

Functional relationships reveal differences in the water cycle representation of global water models

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1 **Global water models are widely used for policy-making and in sci-**
 2 **entific studies, but substantial inter-model differences highlight the**
 3 **need for additional evaluation. Here we evaluate global water mod-**
 4 **els by assessing so-called functional relationships between system**
 5 **forcing and response variables. The more widely used comparisons**
 6 **between observed and simulated fluxes provide insight into model**
 7 **behavior for the representative area of an observation, and can there-**
 8 **fore potentially improve the model for that area. Functional relation-**
 9 **ships, by contrast, aim to capture how system forcing and response**
 10 **variables co-vary across large scales, and thus offer the potential for**
 11 **model improvement over large areas. Using 30-year annual averages**
 12 **from 8 global water models, we quantify such functional relation-**
 13 **ships by calculating correlations between key forcing variables (pre-**
 14 **cipitation, net radiation) and water fluxes (actual evapotranspiration,**
 15 **groundwater recharge, total runoff). We find strong disagreement**
 16 **for groundwater recharge, some disagreement for total runoff, and**
 17 **the best agreement for evapotranspiration. Observation- and theory-**
 18 **derived functional relationships show varying agreements with mod-**
 19 **els, indicating where model representations and our process un-**
 20 **derstanding are particularly uncertain. Overall, our results suggest**
 21 **that model improvement is most important for the representation of**
 22 **energy balance processes, recharge processes, and generally for**
 23 **model behavior in dry and cold regions. We argue that advancing**
 24 **our ability to simulate global hydrology requires a better perceptual**
 25 **understanding of the global water cycle. To evaluate if our models**
 26 **match that understanding, we should explore alternative evaluation**
 27 **strategies, such as the use of functional relationships.**

global hydrological models | land surface models | model evaluation |
 rank correlations | global hydrology

1 **G**lobal water models – including hydrological, land surface,
 2 and dynamic vegetation models (1) – inform water man-
 3 agement policies. Many global modeling studies explicitly aim
 4 to provide policy-relevant information (e.g. 2–6). The Sixth
 5 Assessment Report (AR6) of the Intergovernmental Panel on
 6 Climate Change (IPCC) (7) draws heavily on results from
 7 global water models, which provide information on the im-
 8 pacts of climate change on streamflow (8, 9), terrestrial water
 9 storage (10), and groundwater recharge (11). Some of these
 10 models are embedded in global water information services to

11 provide water information to a wide array of stakeholders.
 12 For instance, the Global Groundwater Information System
 13 (12) shares information required for sustainable groundwater
 14 resources development and management. The Aqueduct frame-
 15 work (13) calculates risk indicators to derive water risk maps
 16 valuable for companies, governments, and non-governmental
 17 organizations. And the African Flood and Drought Monitor
 18 (14) continuously predicts drought and flood indicators using
 19 various forecasting products.

20 Global water models have also become an essential tool in
 21 Earth system science. Measurements of some hydrological vari-
 22 ables are very sparse and insufficient for large-scale analyses.
 23 Hence we regularly use global water models to provide globally
 24 coherent estimates of variables such as groundwater recharge
 25 and groundwater storage change (15–17). These model out-
 26 puts are often the basis for other studies, e.g. by providing
 27 groundwater recharge as input to groundwater models (e.g.

Significance Statement

Global water models inform water management policies and are a cornerstone of Earth system science. Since global water models are increasingly used for projections of environmental change impacts, adequate methods to evaluate these models are imperative. Here we evaluate model behavior by comparing large-scale functional relationships between system drivers (climate forcing) and simulated and observed system outputs (water fluxes). We find substantial variability between models, and disagreements with observation-based functional relationships. For example, some models show a very strong relationship between groundwater recharge and precipitation, while others do not. Thus, projected changes in precipitation would result in different groundwater recharge estimates across models. Existing disagreements underscore the need for adequate evaluation strategies and for multi-model approaches to embrace uncertainty.

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18, 19), making subsequent study results dependent on the reliability of model outputs. Global models also provide a virtual laboratory which is used to assess the impacts of climate and land use change on the water cycle and on hydrological extremes such as floods and droughts (e.g. 8, 9, 20, 21).

Model disagreements highlight the need for model evaluation.

Past studies have revealed substantial disagreements between global water models, showing that estimates of both the current distribution and future trends of key water cycle components remain uncertain (11, 22–25). While some of that uncertainty stems from projected or observed climatic forcing, considerable uncertainty stems from global water models themselves (8, 11, 22, 23, 26, 27). For instance, Beck et al. (23) found distinct inter-model performance differences when comparing simulated and observed streamflow for 10 global water models driven by the same meteorological forcing. Comparing long-term trends in modeled terrestrial water storage to GRACE satellites, Scanlon et al. (24) found that global models generally underestimate trends and even show opposite trends in some parts of the world. Different system conceptualizations, such as including karst-related subsurface heterogeneity, can lead to very different groundwater recharge estimates for current and potential future climates (28). It is therefore not surprising that the IPCC's AR6 (7) concludes from an analysis of currently available global water model projections that "uncertainty in future water availability contributes to the policy challenges for adaptation, for example, for managing risks of water scarcity".

To address inter-model differences as a source of uncertainty, it is imperative that we evaluate how, where and why models differ. Evaluating global models is, however, challenging due to limitations in data availability (spatial and temporal bias, data quality) and scale mismatches between observations and model outputs (29). These challenges are not easy to overcome, but they should motivate us to seek model evaluation strategies that are suitable for global water models and better utilize the information contained in the observations we have.

Towards functional model evaluation. Most evaluation strategies compare model outputs to historical observations over the footprint for which the observation is representative. This can be at the plot (e.g. flux towers), the catchment (e.g. gauging stations), or grid cell (e.g. gridded remote sensing products) scale. Such approaches are necessary but not sufficient to robustly evaluate global models (29). First, these approaches compare simulated and observed values location by location (or catchment by catchment), even though observations in one location might contain information about geographically different, but hydrologically similar, locations. Thus we might miss the opportunity to improve the model for more than one location at a time. Second, relevant information for model evaluation might not just lie in comparing the magnitudes of simulated and observed values of a variable at a single location, but rather in how a model simulates the spatial distribution of a variable (i.e. its relative differences). And third, a comparison with historical observations does not guarantee that a model reliably predicts system behavior under changing conditions (30). We think that an alternative approach can at least partially overcome these three shortcomings.

In this alternative strategy, we focus on the effective functional behavior of models (31). Effective functional behavior

might be characterized by the relationship between system forcing and response variables. For example, the concept of equilibrium climate sensitivity, which quantifies the warming response to doubling carbon dioxide concentrations, is often used to describe how severe climate change might be (32). In hydrology, the sensitivity (or elasticity) of streamflow to changing climatic boundary conditions (33, 34) has been used to better understand how changes in forcing translate into changes in streamflow. This sensitivity can be used as an indicator of how quickly future water availability might change under a changing climate (35). Forcing-response relationships like these might be derived from (or constrained by) observations and theory, but also by expert knowledge, thus enabling us to bring our perception of how a system functions into the model evaluation process (36).

Here we use so-called functional relationships and explore their potential for global water model evaluation. We define the term functional relationship as a relationship between two (or more) variables, such as forcing-response relationships, or relationships between system states and fluxes. Ideally, such relationships should be based on process knowledge and first principles, but empirical relationships may serve as a useful starting point. Functional relationships have been used, for example, to analyze land surface model functioning (31), to evaluate catchment models (37), to derive constraints for model regionalization (38), or to calibrate large-scale hydrological models (39, 40). These examples are, however, scattered among the literature and have not yet been formalized into an evaluation framework. In the following, we outline how an evaluation using functional relationships might look like, show how it can help to shed new light on model behavior, and discuss next steps required to fully benefit from functional relationship based evaluation.

We evaluate 8 global water models (CLM4.5 (41), CWatM (42), H08 (43), JULES-W1 (44), LPJmL (45), MATSIRO (46), PCR-GLOBWB (47), and WaterGAP2 (48)) from phase 2b of the Inter-Sectoral Impact Model Intercomparison Project (ISIMIP 2b; 49). We analyze 30-year (climatological) averages (1975-2004) using HadGEM2-ES forcing; note that the specific forcing chosen does not appear to influence model-based functional relationships (see Materials and Methods section). We analyze the following model variables: precipitation P (the available water; equal for all models), net radiation N (a proxy for the available energy), actual evapotranspiration E_a , groundwater recharge R , and total runoff Q (three key water fluxes), all converted to mm/y. Details on data processing are described in the Materials and Methods section.

We address the following three research questions:

- 1) To what extent do key water fluxes simulated by global water models disagree with each other, and how does the disagreement vary spatially?
- 2) How do global water models translate forcing variables into key water fluxes, i.e. which functional relationships do they represent?
- 3) Can we use data and existing knowledge to derive functional relationships and use them to constrain expected model behavior?

Results

Research question 1: Global model disagreement. We first assess how model outputs (actual evapotranspiration, ground-

148 water recharge, total runoff) vary globally by calculating the
 149 coefficient of variation (CoV) between the 8 models per grid
 150 cell, shown in Figure 1a-c (see Materials and Methods for
 151 details). Actual evapotranspiration (Figure 1a) shows low
 152 CoV values suggesting reasonable agreement between models
 153 (mean grid cell CoV = 0.23), with slightly higher CoV val-
 154 ues in some mountainous regions (e.g. Himalaya) and cold
 155 regions (e.g. northern Russia). Groundwater recharge (Figure
 156 1b) shows many white spaces suggesting strong disagreement
 157 (mean grid cell CoV = 1.17). The highest CoV values are
 158 found in dry regions (e.g. Australia, outer-tropical Africa)
 159 and in cold regions (e.g. large parts of continental Asia and
 160 North America). Total runoff (Figure 1c) shows some white
 161 spaces suggesting moderate disagreement (mean grid cell CoV
 162 = 0.54). The highest CoV values are found in dry regions (e.g.
 163 Australia, outer-tropical Africa, Central Asia). Note that the
 164 CoV can be high even if the absolute differences are small, so
 165 that inter-model differences might be exaggerated in very dry
 166 regions. We thus show maps of the standard deviation in the
 167 Supporting Information (Figures S5-7).

168 When exploring inter-model differences, it is useful to assess
 169 if strong model disagreement (high CoV values) is due to high
 170 ensemble uncertainty (all models disagree with each other) or
 171 because one individual model deviates strongly. Figure 1d-f
 172 shows which model deviates most from the ensemble mean,
 173 indicating which model dominates the ensemble spread (i.e.
 174 the CoV shown in Figure 1a-c). While this does not tell us
 175 which models perform better or worse, it indicates whether
 176 there is a single model that is consistently different (in a
 177 certain region). We find that different models deviate from
 178 the ensemble mean in different places. There is not one model
 179 that consistently deviates the most for a specific variable (the
 180 highest fraction of grid cells dominated by a single model
 181 for E_a , R , and Q , is 12%, 14%, and 13%, respectively), but
 182 mostly multiple models deviate similarly strongly from the
 183 ensemble mean (for E_a , R , and Q , it is 31%, 28%, and 34%,
 184 respectively). Overall, there is little agreement between the
 185 maps and we cannot single out one model that consistently
 186 deviates the most for all fluxes over a large region (Figures
 187 1d-f show different patterns).

188 **Research questions 2 and 3: Functional relationships.** We
 189 can visually assess relationships between forcing (P, N) and
 190 response variables (E_a, R, Q) by inspecting scatter plots, ex-
 191 emplarily shown for some variable combinations and some
 192 models in Figure 2a-c. To facilitate the comparison of multiple
 193 models, we use Spearman rank correlations ρ_s as a summary
 194 metric. A high rank correlation (close to 1) indicates that
 195 spatial variability in the forcing variable (e.g. precipitation)
 196 almost completely explains spatial variability in the output
 197 variable (e.g. groundwater recharge). This corresponds to a
 198 scatter plot with a tight relationship, as in Figure 2b for H08.
 199 A low rank correlation indicates that other factors also matter
 200 (e.g. model parameters, other input data). This corresponds
 201 to a scatter plot with a scattered relationship, as in Figure
 202 2b for PCR-GLOBWB. It is important to note that a high
 203 correlation is not a measure of goodness of fit. The correlations
 204 simply characterize the strength of the relationship between
 205 forcing and response variables.

206 Besides comparing functional relationships between models,
 207 we compare the models to functional relationships based on
 208 several observational datasets and the semi-empirical equation

introduced by Budyko (50), listed in Table 1.

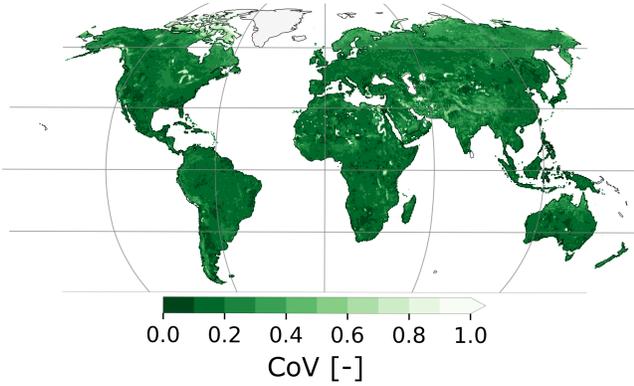
209 Having found clear differences between major climate zones
 210 (Figure 1), we divide the world into four climatic regions (see
 211 Materials and Methods for details). Based on the aridity index
 212 (here defined as N/P), a place is categorized as either wet
 213 ($N/P < 1$) or dry ($N/P > 1$). Based on how many days
 214 per year fall below a 1°C temperature threshold, a place is
 215 categorized as either cold (more than one month below 1°C)
 216 or warm (less than one month below 1°C). This results in four
 217 categories: wet-warm (18% of modeled area), wet-cold (15%),
 218 dry-cold (24%), and dry-warm (43%), shown in Figure 2d.
 219

220 **Precipitation and evapotranspiration** There are some differences
 221 in magnitude, but the ranking between the climate regions is
 222 the same for all models (Figure 3a and Table S3 in the Support-
 223 ing Information). We find the strongest $P-E_a$ -relationships in
 224 dry-warm places (ρ_s ranges from 0.90-0.98) and the weakest
 225 $P-E_a$ -relationships in wet-warm places (ρ_s : 0.57-0.73). The
 226 Budyko equation (50) predicts higher correlations overall, but
 227 the same ranking. This reflects the fact that in dry (i.e. water-
 228 limited) places, precipitation primarily evaporates, while in
 229 wet (i.e. energy-limited) places, evapotranspiration is lim-
 230 ited by the available energy. Contrary to the models and the
 231 Budyko equation, FLUXCOM data (51) show higher values
 232 for wet-cold than for dry-cold places (Figure 3a and Table 1).

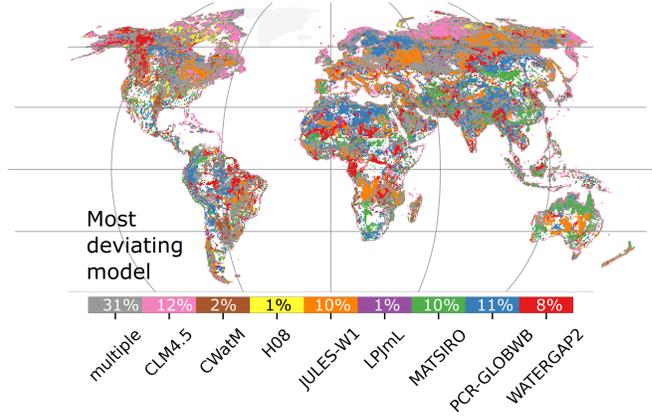
233 **Net radiation and evapotranspiration** Most of the models show
 234 similar magnitudes and a similar ranking between the climate
 235 regions (Figure 3b and Table S3). We find the strongest $N-E_a$ -
 236 relationships in wet-cold places (ρ_s : 0.56-0.96) and the weakest
 237 $N-E_a$ -relationships in dry-cold places (ρ_s : 0.26-0.70). This
 238 agrees with the Budyko equation and reflects the fact that in
 239 wet (i.e. energy-limited) places, net radiation is the primary
 240 control on actual evapotranspiration, while in dry (i.e. water-
 241 limited) places, net radiation is a less strong control. There
 242 are, however, differences in the ranking for some of the models,
 243 especially for dry-warm places. For CWatM and WaterGAP2
 244 dry-warm and not dry-cold places show the lowest correlation
 245 (0.12 and 0.41, respectively), and for MATSIRO dry-warm
 246 places show the highest correlation (0.70). FLUXCOM data
 247 show very high correlations for all regions (0.79-0.94; higher
 248 than most models), even for dry-cold regions (0.79), which
 249 show the lowest correlations in the models (0.26-0.70) and for
 250 Budyko (0.59) (Figure 3b and Table 1).

251 **Precipitation and groundwater recharge** The models show little
 252 agreement in their $P-R$ -relationships (Figure 3c and Table
 253 S3). The largest variability is seen in dry-cold places (ρ_s : 0.35-
 254 0.84), followed closely by dry-warm (0.48-0.95) and wet-cold
 255 (0.47-0.90) places, while the lowest variability is seen in wet-
 256 warm places (0.70-0.88). CLM4.5, MATSIRO, WaterGAP2
 257 and H08 show the highest correlations overall (0.71-0.95 across
 258 all climate regions), while other models (CWatM, JULES-W1,
 259 LPJmL, PCR-GLOBWB) show lower and more variable correla-
 260 tions (0.35-0.85). Some models show a clear difference
 261 between the climate regions (e.g. JULES-W1; ρ_s : 0.35-0.85),
 262 while others show little variability (e.g. MATSIRO; ρ_s : 0.76-
 263 0.88). Groundwater recharge observations for Africa (52) and
 264 the largest global scale groundwater recharge dataset compiled
 265 up to date (53) suggest high to very high correlations (0.74-
 266 0.84) in dry-warm places, which is similar to most models
 267 except for PCR-GLOBWB. Observations (53) suggest no correla-
 268 tion (-0.04) for wet-warm places and low correlation for

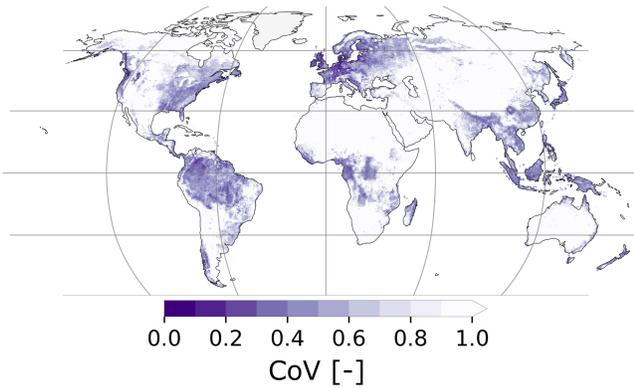
(a) Actual evapotranspiration



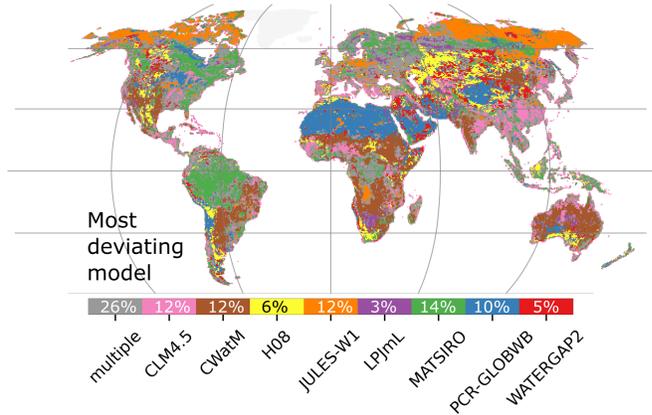
(d) Actual evapotranspiration



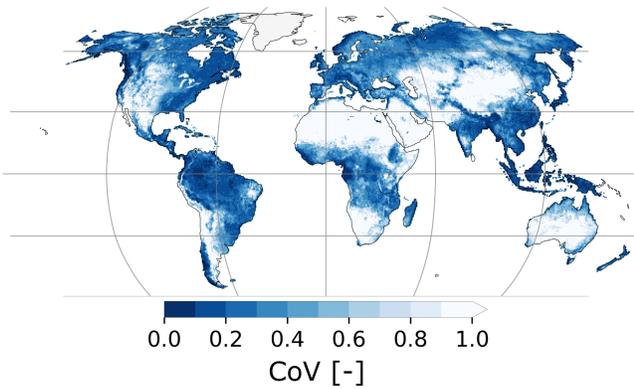
(b) Groundwater recharge



(e) Groundwater recharge



(c) Total runoff



(f) Total runoff

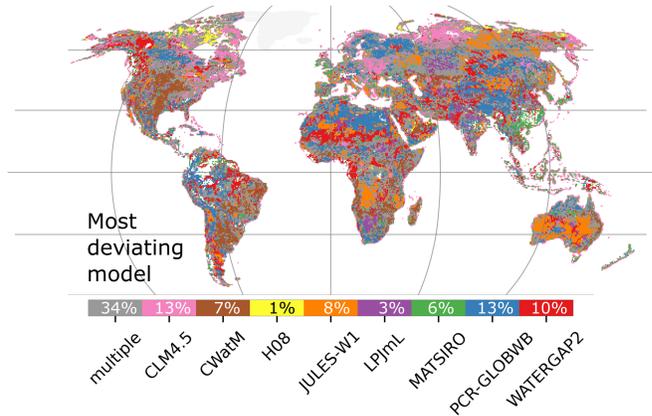


Fig. 1. Left: maps showing the coefficient of variation, calculated per grid cell as the standard deviation divided by the mean of the 8 models, for different water fluxes: actual evapotranspiration (a), groundwater recharge (b), and total runoff (c). Lighter areas ("white spaces"; see 36) indicate high CoV values and thus show where models disagree most. Right: maps showing which model deviates most from the ensemble mean for each grid cell and thus contributes the most to the CoV shown in (a)-(c) for different water fluxes: actual evapotranspiration (d), groundwater recharge (e), and total runoff (f). Dark gray areas in (d)-(f) indicate that multiple models deviate similarly strongly from the ensemble mean. Empty, white areas in (d)-(f) indicate that no model deviates strongly from the ensemble mean. The percentages shown in (d)-(f) refer to the fraction of grid cells (and not land area) covered by each model. Greenland is masked out for the analysis.

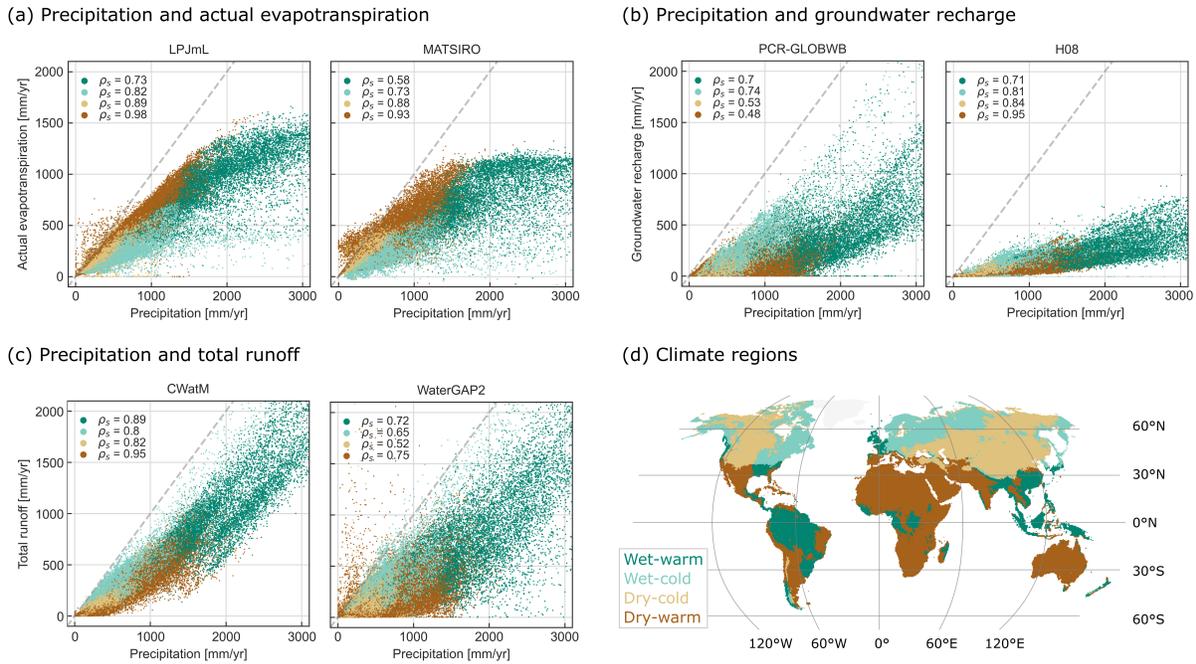


Fig. 2. Scatter plots that exemplarily show functional relationships for selected models and variables. Due to space constraints, we focus on a few examples with differing relationships. Scatter plots for all variable pairs are shown in Figures S18-23 in the Supporting Information. Variables shown are (a) precipitation and actual evapotranspiration for LPJmL and MATSIRO, (b) precipitation and groundwater recharge for H08 and PCR-GLOBWB, and (c) precipitation and total runoff for WaterGAP2 and CWatM. Each dot represents one grid cell and is based on the 30-year average of each flux. Spearman rank correlations ρ_s measure the strength of the relationship between forcing and response variables and are calculated for all grid cells within a climate region. Dots are colored according to the regions shown in (d). The definition of the climate regions can be found in the Materials and Methods section. The dashed line shows the 1:1 line, indicating the water limit assuming all water is supplied by precipitation. Some models have grid cells that exceed this water limit, for instance due to water transfers from neighboring cells. Detailed model-specific explanations are given in the Supporting Information.

269 dry-cold places (0.28), which disagrees with all models (Figure
270 3c and Table 1).

271 **Net radiation and groundwater recharge** Most models show clear
272 differences in magnitude and in ranking between the climate
273 regions, but there is no common pattern in their N - R -relationships (Figure 3d and Table S3). We find the largest
274 variability in dry-cold places (ρ_s : -0.35 - 0.51) and the lowest
275 variability in wet-warm places (0.23-0.54). The mostly positive
276 rank correlation between groundwater recharge and net
277 radiation suggests that higher net radiation is associated with
278 more groundwater recharge. This is counter-intuitive, but can
279 be explained by the positive correlation between net radiation
280 and precipitation (ρ_s : 0.48-0.77 for the four climate regions;
281 see Figure S1 in the Supporting Information).
282

283 **Precipitation and total runoff** The models show mixed agree-
284 ment in their P - Q -relationships (Figure 3e and Table S3).
285 LPJmL, H08, and CWatM show very high correlations (0.77-
286 0.95) for all climate regions, while WaterGAP2 and PCR-
287 GLOBWB show the lowest correlations overall (0.52-0.75).
288 Almost all models show higher correlations for warm places
289 (0.71-0.95) than for cold places (0.52 to 0.82), so the primary
290 distinction here is between warm and cold, and not between
291 wet and dry as for evapotranspiration. This ranking agrees
292 with the Budyko equation and GRUN (an observation-based
293 global gridded runoff dataset; 54), but not with GSIM (data
294 from the global streamflow and metadata archive; 55, 56).
295 The Budyko equation predicts high correlations for all climate
296 regions (0.87-0.99), while GSIM (0.73-0.89) and GRUN (0.28-
297 0.93) show more variability and a different ranking between

the climate regions. Most disagreement can be found in dry-
298 cold places, both between models (ρ_s : 0.52-0.82) and between
299 GRUN (0.28), GSIM (0.89) and Budyko (0.90) (Figure 3e and
300 Table 1).
301

302 **Net radiation and total runoff** The ranking is mostly consistent
303 and all models show rather large variability in their N - Q -
304 relationships between the climate regions (Figure 3f and Table
305 S3). Dry-cold places have low to negative correlations (-0.18 -
306 0.14), wet-warm and wet-cold places have low to medium
307 correlations (0.16-0.50), and dry-warm places have the highest
308 correlations overall (0.12-0.73). This tendency agrees with
309 the Budyko equation (Figure 3f and Table 1). Similar to
310 groundwater recharge, the mostly positive correlation between
311 total runoff and net radiation suggests that higher net radiation
312 is associated with more runoff, which can be explained by the
313 positive correlation between net radiation and precipitation.

314 Discussion

315 **To what extent do key water fluxes simulated by global water
316 models disagree with each other, and how does the disagree-
317 ment vary spatially?** Overall, we find the strongest model
318 disagreement for groundwater recharge (mean grid cell CoV
319 = 1.17), some disagreement for total runoff (mean grid cell
320 CoV = 0.54), and the best agreement for evapotranspiration
321 (mean grid cell CoV = 0.23). This is not unexpected, as
322 groundwater recharge is arguably the least understood process
323 (53, 58) and it is often represented in a rather simplified way
324 in the models (59). Another reason might be that – averaged
325 globally – actual evapotranspiration is the largest flux and

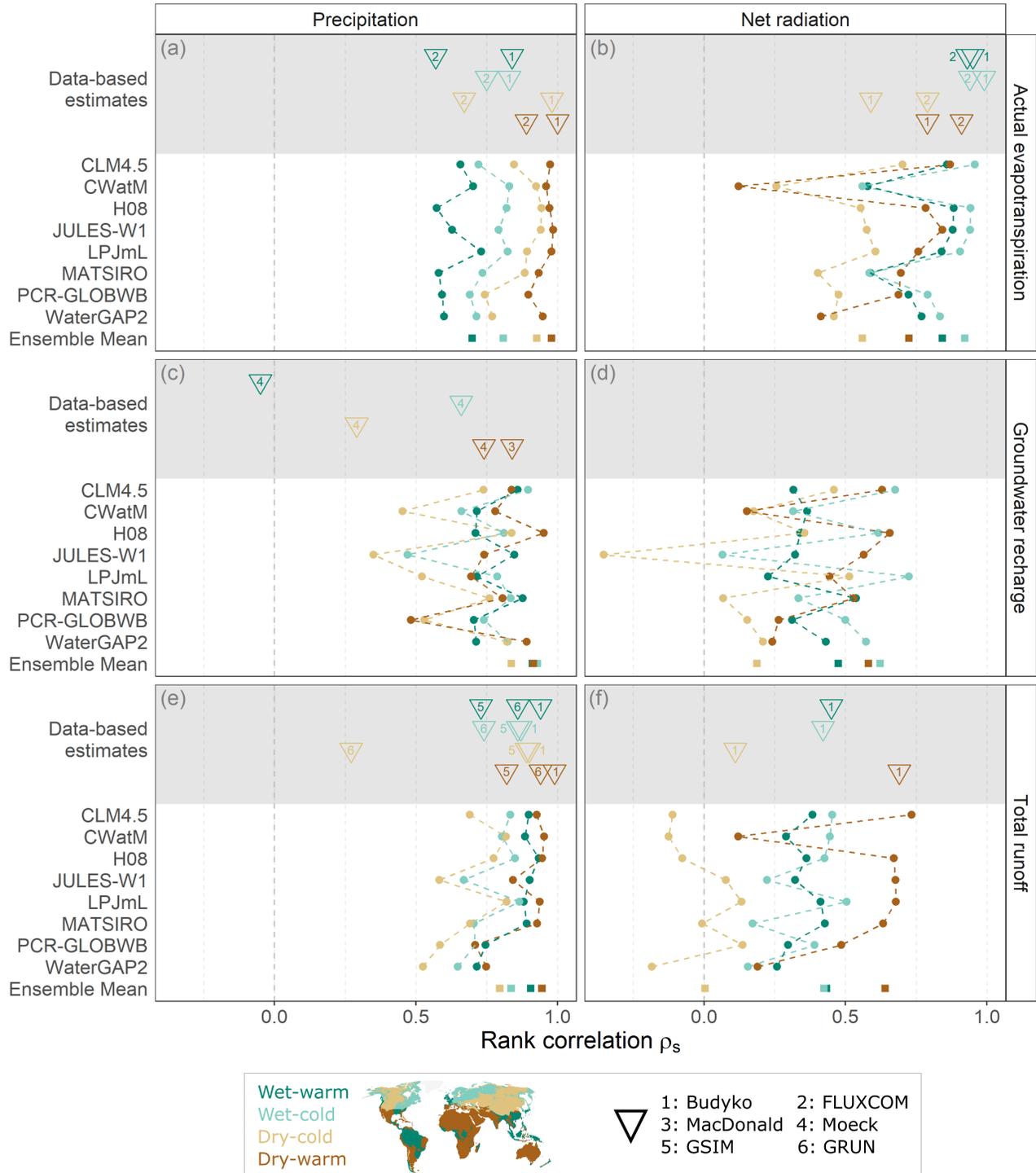


Fig. 3. Spearman rank correlations ρ_s between forcing variables (precipitation, net radiation) and water fluxes (actual evapotranspiration, groundwater recharge, and total runoff), divided into different climate regions. Net radiation for LPJmL and PCR-GLOBWB is not available and is estimated as the median of the other models (per grid cell). The lines connecting the dots are only there as a visual aid. The numbered triangles show observation-based rank correlations, with numbers indicating the corresponding data source (see Table 1). Observation-based rank correlations are only shown if they are based on more than 50 data points.

Table 1. Spearman rank correlations ρ_s between forcing variables and water fluxes and number of observations based on different observation-based datasets and the Budyko equation. The percentage of grid cells per climate region is given in brackets. The Budyko equation was forced per grid cell with the same forcing as the models (indicated by *), and thus covers approximately the same extent as the models (except for cells with negative net radiation). The gridded datasets (FLUXCOM, GRUN) are available at the same resolution as the models and thus also cover approximately the same extent (except for non-vegetated areas in the case of FLUXCOM). This is indicated by *m.e.* for model extent. For datasets without matching precipitation data, we used GSWP3 reanalysis data. *Number* corresponds to the numbers used in Figure 3. FLUXNET rank correlations and the MacDonald rank correlation for the wet-warm region are shown in brackets because of the very small sample sizes (50 or less); they are not shown in Figure 3. Dashes (-) indicate that correlations could not be calculated because no observations were available. Details can be found in the Materials and Methods section.

Water flux	Forcing	Source	Number	Wet-warm (15%)		Wet-cold (23%)		Dry-cold (28%)		Dry-warm (34%)	
				ρ_s	Count	ρ_s	Count	ρ_s	Count	ρ_s	Count
E_a	P	Budyko* (50)	1	0.84	m.e.	0.83	m.e.	0.98	m.e.	1.00	m.e.
E_a	P	FLUXCOM (51)	2	0.57	m.e.	0.75	m.e.	0.67	m.e.	0.89	m.e.
E_a	P	FLUXNET (57)	-	(0.72)	13	(0.36)	50	(0.57)	15	(0.51)	47
E_a	N	Budyko* (50)	1	0.95	m.e.	0.99	m.e.	0.59	m.e.	0.79	m.e.
E_a	N	FLUXCOM (51)	2	0.93	m.e.	0.94	m.e.	0.79	m.e.	0.91	m.e.
E_a	N	FLUXNET (57)	-	(0.67)	13	(0.42)	50	(0.72)	15	(0.41)	47
R	P	MacDonald (52)	3	(0.0)	4	-	0	-	0	0.84	130
R	P	Moeck (53)	4	-0.05	234	0.66	83	0.29	100	0.74	4772
Q	P	Budyko* (50)	1	0.94	m.e.	0.87	m.e.	0.90	m.e.	0.99	m.e.
Q	P	GSIM (55, 56)	5	0.73	1438	0.86	1255	0.89	593	0.82	1207
Q	P	GRUN (54)	6	0.86	m.e.	0.74	m.e.	0.27	m.e.	0.94	m.e.
Q	N	Budyko* (50)	1	0.45	m.e.	0.42	m.e.	0.11	m.e.	0.69	m.e.

thus its relative variability might be smaller than that of total runoff and especially groundwater recharge. The models disagree particularly in dry regions (e.g. Australia, outer-tropical Africa) and in cold regions (e.g. most of continental Asia and North America). This echoes existing literature (e.g. 1, 26, 60) and highlights the need for model refinement in dry and/or cold regions, which are under-researched and strongly affected by climate change (61, 62).

The disagreement between global water models underscores the importance of using a model ensemble to account for model uncertainty (6, 8, 10, 11, 24, 63). However, creating such an ensemble is not straightforward (64). The use of a simple ensemble mean for each grid cell leads to higher correlations overall, sometimes even higher than any individual model (e.g. Figure 3c for wet-warm and wet-cold regions). This is because averaging smooths out variability in the forcing-response relationships compared to individual models (see Figure S26). This finding challenges, in line with Zaherpour et al. (60), the notion that the (unweighted) ensemble mean leads to more robust model estimates. Assigning meaningful weights to models or removing models from the ensemble (1, 65) is also not straightforward. Since no model consistently deviates the most, and since the most deviating models differ between the three fluxes (see Figure 1d-f), model weights would have to vary spatially and for each flux. Without more in-depth analyses it is probably best to use the ensemble spread to capture a wide range of behaviors, while acknowledging that even the ensemble spread might not capture all epistemic uncertainties (66).

How do global water models translate forcing variables into key water fluxes, i.e. which functional relationships do they represent? Our evaluation shows that models differ substantially in the way they translate forcing variables into key water fluxes (see Figure 3 and Table S3).

For precipitation and actual evapotranspiration, the models show the same ranking between climate regions and rather small differences in magnitude, indicating that actual evapotranspiration is strongly constrained by the available water for all models. We find more variability for net radiation and evapotranspiration, with CWatM and WaterGAP2 showing particularly low correlations for dry-warm regions (0.12 and 0.41, respectively), while all other models show much higher correlations (0.69-0.87). There is no obvious correspondence between the potential evapotranspiration scheme used (e.g. Priestley-Taylor for LPJmL and WaterGAP2, or Penman-Monteith for JULES-W1 and CWatM) and the rank correlations, implying that other factors also play an important role (see also 27, 63). It is worth noting that net radiation differs between models (Table S4), which adds uncertainty to this analysis but also highlights that the models already translate the same incoming total radiation differently into net radiation. This warrants a closer look in future studies, since a realistic depiction of the energy balance is important for climate change studies (67).

For precipitation and groundwater recharge, some models (CLM4.5, MATSIRO, WaterGAP2 and H08) show high to very high correlations (0.71-0.95) for all climate regions, suggesting that precipitation is the dominant control on groundwater recharge across all climate regions in these models. Other models (CWatM, JULES-W1, LPJmL, PCR-GLOBWB) show much lower and more variable correlations (0.35-0.85), suggesting different controls on groundwater recharge (e.g. model structural decisions and parameterizations). This difference can also be seen in Figure 2b, where H08 has a much tighter P - R -relationship than PCR-GLOBWB. H08 and WaterGAP2 use the same approach to calculate recharge (59) and they show almost the same rank correlations, indicating that the functional relationships might be related to the model structure in this case. We find high variability, and mostly positive

395 correlations, for net radiation and groundwater recharge. The
 396 models probably produce more groundwater recharge in re-
 397 gions with higher net radiation because precipitation is also
 398 higher in these regions. While it is difficult to interpret these
 399 correlations, the large variability still suggests considerable
 400 differences between models.

401 For precipitation and total runoff, WaterGAP2 and PCR-
 402 GLOBWB both show lower correlations (0.52 to 0.75) than
 403 most other models (0.77 to 0.95 for CLM4.5, CWatM, H08,
 404 LPJmL, and MATSIRO). This suggests clear differences in
 405 how strongly total runoff is controlled by precipitation and in
 406 how these models generate runoff, echoing Bierkens (68), who
 407 highlighted runoff generation as main area for model improve-
 408 ment. This difference can also be seen in Figure 2c, where
 409 CWatM shows a much tighter P - Q -relationship than Water-
 410 GAP2. WaterGAP2 is the only model here that is calibrated
 411 against streamflow observations (59), which might explain why
 412 it shows the lowest rank correlations for total runoff. For total
 413 runoff, it is challenging to relate model structure to functional
 414 behavior, since it consists of different runoff components. Ana-
 415 lyzing the different runoff components individually might shed
 416 more light on how different process conceptualizations (e.g.
 417 dependence of surface runoff on antecedent wetness) affect
 418 model behavior. Similar to groundwater recharge, we find
 419 mostly positive correlations for net radiation and total runoff,
 420 probably because precipitation is higher in regions with higher
 421 net radiation.

422 While rank correlations expose clear differences between
 423 models, our approach here should be seen as a first step in
 424 quantifying functional relationships. Rank correlations only
 425 measure how strongly two variables are related to each other
 426 and they only capture uni-directional dependencies. Hence
 427 they cannot capture all the possible differences (e.g. differences
 428 in average flux magnitudes, visible in Figure 2 and quantified
 429 in Table S4 in the Supplementary Information). For example,
 430 since precipitation and net radiation are correlated, we should
 431 not conclude that higher net radiation causes more ground-
 432 water recharge or runoff. More generally, rank correlations
 433 themselves cannot always be easily explained by underlying
 434 mechanisms. Future studies should aim at getting a better
 435 mechanistic understanding of the patterns found here and
 436 explore additional ways to quantify functional relationships,
 437 including the use of machine learning methods.

438 Can we use data and existing knowledge to derive functional 439 relationships and use them to constrain expected model be- 440 havior?

441 The Budyko equation (50) assumes complete depen-
 442 dence on aridity (here defined as N/P) and likely presents an
 443 upper limit in terms of correlations. It should thus be seen
 444 as a useful comparison, but not as the "correct" model, given
 445 that different studies have shown that climate seasonality (69),
 446 vegetation type (70), snow (71), and inter-catchment ground-
 447 water flow (72) can affect the long-term water balance beyond
 448 aridity. Models and data reflect water- and energy-limited con-
 449 ditions, but tend to show lower correlations than the Budyko
 450 equation (Figure 3). An exception are dry-cold regions, for
 451 which FLUXCOM data show a stronger N - E_a -relationship
 452 and a weaker P - E_a -relationship. This might be due to a poor
 453 representation of energy balance processes in cold places by
 454 the Budyko equation (73) and in current models (67).

455 The Budyko framework also assumes that long-term runoff
 only depends on aridity. Consequently, we find higher corre-

456 lations for the Budyko equation than for both datasets and
 457 most of the models. We again find large differences in dry-
 458 cold regions (see also 1), where GRUN shows a much weaker
 459 P - Q -relationship than the models and GSIM.

460 Recent studies have shown a strong influence of precipita-
 461 tion and aridity on groundwater recharge (52, 53). While our
 462 results also suggest that precipitation is an important control
 463 on groundwater recharge, they show that models tend to over-
 464 estimate the strength of that control, especially in wet-warm
 465 regions and to a lesser extent in dry-cold regions. Perceptual
 466 models of groundwater recharge generation usually include
 467 climate, but also soil characteristics, topography, and land
 468 use (74). Recently, Cuthbert et al. (75) found that local
 469 hydrogeology influences P - R -relationships in Africa, though
 470 this is difficult to generalize to larger regions given limitations
 471 in global datasets (25). In line with those findings, our results
 472 strongly suggest that models overestimate the degree to which
 473 climate forcing variables control groundwater recharge.

474 We have collected several observational or observation-
 475 driven datasets to derive empirical forcing-response relation-
 476 ships, but there remain some challenges. Observation-based
 477 estimates contain uncertainty, inherited from the observational
 478 datasets themselves and due to small numbers of observations
 479 in certain regions. Since not all datasets come with corre-
 480 sponding forcing and response variables, we sometimes had
 481 to pair observations with other forcing datasets, which can
 482 introduce additional uncertainty (see Materials and Methods
 483 for an extended discussion). Looking ahead, the gaps in the
 484 observation-based correlations shown in Table 1 are a first step
 485 to identify regions and variables where more measurements
 486 would be especially useful to constrain expected functional
 487 relationships. In addition, more quality-controlled datasets
 488 with uncertainty estimates (e.g 52) are critical to obtain real-
 489 istic uncertainty estimates for functional relationships. This
 490 would ultimately allow us to obtain robust ranges of functional
 491 behavior which we can benchmark our models against.

492 **A global perspective for global models.** Using functional re-
 493 lationships shifts the focus away from evaluating model per-
 494 formance in specific locations and from matching historical
 495 records to a more diagnostic and process-oriented evaluation
 496 of model behavior (76). Functional relationships allow us to
 497 focus on larger-scale assessments and to explore if dominant
 498 controls in the models are consistent with observations, theory
 499 and expectations, i.e. our perceptual model (36). This is
 500 critical for ensuring that models faithfully represent real-world
 501 systems, leading to more credible projections of environmental
 502 change impacts.

503 An advantage of functional relationships is that they relate
 504 different locations to each other, and thus take information
 505 out of its location-specific context and put it to a more large-
 506 scale use. However, the uneven distribution of observations
 507 poses challenges if we want to derive robust relationships. For
 508 example, recharge measurements have almost entirely been
 509 made in warm dry regions (97% of MacDonald et al. (52) and
 510 92% of Moeck et al. (53)). Streamflow measurements have
 511 been made more frequently in wet regions (60% of the GSIM
 512 data (55, 56) used here) and globally, there is a placement
 513 bias of stream gauges towards wet regions (77), even though
 514 – according to our classification – short of two-thirds of the
 515 global land area are dry. While there are clear reasons for
 516 this spatial bias, we will have to explore how this bias affects

517 functional relationships and how to most effectively enlarge
518 our observational database.

519 In this study, we have focused on rank correlations between
520 long-term averages of two forcing variables and three water
521 fluxes, but this approach can easily be extended. Other vari-
522 ables, including state variables or stores (e.g. soil moisture, ter-
523 restrial water storage), possibly investigated at different time
524 scales (e.g. monthly), should yield additional insights. There
525 are existing metrics such as elasticities (34) that lend them-
526 selves for such an analysis, and there is room for new methods
527 to be developed (e.g. characterizing thresholds in forcing-
528 response relationships). Expanding our range of functional
529 relationships, constrained by various observational datasets
530 and expert knowledge, might eventually give us a knowledge
531 base of realistic system behavior that can be used to evaluate
532 models and diagnose model deficiencies, comparable to the
533 use of emergent constraints in climate modeling (78).

534 More generally, functional relationships invite us to think
535 about how the global water cycle functions, what we know,
536 what we do not know, and what that means for a future under
537 climate change (36). Our results here suggest that improved
538 process understanding will be particularly important for energy
539 balance processes, recharge processes, and generally in dry
540 and/or cold regions. So how can we improve our process
541 understanding? In 1986, Eagleson (79) stated that "science
542 advances on two legs, analysis and experimentation, and at
543 any moment one is ahead of the other. At the present time
544 advances in hydrology appear to be data limited". For some
545 processes, this still seems to be the case. But clearly, we have
546 a wealth of data available and might ask ourselves: are we
547 extracting enough information from the observations we have?
548 Are there hydrological regularities yet to be found (80)? Even
549 if the search for such regularities is challenging, it might be a
550 fruitful and exciting endeavor for global hydrology.

551 Materials and Methods

552 **Model data retrieval and processing.** We analyzed 30-year (clima-
553 tological) averages (1975-2004) from 8 global water models (49):
554 CLM4.5 (41), CWatM (42), H08 (43), JULES-W1 (44), LPJmL
555 (45), MATSIRO (46), PCR-GLOBWB (47), and WaterGAP2 (48).
556 The model simulations were carried out following the ISIMIP 2b
557 protocol and here we used model outputs forced with the Earth
558 system model HadGEM2-ES under historical conditions (historical
559 climate and CO₂ concentrations). We used precipitation P (ISIMIP
560 variable name pr), net radiation N , actual evapotranspiration E_a
561 (ISIMIP variable name $evap$), groundwater recharge R (ISIMIP
562 variable name qr) and total runoff Q (ISIMIP variable name $qtot$).
563 Note that Q here refers to runoff generated on the land fractions
564 (and not surface water bodies) of each grid cell and does not include
565 upstream inflows, which allows for comparison to grid cell P . P ,
566 E_a , R , and Q were downloaded from <https://data.isimip.org/>. Net
567 radiation N is not an official ISIMIP output and was provided by
568 the individual modeling groups. It is not available for all models, so
569 we used the ensemble mean per grid cell for models without N data.
570 We converted all fluxes to mm/y and removed E_a values larger than
571 10000 mm/y and set R values smaller than 0 to 0. A more detailed
572 description is given in the Supporting Information.

573 **CoV and most deviating model maps.** For each grid cell, we calcu-
574 lated the coefficient of variation (CoV) by dividing the standard
575 deviation by the mean using the 8 model outputs. Maps of the
576 standard deviation are shown in the Supporting Information (Fig-
577 ures S5-7). To see which model dominates the ensemble spread, we
578 checked for each grid cell which model shows the largest absolute
579 difference (denoted by d_1) from the ensemble mean (denoted by μ).

To see if multiple models dominate the ensemble spread, we also
checked for each grid cell which model shows the second largest
absolute difference (denoted by d_2) from the ensemble mean. If
the relative difference between the largest and the second largest
difference is less than 20%, i.e. $(d_1 - d_2)/d_1 < 0.2$, the grid cell
falls into the category "multiple". If the relative difference between
the most deviating model and the ensemble mean is less than 20%,
i.e. $d_1/\mu < 0.2$, the grid cell is counted as having no most deviating
model (empty areas on Figure 1d-f).

Functional relationships. As a metric for the strength of the func-
tional relationships between model inputs and outputs, we use
Spearman rank correlations ρ_s for each climate region. The Spear-
man rank correlation is a measure of the monotonicity between two
variables and it is robust to outliers. We use the following categories
for correlations: negative (<0), no to low correlation (0 to 0.25),
medium correlation (0.25-0.5), high correlation (0.5-0.75), very high
correlation (0.75-1.0).

Climate regions Based on the aridity index (here defined as N/P),
a place is categorized as either wet ($N/P < 1$) or dry ($N/P > 1$).
Note that we used the ensemble median for N . Based on how
many days per year fall below a 1°C temperature threshold, a place
is categorized as either cold (more than one month below 1°C)
or warm (less than one month below 1°C). This results in four
categories: wet-warm (15% of model grid cells / 18% of modeled
area), wet-cold (23% / 15%), dry-cold (28% / 24%), and dry-warm
(34% / 43%). To test how different decisions affect our climate
region classification, we also used the ensemble median of potential
evapotranspiration E_p (partially downloaded, partially provided by
the modeling groups) to calculate the aridity index (E_p/P), and
we used a different threshold for our warm/cold distinction. This
resulted in little differences overall, as can be seen in the Supporting
Information (Figure S16).

Observational datasets and theory. For E_a , we used FLUXCOM
data (51) (RS monthly 0.5° from 2001-2015) paired with GSWP3 P
data (81) (downloaded from <https://data.isimip.org/>), and FLUXNET
data (57) which include matching P data. For R , we used data
from MacDonald et al. (52) which include matching P data, and
data from Moeck et al. (53) paired with GSWP3 P data (81). For
 Q , we used GRUN data (54) from 1985-2004 paired with GSWP3 P
data (81), and GSIM data (55, 56) from catchments with areas from
250-25000 km² with minimum 10y of data to ensure a sufficient
number of catchments that do not differ too much in size from the
model grid cells. We paired GSIM data with catchment-averaged
MSWEP P data (82), which were calculated by Stein et al. (83).

To obtain theory-based estimates for E_a and Q , we forced the
Budyko (50) equation (Eq.1) with HadGEM2-ES P and ensemble
median N from the ISIMIP 2b models analyzed here.

$$\frac{E_a}{P} = \sqrt{\frac{N}{P} \tanh\left(\frac{P}{N}\right) \left(1 - \exp\left(-\frac{N}{P}\right)\right)} \quad [1]$$

More details on data processing and quality checks can be found in
the Supporting Information.

Extended discussion on model forcing and scenario uncertainty. The
choice of forcing product and differences in the treatment of human
influences (e.g. water use and dams) might affect the functional
relationships exhibited by the models. To get an idea how much uncer-
tainty this introduces, we calculated correlations using WATCH-
WFDEI forcing with either variable historical conditions (varsoc) or
no human influences (nosoc) for WaterGAP2 and PCR-GLOBWB,
carried out following the ISIMIP 2a protocol. The results, shown in
the Supporting Information, stay essentially the same, suggesting
that the model-based correlations are robust signatures of model
behavior.

Extended discussion on data uncertainty. Since not all datasets come
with matching P data, we sometimes paired the observations with
GSWP3 reanalysis data (81). To get an idea how much uncertainty
this introduces, we calculated rank correlations using different P
data sources. Correlations calculated using the MacDonald et al.
(52) R data with either GSWP3 P data or the accompanying P data
are very similar for dry-warm places (0.83 and 0.84; see Supporting

644 Information). Using HadGEM2-ES P (the model forcing) data
 645 instead of GSWP3 P data to calculate correlations with FLUXCOM
 646 E_a (51), Moeck R (53), and GRUN Q (54), respectively, results
 647 in virtually no differences (results are shown in the Supporting
 648 information). This indicates that the correlations are robust, likely
 649 because rank correlations remain stable as long as relative differences
 650 between forcing values per grid cell stay the same.

651 **Code and data availability.** Model outputs can be accessed via the
 652 ISIMIP website (<https://www.isimip.org/>). Observational datasets can
 653 be accessed via the references shown in Table 1. Multi-annual
 654 averages and rank correlations will be uploaded to a repository
 655 and code can be found at [https://github.com/HydroSysPotsdam/Global_](https://github.com/HydroSysPotsdam/Global_model_evaluation)
 656 [model_evaluation](https://github.com/HydroSysPotsdam/Global_model_evaluation) (DOI for both will be created upon acceptance).

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