

1 **Uncertainty in the response of sudden stratospheric warmings and stratosphere-**
2 **troposphere coupling to quadrupled CO₂ concentrations in CMIP6 models**
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34 **Key Points:**

- 35 • The tropospheric signal of Sudden Stratospheric Warming (SSWs) in the North Atlantic
36 does not change under 4xCO₂ forcing.
- 37 • There is high uncertainty in changes of SSW frequency under 4xCO₂ forcing; single
38 models show the rate to be significantly halved or doubled.
- 39 • The boreal polar vortex will form earlier and disappear later under increased CO₂,
40 extending the season of stratosphere-troposphere coupling.

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44 **Abstract**

45 Major sudden stratospheric warmings (SSWs), vortex formation and final breakdown
46 dates are key highlight points of the stratospheric polar vortex. These phenomena are relevant for
47 stratosphere-troposphere coupling, which explains the interest in understanding their future
48 changes. However, up to now, there is not a clear consensus on which projected changes to the
49 polar vortex are robust, particularly in the Northern Hemisphere, possibly due to short data
50 record or relatively moderate CO₂ forcing. The new simulations performed under the Coupled
51 Model Intercomparison Project, Phase 6, together with the long daily data requirements of the
52 DynVarMIP project in preindustrial and quadrupled CO₂ (4xCO₂) forcing simulations provide a
53 new opportunity to revisit this topic by overcoming the limitations mentioned above.

54 In this study, we analyze this new model output to document the change, if any, in the
55 frequency of SSWs under 4xCO₂ forcing. Our analysis reveals a large disagreement across the
56 models as to the sign of this change, even though most models show a statistically significant
57 change. The models, however, are in good agreement as to the impact of SSWs over the North
58 Atlantic: there is no indication of a change under 4xCO₂ forcing. Over the Pacific, however, the
59 change is more uncertain. Finally, the models show robust changes to the seasonal cycle in the
60 stratosphere. Specifically, we find a longer duration of the stratospheric polar vortex, and thus a
61 longer season of stratosphere-troposphere coupling.

62 **1 Introduction**

63 The stratospheric polar vortex is a strong wintertime circumpolar cyclonic circulation that
64 isolates the polar air masses from air in the lower latitudes [Andrews et al. 1987]. The
65 stratospheric polar vortex forms in Autumn as solar heating vanishes at the pole, establishing
66 strong meridional temperature gradients. The vortex intensifies during winter and then decays in
67 spring as sunlight returns to high latitudes. The springtime breakdown of the vortex, when the
68 zonal winds revert to easterlies, is also known as the stratospheric final warming (SFW).

69 Interest in the polar vortex has increased in the last decades for two different reasons.
70 First, the magnitude of the Antarctic ozone hole is dependent on the state of the polar vortex, as a
71 strong polar vortex is associated with colder temperatures (crucial for heterogeneous ozone
72 chemistry) and reduced mixing with ozone-rich mid-latitude air [Schoeberl and Hartmann,
73 1991]. Secondly, polar stratospheric variability is known to affect not only the stratosphere but
74 also the troposphere, typically projecting onto Annular Mode patterns [e.g.: Baldwin and
75 Dunkerton, 2001; Kidston et al., 2015]. Polar stratospheric variability peaks in the winter
76 hemisphere when the polar vortex is present, as a major source of stratospheric variability is
77 upward propagating, planetary-scale Rossby waves from the troposphere below [Charney and
78 Drazin, 1961]. Under linear theory, the vertical propagation of Rossby waves is limited to
79 regions with westerly winds [Andrews et al. 1987]. Furthermore, because wave activity is greater
80 in the Northern Hemisphere (NH) than in the Southern Hemisphere (SH) so is the polar
81 stratospheric variability. In the SH, stratospheric variability, and thus the coupling to the
82 troposphere, is mainly associated with SFW [Black and McDaniel 2007]. In the NH apart from
83 SFWs [Black et al. 2006; Ayarzagüena and Serrano, 2009; Hardiman et al., 2011], this coupling
84 is primarily associated with polar vortex extremes, in particular, major sudden stratospheric
85 warmings (SSWs). SSWs happen in midwinter and consist in a reversal of wintertime polar
86 stratospheric circulation with a subsequent recovery of the polar vortex after the event. The
87 tropospheric signal of SSWs can persist for up to two months after the occurrence of each event

88 [Charlton and Polvani, 2007]. This signal is particularly strong and persistent after a subset of
89 SSWs, called Polar-night Jet Oscillation events (PJOs), which are characterized by a very
90 persistent warm polar lower stratosphere [Hitchcock et al., 2013].

91 The importance of polar vortex variability for both atmospheric dynamics and ozone
92 chemistry has spurred considerable efforts in identifying if and how the stratospheric polar
93 vortex might respond to increasing greenhouse gases (GHGs). While several studies have been
94 devoted to this question, there is not consensus at this time on which projected changes to the
95 polar vortex are robust. Here, and throughout the paper, we use the word robust to mean a strong
96 agreement across many models as to the size and amplitude of the changes to the stratospheric
97 polar vortex under increased GHG. To offer a trivial example: a two-model ensemble in which
98 one model predicted a halving of SSW frequency and the other model predicted a doubling of
99 SSW frequency would not represent a robust prediction of future changes, although both these
100 changes might be statistically significant in each model. On the contrary, if one model predicted
101 a significant increase of SSW frequency by a factor of 2.5 and the other by a factor of 2, we
102 would regard this as a robust prediction.

103 Early studies using simple models demonstrated polar stratospheric cooling under
104 increased GHG forcing [Manabe and Wetherland, 1967; Fels et al. 1980]. Global atmospheric
105 modeling work in the 1990s (with prescribed changes in sea surface temperatures) projected a
106 boreal polar warming in winter, but no consensus on the changes in the number of SSWs [Rind
107 et al. 1990; Mahfouf et al 1994; Rind et al. 1998; Butchart et al 2000]. Moreover, after decades
108 of improvement in modeling the stratosphere, a clear consensus about future changes to the polar
109 vortex is still missing. For instance, one can find in the literature a number of single-model
110 studies that report a significant increase in the frequency of SSWs in the future [Charlton-Perez
111 et al., 2008; Bell et al., 2010], while other studies report a non-statistically significant increase
112 [e.g. Mitchell et al., 2012a; Ayarzagüena et al. 2013], and others no significant change in SSW
113 frequency at all [McLandress and Shepherd, 2009; Scaife et al., 2012; Karpechko and Manzini,
114 2012]. Multi-model intercomparisons of Chemistry Climate Model Validation (CCMVal) and
115 Coupled Model Intercomparison Project 5 (CMIP5) models have reported large discrepancies in
116 the sign of change among models [Mitchell et al. 2012b; Kim et al., 2017].

117 Recently, Ayarzagüena et al. [2018] revisited this topic, trying to overcome some of the
118 issues suggested in the literature as potential reasons for this disagreement, such as the use of one
119 single model in the analysis or the dependence of results on the SSW identification criterion.
120 They analyzed 12 different models participating in the Chemistry Climate Model Initiative
121 (CCMI) and applied several different (absolute and relative) criteria for the identification of
122 SSWs. The outcome was again a lack of a significant change in SSWs frequency in the future,
123 although most of the models predicted a slight increase in the frequency of these, regardless of
124 the SSW identification algorithm. One might argue, however, that the limited data record
125 available (40 years in each period of study), and the relatively moderate GHG forcing used in the
126 central CCMI scenario (Representative Concentration Pathway 6.0, RCP6.0), might be
127 insufficient to detect significant changes in SSWs in those simulations.

128 The new CMIP6 model generation together with the special data requirements of the
129 DynVarMIP project [Gerber and Manzini, 2016] provide a new opportunity to revisit the
130 question of the effects of increasing CO₂ on the interannual variability of the stratospheric polar
131 vortex. The very long daily data record at stratospheric levels of the Diagnostic, Evaluation and
132 Characterization of Klima (DECK) experiments allows us, for the first time, to try to isolate

133 forced changes in stratospheric variability in a larger ensemble of high-top models than possible
134 previously [Eyring et al. 2016]. Specifically, one of these DECK simulations consists in a very
135 high CO₂ forcing (abrupt4xCO₂) enabling the exploration of changes in the vortex variability
136 under an extreme future scenario. Furthermore, the daily output of the 1pctCO₂ simulation with a
137 gradual increase of CO₂ allows us to investigate the time of emergence of SSW changes.

138 The goal of this study is to analyze the potential changes in the interannual variability of
139 the polar vortex due to increasing CO₂ concentrations, as simulated by CMIP6 models. Apart
140 from the mentioned new possibilities opened up by the availability of CMIP6 data, we have also
141 examined other characteristics that are relevant for the stratosphere-troposphere coupling such as
142 the seasonal cycle of the polar vortex, i.e. formation and final breakdown, in both hemispheres,
143 as well as changes in stratosphere-troposphere coupling during SSWs, given the importance of
144 these aspects for tropospheric impacts and predictability. However, we do not aim here to fully
145 diagnose stratospheric variability in the CMIP6 models, nor to explain why models differ in their
146 estimates of the sensitivity of the stratospheric polar vortex to CO₂ forcing. Instead, we simply
147 aim to provide a timely, quantitative estimate of how stratospheric variability might change
148 under CO₂ forcing since this information is of critical importance to the upcoming
149 Intergovernmental Panel on Climate Change (IPCC) AR6 report, and for future work on the
150 stratosphere in CMIP6 models.

151

152 **2 Data and methodology**

153 **2.1 Data**

154 In this study we analyze the daily output of DECK simulations by 12 CMIP6 models
155 participating in the DynVarMIP initiative (Table 1). All the models are coupled to an ocean and
156 sea ice model, and most (8 out of 12) are “high-top” models, defined by having a model top at or
157 above 0.1hPa as in Domeisen et al. [2019]. A priori, we expect the high-top models to have more
158 realistic polar stratospheric variability and, consequently, to better simulate SSWs, and their
159 frequency and surface impacts, than low-top models [Charlton-Pérez et al. 2013]. For the CMIP6
160 ensemble, there are a much larger number of models that have a high model top than in the
161 previous CMIP5 ensemble. In order to make sure our model sample is unbiased, only a single
162 member of each model ensemble is analyzed here; details are shown in Table 1.

163 We focus on four DECK experiments [Eyring et al., 2016], each of them used for
164 different purposes. The historical run is employed for model validation: we compare the
165 simulated SSW frequency, intensity and seasonality to the values obtained from the JRA-55
166 reanalysis [Kobayashi et al., 2015]. In fact, we have specifically restricted the analysis period to
167 1958-2014 to perform a rigorous quantitative comparison with JRA-55.

168 The piControl experiment is used for two purposes. Since it contains a very long data
169 record (more than 450 years for most of the models, Table 1), it is used to characterize both the
170 baseline estimates of SSW frequency and intensity, and to characterize internal atmospheric
171 variability in SSW frequency and trends.

172

173

174 **Table 1.** List of models included in the analysis indicating their resolution and the ensemble
 175 members considered in simulations. Equilibrium climate sensitivity for CO₂ doubling is taken
 176 from analysis by A. G. Pendergrass using Gregory et al. [2004] method
 177 (<https://github.com/apendergrass/cmip6-ecs>)

178

Models	Model resolution	Ensemble members	Internally generated QBO	Nr. of years piControl run	Equilibrium Climate Sensitivity / K
CanESM5 [Swart et al. 2019a,b]	T63L49, top 1hPa	r1i1p2f1	No	450	5.59
CESM2 [Danabasoglu et al. 2019a, b]	1°x1° L32, top 40km	r1i1p1f1	No	1200	5.12
CESM2-WACCM [Danabasoglu, 2019; Gettelman et al. 2019]	1°x1° L70, top 150km	r1i1p1f1	Yes	500	4.61
CNRM-ESM2-1 [Séférian, 2018; Séférian et al. 2019]	T1127L91, top 0.01hPa	r1i1p1f2	Yes	500	4.66
GFDL-CM4 [Guo et al. 2018; Held et al. 2019]	C96L33, top 1hPa	r1i1p1f1	No	140	3.84
GISS-E2-2-G [NASA-GISS et al. 2018]	2°x2.5°, top 0.002hPa	r1i1p1f1	Yes	81	
HadGEM3-GC31-LL [Roberts, 2017; Williamson et al. 2018]	N261L85, top 85km	r1i1p1f3 except for piControl run: r1i1p1f1	Yes	500	5.41
INM-CM5-0 [Volodin et al. 2017]	2x1.5L73, top 0.2hPa	r1i1p1f1	Yes	154	2.1
IPSL-CM6A-LR [Boucher et al. 2018]	N96, top 80km	r1i1p1f1	Yes	1200	4.49
MIROC6 [Tatebe et al. 2018; 2019]	T85L81, top 0.004hPa	r1i1p1f1	Yes	800	2.54
MRI-ESM2-0 [Yukimoto et al. 2019a b]	TL159L80, top 0.01hPa	r1i1p1f1	Yes	200	3.30
UKESM1-0-LL [Tang et al., 2019; Kuhlbrodt et al. 2018]	N96L85, top 85 km	r1i1p1f2	Yes	1100	5.27

179

180 The abrupt4xCO₂ and 1pctCO₂ runs are used to examine the impact of CO₂ forcing on
 181 SSW properties. Both simulations extend 150 years (except for the abrupt4xCO₂ in IPSL-

182 CM6A-LR, which is 900 years long, and GISS-E2-2-G, which is 81 years long). All forcings in
 183 the abrupt4xCO₂ simulations are identical to those in the piControl run, except for the CO₂
 184 concentrations, which is abruptly quadrupled from piControl levels, and then are held constant
 185 throughout the entire length of the simulation [Eyring et al. 2016]. The large and constant forcing
 186 in the abrupt4xCO₂ makes it possible to isolate robust changes, if any, to the size and nature of
 187 changes to SSW properties. In the 1pctCO₂ simulation, the CO₂ concentration starts at pre-
 188 industrial levels and is increased at the rate of 1% per year. This simulation is used to estimate
 189 the rate at which SSW frequency might change in the future [one aspect of the so-called
 190 ‘dynamical sensitivity’ of the stratosphere, Grise and Polvani 2016].

191 Anomalies are defined as the departure from the daily evolving annual cycle of each
 192 respective model. In the piControl run, the climatology is based on the whole period, while in the
 193 historical run only the 1979-2014. In the abrupt4xCO₂ runs, a trend is identified in some
 194 variables during the first 50 years following the switch-on of the forcing. To avoid this trend, the
 195 climatologies are computed after omitting the first 75 years except for IPSL-CM6A-LR where
 196 we omit the first 300 years as its integration extends longer than 400 years. A similar omission of
 197 data is performed for the analysis of SFW or vortex formation dates. In contrast, the full
 198 abrupt4xCO₂ is considered when looking at SSW frequency as no trend is detectable in the
 199 occurrence of these phenomena.

200 2.2 Methods

201 There has recently been a considerable discussion in the literature as to which metrics
 202 best characterize the variability of the stratospheric polar vortex, in particular, extreme vortex
 203 weakening events [Butler et al. 2015; Butler and Gerber, 2018]. However, in a recent study,
 204 Ayarzagüena et al. [2018] found little dependence on the choice of metrics in terms of
 205 documenting future changes in SSWs. Thus, we here focus only on a few, widely-used and easily
 206 implementing metrics of stratospheric variability. Future work will likely be able to explore
 207 stratospheric variability in more detail, and possibly reveal subtleties in changes to stratospheric
 208 circulation not apparent in our initial analysis. Furthermore, focusing on commonly used
 209 diagnostics allows us to place our work in the context of previously published studies on changes
 210 in, for example, SSW frequency.

211 Several aspects of the stratospheric polar vortex (formation, final breakdown and
 212 variability) are analyzed using the zonal mean zonal wind at 60°N and 10hPa ($u_{60N10hPa}$) for the
 213 NH, and 60°S and 10hPa for the SH.

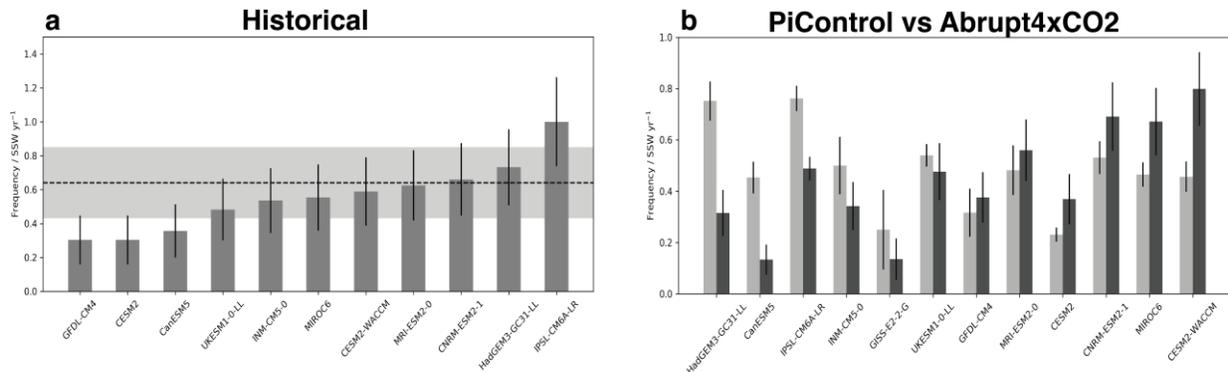
- 214 • SSWs are identified following the criterion proposed in Charlton and Polvani [2007], which
 215 is based on the reversal in the sign of $u_{60N10hPa}$ from November to March. Their criterion
 216 includes two additional restrictions: (1) winds must return to westerly for at least 20
 217 consecutive days between events and (2) winds must return to westerly for at least 10
 218 consecutive days before April 30 of each year. Recall that this definition only identifies so-
 219 called “major” SSWs. Here we do not examine other aspects of polar vortex variability, such
 220 as vortex intensification events, wave reflection events, or minor stratospheric warmings.
- 221 • SFWs is defined as the last date in the spring on which $u_{60N10hPa}$ reverses and does not return
 222 to westerly for more than 10 consecutive days [Butler and Gerber, 2018].
- 223 • The polar vortex formation date is identified as the first time that $u_{60N10hPa}$ turns westerly after
 224 1 July, in the NH, and stays westerly for at least 10 days.

225 • **PJOs** are identified by applying a slight variation of criteria established by Hitchcock et al.
 226 [2013], as the original required finer vertical resolution than available. The new metric has
 227 been validated in reanalysis to ensure that similar results are obtained in this case as to those
 228 obtained by applying the original one (not shown). Here, the identification is based on two
 229 time series $PC_1 = T'(5 \text{ hPa}) - T'(100 \text{ hPa})$ and $PC_2 = T'(50 \text{ hPa})$, where T' indicates the
 230 polar-cap averaged temperature anomaly (from climatology) at the specified pressure level.
 231 These time series are transformed into polar coordinates $r(t)$ and $\phi(t)$, and the central dates
 232 of events are defined by when the phase $\phi(t)$ passes counter-clockwise through $3\pi/2$, so
 233 long as the amplitude $r(t)$ is greater than 2.5σ . Once a central date is defined, the starting date
 234 of the event is defined by the most recent date prior to the central date when $r(t)$ is below
 235 1.5σ , and similarly the ending date of the event is defined by the earliest date following the
 236 central date when the $r(t)$ is below 1.5σ .

237 **2.2 Statistical methods**

238 Two methods to calculate the statistical significance of changes to the SSW frequency are
 239 used: a parametric method based on an assumption that the SSW frequency can be estimated
 240 using a Poisson point process, and a non-parametric bootstrapping technique based on
 241 resampling the piControl run of each model. Trends in SSW frequency and the time of
 242 emergence of these trends are estimated by fitting a Generalized Linear Model (GLM) to the
 243 decadal SSW frequency estimates from each model. All three statistical methods are described in
 244 detail in Appendix 1.

245 **3 Model simulation of SSWs during the Historical Period: Mean frequency and seasonal**
 246 **distribution**



247
 248 **Figure 1. (a)** Average annual SSW frequency in the historical simulations (1958-2014)
 249 of the 11 models. Black lines show 95% confidence estimates for the annual frequency. Dashed
 250 black line corresponds to SSW frequency in the JRA-55 reanalysis, with its 95% confidence
 251 interval in the light gray shading. **(b)** Same as (a) but for SSW occurrence in the piControl (light
 252 gray bars) and abrupt4xCO₂ simulations (dark gray bars). Black lines show 95% confidence
 253 intervals for each estimate. Bars are ordered by the size of the difference between the two
 254 simulations.

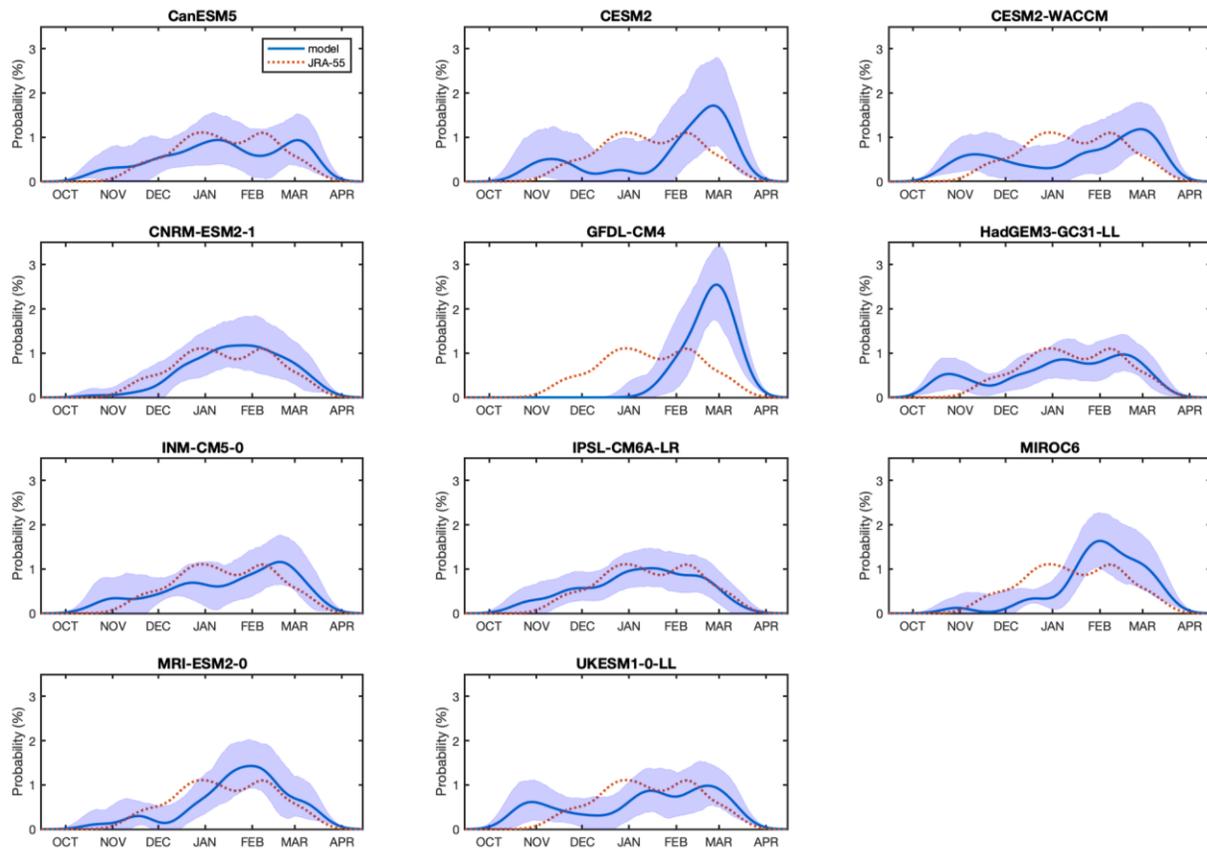
255
 256 Prior to reporting changes in SSWs caused by increased CO₂ concentrations, it is
 257 important to document the models' ability to simulate SSW events during the period of overlap

258 with re-analysis data: we do so by analyzing the historical simulations. Figure 1a shows the
259 average frequency of SSWs during the period 1958-2014 in JRA-55 reanalysis (horizontal
260 dashed line) and the corresponding value for the CMIP6 models (bars; the numerical values are
261 given in Table S1). In agreement with prior studies [e.g., Charlton-Perez et al. 2013;
262 Ayarzagüena et al. 2018] we find a large spread across the models in the mean frequency of
263 SSW over that period. This spread is likely due, in part, to the large internal variability of the
264 polar wintertime stratosphere; even with an identical climate model the frequency of SSWs can
265 vary greatly across different realizations, as demonstrated by Polvani et al. [2017].

266 Mindful of this large internal variability, it appears that only four of the models are
267 significantly different from JRA-55, at the 95% confidence level. Three of these are the models
268 with the lowest model tops (CESM2, CanESM5 and GFDL-CM4) that simulate fewer SSW
269 events than JRA-55 re-analysis. When comparing the seasonal distribution of SSW activity in
270 these models with JRA-55 (Fig. 2) it is clear that for two of them (GFDL-CM4 and CESM2), the
271 SSW activity is significantly shifted towards March, with few SSWs observed in December and
272 January. This is another common bias in low-top models [Charlton-Perez et al., 2013], and more
273 generally, in models with an overly strong polar vortex. It is also worth noting that the three low-
274 top models mentioned above are the only ones lacking a simulated Quasi-Biennial Oscillation
275 (QBO). The fourth model with an unrealistic SSW frequency (IPSL-CM6A-LR), in contrast,
276 simulates a very high number of SSWs, on average one per year during the historical period
277 (instead of one every other year). As detailed below, this model also stands out for its high
278 frequency of warmings in the piControl run. While we retain these four models in our analysis,
279 the simulated changes produced by these models should be treated with caution given these
280 biases.

281 Finally, considering the surprising occurrence of an SSW in the SH in 2002 [Krüger et al.
282 2005], we extended the analysis to that hemisphere. Not a single SSW event was identified in the
283 SH over the historical period in the models analyzed here. One may be tempted to claim that the
284 CMIP6 models are underestimating the stratospheric variability in the SH, as spontaneous SSWs
285 in the absence of stationary waves have been reported in simple models [Kushner and Polvani,
286 2005]. However, it remains to be demonstrated whether five or six decades of observations are
287 sufficient to make that claim.

288



289

290 **Figure 2.** SSW frequency distribution in the historical simulation of each model (blue line) and
 291 JRA-55 reanalysis period (orange dashed line). The distribution has smoothed by a kernel
 292 smoother of a bandwidth of 10 days. Shading corresponds to 2.5th-97.5th percentile range of the
 293 bootstrap samples i.e., the 95% confidence interval on the mean of the piControl simulation. (See
 294 more details about the determination of this interval in Appendix).

295

296 4 Future changes in polar stratospheric variability

297 4.1 Future changes in sudden stratospheric warmings

298 Figure 1b displays the mean frequency of SSWs in both the piControl and abrupt4xCO₂
 299 simulations (numerical values in Table S2). As discussed in Section 2, all SSWs identified in the
 300 entire abrupt4xCO₂ simulation have been considered. We stress, however, that the main results
 301 presented below do not change significantly if only the last 75 years of each abrupt4xCO₂
 302 simulation are used (not shown). Two different tests of the statistical significance of the changes
 303 are conducted, providing a consistent indication of the statistical significance of changes,
 304 although the precise p-values vary due to difference in the underlying assumptions.

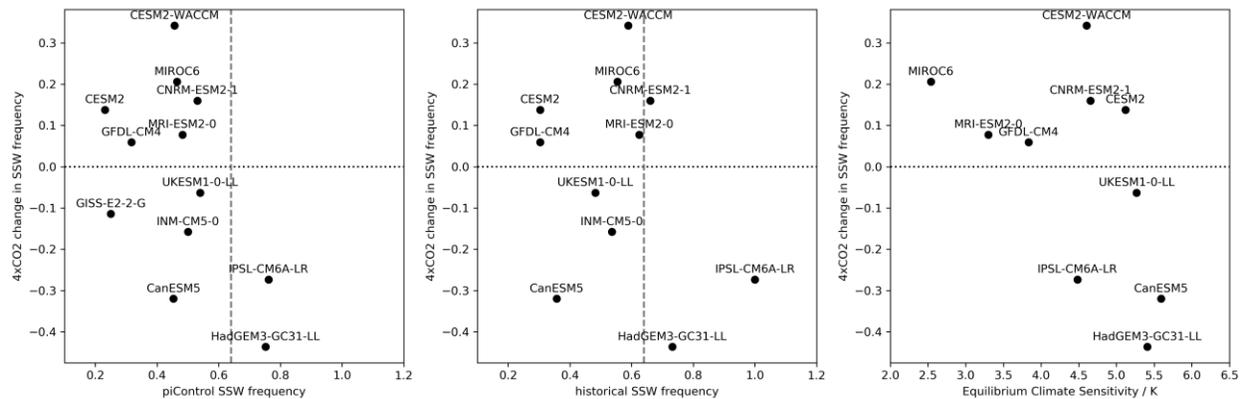
305 Of the 12 models in our study, four models indicate a statistically significant *decrease* in
 306 SSW frequency, while four indicate a statistically significant *increase* in SSW frequency. Thus,
 307 no consensus in the sign of the change exists in the CMIP6 models, in agreement with the
 308 diversity of claims reported in the earlier literature. The lack of a robust change across the

309 models is not due to a lack of sensitivity of SSW frequency to increasing CO₂: in fact, 8 of the 12
 310 models indicate significant changes. Rather, the CMIP6 models suggest that there is a great deal
 311 of uncertainty in the sign of the change, which varies between a near doubling in the frequency
 312 of SSWs in some models, to a near halving in others. These divergent responses of the models
 313 may now be clearer in the CMIP6, where we can consider a stronger forcing (4xCO₂) and have
 314 access to longer records of daily data, compared to previous studies.

315 We also note that the lack of consensus in the CMIP6 models agrees with the recent study
 316 of Ayarzagüena et al. [2018], who analyzed the chemistry climate model projections of the
 317 CCM1 models, which were forced with RCP6.0 scenario. While reporting a general tendency
 318 towards an increased frequency of SSWs by the end of the current century, they also emphasized
 319 that most changes were *not* statistically significant.

320 We do not attempt to further analyze the causes of differences in the model responses
 321 here, other than to note that within our set of models, one of the models indicating a significant
 322 reduction of SSW frequency (CanESM5) and one of the models indicating a significant increase
 323 of SSW frequency (CESM2) have anomalously low SSW frequency and (in the case of CESM2)
 324 a biased seasonal distribution of SSW in the historical simulations (Fig. 2). Additionally, the two
 325 models which show robust decreases in SSW frequency (HadGEM3-GC31-LL and IPSL-
 326 CM6A-LR) have the highest frequency of SSW events in the piControl and historical
 327 simulations. The IPSL-CM6A-LR has a significant bias in SSW frequency and presents some
 328 strong biases in the representation of QBO in the abrupt4xCO₂ simulation.

329



330

331 **Figure 3:** Scatter plots of the change of SSW frequency between the piControl and abrupt4xCO₂
 332 simulations vs. the frequency in the piControl simulations, in the historical simulations and the
 333 ECS. In the first two plots, the grey dashed line shows the observed SSW frequency in the JRA-
 334 55 re-analysis (0.64 SSW yr⁻¹).

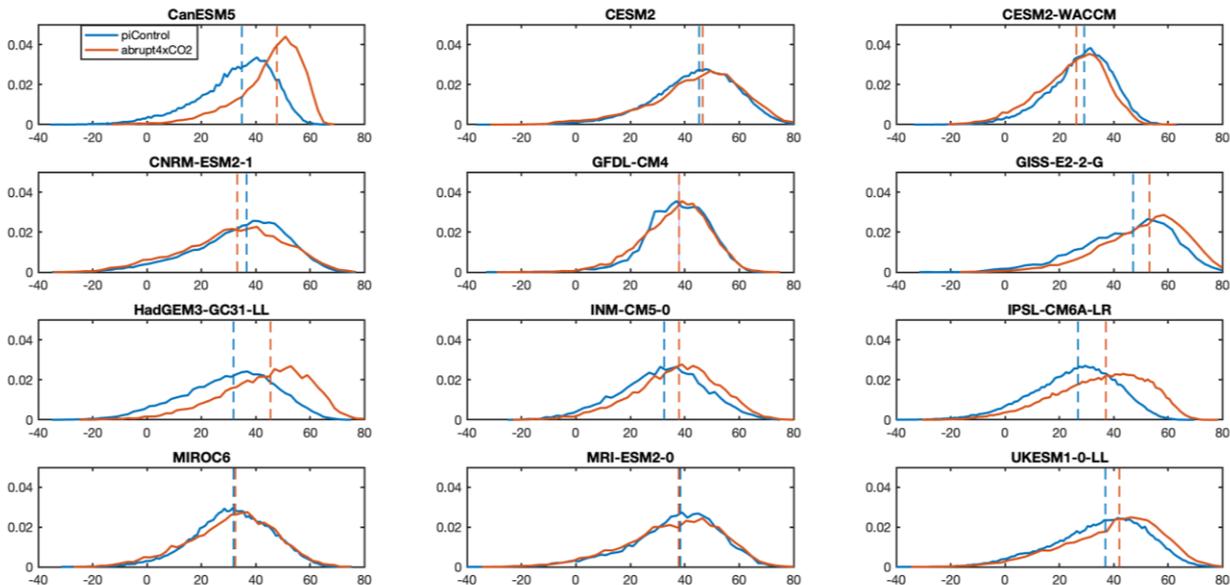
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336 We also briefly examined the relationship between the change in SSW frequency and
 337 possible predictors of the change, including the frequency of SSWs in the piControl and
 338 historical simulations and the Equilibrium Climate Sensitivity (ECS, Gregory et al. [2004]) (Fig.
 339 3). Recall that ECS gives a measure of the equilibrium change of the global surface temperature
 340 after a doubling CO₂. As can be seen from Fig. 3, models that have a larger frequency of SSWs
 341 in the piControl run and models that have a larger ECS seem to produce large reductions in SSW
 342 frequency under large CO₂ forcing. The correlation between SSW frequency changes and ECS is

343 -0.52 with a p-value of 0.12. The correlation between piControl frequency and SSW frequency
 344 changes is -0.50 with a p-value of 0.10. Further analysis of a larger ensemble would be required
 345 to determine the robustness of these relationships. Although not addressed in the literature, a
 346 relationship between ECS and SSW frequency changes might be possible given some previous
 347 results connected to this topic. Shepherd and McLandress, [2011] and Grise and Polvani [2016]
 348 documented a link between the strengthening of the sub-tropical jet and stratospheric wave
 349 driving. Moreover, Li et al. [2007] have argued that the subtropical jet, and tropospheric state in
 350 general, might control the upward planetary wave propagation.

351 To further examine the changes in SSW frequency under 4xCO₂ forcing, we have
 352 analyzed the entire distribution of daily $u_{60N10hPa}$ in December-January-February in the piControl
 353 and abrupt4xCO₂ simulations (Fig. 4). The four models with a significant decrease in SSWs
 354 frequency in Fig. 1b (HadGEM3-GC31-LL, CanESM5, IPSL-CM6A-LR, INM-CM5-0) are also
 355 those that show the largest shift of the $u_{60N10hPa}$ distribution towards stronger vortex speeds in the
 356 abrupt4xCO₂ experiment. Interestingly, the opposite does not always apply to models with a
 357 significant increase in SSWs. The models with the largest changes in SSW frequency, MIROC6
 358 and CESM2-WACCM show small changes to either the median or standard deviation of the
 359 $u_{60N10hPa}$ (Table S3). This would agree with the results of Taguchi [2017] who pointed out SSW
 360 frequency does not only correlate with vortex strength but also wave activity.

361



362

363 **Figure 4.** Probability distribution of daily zonal mean zonal wind at 60°N and 10hPa (m/s) for
 364 the piControl (blue) and abrupt4xCO₂ (orange) experiments. Dashed lines represent the median
 365 value of the distribution in each integration.

366

367 A similar analysis was repeated for the zonal-mean zonal wind at 10hPa averaged
 368 between 70° and 80°N (not shown). That latitude band was found by Manzini et al. [2014] to
 369 display significant future changes in wind in most models, unlike the 60°N latitude where no

370 robust future changes were found in CMIP5 models because the opposed effects of subtropical
371 jet and stratospheric polar vortex changes might combine at that latitude. However, in our case,
372 the main conclusions remain the same. Those models that show a shift of the $u_{60N10hPa}$
373 distribution towards stronger vortex speeds under $4xCO_2$ forcing also display a sharper peak of
374 high values u at $70-80^\circ N$ suggesting lower variability in that region, consistent with a stronger
375 and larger vortex.

376 We have also examined potential changes in SSW seasonality. However, despite the
377 already mentioned changes detected in SSW frequency in some models, the drastic increase in
378 CO_2 concentrations does not appear to substantially affect the seasonal distribution of SSWs (not
379 shown).

380 Finally, motivated by the recent occurrence of a minor but highly publicized SSW event
381 in the SH in September 2019 [Hendon et al., 2019], together with the occurrence of a major SSW
382 in September 2002, we also examined the CMIP6 models to determine the extent to which the
383 likelihood of similar events might change under the extreme climate forcing in the abrupt $4xCO_2$
384 runs. Only one of our twelve models (MRI-ESM2-0) simulates an SSW in both the piControl and
385 the abrupt $4xCO_2$ simulations. Thus, these runs provide no evidence for the claim of possible
386 trends in the frequency of SSWs in the SH that would be caused by increased CO_2
387 concentrations.

388 4.2 Trends in SSW frequency and time of emergence

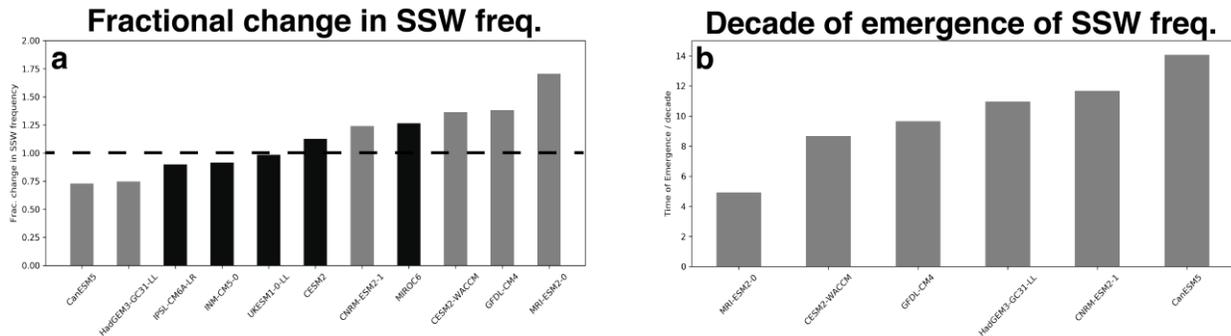
389 For the model integrations which show a statistically significant increase or decrease in
390 SSW frequency between the piControl and the abrupt $4xCO_2$ runs, it is useful to consider when
391 and whether the trend in SSW frequency might be detected in a simulation with continuously
392 increasing CO_2 forcing. A useful way to frame climate trends is in terms of the time of
393 emergence of the signal from the unforced climate noise [Hawkins and Sutton, 2012]. This
394 question is examined by studying the occurrence of SSWs in the 1pct CO_2 runs, an idealized
395 scenario.

396 Trend estimates for each model are shown in the Fig. 5a (numerical values in Table S4).
397 Results reveal that there are six models (light gray bars) for which the null hypothesis of no trend
398 in SSW frequency can be rejected, but consistent with the results of the previous section, the sign
399 of this trend is not robust across models. While CanESM5 and HadGEM3-GC31-LL show a
400 significant decrease, CNRM-ESM2-1, CESM2-WACCM, GFDL-CM4 and MRI-ESM2-0 show
401 a significant increase. Recall that for the abrupt $4xCO_2$ runs (Fig. 1b), CNRM-ESM2-1 and
402 CESM2-WACCM also indicated a statistically significant increase in SSW frequency compared
403 to the piControl runs, while GFDL-CM4 and MRI-ESM2-0 did not (although they did indicate
404 an increased frequency). CanESM5 and HadGEM3-GC31-LL both showed a statistically
405 significant decrease.

406 One can also estimate a time of emergence of the trend by comparing the trend in the
407 1pct CO_2 runs with the natural variability in SSW frequency from the piControl run (see
408 Appendix for details in the procedure). For the models with a significant trend, the decade of
409 emergence is shown in Fig. 5b. There is a wide spread in the projected time of emergence for the
410 models with a significant trend, varying from the 5th decade to 14th decade. This result reflects
411 both the variation in the trend across the models and the spread in the estimated variability in
412 SSW frequency (the noise) in the piControl simulations. Since the time of CO_2 doubling occurs

413 between the 6th and 7th decade in the 1pctCO₂ run and approximately by 2060-70 in the RCP8.5
 414 scenario [Meinshausen et al., 2017], these results indicate that the emergence of a detectable
 415 change in SSW frequency is extremely unlikely prior to the end of the 21st century.

416



417

418 **Figure 5. (a)** Estimated fractional change in SSW frequency by the seventh decade of the
 419 1pctCO₂ simulations. Light gray shaded lines indicate that the trend of SSW frequency in the
 420 model is significantly different from zero at a p-value of 0.05. Dashed line indicates trend equal
 421 to 1, i.e. no trend in the SSWs frequency. **(b)** Decade of emergence of SSW frequency trend for
 422 those models in which the trend term is significantly different from zero, calculated as described
 423 in the main text.

424

425 5 Future changes in the seasonal cycle of the polar stratosphere

426 Since, according to linear theory, the vertical propagation of stationary Rossby waves is
 427 restricted to periods with westerly winds, stratospheric variability is largely confined to the
 428 winter season [e.g., Charney and Drazin 1961]. When considering how stratospheric variability
 429 might change in future climates it is therefore also important to consider the extent to which the
 430 timing and length of the winter season in the stratosphere might also change.

431 Figure 6a and b show the distribution of dates of formation and final breakdown of the
 432 boreal stratospheric polar vortex, respectively, in the piControl, historical and abrupt4xCO₂
 433 CMIP6 simulations. In these plots the first years of the abrupt4xCO₂ simulations (75 or 300
 434 years) have been omitted similarly to the procedure followed to calculate the climatology.
 435 Nevertheless, conclusions do not change when considering the whole data record for
 436 abrupt4xCO₂ runs.

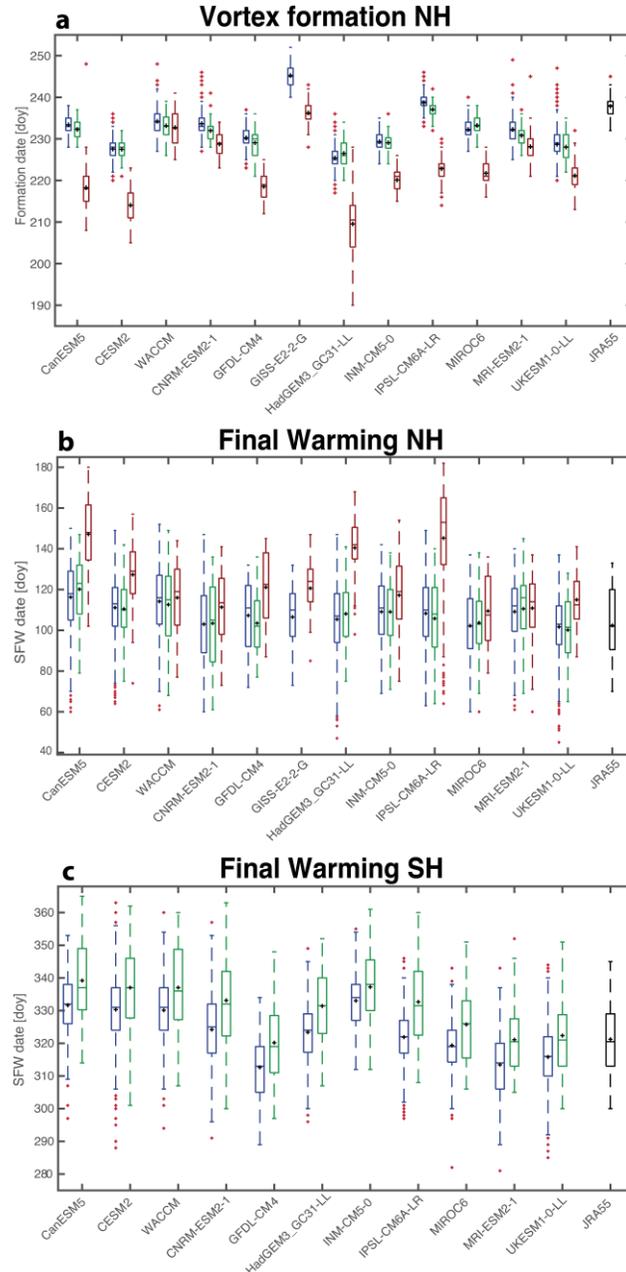
437 First, let us consider the historical model simulations, and contrast them to the reanalysis.
 438 Over the period 1958-2014, the polar vortex forms earlier in all models than it does in the
 439 reanalysis, with the exception of IPSL-CM6A-LR. In contrast, the SFW date is well reproduced
 440 by models. The later implies an improvement with respect to previous generations of climate
 441 models, such as those contributing to CCMVal and CMIP5, which simulated a delayed SFW
 442 [Butchart et al., 2011; Kelleher et al., 2019]. CMIP6 models are also good at simulating the
 443 different range of interannual variability in the dates of vortex formation and SFW, the latter
 444 being considerably larger than the former.

445 Second, we consider the changes caused by increased CO₂, both for the formation and the
446 final breakdown of the boreal polar vortex: these display robust changes across models. The
447 polar vortex forms earlier and persists for longer in the abrupt4xCO₂ scenario than in the
448 piControl runs (Fig. 6a and b). This signal is particularly clear, and is significant in all models in
449 the case of the vortex formation. Although half of the models do not show a significant change,
450 there is a clear consensus in the sign of the SFW change across these models.

451 Interestingly, the models with the largest delay of SFW in the abrupt4xCO₂ simulation
452 (CanESM5, HadGEM3.GC31-LL and IPSL-CM6A-LR) are also those with the largest reduction
453 in the frequency of SSWS. This indicates that the long persistence of the vortex is related to a
454 stronger and colder vortex during the extended winter, rather than to the effect of SSWs on the
455 SFWs timing suggested by Hu et al. [2014]. We hypothesize that the year-round radiative effect
456 of CO₂, which is associated with a warming tropical upper troposphere and a cooling
457 stratosphere, increases the upper-level meridional temperature gradient and leads to a longer-
458 lived polar vortex. Why this influence occurs primarily in early fall and spring may be tied to the
459 seasonality of the upper tropospheric warming [Harvey et al. 2013], and the dynamical driving of
460 the polar vortex. Indeed, the wave activity is typically weaker during the transition season
461 (particularly in Autumn) than in mid-winter [Kodera et al., 2003], explaining the dominance of
462 the radiative effect of increased CO₂ on the stratosphere in the former metric. In sum, models
463 predict an increase of around 30 days of westerly winds in the abrupt4xCO₂ simulations, a
464 substantial increase in the time of the year over which stratospheric variability is active and can
465 couple with the troposphere.

466 A similar analysis has been performed for the SH. Because planetary wave activity is
467 much weaker in the SH than in the NH [Andrews et al. 1987], radiative CO₂ forcing dominates
468 the SH polar vortex response to increasing CO₂ concentrations and so, causes a robust
469 strengthening. In many models the extreme CO₂ concentrations prevent the polar vortex from
470 disappearing at all during austral summer, leading to perpetual westerly conditions in the
471 stratosphere, so we do not show the results for the abrupt4xCO₂ simulation. The distribution of
472 SFW dates for piControl and historical simulations are displayed in Figure 6c. Unlike in the NH,
473 the distribution of SFWs in the SH already shifts towards a later date in the historical period with
474 respect to the piControl conditions. Although the attribution of changes in the length of the
475 winter season to CO₂ is complicated, ozone depletion in austral spring over the historical period
476 might be responsible, based on previous literature [e.g. McLandress et al. 2010; Oberländer-
477 Hayn et al. 2015].

478



479

480 **Figure 6.** Box plots showing the distribution of dates of (a) polar vortex formation and (b)
 481 stratospheric final warming in the Northern Hemisphere for the piControl (blue), historical
 482 (green) and abrupt-4xCO₂ (red) simulations for all models and JRA-55 reanalysis. (c) Same as
 483 (b) but for the Southern Hemisphere and only in piControl and historical runs. The interquartile
 484 range is represented by the size of the box and the inside line (black cross) corresponds to the
 485 median (mean). Whiskers indicate the maximum and minimum points in the distribution that are
 486 not outliers. Outliers (red crosses) are defined as points with values greater than 3/2 times the
 487 interquartile range from the ends of the box.

488

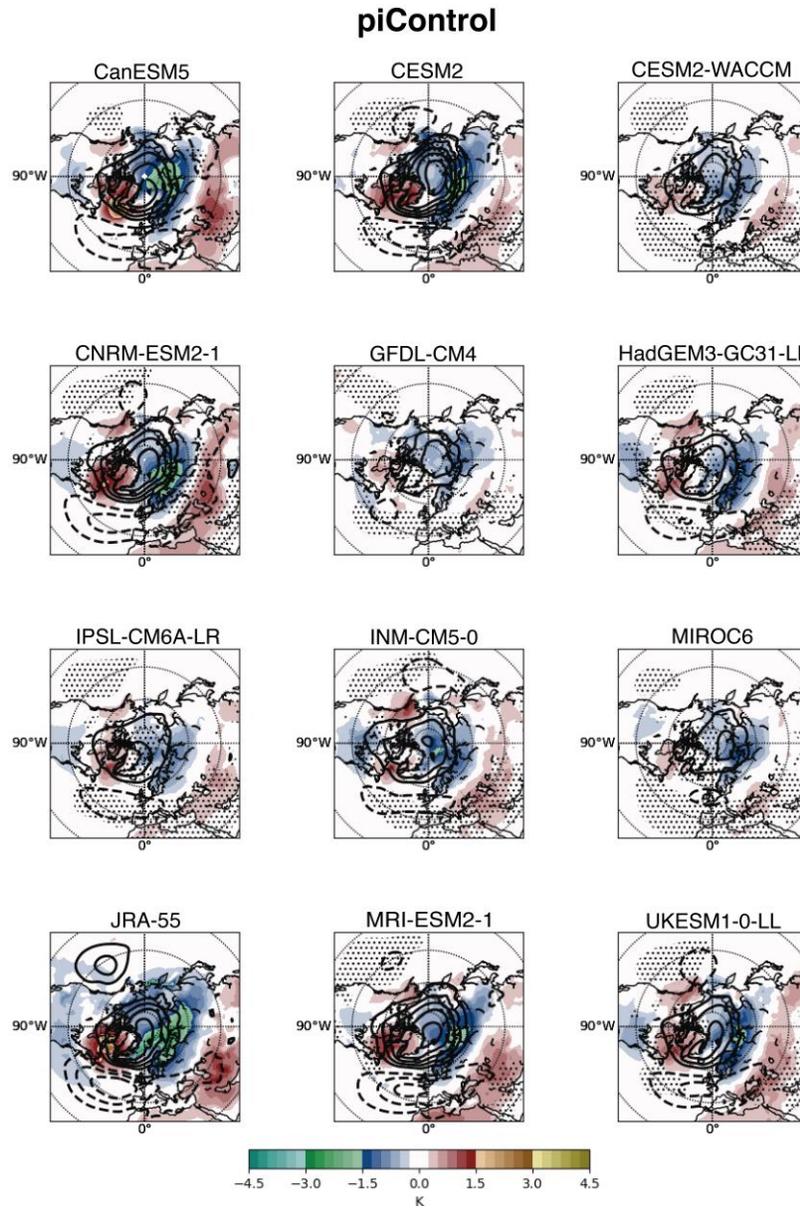
489 **6 Future changes in the surface impact of SSW events**

490 6.1 Surface response to SSW events

491 In addition to changes in SSW frequency, amplitude and seasonality, it is also
492 conceivable that the surface impact of SSW events might change as a consequence of increased
493 CO₂. While detailed quantitative description of the mechanism for coupling between SSW events
494 and surface remains elusive, there is now a large body of evidence quantifying the amplitude and
495 spatial structure of the surface pressure and temperature responses following SSW events [e.g.,
496 Baldwin and Dunkerton, 2001; Polvani et al. 2017; Butler et al. 2017]. A number of studies point
497 to the importance of eddy-jet feedbacks in determining this surface response [e.g.: Kushner and
498 Polvani, 2004; Song and Robinson, 2004; Garfinkel et al. 2013;]. It is therefore plausible that
499 together with changes in the position and variability of the extra-tropical jet caused by CO₂
500 increases, one might be able to detect changes in the surface response following SSW events.

501 To test this idea, we analyze first composite maps of anomalous surface temperature and
502 sea-level pressure (SLP) for the period 15-60 days after SSWs in the piControl simulation (Fig.
503 7). In nearly all models we obtain the typical SLP and surface temperature patterns following
504 SSWs that are also detected in reanalysis (although CO₂ forcing is different), i.e., negative
505 Northern Annular Mode pattern (particularly over the pole), and Eurasian cooling and
506 Northeastern American warming. None of the models produce a positive SLP anomaly that can
507 be found in the JRA55 composite though. Despite the relatively structural similarities across
508 models, the amplitude of the response can vary by a factor of two or three between them. The
509 amplitudes in five of the eleven models (CESM2-WACCM, GFDL-CM4, HADGEM3-GC31-
510 LL, IPSL-CM6A-LR, and MIROC6) are too weak. The amplitude does not correlate with the
511 SSW frequency. The large SSW sample size from the piControl simulations means that the
512 estimates of surface impact are very robust.

513 Secondly, we compare the SLP pattern after SSWs in the abrupt4xCO₂ and piControl
514 simulations (Fig. 8, differences in SLP between both runs are shown in shading). The overall
515 SSW signal in SLP appears unchanged between the piControl and abrupt4xCO₂ simulations,
516 except in three models (CESM2, HadGEM3-GC31-LL IPSL-CM6A-LR) that produce a
517 significantly stronger Northern Annular Mode-like response. However, in the Pacific basin there
518 are some indications about a potential more general change due to a higher CO₂ loading. Indeed,
519 six of the ten models exhibit a statistically stronger negative SLP anomaly in that area under
520 abrupt4xCO₂ forcing than in the piControl runs.

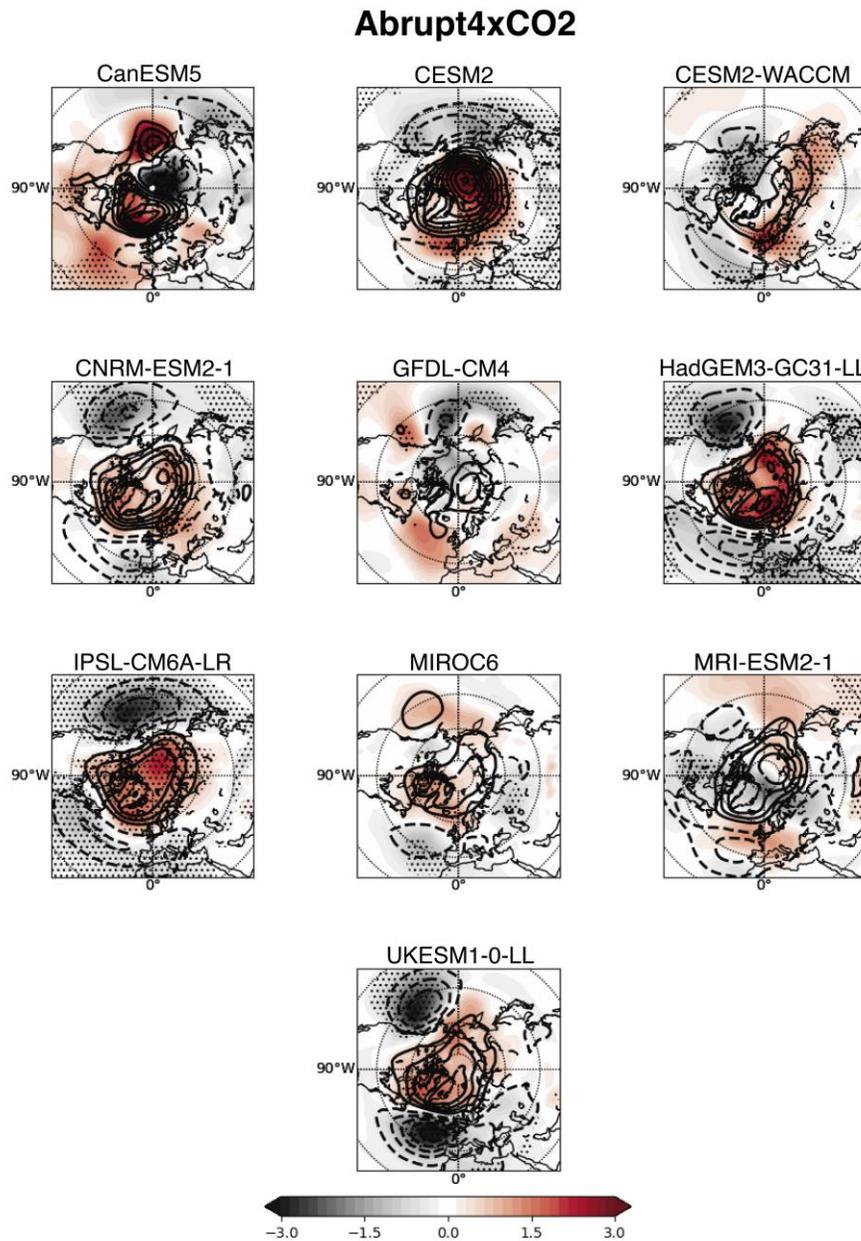


521

522 **Figure 7.** Composite maps of anomalous SLP (contour interval 1hPa) and 2m temperature
 523 (shading) for 15/60 days after SSWs in piControl simulation and JRA-55 reanalysis (bottom
 524 left). Stippling indicates stat. significant differences in SLP from JRA-55 reanalysis at the 95%
 525 confidence level.

526

527



528

529 **Figure 8.** Abrupt4xCO₂-minus-piControl composite maps of anomalous SLP (shading, hPa) for
 530 15/60 days after SSWs. Anomalous SLP after SSWs in the abrupt4xCO₂ run is shown in
 531 contours (interval: 1hPa). Stippling indicates stat. significant differences from piControl run at
 532 the 95% confidence level.

533

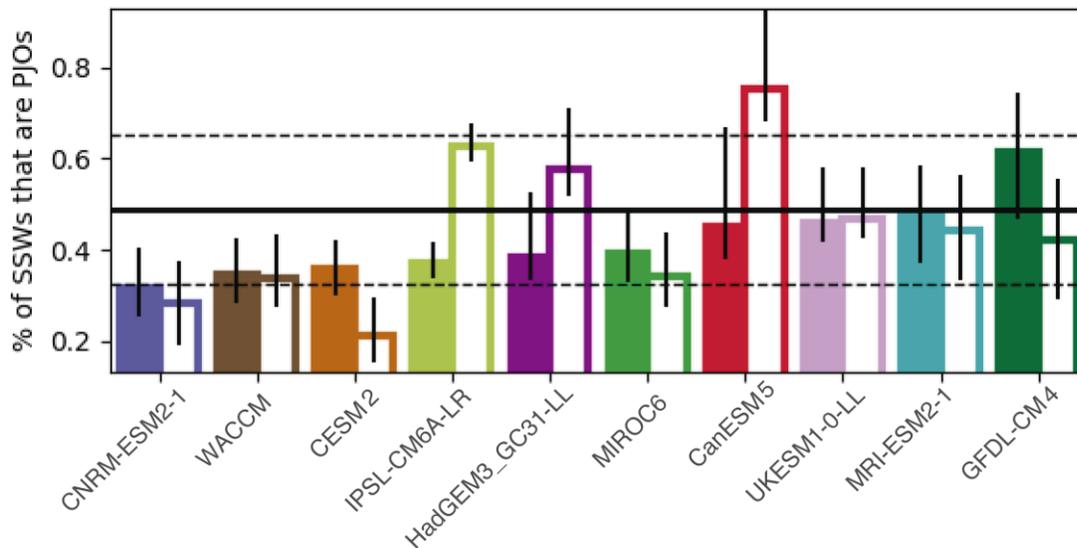
534 6.2 Polar-night Jet Oscillation events

535 In this subsection we focus on specific events (PJO events) that are closely related to
 536 SSWs and to the stratosphere-troposphere coupling [Hitchcock et al. 2013]. As indicated in the

537 Introduction section, their strong and persistent tropospheric response explains the interest in
 538 investigating possible changes in the occurrence of these events for increasing CO₂
 539 concentrations.

540 First, examining the surface response to PJOs in the piControl experiment (Fig. S1)
 541 confirms that these events in models have a stronger signal in the troposphere than all SSWs too.
 542 In JRA-55 roughly half of all SSWs are associated with a PJO event (PJO SSW) (solid bars in
 543 Fig. 9). Five models include the JRA-55 value of the ratio of PJO SSW events in their
 544 confidence interval in the piControl simulations (MRI-ESM2-0, UKESM1-0-LL, CanESM5,
 545 HadGEM3-GC31-LL and GFDL-CM4). The other models underestimate this fraction. However,
 546 we do not find a clear relationship between this fraction and the amplitude of SLP pattern
 547 following SSWs. For instance, HadGEM3-GC31-LL and GFDL-CM4 simulate a very weak SLP
 548 pattern, but the ratio of PJO SSWs is close to observations or even larger (Fig. 7).

549 In the future, similarly to changes in SSW frequency, there is no robust response of PJO
 550 SSWs across models to increasing CO₂ (Fig. 9). Roughly half of the models show a decrease and
 551 half of them an increase in PJO SSW events between the piControl and abrupt4xCO₂
 552 simulations. More interestingly, two of the three models with a stronger Northern Annular
 553 Mode-response to SSWs in the abrupt4xCO₂ run (IPSL-CM6A-LR and HadGEM3-GC31-LL)
 554 display an increase in this subset of SSWs too. The other one (CESM2) shows a significant
 555 decrease in the fraction of SSWs that are PJOs. Nevertheless, given the low number of models, it
 556 is difficult to make a direct link between changes in the number of PJO SSWs and stronger SSW
 557 coupling to the surface under increased CO₂ loading.



558

559 **Figure 9.** Fraction (%) of SSWs that are also PJO events in piControl (solid bars) and
 560 abrupt4xCO₂ (open bar) runs. Horizontal black solid and dashed line correspond to the mean
 561 value and the 2.5th-97.5th percentile range in JRA-55 reanalysis, respectively. Error bars are
 562 based on bootstrapping

563

564

565 7 Conclusions

566 SSWs are the primary dynamical event in the wintertime polar stratosphere and have
 567 clear impacts on the tropospheric circulation on sub-seasonal to seasonal timescales. This study
 568 takes advantage of the new sets of simulations available through the DynVarMIP sub-project of
 569 CMIP6 to revisit a number of questions about how SSW events and the stratospheric seasonal
 570 cycle might respond to quadrupled CO₂ concentrations. In comparison with previous rounds of
 571 CMIP and comparisons made as part of the CCMVal and CCMI projects, the new simulations
 572 provide significant advances in our ability to study SSWs. In particular, the long piControl runs
 573 and the availability of daily data of abrupt4xCO₂ simulations from a large number of high-top
 574 models is unprecedented.

575 From our analysis of the twelve models for which sufficient daily time resolution
 576 stratospheric data was available, these conclusions can be drawn about the impact of extreme
 577 CO₂ concentrations on SSW events:

- 578 • There is no consensus among models on the sign of changes in SSW frequency.
- 579 • It is, however, possible to say with confidence that many models predict that SSW
 580 frequency is sensitive to increase in CO₂ forcing.
- 581 • There is no change to the impact of SSW events in the N. Atlantic between the
 582 abrupt4xCO₂ and piControl simulations. In the N. Pacific, there is some indication that
 583 under large CO₂ forcing there will be a larger mean response to SSW events.
- 584 • With the exception of MRI-ESM-2-0, predicted trends in SSW frequency are small
 585 relative to natural variability (as characterized by the piControl simulations of each
 586 model). This is not to say that SSW changes are themselves small (three models predict
 587 frequency changes of more than a factor of two compared to piControl conditions) but
 588 more a reflection of the large, natural decadal variability in SSW occurrence. As such,
 589 changes in SSW frequency are unlikely to be observed until the end of the 21st century.
- 590 • Robust changes to the seasonal cycle in the stratosphere are predicted by all models. The
 591 stratospheric polar vortex is likely to form earlier and be destroyed later in the future.
 592 This extends the season in which the stratosphere can actively couple to the troposphere
 593 and influence surface weather.
- 594 • There is no evidence of an increased likelihood of major SSWs in the SH in the future.

595 These results underscore the conclusions of a number of previous studies of SSW events
 596 and also motivate the need for more detailed understanding of the stratospheric momentum
 597 budget in models as advocated by, for example, Wu et al. [2019], which is now possible with the
 598 simulations available through DynVarMIP. Similarly, developing an understanding of how both
 599 model formulation and resolution and ECS might influence dynamical sensitivity in the
 600 stratosphere remains an important but unsolved challenge for the stratospheric dynamics
 601 community.

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 621 the ESGF archive on the following website: <https://esgf-node.llnl.gov/projects/cmip6/>. The
 622 Japanese 55-year Reanalysis (JRA-55) project was carried out by the Japan Meteorological
 623 Agency (JMA). JRA-55 data were accessed through NCAR- UCAR Research Data Archive
 624 (<https://rda.ucar.edu>).

625

626 **Appendix 1: Statistical framework**

627 Statistical methodology for comparing SSW frequency

628 *Parametric method*

629 To compare the frequency of SSW events in two models or between a model and
 630 observations, it can be assumed that each data sample is a Poisson process with an annual rate λ_i .
 631 The difference between the intensity of the two processes Δ_λ is given in equation (1)

$$632 \quad \Delta_\lambda = \frac{(\lambda_0 - \lambda_1)}{\sqrt{\frac{\lambda_0}{N_0} + \frac{\lambda_1}{N_1}}} \quad (1)$$

633 This can be modeled with a normal distribution providing the frequency of observed events is
 634 greater than 30 [Charlton et al. 2007]. This approach has been widely used in the literature.

635 An alternative approach that compares the ratio of the rate of the two Poisson processes
 636 has been studied by Gu et al. [2008].

$$637 \quad H_0: \lambda_0/\lambda_1 = 1 \quad \text{against} \quad H_A: \lambda_0/\lambda_1 \neq 1 \quad (2)$$

638 Gu et al. [2008] suggest that a conservative test statistic with high power is the one
 639 suggested by Huffman [1984] (here X_i is the number of SSWs in each dataset and $\rho = t_0/t_1$ the
 640 ratio of the length of observation of the two processes):

$$641 \quad W(X_0, X_1) = \frac{2[\sqrt{X_0+3/8} - \sqrt{\rho(X_1+3/8)}]}{\sqrt{1+\rho}} \quad (3)$$

642 The p-value for this statistic is estimated as in equation (4), where Φ is the cumulative
 643 distribution function of the standard normal and the observed value of the test statistic
 644 $W(X_0, X_1) = w(x_0, x_1)$:

$$645 \quad p = 1 - 2 * \Phi(w_j(x_0, x_1)) \quad (4)$$

646 This is the parametric test statistic used to compare SSW frequency. In addition to
 647 calculating the p-value of any test statistic it is also useful, a priori, to estimate the statistical
 648 power of any testing framework. Tests with high statistical power minimize the likelihood of
 649 Type-II errors (i.e. that the null hypothesis is not rejected when it is, indeed, false). For the test
 650 statistic described above, we estimated the statistical power for a comparison with observations
 651 of 60 winters with an SSW frequency of 0.6. Assuming a p-value of 0.05, the statistical power of
 652 the test is high (above 0.8) for model integrations of more than 100 winters (the null hypothesis
 653 will be rejected with a probability above 0.8) which is the case for all comparisons in this study
 654 apart from the comparison between the historical simulations and the JRA-55 re-analysis. In this
 655 later case, the power of the test is low only for cases in which the observed and modelled SSW
 656 frequency is very similar (i.e. for model SSW frequencies of 0.2 and 1 SSW per year, the power
 657 is greater than 0.8).

658

659 *Bootstrapping method*

660 As an alternative to the parametric test, we can also construct a bootstrapping test as
 661 outlined by Boos [2003]. We assume that there are two sets of independent samples of the
 662 number of SSW events in each season $\{X_1, \dots, X_m\}$ and $\{Y_1, \dots, Y_n\}$. To determine the confidence
 663 interval for the difference of mean frequency of the two sets $\mu_x - \mu_y$ two samples (of equal size
 664 to the original samples) are drawn from the pooled observation set $\{X_1, \dots, X_m, Y_1, \dots, Y_n\}$, with
 665 replacement. The p-value of the true observation is calculated as the number of bootstrap
 666 samples with an absolute difference greater than the true value. In all cases, 10,000 bootstrap
 667 sample are drawn.

668 This bootstrapping technique was also applied to determine the confidence intervals on
 669 the seasonal distribution of SSW frequency. We choose to perform the bootstrapping on
 670 individual winters over a block bootstrapping approach to increase the sample size available for
 671 models that have a limited length of piControl simulation available. We have, therefore, assumed
 672 that there is no autocorrelation from one winter to the next, but comparison with a block-
 673 bootstrapping approach for the models that have long piControl simulations produced similar
 674 uncertainty ranges (not shown), indicating that this assumption is reasonable. For Figure 2, the
 675 uncertainty range is derived from the piControl simulation. Since there are 57 years in the JRA55
 676 record, we resample 57 years from the piControl simulation, with replacement and recalculate
 677 the SSW distribution, normalized by the number of SSWs in that sample. This is repeated 1000
 678 times and the uncertainty range shows the 2.5th to 97.5th percentile range of these 1000 samples
 679 (95% confidence interval) i.e., this is the uncertainty range from the model with an equivalent
 680 number of years to that of the observations.

681

682 Trend in SSW frequency and Time of Emergence

683 Analogously to the method of Hawkins and Sutton [2012] the time of emergence of a
 684 ‘signal’ in the frequency of SSW events is estimated by comparing the size of the trend in SSW
 685 frequency in the 1pctCO2 simulations with the ‘noise’ determined from the piControl simulation
 686 of the same model.

687 To calculate the signal term in each integration, a Generalized Linear Model fit to the
 688 data with a logarithmic link function, implemented in R is used. Trend estimates for decadal
 689 SSW frequency in the 1pctCO2 simulations. Modification to the method following
 690 (<https://stats.idre.ucla.edu/r/dae/poisson-regression/>) to account for cases with mild violation of
 691 the Poisson distribution in the models is included. The resulting regression equation is of the
 692 form:

$$693 \quad F_{SSW}(t) = e^{\beta_0 + \beta_1 t} \quad (5)$$

694 Trend terms are expressed as a fractional multiplier of the count per decade. Due to the low mean
 695 annual frequency of SSW events, the noise on annual mean frequency estimates is large,
 696 therefore when estimating trends in SSW frequency and time of emergence we consider the
 697 decadal mean SSW frequency. This means that time of emergence calculations are limited to the
 698 decade of emergence.

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