

1 **Deep Learning Models Filter Out Local Errors in Hydrological Data**

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11 **Highlights**

- 12 1. Adding global model outputs as input to a locally trained model can improve streamflow
13 simulation accuracy.
- 14 2. Recession flow simulation may be improved by combining global and local information.
- 15 3. Global models avoid over-fitting to local epistemic errors and improve performance
16 relative to local models.

18 **Abstract**

19 This study examines streamflow simulations using deep learning (DL) to: (1) Understand why
20 global DL models trained on multiple watersheds outperform local DL models trained on single
21 watersheds, and (2) Improve recession flow simulation accuracy. It introduces a novel modeling
22 strategy called global-local (GL) modeling, where outputs from the global model are added as
23 input to a locally trained model. The hypothesis is that the GL strategy can leverage both global
24 and watershed-specific information in the form of local errors. GL models demonstrate enhanced
25 accuracy in recession flow prediction for multiple watersheds compared to global and local
26 models. However, considering the entire hydrograph, GL models perform worse than global
27 models. GL model's performance relative to the global model depends on whether hydrological
28 data errors are predominantly stationary or nonstationary. Local nonstationary errors significantly
29 contribute to the global model's superior performance over locally trained process-based and DL
30 models.

31 **Plain language summary**

32 This study presents a new way to generate computer simulations of streamflow by using deep
33 learning methods. The main idea is to use a learning model to extract information from many
34 different watersheds and to also learn unique details of each watershed. These unique details
35 include errors in data (rainfall and streamflow) that are watershed specific. This new approach
36 improves the accuracy of streamflow predictions during recession when there is no rainfall, but it
37 does not work as well when we look at the entire history of streamflow in which case a model built
38 with information from all watersheds is superior. We also found that the errors in measuring the
39 rainfall and streamflow data have a big impact on performance of the different models. Models
40 trained with data from many watersheds are not as affected by these errors as much as models
41 trained with data from just one watershed. This study shows the importance of accounting for
42 errors in the data when building computer simulations of streamflow.

43 **1. Introduction**

44 Several rainfall-runoff models have been used for streamflow simulation including
45 conceptual and process-based (PB) hydrological models (Singh, 1995), statistical time series
46 models (i.e., data-based mechanistic modeling; Beven, 2011), machine learning (ML;
47 Govindaraju, 2000) including deep learning models (DL; Shen & Lawson, 2021). For any
48 approach, model parameters must be calibrated to match the available data which is typically
49 streamflow time series at the watershed outlet. Each watershed is unique with respect to details of
50 the rainfall-runoff processes and in terms of errors in hydrological data (Beven, 2000; Beven
51 2020). Therefore, it is prudent to calibrate rainfall-runoff models on data available within a single
52 watershed where predictions are required. Examples of watershed-specific errors include
53 systematic errors in rainfall magnitude dependent upon rain gauge density (Bárdossy & Anwar,
54 2022) and rain gauge locations (Moličová et al., 1997), and errors in rainfall timing (Gupta et al.,
55 2023).

56 Recent work (e.g., Nearing et al., 2021; Li et al., 2022) has shown that a DL model trained
57 on data across multiple watersheds (referred to as a global model in this study) typically
58 outperforms DL models trained on single watersheds (referred to as local models). Further, the

59 global DL models outperform the PB models in most watersheds (Kratzert et al., 2021). One reason
60 that global DL models outperform the locally calibrated PB and DL models is the extra
61 hydrological information available to the global DL models through data across different
62 watersheds. Another reason for the improved performance may be that local, watershed-specific,
63 nonstationary errors in hydrological data can degrade the performance of local DL and PB models
64 (Beven, 2023) because a local DL model will fit these systematic errors while the global DL model
65 will filter out these errors.

66 In the presence of local-systematic errors, one would expect that the residuals between
67 observed and global model-predicted streamflow would have some non-random structure. In this
68 study, we investigate whether there is any *learnable* structure in these residuals. To this end, we
69 propose a simple and novel strategy that combines global and local modeling approaches to predict
70 streamflow. The benefit of this strategy is that streamflow simulations can be more accurate than
71 the ones simulated by a global model if there is any watershed-specific learnable (in some sense
72 stationary) structure in the residuals.

73 Previous studies have focused on the prediction of entire streamflow hydrographs using
74 ML/DL (e.g., Ma et al., 2021; Li et al., 2022). This may result in suboptimal predictions of the
75 recession flows (Knoben et al., 2020). Therefore, this study separately models recession flows.
76 Accurate predictions of recession flows are important for water quality and ecological purposes.
77 Recession flow dynamics are strongly governed by the geological properties of a watershed (Bear,
78 2013) and watershed geometry (Troch et al., 2003). High flow periods are also impacted by factors
79 such as antecedent moisture conditions and rainfall patterns along with watershed-scale
80 geomorphological structure (Lee & Delleur, 1972; Rodriguez-Iturbe & Rinaldo, 1997). Therefore,
81 due to different controls on the dynamics of the two processes, a global DL model that is accurate
82 for high-flow predictions may not be the best model for recession-flow predictions. Typically,
83 Nash-Sutcliff Efficiency (NSE; Nash & Sutcliffe, 1970) or a similar metric is used as the objective
84 function to be optimized during calibration that gives higher weight to the high flows. Therefore,
85 separate modeling of recession flows is explored in this study.

86 The objective of this study is to test a new DL modeling strategy to combine global and
87 local information for streamflow simulation, that can take advantage of both the ability of a global
88 model to generalize across variability in multiple watersheds and the potential information
89 available in the form of local errors in the hydrological data of a watershed. The proposed DL
90 strategy is an attempt to extract meaningful information from the residuals between observed
91 streamflows and the global model-predicted streamflows. Specifically, this study (1) provides
92 insight into why the global DL models perform better than the locally trained DL and PB models,
93 and (2) explores whether the streamflow simulation performance can be improved by the global-
94 local strategy.

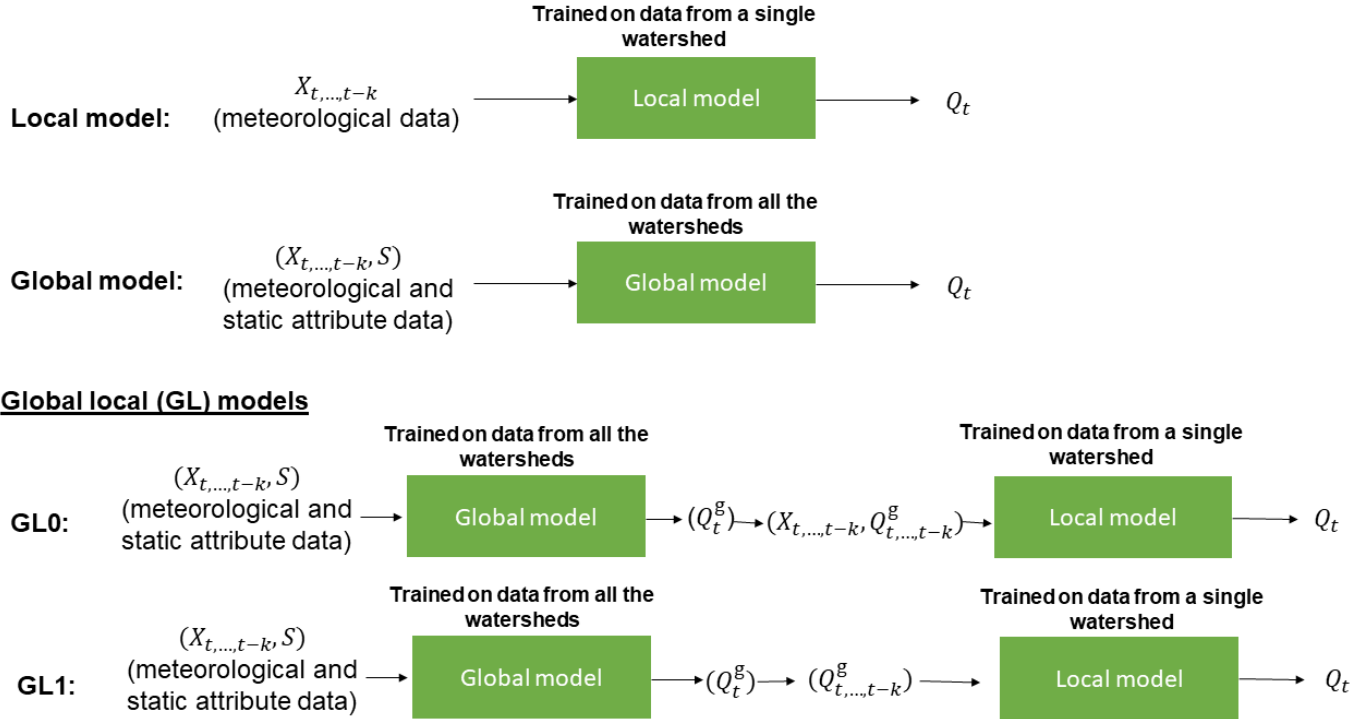
95 **2. Deep learning (DL) models**

96 A long short-term memory (LSTM) network is used as the basic DL model as it has been
97 shown to yield state-of-the-art performance (Nearing et al., 2021). Details of the LSTM can be
98 found in Kratzert et al. (2021) and Goodfellow et al. (2016). For this study, it suffices that LSTM
99 is a variant of the gated recurrent neural network (Goodfellow et al., 2016), designed to address
100 long-memory time series problems and is suitable for streamflow simulations. A single LSTM

101 layer with 128 neurons was used in this study. Four types of models were trained in this study: (1)
102 Trained using data from only the watershed where predictions are required (local model), (2)
103 Trained using data from all the watersheds (global model), (3) A combination of global and local
104 models where the output of a global model is appended with meteorological data and is passed
105 through a local model (GL0 model), and (4) a combination of global and local models where the
106 output of the global model is used as the sole input to the local model (GL1 model). The four
107 modeling strategies are conceptually illustrated in Figure 1. In Figure 1, the symbol X_t denotes the
108 meteorological data that varies with time t including precipitation, minimum and maximum
109 temperatures, vapor pressure, and solar radiation. The symbol S denotes static attributes (see
110 Addor et al., 2017) including soil and geological properties, topographical data, and the long-term
111 climate of a watershed. The symbol k denotes the length of past meteorological data used as input
112 to the LSTM.

113 Further, each of the four models was trained separately using data for both the entire
114 hydrograph and data for recession flows only. Recession flows were defined as the flows during
115 which rainfall was below 0.1 mm, beginning at least three days after the preceding peak
116 streamflow. Thus, there were two global models used to predict streamflow, one for the entire
117 streamflow hydrograph and one for recession flows. The numbers of local and GL models were
118 twice the number of watersheds – two models for each watershed (one for recession and one for
119 the entire hydrograph).

120 The value of k was set to 365 days for the ‘entire hydrograph models’ and 60 days for the
121 ‘recession flow models’. The value of $k = 60$ day was deemed sufficient for recession flows as
122 increasing it further did not improve the performance. NSE (in the form suggested by Kratzert et
123 al., 2019) was used as a performance metric and the objective function to be maximized during
124 model training. The separate models for recession flow periods were trained by giving a weight of
125 1 to all the recession flow time steps and a weight of 0 to other time steps. The training period for
126 all the models was 1980-1989 water years, the validation period was 1990-1994 water years, and
127 the testing period was 2001-2013 years. Simulated daily mean streamflow is the output of each
128 model.



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Figure 1. Illustrative description of the four models. The symbols $X_{t,\dots,t-k}$ and S denote the meteorological data at current and past k time-steps and static watershed attributes, respectively. Q_t denotes the final predicted streamflow in all the models and $Q_{t,\dots,t-k}^g$ denotes the streamflow predicted by global models in the two global-local (GL) models at current time-step and past k time-steps.

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3. Data

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The Catchment Attributes and Meteorology for Large Sample Studies (CAMELS; Addor et al., 2017) dataset was used to develop different models. The CAMELS dataset contains daily timescale hydrometeorological and catchment attribute data from 671 watersheds across the USA (details of these attributes can be found in Addor et al., 2017). All the CAMELS watersheds are free of anthropogenic disturbances. In this study, 210 watersheds that were primarily driven by rainfall were used. These 210 watersheds (see Figure 4 below) cover most of the geographical regions of the USA and have different hydroclimatic conditions.

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4. Comparison of model performance

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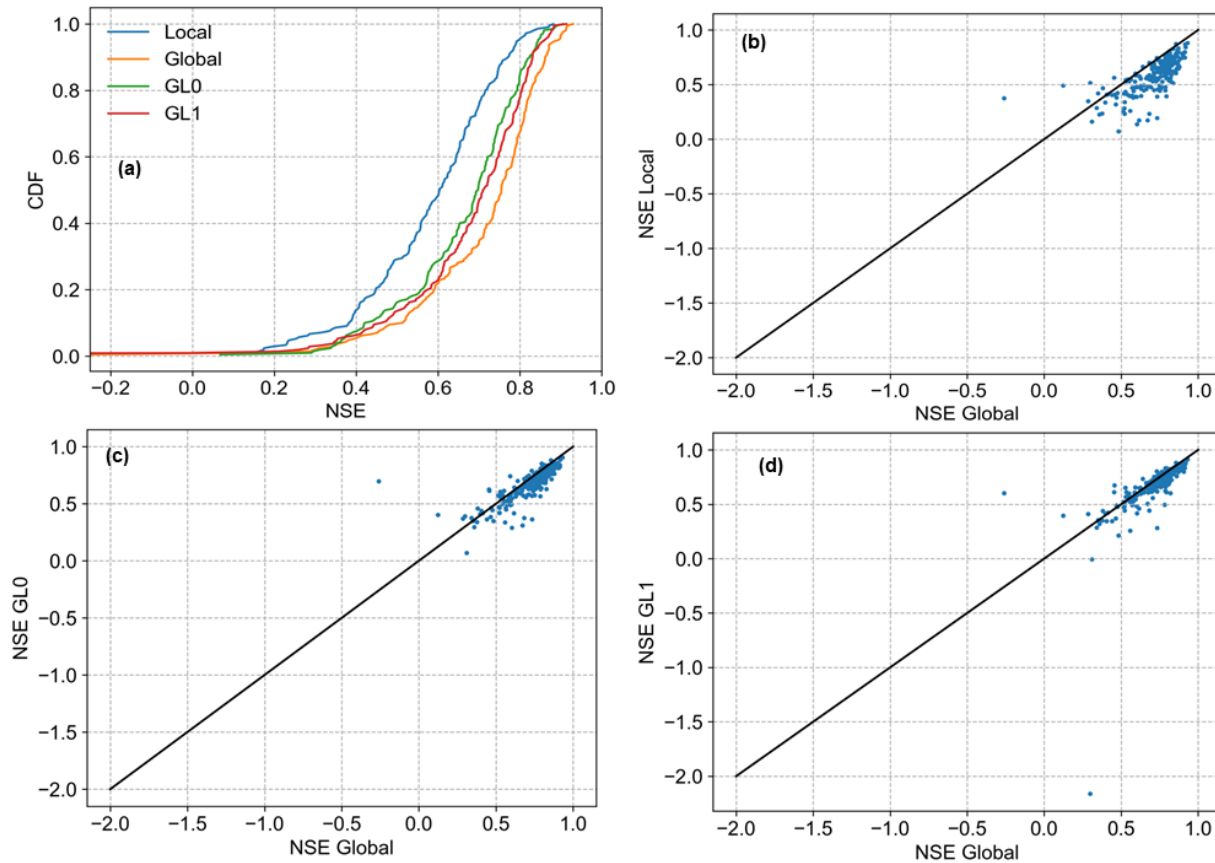
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Cumulative distribution functions (CDFs) of NSE values obtained by the four models (Figure 2a) show that global models outperformed the other three models in predicting the entire hydrograph. Local models performed the worst; the GL0 and GL1 models performed better than the local models. In most watersheds (Figure 2b), the global model outperformed, below the 1:1 line, the local models but there were a few watersheds for which the local models were better. GL0 and GL1 models performed similarly to the global model for a large number of watersheds (Figures 2c and 2d) but performed worse in several others. These results indicate that the global modeling

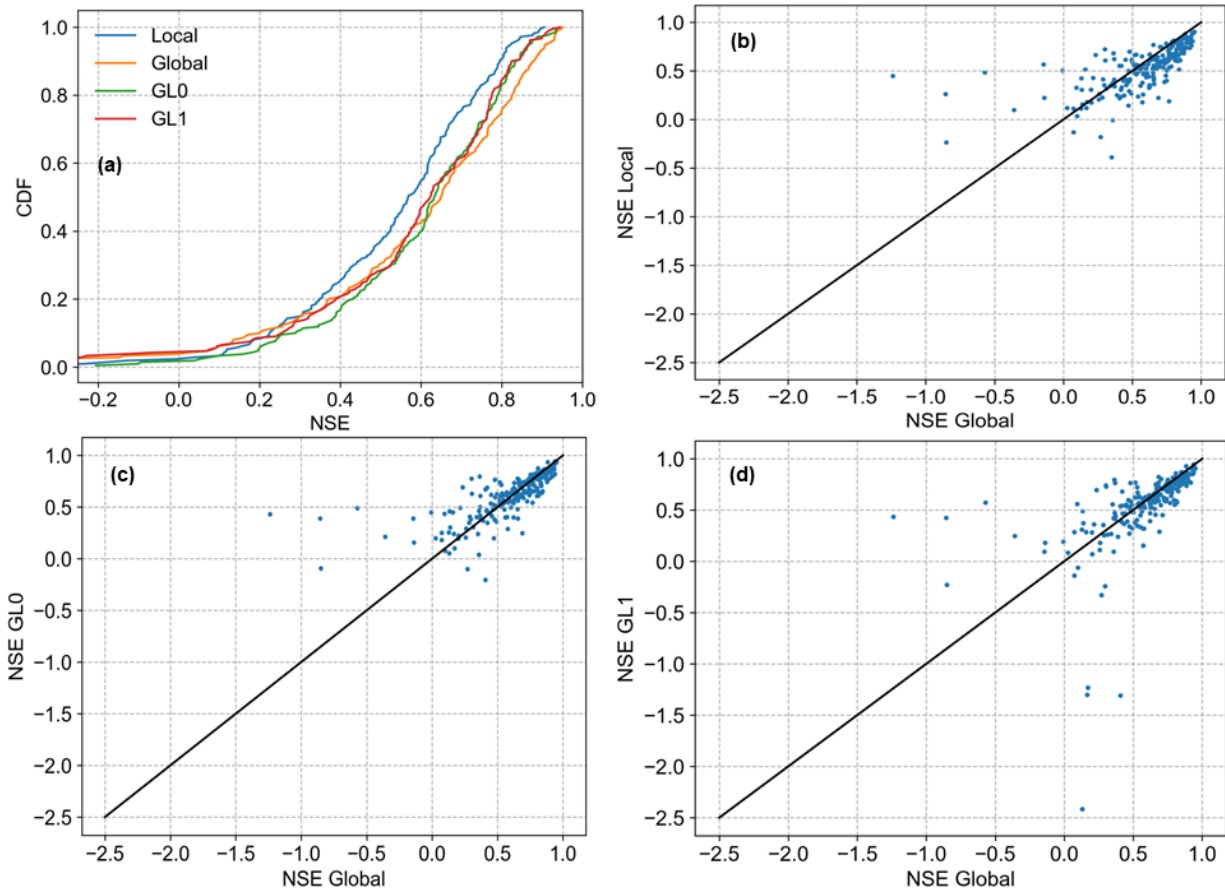
151 strategy is the best (or at least as good as other strategies) for nearly all watersheds when the model
152 is trained for the entire hydrograph and the evaluated using NSE.



153 **Figure 2.** Entire hydrograph models. (a) Cumulative distribution function (CDF) of NSE values
154 obtained by different models. The x-axis is clipped at -0.25. (b), (c) and (d) Comparisons of
155 NSEs obtained by the global model to the NSEs obtained by other models.

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157 When the models were trained to predict recession flows, no clear best strategy emerged
158 (Figure 3a). Local models performed worse than the other three models for most watersheds but
159 even then, there were many watersheds where local models performed better than the global model
160 (Figure 3b). However, in all cases where the local models were better, the NSE values were below
161 0.35. Typically, the GL models outperformed the global model for the watersheds where NSE
162 values obtained by the global model were low (< 0.5 approximately, Figures 3a, 3c, and 3d).
163 Conversely, the global model outperformed GL models in watersheds where the global model NSE
164 values were high (> 0.70 approximately). We conclude that the best model for recession flow
165 depends upon the watershed being considered. Another noteworthy point is that GL0 and GL1
166 models yield significant improvement over the global model in some of the watersheds. Another
167 conclusion is that local information, as captured in GL models, is useful for recession flow
168 simulation but not for the full hydrograph. Thus, postprocessing of the global model predicted
169 streamflow, as is done here, is a viable strategy for recession flow predictions, depending upon the
170 watershed being considered.



171 **Figure 3.** Recession flow models. **(a)** Cumulative distribution function (CDF) of NSE values
 172 obtained by different models. The x-axis is clipped at -0.25. **(b), (c) and (d)** Comparisons of
 173 NSEs obtained by the global model to the NSEs obtained by other models.

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175 **5. Role of errors in model performance**

176 The hydrological data incur significant errors, primarily of epistemic nature, which can be
 177 specific to individual watersheds (referred to as local errors). The errors can be either systematic
 178 or non-systematic. A local DL model will fit the local systematic errors but a global DL model
 179 will not fit these local errors since doing so will degrade the performance of the global model in
 180 other watersheds. We hypothesize that the residuals between observed and global model-predicted
 181 streamflows in a watershed reflect the effect of the local systematic errors. These errors can be
 182 either stationary, nonstationary, or a combination of both. In the nonstationary category, the errors
 183 may or may not depend on the input. Even if some errors are dependent upon the model input,
 184 available data may not be enough to learn that dependency effectively making those errors input
 185 independent.

186 Some examples of these errors include the underestimation of rainfall magnitude by rain
 187 gauges caused by the wind effect, which represents a stationary error. The consistent
 188 underestimation of high rainfall volumes due to low rain gauge density (Bárdossy & Anwar, 2022)
 189 represents a rainfall-dependent nonstationary error. The change in rain gauge density over time

190 may introduce rainfall-independent nonstationary errors. The occurrence of rare flood events
191 during the testing period that were absent during the training period represents another type of
192 input-independent nonstationary error.

193 Both the stationary errors and rainfall-dependent nonstationary errors result in residuals
194 that have learnable structure, that is, there is information contained in the residuals that can be used
195 to further improve the model performance. On the other hand, rainfall-independent nonstationary
196 errors result in residuals that do not contain any learnable structure. Thus, depending upon which
197 types of errors dominate the hydrological data fed to the DL models, the GL models would improve
198 or worsen the streamflow simulation accuracy.

199 Figure 2 shows that the GL models performed worse than the global model in most of the
200 watersheds when the entire hydrograph is considered. This means that the residual between the
201 observed and the global model-predicted streamflow contains a nonstationary structure that cannot
202 be learned by the local model. Therefore, we conclude that the systematic errors are predominantly
203 nonstationary when the entire hydrograph is considered. This further implies that systematic
204 nonstationary errors are one of the reasons that local DL models perform worse than the global
205 model. This result highlights that any model calibrated to a single watershed will fit the local non-
206 stationary errors and perform worse than a global model and we expect this result will also apply
207 to PB models. This interpretation has consequences when PB models are compared to the global
208 DL models because a global DL model may perform better not just because that they are able to
209 extract more hydrological information from global data but also because PB models are often
210 overfit to the local data.

211 Figure 3 shows that the GL models improved the performance compared to global models
212 in many watersheds when only the recession flows were considered. This implies that a learnable
213 structure exists in the residuals between observed and global model-predicted streamflow of these
214 watersheds for recession flows. To further understand the utility of the GL modeling strategy for
215 recession flows, each watershed was categorized into one of four categories based on performance
216 relative to the global model as listed in Table 1. Figure 4 shows the locations of the categories of
217 watersheds according to Table 1. There were several watersheds, especially in the eastern USA,
218 that belonged to category 1 where the GL models significantly improved the performance for
219 recession flows. Also, many watersheds belonged to category 2 where GL models degraded the
220 performance. Therefore, we conclude that in several watersheds (category 1) the GL modeling
221 strategy is better compared to either global or local modeling strategies as it allows the model to
222 learn from both the hydrological information contained in the donor watersheds and the local
223 systematic errors. A few watersheds belonged to category 3 where GL models did not result in any
224 significant change in performance compared to the global model. These watersheds are spread
225 across the USA. Only four watersheds belonged to category 4 where the GL strategy had mixed
226 results in improving performance relative to the global model. Category 4 watersheds are also
227 located in different geographical regions of the USA.

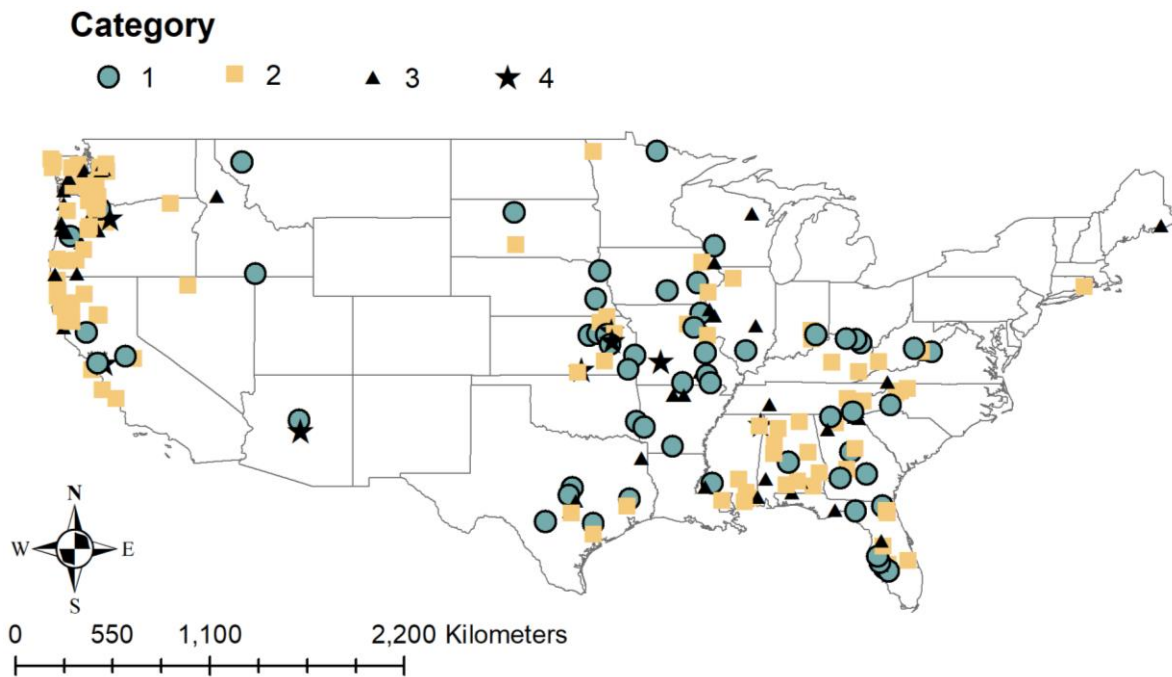
228 The GL modeling proved to be an effective strategy for recession flows (depending upon
229 the watershed) but not for the entire hydrograph. This result may be due to the averaging of
230 nonstationary rainfall errors when recession flows are considered since the nonstationarity of
231 rainfall errors will more strongly impact the rising limb of the hydrograph than the recession flows.
232 This may also be due to recession flows being more strongly controlled by local features of a

233 watershed including the structure of groundwater systems, bank storage capacity, and vegetation
 234 characteristics.

235 Table 1. Categorization of watersheds based on dominant error types when modeling recession
 236 flows

Category	Effect on GL model performance compared to the performance of the global model	Dominant systematic error types
1	At least one GL model improves the performance while the other model does not change the performance	Stationary and input-dependent nonstationary errors
2	At least one GL model worsens the performance while the other model does not change the performance	Unlearnable nonstationary errors
3	No change in performance by any model	Neither learnable nor unlearnable errors dominate
4	GL1 improves the performance while GL0 worsens the performance GL0 improves the performance while GL1 worsens the performance	Stationary and unlearnable errors Learnable nonstationary errors

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238 **Figure 4.** Categorization of watersheds in the CAMELS dataset based on the difference in the
 239 performance of global and GL models. See Table 1 for an explanation of the 4 categories.
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6. Discussions and Conclusions

242 The advent of DL models allows for extraction of hydrological information from multiple
 243 watersheds to calibrate watershed-specific models. As shown in this study, different combinations
 244 of global and local information can be applied to obtain the most accurate model. Three modeling
 245 strategies were tested: local modeling, global modeling, and two combinations of global and local
 246 modeling (GL models). The best modeling strategy depended upon the watershed and the portion
 247 of the hydrograph being considered. The global modeling strategy was better than other strategies

248 for most of the watersheds in predicting the entire hydrograph. When only the recession flows
249 were considered, the global models were less dominant and GL models outperformed the global
250 model for several watersheds. There were many watersheds where GL models and the global
251 model performed similarly. These results echo the discussion by Beven (2023) that it is not
252 possible to define a general best model for all purposes and all watersheds.

253 The idea behind using the GL models is to take advantage of the hydrologic information
254 contained in the global dataset and the information contained in the form of the local systematic
255 errors. The effect of the local errors will be reflected in the residuals between observed and global
256 model-predicted streamflow. If the residuals corresponding to a watershed have a dominantly
257 unlearnable nonstationary structure, the GL model will worsen the performance compared to the
258 global model. It can be concluded that the systematic errors are predominantly unlearnable and
259 nonstationary when the entire hydrograph is considered; this is why GL models do not improve
260 performance in this case. The nonstationary effects are averaged out when only the recession flows
261 are considered; therefore, the GL models improve the performance compared to the global model
262 in several watersheds in this case.

263 This study provides an important insight into why the global models perform better than
264 the local DL models and PB models calibrated to a single watershed. The local DL and PB models
265 fit the systematic nonstationary errors while the global models filter out these errors. Local DL
266 and PB models are essentially overfitting the local erroneous data whereas global models with a
267 much larger training set can generalize over data from a broad set of watersheds. It is noted that
268 the generalization occurs not just because the global DL models are able to extract hydrologically
269 relevant information from the donor watersheds but also because they are able to filter the
270 watershed-specific errors. The presence of epistemic errors in the hydrological data of a watershed
271 has implications for the PB model validation strategy as discussed in Beven (2019) and Gupta et
272 al. (2023), and also for comparison between PB models and global DL models.

273 **Open Research**

274 Data used in this study are freely available online and appropriate references have been provided
275 in the main text.

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281 **References**

282 Bárdossy, A., & Anwar, F. (2022). Why our rainfall-runoff models keep underestimating the
283 peak flows? *Hydrology and Earth System Sciences Discussions*, 1-30.

284 Bear, J. (2013). *Dynamics of fluids in porous media*. Courier Corporation.

285 Beven, K. (2019). Towards a methodology for testing models as hypotheses in the inexact
286 sciences. *Proceedings of the Royal Society A*, 475(2224), 20180862.

287 Beven, K. (2020). Deep learning, hydrological processes and the uniqueness of place.
288 *Hydrological Processes*, 34(16), 3608-3613.

289 Beven, K. (2023). Benchmarking Hydrological Models for an Uncertain Future. *Hydrological*
290 *Processes*, e14882.

291 Beven, K. J. (2000). Uniqueness of place and process representations in hydrological modelling.
292 *Hydrology and Earth System Sciences*, 4(2), 203-213.

293 Beven, K. J. (2011). *Rainfall-runoff modelling: the primer*. John Wiley & Sons.

294 Beven, K., & Smith, P. (2015). Concepts of information content and likelihood in parameter
295 calibration for hydrological simulation models. *Journal of Hydrologic Engineering*, 20(1),
296 A4014010.

297 Frame, J. M., Kratzert, F., Gupta, H. V., Ullrich, P., & Nearing, G. S. (2023). On strictly enforced
298 mass conservation constraints for modelling the Rainfall-Runoff process. *Hydrological Processes*,
299 37(3), e14847.

300 Goodfellow, I., Bengio, Y., & Courville, A. (2016). *Deep learning*. MIT Press.

301 Govindaraju, R. S. (2000). Artificial neural networks in hydrology. I: Preliminary concepts.
302 *Journal of Hydrologic Engineering*, 5(2), 115-123.

303 Gupta, A., Govindaraju, R. S., Li, P. C., & Merwade, V. (2023). On Constructing Limits-of-
304 Acceptability in Watershed Hydrology using Decision Trees. *Advances in Water Resources*,
305 104486.

306 Knoben, W. J., Freer, J. E., Peel, M. C., Fowler, K. J. A., & Woods, R. A. (2020). A brief analysis
307 of conceptual model structure uncertainty using 36 models and 559 catchments. *Water Resources*
308 *Research*, 56(9), e2019WR025975.

309 Kratzert, F., Klotz, D., Shalev, G., Klambauer, G., Hochreiter, S., & Nearing, G. (2019). Towards
310 learning universal, regional, and local hydrological behaviors via machine learning applied to
311 large-sample datasets. *Hydrology and Earth System Sciences*, 23(12), 5089-5110.

312 Lee, H. T., & Delleur, J. W. (1972). A program for Estimating runoff from Indiana watersheds,
313 Part III: analysis of geomorphologic data and a Dynamic Contributing Area Model for Runoff
314 Estimation.

315 Li, X., Khandelwal, A., Jia, X., Cutler, K., Ghosh, R., Renganathan, A., ... & Kumar, V. (2022).
316 Regionalization in a global hydrologic deep learning model: from physical descriptors to random
317 vectors. *Water Resources Research*, 58(8), e2021WR031794.

318 Ma, K., Feng, D., Lawson, K., Tsai, W. P., Liang, C., Huang, X., ... & Shen, C. (2021).
319 Transferring hydrologic data across continents—leveraging data-rich regions to improve hydrologic
320 prediction in data-sparse regions. *Water Resources Research*, 57(5), e2020WR028600.

321 Moličová, H., Grimaldi, M., Bonell, M., & Hubert, P. (1997). Using TOPMODEL towards
322 identifying and modelling the hydrological patterns within a headwater, humid, tropical catchment.
323 *Hydrological Processes*, 11(9), 1169-1196.

- 324 Nash, J. E., & Sutcliffe, J. V. (1970). River flow forecasting through conceptual models part I—
325 A discussion of principles. *Journal of Hydrology*, 10(3), 282-290.
- 326 Nearing, G. S., Kratzert, F., Sampson, A. K., Pelissier, C. S., Klotz, D., Frame, J. M., ... & Gupta,
327 H. V. (2021). What role does hydrological science play in the age of machine learning? *Water*
328 *Resources Research*, 57(3), e2020WR028091.
- 329 Rodriguez-Iturbe, I., & Rinaldo, A. (1997). *Fractal river basins: chance and self-organization*.
330 Cambridge University Press.
- 331 Shen, C., & Lawson, K. (2021). Applications of deep learning in hydrology. *Deep Learning for*
332 *the Earth Sciences: A Comprehensive Approach to Remote Sensing, Climate Science, and*
333 *Geosciences*, 283-297.
- 334 Singh, V. P. (1995). *Computer models of watershed hydrology*. Water Resources Publications.
- 335 Troch, P. A., Paniconi, C., & Emiel van Loon, A. E. (2003). Hillslope-storage Boussinesq model
336 for subsurface flow and variable source areas along complex hillslopes: 1. Formulation and
337 characteristic response. *Water Resources Research*, 39(11).