (W/m$^2$) estimated following Allen et al. (2007), $\alpha$ is surface albedo (dimensionless), estimated following Trezza et al. (2013), $R_{L\downarrow}$ is longwave radiation from the atmosphere (W/m$^2$) estimated following Ferreira et al. (2020) with atmospheric emissivity from Duarte et al. (2006); $R_{L\uparrow}$ is emitted longwave radiation (W/m$^2$) following Ferreira et al. (2020) with $\varepsilon_S$ the surface emissivity (dimensionless), estimated following Long et al. (2010).

Soil heat flux ($G$), expressed as a ratio of net radiation, was estimated following the model by Bastiaanssen et al. (1998):

$$\frac{G}{R_n} = [(LST - 273.15) \times (0.0038 + 0.0074 \times \alpha) \times (1 - 0.98 \times NDVI^4)]$$  \hspace{1cm} (A.3)

where $LST$ is the surface temperature (K) and NDVI is the Normalized Difference Vegetation Index (dimensionless), estimated following Rouse et al. (1973).

Sensible heat flux ($H$) was modeled using:

$$H = \frac{\rho \times c_p \times dT}{rah}$$  \hspace{1cm} (A.4)

where $\rho$ is the air density (kg/m$^3$), $c_p$ refers to the specific heat of air at constant pressure (J/kg/K), $dT$ is the temperature gradient (K), and $rah$ is the aerodynamic resistance for heat transfer (s/m).

Aerodynamic resistance to heat transport was estimated based on the classical equation given in Paul et al. (2013), see also Verhoef et al. (1997a):
\[ rah = \frac{1}{k \times u^*} \times \left[ \ln \left( \frac{z_{ref} - d0}{z0m} \right) - \psi_h \right] + \frac{1}{k \times u^*} \times kB_{umd}^{-1} \quad (A.5) \]

where \( k \) is the von Kármán constant taken as 0.41, \( u^* \) is the friction velocity (m/s), \( z_{ref} \) is the reference height (m), \( d0 \) is zero plane displacement height (m), \( z0m \) is roughness length for momentum transfer (m), \( \psi_h \) is the atmospheric stability correction function for heat transfer (m), as calculated following Paulson (1970), \( kB_{umd}^{-1} \) is the dimensionless parameter formulated to express the excess resistance of heat transfer compared to momentum transfer, corrected for soil moisture derived from remote sensing.

The friction velocity was computed according to Verhoef et al. (1997b) and Paul et al. (2013):

\[ u^* = k \times u \left[ \ln \left( \frac{z_{ref} - d0}{z0m} \right) - \psi_m \right]^{-1} \quad (A.6) \]

where \( u \) is the wind speed (m/s) at a known height \( z_{ref} \), \( \psi_m \) is the atmospheric stability correction function for momentum transfer (m), as calculated following Paulson (1970).

Roughness length for momentum transport was estimated, based on the studies by Verhoef et al. (1997b):

\[ z0m = (HGHT - d0) \times \exp(-k \times \gamma + PSICORR) \quad (A.7) \]

where \( HGHT \) is the height of the vegetation (m), \( PSICORR \) is taken as 0.2 and \( \gamma \) is the inverse of the square root of the bulk surface drag coefficient at the roughness canopy height (Raupach, 1992).

Zero plane displacement height \( (d0) \) was obtained following Raupach (1994) from:

\[ d0 = HGHT \times \left[ \left( 1 - \frac{1}{\sqrt{CD1 \times PAI}} \right) + \left( \exp(-\sqrt{CD1 \times PAI}) \right) \right] \quad (A.8) \]

where \( CD1 \) is taken as 20.6 and \( PAI \) is the Plant Area Index.

\( \gamma \) was following Verhoef et al. (1997b):

\[ \gamma = \left( CD + CR \times \frac{PAI}{2} \right)^{-0.5} \quad (A.9) \]

if \( \gamma < 3.33 \), \( \gamma \) is set to 3.33. Following Verhoef et al. (1997), \( CD \) and \( CR \) are taken as 0.01 and 0.35, respectively.

Plant Area Index was calculated according to Miranda et al. (2020) as:

\[ PAI = 10.1 \times (\rho_{NIR} - \sqrt{\rho_{RED}}) + 3.1 \quad (A.10) \]
where \( \rho_{NIR} \) is the near infrared band reflectance, and \( \rho_{RED} \) is the red band reflectance. If \( PAI < 0 \), \( d0 \) is set to 0.

The dimensionless parameter \( kB^{-1}_{umd} \) is corrected by soil moisture by remote sensing following the equations provided by Gokmen et al. (2012):

\[
kB^{-1}_{umd} = SF \times kB^{-1}
\]

where \( SF \) is a scaling factor, represented by a sigmoid function:

\[
SF = \left[ c + \frac{1}{1 + exp(d - e \times SM_{rel})} \right]
\]

Here, \( c, d, e \) are the sigmoid function coefficients, for which we adopted values of 0.3, 2.5, and 4, respectively, following Gokmen et al. (2012). \( SM_{rel} \) is the relative soil moisture, obtained from:

\[
SM_{rel} = \frac{SM - SM_{min}}{SM_{max} - SM_{min}}
\]

where \( SM \) is the actual soil moisture content, in our case obtained with the GLDAS reanalysis product, and \( SM_{min} \) and \( SM_{max} \) are the minimum and maximum soil moisture. The \( SM_{min} \) and \( SM_{max} \) values were obtained using the annual time series analysis of the soil moisture data.

\( kB^{-1} \) was calculated according to Su et al. (2001):

\[
kB^{-1} = \frac{k \times Cd}{4 \times Ct \times \frac{u^*}{u(h)} \times \left( 1 - exp(-\frac{z0m}{h}) \right)} \times f_c^2 + \frac{k \times \frac{u^*}{u(h)} \times \frac{z0m}{h}}{C_t^*} \times f_s^2 \times f_s^2 + kB_s^{-1} \times f_s^2
\]

where \( kB_s^{-1} = 2.46(Re)^{0.25} - 2 \), \( Cd \) is the drag coefficient of the foliage elements taken as 0.2, \( Ct \) is the heat transfer coefficient of the leaf with value 0.01.

The ratio \( \frac{u^*}{u(h)} \) is parameterized as:

\[
\frac{u^*}{u(h)} = c1 - c2 \times exp(-c3 \times Cd \times PAI)
\]

where \( c1 = 0.320, c2 = 0.264, c3 = 15.1 \).

\( nec \) is the extinction coefficient of the wind speed profile within the canopy given by:
\[ \text{neq} = \frac{Cd \times PAI}{2 u^*^2} u(h)^2 \] (A.16)

\[ C^*_t \] is heat transfer coefficient of the soil given by:

\[ C^*_t = Pr^{-2/3} \times (Re)^{-1/2} \] (A.17)

where \( Pr \) is the Prandtl number with a value 0.71, and \( Re \) is the Reynolds number calculated as:

\[ Re = \frac{u^* \times 0.009}{v}, \quad v = 1.461 \times 10^{-5} \] (A.18)

where \( v \) is the kinematic viscosity \((m^2/s)\).

In Eq. A.14 \( f_c \) is the fractional canopy cover calculated according to Eq. (A19), and \( f_s \) is its complement.

\[ f_c = 1 - \left[ \frac{NDVI - NDVI_{\text{max}}}{NDVI_{\text{min}} - NDVI_{\text{max}}} \right]^{0.4631} \] (A.19)

where \( NDVI_{\text{max}} \) and \( NDVI_{\text{min}} \) are maximum and minimum NDVI values, respectively. \( NDVI_{\text{max}} \) and \( NDVI_{\text{min}} \) values were obtained using the annual time series analysis of the NDVI.

d\( T \) in Eq. (A4) was estimated daily with a linear relationship on the surface temperature \( \text{LST} \) (Bastiaanssen et al., 1998) as:

\[ dT = a + b \times \text{LST} \] (A.20)

To find the coefficients \( a \) and \( b \) in Eq. (A20) requires that hot and cold endmembers pixels are established. The coefficients were found as:

\[ b = \frac{(dT_{\text{hot}} - dT_{\text{cold}})}{(\text{LST}_{\text{hot}} - \text{LST}_{\text{cold}})} \] (A.21)

\[ a = dT_{\text{cold}} - b \times \text{LST}_{\text{cold}} \] (A.22)

\[ dT_{\text{hot/cold}} = \frac{H_{\text{hot/cold}} \times r a h_{\text{hot/cold}}}{\rho \times c_p} \] (A.23)

\[ H_{\text{hot/cold}} = R n_{\text{hot/cold}} - G_{\text{hot/cold}} - \lambda \dot{E} T_{\text{hot/cold}} \] (A.24)
where $dT_{hot/cold}$ are $dT$ values for the hot/dry and cold/wet endmember pixels, respectively, $Rn_{hot/cold}$, $G_{hot/cold}$, $LST_{hot/cold}$, $rah_{hot/cold}$ are the median values extracted on the endmember pixels of each variable. The selection of endmember pixels is detailed in section 2.3.

$\lambda ET_{hot/cold}$ is the term incorporated in the computation of $H$ in the endmember pixels given by the Priestley-Taylor (1972) equation, according to Singh and Irmak (2011) and French et al. (2015):

$$\lambda ET_{hot/cold} = (Rn_{hot/cold} - G_{hot/cold}) \times f_c \times ap t \times \left[ \frac{\Delta}{\Delta + \gamma_c} \right]$$ (A.25)

where $apt$ is the empirical Priestley-Taylor coefficient, nominally set to 1.26, but here adjusted according to local conditions, i.e. we adopted the $apt$ values (0.55 for hot/dry and 1.75 for cold/wet pixels) based on Ai and Yang (2016). $\Delta$ is the slope of the saturation vapor pressure-air temperature curve (kPa/°C) and $\gamma_c$ is the psychrometric constant (kPa/°C).

The actual daily evapotranspiration (mm/day) was obtained by means of the following relationship:

$$ET_{24h} = \frac{86400}{(2.501 - 0.00236 \times T_a) \times 10^6} \times \frac{\lambda ET}{Rn - G} \times Rn_{24h}$$ (A.26)

where $T_a$ is the mean daily air temperature (°C), $\lambda ET$ is derived from Eq. A1, and $Rn_{24h}$ corresponds to the daily net radiation (W/m²); in this study both driving variables were obtained with data from the ERA5-Land product.

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