

1 **Impacts of Carbonate Buffering on Atmospheric Equilibration of CO₂,**
2 **$\delta^{13}\text{C}_{\text{DIC}}$, and $\Delta^{14}\text{C}_{\text{DIC}}$ in Rivers and Streams**

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8
9 **Key Points:**

- 10
11 • We develop models of stream CO₂ degassing that include carbonate buffering and apply
12 across a range of alkalinities and stream processes
13 • Carbonate buffering can support significant contributions to stream CO₂ fluxes but
14 cannot support elevated downstream CO₂ concentrations
15 • Stable and radio- carbon isotopes are highly impacted by carbonate buffering and can be
16 leveraged to partition carbon sources

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25 **Abstract**

26
27 Rivers and streams play an important role within the global carbon cycle, in part through
28 emissions of CO₂ to the atmosphere. However, the sources of this CO₂ and their spatiotemporal
29 variability are difficult to constrain. Recent work has highlighted the role of carbonate buffering
30 reactions that may serve as a source of CO₂ in high alkalinity systems. In this study, we seek to
31 develop a quantitative framework for the role of carbonate buffering in the fluxes and
32 spatiotemporal patterns of CO₂ and the stable and radio- isotope composition of dissolved
33 inorganic carbon (DIC). We incorporate DIC speciation calculations of carbon isotopologues
34 into a stream network CO₂ model and perform a series of experiments, ranging from the
35 degassing of a groundwater seep to the simulation of 5th-order stream network. We find that
36 carbonate buffering reactions contribute >60% of emissions in high-alkalinity, moderate GW-
37 *p*CO₂ environments that may characterize carbonate bedrock systems. However, atmosphere
38 equilibration timescales of *p*CO₂ are minimally affected, which contradicts hypotheses that
39 carbonate buffering maintains high *p*CO₂ across Strahler orders in high alkalinity systems. In
40 contrast, alkalinity dramatically increases isotope equilibration timescales, which significantly
41 complicates isotopic methods of CO₂ source partitioning by decoupling *p*CO₂ from isotopic
42 composition even under low alkalinity. Based on similar impacts on atmospheric equilibration
43 for stable and radio- carbon isotopologues, we develop a quantitative method for distinguishing
44 groundwater from stream corridor CO₂ sources in carbonate-dominated watersheds. Together,
45 these results provide a framework to guide fieldwork and interpretations of stream network CO₂
46 patterns across variable alkalinities.

47 48 **Plain Language Summary**

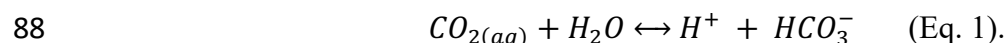
49
50 Streams emit a lot of carbon dioxide (CO₂) to the atmosphere, but it is difficult to figure out
51 where the CO₂ originates. One source is a chemical reaction called carbonate buffering, which
52 happens between different forms of dissolved carbon. This reaction may be important in streams
53 with high alkalinity, but we lack knowledge about how it contributes across different alkalinities
54 and scales. Some studies use isotopes of carbon to trace where CO₂ comes from and how it is
55 released, but we lack knowledge about how carbonate buffering affects isotope patterns. Here,
56 we create mathematical models of CO₂ is production and release including isotopes in streams.
57 Our findings show that carbonate buffering can be a significant source of CO₂ in streams with
58 high alkalinity. However, it doesn't keep CO₂ levels consistently high downstream, as studies
59 previously suggested. Conversely, carbonate buffering has a big effect on patterns of carbon
60 isotopes. This means that common isotope methods for identifying carbon sources streams don't
61 work well. Instead, we propose a way to use stable and radioactive carbon isotopes together to
62 determine the sources of carbon. Our study aims to guide future work and help understand how
63 carbonate buffering impacts CO₂ patterns across stream environments.

64 65 **1. Introduction**

66
67 Rivers and streams are increasingly recognized as integral components of the terrestrial carbon
68 cycle (Cole et al., 2007; Drake et al., 2018; Raymond et al., 2013), through which CO₂ produced
69 both in the terrestrial subsurface and within stream corridor environments is released to the
70 atmosphere (e.g. Hotchkiss et al., 2015). Current estimates suggest global CO₂ emissions from

71 inland waters are roughly half as large as anthropogenic emissions and comparable the net
72 terrestrial carbon sink (DelSontro et al., 2018; Friedlingstein et al., 2022; Gómez-Gener et al.,
73 2021; Lauerwald et al., 2023; Raymond et al., 2013; Sawakuchi et al., 2017); thus, the ability to
74 quantify the magnitude and variability of these fluxes is necessary for gauging terrestrial climate
75 feedbacks. Despite their importance in the terrestrial carbon cycle, the relative balance of CO₂
76 sources that support carbon fluxes to the atmosphere, which include soil respiration, subsurface
77 chemical weathering reactions, hyporheic zone respiration, and net water-column respiration,
78 remains uncertain. More recently, studies have shown the potential role of carbonate buffering
79 reactions to contribute to evasion fluxes and spatial patterns of stream *p*CO₂ (Duvert et al., 2019;
80 Kirk & Cohen, 2023; Stets et al., 2017; Wang et al., 2021). Crucially, these buffering dynamics
81 are not typically included in stream carbon budgets and may represent an overlooked aspect of
82 terrestrial-aquatic carbon cycling.

83
84 Carbonate buffering reactions are historically well-described within the ocean carbon literature
85 (Broecker et al., 1979; Revelle & Suess, 1957); however, relatively few studies have investigated
86 these dynamics in terrestrial water systems where alkalinity and dissolved CO₂ concentrations
87 vary by orders of magnitude. Briefly, dissolved CO₂ is subject to the reaction,



89 This reaction on its own does not alter alkalinity, and essentially acts to ‘store’ dissolved CO₂ at
90 levels above what would be predicted using Henry’s law alone. Conceptually, the role of this
91 CO₂ ‘storage’ can be demonstrated through the application of Le Chatelier’s principle, by which
92 a reaction will occur to partially negate any changes to a system: (1) as dissolved CO₂
93 concentrations increase, for example as rainfall equilibrates with soil environment *p*CO₂ during
94 infiltration, this causes Eq. 1 to move from left to right, ‘storing’ CO₂ in the form of HCO₃⁻ + H⁺;
95 (2) when CO₂ concentrations decrease, for example as groundwater enters streams and
96 equilibrates with the atmosphere, Eq. 1 moves from right to left, acting to replenish dissolved
97 CO₂ concentrations as degassing proceeds. Importantly, the amount of CO₂ that can be ‘stored’
98 in this manner increases with increasing alkalinity (Broecker et al., 1979; Revelle & Suess,
99 1957).

100
101 These storage dynamics have been shown to operate within stream systems, and particularly in
102 those with high alkalinity. In a compilation of US stream data, Stets et al. (2017) showed that
103 diurnal changes in dissolved CO₂ reflecting stream metabolism are smaller than diurnal DIC
104 changes, and that this difference increases with higher stream alkalinity. This effect leads to
105 temporal hysteresis in CO₂:O₂ ratios as DIC concentrations take longer to adjust than O₂ to
106 changing metabolic rates. Further, Stets et al. (2017) suggest that this effect may be responsible
107 for observations of high downstream *p*CO₂ in high alkalinity streams despite significant
108 degassing during downstream transport. These buffering reactions may also contribute
109 significantly to total stream emissions (e.g. Kirk & Cohen, 2023); for example, Duvert et al.
110 (2019) found that up to 60% of emissions were supported by carbonate buffering at some
111 locations within a high alkalinity, tropical Australian river system.

112
113 Carbonate buffering dynamics also impact the evolution of carbon isotopes in DIC (e.g.
114 Venkiteswaran et al., 2014), both in terms of stable carbon ratios (δ¹³C) and radiocarbon ratios
115 (Δ¹⁴C); however, these effects have not been explored in detail within stream and river systems.
116 Stable carbon isotopes are frequently used to partition DIC sources, as respired organic carbon,

117 DIC from carbonate mineral weathering, and atmospheric CO₂ have distinct isotope
 118 compositions (e.g. Campeau et al., 2017, 2018; Polsenae & Abril, 2012). Further, the evolution
 119 of δ¹³C values along stream reaches may provide information on degassing rates as ¹²C is
 120 preferentially lost to the atmosphere, reflecting both kinetic fractionation of diffusion and
 121 equilibration with atmospheric CO₂ which often has a higher δ¹³C_{CO₂} value than stream waters.
 122 Measured Δ¹⁴C_{DIC} values may also be used to partition DIC sources via their age characteristics
 123 (Cole et al., 2022; Sveinbjörnsdóttir et al., 2020). For example, respiration of modern organic
 124 matter represents near-atmospheric Δ¹⁴C values, while respiration of geogenic organic carbon
 125 and weathering of carbonate rock results in low Δ¹⁴C values. The distances over which Δ¹⁴C
 126 equilibrates with the atmosphere and how carbonate buffering reactions impact this equilibration
 127 have not, to our knowledge, been investigated; however, we hypothesize that these dynamics are
 128 crucial in shaping Δ¹⁴C patterns in streams and in determining CO₂ sources.

129
 130 Here we develop a parsimonious model to investigate how carbonate buffering reactions impact
 131 atmospheric equilibration of river and stream DIC pools in terms of overall CO₂ fluxes and
 132 equilibration timescales. While this investigation is model-based, the thermodynamic principles
 133 that underlie these equations have been long-established. Rather than a direct model-observation
 134 comparison, these model experiments are used to develop a generalizable framework to better
 135 conceptualize the role of carbonate buffering in terrestrial-aquatic carbon cycling and guide
 136 sampling strategies and data interpretation schemes across a broad range of environments.

137

138 2. Methods

139

140 2.1 Carbonate System Geochemistry

141

142 To model the speciation of DIC in terrestrial streams and rivers, we incorporate reactions
 143 representing the dissolution of CO₂ gas in water, the dissociation of CO_{2(aq)} (defined here as
 144 equivalent carbonic acid, H₂CO_{3(aq)}), and the dissociation of bicarbonate as applied separately to
 145 ¹²C, ¹³C, and ¹⁴C DIC species. These reactions and their associated equilibrium constants at 25° C
 146 are shown in Table 1, and are based on the methodology of Druhan et al. (2021). Briefly for a
 147 given reaction *x*, the ratio of equilibrium constants (*K_x*) for DIC isotopologues sets the
 148 equilibrium fractionation factor as,

$$149 \quad \alpha_x = \frac{K_x^i}{K_x^{12}} \quad (\text{Eq. 2}),$$

150 where *i* represents either ¹³C or ¹⁴C versions of reaction *x*. We use the equilibrium constants of
 151 Druhan et al. (2021) for ¹³C and ¹⁴C assuming that fractionation factors are doubled for ¹⁴C
 152 relative to ¹³C based on their relative mass differences with ¹²C.

153

154 2.2 Evolution of the carbonate system during degassing

155

156 To model the evolution of stream DIC concentrations and isotopic composition during
 157 degassing, we simulate three distinct scenarios of increasing complexity:

158

- 159 ○ Scenario 1: A groundwater seep degassing with no additional CO₂ inputs
- 160 ○ Scenario 2: A groundwater seep degassing with ongoing groundwater inputs and net
 161 respiration during downstream transport

- 162 ○ Scenario 3: An 87 km² watershed river network in Gothic, CO for which we have
 163 previously developed and validated a reactive transport model incorporating
 164 groundwater inputs, water-column net respiration and hyporheic zone CO₂ sources.
 165

166 These scenarios and the processes incorporated into each are diagrammed conceptually in Fig. 1.

167

168 2.2.1 Scenario 1: Groundwater degassing with no additional sources

169

170 In Scenario 1, we model a groundwater parcel degassing during stream transport with no
 171 additional carbon sources during transport (Fig. 1a). This would correspond physically to a
 172 spring seep with no additional along-stream groundwater inputs or net respiration. In this
 173 scenario, the changes in DIC concentrations are modeled as,

174

$$175 \quad \frac{\partial DIC}{\partial t} = -k_{CO_2}(CO_{2(aq)} - CO_{2(aq)sat}) \quad (\text{Eq. 3}),$$

176

177 where k_{CO_2} is the reaeration coefficient of CO₂, $CO_{2(aq)}$ is the dissolved CO₂ concentration, and
 178 $CO_{2(aq)sat}$ is the theoretical concentration of CO₂ in equilibrium with an atmospheric pCO_2 of 410
 179 ppm.

180

181 We assume an initial DIC value of groundwater (DIC_{gw}) based on a specified groundwater pCO_2
 182 (20,000 ppm) and alkalinity, which ranges in our experiments from 0 – 6 meq/L based on the
 183 range of freshwater stream values from a compilation of United States surface waters (Stets et
 184 al., 2017); the resulting DIC_{GW} is calculated as 0.179 – 6.15 mM depending on alkalinity using a
 185 temperature of 25° C. We additionally specify a k_{CO_2} value (0.05 s⁻¹); however, our analysis
 186 examines CO₂ evolution over a non-dimensional timescale (t^*) calculated as $t^* = (t)(k_{CO_2})$
 187 (unitless); thus, results are scalable to any given k_{CO_2} value. The model is then solved using an
 188 explicit numerical approximation over discretized timesteps. At each timestep following the
 189 calculation of a new DIC value, the carbonate system is speciated using alkalinity and the
 190 updated DIC concentration, following the methods of Venkiteswaran et al. (2014). Briefly, we
 191 develop a system of equations based on the equilibrium constants in Table 1, along with
 192 equations for alkalinity (Alk) and DIC as,

193

$$194 \quad Alk = [HCO_3^-] + 2[CO_3^{2-}] + [OH^-] - [H^+] \quad (\text{Eq. 4}) \text{ and}$$

195

$$196 \quad DIC = [CO_{2(aq)}] + [HCO_3^-] + [CO_3^{2-}] \quad (\text{Eq. 5}), \text{ respectively.}$$

197

198 Model calculation scripts using R software are included in the Supplementary Materials.

199

200 We solve Eq. 3 and speciate the DIC pool separately for each isotopologue of carbon. For
 201 simplicity, we assume that reaeration coefficients are the same for ¹²CO₂, ¹³CO₂, and ¹⁴CO₂.
 202 While molecular diffusion imparts mass-dependent kinetic fractionation (e.g. Zhang et al., 1995),
 203 turbulent atmospheric exchange which dominates in most river systems likely does not. We note
 204 that our equations are flexible to incorporate kinetic fractionation as,

$$205 \quad \alpha_k = \frac{k^i}{k^{12}} \quad (\text{Eq. 6}),$$

206 where i denotes the reaeration coefficient k for either $^{13}\text{CO}_2$ or $^{14}\text{CO}_2$, following the formulation
 207 of Zhang et al. (1995). We also note that within our model simulations, ^{12}C degasses faster than
 208 ^{13}C due to a larger proportional offset between atmospheric and stream $^{12}\text{CO}_2$ concentrations.
 209 This causes apparent fractionation as the stream equilibrates with atmospheric boundary
 210 conditions; however, it does not physically represent kinetic fractionation. We note that these
 211 two processes that cause increasing $\delta^{13}\text{C}$ values during degassing are not often discussed as
 212 separate processes and are typically referred to collectively as fractionation during degassing.

213
 214 We calculate $\delta^{13}\text{C}$ and $\Delta^{14}\text{C}$ values as,
 215

$$216 \quad \delta^{13}\text{C} = \left(\frac{R_{\text{sample}}}{R_{\text{std}}} - 1 \right) * 1000\text{‰} \quad (\text{Eq. 7}), \text{ and}$$

$$217 \quad \Delta^{14}\text{C} = \left(\frac{\left(\frac{^{14}\text{C}}{^{12}\text{C}} \right)_{\text{corr}}}{\left(\frac{^{14}\text{C}}{^{12}\text{C}} \right)_{\text{std}} * \exp\left(\frac{2023-1950}{8267}\right)} - 1 \right) * 1000\text{‰} \quad (\text{Eq. 8}), \text{ where}$$

$$218 \quad \left(\frac{^{14}\text{C}}{^{12}\text{C}} \right)_{\text{corr}} = \left(\frac{^{14}\text{C}}{^{12}\text{C}} \right)_{\text{sample}} \left(\frac{1 + \delta^{13}\text{C}_{\text{std}}/1000}{1 + \delta^{13}\text{C}_{\text{sample}}/1000} \right)^2 \quad (\text{Eq. 9}).$$

219
 220
 221 Within these equations, R_{std} represents the $^{13}\text{C}/^{12}\text{C}$ ratio of the VPDB standard, and $^{14}\text{C}/^{12}\text{C}_{\text{std}}$ is
 222 1.12E-12. Eq. 9 essentially corrects for equilibrium fractionation effects within the ^{14}C system.
 223 In this scenario and across the following sections, we assume an initial GW $\delta^{13}\text{C}_{\text{DIC}}$ value of -
 224 15‰ representing a balance of C_3 soil respiration and carbonate from calcite weathering and
 225 $\Delta^{14}\text{C}_{\text{DIC}}$ value of -500‰ representing a mix of modern soil respiration and ^{14}C -dead carbonate
 226 carbon (Table 1). We also assume that on the timescales of stream transport, radioactive decay of
 227 ^{14}C is negligible.
 228

229 2.2.2 Scenario 2: Groundwater degassing with continuous CO_2 sources

230
 231 In Scenario 2, we incorporate continuous inputs from groundwater inflows and stream corridor
 232 CO_2 production via respiration (Fig. 1b). In this scenario, we amend Eq. 3 to incorporate these
 233 inputs as,
 234

$$235 \quad \frac{\partial \text{DIC}}{\partial t} = -k(\text{CO}_{2(\text{aq})} - \text{CO}_{2(\text{aq})\text{sat}}) + Q(\text{DIC}_{\text{gw}} - \text{DIC}) + F_{\text{prod}} \quad \text{Eq. (10)},$$

236
 237 where Q is the volume-normalized groundwater inflow rate (s^{-1}), and F_{prod} is the net respiration
 238 flux (mol/L/s) which represents a combination of net respiration within the water column along
 239 with hyporheic zone respiration. This method assumes that alkalinity remains constant, ignoring
 240 potential variability in groundwater inflow alkalinities, anaerobic respiration that may contribute
 241 additional alkalinity, and carbonate precipitation which would decrease alkalinity. This situation
 242 is analogous to a homogenous stream reach with active GW inputs. Similar to Scenario 1, we
 243 solve this equation using an explicit numerical scheme across discretized timesteps. The same
 244 methods are applied, whereby at each timestep, a new DIC value is calculated and the DIC
 245 system is speciated based on the Venkiteswaran et al. (2014) scheme. As above, GW is specified
 246

247 with a $p\text{CO}_2$ of 20,000 ppm; $\delta^{13}\text{C}_{\text{DIC}}$ value of -15‰ representing a balance of C_3 soil respiration
 248 and carbonate from calcite weathering; and $\Delta^{14}\text{C}_{\text{DIC}}$ of -500‰ representing a mix of modern soil
 249 respiration and ^{14}C -dead carbonate carbon. Stream corridor respiration is assumed to have a
 250 $\delta^{13}\text{C}_{\text{DIC}}$ value of -27‰ and $\Delta^{14}\text{C}_{\text{DIC}}$ of -66‰ representing modern carbon. As in Scenario 1, we
 251 vary alkalinity across our simulations from 0 – 6 meq/L, though for simplicity we include only
 252 0.1, 1.0, and 4.0 meq/L simulations in the main text. We also vary input flux rates as 10^{-7} (low),
 253 10^{-6} (med), and $10^{-5.5}$ (high) mol/L/s and the ratio of input fluxes from GW versus stream
 254 corridor respiration with ratio values of 0.001 (99.9% GW), 1 (equal contributions), and 1000
 255 (99.9% stream corridor respiration).

256

257 2.2.3 Scenario 3: Stream Network CO_2 Model

258

259 Finally, to explore the complexity of alkalinity controls on stream network-scale CO_2 and isotope
 260 dynamics, we incorporate DIC speciation reactions into an existing stream network advection-
 261 reaction model of dissolved CO_2 (Fig. 1). This model was originally developed, applied, and
 262 validated for the East River watershed in Gothic, CO, USA (Saccardi & Winnick, 2021). Briefly,
 263 the East River watershed is an 87 km^2 , high elevation, mountainous watershed, with annual flow
 264 dominated by spring snowmelt (Winnick et al., 2017). In this model, we consider CO_2 fluxes
 265 from: (1) groundwater with a specified $p\text{CO}_2$ and inflow fluxes that scale with changes in
 266 upstream accumulating area and specified runoff values reflecting flow conditions from August,
 267 2019; (2) hyporheic exchange parameterized using a surface renewal-theory mass-transfer model
 268 (Grant et al., 2018; Winnick, 2021) and assuming a constant offset between hyporheic zone and
 269 stream CO_2 meant to reflect net respiration; (3) water column net respiration at a specified
 270 volume-normalized rate; and (4) atmospheric exchange in which gas exchange velocities (k_{600})
 271 are parameterized based on slope and discharge via empirical correlations between energy
 272 dissipation rates and k_{600} (Ulseth et al., 2019). The full details of model derivation and
 273 parameterization are presented in Saccardi and Winnick (2021), and the simulated map of stream
 274 $p\text{CO}_2$ values is shown in Fig. 1. Here, we update the model and simplify a number of model
 275 parameterizations as: (1) here, we ignore wetland contributions and assume all groundwater
 276 sources have the same $p\text{CO}_2$ across the watershed, as opposed to our original model which
 277 specified high $p\text{CO}_2$ values from wetland areas; (2) we ignore snow-plugs which were
 278 introduced into the model as zones with no atmospheric gas exchange to match field
 279 observations. For simplification, we assume a single groundwater alkalinity value for the whole
 280 watershed, and that stream-corridor respiration does not alter alkalinity, ignoring, for example,
 281 alkalinity contributions from anaerobic respiration. Finally, we update the underlying model
 282 equations to incorporate DIC speciation as,

283

$$284 \frac{\partial \text{DIC}}{\partial t} = -v \frac{\partial \text{DIC}}{\partial x} - k(\text{CO}_{2(aq)} - \text{CO}_{2(aq)sat}) + Q(\text{DIC}_{gw} - \text{DIC}) + F_{wc} + k_{hz} * C_{hz} \quad \text{Eq.}$$

285 (11),

286

287 where v is advection velocity (m/s), x is distance along stream (m), F_{wc} is the water column net
 288 respiration flux ($ER - GPP$; mol/L/s), k_{hz} is the rate of hyporheic exchange (s^{-1}), and C_{hz} is the
 289 offset between stream and hyporheic zone DIC (mol/L). This model is applied to NHD HR
 290 streamlines at sub-reach scales. In this model exercise, we assume steady-state conditions (e.g.
 291 $\partial \text{DIC} / \partial t = 0$), and use a backwards-difference method to solve for changes in DIC spatially
 292 across the stream network. At each new downstream spatial grid, we then use the updated DIC

293 and specified alkalinity value to speciate the DIC system. For modeled cells, we discretize NHD
 294 HR stream flowlines at a 0.5 m spacing.

295

296 We solve the model separately for three alkalinity values: 0, 1 (roughly the average measured
 297 site alkalinity), and 4 meq/L. We assume groundwater $p\text{CO}_2$ of 20,000 ppm in the range of
 298 measured soil values (Winnick et al., 2020), an elevation of hyporheic zone $p\text{CO}_2$ above stream
 299 values of 700 ppm, and an F_{wc} value of 10^{-9} mol/L/s, roughly aligning with optimized values
 300 from the model validation of Saccardi and Winnick (2021). Crucially, our intent here is not to
 301 validate the model against previous field observations, but instead to interrogate how the
 302 carbonate buffering dynamics explored in the idealized Scenario's 1 and 2 may be reflected in
 303 real-world systems. Given previous studies which have shown the importance of carbonate
 304 weathering for generating alkalinity within the East River system (Carroll et al., 2018; Winnick
 305 et al., 2017), we assume end-member isotope compositions from Scenario 2, shown in Table 1.

306

307 3. Results

308

309 3.1 Scenario 1 Results

310

311 The temporal evolution of $p\text{CO}_2$, $\delta^{13}\text{C}_{\text{DIC}}$, and $\Delta^{14}\text{C}_{\text{DIC}}$ for our groundwater degassing
 312 simulations are shown in Fig. 2 across a range of alkalinities. Within these plots, the time axis
 313 (t^*) is non-dimensional, representing the simulation time (s) multiplied by the specified
 314 reaeration rate (s^{-1}); these values are also equivalent to non-dimensional distance, and simulation
 315 time could be scaled to a dimensional distance by multiplying by an advective velocity. As
 316 shown in the top panel, high initial GW $p\text{CO}_2$ values equilibrate with atmospheric values over t^*
 317 timescales of $\sim 5\text{-}40$ (unitless). Higher alkalinity values result in slightly longer equilibration
 318 timescales, as highlighted by the inset, though values eventually approach the same atmospheric
 319 $p\text{CO}_2$ levels. This increase in equilibration timescale is controlled by carbonate buffering
 320 reactions which act to resupply CO_2 as degassing progresses as discussed in Section 1. These
 321 changes in equilibration timescales due to carbonate buffering are relatively muted as compared
 322 to isotopic equilibration.

323

324 In Fig. 2b, $\delta^{13}\text{C}_{\text{DIC}}$ starts at GW values of -15‰ and approach equilibrium with atmospheric
 325 $\delta^{13}\text{C}_{\text{CO}_2}$ values of -9‰ through time. Importantly, the final equilibrated $\delta^{13}\text{C}_{\text{DIC}}$ values vary as a
 326 function of alkalinity. Under low alkalinity conditions, atmosphere-equilibrated $\text{CO}_{2(\text{aq})}$
 327 represents the primary component of DIC, and $\delta^{13}\text{C}_{\text{DIC}}$ values approach atmospheric values of $-$
 328 9‰ . Notably, under no alkalinity conditions, $\delta^{13}\text{C}_{\text{DIC}}$ is slightly elevated above atmospheric as
 329 CO_2 is only $\sim 84\%$ of total DIC. Under high alkalinity conditions, the primary form of DIC is as
 330 HCO_3^- or CO_3^{2-} , which due to equilibrium fractionation are elevated $\sim 9\text{‰}$ above $\text{CO}_{2(\text{aq})}$ values;
 331 thus, the DIC pool approaches $\sim 0\text{‰}$ when equilibrated with the atmosphere. In addition to these
 332 changes in final equilibrated values, alkalinity also strongly impacts the timescales of
 333 equilibration. Under zero alkalinity conditions, isotopic equilibration timescales are comparable
 334 to those of $p\text{CO}_2$. As alkalinity increases, however, $\delta^{13}\text{C}_{\text{DIC}}$ equilibration timescales increase
 335 significantly, with the high alkalinity (6 meq/L) scenario requiring non-dimensional timescales
 336 of >1000 as compared to CO_2 equilibration timescales of >10 .

337

338 Values of $\Delta^{14}\text{C}_{\text{DIC}}$ display similar patterns with a few important differences. First, alkalinity has
339 no impact on final $\Delta^{14}\text{C}_{\text{DIC}}$ values, as the associated equilibrium fractionation is normalized for
340 within Eq. 9. However, as equilibrium fractionation is roughly twice as large for ^{14}C as ^{13}C , a
341 larger initial proportion of ^{14}C is buffered within the $\text{HCO}_3^- + \text{CO}_3^{2-}$ DIC pool; thus, timescales
342 of equilibration are slightly larger.

343
344 In Figure 3, we directly evaluate these timescales of equilibration through the calculation of
345 folding-times of τ^{99} , τ^{90} , and τ^e representing the non-dimensional time required to degas 99%,
346 90%, and ~46% of GW CO_2 , respectively. Figure 3a shows the factor increase in each of these
347 timescales for a given alkalinity compared to a simulation with no alkalinity. Alkalinity has
348 relatively little impact on the τ^{90} and τ^e timescales, though it causes an increase of over 2.5x in
349 τ^{99} in the high alkalinity simulation. Given the nature of our non-dimensional analysis, this factor
350 increase is a scalable result. In other words, for any given combination of reaeration rates, stream
351 velocities, and initial $p\text{CO}_2$ values, this would result in a 2.5x increase in the distance over which
352 a groundwater seep degassed 99% of its CO_2 . Physically, this sensitivity of τ^{99} values
353 demonstrates that the impact of carbonate buffering is highest at near-atmospheric $p\text{CO}_2$,
354 resulting in longer timescales to lose the final 1% of $p\text{CO}_2$. This is visually evident in Figure 2a
355 as the alkalinity curves diverge only as they approach atmospheric values.

356
357 The ratio of isotopic equilibration timescales to $p\text{CO}_2$ equilibration is shown in 3b. Increases in
358 alkalinity result in roughly linear increases in the ratio of these equilibration timescales for τ^{90}
359 and τ^e . In contrast, τ^{99} values plateau above an alkalinity of ~4 meq/L. Importantly, the impacts
360 on equilibration timescales are very similar between $\delta^{13}\text{C}_{\text{DIC}}$ and $\Delta^{14}\text{C}_{\text{DIC}}$, with small variations
361 due to differing equilibrium fractionation factors that result in slight differences in the proportion
362 of ^{13}C v. ^{14}C buffered by the HCO_3^- and CO_3^{2-} pools.

363
364 Lastly for Scenario 1, we calculate the proportion of CO_2 emissions supported by carbonate
365 buffering across a range of alkalinity and GW $p\text{CO}_2$ values, shown in Figure 4. This value is
366 calculated by subtracting the total loss of $\text{CO}_{2(\text{aq})}$ during atmospheric equilibration from total DIC
367 loss during equilibration, normalized by the total DIC loss. Carbonate buffering plays a
368 negligible role in CO_2 emissions when alkalinity is low and GW $p\text{CO}_2$ is high, as both of these
369 conditions result in a smaller proportional storage of CO_2 as $\text{HCO}_3^- + \text{H}^+$. However, under
370 conditions of high alkalinity and low GW $p\text{CO}_2$, carbonate buffering may account for up to 90%
371 of emissions across the alkalinity and $p\text{CO}_2$ values tested. We note that these estimates assume
372 no calcite precipitation. This may become an important factor in high alkalinity systems with
373 available Ca^{2+} , whereby degassing raises the calcite saturation state leading to mineral
374 precipitation and further buffering of $\text{CO}_{2(\text{aq})}$ concentrations.

375 376 *3.2 Scenario 2 Results*

377
378 In Scenario 2, we incorporate continuous GW and net stream corridor respiration fluxes during
379 seep degassing, reflecting more realistic scenarios in which evasion fluxes are partially supported
380 by localized CO_2 sources. The temporal patterns of $p\text{CO}_2$, $\delta^{13}\text{C}_{\text{DIC}}$, and $\Delta^{14}\text{C}_{\text{DIC}}$ are shown in
381 Figure 5 across a range of alkalinities, total CO_2 source fluxes, and ratios of GW to stream
382 corridor sources. Across Figure 4a-c, $p\text{CO}_2$ displays similar patterns to Figure 2. As total CO_2
383 sources increase, steady-state $p\text{CO}_2$ values increase to well above atmosphere-equilibrated

384 values. These elevated $p\text{CO}_2$ values represent a stable balance between specific input fluxes and
 385 evasion rates, which can be calculated by assuming steady-state ($dC/dt = 0$) and rearranging Eq.
 386 10 as,

$$388 \quad CO_{2(aq)steady-state} = \frac{Q(DIC_{gw} - DIC) + F_{prod}}{k} + CO_{2(aq)sat} \quad \text{Eq (12).}$$

389 As steady-state $p\text{CO}_2$ values increase, the effects of alkalinity on degassing patterns becomes
 390 more muted. For example, in Figure 4c, there is little visible difference between the high
 391 alkalinity simulation (4 meq/L) and the low alkalinity simulation (0.1 meq/L). This demonstrates
 392 similar patterns as in Figure 3a, which shows that the impacts of equilibration timescales are
 393 relatively insignificant when evaluated at $p\text{CO}_2$ levels above atmospheric (i.e. τ^{90} and τ^e).
 394 Patterns of $p\text{CO}_2$ are not impacted by the partitioning of fluxes between GW and stream corridor
 395 sources, assuming the total fluxes are the same.

396
 397 Carbon isotope patterns become more complicated when considering multiple sources of
 398 different compositions. This is most clear for $\delta^{13}\text{C}_{\text{DIC}}$ where atmospheric, GW, and stream
 399 corridor respiration all have different sources, versus $\Delta^{14}\text{C}_{\text{DIC}}$ where stream corridor and
 400 atmospheric sources are roughly the same. Broadly, and as demonstrated in Scenario 1, increased
 401 alkalinity results in increasing equilibration timescales or, in this case, steady-state timescales for
 402 both $\delta^{13}\text{C}_{\text{DIC}}$ and $\Delta^{14}\text{C}_{\text{DIC}}$. These steady-state timescales are not significantly impacted by the
 403 magnitude of CO_2 source fluxes or their partitioning between GW and stream corridor
 404 respiration (i.e. comparing the yellow lines within and across the panels). Alkalinity also impacts
 405 the final steady-state value of $\delta^{13}\text{C}_{\text{DIC}}$ for a given CO_2 source flux and partitioning ratio (i.e.
 406 comparing the solid purple curve to the solid yellow curve within a panel), such that low
 407 alkalinity results in a lower $\delta^{13}\text{C}_{\text{DIC}}$ value for a given flux and partitioning ratio of carbon inputs.
 408
 409

410 Across these simulations, steady-state $\delta^{13}\text{C}_{\text{DIC}}$ and $\Delta^{14}\text{C}_{\text{DIC}}$ are also highly sensitive to both the
 411 magnitude of total source fluxes and their partitioning between GW and stream corridor sources.
 412 In the case of $\delta^{13}\text{C}_{\text{DIC}}$, as both GW and stream corridor sources have lower-than-atmospheric
 413 values, increasing CO_2 input fluxes results in a decrease in steady-state values. Further, as
 414 $\delta^{13}\text{C}_{\text{DIC}}$ of stream corridor sources are lower than GW (-27‰ v. -15‰ in these simulations), a
 415 higher proportion of stream corridor sources results in lower steady-state $\delta^{13}\text{C}_{\text{DIC}}$ values.
 416 Comparing across Figure 5d-f, we note a significant degree of equifinality in steady-state $\delta^{13}\text{C}_{\text{DIC}}$
 417 values, whereby different combinations of alkalinity, total CO_2 sources, and source partitioning
 418 can result in similar steady-state $\delta^{13}\text{C}_{\text{DIC}}$ values. Even if alkalinity is constrained, different
 419 combinations of CO_2 sources with different $\delta^{13}\text{C}_{\text{DIC}}$ end-member values can result in the same
 420 steady-state $\delta^{13}\text{C}_{\text{DIC}}$; for example, comparing the 1.0 meq/L All Stream corridor line (green
 421 solid) in Figure 5e with the 1.0 meq/L Equal GW and Stream corridor line (green dashed) in
 422 Figure 5f.

423
 424 The controls of sources on steady-state values are more easily discernible in the $\Delta^{14}\text{C}_{\text{DIC}}$ data,
 425 where values are not sensitive to alkalinity. As we set $\Delta^{14}\text{C}_{\text{DIC}}$ values of stream corridor
 426 respiration to near-atmospheric, stream corridor respiration does not have a significant impact on
 427 $\Delta^{14}\text{C}_{\text{DIC}}$ steady-state values (i.e. comparing the solid lines across panels g-i). Instead, variability
 428 is controlled by the total magnitude of GW CO_2 fluxes, which act as a source of low $\Delta^{14}\text{C}_{\text{DIC}}$ and
 429 draw down steady-state values.

430

431 *3.3 Scenario 3 Results*

432

433 Our previous work evaluated the controls on spatial CO₂ patterns across the East River
434 watershed, CO₂ through comparisons of model simulations and field observations (Saccardi and
435 Winnick, 2021). In this exercise, we compare the results of those simulations, which only
436 represented the CO₂ component of the DIC system (equivalent to a situation with an alkalinity of
437 0), with our updated model. Spatial patterns of CO₂ are shown in the Supplement (SFig.'s 1,3,4)
438 and do not result in significant visual differences in spatial patterns across the watershed as
439 depicted in the inset of Figure 1c. In contrast to our degassing experiments in Scenarios 1 and 2,
440 the full watershed simulation features areas in which *p*CO₂ increases due to inputs (GW and
441 stream corridor respiration) that are locally higher than evasion fluxes. Under these conditions,
442 the inclusion of alkalinity results in lower *p*CO₂ estimates as a proportion of CO₂ inputs is stored
443 as HCO₃⁻ + H⁺. This behavior is equivalent to temporal hysteresis modelled in Stets et al. (2017)
444 for diel metabolic patterns, where CO₂ buildup at night is slower than O₂ depletion. At the
445 watershed scale, there are a comparable number of model cells in which the inclusion of
446 alkalinity results in lower as higher *p*CO₂ relative to no alkalinity (Fig. 7a), with a range of -53 –
447 34 ppm in our 1 meq/L alkalinity simulation. This range increases with increasing alkalinity
448 (SFig.'s 2,5), but the overall pattern is unchanged.

449

450 We demonstrate the primary role of reaeration rate on whether alkalinity results in an increase or
451 decrease in *p*CO₂ through its control on *p*CO₂ buildup versus degassing in Fig. 7b. Here, box
452 plots of model differences for the 1 meq/L simulation are binned by the log of gas exchange
453 velocity. Under low gas exchange velocities, the alkalinity model predicts lower *p*CO₂ values as
454 the buildup of *p*CO₂ results in increased CO₂ 'storage', and only under high gas exchange
455 velocities does the alkalinity model predict higher *p*CO₂ values, equivalent patterns observed in
456 Scenario 1. Patterns in model differences are minimal when compared across stream scale, as
457 defined by Strahler Order in Figure 7c. There is a slight trend towards lower alkalinity model
458 predictions at larger stream scales, and this likely reflects the flatter topography and lower gas
459 exchange velocities in the higher order streams. Averaged across the watershed, the alkalinity
460 model predicts slightly lower *p*CO₂ values by -0.054 ppm. Counterintuitively, total watershed
461 evasion fluxes from the alkalinity model are slightly higher, due to oversized flux contributions
462 from areas with high gas exchange velocities (where the alkalinity model predicts slightly higher
463 *p*CO₂) on total fluxes. The difference in total watershed fluxes reflects the additional CO₂ stored
464 as HCO₃⁻ + H⁺ in exfiltrating groundwater, as both simulations are given the same GW *p*CO₂ and
465 feature the same total stream corridor respiration fluxes.

466

467 We also show how carbonate buffering reactions impact relationships between *p*CO₂ and δ¹³C_{DIC}
468 in Fig. 8 for the East River with an alkalinity of 1 meq/L, which expands on Fig. 5a by
469 incorporating stream corridor respiration sources and scenarios with both increasing and
470 decreasing *p*CO₂. During GW degassing in the headwaters, patterns resemble the degassing
471 experiments from Scenario 1. However, in downstream reaches where *p*CO₂ experiences local
472 variability in response to changing balances between input fluxes and evasion rates, model
473 output deviates significantly from the degassing patterns. When local sources act to increase
474 *p*CO₂, the total amount of DIC added is relatively small compared to the existing pool; thus,
475 δ¹³C_{DIC} is largely insensitive to changes in *p*CO₂. This behavior is highlighted in the inset in Fig.

476 8, in which local changes in $p\text{CO}_2$ result in minimal $\delta^{13}\text{C}_{\text{DIC}}$ changes, and overall patterns feature
477 no large-scale co-variability. We note that this decoupling occurs in spite of the fact that lower
478 $\delta^{13}\text{C}_{\text{DIC}}$ values of stream corridor respiration relative to GW are acting to drive steeper, more
479 sensitive correlations between $p\text{CO}_2$ and $\delta^{13}\text{C}_{\text{DIC}}$. This decoupling of $p\text{CO}_2$ and $\delta^{13}\text{C}_{\text{DIC}}$ is similar
480 with higher alkalinity (SFig 6) and is also significant even in low alkalinity conditions of 0.1
481 meq/L (SFig 7). These results show that even under low alkalinity, $p\text{CO}_2$ and $\delta^{13}\text{C}_{\text{DIC}}$ do not
482 covary systematically across the watershed scale except during initial GW degassing.
483

484 To demonstrate the potential use of paired $\delta^{13}\text{C}_{\text{DIC}}$ and $\Delta^{14}\text{C}_{\text{DIC}}$ in evaluating local partitioning
485 between GW and stream corridor sources of DIC, we plot data from each model cell of the 1
486 meq/L simulation in $\delta^{13}\text{C}_{\text{DIC}}$ v. $\Delta^{14}\text{C}_{\text{DIC}}$ space in Figure 9a. Contour lines represent degassing
487 patterns for an initial DIC pool representing the isotopic end-member composition of varying
488 mixtures of GW and stream corridor sources, generated using the same methods of Scenario 1.
489 We note that while this plot resembles an end-member mixing model, there is some curvature in
490 the contour lines that reflect slight differences in the timescales of equilibration for ^{14}C v. ^{13}C
491 discussed above. As shown, 1st order streams largely fall along All-GW degassing contour lines
492 to start with shift towards higher contributions from stream corridor respiration as values
493 approach atmospheric equilibration. In general, there is a trend towards higher stream corridor
494 respiration contributions at higher stream order, with a significant degree of variability within
495 each order. We show this directly in Figure 9b, where the % GW contribution to DIC is
496 calculated using a nearest-neighbor function to find which contour line passes through each
497 model output point. Across all model cells, GW contributions vary from 100 – 4%. We simulate
498 a consistent transition from GW to stream corridor DIC sources at larger network scales, with the
499 switch from GW to stream corridor dominance occurring between 2nd and 3rd order streams,
500 consistent with our previous modeling results (Saccardi & Winnick, 2021). We note that output
501 from the 4.0 meq/L simulation results in a shift towards higher GW contributions across the
502 watershed, as GW has a significantly larger DIC concentration than the 1.0 meq/L simulation
503 (SFig 8).
504

505 4. Discussion

507 4.1 Alkalinity controls on CO_2 concentrations and fluxes

509 Across the simulated scenarios, we demonstrate quantitatively how alkalinity acts to alter the
510 equilibration of dissolved CO_2 with the atmosphere in rivers and streams. Increased alkalinity, as
511 previously hypothesized, increases the role of carbonate buffering reactions to maintain $p\text{CO}_2$
512 along the stream reach. During active degassing, as shown in Scenarios 1-3, carbonate buffering
513 reactions result in minimally increased atmosphere equilibration timescales, acting to maintain
514 slightly elevated $p\text{CO}_2$. Notably, however, these timescale increases are minimal and are only in
515 evidence at near-atmospheric $p\text{CO}_2$ values. Further, under conditions in which dissolved CO_2 is
516 actively building up, for example when local rates of stream corridor respiration are higher than
517 degassing rates, carbonate buffering maintains lower $p\text{CO}_2$ concentrations as it actively stores
518 CO_2 as $\text{HCO}_3^- + \text{H}^+$. This effect is equivalent to the Revelle factor often discussed in the
519 oceanography literature (Broecker et al., 1979; Revelle & Suess, 1957), and has been shown to
520 impact stream CO_2 fluxes (Wang et al., 2021).
521

522 In a compilation of US stream data, Stets et al. (2017) show that systems with high alkalinity
523 tend to exhibit higher $p\text{CO}_2$ at moderate stream scales (discharge of $0.1 - 6 \text{ m}^3/\text{s}$) than systems
524 with low alkalinity. This was hypothesized to reflect carbonate buffering reactions, through their
525 role in maintaining high $p\text{CO}_2$ during downstream degassing. In our modeling exercises, we
526 show that carbonate buffering is unable to explain these observed patterns. In fact, when
527 simulating at the stream network scale, we find that carbonate buffering reactions result in the
528 opposite pattern as observed in the Stets et al. compilation: $p\text{CO}_2$ is slightly elevated in first
529 order streams but is typically lower in 3rd-5th order streams when alkalinity is included, reflecting
530 the increasing importance of stream corridor respiration sources and lower gas exchange
531 velocities that allow generated CO_2 to be stored as $\text{HCO}_3^- + \text{H}^+$ (Fig. 8b).

532
533 While beyond the scope of our study, we tentatively suggest that if the observational patterns
534 presented in Stets et al. (2017) are robust, they likely reflect either systematically higher source
535 fluxes (GW inputs and/or stream corridor respiration) or systematically lower gas exchange
536 velocities potentially reflecting lower topographic relief (e.g. Rocher-Ros et al., 2019).
537 Regarding elevated source fluxes, we note that Stets et al. (2017) demonstrate lower $p\text{CO}_2$ in the
538 smallest high alkalinity streams which would suggest lower GW $p\text{CO}_2$ sources, and we are
539 unaware of a mechanism that would link high alkalinity with higher stream corridor respiration
540 rates. In terms of topography, as high alkalinity typically reflects increased chemical weathering
541 rates often associated with soluble minerals such as carbonates, these landscapes may
542 preferentially exhibit lower gas exchange velocities in higher order streams, resulting in elevated
543 $p\text{CO}_2$ at larger stream scales. To test this hypothesis would require local flow and topographic
544 data, which are not included in the original compilation, and future work is required to test this
545 hypothesis. We also note that our stream network model simulations, in which the only altered
546 variable is alkalinity, are not directly comparable to the US compilation data. For example, we
547 hold GW $p\text{CO}_2$ constant, whereas increased alkalinity may be expected to co-occur with reduced
548 GW $p\text{CO}_2$ based on chemical weathering reactions (e.g. Winnick & Maher, 2018).

549
550 We also demonstrate that increasing alkalinity and decreasing GW $p\text{CO}_2$ values result in
551 increasing relative contributions of carbonate buffering to total degassing fluxes (Fig. 4). Under
552 conditions where GW is the sole source of stream $p\text{CO}_2$, carbonate buffering may account for
553 $>60\%$ of total degassing fluxes when GW has high alkalinity ($>4 \text{ meq/L}$) and relatively moderate
554 $p\text{CO}_2$ ($<5000 \text{ ppm}$). These values are consistent with findings in Duvert et al. (2019), where
555 carbonate buffering reactions were shown to support as much as $\sim 60\%$ of total fluxes in a high
556 alkalinity, tropical stream system. While not included in our Fig. 4 analysis, carbonate buffering
557 contributions to total fluxes would also decrease with increasing stream corridor respiration.
558 Taken together, these findings highlight the importance of accounting for carbonate buffering
559 reactions in budgeting stream network CO_2 fluxes, particularly in high alkalinity ($>1 \text{ meq/L}$)
560 systems.

561 562 *4.2 Alkalinity impacts on carbon isotope source partitioning*

563
564 In contrast to the effects on CO_2 equilibration timescales, carbonate buffering reactions lead to
565 much longer isotope equilibration timescales for both $\delta^{13}\text{C}_{\text{DIC}}$ and $\Delta^{14}\text{C}_{\text{DIC}}$. Mechanistically, this
566 is due to the fact that $p\text{CO}_2$ is only buffered by the proportion of HCO_3^- that does not contribute
567 to alkalinity (CO_2 stored as $\text{HCO}_3^- + \text{H}^+$). In contrast, the isotopic ratio of DIC is buffered by the

568 entire HCO_3^- and CO_3^{2-} pools, which under high alkalinity are much larger than the CO_2 pool
569 that is actively degassing. As the equilibration timescales for both are regulated by the gas
570 exchange velocity, this larger isotopic buffering results in a much longer equilibration timescale.
571 For example, at an alkalinity of 1 meq/L and initial GW $p\text{CO}_2$ of 20,000 ppm, the CO_2 stored as
572 $\text{HCO}_3^- + \text{H}^+$ is 1.3% the size of the $\text{CO}_{2(\text{aq})}$ pool, whereas the full buffering pool of ^{12}C , ^{13}C , and
573 ^{14}C encapsulated in $\text{HCO}_3^- + \text{CO}_3^{2-}$ is 150% the size of the $\text{CO}_{2(\text{aq})}$ pool. This difference is
574 amplified by the fact that gas exchange rates, and thus isotope equilibration rates, slow
575 significantly as $p\text{CO}_2$ approaches atmospheric values. Further, a higher proportion of total ^{13}C
576 and ^{14}C are contained within HCO_3^- and CO_3^{2-} relative to ^{12}C due to equilibrium fractionation
577 within the DIC pool. Thus, high alkalinity is more effective at buffering the isotopic composition
578 of DIC, which under high alkalinity conditions does not equilibrate until almost all of the net
579 CO_2 degassing has already occurred. At the stream network scale, this results in stream $\delta^{13}\text{C}_{\text{DIC}}$
580 and $\Delta^{14}\text{C}_{\text{DIC}}$ that are much less sensitive to sub-reach changes in topography and source inputs
581 that can dramatically alter $p\text{CO}_2$ over small scales. While these results have been demonstrated
582 indirectly through the application of similar models to groundwater degassing (e.g.
583 Venkiteswaran et al., 2017), this study is the first to identify and quantify these timescales for
584 both $\delta^{13}\text{C}_{\text{DIC}}$ and $\Delta^{14}\text{C}_{\text{DIC}}$.

585
586 These differences in the magnitude impacts of buffering dynamics on $p\text{CO}_2$ versus carbon
587 isotopes greatly complicates methods of CO_2 source evaluation. The size of the isotope buffering
588 pool effectively acts to decouple variations between carbon concentrations ($p\text{CO}_2$ or DIC) and
589 isotopic composition ($\delta^{13}\text{C}_{\text{DIC}}$ or $\Delta^{14}\text{C}_{\text{DIC}}$). During degassing, the bulk of isotopic change occurs
590 after $p\text{CO}_2$ has equilibrated with the atmosphere, which makes measurements of covariation
591 analytically difficult. More importantly, in situations where CO_2 (and DIC) is building up rather
592 than degassing, $\delta^{13}\text{C}_{\text{DIC}}$ or $\Delta^{14}\text{C}_{\text{DIC}}$ are largely insensitive to these new inputs. This results in
593 reach-scale patterns in which $\delta^{13}\text{C}_{\text{DIC}}$ and $p\text{CO}_2$ are largely decoupled and deviate significantly
594 from the overall degassing pattern, as shown in Fig. 8. Typical isotopic source evaluation
595 methods either employ linear mixing models of $p\text{CO}_2$ or DIC and $\delta^{13}\text{C}_{\text{DIC}}$ (e.g. Campeau et al.,
596 2017, 2018) or degassing models (Venkiteswaran et al., 2014). The assumptions underlying both
597 of these methods is that $p\text{CO}_2$ and $\delta^{13}\text{C}_{\text{DIC}}$ co-vary systematically across a given study area. We
598 show that this is not the case; carbonate buffering acts to decouple $p\text{CO}_2$ and $\delta^{13}\text{C}_{\text{DIC}}$ patterns in
599 all but the 1st order headwaters which are dominated by GW degassing. This decoupling occurs
600 even at low and moderate alkalinity values (0.1 meq/L shown in SFig 7; 1 meq/L shown in Fig.
601 8). Therefore, studies that utilize $p\text{CO}_2$ - or DIC- $\delta^{13}\text{C}_{\text{DIC}}$ methods for evaluating carbon sources
602 are only accurate under very low alkalinity conditions or in directly evaluating GW degassing
603 trends in spring-fed headwaters.

604
605 Despite the factors that complicate relationships between isotope composition and $p\text{CO}_2$, our
606 modeling simulations suggest a useful path forward. Specifically, $\delta^{13}\text{C}_{\text{DIC}}$ and $\Delta^{14}\text{C}_{\text{DIC}}$ both
607 represent the full DIC pool and have equilibration timescales that are similarly impacted by
608 alkalinity. Therefore, they may be used to more directly partition DIC sources through end-
609 member mixing analyses. Further, the increased equilibration timescales in high alkalinity
610 systems mean that point measurements of $\delta^{13}\text{C}_{\text{DIC}}$ and $\Delta^{14}\text{C}_{\text{DIC}}$ are more integrative of upstream
611 conditions and may provide useful insight into broader spatial trends than $p\text{CO}_2$, which can often
612 vary over scales of 10's of meters (e.g. Johnson et al., 2008). Paired $\delta^{13}\text{C}_{\text{DIC}}$ and $\Delta^{14}\text{C}_{\text{DIC}}$
613 measurements may be particularly useful for DIC source partitioning in systems where

614 groundwater DIC is controlled by carbonate mineral weathering reactions, such as watersheds
615 with limestone or shale bedrock. Under these conditions and as parameterized across our
616 simulations, GW, stream corridor respiration, and the atmosphere all represent unique end-
617 members in $\delta^{13}\text{C}_{\text{DIC}}-\Delta^{14}\text{C}_{\text{DIC}}$ space (e.g. Table 1). We note that Sveinbjörnsdóttir et al. (2020)
618 have previously employed paired $\delta^{13}\text{C}_{\text{DIC}}-\Delta^{14}\text{C}_{\text{DIC}}$ to evaluate DIC sources; however, they used
619 a linear end-member mixing model, which our results show neglects non-linear variations
620 between $\delta^{13}\text{C}_{\text{DIC}}$ and $\Delta^{14}\text{C}_{\text{DIC}}$ degassing rates and may therefore only be accurate under low
621 alkalinity conditions.

622
623 In our simulations, we calculate the contributions of GW versus stream corridor respiration to
624 DIC using simulated $\delta^{13}\text{C}_{\text{DIC}}-\Delta^{14}\text{C}_{\text{DIC}}$ relationships. At any given simulated stream point,
625 measured values are representing the integration of upstream processes at spatial scales
626 dependent on stream velocity, gas exchange velocity, and the alkalinity-dependent equilibration
627 timescales of carbon isotope values. We propose that these methods may be employed within
628 field systems, which requires the characterization of end-member source $\delta^{13}\text{C}_{\text{DIC}}-\Delta^{14}\text{C}_{\text{DIC}}$ values,
629 along with alkalinity measurements to calculate contour mixing lines (see Supplemental Material
630 for example code). Currently, methods for estimating source contributions within a stream reach
631 are intensive, and typically involve calculating stream corridor metabolic rates through DO
632 sensor deployment and absolute CO_2 fluxes through high resolution sampling (e.g. (Hotchkiss et
633 al., 2015)). While $\Delta^{14}\text{C}_{\text{DIC}}$ measurements are costly, this method has the advantage of allowing for
634 rapid characterization of source partitioning across watershed scales, through sampling
635 campaigns that target multiple streams. Traditionally, source characterization across stream
636 orders within a watershed would require redeployment of DO sensors at each new reach;
637 whereas, this method would only require taking additional samples at each reach assuming
638 relatively consistent end-member sources across the watershed.

639

640 *4.3 Model Limitations*

641

642 While these models are meant to be broadly representative of the processes controlling
643 atmospheric equilibration of river and stream waters, there are a number of assumptions we have
644 made that must be validated on a site-by-site basis for direct data comparisons. First, our
645 simulations parameterize stream corridor metabolism as net respiration rather than separately
646 simulating photosynthesis and respiration. This parameterization assumes that organic matter
647 derived from terrestrial materials is the same as that synthesized in the stream, such that stream
648 corridor photosynthesis and respiration have equal and opposite impacts on isotopic composition.
649 This assumption may be violated, for example, in sites where terrestrially-derived DOC
650 represents C_4 plant matter, and at the field-scale, measurements of distinct isotopic end-member
651 for different DOC sources are needed to evaluate this assumption. As stated throughout the
652 manuscript, we also neglect processes that alter alkalinity concentrations, which may include
653 anaerobic respiration, calcite precipitation, and spatiotemporal changes in GW chemistry. We
654 similarly neglect CO_2 generation from methane oxidation that may result in distinctly low
655 $\delta^{13}\text{C}_{\text{DIC}}$ values. Lastly, we assume that there is no kinetic fractionation associated with CO_2
656 degassing from turbulent exchange, and that apparent fractionation during degassing reflects
657 only equilibration with the elevated atmospheric values of $\delta^{13}\text{C}_{\text{DIC}}$ and $\Delta^{14}\text{C}_{\text{DIC}}$. We feel that this
658 issue remains an open question that has not been directly addressed in stream environments,

659 though our modeling framework is flexible to incorporate it as a specified kinetic fractionation
660 factor when molecular diffusion is a significant factor in degassing rates.

661

662 **5. Conclusions**

663 Given the recent recognition of carbonate buffering reactions as an important control on spatial
664 patterns of CO₂ concentrations and fluxes in stream systems, we develop a non-dimensional
665 reactive transport framework for evaluating their impacts on atmospheric equilibration of
666 dissolved inorganic carbon. We find that while carbonate buffering does increase the timescales
667 over which *p*CO₂ approaches steady-state values, these changes are relatively small and cannot
668 explain observations of elevated *p*CO₂ at increasing spatial scales in high alkalinity versus low
669 alkalinity systems. This increase in equilibration timescale, along with increased contributions of
670 carbonate buffering reactions to total CO₂ fluxes, depends on the size of the buffering reservoir
671 (or amount of CO₂ stored as HCO₃⁻ + H⁺) relative to CO_{2(aq)}, such that carbonate buffering
672 reactions contribute a larger proportion of CO₂ fluxes as alkalinity increases and GW *p*CO₂
673 decreases. In contrast to CO₂, the isotopic composition of DIC is buffered by the entire DIC pool
674 as CO₂ equilibrates with the atmosphere, which is much larger than the pool of CO₂ stored as
675 HCO₃⁻ + H⁺. As a result, isotopic equilibration timescales are much more sensitive to stream
676 alkalinity, with δ¹³C_{DIC} and Δ¹⁴C_{DIC} increasing by ~2 orders of magnitude relative to CO₂
677 timescales. The result of this mismatch in timescales is that under moderate alkalinity conditions,
678 isotope composition becomes largely decoupled from *p*CO₂, rendering typical methods for CO₂
679 source tracing ineffective. We show, however, that due to similar impacts on equilibration
680 timescales, paired δ¹³C_{DIC} and Δ¹⁴C_{DIC} measurements may be effective tracers of GW versus
681 stream corridor respiration sources of DIC in environments where GW DIC is controlled by
682 carbonate weathering reactions, typical of moderate to high alkalinity systems. Taken together,
683 we present a generalizable framework for quantifying and interpreting the role of carbonate
684 buffering reactions on stream CO₂ dynamics and develop a new potential method for utilizing the
685 isotopic composition of DIC to trace stream carbon sources.

686

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691

692 **Data Availability Statement**

693 All code used in this work is available in the Supplemental Information. We will also make all
694 code available publicly via the open-source Hydroshare platform following the first round of
695 review.

696

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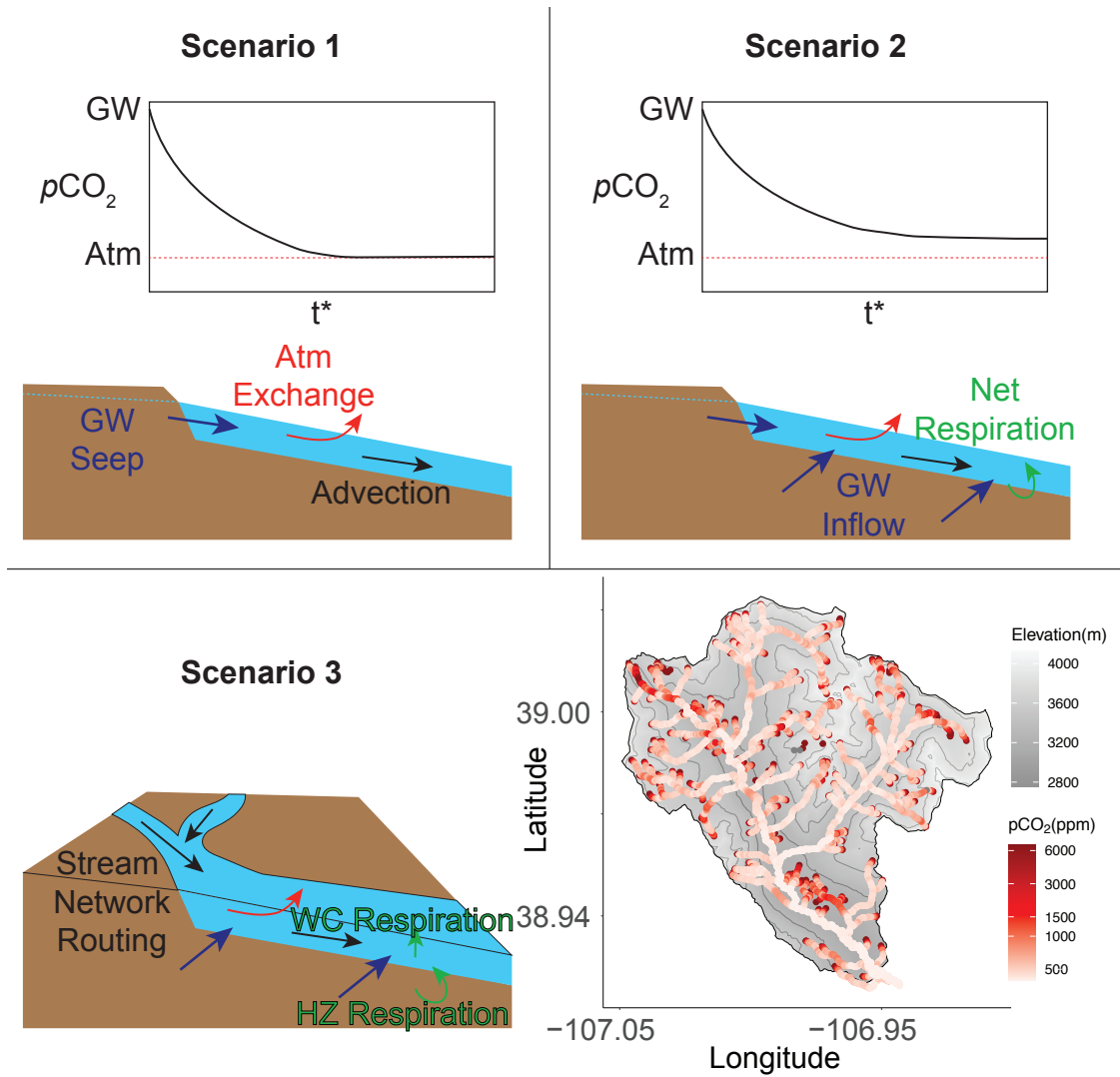
Table 1. Reaction network and end-member source values for modeling experiments

Reaction Network			
Reaction	log(K¹²) @ 25°C	log(K¹³) @ 25°C	log(K¹⁴) @ 25°C
${}^i\text{CO}_{2(\text{aq})} \leftrightarrow \text{H}^+ + \text{H}^i\text{CO}_3^-$	-6.3447	-6.340835	-6.336995
$\text{H}^i\text{CO}_3^- \leftrightarrow \text{H}^+ + {}^i\text{CO}_3^{2-}$	-10.3288	-10.328986	-10.32914
$\text{H}_2\text{O} \leftrightarrow \text{H}^+ + \text{OH}^-$	-14*	-	-
End-member Sources			
Source	pCO₂ (ppm)	δ¹³C (‰ VPDB)	Δ¹⁴C (‰)
Groundwater	20,000	-15	-500
Stream Corridor Respiration	-	-27	-66
Atmosphere	410	-9	-66

* log(K)

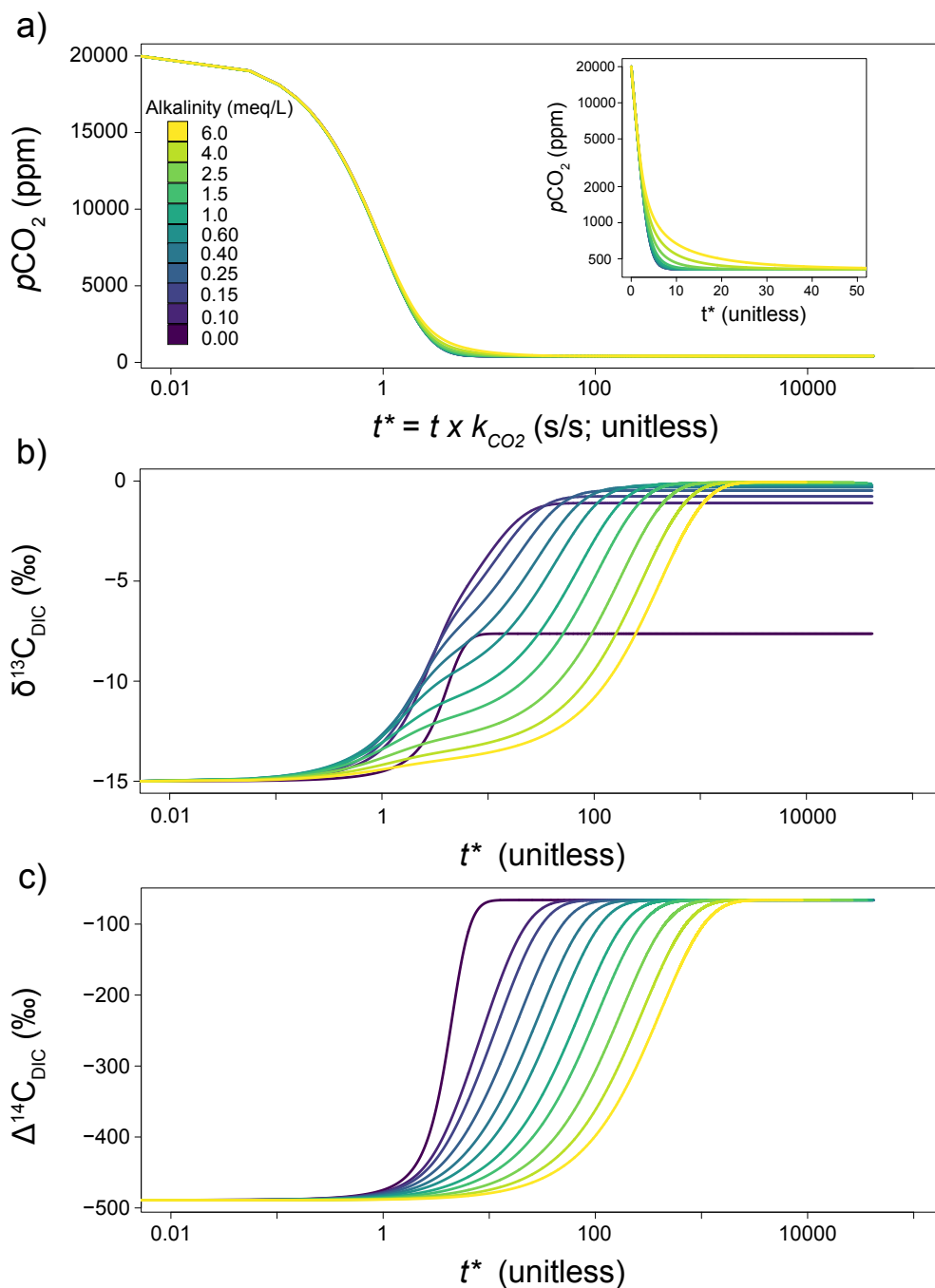
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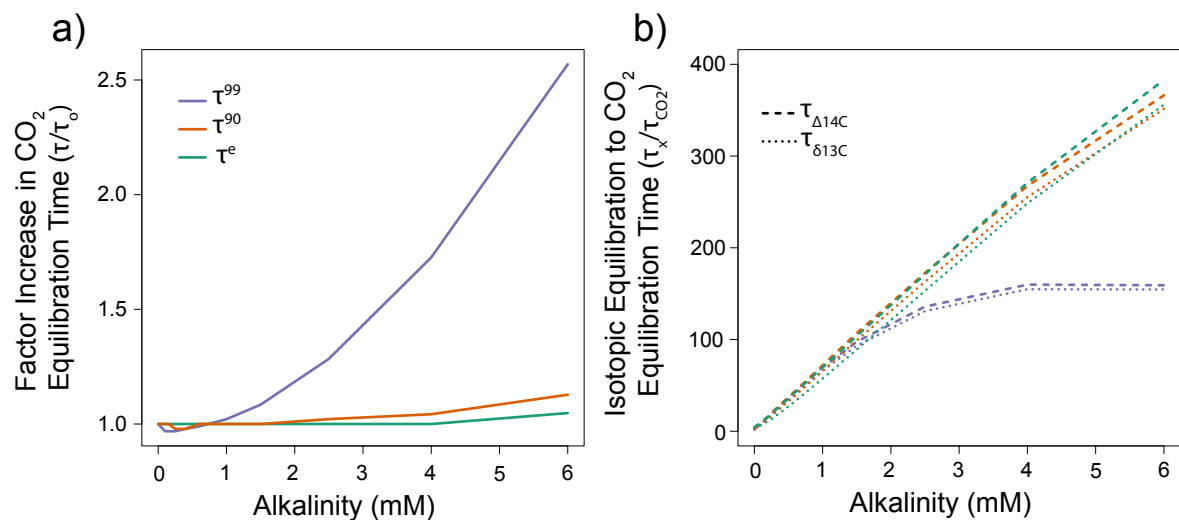
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Figure 1. Conceptual diagram of the modelling scenarios including characteristic patterns of $p\text{CO}_2$ and the processes incorporated. Scenario 1 is analogous to a degassing GW seep with no additional CO_2 inputs. Scenario 2 represents a GW seep degassing with simultaneous CO_2 inputs from GW and stream corridor respiration, analogous to a small headwaters stream. Scenario 3 is the modeling of a full 87 km^2 5th order watershed in the East River, CO, USA. It incorporates stream network water routing via advection, groundwater inputs, hyporheic exchange, net water column respiration, and atmospheric exchange. Simulated watershed $p\text{CO}_2$ values are from Saccardi and Winnick (2021) and represent a no-alkalinity simulation, which is compared to the updated model in Scenario 3. Note, symbol definitions translate between Scenarios, and GW Seep and Inflow end-member values are identical.

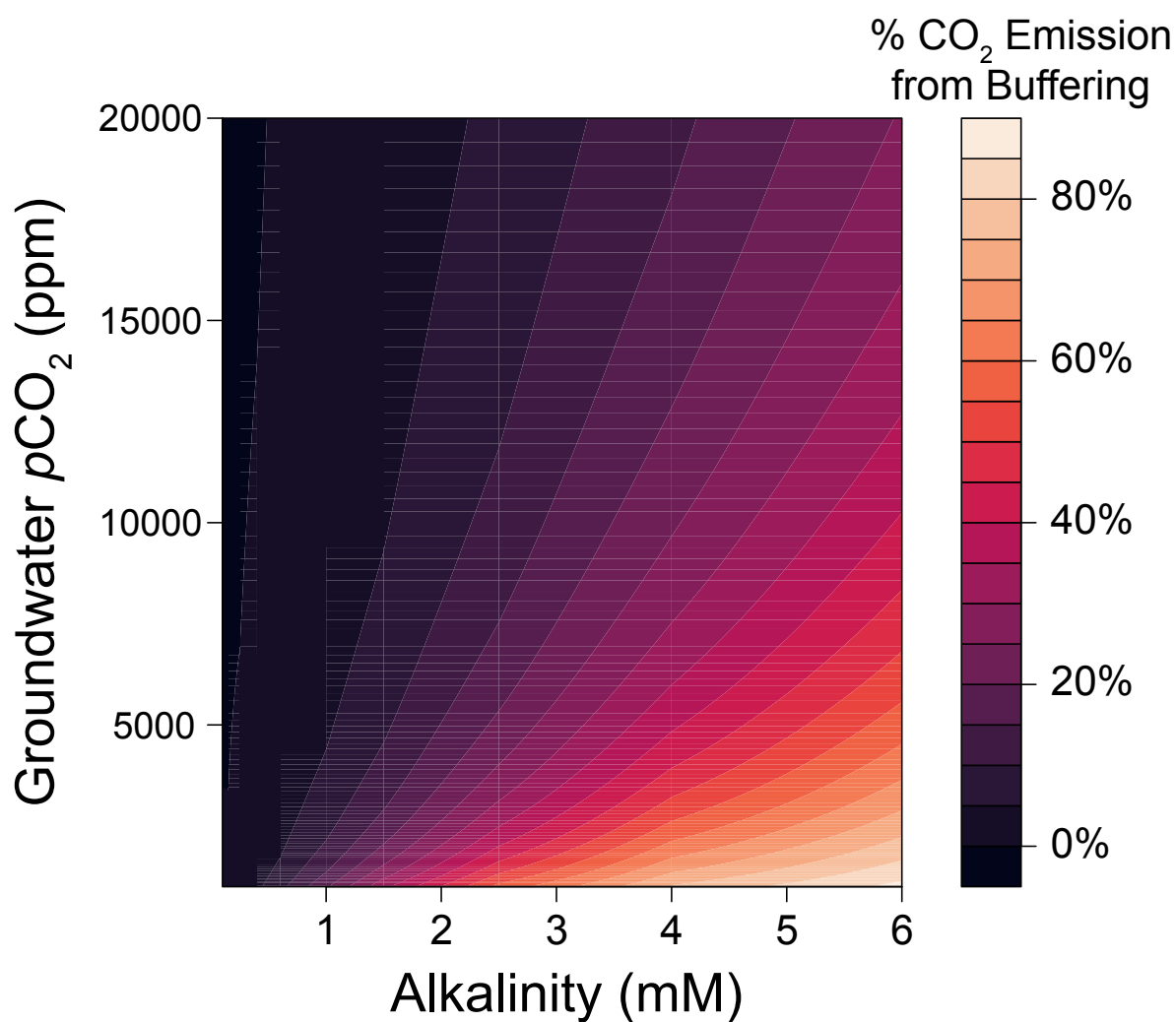


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Figure 2. Temporal evolution of (a) $p\text{CO}_2$, (b) $\delta^{13}\text{C}_{\text{DIC}}$, and (c) $\Delta^{14}\text{C}_{\text{DIC}}$ in Scenario 1 simulations. The x-axis in all plots represents nondimensional time, calculated by multiplying simulation time (s) by the specified reaeration rate (s^{-1}). Line colors represent the specified GW alkalinity. Note the large difference between the 0 and 0.1 meq/L alkalinity lines in plot (b) reflects the non-linear decrease in the fractional contribution of $\text{CO}_{2(\text{aq})}$ to total DIC as alkalinity increases.

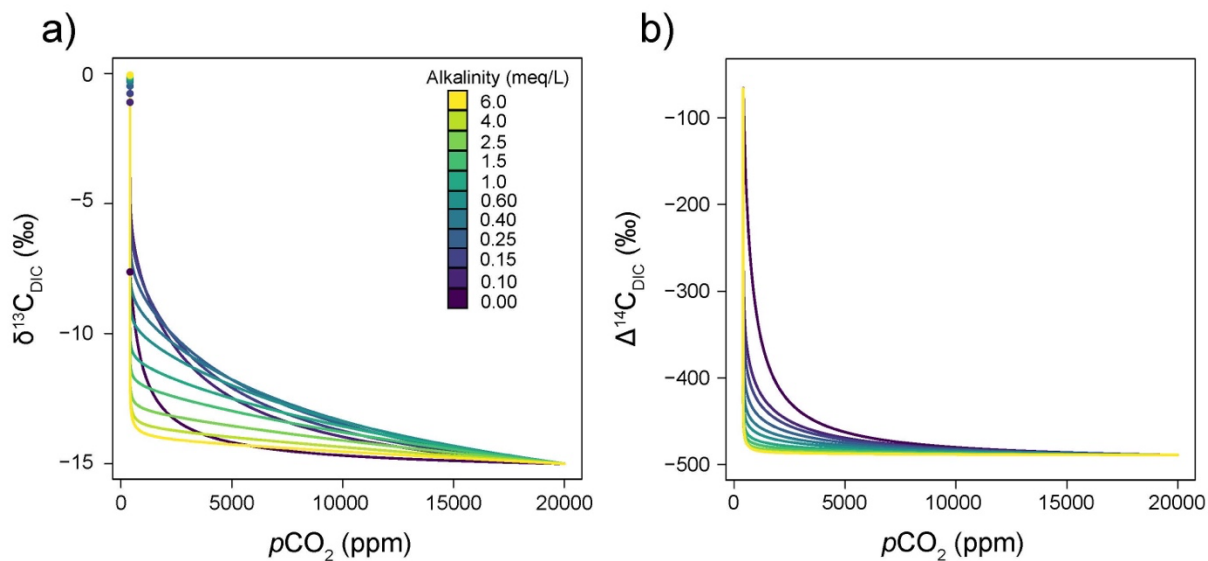


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 847 **Figure 3.** Impacts of alkalinity on atmosphere equilibration timescales for Scenario 1
 848 simulations of (a) pCO_2 , and (b) $\delta^{13}C_{DIC}$ and $\Delta^{14}C_{DIC}$ relative to pCO_2 . Line colors represent
 849 different metrics of equilibration timescales. Dashed and dotted lines in (b) represent $\Delta^{14}C_{DIC}$
 850 and $\delta^{13}C_{DIC}$, respectively.
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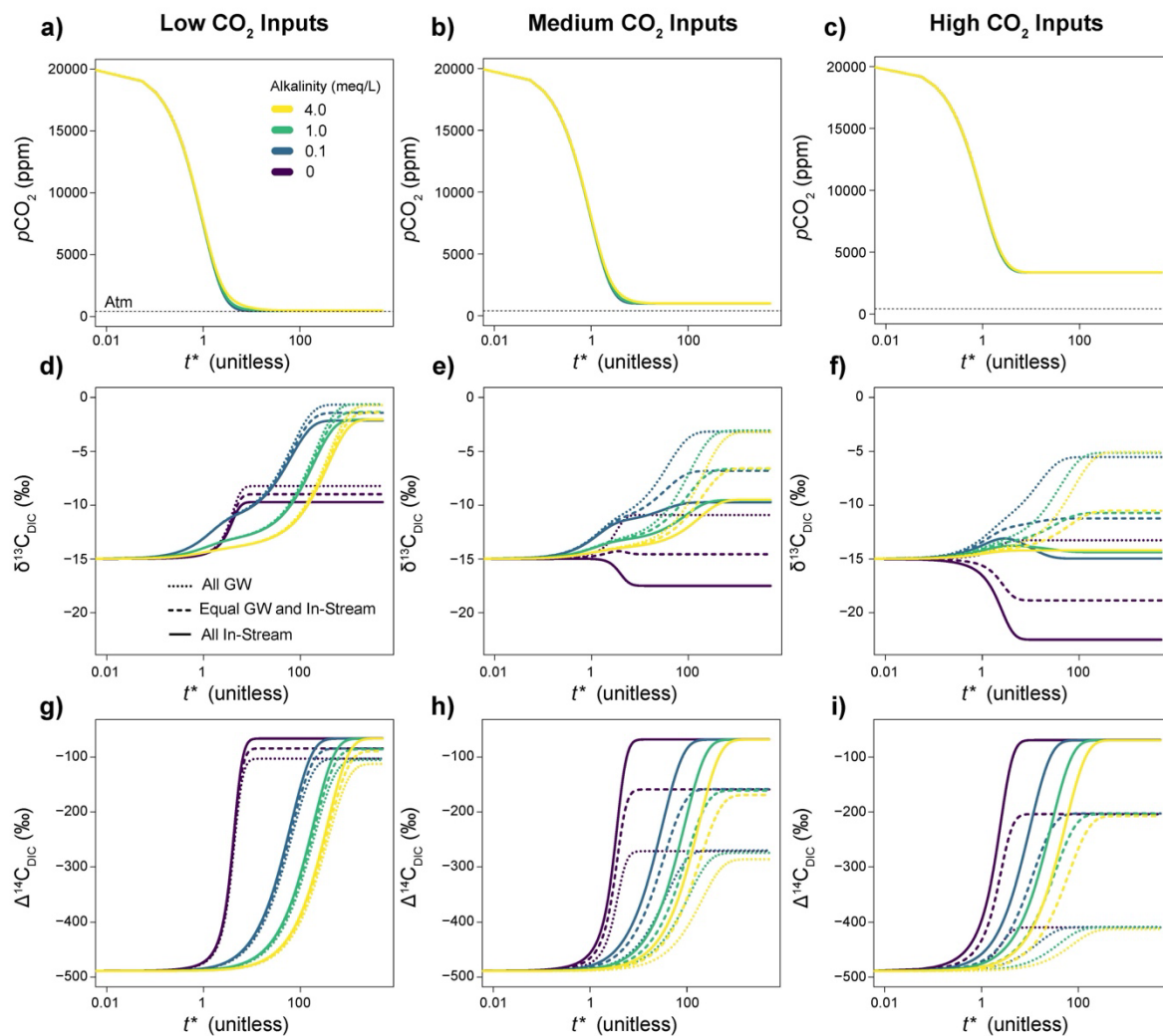
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Figure 4. Contour map of the % contributions of carbonate buffering reactions to total CO₂ emissions in Scenario 1 as a function of GW alkalinity and pCO₂. Carbonate buffering reactions contribute proportionally more to overall emissions as GW alkalinity increases and GW pCO₂ decreases.

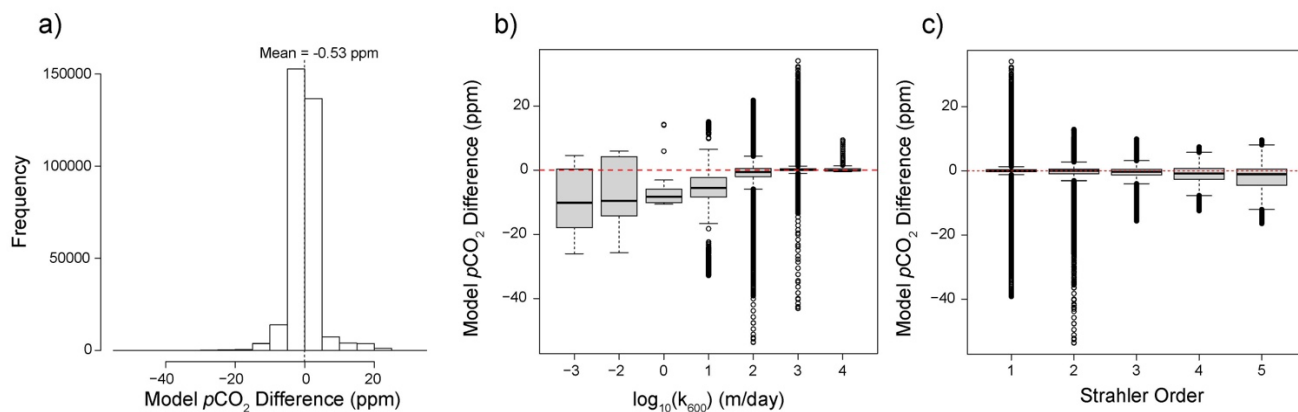


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Figure 5. Covariation between $p\text{CO}_2$ and the isotopic composition of DIC as a function of alkalinity for (a) $\delta^{13}\text{C}_{\text{DIC}}$ and (b) $\Delta^{14}\text{C}_{\text{DIC}}$ in Scenario 1 simulations. Points in (a) represent the final atmosphere-equilibrated values, which vary with alkalinity. Notably, these patterns only represent degassing, contrasted with Figure 8 which includes degassing and input sources.

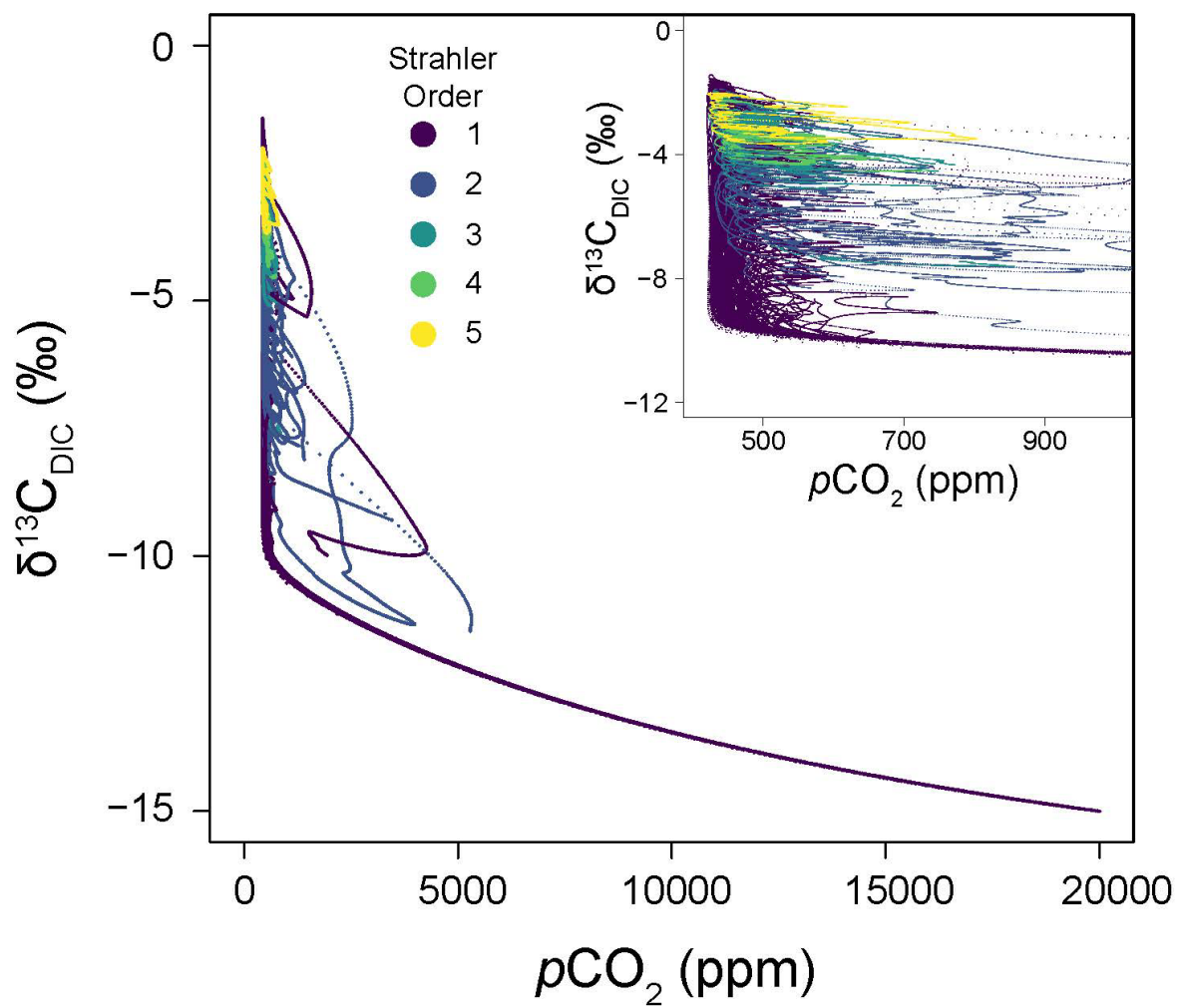


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 868 **Figure 6.** Temporal evolution of simulations in Scenario 2 showing $p\text{CO}_2$, $\delta^{13}\text{C}_{\text{DIC}}$, and $\Delta^{14}\text{C}_{\text{DIC}}$
 869 (rows) for varying CO₂ input fluxes (columns). As in Fig. 2, x-axes represent non-dimensional
 870 time. Line color represents alkalinity, and line types represent the ratio of GW versus stream
 871 corridor respiration contributions to CO₂ inputs.
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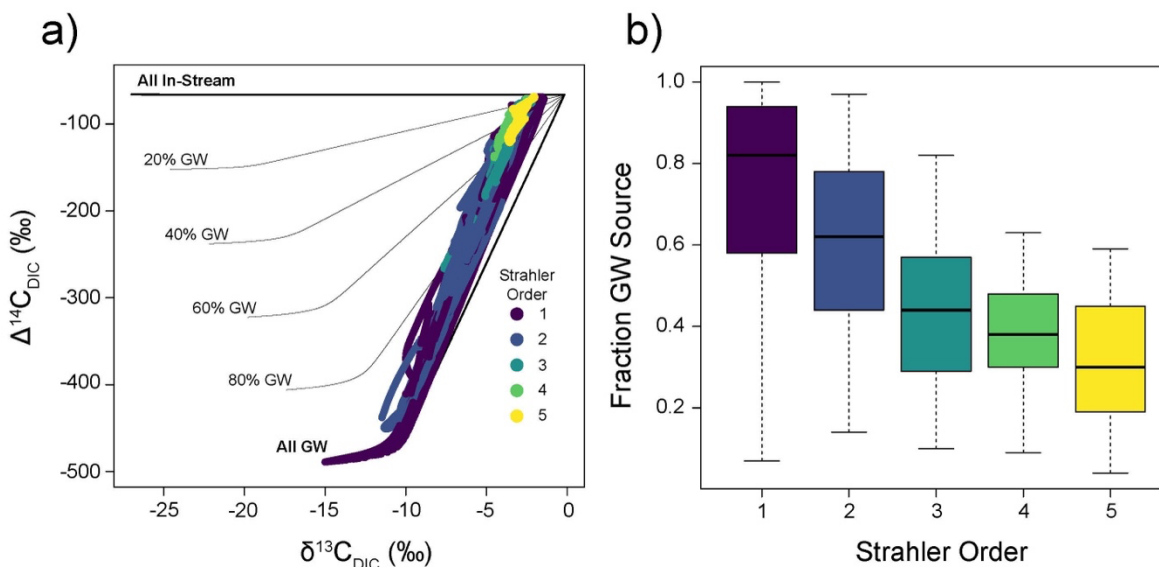


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875 **Figure 7.** Comparisons of Scenario 3 simulations with 1 meq/L alkalinity and no alkalinity,
876 showing (a) a histogram of the differences, (b) boxplot of differences binned by gas exchange
877 velocity, and (c) boxplot of differences binned by Strahler Order. The inclusion of alkalinity
878 results in both increased and decreased simulated $p\text{CO}_2$, with decreased values occurring in areas
879 with low gas exchange rates that allow for $p\text{CO}_2$ to build up locally. Alkalinity does not result in
880 increased downstream $p\text{CO}_2$ at the stream network scale as shown in (c).
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883 **Figure 8.** Simulated relationships between $\delta^{13}\text{C}_{\text{DIC}}$ and $p\text{CO}_2$ in the Scenario 3 simulations with
884 1 meq/L alkalinity. Point colors represent Strahler Order, and the inset highlights variability
885 following GW degassing. Following GW degassing, $p\text{CO}_2$ and $\delta^{13}\text{C}_{\text{DIC}}$ are largely decoupled.
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 888 **Figure 9.** Carbon source partitioning using $\delta^{13}\text{C}_{\text{DIC}}$ - $\Delta^{14}\text{C}_{\text{DIC}}$. (a) Simulated Scenario 3 (1 meq/L
 889 alkalinity) relationships between $\delta^{13}\text{C}_{\text{DIC}}$ and $\Delta^{14}\text{C}_{\text{DIC}}$ represent contributions from stream
 890 corridor, GW, and atmospheric end-member sources. Contour lines represent degassing
 891 simulations from mixed GW-stream corridor end-member sources. Non-linearity of the contour
 892 curves represents slight offsets in $\delta^{13}\text{C}_{\text{DIC}}$ and $\Delta^{14}\text{C}_{\text{DIC}}$ equilibration timescales (e.g. Fig. 3b). (b)
 893 Fractional contributions of DIC from GW sources (versus stream corridor respiration) as a
 894 function of Strahler Order. Simulations show a shift in sources from GW in the headwaters to
 895 stream corridor respiration in higher order streams.