

1 Subsurface fracturing of sedimentary stones caused by bullet impacts

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10 This is a non-peer reviewed preprint submitted to Earth Arxiv. It has been
11 submitted to PLOS One for peer review.

12 ABSTRACT

13 The immovable nature of built heritage means that it is particularly vulnerable during times of armed
14 conflict. Although impacts from small arms and shrapnel leave relatively inconspicuous impact scars,
15 they may elevate the risk of future stone deterioration. This study investigates the subsurface damage
16 caused by bullet impacts, which is not apparent from surface inspection, in order to better understand
17 the geometry and mechanics of this form of conflict damage to heritage. Controlled firearm experiments
18 were conducted to simulate conflict damage to sandstone and limestone buildings. The bullet impacts
19 created conical fractures or zones of increased fracture intensity below the impact, radial fractures and
20 spallation, in addition to a crater. Dynamic fracture distinguishes the formation of these features from
21 quasi static cone crack experiments, while the lack of a shockwave differentiates these bullet impacts
22 from hypervelocity experiments. Damage was created by momentum transfer from the bullet, so that
23 differences in target properties had large effects on the nature of the damage. The crater in the limestone
24 target was almost an order of magnitude deeper than the sandstone crater, and large open fractures
25 formed in the limestone below the crater floor, compared with zones of increased fracture intensity in
26 the sandstone target. Microstructural analysis of subsurface damage showed that fracture intensity
27 decreased with increasing distance from the impact centre, suggesting that regions proximal to the
28 impact are at increased risk of future deterioration. Conical subsurface fractures dipping away from
29 the impact beneath multiple impact craters could link up, creating a continuous fracture network. By
30 providing pathways for moisture and other weathering agents, fractures enlarge the region at increased
31 risk of deterioration. Their lack of surface expression makes understanding their formation a vital part
32 of future surveying and post conflict assessments.

33 INTRODUCTION

34 The recent invasion of Ukraine has brought the damage and destruction caused by modern
35 weaponry to the forefront of public attention. Long range artillery and missiles cause significant
36 destruction to their targets, and shrapnel generated in explosions can damage surrounding structures.
37 Bullet impacts from small arms add further damage to buildings and monuments, especially during
38 urban firefights. Russian advances into Kyiv's western suburbs of Irpin, Bucha, and Hostomel in late
39 February 2022 led to urban tank and infantry battles, damaging multiple heritage sites and buildings
40 (Figure 1)(1,2).

41 There is a growing understanding of the nature of the surface damage caused by bullet and shrapnel
42 impacts, and its relationship to the subsurface damage. In a study of bullet and shrapnel impacts to
43 limestone walls and window ledges, Mol and Gomez-Heras (3) observed lower surface hardness
44 measurements in the regions surrounding impact craters and fractures than in areas of undamaged
45 stone. Ultra-pulse velocity measurements suggested an increase in subsurface fractures in regions
46 proximal to the surficial impacts (3). A controlled impact study by Gilbert et al. (4) found similar
47 reduced surface hardness near the surface crater caused by a bullet impact, as well as a spatial
48 correlation between increased surface permeability measurements and surface fractures and impact
49 crater. Microstructural analysis of the same sandstone sample found grain crushing at the floor of the
50 impact crater, as well as intra- and intergranular fracturing (5). Subsurface imaging from thin sections
51 showed fractures had a mix of inter- and intragranular pathways close to the crater floor, becoming
52 predominantly intergranular with increasing distance from the crater floor, with fracture intensity
53 decreasing with increasing distance from the crater centre (5). These studies show that extensive
54 subsurface damage can occur from bullet impacts, which is not readily appreciated from the surface

55 effects. However, details of subsurface damage from bullet impacts, and particularly the mechanisms
56 that cause it, are not known.



Figure 1: (a) Shrapnel damage to the facade of the St Nicholas Church caused by Russian shelling in the town of Irpin, a suburb to the NW of Kyiv in Northern Ukraine (2). (b) Impact damage to columns of the Alley of ATO Heroes memorial, also in Irpin. It is reported to have been fired upon intentionally by Russian forces in February 2022 (1, 2).

57 Fracturing within a rock mass reduces its overall strength, increases its effective porosity, and can
58 act as conduits for moisture ingress (6–8). Moisture can dissolve constituent grains and/or cement in
59 sedimentary rocks, widening pore spaces and further decreasing overall rock strength, exacerbating a
60 negative feedback loop of stone deterioration. Moisture also transports dissolved salts, which apply an
61 outward pressure upon crystallisation, weakening cement-grain boundaries and the cohesiveness of
62 the stone, resulting in material loss from the surface of the stone over time (9–13). Increased fracture
63 intensity enhances the progression of weathering fronts in granitic rocks (14). Other fracture
64 characteristics, such as aperture, orientation, and connectivity, influence stone permeability and the
65 flow of fluids (15). A thorough characterisation of internal damage caused by bullet impacts is therefore
66 important for understanding the vulnerability of stone to weathering processes and deterioration.

67 This study aims to characterise and quantify the subsurface damage caused by modern rifle bullets
68 in two sedimentary stone types, to understand the damage mechanisms, and to link the damage to
69 potential deterioration of built heritage. Observations of fracture morphology from optical thin sections
70 are combined with fracture intensity analysis of digitised fracture maps to examine how subsurface
71 damage changes with distance to the crater centre.

72 METHODS AND MATERIALS

73 *Impact Experiments*

74 Freshly quarried cubes (15 x 15 x 15 cm) of Stoneraise Red Sandstone (SRS) and Cotswold Hill Cream
75 Limestone (CHCL) were selected as the target lithologies because they are broadly representative of
76 sandstones and oolitic limestones used for construction. SRS is a fine-medium (0.125-0.5 mm), quartz
77 rich sandstone from the Permian New Red Sandstones (quarried near Penrith, U.K.). With a porosity of
78 11%, it is generally massive, with some target blocks exhibiting visible beds of coarser grains (~1 mm)
79 (Figure 2a). Target blocks have an average uniaxial compressive strength perpendicular and parallel to
80 bedding of 40.0 ± 5.9 MPa and 45.0 ± 13.1 MPa respectively (16). The average indirect tensile strength
81 parallel to bedding (loading direction perpendicular to bedding) measured via Brazil disc tests is $5.0 \pm$
82 0.3 MPa (16). CHCL is an oolitic grainstone from the Middle Jurassic Inferior Oolite (quarried near Ford,
83 U.K.). The average grain size is 0.5 mm and has a porosity of ~20% (Figure 2b). Target blocks have an
84 average uniaxial compressive strength perpendicular and parallel to bedding of 10.6 ± 1.5 MPa and $8.$
85 8 ± 2.1 MPa respectively (16). The average indirect tensile strength parallel to bedding (loading direction
86 perpendicular to bedding) measured via Brazil disc tests is 2.2 ± 0.2 MPa (16). Thin section micrographs
87 from undamaged samples of each lithology show no inherent fractures (Figure 2), showing that the
88 observed damage is the result of bullet impacts and not inherited.

89 Controlled firearm experiments were carried out at Cranfield Ordnance Test and Evaluation Centre
90 (Gore Cross, UK) to simulate conflict damage to stone. 7.62 x 39 mm (abbreviated in this study as AK-
91 47) is a commonly used ammunition cartridge fired from AK-variant rifles, such as the widely known
92 AK-47 and has been used in contemporary and past conflicts. Shots were fired from a fixed proof barrel
93 at incident angles of 90° to the target face. The AK-47 projectile has a spitzer ogive nose shape and is
94 comprised of a brass jacket and lead core weighing 7.95 grams (123 grains). Propellant loads for each
95 cartridge were adjusted to reduce velocity and simulate impacts at distances of 200 m (532 ms^{-1} for the
96 impact into the CHCL sample and 539 ms^{-1} for the impact into SRS). Average engagement distances in
97 urban firefights during the Iraq War ranged from 26 m to over 126 m between combatants, and most
98 soldiers are trained for engagement distances of 0 – 600 m, so 200 m represents a reasonable distance
99 for simulating impacts in both urban and open scenarios (17,18). The kinetic energy ($K_e = 1/2mv^2$) of the
100 projectile at impact will be ~1125 J for the CHCL experiment and ~1154 J for the SRS experiment.
101 Concrete blocks were placed on all faces, except the target face, for confinement. Target blocks with
102 bedding were oriented so that any bedding planes present were parallel to the target face (XY plane).

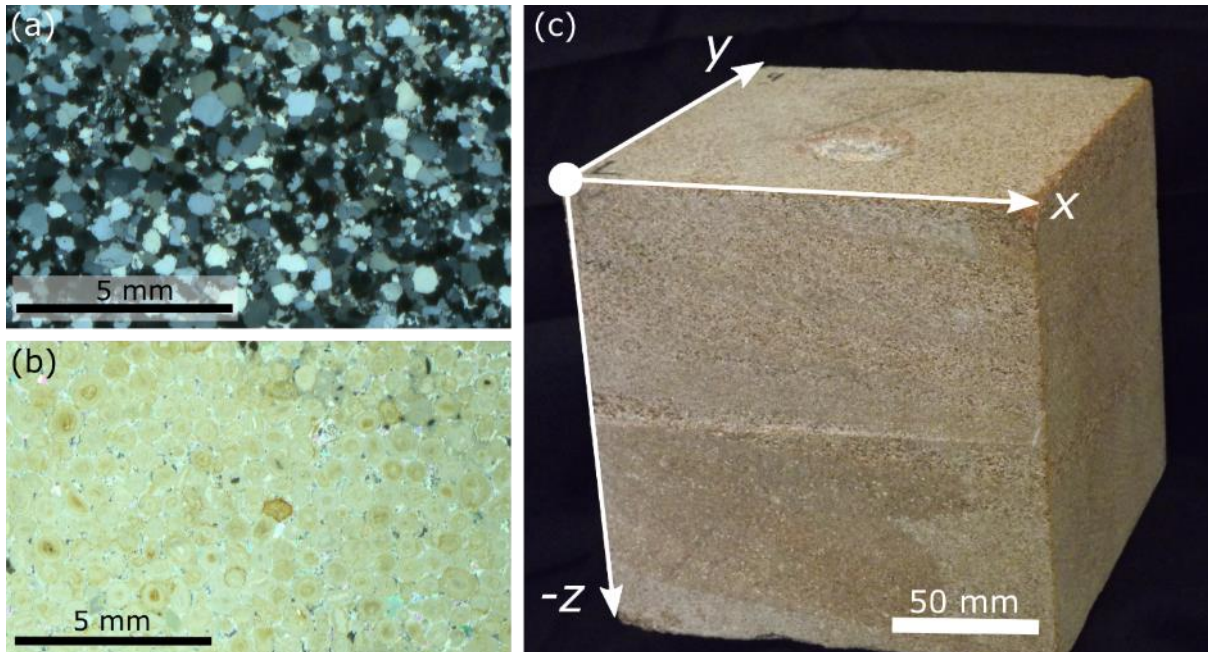


Figure 2: Thin section micrographs taken under cross polarised light of undamaged Cotswold Hill Cream Limestone (a), an oolitic limestone with an average grain size of 0.5 mm, and undamaged Stoneraise Red Sandstone under cross polarised light (b), a fine-medium grained (0.125-0.5 mm) quartz rich sandstone. Both lithologies show no inherent fracturing in the undamaged section. (c) Damaged target block of Stoneraise Red Sandstone indicating the reference scheme adapted from (19).

103 Microstructural Damage

104 A 3D reference scheme, adapted from Tikoff et al., (19), was employed to retain the spatial position
 105 of thin sections within the larger block. This enables the position of observations and measurements in
 106 3D space to be incorporated into analysis and interpretation. The target face of the sample is defined as
 107 the XY plane and the Z axis is orthogonal to this and negative into the block (Figure 2c). The crater
 108 centre is defined as the point at the centre of the crater floor, typically the deepest point, and is used as
 109 the reference location from which to measure distances to fractures and damage within the sample.

110 Polished thin sections were cut from damaged samples of SRS and CHCL parallel to the XZ plane
 111 and transecting the centre of the crater. A combination of large (75 x 50 mm) and small sections (28 x
 112 48 mm) were cut to maximise the coverage of impact related damage. Thin sections were scanned using
 113 an Epson Perfection 3170 photo scanner at 6400 dpi under plane and cross polarise light. Reflected light
 114 photomicrographs of each section were taken at x1 magnification using a Leica DM750P optical
 115 microscope fitted with a MC190HD camera. Microsoft ICE (Image Composite Editor) (version 2.0.3.0)
 116 was used to create a photo-mosaic of full sections. Complete photo-mosaics and thin section scans were
 117 georeferenced and fractures manually digitised in QGIS. Closed fractures were digitised as a single
 118 polyline and open fractures as a polygon to create a complete fracture map. Closed fractures are defined
 119 as fractures that, at the scale of observation, do not have a distinguishable aperture. Some thin sections
 120 were subject to material loss during section production, though every effort was made to prevent this.
 121 These regions were digitised and removed from the sampling area of later analyses. The fracture map

122 was thresholded into a binary image and the automatic fracture digitisation tool of NetworkGT (a QGIS
 123 plugin) used to generate a fracture network of polylines for analysis. This automatic digitisation
 124 approach ensures a consistent interpretation of fracture geometries and fracture characteristics across
 125 samples.

126 Different methods can result in varying values for important characteristics of fracture networks,
 127 such as length and orientation (20,21). Analysing fracture branches instead of full traces reduces this
 128 bias, as well as mitigating any censoring effects of the sample region because intersection with the edge
 129 only affects a single branch, instead of a full fracture trace (20). A sample grid of systematically spaced
 130 points 0.25 mm apart, each with a sampling radius of 0.75 mm, was created within the outlines of each
 131 thin section, excluding areas of material lost during section production.

132 P_{xy} values provide a useful measure of fracture damage that can be compared between lithologies.
 133 P_{xy} values characterise fracture frequency, intensity and volume, depending on the dimensions
 134 analysed. x represents the dimension of the sampling region and y the dimension of measurement
 135 (22,23). For example, P_{21} is a measure of fracture length (L) per area (A):

$$136 \quad P_{21} = \Sigma L / A \quad (1)$$

137 Uncertainty in the distance from the crater centre measurements is estimated to be ± 2 mm, which
 138 combined with the uncertainty in the digitisation of fracture networks, results in the fracture intensity
 139 uncertainties presented in Table 1. A full description of uncertainty methodology is available in
 140 Appendix 1. Fracture orientations are weighted based on fracture length and presented on equal area
 141 rose diagrams.

Sample	Max Uncertainties (mm ⁻¹)		Average Uncertainty (mm ⁻¹)
SRS_09	- 0.0101	+ 0.0720	+ 0.0004
CHCL_09	- 0.0178	+0.018	+ 0.0005

Table 1: Summary of the uncertainty values for fracture intensity measurements from Stoneraise Red Sandstone (SRS) and Cotswold Hill Cream Limestone (CHCL) target lithologies.

142 RESULTS

143 Sandstone Target

144 The sandstone sample (SRS_09) has a shallow, bowl shaped crater with an area equivalent diameter
 145 of 40 mm and a maximum depth of 5.1 mm (24). 20 mm directly below the crater floor is an open (<1.5
 146 mm) fracture that is 16 mm in length, but does not reach the edge of the section (Figure 3a). 80 mm
 147 directly below the crater centre there is an open fracture with a minimum aperture of 1.4 mm.
 148 Maximum aperture cannot be determined because the upper fracture wall shows evidence of material
 149 loss from sectioning (Figure 3a, b). Both of these open fractures are sub-parallel to the orientation of
 150 beds defined by grain size changes, $\sim 5^\circ$ from the target face (XY plane i.e. $90^\circ/270^\circ$ relative to the Z axis

151 in the thin sections). Two dominant orientations of fractures become apparent from the rose diagram:
 152 the first are, as described above, sub-parallel to the bedding orientation of $90^{\circ}/270^{\circ}$, while the second
 153 group is approximately orthogonal to this, with orientations $0^{\circ}/180^{\circ}$ (Figure 3c).

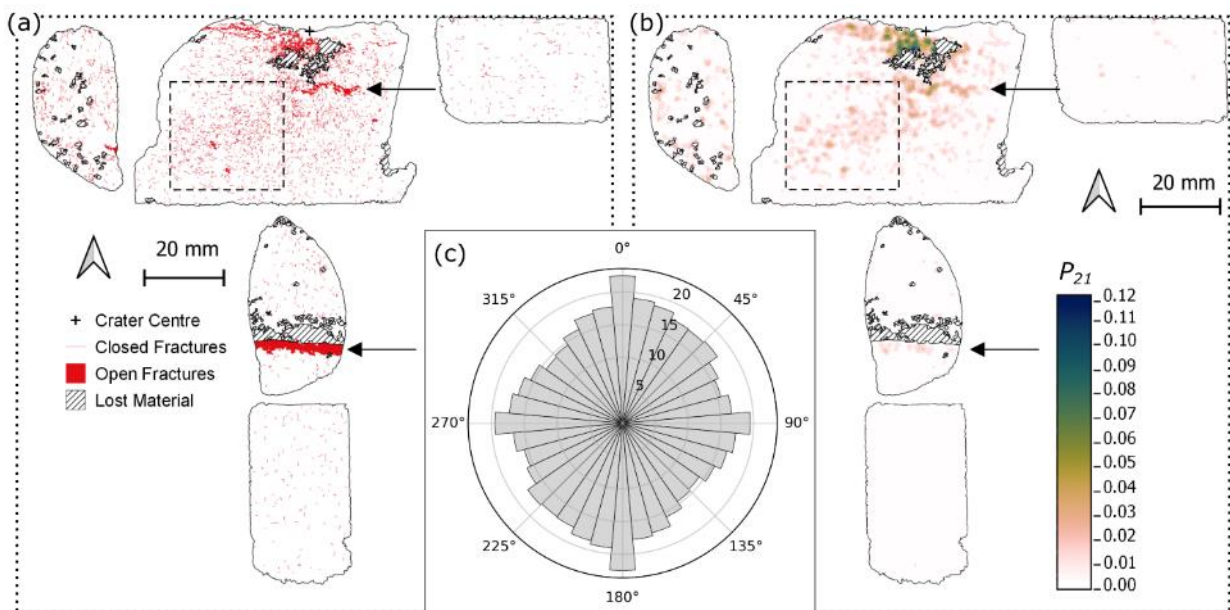


Figure 3: Fracture map (a) through the centre plane (XZ) of a Stoneraise Red Sandstone sample (SRS_09). Open fractures (solid red regions) are visible oriented sub-parallel to the target surface close to the impact crater, at a depth of 20 mm and ~80 mm below the crater (black arrows). There is a high number of closed (red line) fractures within a 7 mm radius of the crater centre. (b) Map of P_{21} fracture intensity values across the thin sections. The highest values (dark blue) are within 7 mm of the crater centre. There is a region of relatively higher fracture intensity (dashed square) with an approximate orientation of $35^{\circ}/215^{\circ}$. For both maps impact direction is top to bottom and the original block outline is shown as a dotted line. (c) Equal area rose diagram showing the orientation of all fractures, weighted for fracture length, mapped within the sandstone sample. Radial scale is the square root of frequency.

154 Directly below the crater centre is a zone of primarily closed intra- and trans-granular fractures,
 155 forming a region of intense fracturing that extends to a depth of ~ 7 mm below the crater floor (Figure
 156 4a-e). The highest P_{21} fracture intensity value calculated (0.124) is in this region, 5.9 mm away from the
 157 crater centre (Figure 3b, 5d). Many grains exhibit multiple closed fractures that originate at contact
 158 points with adjacent grains, forming connected networks across multiple grains. Open extensional
 159 fractures are visible just beneath the crater floor traversing from the crater centre towards the rim
 160 (Figure 4f-g). These fractures have both inter- and trans-granular pathways, with no measurable lateral
 161 displacement between fracture walls. They are primarily sub-parallel to the target face of the samples
 162 (Figure 4h). In the top central section there appears to be a band of damage stretching from the SW
 163 corner of the section to an area of material loss directly below the crater centre (Figure 4a, i-k). The band
 164 has an approximate orientation of $35^{\circ}/215^{\circ}$.

165 There are few fractures in the thin sections further than 80 mm below the crater floor, and those
 166 present are short, intra-granular fractures, typically confined to a single grain. This is visible in the small
 167 peak in P_{21} intensity at 80 mm below the crater centre (the large open fracture), followed by very low
 168 intensity values with increasing distance from the crater centre (Figure 5a).

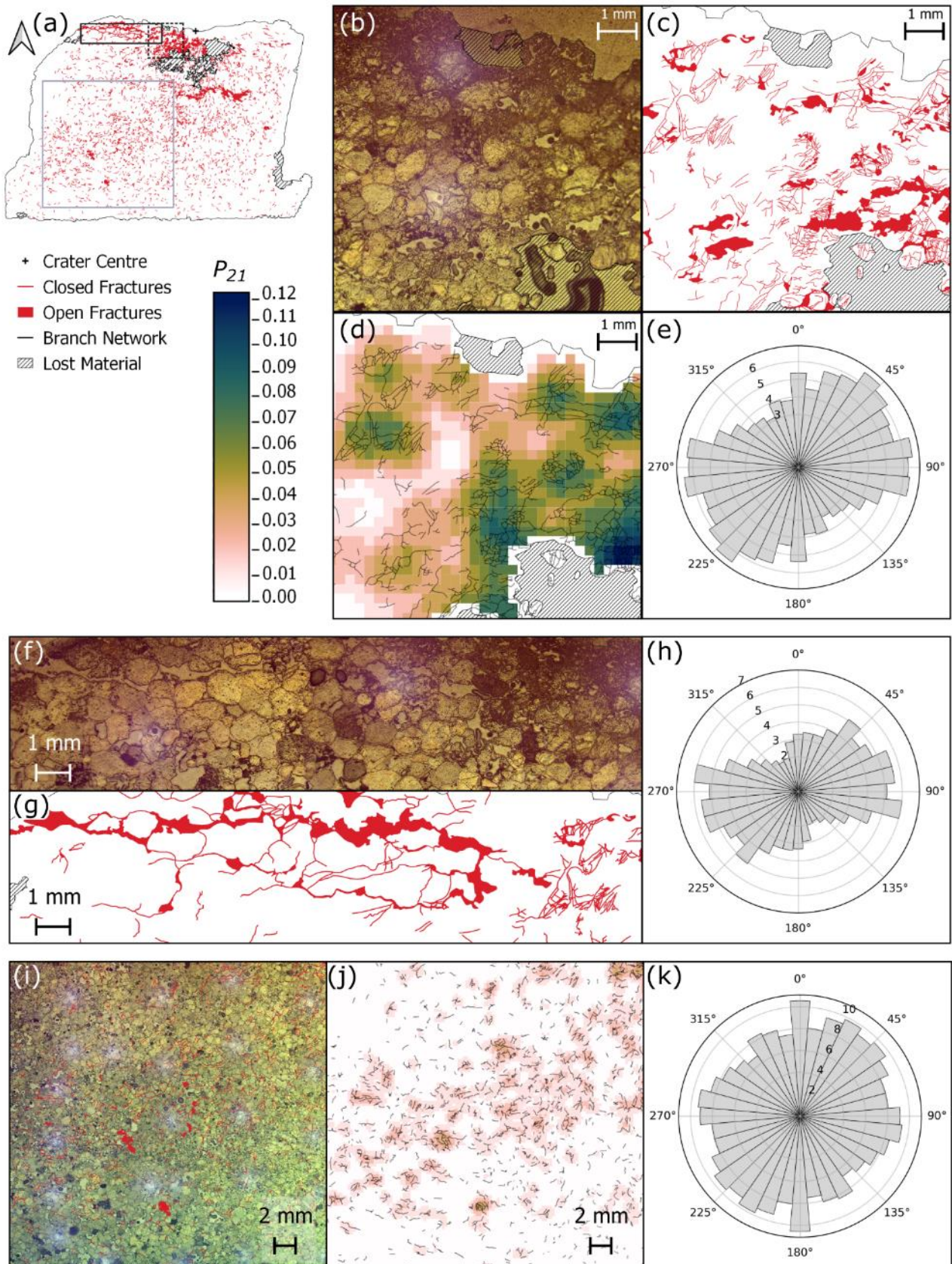


Figure 4: (previous page) (a) Fracture map of the thin section through the impact crater in Stoneraise Red Sandstone (SRS_09), showing closed and open fractures (red). Dashed box shows the location of panels (b-e). Solid black box outlines the location of panels (f-h). Grey box shows the location of panels (i-k). (b) Reflected light photomicrograph showing substantial grain crushing (top of frame) at the crater floor and a high number of trans- and intergranular fractures in the region beneath. Interconnected fracture pathways are seen in the fracture map in panel (c). The highest fracture intensity value (0.124) is observed in the lower right of the P_{21} intensity map (d), 5.9 mm from the crater centre (out of frame towards the top right). Topology parameters were calculated using the branch network (black lines) interpreted by the NetworkGT plugin based on a threshold image of the digitised fractures (red lines). The orientations of the digitised fracture network show a slight predominance in orientation around $45^{\circ}/225^{\circ}$ and $90^{\circ}/270^{\circ}$. (f-g) Reflected light micrograph and corresponding fracture map of open, extensional fractures directly below the crater edges. Fractures are oriented sub-parallel to the target face as seen in the rose diagram for the region (h). (i) Reflected light photo micrograph and fracture network showing a region of fracturing from below the crater to the SW corner of the central section. (j) P_{21} fracture intensities and NetworkGT branch map for the same region. There appears to be a slight trend of fracture orientations from $45^{\circ}/225^{\circ}$ (k), though the dominant orientation for the region is perpendicular to the target face. All rose diagrams (e, h, k) are plotted as equal area diagrams, orientation frequency is weighted for fracture length, and the radial scale is the square root of the weighted frequency.

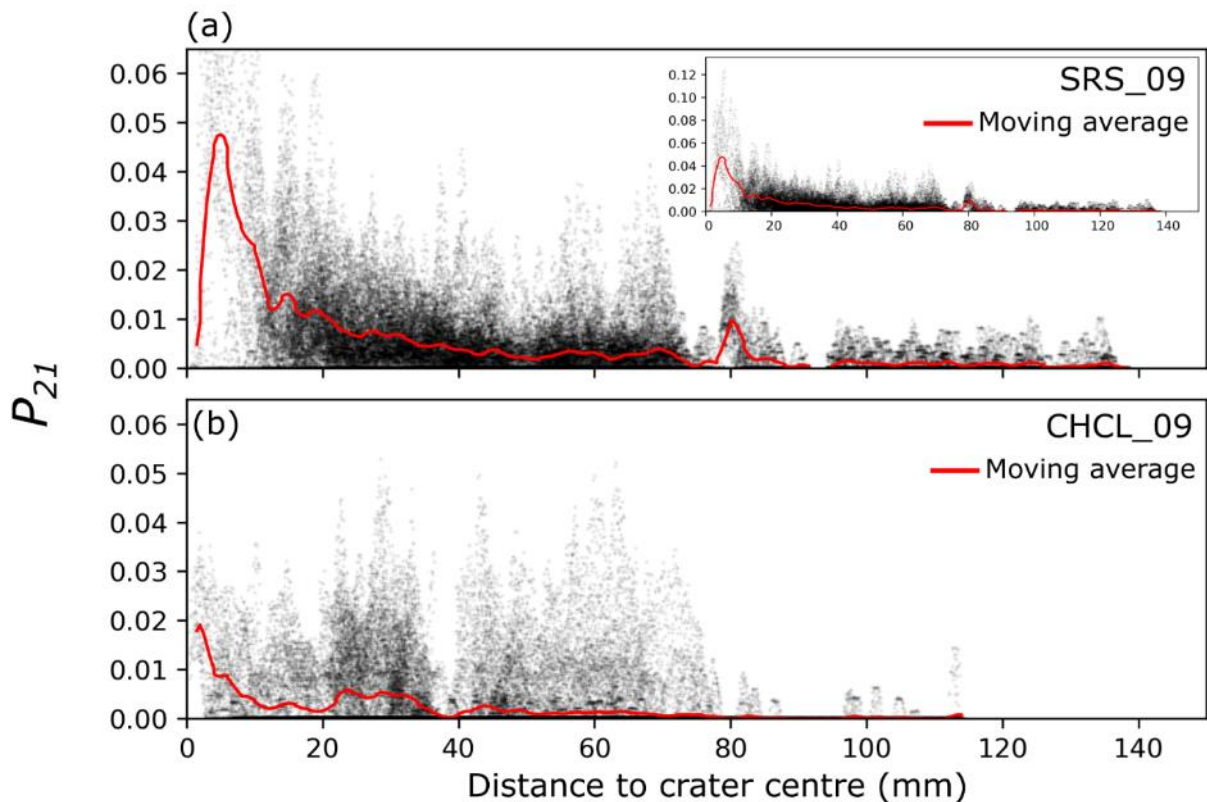


Figure 5: P_{21} fracture intensity with increasing distance from the crater centre for the sandstone (a) and limestone (b) target blocks. Red line is a 2 mm moving average of P_{21} intensity with distance from crater centre. Inset shows the full extent of P_{21} values in the sandstone target.

171 The limestone target (CHCL_09) has a wider (101.9 mm) and deeper (42.5 mm) crater than the
 172 sandstone sample (SRS_09) (24). The crater has a two-part structure of a shallow dipping outer spall
 173 zone surrounding a deeper, flat-bottomed pit. The inflection point between these two regions on the
 174 crater edges forms an overhang with the upper wall of a large open fracture. The open fracture has a
 175 gently convex up shape across multiple thin sections, reaching the edge of the target block (Figure 6a).
 176 It was noted during thin section production that this fracture reaches the surface of faces adjacent to
 177 the impacted face. The exposure in thin section represents a 2D profile through an axisymmetric,
 178 roughly conical fracture plane with its apex at the impact crater. The aperture of the open fracture is
 179 widest (~13 mm) where it intersects the crater, narrowing to ~1.5 – 2 mm near the edge of the target
 180 block. This fracture forms a wedge of material (incipient wedge) that appears to be unconnected to the
 181 rest of the target block within the plane of observation. Peak P_{21} values in the limestone target are lower
 182 than those in sandstone (0.053 vs. 0.124), with high P_{21} values localised in the near surface region of the
 183 spall zone in the top right section, beneath the crater floor, and around the open fractures (Figure 6b).
 184 The highest P_{21} intensity values are within ~5 mm from the crater centre, decreasing by at least a factor
 185 of 2 beyond this distance (Figure 5b).

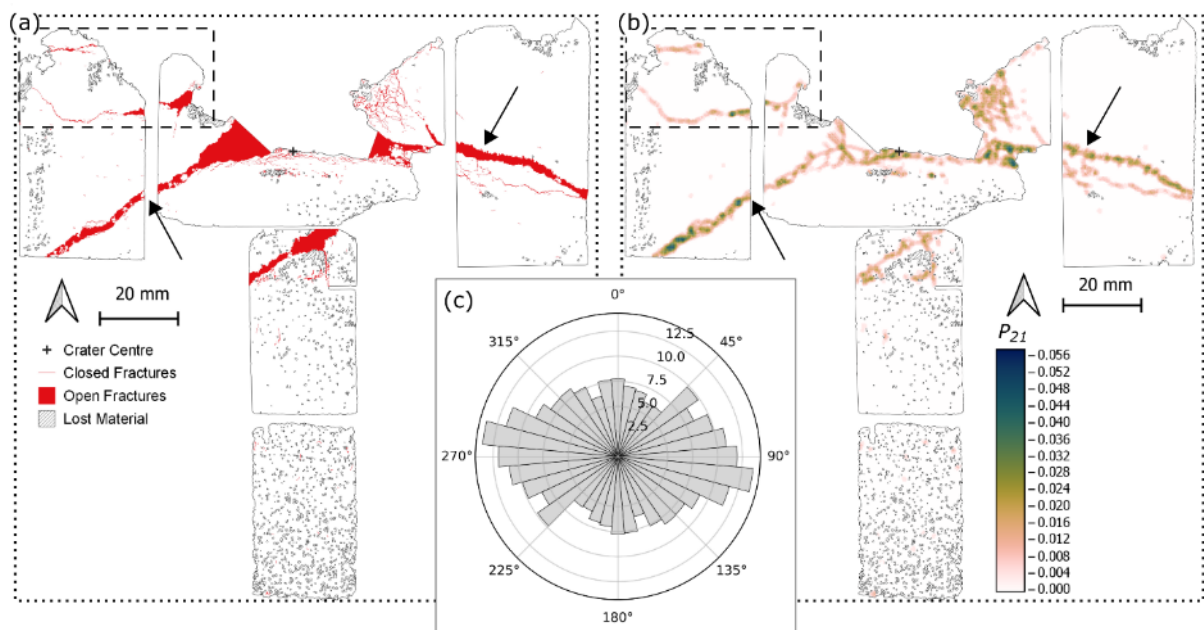


Figure 6: Fracture map (a) through the centre plane (XZ) of the Cotswold Hill Cream Limestone (CHCL) sample (CHCL_09). An open fracture (black arrows) is present across multiple thin sections, intersecting the edges of the target block and the crater. Open fractures are visible sub-parallel to the target face and forming incipient spall fragments (dashed rectangle). There are crater floor parallel, closed fractures (red line) directly below the crater centre. (b) Map of P_{21} fracture intensity values across the thin sections. The highest values (dark blue) are localised along the wide open fracture (black arrows) and around the crater centre. For both maps impact direction is top to bottom and the original block outline is shown with a dotted line. (c) Equal area rose diagram showing the orientation of all fractures, weighted for fracture length, mapped within the limestone sample. The fractures are predominantly sub-parallel to the target face. Radial scale is the square root of frequency.

186 Fractures throughout the sample are generally sub-parallel to the target face (Figure 6c), although
 187 there is another group of fractures with an orientation of $50^\circ/230^\circ$. Material below the spall zone surface
 188 is highly fractured, with grain sizes beyond the scale of observation in optical sections (Figure 7a-c).
 189 The top surface of the incipient wedge is the floor of the spall zone surrounding the central excavation
 190 and has an orientation of approximately $45^\circ/225^\circ$. Some fractures within the wedge, particularly those
 191 close to the spall surface, are oriented parallel to the spall surface, while other fractures throughout the
 192 wedge are perpendicular to this surface (Figure 7c). Higher P_{21} values reflect the higher fracture
 193 intensity in these regions (Figure 7d). This orthogonal pair of fractures is bisected by a third group, with
 194 orientations of approximately $100^\circ/280^\circ$ (Figure 7e.)

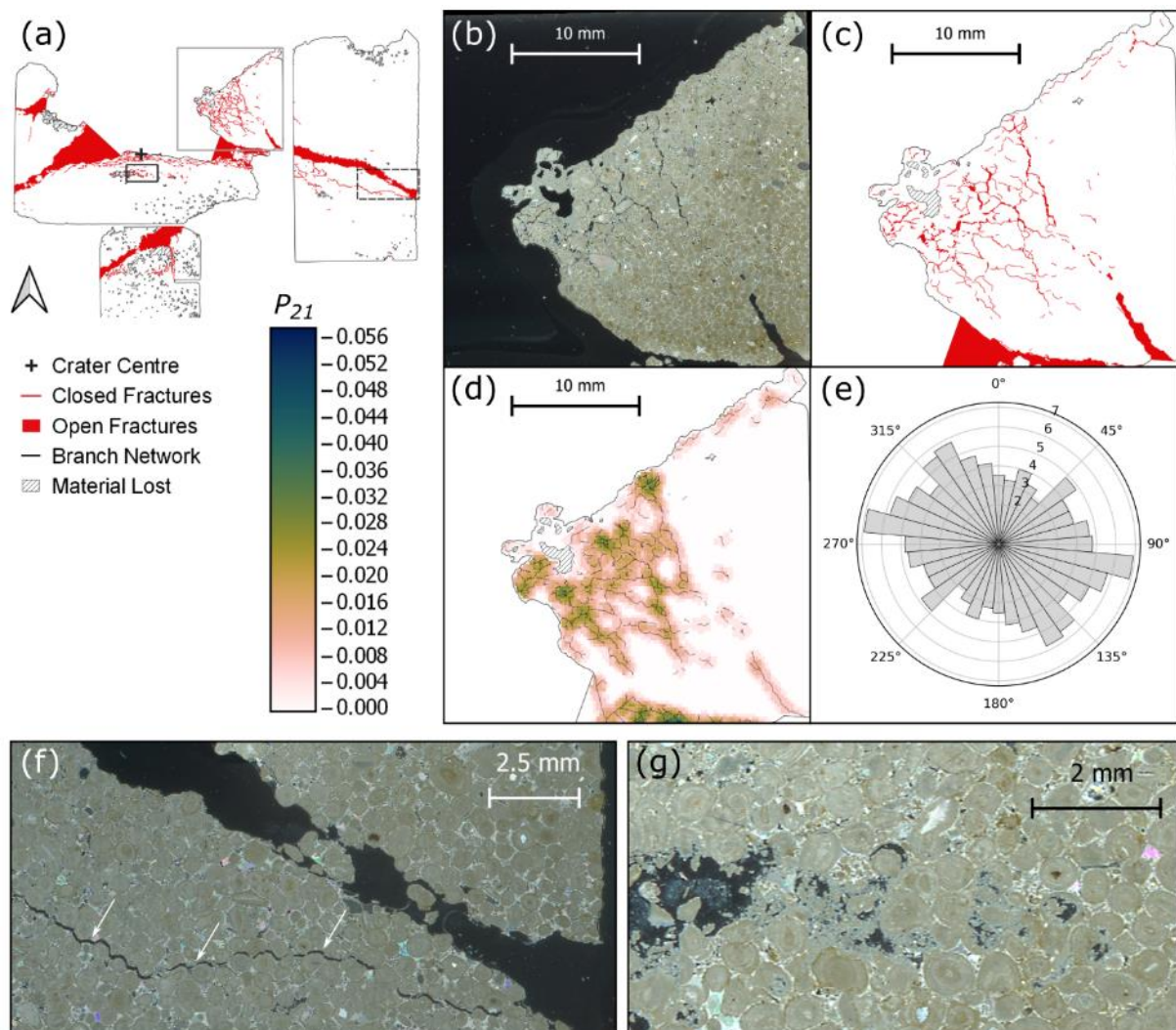


Figure 7: (a) Fracture map of the top central and right thin sections of sample CHCL_09 showing closed (red line) and open (solid red) fractures. Grey box indicates the location of panels (b-e), dashed black box indicates location of panel f and solid black box panel g. (b) Photomicrograph taken under cross polarised light (XPL) of an incipient wedge formed at the edge of the crater. (c) Fracture map showing multiple orientations of open and closed fractures in the wedge, corresponding to increased P_{21} intensity, as shown in panel d. (e) Equal area rose diagram of length weighted fracture orientations in panels b-d. Radial scale is the square root of frequency. (f) Photomicrograph under cross polarised light of a large open fracture present across several sections that intersects the edge of the target block. The fracture contains clasts of wall rock and has narrower fractures sub-parallel to it but several mm away (white arrows). (g) Photomicrograph under XPL highlighting a region of crushed ooids and carbonate material 6 mm below the crater floor.

195 Clasts of wall rock are present within the aperture of the large open fracture that is present across
 196 multiple thin sections. There are several narrower (< 0.15 mm) open fractures sub-parallel to, but
 197 distinct from, the large fracture (Figure 7f). Up to 2 mm beneath the floor of the central excavation there
 198 is a set of open fractures <0.2 mm wide and parallel to the crater floor. 6 mm below the crater floor is a
 199 zone of crushed ooids and very fine grained material, below the scale of observation (Figure 7g). There
 200 is another large open fracture (0.6-5.5 mm wide) starting at least 20 mm below the crater floor and
 201 oriented towards the lower left of the block (in section view), intersecting the edge of the section area
 202 at a depth of 30 mm below the crater floor (thin section below the crater centre in Figure 7a).

203 **DISCUSSION**

204 **Damage Mechanics**

205 The experiments conducted here were carried out at conditions intermediate between hypervelocity
 206 and quasi-static experiments (Table 2), with potentially some overlap between the conditions for these
 207 ordnance impacts and those of hypervelocity impacts. Strain rates of 10^3 - 10^6 s⁻¹ here compare with 10^4 -
 208 10^9 s⁻¹ for hypervelocity experiments and $<10^3$ s⁻¹ for quasi-static experiments. Another way to compare
 209 the experimental conditions is the ratio of impact velocity to P wave velocity in the target: these
 210 experiments have values of 0.66 to 0.94 compared to the values of 0.9 to 2.9 for hypervelocity and $\sim 10^{10}$
 211 for quasi-static experiments. Despite these considerable differences, there are several features in
 212 common between the different experiments (Table 2).

	Hypervelocity Impact	Ordnance Velocity Impact (This Study)	Quasi-Static Indentation
Strain Rate (s⁻¹)	10 ⁴ - 10 ⁹	10 ³ -10 ⁶	<10 ³
Impact velocity / P-wave Velocity	0.9 – 2.9	0.66 – 0.94	$\sim 10^{10}$
Spall fractures	✓	✓	-
Conical fractures or zones of fracture	At the boundary of the near surface zone	5-10× the depth of the near surface zone	Cone cracks
Radial Fractures	✓	✓	✓
Concentric fractures	✓	✓	✓
Crater Mechanics	A point source equivalent to an explosion at depth	Momentum transfer	Quasi-static crack growth

References

(25–27)

(28–30)

(27,31–33)

Table 2: Summary of the similarities and differences in damage appearance and mechanisms for hypervelocity impacts, ordnance velocity impacts, and quasi-static indentation experiments.

213 The open fracture observed in the limestone sample dipping away from the crater resembles the
214 ‘near surface’ fractures observed below hypervelocity impacts into gabbro (Figure 8) (34). Polanskey
215 and Ahrens (34) suggest that the fractures form along the boundary between a near surface region, as
216 defined by Melosh (35), and deeper regions of the target. In the near surface region, target material
217 experiences reduced peak compressive stress due to the reflection at a free surface of compressive stress
218 waves as tensile waves of equal magnitude. As rock is generally weaker in tension than compression,
219 these tensile waves can overcome rock strength and result in extensional fracturing, i.e. spallation.
220 Polanskey and Ahrens (34) show good correlation of both location and orientation between the
221 boundary of the near surface zone and ‘near surface’ fractures below hypervelocity impacts.
222 Calculation of the near surface boundary for the experiments conducted here, as defined in Melosh (35)
223 (Equation 2), resulted in a depth below target surface (Z_p) of 4.2 – 9.3 mm for the limestone experiment
224 (Figure 9a) and 4.1 – 14.2 mm for the sandstone experiment (Figure 9b).

225
$$Z_p = \frac{c_L T}{2} \left(\frac{4(d^2 + s^2)}{4d^2 - c_L^2 T^2} \right)^{\frac{1}{2}} \quad (2)$$

226 Where C_L is the target sound speed, T is the rise time of the stress pulse (and $T \approx a/U$) where a is
 227 projectile diameter and U is its impact velocity, d is the depth of burst, and s is the distance along the
 228 surface (X axis) from the impact point. The depth of burst is the effective centre of the spherical stress
 229 wave that diverges from the impact site and defined here as $d \approx 2a(\rho_p / \rho_t)^{1/2}$ with ρ_p the projectile density

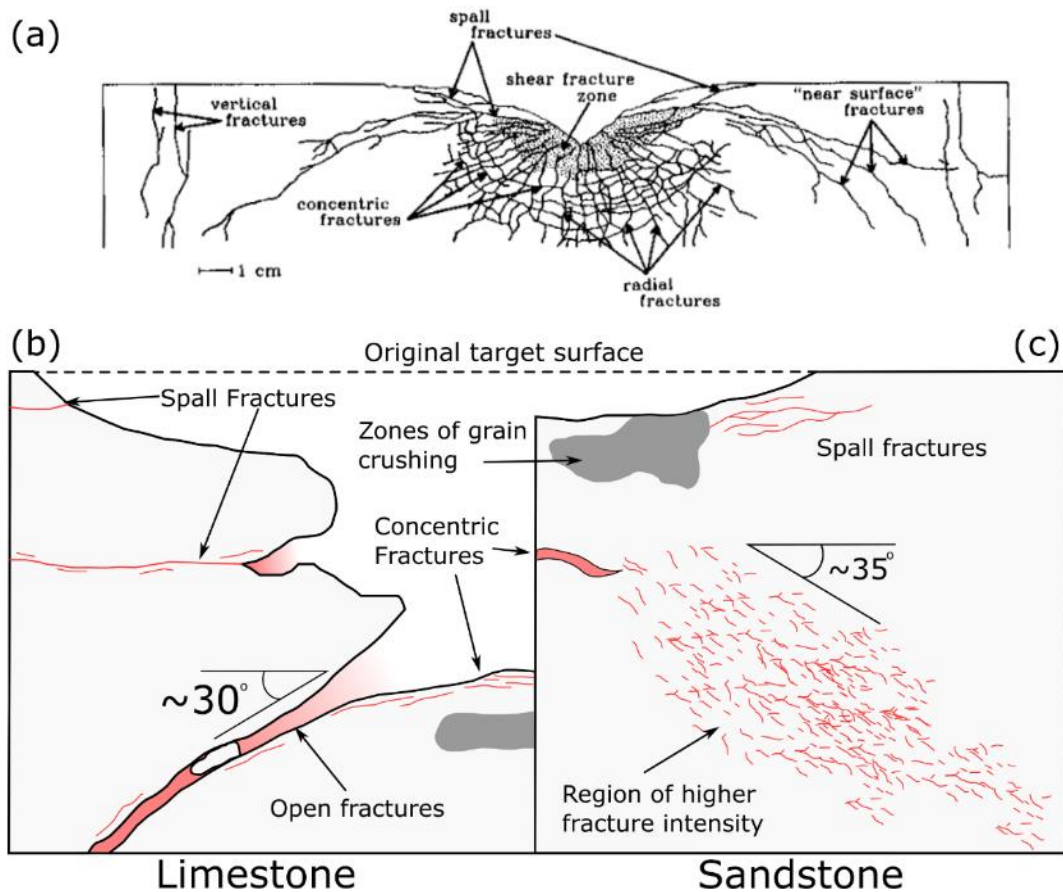


Figure 8: (a) Summary sketch of damage to San Marcos Gabbro during a hypervelocity impact (Polanskey and Ahrens, 1990). Schematics (not to scale) of damage observed in limestone (b) and sandstone (c) targets shot with 7.62 x 39 mm ammunition.

230 and ρ_t the target density (35). In this equation d is similar to, but not the same as the 'depth of burst' for
 231 an explosion that produces a crater the same size as the impact, a common reference depth used in
 232 hypervelocity experiments. The value of d (38.8 mm) for the limestone target is similar to the maximum
 233 crater depth (42.5 mm), a similarity not observed in the sandstone target (36.6 vs. 5.1 mm). For both
 234 targets in this study, the theoretical hyperbola of the near surface boundary does not have a strong
 235 correlation with the observed subsurface fracturing (Figure 9). Fractures are present in the near surface
 236 zone of the sandstone target, but they are parallel to the crater floor or target surface, comparable to
 237 those labelled 'spall fractures' by Polanskey and Ahrens (34) (Figure 8a). One experiment of Polanskey
 238 and Ahrens (34), using a commercial lead bullet fired at 890 ms^{-1} , created near surface fractures with a
 239 steeper inclination than predicted by their theoretical near surface parabolas. The results of this
 240 experiment resemble the orientation of the increased fracture intensity zone in the sandstone target of
 241 this study. Winkler et al. (36) observed localised shear zones below hypervelocity impacts into

242 quartzites that dip away radially from the crater centre, some of which have orientations similar to
243 those observed in the sandstone target of this study. The shape of the near surface zone is strongly
244 controlled by the stress pulse caused by the impact (34,35). The model discussed above assumes the
245 rise time remains constant as shock/stress propagates (35), which is unlikely for the ogive nose shape
246 of the projectile in this study.

247 The conical form of the subsurface fractures in the target lithologies presented here also resemble
248 conical cracks below indentation and contact loading studies into glass and ceramic targets (37–41).
249 Cone fractures, also known as Hertzian cracks, form initially as a ring crack around an indenter, before
250 propagating in a conical form with continued load. It is conventionally assumed that the angle of the
251 cone crack matches the pre-existing stress field with an angle of approximately 30° to the surface (42),
252 which is similar to the angle of the fracture in the limestone target and the zone of increased fracture
253 intensity in the sandstone target. Cone cracks are considered to propagate stably, requiring quasi-static
254 conditions (43–46). However, impact induced fracturing is generally thought to be a dynamic process,
255 leading to multiple flaws propagating unstably instead of a single, stable fracture (25,47,48).
256 Furthermore, the cone crack experiments use target materials with no porosity, contrasting with the
257 relatively porous (11-20%) targets presented here. Chen et al. (2016) observed radial fractures around
258 an indenter for target porosities between 5% and 45%, but no Hertzian cone cracks. They suggest this
259 was due to the small radius of the indenter and relatively low target hardness resulting in plastic
260 deformation before the critical load for cone crack formation could be reached. Impacts of a flat ended
261 projectile into granite tiles at velocities of 207-537 ms⁻¹ by Hogan et al. (49) created conical cracks that
262 reached the rear face of the target tiles. Other experiments impacting spherical projectiles into fused-
263 silica and Pyrex targets, at velocities up to 340 ms⁻¹, also resulted in conical cracks below the impact
264 (41). Similar impacts in the same study, but into soda-lime glass targets, produced an array of splinter
265 cracks that resemble dynamic fracturing more than stable propagation, suggesting that target material
266 has an influence on cone crack formation from impacts (41). The loading rate (25 μms⁻¹) of Chen et al.'s
267 (50) indentation experiments is orders of magnitude slower than experienced by the experiments of
268 Chaudhri (41), Hogan et al. (49), and those presented here. Both Chaudri (41) and Hogan et al. (49)
269 described these conical fractures as Hertzian cone cracks, but their similarity to the experiments here,
270 the limestone target in particular, suggests an alternative dynamic mechanism.

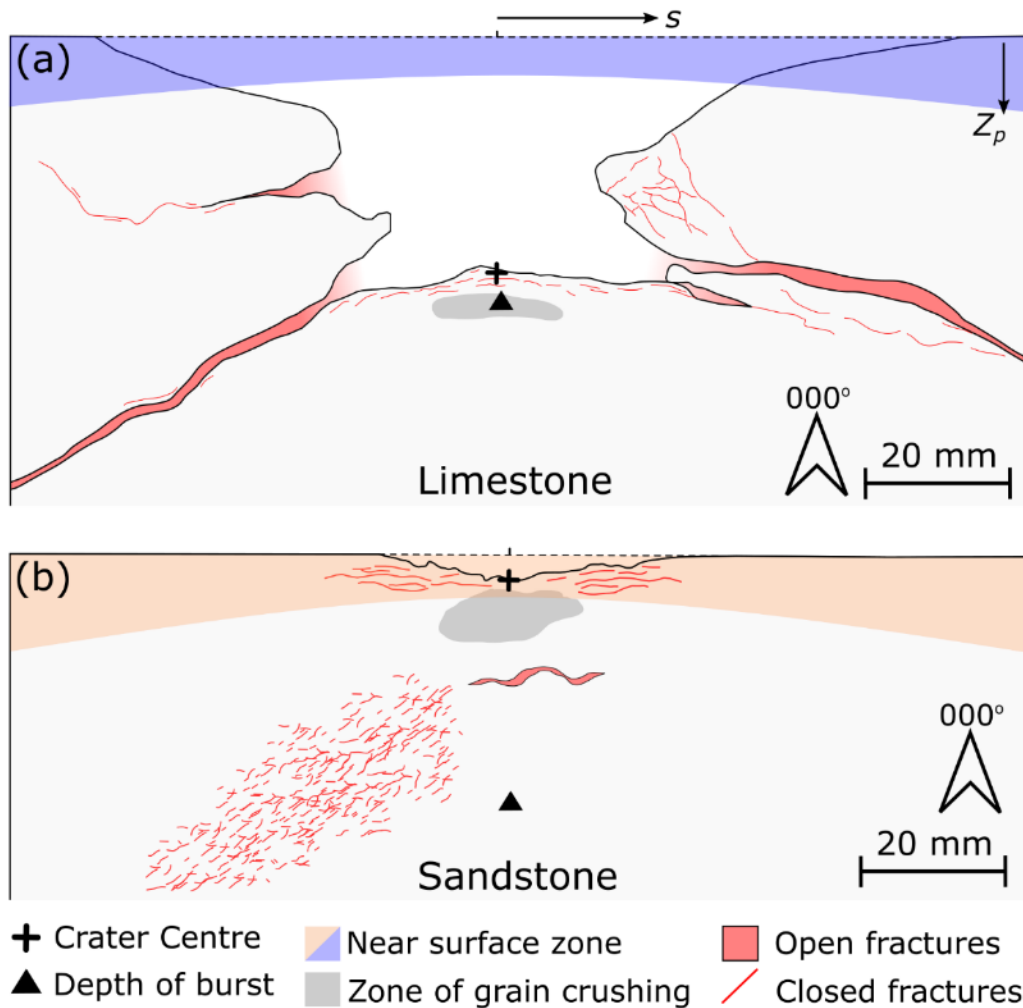


Figure 9: (a) Summary diagram of damage to Cotswold Hill Cream Limestone. The predicted depth of burst (d) (triangle) and crater centre are a similar distance below the original target face (dashed line). Z_p is the depth of the near surface zone parabola at lateral distance (s) from the impact point. The theoretical near surface zone is shaded blue. (b) Summary diagram of damage to Stoneraise Red Sandstone. The predicted depth of burst (d) (triangle) is substantially deeper in the target than the crater centre. Z_p is the depth of the near surface zone parabola at lateral distance (s) from the impact point. The theoretical near surface zone is shaded orange. Vertical and horizontal scales are the same.

271 The propagation of radial fractures is observed in hypervelocity, ordnance velocity, and quasi-static
 272 indentation experiments. Radial fractures form due to tensile stresses perpendicular to the spherical
 273 compressive stress (or shock) wave caused by contact loading or impact into a target (51). Chen et al.
 274 (50) observed four radial fractures in glass targets at orthogonal orientations around the indenter. They
 275 suggest the propagation of fractures in these orientations relieves stress in the interim regions, meaning
 276 that the growth of the four fractures accommodates the increasing indentation load. The radial fractures
 277 observed in hyper- and ordnance velocity experiments are more numerous and have less regularity in
 278 their spacing. Impact loading creates far greater strain rates (Table 2) compared to those in Chen et al.'s
 279 (50) experiments, possibly exceeding the ability of only a few orthogonally oriented radial fractures to
 280 accommodate strain, resulting in new fractures forming in the interim areas. The propagation of
 281 multiple fracture strands at once is indicative of dynamic fracturing, observed by Hogan et al (49) and
 282 Chaudhri (41).

283 Both target lithologies of this study exhibit extensional fractures parallel to the crater floor,
284 resembling observations of concentric fractures below hypervelocity impacts (26,34,50,52) (Figure 8a,
285 c). Similarly concentric fractures are also present beneath point loading experiments in glass and
286 ceramics. However the fractures beneath the point loading experiments are thought to be caused during
287 the unloading phase, as the load on the compressive zone below the indenter is released (50,53).

288 Both hypervelocity and ordnance velocity impacts exhibit spall fractures at the edge of the crater.
289 Where not directly visible in the subsurface, the presence of spallation is evident in the shallow dipping
290 region surrounding the central excavation (24,26,34). The spall fractures form when the initial
291 compressive stress wave reaches the free surface of the target face and reflects back as tensile wave of
292 equal magnitude (35). Spall fractures are typically found close to the target face because the radial decay
293 function causes wave energy to drop below the failure strength of the target material (34,35,54). There
294 are no spall fractures in quasi-static indentation experiments because the loading rates do not produce
295 a stress wave of substantial magnitude. Instead the continual loading increases compressive stresses in
296 the region directly below the loading.

297 The observations in this study have some similarities to those in both the near surface zone of
298 hypervelocity experiments and Hertzian cone cracks, but different mechanisms involved in these
299 ordnance velocity impacts preclude either the hypervelocity or cone crack mechanics from fully
300 explaining the observations made here. The formation of spall fractures parallel to the target face and
301 crater floor show that tensile stress waves formed when the initial compressive stress wave was
302 reflected at the surface. The interaction of these waves reflecting from the impacted face and adjacent
303 sides of the target block may have caused regions of tensile failure, similar to the formation of the near
304 surface zone in the hypervelocity experiments. However, the mechanics of the ordnance impacts,
305 involving momentum transfer and longer interaction time between the projectile and target, and the
306 geometry of the target blocks has resulted in a sufficiently different expression of subsurface damage
307 that the theoretical near surface zone is not applicable. The hypervelocity ($>1500\text{ms}^{-1}$) experiments used
308 spherical projectiles and cratering in these experiments was primarily controlled by the generation of a
309 shock wave originating at some depth below the surface, but these conditions and processes may not
310 be applicable to experiments presented here. Campbell et al. (16) found that bullet impacts with
311 velocities of $400\text{-}900\text{ ms}^{-1}$ did not follow crater scaling relationships found in hypervelocity impacts.
312 They also found that impact craters had identifiable crater asymmetry when impact trajectories were
313 oblique (24). This asymmetry is not observed in hypervelocity impacts, except for those with very
314 oblique trajectories ($<15^\circ$ to target face), because of the symmetrical nature of the point source model
315 for hypervelocity cratering mechanics. Campbell et al. (24) suggest they observed crater asymmetry in
316 their experiments because the impact velocity was lower than, or similar to, the sound speed of the

317 target materials, so no shockwave was generated upon impact. Cratering was instead controlled by
318 momentum transfer from the projectile to the target. This invalidates the point source assumption
319 critical to hypervelocity. The impact velocities in this study (532 ms^{-1} and 539 ms^{-1}) are lower than the
320 respective P-wave velocity of the limestone (569 ms^{-1}) and sandstone (822 ms^{-1}) targets, so the
321 generation of a shock wave at impact is unlikely. The results presented here support the suggestions
322 made by Campbell et al. (16) that bullet impacts into stone are predominantly controlled by target
323 properties, primarily material strength. Although there are some similarities between the damage
324 created by hypervelocity experiments and this study, such as the near-surface fractures, spalling, and
325 grain crushing below the impact, the damage mechanisms in each case are probably different.

326 **Implications for Conservation**

327 Fractures play a fundamental role in the transport of moisture and weathering agents by increasing
328 porosity and linking together isolated pores within the stone (55,56). Both stone types have increased
329 fracture intensity in the regions proximal to the bullet impact, as well as regions of increased fracture
330 intensity or open fractures dipping away from the impact crater at about 30° . Fracture width and
331 intensity play a substantial role in influencing fracture capacity and transmissivity, with fracture
332 intensity strongly correlated to overall permeability (56,57). The pattern of higher fracture intensities
333 closer to the crater centre suggests that regions directly surrounding the impact will have the highest
334 induced porosity and permeability, and may therefore be at the highest risk of weathering from
335 moisture related processes. Higher surface permeability surrounding impact craters has been observed
336 in historic and experimental impacts (3,4). The large open fractures present in the limestone target
337 creates localised areas of high fracture intensity that penetrate deep into the block. Higher fracture
338 intensity has been linked to greater rates of weathering (14).

339 Because the open fracture dips away from the crater centre, most of the fracture is not visible from
340 the surface. Hidden subsurface damage may affect a much larger region than visible surface damage.
341 Fractures that intersect the sides of the impacted block can break along the mortar block boundary, or
342 the mortar itself, possibly destabilising a wider region than just the impacted block (58). Impact craters,
343 particularly from shrapnel, commonly do not occur in isolation; structures typically have multiple
344 impacts across their surface. If these impacts have subsurface damage zones similar to those in this
345 study, there is the possibility they may link up in the subsurface. Figure 10 illustrates how multiple
346 impacts with a spacing less than the impacted blocks diameter may form interconnect fracture networks
347 below the surface that have greater footprint than the observable surface damage. The increased
348 permeability and decreased stone strength resulting from the interconnected damage zones may lead
349 to exacerbated material loss and greatly increase degree and rate of future deterioration. The interaction
350 of subsurface damage from multiple impacts is an interesting and important avenue for future research.

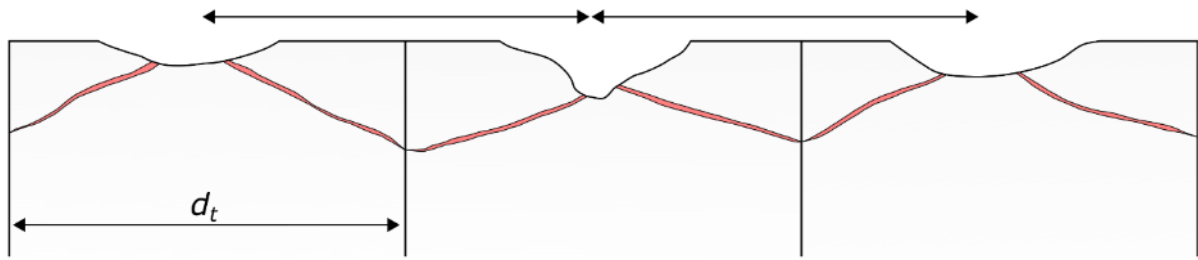


Figure 10: For impacts with a spacing less than the diameter of the impacted block d_t , subsurface conical fracture and damage zones can form an interconnected network that affects a greater region than suggested by the surface damage alone.

351 The limestone target in this study has lower fracture intensities throughout, despite exhibiting
 352 greater surface damage than the sandstone sample. The P_{21} values of the limestone target do not show
 353 a sharp increase within 10mm of the crater centre, as observed in the sandstone target. Energy above
 354 the requirement to exceed the target strength can be transferred as kinetic energy, causing material to
 355 be ejected from the impact site as ejecta, or the surrounding areas as spall fragments (35). The lower
 356 tensile strength of the limestone compared to the sandstone may explain the larger crater dimensions
 357 in the limestone target, the maximum depth of the limestone crater is 42.5mm, 8 times deeper than the
 358 crater in the sandstone. The region of highest fracture intensity in the limestone target may thus have
 359 been ejected.

360 The observations of impact induced fracturing in this study are important for conservator's post-
 361 conflict approaches to damaged heritage. Surface parallel spall fractures and interconnected subsurface
 362 conical fractures mean that regions with multiple impacts in close proximity may require rapid
 363 stabilisation to prevent substantial material loss. The increased permeability and porosity surrounding
 364 the impact mean these regions are at increased risk from moisture related deterioration (e.g.
 365 dissolution, salt crystallisation), so efforts for protecting against moisture, such as erecting temporary
 366 rain covers or shelters, can be prioritised where impacts are most numerous or exposed. Rapid
 367 observation of surface damage suggest where these priority actions should be focussed for short term
 368 protection. Once a more detailed and comprehensive assessment of the damage and the risk of
 369 deterioration it poses, has been undertaken, then targeted and specific remediation efforts can be
 370 conducted. The results of this study support the results of (3) and (4), further aiding the identification
 371 of priority regions for post conflict stabilisation

372 CONCLUSIONS

373 Apart from the visible surface crater, bullet impacts into rocks create conical fractures or zones of
 374 increased fracture intensity below the impact, radial fractures, and spallation. Similar features are also
 375 seen in hypervelocity experiments and quasistatic indentation experiments that form cone cracks.
 376 However, the strain rates and impact velocities of bullet impacts are intermediate between the
 377 hypervelocity and quasistatic experiments, and the mechanisms causing damage are distinct from these

378 experiments. Fracturing from the bullet impacts was dynamic (unlike cone crack experiments) but a
379 shock wave did not form (as in hypervelocity experiments). Damage was caused by momentum
380 transfer. The distinct conditions and damage mechanics in the bullet impacts created differences in the
381 details of the geometry of their damage compared to the faster and slower impacts.

382 The subsurface damage caused by bullet impacts differs between target lithologies. Sandstone
383 exhibits predominantly closed aperture inter- and intragranular fracturing, with some open fractures
384 sub-parallel to the target face, as well as zone of grain size reduction and compaction directly below
385 the crater. Limestone exhibits target surface parallel open fractures and open fractures curving away
386 from the crater at angles of 30° and propped open by clasts of wall rock. These open fractures can
387 intersect sides of the target adjacent to the impacted face, potentially leading to the loss of large volumes
388 of material.

389 P_{21} fracture intensity is highest closer to the crater centre in both lithologies and greatly decreases
390 beyond 5-10 mm from the crater centre. This shows that the region directly surrounding the crater
391 centre is at the greatest risk of deterioration from weathering. Regions at risk are not limited to the
392 impact crater, open fractures and zones of higher fracture intensity adjacent to them provide conduits
393 for moisture ingress and regions of increased susceptibility to weathering processes. These fractures
394 have the potential to link up with subsurface fractures below adjacent impacts and exacerbate the risk
395 of future deterioration from weathering processes across a much larger area. Small and apparently
396 inconspicuous impact craters have subsurface damage that can extend up to 80 mm from the target face
397 into the targeted block, but have little to no visible surface expression. This is important for proper
398 surveying and post conflict risk assessments of heritage sites.

399 ACKNOWLEDGEMENTS

400 We would like to thank the technicians and staff at Cranfield Ordnance Test and Evaluation Centre
401 (COTEC) for their expertise and assistance in conducting the live fire experiments. Additional thanks
402 to Lieutenant Martin RE for information and discussion surrounding engagement distances. Finally we
403 would like to thank Anthony Oldroyd for their valuable assistance during sample preparation,

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