Re-examining Temporal Variations in Intermediate-Depth Seismicity

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1 Abstract

Changes in the frequency of intermediate-depth (60–300 km) earthquakes in response to static stress 2 transfer can provide insights into the mechanisms of earthquake generation within subducting slabs. 3 In this study, we use the most up-to-date global and regional earthquake catalogues to show that both 4 the aftershock productivity of large earthquakes, and the changes in the frequency of intermediate-5 depth earthquakes around the timing of major megathrust slip, support the view that faults within 6 the slab are relatively insensitive to static stress transfer on the order of earthquake stress drops. We 7 interpret these results to suggest the population of faults within the slab are much further from their 8 failure stress than is typical for shallow fault systems. We also find that aftershock productivity varies 9 within slabs over small spatial scales, indicating that the mechanism that enables faults to rupture at 10 intermediate depths is likely to be spatially heterogeneous over length-scales of a few tens of kilometres. 11 We suggest dehydration-related weakening mechanisms can best account for this heterogeneity. 12

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¹⁶ Plain Language Summary

Earthquakes at 60–300 km depth within subducting slabs are known as 'intermediate-depth' earth-17 quakes. At such depths, the high pressures should act to clamp faults shut, preventing them from 18 breaking in earthquakes through frictional sliding. In this study, we investigate the mechanisms 19 that enable the generation of intermediate-depth earthquakes by examining the temporal changes of 20 intermediate-depth seismicity caused by other, nearby earthquakes. We find that seismicity within 21 slabs is relatively insensitive to the stress changes caused by nearby earthquakes when compared to 22 shallow earthquakes of equivalent size. We interpret these results to suggest that faults within the slab 23 are much further from their failure stress than is typical for shallow faults, and that the mechanism 24 that enables faults to rupture at intermediate depth is likely to be spatially variable over length-scales 25 of a few tens of kilometres. We suggest weakening mechanisms related to water release within slabs 26 can best account for this heterogeneity. 27

28 Key Points:

- Large intraslab and megathrust earthquakes have a limited influence on the frequency of
 intermediate-depth seismicity.
- Faults within subducted slabs are relatively insensitive to static stress transfer caused by earthquake stress drops.
- Low stress drops and heterogeneous aftershock productivity can be best explained by
 dehydration-related weakening mechanisms.

35 1 Introduction

Temporal variations in the frequency of intermediate-depth (60–300 km) earthquakes have the potential to provide insights into the enigmatic conditions and mechanism(s) of earthquake nucleation within subducting slabs. These intraslab earthquakes have dominantly double-couple focal mechanisms, indicating they represent shear failure on a population of faults [Frohlich, 1989]. However, at depths ≥ 60 km, the high confining pressures and high temperatures should prevent frictional failure on faults subject to normal plate-driving forces without an additional mechanism that reduces the stress needed to generate earthquake rupture [Zhan, 2020].

Two main mechanisms have been proposed: dehydration-related weakening and self-localising thermal 43 runaway. Dehydration-related weakening is caused by the breakdown of hydrous mafic minerals as 44 the slab subducts, which either releases water that reduces the effective frictional strength of intraslab 45 faults (dehydration embrittlement; Green and Houston [1995]; Hacker et al. [2003]), or causes extreme 46 stress concentrations through the breakdown of load-bearing hydrous phases (dehydration-assisted 47 stress transfer; Ferrand et al. [2017]), allowing faults to fail through frictional sliding. Alternatively, 48 self-localising thermal runaway is a process by which creep in hydrated or fine-grained shear zones 49 causes shear heating and the development of ductile instabilities that relax elastic strain [Ogawa, 50 1987; Hobbs and Ord, 1988]. Thermal runaway may have a nucleation phase involving progressive 51 ductile strain, eventually leading up to seismogenic failure that relaxes the majority of the stored 52 elastic strain in high stress-drop events (500–1000 MPa; Kelemen and Hirth [2007]; John et al. [2009]). 53 These different mechanisms can account for the observation of earthquake generation at high confining 54 pressures, but they should be sensitive to different physical and mechanical conditions within the slab, 55 such as temperature and the availability of hydrous mineral phases. 56

Progress in our understanding of intermediate-depth earthquake generation has therefore focused on 57 explaining the spatial pattern of seismicity within subduction zones, such as the structure of double-58 seismic zones [e.g. Wei et al., 2017; Florez and Prieto, 2019; Sippl et al., 2019], or the relationship 59 between intermediate-depth earthquake focal mechanisms, seismicity rates, and the orientation and 60 density of outer-rise normal faulting [e.g. Warren et al., 2007; Boneh et al., 2019]. Analysis of any 61 temporal variations in the frequency of intermediate-depth seismicity can potentially provide com-62 plementary information to these studies. In particular, variations in the frequency of seismicity in 63 response to known stress changes can provide insights into the population of faults that are close to 64 failure, as well as the sensitivity of the failure mechanism to small stress perturbations, and how these 65

⁶⁶ vary between different pressure-temperature conditions and slab environments [e.g. Tibi et al., 2003;

⁶⁷ Persh and Houston, 2004; Zhan and Shearer, 2015; Bouchon et al., 2016, 2018; Luo and Wiens, 2020].

Two observations have emerged that suggest different sensitivities of intraslab faults systems to changes 68 in static stress. First, studies have reported changes in the frequency of intraslab intermediate-depth 69 earthquakes related to the occurrence of shallow earthquakes, including: (1) year-long changes in 70 earthquake frequency that begin after large, shallow earthquakes on the adjacent subduction megath-71 rust [Lay et al., 1989; Bouchon et al., 2016; Jara et al., 2017; Mitsui et al., 2021], and (2) month-long 72 transient changes in intraslab earthquake frequency following slip on the megathrust [Delbridge et al., 73 2017]. These observations suggest that intraslab faults in some settings are relatively sensitive to 74 the small (<1 MPa) stress changes that shallow earthquakes impose on the slab through static stress 75 transfer, and that faults within the subduction system are interacting with one another over dis-76 tances of tens to hundreds of kilometres. In contrast, intermediate-depth earthquakes are consistently 77 followed by far fewer aftershocks compared to shallow crustal earthquakes of equivalent magnitude 78 (low 'aftershock productivity') [Frohlich, 1987; Wiens and Gilbert, 1996; Persh and Houston, 2004; Ye 79 et al., 2020]. As the stress drops in intermediate-depth earthquakes are similar to shallow earthquakes 80 (~1-50 MPa) [Allmann and Shearer, 2009; Poli and Prieto, 2016; Tian et al., 2022], the difference 81 in aftershock productivity between shallow and intermediate-depth mainshocks is not related to the 82 amplitude of the stress changes. Rather, the low productivity of intermediate-depth aftershock se-83 quences indicates that the faults within the slab are relatively insensitive to the stress changes caused 84 by nearby large earthquakes within the slab, and that they only weakly interact with one another. 85 These two inferences relating to intraslab seismicity appear to be in contradiction. This study aims to 86 reconcile them by re-examining the evidence for temporal changes in the frequency of intermediate-87 depth seismicity around the timing of large earthquakes using the most up-to-date global and regional 88 earthquake catalogues. 89

Section 2 focuses on the aftershock sequences of large intermediate-depth earthquakes, verifying previous results regarding their low aftershock productivity and testing whether aftershock productivity varies systematically with source or slab setting. Section 3 then explores the response of intermediatedepth seismicity to slip in megathrust earthquakes. We find that, although there are temporal variations in the frequency of intermediate-depth seismicity, they do not consistently correlate with the timing of stress changes caused by large megathrust earthquakes. In Section 4, we discuss the implications of our findings for the mechanics of faulting at intermediate depths within slabs. Wimpenny et al.,

⁹⁷ 2 Aftershock Productivity of Intermediate-Depth Earthquakes

Aftershocks are the most obvious manifestation of changes in seismicity rates, and reflect the rupture 98 of faults in response to changes in the local stress state following a larger earthquake [King et al., 99 1994; Lin and Stein, 2004]. Analyses of aftershock sequences following intermediate-depth earthquakes 100 show that they are typically less productive compared to shallow earthquakes of equivalent magnitude 101 [Frohlich, 1987; Wiens and Gilbert, 1996; Dascher-Cousineau et al., 2020; Ye et al., 2020]. Aftershock 102 productivity is also known to be depth-dependent, with most large earthquakes between 300–500 km 103 often having no aftershocks at all with $m_b \ge 4.5$ [Persh and Houston, 2004]. Early studies suggested 104 that the aftershock productivity correlates with a slab's thermal structure [Wiens and Gilbert, 1996], 105 though more recent work using longer-duration catalogues with lower magnitudes of completeness has 106 argued that aftershock productivity is independent of slab temperature, but may be related to the 107 heterogeneity of the stress field and fault network surrounding the mainshock [Ye et al., 2020] or the 108 availability of highly pressurised free fluid in the slab [Cabrera et al., 2021; Chu and Beroza, 2022]. 109

Below, we re-examine aftershock productivity at both global and regional scales using modern earthquake catalogues, focusing particularly on seismicity within the depth range 60–300 km. In this depth range, earthquakes are mostly within subducted oceanic lithosphere. Through this updated analysis, we aim to characterise the relative sensitivity of fault systems to earthquake stress changes in different slab environments by first focusing on global patterns in aftershock productivity and then zooming in to region-scale patterns.

¹¹⁶ 2.1 Global Analysis

117 2.1.1 Method of Measuring Aftershock Productivity

We first studied the aftershock sequences of all $M_w > 6.5$ earthquakes using a simple clustering 118 algorithm applied to the ISC's reviewed global catalogue following the methods of Baiesi and Paczuski 119 [2004] and Zaliapin and Ben-Zion [2013]. We use this non-parametric clustering method, as it does not 120 assume any particular form for the temporal evolution of aftershock frequency [e.g. Dascher-Cousineau 121 et al., 2020; Chu and Beroza, 2022]. The ISC's reviewed earthquake catalogue is derived from a location 122 procedure that uses the body-wave phase arrivals from teleseismic and regional stations to provide the 123 most accurate estimates of earthquake hypocentral parameters and consistent body-wave magnitude 124 estimates globally [Bondár and Storchak, 2011; Di Giacomo and Storchak, 2016]. We complement 125

these data with moment tensor information for each mainshock derived using long-period body and surface wave inversion from the global Centroid Moment Tensor (gCMT) catalogue [Dziewonski et al., 1981; Ekström et al., 2012], which limits the time-span of our analysis to mainshocks between 1976 and 2020. We choose to represent the size of the mainshocks using the moment magnitude M_w derived by the gCMT, and not body-wave magnitude m_b , because the body-wave magnitude scale saturates for the largest mainshocks included in our analysis at $m_b \gtrsim 7.5$.

For each mainshock, we began by taking a subset of events from the ISC catalogue that are within 132 500 km of the mainshock hypocentre and which have $m_b \ge 4.5$. For all events within this subset, we 133 then calculated the space-time distance η_{ij} between each event hypocentre i and every other event 134 hypocentre j [Zaliapin et al., 2008]. The space-time distance is defined as $\eta_{ij} = t_{ij}(r_{ij})^d 10^{-bm_i}$, where 135 $t_{ij} = t_j - t_i$ is the time difference between event origin times, r_{ij} is the 3-dimensional cartesian distance 136 between the event hypocentres, m_i is the magnitude of event *i*, and d = 1.6 and b = 1 are constants 137 [Zaliapin and Ben-Zion, 2013]. If $t_{ij} \leq 0$ then we set $\eta_{ij} = \infty$ to enforce causality (i.e. event j must 138 have occurred after event i for it to be an aftershock). The choice of $m_b \ge 4.5$ is designed to capture 139 a global average for the magnitude of completeness for intermediate-depth seismicity [Ye et al., 2020]. 140 Although changing this value to $m_b \geq 5.0$ has an effect on the absolute count of aftershocks, it has 141 little affect on the trends in relative aftershock productivity (Supplementary Text S1). 142

For every event j in the catalogue we define its parent as the event i for which $\eta_j = \min(\eta_{ij})$. At this 143 stage we check that the mainshock is not an aftershock of an even larger earthquake by ensuring that, 144 for the event to be considered a mainshock, it has no parent events that have a larger magnitude. The 145 resulting distribution of $\log_{10}(\eta_j)$ forms two peaks (Supplementary Figure 1a), with events with low 146 $\log_{10}(\eta_j)$ being clustered events and those with high $\log_{10}(\eta_j)$ being independent events [Zaliapin and 147 Ben-Zion, 2013]. To determine the cut-off between the two, we fit a two-component Gaussian mixture 148 model to the distribution and determined the overlap between the two curves η_0 (Supplementary 149 Figure 1b). We then recursively counted all of the offspring of the mainshock that have $\eta_j \leq \eta_0$ to 150 yield the final aftershock count. The seismicity that is not clustered, which consists of all events for 151 which $\eta_j > \eta_0$, is used to calculate the background seismicity rate within ± 50 km horizontal distance 152 and ± 30 km depth around each mainshock (Supplementary Figure 2). 153

The analysis described above yields aftershock counts for 2432 mainshocks. For the remaining 1586 events with $M_w \ge 6.5$ in the gCMT catalogue, we were either not able to separate the background from the clustered seismicity, or the earthquake was itself an aftershock. Although the absolute aftershock count is weakly dependent on the constants used in the space-time distance calculation $(b, d, \text{ and } \eta_0)$, the relative count between mainshocks is insensitive to the parameter selection (Supplementary Text S1). Below we only interpret changes in relative aftershock productivity.

160 2.1.2 Results of Aftershock Productivity Analysis

Figure 1 shows the number of aftershocks for each mainshock plotted against a set of possible dependent 161 variables. The two clear trends within the data are that the aftershock productivity changes as 162 a function of mainshock depth and mainshock magnitude (Figure 1a,b) [Frohlich, 1987; Persh and 163 Houston, 2004; Ye et al., 2020]. In terms of mainshock depth, we find that there is a sharp decrease in 164 aftershock productivity as mainshocks exceed 50–60 km depth (Figure 1a), which roughly corresponds 165 to the transition from shallow crustal and intraplate seismicity to intraslab seismicity. Below 60 km 166 depth, the median aftershock productivity continues to decrease with depth until 300 km, then remains 167 consistently low for mainshocks between 300 km and 500 km depth, before increasing again between 168 500 km and 700 km depth, mirroring the distribution of mainshocks (Figure 1a). 169

Aftershock productivity also increases with mainshock magnitude (Figure 1b). For earthquakes within 170 both the shallow (<60 km) and intermediate-depth range (60-300 km), the median aftershock produc-171 tivity scaling with mainshock magnitude M can be fit by an equation of the form $a10^{\gamma(M-M_c)}$ where 172 $\gamma \approx 1$ and M_c is the magnitude of completeness [Frohlich, 1987] (Supplementary Figure 5). The median 173 aftershock productivity for the intermediate depth earthquakes consistently falls below that for shallow 174 earthquakes across the mainshock magnitude range (Figure 1b), indicating that intermediate-depth 175 earthquakes have, at least on average, fewer aftershocks for a given magnitude mainshock. However, 176 there is still significant scatter in aftershock productivity around the median for intermediate-depth 177 earthquakes. The scatter indicates there is some other control on the measured aftershock productivity 178 beyond just mainshock depth and magnitude. 179

One possibility is that the scatter is related to our method of aftershock counting. We found no correlation between the aftershock productivity and the date of the mainshock, suggesting temporal changes in the ISC catalogue's completeness are not contributing to the scatter (Figure 1c). In addition, the aftershock productivity does not correlate with the gradient in down-dip slab curvature or background seismicity rate (Figure 1d,e), which implies that aliasing high rates of background seismicity into aftershock productivity is also not contributing to the scatter.

Alternatively, the scatter in aftershock productivity may relate to an unidentified mechanism associated with the mainshock source or setting, such as the mechanical properties of the slab [Wiens and Gilbert, 1996] or stress heterogeneity and variability in fault geometries within the slab [Ye et al., 2020]. For almost every mainshock the aftershocks of large intermediate-depth earthquakes are too small to have mechanisms in the gCMT catalogue, limiting our ability to test whether aftershock productivity is related to the geometry of the receiver faults. However, if aftershock productivity were related to the slab setting, then it should vary systematically between subduction zones.

After removing the scaling between the median aftershock productivity and mainshock magnitude, we did not find any systematic spatial variability in aftershock productivity at the scale of individual subduction zones (Supplementary Text S2). However, this analysis is limited by there being too few $M_w \ge 7.5$ events to identify any spatially robust trends, and earthquakes in the magnitude range $6.5 \le M_w < 7.5$ have too few aftershocks (generally <5; see Figure 1b) of $m_b \ge 4.5$ to record spatial variability in the aftershock productivity using global catalogues (Supplementary Text S2).

Earthquakes on transform faults produce the fewest aftershocks of any shallow fault zones [Boettcher 199 and Jordan, 2004; Dascher-Cousineau et al., 2020]. Therefore, we also examined whether aftershock 200 productivity is controlled by the geometry of pre-existing faults present in subducted oceanic litho-201 sphere, particularly whether intermediate-depth earthquakes may be reactivating outer-rise faults or 202 fracture zones. As outer-rise faults form parallel to the trench and perpendicular to the slab dip direc-203 tion, we first tested whether aftershock productivity depends on whether the mainshock accommodates 204 down-dip or along-strike deformation of the slab based on the mainshock's P and T axes. We found 205 that, irrespective of whether the mainshock accommodates down-dip or along-strike deformation, the 206 two populations of intermediate-depth events have similar aftershock productivity statistics (Figure 207 1f). Identifying where intermediate-depth earthquakes may be reactivating fracture zones is more 208 difficult, because of the ambiguity in which nodal plane is the rupture plane. However, we note that 209 areas where the fracture zones are almost perpendicular to the trench, such as in South America, the 210 intermediate-depth earthquakes accommodate down-dip extension of the slab and are not reactivating 211 fracture zones, but still have low aftershock productivity for their magnitude (Supplementary Text 212 S2). 213

Therefore, features unique to a particular slab, at least at the scale of hundreds of kilometres resolvable with global catalogue data, seem unable to explain the scatter in aftershock productivity between events of similar magnitude. In the next section, we test whether higher-resolution regional earthquake catalogues with lower magnitudes of completeness can provide insights into the controls on intermediate-depth aftershock productivity not resolvable using the global seismic catalogue. Wimpenny et al.,

219 2.2 Regional Analysis: Northern Chile

High-resolution regional earthquake catalogues can provide better constraints on the spatial variability in aftershock productivity and its relationships with the mainshock setting [Sippl et al., 2019; Gomberg and Bodin, 2021; Chu and Beroza, 2022]. We re-assessed the aftershock productivity of moderatemagnitude earthquakes in northern Chile, because this region has: (1) an earthquake catalogue that contains over 100,000 earthquakes of $M_L \geq 2.0$ from 2006–2015 [Sippl et al., 2018], (2) a highly seismogenic slab at intermediate depths, and (3) relatively consistent earthquake mechanisms and magnitudes that allows for comparison between events with a similar source.

We applied the same aftershock identification algorithm to the catalogue of Sippl et al. [2018] for all 227 earthquakes with $M_w \ge 5.3$ that have moment tensors in the gCMT catalogue and include all events 228 above the completeness $M_L \ge 2.8$ as possible aftershocks (Figure 2). This analysis leads to aftershock 229 counts for 22 shallow mainshocks (<60 km depth) and 92 intermediate-depth mainshocks (60-300 km230 depth). There is not enough diversity amongst the magnitudes of these large mainshocks to robustly 231 calculate a scaling between mainshock magnitude and aftershock productivity, which limits our ability 232 to compare the relative aftershock productivity of shallow and intermediate-depth mainshocks using 233 this data set. Therefore, we focus our analysis on the relative aftershock productivity amongst the 234 population of intermediate-depth earthquakes that have similar magnitudes. 235

The majority of the large intermediate-depth earthquakes beneath northern Chile occur in a cluster 236 in the depth range of 80–140 km and 200–300 km from the trench (Figure 2b). Within this cluster, 237 the 12 largest $M_w > 6$ earthquakes have near-identical magnitudes, focal mechanisms, hypocentral 238 depths, and are in similar parts of the slab, but can still have significant differences in the number of 239 aftershocks they produce (Figure 2b, see inset). There is no clear change in the number of aftershocks 240 with depth for events within the intermediate-depth cluster Figure 2c. Cabrera et al. [2021] suggested 241 that the aftershock productivity may decrease systematically as a function of distance below the slab 242 surface using six well-located mainshocks, though we did not find this pattern when considering our 243 data set of 114 mainshocks (Figure 2d). The spatial heterogeneity in aftershock productivity even in 244 this small study area suggest that the controls on aftershock productivity may vary on length-scales 245 that are small compared to the location differences between mainshocks, which is equivalent to a few 246 tens of kilometers. 247

Similar analyses of high-resolution regional earthquake catalogues have been performed for
intermediate-depth earthquakes in Cascadia [Gomberg and Bodin, 2021] and Japan [Chu and Beroza,

2022]. The analysis from Cascadia included 63 mainshocks and used a catalogue complete down to 250 $M_L = 1.9$. Gomberg and Bodin [2021] found that the aftershock productivity increased with main-251 shock magnitude and decreased with mainshock depth. A notable difference between Cascadia and 252 northern Chile is that the background seismicity rate correlates weakly with the aftershock produc-253 tivity in Cascadia, whilst we did not find this trend in either our global analysis or for northern Chile 254 (Supplementary Text S3). The analysis of aftershock productivity in Japan included 64 mainshocks 255 and used the JMA catalogue, which is complete to $M_{JMA} = 2.0$. Chu and Beroza [2022] found that the 256 aftershock productivity of intermediate-depth earthquakes was consistently lower than shallow earth-257 quakes of equivalent magnitude, and that aftershock productivity increased with magnitude. However, 258 there was not enough variability amongst the intermediate-depth events to determine whether after-259 shock productivity varied with depth. Chu and Beroza [2022] found that around half of all events have 260 no recorded aftershocks, whilst for those that do have aftershock sequences the aftershock productivity 261 scales with the V_p/V_s ratio in the region. In northern Chile, we find more of a continuum of aftershock 262 productivity, but our results support the view of Chu and Beroza [2022] that some mechanism in 263 addition to just the depth and magnitude of the mainshock is influencing the variability in aftershock 264 productivity. 265

266 2.3 Summary of Aftershock Productivity Results

We find that the low aftershock productivity of intermediate-depth earthquakes compared to shallow 267 earthquakes of equivalent magnitude is a robust result between both global and regional earthquake 268 catalogues. For intermediate-depth earthquakes, the aftershock productivity increases systematically 269 with mainshock magnitude as $\approx 10^{M_w}$, and we have shown tentative evidence that it decreases slightly 270 as a function of depth. We interpret the increase in aftershock productivity with magnitude to reflect 271 the fact that larger main shocks having larger rupture areas A with $A \propto 10^{M_w}$ causing stress changes 272 on a larger fault area, or in a larger volume, surrounding the mainshock rupture [Wetzler et al., 273 2016]. Assuming that the number of faults within the slab remains constant with depth, the slight 274 decrease in aftershock productivity with depth for earthquakes between 60 km and 300 km implies 275 that the mechanism that controls aftershock productivity is also itself depth dependent. However, an 276 important conclusion is that there is still variability in the aftershock productivity of intermediate-277 depth earthquakes that cannot be explained by the magnitude of the mainshock and mainshock depth 278 alone. 279

280 We did not find any robust evidence for systematic variations in aftershock productivity between dif-

ferent slab settings. For example, the aftershock productivity does not vary systematically with the background rate of seismicity within the slab. Rather, aftershock productivity seems to be heterogeneous at the scale of individual subduction zones and within individual slabs. The variability in aftershock productivity within the cluster of near-identical intermediate-depth earthquakes beneath northern Chile is the type example of this behaviour, and which leads us to suggest that the mechanism that controls aftershock productivity may also be heterogeneous over length-scales of only a few tens of kilometres.

The low aftershock productivity of intermediate-depth earthquakes compared to shallow earthquakes of equivalent magnitude suggests fault systems within the slab are less sensitive to stress transfer than those within the shallow parts of the lithosphere. In the next section, we explore whether intraslab faults are also insensitive to slip on the subduction interface in major megathrust earthquakes.

²⁹² 3 Response of Intermediate-Depth Seismicity to Megathrust Slip

Intraslab faults will experience stress changes in response to slip on the megathrust [Lin and Stein, 2004]. These stress changes have been suggested to modulate the frequency of earthquakes that accommodate down-dip extension or compression within the slab [Astiz et al., 1988; Dmowska et al., 1988; Lay et al., 1989]. In particular, Astiz et al. [1988] argued that down-dip compressional earthquakes at intermediate depths are more frequent after megathrust earthquakes, and down-dip extensional earthquakes less frequent, as megathrust slip may cause incremental down-dip compression of the slab.

³⁰⁰ 3.1 Stress Changes in Slabs Caused by Megathrust Slip

The stress changes caused by slip on a megathrust will vary throughout the slab, and may therefore 301 modulate where earthquakes are triggered. Therefore, to test the conceptual model of Astiz et al. [1988] 302 and inform our data processing strategy, we first performed a set of calculations to examine the stress 303 changes caused by slip on the megathrust in different slab settings. We calculated the stress changes 304 in two dimensions using the elastic dislocation model of Okada [1992] and a synthetic slip distribution 305 on the slab surface defined by Slab 2.0 [Hayes et al., 2018]. The two-dimensional approximation 306 is reasonable given that, for $M_w > 8$ megathrust earthquakes, the rupture area is typically longer 307 along-strike than it is wide down-dip [Allen and Hayes, 2017]. In our models, slip on the slab surface 308

extended from the up-dip edge of Slab 2.0 to 50 km depth, and had a trapezoidal distribution with slip tapering over a down-dip distance of 50 km towards the edge of the slip patch. Synthetic tests showed that applying more complex slip distributions derived from finite-fault slip inversions had little effect on either the amplitude or the geometry of the stress changes at distances >20 km from the megathrust, as long as the average amount and depth-extent of slip on the megathrust is accurate (Supplementary Text S4). The results of these calculations for three different slab geometries (Japan, Kermadec and northern Chile) are shown in Figure 3.

To first-order, slip on the megathrust adds a predominantly horizontal tensional stress within the outer-rise region, and adds a predominantly down-dip compressional stress in the area of slab downdip of megathrust slip. The orientation of the principal stress axes rotate from being sub-parallel to the megathrust within the shallow parts of the slab to being oblique to the slab near its base. However, irrespective of the geometry of the slab, slip on the megathrust will lead to down-dip compression in the epicentral region of intermediate-depth earthquake generation (Figure 3).

The amplitude of the stress changes increases linearly with the average slip on the megathrust. Larger 322 magnitude earthquakes will cause stress increases of a particular amplitude within a larger volume of 323 the slab, and therefore potentially lead to a stronger signal of triggered seismicity. More generally, the 324 largest stress changes occur at the tips of the slip area, which corresponds to the trench and, at its 325 down-dip end, the brittle-ductile transition on the megathrust. Stress changes decrease with distance 326 as approximately r^{-3} with distance from the megathrust [Okada, 1992], and the amplitude of the 327 stress changes within the slab interior at intermediate depths are similar to those within the outer-328 rise, where there is often extensive triggered seismicity after megathrust earthquakes [Christensen and 329 Ruff, 1983; Bilek and Lay, 2018]. 330

Overall, these physical models of stress change due to megathrust slip support the conceptual model of Astiz et al. [1988]. In the next section, we therefore extend the original analyses of changes in intermediate-depth seismicity around the timing of major megathrust earthquakes from Astiz et al. [1988] and Lay et al. [1989] using the more temporally complete gCMT catalogue [Dziewonski et al., 1981; Ekström et al., 2012].

336 3.2 Global Analysis

We focus our analysis on the largest megathrust earthquakes of $M_w \ge 8.0$ between 1990 and 2017, which provides us with a set of events that are likely to be on kinematically coupled sections of the

megathrust and that were late in their earthquake cycle. Based on our modelling in Section 3.1, 339 these large earthquakes are also the ones most likely to have led to changes in seismicity rates within 340 the slab. For each large megathrust earthquake, we extracted all of the earthquakes surrounding 341 the mainshock from the gCMT catalogue with centroid depths in the range 60–300 km and that are 342 within ± 200 km of the projection of the megathrust earthquake's T-axis in the down-dip direction of 343 the slab. We then removed all earthquakes with centroids that are above the slab surface defined by 344 Slab 2.0 [Hayes et al., 2018]. We also repeated the analysis but without excluding events based on 345 their position relative to the slab, given that both the slab surface and the earthquake centroid depths 346 can be uncertain by ± 10 km or more, but found this had only a minor effect on the resulting patterns. 347

To assign each earthquake to either down-dip compression or extension, we filtered the events based 348 on the angle between their P, T, and N-axes and the normal and dip vector of the slab derived 349 from Slab 2.0. Earthquakes are associated with down-dip compression if the T-axis is within 45° of 350 the slab normal, the N-axis makes an angle greater than 45° with the slab normal, and the N-axis 351 makes an angle greater than 45° with the slab dip vector. The same filter was used to isolate down-352 dip extensional earthquakes, but with the constraint that the P-axis is within 45° of the slab normal 353 vector. Earthquakes that do not fit these two conditions (denoted 'other' in the analysis below) mostly 354 accommodate along-strike deformation of the slab or shearing of the slab in the plane parallel to the 355 slab dip direction (slab tearing). We also assess the temporal variability in these events to ensure that 356 the method of data selection does not bias the results. 357

To examine changes in the frequency of intermediate-depth earthquakes associated with megathrust 358 slip, we calculated the difference in the number of earthquakes before (N_b) and after (N_a) the main-359 shock at time t_0 . We then divide this by the total number of earthquakes in the period $[t_0 - \Delta t, t_0 + \Delta t]$, 360 yielding a value $\Delta N/N = (N_a - N_b)/(N_a + N_b)$ that is in the range [-1,1]. A value of 1 means all 361 earthquakes of a particular mechanism occurred after the mainshock, whilst -1 means they all oc-362 curred before the mainshock. We calculated $\Delta N/N$ for all earthquakes with magnitude $M \geq M_c$ 363 where M_c is in the range [5.0, 6.0] and for Δt of 5 years or 10 years. This simple approach captures 364 the rate changes without relying on any assumptions about the statistical distribution of seismicity in 365 time, as a more complex approach is not warranted by the limited number of earthquakes. 366

The analyses of three different earthquakes illustrate the key results (Figure 4). For the 2011 M_w 9.1 Tohoku-oki earthquake, the largest event in the gCMT catalogue, there are only 12 down-dip extensional and 21 down-dip compressional earthquakes at intermediate depths within 20 years of the mainshock (Figure 4a). All of the down-dip extensional earthquakes with $M_w \geq 5.5$ occurred

prior to the mainshock, and there were no down-dip extensional earthquakes in the 10 years following 371 the mainshock. Evidence for changes in the frequency of down-dip compressional earthquakes is less 372 clear, as there are too few events (Figure 4a). Therefore, the extensional seismicity down-dip of 373 the Tohoku-oki mainshock appears to follow the trend predicted by the model of Astiz et al. [1988]. 374 The slab down-dip of the 2001 M_w 8.1 Arequipa earthquake is far more seismogenic compared to 375 Japan, with predominantly down-dip extensional seismicity as the slab bends into the mantle beneath 376 the Andes (Figure 4b). The number of down-dip extensional earthquakes systematically increased 377 following slip on the megathrust in the Arequipa earthquake, which is opposite to the trend expected if 378 megathrust slip puts the slab into incremental down-dip compression and inhibits down-dip extensional 379 earthquakes. The intermediate-depth seismicity down-dip of the 2006 M_w 8.2 Kermadec earthquake 380 shows a different result again. In this region, the majority of the intermediate-depth earthquakes 381 are associated with down-dip compression. We find no robust change in the frequency of down-dip 382 extensional earthquakes caused by megathrust slip. However, the data suggests that the number of 383 down-dip compressional earthquakes with $M_w \geq 5.5$ decreased after megathrust slip, which is again 384 contrary to the prediction that megathrust earthquakes promote down-dip compressional seismicity. 385

The three examples in Figure 4 demonstrate that changes in the frequency of earthquakes associated 386 with down-dip extension or compression can occur around megathrust earthquakes, but they are not 387 necessarily consistent between events. To further demonstrate this point, we performed the following 388 test. For every mainshock j, we assign a decrease in rate $\Delta N/N < 0$ a value of $n_j = -1$ and an increase 389 in rate $\Delta N/N > 0$ a value of $n_j = 1$ for a given time-span Δt relative to the mainshock and magnitude 390 cut-off M_c . We then compute $\sum_{j=1}^k n_j(M_c, \Delta t)$ for all megathrust mainshocks $j = \{1, 2...k\}$. If there 391 is a consistent pattern of rate increases after the mainshock, then $\sum_{j=1}^{k} n_j(M_c, \Delta t) > 0$, whilst a rate 392 decrease would be associated with $\sum_{j=1}^{k} n_j(M_c, \Delta t) < 0$. This process is equivalent to a 1-dimensional 393 simple random walk. In the case of the null hypothesis that an increase in seismicity is equally likely 394 as a decrease, the expected value of $\sum_{j=1}^{k} n_j(M_c, \Delta t)$ is 0 and the standard deviation is \sqrt{k} . The 395 results of this stacking process are shown in Figure 5. 396

For down-dip extensional seismicity the sum $\sum_{j=1}^{k} n_j(M_c, \Delta t)$ is similar to the expected value for the null hypothesis (Figure 5a), suggesting there is no consistent change in down-dip extension of the slab after megathrust earthquakes. Down-dip compressional seismicity does typically increase after megathrust earthquakes, but only for intermediate-depth earthquakes with $M_w \leq 5.5$ (Figure 5b), which is around the magnitude of completeness of the gCMT catalogue [Kagan, 2003]. The smallest M_w 5 earthquakes are also likely to have the largest depth and mechanism uncertainties

[Wimpenny and Watson, 2020], and so thrust-faulting on the megathrust may also be incorrectly 403 assigned to being within the slab. The amplitude of the deviation from the expected value for the null 404 hypothesis for earthquakes $M_w > 5.5$ is smaller than 2 standard deviations, therefore we cannot reject 405 the hypothesis that these changes in earthquake frequency are random when only considering events 406 above the magnitude of completeness. Given that down-dip extension, compression, and other types 407 of earthquake mechanisms at intermediate-depths generally increase in frequency in the 5–10 years 408 after a mainshock (Figure 5a-c), and the increase becomes more robust for longer time-spans Δt , then 409 these trends most likely reflect the increase in the gCMT catalogue completeness through time. 410

In summary, we find no robust evidence in the gCMT catalogue for systematic changes in the frequency of moderate-to-large magnitude earthquakes that accommodate down-dip deformation of the slab in the intermediate-depth range. In the next two sections, we test whether the apparent lack of triggered intraslab seismicity might reflect the limited number of earthquakes within the gCMT catalogue by focusing on two regions with extensive intraslab seismicity and high-quality regional catalogues.

416 3.3 Regional Analysis: Japan

Japan has the highest-resolution earthquake catalogue of any subduction zone due to the dense onshore 417 seismic network, and is therefore an ideal natural laboratory for this type of analysis. Delbridge et al. 418 [2017] previously reported an increase in intermediate-depth seismicity down-dip of the rupture area of 419 the 2011 Tohoku-oki earthquake in the upper plane of the double-seismic zone (DSZ) recorded by the 420 regional earthquake catalogue, which consists mostly of compressional earthquakes accommodating 421 unbending of the Pacific plate. Our analysis of the earthquake moment tensors from the gCMT 422 catalogue failed to identify such a trend (Figure 4a). We therefore re-analysed the frequency variations 423 of intermediate-depth earthquakes recorded in the JMA catalogue down-dip of the Tohoku-oki rupture 424 area (Figure 6a,b). A total of 6595 intermediate-depth earthquakes occurred in this region between 425 2006 and 2019 that are >100 km from the trench and >60 km deep, and which are larger than the 426 magnitude of completeness of the catalogue $(M_{JMA} = 2.0)$. We assigned events to the upper or lower 427 plane of the DSZ by binning the event depths relative to Slab 2.0 as a function of distance from the 428 trench and fitting a Gaussian mixture model to the relative depth distributions. 429

To examine changes in the earthquake frequency, we calculated the average earthquake rate in the upper and lower plane of the DSZ using a moving window that has width T and moves in steps Δt . The results shown in Figure 6b-d use T = 0.2 years and $\Delta t = 0.05$ years. From this moving

window analysis, we confirm there is a spike in the frequency of earthquakes assigned to the upper 433 plane within a month of the Tohoku-oki mainshock, with the rate increasing from ~ 0.5 earthquakes 434 per day to nearly 6 per day (Figure 6c). There is no clear change in the frequency of lower-plane 435 earthquakes over the same period. The peak seismicity rate in the upper plane occurred 1 month after 436 the mainshock and decayed over 7 years before returning to the background rate in 2018. However, this 437 result is extremely sensitive to the cut-off depth (Figure 6d). For an identical analysis of earthquakes 438 that have depths >70 km, the spike in earthquake frequency disappears and there is no clear deviation 439 from the pre-Tohoku seismicity (Figure 6e). 440

The large number of earthquakes in the JMA catalogue, and the relatively stable rate of seismicity 441 prior to Tohoku, allows us to test the statistical significance of the seismicity rate changes using the 442 β -statistic of Matthews and Reasenberg [1988]. The β -statistic is calculated as $\beta = (N - N_0)/\sigma_0$ where 443 N is the observed number of earthquakes within a sliding window of length T, and N_0 and σ_0 are the 444 mean and standard deviation of the number of earthquakes within time windows of length T selected 445 randomly from within the reference time period (in our case 2006–2011). The results of the β -statistic 446 analysis applied to the JMA data shows that there are no variations in the earthquake frequency for 447 events >70 km that are greater than 2 standard deviations from the pre-Tohoku seismicity (Figure 448 6f). An analysis of the seismicity in the ISC reviewed catalogue from the same region, which support 449 our observations made using the JMA catalogue, is discussed in Supplementary Text S5. 450

Further investigation revealed that the seismicity contributing to the spike in earthquake frequency 451 in the upper plane in Figure 6c mostly derived from the region of the 7th April 2011 M_w 7.2 Miyagi-452 oki reverse-faulting earthquake, which ruptured the slab at \sim 55–65 km depth less than a month 453 after the Tohoku-oki mainshock. Removing the seismicity within 50 km of the Miyagi-oki earthquake 454 suppresses the spike in the intermediate-depth seismicity rate (Supplementary Text S5). It is also 455 possible that the $\sim 5-10$ km uncertainties in earthquake hypocentral depths for small earthquakes in 456 the JMA catalogue mean that some aftershocks occurring at the down-dip edge of the megathrust, or 457 within the overriding plate, are mislocated and have been incorrectly assigned to the upper plane of 458 the DSZ [e.g. Sippl et al., 2019]. To test this possibility, we removed all events that are within 10 km 459 of the plate interface from the analysis, which also suppresses the spike in seismicity rate related to 460 the Tohoku-oki and Miyagi-oki earthquakes (Supplementary Text S5). Therefore, we conclude that 461 the change in earthquake frequency identified by Delbridge et al. [2017] may not indicate a slab-wide 462 increase in intermediate-depth earthquake frequency in response to the 2011 Tohoku-oki earthquake, 463 but rather the aftershock sequence of the Miyagi-oki earthquake (Figure 6b, inset). This difference 464

is important, because it suggests that the majority of faults that are definitively within the slab are
insensitive to the stress changes caused by megathrust slip in the Tohoku-oki earthquake.

467 3.4 Regional Analysis: Northern Chile

Megathrust slip has also been proposed to modulate intermediate-depth seismicity in northern Chile. 468 Jara et al. [2017] suggested that the 1995 Antofagasta and 2014 Iquique megathrust earthquakes 469 were followed by periods of reduced moderate-magnitude seismicity at intermediate depths beneath 470 northern Chile, whilst the 2005 Tarapaca intraslab earthquake was followed by nine years of increased 471 seismicity at both shallow and intermediate depths (Figure 7a,b). Since Jara et al. [2017]'s original 472 analysis, Sippl et al. [2018] has published an earthquake catalogue spanning 2006–2015 in northern 473 Chile that is complete down to $M_L = 2.8$, which allows us to examine the changes in intermediate-474 depth earthquake frequency before and after the Iquique earthquake in more detail. We calculated the 475 earthquake rate through time using the moving window analysis described in Section 3.3, but found 476 no significant deviations in the frequency of intermediate-depth seismicity following the 2014 Iquique 477 earthquake or the 2007 Tocopilla earthquake (Figure 7c,d). 478

The catalogue of Sippl et al. [2018] is too short to capture any of the multi-year trends in earthquake 479 frequency identified by Jara et al. [2017]. Therefore, we re-analysed the temporal variations in seis-480 micity in northern Chile between 1980 and 2020 using four more years of data in the ISC's reviewed 481 catalogue than were available to Jara et al. [2017] (Figure 7a). An important limitation in comparing 482 temporal variations in the shallow and intermediate-depth seismicity in this region is that the ISC 483 catalogue's magnitude of completeness is higher for shallow earthquakes that are offshore $(m_b = 4.7)$ 484 than for intermediate-depth earthquakes that are beneath the land $(m_b = 4.3; \text{ see Supplementary Text})$ 485 S6). To ensure that this spatial variability in completeness does not bias our analysis, we only studied 486 events with $m_b \ge 4.7$, which for the region shown on Figure 7 includes 925 earthquakes between 1980 487 and 2020. 488

The annual variations in the frequency of shallow (<50 km) and intermediate-depth (70–170 km) earthquakes are shown as histograms in Figure 7e-f, and as a cumulative distribution in Figure 8a. We plot the data as histograms, as opposed to using the moving window analysis of Section 3.3, because there are so few earthquakes above the magnitude of completeness. The depth intervals were selected to closely replicate the analysis of Jara et al. [2017]. Unlike Jara et al. [2017], however, we describe the trends in the undeclustered catalogue, and present the equivalent analyses of the declustered catalogue in Supplementary Text S6. We take this approach, because the deficiency of intermediate-depth aftershock sequences means that declustering has little effect on the trends in intermediate-depth earthquake frequency through time.

There is little shallow seismicity in northern Chile between 1980 and 2007 with typically fewer than 5 498 earthquakes per year with $m_b \ge 4.7$ (Figure 7e), which makes identifying any changes in earthquake 499 frequency during this period difficult. There are so few events in 1980–2007 that the cumulative 500 earthquake distribution with time is not significantly different (<2 standard deviations) from synthetic 501 catalogues that contain the same number of events but with randomised times (Figure 8b), suggesting 502 the shallow seismicity contains no robust information about temporal changes in earthquake frequency 503 in response to the 1995 Antofagasta, 2001 Arequipa, or 2005 Tarapaca earthquakes. Between the 2007 504 Tocopilla and 2014 Iquique earthquakes the annual number of shallow earthquakes increased (Figure 505 7e), which is associated with the well-documented foreshock sequence of the Iquique earthquake [Ruiz 506 et al., 2014]. The Iquique earthquake is then followed by an extensive aftershock sequence that lasts 507 until the end of the catalogue in 2020 (Figures 7e and 8a). 508

At intermediate depths the seismicity is more frequent and variable through time (Figure 7f). Between 509 1980 and 1995 the annual earthquake frequency changes from year-to-year (Figure 7f), but does not 510 deviate from the behaviour of time-randomised catalogues (Figure 8c). During 1980–1995, pulses 511 of seismicity occurred in 1983, 1985, and 1990 that were not associated with a large megathrust or 512 intermediate-depth earthquake (Figure 8c, black arrows). After 1995, there are two distinct changes 513 in the earthquake frequency that last for multiple years: first a decrease around the timing of the 1995 514 Antofagasta earthquake and then an increase around the timing of the 2001 Arequipa earthquake 515 (Figure 7f). This period of seismic quiescence at intermediate-depths between 1995 and 2001 appears 516 to be robust in northern Chile for magnitudes at least 0.5 units larger than the catalogue completeness 517 (Figure 7f). After 2001, we found no evidence for robust changes in the intermediate-depth earthquake 518 frequency caused by the 1987 Antofagasta, 2007 Tocopilla, and 2014 Iquique earthquakes (Figure 8c,d). 519

⁵²⁰ Our observations support the view that temporal changes in intermediate-depth earthquake frequency ⁵²¹ in northern Chile did occur, and in some cases lasted for multiple years. However, they are not ⁵²² consistently associated with megathrust earthquakes or large intermediate-depth earthquakes. If there ⁵²³ were a consistent physical reason for the frequency changes in response to megathrust slip, then ⁵²⁴ it is unclear why they should occur for only two megathrust events out of six between 1980 and ⁵²⁵ 2020. In addition, using the longer earthquake catalogue, we found that the 2014 Iquique megathrust ⁵²⁶ earthquake had no resolvable effect on the frequency of intermediate-depth earthquakes within the slab directly down-dip from the rupture area. Therefore, we argue that large megathrust earthquakes
are not the cause of changes in earthquake frequency at intermediate depths beneath northern Chile.

529 4 Discussion

530 4.1 Stress Sensitivity of Intermediate-Depth Seismicity

We initially set out to reconcile two contrasting views of intermediate-depth seismicity: one that 531 suggested intraslab fault systems are sensitive to small stress changes associated with megathrust 532 earthquakes, and another that suggested intraslab fault systems are insensitive to the stress changes 533 caused by large intraslab earthquakes. Our analyses support the view that intermediate-depth seis-534 micity within subducting slabs is relatively insensitive to static stress transfer as a result of slip in 535 large earthquakes with typical stress drops ($\sim 1-50$ MPa; see Allmann and Shearer [2009]; Poli and 536 Prieto [2016]; Tian et al. [2022]). This insensitivity is manifest as consistently low aftershock pro-537 ductivity of intermediate-depth earthquakes, and no consistent triggering of down-dip compressional 538 seismicity, or inhibition of down-dip extensional seismicity, within slabs following megathrust slip. We 539 also did not find any clear evidence that the sensitivity of intraslab faults to static stress transfer 540 varies systematically between subduction zones with different slab conditions. 541

The lack of seismicity triggered by static stress transfer at intermediate depths is similar to lack of 542 seismicity triggered by earthquakes on oceanic transform faults [Boettcher and Jordan, 2004], but in 543 stark contrast to the extensive seismicity that is triggered within the outer rise and outer trench-544 slope region following many major megathrust earthquakes that slip to the trench [Christensen and 545 Ruff, 1983; Bilek and Lay, 2018]. Earthquakes in the outer rises also have aftershock productivities 546 similar to earthquakes of equivalent magnitude within the continents [Dascher-Cousineau et al., 2020]. 547 This comparison between intermediate-depth and outer-rise seismicity is informative, because the 548 earthquake sources are in similar host material, just at different confining pressures and temperatures. 549 Therefore, the difference in sensitivity to stress change between outer-rise and intermediate-depth 550 seismicity does not appear to related to the distinct composition of the oceanic lithosphere. Rather, 551 it suggests that either: (a) the fault systems in the subducted oceanic lithosphere are not as close to 552 failure as those at the outer rise, or (b) that the mechanism of earthquake generation at intermediate 553 depth is not as sensitive to changes in static stress on the order of earthquake stress drops. This new 554 view of the sensitivity of fault systems within subducted oceanic lithosphere places constraints on the 555

mechanics of earthquake generation at intermediate depths, and the interplay between the source of stress and the mechanism allowing the release of stress in earthquakes on intraslab faults, which we explore further below.

559 4.2 Fault Mechanics of Intermediate-Depth Seismicity

Based on the earthquake catalogue data, and recent work on the source properties of intermediate depth earthquakes, any model of intermediate-depth seismicity should account for three observations:

Intermediate-depth earthquake stress drops (for both mainshocks and aftershocks) should be of
 a similar order of magnitude to those at shallow depth [Allmann and Shearer, 2009; Poli and
 Prieto, 2016; Tian et al., 2022].

2. The response of intermediate-depth seismicity to stress changes caused by earthquake stress
 drops must be limited, in order to explain the observations of low aftershock productivity and
 the low sensitivity of intraslab seismicity to slip on the megathrust interface.

3. There must be *some* capacity to generate limited aftershocks after intermediate-depth earthquakes, and this capacity should broadly scale with mainshock depth and mainshock magnitude.

For shallow faulting, the clock-advance model has proven a simple way of interpreting the sensitivity 570 of fault systems to static stress transfer [King et al., 1994; Hainzl et al., 2010]. In this model after-571 shocks reflect earthquakes on faults that would have eventually ruptured in response to slow stress 572 accumulation, but occurred earlier than expected due to an additional source of stress. A stress drop 573 of $\Delta \tau$ due to slip in an earthquake leads to stress transfer onto the surrounding faults of magnitude 574 $a_j \Delta \tau$, where a_j denotes a vector containing the elastic constants, distance, and relative geometry of 575 the newly stressed fault [Hainzl et al., 2010]. If the faults surrounding the mainshock have a stress dis-576 tribution τ_j and a yield stress τ_y , then any fault patches around the mainshock where $\tau_j + a_j \Delta \tau > \tau_y$ 577 will rupture in an aftershock (Figure 9a). In Figure 9a we assume that τ_j follows a distribution that 578 is symmetrical about the mean stress, and has a mean value set by the requirement for equilibrium. 579 We also assume that τ_y is roughly constant. Under these assumptions, fewer aftershocks would be 580 produced if the static stress transfer from the mainshock $a_j \Delta \tau$ is a smaller fraction of the failure 581 stress τ_y , or if the shape of the fault stress population becomes more skewed towards lower stresses. 582 More aftershocks will be produced for larger magnitude earthquakes, because the volume of material 583

around the mainshock that experiences stress changes will be larger meaning the curve in Figure 9a will be taller.

A simple prediction of the clock-advance model is that for a given background seismicity rate r and 586 stressing rate $\dot{\tau}$, then a change in static stress $\Delta \tau$ should lead to a change in the number of earthquakes 587 in a region proportional to $r\Delta \tau/\dot{\tau}$. Our analysis suggests that aftershock productivity for intermediate-588 depth earthquakes does not correlate with the background seismicity rate within the slab (see also 589 Sippl et al. [2019]; Chu and Beroza [2022]). Similarly, the aftershock productivity does not correlate 590 with the down-dip gradient in slab curvature, which is a proxy for the bending-related loading rate of 591 faults within the slab [Sandiford et al., 2020]. In addition, areas where intermediate-depth seismicity 592 is particularly common (e.g. northern Chile) are not more sensitive to earthquake stress changes 593 than places where the slab has relatively few earthquakes (e.g. central Japan). We suggest these 594 departures from predictions of the clock-advance model may indicate that the stresses sustained by 595 the intraslab fault population are significantly below the failure stress, and changes in the failure stress 596 through fault weakening mechanisms far exceed the stress transfer from earthquake stress drops. The 597 modifications to the clock-advance model for the three main weakening mechanisms proposed to enable 598 intermediate-depth seismicity (dehydration embrittlement, dehydration-assisted stress transfer, self-599 localising thermal runaway) are shown in Figure 9b-d. We discuss each mechanism, and its ability to 600 account for the three features of intermediate-depth seismicity, in turn below. 601

602 4.2.1 Dehydration Embrittlement

⁶⁰³ Dehydration embrittlement involves the weakening of fault zones through the build up of highly-⁶⁰⁴ pressurised fluids released by the breakdown of hydrous mafic minerals during prograde metamorphism ⁶⁰⁵ (Figure 9b). For this mechanism, the low stress drops in intermediate-depth earthquakes compared ⁶⁰⁶ to the stresses required for frictional failure on a fault formed of dry olivine at equivalent depths (\sim 1 ⁶⁰⁷ GPa at 100 km depth) may either reflect partial stress release, the low shear stresses needed to break ⁶⁰⁸ faults with a low effective strength, or some combination of both of these.

To simplify the representation of dehydration embrittlement in Figure 9b, we consider two populations of faults within the slab: those that contain highly pressurised fluids, and those that do not. Faults containing pressurised fluid are breaking in earthquakes at a low failure stress (Figure 9b), whilst dry faults will be far from their failure stress because the finite size of the forces acting on the slab can only load them to a fraction of their failure stress. For the dry fault population, static stress transfer ⁶¹⁴ is unlikely to trigger aftershocks, because most of the faults support stresses that are a small fraction ⁶¹⁵ of the failure stress (Figure 9b, black curve). In contrast, stress transfer could trigger slip on the ⁶¹⁶ fault population containing pressurised fluids, with the number of aftershocks being related to the ⁶¹⁷ number of faults that have been able to trap and build up high fluid pressures (Figure 9b, blue curve). ⁶¹⁸ Pervasive dehydration embrittlement, in which most faults in the slab contain near-lithostatic pore ⁶¹⁹ fluids, seems unlikely, as this would cause the intraslab faults to be sensitive to stress transfer, and we ⁶²⁰ would expect an aftershock productivity similar to that seen in the shallow crust or higher.

Recent work has highlighted the link between aftershock productivity in the subducted Pacific slab beneath Japan and the V_p/V_s structure of the surrounding medium [Chu and Beroza, 2022], with higher aftershock productivity linked to higher V_p/V_s ratios and by inference more fluid, which supports this model. The effects of dehydration embrittlement are expected to be spatially heterogeneous due to its dependence on the availability of hydrous minerals and the trapping of the released fluid in faults, then this mechanism has the capacity to account for the spatial variability in aftershock productivity within slabs. Dehydration embrittlement can therefore account for the observations outlined in Section 4.2.

628 4.2.2 Dehydration-Assisted Stress Transfer

An alternative mechanism is dehydration-assisted stress transfer, where the loss of load-bearing capac-629 ity of hydrous minerals within a mixed-composition aggregate leads to the support of the total force 630 acting on a fault onto a fraction of its surface area, allowing the fault to locally reach its failure stress 631 [Ferrand et al., 2017] (Figure 9c). Whilst the failure stress and stress drops at contact level for this 632 mechanism need to be extremely high (500–1000 MPa), fault-averaged stress drops could be far lower 633 if the fault can rupture through patches of weaker hydrous minerals at low shear stresses to account 634 for the $\sim 1-50$ MPa seismologically-observed stress drops. Melting of the rupture plane at high stresses 635 could also lead to a proportion of the stress release being accommodated aseismically as ductile shear-636 ing during the latter stages of slip, after an initial seismically-radiating phase. The resulting stress 637 transfer onto the surrounding faults would be moderated by elastic parameters, the relative location 638 and fault geometry, plus an additional factor describing the degree to which dehydration-assisted stress 639 transfer concentrates stresses at the contact level $(b_j \Delta \tau;$ Figure 9c). 640

As with dehydration embrittlement, the fault population will support average stresses that are significantly lower than the failure stress of faults containing dry olivine (Figure 9c, black curve). Following
a mainshock the stress transfer onto the surrounding faults will be a small fraction of the total fault

strength, but will be boosted by the focusing of the stress onto small asperities described by the factor 644 b_j . The controls on aftershock productivity will therefore be similar to the dehydration embrittle-645 ment mechanism described above, as it will depend on the degree to which the surrounding material 646 had already dehydrated, and therefore the proportion of the fault population within the slab that 647 can generate the locally high contact stresses needed for failure (Figure 9c, red curve). Zero or low 648 aftershock productivity will occur where the majority of the weak, hydrous phases have broken down 649 into stronger anhydrous phases, meaning that the factor b_j is smaller. The relative insensitivity of 650 intermediate-depth seismicity to slip on the subduction interface is a result of the stress transfer being 651 a smaller fraction of the failure stress compared to shallow faulting (Figure 9c). Hence, dehydration 652 stress-transfer can also match the three observational requirements described above. 653

654 4.2.3 Self-Localising Thermal Runaway

The final weakening mechanism is self-localising thermal runaway, in which creep in shear zones causes 655 shear heating and the development of ductile instabilities that relax elastic strain [Ogawa, 1987; Hobbs 656 and Ord, 1988]. Numerical models of self-localising thermal runaway suggest that the stress drops 657 generated by an earthquake are a significant fraction of the fault's failure stress (often \sim 500–1000 658 MPa at ~ 1 GPa confining pressure), as the positive feedback between strain and shear heating drives 659 runaway failure that relaxes the majority of the elastic strain stored around the fault [Kelemen and 660 Hirth, 2007; John et al., 2009]. Not all of the stress drop and strain release may be seismogenic, and 661 therefore this mechanism might be consistent with the low seismologically-determined stress drops. 662 However, the resulting stress transfer onto surrounding fault systems $a_j \Delta \tau$ should be a larger fraction 663 of the failure stress than for the dehydration-based mechanisms described above (Figure 9d). 664

The self-localising thermal runaway weakening mechanism is mostly dependent on the stress state of 665 the given shear zone, and does not require any additional chemical processes to weaken the fault. 666 We would not expect to see sensitivity of intermediate-depth seismicity to the shallow, lower-stress 667 drop megathrust earthquakes because the fault failure stress is much larger than the static stress 668 transfer. However, we might expect aftershock productivity to be similar at intermediate-depths to 669 shallow depths, because the ratio between the amplitude of the static stress transfer $a_j\Delta\tau$ and the 670 fault failure stress τ_y will be similar to that at shallow depths (Figure 9d). Therefore, self-localising 671 thermal runaway is less consistent with our observations of low intraslab aftershock productivity for 672 intermediate-depth earthquakes. 673

674 5 Conclusions

Intermediate-depth earthquakes produce fewer aftershocks compared to shallow (<60 km) earthquakes 675 of similar magnitude. The areas of intermediate-depth seismicity down-dip of major megathrust 676 earthquakes are also insensitive to the static stress transfer on the order of earthquakes stress drops 677 caused by megathrust slip. We interpret the relative insensitivity of intermediate-depth seismicity to 678 static stress transfer to suggest that faults within the slab are further from their failure stress than 679 is typical for shallow fault systems. It follows that the availability of the weakening mechanism is 680 the likely control on intermediate-depth aftershock productivity, and this mechanism is heterogeneous 681 over length-scales of a few tens of kilometres to account for the variability in aftershock productivity 682 within slabs. We suggest dehydration-related weakening mechanisms are most consistent with these 683 observations. 684

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⁶⁹² Data Availability

All data used in this study are freely available. The ISC catalogue is available from https://doi. org/10.31905/D808B830, the gCMT catalogue is available from https://www.globalcmt.org/, the JMA catalogue is available from https://www.data.jma.go.jp/svd/eqev/data/bulletin/index_ e.html, and the IPOC catalogue is available from doi.org/10.5880/GFZ.4.1.2018.001 (all last accessed December 2022). All of the codes needed to reproduce the aftershock productivity results and analysis of seismicity rates through time are available from https://doi.org/10.5281/zenodo. 7817786.

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Figures



Figure 1: Aftershock productivity for earthquakes in the gCMT catalogue with $M_w \ge 6.5$. (a) Aftershock productivity as a function of the mainshock depth. Intermediate-depth earthquakes (60– 300 km) are shown in dark grey. The histogram of the logarithm of mainshock frequency with depth is shown above. (b) Aftershock productivity as a function of mainshock magnitude. Intermediatedepth earthquakes are shown in dark grey with black outline, whilst earthquakes with hypocentral depths <60 km are shown as light grey circles. The median aftershock productivity scaling is shown for shallow and intermediate-depth mainshocks. R_s is the Spearman's Correlation Coefficient. (c) Aftershock productivity as a function of mainshock date, (d) the gradient in the down-dip curvature of the slab at the centroid location computed from Slab 2.0 [Hayes et al., 2018], and (e) the background seismicity rate within 50 km horizontal distance and ±30 km depth difference from the mainshock hypocentre. (f) Histogram of aftershock productivity for mainshocks that accommodate either alongstrike or down-dip deformation of the slab. The red histogram shows the productivity for shallow earthquakes with hypocentral depths <60 km.



Figure 2: Aftershock productivity of moderate-magnitude earthquakes in northern Chile using the IPOC catalogue of Sippl et al. [2018]. (a) Map of the spatial distribution of the seismicity overlain with the focal mechanisms of the mainshocks taken from the gCMT catalogue. The focal mechanisms are coloured by the number of counted aftershocks. Mainshocks that are M_w 6.0–6.5 and at depths \geq 70 km are highlighted by a black outline. Slab contours are from Slab 2.0 [Hayes et al., 2018]. (b) Cross-section through the IPOC seismicity overlain by the mainshocks shown as blue circles. Mainshocks are scaled by magnitude. (c) Aftershock productivity as a function of mainshock depth for mainshocks with hypocentral depths >70 km only.



Figure 3: Stress changes imposed on the slab due to slip on the megathrust in regions with different slab geometries, including (a) Japan, (b) Kermadec, and (c) northern Chile. The slip distribution in each calculation is limited to between the section of the slab surface highlighted in white, has a peak of 5 m, and linearly tapers towards the up-dip and down-dip edge of the slip patch over a distance of 50 km. σ_{II} is the second invariant of the stress tensor, which represents the maximum shear stress imposed on faults within the slab. The principal stress axes show the geometry of the stress changes. Seismicity within 200 km of the slab profile is shown as circles scaled in size by the earthquake magnitude. The seismicity is taken from the global CMT catalogue [Ekström et al., 2012], and is defined as down-dip extensional, down-dip compressional or 'other' based on the criteria outlined in Section 3.2.



Figure 4: Examples of changes in intermediate-depth earthquake mechanisms before and after three major megathrust earthquakes. Mechanisms are coloured red if the are related to down-dip compression, blue for down-dip extension and grey for along-strike deformation. Contours represent the depth to the slab surface from Slab 2.0 [Hayes et al., 2018] and are every 20 km. The middle panel is a time-series of earthquake mechanisms as a function of magnitude. The dark grey horizontal line represents the global magnitude of completeness of the gCMT catalogue. The bottom panel shows the difference in the number of earthquakes after and before the megathrust event divided by the total number of earthquakes after and before the megathrust event divided by the total number of earthquakes the range of completeness for the gCMT catalogue. Squares and triangles represent $\Delta N/N$ for the period 5 years and 10 years either side of the mainshock, respectively. The size of the symbol is scaled by the number of earthquakes in that bin and decreases in size as the number of events in the bin gets smaller.



Figure 5: Compilation of changes in the frequency of intermediate-depth earthquakes following megathrust slip as a function of magnitude cut-off M_c and time-span Δt for (a) down-dip extensional, (b) down-dip compressional, and (c) other types of earthquakes. The colour in each panel represents the number of standard deviations from the mean distance that the summation reaches in k steps, equivalent to $\sum_{j=1}^{k} n_j / \sqrt{k}$. Given the null hypothesis is that an increase and a decrease in earthquake frequency are both equally likely, the expected value of $\sum_{j=1}^{k} n_j / \sqrt{k}$ is zero. The vertical dashed lines represent the approximate range in magnitude of completeness of the gCMT catalogue. The solid black line marks the 2 standard deviations boundary, with ticks on the inside of the boundary enclosing regions where the changes in earthquake frequency are unlikely to arise due to chance.



Figure 6: Temporal variations in intermediate-depth seismicity in response to the 2011 M_w 9.1 Tohoku-oki earthquake. (a) Spatial distribution of seismicity used in the analysis from the JMA catalogue. Contours of the slab surface are shown as black-dashed lines from Slab 2.0 [Hayes et al., 2018]. (b) Cross-section through the seismicity with the two depth cut-offs used in the analysis at 60 km and 70 km shown as black dashed lines. Inset is a zoom-in of the seismicity within ±1 month of the 7th April 2011 Miyagi-oki earthquake. The aftershocks of the Miyagi-oki earthquake clearly extend 10–15 km below the slab surface, but remain shallower than 70 km depth. (c) Average number of earthquakes per day in the upper plane (light red) and lower plane (light blue) of the double-seismic zone (DSZ) for all events >60 km depth. The time-series is calculated using a sliding window of length 0.2 years and time step 0.05 years. The vertical black line marks the timing of the Tohoku-oki mainshock. (d) Equivalent plot to (c), but for all events >70 km. (e) and (f) show the β -statistic of Matthews and Reasenberg [1988] for all events >60 km and >70 km depth, respectively. If β exceeds 2, this is equivalent to the earthquake rate deviating more than 2 standard deviations from background, with the background defined by the seismicity rate during the period 2006–2011.



Figure 7: Overview of seismicity in northern Chile between 1980 and 2020. (a) Map view of the distribution of seismicity from the ISC catalogue with $m_b \ge 4.7$ with the focal mechanisms of the largest mainshocks. Grey circles represent earthquake hypocentres, and coloured circles represent earthquakes used in the analyses in (b,e,f). Dark coloured circles are shallow earthquakes and redorange coloured circles are intermediate-depth earthquakes. (b) Cross-sectional view of the seismicity projected onto the black-dashed path in (a) showing the cluster of seismicity at ~400 km distance along the profile. (c) Temporal evolution of shallow (<50 km) seismicity in northern Chile from the IPOC catalogue of Sippl et al. [2018] calculated using a sliding window of width 0.1 year and time steps of 0.02 years. (d) Same as (c), but for the intermediate-depth seismicity between 70 km and 300 km depth. (e) and (f) show histograms of the number of earthquakes in the ISC catalogue with $m_b > M$ each year for the shallow and intermediate-depth seismicity, respectively. The area in grey marks the installment of the IPOC network in northern Chile in 2006. Vertical dashed lines mark the timing of major earthquakes in the region and their magnitudes, with megathrust events represented by a light blue box and intraslab events by a light red box.



Figure 8: Cumulative distribution of shallow and intermediate-depth earthquakes in northern Chile shown in Figure 7a. (a) Cumulative distribution between 1980 and 2020 of events $m_b \ge 4.7$. Major $(M_w \ge 7.5)$ megathrust and intermediate-depth earthquakes are shown by vertical dashed lines, with Ant = Antofagasta, Are = Arequipa, Tar = Tarapaca, Toc = Tocopilla and Iqu = Iquique. (b-d) Cumulative distributions of seismicity over particular periods of time compared to the predictions of time-randomised catalogues. The grey polygons show the area in which 67%, 95% and 99% of catalogues with the same number of events N but randomised earthquake times would plot. The confidence intervals are wider for catalogues with fewer events. In (c) vertical arrows point out distinct changes in the frequency of earthquakes that do not correlate with any major earthquakes. The equivalent plot for the declustered catalogue is shown in Supplementary Figure 14.



Figure 9: Sketch of the effect of stress transfer from an earthquake stress drop of amplitude $\Delta \tau$ on the triggering of nearby seismicity for (a) shallow earthquakes, and intermediate-depth earthquakes generated by (b) dehydration embrittlement, (c) dehydration-assisted stress transfer, and (d) self-localising thermal runaway (SLTR). For each mechanism, the top row shows the shear stress distribution on a population of seismogenic faults within a fixed (arbitrary) volume around the mainshock, where τ_y is the maximum failure stress for a given failure mechanism. In (b) and (c) the maximum failure stress would be dry olivine friction, or the effective failure stress needed to drive self-localising thermal runaway. The coloured region shows schematically the number of faults that would fail in aftershocks in response to a fixed stress transfer. The bottom row shows the failure strength envelope. The envelope shape in (d) is modified from John et al. [2009].