

1 Processing Seismic Ambient Noise Data with the Continuous Wavelet Transform to Obtain
2 Reliable Empirical Green's Functions

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SUMMARY

We propose a new data processing flow to compute empirical Green’s functions (EGF) from ambient seismic noise based on a soft thresholding designating and denoising method using the continuous wavelet transform. The designating algorithm is carried out during the initial data processing to remove earthquakes and other transient signals in the seismic record. A continuous wavelet transform denoising algorithm removes the noise in the final stacked cross-correlogram. The overall data processing procedure is divided into four stages: (1) single station data preparation, (2) remove earthquakes and other signals in the seismic record, (3) spectrum whitening, cross-correlation and temporal stacking, (4) remove the noise in the stacked cross-correlogram to deliver the final EGF. The whole process is automated to make it accessible for large datasets. Synthetic data constructed with a recorded earthquake and recorded ambient noise is used to test the designating method. We then apply the new processing flow to data recorded by the USArray Transportable Array stations near the New Madrid Seismic Zone where many seismic events and transient signals are observed in the data. We compare the EGFs calculated from our new flow with time domain normalization and our results show improved signal-to-noise ratios and deliver more reliable measurements that can be used for further processing. The designating method improves the homogeneity of the ambient noise wavefield which is an intrinsic requirement for seismic interferometry. The final denoising step suppresses random noise and provides clearer EGFs for the next processing step.

Keywords: Seismic interferometry, seismic noise, wavelet transform

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INTRODUCTION

Cross-correlation of diffuse wave fields, such as from ambient noise or scattered coda waves, can be used to estimate the medium Green’s function termed the empirical Green’s function (EGF) between a pair of stations (e.g. Shapiro et al. 2005; Sabra et al. 2005; Wapenaar & Fokkema 2006). This method has been widely applied to data collected in different regions over the past 15 years to extract surface waves and body waves. Densely deployed networks have provided an opportunity for high-resolution surface wave tomography (e.g. Yao et al. 2006; Lin et al. 2008; Bensen et al. 2008) and full waveform inversion (e.g. Gao & Shen 2014; Emry et al. 2018). In spite of these applications, there have been fewer efforts to develop improved ambient noise data processing procedures in order to acquire more reliable and higher signal-to-noise ratio (SNR) EGFs. Bensen et al. (2007) summarized and compared different procedures on the use of seismic records to obtain surface wave dispersion measurements and their suggestions are still the main procedures that are generally used today to process ambient noise data.

Ground motion produced by earthquakes and other sources, such as non-stationary noise sources near a station or weather storm signals, will be recorded on the seismogram and are often considered as “useful signals” that contain important information about the seismic source and underground structure. However, in ambient noise tomography, these signals destroy the diffuse wave field assumption and need to be considered as “noise” in correlation processing. One of the most important steps during the processing is to remove these signals to obtain as “pure” ambient noise as possible. In Bensen et al. (2007), this step is called “time-domain normalization” or “temporal normalization”, which is a procedure for reducing the effect of earthquakes, instrumental irregularities and non-stationary noise sources near to stations on the cross-correlations. This process balances the amplitude of ambient noise relative to the amplitude of

70 unwanted signals. Here, “signal” and “noise” are related to what is being studied and depend on
71 whether removing “signal” or “noise” is useful for our purpose. Earthquakes and other source
72 “signals” should be removed before cross-correlation because large amplitude signals at zero-
73 delay time in the cross-correlation disguise the surface wave arrival from the microseisms. To
74 avoid confusion, based on the common way of naming “ambient noise”, we call the removing of
75 earthquakes and other non-stationary noise source “signals” as *designaling* in this paper although
76 the mathematics of doing so is the same as *denoising*.

77 Bensen et al. (2007) summarized different methods for identifying and removing
78 earthquakes and other contaminants from the original recordings. These include 1-bit
79 normalization, running absolute mean normalization and water level normalization that all
80 suppress the contaminating signals. However, amplitude information is not fully retained in the
81 cross-correlation because of the inherent amplitude down-weighting process in these methods.
82 Amplitude is of fundamental importance for body wave anelastic attenuation estimation and
83 basement resonance estimation based on the horizontal to vertical amplitude ratio (H/V ratio) of
84 surface waves. Bensen et al. (2007) also suggested using running absolute mean normalization as
85 the best practice to process the ambient noise data. In the rest of this paper, we will call this
86 method as “time domain normalization” and it will be used as the benchmark method for
87 comparison.

88 Removing transient signals while not touching the ambient noise itself is a crucial
89 requirement for successful ambient noise data processing. We propose a method based on the
90 Continuous Wavelet Transform (CWT) for dealing with this problem. The CWT has been widely
91 used to for seismic analysis and denoising purposes (Pazos et al. 2003; Chik et al. 2009; To et al.
92 2009; Ansari et al. 2010; Beenamol et al. 2012; Mousavi & Langston 2016; Mousavi et al. 2016).

93 Compared with other denoising methods, using the CWT to achieve denoising has many natural
94 translation-invariant and time-frequency properties such as reducing pseudo-Gibbs artifacts in
95 the denoised signal (Elad & Aharon, 2006). In ambient noise data, the noise record usually
96 dominates the time series with earthquakes or other transient signals contaminating only a small
97 portion of the whole record. The statistical properties of the ambient noise can be estimated
98 based on a segment of the noise record and time-frequency CWT analysis allows us to navigate
99 the rest of data and remove the unwanted signals. The CWT provides one of the best choices for
100 ambient noise designating. Unlike its normal purpose for removing noise, we use this method in
101 a reverse manner to take the signal out and keep the background ambient noise.

102 The motivation of this paper is to introduce a designating procedure based on the CWT
103 and apply it to ambient noise data processing. We also use essentially the same method to
104 remove noise in the final stacked cross-correlograms. Details of the designating and denoising
105 methods will be given and then explored using a synthetic data example. Next, we use our new
106 ambient noise processing flow to process data collected from EarthScope's USArray
107 Transportable Array within the northern Mississippi embayment. The New Madrid Seismic Zone
108 (NMSZ) inside of the Mississippi embayment is one of the most earthquake-active intraplate
109 regions in North America (Hildenbrand, 1985; Cox et al., 2001; Tuttle et al., 2002; Thomas,
110 2006; Van Arsdale et al., 2007; Powell et al., 2010; Dunn et al., 2013; Van Arsdale and Cupples,
111 2013; Nyamwandha et al., 2016; Yang & Langston, 2019). Abundance of seismic events in the
112 NMSZ could be used to test the efficiency and robustness of our method. Using the real data, the
113 resulting EGFs and the final dispersion curves obtained from our method and Bensen's method
114 are compared.

115

116 **CWT DENOISING AND DESIGNALING**

117 **CWT**

118 The CWT (Daubechies 1992) is a popular tool to study time-frequency representations of
 119 continuous or discrete time series. This mathematical transformation decomposes a signal into
 120 different scales as a function of time. Different scales provide different resolutions (or can be
 121 considered as different pseudo-frequency components) of the original signal. From this point of
 122 view, it provides better resolution compared to the short time Fourier transform (Tary et al.
 123 2014). Assuming we have a time series $s(t)$, for a given mother wavelet $\psi(t)$, the CWT of time
 124 series $s(t)$ at scale a ($a > 0$) and time shift b can be expressed as (Daubechies 1992)

$$Ws(a, b) = \int_{-\infty}^{+\infty} s(t) a^{-1/2} \psi^* \left(\frac{t-b}{a} \right) dt, \quad (1)$$

125 where the $*$ indicates the complex conjugate and $Ws(a, b)$ is the wavelet coefficient
 126 representation of the signal $s(t)$ at scale a and time shift b . The Fourier transform of the mother
 127 wavelet $\psi(t)$ should satisfy the admissibility condition (Daubechies 1992; Farge 1992)

$$0 < C_\psi = \int_{-\infty}^{+\infty} |\omega|^{-1} |\hat{\psi}(\omega)|^2 d\omega < \infty, \quad (2)$$

128 in which $\hat{\psi}(\omega)$ is the Fourier transform of the mother wavelet $\psi(t)$ and C_ψ is called the wavelet
 129 admissibility constant. Such a wavelet is called an admissible wavelet. An admissible wavelet
 130 also implies that $\hat{\psi}(0) = 0$ so that the integration over time must be zero (Daubechies 1992). To
 131 recover the original signal from the CWT representations, the inverse CWT can be expressed as

$$s(t) = \frac{1}{C_\psi} \int_0^\infty \int_{-\infty}^{+\infty} \frac{1}{\sqrt{a}} Ws(a, b) \psi \left(\frac{t-b}{a} \right) \frac{dad b}{a^2}. \quad (3)$$

132 The CWT of a discrete time series can be expressed in the similar way by replacing
 133 integration with summation (Torrence & Compo 1998) and different fast algorithms are

134 developed to make it computation affordable (Rioul & Duhamel 1992). In another mathematical
135 view of equation (1), the CWT can be considered as a cross-correlation of the target time series
136 $s(t)$ with different wavelets that are stretched or compressed and shifted versions of the selected
137 mother wavelet $\psi(t)$. Because of this cross-correlation property, the CWT can be calculated
138 using the fast Fourier transform (FFT) in the frequency domain (Daubechies 1992). The CWT
139 spectrum $Ws(a, b)$ for the time series $s(t)$ is the time-frequency decomposition of the original
140 signal, with different scales a analogous to wave period (inverse frequency) and b indicating
141 time lag.

142

143 **Designing and denoising via soft thresholding**

144 Langston & Mousavi (2019) discussed an efficient method based on the CWT to denoise
145 or designal a time series using the statistical estimation of the noise. In this study, we implement
146 the soft thresholding method in the ambient noise data processing flow. Essentially, the noise is
147 estimated and then removed for different scales of wavelets by a less severe manner. The size of
148 datasets used for ambient noise tomography is usually very large. Thus, processing ambient
149 noise data requires an algorithm that is not time-consuming and works efficiently. Soft
150 thresholding (Weaver et al., 1991) can remove noise efficiently compared to computationally
151 intensive block thresholding algorithms on the wavelet scale-time plane (Mousavi & Langston,
152 2016).

153 In order to apply the CWT soft thresholding denoising, the original time series $s(t)$ is
154 first transformed into the CWT time-frequency domain to get the CWT spectrum $Ws(a, b)$. The
155 noise level for a specific scale a is estimated and the CWT coefficients for this scale are
156 modified by the non-linear soft thresholding given by

$$\bar{W}_s(a, b) = \begin{cases} \text{sign}[W_s(a, b)](\|W_s(a, b)\| - \beta(a)) & \text{if } \|W_s(a, b)\| \geq \beta(a), \\ 0 & \text{otherwise} \end{cases}, \quad (4)$$

157 where

$$\text{sign}[W_s(a, b)] = \frac{W_s(a, b)}{\|W_s(a, b)\|}, \quad (5)$$

158 $\bar{W}_s(a, b)$ is the CWT spectrum after denoising for the scale a and $\|\cdot\|$ stands for the modulus of
 159 the complex spectrum in the CWT domain. The threshold function $\beta(a)$ is determined based on
 160 the statistics of the absolute value of the noise for scale a . If the CWT spectrum is less than
 161 $\beta(a)$, it is considered as the noise and we will remove it by setting it to zero. Otherwise, it
 162 contains both noise and signal, and the predefined noise is subtracted from the original spectrum.
 163 This criterion is applied to data at each scale in the CWT spectrum. Ambient noise data is
 164 continuously recorded and earthquakes and other signals only make up a small proportion of the
 165 whole record. The noise level $\beta(a)$ can be well estimated with a predetermined time segment
 166 which contains only ambient noise. Much of the signal processing procedures start from an
 167 assumption of Gaussian noise. The threshold function can be computed using the mean and
 168 standard deviation of the CWT spectrum for scale a within the selected time segment:

$$\beta(a) = \text{mean}(\|W_s(a, b)\|) + N \text{std}(\|W_s(a, b)\|), \quad (6)$$

169 where

$$\text{mean}(\|W_s(a, b)\|) = \frac{1}{T_2 - T_1} \int_{T_1}^{T_2} \|W_s(a, b)\| db, \quad (7)$$

$$\text{std}(\|W_s(a, b)\|) = \left[\frac{1}{T_2 - T_1} \int_{T_1}^{T_2} (\|W_s(a, b)\| - \text{mean}(\|W_s(a, b)\|))^2 db \right]^{\frac{1}{2}}, \quad (8)$$

170 and N is a parameter that controls the threshold noise level. The time limits T_1 and T_2 represent
 171 the start and end time of the selected time segment.

172 There are different criteria to choose the threshold coefficient, N , in equation (6). Simply
 173 choosing $N = 3$ will yield a signal at 99.7% confidence level (Starck et al., 2010) if the CWT
 174 coefficients of the noise follow a normal distribution. This method is straightforward to estimate
 175 the noise level. But unfortunately, the assumption that the CWT coefficients follow a Gaussian
 176 distribution is rarely seen in seismic noise data (Langston & Mousavi, 2019). The distribution for
 177 real ambient noise is usually unpredictable. However, we can estimate a data-driven noise level
 178 by taking the approach of empirically estimating the cumulative distribution of noise and then
 179 calculating the 99% confidence value for the distribution. To calculate the empirical cumulative
 180 distribution function (ECDF), we can order the N samples noise values and then assign a
 181 probability jump of $1/N$ when a value is attained, starting with the smallest value. Thus, the
 182 threshold function becomes:

$$\beta(a) = \text{ECDF}^{-1}(P = 0.99), \quad (9)$$

183 where ECDF^{-1} is the inverse of the cumulative distribution function or the quantile.

184 In Fig. 1, we compare the threshold functions assuming Gaussian statistics in equation (6)
 185 and non-Gaussian statistics in equation (9). The distribution of the empirical probability
 186 distribution function of the real noise is different compared to a Gaussian distribution and gives
 187 quite different estimated noise levels. Overall, there are significant differences between the
 188 ECDF and Gaussian threshold functions. It also suggests that the ECDF method would lead to a
 189 better estimate of the threshold and thus we use the ECDF method to estimate the noise level in
 190 our processing.

Fig.1

191 Designating reverses the denoising process. This procedure can be applied in our ambient
 192 noise processing to remove earthquakes and other signals. For the soft thresholding case, signal
 193 is removed by using

$$\bar{W}_s(a, b) = \begin{cases} \text{sign}[W_s(a, b)]\beta(a) & \text{if } \|W_s(a, b)\| \geq \beta(a) \\ W_s(a, b) & \text{otherwise} \end{cases}. \quad (10)$$

194 At each scale, if the CWT spectrum is less than the estimated noise level, we consider it as the
 195 noise and keep the spectrum. Otherwise, we consider it as the signal and remove it by setting the
 196 coefficient to the noise level.

197 Using the soft thresholding method to remove noise or signal based on ECDF is very
 198 straightforward and efficient. After applying equation (4) for denoising or equation (10) for
 199 designating, we get our new CWT spectrum and get the final denoised or designated output for
 200 our next processing step by doing the inverse CWT from equation (3).

201

202 DATA AND DATA PROCESSING FLOW

203 Data preprocessing

204 We use data from 55 broadband seismic stations of EarthScope’s USArray Transportable
 205 Array (TA) recorded during July, 2012, within and around the northern Mississippi embayment
 206 (Fig. 2) to demonstrate our ambient noise data processing flow. Velocity models for this area are
 207 developed using full waveform tomography of the EGFs extracted from all temporary and
 208 permanent stations. The crustal and upper mantle structures underneath the northern Mississippi
 209 embayment are investigated. These models will be the subject of future reports.

210 In order to compare the robustness of our method, we compare cross-correlations and
 211 dispersion curves with those computed based on time domain normalization (TDN). The
 212 “MSNoise” package (Lecocq et al., 2014) is a python package which implements the TDN
 213 method.

214 We first download daily vertical component waveform data for each station through the
 215 IRIS (www.iris.edu) FDSN web service and work with them in SAC format, remove the

Fig.2

216 instrument response, remove the mean and trend, apply a bandpass filter from 0.02Hz to 1Hz and
217 downsample the sampling rate from 40Hz to a 5Hz. The reason why we choose the passband
218 0.02-1Hz is that previous studies (e.g. Liang et al., 2008; Langston et al., 2009; Liu et al., 2018a;
219 Yang & Langston, 2019) observed prominent surface wave arrivals in this frequency band.
220 Downsampling the sampling rate to 5 Hz not only reduces the storage but also reduces the
221 computation time of cross-correlations. Small events are usually higher frequency and are
222 filtered out during the downsampling.

223

224 **CWT ambient noise data processing flow**

225 The temporal normalization step is replaced by the designating method described above.
226 After single station data preparation, the CWT designating method is applied on each day of the
227 data, followed by spectral whitening to provide spectrum-balanced data. A 5% taper is applied at
228 the beginning and end of each data segment to avoid artifacts during cross-correlation. Each pair
229 of stations are then cross-correlated and all one-day cross-correlograms for the month are stacked
230 to increase the SNR.

231 In order to estimate the noise statistics for each day, we need to find a segment of the data
232 that only contains noise. This is realized by a simple algorithm. For each day's data, we divide
233 the time series into 48 half hour segments. The maximum absolute value in each segment is
234 determined and the segment with the minimum absolute value is chosen to estimate noise
235 statistics. There is no guarantee that earthquakes or other signals will not appear within the
236 selected segment, but it provides a fast and accurate way to find this estimate. The time duration
237 for each segment could be shorter when teleseismic events occur more frequently but each

238 segment still needs to be long enough to make a robust estimate. The test in Fig. 2 shows that the
239 noise level could be estimated accurately with data time series as short as 500 seconds.

240 Besides removing the signal, soft thresholding can also be used to remove the noise in the
241 final stacked EGFs to increase the SNR (equation 4). This step is applied to deliver the final
242 EGFs.

243 Our new ambient noise data processing flow can be summarized into the following steps:

244 Step 1: Pre-processing: prepare waveform data for each station individually, which
245 includes cutting the data into intervals of one-day, removing the instrument response, removing
246 the mean and trend, applying a bandpass filter and resampling the data to a 5Hz sampling rate.

247 Step 2: Designal: for each one-day time series for a station, apply the soft thresholding
248 designaling method to remove earthquakes and other transients.

249 Step 3: Spectral whitening, cross-correlation and stack: applying spectral whitening for
250 each one-day time series for a station to provide a broader-band and spectrum-balanced data.
251 Calculate the cross-correlation for each possible day and each station pair. Stack the desired
252 number of day-correlations for each station.

253 Step 4: Applying the soft thresholding denoising method to remove the noise in each of
254 the stacked cross-correlograms.

255 After step 4, we get the final EGFs for a pair of station, which can then be used to
256 measure group and phase velocity (Liu et al., 2019) or to do full waveform tomography (Yang &
257 Langston, 2019) to determine earth structure.

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RESULTS

We first apply the designating algorithm to “synthetic” seismic data constructed from real data. The whole designating procedure can be better examined and compared with the known noise input signal. Next, the entire flow will be applied to our subset of the TA array data and compared with results from using TDN.

In our implementation of the CWT, we use the Morlet wavelet as the mother wavelet $\psi(t)$ in equation (1) and (3) with 16 voices per octave. The designating method is not sensitive to the number of the decomposition levels and smaller scale numbers will speed up the whole processing (Mousavi and Langston, 2016). Using 16 voices per octave in the processing is large enough for resolution while retaining efficiency. Choosing the right mother wavelet is also a difficult task. Different target problems require different optimal wavelets. We tried a number of different mother wavelets and by comparing the RMS error between the input noise and the final designated results from the synthetic test, we achieve the least misfit using the Morlet wavelet. Therefore, we will use the Morlet wavelet in our data processing.

Synthetic Data

To best simulate real data, we construct a synthetic time series by using two segments of recorded seismograms at station U41A. One segment contains 3,000 seconds of ambient noise data. The other seismogram segment is with the same length but contains a teleseismic event. The ambient noise segment is chosen to make sure that there is no earthquake or other obvious transient signal in the selected time period by looking at the seismogram in the time domain and the scalogram in the CWT domain. A teleseismic event occurred on July 25, 2012, was recorded by the station and is used as the earthquake input. The soft thresholding denoising algorithm is

284 first applied on the earthquake segment to remove any ambient noise contained in the
285 seismogram. Then, both the ambient noise segment and the denoised earthquake segment are
286 filtered with a 1Hz low-pass filter. The earthquake segment is then tapered before the first arrival
287 time and at 1400 seconds to make sure there is no noise or signal before or after. The ambient
288 noise segment and the teleseismic event segment are then summed to produce the final synthetic
289 data (Fig. 3).

Fig.3

290 The CWT spectrum of the synthetic data is calculated and shown in Fig. 3(d). The
291 earthquake and ambient noise are clearly distinguished and are indicated in the spectrum. The
292 CWT spectrum for ambient noise only falls into a specific range of scales and keeps a very stable
293 amplitude pattern. These scales correspond to the main frequency band of the ambient noise. The
294 earthquake contains signals over a wider range of scales which corresponding higher scale or
295 lower frequency data and with much larger amplitude. The CWT spectrum for the earthquake is
296 also changing with time and the pattern looks irregular. The overlapping scale band between the
297 earthquake data and the ambient noise data makes it impossible to separate them by just using a
298 bandpass filter.

299 After 1500 seconds, the seismogram is pure ambient noise and we use this segment to
300 calculate the ECDF of the ambient noise and estimate the noise level for each scale. After
301 obtaining the statistical properties of the ambient noise, we will decide whether the CWT
302 spectrum is kept the same or modified by using the criteria in equation (10). The CWT spectrum
303 after soft thresholding and the final designaled seismogram are shown in Figs 3e and f. The
304 designaling algorithm removes most of the earthquake signal and the noise superficially looks
305 the same before and after designaling. The time series after designaling looks more like the
306 original ambient noise since it has a balanced amplitude throughout. A comparison of particular

307 time windows before and after designating is also shown in Figs 3g and h. Noise is not modified
308 by this algorithm and appears qualitatively the same before and after designating. The CWT
309 spectrum of the designated time series is like a clipped version of the original spectrum which
310 suggests that there is still some small effects of the teleseism in the time series. We compare the
311 Fourier amplitude spectrum of input noise, input synthetic data and final designated results (Fig.
312 4). The designated time series has a slightly larger amplitude spectrum than the original spectrum
313 of the input noise due to the existence of some signals. But overall, the designated result shows
314 very good amplitude recovery.

Fig. 4

315

316 **Real Data**

317 All of data recorded by the selected TA stations during July 2012 are used as input data
318 to test the new processing flow. We will use the station V44A (Fig. 2) which is located within
319 the NMSZ as an example to show the results. There are plenty of earthquakes and transient
320 signals appearing in the original recording (Fig. 5), which make it perfect to test the new
321 processing flow. For comparison, we also process the same data with TDN as a benchmark.

Fig. 5

322 Station V44A and S38A are used to show the details of each processing step (Fig. 6). A
323 teleseismic event is obviously present in these particular data. Ambient noise is barely seen and
324 is buried beneath the earthquake signals. Earthquake signals are efficiently removed after soft
325 threshold designating and we get an amplitude-stable time series. Both stations show similar
326 results and no obvious earthquakes or transient signals are seen in the data after designating.

Fig. 6

327 The designated data are then correlated. The cross-correlogram from the soft thresholding
328 designated data has higher SNR compared with the one from TDN. The Rayleigh wave at
329 positive time lags is not clearly seen in the result using TDN. The running absolute mean

330 normalization method will only balance the amplitude of the original data to match the amplitude
331 of the ambient noise. However, the spectrum is dominated by the truncation of peaks and troughs
332 of the high amplitude signal in the time domain that non-linearly increases its high frequency
333 parts. Truncating the CWT is less severe because individual wavelets are intrinsically smooth
334 and are smoothed yet again during the inverse transform integration. The data of the two
335 stations for other days are processed in the same way and the final one-month stacked cross-
336 correlogram calculated from our processing flow also shows higher SNR (Fig. 6d). The
337 designating method removes earthquakes and other transient signals in a physical meaningful
338 way and it does not touch any ambient noise data. TDN achieves temporal normalization but
339 modifies the ambient noise while using a relatively harsh way to balance the amplitude of the
340 whole time series. We suggest that CWT designating preserves more of the noise characteristics
341 within the event time window.

342 After correlation and stacking, random noise is still clearly seen in the stacked EGF. To
343 further increase the SNR, we apply soft threshold denoising on the stacked EGF (Fig. 6e). This
344 will remove much of the noise within the final stacked cross-correlogram and give us an even
345 higher SNR result.

346 A more dramatic example is shown in Fig. 7. One-month correlation results are stacked
347 for stations W42A and W46A to get the EGF. Fourier filtering and the soft threshold denoising
348 method are applied to improve the SNR of the stacked EGF. The noise frequency range overlaps
349 with the signal frequency range. After the low-pass filter, noise is still obvious in the EGF and
350 the SNR does not increase significantly. However, with the soft threshold denoising method, the
351 noise is removed and the denoised EGF has a very high SNR, which provides for better input in
352 later processing steps, such as group and phase velocity extraction.

Fig. 7

353 Fig. 8 shows a record section of final EGFs for master station V44A from our processing
354 flow and TDN. Both processing flows give clear EGFs. Symmetric Rayleigh waves are also
355 observed. To better compare the two processing flows quantitatively, we compute the SNR by
356 using the ratio of maximum amplitude between -200s and 200s and the maximum amplitude for
357 the rest of data. Our new processing flow gives five to ten times higher SNR over using TDN.
358 Rayleigh waves are clearly observed on both positive and negative time lags with smaller
359 amplitude noise in between.

Fig. 8

360 The next step after acquiring the final EGFs is to calculate phase or group velocities
361 between each station pair. Although this is not the primary purpose of this paper, it is useful to
362 examine the differences in results obtained using the two data processing schemes. Readers may
363 refer to other studies and reports (e.g. Yao et al., 2006; Bensen et al., 2007) for more details of
364 dispersion calculation. Here, we show a comparison of the group velocities determined from
365 EGFs between the two processing flows for one station pair (Fig. 9). We calculated the group
366 velocity dispersion curve for station S38A using frequency-time analysis (Dziewonski et al.,
367 1969). Although group velocities have significant overlap between the two methods, they clearly
368 have different trends for periods greater than 15s. It is likely that these changes in the dispersion
369 curves will give rise to differences in the resulting velocity models.

Fig. 9

370

371 **DISCUSSION**

372 When deciding which processing flow to use for a specific dataset, we should observe
373 how many earthquakes and other transient signals are contained in the data. In the interest of
374 computational efficiency, if there are few transient events then CWT designating may be
375 overkill, wasting valuable compute cycles.

376 The new processing flow will deliver reliable and high SNR EGFs, which will be very
377 helpful in further processing steps, such as studying the attenuation or extracting body waves
378 from ambient noise seismic interferometry. However, some drawbacks of our processing flow
379 still need to be considered. The main concern is its relatively high computational cost. The CWT
380 is the most time-consuming part, which requires many forward and inverse Fourier transforms.
381 When processing large datasets such as years of ambient noise recording from large networks,
382 the computational time to designal will not be insignificant. Based on our processing experience,
383 it will take about half a minute to designal one-day of data for one station on a Macbook Pro
384 laptop. One possible solution is to use graphic processor unit (GPU) to calculate the wavelet
385 transform and remove the signals when processing large amounts of data, which will speed up
386 the processing significantly. It will take about 8 seconds to designal one-day of data for all 55
387 stations on a NVidia V100 GPU. Another possibility is to check the data first and only apply the
388 soft threshold designaling if signals are observed in the data. In this study, we only processed
389 one-month of data at 55 stations and the time for the processing is acceptable.

390 Another assumption for this method is that the ambient noise time series should be stable
391 in that its statistical properties should not change significantly in each one-day data segment. If
392 such changes are observed in the data, the largest noise level should be used in the designaling
393 process to avoid accidentally removing any ambient noise.

394 Ambient noise tomography has been widely used during the last 15 years and will be
395 continuously developed in the future. Acquiring more reliable EGFs and getting more
396 information from seismic interferometry will make this method more powerful and robust.

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CONCLUSIONS

We propose a new ambient noise data processing flow to compute reliable EGFs. The denoising and desIGNALing algorithm is based on the CWT with soft thresholding and is essential to this flow. The whole processing flow is automated without any manual interference. The new processing flow is suitable for data containing regional and teleseismic events or other transient signals. The whole processing flow is divided into four steps: (1) single station data preparation, (2) remove earthquakes and other transient signals in the seismic record, (3) spectrum whitening, cross-correlation and temporal stacking, (4) remove the noise in stacked cross-correlogram to deliver the final EGFs. The final EGFs can be used to extract phase or group velocity or to invert for velocity structure by full waveform tomography.

The principal step during data preparation is to acquire pure ambient noise that is free of earthquake and other transient signals (instrument irregularities and non-stationary noise sources near to stations, etc.). We adopt a method based on the CWT to remove these unwanted signals. The intrinsic time-frequency property of the CWT makes it possible to isolate noise and signal efficiently. A segment of pure ambient noise is usually obtainable and can be used to estimate the statistical property of the noise in the CWT domain. The estimated noise statistical properties are then used as a guide to detect whether the data point at different time and scales in the CWT domain is noise or not. A soft thresholding method is used to remove the signal if the data exceeds the noise level. We constructed synthetic data based on recorded noise and an earthquake to successfully test the method. Use on more extensive data shows excellent signal removal. Other denoising algorithms based on the CWT such as block thresholding (Mousavi et al., 2016) could also be used to remove earthquakes and other signals in the time series but they also require much more computational cost. Our method is efficient for large datasets.

422 The denoising method can also be used to remove the noise in the final EGFs to further
423 increase the SNR. We use the same algorithm as in the designating step but in a reverse manner
424 to significantly increase the SNR in the final EGF. This denoising method performs better than
425 bandpass filters since a Fourier filter has no time resolution.

426 We applied our processing flow to one-month of data from EarthScope TA stations near
427 the NMSZ. Many earthquakes and other transient signals were recorded by the stations which
428 make this dataset an appropriate test dataset for the algorithm. We obtain better EGFs with
429 higher SNR than results using TDN. Except for removing earthquake and other transient signals
430 that obscure the ambient noise data, and noise removal for the final stacked empirical Green's
431 function, our processing flow is basically the same as previously proposed (Bensen et al., 2007).
432 In regions where few earthquakes occur, there should not be many differences in the resulting
433 EGFs between these two processing flows. However, the stacked EGF denoising step is
434 recommended for both methods because it has relatively low computational cost but dramatically
435 increases the SNR.

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DATA AND RESOURCES

438 Seismogram data used in this study are collected from IRIS (<http://www.iris.edu>, last
439 accessed on January 2019). A MATLAB GUI code to process simple dataset and visualize the
440 results from the CWT denoising and designating method used in this study can be accessed at
441 <http://www.ceri.memphis.edu/people/clangstn/software.html> (last accessed on August 2019).

442 A CPU/GPU code to process large ambient noise datasets can be downloaded from

443 https://github.com/SwiftHickory/bc_denoise.git (last accessed on August 2019).

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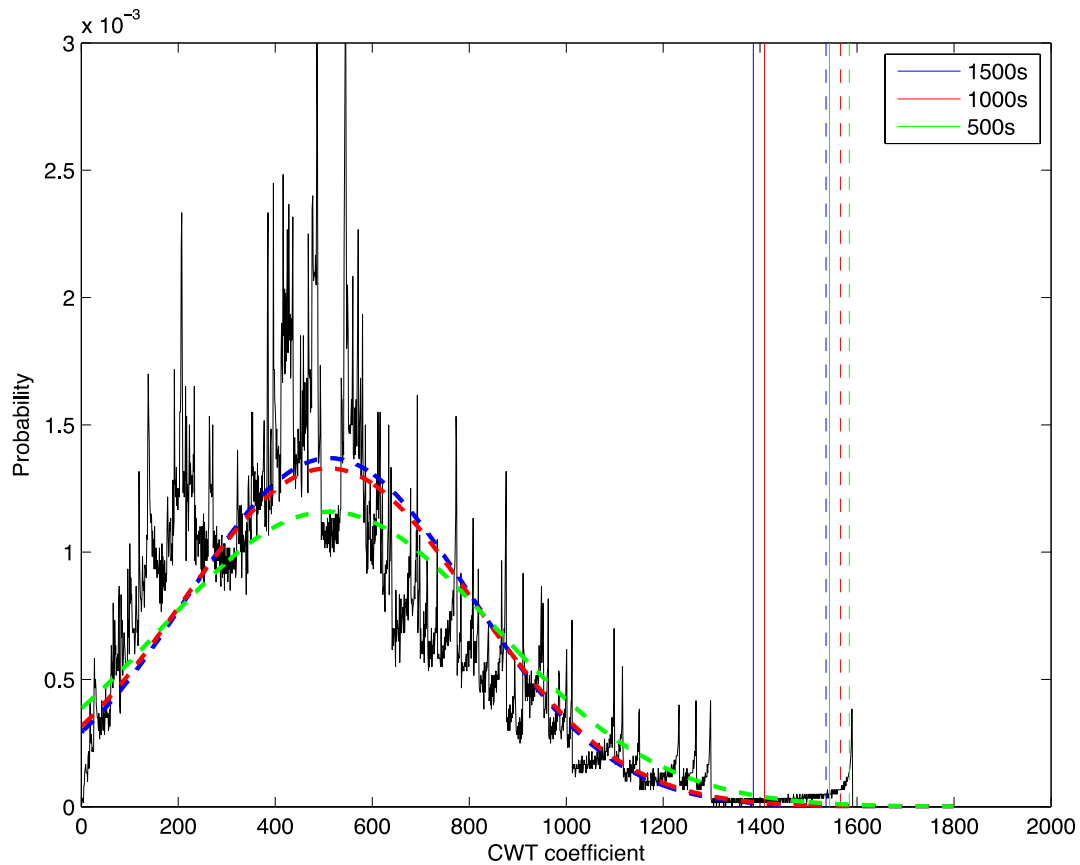
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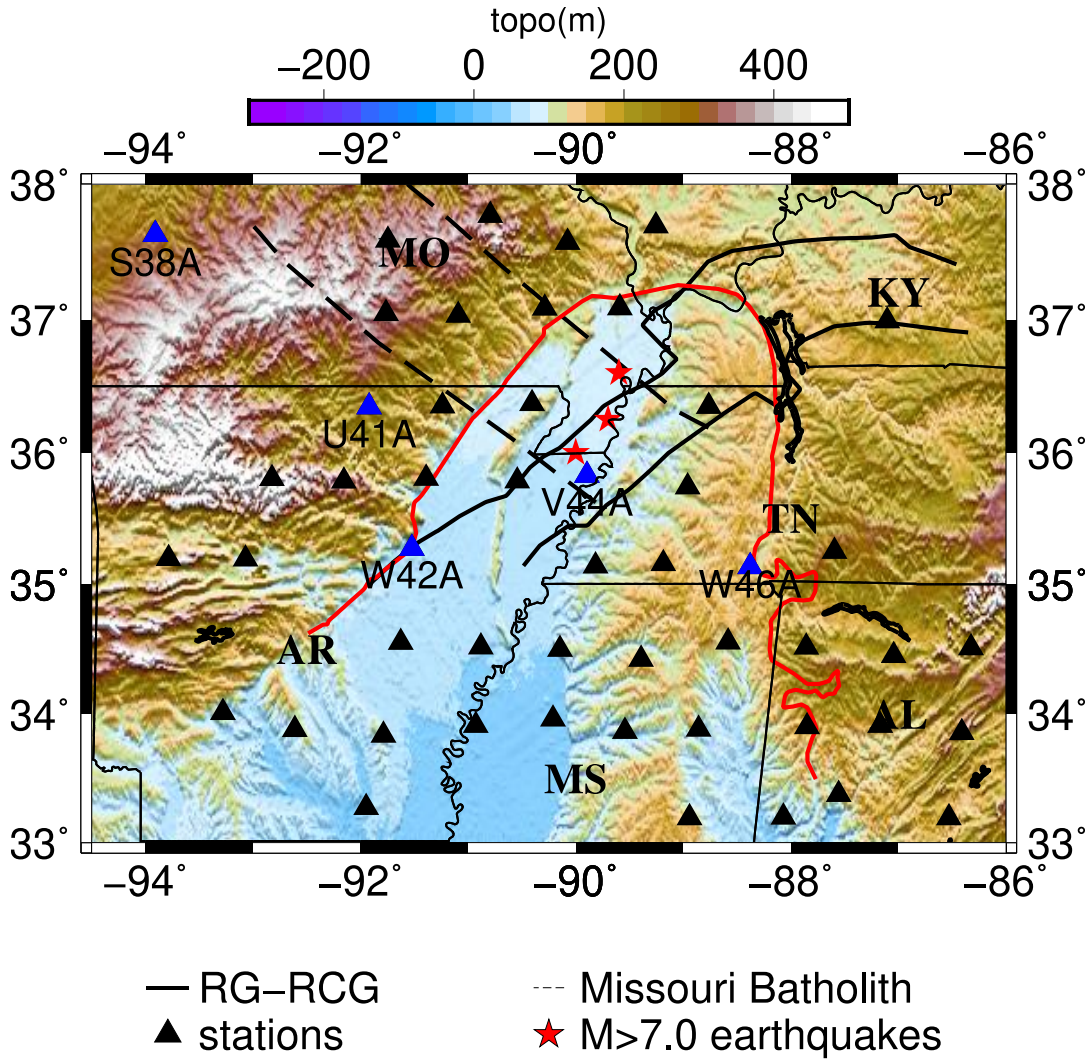
FIGURES



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555 Figure 1. Empirical probability density function of the ambient noise CWT coefficients (black
 556 line) and the estimated probability density function (dashed line) with the assumption of normal
 557 distribution. The ambient noise data used for this plot are shown in the synthetic test figure. The
 558 empirical probability density function is plotted only with 1500s data and the noise level is
 559 estimated with different data length of 1500s, 1000s and 500s, respectively. The vertical solid
 560 line and dashed line show the estimated noise level based on Gaussian distribution and empirical
 561 probability distribution with 99% confidence value, respectively. Notice that the estimated noise
 562 level is more stable with ECDF method.

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565 Figure 2. The distribution of the seismic stations used in this study (filled triangles).

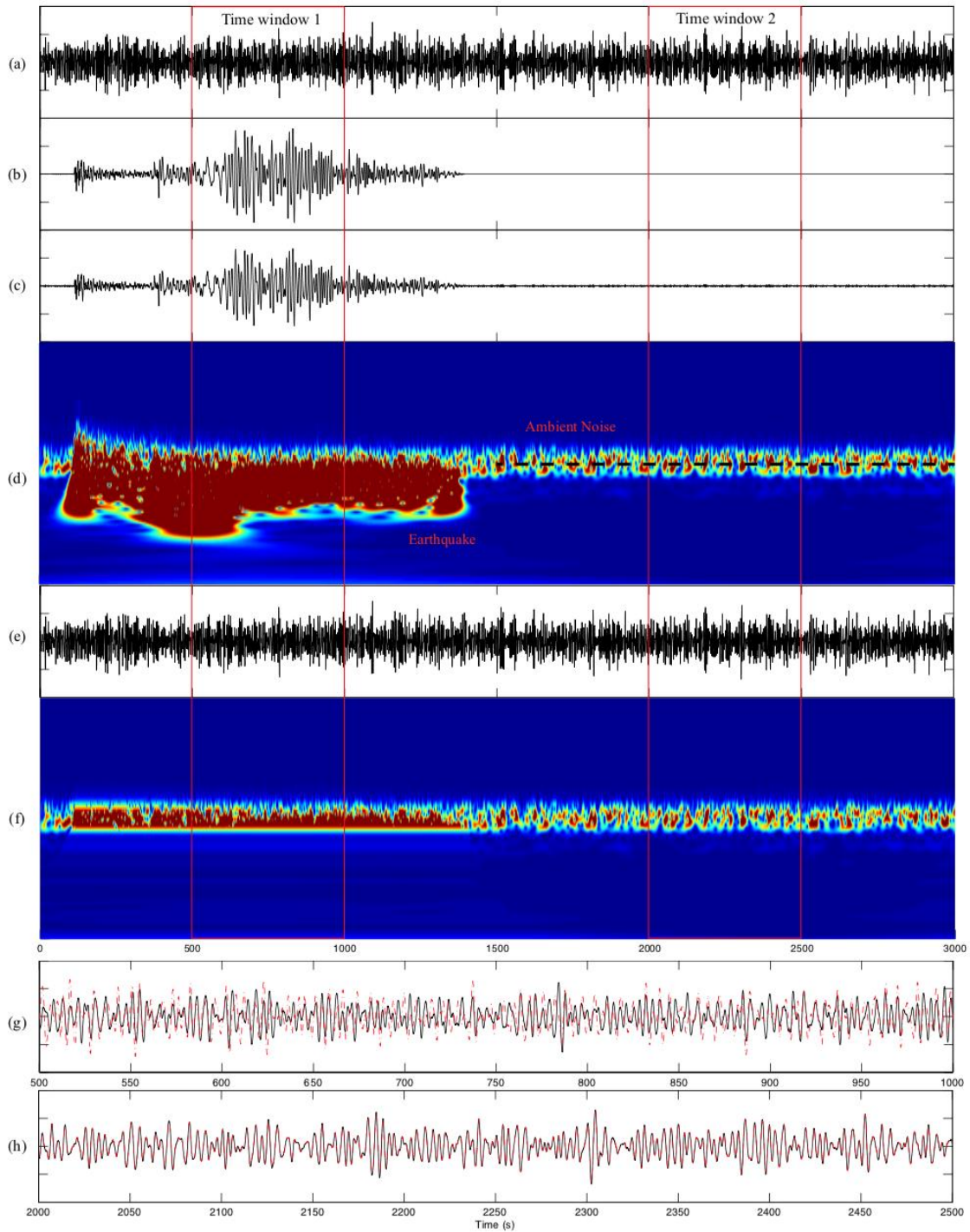
566 Continuously seismic recordings during July 2012 from a subset of the USArray Transportable
567 Array stations in and around the northern Mississippi embayment are our benchmark test dataset.

568 Major geological features include the Reelfoot Graben (RG), Rough Creek Graben (RCG) and
569 Missouri batholith (between two dashed lines). The boundary of the Mississippi embayment is

570 shown by the red lines. The locations of the three large earthquakes that occurred in 1811 and
571 1812 are shown as the red stars (Johnston & Schweg, 1996). Several specific stations used as

572 examples in the rest of this article are annotated.

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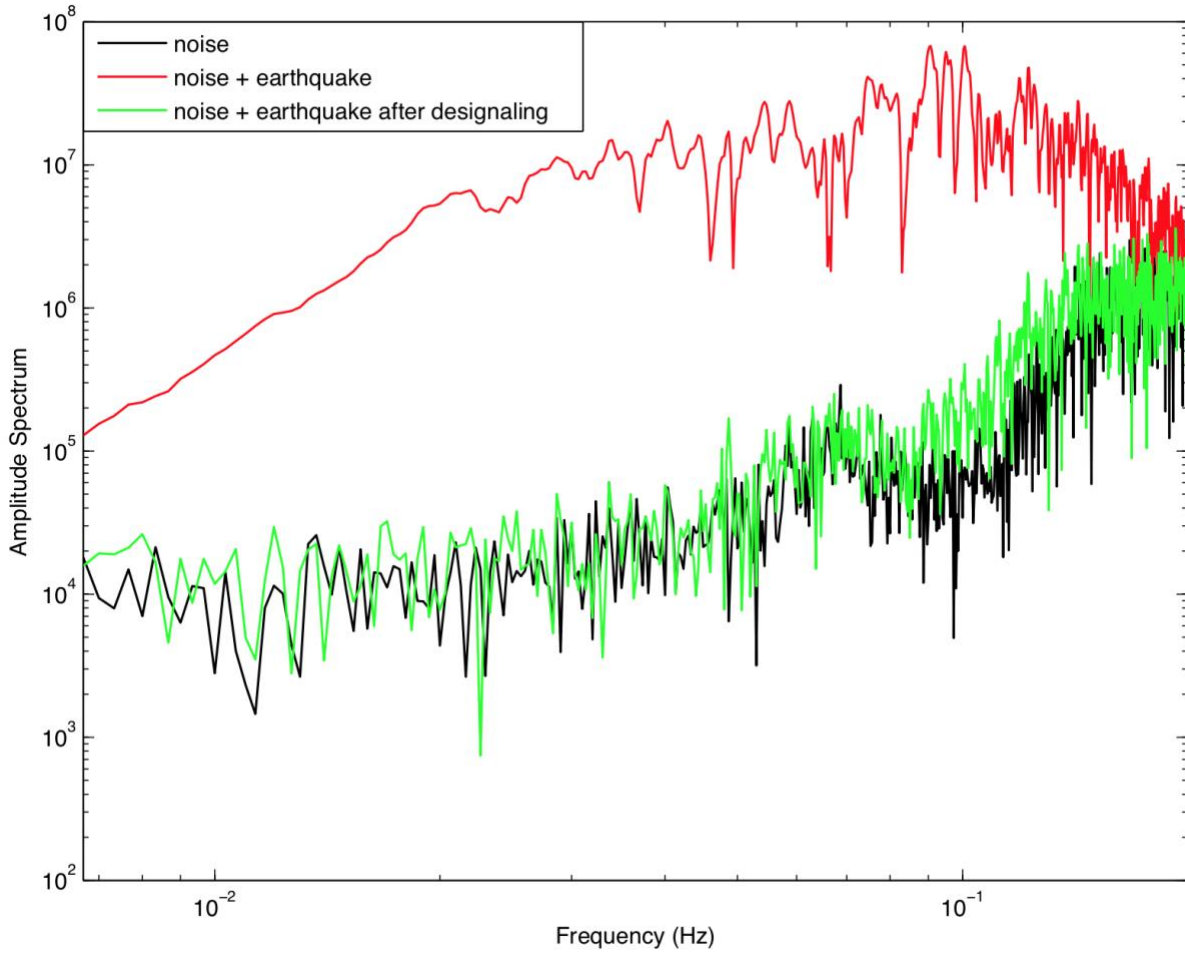
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575 Figure 3. Designing synthetic test based on recorded ambient noise and earthquake data. (a)

576 3000s ambient noise data from station U41A. (b) The July 25, 2012, teleseismic earthquake

577 recorded by station U41A. The data are denoised with the CWT soft thresholding denoising

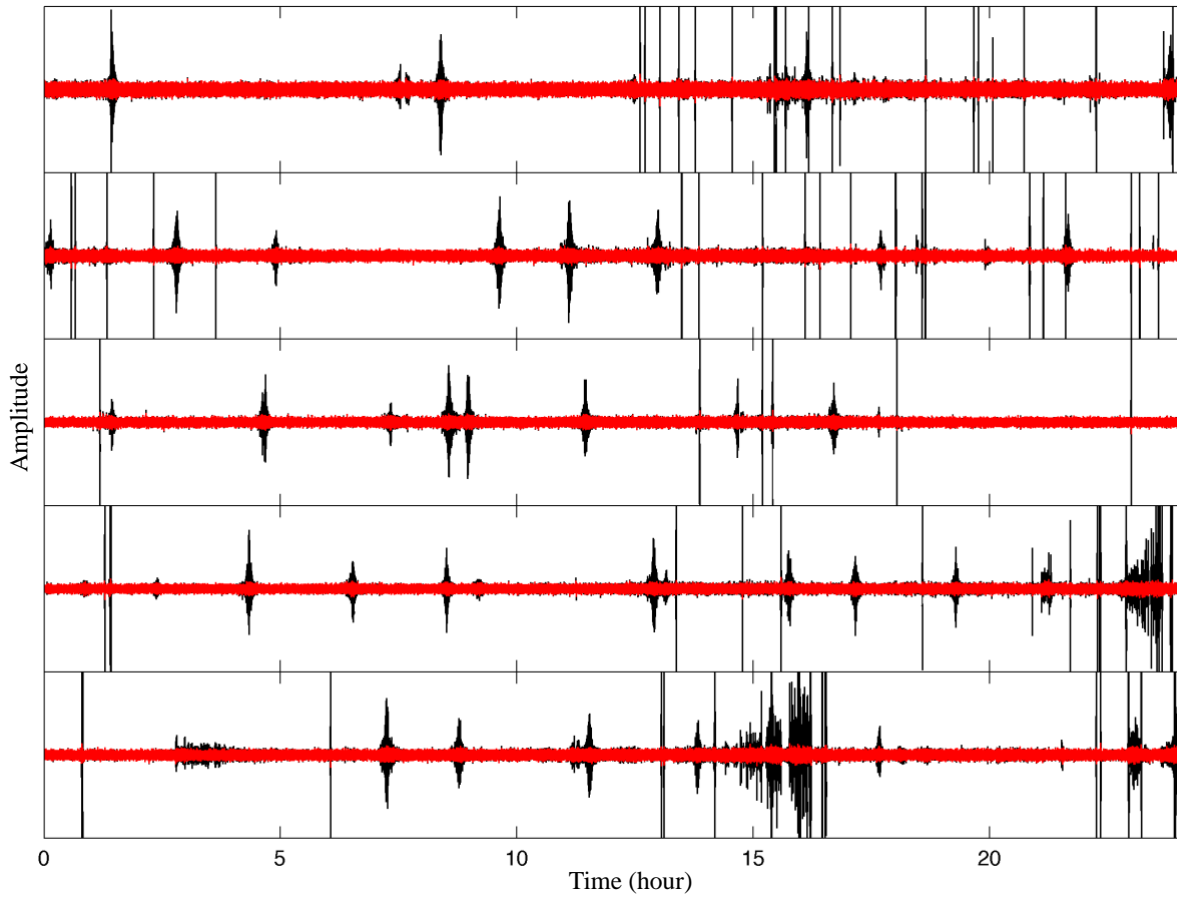
578 algorithm and a 1Hz low-pass filter is applied after denoising. Data before the first arrival and
579 after 1400 seconds are tapered. (c) Synthetic data constructed by summing ambient noise data in
580 (a) and seismic event data in (b). (d) The modulus of the complex CWT spectrum of synthetic
581 data in (c). The dashed line indicates the data used in (a). (e) Synthetic data after designating
582 shown in the time domain. (f) Synthetic data after designating shown in the CWT domain. (g)
583 The comparison of seismic data before designating (solid line) and after designating (dashed
584 line) with the data in the time window 1. (h) Same as (g) but for time the window 2. The vertical
585 red lines delineate the two 500s time windows.



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587 Figure 4. The comparison of the Fourier amplitude spectrum between the original noise data, the
588 noise data added with earthquake data and the final designaled data.

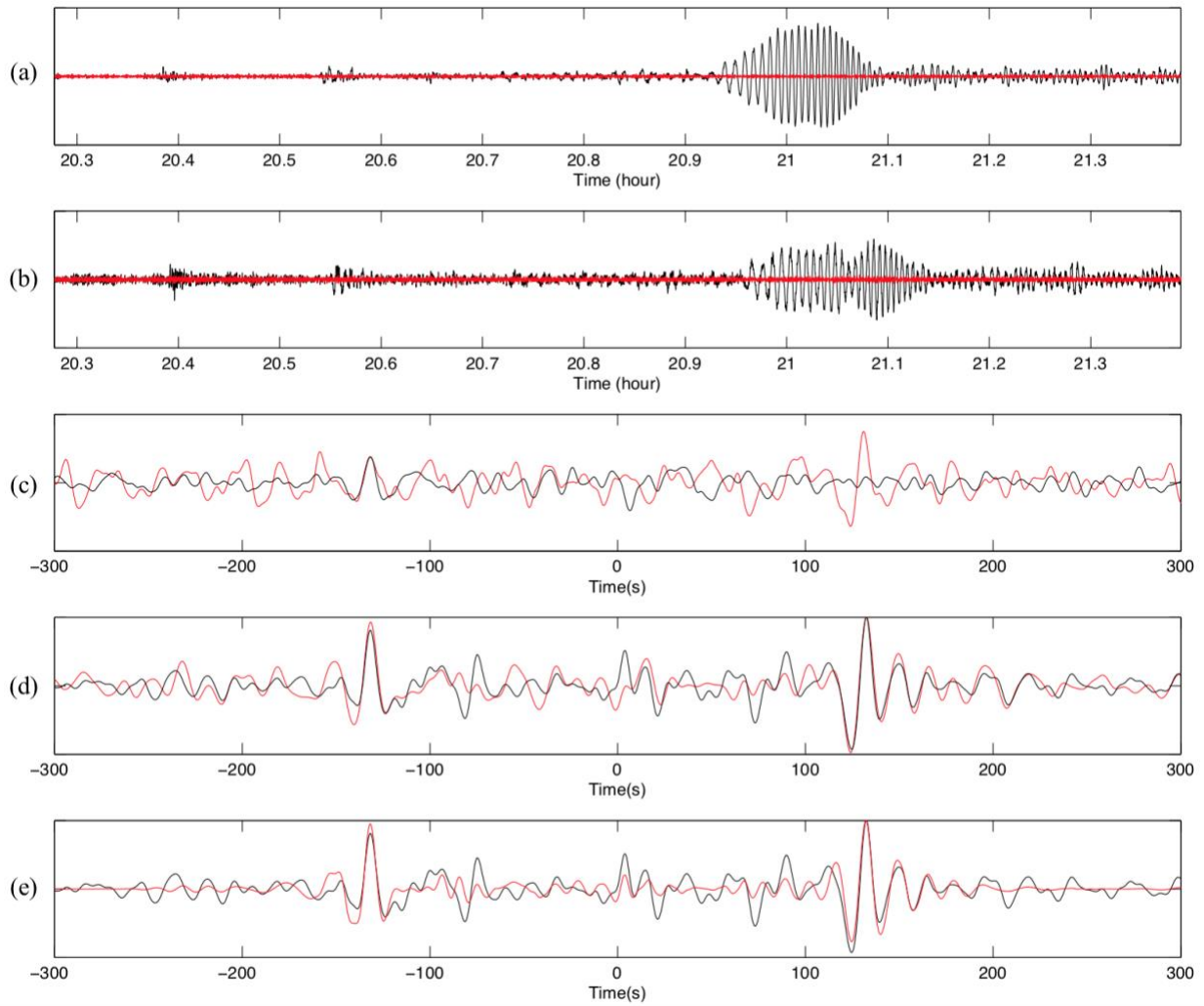
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591 Figure 5. Vertical component seismograms of station V44A recorded during the first five-days of
592 July 2012 (black) and the designated result (red). Each row shows one-day of seismic data. There
593 are many earthquakes and transient signals recorded by the station. These signals are
594 successfully removed after designating.

595



596

597 Figure 6. EGF calculation between station V44A and S38A. (a) A segment of seismic record for

598 station S38A on July 28, 2012, with the black line indicating the original data and the red line

599 showing the desigined results. A teleseismic event is seen within this time period and is

600 removed after desigining. (b) Same as (a) but for station V44A. (c) One-day cross-correlation

601 between station S38A and station V44A for date July 28, 2012, calculated using TDN (black)

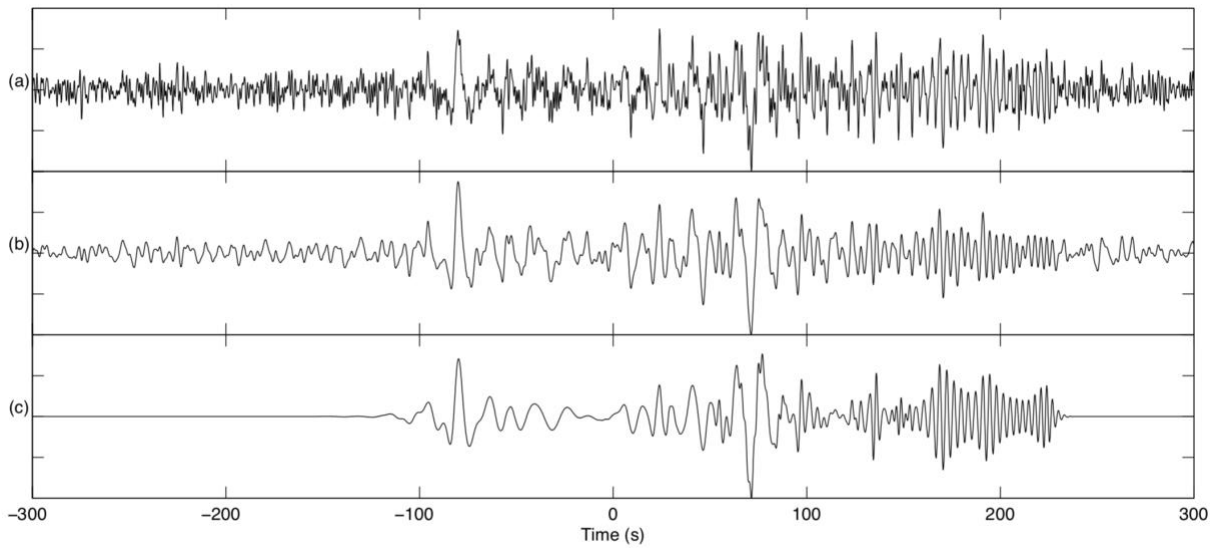
602 and the desigined data (red). (d) One-month stacked cross-correlogram obtained from TDN

603 (black) and our processing flow before the final denoising step (red). (e) One-month stacked

604 cross-correlogram obtained from TDN and our processing after the final denoising step (red).

605 Absolute amplitude is plotted in (c). The amplitude is normalized in (d) and (e).

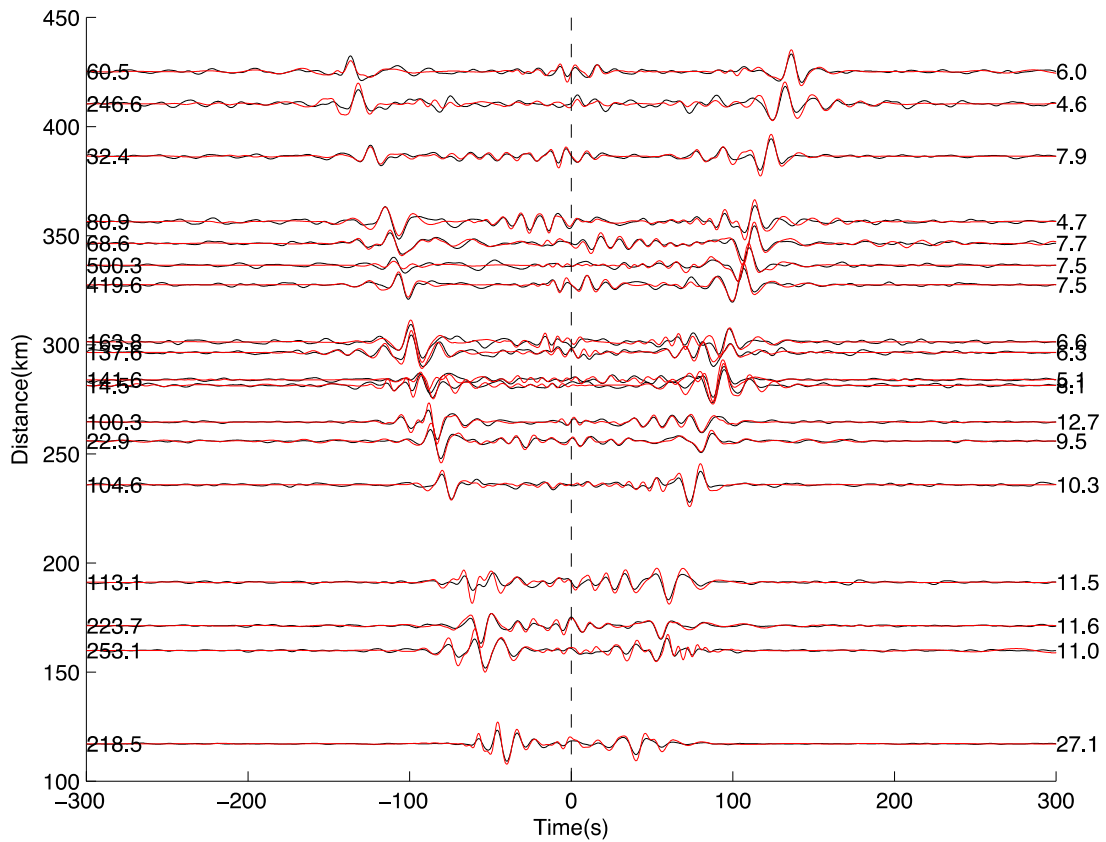
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608 Figure 7. Application of soft threshold denoising on the final stacked cross-correlogram for
609 stations W42A and W46A. (a) Original stacked cross-correlogram. (b) Stacked cross-
610 correlogram with a 0.3Hz low-pass filtered applied. (c) Stacked cross-correlogram after soft
611 thresholding denoising.

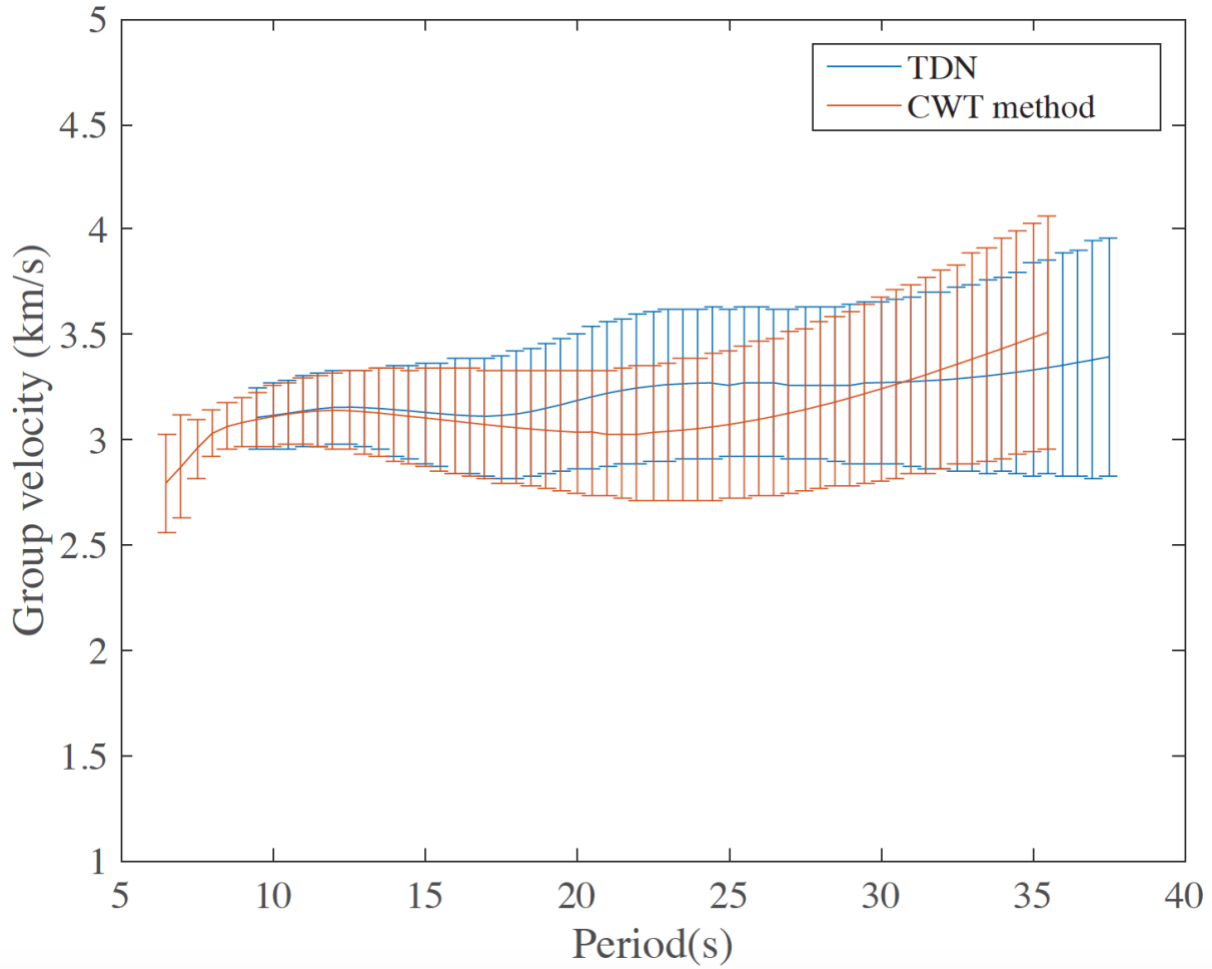
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614 Figure 8. EGFs record section acquired from TDN (black) and our processing flow (red) for
 615 station V44A. SNR for the results from TDN is shown on the right side and for our method on
 616 the left side. The SNR is calculated using the ratio between the maximum amplitude from the
 617 time window -200s to 200s and maximum amplitude of the remaining part. A bandpass filter
 618 between 0.01s and 0.15s is applied to all data. The amplitude is the stacked absolute amplitude
 619 without normalization.

620



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622 Figure 9. Comparison of group velocity dispersion curves from station V44A to station S38A

623 from an EGF using TDN (blue) and our processing flow (red).

624