Re-examining Temporal Variations in Intermediate-Depth Seismicity

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Abstract

Changes in the frequency of intermediate-depth (60–300 km) earthquakes in response to static stress transfer can provide insights into the mechanisms of earthquake generation within subducting slabs. In this study, we use the most up-to-date global and regional earthquake catalogues to show that both the aftershock productivity of large earthquakes, and the changes in the frequency of intermediate-depth earthquakes around the timing of major megathrust slip, support the view that faults within the slab are relatively insensitive to static stress transfer on the order of earthquake stress drops. We interpret these results to suggest the population of faults within the slab are much further from their failure stress than is typical for shallow fault systems. We also find that aftershock productivity varies within slabs over small spatial scales, indicating that the mechanism that enables faults to rupture at intermediate depths is likely to be spatially heterogeneous over length-scales of a few tens of kilometres. We suggest dehydration-related weakening mechanisms can best account for this heterogeneity.

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Plain Language Summary

Earthquakes at 60–300 km depth within subducting slabs are known as ‘intermediate-depth’ earthquakes. At such depths, the high pressures should act to clamp faults shut, preventing them from breaking in earthquakes through frictional sliding. In this study, we investigate the mechanisms that enable the generation of intermediate-depth earthquakes by examining the temporal changes of intermediate-depth seismicity caused by other, nearby earthquakes. We find that seismicity within slabs is relatively insensitive to the stress changes caused by nearby earthquakes when compared to shallow earthquakes of equivalent size. We interpret these results to suggest that faults within the slab are much further from their failure stress than is typical for shallow faults, and that the mechanism that enables faults to rupture at intermediate depth is likely to be spatially variable over length-scales of a few tens of kilometres. We suggest weakening mechanisms related to water release within slabs can best account for this heterogeneity.

Key Points:

• Large intraslab and megathrust earthquakes have a limited influence on the frequency of intermediate-depth seismicity.

• Faults within subducted slabs are relatively insensitive to static stress transfer caused by earthquake stress drops.

• Low stress drops and heterogeneous aftershock productivity can be best explained by dehydration-related weakening mechanisms.
1 Introduction

Temporal variations in the frequency of intermediate-depth (60–300 km) earthquakes have the potential to provide insights into the enigmatic conditions and mechanism(s) of earthquake nucleation within subducting slabs. These intraslab earthquakes have dominantly double-couple focal mechanisms, indicating they represent shear failure on a population of faults [Frohlich, 1989]. However, at depths $\gtrsim 60$ km, the high confining pressures and high temperatures should prevent frictional failure on faults subject to normal plate-driving forces without an additional mechanism that reduces the stress needed to generate earthquake rupture [Zhan, 2020].

Two main mechanisms have been proposed: dehydration-related weakening and self-localising thermal runaway. Dehydration-related weakening is caused by the breakdown of hydrous mafic minerals as the slab subducts, which either releases water that reduces the effective frictional strength of intraslab faults (dehydration embrittlement; Green and Houston [1995]; Hacker et al. [2003]), or causes extreme stress concentrations through the breakdown of load-bearing hydrous phases (dehydration-assisted stress transfer; Ferrand et al. [2017]), allowing faults to fail through frictional sliding. Alternatively, self-localising thermal runaway is a process by which creep in hydrated or fine-grained shear zones causes shear heating and the development of ductile instabilities that relax elastic strain [Ogawa, 1987; Hobbs and Ord, 1988]. Thermal runaway may have a nucleation phase involving progressive ductile strain, eventually leading up to seismogenic failure that relaxes the majority of the stored elastic strain in high stress-drop events (500–1000 MPa; Kelemen and Hirth [2007]; John et al. [2009]).

These different mechanisms can account for the observation of earthquake generation at high confining pressures, but they should be sensitive to different physical and mechanical conditions within the slab, such as temperature and the availability of hydrous mineral phases.

Progress in our understanding of intermediate-depth earthquake generation has therefore focused on explaining the spatial pattern of seismicity within subduction zones, such as the structure of double-seismic zones [e.g. Wei et al., 2017; Florez and Prieto, 2019; Sippl et al., 2019], or the relationship between intermediate-depth earthquake focal mechanisms, seismicity rates, and the orientation and density of outer-rise normal faulting [e.g. Warren et al., 2007; Boneh et al., 2019]. Analysis of any temporal variations in the frequency of intermediate-depth seismicity can potentially provide complementary information to these studies. In particular, variations in the frequency of seismicity in response to known stress changes can provide insights into the population of faults that are close to failure, as well as the sensitivity of the failure mechanism to small stress perturbations, and how these
vary between different pressure-temperature conditions and slab environments [e.g. Tibi et al., 2003; Persh and Houston, 2004; Zhan and Shearer, 2015; Bouchon et al., 2016, 2018; Luo and Wiens, 2020].

Two observations have emerged that suggest different sensitivities of intraslab faults systems to changes in static stress. First, studies have reported changes in the frequency of intraslab intermediate-depth earthquakes related to the occurrence of shallow earthquakes, including: (1) year-long changes in earthquake frequency that begin after large, shallow earthquakes on the adjacent subduction megathrust [Lay et al., 1989; Bouchon et al., 2016; Jara et al., 2017; Mitsui et al., 2021], and (2) month-long transient changes in intraslab earthquake frequency following slip on the megathrust [Delbridge et al., 2017]. These observations suggest that intraslab faults in some settings are relatively sensitive to the small (<1 MPa) stress changes that shallow earthquakes impose on the slab through static stress transfer, and that faults within the subduction system are interacting with one another over distances of tens to hundreds of kilometres. In contrast, intermediate-depth earthquakes are consistently followed by far fewer aftershocks compared to shallow crustal earthquakes of equivalent magnitude (low ‘aftershock productivity’) [Frohlich, 1987; Wiens and Gilbert, 1996; Persh and Houston, 2004; Ye et al., 2020]. As the stress drops in intermediate-depth earthquakes are similar to shallow earthquakes (~1–50 MPa) [Allmann and Shearer, 2009; Poli and Prieto, 2016; Tian et al., 2022], the difference in aftershock productivity between shallow and intermediate-depth mainshocks is not related to the amplitude of the stress changes. Rather, the low productivity of intermediate-depth aftershock sequences indicates that the faults within the slab are relatively insensitive to the stress changes caused by nearby large earthquakes within the slab, and that they only weakly interact with one another. These two inferences relating to intraslab seismicity appear to be in contradiction. This study aims to reconcile them by re-examining the evidence for temporal changes in the frequency of intermediate-depth seismicity around the timing of large earthquakes using the most up-to-date global and regional earthquake catalogues.

Section 2 focuses on the aftershock sequences of large intermediate-depth earthquakes, verifying previous results regarding their low aftershock productivity and testing whether aftershock productivity varies systematically with source or slab setting. Section 3 then explores the response of intermediate-depth seismicity to slip in megathrust earthquakes. We find that, although there are temporal variations in the frequency of intermediate-depth seismicity, they do not consistently correlate with the timing of stress changes caused by large megathrust earthquakes. In Section 4, we discuss the implications of our findings for the mechanics of faulting at intermediate depths within slabs.
2 Aftershock Productivity of Intermediate-Depth Earthquakes

Aftershocks are the most obvious manifestation of changes in seismicity rates, and reflect the rupture of faults in response to changes in the local stress state following a larger earthquake [King et al., 1994; Lin and Stein, 2004]. Analyses of aftershock sequences following intermediate-depth earthquakes show that they are typically less productive compared to shallow earthquakes of equivalent magnitude [Frohlich, 1987; Wiens and Gilbert, 1996; Dascher-Cousineau et al., 2020; Ye et al., 2020]. Aftershock productivity is also known to be depth-dependent, with most large earthquakes between 300–500 km often having no aftershocks at all with $m_b \geq 4.5$ [Persh and Houston, 2004]. Early studies suggested that the aftershock productivity correlates with a slab’s thermal structure [Wiens and Gilbert, 1996], though more recent work using longer-duration catalogues with lower magnitudes of completeness has argued that aftershock productivity is independent of slab temperature, but may be related to the heterogeneity of the stress field and fault network surrounding the mainshock [Ye et al., 2020] or the availability of highly pressurised free fluid in the slab [Cabrera et al., 2021; Chu and Beroza, 2022].

Below, we re-examine aftershock productivity at both global and regional scales using modern earthquake catalogues, focusing particularly on seismicity within the depth range 60–300 km. In this depth range, earthquakes are mostly within subducted oceanic lithosphere. Through this updated analysis, we aim to characterise the relative sensitivity of fault systems to earthquake stress changes in different slab environments by first focusing on global patterns in aftershock productivity and then zooming in to region-scale patterns.

2.1 Global Analysis

2.1.1 Method of Measuring Aftershock Productivity

We first studied the aftershock sequences of all $M_w > 6.5$ earthquakes using a simple clustering algorithm applied to the ISC’s reviewed global catalogue following the methods of Baiesi and Paczuski [2004] and Zaliapin and Ben-Zion [2013]. We use this non-parametric clustering method, as it does not assume any particular form for the temporal evolution of aftershock frequency [e.g. Dascher-Cousineau et al., 2020; Chu and Beroza, 2022]. The ISC’s reviewed earthquake catalogue is derived from a location procedure that uses the body-wave phase arrivals from teleseismic and regional stations to provide the most accurate estimates of earthquake hypocentral parameters and consistent body-wave magnitude estimates globally [Bondár and Storchak, 2011; Di Giacomo and Storchak, 2016]. We complement
these data with moment tensor information for each mainshock derived using long-period body and surface wave inversion from the global Centroid Moment Tensor (gCMT) catalogue [Dziewonski et al., 1981; Ekström et al., 2012], which limits the time-span of our analysis to mainshocks between 1976 and 2020. We choose to represent the size of the mainshocks using the moment magnitude $M_w$ derived by the gCMT, and not body-wave magnitude $m_b$, because the body-wave magnitude scale saturates for the largest mainshocks included in our analysis at $m_b \gtrsim 7.5$.

For each mainshock, we began by taking a subset of events from the ISC catalogue that are within 500 km of the mainshock hypocentre and which have $m_b \geq 4.5$. For all events within this subset, we then calculated the space-time distance $\eta_{ij}$ between each event hypocentre $i$ and every other event hypocentre $j$ [Zaliapin et al., 2008]. The space-time distance is defined as $\eta_{ij} = t_{ij}(r_{ij})^d10^{-bm_i}$, where $t_{ij} = t_j - t_i$ is the time difference between event origin times, $r_{ij}$ is the 3-dimensional cartesian distance between the event hypocentres, $m_i$ is the magnitude of event $i$, and $d = 1.6$ and $b = 1$ are constants [Zaliapin and Ben-Zion, 2013]. If $t_{ij} \leq 0$ then we set $\eta_{ij} = \infty$ to enforce causality (i.e. event $j$ must have occurred after event $i$ for it to be an aftershock). The choice of $m_b \geq 4.5$ is designed to capture a global average for the magnitude of completeness for intermediate-depth seismicity [Ye et al., 2020]. Although changing this value to $m_b \geq 5.0$ has an effect on the absolute count of aftershocks, it has little affect on the trends in relative aftershock productivity (Supplementary Text S1).

For every event $j$ in the catalogue we define its parent as the event $i$ for which $\eta_j = \min(\eta_{ij})$. At this stage we check that the mainshock is not an aftershock of an even larger earthquake by ensuring that, for the event to be considered a mainshock, it has no parent events that have a larger magnitude. The resulting distribution of $\log_{10}(\eta_j)$ forms two peaks (Supplementary Figure 1a), with events with low $\log_{10}(\eta_j)$ being clustered events and those with high $\log_{10}(\eta_j)$ being independent events [Zaliapin and Ben-Zion, 2013]. To determine the cut-off between the two, we fit a two-component Gaussian mixture model to the distribution and determined the overlap between the two curves $\eta_0$ (Supplementary Figure 1b). We then recursively counted all of the offspring of the mainshock that have $\eta_j \leq \eta_0$ to yield the final aftershock count. The seismicity that is not clustered, which consists of all events for which $\eta_j > \eta_0$, is used to calculate the background seismicity rate within $\pm 50$ km horizontal distance and $\pm 30$ km depth around each mainshock (Supplementary Figure 2).

The analysis described above yields aftershock counts for 2432 mainshocks. For the remaining 1586 events with $M_w \geq 6.5$ in the gCMT catalogue, we were either not able to separate the background from the clustered seismicity, or the earthquake was itself an aftershock. Although the absolute aftershock count is weakly dependent on the constants used in the space-time distance calculation ($b$, $d$, and $\eta_0$),
the relative count between mainshocks is insensitive to the parameter selection (Supplementary Text S1). Below we only interpret changes in relative aftershock productivity.

2.1.2 Results of Aftershock Productivity Analysis

Figure 1 shows the number of aftershocks for each mainshock plotted against a set of possible dependent variables. The two clear trends within the data are that the aftershock productivity changes as a function of mainshock depth and mainshock magnitude (Figure 1a,b) [Frohlich, 1987; Persh and Houston, 2004; Ye et al., 2020]. In terms of mainshock depth, we find that there is a sharp decrease in aftershock productivity as mainshocks exceed 50–60 km depth (Figure 1a), which roughly corresponds to the transition from shallow crustal and intraplate seismicity to intraslab seismicity. Below 60 km depth, the median aftershock productivity continues to decrease with depth until 300 km, then remains consistently low for mainshocks between 300 km and 500 km depth, before increasing again between 500 km and 700 km depth, mirroring the distribution of mainshocks (Figure 1a).

Aftershock productivity also increases with mainshock magnitude (Figure 1b). For earthquakes within both the shallow (<60 km) and intermediate-depth range (60–300 km), the median aftershock productivity scaling with mainshock magnitude $M$ can be fit by an equation of the form $a10^{\gamma(M-M_c)}$ where $\gamma \approx 1$ and $M_c$ is the magnitude of completeness [Frohlich, 1987] (Supplementary Figure 5). The median aftershock productivity for the intermediate depth earthquakes consistently falls below that for shallow earthquakes across the mainshock magnitude range (Figure 1b), indicating that intermediate-depth earthquakes have, at least on average, fewer aftershocks for a given magnitude mainshock. However, there is still significant scatter in aftershock productivity around the median for intermediate-depth earthquakes. The scatter indicates there is some other control on the measured aftershock productivity beyond just mainshock depth and magnitude.

One possibility is that the scatter is related to our method of aftershock counting. We found no correlation between the aftershock productivity and the date of the mainshock, suggesting temporal changes in the ISC catalogue’s completeness are not contributing to the scatter (Figure 1c). In addition, the aftershock productivity does not correlate with the gradient in down-dip slab curvature or background seismicity rate (Figure 1d,e), which implies that aliasing high rates of background seismicity into aftershock productivity is also not contributing to the scatter.

Alternatively, the scatter in aftershock productivity may relate to an unidentified mechanism associated with the mainshock source or setting, such as the mechanical properties of the slab [Wiens and
Gilbert, 1996] or stress heterogeneity and variability in fault geometries within the slab [Ye et al., 2020]. For almost every mainshock the aftershocks of large intermediate-depth earthquakes are too small to have mechanisms in the gCMT catalogue, limiting our ability to test whether aftershock productivity is related to the geometry of the receiver faults. However, if aftershock productivity were related to the slab setting, then it should vary systematically between subduction zones.

After removing the scaling between the median aftershock productivity and mainshock magnitude, we did not find any systematic spatial variability in aftershock productivity at the scale of individual subduction zones (Supplementary Text S2). However, this analysis is limited by there being too few $M_w \geq 7.5$ events to identify any spatially robust trends, and earthquakes in the magnitude range $6.5 \leq M_w < 7.5$ have too few aftershocks (generally <5; see Figure 1b) of $m_b \geq 4.5$ to record spatial variability in the aftershock productivity using global catalogues (Supplementary Text S2).

Earthquakes on transform faults produce the fewest aftershocks of any shallow fault zones [Boettcher and Jordan, 2004; Dascher-Cousineau et al., 2020]. Therefore, we also examined whether aftershock productivity is controlled by the geometry of pre-existing faults present in subducted oceanic lithosphere, particularly whether intermediate-depth earthquakes may be reactivating outer-rise faults or fracture zones. As outer-rise faults form parallel to the trench and perpendicular to the slab dip direction, we first tested whether aftershock productivity depends on whether the mainshock accommodates down-dip or along-strike deformation of the slab based on the mainshock’s $P$ and $T$ axes. We found that, irrespective of whether the mainshock accommodates down-dip or along-strike deformation, the two populations of intermediate-depth events have similar aftershock productivity statistics (Figure 1f). Identifying where intermediate-depth earthquakes may be reactivating fracture zones is more difficult, because of the ambiguity in which nodal plane is the rupture plane. However, we note that areas where the fracture zones are almost perpendicular to the trench, such as in South America, the intermediate-depth earthquakes accommodate down-dip extension of the slab and are not reactivating fracture zones, but still have low aftershock productivity for their magnitude (Supplementary Text S2).

Therefore, features unique to a particular slab, at least at the scale of hundreds of kilometres resolvable with global catalogue data, seem unable to explain the scatter in aftershock productivity between events of similar magnitude. In the next section, we test whether higher-resolution regional earthquake catalogues with lower magnitudes of completeness can provide insights into the controls on intermediate-depth aftershock productivity not resolvable using the global seismic catalogue.
2.2 Regional Analysis: Northern Chile

High-resolution regional earthquake catalogues can provide better constraints on the spatial variability in aftershock productivity and its relationships with the mainshock setting [Sippl et al., 2019; Gomberg and Bodin, 2021; Chu and Beroza, 2022]. We re-assessed the aftershock productivity of moderate-magnitude earthquakes in northern Chile, because this region has: (1) an earthquake catalogue that contains over 100,000 earthquakes of $M_L \geq 2.0$ from 2006–2015 [Sippl et al., 2018], (2) a highly seismogenic slab at intermediate depths, and (3) relatively consistent earthquake mechanisms and magnitudes that allows for comparison between events with a similar source.

We applied the same aftershock identification algorithm to the catalogue of Sippl et al. [2018] for all earthquakes with $M_w \geq 5.3$ that have moment tensors in the gCMT catalogue and include all events above the completeness $M_L \geq 2.8$ as possible aftershocks (Figure 2). This analysis leads to aftershock counts for 22 shallow mainshocks (<60 km depth) and 92 intermediate-depth mainshocks (60–300 km depth). There is not enough diversity amongst the magnitudes of these large mainshocks to robustly calculate a scaling between mainshock magnitude and aftershock productivity, which limits our ability to compare the relative aftershock productivity of shallow and intermediate-depth mainshocks using this data set. Therefore, we focus our analysis on the relative aftershock productivity amongst the population of intermediate-depth earthquakes that have similar magnitudes.

The majority of the large intermediate-depth earthquakes beneath northern Chile occur in a cluster in the depth range of 80–140 km and 200–300 km from the trench (Figure 2b). Within this cluster, the 12 largest $M_w > 6$ earthquakes have near-identical magnitudes, focal mechanisms, hypocentral depths, and are in similar parts of the slab, but can still have significant differences in the number of aftershocks they produce (Figure 2b, see inset). There is no clear change in the number of aftershocks with depth for events within the intermediate-depth cluster Figure 2c. Cabrera et al. [2021] suggested that the aftershock productivity may decrease systematically as a function of distance below the slab surface using six well-located mainshocks, though we did not find this pattern when considering our data set of 114 mainshocks (Figure 2d). The spatial heterogeneity in aftershock productivity even in this small study area suggest that the controls on aftershock productivity may vary on length-scales that are small compared to the location differences between mainshocks, which is equivalent to a few tens of kilometers.

Similar analyses of high-resolution regional earthquake catalogues have been performed for intermediate-depth earthquakes in Cascadia [Gomberg and Bodin, 2021] and Japan [Chu and Beroza,
Wimpenny et al., 2022]. The analysis from Cascadia included 63 mainshocks and used a catalogue complete down to $M_L = 1.9$. Gomberg and Bodin [2021] found that the aftershock productivity increased with mainshock magnitude and decreased with mainshock depth. A notable difference between Cascadia and northern Chile is that the background seismicity rate correlates weakly with the aftershock productivity in Cascadia, whilst we did not find this trend in either our global analysis or for northern Chile (Supplementary Text S3). The analysis of aftershock productivity in Japan included 64 mainshocks and used the JMA catalogue, which is complete to $M_{JMA} = 2.0$. Chu and Beroza [2022] found that the aftershock productivity of intermediate-depth earthquakes was consistently lower than shallow earthquakes of equivalent magnitude, and that aftershock productivity increased with magnitude. However, there was not enough variability amongst the intermediate-depth events to determine whether aftershock productivity varied with depth. Chu and Beroza [2022] found that around half of all events have no recorded aftershocks, whilst for those that do have aftershock sequences the aftershock productivity scales with the $V_p/V_s$ ratio in the region. In northern Chile, we find more of a continuum of aftershock productivity, but our results support the view of Chu and Beroza [2022] that some mechanism in addition to just the depth and magnitude of the mainshock is influencing the variability in aftershock productivity.

2.3 Summary of Aftershock Productivity Results

We find that the low aftershock productivity of intermediate-depth earthquakes compared to shallow earthquakes of equivalent magnitude is a robust result between both global and regional earthquake catalogues. For intermediate-depth earthquakes, the aftershock productivity increases systematically with mainshock magnitude as $\approx 10^{M_w}$, and we have shown tentative evidence that it decreases slightly as a function of depth. We interpret the increase in aftershock productivity with magnitude to reflect the fact that larger mainshocks having larger rupture areas $A$ with $A \propto 10^{M_w}$ causing stress changes on a larger fault area, or in a larger volume, surrounding the mainshock rupture [Wetzler et al., 2016]. Assuming that the number of faults within the slab remains constant with depth, the slight decrease in aftershock productivity with depth for earthquakes between 60 km and 300 km implies that the mechanism that controls aftershock productivity is also itself depth dependent. However, an important conclusion is that there is still variability in the aftershock productivity of intermediate-depth earthquakes that cannot be explained by the magnitude of the mainshock and mainshock depth alone.

We did not find any robust evidence for systematic variations in aftershock productivity between dif-
ferent slab settings. For example, the aftershock productivity does not vary systematically with the background rate of seismicity within the slab. Rather, aftershock productivity seems to be heterogeneous at the scale of individual subduction zones and within individual slabs. The variability in aftershock productivity within the cluster of near-identical intermediate-depth earthquakes beneath northern Chile is the type example of this behaviour, and which leads us to suggest that the mechanism that controls aftershock productivity may also be heterogeneous over length-scales of only a few tens of kilometres.

The low aftershock productivity of intermediate-depth earthquakes compared to shallow earthquakes of equivalent magnitude suggests fault systems within the slab are less sensitive to stress transfer than those within the shallow parts of the lithosphere. In the next section, we explore whether intraslab faults are also insensitive to slip on the subduction interface in major megathrust earthquakes.

3 Response of Intermediate-Depth Seismicity to Megathrust Slip

Intraslab faults will experience stress changes in response to slip on the megathrust [Lin and Stein, 2004]. These stress changes have been suggested to modulate the frequency of earthquakes that accommodate down-dip extension or compression within the slab [Astiz et al., 1988; Dmowska et al., 1988; Lay et al., 1989]. In particular, Astiz et al. [1988] argued that down-dip compressional earthquakes at intermediate depths are more frequent after megathrust earthquakes, and down-dip extensional earthquakes less frequent, as megathrust slip may cause incremental down-dip compression of the slab.

3.1 Stress Changes in Slabs Caused by Megathrust Slip

The stress changes caused by slip on a megathrust will vary throughout the slab, and may therefore modulate where earthquakes are triggered. Therefore, to test the conceptual model of Astiz et al. [1988] and inform our data processing strategy, we first performed a set of calculations to examine the stress changes caused by slip on the megathrust in different slab settings. We calculated the stress changes in two dimensions using the elastic dislocation model of Okada [1992] and a synthetic slip distribution on the slab surface defined by Slab 2.0 [Hayes et al., 2018]. The two-dimensional approximation is reasonable given that, for $M_w > 8$ megathrust earthquakes, the rupture area is typically longer along-strike than it is wide down-dip [Allen and Hayes, 2017]. In our models, slip on the slab surface
extended from the up-dip edge of Slab 2.0 to 50 km depth, and had a trapezoidal distribution with
slip tapering over a down-dip distance of 50 km towards the edge of the slip patch. Synthetic tests
showed that applying more complex slip distributions derived from finite-fault slip inversions had little
effect on either the amplitude or the geometry of the stress changes at distances >20 km from the
megathrust, as long as the average amount and depth-extent of slip on the megathrust is accurate
(Supplementary Text S4). The results of these calculations for three different slab geometries (Japan,
Kermadec and northern Chile) are shown in Figure 3.

To first-order, slip on the megathrust adds a predominantly horizontal tensional stress within the
outer-rise region, and adds a predominantly down-dip compressional stress in the area of slab down-
dip of megathrust slip. The orientation of the principal stress axes rotate from being sub-parallel to
the megathrust within the shallow parts of the slab to being oblique to the slab near its base. However,
irrespective of the geometry of the slab, slip on the megathrust will lead to down-dip compression in
the epicentral region of intermediate-depth earthquake generation (Figure 3).

The amplitude of the stress changes increases linearly with the average slip on the megathrust. Larger
magnitude earthquakes will cause stress increases of a particular amplitude within a larger volume of
the slab, and therefore potentially lead to a stronger signal of triggered seismicity. More generally, the
largest stress changes occur at the tips of the slip area, which corresponds to the trench and, at its
down-dip end, the brittle-ductile transition on the megathrust. Stress changes decrease with distance
as approximately $r^{-3}$ with distance from the megathrust [Okada, 1992], and the amplitude of the
stress changes within the slab interior at intermediate depths are similar to those within the outer-
rise, where there is often extensive triggered seismicity after megathrust earthquakes [Christensen and
Ruff, 1983; Bilek and Lay, 2018].

Overall, these physical models of stress change due to megathrust slip support the conceptual model
of Astiz et al. [1988]. In the next section, we therefore extend the original analyses of changes in
intermediate-depth seismicity around the timing of major megathrust earthquakes from Astiz et al.
[1988] and Lay et al. [1989] using the more temporally complete gCMT catalogue [Dziewonski et al.,
1981; Ekström et al., 2012].

3.2 Global Analysis

We focus our analysis on the largest megathrust earthquakes of $M_w \geq 8.0$ between 1990 and 2017,
which provides us with a set of events that are likely to be on kinematically coupled sections of the
megathrust and that were late in their earthquake cycle. Based on our modelling in Section 3.1, these large earthquakes are also the ones most likely to have led to changes in seismicity rates within the slab. For each large megathrust earthquake, we extracted all of the earthquakes surrounding the mainshock from the gCMT catalogue with centroid depths in the range 60–300 km and that are within ±200 km of the projection of the megathrust earthquake’s T-axis in the down-dip direction of the slab. We then removed all earthquakes with centroids that are above the slab surface defined by Slab 2.0 [Hayes et al., 2018]. We also repeated the analysis but without excluding events based on their position relative to the slab, given that both the slab surface and the earthquake centroid depths can be uncertain by ±10 km or more, but found this had only a minor effect on the resulting patterns.

To assign each earthquake to either down-dip compression or extension, we filtered the events based on the angle between their P, T, and N-axes and the normal and dip vector of the slab derived from Slab 2.0. Earthquakes are associated with down-dip compression if the T-axis is within 45° of the slab normal, the N-axis makes an angle greater than 45° with the slab normal, and the N-axis makes an angle greater than 45° with the slab dip vector. The same filter was used to isolate down-dip extensional earthquakes, but with the constraint that the P-axis is within 45° of the slab normal vector. Earthquakes that do not fit these two conditions (denoted ‘other’ in the analysis below) mostly accommodate along-strike deformation of the slab or shearing of the slab in the plane parallel to the slab dip direction (slab tearing). We also assess the temporal variability in these events to ensure that the method of data selection does not bias the results.

To examine changes in the frequency of intermediate-depth earthquakes associated with megathrust slip, we calculated the difference in the number of earthquakes before \( N_b \) and after \( N_a \) the mainshock at time \( t_0 \). We then divide this by the total number of earthquakes in the period \( [t_0 - \Delta t, t_0 + \Delta t] \), yielding a value \( \Delta N/N = (N_a - N_b)/(N_a + N_b) \) that is in the range \([-1, 1]\). A value of 1 means all earthquakes of a particular mechanism occurred after the mainshock, whilst −1 means they all occurred before the mainshock. We calculated \( \Delta N/N \) for all earthquakes with magnitude \( M \geq M_c \) where \( M_c \) is in the range \([5.0, 6.0]\) and for \( \Delta t \) of 5 years or 10 years. This simple approach captures the rate changes without relying on any assumptions about the statistical distribution of seismicity in time, as a more complex approach is not warranted by the limited number of earthquakes.

The analyses of three different earthquakes illustrate the key results (Figure 4). For the 2011 \( M_w \) 9.1 Tohoku-oki earthquake, the largest event in the gCMT catalogue, there are only 12 down-dip extensional and 21 down-dip compressional earthquakes at intermediate depths within 20 years of the mainshock (Figure 4a). All of the down-dip extensional earthquakes with \( M_w \geq 5.5 \) occurred
prior to the mainshock, and there were no down-dip extensional earthquakes in the 10 years following the mainshock. Evidence for changes in the frequency of down-dip compressional earthquakes is less clear, as there are too few events (Figure 4a). Therefore, the extensional seismicity down-dip of the Tohoku-oki mainshock appears to follow the trend predicted by the model of Astiz et al. [1988]. The slab down-dip of the 2001 $M_w$ 8.1 Arequipa earthquake is far more seismogenic compared to Japan, with predominantly down-dip extensional seismicity as the slab bends into the mantle beneath the Andes (Figure 4b). The number of down-dip extensional earthquakes systematically increased following slip on the megathrust in the Arequipa earthquake, which is opposite to the trend expected if megathrust slip puts the slab into incremental down-dip compression and inhibits down-dip extensional earthquakes. The intermediate-depth seismicity down-dip of the 2006 $M_w$ 8.2 Kermadec earthquake shows a different result again. In this region, the majority of the intermediate-depth earthquakes are associated with down-dip compression. We find no robust change in the frequency of down-dip extensional earthquakes caused by megathrust slip. However, the data suggests that the number of down-dip compressional earthquakes with $M_w \geq 5.5$ decreased after megathrust slip, which is again contrary to the prediction that megathrust earthquakes promote down-dip compressional seismicity.

The three examples in Figure 4 demonstrate that changes in the frequency of earthquakes associated with down-dip extension or compression can occur around megathrust earthquakes, but they are not necessarily consistent between events. To further demonstrate this point, we performed the following test. For every mainshock $j$, we assign a decrease in rate $\Delta N/N < 0$ a value of $n_j = -1$ and an increase in rate $\Delta N/N > 0$ a value of $n_j = 1$ for a given time-span $\Delta t$ relative to the mainshock and magnitude cut-off $M_c$. We then compute $\sum_{j=1}^{k} n_j(M_c, \Delta t)$ for all megathrust mainshocks $j = \{1, 2...k\}$. If there is a consistent pattern of rate increases after the mainshock, then $\sum_{j=1}^{k} n_j(M_c, \Delta t) > 0$, whilst a rate decrease would be associated with $\sum_{j=1}^{k} n_j(M_c, \Delta t) < 0$. This process is equivalent to a 1-dimensional simple random walk. In the case of the null hypothesis that an increase in seismicity is equally likely as a decrease, the expected value of $\sum_{j=1}^{k} n_j(M_c, \Delta t)$ is 0 and the standard deviation is $\sqrt{k}$. The results of this stacking process are shown in Figure 5.

For down-dip extensional seismicity the sum $\sum_{j=1}^{k} n_j(M_c, \Delta t)$ is similar to the expected value for the null hypothesis (Figure 5a), suggesting there is no consistent change in down-dip extension of the slab after megathrust earthquakes. Down-dip compressional seismicity does typically increase after megathrust earthquakes, but only for intermediate-depth earthquakes with $M_w \leq 5.5$ (Figure 5b), which is around the magnitude of completeness of the gCMT catalogue [Kagan, 2003]. The smallest $M_w$, 5 earthquakes are also likely to have the largest depth and mechanism uncertainties.
and so thrust-faulting on the megathrust may also be incorrectly assigned to being within the slab. The amplitude of the deviation from the expected value for the null hypothesis for earthquakes $M_w > 5.5$ is smaller than 2 standard deviations, therefore we cannot reject the hypothesis that these changes in earthquake frequency are random when only considering events above the magnitude of completeness. Given that down-dip extension, compression, and other types of earthquake mechanisms at intermediate-depths generally increase in frequency in the 5–10 years after a mainshock (Figure 5a-c), and the increase becomes more robust for longer time-spans $\Delta t$, then these trends most likely reflect the increase in the gCMT catalogue completeness through time.

In summary, we find no robust evidence in the gCMT catalogue for systematic changes in the frequency of moderate-to-large magnitude earthquakes that accommodate down-dip deformation of the slab in the intermediate-depth range. In the next two sections, we test whether the apparent lack of triggered intraslab seismicity might reflect the limited number of earthquakes within the gCMT catalogue by focusing on two regions with extensive intraslab seismicity and high-quality regional catalogues.

### 3.3 Regional Analysis: Japan

Japan has the highest-resolution earthquake catalogue of any subduction zone due to the dense onshore seismic network, and is therefore an ideal natural laboratory for this type of analysis. Delbridge et al. [2017] previously reported an increase in intermediate-depth seismicity down-dip of the rupture area of the 2011 Tohoku-oki earthquake in the upper plane of the double-seismic zone (DSZ) recorded by the regional earthquake catalogue, which consists mostly of compressional earthquakes accommodating unbending of the Pacific plate. Our analysis of the earthquake moment tensors from the gCMT catalogue failed to identify such a trend (Figure 4a). We therefore re-analysed the frequency variations of intermediate-depth earthquakes recorded in the JMA catalogue down-dip of the Tohoku-oki rupture area (Figure 6a,b). A total of 6595 intermediate-depth earthquakes occurred in this region between 2006 and 2019 that are $>100$ km from the trench and $>60$ km deep, and which are larger than the magnitude of completeness of the catalogue ($M_{JMA} = 2.0$). We assigned events to the upper or lower plane of the DSZ by binning the event depths relative to Slab 2.0 as a function of distance from the trench and fitting a Gaussian mixture model to the relative depth distributions.

To examine changes in the earthquake frequency, we calculated the average earthquake rate in the upper and lower plane of the DSZ using a moving window that has width $T$ and moves in steps $\Delta t$. The results shown in Figure 6b-d use $T = 0.2$ years and $\Delta t = 0.05$ years. From this moving
window analysis, we confirm there is a spike in the frequency of earthquakes assigned to the upper plane within a month of the Tohoku-oki mainshock, with the rate increasing from ~0.5 earthquakes per day to nearly 6 per day (Figure 6c). There is no clear change in the frequency of lower-plane earthquakes over the same period. The peak seismicity rate in the upper plane occurred 1 month after the mainshock and decayed over 7 years before returning to the background rate in 2018. However, this result is extremely sensitive to the cut-off depth (Figure 6d). For an identical analysis of earthquakes that have depths >70 km, the spike in earthquake frequency disappears and there is no clear deviation from the pre-Tohoku seismicity (Figure 6e).

The large number of earthquakes in the JMA catalogue, and the relatively stable rate of seismicity prior to Tohoku, allows us to test the statistical significance of the seismicity rate changes using the $\beta$-statistic of Matthews and Reasenberg [1988]. The $\beta$-statistic is calculated as $\beta = (N - N_0)/\sigma_0$ where $N$ is the observed number of earthquakes within a sliding window of length $T$, and $N_0$ and $\sigma_0$ are the mean and standard deviation of the number of earthquakes within time windows of length $T$ selected randomly from within the reference time period (in our case 2006–2011). The results of the $\beta$-statistic analysis applied to the JMA data shows that there are no variations in the earthquake frequency for events >70 km that are greater than 2 standard deviations from the pre-Tohoku seismicity (Figure 6f). An analysis of the seismicity in the ISC reviewed catalogue from the same region, which support our observations made using the JMA catalogue, is discussed in Supplementary Text S5.

Further investigation revealed that the seismicity contributing to the spike in earthquake frequency in the upper plane in Figure 6c mostly derived from the region of the 7th April 2011 $M_w$ 7.2 Miyagi-oki reverse-faulting earthquake, which ruptured the slab at ~55–65 km depth less than a month after the Tohoku-oki mainshock. Removing the seismicity within 50 km of the Miyagi-oki earthquake suppresses the spike in the intermediate-depth seismicity rate (Supplementary Text S5). It is also possible that the ~5–10 km uncertainties in earthquake hypocentral depths for small earthquakes in the JMA catalogue mean that some aftershocks occurring at the down-dip edge of the megathrust, or within the overriding plate, are mislocated and have been incorrectly assigned to the upper plane of the DSZ [e.g. Sippl et al., 2019]. To test this possibility, we removed all events that are within 10 km of the plate interface from the analysis, which also suppresses the spike in seismicity rate related to the Tohoku-oki and Miyagi-oki earthquakes (Supplementary Text S5). Therefore, we conclude that the change in earthquake frequency identified by Delbridge et al. [2017] may not indicate a slab-wide increase in intermediate-depth earthquake frequency in response to the 2011 Tohoku-oki earthquake, but rather the aftershock sequence of the Miyagi-oki earthquake (Figure 6b, inset). This difference
is important, because it suggests that the majority of faults that are definitively within the slab are insensitive to the stress changes caused by megathrust slip in the Tohoku-oki earthquake.

3.4 Regional Analysis: Northern Chile

Megathrust slip has also been proposed to modulate intermediate-depth seismicity in northern Chile. Jara et al. [2017] suggested that the 1995 Antofagasta and 2014 Iquique megathrust earthquakes were followed by periods of reduced moderate-magnitude seismicity at intermediate depths beneath northern Chile, whilst the 2005 Tarapaca intraslab earthquake was followed by nine years of increased seismicity at both shallow and intermediate depths (Figure 7a,b). Since Jara et al. [2017]'s original analysis, Sippl et al. [2018] has published an earthquake catalogue spanning 2006–2015 in northern Chile that is complete down to $M_L = 2.8$, which allows us to examine the changes in intermediate-depth earthquake frequency before and after the Iquique earthquake in more detail. We calculated the earthquake rate through time using the moving window analysis described in Section 3.3, but found no significant deviations in the frequency of intermediate-depth seismicity following the 2014 Iquique earthquake or the 2007 Tocopilla earthquake (Figure 7c,d).

The catalogue of Sippl et al. [2018] is too short to capture any of the multi-year trends in earthquake frequency identified by Jara et al. [2017]. Therefore, we re-analysed the temporal variations in seismicity in northern Chile between 1980 and 2020 using four more years of data in the ISC’s reviewed catalogue than were available to Jara et al. [2017] (Figure 7a). An important limitation in comparing temporal variations in the shallow and intermediate-depth seismicity in this region is that the ISC catalogue’s magnitude of completeness is higher for shallow earthquakes that are offshore ($m_b = 4.7$) than for intermediate-depth earthquakes that are beneath the land ($m_b = 4.3$; see Supplementary Text S6). To ensure that this spatial variability in completeness does not bias our analysis, we only studied events with $m_b \geq 4.7$, which for the region shown on Figure 7 includes 925 earthquakes between 1980 and 2020.

The annual variations in the frequency of shallow (<50 km) and intermediate-depth (70–170 km) earthquakes are shown as histograms in Figure 7e-f, and as a cumulative distribution in Figure 8a. We plot the data as histograms, as opposed to using the moving window analysis of Section 3.3, because there are so few earthquakes above the magnitude of completeness. The depth intervals were selected to closely replicate the analysis of Jara et al. [2017]. Unlike Jara et al. [2017], however, we describe the trends in the undeclustered catalogue, and present the equivalent analyses of the
declustered catalogue in Supplementary Text S6. We take this approach, because the deficiency of intermediate-depth aftershock sequences means that declustering has little effect on the trends in intermediate-depth earthquake frequency through time.

There is little shallow seismicity in northern Chile between 1980 and 2007 with typically fewer than 5 earthquakes per year with $m_b \geq 4.7$ (Figure 7e), which makes identifying any changes in earthquake frequency during this period difficult. There are so few events in 1980–2007 that the cumulative earthquake distribution with time is not significantly different (<2 standard deviations) from synthetic catalogues that contain the same number of events but with randomised times (Figure 8b), suggesting the shallow seismicity contains no robust information about temporal changes in earthquake frequency in response to the 1995 Antofagasta, 2001 Arequipa, or 2005 Tarapaca earthquakes. Between the 2007 Tocopilla and 2014 Iquique earthquakes the annual number of shallow earthquakes increased (Figure 7e), which is associated with the well-documented foreshock sequence of the Iquique earthquake [Ruiz et al., 2014]. The Iquique earthquake is then followed by an extensive aftershock sequence that lasts until the end of the catalogue in 2020 (Figures 7e and 8a).

At intermediate depths the seismicity is more frequent and variable through time (Figure 7f). Between 1980 and 1995 the annual earthquake frequency changes from year-to-year (Figure 7f), but does not deviate from the behaviour of time-randomised catalogues (Figure 8c). During 1980–1995, pulses of seismicity occurred in 1983, 1985, and 1990 that were not associated with a large megathrust or intermediate-depth earthquake (Figure 8c, black arrows). After 1995, there are two distinct changes in the earthquake frequency that last for multiple years: first a decrease around the timing of the 1995 Antofagasta earthquake and then an increase around the timing of the 2001 Arequipa earthquake (Figure 7f). This period of seismic quiescence at intermediate-depths between 1995 and 2001 appears to be robust in northern Chile for magnitudes at least 0.5 units larger than the catalogue completeness (Figure 7f). After 2001, we found no evidence for robust changes in the intermediate-depth earthquake frequency caused by the 1987 Antofagasta, 2007 Tocopilla, and 2014 Iquique earthquakes (Figure 8c,d).

Our observations support the view that temporal changes in intermediate-depth earthquake frequency in northern Chile did occur, and in some cases lasted for multiple years. However, they are not consistently associated with megathrust earthquakes or large intermediate-depth earthquakes. If there were a consistent physical reason for the frequency changes in response to megathrust slip, then it is unclear why they should occur for only two megathrust events out of six between 1980 and 2020. In addition, using the longer earthquake catalogue, we found that the 2014 Iquique megathrust earthquake had no resolvable effect on the frequency of intermediate-depth earthquakes within the
slab directly down-dip from the rupture area. Therefore, we argue that large megathrust earthquakes are not the cause of changes in earthquake frequency at intermediate depths beneath northern Chile.

4 Discussion

4.1 Stress Sensitivity of Intermediate-Depth Seismicity

We initially set out to reconcile two contrasting views of intermediate-depth seismicity: one that suggested intraslab fault systems are sensitive to small stress changes associated with megathrust earthquakes, and another that suggested intraslab fault systems are insensitive to the stress changes caused by large intraslab earthquakes. Our analyses support the view that intermediate-depth seismicity within subducting slabs is relatively insensitive to static stress transfer as a result of slip in large earthquakes with typical stress drops ($\sim$1–50 MPa; see Allmann and Shearer [2009]; Poli and Prieto [2016]; Tian et al. [2022]). This insensitivity is manifest as consistently low aftershock productivity of intermediate-depth earthquakes, and no consistent triggering of down-dip compressional seismicity, or inhibition of down-dip extensional seismicity, within slabs following megathrust slip. We also did not find any clear evidence that the sensitivity of intraslab faults to static stress transfer varies systematically between subduction zones with different slab conditions.

The lack of seismicity triggered by static stress transfer at intermediate depths is similar to lack of seismicity triggered by earthquakes on oceanic transform faults [Boettcher and Jordan, 2004], but in stark contrast to the extensive seismicity that is triggered within the outer rise and outer trench-slope region following many major megathrust earthquakes that slip to the trench [Christensen and Ruff, 1983; Bilek and Lay, 2018]. Earthquakes in the outer rises also have aftershock productivities similar to earthquakes of equivalent magnitude within the continents [Dascher-Cousineau et al., 2020]. This comparison between intermediate-depth and outer-rise seismicity is informative, because the earthquake sources are in similar host material, just at different confining pressures and temperatures. Therefore, the difference in sensitivity to stress change between outer-rise and intermediate-depth seismicity does not appear to related to the distinct composition of the oceanic lithosphere. Rather, it suggests that either: (a) the fault systems in the subducted oceanic lithosphere are not as close to failure as those at the outer rise, or (b) that the mechanism of earthquake generation at intermediate depth is not as sensitive to changes in static stress on the order of earthquake stress drops. This new view of the sensitivity of fault systems within subducted oceanic lithosphere places constraints on the
mechanics of earthquake generation at intermediate depths, and the interplay between the source of
stress and the mechanism allowing the release of stress in earthquakes on intraslab faults, which we
explore further below.

4.2 Fault Mechanics of Intermediate-Depth Seismicity

Based on the earthquake catalogue data, and recent work on the source properties of intermediate-
depth earthquakes, any model of intermediate-depth seismicity should account for three observations:

1. Intermediate-depth earthquake stress drops (for both mainshocks and aftershocks) should be of
a similar order of magnitude to those at shallow depth [Allmann and Shearer, 2009; Poli and
Prieto, 2016; Tian et al., 2022].

2. The response of intermediate-depth seismicity to stress changes caused by earthquake stress
drops must be limited, in order to explain the observations of low aftershock productivity and
the low sensitivity of intraslab seismicity to slip on the megathrust interface.

3. There must be some capacity to generate limited aftershocks after intermediate-depth earth-
quakes, and this capacity should broadly scale with mainshock depth and mainshock magnitude.

For shallow faulting, the clock-advance model has proven a simple way of interpreting the sensitivity
of fault systems to static stress transfer [King et al., 1994; Hainzl et al., 2010]. In this model after-
shocks reflect earthquakes on faults that would have eventually ruptured in response to slow stress
accumulation, but occurred earlier than expected due to an additional source of stress. A stress drop
of $\Delta \tau$ due to slip in an earthquake leads to stress transfer onto the surrounding faults of magnitude
$a_j \Delta \tau$, where $a_j$ denotes a vector containing the elastic constants, distance, and relative geometry of
the newly stressed fault [Hainzl et al., 2010]. If the faults surrounding the mainshock have a stress dis-
tribution $\tau_j$ and a yield stress $\tau_y$, then any fault patches around the mainshock where $\tau_j + a_j \Delta \tau > \tau_y$
will rupture in an aftershock (Figure 9a). In Figure 9a we assume that $\tau_j$ follows a distribution that
is symmetrical about the mean stress, and has a mean value set by the requirement for equilibrium.

We also assume that $\tau_y$ is roughly constant. Under these assumptions, fewer aftershocks would be
produced if the static stress transfer from the mainshock $a_j \Delta \tau$ is a smaller fraction of the failure
stress $\tau_y$, or if the shape of the fault stress population becomes more skewed towards lower stresses.

More aftershocks will be produced for larger magnitude earthquakes, because the volume of material
around the mainshock that experiences stress changes will be larger meaning the curve in Figure 9a will be taller.

A simple prediction of the clock-advance model is that for a given background seismicity rate $r$ and stressing rate $\dot{\tau}$, then a change in static stress $\Delta \tau$ should lead to a change in the number of earthquakes in a region proportional to $r \Delta \tau / \dot{\tau}$. Our analysis suggests that aftershock productivity for intermediate-depth earthquakes does not correlate with the background seismicity rate within the slab (see also Sippl et al. [2019]; Chu and Beroza [2022]). Similarly, the aftershock productivity does not correlate with the down-dip gradient in slab curvature, which is a proxy for the bending-related loading rate of faults within the slab [Sandiford et al., 2020]. In addition, areas where intermediate-depth seismicity is particularly common (e.g. northern Chile) are not more sensitive to earthquake stress changes than places where the slab has relatively few earthquakes (e.g. central Japan). We suggest these departures from predictions of the clock-advance model may indicate that the stresses sustained by the intraslab fault population are significantly below the failure stress, and changes in the failure stress through fault weakening mechanisms far exceed the stress transfer from earthquake stress drops. The modifications to the clock-advance model for the three main weakening mechanisms proposed to enable intermediate-depth seismicity (dehydration embrittlement, dehydration-assisted stress transfer, self-localising thermal runaway) are shown in Figure 9b-d. We discuss each mechanism, and its ability to account for the three features of intermediate-depth seismicity, in turn below.

### 4.2.1 Dehydration Embrittlement

Dehydration embrittlement involves the weakening of fault zones through the build up of highly-pressurised fluids released by the breakdown of hydrous mafic minerals during prograde metamorphism (Figure 9b). For this mechanism, the low stress drops in intermediate-depth earthquakes compared to the stresses required for frictional failure on a fault formed of dry olivine at equivalent depths ($\sim 1$ GPa at 100 km depth) may either reflect partial stress release, the low shear stresses needed to break faults with a low effective strength, or some combination of both of these.

To simplify the representation of dehydration embrittlement in Figure 9b, we consider two populations of faults within the slab: those that contain highly pressurised fluids, and those that do not. Faults containing pressurised fluid are breaking in earthquakes at a low failure stress (Figure 9b), whilst dry faults will be far from their failure stress because the finite size of the forces acting on the slab can only load them to a fraction of their failure stress. For the dry fault population, static stress transfer
is unlikely to trigger aftershocks, because most of the faults support stresses that are a small fraction of the failure stress (Figure 9b, black curve). In contrast, stress transfer could trigger slip on the fault population containing pressurised fluids, with the number of aftershocks being related to the number of faults that have been able to trap and build up high fluid pressures (Figure 9b, blue curve).

Pervasive dehydration embrittlement, in which most faults in the slab contain near-lithostatic pore fluids, seems unlikely, as this would cause the intraslab faults to be sensitive to stress transfer, and we would expect an aftershock productivity similar to that seen in the shallow crust or higher.

Recent work has highlighted the link between aftershock productivity in the subducted Pacific slab beneath Japan and the $V_p/V_s$ structure of the surrounding medium [Chu and Beroza, 2022], with higher aftershock productivity linked to higher $V_p/V_s$ ratios and by inference more fluid, which supports this model. The effects of dehydration embrittlement are expected to be spatially heterogeneous due to its dependence on the availability of hydrous minerals and the trapping of the released fluid in faults, then this mechanism has the capacity to account for the spatial variability in aftershock productivity within slabs. Dehydration embrittlement can therefore account for the observations outlined in Section 4.2.

4.2.2 Dehydration-Assisted Stress Transfer

An alternative mechanism is dehydration-assisted stress transfer, where the loss of load-bearing capacity of hydrous minerals within a mixed-composition aggregate leads to the support of the total force acting on a fault onto a fraction of its surface area, allowing the fault to locally reach its failure stress [Ferrand et al., 2017] (Figure 9c). Whilst the failure stress and stress drops at contact level for this mechanism need to be extremely high (500–1000 MPa), fault-averaged stress drops could be far lower if the fault can rupture through patches of weaker hydrous minerals at low shear stresses to account for the ~1–50 MPa seismologically-observed stress drops. Melting of the rupture plane at high stresses could also lead to a proportion of the stress release being accommodated aseismically as ductile shearing during the latter stages of slip, after an initial seismically-radiating phase. The resulting stress transfer onto the surrounding faults would be moderated by elastic parameters, the relative location and fault geometry, plus an additional factor describing the degree to which dehydration-assisted stress transfer concentrates stresses at the contact level ($b_j \Delta \tau$; Figure 9c).

As with dehydration embrittlement, the fault population will support average stresses that are significantly lower than the failure stress of faults containing dry olivine (Figure 9c, black curve). Following a mainshock the stress transfer onto the surrounding faults will be a small fraction of the total fault
strength, but will be boosted by the focusing of the stress onto small asperities described by the factor $b_j$. The controls on aftershock productivity will therefore be similar to the dehydration embrittlement mechanism described above, as it will depend on the degree to which the surrounding material had already dehydrated, and therefore the proportion of the fault population within the slab that can generate the locally high contact stresses needed for failure (Figure 9c, red curve). Zero or low aftershock productivity will occur where the majority of the weak, hydrous phases have broken down into stronger anhydrous phases, meaning that the factor $b_j$ is smaller. The relative insensitivity of intermediate-depth seismicity to slip on the subduction interface is a result of the stress transfer being a smaller fraction of the failure stress compared to shallow faulting (Figure 9c). Hence, dehydration stress-transfer can also match the three observational requirements described above.

### 4.2.3 Self-Localising Thermal Runaway

The final weakening mechanism is self-localising thermal runaway, in which creep in shear zones causes shear heating and the development of ductile instabilities that relax elastic strain [Ogawa, 1987; Hobbs and Ord, 1988]. Numerical models of self-localising thermal runaway suggest that the stress drops generated by an earthquake are a significant fraction of the fault’s failure stress (often $\sim$500–1000 MPa at $\sim$1 GPa confining pressure), as the positive feedback between strain and shear heating drives runaway failure that relaxes the majority of the elastic strain stored around the fault [Kelemen and Hirth, 2007; John et al., 2009]. Not all of the stress drop and strain release may be seismogenic, and therefore this mechanism might be consistent with the low seismologically-determined stress drops. However, the resulting stress transfer onto surrounding fault systems $a_j \Delta \tau$ should be a larger fraction of the failure stress than for the dehydration-based mechanisms described above (Figure 9d).

The self-localising thermal runaway weakening mechanism is mostly dependent on the stress state of the given shear zone, and does not require any additional chemical processes to weaken the fault. We would not expect to see sensitivity of intermediate-depth seismicity to the shallow, lower-stress drop megathrust earthquakes because the fault failure stress is much larger than the static stress transfer. However, we might expect aftershock productivity to be similar at intermediate-depths to shallow depths, because the ratio between the amplitude of the static stress transfer $a_j \Delta \tau$ and the fault failure stress $\tau_y$ will be similar to that at shallow depths (Figure 9d). Therefore, self-localising thermal runaway is less consistent with our observations of low intraslab aftershock productivity for intermediate-depth earthquakes.
5 Conclusions

Intermediate-depth earthquakes produce fewer aftershocks compared to shallow (<60 km) earthquakes of similar magnitude. The areas of intermediate-depth seismicity down-dip of major megathrust earthquakes are also insensitive to the static stress transfer on the order of earthquakes stress drops caused by megathrust slip. We interpret the relative insensitivity of intermediate-depth seismicity to static stress transfer to suggest that faults within the slab are further from their failure stress than is typical for shallow fault systems. It follows that the availability of the weakening mechanism is the likely control on intermediate-depth aftershock productivity, and this mechanism is heterogeneous over length-scales of a few tens of kilometres to account for the variability in aftershock productivity within slabs. We suggest dehydration-related weakening mechanisms are most consistent with these observations.

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Data Availability

All data used in this study are freely available. The ISC catalogue is available from https://doi.org/10.31905/D808B830, the gCMT catalogue is available from https://www.globalcmt.org/, the JMA catalogue is available from https://www.data.jma.go.jp/svd/eqev/data/bulletin/index_e.html, and the IPOC catalogue is available from doi.org/10.5880/GFZ.4.1.2018.001 (all last accessed December 2022). All of the codes needed to reproduce the aftershock productivity results and analysis of seismicity rates through time are available from https://doi.org/10.5281/zenodo.7817786.
References


Figures

Figure 1: Aftershock productivity for earthquakes in the gCMT catalogue with $M_w \geq 6.5$. (a) Aftershock productivity as a function of the mainshock depth. Intermediate-depth earthquakes (60–300 km) are shown in dark grey. The histogram of the logarithm of mainshock frequency with depth is shown above. (b) Aftershock productivity as a function of mainshock magnitude. Intermediate-depth earthquakes are shown in dark grey with black outline, whilst earthquakes with hypocentral depths <60 km are shown as light grey circles. The median aftershock productivity scaling is shown for shallow and intermediate-depth mainshocks. $R_s$ is the Spearman’s Correlation Coefficient. (c) Aftershock productivity as a function of mainshock date, (d) the gradient in the down-dip curvature of the slab at the centroid location computed from Slab 2.0 [Hayes et al., 2018], and (e) the background seismicity rate within 50 km horizontal distance and ±30 km depth difference from the mainshock hypocentre. (f) Histogram of aftershock productivity for mainshocks that accommodate either along-strike or down-dip deformation of the slab. The red histogram shows the productivity for shallow earthquakes with hypocentral depths <60 km.
Figure 2: Aftershock productivity of moderate-magnitude earthquakes in northern Chile using the IPOC catalogue of Sippl et al. [2018]. (a) Map of the spatial distribution of the seismicity overlain with the focal mechanisms of the mainshocks taken from the gCMT catalogue. The focal mechanisms are coloured by the number of counted aftershocks. Mainshocks that are $M_w$ 6.0–6.5 and at depths $\geq$70 km are highlighted by a black outline. Slab contours are from Slab 2.0 [Hayes et al., 2018]. (b) Cross-section through the IPOC seismicity overlain by the mainshocks shown as blue circles. Mainshocks are scaled by magnitude. (c) Aftershock productivity as a function of mainshock depth for mainshocks across all depths. (d) Aftershock productivity as a function of depth below the slab surface for mainshocks with hypocentral depths $>70$ km only.
Figure 3: Stress changes imposed on the slab due to slip on the megathrust in regions with different slab geometries, including (a) Japan, (b) Kermadec, and (c) northern Chile. The slip distribution in each calculation is limited to between the section of the slab surface highlighted in white, has a peak of 5 m, and linearly tapers towards the up-dip and down-dip edge of the slip patch over a distance of 50 km. $\sigma_{II}$ is the second invariant of the stress tensor, which represents the maximum shear stress imposed on faults within the slab. The principal stress axes show the geometry of the stress changes. Seismicity within 200 km of the slab profile is shown as circles scaled in size by the earthquake magnitude. The seismicity is taken from the global CMT catalogue [Ekström et al., 2012], and is defined as down-dip extensional, down-dip compressional or ‘other’ based on the criteria outlined in Section 3.2.
Figure 4: Examples of changes in intermediate-depth earthquake mechanisms before and after three major megathrust earthquakes. Mechanisms are coloured red if they are related to down-dip compression, blue for down-dip extension and grey for along-strike deformation. Contours represent the depth to the slab surface from Slab 2.0 [Hayes et al., 2018] and are every 20 km. The middle panel is a time-series of earthquake mechanisms as a function of magnitude. The dark grey horizontal line represents the global magnitude of completeness of the gCMT catalogue. The bottom panel shows the difference in the number of earthquakes after and before the megathrust event divided by the total number of earthquakes \( \Delta N/N = (N_a - N_b)/(N_a + N_b) \), for down-dip extensional and compressional events. The vertical grey line shows the range of completeness for the gCMT catalogue. Squares and triangles represent \( \Delta N/N \) for the period 5 years and 10 years either side of the mainshock, respectively. The size of the symbol is scaled by the number of earthquakes in that bin and decreases in size as the number of events in the bin gets smaller.
Figure 5: Compilation of changes in the frequency of intermediate-depth earthquakes following megathrust slip as a function of magnitude cut-off $M_c$ and time-span $\Delta t$ for (a) down-dip extensional, (b) down-dip compressional, and (c) other types of earthquakes. The colour in each panel represents the number of standard deviations from the mean distance that the summation reaches in $k$ steps, equivalent to $\sum_{j=1}^{k} \frac{n_j}{\sqrt{k}}$. Given the null hypothesis is that an increase and a decrease in earthquake frequency are both equally likely, the expected value of $\sum_{j=1}^{k} \frac{n_j}{\sqrt{k}}$ is zero. The vertical dashed lines represent the approximate range in magnitude of completeness of the gCMT catalogue. The solid black line marks the 2 standard deviations boundary, with ticks on the inside of the boundary enclosing regions where the changes in earthquake frequency are unlikely to arise due to chance.
Figure 6: Temporal variations in intermediate-depth seismicity in response to the 2011 $M_w$ 9.1 Tohoku-oki earthquake. (a) Spatial distribution of seismicity used in the analysis from the JMA catalogue. Contours of the slab surface are shown as black-dashed lines from Slab 2.0 [Hayes et al., 2018]. (b) Cross-section through the seismicity with the two depth cut-offs used in the analysis at 60 km and 70 km shown as black dashed lines. Inset is a zoom-in of the seismicity within ±1 month of the 7th April 2011 Miyagi-oki earthquake. The aftershocks of the Miyagi-oki earthquake clearly extend 10–15 km below the slab surface, but remain shallower than 70 km depth. (c) Average number of earthquakes per day in the upper plane (light red) and lower plane (light blue) of the double-seismic zone (DSZ) for all events >60 km depth. The time-series is calculated using a sliding window of length 0.2 years and time step 0.05 years. The vertical black line marks the timing of the Tohoku-oki mainshock. (d) Equivalent plot to (c), but for all events >70 km. (e) and (f) show the $\beta$-statistic of Matthews and Reasenberg [1988] for all events >60 km and >70 km depth, respectively. If $\beta$ exceeds 2, this is equivalent to the earthquake rate deviating more than 2 standard deviations from background, with the background defined by the seismicity rate during the period 2006–2011.
Figure 7: Overview of seismicity in northern Chile between 1980 and 2020. (a) Map view of the distribution of seismicity from the ISC catalogue with $m_b \geq 4.7$ with the focal mechanisms of the largest mainshocks. Grey circles represent earthquake hypocentres, and coloured circles represent earthquakes used in the analyses in (b,e,f). Dark coloured circles are shallow earthquakes and red-orange coloured circles are intermediate-depth earthquakes. (b) Cross-sectional view of the seismicity projected onto the black-dashed path in (a) showing the cluster of seismicity at $\sim 400$ km distance along the profile. (c) Temporal evolution of shallow (<50 km) seismicity in northern Chile from the IPOC catalogue of Sippl et al. [2018] calculated using a sliding window of width 0.1 year and time steps of 0.02 years. (d) Same as (c), but for the intermediate-depth seismicity between 70 km and 300 km depth. (e) and (f) show histograms of the number of earthquakes in the ISC catalogue with $m_b > M$ each year for the shallow and intermediate-depth seismicity, respectively. The area in grey marks the installment of the IPOC network in northern Chile in 2006. Vertical dashed lines mark the timing of major earthquakes in the region and their magnitudes, with megathrust events represented by a light blue box and intraslab events by a light red box.
Figure 8: Cumulative distribution of shallow and intermediate-depth earthquakes in northern Chile shown in Figure 7a. (a) Cumulative distribution between 1980 and 2020 of events $m_b \geq 4.7$. Major ($M_w \geq 7.5$) megathrust and intermediate-depth earthquakes are shown by vertical dashed lines, with Ant = Antofagasta, Are = Arequipa, Tar = Tarapaca, Toc = Tocopilla and Iqu = Iquique. (b-d) Cumulative distributions of seismicity over particular periods of time compared to the predictions of time-randomised catalogues. The grey polygons show the area in which 67%, 95% and 99% of catalogues with the same number of events $N$ but randomised earthquake times would plot. The confidence intervals are wider for catalogues with fewer events. In (c) vertical arrows point out distinct changes in the frequency of earthquakes that do not correlate with any major earthquakes. The equivalent plot for the declustered catalogue is shown in Supplementary Figure 14.
Figure 9: Sketch of the effect of stress transfer from an earthquake stress drop of amplitude $\Delta \tau$ on the triggering of nearby seismicity for (a) shallow earthquakes, and intermediate-depth earthquakes generated by (b) dehydration embrittlement, (c) dehydration-assisted stress transfer, and (d) self-localising thermal runaway (SLTR). For each mechanism, the top row shows the shear stress distribution on a population of seismogenic faults within a fixed (arbitrary) volume around the mainshock, where $\tau_y$ is the maximum failure stress for a given failure mechanism. In (b) and (c) the maximum failure stress would be dry olivine friction, or the effective failure stress $\tau_y^{eff}$ for faults containing highly-pressurised fluids. In (c) the maximum failure stress would be the stress needed to drive self-localising thermal runaway. The coloured region shows schematically the number of faults that would fail in aftershocks in response to a fixed stress transfer. The bottom row shows the failure strength envelope. The envelope shape in (d) is modified from John et al. [2009].