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Abyssal Circulation Driven By Near-Boundary Mixing:

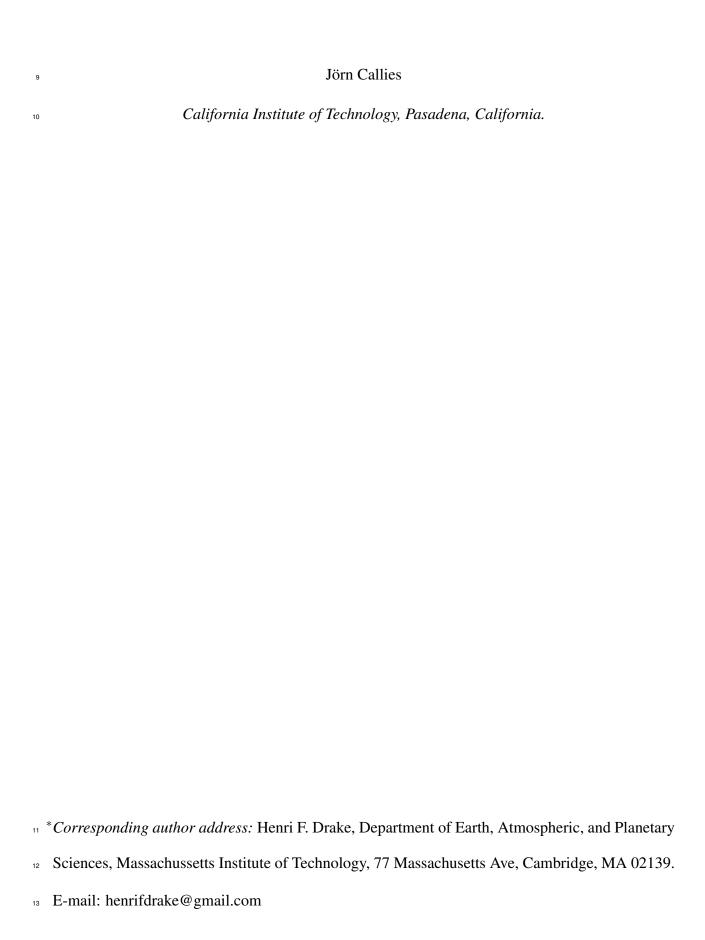
Water Mass Transformations and Interior Stratification

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ABSTRACT

The emerging view of the abyssal circulation is that it is associated with bottom-enhanced mixing, which results in downwelling in the stratified ocean interior and upwelling in a bottom boundary layer along the insulating and sloping seafloor. In the limit of slowly-varying vertical stratification and topography, however, boundary layer theory predicts that these up- and downslope flows largely compensate, such that net watermass transformations along the slope are vanishingly small. Using a Planetary-Geostrophic Circulation Model that resolves both the boundary-layer dynamics and the largescale overturning in an idealized basin with bottom-enhanced mixing along a mid-ocean ridge, we show that vertical variations in stratification become sufficiently large at equilibrium to reduce the degree of compensation along the mid-ocean ridge flanks. The resulting large net transformations are similar to estimates for the abyssal ocean and span the vertical extent of the ridge. These results suggest that boundary flows generated by mixing play a crucial role in setting the global ocean stratification and overturning circulation, requiring a revision of abyssal ocean theories.

30 1. Motivation

The abyssal ocean, below 2500 m, is a massive reservoir for climatically active tracers such 31 as carbon and heat. The rates at which heat is mixed and advected into the high capacity abyssal 32 ocean are key parameters in understanding both past climate reconstructions (e.g. Toggweiler et al. 33 1989) and future projections of climate change (e.g. Hansen et al. 1985). Similarly, the partitioning 34 of carbon between the deep ocean and the atmosphere is a major factor on millennial-scale climate change, whether natural (e.g. Sarmiento and Toggweiler 1984) or anthropogenic in origin (Archer et al. 1998). It is thus vital to have a firm phenomenological and dynamical understanding of the 37 abyssal ocean's mean state. 38 The general structure of the abyssal ocean circulation is easily inferred from surface buoyancy 39 fluxes and large-scale tracer properties (Sverdrup et al. 1942). Antarctic Bottom Waters, the densest oceanic waters, form in the Southern Ocean and fill the global abyssal oceans up to a depth of about 2500 m (Talley 2013a). They outcrop at the surface only in the Southern Ocean, where they experience a significant area-integrated buoyancy loss (Abernathey et al. 2016) and are converted 43 back into lighter waters by mixing with lighter overlying waters, resulting in a diabatic abyssal overturning circulation of O(15 Sy), where $1 \text{ Sy} = 10^6 \text{ m}^3 \text{s}^{-1}$. Non-linearities in the equation of state of seawater and geothermal heating at the seafloor are thought to play secondary roles in shaping this circulation (Emile-Geay and Madec 2009; de Lavergne et al. 2016a) and will be ignored in the conceptual models described below. 48 Classical theories for the abyssal ocean describe the steady state circulation and stratification of 49 a flat-bottom ocean forced by uniform turbulent mixing (Stommel 1957; Robinson and Stommel 1959; Stommel and Arons 1959b,a; Munk 1966). These theories remain pedagogically useful, 51

but are at best qualitative descriptions, as demonstrated for example by the fact that the direction

of the flow in the Stommel and Arons (1959b) solution changes sign when a sloping seafloor is introduced (Rhines 1993) and that the Munk (1966) solution does not satisfy the no-flux boundary condition at the seafloor. The classical view of a uniform mixing-driven upwelling is further 55 challenged by the observation that turbulent mixing is typically bottom-enhanced over rough topography (see MacKinnon et al. 2017 for a recent review), reversing the sign of the vertical flow 57 implied by the interior ocean vertical density balance (Polzin et al. 1997; Ferrari et al. 2016). Since Munk (1966), several approaches have been taken to address the limitations of classical 59 theories. First, boundary layer theories (Wunsch 1970; Thorpe 1987; Garrett 1990; Thompson and Johnson 1996) arose to elucidate the local behavior of mixing-induced flow along a sloping 61 and insulating sea floor. Second, the limitations of the Stommel and Arons (1959b) theory inspired a number of extensions to account for baroclinic structure (Kawase 1987; Pedlosky 1992), non-uniform seafloor depth (Rhines 1993), and/or non-uniform turbulent diffusivities κ (Marotzke 1997; Samelson 1998). Third, the observation of bottom-enhanced mixing motivated the development of progressively more sophisticated parameterizations of vertical (or diapycnal) turbulent diffusivities (Bryan and Lewis 1979; St. Laurent and Garrett 2002; Polzin 2009) which have 67 been subsequently implemented into general circulation models (Huang and Jin 2002; Jayne 2009; Melet et al. 2016). Fourth, the conundrum of interior downwelling implied by bottom-enhanced mixing was resolved by applying the watermass transformation framework to a downwelling interior layer of turbulent buoyancy flux divergence and an upwelling bottom boundary layer of turbulent buoyancy flux convergence, respectively (Ferrari et al. 2016; de Lavergne et al. 2016b; McDougall and Ferrari 2017). Despite the direct relevance of all of these approaches to the abyssal circulation, there has been little work done to unify them into a general theory of the abyssal circulation and stratification.

Building on the framework introduced by Callies and Ferrari (2018) (hereafter, CF18), we present a unified prognostic model of the circulation in an abyssal basin forced by bottom-enhanced mixing along a mid-ocean ridge. We modify the geometry, buoyancy forcing, and initial condition of the CF18 model to include the effects of a smooth mid-ocean ridge (with the effects of local roughness parameterized by bottom-enhanced mixing) and of a non-uniform background stratification on the circulation. Our approach is to formulate the simplest possible model which captures what we believe to be the key aspects of the problem: 1) the transformation of abyssal bottom waters into relatively lighter deep waters by bottom-enhanced mixing on the flanks of a mid-ocean ridge, 2) frictional processes acting on boundary currents, 3) restratification of abyssal mixing layers by baroclinic turbulence (crudely parameterized as a linear drag on the horizontal flow), and 4) bottom water formation in the Southern Ocean.

The general structure of the abyssal circulation that emerges from the model consists of layered
deep western boundary currents along the western continental slope which are connected by zonal
flows to watermass transformations driven by bottom-enhanced mixing along a mid-ocean ridge,
as schematized in Figure 1. The evolution of the interior stratification and the mixing layer watermass transformations are coupled by slope-normal exchange flows, with the vertically-varying
equilibrium stratification being determined by a combination of the mixing layer dynamics and the
formation of dense waters in the south. Finite net watermass transformations arise ubiquitously
along the flanks of the mid-ocean ridge, supported by vertical variations in the interior stratification, such that the crest of the mid-ocean ridge determines the vertical extent of the abyssal
overturning cell, in contrast to a previous constant-stratification interpretation in which finite net
transformations are confined to the base of topographic slopes (CF18).

The paper is structured as follows. Section 2 reviews the results of several theories of abyssal stratification and circulation in the literature. Section 3 presents the formulation of the Planetary

Geostrophic Circulation Model (PGCM) used to produce the simulation results presented in the paper. Section 4 describes the general structure of the abyssal circulation as it emerges in the 101 PGCM. In Section 5 we use local solutions to the one-dimensional boundary layer equations to 102 emulate the three-dimensional abyssal circulation in the PGCM. Section 6 describes the spin-up to 103 equilibrium of the vertical structure of abyssal interior stratification and its influence on watermass 104 transformations. Section 7 compares watermass transformations in our PGCM simulations with 105 estimates for the mid-ocean ridges of the Pacific, Atlantic, and Indian Ocean basins. Section 8 106 compares diagnostic estimates of abyssal upwelling from the watermass transformation framework with the classic vertical advection-diffusion framework and evaluates the relative contributions of 108 various physical terms of the watermass transformation. Section 9 discusses the implications of 109 our results, some key caveats, and some promising future directions.

2. Theoretical Background

a. Classical theories of abyssal stratification and circulation

Modern theories of the abyssal circulation begin with a series of papers by Stommel and Arons (1959b,a). In their theory, the circulation of a homogeneous abyssal layer is fed by high-latitude sources of abyssal water (diabatic downwelling) and driven by a uniformly-distributed sink (diabatic upwelling) of abyssal water. A uniform upwelling across the base of the thermocline is prescribed, inspired by the thermocline-thermohaline theory of Robinson and Stommel (1959). Munk (1966) further simplifies the Robinson and Stommel (1959) balance by restricting his attention to the deep ocean (i.e. below the thermocline) and by considering only vertical advection and diffusion,

$$u^{z}\partial_{z}b = \partial_{z}\left(\kappa\partial_{z}b\right),\tag{1}$$

where b is buoyancy, u^z is a uniform vertical velocity, κ is a uniform turbulent diffusivity. The Munk formulation allows exponential solutions which can be fit to the observed temperature profiles and combined with fits of an advection-diffusion-decay equation to radiocarbon profiles to yield the canonical estimate of deep ocean mixing $\kappa \simeq 10^{-4} \text{ m}^2 \text{s}^{-1}$ for a uniform upwelling of $u^z = 1.4 \times 10^{-7} \text{ m/s}$.

The horizontal abyssal circulation associated with the upwelling is described by Stommel and Arons (1959b,a): interior flow is geostrophically-balanced and its meridional component u^y is driven by vortex stretching, as shown by the vertically-integrated planetary-geostrophic vorticity balance

$$\beta U^{y} = f \frac{u_0^{z}}{H},\tag{2}$$

where H is the thickness of the abyssal layer, $u_0^z > 0$ is the upwelling across the base of the thermocline, f is the Coriolis parameter, $\beta > 0$ is the meridional gradient of the Coriolis parameter, and the vertically-integrated flow U^y is thus poleward in both hemispheres (see Pedlosky 1996 for an elucidating derivation). Inspired by the success of analogous theories for the wind-driven gyre circulation (Stommel 1948), Stommel and Arons (1959b,a) suppose the existence of a deep western boundary current in which frictional effects allow the current to deviate from geostrophy and return the interior flow such that the abyss conserves mass.

b. Turning ocean mixing upside down

The Stommel and Arons (1959b,a) and Munk (1966) theories rely on the existence of a uniform turbulent diffusivity $\kappa \simeq 10^{-4} \text{ m}^2 \text{s}^{-1}$, roughly an order of magnitude larger than the interior ocean mixing inferred from observations (Gregg 1989; Ledwell et al. 1993). While sufficiently vigorous mixing was eventually discovered deeper in the ocean near rough seafloor topography (Polzin et al. 1997; Ledwell et al. 2000; Sheen et al. 2013), the abyssal mixing problem only became

more complicated: applying the vertical advection-diffusion balance (eq.1) point-wise to mixing profiles $\kappa(z)\partial_z b$ that increase with depth implies diapycnal *downwelling*

$$u^{z} = (\partial_{z}b)^{-1}\partial_{z}(\kappa\partial_{z}b) < 0, \tag{3}$$

in contrast to the diapycnal *upwelling* required to balance diapycnal downwelling at high latitudes¹!

This apparent conundrum is resolved by considering the insulating boundary condition at a sloping seafloor, which causes buoyancy convergence and hence diapycnal upwelling in a thin bottom boundary layer (Polzin et al. 1997; Ferrari et al. 2016; de Lavergne et al. 2016b). In this framework, the abyssal overturning is the net effect of downwelling driven by bottom-enhanced mixing in a stratified mixing layer and upwelling driven by buoyancy convergence in a bottom boundary layer, which we collectively refer to as abyssal mixing layers (CF18).

c. A puzzling constraint from boundary layer theory

Bottom boundary layer theory (see review of Garrett et al. 1993) is a useful dynamical approach to the problem of flow driven by near-boundary mixing on a slope, which exerts a strong control on the basin-scale abyssal circulation (CF18). Following Thorpe (1987), who built on the approaches of Wunsch (1970) and Phillips (1970), we rotate the Boussinesq equations into slope coordinates and assume the flow depends only on the slope-normal coordinate z', which gives the simplified buoyancy equation (see derivation of full equation set in Section 5a):

$$\partial_t b' + u^{\chi'} N_0^2 \sin \theta = \partial_{z'} \left[\kappa \left(N_0^2 \cos \theta + \partial_{z'} b' \right) \right] \tag{4}$$

where $u^{x'}$ is the up-slope velocity, θ the slope angle, $\kappa = \kappa(z')$ the turbulent diffusivity, and we decompose the buoyancy field $b(x,y,z,t) = N_0^2 z + b'(x,y,z,t)$ into a background corresponding to

¹While the sign of the vertical velocity changes, we note that $\partial_z u^z > 0$ and thus the interior geostrophic flow driven by vortex stretching is still of the same sign as in the Stommel-Arons solution.

a constant stratification N_0^2 and a buoyancy anomaly b' = b'(z'). The boundary conditions are a noflux condition $\partial_{z'}b = \partial_{z'}b' + N_0^2\cos\theta = 0$ at the seafloor z' = 0 and decay conditions $\partial_{z'}u^{x'}, \partial_{z'}b' \to 0$ as $z' \to \infty$. At steady state, the boundary layer equation for the buoyancy anomaly (eq. 4) can be integrated from z' = 0 to $z' \to \infty$, which yields

for the net up-slope transport per unit length $\Psi_{\rm bg}=\int_0^\infty u^{x'}{\rm d}z',$ where $\kappa_{\rm bg}\equiv\kappa(z\to\infty)$ is the

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$$\Psi_{\rm bg} \equiv \kappa_{\rm bg} \cot \theta \tag{5}$$

background diffusivity. The simplicity of this integral constraint is surprising: the net up-slope transport depends only on the background turbulent diffusivity $\kappa_{\rm bg}$ and the slope angle θ , and is 168 independent of other environmental parameters which might be expected to influence diapycnal 169 transport, such as frictional parameters, the background stratification N_0^2 , the Coriolis parameter f, and the vertical structure of the turbulent diffusivity $\kappa(z)$. 171 Integrating the prediction Ψ_{bg} for the diapycnal transport per unit length along the perimeter 172 $L_{\rm global} \simeq 10^8$ m of the global mid-ocean ridge system (Callies 2018) for a typical ridge slope $\tan(\theta) = 2 \times 10^{-3}$ and a background diffusivity of $\kappa_{bg} \simeq 10^{-5} \ m^2 s^{-1}$ produces a global mixing-174 driven diapycnal overturning transport of $L_{\rm global} \kappa_{\rm bg} \cot \theta \simeq 0.5$ Sv, more than an order of magni-175 tude smaller than the observed abyssal diapycnal overturning transport of roughly 15 Sv (Lumpkin and Speer 2007). 177 CF18 resolve this conundrum by using the magnitude of the upwelling-downwelling 'dipole' 178 from boundary layer theory as a prediction for the net watermass transformation, since at the 179 base of topographic slopes the flows in and out of the boundary layers occur at different density 180 classes and thus drive a diabatic overturning. They find that the strictly upwelling transport in the 181 bottom boundary layer accurately predicts the scaling of the maximum net diapycnal overturning

transport, although the predicted overturning is unrealistically confined to the base of topographic slopes, where the constraints from one-dimensional boundary layer theory break down.

The integral constraint $\Psi_{bg} \equiv \kappa_{bg} \cot \theta$ (eq. 5) relies on the assumption of constant background

d. Boundary-interior exchange

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stratification N_0^2 and slope angle θ . By construction, none of the other terms are assumed to vary in the plane of the slope (x', y') either; it follows that there are no cross-slope convergences $\partial_{x'} u^{x'} = 0$ and hence no slope-normal exchange between the abyssal mixing layers and the interior, $u^{z'} = 0$ 189 (Wunsch 1970). 190 With a vertically varying stratification $N^2(z)$, however, variations in the buoyancy gradient project onto the cross-slope direction $x' = x\cos\theta + z\sin\theta$, introducing a second dimension to the 192 problem (e.g. Phillips et al. 1986; Salmun et al. 1991) and permitting both slope-normal exchange flows $u^{z'} \neq 0$ and a net diapycnal transport $\Psi_{\infty} \equiv \int_0^{\infty} u^{x'} dz' \neq \Psi_{bg}$. Heterogeneities can also arise due to cross-slope variations in the turbulent diffusivity $\kappa(x,y)$ or the slope angle $\theta(x,y)$ (Dell and 195 Pratt 2015), and have been argued to contribute significantly to oceanic watermass transformations (McDougall and Ferrari 2017; de Lavergne et al. 2017; Holmes et al. 2018). These additional heterogeneities are both kept relatively small by construction in our idealized model configuration to 198

e. Dynamics controlling the interior abyssal stratification

keep the focus on the effects of variations in the basin stratification.

The abyssal stratification is thought to be controlled by the combined effects of 1) diapycnal mixing in ocean basins and 2) the competing effects of winds and mesoscale eddies in setting the slope
of isopycnals in the Southern Ocean. Diapycnal mixing maintains the stable stratification of the
abyssal ocean by effectively diffusing buoyancy downwards, transforming dense abyssal waters

into lighter deep waters (Munk 1966). This vertical advection-diffusion model is an incomplete model of the abyssal stratification, however, as it omits the complementary process which closes 206 the overturning circulation by transforming light deep waters into denser abyssal waters. Munk 207 and Wunsch (1998) consider a heuristic correction to Munk (1966)'s vertical advection-diffusion equation for the effect of horizontal advection from regions of high mixing (or homogenization 209 by convection), which acts to restratify regions of weak mixing. A breakthrough in understanding 210 the abyssal stratification was the development of quasi-adiabatic theories of Southern Ocean circulation. In these theories, deep waters are upwelled adiabatically along sloping isopycnals in the Southern Ocean, are transformed into abyssal waters in the Southern Ocean mixed layer by a neg-213 ative surface buoyancy flux, and return to the abyss adiabatically along isopycnals (Marshall and Speer 2012, and references therein). The Southern Ocean isopycnal slope is determined by a bal-215 ance between wind stress and stirring by mesoscale eddies, which steepen and flatten isopycnals, 216 respectively (Marshall and Radko 2003).

Building on these two independent theories, Nikurashin and Vallis (2011) develop an idealized model which couples quasi-adiabatic Southern Ocean dynamics to a diabatic abyssal ocean basin and predicts the abyssal stratification and circulation, given only surface boundary conditions and mixing coefficients. For moderate diapycnal mixing of 10^{-5} m²s⁻¹ < κ < 10^{-3} m²s⁻¹, a regime applicable to both the Ocean and the model described here, the Nikurashin and Vallis (2011) model predicts that the interior abyssal stratification depends both on winds and eddies in the Southern Ocean and diapycnal mixing in the basin.

A promising aspect of zonally-integrated models of the meridional overturning circulation (e.g. Nikurashin et al. 2012; Thompson et al. 2016) is that they accurately reproduce the overturning and stratification exhibited by idealized "box"-geometry general circulation models. The emerging view, however, is that the abyssal circulation of the ocean is controlled by mixing layer flows

along sloping boundaries and thus that the commonly-used "box" geometry models may be a misleading point of reference for theories of the abyssal stratification and circulation (Ferrari et al. 2016). Building on CF18, we describe the formulation of an improved idealized general circulation model in a "bowl + ridge" geometry which accommodates the recent revisions to our theoretical understanding of the abyssal ocean circulation.

4 3. Planetary Geostrophic Circulation Model (PGCM)

The numerical model used here is the Planetary Geostrophic Circulation Model (PGCM) developed by CF18 to study how bottom-enhanced mixing on slopes drives an abyssal circulation. We
describe the key elements of our PGCM configuration below, which closely follows the exposition of CF18. The main differences between the present study and CF18 are the inclusion of the
mid-ocean ridge, the localization of vigorous bottom-enhanced mixing to a mid-ocean ridge, and
the generalization to vertically-varying interior stratifications. Readers familiar with the methods
of CF18 can skip Section 3 and simply consult Figure 2, which summarizes our changes to the
configuration.

243 a. Equations

The model solves the Navier-Stokes equations under the Boussinesq and planetary-scale geostrophic approximations, with parameterizations for the frictional and diabatic effects of unresolved solved processes, given by

$$f\mathbf{z} \times \mathbf{u} = -\nabla p + b\mathbf{z} - r(u^{x}\mathbf{x} + u^{y}\mathbf{y}), \tag{6}$$

$$\nabla \cdot \mathbf{u} = 0$$
, and (7)

$$\frac{\partial b}{\partial t} + \mathbf{u} \cdot \nabla b = \nabla \cdot (\kappa \nabla b) - \lambda(y)(b - B(z)), \tag{8}$$

where t is time; $\mathbf{x}, \mathbf{y}, \mathbf{z}$ are unit vectors pointing east, north, and up, respectively; $f = \beta y$ is the linearized Coriolis parameter (β -plane approximation); $\mathbf{u} = (u^x, u^y, u^z)$ is the velocity vector; p is the pressure divided by a reference density; b is the buoyancy; r is a frictional parameter; $\kappa = \kappa(x, y, z)$ is a spatially-dependent turbulent diffusivity; and $\lambda = \lambda(y)$ is a meridionally-varying restoring rate (see Section 3c). The system of equations (6) - (8), with appropriate initial and boundary conditions, yields a self-consistent and prognostic model of abyssal circulation and stratification.

The Boussinesq approximation filters out acoustic waves while the planetary-geostrophic ap-253 proximation filters out gravity waves and geostrophic turbulence. The resulting planetarygeostrophic equations are appropriate for basin-scale oceanic circulations and are typically used 255 for idealized studies of the abyssal circulation (e.g Pedlosky 1996, and references therein) and intermediate-complexity earth system models (e.g. Holden et al. 2016). While it is computation-257 ally and conceptually useful that the planetary-geostrophic equations filter out the effects of fast 258 waves and turbulence, the turbulent fluxes of these relatively small-scale flows are thought to 259 have leading order effects on abyssal mixing layers. We include their qualitative effects in the planetary-geostrophic formulation by way of two idealized parameterizations. 261

First, to include the effects of turbulent mixing produced by the local breaking of internal waves generated by flow over rough topography, we introduce a term for the turbulent buoyancy flux convergence $\nabla \cdot (\kappa \nabla b)$ to the buoyancy equation (e.g. as in St. Laurent and Garrett 2002). The imposed spatially-dependent turbulent diffusivity $\kappa(x,y,z)$ approximates the leading-order spatial structure described by observational estimates² (e.g. Polzin et al. 1997; Waterhouse et al. 2014) and is described in detail in Section 3c.

²Quantitatively similar profiles of turbulent kinetic energy dissipation are reproduced in simulations of internal wave turbulence above rough topography, wherein energy from a geostrophic mean flow (Nikurashin and Ferrari 2009) or the barotropic tide (Nikurashin and Legg 2011) is converted into unstable high-mode internal waves via a cascade of wave-wave interactions.

Second, to include the qualitative effects of isopycnal mixing by baroclinic turbulence in restratifying the abyssal mixing layers (Callies 2018) and in thickening western boundary currents

(e.g. Stommel 1948), we introduce a dissipative term to the momentum equation. Greatbatch
and Lamb (1990) show that introducing vertical momentum diffusion $\partial_z \left(v_{\text{eddy}} \, \partial_z \mathbf{u} \right)$ to the planetary geostrophic equations with an eddy viscosity $v_{\text{eddy}} = \kappa_{\text{GM}} f^2 / N^2$ is equivalent to introducing
isopycnal diffusion of potential vorticity with an effective isopycnal diffusivity of κ_{GM} (Gent and
McWilliams 1990). Following Salmon (1992), we simplify the dynamics further by using a linear
friction term (Rayleigh drag), $-r(u^x\mathbf{x} + u^y\mathbf{y})$ and scale the frictional parameter r according to the
Greatbatch and Lamb (1990) parameterization,

$$r = \kappa_{\text{GM}} \frac{f^2}{\delta^2 N^2} \approx 1.2 \times 10^{-5} \text{ s}^{-1},$$
 (9)

where we choose $\delta = 400$ m to be roughly the thickness of the abyssal mixing layers observed in the Brazil Basin (Callies 2018); typical abyssal mixing layer values of $f = 5 \times 10^{-5} \text{ s}^{-1}$ and $N^2 =$ $5 \times 10^{-7} \ {\rm s}^{-1}$; and in the absence of observational or theoretical constraints assume $\kappa_{\rm GM} = 100$ m²s⁻¹, which yields a value $v_{eddy} = 0.5 \text{ m}^2\text{s}^{-1}$ similar to the value $v_{eddy} = \sigma \kappa_{bot} = 0.4 \text{ m}^2\text{s}^{-1}$ proposed by Callies (2018) and Holmes et al. (2019), where σ is the turbulent Prandtl number. We use a constant r since the parameterization is meant to be a crude placeholder for boundary 282 layer restratification. To our relief, supplementary sensitivity experiments showed that watermass 283 transformations and the boundary layer structure are relatively insensitive to the friction parameter r, in agreement with CF18. The linear drag parameter is small enough that the frictional terms 285 are negligible in the interior where the flow is approximately geostrophic and are important only 286 in near-boundary flows (both the deep western boundary currents and the abyssal mixing layers along the mid-ocean ridge) where the horizontal velocities are large (Salmon 1992, CF18). The 288 choice of $r = 1.2 \times 10^{-5} \text{ s}^{-1}$ gives a non-dimensional value $\hat{r} = \frac{r}{\beta L} = 0.1$ such that the width of the Stommel and Arons (1959b,a) deep western boundary currents is one-tenth the domain width (see Section 3d).

b. Geometry and boundary conditions

We configure the PGCM to approximate the leading-order structure of a typical cross-293 hemispheric abyssal ocean basin with a rectangular basin of zonal width L = 3000 km and meridional length 2L = 6000 km. Our idealized basin contains a mid-ocean ridge caused by seafloor 295 spreading in the middle and is bounded in the west, east, and north by continental slopes (Figure 296 2a). Although the southern region in our configuration (y < -L/2 = -3000 km) is also zonally bounded, it should be thought of as a Southern Ocean-like sponge layer. In this southern region, 298 the transformation of deep waters into bottom waters arising from complex circumpolar channel 299 dynamics (e.g. as described in Marshall and Speer 2012) are parameterized by an idealized buoyancy restoring forcing which pins the buoyancy field to a reference vertical profile (described in 301 detail in the next Section 3c). The model extends from z = -2500 m at the upper boundary to a 302 maximum depth of z = -5000 m and should be interpreted as representing only the diabatic lower cell of the meridional overturning circulation. The idealized configuration can be thought to apply 304 locally to the Atlantic, Pacific, and Indian Ocean basins below z = -2500 m, which in the present 305 climate are all bounded by topography in the west, east, and north and have roughly meridionallyaligned mid-ocean ridges (e.g. those highlighted in Figure 12). The idealized continental slopes 307 are half-Gaussian and the mid-ocean ridge is Gaussian in the zonal direction and tapers down 308 to zero meridionally in the southern restoring region to allow unconstrained zonal flows to close the circulation of interest in the diffusively-forced basin to the north. The characteristic seafloor 310 slopes of roughly $\tan(\theta_{ridge}) \simeq 2 \times 10^{-3}$ for the mid-ocean ridge and $\tan(\theta_{cont.}) \simeq 4 \times 10^{-3}$ for the 311 continental slope are inspired by the South Atlantic, where the abyssal mixing layers and largescale abyssal circulation are best constrained by existing observations (Hogg et al. 1982; Polzin et al. 1997; Ledwell et al. 2000; St. Laurent et al. 2001; Thurnherr et al. 2005). The PGCM is bounded from above by assuming isopycnals are flat, i.e. b = 0 at z = -2500 m, which is approximately valid in all basins north of the Southern Ocean (Talley 2007; Koltermann et al. 2011; Talley 2013b). The PGCM is bounded from below by an insulating seafloor, $\mathbf{n} \cdot \nabla b = 0$ at z = -d(x, y), where d(x, y) is the seafloor depth and \mathbf{n} is the unit vector normal to the boundary.

319 c. Buoyancy forcing

The abyssal circulation in our model is forced by two competing diabatic terms in the buoyancy equation: minus the divergence of the turbulent buoyancy flux $-\nabla \cdot (-\kappa \nabla b)$, which has a
positive integral contribution (diapycnal upwelling); and restoring to a reference buoyancy profile $-\lambda(b-B)$, which must necessarily have a negative integral contribution (diapycnal downwelling). Available potential energy is produced by parameterized turbulent mixing and converted
into kinetic energy via the buoyancy production term $u^z b$ to drive a planetary-geostrophic abyssal
circulation and balance the available potential energy loss due to restoring.

327 (i) Turbulent mixing

The prescribed turbulent diffusivity $\kappa = \kappa(x,y,z)$ is everywhere bottom-enhanced with a contribution equal to $\kappa_{\rm bot} \exp\{-(z+d)/h\}$ over the mid-ocean ridge, where we choose $\kappa_{\rm bot} = 5 \times 10^{-3}$ m²s⁻¹ and h = 250 m to roughly match observations in the Brazil Basin (Figure 11). The bottom-enhanced contribution to κ is reduced by a factor of 20 to $\frac{\kappa_{\rm bot}}{20} \exp\{-(z+d)/h\}$ over the continental slopes to reflect the observed weakness of local wave-driven turbulence over smooth continental slopes (Figure 11 and Polzin et al. 1997). A uniform weak background diffusivity $\kappa_{\rm bg} = \frac{\kappa_{\rm bot}}{200} = 2.5 \times 10^{-5} \, {\rm m}^2 {\rm s}^{-1}$ is added to stabilize the numerical solution, yielding a total diffusivity

sivity distribution

$$\kappa(x, y, z) = \kappa_{\text{bg}} + \begin{cases}
\kappa_{\text{bot}} \exp\{-(z + d(x, y))/h\}, & \text{if } L/2 < x < 3L/2 \text{ (mid-ocean ridge)} \\
\frac{\kappa_{\text{bot}}}{20} \exp\{-(z + d(x, y))/h\}, & \text{else (continental slopes)},
\end{cases}$$
(10)

with a smoothing function applied over a horizontal distance of L/10 near the transitions at x = L/2 and x = 3L/2. The net effect of this prescribed mixing is to power a diabatic upwelling along the mid-ocean ridge, where mixing is vigorous.

339 (ii) Buoyancy restoring in the southern restoring region

The prescribed restoring rate λ is has a meridional dependence

$$\lambda(y) = \lambda_0 \left[0.5 \left(1 - \tanh\left(\frac{y + L/2}{10L}\right) \right) \right],\tag{11}$$

which is equal to $\lambda_0 \simeq (10 \text{ years})^{-1}$ in the southern restoring region and vanishes rapidly northwards, $\lambda \to 0$ as y > -L/2. The prescribed restoring rate is chosen based on the baroclinic ad-342 justment timescale given by a lateral diffusive timescale $\tau_{SO} = L_{SO}^2/\kappa_{GM} = \frac{(10^6 \text{ m})^2}{3000 \text{ m}^2 \text{s}^{-1}} \simeq 10 \text{ years},$ determined for an isopycnal diffusivity $\kappa_{GM} \simeq 3000~\text{m}^2\text{s}^{-1}$ (Abernathey et al. 2013) and a Southern Ocean of width $L_{SO} \simeq 1000$ km. This restoring rate is much faster than the vertical diffusive 345 timescale which spins up the overturning circulation $au_{
m mix}=H^2/\overline{\kappa}\simeq 1000$ years, where H=2500346 m is the maximum thickness of the abyssal ocean and $\overline{\kappa} \simeq 10^{-4}~\text{m}^2\text{s}^{-1}$ is the volume-weighted mean diffusivity in the basin. Thus, the stratification in the southern restoring region does not 348 deviate much from the prescribed profile (see Figure 7). The net effect of this parameterized 349 buoyancy forcing in the southern restoring region is to transform deep waters into bottom waters (diabatic downwelling) to balance the transformation of bottom waters into deep waters (diabatic 351 upwelling) driven by mixing along the mid-ocean ridge in the basin to the north. In contrast to 352 CF18, we allow reference buoyancy profiles B(z) corresponding to vertically-varying stratification

 $\partial_z B = N^2(z)$, complicating the interpretation of the solution in terms of one-dimensional boundary layer dynamics which require a constant interior stratification N_0^2 .

d. Dimensional parameters and scaling

While the PGCM is discussed in dimensional terms, the PGCM is formulated and implemented non-dimensionally. The following dimensional scales, 358

$$L=6000 \text{ km}$$
 (basin width),
 $H=2500 \text{ m}$, (abyssal ocean vertical extent),
 $\beta=2\times 10^{-11} \text{ m}^{-1} \text{s}^{-1}$, (meridional gradient of Coriolis parameter),
 $N^2=1.5\times 10^{-6} \text{ s}^{-2}$, (reference stratification at $z=-2500 \text{ m}$),
 $\kappa_{bot}=5\times 10^{-3} \text{ m}^2 \text{s}^{-1}$, (diffusivity at the mid-ocean ridge seafloor),
 $r=1.2\times 10^{-5} \text{ s}^{-1}$, (frictional parameter),

are used to non-dimensionalize the system, with the coordinate transformation

$$x = L\hat{x}, \quad y = L\hat{y}, \quad z = H\hat{z} \tag{12}$$

and the substitutions

$$t = \frac{\beta L^3}{N^2 H^2} \hat{t},$$
 $b = N^2 H \hat{b},$ $p = N^2 H^2 \hat{p},$ (13)

$$t = \frac{\beta L^{3}}{N^{2}H^{2}}\hat{t}, \qquad b = N^{2}H\hat{b}, \qquad p = N^{2}H^{2}\hat{p}, \qquad (13)$$

$$u^{x} = \frac{N^{2}H^{2}}{\beta L^{2}}\hat{u}^{\hat{x}}, \qquad u^{y} = \frac{N^{2}H^{2}}{\beta L^{2}}\hat{u}^{\hat{y}}, \qquad u^{z} = \frac{N^{2}H^{3}}{\beta L^{3}}\hat{u}^{\hat{z}}. \qquad (14)$$

For reference, the non-dimensional time $\hat{t}=1$ corresponds to $t=\tau\simeq 10$ years, where $\tau\equiv$ $\beta L^3/N^2H^2$. While the basin scale circulation takes a long time $\tau_{\rm mix} = H^2/\overline{\kappa} \simeq 1000$ years $\gg \tau$ to spin up, the abyssal mixing layers are spun up on a fast timescale $au_{BL}=q^{-2}/\kappa_{bot}\simeq 1$ year $\ll au,$ where

$$q^{-1} = \sqrt{\frac{\kappa_{\text{bot}}(f^2 + r^2)}{rN^2 \tan^2 \theta}} \simeq 400 \text{ m}$$
 (15)

is the thickness of the mixing layer predicted by 1D theory (CF18), $\kappa_{bot} = 5 \times 10^{-3} \text{ m}^2/\text{s}$ is the diffusivity at the seafloor, and $f = \beta L/2$ is a representative value of the Coriolis parameter.

The non-dimensionalized equations (see CF18) depend only on the non-dimensional parameters

$$\hat{\alpha} = \frac{H}{L}, \quad \hat{\kappa} = \frac{\kappa \beta L^3}{N^2 H^4}, \quad \hat{r} = \frac{r}{\beta L}, \tag{16}$$

where $\hat{\alpha}$ is the aspect ratio of the basin; $\hat{\kappa} = \tau/\tau_{\rm mix}$ is the ratio of the cross-basin propagation timescale of long Rossby waves (with $f = \beta L$)

$$\tau \equiv L/c_g = L/\frac{\beta L^{-2}}{(NH/f)^2} = \frac{\beta L^3}{N^2 H^2},\tag{17}$$

to the diffusive spin-up timescale $\tau_{\rm mix} \equiv H^2/\overline{\kappa}$. \hat{r} is the ratio of the Stommel (1948) western 370 boundary layer width r/β to the basin width L. Since the prescribed κ is spatially-dependent, the non-dimensional diffusivity \hat{k} inherits its spatial dependence in the numerical implementation. Scaling κ by using the volume-weighted average value $\overline{\kappa}$ in τ_{mix} gives $\hat{\kappa} = \tau/\tau_{mix} \simeq 0.01$. 373 Because the imposed turbulent diffusivity is isotropic, the small aspect ratio $\hat{\alpha} \sim 5 \times 10^{-4}$ re-374 sults in a non-dimensionalized horizontal diffusivity many orders of magnitude smaller than the non-dimensionalized vertical diffusivity, which is difficult to implement numerically. Instead, 376 we artificially increase the horizontal diffusivity for numerical stability by increasing the as-377 pect ratio parameter to $\hat{\alpha} = 0.2$. This parameter only enters in the horizontal diffusion term $\hat{\alpha}^2 \left[\partial_{\hat{x}} \left(\hat{\kappa} \partial_{\hat{x}} \hat{b} \right) + \partial_{\hat{y}} \left(\hat{\kappa} \partial_{\hat{y}} \hat{b} \right) \right]$ (CF18) and remains small enough that it does not qualitatively affect the results presented here, as evidenced by the negligible role of horizontal buoyancy fluxes 380 in the watermass transformations (Figure 5).

e. Numerical implementation

The model is formulated in terrain-following coordinates to accurately resolve the thin mixingdriving flows along the sloped bottom boundary. The numerical implementation is described in

CF18. The Julia (Bezanson et al. 2017) implementation is available at https://github.com/

joernc/pgcm. The input files, output files, and post-processing notebooks necessary to replicate the study are available at https://github.com/hdrake/AbyssalFlow (Drake 2020).

4. Abyssal Circulation Controlled By Mixing Layer Dynamics

We begin by describing the general structure of the abyssal circulation at equilibrium in the PGCM, i.e. at $\hat{t}=50$ or $t\simeq 500$ years $\simeq \tau_{\rm mix}$, when buoyancy tendencies have become sufficiently small (Figure 7a). The stratification in the PGCM solution presented in this section is restored to an exponential profile with a decay scale of $\delta=1000$ m in the southern region (solid red dashed line in Figure 2), which exhibits vertical variations of similar magnitude to those observed in the Southern Ocean (black solid line). This is arguably our most "realistic" simulation of the abyssal ocean and hereafter we refer to it as PGCM-REAL.

396 a. Abyssal Mixing Layers and Deep Western Boundary Currents

Figure 3 (a-c) shows the three Cartesian components of the abyssal flow field along a zonal sec-397 tion 3000 km north of the equator. In the abyssal mixing layers spanning both flanks of the midocean ridge, buoyancy surfaces plunge to intersect the seafloor at a right angle (visually distorted 399 by the aspect ratio) to satisfy the no-flux boundary condition. As expected from 1D theory (CF18), 400 the boundary flows are thicker and stronger over the mid-ocean ridge where mixing is strong than over the continental slopes where mixing is weak. In the bottom boundary layer (BBL), plung-402 ing buoyancy surfaces drive frictionally-balanced upwelling (Figure 3c) and frictional-geostrophic 403 flow opposite the direction of Kelvin wave propagation (Figure 3b), i.e. anti-cyclonic in the northern hemisphere. In the stratified mixing layer (SML) just above the BBL, buoyancy surfaces are 405 at leading order flat and the bottom-enhanced mixing drives downwelling (Figure 3c), as expected 406 from the vertical advection-diffusion balance (eq. 3) reviewed in Section 2.

Net diapycnal upwelling in the Northern Hemisphere can be inferred from the meridional flow 408 field at the equator: dense bottom waters flow into the northern hemisphere and relatively lighter 409 deep waters flow out (Figure 3e). Since the Coriolis force vanishes at the equator, the buoyant force 410 associated with the bending of buoyancy surfaces to satisfy the bottom-boundary condition can only be balanced by a cross-slope frictional flow (Figure 3d,f) and any along-slope flows associated 412 with the abyssal mixing layers vanishes (compare Figure 3e to Figure 3b). The only meridional 413 flow are Stommel (1948)-like deep western boundary currents (DWBC) along the continental slope 414 on the western side of the domain and the eastern flank of the ridge (Figure 3e). In this particular configuration, a southward-flowing DWBC develops on the eastern flank of the ridge near its crest 416 and is much weaker than the DWBC on the western continental slope. The southward DWBC on the ridge is relatively intensified in simulations with a taller ridge.

b. Depth-integrated and Overturning Circulations

The global abyssal circulation is more intuitively visualized by considering the three Cartesian streamfunctions that describe the flow, which we compute by integrating the u^x , u^y , and u^z velocities in x, y, and z, respectively³ (Figure 4). Figure 4b shows the familiar streamfunction for the meridional overturning circulation (MOC) in the y-z plane, which should be thought of as corresponding to the lower-cell of the global MOC. This circulation has a strength of about 1.6 Sv at the equator, with water 1) downwelling diabatically in the southern restoring region, 2) flowing northwards to fill the abyssal depths, 3) gradually upwelling along the length of the basin, and 4) returning to the southern restoring region to close the circulation. We note in particular that the

³Integrating the continuity equation in $\frac{\partial u^x}{\partial x} + \frac{\partial u^y}{\partial y} + \frac{\partial u^z}{\partial z} = 0$ along any of the three directions x, y, or z and imposing the no-normal flow boundary condition yields an equation of the form $\int \left(\frac{\partial u^{x_1}}{\partial x_1} + \frac{\partial u^{x_2}}{\partial x_2} + \frac{\partial u^{x_3}}{\partial x_3} \right) dx_3 = \frac{\partial U^{x_1}}{\partial x_1} + \frac{\partial U^{x_2}}{\partial x_2} = 0$, where x_1, x_2, x_3 are permutations of x, y, z, $U^{x_1} = \int u^{x_1} dx_3$ and $U^{x_2} = \int u^{x_2} dx_3$. The resulting non-divergent flow field can then be expressed as a streamfunction ψ_3 defined by $\mathbf{U} = U^{x_1} \mathbf{x}_1 + U^{x_2} \mathbf{x}_2 = (-\nabla \times \psi_3 \mathbf{x}_3)$.

MOC extends all the way from the ocean seafloor to the top of the mid-ocean ridge, in contrast to the MOC in the CF18 framework, in which significant overturning is confined to the base of topographic slopes (see Section 6c for a discussion on the role of the ridge height in setting the vertical extent of the MOC).

The up- and down-welling in the abyssal mixing layers is evident in the zonal overturning 432 streamfunction in the x-z plane, which shows upwelling in a thin BBL and broader downwelling 433 in the SML above (Figure 4c). The upwelling in bottom boundary layers is confined to the two 434 flanks of the mid-ocean ridge, where mixing is vigorous and bottom-enhanced, and is negligible over the weakly-mixed continental slopes. In this case, the upwelling and downwelling transports 436 are equal and opposite in strength, i.e. the circulation closes, because the downwelling flow in-437 cludes both the residual diabatic upwelling along the ridge as well as the net diabatic downwelling by the restoring condition in the southern region, which is concentrated on the eastern continental 439 slope. Nonetheless, the zonal overturning streamfunction provides a qualitative sense of the zonal overturning circulations driven by mixing layer dynamics along the mid-ocean ridge. 441

The depth-integrated circulation in our simulations stands in contrast to that of Stommel and 442 Arons (1959a)'s barotropic model and is the expression of a combination of various baroclinic 443 deep western boundary currents and mixing layer flows (Figure 4a). Within 2000 km of the equator, the northward and southward components of the deep western boundary currents alternatively 445 dominate (compare with the meridional velocity at the equator in Figure 3). North of y = 2000 km, 446 the depth-integrated circulation is dominated by the along-slope flow in the bottom boundary layer, which is opposite the direction of Kelvin wave propagation. The depth-integrated circulation is 448 strongly influenced by mixing layer dynamics, both near the boundaries and in the interior, and 449 is structurally distinct from that predicted by the linear response to vortex stretching alone (Stommel and Arons 1959b; Pedlosky 1992; Cember 1998). Sverdrup balance only holds far from the 451

boundaries and accounts for little of the net transport compared to the abyssal mixing layer and western boundary current flows, where friction is important.

454 c. Partially-Compensating Watermass Transformations

The watermass transformation represents the net flow across a buoyancy surface driven by diabatic forcing. Watermass transformation in the PGCM is driven by: 1) bottom-enhanced turbulent mixing (positive in the net) and 2) restoring to a reference buoyancy profile in the southern
restoring region (negative in the net). In the northern hemisphere, the restoring rate vanishes by
construction and watermass transformation is dominated by the mixing-driven component. Its
calculation, following Walin (1982) and Ferrari et al. (2016), is given by

$$T(b) = \frac{\partial}{\partial b} \int_{V_{b' < b}} \nabla \cdot (\kappa \nabla b') dV, \tag{18}$$

where $V_{b' < b}$ is the volume of water less buoyant than b. Watermass transformation is conveniently 461 expressed in units of volumetric transport (m³/s) and can be decomposed into various contributions. When applied to regions of bottom-enhanced mixing in the abyss, it is informative to de-463 compose the net watermass transformation into the typically negative contribution (balanced by 464 diapycnal downwelling) in the SML and the typically positive contribution (balanced by diapycnal upwelling) in the BBL (e.g. Ferrari et al. 2016; McDougall and Ferrari 2017). For the purposes 466 of watermass transformation calculations in this paper, we define the BBL as the layer with a 467 convergent buoyancy flux, $\nabla \cdot (\kappa \nabla b) > 0$, which extends upwards from the seafloor to the level at which buoyancy flux attains its maximum magnitude; the remainder of the ocean is considered 469 the SML and is dominated by a buoyancy flux divergence, $\nabla \cdot (\kappa \nabla b) < 0$. For convenience, all 470 watermass transformations in this paper are computed in buoyancy space and remapped into depth space according to the average depth of buoyancy surfaces,

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i.e.

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$$\bar{z}(b) = \frac{1}{A(b)} \int z(b) dA, \tag{19}$$

against the fixed depths of topographic features in the ocean.

The net northern hemisphere watermass transformation of $T_{\rm net} = 1.6$ Sv at 3750 m (Figure 5a),

where it reaches its maximum, is consistent with the depth and magnitude of the maximum of

the MOC streamfunction at the equator (Figure 4b). The net watermass transformation $T_{\rm net} = T_{\rm BBL} + T_{\rm SML} = 1.6$ Sv (black line) is the residual of a positive contribution of $T_{\rm BBL} = 2.1$ Sv from

the BBL (red line) and a negative contribution of $T_{\rm SML} = -0.5$ Sv from the SML (blue line), both

of which are dominated by the vertical component of the buoyancy flux divergence (dashed lines),

which facilitates comparison across simulations with dramatically different stratifications and

$$T(b) = \partial_b \int_{V_{b' < b}} \nabla \cdot (\kappa \nabla b') dV \simeq \partial_b \int_{V_{b' < b}} \partial_z (\kappa \partial_z b') dV.$$
 (20)

Virtually all of this transformation occurs on the flanks of the mid-ocean ridge (compare Figure 5a,b).

For the convenience of being able to ignore meridional variations in the basin geometry (and their effects on watermass transformations via the "perimeter" effect, as described by Holmes et al. 2018), we limit the remaining discussion to a domain from L/2 < x < 3L/2 and 0 < y < L/2 along the north-hemisphere mid-ocean ridge, which is responsible for roughly 1 Sv of the full basin's transformation (Figure 5c; limited domain outlined in Figure 2a).

The net watermass transformation $T_{\rm net} = 1$ Sv at equilibrium is much larger than the $L\Psi_{\rm bg} \le$ 0.1 Sv predicted by the integral constraint (eq. 5) from 1D boundary layer theory. To clarify the discrepancy between the watermass transformations that emerge from the 3D PGCM and the

watermass transformations predicted by 1D dynamics, we emulate the 3D PGCM simulation by solving the 1D boundary layer equations locally and interpolating onto the 3D PGCM grid.

5. Emulating the 3D PGCM with local 1D boundary layer models

495 a. Boundary layer theory

Following CF18, we transform the planetary-geostrophic equations (6) - (8) from the Cartesian coordinates (x, y, z) to a coordinate system (x', y', z') aligned with an infinitely extending sea floor at $z = x \tan \theta$, with slope angle θ , and ignoring the southern region restoring condition on buoyancy.

The transformation is given by $x' = x \cos \theta + z \sin \theta$, y' = y, $z' = -x \sin \theta + z \cos \theta$. Buoyancy b = B(z) + b' is decomposed into a background B(z) with constant stratification $\partial_z B = N_0^2$ and an anomaly b'(z'). The steady state boundary layer equations are thus given by:

$$-f\cos\theta u^{y'} = b'\sin\theta - r\cos\theta^2 u^{x'} \tag{21}$$

$$f\cos\theta u^{x'} = -ru^{y'} \tag{22}$$

$$u^{x'}N_0^2\sin\theta = \partial_{z'}\left[\kappa\left(N^2\cos\theta + \partial_{z'}b'\right)\right],\tag{23}$$

with a no-flux boundary condition $\partial_{z'}b' + N_0^2\cos\theta = 0$ at the seafloor z' = 0 and decay conditions $\partial_{z'}u^{x'}, \partial_{z'}u^{x'}, \partial_{z'}b' \to 0$ as $z' \to 0$. These equations yield exact analytical solutions for constant κ (CF18) and approximate analytical solutions for elementary $\kappa(z)$ profiles (Callies 2018).

505 b. Emulator setup

We emulate the PGCM solution by using finite differences to solve the time-dependent boundary-layer equations (21) - (23) with the local Coriolis parameter f(y) and slope angle $\theta(x,y)$ at each $(x,y)=(\xi,\eta)$ of the PGCM grid, which is a sensible approach given that the parameters f(y) and f(y) and f(y) vary on scales larger than the those of the boundary-layer solutions (Dell and Pratt

2015). Since these local boundary layer solutions are given in terms of the local slope-normal direction z' rather than the true vertical direction z, we project the solution onto the true vertical direction z with the substitution $z' \to z/\cos\theta$ and linearly interpolate from the projected z-levels of the boundary layer solution to the PGCM's local σ -levels. This process provides an emulator of the PGCM which is purely the result of local 1D dynamics but is re-gridded to the same grid as the 3D PGCM and can thus be directly compared.

16 c. Emulator evaluation

We evaluate the emulator against the spin-up of a PGCM simulation with a constant stratification 517 initial condition N_0^2 , hereafter PGCM-CONST. The 1D emulator accurately reproduces the initial spin-up of buoyancy and velocity fields of the PGCM-CONST simulation along most of the mid-519 ocean ridge flanks, but fails at the top and bottom of the ridge where the topographic curvature is 520 large and the cross-slope convergences omitted by 1D dynamics become important (Figure 6a,b). 521 As the solution nears equilibrium, however, the interior basin stratification drifts away from its 522 constant initial value (compare gray and black contours in Figure 6d) and the boundary layer flows 523 diverge from the 1D emulator's prediction (Figure 6c,d). This is expected, as the basin stratification of PGCM-CONST is allowed to evolve in response to the 3D circulation while the background 525 interior stratification N_0^2 is a constant parameter in the emulator. Relative to the emulator, the 526 equilibrium PGCM-CONST solution exhibits reduced downwelling in the SML and enhanced upwelling in the BBL, both of which contribute to enhancing the net diapycnal upwelling. In 528 Section 6, we use the 1D emulator to identify properties of the watermass transformations in the 529 PGCM that can be explained by one-dimensional dynamics alone.

6. The Effect of Variable Interior Stratification on the Abyssal Circulation

a. What sets the abyssal stratification?

In our PGCM simulations, the drift of interior buoyancy surfaces over time (Figure 6d) suggests 533 that the interior stratification at equilibrium may differ substantially from the stratification of the 534 southern region buoyancy profile. Figure 7a shows the temporal evolution of the horizontally-535 averaged vertical stratification profile, averaged over the northern hemisphere basin in the PGCM, where darker greys represent later times. In PGCM-CONST, the abyssal stratification develops 537 substantial vertical structure in the basin over time, despite being rapidly restored back to a con-538 stant stratification in the southern restoring region (solid lines, Figure 7a). Net watermass transformation is initially unbalanced by Eulerian diapycnal flow (compare Figure 8b,f) and thus drives 540 changes in the volume of buoyancy layers, which can be interpreted as a component of the diapy-541 cnal transport due to the velocity of buoyancy surfaces (Marshall et al. 1999). Excess watermass transformations near the base of the slope destroy the densest layers and expand the deep layers, which translate into a reduction of the stratification that originates at the bottom of the ridge and 544 propagates upwards over time. The details of the vertical structure of the equilibrium basin stratification depend on ridge height (not shown), but in all cases the basin stratification increases from 546 zero at the maximum depth (imposed by the no-flux condition at the flat bottom) up to near the 547 restoring reference value of N_0^2 at the top boundary. The zonal-mean basin stratification develops a significant meridional structure, wherein the 549

The zonal-mean basin stratification develops a significant meridional structure, wherein the zonal-mean stratification along the ridge weakens with distance from the Southern restoring region (Figure 7b,c). In contrast to the mixing layer stratification, which is strongest at the equator and weaker polewards (Callies 2018, CF18), the zonal-mean stratification decreases roughly monotonically with increasing latitude.

Simulations using a reference buoyancy profile that corresponds to an exponential stratification 554 with decay scale of $\delta = 1000$ m exhibit much less drift in their stratifications over time (dashed 555 lines, Figure 7a,b). Although the equilibrium basin stratifications in all of the different PGCM 556 experiments develop vertical structure, there does not seem to be a single preferred equilibrium 557 stratification that depends only on the mixing: both the geometry of the abyssal topography and the restoring profile in the southern restoring region influence the interior stratification at equilibrium. 559

We begin by considering the case of transient spin-up from a reference buoyancy profile with

b. Effect of variable stratification on watermass transformations 560

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constant stratification N_0^2 , PGCM-CONST. It is useful to consider the evolution of the PGCM during its initial spin-up ($\hat{t} \simeq \tau_{\rm BL}/\tau = 0.1$) when only mixing layer dynamics are relevant and the solution is thus well-predicted by the 1D Emulator (Figure 6). Figure 8a shows the water-564 mass transformations in the 1D Emulator at $\hat{t} = 0.1$, which almost exactly predicts the watermass 565 transformations in the full 3D PGCM (Figure 8b). Between -4200 m < z < -3000 m, where the slope of the mid-ocean ridge is roughly constant, 567 the near-boundary flow exhibits a vanishingly small net transport (solid black line in Figure 8a), 568 which is approximately equal to the integral constraint $T_{\text{net}} \simeq L\Psi_{\text{bg}} = L\kappa_{\text{bg}} \cot \theta \leq 0.1 \text{ Sv predicted}$ by 1D boundary layer theory (dashed black line in Figure 8a). This vanishingly small net transport 570 is the result of large positive transformation $T_{\rm BBL}$ (diabatic upwelling, in red) in the BBL and 571 almost-as-large negative transformation T_{SML} (diabatic downwelling, in blue) in the SML. Below z = -4200 m, at the base of the topographic slope, abyssal bottom waters feed the upwelling in the 573 BBL and the maximum net watermass transformation is well predicted by the strictly upwelling 574 transport in the bottom boundary layer from 1D theory (Figure 8a,b), as suggested by CF18.

For the spin-up from a reference stratification that increases exponentially with height (as is al-576 most ubiquitously the case in the abyssal ocean), the integral constraint (eq. 5) no longer holds at 577 $\hat{t} = 0.1$ and the solution already exhibits a net transformation much larger than $L\Psi_{\rm bg}$ at all depths 578 from the base of the slope to the ridge crest (Figure 8c,d). The increase in the net transformation, which spans the full vertical extent of the ridge, is primarily due to a decrease in the downwelling 580 in the SML which, in the extreme case of an exponential scale height of $\delta = 500$ m for the restor-581 ing stratification, vanishes completely (Figure 8d). The strongly positive net transformation is 582 primarily due to the buoyancy convergence driven by the rapid increase of the initial stratification with height, i.e. $\kappa \partial_{zz} B > 0$ reduces the divergence $\nabla \cdot (\kappa \nabla b) < 0$ due to $\partial_z \kappa < 0$ in the SML (see 584 also Figure 14).

As these solutions reach equilibrium, they retain a finite net transformation at all depths from 586 the base of the slope to the ridge crest, slightly reduced by gradually strengthening negative trans-587 formations in the SML (compare Figure 8g,h to Figure 8c,d). At equilibrium, we find the degree 588 of compensation near the ridge crest depends on the vertical scale over which the restoring stratification varies (within a range applicable to the ocean): the more rapidly the stratification increases 590 with height, the less upwelling in the BBL is compensated by downwelling in the SML (Figure 8f-591 h and Figure 9a). In contrast, upwelling in the BBL is remarkably invariant to vertical variations in 592 the stratification and remains a reasonable prediction for the maximum net transformation (Figure 593 9a,b), which occurs at the base of the slope where the compensating downwelling contribution 594 from the SML vanishes (Figure 9c). Thus, while the maximum net watermass transformation is accurately predicted by upwelling in the BBL alone, the vertical structure and extent of watermass 596 transformations depend also on downwelling in the SML, which itself is strongly dependent on 597 the vertical stratification, and is not predicted by 1D theory.

c. Vertical extent of overturning set by ridge height

We have shown that most of the watermass transformation occurs within abyssal mixing layers along the mid-ocean ridge (Figure 5a,b). We further hypothesize that variations in the height of 601 the ridge modulate the vertical extent of abyssal watermass transformations and thus the vertical 602 extent of the abyssal overturning cell. We test this hypothesis by running variations of the PGCM-603 CONST where we vary the ridge height from 500 m to 2000 m, in increments of 500 m. In the initial spin-up, largely compensating positive and negative transformations develop in the BBL 605 and SML, respectively, from the base of the ridge slope up to the ridge crest (Figure 10a-d). The 606 net transformation below the ridge crest vanishes according to the integral constraint (eq. 5), 607 except near the sea-floor where bottom water feeds into the BBL. At equilibrium, however, the 608 stratification drifts away from its constant reference state (e.g. Figure 7) and permits a finite net 609 transformation (Figure 10e-h), which spans the full vertical extent of the ridge. The result that the vertical extent of the abyssal MOC follows the vertical extent of the mid-ocean ridge is consistent 611 with Lumpkin and Speer (2007)'s global inversion for the MOC, which shows that the vertical 612 extent of the Atlantic and Indo-Pacific lower MOC cells appear to closely follow the vertical extent of their respective major bathymetric features (i.e. mid-ocean ridges). 614

7. Comparison with realistic mid-ocean ridges

The topography and mixing in the PGCM is inspired by observations from the Brazil Basin (Figure 11), one of the regions of the abyssal ocean best characterized by observations (e.g. St. Laurent
et al. 2001; Thurnherr and Speer 2003). The circulation that emerges from the PGCM-REAL simulation (Figure 11b) is qualitatively similar to the circulation inferred from observations using an
inverse model (Figure 11a, based on St. Laurent et al. 2001): bottom-enhanced mixing along the

slope of the mid-ocean ridge drives upwelling in a bottom boundary layer and downwelling in a stratified mixing layer above.

To contextualize our simulated watermass transformations, we estimate watermass transforma-623 tions in the ocean based on hydrography and a commonly-used mixing parameterization, following Ferrari et al. (2016)'s modifications of Nikurashin and Ferrari (2013). The buoyancy flux is 625 parameterized by $\overline{w'b'} = -\Gamma \varepsilon$, where ε is the kinetic energy dissipation and Γ is a 'mixing effi-626 ciency' set to $\Gamma = 0.2$ (Osborn 1980); the buoyancy field (computed from the neutral density γ) is 627 taken from a gridded product derived from hydrographic sections of the World Ocean Circulation Experiment (Gouretski and Koltermann 2004); and we impose the insulating bottom boundary 629 condition $\mathbf{n} \cdot \overline{\mathbf{u}'b'} \simeq \overline{w'b'} = 0$ (where $\mathbf{n} \simeq \mathbf{z}$ for typical bathymetric slopes of $\tan \theta \ll 1$). The dissipation rate ε is produced by applying linear wave radiation theory for internal tides (Nycander 631 2005) and lee waves (Nikurashin and Ferrari 2011) and assuming a fraction q = 0.3 of the radiated 632 energy is locally dissipated according to a bottom-enhanced structure function with a height scale 633 of 500 m (St. Laurent and Garrett 2002). We compare watermass transformation estimates from the ocean with estimates from PGCM-REAL, a simulation with restoring to an exponential refer-635 ence stratification with a decay scale of 1000 m and which is our simulation with a stratification 636 in the southern restoring region most similar to the Southern Ocean's (Figure 2c). We focus on 637 rectangular regions with dimensions 3000 km by 3000 km (in the PGCM) or 30° longitude by 30° 638 latitude (in the ocean), which encompass comparable ridge lengths and surface areas at subtropical 639 latitudes. Watermass transformations in the PGCM-REAL simulation (Figure 12a) are the result of partially compensating buoyancy flux convergence (Figure 12e) in the BBL (red colors) and 641 buoyancy flux divergence in the SML (blue colors). Qualitatively similar (but noisier) watermass 642 transformations emerge for the mid-ocean ridge regions in the Pacific, Atlantic, and Indian (Figure 12b-d, regions delineated by boxes in panels e,f). While the net transformation varies from 0.5

Sv in the South Pacific region to 2 Sv in the Indian Ocean region, the net transformation is always the result of partially compensating upwelling and downwelling. This qualitative similarity 646 emerges in the large-scale watermass diagnostic, despite the relatively heterogeneous nature of the 647 estimated buoyancy flux and topography in the ocean basins (compare Figure 12f, e), because in all cases the turbulent buoyancy flux is bottom-enhanced (driving downwelling) and tapers to zero over the last grid cell to meet the insulating boundary condition within some bottom boundary 650 layer (driving upwelling). This property of compensating watermass transformations is in contrast 651 to the case of a constant buoyancy flux (Ferrari et al. 2016; Holmes et al. 2018), in which there is no compensating downwelling. Estimates of *global* abyssal watermass transformations, however, 653 exhibit stronger compensation by downwelling in the SML than shown here for mid-ocean ridge regions (by factors of 2 and 3 for Ferrari et al. 2016 and McDougall and Ferrari 2017, respectively). 655 In Section 8 we present evidence in support of McDougall and Ferrari (2017)'s speculation that 656 much of this discrepancy arises due to the effects of correlations between the buoyancy flux and 657 the stratification, which are omitted in their calculations. Ferrari et al. (2016)'s estimate includes these correlation terms but relies on poorly-sampled knowledge of the buoyancy flux and stratifi-659 cation close to the seafloor, which likely introduces substantial uncertainty in their estimate. While 660 much work has gone into understanding how the compensation factor depends on various param-661 eters of the diagnostic approach based on climatological observations and parameterized mixing 662 (McDougall and Ferrari 2017; Holmes et al. 2018; Cimoli et al. 2019), the functional dependence 663 of the compensation factor in the prognostic dynamic approach has received comparably little attention and is not well known.

8. Classic recipes and new trends in abyssal cuisine

Quantitative study of the abyssal stratification began with the classic study of Munk (1966): a
point-wise theory in which the observed abyssal stratification is the result of a balance between
uniform upwelling and a uniform turbulent vertical mixing. As anticipated by Munk (1966), subsequent observations show turbulent mixing to be strongly heterogeneous, with an emerging pattern of weak background mixing and vigorous mixing near rough topography (Polzin et al. 1997;
Waterhouse et al. 2014). In light of these observations, Munk and Wunsch (1998) revisited Munk
(1966)'s theorized point-wise vertical balance and re-derive it as a horizontally-averaged buoyancy
budget, which we transcribe as

$$\langle w \rangle A \simeq \langle N^2 \rangle^{-1} \frac{d}{dz} \left[A(z) \langle \kappa \rangle \langle N^2 \rangle \right]$$
 (24)

in our notation, where the key assumption is that correlations between the turbulent diffusivity κ , the stratification N^2 , and the vertical velocity w are all assumed to be negligible, such that $\langle wN^2\rangle$ = $\langle w \rangle \langle N^2 \rangle$ and $\langle \kappa N^2 \rangle = \langle \kappa \rangle \langle N^2 \rangle$. In Figure 13a,b,c, we show, respectively, the three terms in eq. 24: the horizontally-averaged stratification $\langle N^2 \rangle$, the turbulent buoyancy flux $\langle \kappa \rangle \langle N^2 \rangle$, and the isobath 678 surface area (ocean area at a fixed depth) A(z). In Figure 13d we show the left- and right-hand 679 sides of eq. 24 in the PGCM-REAL simulation at equilibrium. The horizontally-averaged vertical flux divergence (right-hand side of eq. 24) is a poor prediction for the diagnosed vertical transport. 681 This is not surprising, given that 1) w, N^2 , and κ are spatially-correlated in our solutions and 2) that 682 density surfaces are strongly sloping near boundaries. Analysis in buoyancy coordinates, such as either the thickness-weighted average framework (De Szoeke and Bennett 1993; Young 2011) or the watermass transformation framework (Walin 1982), are more appropriate. The mixing-driven 685 watermass transformation (solid black line) equals the diapycnal transport (the diabatic MOC of interest here), by definition, but also serves as a better approximation of the vertical transport $\langle w \rangle A$ than the right hand side of eq. 24.

In Figure 13c, we show that ignoring correlations within the buoyancy flux $\langle \kappa N^2 \rangle \approx \langle \kappa \rangle \langle N^2 \rangle$ introduces large biases relative to the full horizontal-mean buoyancy flux, which results in even larger biases in the flux divergence (Figure 13d). To investigate the role of these spatial correlations between κ and N^2 more exactly, we return to the watermass transformation framework, where we now define $\langle \cdot \rangle \equiv A_b^{-1} \int_{A_b} \cdot dA$ as the average along a buoyancy surface. We can thus decompose the vertical component of the watermass transformation into uncorrelated and correlated components, respectively:

$$T_{\text{net}} \approx \partial_b \left(A \langle \kappa \partial_z b \rangle \right) = \partial_b \left(A \langle \kappa \rangle \langle \partial_z b \rangle \right) + \partial_b \left(A \langle \kappa' \partial_z b' \rangle \right), \tag{25}$$

where $\kappa' = \kappa - \langle \kappa \rangle$ and $\partial_z b' = \partial_z b - \langle \partial_z b \rangle$ are deviations from the mean along a buoyancy surface. Figures 14a,c show that ignoring the correlation terms in the watermass transformation results in an overestimation of the net transformation by 20% to 200% because the stratification $\partial_z b'$ is locally reduced in the abyssal mixing layers where κ' is high (orange lines in Figure 14a,c), with the magnitude of this bias varying dramatically across simulations with different topographic geometries and restoring profiles.

To support our hypothesis that vertical variations in the stratification are necessary to support large net watermass transformations, we further decompose the uncorrelated component into a component related to the change in the mean stratification and a residual component related to changes in both the area of the buoyancy surface and the mean diffusivity, respectively:

$$\partial_b (A\langle \kappa \rangle \langle \partial_z b \rangle) = A\langle \kappa \rangle \partial_b \langle \partial_z b \rangle + (\partial_z b) \partial_b (A\langle \kappa \rangle). \tag{26}$$

In the experiment shown in Figure 14a,b, where the uncorrelated component is a reasonable approximation of the net transformation, we find the net transformation to be largely driven by vari-

ations of the stratification with buoyancy, $A\langle\kappa\rangle\partial_b\langle\partial_zb\rangle$, although variations in the diffusivity integrated along a buoyancy surface are also important. Variations in the stratification also appear important in the experiment shown in Figure 14d, although this decomposition is more difficult to interpret since the uncorrelated component overestimates the net transformation by a factor of 3 (Figure 14c).

9. Discussion

The idealized numerical model presented here describes an abyssal circulation and stratification 714 controlled by mixing-driven flows along a mid-ocean ridge in a cross-equatorial basin (Figure 1). By initializing with- and restoring to- a series of reference buoyancy profiles in the south of 716 the basin, we investigate transient and equilibrium coupling between the basin stratification and the mixing-driven boundary flows. At equilibrium, dense abyssal waters form in the southern restoring region and flow north via adiabatic deep western boundary currents (red circle), filling 719 the abyssal depths in both hemispheres. Along the mid-ocean ridge, bottom-enhanced mixing 720 (squiggly lines) drives a net transformation of dense abyssal waters into lighter deep waters, the 721 residual of partially-compensating upwelling in a bottom boundary layer (BBL) and downwelling 722 in a stratified mixing layer (SML) right above it. The newly formed light deep waters flow zonally 723 towards the western continental slope (solid arrow), returning southward via an adiabatic deep western boundary current to the restoring region (blue circles), and closing the abyssal overturning 725 circulation as they are once again transformed into dense abyssal waters. 726

Despite the extreme degree of idealization in our formulation of the Planetary Geostrophic Circulation Model (PGCM), the watermass transformations that emerge at equilibrium are qualitatively similar to diagnostic estimates of watermass transformations near mid-ocean ridges in the
Pacific, Atlantic, and Indian Oceans (Figure 12), which are themselves fairly uncertain (Cimoli

et al. 2019). Similarly, the zonal overturning that emerges within bottom mixing-driven flows
along the mid-ocean ridge are qualitatively similar to that described by an inverse model of the
abyssal Brazil Basin based on in-situ measurements (St. Laurent et al. 2001, and Figure 11). Remaining differences between our simulations and observations are likely due to the crude nature
of our parameterizations for the restratification by submesoscale turbulence and for the formation
of bottom waters in the Southern Ocean, as well as uncertainties in the observational estimates.

The equilibrium interior stratification in the PGCM always exhibits dynamically significant vertical variations, the structure of which is determined by a combination of mixing layer dynamics
and the restoring condition in the south. Even in our simulations that are initialized from- and
restored to- a constant stratification reference buoyancy profile, heterogeneities in the topographic
slope cause cross-slope divergence and a corresponding exchange flow between the abyssal mixing layers and the interior. Over time, these exchange flows modify the interior stratification and
associated watermass transformations.

As in CF18, we find the prediction of upwelling in the BBL by one-dimensional (1D) boundary layer theory provides a reasonable approximation to the maximum net transformation or, equiv-745 alently, the strength of the diabatic meridional overturning circulation (Figures 8 and 9). While 746 this interpretation provides a useful prediction for the maximum net transformation which occurs 747 at the base of topographic slopes, it does not inform the net transformation along the flanks of the 748 mid-ocean ridge, where upwelling in the BBL is instead partially compensated by downwelling in 749 a SML. At depths where both the BBL and the SML are active, 1D theory predicts almost perfect compensation and a resulting net transformation that is vanishingly small (eq. 5 and Figure 8a,e). 751 In contrast, our PGCM simulations exhibit finite net watermass transformations that extend from 752 the base of the ridge slopes all the way up to the ridge crest (Figure 10), consistent with both our oceanic estimates (Figure 12) and inverse models of the Indo-Pacific overturning circulation 754

Clumpkin and Speer 2007). We attribute the existence of a finite net transformation to vertical variations in the basin stratification (Figures 8 and 14). As we increase the degree to which the restoring stratification varies in the vertical, the compensation of BBL upwelling by SML downwelling (evaluated near the depth of the ridge crest) ranges from nearly-perfect compensation to nearly-zero compensation (Figure 9a). Thus, while 1D bottom boundary layer theory provides a reasonable approximation to *maximum net* watermass transformation, the vertical extent and structure of watermass transformations depends on the degree of compensation by downwelling in the SML, which is itself coupled to the vertically-varying basin stratification.

Our simulations show that correlations between mixing and stratification (Figure 14a,c), which 763 are typically ignored in idealized models of the zonal-mean abyssal overturning (Nikurashin and 764 Vallis 2011; Jansen and Nadeau 2019), can be of leading-order importance in abyssal watermass 765 transformations; whether these correlations are important in the ocean remains an open question. 766 Despite our improved understanding of the roles of bottom mixing and the interior basin strat-767 ification on the abyssal watermass transformations and circulation, we fall short of a predictive analytical theory for the abyssal overturning and stratification that couples boundary layer dynam-769 ics with a model for the evolution of the interior stratification. Recent and ongoing work in 1) 770 observing abyssal mixing layers (e.g. Garabato et al. 2019), 2) investigating their dynamics with 771 idealized theory and simulations (Wenegrat et al. 2018; Callies 2018; Holmes et al. 2019), 3) de-772 veloping and evaluating parameterizations of their turbulent fluxes, 4) and coupling them to the 773 basin stratification (e.g. refining the approach of Salmun et al. 1991) will all be key ingredients for cooking up a revised theory of the abyssal circulation and stratification.

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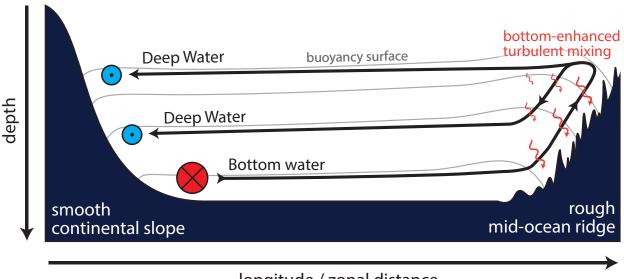
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202		PGCM-REAL experiment (top row) and an experiment with a shorter ridge and constant ref-	
203		erence stratification (bottom row). In panels (a,c) , we approximate the full watermass transformation (doshed block) by the contribution from the vertical by every flav $\frac{\partial}{\partial x} (A/x \partial h)$	
204		formation (dashed black) by the contribution from the vertical buoyancy flux $\partial_b (A \langle \kappa \partial_z b \rangle)$	
205		(solid black), which we then decompose into an uncorrelated component $\partial_b (A\langle \kappa \rangle \langle \partial_z b \rangle)$ (solid blue) and a residual $\partial_b (A\langle \kappa' \partial_z b' \rangle)$ (solid orange), where $\langle \cdot \rangle$ denotes averaging along	
206		a buoyancy surface. In panels (b,d), we further decompose the uncorrelated component into	
207		contributions due to the buoyancy derivative of the mean stratification $\partial_b \langle \partial_z b \rangle$ (dashed) and	
208		the integrated diffusivity along a buoyancy surface $\partial_L(A\langle \kappa \rangle)$ (dotted)	69



longitude / zonal distance

FIG. 1. Schematic of a basin-scale abyssal circulation driven by near-boundary mixing. Dense bottom waters flow northward out of the Southern Ocean via a deep western boundary current (red circle) along the smooth and relatively quiescent continental slope, where little watermass transformation occurs. A cross-basin zonal flow feeds bottom waters from the deep western boundary current into a system of abyssal mixing layers driven by bottom-enhanced turbulent mixing over the rough topography of the mid-ocean ridge flanks (squiggly orange arrows). The turbulent buoyancy flux converges in a bottom boundary layer (BBL), driving vigorous diabatic upwelling across buoyancy surfaces (grey lines). In a stratified mixing layer (SML) above, the buoyancy flux diverges, driving diabatic downwelling. The net effect of the up- and down-welling in the abyssal mixing layers is a net transformation of bottom waters into deep waters. The newly formed deep waters return via cross-basin zonal flows to the smooth continental slope, wherein they flow southward in a deep western boundary current (blue circles) to close the abyssal circulation in the Southern Ocean. For simplicity, we omit the alternating along-ridge flows (see Figure 3b) that are in frictional thermal-wind balance with the plunging isopycnals.

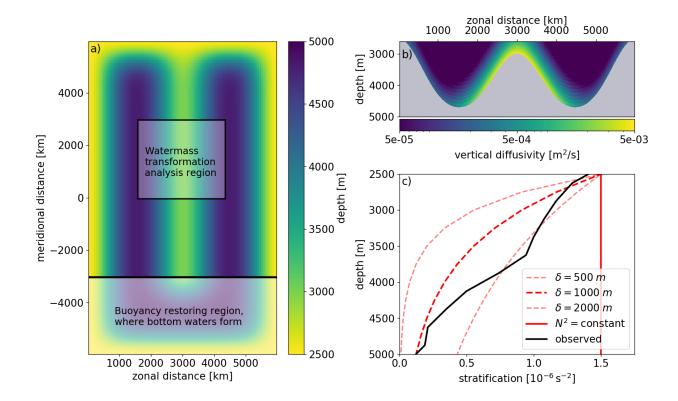


FIG. 2. Configuration of the Planetary Geostrophic Circulation Model (PGCM). (a) Seafloor depth in the PGCM. We highlight the southern restoring region where we apply a buoyancy restoring which acts to transform deep waters into bottom waters (see Section 3c) and a northern-hemisphere region in which we diagnose watermass transformations along the mid-ocean ridge (see Section 4c). (b) Zonal section of the imposed turbulent diffusivity κ , which is bottom-enhanced over the mid-ocean ridge. (c) The red lines show the four stratification profiles B_z used in the PGCM as both the initial condition and as the reference profile for buoyancy restoring in the southern restoring region. The black line shows the observed stratification profile from the World Ocean Circulation Experiment (Gouretski and Koltermann 2004) in the South Pacific, averaged horizontally from 55°S to 45°S and 175°E to 115°W.

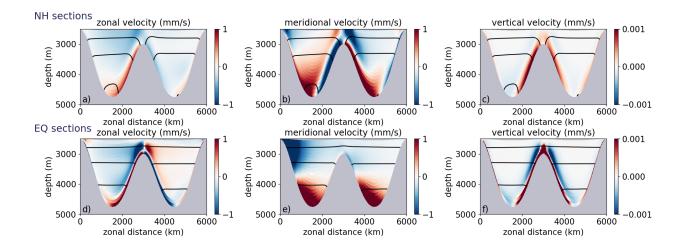


FIG. 3. Cartesian components of the velocity vector in the PGCM-REAL simulation along: (a-c) a midlatitude section in the northern hemisphere, y = 3000 km, and (d-f) a section at the equator, y = 0 km. Black lines show three equally spaced buoyancy surfaces.

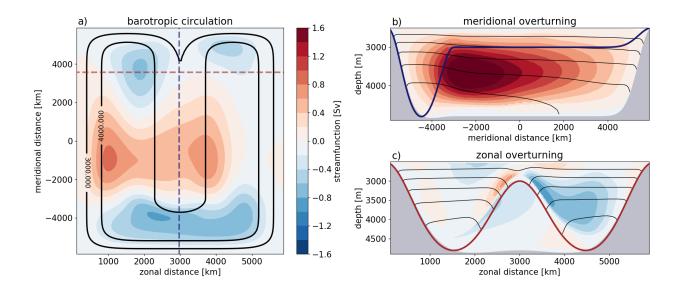


FIG. 4. (a) Barotropic, (b) meridional, and (c) zonal overturning circulations in the PGCM-REAL simulation (see definitions in Section 4b). In all cases, positive values (red) correspond to counter-clockwise circulations. The blue and red solid lines in (b) and (c), respectively, show the height of the mid-ocean ridge along the dashed lines of the same colors in (a). The thick black lines in (a) are the 3000 m and 4000 m isobaths, which highlight both the continental slopes and the mid-ocean ridge. The thin black lines in (b) and (c) are equally-spaced buoyancy surfaces, sampled at x = L/4 and y = L/2, respectively.

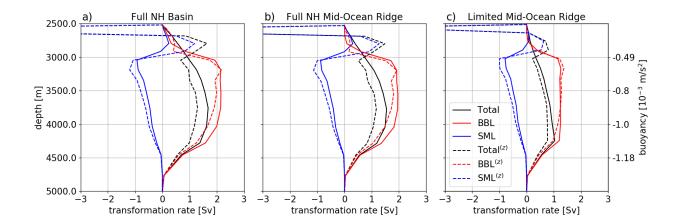


FIG. 5. Watermass transformations from the PGCM-REAL simulation in (a) the full northern hemisphere basin (y > 0), (b) along the northern-hemisphere mid-ocean ridge (y > 0, L/2 < x < 3L/2), and (c) in a limited watermass analysis region along the northern-hemisphere mid-ocean ridge (0 < y < L/2, L/2 < x < 3L/2), as highlighted in Figure 2. The black line shows the net watermass transformation, defined by equation (18). The red and blue lines show the contributions from the bottom boundary layer (BBL) and the stratified mixing layer above (SML). The dashed lines show the contributions from only the vertical component of the buoyancy flux. All watermass transformations in the paper are computed in buoyancy space and remapped into depth space (according to eq. 19).

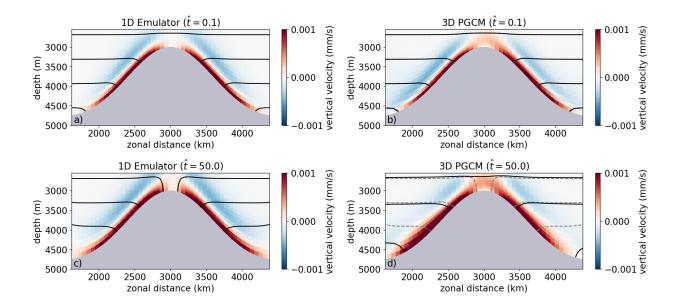


FIG. 6. Vertical velocity (colors) and buoyancy surfaces (black lines) in abyssal mixing layers along a zonal section across the mid-ocean ridge at y = L/2 in (a,c) the 1D PGCM emulator and (b,d) the full 3D PGCM, where both are initialized from identical constant stratification buoyancy fields. The top row shows the solutions at an initial time $\hat{t} = 0.1$, at which point the abyssal mixing layers have spun up but the basin-scale circulation has not (see Section 3d). The bottom row shows the solution at $\hat{t} = 50$, at which point the full solution has roughly come to equilibrium with the buoyancy restoring in the Southern Ocean. The predicted buoyancy surfaces in (a,c) are reproduced as dashed grey lines in (b,d) to show how the 1D emulator predicts the buoyancy field well for short times but that the interior stratification in the PGCM drifts far from the 1D emulator's prediction as it approaches equilibrium.

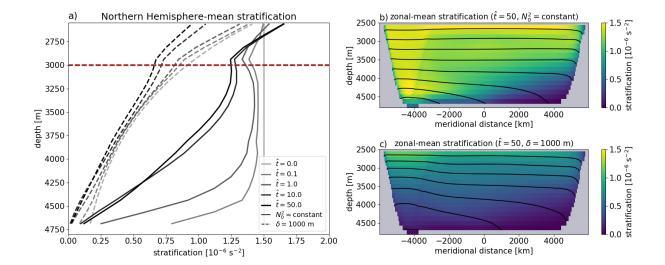


FIG. 7. (a) Temporal evolution and (b,c) meridional structure of the stratification in PGCM simulations. Grey-scale lines in (a) show the temporal evolution of the horizontal-mean stratification in the Northern Hemisphere for simulations with a constant stratification restoring buoyancy profile (solid lines) and a restoring buoyancy profile corresponding to stratification that decays with depth with a scale height of $\delta = 1000$ m (dashed lines). The dashed brown line delineates the height of the ridge crest. Panels (b) and (c) show the zonal-mean stratification at equilibrium $\hat{t} = 50$ (colors) and equally-spaced buoyancy surfaces (black lines) for experiments with restoring to constant and exponential stratification, respectively.

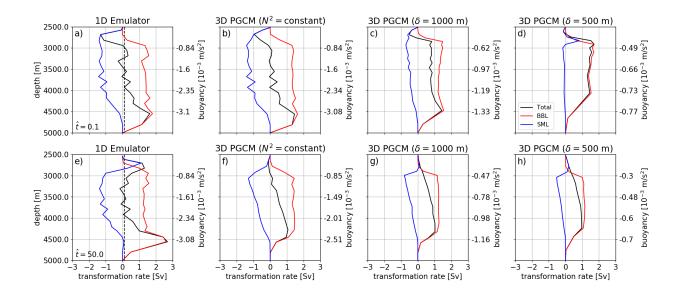


FIG. 8. Watermass transformations in: (a, e) a 1D emulator of the PGCM and (b-d, f-h) the 3D PGCM simulations with restoring buoyancy profiles corresponding to stratification profiles with various exponential scale heights δ (we recover $N^2 = \text{constant}$ as $\delta \to \infty$). The initial spin-up at $\hat{t} = 0.1$ is shown in (a-d) and the equilibrium state at $\hat{t} = 50$ is show in (e-h). Black, red, and blue lines show the net, bottom boundary layer (BBL), and stratified mixing layer (SML) contributions to the watermass transformations, respectively. The black dashed line in (a,e) shows the integral constraint $L\Psi_{\infty} = L\kappa_{bg} \cot \theta_{max}$ derived from boundary layer theory, where we take θ_{max} as the maximum slope angle of the mid-ocean ridge flank.

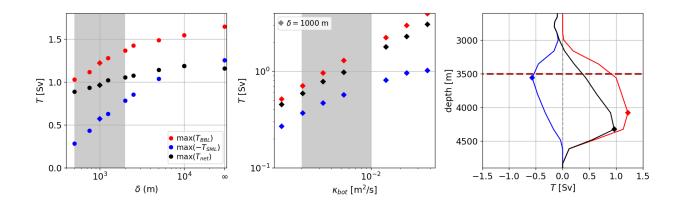


FIG. 9. Scaling of watermass transformations in mixing layers with (a) the height δ over which the restoring stratification varies and (b) the bottom diffusivity κ_{bot} . Colored symbols represent the absolute value of the maximum transport in the BBL (red), the SML (blue), and the net (black), with diamonds representing the PGCM-REAL simulations. The grey shading in (a) represents realistic vertical scales δ over which abyssal stratification varies and in (b) represents plausible values of the bottom diffusivity κ_{bot} . Panel (c) provides an example of the watermass transformations for a bottom diffusivity $\kappa_{bot} = 5 \times 10^{-3} \text{ m}^2 \text{s}^{-1}$, a stratification height scale $\delta = 1000 \text{ m}$, and a ridge height of $r_h = 1500 \text{ m}$, where the corresponding maxima are marked by diamonds and the dashed brown line represents the ridge crest. In all experiments, the maximum net and BBL transformations occur at depths of roughly 4250 m, at the base of the ridge slope, while the maximum SML transformation occurs at the ridge crest.

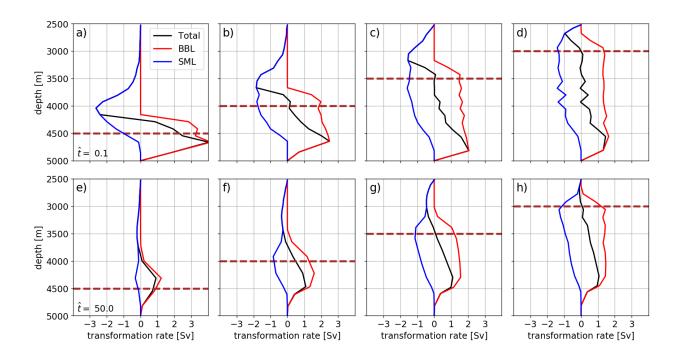


FIG. 10. Watermass transformations in PGCM simulations as a function of ridge height. All panels are for a fixed constant stratification restoring buoyancy profile. The initial spin-up at $\hat{t}=0.1$ is shown in (a-d) and the equilibrium state at $\hat{t}=50$ is shown in (e-h). Mid-ocean ridge height increases in increments of 500 m from left to right, as indicated by the dashed brown lines. Black, red, and blue lines show the net, bottom boundary layer (BBL), and stratified mixing layer (SML) contributions to the watermass transformations, respectively.

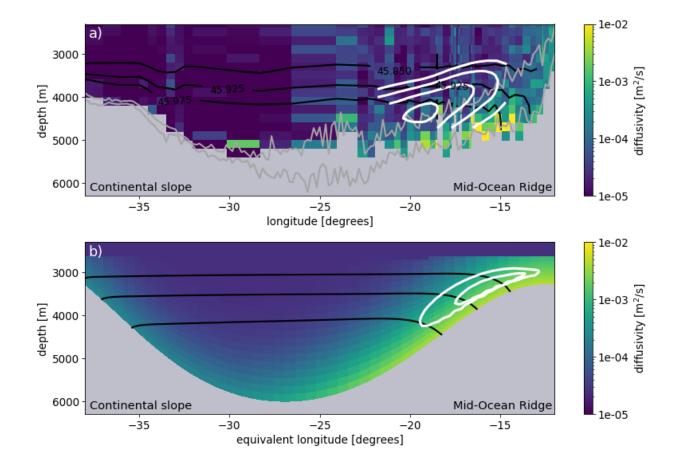


FIG. 11. Diabatic zonal overturning circulation driven by bottom-enhanced mixing on the western flank of a mid-ocean ridge in (a) the South Atlantic Ocean and (b) the western half of the PGCM-REAL simulation domain. White lines show arbitrarily chosen contours of the counter-clockwise zonal overturning streamfunction, where the values for (a) are digitized from Figure 14 of St. Laurent et al. (2001) and for (b) are diagnosed from PGCM-REAL simulation. Coloring shows the vertical diffusivity in log-scale (light-grey shading represents depths with no microstructure measurements and does not necessarily represent topography), where panel (a) is inspired by Figure 2 of Polzin et al. (1997) and the diffusivity is calculated with microstructure profiles from the BBTRE experiment (Polzin et al. 1997; St. Laurent et al. 2001, archived at microstructure.ucsd.edu). Black lines are: (a) potential density σ_4 surfaces (referenced to 4000 m) from the microstructure profiles and (b) buoyancy surfaces from the PGCM solution, chosen arbitrarily to show that the zonal overturning circulation is indeed diabatic. The dark grey lines in (a) show the depth minimum (canyon thalweg) and maximum (canyon crest) seafloor depth within 0.5° latitude of the microstructure profiles. In (b), zonal distance along the PGCM section has been converted to an equivalent longitude at 25°S so that length scales can be directly compared between the two panels.

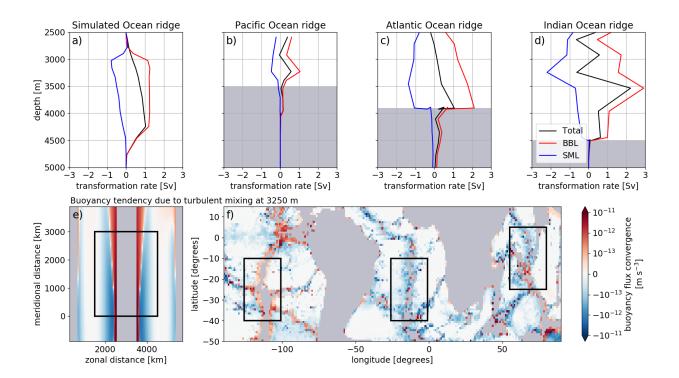


FIG. 12. (a-d) Watermass transformations at all abyssal depths and (e,f) buoyancy flux convergence at 3250 m depth in similarly-sized domains containing mid-ocean ridges, as diagnosed from (a,e) the PGCM-REAL simulation and estimated for the (b,f) Pacific, (c,f) Atlantic, and (d,f) Indian Oceans. In (a-d), the black, red, and blue lines show the net, bottom boundary layer (BBL), and stratified mixing layer (SML) contributions to the watermass transformations, respectively (grey shaded indicates depths representing very little ocean volume). The black boxes in (e,f) delineate the similarly-sized regions (each with dimensions of roughly 3000 km \times 3000 km) for which we compute the watermass transformations. In (e,f), red and blue show regions of buoyancy flux convergence (positive buoyancy tendency) and buoyancy flux divergence (negative buoyancy tendency), respectively.

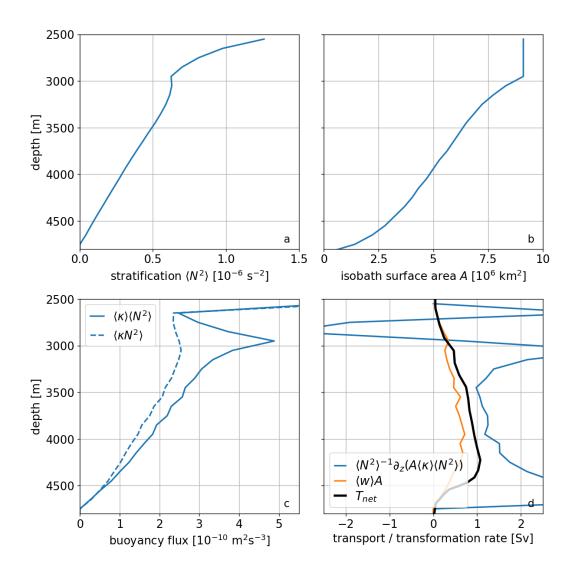


FIG. 13. Comparison of abyssal upwelling diagnostics in the PGCM-REAL simulation for the water-mass transformation analysis region highlighted in Figure 2a. The orange and blue lines in panel (d) represent the left- and right-hand sides, respectively, of the horizontally-averaged advection-diffusion balance $\langle w \rangle A \simeq \langle N^2 \rangle^{-1} \frac{d}{dz} \left[A(z) \langle \kappa \rangle \langle N^2 \rangle \right]$ (eq. 24), which accounts for changes in isobath surface area A(z) with depth but ignores correlations between w, κ , and N^2 and excludes the horizontal advection. The solid blue lines in panels (a), (b), and (c) show the individual components of the expressions: (a) the horizontally-averaged stratification $\langle N^2 \rangle$, (b) the horizontally-averaged buoyancy flux $\langle \kappa \rangle \langle N^2 \rangle$, and (c) the isobath surface area A(z). The dashed line in (b) shows the role of correlation terms $\langle \kappa N^2 \rangle - \langle \kappa \rangle \langle N^2 \rangle$ in setting the vertical structure of the buoyancy flux. Finally, the solid black line in (d) shows the net watermass transformation, where its native density coordinate has been mapped into a pseudo-depth coordinate by taking the average depth of a given buoyancy surface (eq. 19). For all of our simulations, vertical advection-diffusion bulk models are poor approximations of diapycnal abyssal upwelling.

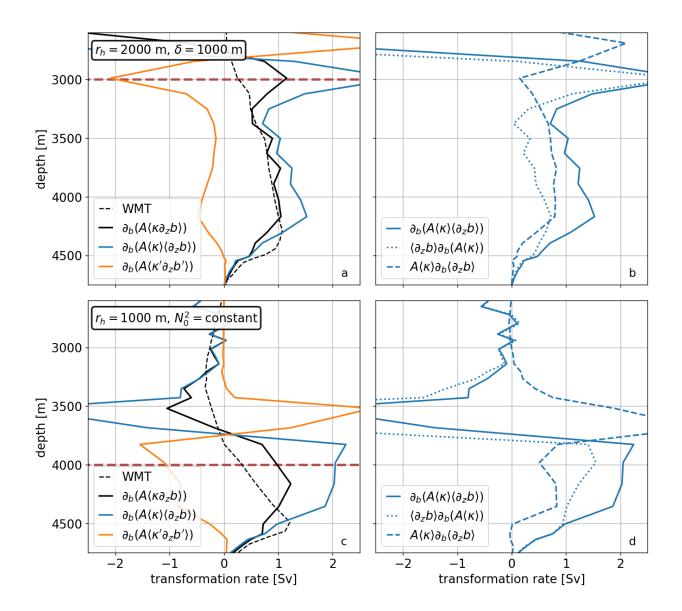


FIG. 14. Decomposition of the watermass transformation into various physical components in the PGCM-REAL experiment (top row) and an experiment with a shorter ridge and constant reference stratification (bottom row). In panels (a,c), we approximate the full watermass transformation (dashed black) by the contribution from the vertical buoyancy flux $\partial_b (A\langle\kappa\partial_z b\rangle)$ (solid black), which we then decompose into an uncorrelated component $\partial_b (A\langle\kappa\rangle\langle\partial_z b\rangle)$ (solid blue) and a residual $\partial_b (A\langle\kappa'\partial_z b'\rangle)$ (solid orange), where $\langle\cdot\rangle$ denotes averaging along a buoyancy surface. In panels (b,d), we further decompose the uncorrelated component into contributions due to the buoyancy derivative of the mean stratification $\partial_b \langle \partial_z b \rangle$ (dashed) and the integrated diffusivity along a buoyancy surface $\partial_b (A\langle\kappa\rangle)$ (dotted).